Syntax Analysis

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Topic:

Syntax Analysis

Section:

Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsing

Outline

- Grammars, derivations, and parse trees
- Introduction to bottom-up parsing
- Shift reduce parsing
- SLR(1) parsing
- Conceptual issues in LR parsing
- CLR(1) parsing
- LALR(1) parsing



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IIT Bombay cs302: Implementation

of Programming Languages

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Grammars, derivations, and parse trees



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Introduction to Parsing

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Shift Reduce Parsing

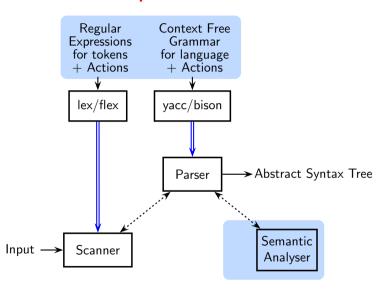
SLR(1) Parsing

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A Compiler Front End





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Syntax Analysis aka Parsing

- Determines a structure in the input by discovering relationships between tokens representing the input
- This structure is represented by a syntax tree (aka parse tree)
- If a parse tree can be constructed, the input is syntactically valid i.e., it is well-formed as defined by the language
 It may not be semantically valid
- A description of syntax should be
 - o unambiguous, correct, complete, and
 - o convenient for use by the designers and implementers of a language

A Context-free grammar (aka grammar) meets these requirements



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Derivation

- Transformation of a sequence of grammar symbols
- Obtained by replacing non-terminals by the RHS of a production



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Derivation

- Transformation of a sequence of grammar symbols
- Obtained by replacing non-terminals by the RHS of a production
- Consider the following grammar of expressions

$$E\!\to E\!+\!T\mid T$$

$$T \rightarrow T * F \mid F$$
 $F \rightarrow id$



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Derivation

- Transformation of a sequence of grammar symbols
- Obtained by replacing non-terminals by the RHS of a production
- Consider the following grammar of expressions

$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow id$

A possible derivation is

$$E \Rightarrow E + T$$

$$\Rightarrow T + T$$

$$\Rightarrow F + T$$

$$\Rightarrow id + T$$

$$\Rightarrow id + T * F$$

$$\Rightarrow id + id * F$$

$$\Rightarrow id + id * id$$



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Notational Conventions

Convention
letters a, b, c, operators
delimiters, keywords
letters A , B , C and names
such as <i>declaration</i> , <i>list</i>
and S is the start symbol
X, Y, Z
letters x , y , z
α , β , γ
ϵ



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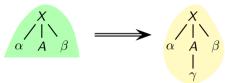
Parsing Parsing

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Formalizing a Derivation

- Let $A \rightarrow \gamma$ denote a production and $\alpha A \beta$ denote a string of grammar symbols
- Replacing A in $\alpha A\beta$ by γ gives $\alpha \gamma \beta$
 - \circ We say that $\alpha A\beta$ derives $\alpha \gamma \beta$ in one step
 - We write it as $\alpha A\beta \Rightarrow \alpha \gamma \beta$
 - o It represents the expansion of a subtree during parsing



- Formally $\alpha_1 \Rightarrow \alpha_2$ is a relation $(N \cup T)^* \times (N \cup T)^*$
- A multi-step derivation is a composition of multiple single step derivations
 - $\circ \ \alpha_1 \stackrel{*}{\Rightarrow} \alpha_2$ means α_1 derives α_2 in zero or more steps
 - $\circ \ \alpha_1 \stackrel{+}{\Rightarrow} \alpha_2$ means α_1 derives α_2 in one or more steps



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The Language Generated by a Grammar

- $L(G) = \{ w \mid S \stackrel{+}{\Rightarrow} w, w \in T^* \}$, where
 - \circ S is the start non-terminal of grammar G, and
 - T is the set of terminal symbols of G
- The strings in *L*(*G*) are called the sentences of *G*
- A string $S \stackrel{*}{\Rightarrow} \alpha$ is called a sentential form of G
- Every sentence of G is also a sentential form of G
- Grammars G_1 and G_2 are equivalent if $L(G_1) = L(G_2)$



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Sentential Forms and Sentences

$$\begin{array}{|c|c|c|c|c|}\hline G_1 & E \to E + T \mid T \\ & T \to T * F \mid F \\ & F \to \operatorname{id} \end{array} \qquad \begin{array}{|c|c|c|}\hline G_2 & E \to E + E \\ & E \to E * E \\ & E \to \operatorname{id} \end{array}$$

- $L(G_1) = L(G_2)$
- $\{id + id * id, id * id + id\} \subset L(G_1)$ (and hence, also of $L(G_2)$)
- E + T. F + E. id + T * F are sentential forms of G_1 but not of G_2
- E + E. E * E. id + E * E are sentential forms of G_2 but not of G_1

Sentential forms depend on the grammars whereas the sentences depend on the languages generated by grammars



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Leftmost and Rightmost Derivations

- A derivation $\alpha_1 \Rightarrow \alpha_2 \Rightarrow \ldots \Rightarrow \alpha_k$ is a
 - o leftmost derivation, denoted $\alpha_1 \stackrel{lm}{\Rightarrow} \alpha_2 \stackrel{lm}{\Rightarrow} \dots \stackrel{lm}{\Rightarrow} \alpha_k$, if every α_{i+1} is obtained from α_i by replacing the leftmost non-terminal occurring in α_i by the RHS of some production of the non-terminal
 - \circ rightmost derivation, denoted $\alpha_1 \stackrel{rm}{\Rightarrow} \alpha_2 \stackrel{rm}{\Rightarrow} \dots \stackrel{rm}{\Rightarrow} \alpha_k$, if every α_{i+1} is obtained from α_i by replacing the rightmost non-terminal occurring in α_i by the RHS of some production of the non-terminal
- A sentential form α is called
 - o a left sentential form, if it occurs in a leftmost derivation
 - o a right sentential form, if it occurs in a rightmost derivation

Note that α could be both a right and a left sentential form



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Leftmost and Rightmost Derivations

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \operatorname{id} \end{array}$$

Sentence: id + id * id

	Leftmost Derivation	Rightmost Derivation
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Sentence: id + id * id

Leftmost Derivation







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Leftmost and Rightmost Derivations

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \mathrm{id} \end{array}$$

Sentence: id + id * id

Leftmost Derivation

$$E \stackrel{lm}{\Rightarrow} E + T$$
$$\stackrel{lm}{\Rightarrow} T + T$$





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Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation Rightmost Derivation $F \stackrel{lm}{\Rightarrow} E + T$ $\stackrel{lm}{\Rightarrow} T + T$ $\stackrel{lm}{\Rightarrow} F + T$



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Leftmost and Rightmost Derivations

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 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation	Rightmost Derivation
$E \stackrel{lm}{\Rightarrow} E + T$ $\stackrel{lm}{\Rightarrow} T + T$ $\stackrel{lm}{\Rightarrow} F + T$ $\stackrel{lm}{\Rightarrow} id + T$ E $+$ T I F I	



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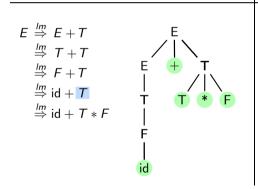
Leftmost and Rightmost Derivations

Grammar
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 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation





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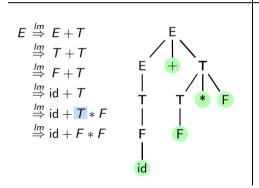
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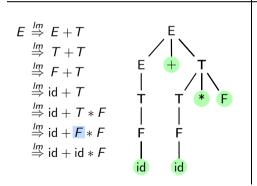
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Grammar
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Sentence: id + id * id

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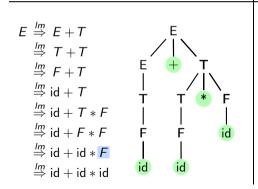
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Grammar
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 $T \rightarrow T * F \mid F$
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Sentence: id + id * id

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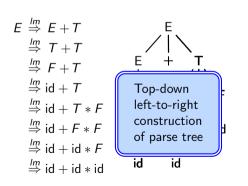
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Grammar
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Sentence: id + id * id

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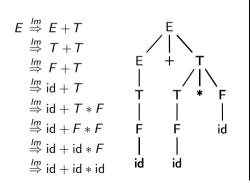
Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation









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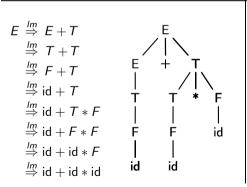
Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$

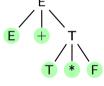
 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation









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Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

 $\stackrel{lm}{\Rightarrow}$ id + T

 $\stackrel{lm}{\Rightarrow} id + T * F$ $\stackrel{lm}{\Rightarrow} id + F * F$

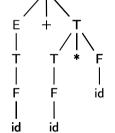
 $\stackrel{lm}{\Rightarrow}$ id + id * F

 $\stackrel{lm}{\Rightarrow}$ id + id * id

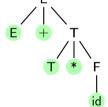
Sentence: id + id * id

Leftmost Derivation

$E \stackrel{lm}{\Rightarrow} E + T$ $\stackrel{lm}{\Rightarrow} T + T$ $\stackrel{lm}{\Rightarrow} F + T$ E + T









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Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation

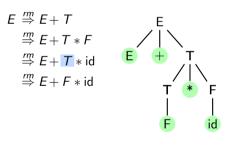
$E \stackrel{lm}{\Rightarrow} E + T$ $\stackrel{lm}{\Rightarrow} T + T$ $\stackrel{lm}{\Rightarrow} F + T$ $\stackrel{lm}{\Rightarrow} id + T$ $\stackrel{lm}{\Rightarrow} id + T * F$ $\stackrel{lm}{\Rightarrow} id + F * F$ F = F

id

id

 $\stackrel{lm}{\Rightarrow}$ id + id * F

 $\stackrel{lm}{\Rightarrow}$ id + id * id





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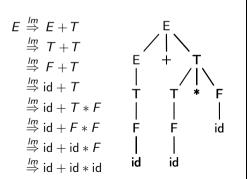
Leftmost and Rightmost Derivations

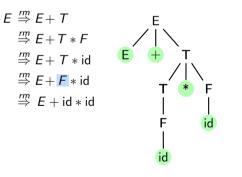
Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation







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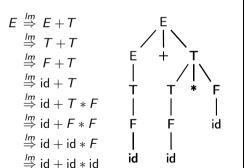
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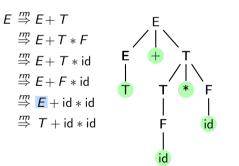
Grammar
$$E \rightarrow E + T \mid T$$

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 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation







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Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

 $F \stackrel{lm}{\Rightarrow} F + T$

 $\stackrel{lm}{\Rightarrow} T + T$

 $\stackrel{lm}{\Rightarrow} F + T$

 $\stackrel{lm}{\Rightarrow}$ id + T

 $\stackrel{lm}{\Rightarrow} id + T * F$

 $\stackrel{lm}{\Rightarrow}$ id + F * F

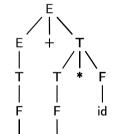
 $\stackrel{lm}{\Rightarrow}$ id + id * F

 $\stackrel{lm}{\Rightarrow}$ id + id * id

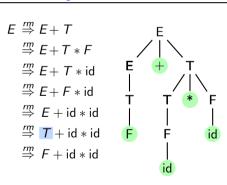
Sentence: id + id * id

Leftmost Derivation

id



id





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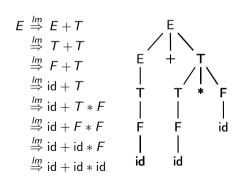
Leftmost and Rightmost Derivations

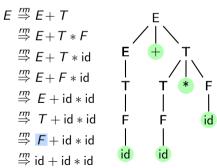
Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

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Leftmost and Rightmost Derivations

Grammar
$$E \rightarrow E + T \mid T$$
 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Leftmost Derivation

$E \stackrel{lm}{\Rightarrow} E + T$ $\stackrel{lm}{\Rightarrow} T + T$ $\stackrel{lm}{\Rightarrow} F + T$ $\stackrel{lm}{\Rightarrow} id + T$ $\stackrel{lm}{\Rightarrow} id + T * F$ $\stackrel{lm}{\Rightarrow} id + F * F$

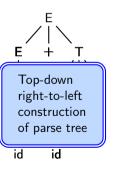
id

id

 $\stackrel{lm}{\Rightarrow}$ id + id * F

 $\stackrel{lm}{\Rightarrow}$ id + id * id







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Derivations and Sentences

$$\begin{array}{|c|c|c|c|c|}\hline G_1 & E \to E + T \mid T \\ T \to T * F \mid F \\ F \to \operatorname{id} & & & E \to E + E \\ E \to E * E \\ E \to \operatorname{id} & & & & E \to \operatorname{id} \\ \hline \end{array}$$

- Although $L(G_1) = L(G_2)$,
 - \circ G_1 has a unique leftmost(rightmost) derivation for every sentence
 - o G₂ admits multiple leftmost(rightmost) derivations for some sentences
- For sentence id + id * id, G_2 admits the following two leftmost derivations

○
$$E \stackrel{lm}{\Rightarrow} E + E \stackrel{lm}{\Rightarrow} id + E \stackrel{lm}{\Rightarrow} id + E * E \stackrel{lm}{\Rightarrow} id + id * E \stackrel{lm}{\Rightarrow} id + id * id$$
This derivation represents the grouping $id + (id * id)$

○
$$E \stackrel{lm}{\Rightarrow} E * E \stackrel{lm}{\Rightarrow} E + E * E \stackrel{lm}{\Rightarrow} id + E * E \stackrel{lm}{\Rightarrow} id + id * E \stackrel{lm}{\Rightarrow} id + id * id$$
This derivation represents the grouping (id + id) * id



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Ambiguous Grammars

- A grammar G is ambiguous, if L(G) contains a sentence for which there are
 - multiple parse tress, or equivalently
 - o multiple leftmost derivations, or equivalently
 - o multiple rightmost derivations
- ullet Between the two expressions grammars, G_1 is unambiguous, G_2 is ambiguous

$$G_1 egin{array}{c} E
ightarrow E + T \mid T \ T
ightarrow T * F \mid F \ F
ightarrow \mathrm{id} \end{array}$$

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow id$$



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Ambiguity in Expressions Grammar

Grammar

Input

 $E \rightarrow E + E$ $E \rightarrow E * E$

 $E \rightarrow id$

id + id * id



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Ambiguity in Expressions Grammar

Grammar

Input

$$E \rightarrow E + E$$

 $F \rightarrow F * F$

$$id + id * id$$

$$extit{E}
ightarrow ext{id}$$

$$E \stackrel{lm}{\Rightarrow} E + E$$

$$\overset{\mathit{lm}}{\Rightarrow} \mathsf{id} + \mathit{E}$$

$$\stackrel{\textit{Im}}{\Rightarrow} \mathsf{id} + \textit{E} * \textit{E}$$

$$\stackrel{lm}{\Rightarrow}$$
 id + id * E

$$\stackrel{lm}{\Rightarrow}$$
 id + id * id



Topic:

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Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsin

Ambiguity in Expressions Grammar

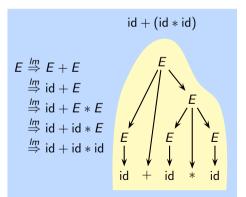
Grammar

Input

$$E\rightarrow E+E$$

$$id + id * id$$

 $E \rightarrow E * E$ $E \rightarrow id$





Language Topic:

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Ambiguity in Expressions Grammar

Grammar

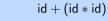
Input

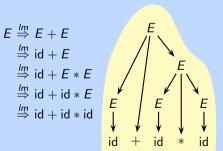
$$E \rightarrow E + E$$

 $E \rightarrow id$

 $E \rightarrow E * E$

id + id * id





$$E \stackrel{lm}{\Rightarrow} E * E$$

$$\stackrel{lm}{\Rightarrow} E + E * E$$

$$\stackrel{lm}{\Rightarrow} id + E * E$$

$$\stackrel{lm}{\Rightarrow} id + id * E$$

$$\stackrel{lm}{\Rightarrow} id + id * id$$



Languages

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Ambiguity in Expressions Grammar

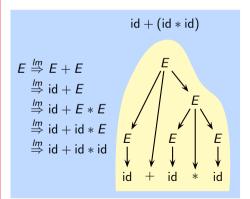
Grammar

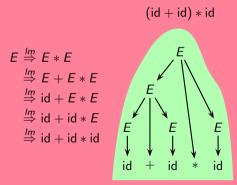
Input

$$E \rightarrow E + E$$

id + id * id

 $E \rightarrow E * E$ $E \rightarrow id$







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Disambiguating Expressions Grammar

- Option 1: Choose the right derivation during parsing Specify the following in the yacc script
 - Give higher precedence to * than +
 - Make both + and * as left-associative
- Option 2: Rewrite the grammar to use the same rules as above

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow id$$

- ∘ Since "*" is buried inside T, rule $E \rightarrow E + T$ gives higher precedence to "*"
- \circ Since rule $E \to E + T$ is left-recursive, it makes "+", left-associative
- \circ Since rule $T \to T * F$ is left-recursive, it makes "*", left-associative



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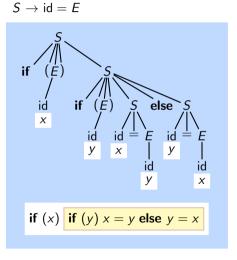
Ambiguity in IF-ELSE Grammar

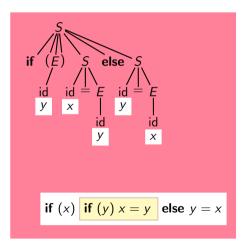
$$S \rightarrow \mathbf{if} (E) S \mathbf{else} S$$

 $S \rightarrow \mathbf{if} (E) S$

Consider Sentence

if
$$(x)$$
 if $(y) x = y$ else $y = x$







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Disambiguating IF-ELSE Grammar

Common rule followed by programming languages
 Every else must belong to the closest unmatched if

Option 1: Give higher precedence to else than ")"
 Question: What associativities should we use?

Option 2: Rewrite the grammar by defining matchedIF and unmatchedIF statements

```
S 
ightarrow matchedIF | unmatchedIF | id = E matchedIF 
ightarrow if (E) matchedIF else matchedIF unmatchedIF 
ightarrow if (E) S unmatchedIF 
ightarrow if (E) matchedIF else unmatchedIF
```

Intuition: When **if** and **else** are derived from the same production, the parse tree between them should not have an unmatched **if**



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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \mathrm{id} \end{array}$$

Sentence: id + id * id

Rightmost Derivation







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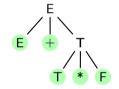
Rightmost Derivation for Bottom-Up Parsing

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \operatorname{id} \end{array}$$

Sentence: id + id * id

Rightmost Derivation

$$E \stackrel{rm}{\Rightarrow} E + T$$
$$\stackrel{rm}{\Rightarrow} E + T * F$$





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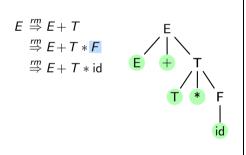
LALR(1) Parsir

Rightmost Derivation for Bottom-Up Parsing

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \operatorname{id} \end{array}$$

Sentence: id + id * id

Rightmost Derivation





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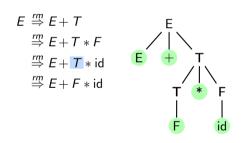
LALR(1) Parsin

Rightmost Derivation for Bottom-Up Parsing

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \operatorname{id} \end{array}$$

Sentence: id + id * id

Rightmost Derivation





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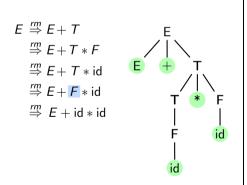
LALR(1) Parsii

Rightmost Derivation for Bottom-Up Parsing

Grammar
$$\begin{array}{|c|c|} \hline E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \operatorname{id} \end{array}$$

Sentence: id + id * id

Rightmost Derivation





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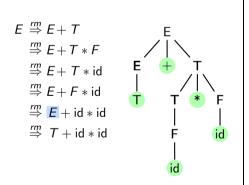
Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation





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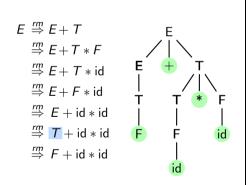
Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation





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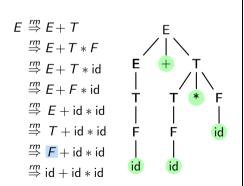
Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation





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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation

$$E \stackrel{rm}{\Rightarrow} E + T$$
 $\stackrel{rm}{\Rightarrow} E + T * F$
 $\stackrel{rm}{\Rightarrow} E + F * id$
 $\stackrel{rm}{\Rightarrow} E + F * id * id$
 $\stackrel{rm}{\Rightarrow} F + id * id$
 $\stackrel{rm}{\Rightarrow} F + id * id$
 $\stackrel{rm}{\Rightarrow} F + id * id$
 $\stackrel{rm}{\Rightarrow} id + id * id$



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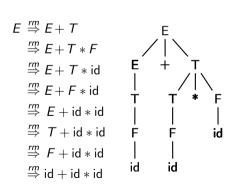
Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation





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Rightmost Derivation for Bottom-Up Parsing

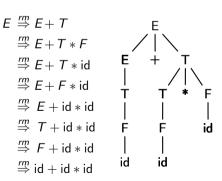
Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation

id + id * id













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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation

$E \stackrel{rm}{\Rightarrow} E + T$ $\stackrel{rm}{\Rightarrow} E + T * F$ $\stackrel{rm}{\Rightarrow} E + T * id$ $\stackrel{rm}{\Rightarrow} E + F * id$ $\stackrel{rm}{\Rightarrow} E + id * id$ $\stackrel{rm}{\Rightarrow} T + id * id$ id $\stackrel{rm}{\Rightarrow} F + id * id$ id id $\stackrel{rm}{\Rightarrow}$ id + id * id

$$id + id * id$$

$$\stackrel{rm}{\Rightarrow} F + id * id$$













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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation

$E \stackrel{rm}{\Rightarrow} E + T$ $\stackrel{rm}{\Rightarrow} E + T * F$

id

 $\stackrel{rm}{\Rightarrow} E + T * id$ $\stackrel{rm}{\Rightarrow} E + F * id$ $\stackrel{rm}{\Rightarrow} E + id * id$ $\stackrel{rm}{\Rightarrow} T + id * id$ id

id

 $\stackrel{rm}{\Rightarrow} F + id * id$

 $\stackrel{rm}{\Rightarrow}$ id + id * id

$$id + id * id$$

$$\stackrel{rm}{\Rightarrow} F + id * id$$

$$\stackrel{rm}{\Rightarrow} T + id * id$$











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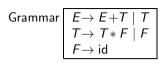
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Sentence: id + id * id

id + id * id

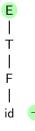
Rightmost Derivation

$F \stackrel{rm}{\Rightarrow} F + T$ $\stackrel{rm}{\Rightarrow} E + T * F$ $\stackrel{rm}{\Rightarrow} E + T * id$ $\stackrel{rm}{\Rightarrow} E + F * id$ $\stackrel{rm}{\Rightarrow} E + id * id$ $\stackrel{rm}{\Rightarrow} T + id * id$ id $\stackrel{rm}{\Rightarrow} F + id * id$ id id $\stackrel{rm}{\Rightarrow}$ id + id * id

$$\stackrel{m}{\Rightarrow} F + \mathrm{id} * \mathrm{id}$$

$$\stackrel{m}{\Rightarrow} T + \mathrm{id} * \mathrm{id}$$

$$\stackrel{m}{\Rightarrow} E + \mathrm{id} * \mathrm{id}$$











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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

id + id * id

Rightmost Derivation

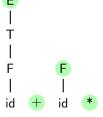
$F \stackrel{rm}{\Rightarrow} F + T$ $\stackrel{rm}{\Rightarrow} E + T * F$ $\stackrel{rm}{\Rightarrow} E + T * id$ $\stackrel{rm}{\Rightarrow} E + F * id$ $\stackrel{rm}{\Rightarrow} E + id * id$ $\stackrel{rm}{\Rightarrow} T + id * id$ id $\stackrel{rm}{\Rightarrow} F + id * id$ id id $\stackrel{rm}{\Rightarrow}$ id + id * id

$$\stackrel{m}{\Rightarrow} F + id * id$$

$$\stackrel{m}{\Rightarrow} T + id * id$$

$$\stackrel{m}{\Rightarrow} E + id * id$$

$$\stackrel{m}{\Rightarrow} E + F * id$$





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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

id + id * id

Rightmost Derivation

$E \stackrel{rm}{\Rightarrow} E + T$ $\stackrel{rm}{\Rightarrow} E + T * F$ $\stackrel{rm}{\Rightarrow} E + F * id$ $\stackrel{rm}{\Rightarrow} E + id * id$ $\stackrel{rm}{\Rightarrow} T + id * id$ $\stackrel{rm}{\Rightarrow} F + id * id$ $\stackrel{rm}{\Rightarrow} id + id * id$ $\stackrel{rm}{\Rightarrow} id + id * id$ $\stackrel{rm}{\Rightarrow} id + id * id$

$$\stackrel{rm}{\Rightarrow} F + \mathrm{id} * \mathrm{id}$$
 $\stackrel{rm}{\Rightarrow} F + \mathrm{id} * \mathrm{id}$
 $\stackrel{rm}{\Rightarrow} E + \mathrm{id} * \mathrm{id}$
 $\stackrel{rm}{\Rightarrow} E + F * \mathrm{id}$
 $\stackrel{rm}{\Rightarrow} E + T * \mathrm{id}$
 $\stackrel{rm}{\Rightarrow} F + \mathrm{id} * \mathrm{id}$
 $\stackrel{rm}{\Rightarrow} F + \mathrm{id}$
 \stackrel



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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation

Rightmost Derivation

 $\stackrel{rm}{\Rightarrow}$ id + id * id

$E \stackrel{m}{\Longrightarrow} E + T$ $\stackrel{m}{\Longrightarrow} E + T * F$ $\stackrel{m}{\Longrightarrow} E + T * id$ $\stackrel{m}{\Longrightarrow} E + F * id$ $\stackrel{m}{\Longrightarrow} E + id * id$ $\stackrel{m}{\Longrightarrow} T + id * id$ $\stackrel{m}{\Longrightarrow} F + id * id$ $\stackrel{m}{\Longrightarrow} F + id * id$

id

id

$$id + id * id$$

$$\stackrel{m}{\Rightarrow} F + id * id$$

$$\stackrel{m}{\Rightarrow} T + id * id$$

$$\stackrel{m}{\Rightarrow} E + id * id$$

$$\stackrel{m}{\Rightarrow} E + F * id$$

$$\stackrel{m}{\Rightarrow} E + T * id$$

$$\stackrel{m}{\Rightarrow} E + T * F$$

$$\stackrel{m}{\Rightarrow} E + T * F$$

$$\stackrel{m}{\Rightarrow} E + T * F$$

$$\stackrel{m}{\Rightarrow} F + T * F$$

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Rightmost Derivation for Bottom-Up Parsing

Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

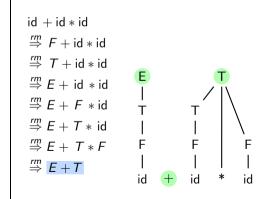
Rightmost Derivation

$E \stackrel{rm}{\Longrightarrow} E + T$ $\stackrel{rm}{\Longrightarrow} E + T * F$ $\stackrel{rm}{\Longrightarrow} E + F * id$ $\stackrel{rm}{\Longrightarrow} E + id * id$ $\stackrel{rm}{\Longrightarrow} T + id * id$ $\stackrel{rm}{\Longrightarrow} F + id * id$ $\stackrel{rm}{\Longrightarrow} F + id * id$

 $\stackrel{rm}{\Rightarrow}$ id + id * id

id

id





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SLR(1) Parsing

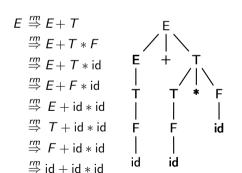
CLR(1) Parsing

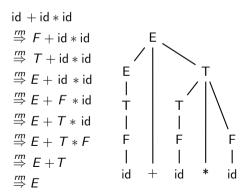
Rightmost Derivation for Bottom-Up Parsing

 $\overline{E} \rightarrow \overline{E} + T$ Grammar

Sentence: id + id * id

Rightmost Derivation







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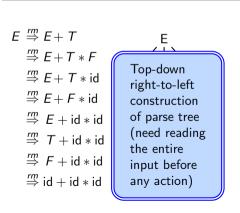
Rightmost Derivation for Bottom-Up Parsing

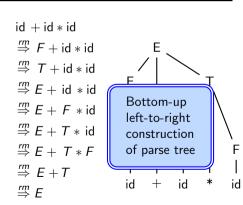
Grammar
$$E \rightarrow E + T \mid T$$

 $T \rightarrow T * F \mid F$
 $F \rightarrow \text{id}$

Sentence: id + id * id

Rightmost Derivation







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An Overview of Shift Reduce Parsing

Grammar Input

 $E \rightarrow id$

 $E \rightarrow E + E$ id + id * id

 $E \rightarrow E * E$



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 $\mathsf{LALR}(1) \; \mathsf{Parsing}$

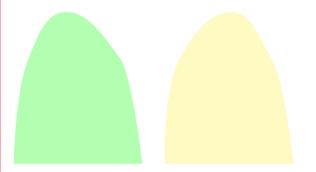
An Overview of Shift Reduce Parsing

Grammar

Input

 $E \rightarrow E + E$ $E \rightarrow E * E$ id + id * id

 $E{
ightarrow}$ id





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An Overview of Shift Reduce Parsing

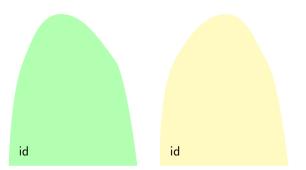
Grammar Input

 $E \rightarrow E + E$

 $E \rightarrow E * E$

 $E \rightarrow id$

 $\mathsf{id} + \mathsf{id} * \mathsf{id}$





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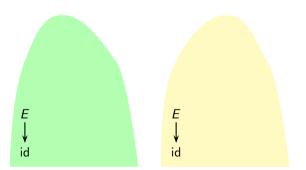
An Overview of Shift Reduce Parsing

Grammar Inp

Input

 $E \rightarrow E + E$ $E \rightarrow E * E$ id + id * id

 $E \rightarrow id$





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 $\mathsf{LALR}(1) \; \mathsf{Parsing}$

An Overview of Shift Reduce Parsing

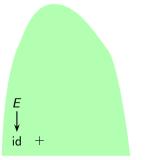
Grammar

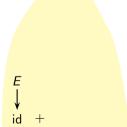
Input

 $E \rightarrow E + E$ $E \rightarrow E * E$

 $E \rightarrow id$

id + id * id







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SLR(1) Parsing

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CLR(1) Parsing

LALR(1) Parsing

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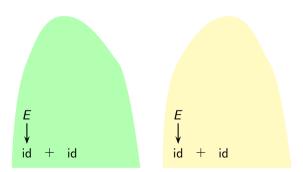
Grammar

Input

 $E \rightarrow E + E$

id + id * id

 $E \rightarrow E * E$ $E \rightarrow id$





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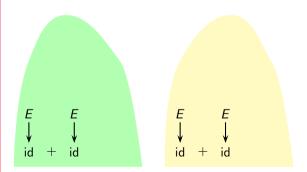
Input

$$E \rightarrow E + E$$

 $E \rightarrow E * E$

id + id * id

 $extit{E}
ightarrow ext{id}$





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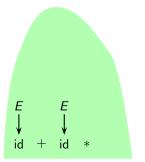
An Overview of Shift Reduce Parsing

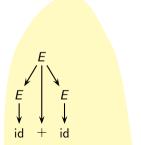
Grammar

Input

 $E \rightarrow E + E$ $E \rightarrow E * E$ id + id * id

 $extit{E}
ightarrow ext{id}$







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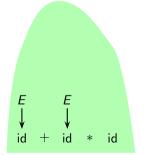
Grammar Ir

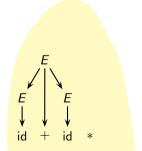
 $E \rightarrow E + E$ $E \rightarrow E * E$

 $E
ightarrow \operatorname{\mathsf{id}}$

Input

id + id * id







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Grammar

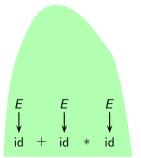
Input

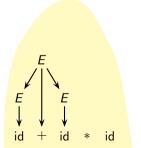
$$E \rightarrow E + E$$

 $E \rightarrow E * E$

$$id + id * id$$

 $E{
ightarrow}$ id







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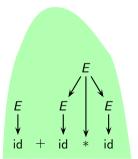
An Overview of Shift Reduce Parsing

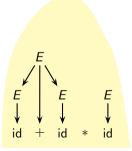
Grammar

Input

 $E \rightarrow E + E$ $E \rightarrow E * E$ id + id * id

 $E \rightarrow id$







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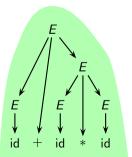
An Overview of Shift Reduce Parsing

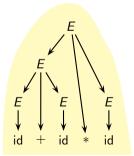
Grammar

Input

 $E \rightarrow E + E$ $E \rightarrow E * E$ id + id * id

 $E {
ightarrow} \operatorname{\mathsf{id}}$







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Grammar

Input

$$E \rightarrow E + E$$

 $E \rightarrow E * E$

$$id + id * id$$

$$E \rightarrow id$$

id

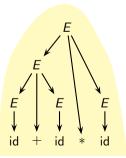
$$id + (id * id)$$

id



id

$$(id + id) * id$$





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Input

$$E \rightarrow E + E$$

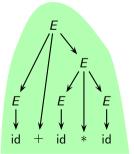
 $E \rightarrow E * E$

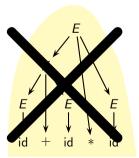
id + id * id

$$E{
ightarrow}$$
 id

$$id + (id * id)$$

$$(id + id) * id$$







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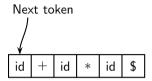
LALR(1) Parsin

An Overview of Shift Reduce Parsing

Grammar Input

 $E \rightarrow E + E$ id + id * id

 $E \rightarrow E * E$ $E \rightarrow id$



Next Action: Shift

id + (id * id)

1 1

Parsing Stack



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Grammar Input

 $E \rightarrow E + E$ id + id * id $F \rightarrow F * F$

Next token id id

id + (id * id)

 $E \rightarrow id$

Next Action: Reduce by $E \rightarrow id$

id

Parsing Stack

id



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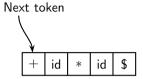
An Overview of Shift Reduce Parsing

Grammar Input

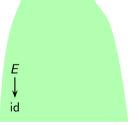
$$E \rightarrow E + E$$
 id + id * id

$$E \rightarrow E * E$$

 $E \rightarrow id$



$$id + (id * id)$$



Next Action: Shift



 ${\sf Parsing} \,\, {\sf Stack}$



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Grammar

Input

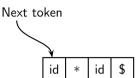
$$E \rightarrow E + E$$

 $F \rightarrow F * F$

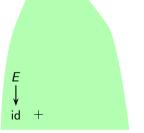
 $E \rightarrow id$

$$id + id * id$$

id + id * id



$$id + (id * id)$$



Next Action: Shift

Parsing Stack



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Grammar Input

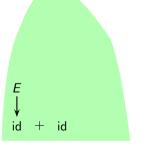
 $E \rightarrow E + E$

 $F \rightarrow F * F$ $E \rightarrow id$

id + id * id

Next token id

id + (id * id)



Next Action: Reduce by $E \rightarrow id$

Ε

id



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Input

$$E \rightarrow E + E$$

 $F \rightarrow F * F$

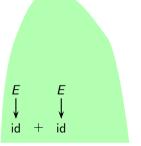
 $E \rightarrow id$

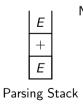
$$id + id * id$$

Next token

* id \$

$$id + (id * id)$$





Next Action: Shift



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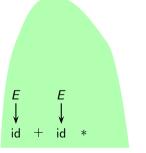
Grammar Input

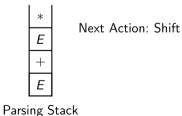
 $E \rightarrow E + E$ id + id * id

 $E \rightarrow E * E$ $E \rightarrow id$

Next token id \$

id + (id * id)







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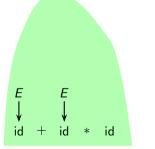
Grammar Input

 $E \rightarrow E + E$

 $E \rightarrow E * E$ $E \rightarrow id$ id + id * id

Next token

id + (id * id)





Next Action: Reduce by $E \rightarrow id$

Parsing Stack



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Grammar Input

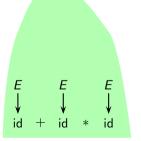
 $E \rightarrow E + E$ $F \rightarrow F * F$

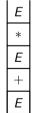
 $E \rightarrow id$

id + id * id

Next token

id + (id * id)





Next Action: Reduce by $E \rightarrow E * E$



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Grammar

Input

$$E \rightarrow E + E$$

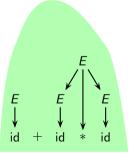
 $F \rightarrow F * F$

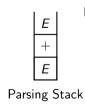
 $E \rightarrow id$

$$id + id * id$$

Next token

$$id + (id * id)$$





Next Action: Reduce by $E \rightarrow E + E$



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Grammar

Input

$$E \rightarrow E + E$$

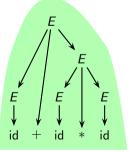
 $F \rightarrow F * F$

 $E \rightarrow id$

$$id + id * id$$

Next token

$$id + (id * id)$$



Next Action: Accept

Ε

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Grammar

Input

1. $E \rightarrow E + E$ 2. $E \rightarrow E * E$ id + id * id

3. $E \rightarrow id$



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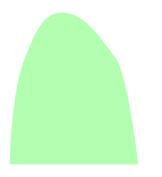
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift





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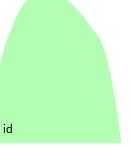
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id	+ id * id\$	reduce by 3





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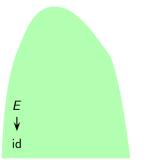
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift





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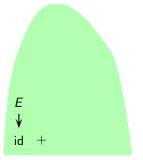
Grammar

Input

1. $E \rightarrow E + E$ 2. $E \rightarrow E * E$ id + id * id

3. $E \rightarrow id$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	shift





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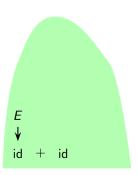
An Overview of Shift Reduce Parsing

Grammar

Input

1. $E \rightarrow E + E$

IC	+	- IC	*	ıd



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$E +	id * id\$	shift
5	E + id	* id\$	reduce by 3



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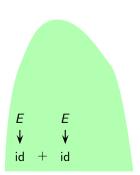
An Overview of Shift Reduce Parsing

Grammar

Input

1. $E \rightarrow E + E$

ıd	+	ıd	*	id



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	\$E + E	* id\$	shift



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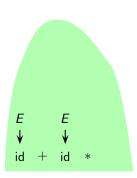
An Overview of Shift Reduce Parsing

Grammar

Input

1. $E \rightarrow E + E$

ıd	+	Ιd	*	id



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	\$E + E	* id\$	shift
7	\$E + E *	id\$	shift
i			



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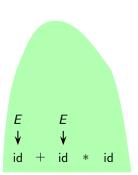
Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

3. $E \rightarrow id$



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	E + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3



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1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

3. $E \rightarrow id$

<i>E</i>	+	<i>E</i> ↓ id	*	<i>E</i> ↓ id	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$E +	id * id\$	
5	\$ <i>E</i> + id	* id\$	reduce by 3
6	\$E + E	* id\$	
7	\$E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	\$E+E*E	\$	reduce by 2



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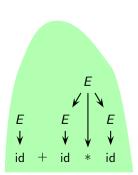
An Overview of Shift Reduce Parsing

Grammar

Input

1. $E \rightarrow E + E$

IC	1	- I	d	*	ıd



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$E +	id * id\$	shift
5	E + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift
7	\$E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	\$E+E*E	\$	reduce by 2
10	E + E	\$	reduce by 1
		_	



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Derivations, and Parse Trees

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SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsing

An Overview of Shift Reduce Parsing

Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$ 3. $E \rightarrow id$... , .

		E `\	E		
E		E		E	
↓ id	+	∀ id	*	∀ id	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$E +	id * id\$	shift
5	E + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift
7	\$E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	\$E+E*E	\$	reduce by 2
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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An Overview of Shift Reduce Parsing

Grammar

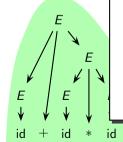
Input

1. $E \rightarrow E + E$ 2. $F \rightarrow F * F$

3. $F \rightarrow id$

- Observations
 - A shift corresponds to creating a leaf node in the parse tree whereas a reduce corresponds to creating an internal node
 - In every step i, concatenation of the stack and the remaining input gives a right sentential form (rsf_i)
 - For every step i, $rsf_{i+1} \stackrel{rm}{\Rightarrow} rsf_i$
 - In every step, the partial parse tree constructed until then, consists of a forest of trees
 - In every step, the stack holds the root nodes of the trees contained in the forest

A reduce action may amount to joining some of these trees



)	1	•	3
11	\$ <i>E</i>	\$	accept



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Shift Reduce Parsing

- In every step *i*, concatenation of the stack and the remaining input gives a right sentential form (rsf_i)
- For every step i, $rsf_{i+1} \stackrel{rm}{\Rightarrow} rsf_i$
- How do we go from rsf_i to rsf_{i+1} ?
 - $\circ S \stackrel{*rm}{\Rightarrow} \alpha A w \stackrel{rm}{\Rightarrow} \alpha \beta w$
 - $\circ~$ A bottom-up parser reduces β occurring in $\alpha\beta w$ to A using the production $A\to\beta$
 - $\circ~$ The rule ${\it A} \rightarrow \beta$ and the occurrence of β is the handle in $\alpha\beta {\it w}$



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Shift Reduce Parsing

- Bottom up parsing is essentially the process of detecting handles and reducing them
- Different bottom-up parsers differ in the way they detect handles



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Why do Handles Form the Basis of Bottom Up Parsing?

 Only terminal symbols can appear to the right of a handle in a rightmost sentential form

Why?

- \circ $S \stackrel{*rm}{\Rightarrow} \alpha A w \stackrel{rm}{\Rightarrow} \alpha \beta w$
- \circ Since we are using a rightmost derivation, there cannot be a non-terminal to the right of A.
- The beauty of bottom up parsing lies in dividing a right sentential form $\alpha\beta w$ into two parts



such that the handle always appears on the top of the stack



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Why do Handles Form the Basis of Bottom Up Parsing?

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Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

3. $E \rightarrow id$



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Why do Handles Form the Basis of Bottom Up Parsing?

Grammar

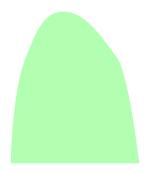
Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift





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Why do Handles Form the Basis of Bottom Up Parsing?

Grammar

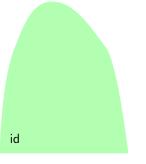
Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id	+ id * id\$	reduce by 3





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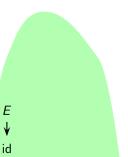
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift



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Why do Handles Form the Basis of Bottom Up Parsing?

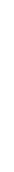
Grammar

Input

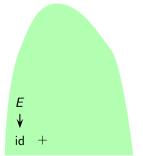
1. $E \rightarrow E + E$

id + id * id

2. $F \rightarrow F * F$ 3. $E \rightarrow id$



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	shift





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Why do Handles Form the Basis of Bottom Up Parsing?

Grammar

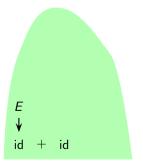
Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	shift
5	\$ <i>E</i> + id	* id\$	reduce by 3





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Why do Handles Form the Basis of Bottom Up Parsing?

Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift

E ↓ id	+	<i>E</i> ↓ id	



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Why do Handles Form the Basis of Bottom Up Parsing?

Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$ 3. $E \rightarrow id$ ia į ia s

E	Ε	

id

Step	$Stack \to$	Input	Action	
1	\$	id + id * id\$	shift	
2	\$ id	+ id * id\$	reduce by 3	
3	\$ <i>E</i>	+ id * id\$		
4	\$ <i>E</i> +	id * id\$		
5	\$ <i>E</i> + id		reduce by 3	
6	F + E	* id\$		
7	E + E *	id\$	shift	



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Why do Handles Form the Basis of Bottom Up Parsing?

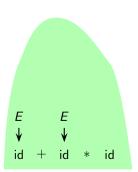
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	shift
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	shift
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
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Why do Handles Form the Basis of Bottom Up Parsing?

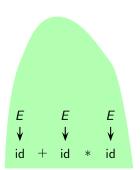
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	shift
5	\$ <i>E</i> + id	* id\$	reduce by 3
6	E + E	* id\$	shift
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
	•	•	•



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Why do Handles Form the Basis of Bottom Up Parsing?

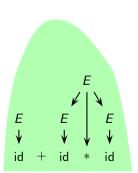
Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$



Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	shift
5	E + id		reduce by 3
6	F + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	E + E	\$	reduce by 1



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Why do Handles Form the Basis of Bottom Up Parsing?

Grammar

Input

1. $E \rightarrow E + E$

id + id * id

2. $E \rightarrow E * E$

3. $E \rightarrow id$

Ε

↓ id

, /	E	L E		
	E ↓	¥ [`	¥ E ↓	
+	id	*	id	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$ id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	shift
5	\$ <i>E</i> + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift
7	\$E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	F + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$



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SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		> 3√r1	<i>s</i> 4/ 冰 €	<i>r</i> 1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	r2	



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LALR(1) Parsin

SLR(1) Parsing Example

 $\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$

Shift reduce conflicts resolved using precedence and associativity

Parsing/Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2	,	/		<i>c</i> 6
5		≽ 3(/r1	<i>s</i> 4/ 冰 €	<i>r</i> 1	
6		≽ ₹/ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



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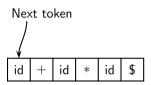
CLR(1) Parsing

LALR(1) Parsir

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$





Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	асс	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		> 3√r1	<i>5</i> 4/ 冰 €	r1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

Next Action: Shift 2



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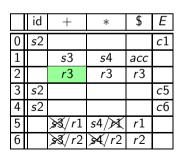
CLR(1) Parsing

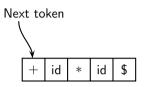
LALR(1) Parsir

SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$







Next Action: Reduce by Rule 3



Parsing Stack



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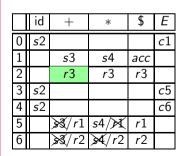
CLR(1) Parsing

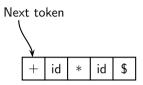
LALR(1) Parsii

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table





Next Action: Reduce by Rule 3

2 id 0



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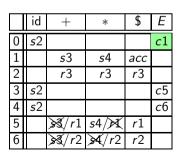
CLR(1) Parsing

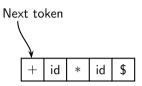
LALR(1) Parsin

SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$







Next Action: Cover by 1



Parsing Stack



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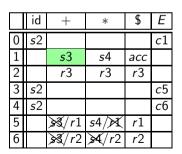
CLR(1) Parsing

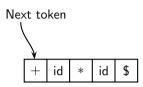
LALR(1) Parsin

SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$







Next Action: Shift 3



Parsing Stack



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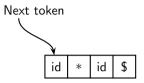
Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsir

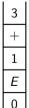
SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$



Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		≥ 3√r1	<i>s</i> 4/ <i>≯</i> €	<i>r</i> 1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Next Action: Shift 2



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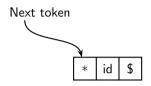
LALR(1) Parsii

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		. ,	<i>5</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Next Action: Reduce by Rule 3

id

3

+

E



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SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

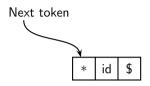
LALR(1) Parsii

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		. ,	<i>5</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



3 + 1 *E*

Next Action: Reduce by Rule 3



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

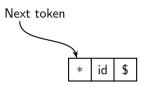
Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsin

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$



Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

Ε	
3	
+	
1	
Ε	
	3 +

Next Action: Cover by 5



Topic:

Syntax Analysis

Section:

Grammars,
Derivations, and Parse
Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

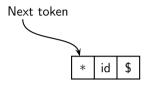
LALR(1) Parsir

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$		r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



3 + 1 E

5

Next Action: Shift 4



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

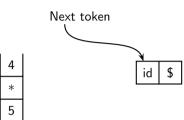
LALR(1) Parsir

SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Next Action: Shift 2

Ε

3

+

E



Topic:

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Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsir

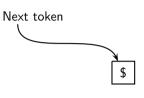
SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

2
id
4
*
5
Ε
3
+
1
Ε



Next Action: Reduce by Rule 3



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CLR(1) Parsing

LALR(1) Parsii

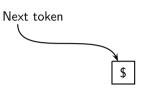
SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				c1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

2
id
4
*
5
Ε
3
+
1
Ε



Next Action: Reduce by Rule 3



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues i Parsing

CLR(1) Parsing

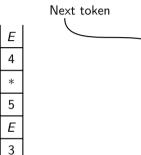
LALR(1) Parsir

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Next Action: Cover by 6

+

E



Topic:

 ${\sf Syntax} \ {\sf Analysis}$

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues i Parsing

CLR(1) Parsing

LALR(1) Parsir

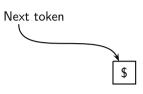
SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	//	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

6
Ε
4
*
5
Ε
3
+
1
Ε



Next Action: Reduce by 2



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues i Parsing

CLR(1) Parsing

LALR(1) Parsir

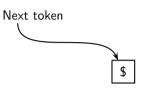
SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	/ /	r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

6
Ε
4
*
5
Ε
3
+
1
Ε



Next Action: Reduce by 2



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SLR(1) Parsing

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CLR(1) Parsing

LALR(1) Parsir

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$



Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	r1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

E	
3	
+	
1	
Ε	
	ı

Next Action: Cover by 5



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

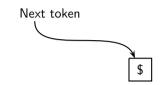
LALR(1) Parsir

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	<i>r</i> 1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



3 + 1 E

5

Next Action: Reduce by Rule ${\bf 1}$



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Trees

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Conceptual Issues in Parsing

CLR(1) Parsing

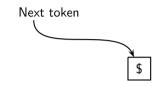
LALR(1) Parsii

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$

Parsing Table

_					_
	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 €	<i>r</i> 1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



E 3 + 1 E

Next Action: Reduce by Rule 1



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SLR(1) Parsing

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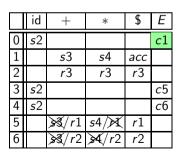
CLR(1) Parsing

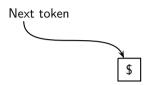
LALR(1) Parsin

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$







Next Action: Cover by 1



Parsing Stack



Topic:

Syntax Analysis

Section:

Derivations, and Parse

SLR(1) Parsing

CLR(1) Parsing

SLR(1) Parsing Example

$$\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$$



Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$		r1	
6		≽ 3√ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Next Action: Accept



Parsing Stack



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Syntax Analysis

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Derivations, and Pars Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsing

SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$



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Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsing

SLR(1) Parsing Example

$$1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		≥ 3√r1	<i>s</i> 4/ <i>≯</i> €	<i>r</i> 1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Topic:

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Trees

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SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsin

SLR(1) Parsing Example

 $\begin{array}{c} 1 \ E \rightarrow E + E \\ 2 \ E \rightarrow E * E \\ 3 \ E \rightarrow \text{id} \end{array}$

Shift reduce conflicts resolved using precedence and associativity

Parsing/Table

	id	+	*	\$	Ε
0	<i>s</i> 2				c1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2	,	/		<i>c</i> 6
5		≽ 3(/r1	<i>s</i> 4/ 冰 €	<i>r</i> 1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	<i>r</i> 2	



Topic:

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SLR(1) Parsing

Conceptual Issues i Parsing

CLR(1) Parsing

LALR(1) Parsii

SLR(1) Parsing Example

Combining the reduce and the following cover operation into a single step for convenience

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		> 3√r1	<i>s</i> 4/ 冰 €	<i>r</i> 1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

Step	Stack o -	Input	Action
1	\$0	.ંત + id ∗ id\$	<i>s</i> 2
2	\$0 id 2	+ id * iu 🗘	<i>r</i> 3 and <i>c</i> 1
3	\$0 E 1	+ id * id\$	<i>s</i> 3
4	\$0 E 1 + 3	id * id\$	<i>s</i> 2
5	\$0 E 1 + 3 id 2	* 10.4	r3 and <i>c</i> 5
6	\$0 E 1 + 3 E 5	* id\$	<i>s</i> 4
7	\$0 E 1 + 3 E 5 * 4	id\$	<i>s</i> 2
8	\$0 E 1 + 3 E 5 * 4 id 2	*	<i>r</i> 3 and <i>c</i> 6
9	\$0 E 1 + 3 E 5 * 4 E6	**	r2 and <i>c</i> 5
10	\$0 E 1 + 3 E 5	+	<i>r</i> 1 and <i>c</i> 1
11	\$0 E 1	\$	accept



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Shift Reduce Parsing

SLR(1) Parsing

Parsing

CLR(1) Parsing

LALR(1) Parsing

SLR(1) Parsing Example

 $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$

Parsing Table

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		≥ 3√r1	<i>s</i> 4/ <i>≯</i> €	<i>r</i> 1	
6		≽ 3√r2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

Step	$Stack \to$	Input	Action
1	\$0	id + id * id\$	<i>s</i> 2
2	\$0 id 2	+ id * id\$	<i>r</i> 3 and <i>c</i> 1
3	\$0 E 1	+ id * id\$	<i>s</i> 3
4	\$0 E 1 + 3	id * id\$	<i>s</i> 2
5	\$0 E 1 + 3 id 2	* id\$	<i>r</i> 3 and <i>c</i> 5
6	\$0 E 1 + 3 E 5	* id\$	<i>s</i> 4
7	\$0 E 1 + 3 E 5 * 4	id\$	<i>s</i> 2
8	\$0 E 1 + 3 E 5 * 4 id 2	\$	<i>r</i> 3 and <i>c</i> 6
9	\$0 E 1 + 3 E 5 * 4 E6	\$	<i>r</i> 2 and <i>c</i> 5
10	\$0 E 1 + 3 E 5	\$	<i>r</i> 1 and <i>c</i> 1
11	\$0 E 1	\$	accept



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LALR(1) Parsii

Shift Reduce Parsing: From Intuitions to Formal Algorithms

We undertake this journey in six steps using the ambiguous grammar of expressions. It illustrates how yacc allows disambiguating a grammar without rewriting it

$$\begin{array}{ccc} E & \rightarrow & E+E \\ E & \rightarrow & E*E \\ E & \rightarrow & \text{id} \end{array}$$

1. We assume that both + and * are left associative and * takes precedence over + We see the influence of these choices on derivations by considering four inputs

$$id + id + id$$
, $id * id * id$, $id + id * id$, and $id * id + id$.

2. We see the meaning of a shift reduce parser tracing the rightmost derivation in reverse

We see the meaning of handle pruning in tracing the rightmost derivation

- 3. We define the notions of viable prefixes for discovering handles
- 4. We define valid items to recognize viable prefixes
- 5. We define FOLLOW sets to define a criterion of handle pruning
- 6. We see the algorithm that constructs valid items



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Shift Reduce Parsing: From Intuitions to Formal Algorithms

$$1 E \rightarrow E + E$$

$$2 E \rightarrow E * E$$

$$3~\textit{E} \rightarrow id$$



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Grammars,
Derivations, and Parse
Trees

Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsing

Shift Reduce Parsing: From Intuitions to Formal Algorithms

$$1 E \rightarrow E + E$$
$$2 E \rightarrow E * E$$

 $3 E \rightarrow id$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	E + E	* id\$	shift
7	E + E *		shift
8	E + E * id		reduce by 3
9	E + E * E		reduce by 2
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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Shift Reduce Parsing: From Intuitions to Formal Algorithms

 $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$ Shift reduce conflicts resolved using precedence and associativity

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5	1	$\Re/r1$	<i>5</i> 4/ 冰 €	r1	
6		≽ €/r2	≽4 /r2	<i>r</i> 2	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	E + E	* id\$	shift
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept

Step	$Stack \to$	Input	Action
1	\$0	id + id * id\$	<i>s</i> 2
2	\$0 id 2	+ id * id\$	<i>r</i> 3 and <i>c</i> 1
3	\$0 E 1	+ id * id\$	<i>s</i> 3
4	\$0 E 1 + 3	id * id\$	<i>s</i> 2
5	\$0 E 1 + 3 id 2		<i>r</i> 3 and <i>c</i> 5
6	\$0 E 1 + 3 E 5	* id\$	<i>s</i> 4
7	\$0 E 1 + 3 E 5 * 4	id\$	<i>s</i> 2
8	\$0 E 1 + 3 E 5 * 4 id 2	\$	r3 and c 6
9	\$0 E 1 + 3 E 5 * 4 E6	\$	<i>r</i> 2 and <i>c</i> 5
10	\$0 E 1 + 3 E 5	\$	<i>r</i> 1 and <i>c</i> 1
11	\$0 <i>E</i> 1	\$	accept



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Shift Reduce Parsing: From Intuitions to Formal Algorithms

 $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$

Combining the reduce and the following cover operation into a single step for convenience

_	id	+	*	\$	Ε
	-2				<i>c</i> 1
		<i>s</i> 3	<i>s</i> 4	acc	
		r3	<i>r</i> 3	<i>r</i> 3	
					<i>c</i> 5
	/				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 (r1	
6		≽ 3√ <i>r</i> 2	≽4 / <i>r</i> 2	<i>r</i> 2	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	E + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id		
9	E + E * E		reduce by 2
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept

- '			
2\te\	\stack →	Input	Action
1		id + id * id\$	<i>s</i> 2
2	\$7 ic 2	+ iu - iu	<i>r</i> 3 and <i>c</i> 1
3	\$0 = 1	+ id * id\$	<i>s</i> 3
4	37 E 7 + 3	id * id\$	<i>s</i> 2
5	\$0 <u>5</u> 1 + 3 ià 2	* IU#	<i>r</i> 3 and <i>c</i> 5
6	\$0 E 1 - 3 \(\bar{5} \)	* id\$	<i>s</i> 4
7	\$0 E 1 + 3 = 5 * 1	id\$	<i>s</i> 2
8	\$0 E 1 + 3 E 5 . 4 id 2	7	<i>r</i> 3 and <i>c</i> 6
9	\$0 E 1 + 3 E 5 * 4 E		<i>r</i> 2 and <i>c</i> 5
10	\$0 E 1 + 3 E 5	+	<i>r</i> 1 and <i>c</i> 1
11	\$0 <i>E</i> 1	\$	accept



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Shift Reduce Parsing: From Intuitions to Formal Algorithms

 $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$ How do we make this journey?

	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		$\mathcal{A}/r1$	<i>s</i> 4/ 冰 (r1	
6		≽ 3√r2	≽4 /r2	<i>r</i> 2	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	E + E	* id\$	
7	\$E + E *		shift
8	E + E * id		reduce by 3
9	\$E + E * E		reduce by 2
10	F + E		reduce by 1
11	\$ <i>E</i>	\$	accept

>	Step	$Stack \to$	Input	Action
	1	\$0	id + id * id\$	<i>s</i> 2
	2	\$0 id 2	+ id * id\$	<i>r</i> 3 and <i>c</i> 1
	3	\$0 <i>E</i> 1	+ id * id\$	<i>s</i> 3
	4	\$0 E 1 + 3	id * id\$	<i>s</i> 2
	5	\$0 E 1 + 3 id 2	* id\$	<i>r</i> 3 and <i>c</i> 5
	6	\$0 E 1 + 3 E 5	* id\$	<i>s</i> 4
	7	\$0 E 1 + 3 E 5 * 4	id\$	<i>s</i> 2
	8	\$0 E 1 + 3 E 5 * 4 id 2	\$	<i>r</i> 3 and <i>c</i> 6
	9	\$0 E 1 + 3 E 5 * 4 E6	\$	<i>r</i> 2 and <i>c</i> 5
	10	\$0 E 1 + 3 E 5	\$	<i>r</i> 1 and <i>c</i> 1
	11	\$0 <i>E</i> 1	\$	accept



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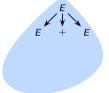
CLR(1) Parsing

LALR(1) Parsing

Step 1: Precedence and Associativity Rule Out Undesirable Derivations

 $\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$

 $E \stackrel{rm}{\Rightarrow} E + E$





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CLR(1) Parsing

LALR(1) Parsing

Step 1: Precedence and Associativity Rule Out Undesirable Derivations

 $\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$





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CLR(1) Parsing

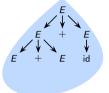
LALR(1) Parsing

$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$





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LALR(1) Parsing

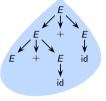
$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$





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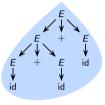
$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{\mathit{rm}}{\Rightarrow} \mathit{E} + \mathsf{id} + \mathsf{id}$$

$$\stackrel{\mathit{rm}}{\Rightarrow} \mathsf{id} + \mathsf{id} + \mathsf{id}$$





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LALR(1) Parsing

$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

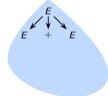
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$

$$E \stackrel{rm}{\Rightarrow} E + E$$





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$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

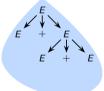
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + E + E$$





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$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

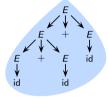
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

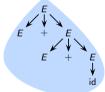
$$\stackrel{\mathit{rm}}{\Rightarrow} E + \mathsf{id} + \mathsf{id}$$

$$\Rightarrow E + id + id
\Rightarrow E + id + id
\Rightarrow id + id + id$$



$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + E + E$$

$$\stackrel{\mathit{rm}}{\Rightarrow} E + E + \mathsf{id}$$





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Input
$$id + id + id$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

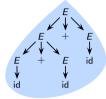
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{\mathit{rm}}{\Rightarrow} E + \mathsf{id} + \mathsf{id}$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

$$\stackrel{rm}{\Rightarrow} id + id + id$$



$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + E + E$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$





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$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$

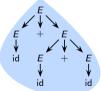
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + E + E$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{\mathit{rm}}{\Rightarrow} E + \mathrm{id} + \mathrm{id}$$

$$\stackrel{\mathit{rm}}{\Rightarrow} \mathsf{id} + \mathsf{id} + \mathsf{id}$$





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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

 $\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$

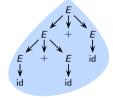
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

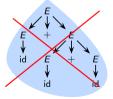
$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$







 $+\ \mbox{is left associative}$



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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

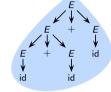
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$

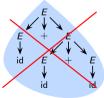


Input
$$id * id + id$$

$$E \stackrel{rm}{\Rightarrow} E + E$$



$$\stackrel{m}{\Longrightarrow} E + E \\
\stackrel{m}{\Longrightarrow} E + E + E \\
\stackrel{m}{\Longrightarrow} E + id \\
\stackrel{m}{\Longrightarrow} E + id + id \\
\stackrel{m}{\Longrightarrow} id + id + ic$$



+ is left associative



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Step 1: Precedence and Associativity Rule Out Undesirable **Derivations**

Input
$$id + id + id$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$
 $\stackrel{rm}{\Rightarrow} E + E + id$

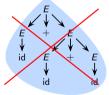
$$\Rightarrow E + E + id$$

 $\stackrel{rm}{\Rightarrow} E + id + id$

$$\stackrel{rm}{\Rightarrow}$$
 id + id + id







+ is left associative

Input id * id + id

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$





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Step 1: Precedence and Associativity Rule Out Undesirable **Derivations**

$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

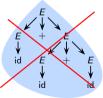
$$\stackrel{rm}{\Rightarrow} E + id$$
 $\stackrel{rm}{\Rightarrow} E + E + id$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

$$\stackrel{rm}{\Rightarrow}$$
 id + id + id







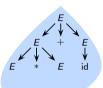
+ is left associative

Input
$$id * id + id$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E * E + id$$





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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

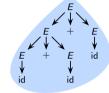
$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$



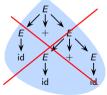
$$E \Rightarrow E + E$$

$$\Rightarrow E + E + E$$

$$\Rightarrow E + E + id$$

$$\Rightarrow E + id + id$$

$$\Rightarrow id + id + id$$



+ is left associative

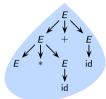
 $\mathsf{Input}\;\mathsf{id}*\mathsf{id}+\mathsf{id}$

$$E \stackrel{m}{\Longrightarrow} E + E$$

$$\stackrel{m}{\Longrightarrow} E + id$$

$$\stackrel{m}{\Longrightarrow} E * E + id$$

$$\stackrel{m}{\Longrightarrow} E * id + id$$





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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

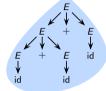
$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

$$\stackrel{rm}{\Rightarrow} id + id + id$$

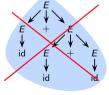


$$E \stackrel{rm}{\Longrightarrow} E + E$$

$$\stackrel{rm}{\Longrightarrow} E + E + id$$

$$\stackrel{rm}{\Longrightarrow} E + id + id$$

$$\stackrel{rm}{\Longrightarrow} id + id + id$$



+ is left associative

 $\mathsf{Input}\;\mathsf{id}*\mathsf{id}+\mathsf{id}$

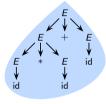
$$E \stackrel{m}{\Longrightarrow} E + E$$

$$\stackrel{m}{\Longrightarrow} E + id$$

$$\stackrel{m}{\Longrightarrow} E * E + id$$

$$\stackrel{m}{\Longrightarrow} E * id + id$$

$$\stackrel{m}{\Longrightarrow} id * id + id$$





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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

Input
$$id + id + id$$

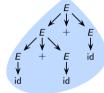
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$
 $\stackrel{rm}{\Rightarrow} E + E + id$

$$\Rightarrow E + E + id$$

 $\stackrel{rm}{\Rightarrow} E + id + id$

$$\stackrel{rm}{\Rightarrow}$$
 id + id + id



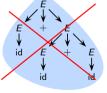
$$E \stackrel{m}{\Rightarrow} E + E$$

$$\stackrel{m}{\Rightarrow} E + F + E$$

$$\stackrel{m}{\Rightarrow} E + id$$

$$\stackrel{m}{\Rightarrow} E + id + id$$

$$\stackrel{m}{\Rightarrow} id + id + id$$



+ is left associative

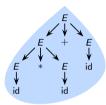
Input id*id+id

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$

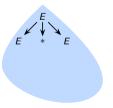
$$\stackrel{rm}{\Rightarrow} E * E + id$$

$$\stackrel{rm}{\Rightarrow} E * id + id$$





$$E \stackrel{rm}{\Rightarrow} E * E$$





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CLR(1) Parsing

Step 1: Precedence and Associativity Rule Out Undesirable Derivations

Input
$$id + id + id$$

$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$







+ is left associative

Input
$$id*id+id$$

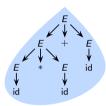
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

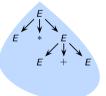
$$\stackrel{rm}{\Rightarrow} E * E + id$$

$$\stackrel{rm}{\Rightarrow} E * id + id$$

$$\stackrel{rm}{\Rightarrow} id * id + id$$









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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

Input
$$id + id + id$$

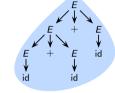
$$E \stackrel{rm}{\Longrightarrow} E + E$$

$$\stackrel{rm}{\Longrightarrow} E + id$$

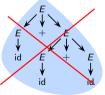
$$\stackrel{rm}{\Longrightarrow} E + E + id$$

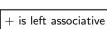
$$\stackrel{rm}{\Longrightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$









Input id*id+id

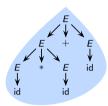
$$E \stackrel{rm}{\Longrightarrow} E + E$$

$$\stackrel{rm}{\Longrightarrow} E + id$$

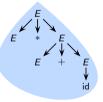
$$\stackrel{rm}{\Longrightarrow} E * E + id$$

$$\stackrel{rm}{\Longrightarrow} E * id + id$$

$$\stackrel{rm}{\Longrightarrow} id * id + id$$









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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

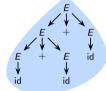
Input
$$id + id + id$$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$

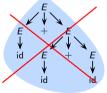
$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

$$\stackrel{\it rm}{\Rightarrow}$$
 id + id + id







+ is left associative

Input id*id+id

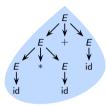
$$E \stackrel{mm}{\Rightarrow} E + E$$

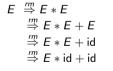
$$\stackrel{mm}{\Rightarrow} E + id$$

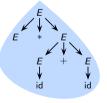
$$\stackrel{m}{\Rightarrow} E * E + id$$

$$\stackrel{m}{\Rightarrow} E * id + id$$

$$\stackrel{m}{\Rightarrow} id * id + id$$









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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

$$\mathsf{Input}\;\mathsf{id} + \mathsf{id} + \mathsf{id}$$

$$E \stackrel{rm}{\Rightarrow} E + E$$
$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$







+ is left associative

Input
$$id * id + id$$

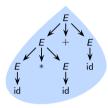
$$E \stackrel{rm}{\Rightarrow} E + E$$

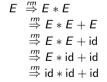
$$\stackrel{rm}{\Rightarrow} E + id$$

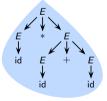
$$\stackrel{rm}{\Rightarrow} E * E + id$$

$$\stackrel{rm}{\Rightarrow} E * id + id$$

$$\stackrel{rm}{\Rightarrow} id * id + id$$









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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

Input
$$id + id + id$$

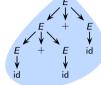
$$E \stackrel{rm}{\Rightarrow} E + E$$

$$\stackrel{rm}{\Rightarrow} E + id$$

$$\stackrel{rm}{\Rightarrow} E + E + id$$

$$\stackrel{rm}{\Rightarrow} E + id + id$$

 $\stackrel{rm}{\Rightarrow} id + id + id$



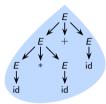




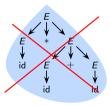












* has a higher precedence than +



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Step 1: Precedence and Associativity Rule Out Undesirable Derivations

Input id + id + id

Input id * id + id

rm ⊏ . ⊏

 $F \stackrel{rm}{\rightleftharpoons} F \perp F$

The moral of the story

- Right sentential forms containing the strings E+E+E, E*E*E, and E*E+E are ruled out by our choice of precedence and associativity
- The grouping that we want is (E+E)+E, (E*E)*E, and (E*E)+E so the non-terminals in the parenthesis should be derived first
- However, the parenthesized term does not occur in the rightmost position and hence it cannot be derived first in a rightmost derivation
- The string E + E * E can appear in a rightmost derivation because the grouping is E + (E * E) and the parenthesized term occurs in the rightmost position

+ is left associative

* has a higher precedence than +



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Step 2: Shift Reduce Actions, Rightmost Derivations, and Handles

 $E \stackrel{rm}{\Rightarrow} E + E \stackrel{rm}{\Rightarrow} E + E * E \stackrel{rm}{\Rightarrow} E + E * id \stackrel{rm}{\Rightarrow} E + id * id \stackrel{rm}{\Rightarrow} id + id * id$

 $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id	\$	
9	E + E * E	\$	reduce by 2
10	\$ <i>E</i> + <i>E</i>	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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Step 2: Shift Reduce Actions, Rightmost Derivations, and Handles

 $E \stackrel{m}{\Rightarrow} E + E \stackrel{m}{\Rightarrow} E + E * E \stackrel{m}{\Rightarrow} E + E * id \stackrel{m}{\Rightarrow} E + id * id \stackrel{m}{\Rightarrow} id + id * id$ $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	E + E *	id\$	
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$ <i>E</i> + <i>E</i>	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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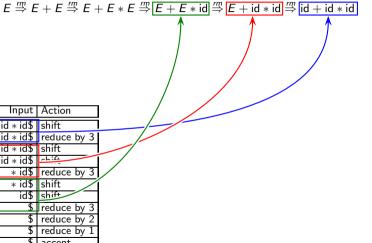
Conceptual Issues in Parsing

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Step	Stack o	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	\$E + E	* id\$	
7	E + E *		shif+
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept





 $1 E \rightarrow E + E$

 $2 E \rightarrow E * E$

Step Stack \rightarrow

\$id

\$E

10

\$E +

E + id

\$E + E

\$E + E

\$E

 $3 E \rightarrow id$

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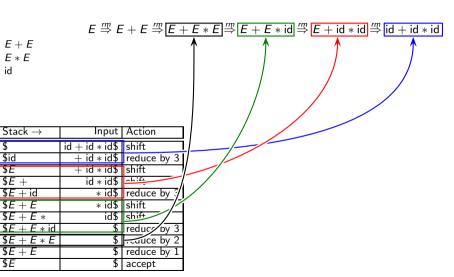
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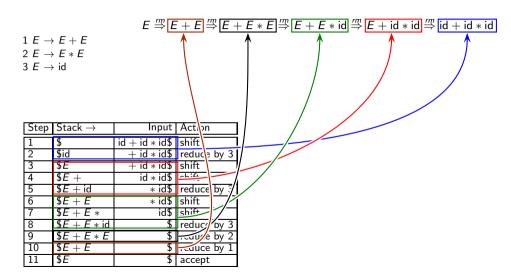
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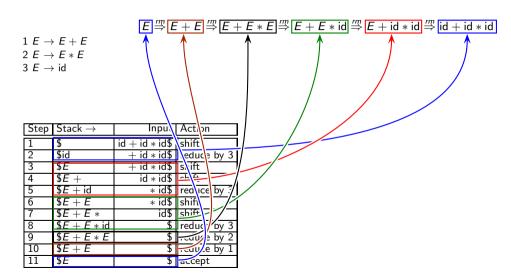
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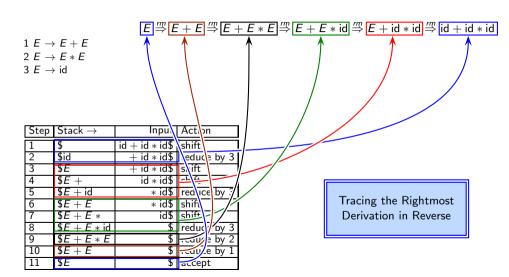
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Step 2: Shift Reduce Actions, Rightmost Derivations, and Handles

 $E \stackrel{m}{\Rightarrow} E + E \stackrel{m}{\Rightarrow} E + E * E \stackrel{m}{\Rightarrow} E + E * id \stackrel{m}{\Rightarrow} E + id * id \stackrel{m}{\Rightarrow} id + id * id$

 $1 E \rightarrow E + E$ $2 E \rightarrow E * E$ $3 E \rightarrow id$

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id	+ id * id\$	reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	F + E	* id\$	
7	E + E *		shift
8	E + E * id		reduce by 3
9	E + E * E		reduce by 2
10	\$E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept

Rightmost derivations are traced in reverse by identifying handles in right sentential forms (beginning with the sentence) and pruning them for constructing the previous right sentential form



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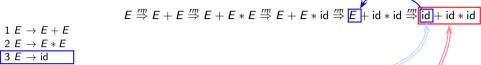
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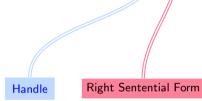
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Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$ <i>E</i> + <i>E</i>	\$	reduce by 1
11	\$ <i>E</i>	\$	accept





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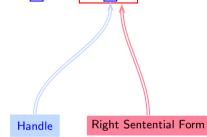
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Step	Stack o	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
	\$ <i>E</i> +	id*id\$	
5	\$ <i>E</i> + id		reduce by 3
6	\$ <i>E</i> + <i>E</i>	* id\$	shift
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$ <i>E</i> + <i>E</i>	\$	reduce by 1
11	\$ <i>E</i>	\$	accept





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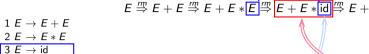
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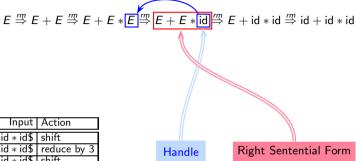
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Step	Stack o	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	\$ <i>E</i> + <i>E</i> ∗		_shift
8	E + E * id		reduce by 3
9	E + E * E	\$	reduce by 2
10	\$ <i>E</i> + <i>E</i>	\$	reduce by 1
11	\$ <i>E</i>	\$	accept





 $1~E \rightarrow E + E$

 $2 E \rightarrow E * E$

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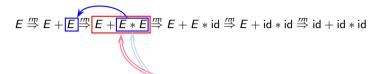
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Step 2: Shift Reduce Actions, Rightmost Derivations, and Handles



Step	Stack \rightarrow	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	E + E *		
8	E + E * id		reduce by 3
9	E + E * E		reduce by 2
10	\$ <i>E</i> + <i>E</i>	\$	reduce by 1
11	\$ <i>E</i>	\$	accept

Handle

Right Sentential Form



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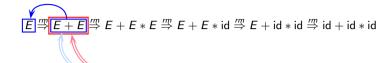
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Step 2: Shift Reduce Actions, Rightmost Derivations, and Handles



Step	Stack o	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	\$ <i>E</i> + id		reduce by 3
6	E + E	* id\$	
7	E + E *		shift
8	E + E * id		reduce by 3
9	\$E + E * E		reduce by 2
10	\$ <i>E</i> + <i>E</i>		reduce by 1
11	\$ <i>E</i>	\$	accept

1~E
ightarrow E + E

 $2 E \rightarrow E * E$

 $3 E \rightarrow id$

Handle

Right Sentential Form



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Step 3: Identifying Handles in Right Sentential Forms

- Our goal is to discover a prefix of right sentential form that ends with a handle
- Viable Prefix. A prefix of a right sentential form that does not extend beyond the handle
 - It is either a string with no handle, or
 - o a string that ends with the handle
- By suffixing appropriate symbols to a viable prefix of the first kind, we can create a viable prefix of the second kind
- By suffixing terminal symbols to the viable prefix of the second kind, we can create a right sentential form
- The set of viable prefixes forms a regular language, thus they can be recognized by a DFA
- The handles in a viable prefix can be identified using a stack
- We keep pushing viable prefixes on the stack until the handle appears on the top of the stack



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Step 3: Viable Prefixes for Our Grammar (After Incorporating Precedences and Associativities)

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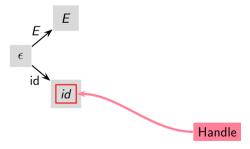
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Step 3: Viable Prefixes for Our Grammar (After Incorporating Precedences and Associativities)



Viable prefix id must be reduced to *E* and no grammar symbol can be suffixed to it (because there is no rule with a symbol after id)



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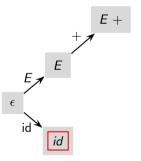
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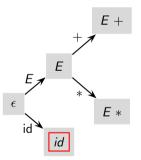
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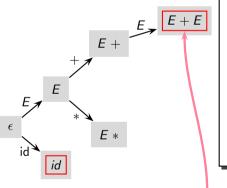
SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsi

Step 3: Viable Prefixes for Our Grammar (After Incorporating Precedences and Associativities)



Viable prefix E + E must be reduced to E if it is not followed by a "*"

If E + E is followed by a "*", "*" should be shifted and E + E should not be reduced

The occurrence of a potential handle does not mean it should be reduced, the next terminal symbol decides whether it is an actual handle (and if so, it should be reduced)

Handle



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Shift Reduce Parsing

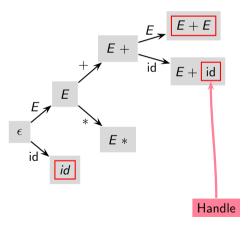
SLR(1) Parsing

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Step 3: Viable Prefixes for Our Grammar (After Incorporating Precedences and Associativities)



Viable prefix E + id must be reduced to E + E and no grammar symbol can be suffixed to it



Topic:

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Shift Reduce Parsing

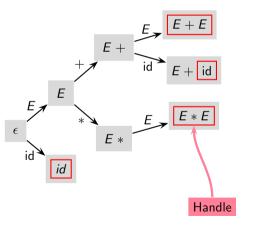
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Step 3: Viable Prefixes for Our Grammar (After Incorporating Precedences and Associativities)



Viable prefix E * E must be reduced to E and no grammar symbol can be suffixed to it



Topic:

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Shift Reduce Parsing

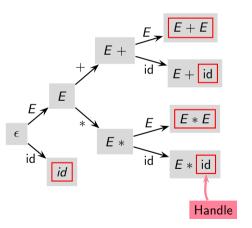
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Step 3: Viable Prefixes for Our Grammar (After Incorporating Precedences and Associativities)



Viable prefix E * id must be reduced to E * E and no grammar symbol can be suffixed to it



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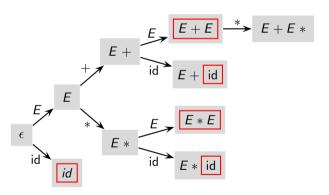
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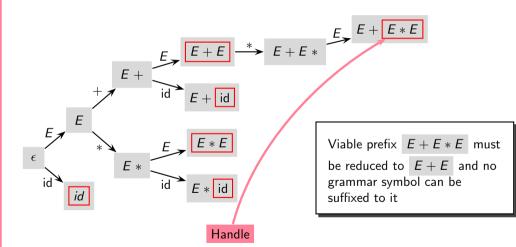
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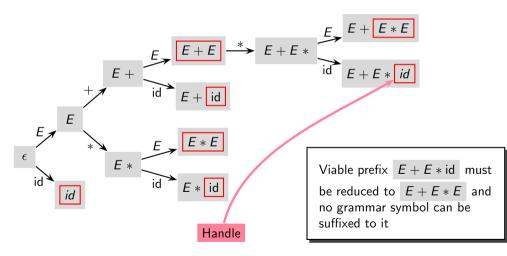
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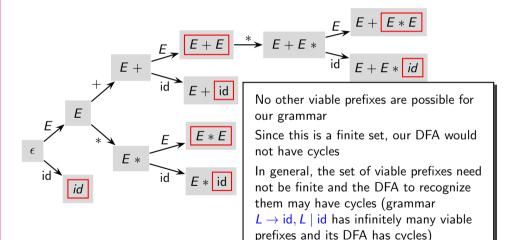
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Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	\$E + E	* id\$	
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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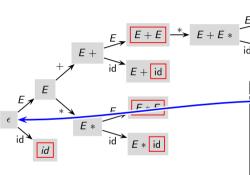
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	$Stack \to$	Input	Action
-	Œ	11 11 110	-L:C
_	\$	id + id * id\$	
2 3	\$id		reduce by 3
	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	
5	E + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift
7	\$E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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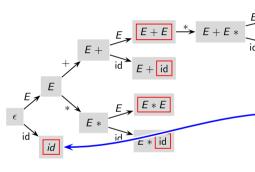
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Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	
5	E + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	\$E + E * E	\$	reduce by 2
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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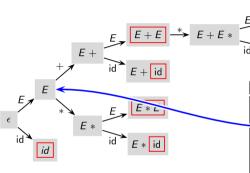
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Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	shift
2	\$id		reduce by 3
-	\$ <i>E</i>	+ id * id\$	shift
4	\$ <i>E</i> +	id * id\$	
5	E + id	* id\$	reduce by 3
6	\$E + E	* id\$	shift
7	E + E *	id\$	shift
8	E + E * id	\$	reduce by 3
9	E + E * E	\$	reduce by 2
10	\$E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept



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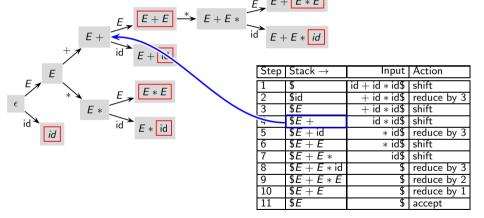
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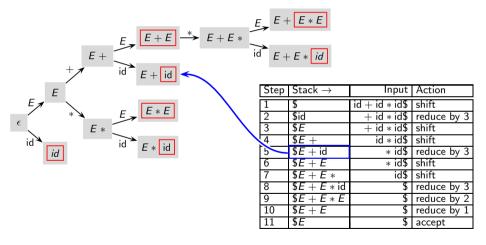
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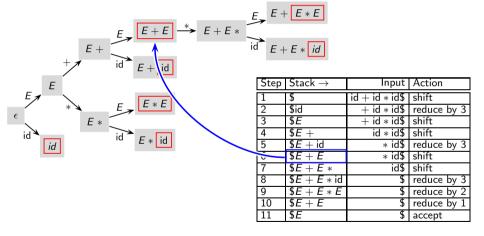
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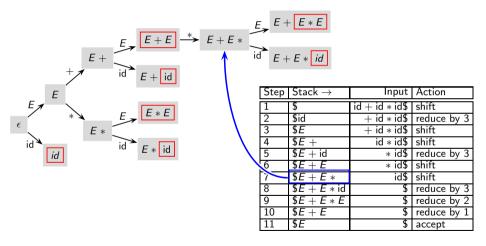
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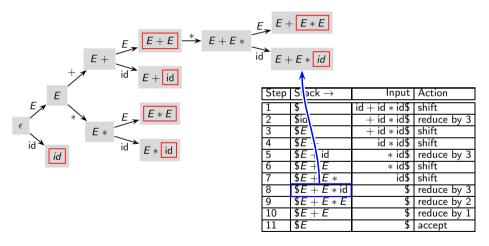
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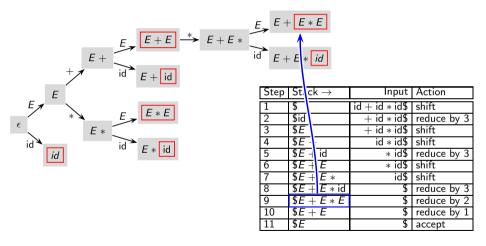
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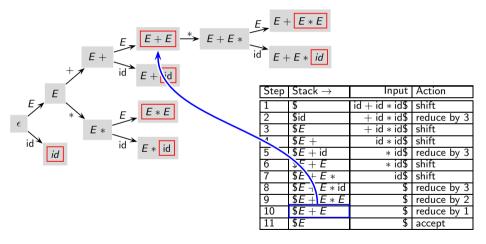
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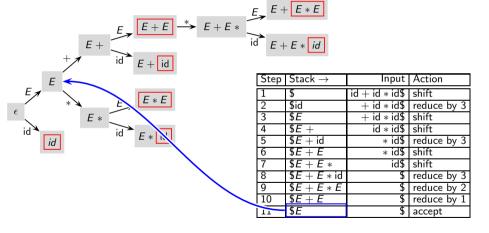
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- An item is a grammar production with a dot (•) in it somewhere in the RHS
- The dot separates what has been seen from what may be seen in the input
- We identify a set of items for a viable prefix to form a state of the parser



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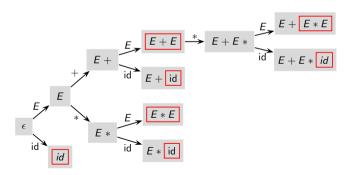
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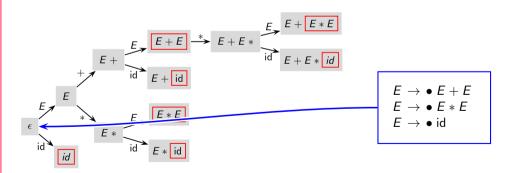
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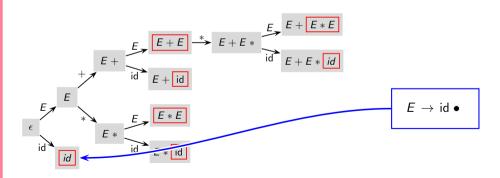
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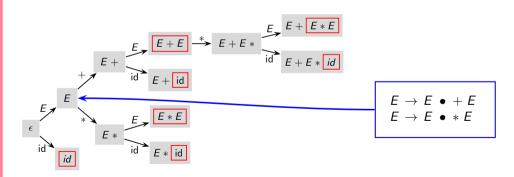
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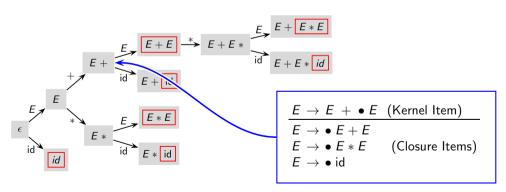
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Shift Reduce Parsir

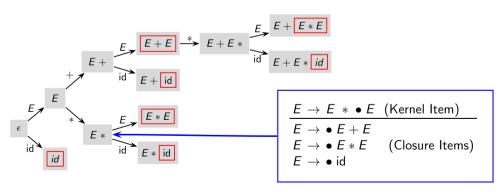
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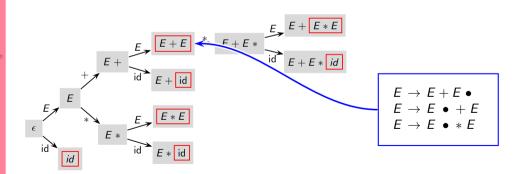
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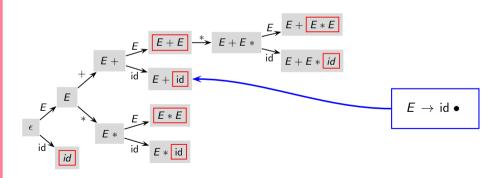
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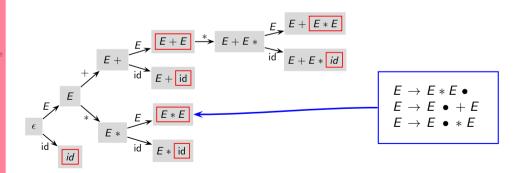
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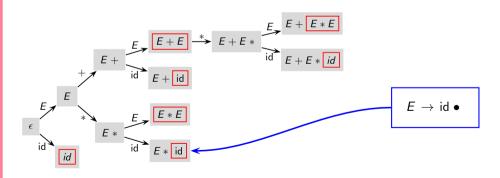
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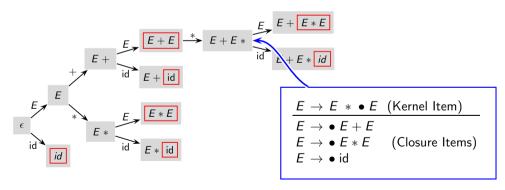
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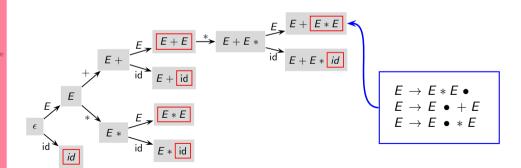
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Step 4: Valid Items for Viable Prefixes

• An item is a grammar production with a dot (•) in it somewhere in the RHS

• The dot separates what has been seen from what may be seen in the input

- We iden
- An item set may not describe a viable prefix on its own (Prefixes of a viable prefix may be described by other item sets)
- Item sets for different viable prefixes may be same
- In practice, we do not construct the viable prefixes and then the item sets for them

We do the opposite: we construct the item sets and the transitions between them give us the viable prefixes





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Step 5: The Last Piece of Jigsaw Puzzle: Computing FOLLOW Sets

Consider $\beta Aw \stackrel{rm}{\Rightarrow} \beta \alpha w$ and $A \rightarrow \alpha$

When do we reduce occurrence of α in $\gamma = \beta \alpha$ using $A \to \alpha$ using LR(k) items? (i.e., when do we decide that α and $A \to \alpha$ form a handle in γ ?)

Read the input from Left to right -

Trace the Rightmost derivation in Reverse -

The number of lookahead symbols in the items -



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Read the input from Left to right

Trace the Rightmost derivation in Reverse

The number of lookahead symbols in the items

• As soon as we find α in γ

 \bullet When we find α in γ and the next input token can follow A in some sentential form

ullet When we find lpha in γ and the next input token follows A in γ



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Read the input from Left to right

Trace the Rightmost derivation in Reverse

The number of lookahead symbols in the items

• As soon as we find α in γ LR(0) items and no lookahead in the input

- SLR(0) Parser
- \bullet When we find α in γ and the next input token can follow A in some sentential form

ullet When we find lpha in γ and the next input token follows A in γ



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Step 5: The Last Piece of Jigsaw Puzzle: Computing FOLLOW Sets

Consider $\beta Aw \stackrel{rm}{\Rightarrow} \beta \alpha w$ and $A \rightarrow \alpha$ When do we reduce occurrence of α in $\gamma = \beta \alpha$ using $A \rightarrow \alpha$ using LR(k) items? (i.e., when do we decide that α and $A \rightarrow \alpha$ form a handle in γ ?)

Read the input from Left to right

Trace the Rightmost derivation in Reverse

The number of lookahead symbols in the items

• As soon as we find α in γ LR(0) items and no lookahead in the input

- SLR(0) Parser
- When we find α in γ and the next input token can follow A in some sentential form
 - LR(0) items and 1 lookahead in the input

SLR(1) Parser

• When we find α in γ and the next input token follows A in γ



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Read the input from Left to right — — — Trace the Rightmost derivation in Reverse —

The number of lookahead symbols in the items -

• As soon as we find α in γ LR(0) items and no lookahead in the input

SLR(0) Parser

 \bullet When we find α in γ and the next input token can follow A in some sentential form

LR(0) items and 1 lookahead in the input

SLR(1) Parser

• When we find α in γ and the next input token follows A in γ LR(1) items and 1 lookahead in the input

CLR(1) Parser



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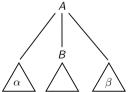
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Step 5: FIRST and FOLLOW Sets

• FIRST(β) contains the terminals that may begin a string derivable from β If β derives ϵ , then $\epsilon \in \text{FIRST}(\beta)$ It is computed as the least fixed point solution of the following constraints For $A \to X_1 X_2 \dots X_k$, FIRST(A) $\supset X_i, 1 < i < k$, provided $\forall i < i, \epsilon \in \text{FIRST}(X_i)$

FOLLOW(A) contains the terminals that follow A in some sentential form
 It is computed as the least fixed point solution of the following constraints

For production $A \rightarrow \alpha B \beta$



- If A is the start non-terminal FOLLOW(A) ⊇ {\$}
- FOLLOW(B) \supseteq FIRST(β) { ϵ }
- If β is ϵ or $\epsilon \in \mathsf{FIRST}(\beta)$ $\mathsf{FOLLOW}(B) \supseteq \mathsf{FOLLOW}(A)$



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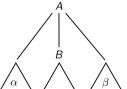
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Step 5: FIRST and FOLLOW Sets

FIRST(β) contains the terminals that may begin a string derivable from β
 If β derives ε, then ε ∈ FIRST(β)
 It is computed as the least fixed point solution of the following constraints
 For A → X₁X₂...X_k, FIRST(A) ⊃ X_i, 1 < i < k, provided ∀i < i, ε ∈ FIRST(X_i)

FOLLOW(A) contains the terminals that follow A in some sentential form
It is computed as the least fixed point solution of the following constraints

For production $A \rightarrow \alpha B \beta$



- If A is the start non-terminal FOLLOW(A) ⊇ {\$}
- $FOLLOW(B) \supseteq FIRST(\beta) \{\epsilon\}$
- If β is ϵ or $\epsilon \in \mathsf{FIRST}(\beta)$ $\mathsf{FOLLOW}(B) \supseteq \mathsf{FOLLOW}(A)$

For our grammar $E \rightarrow E + E$ $E \rightarrow E * E$ $E \rightarrow \mathrm{id}$ $\mathrm{FIRST}(E) = \{\mathrm{id}\}$ $\mathrm{FOLLOW}(E) = \{\$, +, *\}$



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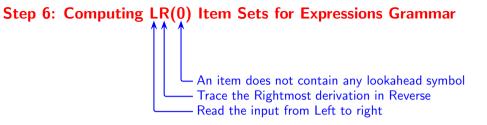
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Step 6: LR(0) Items Sets

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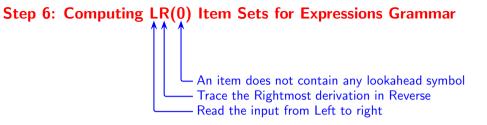
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$$0 E' \rightarrow E
1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$

- Augment the grammar by adding a synthetic start symbol
- Construct the start state by putting a dot at the start of the start symbol and taking a closure (add every rule for every non-terminal that has a dot before it in some rule)
- Identify transitions on every symbol that has a dot before it to construct new states
- For every state so identified, take a closure and identify transitions on every symbol that has a dot before it



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Step 6: Computing LR(0) Item Sets for Expressions Grammar

$$0 E' \rightarrow E
1 E \rightarrow E + E
2 E \rightarrow E * E
3 E \rightarrow id$$

 $\begin{array}{c}
I_0 \\
E' \to \bullet E \\
E \to \bullet E + E \\
E \to \bullet E * E
\end{array}$

Kernel items

- Augment the grammar by adding a synthetic start symbol
- Construct the start state by putting a dot at the start of the start symbol and taking a closure (add every rule for every non-terminal that has a dot before it in some rule)
- Identify transitions on every symbol that has a dot before it to construct new states
- For every state so identified, take a closure and identify transitions on every symbol that has a dot before it

Closure items



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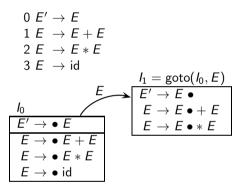
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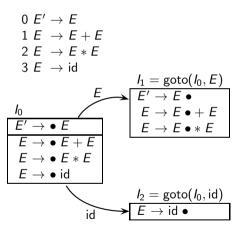
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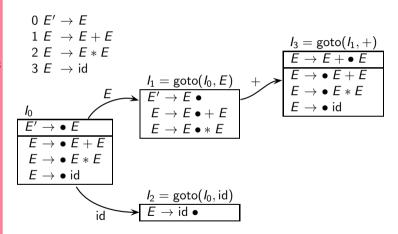
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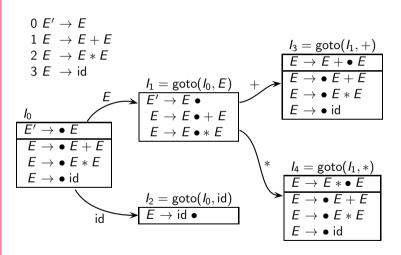
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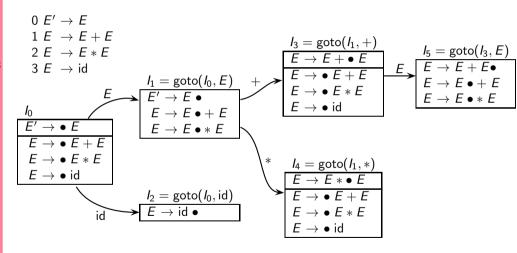
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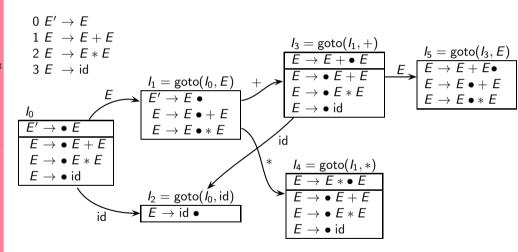
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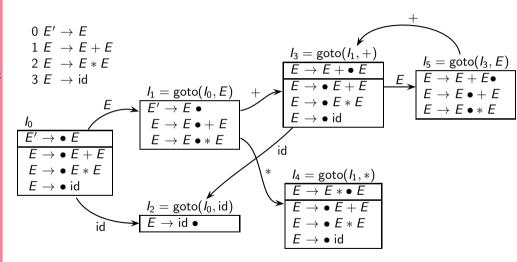
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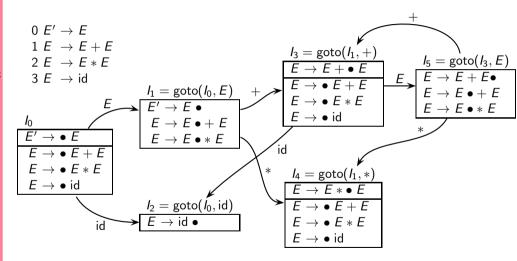
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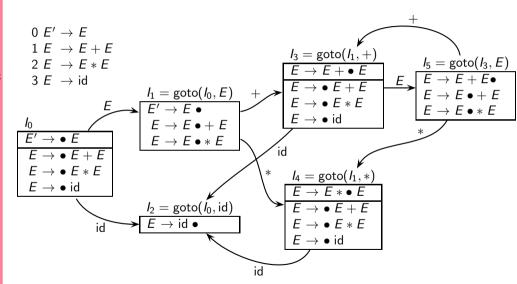
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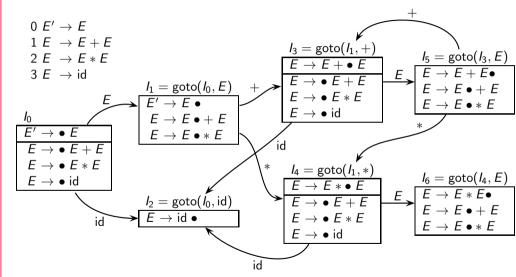
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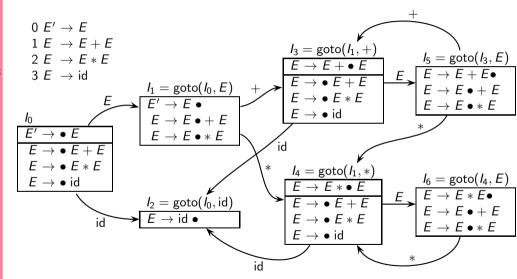
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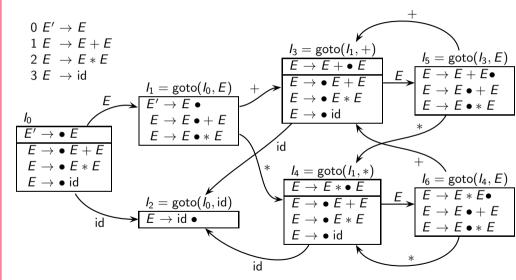
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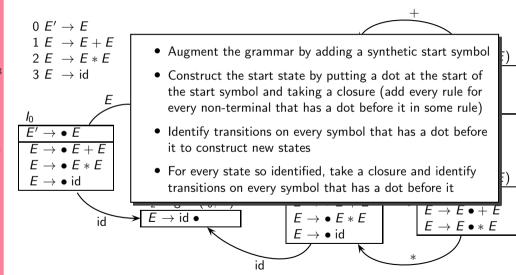
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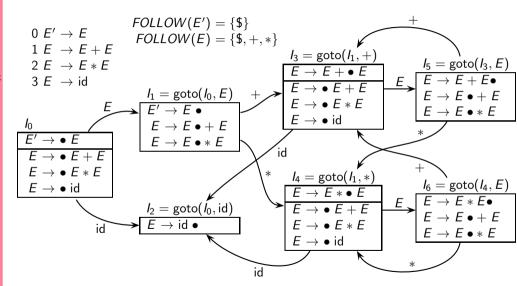
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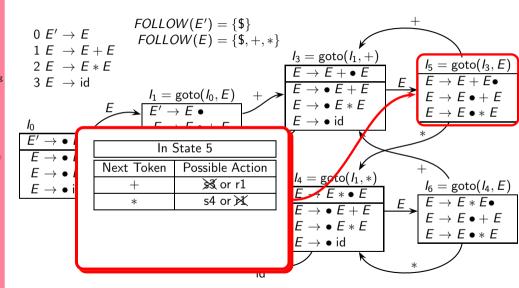
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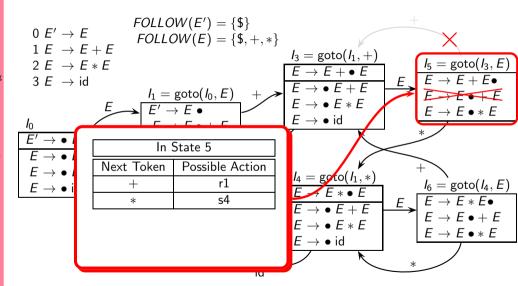
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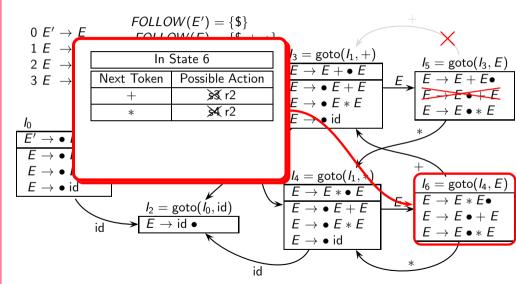
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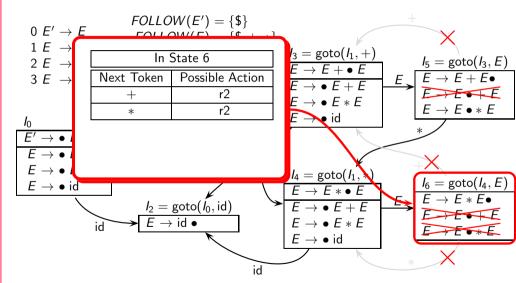
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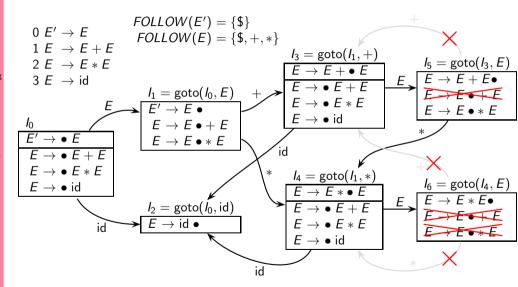
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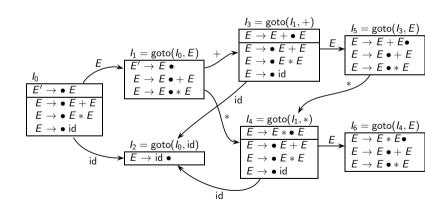
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The DFA of Item Sets Accepts Viable Prefixes





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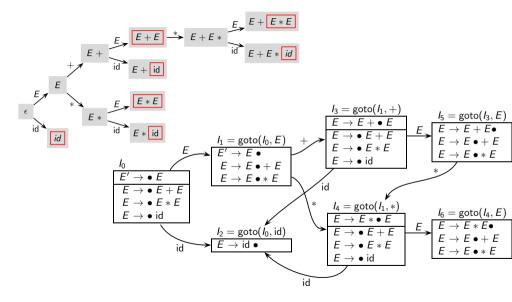
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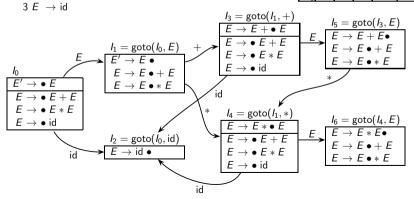
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1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		r^2	<i>r</i> 2	<i>r</i> 2	





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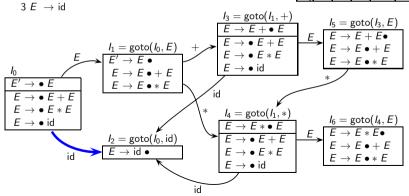
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	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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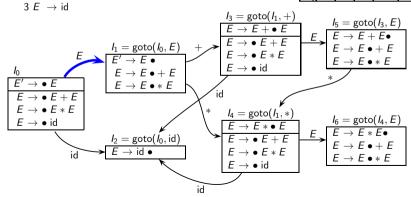
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0	<i>s</i> 2				c1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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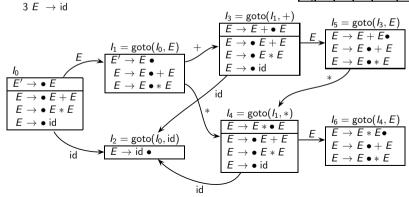
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	id	+	*	\$	Ε
0	<i>s</i> 2				c1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	2	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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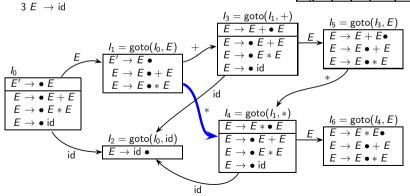
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	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	73	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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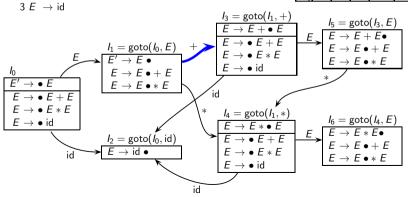
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	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		73	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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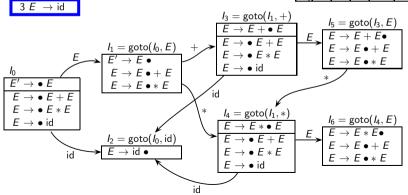
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0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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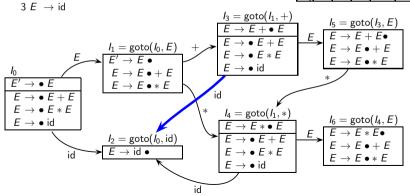
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0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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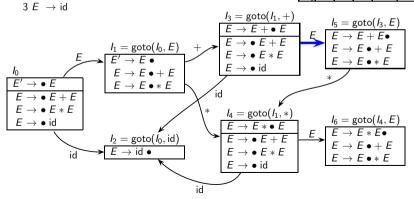
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0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				сb
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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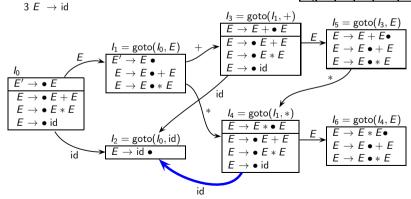
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	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>5</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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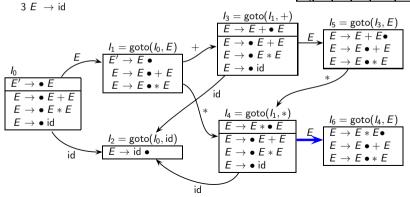
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1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	r^2	<i>r</i> 2	





Topic:

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Jillit Reduce i a

SLR(1) Parsing

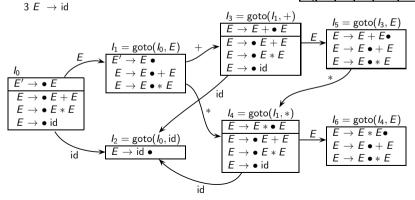
Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsi



	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





Topic:

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Snitt Reduce Pars

SLR(1) Parsing

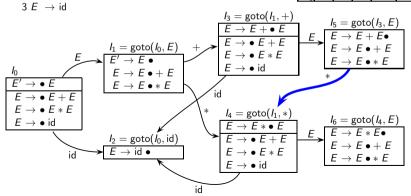
Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsi



	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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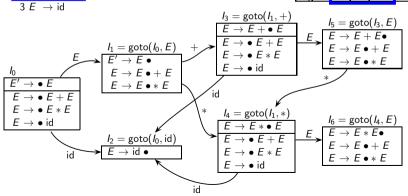
Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsi



	id	+	*	\$	Ε
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5	Ī .	r1	<i>s</i> 4	r1	
6		<i>r</i> 2	<i>r</i> 2	<i>r</i> 2	





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Destination Reached: From Intuitions to Formal Algorithms in Shift Reduce Parsing

1	Ε	\rightarrow	Ε	+E
2	Ε	\rightarrow	Ε	* E

 $3 E \rightarrow id$

	١		- 1	}	ı
0	<i>s</i> 2				<i>c</i> 1
1		<i>s</i> 3	<i>s</i> 4	acc	
2		<i>r</i> 3	<i>r</i> 3	<i>r</i> 3	
3	<i>s</i> 2				<i>c</i> 5
4	<i>s</i> 2				<i>c</i> 6
5		> 3√ <i>r</i> 1	<i>s</i> 4/ 冰 (r1	
6		≽ €/ <i>r</i> 2	≽ 4/ <i>r</i> 2	<i>r</i> 2	

Step	$Stack \to$	Input	Action
1	\$	id + id * id\$	-
2	\$id		reduce by 3
3	\$ <i>E</i>	+ id * id\$	
4	\$ <i>E</i> +	id * id\$	
5	E + id		reduce by 3
6	E + E	* id\$	
7	E + E *		shift
8	E + E * id		reduce by 3
9	E + E * E		reduce by 2
10	E + E	\$	reduce by 1
11	\$ <i>E</i>	\$	accept

	Step	$Stack \to$	Input	Action
	1	\$0	id + id * id\$	<i>s</i> 2
	2	\$0 id 2		<i>r</i> 3 and <i>c</i> 1
	3	\$0 <i>E</i> 1	+ id * id\$	<i>s</i> 3
	4	\$0 E 1 + 3	id * id\$	<i>s</i> 2
\Rightarrow	5	\$0 E 1 + 3 id 2	* id\$	<i>r</i> 3 and <i>c</i> 5
	6	\$0 E 1 + 3 E 5	* id\$	<i>s</i> 4
	7	\$0 E 1 + 3 E 5 * 4	id\$	<i>s</i> 2
	8	\$0 E 1 + 3 E 5 * 4 id 2	\$	<i>r</i> 3 and <i>c</i> 6
	9	\$0 E 1 + 3 E 5 * 4 E6	\$	<i>r</i> 2 and <i>c</i> 5
	10	\$0 E 1 + 3 E 5	\$	<i>r</i> 1 and <i>c</i> 1
	11	\$0 E 1	\$	accept



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Explaining Conflicts in Yacc

- Using bison -d option to generate .output file
- Using bison -g option to generate dot file of LR(0) automaton
- lex-yacc-intro-programs/yacc-conflict-demo/README
- yacc-actions-demo/simcalc-using-lex-yacc-c++
 To show the need of %prec UMINUS



Topic:

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parsing-slides-sanyal-part4.pdf



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Limitation of SLR(1) Parsing

• We illustrate the limitations of SLR(1) parsing by using the pointer assignment grammar given below

$$S \rightarrow L = R \mid R$$

$$L \rightarrow *R \mid id$$

$$R \rightarrow L$$

- We compute the FOLLOW sets and sets of LR(0) items to demonstrate the problem
- We explain the cause of the problem
- This explanation leads us to a more precise method of CLR(1) parsing (Canonical LR(1) parsing that uses the LR(1) items)



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$$S' \rightarrow S$$

$$S \rightarrow L = R \mid R$$

$$\begin{array}{ccc}
L & \rightarrow & *R \mid \text{id} \\
R & \rightarrow & L
\end{array}$$



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$$S' \rightarrow S$$
 \Rightarrow FOLLOW(S') \supseteq {\$} FOLLOW(S')

$$S \rightarrow L = R \mid R$$

$$L \rightarrow *R \mid id$$

 $R \rightarrow I$



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$$S' \rightarrow S$$
 \Rightarrow FOLLOW(S') \supseteq {\$}
FOLLOW(S) \supseteq FOLLOW(S')
 $S \rightarrow L = R \mid R \Rightarrow$ FOLLOW(L) \supseteq {=}
FOLLOW(R) \supseteq FOLLOW(R)
 $L \rightarrow *R \mid id$
 $R \rightarrow L$



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$$S' \rightarrow S$$
 \Rightarrow FOLLOW(S') \supseteq {\$}
FOLLOW(S) \supseteq FOLLOW(S')
 $S \rightarrow L = R \mid R \Rightarrow$ FOLLOW(L) \supseteq {=}
FOLLOW(R) \supseteq FOLLOW(S)
 $L \rightarrow *R \mid id \Rightarrow$ FOLLOW(R) \supseteq FOLLOW(L)
 $R \rightarrow I$



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$$S' o S$$
 \Rightarrow FOLLOW(S') \supseteq {\$}
FOLLOW(S) \supseteq FOLLOW(S')
 $S o L = R \mid R \Rightarrow$ FOLLOW(L) \supseteq {=}
FOLLOW(R) \supseteq FOLLOW(R)
 $L o *R \mid id \Rightarrow$ FOLLOW(R) \supseteq FOLLOW(R)
 $R o L \Rightarrow$ FOLLOW(R) \supseteq FOLLOW(R)

	FOLLOW
<i>S'</i>	{\$ }
S	{\$ }
R	${=,\$}$
L	$\{=,\$\}$



Topic:

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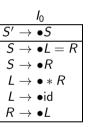
Shift Reduce Parsing

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 $\mathsf{LALR}(1) \; \mathsf{Parsing}$





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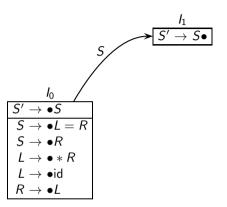
Shift Reduce Parsing

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Topic:

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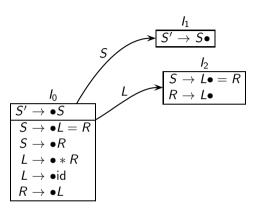
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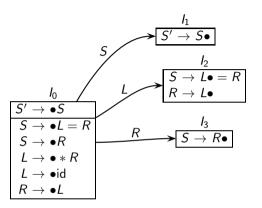
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Topic:

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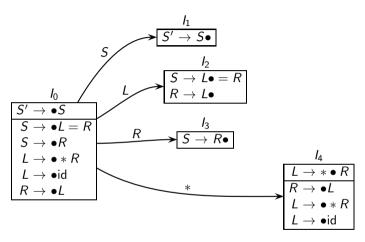
Shift Reduce Parsing

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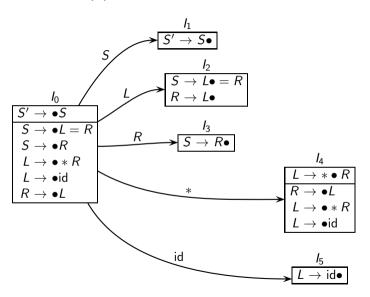
Shift Reduce Parsing

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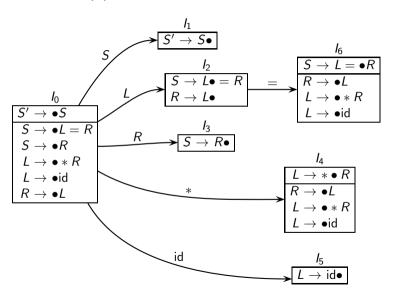
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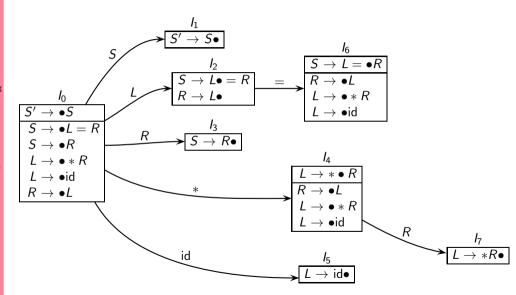
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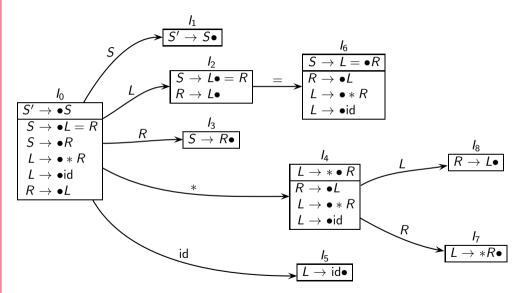
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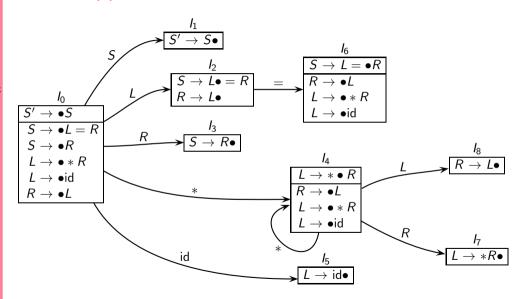
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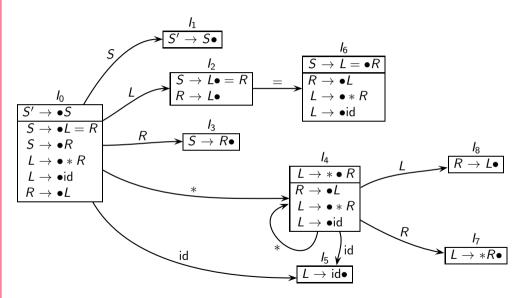
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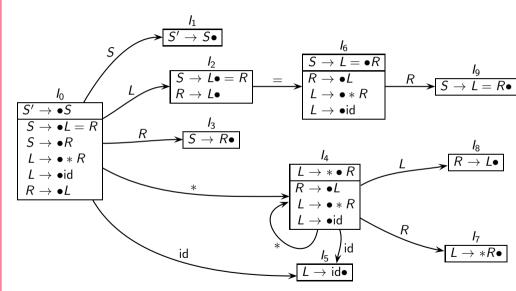
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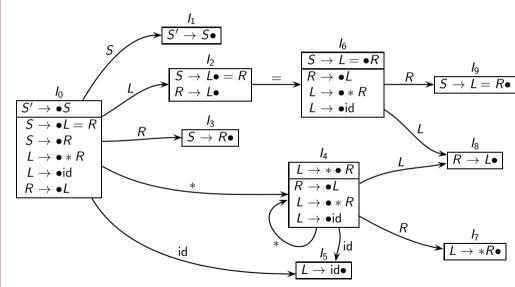
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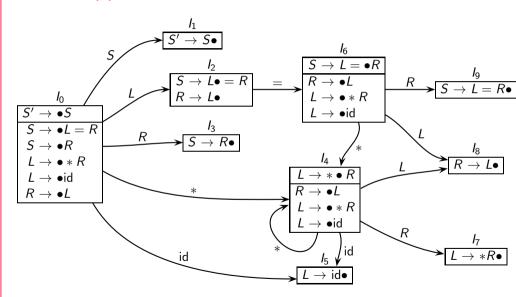
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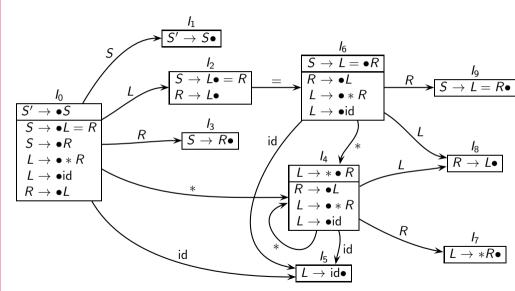
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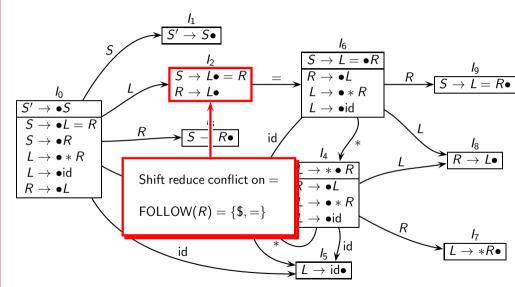
Shift Reduce Parsing

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Shift Reduce Parsir

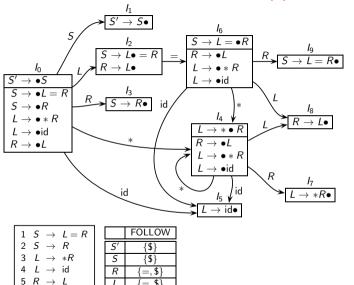
SLR(1) Parsing

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LALR(1) Parsin

Limitation of SLR(1) Parsing



Input



Stack



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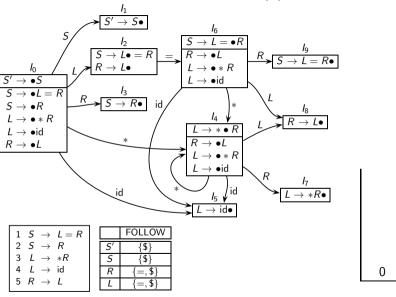
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Shift 5

Input

id = id\$





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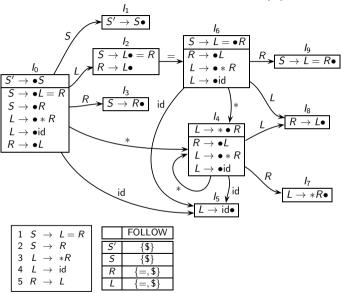
SLR(1) Parsing

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LALR(1) Parsin

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Reduce by 4

Input

= id\$



5

id



Topic:

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Shift Reduce Parsing

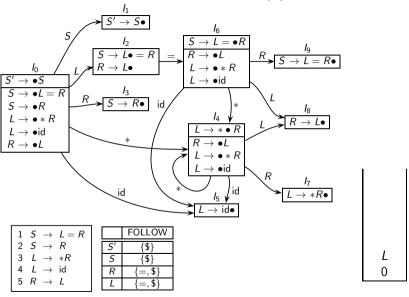
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$\mathsf{CLR}(1)$ Parsing

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Stack

Cover by 2

Input

= id\$



Topic:

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Sillit Reduce i a

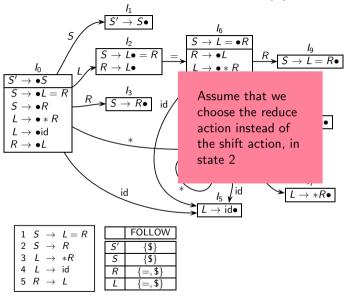
SLR(1) Parsing

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Reduce by 5

Input

= id\$

Stack



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Shift Reduce Parsin

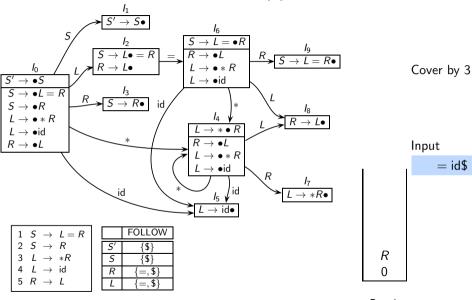
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Stack



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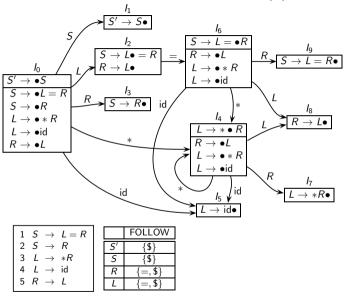
SLR(1) Parsing

Conceptual Issues in Parsing

$\mathsf{CLR}(1)$ Parsing

LALR(1) Parsir

Limitation of SLR(1) Parsing



Error

No action on =

Input

= id\$



3

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Topic:

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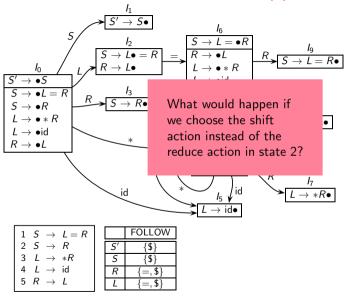
SLR(1) Parsing

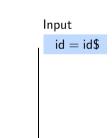
Conceptual Issues in Parsing

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LALR(1) Parsin

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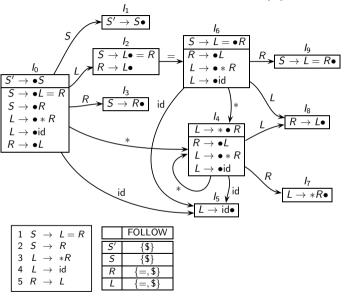
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Shift 5

Input

id = id\$





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Shift Reduce Parsing

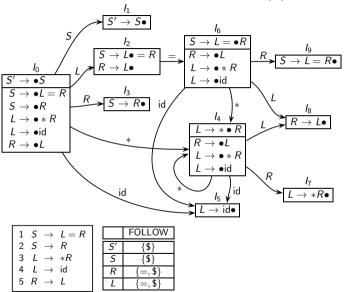
SLR(1) Parsing

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 $\mathsf{CLR}(1)$ Parsing

LALR(1) Parsin

Limitation of SLR(1) Parsing



Reduce by 4

Input

= id\$

Stack

5

id



Topic:

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Shift Reduce Parsin

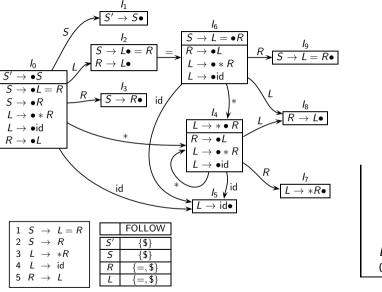
SLR(1) Parsing

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$\mathsf{CLR}(1)$ Parsing

LALR(1) Parsin

Limitation of SLR(1) Parsing



Cover by 2

Input

= id\$

Stack



Topic:

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Shift Reduce

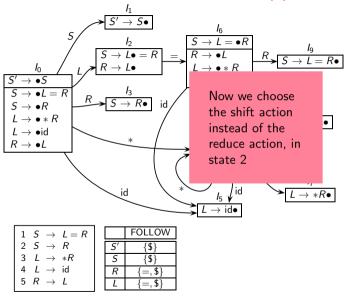
SLR(1) Parsing

Parsing Parsing

 $\mathsf{CLR}(1)$ Parsing

LALR(1) Parsin

Limitation of SLR(1) Parsing



shift 6

Input



2 *L*

 ${\sf Stack}$



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsir

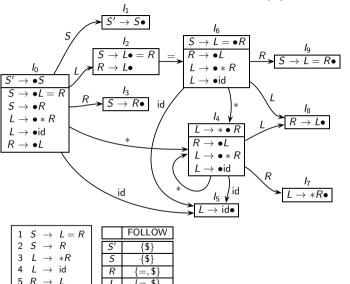
SLR(1) Parsing

Conceptual Issues in Parsing

$\mathsf{CLR}(1)$ Parsing

LALR(1) Parsin

Limitation of SLR(1) Parsing



Shift 5

Input

id\$



Stack



Topic:

Syntax Analysis

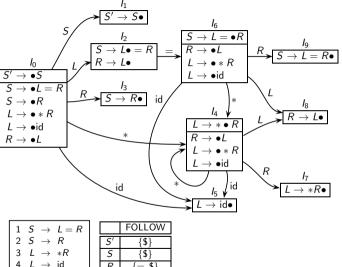
Section:

Derivations, and Parse

SLR(1) Parsing

CLR(1) Parsing

Limitation of SLR(1) Parsing



	FOLLOW
S'	{\$ }
S	{\$ }
R	$\{=,\$\}$
L	$\{=,\$\}$

Reduce by 4

Input

Stack

5 iЫ

6

=

5



Topic:

Syntax Analysis

Section:

Grammars, Derivations, and Parse Trees

Shift Reduce Parsin

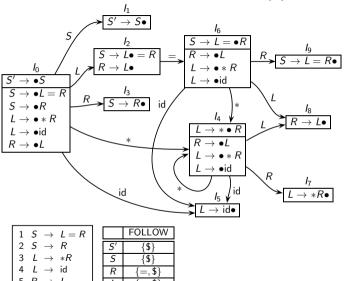
SLR(1) Parsing

Conceptual Issues in Parsing

 $\mathsf{CLR}(1)$ Parsing

LALR(1) Parsin

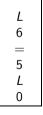
Limitation of SLR(1) Parsing



Cover by 8

Input

put





Topic:

Syntax Analysis

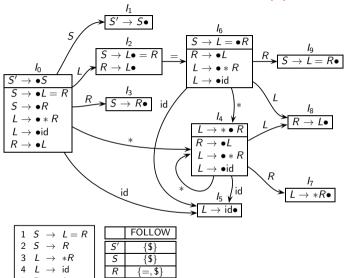
Section:

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CLR(1) Parsing

Limitation of SLR(1) Parsing



Reduce by 5

Input

	O
	L
	6
:	=
	5
	L
	0

0



Topic:

Syntax Analysis

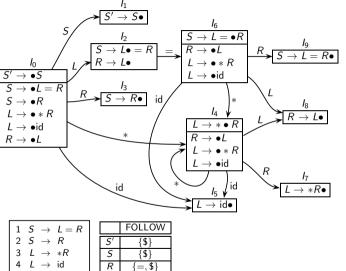
Section:

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Cover by 9

Input

R

6

=

5



Topic:

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Section:

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Shift Reduce Parsi

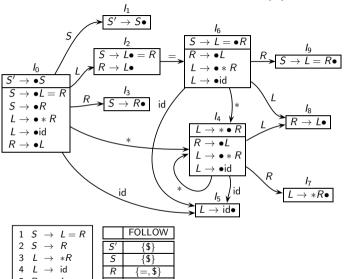
SLR(1) Parsing

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Reduce by 1

Input

9 R 6 = 5 L



Topic:

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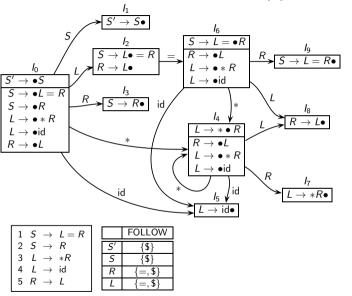
SLR(1) Parsing

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LALR(1) Parsin

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Cover by 1

Input

S 0



Topic:

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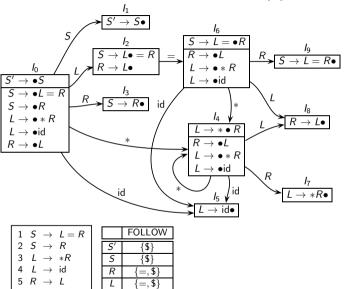
SLR(1) Parsing

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LALR(1) Parsin

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Accept

Input

1 5 0



Topic:

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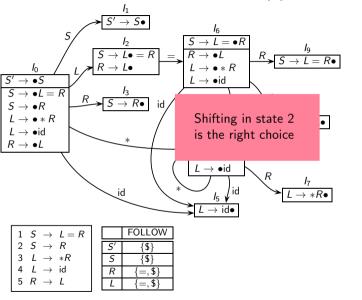
SLR(1) Parsing

Conceptual Issues in Parsing

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LALR(1) Parsin

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Accept

Input

1 5 0

 ${\sf Stack}$



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Limitation of SLR(1) Parsing: Use of FOLLOW Information

• Let FOLLOW(A) = {b, c}. Then b may follow A in some right sentential forms whereas in some other right sentential form, c may follow A

A symbol in follow set need not follow A in every right sentential form



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• We should declare handle $A \to \alpha$ in a viable prefix γ only if the follow symbols actually follows A in the right sentential form containing γ



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Limitation of SLR(1) Parsing: Use of FOLLOW Information

• Let $FOLLOW(A) = \{b, c\}$. Then b may follow A in some right sentential forms whereas in some other right sentential form, c may follow A

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- We should declare handle $A \to \alpha$ in a viable prefix γ only if the follow symbols actually follows A in the right sentential form containing γ
- In our grammar, there is no right sentential form with a prefix 'R ='
 - Since we need '=' in our right sentential form, consider $S \stackrel{rm}{=} L = R$
 - \circ 1 can derive either id or *R but not R

$$\begin{array}{ccc} S & \rightarrow & L = R \mid R \\ L & \rightarrow & *R \mid \mathrm{id} \\ R & \rightarrow & L \end{array}$$

'=' is in FOLLOW(R) only for the right sentential forms that begin with a '*'



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LR(1) Item Sets

Two changes from LR(0) construction

- Items are of the form $A \rightarrow \alpha \bullet \beta, a$ consisting of
 - \circ the *core* $A \rightarrow \alpha \bullet \beta$ and
 - o the lookahead a

If S is the start symbol, then I_0 contains $S' \to \bullet S, \$$

• Closure of an item $A \to \alpha \bullet B\beta$, a contains the items of the form $B \to \bullet \gamma$, FIRST(βa)

Transition of an item $A \to \alpha \bullet B\beta, a$ on B gives an item

$${\it A}
ightarrow lpha {\it B} ullet eta, {\it a}$$



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LR(1) Item Sets

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• Items are of the form $A \to \alpha \bullet \beta$, a consisting of

$$\circ$$
 the $\mathit{core}\ A o lpha ullet eta$ and

The goal is to compute different subsets of FOLLOW(A) for $A \rightarrow \alpha$ in different right sentential forms

Closi Since the construction of sets of items creates a DFA to recognize all viable prefixes, the subsets of FOLLOW can of the be computed for the productions in sets of items

Transition of an item $A \to \alpha \bullet B\beta, a$ on B gives an item

$$A \rightarrow \alpha B \bullet \beta, a$$



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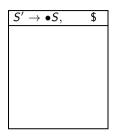
If S is the start symbol, then I_0 contains $S' \to \bullet S$,\$

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Transition of an item $A \to \alpha \bullet B\beta$, a on B gives an item

$${\it A} \rightarrow \alpha {\it B} \bullet \beta, {\it a}$$

The lookahead does not change during a transition



 $\begin{array}{ccc} S & \rightarrow & L = R \mid R \\ L & \rightarrow & *R \mid \mathrm{id} \\ R & \rightarrow & L \end{array}$



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$$S' \to \bullet S, \qquad \$$$

$$S \to \bullet L = R, \$$$

$$S \to \bullet R, \qquad \$$$

0

$$\begin{array}{ccc} S & \rightarrow & L = R \mid R \\ L & \rightarrow & *R \mid \mathrm{id} \\ R & \rightarrow & L \end{array}$$



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$$S \to \bullet L = R, \$$$

$$S \to \bullet R, \qquad \$$$

$$L \to \bullet * R, \qquad =$$

$$L \to \bullet \text{id}, \qquad =$$

$$\begin{array}{ccc} S & \rightarrow & L = R \mid R \\ L & \rightarrow & *R \mid \mathrm{id} \\ R & \rightarrow & L \end{array}$$



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LR(1) Item Sets

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$$A o \alpha B ullet eta, a$$

'	\rightarrow	● <i>S</i> ,	\$	
S	\rightarrow	$\bullet L = R,$	\$	
S	\rightarrow	• <i>R</i> ,	\$	
L	\rightarrow	$\bullet * R$,	=	,
L	\rightarrow	∙id,	=	I_0
7	\rightarrow	• <i>L</i> ,	\$	
L	\rightarrow	$\bullet * R$,	\$	
L	\rightarrow	∙id,	\$	

$$\begin{array}{ccc} S & \rightarrow & L = R \mid R \\ L & \rightarrow & *R \mid \mathrm{id} \\ R & \rightarrow & L \end{array}$$



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Two changes from LR(0) construction

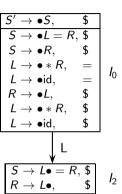
- Items are of the form $A \to \alpha \bullet \beta, a$ consisting of
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			_
- ,	$S' \to \bullet S$	\$	
	$S \rightarrow \bullet L =$	= <i>R</i> , \$	
	$S \rightarrow \bullet R$,	\$	
	$L \rightarrow ullet *$	R, =	,
	$L \rightarrow \bullet id$,	=	10
	$R \to \bullet L$,	\$	
	L o ullet *	R, \$	
	$L \rightarrow \bullet id$,	\$	
_	↓ ↓	L	•
ſ	$S \to L \bullet$	= R, \$	L
	$R \to L \bullet$,	\$	12

Transition of an item $A \to \alpha \bullet B\beta, a$ on B gives an item

$${\it A}
ightarrow lpha {\it B} ullet eta, {\it a}$$

The lookahead does not change during a transition

Reduction by $R \to L \bullet$ only on \$ and not on = No shift reduce conflict



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 I_0

$S' \to \bullet S$,	\$
$S \rightarrow \bullet L = R$?, \$
$S \rightarrow \bullet R$,	\$
$L \to \bullet * R$,	= /\$
$L \rightarrow \bullet id$,	= /\$
$R \rightarrow \bullet L$,	\$



Topic:

 ${\sf Syntax} \ {\sf Analysis}$

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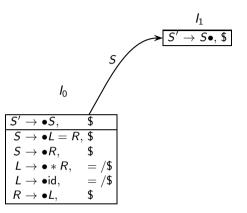
Shift Reduce Parsing

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Topic:

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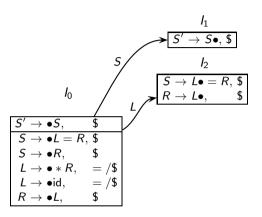
Shift Reduce Parsing

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Topic:

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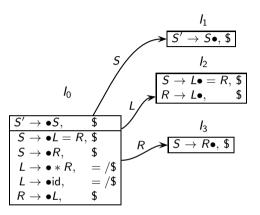
Shift Reduce Parsing

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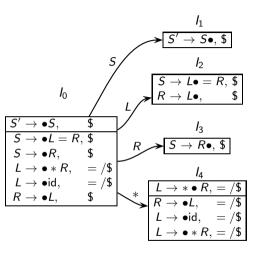
Shift Reduce Parsing

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LALR(1) Parsing





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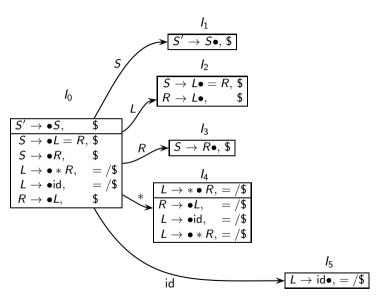
Shift Reduce Parsing

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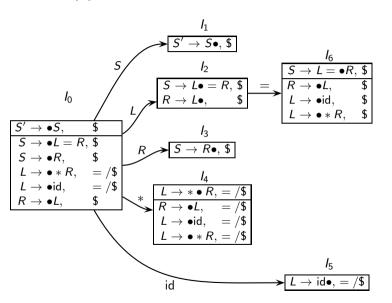
Shift Reduce Parsing

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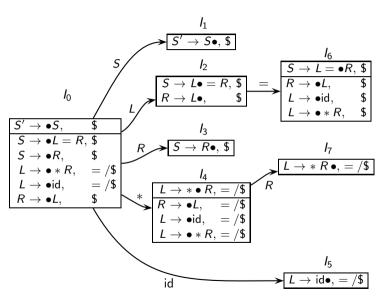
Shift Reduce Parsing

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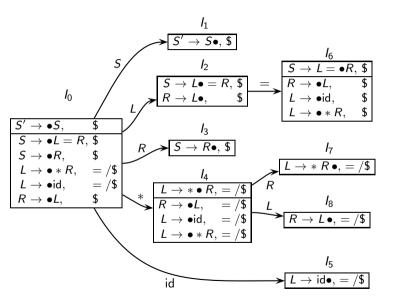
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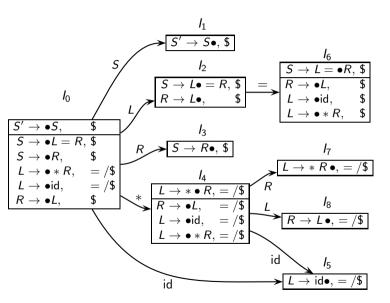
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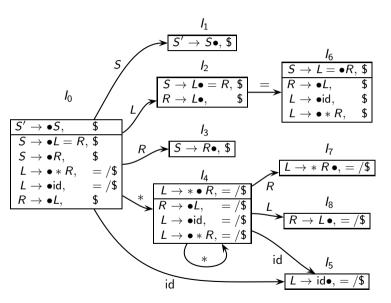
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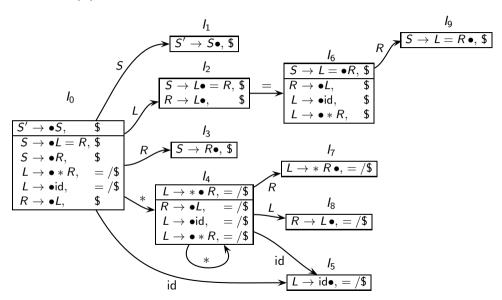
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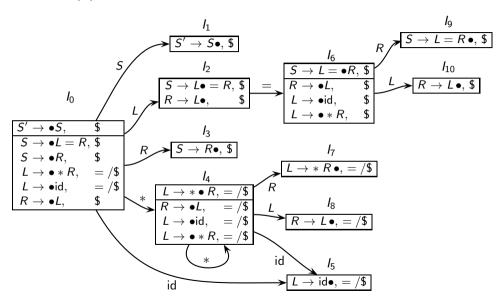
Shift Reduce Parsing

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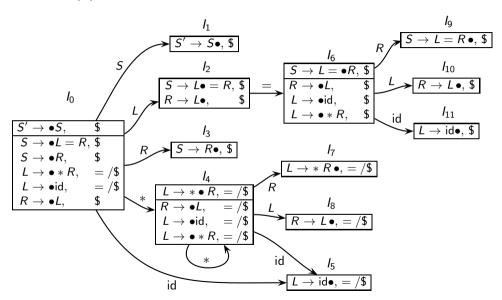
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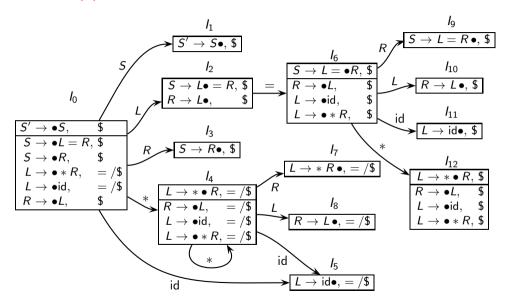
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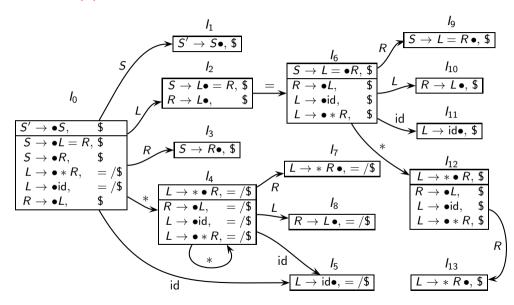
Shift Reduce Parsing

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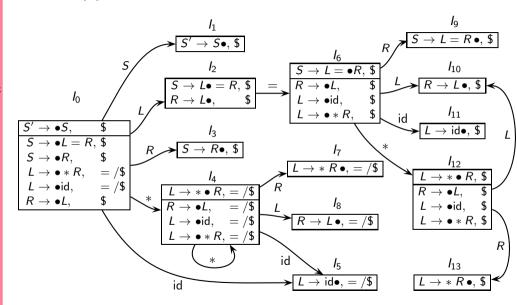
SLR(1) Parsing

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LR(1) Sets of Items for Pointer Assignment Grammar





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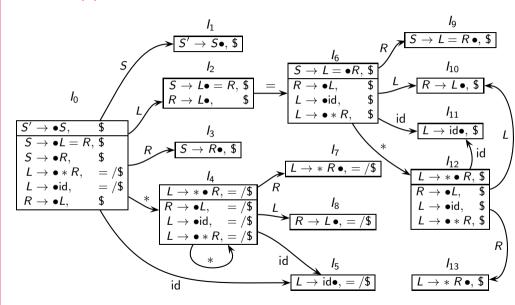
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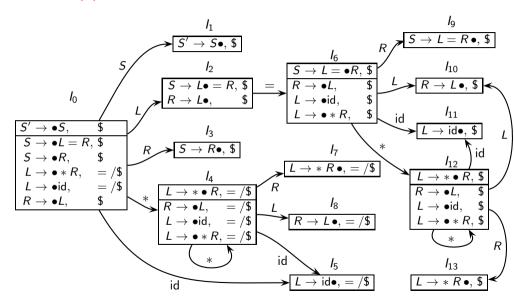
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LALR(1) Parsing

LR(1) (aka CLR(1)) Parsing Table for Pointer Assignment Grammar

Ü	$S' \rightarrow S$
1	$S \rightarrow L =$
2	$S \rightarrow R$
3	$L \rightarrow *R$
4	L o id
5	R o L

R

State		Acti	on			Goto	
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	c7
5			r4	<i>r</i> 4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				r1			
10				<i>r</i> 5			
11				r4		·	
12	<i>s</i> 11	<i>s</i> 12		·		c10	c13
13				<i>r</i> 3			



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Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	on		Goto		
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	c7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13		·		r3			, and the second

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

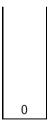
$$S \rightarrow R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input





Topic:

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LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	on	Goto			
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	c7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

 $S \rightarrow L = R$
 $S \rightarrow R$
 $L \rightarrow *R$
 $L \rightarrow id$
 $R \rightarrow L$

Input

id = id\$

Shift 5

0



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LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

Ctata		Act	ion			Goto	
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	s11	<i>s</i> 12				c10	c13
13				r3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

= id\$

Reduce by 4

5 id



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LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

Ctata		Act	ion			Goto	
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	s11	<i>s</i> 12				c10	c13
13				r3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

= id\$

Cover by 2



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LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	on	Goto			
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

= id\$

Shift 6

2 *L* Snift



Topic:

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Derivations, and Parse Trees

Shift Reduce Parsing

SLR(1) Parsing

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LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	on		Goto		
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			r3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow * R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

id\$

Shift 11

6 | S | 2 | L |



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SLR(1) Parsing

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CLR(1) Parsing

LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	on	Goto			
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				<i>r</i> 2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			r3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				r1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

\$

Reduce by 4

Stack

11

id



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LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	on	Goto			
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				<i>r</i> 2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			r3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				r1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

 $S \rightarrow L = R$
 $S \rightarrow R$
 $L \rightarrow *R$
 $L \rightarrow id$
 $R \rightarrow L$

Input

\$

Cover by 10





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CLR(1) Parsing

LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Act	on			Goto		
State	id	*	=	\$	S	L	R	
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3	
1				acc				
2			<i>s</i> 6	<i>r</i> 5				
3				r2				
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7	
5			r4	r4				
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9	
7			r3	<i>r</i> 3				
8			<i>r</i> 5	<i>r</i> 5				
9				<i>r</i> 1				
10				<i>r</i> 5				
11				r4				
12	<i>s</i> 11	<i>s</i> 12				c10	c13	
13				r3				

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

\$

Reduce by 5

Stack

10



Topic:

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SLR(1) Parsing

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LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State		Acti	ion			Goto	
State	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				<i>r</i> 2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				r1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

 $S \rightarrow L = R$
 $S \rightarrow R$
 $L \rightarrow *R$
 $L \rightarrow id$
 $R \rightarrow L$

Input

\$

Cover by 9

Stack

R

6

2



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SLR(1) Parsing

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CLR(1) Parsing

LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State	Action				Goto		
	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				<i>r</i> 2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				r1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

\$

Reduce by 1

Stack

R

2



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SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State	Action				Goto		
	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow * R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

Input

\$

Cover by 1

S



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LALR(1) Parsin

LR(1) (aka CLR(1)) Parsing for the Pointer Assignment Grammar

State	Action				Goto		
	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				r2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 11	<i>s</i> 12				c10	<i>c</i> 9
7			r3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			
10				<i>r</i> 5			
11				r4			
12	<i>s</i> 11	<i>s</i> 12				c10	c13
13				<i>r</i> 3			

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$S \rightarrow R$$

$$L \rightarrow R$$

$$L \rightarrow id$$

$$R \rightarrow L$$





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Another Example of LR(1) (aka CLR(1)) Parsing

A
ightarrow aBe

A
ightarrow aCd

 $A \rightarrow bBd$ $A \rightarrow bCe$

 $B \rightarrow f$

 $C \to f$



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LALR(1) Parsing

$$A \rightarrow aBe$$

 $A \rightarrow aCd$
 $A \rightarrow bBd$
 $A \rightarrow bCe$

$$B \rightarrow f$$

 $C \rightarrow f$

I ₀	
$A' \rightarrow \bullet A$,	\$
$A \rightarrow ullet aBe,$	\$
$A \rightarrow \bullet aCd$,	\$
$A \rightarrow \bullet bBd$,	\$
$A \rightarrow ullet bCe$,	\$



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SLR(1) Parsing

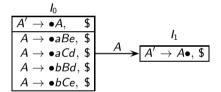
Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsing

$$A \rightarrow aBe$$

 $A \rightarrow aCd$
 $A \rightarrow bBd$
 $A \rightarrow bCe$
 $B \rightarrow f$
 $C \rightarrow f$





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Shift Reduce Parsing

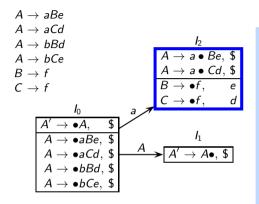
SLR(1) Parsing

Conceptual Issues in Parsing

CLR(1) Parsing

LALR(1) Parsin

Another Example of LR(1) (aka CLR(1)) Parsing



Closure of
$$P o lpha ullet Qeta, p$$
 contains items of the form $Q o ullet \gamma, \ \mathsf{FIRST}(eta p)$

In our example

- For Q = B, β is e and p is \$

 If we expect to see a string derivable from B in this state, the string must be followed by

 FIRST(βp) = FIRST(e\$) = e
- For Q = C, β is d and p is \$

 If we expect to see a string derivable from C in this state, the string must be followed by

 FIRST(βp) = FIRST(d\$) = d



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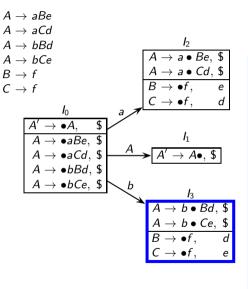
SLR(1) Parsing

Conceptual Issues in Parsing

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LALR(1) Parsin

Another Example of LR(1) (aka CLR(1)) Parsing



Closure of P o lpha ullet Qeta, p contains items of the form $Q o ullet \gamma, \ \mathsf{FIRST}(eta p)$

In our example

- For Q = B, β is d and p is \$

 If we expect to see a string derivable from B in this state, the string must be followed by

 FIRST(βp) = FIRST(d\$) = d
- For Q = C, β is e and p is \$

 If we expect to see a string derivable from C in this state, the string must be followed by

 FIRST(βp) = FIRST(e\$) = e



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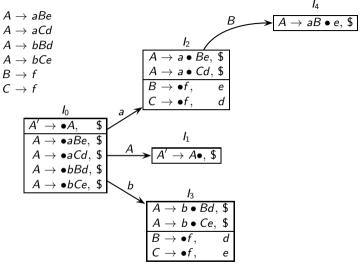
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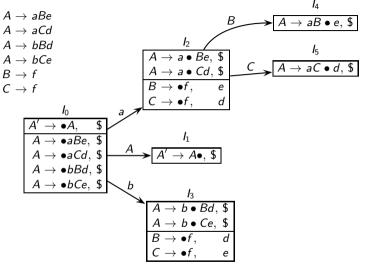
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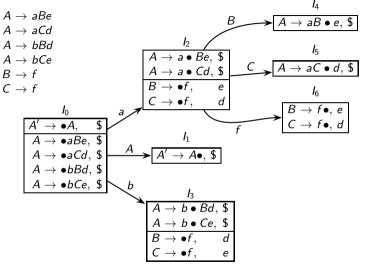
Shift Reduce Parsing

SLR(1) Parsing

Conceptual Issues in Parsing

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LALR(1) Parsing





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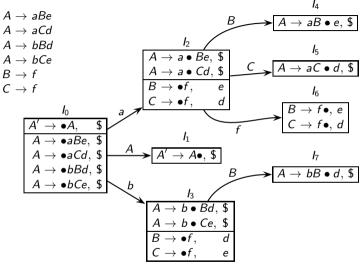
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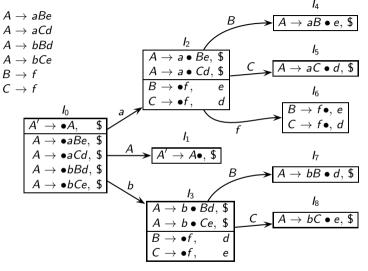
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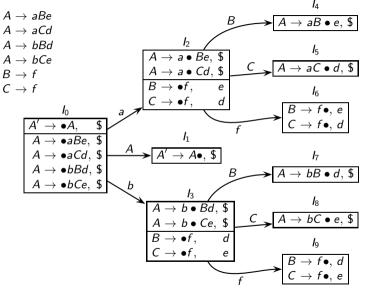
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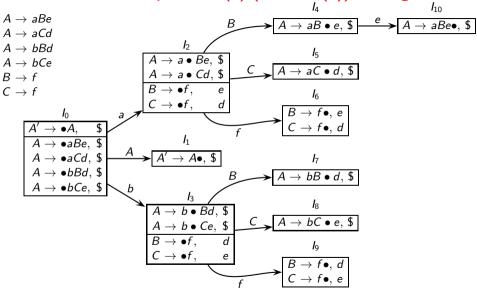
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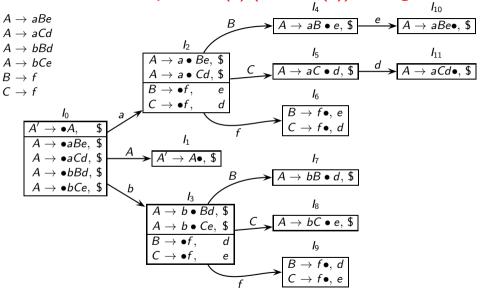
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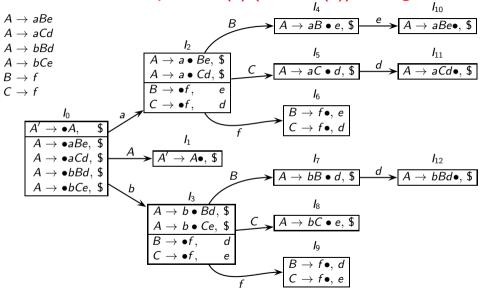
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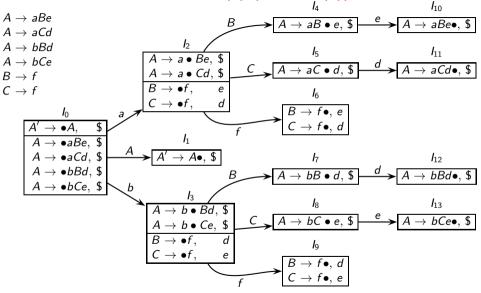
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• Merge item sets with identical cores (may have different lookaheads)

States $I_i: A \to \alpha \bullet \beta, a$ and $I_j: A \to \alpha \bullet \beta, b$

can be merged to create a new state I_{ij} : $A \rightarrow \alpha \bullet \beta, a/b$

• In practice, we do not construct LR(1) items to construct LALR(1) parser We construct LR(0) items and use a look-ahead propagation algorithm



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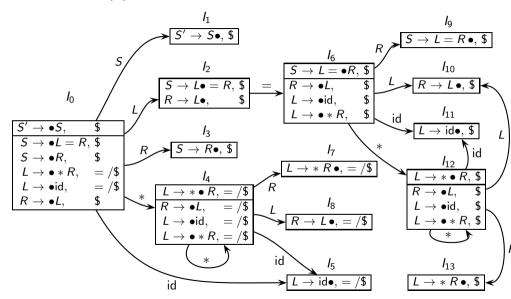
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LALR(1) Parsing for Pointer Assignment Grammar





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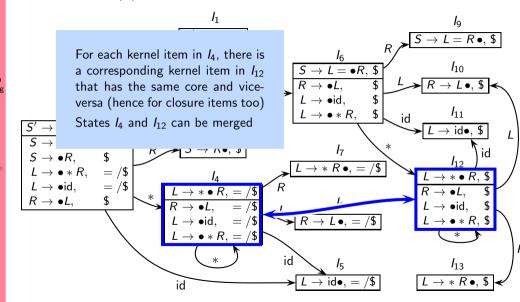
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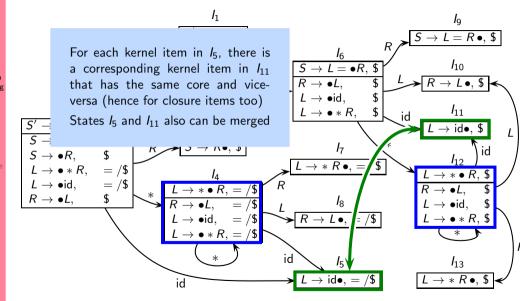
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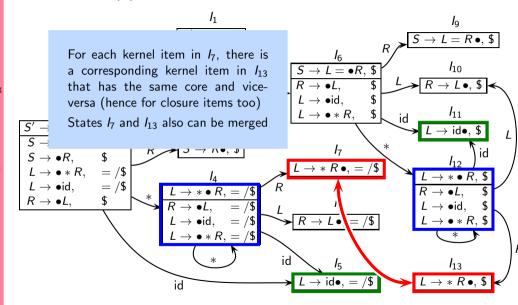
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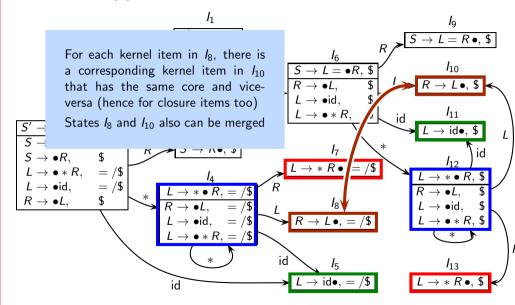
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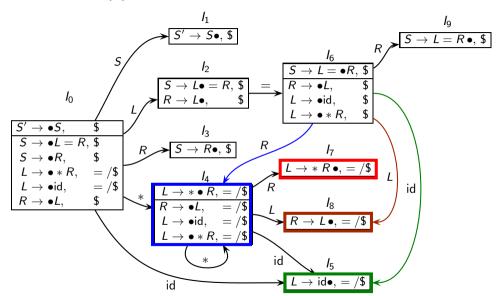
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$$\begin{array}{ll} 0 & S' \rightarrow S \\ 1 & S \rightarrow L = R \\ 2 & S \rightarrow R \\ 3 & L \rightarrow *R \\ 4 & L \rightarrow \mathrm{id} \\ 5 & R \rightarrow L \end{array}$$

State	Action				Goto		
	id	*	=	\$	S	L	R
0	<i>s</i> 5	<i>s</i> 4			<i>c</i> 1	<i>c</i> 2	<i>c</i> 3
1				acc			
2			<i>s</i> 6	<i>r</i> 5			
3				<i>r</i> 2			
4	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 7
5			r4	r4			
6	<i>s</i> 5	<i>s</i> 4				<i>c</i> 8	<i>c</i> 9
7			<i>r</i> 3	<i>r</i> 3			
8			<i>r</i> 5	<i>r</i> 5			
9				<i>r</i> 1			



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LALR(1) Vs CLR(1) Parsing

- Can merging of LR(1) states introduce shift-reduce conflict?
- Can merging of LR(1) states introduce reduce-reduce conflict?



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Can Merging LR(1) Sets of Items Introduce Shift-Reduce Conflict?

• To merge states l_i and l_j , they should have identical cores but different lookaheads (if the lookaheads are same then the states will not be distinct)



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Can Merging LR(1) Sets of Items Introduce Shift-Reduce Conflict?

• To merge states l_i and l_j , they should have identical cores but different lookaheads (if the lookaheads are same then the states will not be distinct)

• Let $I_i: \begin{bmatrix} A \to \alpha \bullet a\beta, & p \\ B \to \gamma \bullet, & q \end{bmatrix}$ and $I_j: \begin{bmatrix} A \to \alpha \bullet a\beta, & r \\ B \to \gamma \bullet, & s \end{bmatrix}$ where p, q, r, s are arbitrary terminals

So that the merged state is
$$I_{ij}: \begin{array}{c} A \to \alpha \bullet a\beta, & p/r \\ B \to \gamma \bullet, & q/s \end{array}$$



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Can Merging LR(1) Sets of Items Introduce Shift-Reduce Conflict?

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So that the merged state is $I_{ij}: \begin{array}{c} A \to \alpha \bullet a\beta, & p/r \\ B \to \gamma \bullet, & q/s \end{array}$

• For a shift-reduce conflict in I_{ii} , either q or s must be a.



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Can Merging LR(1) Sets of Items Introduce Shift-Reduce Conflict?

• To merge states l_i and l_j , they should have identical cores but different lookaheads (if the lookaheads are same then the states will not be distinct)

• Let $I_i: \begin{bmatrix} A \to \alpha \bullet a\beta, & p \\ B \to \gamma \bullet, & q \end{bmatrix}$ and $I_j: \begin{bmatrix} A \to \alpha \bullet a\beta, & r \\ B \to \gamma \bullet, & s \end{bmatrix}$ where p, q, r, s are arbitrary terminals

So that the merged state is $I_{ij}: \begin{array}{c} A \to \alpha \bullet a\beta, & p/r \\ B \to \gamma \bullet, & q/s \end{array}$

• For a shift-reduce conflict in I_{ij} , either q or s must be a.

o If q is a, then I_i is $A \to \alpha \bullet a\beta$, $P \to \alpha \bullet a\beta$ and thus I_i has a shift-reduce conflict



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Can Merging LR(1) Sets of Items Introduce Shift-Reduce Conflict?

• To merge states I_i and I_j , they should have identical cores but different lookaheads (if the lookaheads are same then the states will not be distinct)

• Let $I_i: \begin{bmatrix} A \to \alpha \bullet a\beta, & p \\ B \to \gamma \bullet, & q \end{bmatrix}$ and $I_j: \begin{bmatrix} A \to \alpha \bullet a\beta, & r \\ B \to \gamma \bullet, & s \end{bmatrix}$ where p, q, r, s are arbitrary terminals

So that the merged state is $I_{ij}: \begin{array}{c} A \to \alpha \bullet a\beta, & p/r \\ B \to \gamma \bullet, & q/s \end{array}$

• For a shift-reduce conflict in I_{ij} , either q or s must be a.

- $\circ \text{ If } q \text{ is } a \text{, then } I_i \text{ is } \begin{array}{c} A \to \alpha \bullet a\beta, & p \\ B \to \gamma \bullet, & a \end{array}$
- o If s is a, then I_j is $A \to \alpha \bullet a\beta$, $A \to \alpha \bullet \alpha$, $A \to \alpha \bullet$

and thus I_j has a shift-reduce conflict

and thus I_i has a shift-reduce conflict



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Can Merging LR(1) Sets of Items Introduce Shift-Reduce Conflict?

• To merge states I_i and I_i , they should have identical cores but different lookaheads (if the lookaheads are same then the states will not be distinct)

• Let *l_i* :

arbitrary ter

So that the

For a shift-r

A set I_{ii} of items in an LALR(1) parser can have a shift-reduce conflict if and only if a set I_i of LR(1) items merged to form I_{ii} has the same shift-reduce conflict

This is because a shift-reduce conflict depends both on a lookahead and a terminal in the core of an item

If q is

reduce conflict

s are

o If s is a, then I_i is

$$A o lpha ullet aeta, \quad r \ B o \gammaullet, \quad a$$

and thus I_i has a shift-reduce conflict



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Can Merging LR(1) Sets of Items Introduce Reduce-Reduce Conflict?

• Let $I_j: \begin{bmatrix} A \to \alpha \bullet, & p \\ B \to \alpha \bullet, & q \end{bmatrix}$ and $I_j: \begin{bmatrix} A \to \alpha \bullet, & r \\ B \to \alpha \bullet, & s \end{bmatrix}$

$$A \to \alpha \bullet$$
, p
 $B \to \alpha \bullet$, q

$$A \to \alpha \bullet$$
, r
 $B \to \alpha \bullet$, s

So that the merged state is I_{ii} :

$$A \to \alpha \bullet$$
, p/r
 $B \to \alpha \bullet$, q/s



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Can Merging LR(1) Sets of Items Introduce Reduce-Reduce Conflict?

• Let $I_i: \begin{bmatrix} A \to \alpha \bullet, & p \\ B \to \alpha \bullet, & a \end{bmatrix}$ and $I_j: \begin{bmatrix} A \to \alpha \bullet, & r \\ B \to \alpha \bullet, & s \end{bmatrix}$

$$A \to \alpha \bullet$$
, r
 $B \to \alpha \bullet$, s

So that the merged state is I_{ii} :

$$A \to \alpha \bullet$$
, p/r
 $B \to \alpha \bullet$, q/s

- For a reduce-reduce conflict in I_{ii} such that there is no reduce-reduce conflict in I_i or I_i ,
 - $\circ p = s$. This is possible without a reduce-reduce conflict in I_i and I_i
 - \circ r=q. This is also possible without a reduce-reduce conflict in I_i and I_i



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Can Merging LR(1) Sets of Items Introduce Reduce-Reduce Conflict?

Let I_i: A
 B
 Merging LR(1) sets of items can introduce reduce-reduce conflicts even if the original sets do not have a reduce-reduce conflict
 This is because a reduce-reduce conflict depends only on lookaheads and a complete item. The terminals in a core do not play any role
 p = s.



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LALR(1) Vs LR(1) Parsing

- Merging of LR(1) states for LALR(1) parsing cannot introduce shift-reduce conflicts
- Merging of LR(1) states for LALR(1) parsing may introduce reduce-reduce conflicts



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LALR(1) Vs LR(1) Parsing

- Merging of LR(1) states for LALR(1) parsing cannot introduce shift-reduce conflicts
- Merging of LR(1) states for LALR(1) parsing may introduce reduce-reduce conflicts
- Let $\mathbb{G}(P)$ be the set of grammars admitted by a parsing method P (i.e. conflict-free parsers can be created for these grammars using P)
 Then, $\mathbb{G}(LALR(1)) \subset \mathbb{G}(LR(1))$



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- Merging of LR(1) states for LALR(1) parsing cannot introduce shift-reduce conflicts
- Merging of LR(1) states for LALR(1) parsing may introduce reduce-reduce conflicts
- Let $\mathbb{G}(P)$ be the set of grammars admitted by a parsing method P (i.e. conflict-free parsers can be created for these grammars using P)
 Then, $\mathbb{G}(LALR(1)) \subset \mathbb{G}(LR(1))$
- Consider a grammar $G \in \mathbb{G}(LALR(1))$
 - Can an LALR(1) parser for G reject $w \in L(G)$ because of merging of states?
 - Can an LALR(1) parser for G accept $w' \notin L(G)$ because of merging of states?



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LALR(1) Vs LR(1) Parsing

- Merging of LR(1) states for LALR(1) parsing cannot introduce shift-reduce conflicts
- Merging of LR(1) states for LALR(1) parsing may introduce reduce-reduce conflicts
- Let $\mathbb{G}(P)$ be the set of grammars admitted by a parsing method P (i.e. conflict-free parsers can be created for these grammars using P)
 Then, $\mathbb{G}(LALR(1)) \subset \mathbb{G}(LR(1))$
- Consider a grammar $G \in \mathbb{G}(LALR(1))$
 - Can an LALR(1) parser for G reject $w \in L(G)$ because of merging of states? No
 - ∘ Can an LALR(1) parser for G accept $w' \notin L(G)$ because of merging of states? No

If a parsing method admits a grammar G then the corresponding parser for G accepts all sentences in L(G) and rejects all sentences not in L(G)



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LALR(1) Vs LR(1) Parsing

- Merging of LR(1) states for LALR(1) parsing cannot introduce shift-reduce conflicts
- Merging of LR(1) states for LALR(1) parsing may introduce reduce-reduce conflicts
- Let $\mathbb{G}(P)$ be the set of grammars admitted by a parsing method P (i.e. conflict-free parsers can be created for these grammars using P)

 Then, $\mathbb{G}(LALR(1)) \subset \mathbb{G}(LR(1))$
- Consider a grammar $G \in \mathbb{G}(LALR(1))$
 - o Can an LALR(1) parser for G reject $w \in L(G)$ because of merging of states? No
 - Can an LALR(1) parser for G accept $w' \notin L(G)$ because of merging of states? No

If a parsing method admits a grammar G then the corresponding parser for G accepts all sentences in L(G) and rejects all sentences not in L(G)

• Consider a grammar $G \notin \mathbb{G}(LALR(1))$ An LALR(1) parser may still accept L(G) because it may admit G' such that L(G) = L(G')



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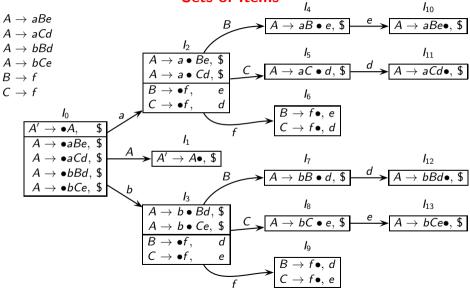
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Example of Reduce-Reduce Conflict Caused by Merging LR(1) Sets of Items





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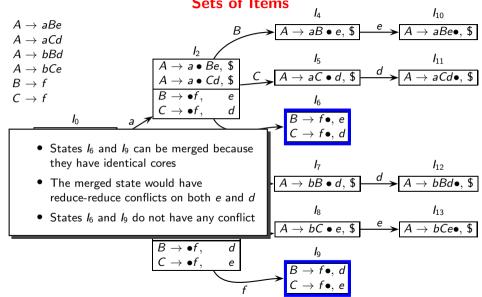
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Example of Reduce-Reduce Conflict Caused by Merging LR(1) Sets of Items





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A Practical Example of Reduce-Reduce Conflict in LR(1) Parsing

program → func_decl var_decl program \rightarrow var_decl func_decl $var_decl \rightarrow data_type ID$; $data_type \rightarrow INT$

func_decl \rightarrow return_type ID ()

return_type \rightarrow INT

return_type → VOID

For the input "int f . . . ", when we see the token INT, the next token is ID

In this situation, the parser does not know if it should reduce INT to return_type or data_type

State I_0 contains the following items

```
data_type \rightarrow \bullet INT. ID
return_type \rightarrow • INT, ID
```

The transition on INT gives the following set of items showing a reduce-reduce conflict on ID

```
data_type \rightarrow INT \bullet, ID
return_type → INT •. ID
```



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A Practical Example of Reduce-Reduce Conflict in LR(1) Parsing

In this particular case, the conflict can be removed by replacing every occurrence of the non-terminals data_type and return_type by every RHS of the non-terminal

Original Grammar	Transformed Grammar		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		



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A Summary of Bottom Up Parsing Methods

Parsing Method	Items Used	Reduction by $A \rightarrow \alpha$	Remarks
SLR(0)	LR(0)	On any terminal	
SLR(1)	LR(0)	On the terminals in $FOLLOW(A)$	
LR(1), also known as Canonical LR(1) or CLR(1)	LR(1)	On lookahead a in the item " $A \rightarrow \alpha \bullet$, a "	
LALR(1)	LR(1)	On lookahead a in the item " $A o lpha ullet , a$ "	Conceptually, the sets of items are obtained by merging LR(1) item sets that differ only in the lookahead symbols Practically, lookaheads are propagated starting from \$ on LR(0) items



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Comparison of Bottom-Up Methods and Corresponding Grammars

- A grammar G is accepted by a parsing method P if a conflict-free parser can be constructed for G using P
- An ambiguous grammar is not accepted by any parsing method
- A grammar is called SLR(0), SLR(1), LR(1), or LALR(1) if it is accepted respectively, by the SLR(0), SLR(1), LR(1), or LALR(1) parsing method
 - \circ Every SLR(0) grammar is also SLR(1) grammar but not vice-versa
 - o Every SLR(1) grammar is also LALR(1) grammar but not vice-versa
 - o Every LALR(1) grammar is also LR(1) grammar but not vice-versa
- The expressions grammar (E → E + E | E * E | id) is not accepted by any parsing method because it is ambiguous
 (without post-facto instrumentation of parsing tables using precedences and associativities)