

Note template

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Abstract

This is a note template, with all but minimal compilable files provided. Feel free to adjust for your usage.
Now let's start a simple demo for you to take fancy notes in L^AT_EX!

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Chapter 1

Entropy

Definition 1.0.1 (Entropy). A measure of uncertainty of a physical system.

$$H(x) = H(p_1, p_2, \dots, p_n) = - \sum_x p_x \log p_x$$

$$\lim_{p \rightarrow 0} p \log p = 0$$

X - Information we gain, on an average when we learn the value of X.

Example. Coin toss :- HHHH - H, if it gives only heads, Information gain is zero.

Operational interpretation of entropy

Entropy is tied to memory resources.

Example. X takes values (x_1, x_2, x_3, x_4) with probability $(\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{8})$
encoding them with (0, 10, 110, 111) $\Rightarrow \frac{1}{2}[1] + \frac{1}{4}[2] + \frac{1}{8}[3] + \frac{1}{8}[3] = \frac{7}{4}$ bits

$$- \sum_{x=1}^4 p_x \log p_x = \frac{7}{4} \text{ bits}$$

Example. For a coin $p_H = 1$ and $p_T = 0$ size of memory = 0

Entropy from intuitive axioms

1. $I(p)$
2. $I(p)$ is smooth
3. $I(pq) = I(p) + I(q)$

Appendix

Appendix A

Additional Proofs

A.1 Proof of ??

We can now prove ??.

Proof of ??. See https://en.wikipedia.org/wiki/Mass%E2%80%93energy_equivalence. ■