

Lecture 29: PDA from CFG; "Cleaning" up CFGs; Chomsky Normal Form CFGs; Pumping Lemma for CFLs

$$S \rightarrow C \cdot S \mid \epsilon$$

$$C \rightarrow A \cdot B$$

$$A \rightarrow 0A1 \mid 01$$

$$B \rightarrow 1B \mid \epsilon$$

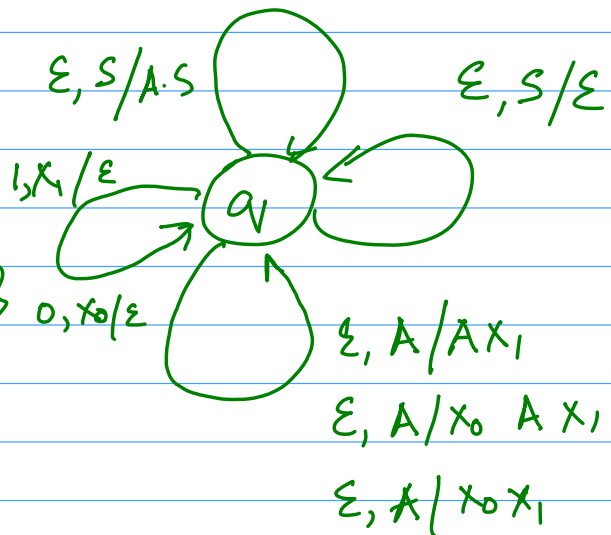
$$S \rightarrow A \mid B$$

$$\underline{S} \rightarrow A \cdot \underline{S} \mid \epsilon$$

$$\underline{A} \rightarrow A1 \mid 0A1 \mid 01$$

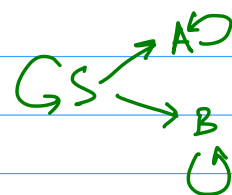
$$\Sigma = \{0, 1\}$$

$$\Gamma = \{\underline{S}, A, X_0, X_1\}$$



$$\begin{array}{l} \underline{S} \rightarrow \quad \quad \quad \begin{array}{c} 0S1 \\ 0D1 \\ 0A1 \end{array} / 01 \\ \checkmark \underline{A} \rightarrow 01 \mid 1A0 \mid \quad \mid 10 \end{array}$$

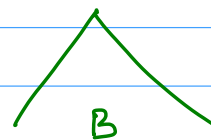
1D0
1S0



$$S \rightarrow X_0 S_1$$

$$S_1 \rightarrow S X_1$$

$$D \rightarrow \quad \mid 0AD \mid 0AS$$



$$S \rightarrow X_0 S X_1 \mid X_0 D X_1 \mid X_0 A X_1 \mid X_0 X_1$$

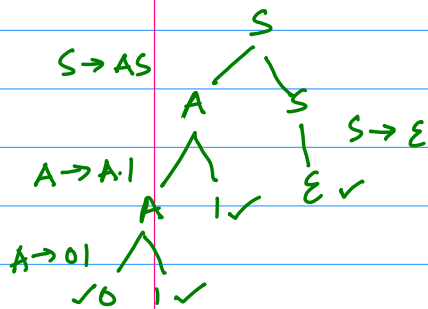
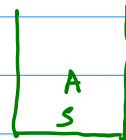
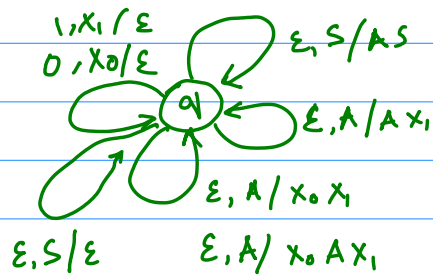
$$\checkmark X_0 \rightarrow 0$$

$$\checkmark X_1 \rightarrow 1$$

$$A \rightarrow X_0 X_1 \mid X_1 A X_0 \mid X_1 D X_0 \mid X_1 S X_0 \mid X_1 X_0$$

$$D \rightarrow X_0 A D \mid X_0 A S \dots D \rightarrow X_0 D, D_1 \rightarrow A S$$

$$\begin{aligned} S &\rightarrow A \cdot S \mid \epsilon \\ A &\rightarrow A1 \mid 0A1 \mid 01 \end{aligned}$$

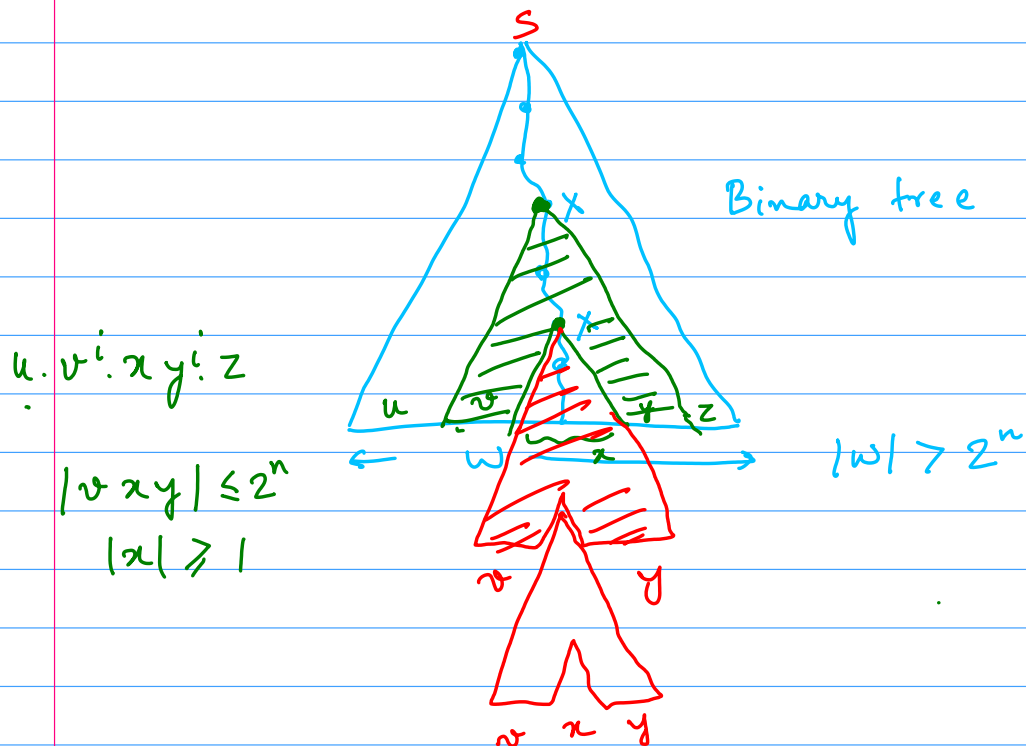


Chomsky Normal Form (CNF)

- No useless symbols
- No ϵ production $X \rightarrow \epsilon$
- No unit production $X \rightarrow Y$
- All prod. rules: $A \rightarrow BC$
- $D \rightarrow 0$

CNF CFG.

$G \dots n$ non-terminals



PL for CFLs

$$w = u.v.x.y.z.$$

$$|w| \geq 2^n$$

$$\forall i \ u v^i . x y^i z \in L$$

$$L = \{0^n 1^m 2^n \mid n \geq 0\}$$

$$\Sigma = \{0, 1, 2\}$$

$$\begin{matrix} \overbrace{0}^{2k} & \overbrace{1}^{2k} & \overbrace{2}^{2k} \\ \underbrace{} & \underbrace{} & \underbrace{} \end{matrix}$$

$$k = 2 \quad \# \text{ NT in CNF Grammar}$$