

(Homework 5)

*3. $L3 = \{ 0^i 1^j : i \geq j \}$

- Assume $L3$ is regular, Let m be the number of states in DFA.
- We pick a string $w \in L3$, $|w| \geq m \Rightarrow 0^m 1^m$
- Opponent decomposes w into xyz , $|xy| \leq m$, $|y| \geq 1$
- We pick $i = 0$ to pump xz . The result is $0^{m-k} 1^m$ where $k = |y|$
 $k \geq 1$
- Since $m-k < m$, $0^{m-k} 1^m \notin L3$
- Contradiction with Pumping Lemma! Therefore, $L3$ is not regular language.

