EP3110 - Electro-magnetics and Applications

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Abstract

Instructor:P Murugavel (HSB 116B)
Lecture Timings: D Slot (Mon – 11am, Tue – 10am, Wed - 9am)
Venue: HSB 263
Course Outline: Learning objectives This is an intermediate level course in electromagnetic fields and assumes background in electrostatics, magneto-statics and introductory knowledge in electrodynamics. The main objective is to introduce electromagnetic fields with emphasis on analytical rigour and physical reasoning required for solving problems having direct application. The course will also provide sufficient background to motivate students to take up advanced levels courses such as, electromagnetic scattering, computational electrodynamics, etc. Learning outcomes Upon successful completion, the students will have learned i. the importance of constitutive properties of materials and their use in applications, ii. the effect of boundaries and be able to develop and analyze optical coatings, iii. time dependent formulation of potentials and fields, and fields dues to moving charges, iv. the fundamental ideas in electromagnetic scattering with relevance to applications and v) the concept of waveguides and propagation of guided electromagnetic waves. **Pre-requisite**: PH1020 - Physics II

Grading: Assignments - 10 marks Quiz I - 20 marks Quiz II - 20 marks End-semester - 50 marks

Contents

Chapter 1

Electrodynamics(Review)

Lecture 1: First Lecture

1.1   Electrostatics(Review)

Two postulates(propositions) in Electrostatics

Proposition 1.1.1.

$$\vec{\nabla}.\vec{E} = \frac{\rho}{\epsilon_o}$$

$$\oint_s \vec{E}.\vec{ds} = \frac{Q_{en}}{\epsilon_o}$$

Proposition 1.1.2.

$$\vec{\nabla} X \vec{E} = \vec{0}$$

$$\oint_c \vec{E}.\vec{dl} = 0$$

Electric field around a closed path is 0.

Theorem 1.1.1. kirchhoff's voltage Law, Algebraic sum of voltage drop in a closed loop is zero.

Theorem 1.1.2 (Coloumbs Law). $\vec{E}$ due to a point charge "q" is

$$\vec{E} = \frac{1}{4\pi\epsilon_o} \frac{q}{\left|\vec{R}\right|^3} \vec{R}$$

For a discrete distribution of charges

$$\vec{E} = \frac{1}{4\pi\epsilon_o} \sum_{j=1}^{n} \frac{q_j}{\left|\vec{R}-\vec{R_j}\right|^3} (\vec{R}-\vec{R_j})$$

For a continuos distribution of charges

$$\vec{E} = \frac{1}{4\pi\epsilon_o} \int \hat{R} \frac{\rho}{\vec{R}^2} dV'$$

since,

$$\vec{\nabla} X \vec{E} = \vec{0}$$

$$\vec{E} = -\vec{\nabla} V$$

Negative sign because potential decreases in the direction of electric field by convention.

> **Definition 1.1.1.**
> $$\vec{E} = -\vec{\nabla}V$$
> $$V_2 - V_1 = \int_{P_1}^{P_2} \vec{E}.\vec{dl}$$
> $$V(R) = \frac{1}{4\pi\epsilon_o} \int \frac{\rho}{R} dV'$$
> prime indicates coordinate system w.r.t source.

> **Definition 1.1.2** (Dipole)**.** A pair of equal and opposite charges separated by a distance.

$$V_p(R) = \frac{q}{4\pi\epsilon_o}[\frac{1}{R_+} - \frac{1}{R_-}]$$

$$V_p(R) = \frac{qd\cos\theta}{4\pi\epsilon_o R^2} = \frac{\vec{p}.\hat{R}}{4\pi\epsilon_o R^2}$$

$$\vec{E_p}(R) = -\vec{\nabla}V_p(R)$$

$$\vec{E_p}(R) = [-\hat{R}\frac{\partial}{\partial R} - \frac{\hat{\theta}}{R}\frac{\partial}{\partial\theta}]V_p(R)$$

$$\vec{E} = \frac{\vec{p}}{4\pi\epsilon_o R^3}[2\cos\theta\hat{R} + \sin\theta\hat{\theta}]$$

$$\vec{E} = \frac{1}{4\pi\epsilon_o R^3}[3(\vec{p}.\hat{R})\hat{R} - \vec{p}]$$

Conductor

$\vec{E} = 0$ inside a conductor.

$$\oint_c \vec{E}.\vec{dl} = 0$$

$$\vec{E_{t1}}.\Delta\vec{w} - \vec{E_{t2}}\Delta\vec{w} = 0$$

$\vec{E_{t1}} = 0 \because$ inside a conductor.

$\therefore \vec{E_{t2}} = 0$.
$\therefore$ No tangential electric field.

$$\frac{\sigma_s\Delta s}{\epsilon_o} = [\vec{E_1}.\vec{n_1} + \vec{E_2}.\vec{n_2}]\Delta s$$

$$\vec{E_2} = 0$$

inside a conductor.

$$\vec{E_1} = \frac{\sigma_s}{\epsilon_o}\hat{n}$$

Normal electric field is $\vec{E_n} = \frac{\sigma_s}{\epsilon_o}\hat{n}$

Dielectric in a static $\vec{E}$

$$\vec{p} = q\vec{d}$$
$$\vec{\tau} = \vec{p}X\vec{E}$$
$$U = -\vec{p}.\vec{E}$$

Gauss law in differential form

$$\vec{\nabla}.\vec{E} = \frac{\rho}{\epsilon_o} = \frac{1}{\epsilon_o}[\rho_f + \rho_b]$$

> **Definition 1.1.3.** The *polarization* of a medium P gives the electric dipole moment per unit volume of the material.
> $$\vec{P} = \frac{n\vec{p}}{V}$$

Bound charges

$$\sigma_b = -\vec{P}.\hat{n}$$

$$\rho_b = -\vec{\nabla}.\vec{P}$$

Potential V,

$$V = \frac{1}{4\pi\epsilon_o} \oint \frac{\vec{P}.\hat{n}}{R} ds + \frac{1}{4\pi\epsilon_o} \int \frac{-\vec{\nabla}.\vec{P}}{R} dV$$

refer David J griffith's for detailed explanation.

For a Dielectric,

$$\vec{\nabla}.\vec{E} = \frac{1}{\epsilon_o}(\rho_f - \vec{\nabla}.\vec{P})$$

$$\vec{\nabla}.[\epsilon_o\vec{E} + \vec{P}] = \rho_f$$

> **Definition 1.1.4.** Displacement vector, $\vec{D} = \epsilon_o\vec{E} + \vec{P}$
> $$\vec{\nabla}.\vec{D} = \rho_f$$

Lecture 2: Second Lecture

Linear isotropic

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Appendix

Appendix A

Additional Proofs

A.1 Proof of ??

We can now prove **??**.

> **Proof of ??.** See https://en.wikipedia.org/wiki/Mass%E2%80%93energy_equivalence. ∎