## ARE213 Problem Set #3

Peter Alstone & Frank Proulx November 30, 2013

## 1 Problem 1: Linear models

## 1.1 Part A: LM results comparison

Using a series of linear models (with heteroskedasticity consistent "robust" standard errors), we find that for a range of model formulations there is a significant effect on housing price from the presence of hazardous waste cleanup sites, but not in the direction one would expect. Instead of a reduction in housing value we estimate an increase in the value, which does not seem likely to be true. The coefficient for the hazardous waste indicator variable (npl2000) takes a wide range of values depending on which additional explanatory variables are included in the model, from 0.04 (i.e., approximately a 4% increase) for the simple model only including 1980 housing values and npl2000 to estimate 2000 housing values, to 0.09 for a model including both housing and demographic characteristics.

Requirements for Unbiased Estimates [add to this]: For our estimates to be unbiased we would need to include all of the potential sources of variation in housing price in a linear model. A particular challenge is that there are very few sites with NPL2000 status (only 2% of sites), so while the overall sample size is large there is very little support for estimates related to NPL2000 status compared to other covariates.

Table 1: Linear models for effect of  $\mathrm{NPL}(2000)$  on housing value (with many additional state fixed effects omitted)

	simple model	+housing char.	+demographics	+state fixed effects
	(1)	(2)	(3)	(4)
npl2000	0.040*** (0.012)	0.055*** (0.012)	0.090*** (0.010)	0.068*** (0.009)
lnmeanhs8	$0.856^{***} (0.011)$	$0.866^{***} (0.018)$	$0.619^{***} (0.022)$	$0.514^{***}(0.022)$
firestoveheat80		$0.074^{***} (0.020)$	0.182***(0.023)	0.230*** (0.033)
nofullkitchen80		-1.776**** (0.176)	-0.751****(0.164)	-0.559***(0.152)
zerofullbath80		$1.243^{***}$ (0.139)	$1.044^{***} (0.124)$	$0.863^{***} (0.116)$
bedrms1_80occ		$0.421^* (0.249)$	0.404*(0.237)	$0.240 \ (0.234)$
bedrms2_80occ		-0.436*(0.229)	$0.156 \ (0.216)$	-0.004 (0.214)
bedrms3_80occ		-0.524**(0.230)	-0.147 (0.217)	-0.153(0.214)
bedrms4_80occ		-0.111(0.226)	$0.004 \ (0.217)$	-0.213 (0.214)
bedrms5_80occ		0.721***(0.231)	$0.732^{***}$ (0.222)	$0.430^* (0.220)$
blt0_1yrs80occ		-0.216**** (0.045)	-0.010 (0.044)	0.109**(0.045)
blt2_5yrs80occ		-0.295****(0.029)	$0.011 \ (0.028)$	0.039(0.026)
blt6_10yrs80occ		$-0.271^{***}$ (0.021)	-0.048**(0.021)	0.002(0.021)
blt10_20yrs80occ		$-0.242^{***} (0.017)$	-0.136***(0.015)	-0.123****(0.014)
blt20_30yrs80occ		-0.191***(0.017)	-0.181****(0.014)	-0.156***(0.013)
blt30_40yrs80occ		-0.190***(0.026)	-0.121****(0.025)	-0.104***(0.023)
occupied80		0.730*** (0.050)	0.242*** (0.046)	-0.093**(0.044)
pop_den8		, ,	0.00001*** (0.00000)	0.00001*** (0.00000)
shrblk8			-0.161***(0.014)	-0.058***(0.013)
shrhsp8			-0.329***(0.021)	-0.100***(0.022)
child8			-0.630****(0.058)	$-0.431^{***}$ (0.052)
old8			-0.737***(0.047)	-0.447***(0.044)
shrfor8			1.377*** (0.048)	$0.567^{***} (0.041)$
ffh8			-0.006 (0.034)	-0.084***(0.032)
smhse8			0.407****(0.022)	0.323*** (0.022)
hsdrop8			$0.010 \; (0.025)$	0.042*(0.024)
no_hs_diploma8			$-0.537^{***} (0.039)$	$-0.262^{***}$ (0.034)
ba_or_better8			0.112*** (0.034)	0.450*** (0.035)
unemprt8			-0.654***(0.071)	-1.420****(0.076)
povrat8			-0.275****(0.051)	0.118** (0.048)
welfare8			1.271*** (0.070)	0.284*** (0.067)
avhhin8			0.00001*** (0.00000)	0.00001*** (0.00000)
as.factor(statefips)2				-0.129***(0.027)
as.factor(statefips)4				0.011 (0.015)
as.factor(statefips)5				$-0.150^{***} (0.025)$
as.factor(statefips)6				0.340***(0.017)
as.factor(statefips)8				0.207***(0.015)
as.factor(statefips)9				0.157***(0.015)
as.factor(statefips)10				$0.230^{***}(0.018)$
as.factor(statefips)11				0.102***(0.024)
as.factor(statefips)12				$-0.005\ (0.013)$
as.factor(statefips)13				0.182*** (0.015)
as.factor(statefips)15				0.081** (0.038)
				0.001 (0.000)

Notes:

<sup>\*\*\*</sup>Significant at the 1 percent level.

\*\*Significant at the 5 percent level.

\*Significant at the 10 percent level.

Table 2: Contingency table for a range of factors by nbr

	N	0	1
		N = 42540	N = 5705
npl1990:0	48245	99% (42137)	94% (5362)
1		1% (403)	6% ( 343)
npl2000:0	48245	99% (41989)	92% (5271)
1		1% ( 551)	8% ( 434)
pop_den8	48245	674.4158 2887.1943 6473.8845	194.1788 961.2832 3344.8530
shrblk8	48245	$0.002638 \ 0.015964 \ 0.082081$	$0.001940 \ 0.011711 \ 0.058053$
shrhsp8	48245	$0.0064900 \ 0.0185855 \ 0.0634445$	$0.0049900 \ 0.0131040 \ 0.0369590$
child8	48245	$0.2328310 \ 0.2846455 \ 0.3289673$	$0.2587950 \ 0.2974520 \ 0.3323570$
shrfor8	48245	$0.01912050 \ 0.04256600 \ 0.08668875$	$0.01689000 \ 0.03570600 \ 0.06528300$
ffh8	48245	$0.09759375 \ 0.15094300 \ 0.24082675$	$0.08582000 \ 0.12909600 \ 0.19591101$
smhse8	48245	$0.4122337 \ 0.5306680 \ 0.6283828$	$0.4513610 \ 0.5558160 \ 0.6362780$
hsdrop8	48245	$0.054545 \ 0.111739 \ 0.192307$	$0.056338 \ 0.107438 \ 0.182572$
no_hs_diploma8	48245	$0.1816847 \ 0.2916233 \ 0.4290175$	$0.2093909 \ 0.3010590 \ 0.4139572$
ba_or_better8	48245	$0.07740766 \ 0.13831653 \ 0.24082869$	$0.07717157 \ 0.12516019 \ 0.20234250$
unemprt8	48245	$0.03652375 \ 0.05492750 \ 0.08234525$	$0.04026800 \ 0.05844100 \ 0.08421600$
povrat8	48245	$0.0452915 \ 0.0800220 \ 0.1442960$	$0.0455540 \ 0.0744300 \ 0.1235710$
welfare8	48245	$0.0286895 \ 0.0510035 \ 0.0952380$	$0.0317910 \ 0.0513860 \ 0.0844040$
favinc8	48245	18678.15 $22858.37$ 27771.77	19537.96 22877.64 26884.79
avhhin8	48245	$16223.85\ 20316.22\ 25271.48$	$17278.15\ 20688.77\ 24637.19$
meanrnt80	48115	222.7207 268.2003 324.8214	224.3905 264.1910 313.5771
mdvalhs9	48245	43600 69000 125600	47300 72200 126112
meanrnt9	48190	389.6826 491.0426 635.9742	387.5005 487.7268 628.6454
mdvalhs0	48245	81900 120300 179700	87000 123100 167700
meanrnt0	48127	520.2832 645.7830 823.5361	520.2703 638.1877 800.3922
tothsun8	48245	873 1280 1739	891 1278 1718
ownocc8	48245	438 740 1080	544 831 1156
owner_occupied80	48245	$0.4729324 \ 0.6618154 \ 0.7839525$	$0.5725154 \ 0.7147436 \ 0.8039216$
bltlast5yrs80	48245	$0.01945995 \ 0.08701160 \ 0.22249195$	$0.04517272 \ 0.11816839 \ 0.22092116$
bltlast10yrs80	48245	$0.06065490 \ 0.21716790 \ 0.45006267$	$0.12627292 \ 0.26502535 \ 0.42857143$
firestoveheat80	48245	$0.002498829 \ 0.011919458 \ 0.042651323$	$0.005777961 \ 0.021126760 \ 0.060995184$
noaircond80	48245	$0.1612903 \ 0.3921197 \ 0.6600715$	$0.2464638 \ 0.4505289 \ 0.6935139$
nofullkitchen80	48245	$0.004088785 \ 0.009900990 \ 0.020574207$	$0.004839685 \ 0.010771993 \ 0.020997375$
zerofullbath80	48245	$0.004034873 \ 0.011940299 \ 0.028044170$	$0.005586592 \ 0.013818182 \ 0.029411765$
northeast:0	48245	79% (33483)	66% (3779)
1		3  21%  (9057)	34% (1926)
midwest: 0	48245	77% (32659)	78% (4449)
1		23% (9881)	22% (1256)
south: 0	48245	68% (28851)	76% (4327)
1		32% (13689)	24% (1378)
west:0	48245	77% (32627)	80% (4560)
1		23% (0012)	20% (1145)

23% (9913)

20% (1145)

- 1.2 Part B: Comparing covariates
- 2 Problem 2: RDD setup
- 3 Problem 3: RDD First Stage
- 4 Problem 4: RDD Second Stage
- 5 Problem 5: Synthesis
- 6 Appendix: Code Listings

```
# Econometrics helper functions for [R]
2 #
3 # Peter Alstone and Frank Proulx
 4 # 2013
5 # version 1
6 \, | \, # contact: peter.alstone AT gmail.com
  # Category: Data Management -----
10
11 # Category: Data Analysis -----
13| # Function: Find adjusted R^2 for subset of data
|14| # This requires a completed linear model...pull out the relevant y-values
       and residuals and feed them to function
15 | \,# [TODO @Peter] Improve function so it can simply evaluate lm or glm object,
       add error handling, general clean up.
16 adjr2 <- function(y,resid){
    r2 <- 1-sum(resid^2) / sum((y-mean(y))^2)
18
    return(r2)
19
  } #end adjr2
20
21
|\widetilde{22}| # Category: Plots and Graphics ------
24 | ## Function for arranging ggplots. use png(); arrange(p1, p2, ncol=1); dev.
       off() to save.
25| require(grid)
26| vp.layout <- function(x, y) viewport(layout.pos.row=x, layout.pos.col=y)
  arrange_ggplot2 <- function(..., nrow=NULL, ncol=NULL, as.table=FALSE) {</pre>
    dots <- list(...)
     n <- length(dots)</pre>
    if(is.null(nrow) & is.null(ncol)) { nrow = floor(n/2) ; ncol = ceiling(n/
     if(is.null(nrow)) { nrow = ceiling(n/ncol)}
     if(is.null(ncol)) { ncol = ceiling(n/nrow)}
    ## NOTE see n2mfrow in grDevices for possible alternative
```

```
grid.newpage()
35
     pushViewport(viewport(layout=grid.layout(nrow,ncol)))
36
     ii.p <- 1
37
     for(ii.row in seq(1, nrow)){
38
       ii.table.row <- ii.row</pre>
39
       if(as.table) {ii.table.row <- nrow - ii.table.row + 1}</pre>
40
       for(ii.col in seq(1, ncol)){
41
         ii.table <- ii.p
42
         if(ii.p > n) break
43
         print(dots[[ii.table]], vp=vp.layout(ii.table.row, ii.col))
44
         ii.p <- ii.p + 1
45
       }
46
    }
47
   }
48
   robust <- function(model){  #This calculates the Huber-White Robust standard
       errors -- code from http://thetarzan.wordpress.com/2011/05/28/
       heteroskedasticity-robust-and-clustered-standard-errors-in-r/
50
       s <- summary(model)
51
       X <- model.matrix(model)</pre>
52
       u2 <- residuals(model)^2
53
       XDX <- 0
54
5\overline{5}
       for(i in 1:nrow(X)) {
56
           XDX <- XDX +u2[i]*X[i,]%*%t(X[i,])</pre>
57
58
59
   # inverse(X'X)
60
       XX1 <- solve(t(X)%*%X)
61
62
   #Compute variance/covariance matrix
63
       varcovar <- XX1 %*% XDX %*% XX1
64
65
   # Degrees of freedom adjustment
66
       dfc <- sqrt(nrow(X))/sqrt(nrow(X)-ncol(X))</pre>
67
68
       stdh <- dfc*sqrt(diag(varcovar))</pre>
69
70
       t <- model$coefficients/stdh
71
       p <- 2*pnorm(-abs(t))</pre>
72
73
74
75
       results <- cbind(model$coefficients, stdh, t, p)</pre>
       dimnames(results) <- dimnames(s$coefficients)</pre>
       results
76
   ## Two functions for clustered standard errors below from: http://people.su.
       se/~ma/clustering.pdf -----
78
79
   clx <-
80
     function(fm, dfcw, cluster){
81
       # R-codes (www.r-project.org) for computing
82
       # clustered-standard errors. Mahmood Arai, Jan 26, 2008.
83
84
       # The arguments of the function are:
85
       # fitted model, cluster1 and cluster2
86
       # You need to install libraries 'sandwich' and 'lmtest'
87
```

```
# reweighting the var-cov matrix for the within model
 89
        library(sandwich); library(lmtest)
 90
        M <- length(unique(cluster))</pre>
 91
        N <- length(cluster)
        K <- fm$rank
 92
 93
        dfc \leftarrow (M/(M-1))*((N-1)/(N-K))
 94
        uj <- apply(estfun(fm),2, function(x) tapply(x, cluster, sum));
 95
        vcovCL \leftarrow dfc*sandwich(fm, meat=crossprod(uj)/N)*dfcw
 96
        coeftest(fm, vcovCL) }
 97
 98
    mclx <-
 99
      function(fm, dfcw, cluster1, cluster2){
100
        # R-codes (www.r-project.org) for computing multi-way
101
        # clustered-standard errors. Mahmood Arai, Jan 26, 2008.
102
        # See: Thompson (2006), Cameron, Gelbach and Miller (2006)
103
        # and Petersen (2006).
104
        # reweighting the var-cov matrix for the within model
105
106
        # The arguments of the function are:
107
        # fitted model, cluster1 and cluster2
108
        # You need to install libraries 'sandwich' and 'lmtest'
109
110
        library(sandwich); library(lmtest)
111
        cluster12 = paste(cluster1,cluster2, sep="")
112
        M1 <- length(unique(cluster1))</pre>
113
        M2 <- length(unique(cluster2))</pre>
114
        M12 <- length(unique(cluster12))</pre>
115
            <- length(cluster1)
        N
            <- fm$rank
116
        K
117
        dfc1 <- (M1/(M1-1))*((N-1)/(N-K))
118
        dfc2 <- (M2/(M2-1))*((N-1)/(N-K))
119
        dfc12 \leftarrow (M12/(M12-1))*((N-1)/(N-K))
               <- apply(estfun(fm), 2, function(x) tapply(x, cluster1,
<- apply(estfun(fm), 2, function(x) tapply(x, cluster2,</pre>
120
        u1j
121
        u2j
122
        u12j <- apply(estfun(fm), 2, function(x) tapply(x, cluster12, sum))
123
        vc1
               <- dfc1*sandwich(fm, meat=crossprod(u1j)/N )
124
               <- dfc2*sandwich(fm, meat=crossprod(u2j)/N )
        vc2
125
        vc12 <- dfc12*sandwich(fm, meat=crossprod(u12j)/N)
126
        vcovMCL \leftarrow (vc1 + vc2 - vc12)*dfcw
127
        coeftest(fm, vcovMCL)}
128
129| ## Function to compute ols standard errors , robust, clustered...
130 | ## Based on http://diffuseprior.wordpress.com/2012/06/15/standard-robust-and
        -clustered-standard-errors-computed-in-r/
131 ols.hetero <- function(form, data, robust=FALSE, cluster=NULL, digits=3){
132
      r1 <- lm(form, data)
133
      if(length(cluster)!=0){
134
        data <- na.omit(data[,c(colnames(r1$model),cluster)])</pre>
135
        r1 <- lm(form, data)
136
137
      X <- model.matrix(r1)</pre>
138
      n \leftarrow dim(X)[1]
      k <- dim(X)[2]
139
      if(robust==FALSE & length(cluster)==0){
141
        se <- sqrt(diag(solve(crossprod(X)) * as.numeric(crossprod(resid(r1))/(n
            -k))))
142
        res <- cbind(coef(r1),se)
```

```
143
      }
144
      if(robust == TRUE) {
145
        u <- matrix(resid(r1))
146
        meat1 <- t(X) %*% diag(diag(crossprod(t(u)))) %*% X</pre>
        dfc <- n/(n-k)
147
148
        se <- sqrt(dfc*diag(solve(crossprod(X)) %*% meat1 %*% solve(crossprod(X)
            )))
        res <- cbind(coef(r1),se)
149
150
151
      if(length(cluster)!=0){
152
        clus <- cbind(X,data[,cluster],resid(r1))</pre>
153
        colnames(clus)[(dim(clus)[2]-1):dim(clus)[2]] <- c(cluster, "resid")</pre>
154
        m <- dim(table(clus[,cluster]))</pre>
155
        dfc <- (m/(m-1))*((n-1)/(n-k))
156
         uclust <- apply(resid(r1)*X,2, function(x) tapply(x, clus[,cluster],\\
            sum))
157
        se <- sqrt(diag(solve(crossprod(X)) %*% (t(uclust) %*% uclust) %*% solve
            (crossprod(X)))*dfc)
158
        res <- cbind(coef(r1),se)
159
160
      res <- cbind(res,res[,1]/res[,2],(1-pnorm(abs(res[,1]/res[,2])))*2)
161
      res1 <- matrix(as.numeric(sprintf(paste("%.",paste(digits,"f",sep=""),sep=</pre>
          ""),res)),nrow=dim(res)[1])
162
      rownames(res1) <- rownames(res)</pre>
163
      colnames(res1) <- c("Estimate","Std. Error","t value","Pr(>|t|)")
164
      return(res1)
165|}
```

../util/are213-func.R