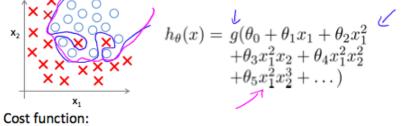
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## Regularized Logistic Regression

We can regularize logistic regression in a similar way that we regularize linear regression. As a result, we can avoid overfitting. The following image shows how the regularized function, displayed by the pink line, is less likely to overfit than the non-regularized function represented by the blue line:

## Regularized logistic regression.



$$\Rightarrow J(\theta) = -\left[\frac{1}{m}\sum_{i=1}^{m}y^{(i)}\log h_{\theta}(x^{(i)}) + (1 - y^{(i)})\log(1 - h_{\theta}(x^{(i)}))\right] + \frac{\lambda}{2m}\sum_{j=1}^{n}\bigotimes_{j}^{n}\bigotimes_{j}^{n}$$

## **Cost Function**

Recall that our cost function for logistic regression was:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} [y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))]$$

We can regularize this equation by adding a term to the end:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^{m} [y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))] + \frac{\lambda}{2m} \sum_{j=1}^{n} \theta_{j}^{2}$$

The second sum,  $\sum_{j=1}^n \theta_j^2$  means to explicitly exclude the bias term,  $\theta_0$ . I.e. the  $\theta$  vector is indexed from 0 to n (holding n+1 values,  $\theta_0$  through  $\theta_n$ ), and this sum explicitly skips  $\theta_0$ , by running from 1 to n, skipping 0. Thus, when computing the equation, we should continuously update the two following equations:

## **Gradient descent**

Repeat {  $\Rightarrow \quad \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_0^{(i)}$   $\Rightarrow \quad \theta_j := \theta_j - \alpha \underbrace{\left[ \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \frac{\lambda}{m} \mathfrak{S}_j \right]}_{\left[j = \mathbf{X}, 1, 2, 3, \dots, n\right)}$  }  $\underbrace{\left[ \frac{\lambda}{\partial \mathfrak{S}_j} \underbrace{\mathcal{I}(\mathfrak{S})}_{i} \underbrace{\mathcal{I}(\mathfrak{S}_j)}_{i} \underbrace{\mathcal{I}$ 

✓ Complete

