Creating Power of 10 in 8-Byte Word

- If you are creating up to 10^{19} , you need to reserve $19\times8=152$ bytes of memory as a buffer and call it POW_10.
- Create a subroutine to multiply 8-byte number by 10 and call it (MUL_10).
- Start with putting 1 in an 8-byte number say 'Res'.
- Call MUL_10 to multiply 'Res' by 10 and store the result at the *bottom* of POW_10 buffer.
- Adjust your pointer on the buffer for next result.
- Repeat the process till you generate all the necessary power of 10s.

Creating Power of 10 in 8-Byte Word

```
Pow-10
        MOVW
                #0,Res
                                 ; set 8-byte number to 1.
        MOVW
                #0,Res+2
                #0,Res+4
        MOVW
                #1,Res+6
        MOVW
        LDY
                #Pow10+150
                                 ; set pointer at the bottomn
        MOVB
                #19,count
                                          ; set counter
Lpow
        PSHY
                                 ; save pointer and multiply 8-byte
                                  ; number by 10.
        LDX
                #Res
        JSR
                mul10
                                 ; recover the pointer
        PULY
                                 ; store the result in Pow10
        MOVW
                Res+6,2,Y-
        MOVW
                Res+4,2,Y-
        MOVW
                Res+2,2,Y-
        MOVW
                Res,2,Y-
        DEC
                count
                                 ; if not done repeat
        BNE
                Lpow
        RTS
Res
        RMB
                8
temp
        RMB
Pow10
                152
        RMB
        RMB
count
```

Successive Subtraction Algorithm

- 1. Lets assume your 8-byte number is sitting in 'Res'.
- 2. Create a temporary 8-byte variable called 'temp'.
- 3. Create a 20-byte variable called 'decnum' as well as 1-byte counter.
- 4. Set pointers at the top of 'POW_10' and 'decnum'.
- 5. Clear counter and copy 'Res' in 'temp'.
- 6. Subtract 'POW_10' from 'Res', if result positive, increment counter, copy 'Res' in 'temp' and subtract again.
- 7. If result not positive, store counter in 'decnum', clear counter, copy 'temp' to 'Res', adjust both pointers and go back to step 6.
- 8. Continue till all digits are established.

How to Output 10-digit number

Out	LDY	#dnum
rep	LDAB	1,Y+
	BNE	prt
	CPY	#dnum+9
	BLO	rep
prt	CLRA	
	ADDB	#\$30
	PSHY	
	LDX	putchar
	JSR	0,X
	PULY	
	CPY	#dnum+9
	BHI	done
	LDAB	1,Y+
	JMP	prt
done	RTS	

8905600

Deque data Structure

A *deque* is a generalized data structure that includes two special cases: the *stack* and the *queue*.

- A deque is a sequence of elements with two ends that we call them the top and the bottom.
- Either top or bottom element in the deque can be accessed.
- Ideally, deques are of infinite length, but practical deques have a maximum capacity.
- If this capacity is exceeded, we have an *overflow error*.
- A deque is implemented in assembly language by allocating an area of N bytes of *memory* as a *buffer* to it.

How to implement a Deque

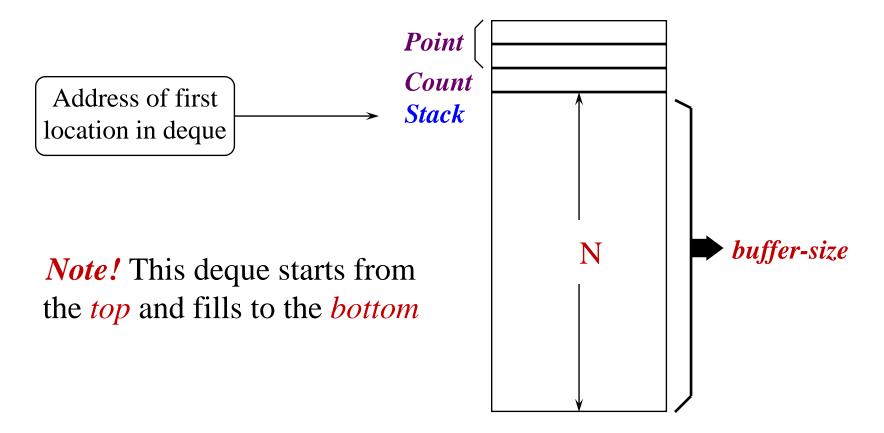
There are various ways to configure a deque:

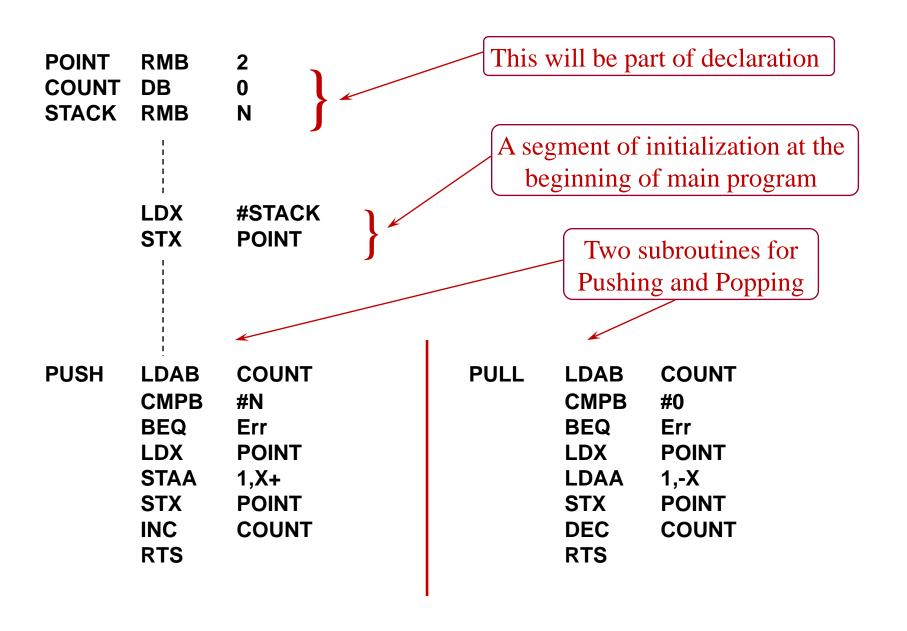
- First-In-First-Out system called (*FIFO*)
- Last-In-First-Out system called (*LIFO*)
- Use one pointer or Two pointers
- Start from bottom of the deque and go to top
- Start from top of the deque and go to bottom

Also each deque needs a *counter* to detect *Overflow* (exceeding the capacity) and *underflow* (pull more than you push).

Example: Write the necessary source code to create a LIFO (Last-In-First-Out) deque with one pointer.

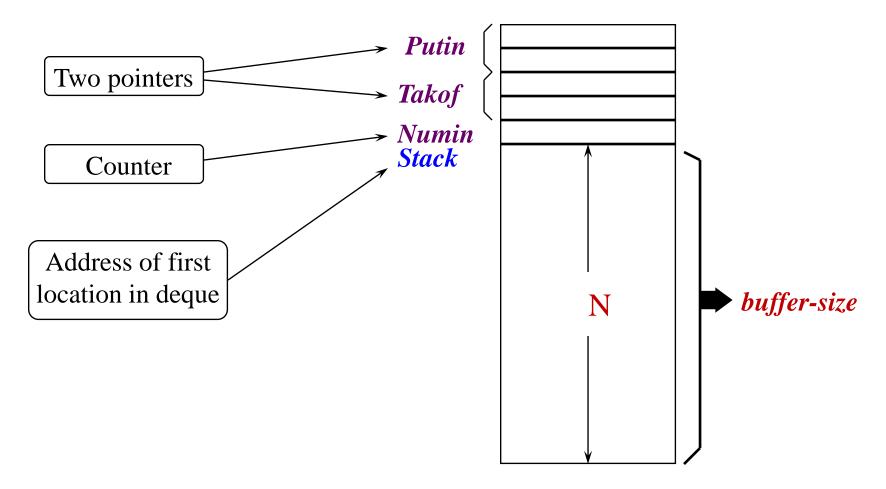
Solution:





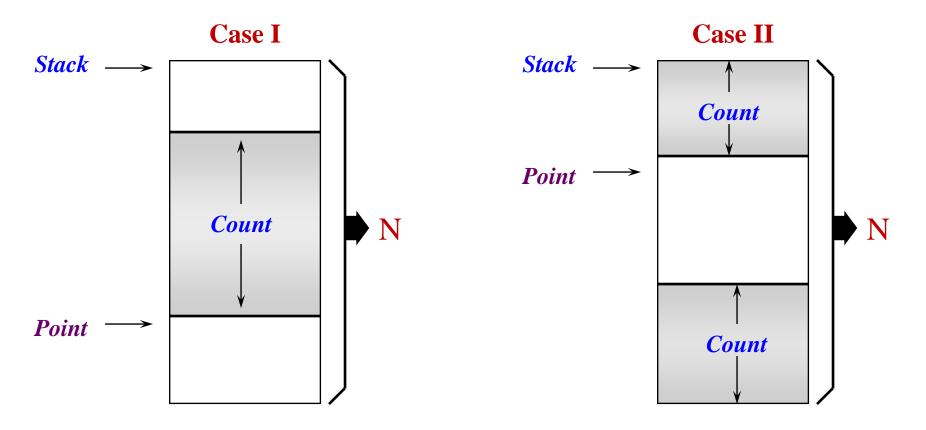
Example: Write the necessary source code to create a FIFO deque with two pointers.

Solution:



Example: Write the algorithm to create a FIFO deque using ONE pointer.

Solution: There are two cases to be considered.



St. Mary's University

Algorithm for Popping (Pulling)

Compare *Count* with zero If *equal*, branch to ERROR

Compare [point - Stack] with Count

If greater or equal branch to CASE I

CASE II E.A. = Point + [\$N - Count]

Branch to CONT

CASE I E.A. = Point - Count

CONT Load X with E.A.

Load Acc. A from 0,X

Decrement Count

Return from subroutine

```
Subroutine to pop from stack which uses one pointer and FIFO concept. The assumption is *
*
   that buffer size is less than 256 and data byte will be popped into Accumulator A.
******************************
POP
         LDAA
                  COUNT
                                    ;check if buffer is empty, then
         CMPA
                  #0
                                    ;jump to error message.
         BEQ
                  ERR
         LDD
                  POINT
                                    ;find out which case are you dealing
                                    ;with and find effective address
         SUBD
                  #STACK
         LDAA
                  COUNT
                                     ;accordingly.
         CBA
                  CASEII
         BHI
         LDD
                  POINT
                                    ; case I, E.A. = point - count
                  COUNT
         SUBB
         SBCA
                  #0
         XGDX
                  CONT
         BRA
CASEII
         LDAB
                  #N
                                    ; case II, E.A. = point + [N - count]
         SUBB
                  COUNT
         LDX
                  POINT
         ABX
CONT
         LDAA
                  0,X
                                    pop the data into acc. A
         DEC
                  COUNT
                                    ;update count.
         RTS
ERR
         LDD
                  #ERRMSG
                                    ;let the user know that buffer is
         LDX
                  printf
         JSR
                  0,X
                                    ;empty and return.
         RTS
```

Indexable Data Structures

Indexable structures include:

- Vectors
 - Lists
 - Arrays
 - Tables

A *Vector* is a sequence of elements, where each element is associated with an index *i* that can be used to access it.

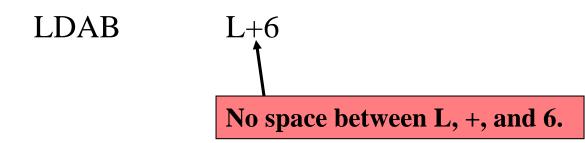
Example:

V FCB 36,17,58,4,29 U FDB 28,1028,876,425 The elements in these vectors can be accessed using indexed-addressing mode.

LDX LDAB ABX LDAA	#V #n th -element 0,X	LDX LDAB LDAA	#V #n th -element B,X
LDX #U LDAB #numb ASLB ; ABX LDD 0,X	oer_i multiply i by 2	LDAB #	#U #number_i ; multiply i by 2 3,X

A *List* is like a vector, being accessed by means of an index, but the elements of the list can be any combination of different precision words, characters, code words, and so on.

L FDB	\$F2A		
FCC	'Null'	L	0F
FCB	109		2A
			4E
			75
			6C
			6C
To get 109 in accum	ulator B:		6D



An *Array* is a vector whose elements are vectors of the same length. Normally, array is perceived as two-dimensional pattern.

If rows of the array are assumed as the elements of vector, data structure is called *row major order array*

A1	FCB	11,12,13
	FCB	14,15,16
	FCB	17,18,19
	FCB	20,21,22

If the array is considered a vector of column vectors, the structure is a *Column major order array*.

Based on which order is used, an element from the ith row and jth column can be extracted from an array by a polynomial evaluation.

Example: address of (i,j)th element of a row major order array with N rows and M columns will be:

$$addressof(i, j) = (i \times M) + j + addressof(0,0)$$

Example: In a major row order, assume number of rows are 8 and number of columns are 10, i and j are in accumulators A and B respectively, and address of (0,0) element be A1. Write the instruction sequence to find the address of (i,j)th element.

; save it for after multiply ; put M into acc. B
; get i times M
; add j
; propagate carry
; add offset to initial address
; point X to A1(i,j)
; get A1(i,j) into acc. A
; balance the stack
•

$$i = 4, j = 6$$

$N = 8 \ and \ M = 10$

Address of $a_{i,j} = Address \ of \ a_{0,0} + (i \times M) + j$

Microprocessors

```
ISR
                               INSERT
* The subroutine puts A(i,j) which is 3-bytes long (triple precision) into
* locations N, N+1, and N+2. The size of array is 8×10 and stored in a row
* major order. Subroutine jumps to location ERROR if the indices are outside
* the array's range.
                                                               *
* Initial conditions on entering the subroutine:
* A contains index i, 0 < i < 8
                                                               *
* B contains index j, 0 \le j < 10
* X points to array A(i,j), specifically address of A(0,0)
* Y points to location N
* A(i,j) = A(0,0) + 3(10i+j)
     = A(0,0) + 30i + 3i is used
* Registers A, B, and X are destroyed.
                                                               *
```

```
INSERT CMPA #8
                                   ;check the range of index i
         BHS
                                    ;use unsigned comparison to check for
                err
         CMPB #10
                                   ;check for the range 0 \le j \le 10
         BHS
                err
Back
        RTS
         LDD
                  #Ermsg
                                    print the error message on the screen
err
         LDX
                  printf
                  0,X
         JSR
                                    ;and return from subroutine.
         BRA
                  Back
```

Ermsg

FCC

DB

'Indices out of range!'

\$0D,\$0A,0

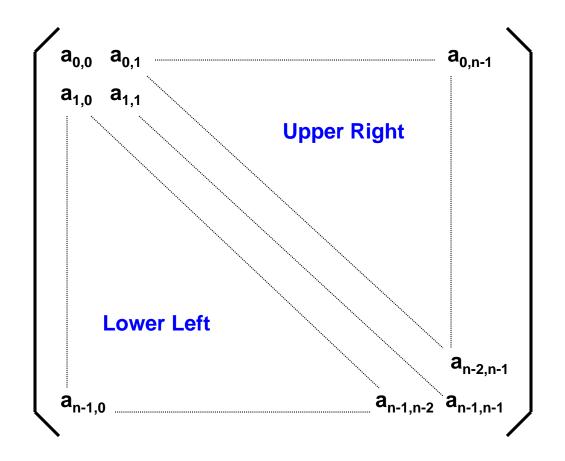
INSERT	CMPA BHS CMPB BHS	err	;check the range of index i ;use unsigned comparison to check for ;check for the range 0 <= j < 10
	PSHB		;save j
	LDAB MUL TBA PULB ABA ASLB ABA TAB	#30	;load 30 to multiply it with i in acc. A ;acc. B contains 30i, since i < 8 ;move 30i from B to A ;restore j in acc. B ;now acc. A has 30i+j ;acc. B has 2j ;now acc. A has 30i+3j ;acc. B has 30i+3j ;point X to the location A(i,j)
		0,X	get first two bytes of A(i,j)
Book		0,Y 2,X	;store two bytes at N and N+1 locations ;get third byte of A(i,j) ;store the third byte at N+2 location
Back			
err	LDD LDX JSR BRA	#Ermsg printf 0,X Back	;print the error message on the screen ;and return from subroutine. ;
Ermsg	FCC DB	'Indices out of \$0D,\$0A,0	range!'

Example:

Write a program to transpose an $N \times N$ matrix.

Solution:

Note that matrix can be divided into *upper right*, *lower left*, and *diagonal*.



```
NAM
                         EXAMPLE
            ORG
                         $1000
            EQU
                         8
                                     ; dimension of the matrix
Ν
ILIMIT
            EQU
                         N-2
                                     ; upper limit of i
JLIMIT
            EQU
                         N-1
                                     ; upper limit of j
            RMB
                                     ; row index
            RMB
                                     ; column index
MAT
            FCB
                         01,02,03,04,05,06,07,08
            FCB
                         09,10,11,12,13,14,15,16
            FCB
                         17,18,19,20,21,22,23,24
            FCB
                         25,26,27,28,29,30,31,32
            FCB
                         33,34,35,36,37,38,39,40
            FCB
                         41,42,43,44,45,46,47,48
            FCB
                         49,50,51,52,53,54,55,56
            FCB
                         57,58,59,60,61,62,63,64
            ORG
                         $1100
            CLR
                                     ; initialize i to 0
LOOP1
            LDAA
            INCA
            STAA
                                     ; initialize j to i+1
* The following 7 instructions compute the address of element MAT(i,j) and leave it in X
LOOP2
            LDAA
                                     ; place the row index in A
            LDAB
                         #N
                                     ; put N into B
            MUL
                                     ; multiply i x N
            ADDB
                                     ; compute i x N + j
            ADCA
                         #0
            ADDD
                         #MAT
                                     ; compute MAT(0,0) + i \times N + i
            XGDX
                                     ; place the result in X
```

Continued in next slide

Continuation of the program:

```
* The following 7 instructions compute the address of element MAT(j,i) and leave it in Y
            LDAA
                                    ; place the row index in A
                        #N
            LDAB
                                    ; put N into B
            MUL
                                    ; multiply j x N
            ADDB
                                    ; compute j x N + i
            ADCA
                        #0
            ADDD
                        #MAT
                                    ; compute MAT(0,0) + j \times N + i
            XGDY
                                    ; place the result in Y
* The following 4 instructions swap MAT(i,j) with MAT(j,i)
            LDAA
                        0,X
            LDAB
                        0,Y
            STAA
                        0,Y
            STAB
                        0,X
            LDAB
            INC
            CMPB
                                    ; is j = N-1?
                        #JLIMIT
            BNE
                        LOOP2
            LDAA
            INC
            CMPA
                        #ILIMIT
                                    ; is i = N-2?
            BNE
                        LOOP1
            SWI
            END
```

Sequential Data Structure

Sequential data is accessed by relative position. That is from pointer location the data before or after can be retrieved.

A *string* is an example of sequential data. After i^{th} element of sequence either $(i+1)^{th}$ or $(i-1)^{th}$ can be reached.

How to take care of end of data In sequential structure?

- 1- Keep track of length of data with counter.
- 2- Know the end address and compare it every time.
- 3- Put special character at the end of string.
- 4- For ASCII code, put 1 in the 7-bit of last character and check for it.

How to check for certain message to do certain task? For instance, check for user's input. If input is 'Happy' then go to routine which starts at address START.

	NAM ORG	SEARCH \$1100	
user pass	RMB FCC	2 'Happy'	;holds initial address of string to ;be inserted by user
	ORG	\$1200	
SRCH	LDX LDY LDAA	user #pass #5	get starting address of user string
LOOP	LDAB CMPB BNE DBNE	1,X+ 1,Y+ nogood A,LOOP	
nogood	JMP RMB END	START 0	

Example: Write a program that asks user for password. Store the password and echo '*' for every character that user enters. Once carriage return is encountered, examine the password and allow or deny access accordingly.

Again	ORG LDD LDX JSR LDY PSHY	\$1000 #askpass printf 0,X #usepass	;ask user to enter password ; ; ; ;set pointer to receive user's password ; save pointer
wait	LDX JSR CMPB BEQ PULY	getchar 0,X #\$0D check	;receive password character by character ;output asterisk for each character and ;check for carriage return. Once you ;encounter CR, go ahead and check the ;password.
	STAB PSHY CLRA LDAB LDX	1,Y+ #'*' putchar	; ; ;
check	JSR BRA LDX LDY	0,X wait #pass #usepass	; ; ;start checking password. If there is an ;error, display an error message and

```
1,X+
                               ;ask again. If password is correct, send
loop
       LDAA
               1,Y+
                                ;a greeting message and start the
       CMPA
       BNE
               err
                                ; program.
       CPX
               #endpass
       BNE
               loop
       LDD
               #greet
       LDX
               printf
       JSR
               0,X
       JMP
               start
       LDD
               #errmsg
                              ;send error message and ask again
err
       LDX
               printf
       JSR
               0,X
       JMP
               again
start
        FCC
               'What ever!'
pass
endpass RMB
usepass RMB
               50
askpass FCC 'Enter Password:'
        DB
               $0D,$0A,0
        FCC
               'Wrong Password, Try again.'
errmsg
        DB
               $0D,$0A,0
        FCC
greet
               'Welcome to our humble game!'
        DB
               $0D,$0A,0
```

Binary Search

- If an array (e.g. look up table) needs to be searched frequently, then *sequential search* is very inefficient.
- A better approach is to sort the array and use the *binary search* algorithm.
- Suppose that sorting array (in ascending order) has **n** elements and stored in memory locations starting at the label **arr**.
- Let *max* and *min* represent the highest and the lowest range of array indices to be searched and the variable *mean* represent the average of *max* and *min*.
- The idea of the binary search algorithm is to divide the stored array into three part:
 - The portion of the array with indices ranging from *mean*+1 to *max*.
 - The element with index equal to *mean* (middle element).
 - The portion of the array with indices ranging from *min* to *mean-1*.
- The binary search algorithm compares the key with the middle element and takes one of the following actions based on the comparison result:

Binary Search continued ...

- If the key equals the middle element, then stop.
- If the key is larger than the middle element, then the key only can be found in the portion of the array with larger indices. The search will be continued on the upper half.
- If the key is smaller than the middle element, then the key only can be found in the portion of the array with smaller indices. The search will be continued on the lower half.
- > the *binary search* algorithm can be formulated as follow:

```
step 1 – Initialize variables max and min to n-1 and 0, respectively.
```

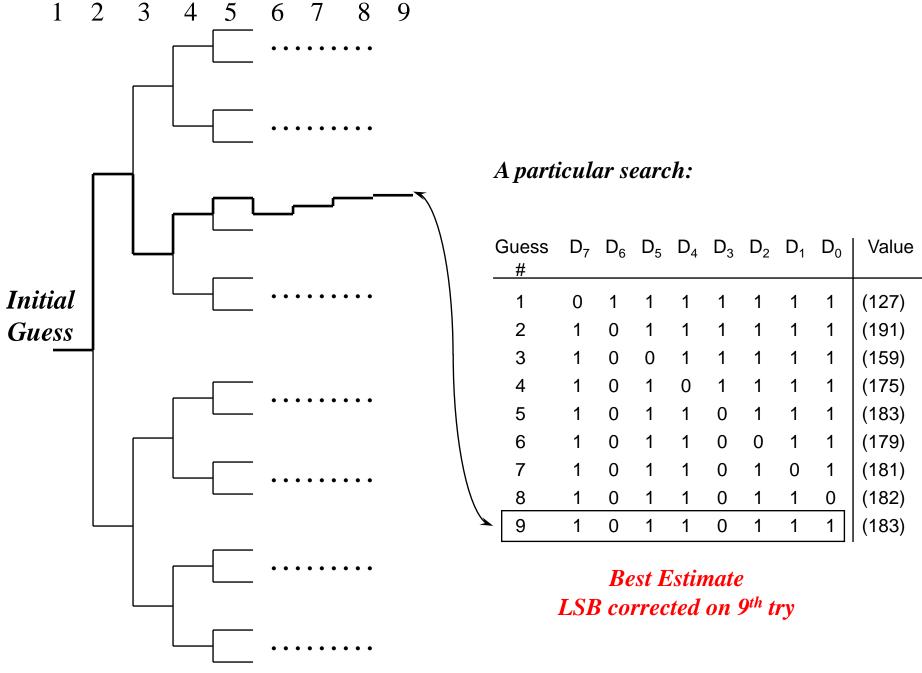
step 2 – If max < min, then stop. No element matches the key.

step 3 – Let mean = (max + min)/2.

step 4 – If key equals arr[mean], then key is found in the array, exit.

step 5 – If key < arr[mean], then set max to mean-1 and go to step 2.

step 6 – If key > arr[mean], then set *min* to mean+1 and go to step 2.



Example: Write a program to implement the binary search algorithm and a sequence of instructions to test it. Use an array of n 8-bit elements for implementation.

n key	EQU EQU	45 69	srch_lo	BRA LDAA	loop mean
	ORG CLRA	\$1000		DECA STAA BRA	max loop
	STAA STAA LDAB	min ; initialize result ; min \$ result #n-1	found nfound	STAA SWI	result
	STAB	max ; initialize max			
loop	LDX CLRA	#arr ; set pointer	max min	RMB RMB	1
	LDAB CMPB	min max	mean result	RMB RMB	1
	LBHI	nfound			-
	ADDB ADCA	max #0	arr	DB DB	1,3,6,9,11,20,30,45 48,60,61,63,64,65
	LSRD STAB	mean		DB DB	67,69,72,74,76,79,80 83,85,88,90,110,113
	LDAA CMPA	B,X #key		DB DB	114,120,123,142,151 175,183,186,190,199
	BEQ	found		DB	200,215,218,222,234
	BHI LDAA	srch_lo mean		DB	237,241,252
	INCA STAA	min		END	

Passing Parameters in Subroutine

The passing of arguments is implemented by means of:

- Registers
- Global variables
- > Stack
- > An argument list
- A table

An example for some cases will follow.

Passing Parameters By Register(s)

Example:

Write a subroutine to compute the average of an array with N 8-bit elements, and write the instruction sequence to call the subroutine. The array starts at ARRAY. Use registers to pass parameters and return the average in the B accumulator.

average	CMPA BLO BEQ	#1 err ans	; check if N < 1 ; if array empty, exit with message ; single element array
ans	LDAB RTS	0,X	; get the single element and return ;
err errmsg	LDD LDX JSR RTS FCC	#errmsg printf 0,X	; let user know that array is empty ; display the message ; ; is empty!! Can not find the average.'

average	СМРА	#1	; check if N < 1
	BLO	err	; if array empty, exit with message
	BEQ	ans	; single element array
	TAB		; create a 2-byte number out of N
	CLRA		;
	XGDY		; place N in Y
	PSHY		; secure N in stack
	CLRA		; initialize the array sum to zero
	CLRB		;
loop	ADDB	1,X+	; add an element to the sum
	ADCA	#0	; add carry to the upper 8-bit of the sum
	DBNE	Y,loop	; is this end of the loop?
	PULX		; load N into X
	IDIV		; compute the array average
	XGDX		; B accumulator has the average
	RTS		;
ans	LDAB	0,X	; get the single element and return
	RTS	•	;
err	LDD	#errmsg	; let user know that array is empty
011	LDX	printf	; display the message
	JSR	OUTSTRG	·
	RTS	OUTOTING	•
errmsg	FCC	'The array i	s empty!! Can not find the average.'
- -	DB	\$0D,\$0A,0	

Passing Parameters Using Stack

Example:

Write a subroutine to find the maximum element of an array, and write an instruction sequence to call this subroutine. The following parameters are passed in the stack: *array* - the starting address of the given array; *arcnt* - the array count; and *armax* - address to hold the maximum element of the array.

```
* Calling sequence ......

. LDX #array
PSHX
LDAA #arcnt
PSHA
LDX #armax
PSHX
JSR MAX
LEAS 5,SP ; clean up the stack
. . .
```

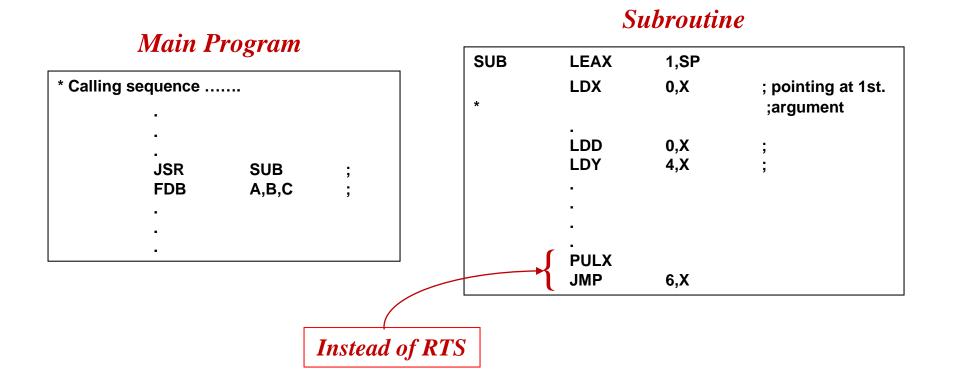
MAX	LEAY LDX LDAA	1,SP 3,Y 0,X	; point Y to top element of stack ; place address 'array' in X ; get the first element
	LDAB CMPB BLO BEQ	2,Y #1 err ans	; load the array count into B ; check array count ; let user know array is empty ; single element array
ans	STAA	0,X	; save the array MAX
err	RTS LDD	#errmsg	; ; let user know that array is empty
GII	LDX JSR RTS	printf 0,X	; display the message
errmsg	FCC DB	'The array \$0D,\$0A,0	is empty!! Can not find the maximum.'

MAX	LEAY	3,SP	; point Y to top element of stack
	LDX	3,Y	; place address 'array' in X
	LDAA	0,X	; get the first element
	LDAB	2,Y	; load the array count into B
	CMPB	#1	; check array count
	BLO	err	; let user know array is empty
	BEQ	ans	; single element array
Іоор	CMPA	1,+X	; compare the next element with the MAX
	BHS	noswap	; should MAX be updated
	LDAA	0,X	; update MAX
noswap	DBNE	B,loop	; decrement loop count, is this end of the loop?
ans	LDX	0,Y	; load 'armax' into X
	STAA	0,X	; save the array MAX
	RTS		;
err	LDD	#errmsg	; let user know that array is empty
	LDX	printf	; display the message
	JSR	0,X	;
	RTS	•	;
errmsg	FCC	'The array is empty!! Can not find the maximum.'	
	DB	\$0D,\$0A,0	

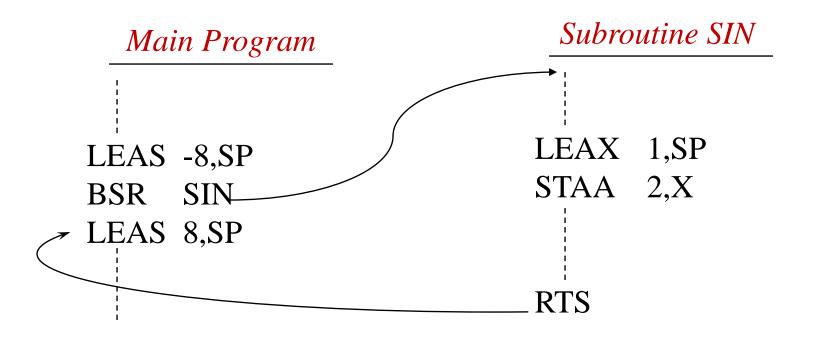
Passing Parameters By Argument List

Example:

How to implement equivalent of CALL SUB(A,B,C)?



How to Create Hole in the Stack



This example created an 8-byte hole in the stack. The hole can be as many byte as desired.