ARE213 Problem Set #2A

Peter Alstone & Frank Proulx November 6, 2013

1 Problem #1 and #2

These are hand written and attached separately.

2 Problem #3

2.1 Part A

Running pooled bivariate OLS, adding a quadratic time trend, and adding the covariates that we expect to belong produces the models shown in Table 1. The pooled OLS is an ill-informed baseline model but nonetheless tells us that there is a statistically significant negative correlation between the states with primary seatbelt laws and those without. In particular, the mean of the log fatalities per capita is reduced by 0.14 for states with primary seatbelt laws. This does not, however, account for the year to year trends that are captured by including a set of quadratic year terms in the regression as shown in the "quadratic time" regression. This basic trend is that deaths have gone down over time. Correcting for these trends may allow our OLS estimates approach the true ATE, and indeed the apparent effect of primary seatbelt laws is reduced. When further covariates are added that are relevant (see Table 1) further reductions in the apparent effect occur and the effect is no longer statistically significant.

2.2 Part B

No, the standard errors are most likely not correct (are they ever really, truly correct outside a purely theoretical framework?). In this case the error

Table 1: Pooled Models of Fatalities Per Capita

	bivariate	$\log ext{fatalpc}$ quadratic time	covariates
	(1)	(2)	(3)
primary	-0.144*** (0.026)	-0.075*** (0.026)	0.015 (0.027)
year		-0.025^{***} (0.006)	$-0.042^{***} $ (0.005)
sqr.year		$0.0005^* \ (0.0002)$	0.001*** (0.0002)
secondary			-0.001 (0.022)
college			-2.902^{***} (0.176)
beer			0.268*** (0.031)
totalvmt			-0.00000^{***} (0.00000)
precip			-0.015** (0.006)
snow32			-0.297^{***} (0.017)
rural_speed			0.016*** (0.002)
urban_speed			0.005*** (0.002)
Constant	-1.703^{***} (0.011)	-1.506*** (0.031)	-2.153^{***} (0.143)
N R^2 Adjusted R^2 F Statistic	$ \begin{array}{c} 1,127 \\ 0.027 \\ 0.027 \\ 31.007**** (df = 1; 1125) \end{array} $	$ \begin{array}{c} 1,127 \\ 0.094 \\ 0.094 \\ 39.030^{***} \text{ (df = 3; 1123)} \end{array} $	$ \begin{array}{c} 1,127 \\ 0.596 \\ 0.590 \\ 149.510^{***} \text{ (df} = 11; 1115) \end{array} $

Notes:

^{***}Significant at the 1 percent level.
**Significant at the 5 percent level.

^{*}Significant at the 10 percent level.

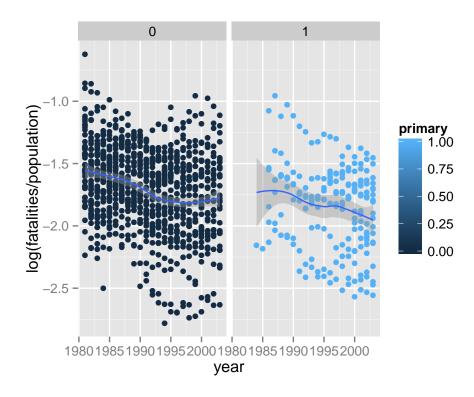


Figure 1: Year to year trends in the log of traffic fatalities per capita, divided by primary seatbelt law presence. A LOESS fit to each dataset is included for reference but is not necessarily indicative of the true underlying function.

in the SE estimates comes from heteroscedasticity in the error terms from the regression. Table 2 shows that introducing robust standard errors (using the HC1 estimator for the OLS covariance matrix). Clustering on the state grouping only increases the SE slightly over the robust pooled version, indicating most of the heteroscedasticity is in the full sample and not withingroup. Table 3 shows the results of calculating the standard errors by hand, using the code shown in the code listings section at the end (with a call out to that section of code).

2.3 Part C

The between estimator will give an unbiased estimate of the effect of primary seat belt laws insofar as variation within states (across time) is uncorrelated with the observables.

We don't think that this criterion is met here. For example, within a given state, the total vmt per year probably tracks very closely with fatalities, as the higher VMT within a given year, the more likely there are to be fatal crashes (ceteris paribus).

The standard errors are sufficiently large in this model that we cannot rule out the null hypothesis (no effect of primary seatbelt laws) in either the simple case or the case with covariates.

2.4 Part D

The RE estimator will give an unbiased estimate so long as the within states variation is uncorrelated with observables. Again, this assumption is probably not met here. In the RE model we find (for the first time) that seat belt laws appear to be correlated with statistical significance with reduced fatalities....but do we trust these? Table ?? summarizes the results for the RE model both with and without covariates.

The Random Effects estimator has the advantage over pooled OLS that it allows for (and assumes) unobserved heterogeneity. OLS has the advantage that it is more efficient than the Random Effects estimator when said heterogeneity does not exist.

Table 2: Comparison of Standard Error HC Methods for Full Pooled Model

	Conventional	HC1 Robust	HC1 Robust + Cluster
	(1)	(2)	(3)
primary	0.015 (0.027)	0.015 (0.054)	0.015 (0.054)
year	-0.042^{***} (0.005)	-0.042^{***} (0.008)	-0.042^{***} (0.008)
sqr.year	0.001*** (0.0002)	0.001*** (0.0002)	0.001*** (0.0002)
secondary	-0.001 (0.022)	-0.001 (0.036)	-0.001 (0.036)
college	-2.902^{***} (0.176)	-2.902^{***} (0.446)	-2.902^{***} (0.448)
beer	0.268*** (0.031)	0.268*** (0.082)	0.268*** (0.082)
totalvmt	-0.00000*** (0.00000)	-0.00000*** (0.00000)	-0.00000*** (0.00000)
precip	-0.015** (0.006)	-0.015 (0.020)	-0.015 (0.020)
snow32	-0.297^{***} (0.017)	-0.297^{***} (0.052)	-0.297^{***} (0.053)
rural_speed	0.016*** (0.002)	0.016*** (0.004)	0.016*** (0.004)
urban_speed	0.005*** (0.002)	0.005 (0.003)	0.005 (0.003)
Constant	-2.153^{***} (0.143)	-2.153^{***} (0.277)	-2.153^{***} (0.278)

Notes:

 $^{^{***} \}mbox{Significant}$ at the 1 percent level. $^{**} \mbox{Significant}$ at the 5 percent level.

^{*}Significant at the 10 percent level.

Table 3: Comparison of Standard Error HC Methods for Full Pooled Model, as calculated by hand

Estimand	Conventional	Robust	Clustered
(Intercept)	0.143092450051489	0.126275629333705	0.281056533719271
primary	0.0265477092390901	0.0242822007396392	0.0546894368905662
year	0.00545503338475101	0.00598682459203165	0.008116358583959
sqr.year	0.000190755819683876	0.000207479039052758	0.000246751758184774
secondary	0.0217508276594709	0.0209373279397145	0.0366521092326508
college	0.176245827507398	0.160526783925961	0.452606339396885
beer	0.0308798425250644	0.0281117000066882	0.0832087347114592
totalvmt	1.49368657811726e-07	1.27908631373882e-07	$4.18638264362754 \mathrm{e}\text{-}07$
precip	0.00596563120372605	0.00600959436593229	0.0203958411221209
snow32	0.0174085751012179	0.0181916999791943	0.0531907707309941
$rural_speed$	0.0021413549507371	0.00209161539190941	0.00376049997220133
$\underline{\text{urban_speed}}$	0.00176934150104297	0.00163910252777972	0.00316920102721627

2.5 Part E

The conventional standard errors for the RE model are likely incorrect because of a built-in assumption that the errors within each individual are correlated equally over time. Because this is a long-term dataset we would prefer to relax this assumption by introducing robust clustered SE estimates. Table 6 shows that this increases the SE of the coefficient on primary seatbelt use, but only by about double. The SE is still small compared to the estimand.

2.6 Part F

The conventional and clustered standard errors differ (as they have for many other approaches) by about a factor of two in the FE method. These are compared in Table 7. The baseline standard errors (or roughly the coefficient of variation) is small for the fixed effects model because all of the unobserved individual state characteristics are wrapped up in the FE model without any between-ness muddying their influence. However, there remain heteroscedastic errors within each state from idiosyncrasies between time periods when states did and did not have seat belt laws (national-level trends, automobile manufacturing standards, etc.) that are exogenous to the states and link

Table 4: Between models of effects of primary seatbelt use laws

	Dependent variable:	
	logfatalpc	
	(1)	(2)
primary	-0.071	0.114
	(0.155)	(0.165)
secondary		-0.025
v		(0.159)
college		-2.603***
		(0.636)
totalvmt		-0.00000**
		(0.00000)
snow32		-0.266***
		(0.083)
rural_speed		0.063***
		(0.012)
Constant	-1.716***	-4.978***
	(0.052)	(0.789)
Observations	49	49
$ m R^2$	0.004	0.758
Adjusted R ²	0.004	0.650
F Statistic	0.212 (df = 1; 47)	$21.898^{***} (df = 6; 42)$
Note:	*n<0.1·**n<0.05·***n<0.01	

Note:

*p<0.1; **p<0.05; ***p<0.01

Table 5: Random Effects Models

	Depender	nt variable:
	$\log f_{i}$	atalpc
	(1)	(2)
primary	-0.230***	-0.138***
	(0.016)	(0.015)
secondary		-0.065***
		(0.010)
college		-1.420***
		(0.169)
unemploy		-0.024***
		(0.002)
beer		0.757***
		(0.038)
totalvmt		-0.00000***
		(0.00000)
precip		-0.024***
		(0.006)
snow32		-0.018
		(0.014)
rural_speed		-0.006***
		(0.001)
urban_speed		0.003***
		(0.001)
Constant	-1.688***	-1.902***
	(0.044)	(0.092)
Observations	1,127	1,127
\mathbb{R}^2	0.153	0.604
Adjusted R ²	0.153	0.598
F Statistic	$203.173^{***} (df = 1; 1125)$	$170.214^{***} (df = 10; 1116)$

Note:

*p<0.1; **p<0.05; ***p<0.01

Table 6: Comparison of Standard Error HC Methods for RE model with covariates

	Conventional SE	HC1 Robust + Cluster
	(1)	(2)
primary	-0.138***	-0.138***
	(0.015)	(0.029)
secondary	-0.065***	-0.065^{***}
	(0.010)	(0.018)
college	-1.420^{***}	-1.420^{***}
	(0.169)	(0.296)
unemploy	-0.024***	-0.024***
1 0	(0.002)	(0.003)
beer	0.757***	0.757***
	(0.038)	(0.068)
totalvmt	-0.00000***	-0.00000**
	(0.00000)	(0.00000)
precip	-0.024***	-0.024***
	(0.006)	(0.007)
snow32	-0.018	-0.018
	(0.014)	(0.020)
$rural_speed$	-0.006***	-0.006***
-	(0.001)	(0.002)
urban_speed	0.003***	0.003**
-	(0.001)	(0.001)
Constant	-1.902***	-1.902***
	(0.092)	(0.149)

Notes:

^{***}Significant at the 1 percent level.

^{**}Significant at the 5 percent level.

^{*}Significant at the 10 percent level.

them. Figure 2 shows how the adoption of state-level primary seatbelt laws occurred non-uniformly through the sample.

Table 7: Comparison of Standard Error HC Methods for basic FE model

	Conventional SE	HC1 Robust + Cluster
	(1)	(2)
primary	-0.080***	-0.080**
	(0.015)	(0.033)
year	-0.025***	-0.025***
	(0.002)	(0.004)
sqr.year	0.0005***	0.0005***
	(0.0001)	(0.0001)

Notes:

2.7 Part G

The addition of covariate terms to the FE model reduces the estimate of the ATE for enacting primary seatbelt laws to about a 6% reduction in annual fatalities. With robust / clustered standard errors this is estimate maintains its significance at a 5% confidence level.

3 Code Listings

We used R to complete this assignment...which turned out to be quite challenging in this case, since R has no equivalently easy version of "robust" or "cluster(group)," but it was a learning experience. The code is below:

^{***}Significant at the 1 percent level.

^{**}Significant at the 5 percent level.

^{*}Significant at the 10 percent level.

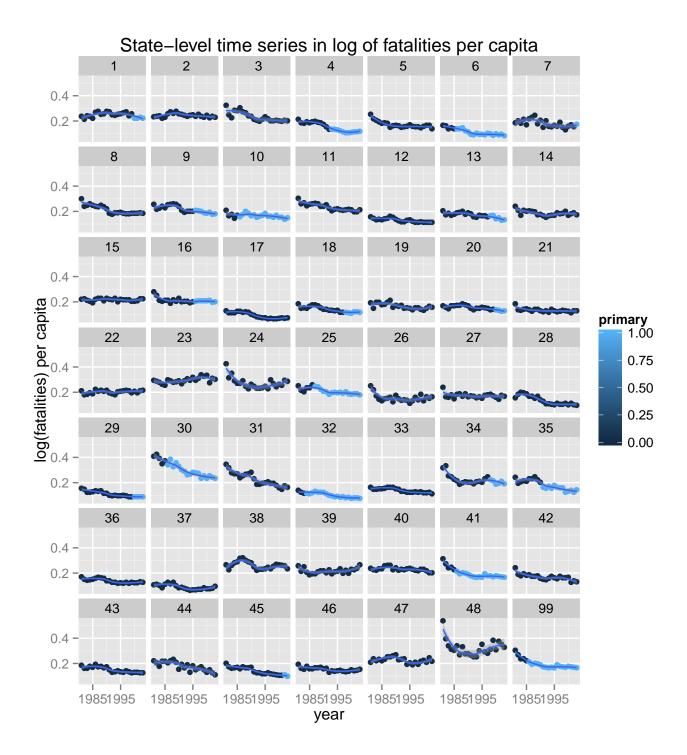


Figure 2: Year to year trends in the log of traffic fatalities per capita, with facets by state ID. A LOESS fit to each dataset is included for reference but is not necessarily indicative of the true underlying function.

Table 8: Fixed Effects Models

		Dependent variable:	
	logfa	atalpc	
	$panel \ linear$		${coefficient} \ {test}$
	Simple FE	FE with Cov.	Robust/Clustered SE
	(1)	(2)	(3)
primary	-0.080***	-0.063***	-0.063**
	(0.015)	(0.016)	(0.032)
year	-0.025***	-0.017***	-0.017***
	(0.002)	(0.003)	(0.004)
sqr.year	0.0005***	0.0002^*	0.0002
	(0.0001)	(0.0001)	(0.0002)
secondary		0.006	0.006
v		(0.011)	(0.021)
college		0.377	0.377
		(0.236)	(0.462)
beer		0.788***	0.788***
		(0.041)	(0.079)
totalvmt		-0.00000	-0.00000
		(0.00000)	(0.00000)
precip		-0.032***	-0.032***
		(0.006)	(0.005)
snow32		-0.007	-0.007
		(0.014)	(0.017)
rural_speed		0.004***	0.004***
-		(0.001)	(0.001)
urban_speed		0.001	0.001
-		(0.001)	(0.001)
Observations	1,127	1,127	
$ m R^2$	0.459	0.625	
Adjusted R ²	0.438	0.591	
F Statistic	$304.360^{***} (df = 3; 1075)$	$\frac{161.455^{***} \text{ (df} = 11; 1067)}{2}$	7)

12

```
51
 6
 7
   library(foreign) #this is to read in Stata data
 8
   library(Hmisc)
 9| library(psych)
10 library(stargazer)
11 library(ggplot2) # for neato plotting tools
|12| library(plyr) # for nice data tools like ddply
13 library(car) # "companion for applied regression" - recode fxn, etc.
|14| library(gmodels) #for Crosstabs
15 library(plm) # for panel data
16 require (lmtest)
17 # require(sandwich)
18
19 source("../util/are213-func.R")
20 #source("../util/watercolor.R") # for watercolor plots
21
22|ps2a.data \leftarrow read.dta('traffic_safety2.dta')
23 ps2a.datakey <- data.frame(var.name=names(ps2a.data), var.labels = attr(ps2a
       .data, "var.labels"))
   ps2a.data$logfatalpc <- with(ps2a.data, log(fatalities/population))
25
   ps2a.data$sqyears <- with(ps2a.data, year^2)</pre>
26
27ert # Graphical exploration of data
28 pdf(file="allstates.pdf", width = 7, height = 7.5)
29|_{\text{ggplot}(\text{ps2a.data, aes(year, fatalities/population))}} +
30
    geom_point(aes(color=primary)) +
31
     scale_x_continuous(breaks = c(1985, 1995)) +
32
    scale_y_continuous(breaks = c(0.2, 0.4)) +
33
    facet_wrap("state") +
34
    ylab("log(fatalities) per capita") +
35
    ggtitle("State-level time series in log of fatalities per capita") +
36
    stat_smooth()
37
   dev.off()
38
39| #plot 3a
40 makeplot3a <- FALSE
41 if (makeplot3a) {
42 pdf("plot3a.pdf", width=5, height=4)
43 ggplot(ps2a.data, aes(year, log(fatalities/population))) + geom_point(aes(
       color=primary)) + facet_grid(.~primary) + stat_smooth()
   dev.off()
45
   }
46
47
48 \vert #Puts data into pdata.frame for use with the plm package.
   ps2a.pdata <- pdata.frame(ps2a.data, index = c("state", "year"))
50
51| ## Problem 3
52
53| # Issues with non-conforming matrix seem to trace to bad factor class for
       year .... fixed here.
   ps2a.pdata$year <- as.numeric(ps2a.pdata$year)</pre>
56| # ADDDING square year term HERE WORKS FOR WHATEVER REASON
|57| ps2a.pdata$sqr.year <- with(ps2a.pdata, year^2)
58
```

```
59| ## Part A (pooled OLS, quadratic time trend, and all possible covariates)
   pooled.OLS <- plm(logfatalpc ~ primary, data = ps2a.pdata, model = "pooling"</pre>
 61
 62 pooled.quadtime <- plm(logfatalpc ~ primary + year + sqr.year, data = ps2a.
       pdata, model = "pooling")
 63
   |64|
        data = ps2a.pdata, model = "pooling")
 65
 66
   stargazer(pooled.OLS, pooled.quadtime, pooled.full,
 67
              title = "Pooled Models of Fatalities Per Capita",
              style="qje",
 68
 69
              out = 'p3a.tex',
 70
              font.size = "footnotesize",
 71
              column.labels = c("bivariate", "quadratic time", "covariates"),
 72
              label="tab:3a")
 73
 74
   ## Part B (Standard Error Errors) -----
 75
 76 #typical
 77
   a.typ.full <- coeftest(pooled.full)</pre>
 78 #robust
 79 a.robust.full <- coeftest(pooled.full, vcov = vcovHC)
 80| #clustered
a.clust.full <- coeftest(pooled.full, vcov = vcovHC(pooled.full, type="HC1", cluster = "group"))
 82
 83
   stargazer(a.typ.full, a.robust.full, a.clust.full,
              title = "Comparison of Standard Error HC Methods for Full Pooled
                  Model",
 85
              style = "qje",
 86
              out = 'p3b1.tex',
 87
              font.size = "footnotesize",
 88
              column.labels = c("Conventional", "HC1 Robust", "HC1 Robust +
                  Cluster"),
              label="tab:3b1"
 90
 91
 93 ## Robust by hand
                                            #This calculates the Huber-White
                                                Robust standard errors -- code
                                                based on http://thetarzan.
                                                wordpress.com/2011/05/28/
                                                heteroskedasticity-robust-and-
                                                clustered-standard-errors-in-r/
 95 s <- summary(pooled.full)
 96 \mid X \leftarrow model.matrix(pooled.full)
 97 | u2 \leftarrow residuals(pooled.full)^2
98 XDX <- 0
 99
100| for(i in 1:nrow(X)) {
101
       XDX <- XDX +u2[i]*X[i,]%*%t(X[i,])</pre>
102|}
```

```
1031
104
                                                                                                                                           # inverse(X'X)
105 \times 105 
106
107
                                                                                                                                           #Compute variance/covariance matrix
108 varcovar <- XX1 %*% XDX %*% XX1
109
110
                                                                                                                                           # Degrees of freedom adjustment
111 dfc <- sqrt(nrow(X))/sqrt(nrow(X)-ncol(X))
112
113 stdh <- dfc*sqrt(diag(varcovar))
114
115 t <- pooled.full$coefficients/stdh
116|p \leftarrow 2*pnorm(-abs(t))
117 results.robust <- cbind(pooled.full$coefficients, stdh, t, p)
118 dimnames (results.robust) <- dimnames (s$coefficients)
119 results.robust
120
121| ## cluster by hand -- using many of the same variables as defined in the
                      robust section (above), with some modifications:
122| cluster <- "state"
| 123 | clus <- cbind(X, "state"=ps2a.data[,cluster], "resid" = resid(pooled.full))
124
                                                                                                                                           #number of clusters
125|_{\,\mathrm{m}} \leftarrow \dim(\mathrm{table}(\mathrm{clus}[,\mathrm{cluster}]))
126 | k \leftarrow dim(X)[2]
127
128 uj <- matrix(NA, nrow=m, ncol = k)
129 gs <- names(table(ps2a.data[,cluster]))
130| for (i in 1:m){
131
                      uj[i,] <- t(matrix(clus[clus[,cluster]==gs[i], 'resid'])) %*% clus[clus
                                      [,cluster] == gs[i], 1:k]
132|}
133
134
135
                                                                                                                                           #Compute variance/covariance matrix
136 varcovar <- XX1 %*% crossprod(uj) %*% XX1
137
138
                                                                                                                                           # Degrees of freedom adjustment
139 dfc <- sqrt((m/(m-1)) * (nrow(X)-1)/(nrow(X)-ncol(X)))
140
141 stdh <- dfc*sqrt(diag(varcovar))
142
143|\,\mathrm{t} <- pooled.full$coefficients/stdh
144|p \leftarrow 2*pnorm(-abs(t))
|145| results.cluster <- cbind(pooled.full$coefficients, stdh, t, p)
146 dimnames (results.cluster) <- dimnames (s$coefficients)
147 results.cluster
148
|149| hand.comparison <- cbind(rownames(results.cluster), a.typ.full[,2], results.
                       robust[,2], results.cluster[,2])
150
            colnames(hand.comparison) <- c("Estimand", "Conventional", "Robust", "</pre>
                         Clustered")
151
            stargazer(data.frame(hand.comparison),
152
                                            summary = FALSE,
                                            title = "Comparison of Standard Error HC Methods for Full Pooled
153
                                                        Model, as calculated by hand",
154
                                            style = "qje",
```

```
155
              out = 'p3b2.tex',
156
              font.size = "footnotesize",
157
              column.labels = c("Conventional", "HC1 Robust", "HC1 Robust +
                  Cluster"),
158
              label="tab:3b2"
159
160
161
162 \, | \, ## Part C: compute between estimator w/ and w/o covariates----
163 between.nocov <- plm(logfatalpc ~ primary, data = ps2a.pdata, model = "
        between")
164| between.cov <- plm(logfatalpc \tilde{\ } primary + secondary + college + totalvmt +
        snow32 + rural_speed, data = ps2a.pdata, model = "between")
165
166 stargazer(between.nocov, between.cov, title = "Between models of effects of
        primary seatbelt use laws", out = "p3c.tex", font.size = "footnotesize")
167
168 ## Part D
169 RE.nocov <- plm(logfatalpc ~ primary, data = ps2a.pdata, model = "random") #
        Assumes effects are uncorrelated
|170| RE.cov <- plm(logfatalpc \tilde{} primary + secondary + college + unemploy + beer +
        totalvmt + precip + snow32 + rural_speed + urban_speed, data = ps2a.
        pdata, model = "random")
171
172 stargazer(RE.nocov, RE.cov, title = "Random Effects Models", out = "p3d.tex"
        , font.size = "footnotesize")
173
|174| ## Part E compute cluster standard errors for RE
175
176| e.typ.recov <- coeftest(RE.cov)
177 e.clust.recov <- coeftest(RE.cov, vcov = vcovHC(RE.cov, type = "HC1",
        cluster = "group"))
178
179|\,\mathrm{stargazer}\,(\mathrm{e.typ.recov}\,,\,\,\mathrm{e.clust.recov}\,,
180
              title = "Comparison of Standard Error HC Methods for RE model with
                   covariates",
              style = "qje",
181
182
              out = 'p3e.tex',
183
              font.size = "footnotesize",
184
              column.labels = c("Conventional SE", "HC1 Robust + Cluster"),
185
              label="tab:p3e"
186)
187
188
189
190| ## Part F compute FE estimator
191 fixed.primary <- plm(logfatalpc ~ primary + year + sqr.year, data = ps2a.
        pdata, model = "within")
193 f.typ.fe <- coeftest(fixed.primary)
194| f.clust.fe <- coeftest(fixed.primary, vcov = vcovHC(fixed.primary, type='HC1
        ', cluster = "group"))
195
196 stargazer(f.typ.fe, f.clust.fe,
197
              title = "Comparison of Standard Error HC Methods for basic FE
                  model",
198
              style = "qje",
```

```
199
                out = 'p3f.tex',
200
                font.size = "footnotesize",
201
                column.labels = c("Conventional SE", "HC1 Robust + Cluster"),
202
                label="tab:p3f"
203)
204
205
206 ## Part G
fixed.cov <- plm(logfatalpc ~ primary + year + sqr.year + secondary + college + beer + totalvmt + precip + snow32 + rural_speed + urban_speed,
          data = ps2a.pdata, model = "within")
208
209
    stargazer(fixed.primary, fixed.cov,
210
                coeftest(fixed.cov, vcov = vcovHC(fixed.cov, type="HC1", cluster =
                      "group")),
211
                title = "Fixed Effects Models",
\frac{212}{213}
                out = "p3g.tex", font.size = "footnotesize",
                label = "tab:p3g",
214
                column.labels = c("Simple FE", "FE with Cov.", "Robust/Clustered
                    SE")
215
                )
```

ps2a-paworking.R

3.1 Hand-coded HC Robust Clustered Standard Errors

```
1 ## Robust by hand
  #This calculates the Huber-White Robust standard errors -- code based on
       http://thetarzan.wordpress.com/2011/05/28/heteroskedasticity-robust-and-
       clustered-standard-errors-in-r/
3 s <- summary(pooled.full)
 4 X <- model.matrix(pooled.full)
  u2 <- residuals(pooled.full)^2</pre>
6 x x <- 0
8
  for(i in 1:nrow(X)) {
       XDX <- XDX +u2[i]*X[i,]%*%t(X[i,])</pre>
10|}
11
12 # inverse(X'X)
13 \mid XX1 \leftarrow solve(t(X)\%*\%X)
15 | #Compute variance/covariance matrix
16 varcovar <- XX1 %*% XDX %*% XX1
17
18 # Degrees of freedom adjustment
19 dfc <- sqrt(nrow(X))/sqrt(nrow(X)-ncol(X))
21
   stdh <- dfc*sqrt(diag(varcovar))</pre>
23|t <- pooled.full$coefficients/stdh
24|p \leftarrow 2*pnorm(-abs(t))
```

```
25| results.robust <- cbind(pooled.full$coefficients, stdh, t, p)
26 dimnames (results.robust) <- dimnames (s$coefficients)
27
  results.robust
28
\left.29\right| ## cluster by hand -- using many of the same variables as defined in the
      robust section (above), with some modifications:
30 cluster <- "state"
  clus <- cbind(X, "state"=ps2a.data[,cluster], "resid" = resid(pooled.full))</pre>
32
                                             #number of clusters
33 m <- dim(table(clus[,cluster]))
34 | k < - dim(X)[2]
35
36| uj <- matrix(NA, nrow=m, ncol = k)
371
  gs <- names(table(ps2a.data[,cluster]))</pre>
38 for (i in 1:m){
       uj[i,] <- t(matrix(clus[clus[,cluster]==gs[i], 'resid'])) %*% clus[clus
           [,cluster] == gs[i], 1:k]
40|}
41
42
43 #Compute variance/covariance matrix
44 varcovar <- XX1 %*% crossprod(uj) %*% XX1
45
46 \mid # Degrees of freedom adjustment
47 dfc <- sqrt((m/(m-1)) * (nrow(X)-1)/(nrow(X)-ncol(X)))
48
49 stdh <- dfc*sqrt(diag(varcovar))
50
51| t <- pooled.full$coefficients/stdh
52|p \leftarrow 2*pnorm(-abs(t))
53 results.cluster <- cbind(pooled.full$coefficients, stdh, t, p)
54 dimnames (results.cluster) <- dimnames (s$coefficients)
55
  results.cluster
56
57 hand.comparison <- cbind(a.typ.full[,2], results.robust[,2], results.cluster
       [,2])
58
  colnames(hand.comparison) <- c("Conventional", "Robust", "Clustered")</pre>
59
   stargazer (data.frame (hand.comparison),
             summary = FALSE,
             title = "Comparison of Standard Error HC Methods for Full Pooled
61
                 Model, as calculated by hand",
             style = "qje",
62
63
             out = 'p3b2.tex',
64
             font.size = "footnotesize",
65
             column.labels = c("Conventional", "HC1 Robust", "HC1 Robust +
                 Cluster"),
66
             label="tab:3b2"
67
```

```
# Econometrics helper functions for [R]

# Peter Alstone and Frank Proulx

# 2013

# version 1

6 # contact: peter.alstone AT gmail.com
```

```
# Category: Data Management -----
10
11| # Category: Data Analysis -----
13| # Function: Find adjusted R^2 for subset of data
|14| # This requires a completed linear model...pull out the relevant y-values
       and residuals and feed them to function
15ert # [TODO @Peter] Improve function so it can simply evaluate lm or glm object,
        add error handling, general clean up.
16 adjr2 <- function(y,resid){
17
    r2 <- 1-sum(resid^2) / sum((y-mean(y))^2)
18
     return(r2)
   } #end adjr2
19
20

\begin{array}{c}
\bar{21} \\
22
\end{array}

   # Category: Plots and Graphics -----
23
24 ## Function for arranging ggplots. use png(); arrange(p1, p2, ncol=1); dev.
      off() to save.
   require(grid)
   vp.layout <- function(x, y) viewport(layout.pos.row=x, layout.pos.col=y)</pre>
27
   arrange_ggplot2 <- function(..., nrow=NULL, ncol=NULL, as.table=FALSE) {</pre>
     dots <- list(...)
29
     n <- length(dots)</pre>
30
     if(is.null(nrow) & is.null(ncol)) { nrow = floor(n/2) ; ncol = ceiling(n/
         nrow)}
31
     if(is.null(nrow)) { nrow = ceiling(n/ncol)}
32
     if(is.null(ncol)) { ncol = ceiling(n/nrow)}
33
     ## NOTE see n2mfrow in grDevices for possible alternative
34
     grid.newpage()
35
     pushViewport(viewport(layout=grid.layout(nrow,ncol) ) )
36
     ii.p <- 1
37
     for(ii.row in seq(1, nrow)){
38
       ii.table.row <- ii.row</pre>
39
       if(as.table) {ii.table.row <- nrow - ii.table.row + 1}</pre>
40
       for(ii.col in seq(1, ncol)){
41
         ii.table <- ii.p</pre>
42
         if(ii.p > n) break
43
         print(dots[[ii.table]], vp=vp.layout(ii.table.row, ii.col))
44
         ii.p <- ii.p + 1
45
46
     }
47
   }
48
   robust <- function(model){  #This calculates the Huber-White Robust standard
       errors -- code from http://thetarzan.wordpress.com/2011/05/28/
       heteroskedasticity-robust-and-clustered-standard-errors-in-r/
       s <- summary(model)</pre>
51
       X <- model.matrix(model)</pre>
       u2 <- residuals(model)^2
53
       XDX <- 0
54
55
       for(i in 1:nrow(X)) {
56
           XDX <- XDX +u2[i]*X[i,]%*%t(X[i,])</pre>
57
```

```
# inverse(X'X)
 60
        XX1 <- solve(t(X)%*%X)
 61
 62
    #Compute variance/covariance matrix
 63
        varcovar <- XX1 %*% XDX %*% XX1</pre>
 64
 65
    # Degrees of freedom adjustment
 66
        dfc <- sqrt(nrow(X))/sqrt(nrow(X)-ncol(X))</pre>
 67
 68
        stdh <- dfc*sqrt(diag(varcovar))</pre>
 69
 70
        t <- model$coefficients/stdh
 71
        p <- 2*pnorm(-abs(t))</pre>
 72 \\ 73 \\ 74 \\ 75
        results <- cbind(model$coefficients, stdh, t, p)</pre>
        dimnames(results) <- dimnames(s$coefficients)</pre>
 76
    ## Two functions for clustered standard errors below from: http://people.su.
        se/~ma/clustering.pdf -----
 78
 79
    clx <-
 80
      function(fm, dfcw, cluster){
 81
        # R-codes (www.r-project.org) for computing
 82
        # clustered-standard errors. Mahmood Arai, Jan 26, 2008.
 83
 84
        # The arguments of the function are:
 85
        # fitted model, cluster1 and cluster2
 86
        # You need to install libraries 'sandwich' and 'lmtest'
 87
 88
        # reweighting the var-cov matrix for the within model
 89
        library(sandwich); library(lmtest)
 90
        M <- length(unique(cluster))</pre>
 91
        N <- length(cluster)
 92
        K <- fm$rank
 93
        dfc \leftarrow (M/(M-1))*((N-1)/(N-K))
 94
        uj <- apply(estfun(fm),2, function(x) tapply(x, cluster, sum));</pre>
 95
        vcovCL <- dfc*sandwich(fm, meat=crossprod(uj)/N)*dfcw
 96
        coeftest(fm, vcovCL) }
 97
 98
    mclx <-
99
      function(fm, dfcw, cluster1, cluster2){
100
        # R-codes (www.r-project.org) for computing multi-way
101
        # clustered-standard errors. Mahmood Arai, Jan 26, 2008.
102
        # See: Thompson (2006), Cameron, Gelbach and Miller (2006)
103
        # and Petersen (2006).
104
        # reweighting the var-cov matrix for the within model
105
106
        # The arguments of the function are:
107
        # fitted model, cluster1 and cluster2
108
        # You need to install libraries 'sandwich' and 'lmtest'
109
110
        library(sandwich); library(lmtest)
111
        cluster12 = paste(cluster1,cluster2, sep="")
112
        M1 <- length(unique(cluster1))
113
        M2 <- length(unique(cluster2))
```

```
114|
        M12 <- length(unique(cluster12))</pre>
115
            <- length(cluster1)
116
        K
            <- fm$rank
117
        dfc1 <- (M1/(M1-1))*((N-1)/(N-K))
        dfc2 <- (M2/(M2-1))*((N-1)/(N-K))
118
119
        dfc12 \leftarrow (M12/(M12-1))*((N-1)/(N-K))
120
               <- apply(estfun(fm), 2, function(x) tapply(x, cluster1,</pre>
121
        u2j
               <- apply(estfun(fm), 2, function(x) tapply(x, cluster2,
122
              <- apply(estfun(fm), 2, function(x) tapply(x, cluster12, sum))</pre>
        u12j
123
               <- dfc1*sandwich(fm, meat=crossprod(u1j)/N)
        vc1
124
               <- dfc2*sandwich(fm, meat=crossprod(u2j)/N)
125
        vc12 <- dfc12*sandwich(fm, meat=crossprod(u12j)/N)
126
        vcovMCL \leftarrow (vc1 + vc2 - vc12)*dfcw
127
        coeftest(fm, vcovMCL)}
128
129 ## Function to compute ols standard errors , robust, clustered...
130| ## Based on http://diffuseprior.wordpress.com/2012/06/15/standard-robust-and
        -clustered-standard-errors-computed-in-r/
131
    ols.hetero <- function(form, data, robust=FALSE, cluster=NULL,digits=3){
132
      r1 <- lm(form, data)
133
      if(length(cluster)!=0){
134
        data <- na.omit(data[,c(colnames(r1$model),cluster)])</pre>
135
        r1 <- lm(form, data)
136
137
      X <- model.matrix(r1)</pre>
138
      n \leftarrow dim(X)[1]
139
      k \leftarrow dim(X)[2]
140
      if(robust==FALSE & length(cluster)==0){
141
        se <- sqrt(diag(solve(crossprod(X)) * as.numeric(crossprod(resid(r1))/(n</pre>
            -k))))
142
        res <- cbind(coef(r1),se)
143
      }
144
      if(robust == TRUE) {
145
        u <- matrix(resid(r1))
146
        meat1 \leftarrow t(X) %*% diag(diag(crossprod(t(u)))) %*% X
147
        dfc \leftarrow n/(n-k)
148
        se <- sqrt(dfc*diag(solve(crossprod(X)) %*% meat1 %*% solve(crossprod(X))  
            )))
149
        res <- cbind(coef(r1),se)
150
151
      if(length(cluster)!=0){
152
        clus <- cbind(X,data[,cluster],resid(r1))</pre>
153
        colnames(clus)[(dim(clus)[2]-1):dim(clus)[2]] <- c(cluster, "resid")</pre>
154
        m <- dim(table(clus[,cluster]))</pre>
155
        dfc \leftarrow (m/(m-1))*((n-1)/(n-k))
156
        uclust <- apply(resid(r1)*X,2, function(x) tapply(x, clus[,cluster],
            sum))
157
           <- sqrt(diag(solve(crossprod(X)) %*% (t(uclust) %*% uclust) %*% solve</pre>
            (crossprod(X)))*dfc)
158
        res <- cbind(coef(r1),se)
159
160
      res <- cbind(res,res[,1]/res[,2],(1-pnorm(abs(res[,1]/res[,2])))*2)
      res1 <- matrix(as.numeric(sprintf(paste("%.",paste(digits,"f",sep=""),sep=
161
          ""),res)),nrow=dim(res)[1])
162
      rownames(res1) <- rownames(res)</pre>
163
      colnames(res1) <- c("Estimate","Std. Error","t value","Pr(>|t|)")
164
      return(res1)
```

165	}
	/util/are213-func.R