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# Matrices and Vectors

Matrices are 2-dimensional arrays:

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \\ j & k & l \end{bmatrix}$$

The above matrix has four rows and three columns, so it is a 4 x 3 matrix.

A vector is a matrix with one column and many rows:

$$\begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix}$$

So vectors are a subset of matrices. The above vector is a 4 x 1 matrix.

## Notation and terms:

- $A_{ij}$  refers to the element in the  $i$ th row and  $j$ th column of matrix  $A$ .
- A vector with ' $n$ ' rows is referred to as an ' $n$ '-dimensional vector.
- $v_i$  refers to the element in the  $i$ th row of the vector.
- In general, all our vectors and matrices will be 1-indexed. Note that for some programming languages, the arrays are 0-indexed.
- Matrices are usually denoted by uppercase names while vectors are lowercase.
- "Scalar" means that an object is a single value, not a vector or matrix.
- $\mathbb{R}$  refers to the set of scalar real numbers.
- $\mathbb{R}^n$  refers to the set of  $n$ -dimensional vectors of real numbers.

Run the cell below to get familiar with the commands in Octave/Matlab. Feel free to create matrices and vectors and try out different things.

```
1 % The ; denotes we are going back to a new row.
2 A = [1, 2, 3; 4, 5, 6; 7, 8, 9; 10, 11, 12]
3
4 % Initialize a vector
5 v = [1;2;3]
6
7 % Get the dimension of the matrix A where m = rows and n = columns
8 [m,n] = size(A)
9
10 % You could also store it this way
11 dim_A = size(A)
12
13 % Get the dimension of the vector v
14 dim_v = size(v)
15
16 % Now let's index into the 2nd row 3rd column of matrix A
17 A_23 = A(2,3)
18
```

A =

|    |    |    |
|----|----|----|
| 1  | 2  | 3  |
| 4  | 5  | 6  |
| 7  | 8  | 9  |
| 10 | 11 | 12 |

v =

|   |
|---|
| 1 |
| 2 |
| 3 |

m = 4

n = 3

dim\_A =

|   |   |
|---|---|
| 4 | 3 |
|---|---|

dim\_v =

|   |   |
|---|---|
| 3 | 1 |
|---|---|

A\_23 = 6

