24/09

Sieve of Eratosthenes - to find prime numbers.

List (infinite) of numbers...

~~2~~ ~~3~~ ~~4~~ ~~5~~ ~~6~~ 7 ~~8~~ 9 ~~10~~ 11 ~~12~~ 13
~~14~~ ~~15~~ ~~16~~ 17 ~~18~~ 19 ~~20~~ ~~21~~ ~~22~~ 23 ~~24~~ ~~25~~
~~26~~ ~~27~~ ~~28~~ 29 ~~30~~ 31 ~~32~~ ~~33~~ ~~34~~ ~~35~~ ~~36~~ 37
~~38~~ ~~39~~ ~~40~~ 41 ~~42~~ 43 ~~44~~ ~~45~~ ~~46~~ ~~47~~ ~~48~~ 49.

remove numbers divisible by 2, then 3, then 5- ...

```
> (define (sieve s)
    (cons-stream (stream-car s)
                 (sieve
                   (stream-filter
                     (lambda (x) (not (divisible? x
                                        (stream-car s))))
                     (stream-cdr s)))))).
> (define primes (sieve (integers-starting-from 2))).
> (stream-ref 5 primes).
  13
> (stream-ref 100 primes)
  547.
```

0	1	2	3	4	5
2	3	5	7	11	13

```
> (define primes
    (cons-stream 2
                 (stream-filter prime? (integers-starting-from 3))))
```

this also works ↓ using the smallest-divisor procedure

```
>(define (prime2? x)
   (define (iter ps)
      (cond ((> (square (stream-car ps)) x) true)
            ((divisible? x (stream-car ps)) false)
            (else (iter (stream-cdr ps)))))
   (iter primes)).
>(define primes (cons-stream 2 (stream-filter prime2?
                  (integers-starting-from 3)))).

>(stream-ref 5 primes)
13
>(stream-ref 100 primes)
547
```

Defining primes ~~iter~~ by checking for prime2? nesse.

prime2 - checking primeness using primes we've found till now.

Can generate a infinite streams using each other

primes had 2. promise initially.

The numbers we are checking divisibility with are already generated

Stream of guesses to compute square root

```
>(define (sqrt-stream x)
   (define guesses
      (cons-stream 1.0
         (stream-map (lambda (guess)
                        (sqrt-improve guess x))
                     guesses)))
   guesses).
```

> (define sqrt2s (sqrt-stream 2)).

> sqrt2s

#(1.0 #<proc ... >).

> (stream-ref 1 sqrt2s)

1.5

> (stream-ref 5 sqrt2s)

1.4142135623730950

Moving withdraw amounts for joint accounts (fair way - round robin).

One can withdraw money if they just had and the other still hasn't

Time doesn't go well with the stream paradigm

Haskell

Function: Map from values in a domain D to range R

Type signature gives contract for a function

List in haskell is written in [ ].

Input: an integer, list of characters.

Int, [char).

Output: [Char).

commonWords :: Int → ([Char) → [Char]).

In Haskell, internally all functions take only one input at a time like the second way of writing. 'add'.

This is called currying.

They supply functions forward.