

# Solid State for Devices Physics

## Tutorial Problems (Questions Only)

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### 1 Basic Review Questions

#### Semiconductor Materials

**Question:** List two elemental semiconductor materials and two compound semiconductor materials.

#### Lattice Structures

**Question:** Sketch three lattice structures: (a) simple cubic, (b) body-centered cubic, and (c) face-centered cubic.

#### Volume Density of Atoms

**Question:** Describe the procedure for finding the volume density of atoms in a crystal.

#### Miller Indices

**Question:** Describe the procedure for obtaining the Miller indices that describe a plane in a crystal.

## Impurities in Crystals

**Question:** What is meant by a substitutional impurity in a crystal? What is meant by an interstitial impurity?

## Wave–Particle Duality

**Question:** State the wave–particle duality principle and state the relationship between momentum and wavelength.

## Quantized Energy Levels

**Question:** What is meant by quantized energy levels? Can an electron in a potential well have an arbitrary energy?

# 2 Schrödinger Equation Review

## Schrödinger Equation: Basic Form

**Question:** Write down the time-dependent Schrödinger equation. What physical quantity does the wavefunction  $\Psi(x, t)$  describe?

## Separation of Variables

**Question:** Explain why we can write  $\Psi(x, t) = \psi(x)\phi(t)$  when the potential is time-independent. What form does  $\phi(t)$  take?

## Stationary States

**Question:** What does it mean for a wavefunction to be a *stationary state*? Why is the probability density  $|\Psi(x, t)|^2$  time-independent in this case?

## Infinite Square Well

**Question:** For a particle in a 1D infinite square well of width  $a$ :

What is the general form of the wavefunction inside the well? State the boundary conditions at  $x = 0$  and  $x = a$ . Write the expression for the allowed energy levels  $E_n$ .

## Free Particle

**Question:** Write down the solution of the Schrödinger equation for a free particle of energy  $E = \frac{\hbar^2 k^2}{2m}$ . What is the physical meaning of the parameter  $k$ ?

## Finite Barrier

**Question:** If a particle has energy  $E < V_0$  in a finite potential barrier, what form does the wavefunction take inside the barrier?

## Normalisation

**Question:** Why must the total wavefunction satisfy

$$\int_{-\infty}^{+\infty} |\Psi(x, t)|^2 dx = 1 \text{ ?}$$

### 3 Arrhenius Relationship

#### Arrhenius Relation for Thermal Defects

**Question:** A material has an atomic density  $N = 8.5 \times 10^{22} \text{ cm}^{-3}$  and a vacancy formation energy  $E_f = 1.2 \text{ eV}$ .

1. Calculate the fractional vacancy concentration  $f$  and the vacancy density  $n_d$  at  $T = 1500 \text{ K}$ .
2. What is the general formula for the defect concentration  $n_d$  as a function of temperature  $T$ ?

#### Estimating $E_f$ from Two Concentrations

**Question:** The defect concentration in a material is measured to be  $n_1 = 2.0 \times 10^{15} \text{ cm}^{-3}$  at  $T_1 = 1000 \text{ K}$  and  $n_2 = 4.0 \times 10^{16} \text{ cm}^{-3}$  at  $T_2 = 1200 \text{ K}$ . Estimate the defect formation energy  $E_f$  in eV.

#### Effect of Entropy Factor

**Question:** A material has  $E_f = 2.5 \text{ eV}$  and  $N = 6.0 \times 10^{22} \text{ cm}^{-3}$ . Calculate the defect concentration  $n_d$  at  $T = 1000 \text{ K}$ . How does the concentration change if an entropy factor  $S_f/k_B = 1.5$  is included?

#### Temperature for Given Vacancy Density

**Question:** Find the temperature  $T$  (in Kelvin) required to achieve a vacancy density of  $n_d = 1.0 \times 10^{15} \text{ cm}^{-3}$  in a material with  $N = 1.0 \times 10^{23} \text{ cm}^{-3}$  and  $E_f = 1.8 \text{ eV}$ .

## Comparing Two Materials

**Question:** Two materials (A and B) have the same atomic density  $N = 7.0 \times 10^{22} \text{ cm}^{-3}$  and are held at  $T = 1200 \text{ K}$ . Material A has a defect formation energy  $E_f = 2.0 \text{ eV}$  and Material B has  $E_f = 2.8 \text{ eV}$ . Calculate the defect concentration in both materials and state the ratio  $n_A/n_B$ .

## 4 Crystal Structure

### Miller Indices and Interplanar Spacing

**Given:** Simple cubic crystal with lattice constant  $a = 0.30 \text{ nm}$ . A plane intersects the axes at  $(x, y, z) = (2a, a, a/2)$ .

- (i) Find the Miller Indices  $(hkl)$  for this plane.
- (ii) Find the interplanar spacing  $d_{hkl}$  for this plane.

## 5 Quantum Mechanics Exercises

### Photon Energy and Wavelength

**Problem:** Calculate the energy of each photon of blue light of frequency  $\nu = 6.40 \times 10^{14} \text{ Hz}$ . What is the wavelength of this photon?

### de Broglie Wavelength

**Problem:**

- Calculate the de Broglie wavelength of an electron moving at  $v = 1 \times 10^5 \text{ m/s}$ .

- Calculate the de Broglie wavelength of a person (mass = 70 kg) walking at 1 m/s.

### Heisenberg Uncertainty Principle

**Problem:** The uncertainty in the position of an electron is  $\Delta x = 8 \text{ \AA}$ .

- Determine the minimum uncertainty in the momentum  $\Delta p$ .
- Calculate the uncertainty in the kinetic energy (assume  $p \approx \Delta p$ ).