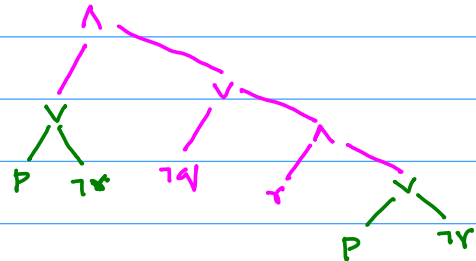


q32, q33, q34, q35

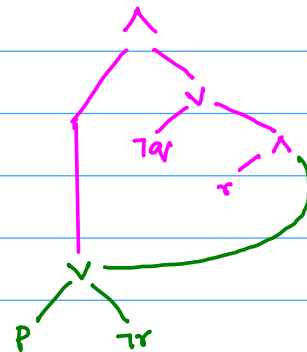
Normal forms

Negation Normal Form: $(p \vee \neg r) \wedge (\neg q \vee (r \wedge (p \vee \neg r)))$

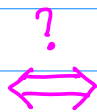
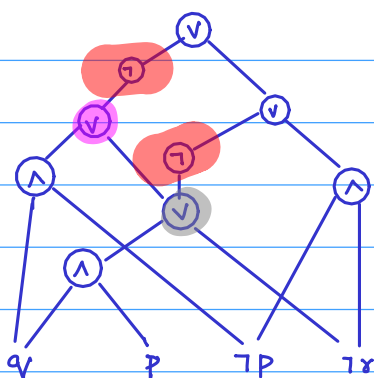
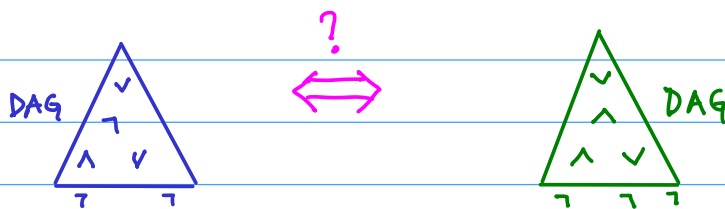
Tree representation:



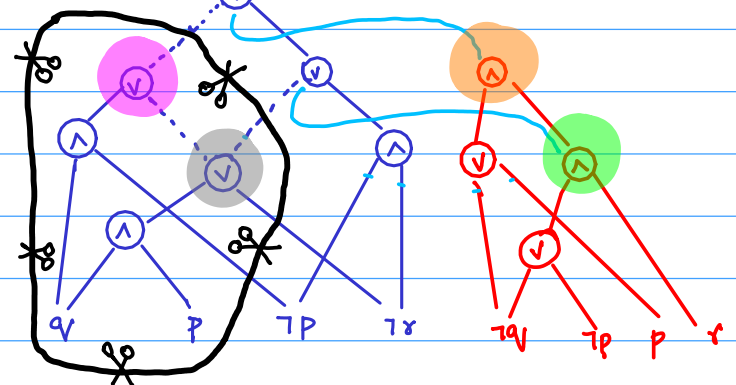
DAG representation:



Given a DAG representing a prop. logic formula with only \wedge, \vee, \neg nodes, can we efficiently get a DAG representing a semantically equivalent NNF formula?



Remove



\neg (pink circle) is (orange circle); \neg (grey circle) is (green circle)

Literal: variable or its complement $p, \neg p, q, \neg r$

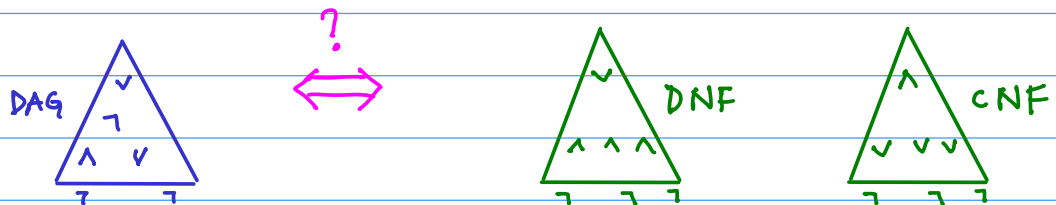
Clause: Disjunction of literals $(p \vee q \vee \neg r), (\cancel{q \vee \neg q \vee r})$

Cube: Conjunction of literals $(p \wedge q \wedge \neg r), (\cancel{q \wedge \neg q \wedge r})$

Conjunctive Normal Form (CNF): Conjunction of clauses
(Product of Sums) $(p \vee q \vee \neg r) \wedge (q \vee r \vee \neg s \vee t)$

Disjunctive Normal Form (DNF): Disjunction of cubes
(Sum of Products) $(\neg p \wedge \neg q \wedge r) \vee (\neg q \wedge \neg r \wedge s \wedge t)$

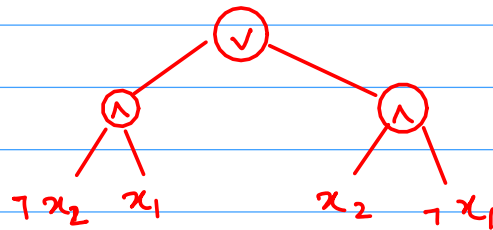
Given a DAG representing a prop. logic formula with only \wedge, \vee, \neg nodes, can we efficiently get a DAG representing a semantically equivalent ~~DNF~~ ^{CNF/DNF} formula?



Validity checking of $\begin{cases} \text{CNF} \\ \text{DNF} \end{cases}$

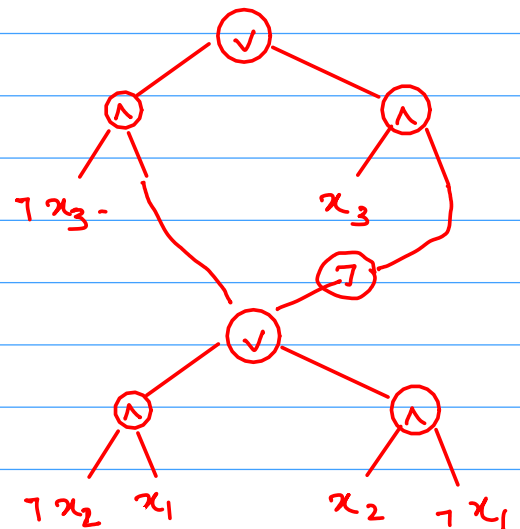
Satisfiability checking of $\begin{cases} \text{CNF} \\ \text{DNF} \end{cases}$

$$x_1 \oplus x_2 \Leftrightarrow (x_1 \wedge \neg x_2) \vee (\neg x_1 \wedge x_2)$$

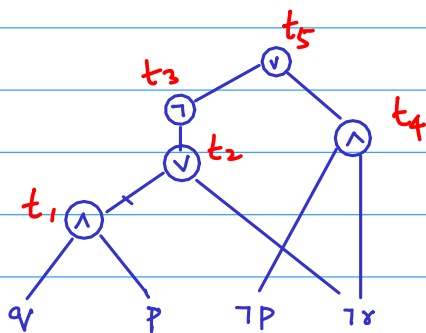


$$\underbrace{(x_1 \oplus x_2)}_{\varphi} \oplus x_3$$

4n nodes



$$\varphi(p, q, r)$$



$$\varphi'(p, q, r, t_1, \dots, t_5) \text{ Equisatisfiable. CNF}$$

$$(t_1 \leftrightarrow p \wedge q) \wedge$$

$$(t_2 \leftrightarrow t_1 \vee \neg r) \wedge$$

$$(t_3 \leftrightarrow \neg t_2) \wedge$$

$$(t_4 \leftrightarrow \neg p \wedge \neg r) \wedge$$

$$(t_5 \leftrightarrow t_3 \vee t_4) \wedge t_5$$

$$\Leftrightarrow (t_1 \rightarrow (p \wedge q)) \wedge ((p \wedge q) \rightarrow t_1) \Leftrightarrow (\neg t_1 \vee (p \wedge q)) \wedge (t_1 \vee (\neg p \vee \neg q)) \Leftrightarrow (\neg t_1 \vee p) \wedge (\neg t_1 \vee q) \wedge (t_1 \vee \neg p \vee \neg q)$$