ARE213 Problem Set #1B

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1 Problem #1

1.1 Part A

Under the assumption of random assignment conditional on the observables, what are the sources of misspecification bias in the estimates generated by the linear model estimated in Problem Set 1a?

Wrong functional form. In Problem Set 1A we used linear (i.e., $y = \beta x + \epsilon$) estimators to make "corrections" while the true functional form of the relationships between the covariates we included in the modern were certainly not linear. By imposing a linear function on a non-linear data generating process (described by the CEF), we introduce misspecification bias in the model.

Omitted Variables Bias. We were able to use variables included in the dataset in our linear model, but not the unobserved variables that may be important for control. If omitted variables exist that both determine outcomes related to birth weight and are correlated with smoking status we will over- or under-estimate the effect (depending on the characteristics of the omission).

1.2 Part B

Now, consider a series estimator. Estimate the smoking effects using a flexible functional form for the control variables (e.g., higher order terms and interactions). What are the benefits and drawbacks to this approach?

2 Problem #2

2.1 Part A

To calculate the propensity score, we estimated a logit model of mother's tobacco use (0=non-smoker, 1=smoker) as determined by the predetermined covariates shown in Table ??. Model #1 shows the full model using all of the covariates suspected to be predetermined. Model #2 is a reduced form of the same model, preserving just those covariates that were significant at the 1% level in Model #1.

To test whether the propensity scores predicted by these two models are significantly different we perform a likelihood ratio test between the full and reduced model. This test yields the following output:

NOTE from class: including insignificant terms can be beneficial in terms of getting better fit (by reducing

2.2 Part B

This estimation assumes unconfoundedness. and conditional independence

2.3 Part C

We used R to complete this assignment. The code is below:

Table 1: Propensity scores calculated for mother's smoking status

	Mother Tobacco-Use Status	
	(1)	(2)
Mother's Race not White or Black	-1.956***	-1.954***
	(0.134)	(0.133)
Mother's Years of Education	-0.817***	-0.818***
	(0.028)	(0.028)
Marital status	-0.205***	-0.204***
	(0.005)	(0.005)
Father's age	-1.256***	-1.251***
	(0.022)	(0.021)
Father's Years of Education	0.029***	0.030***
	(0.002)	(0.001)
Father Mexican	-0.131***	-0.131***
	(0.005)	(0.005)
Father Puerto Rican	-1.961***	-1.957***
	(0.173)	(0.173)
Father Cuban	-1.267^{***}	-1.268***
	(0.058)	(0.058)
Father Central or South American	-0.567	-0.567
	(0.364)	(0.364)
Father Race Other or Unknown Hispanic	-1.933***	-1.932***
	(0.205)	(0.205)
Plurality of Infant	-0.890***	-0.889***
	(0.120)	(0.120)
Sex of Infant	-0.148***	
	(0.054)	
Mother's age	-0.019	
	(0.017)	
dmage	0.003	
	(0.002)	
Constant	2.873***	2.707***
	(0.088)	(0.064)
N	114,610	114,610
Log Likelihood	-44,310.690	-44,315.790
Akaike Inf. Crit.	88,651.370	88,655.580

Notes: ***Significant at the 1 percent level.

```
18 library(plyr) # for nice data tools like ddply
19 library(epicalc) # For likelihood ratio test
20| library(car) # "companion for applied regression" - recode fxn, etc.
   library(gmodels) #for Crosstabs
  library(splines) # for series regression
24
   # Homebrewed functions
25
  source("../util/are213-func.R")
26
   source("../util/watercolor.R") # for watercolor plots
28
29
  ps1.data <- read.dta(file="ps1.dta")</pre>
30
31
  # Data Cleaning Step
   full.record.flag <- which(ps1.data$cardiac != 9 &</pre>
33
                                ps1.data$cardiac != 8 &
34
                                ps1.data$lung != 9 &
35
                                ps1.data$lung != 8 &
36
                                ps1.data$diabetes !=9 &
37
                                ps1.data$diabetes !=8 &
38
                                ps1.data$herpes != 9 &
39
                                ps1.data$herpes != 8 &
40
                                ps1.data$chyper != 9 &
41
                                ps1.data$chyper != 8 &
42
                                ps1.dataphyper != 9 \&
43
                                ps1.data$phyper != 8 &
44
                                ps1.data$pre4000 !=9 &
45
                                ps1.data$pre4000 !=8 &
46
                                ps1.data$preterm != 9 &
47
                                ps1.data$preterm != 8 &
48
                                ps1.data$tobacco != 9 &
49
                                ps1.data$cigar != 99 &
50
                                ps1.data$cigar6 !=6 &
51
                                ps1.data$alcohol != 9 &
52
                                ps1.data$drink != 99 &
53
                                ps1.data$drink5 !=5 &
54
                                ps1.data$wgain !=99
55
56
  ps1.data$full.record <- FALSE # initialize column as F
58|\,\mathrm{ps1.data\$full.record[full.record.flag]} <- TRUE #reassign level to T for full
59
60|\,\mathrm{ps1.data.clean} <- subset (ps1.data, full.record == TRUE)
  ps1.data.missingvalues <- subset(ps1.data, full.record == FALSE)
63 # Problem 1a is only in ps1b.tex
64 # Problem 1b
65 # This is using a series estimator. I think smooth.spline() is the right
       function to use, but let me know if you think we should be doing kernel
       regression instead. I'm also not sure how to go about adding interaction
        terms
66
67
68
  sm.flex <- with(ps1.data.clean, smooth.spline(cigar, y=dbrwt, nknots=10,
       spar = 0.7, tol = 0.0001)) # Fits a smooth line to the data
```

```
70| sm.flex.df <- data.frame(sm.flexx, sm.flexy) #converts the fitted values
        into a data frame for ggplot
 71
    splineplot <- ggplot(sm.flex.df, aes(x = sm.flex.x, y=sm.flex.y))
splineplot <- splineplot +</pre>
 72
 73
      geom_point(data=ps1.data.clean, aes(x = cigar, y = dbrwt), pch = 1) +
 75
      geom_line(color='red') +
 76
      labs(x = 'Cigarettes smoked per day by mother', y= 'Birthweight')
 77
    splineplot
 78
 79
    ggsave(filename = 'img/splineplot.pdf')
 80
 81
 82| # Problem 2a
 83
    ps1.data.clean$tobacco.rescale <- with(ps1.data.clean, recode(tobacco, "
        2='0'", as.numeric.result=TRUE)) #rescales the tobacco use variable to
        be 0/1, where 0=no and 1 = yes
    ps1.data.clean$dmar.rescale <- with(ps1.data.clean, recode(dmar, "2='0',"))
 85
 86
    smoke.propensity.all <- glm(tobacco.rescale ~ as.factor(mrace3) + dmeduc +</pre>
        dmar.rescale + dfage + dfeduc + as.factor(orfath) + dplural + csex +
        dmage, data=ps1.data.clean, family = binomial()) ## Did I miss any
        predetermined covariates here?
 87
    smoke.propensity.reduced <- glm(tobacco.rescale ~ as.factor(mrace3) + dmeduc</pre>
         + dmar.rescale + dfage + dfeduc + as.factor(orfath), data=ps1.data.
        clean, family = binomial())
 89
 90
    \verb|stargazer(smoke.propensity.all|, \verb|smoke.propensity.reduced|, \\
 91
 92
                type = "latex",
 93
                covariate.labels = c("Mother's Race not White or Black", "Mother'
                    s Years of Education", "Marital status", "Father's age", "
                    Father's Years of Education", "Father Mexican", "Father
                    Puerto Rican", "Father Cuban", "Father Central or South
                    American", "Father Race Other or Unknown Hispanic", "
                    Plurality of Infant", "Sex of Infant", "Mother's age"),
 94
                style ="qje",
                align = TRUE,
 95
               font.size = "scriptsize",
 96
 97
               label = "tab:propensities",
              title = "Propensity scores calculated for mother's smoking status
 98
 99| logit model specification",
100|
               dep.var.labels = "Mother Tobacco-Use Status",
101
                out = "propensityscores.tex"
102
103
104| ps1.data.clean$propensityfull <- predict(smoke.propensity.all, type = "
        response")
105| ps1.data.clean$propensityreduced <- predict(smoke.propensity.reduced, type =
         "response")
107 sink(file = "lrtest.tex", append = FALSE)
108 \, | \, 	ext{lrtest(smoke.propensity.all, smoke.propensity.reduced)} \, \, 	ext{\#Test whether the two}
         scores are statistically different
109|\sin k()
```

```
1101
111 Problem 2b - Estimating a regression model using propensity scores
112
113 sm.propensityregression <- lm(dbrwt ~ tobacco.rescale + (propensityreduced *
                  tobacco.rescale) + propensityreduced, ps1.data.clean)
115 | #calculation of average treatment effect:
|116| coefficients (sm. propensity regression) [2] + coefficients (sm.
               propensityregression) [4] *mean(ps1.data.clean$propensityreduced)
117
118
\left|119\right| stargazer(sm.propensityregression,
120
                             type = "latex",
121
                              covariate.labels = c("Delta1", "Beta", "Delta2", "Constant"),
122
                              style ="qje",
123
                              align = TRUE,
124
                             font.size="footnotesize",
125
                            label = "tab:propensitymodel",
126
                            title = "Model of effects of tobacco use on birthweight using
                                  propensity score as a control",
127
                              dep.var.labels = "Mother Tobacco-Use Status",
128
                              out = "propensityscoremodel.tex"
129
130
131 #Problem 2c - Using reweighting with propensity scores
132
133 | \texttt{term1} \leftarrow \texttt{with(ps1.data.clean, sum((tobacco.rescale*dbrwt)/propensityreduced)} \\
               /sum(tobacco.rescale/propensityreduced))
134
       term2 <- with(ps1.data.clean, sum(((1-tobacco.rescale)*dbrwt)/(1-</pre>
               propensityreduced))/sum((1-tobacco.rescale)/(1-propensityreduced)))
135
136
       weightingestimator <- term1-term2 #This should be the average treatment
137
138
        term1.T <- with(subset(ps1.data.clean, tobacco.rescale=1), sum((tobacco.</pre>
                rescale*dbrwt)/propensityreduced)/sum(tobacco.rescale/propensityreduced)
139 | #term2.T <- with(subset(ps1.data.clean, tobacco.rescale=1), sum(((1-tobacco.
               \tt rescale)*dbrwt)/(1-propensity reduced))/sum((1-tobacco.rescale)/(1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-tobacco.rescale))/sum((1-
                propensityreduced)))
140
141
        weightingestimator.T <- term1.T#-term2.T #This should be the average
                treatment on treated
142
143
144
|145| # Problem 2d - Kernel Density Estimator
146 tot.propensity.nosm <- with(subset(ps1.data.clean, tobacco.rescale == 0),
               sum(propensityreduced))
147 tot.propensity.sm <- with(subset(ps1.data.clean, tobacco.rescale == 1), sum(
              propensityreduced))
148|\,\mathrm{h} <- 35 # This is to play with the bandwidth
149
150 kerndensity.nosm <- with(subset(ps1.data.clean, tobacco.rescale == 0),
                density(dbrwt, #if nobody smoked
151
                       kernel = "epanechnikov",
152
                        bw = h,
```

```
weights = propensityreduced/tot.propensity.nosm))
154
    kerndensity.nosm.df <- data.frame(kerndensity.nosm[1], kerndensity.nosm[2])
155
156
    kerndensity.sm <- with(subset(ps1.data.clean, tobacco.rescale == 1), density
        (dbrwt, #if everybody smoked
157
            kernel = "epanechnikov",
158
            bw = h,
159
            weights = propensityreduced/tot.propensity.sm))
160| kerndensity.sm.df <- data.frame(kerndensity.sm[1], kerndensity.sm[2])
161
|162| kerndensity.plot <- ggplot(kerndensity.nosm.df, aes(x, y))
163| kerndensity.plot <- kerndensity.plot +
      geom_line(linetype = 'dotted') +
164
165
      geom_line(data = kerndensity.sm.df, aes(x, y)) +
166
      labs(title = paste("Density of birthweights estimated using \n propensity
          score-weighted kernel regression \n Bandwidth=", as.factor(h)), x = "
          Birthweight (grams)", y = "Density") +
167
      guides(linetype = "Legend") # Having trouble getting a legend.
168
169| kerndensity.plot
170
171| ggsave(file = 'img/kerndensity.pdf', plot = kerndensity.plot)
172
173 #2d - calculating kernel value by 'hand' at dbrwt = 3000
174 # y_pred = sum_onj(K(pi-pj/h)*yj)/sum_onj(K(pi-pj/h))
175
176| #h <- 30
177 | #kernel.epa <- function(u){
178 | #return(if (abs(u) < 1){0.75*(1-u*u))}
179 | #}
180 \, | \, #propensity3000 <- # I'm not sure how we get the estimated propensity score
        at dbrwt = 3000
181
182
183 #Problem 2e
184 \, | \, \text{\#\#} This is in progress
185 | \, \text{\#kerndensity.plot.bws} < - \, \text{ggplot()}
186 | #for(h in seq(from = 15, to = 40, by = 5)) {
187 | #paste0('kerndensity.sm.', h) <- with(subset(ps1.data.clean, tobacco.rescale
         == 1), density(dbrwt, #if everybody smoked
188 #
             kernel = "epanechnikov",
189 #
             bw = h,
190 #
             weights = propensityreduced/tot.propensity.sm))
191| #paste0('kerndensity.sm.df.', h) <- data.frame(paste0('kerndensity.sm.', h
        ,'[1]'), paste0('kerndensity.sm.', h, '[2]'))
192| #kerndensity.plot.bws <- kerndensity.plot.bws +
193 # geom_line(data = paste0('kerndensity.sm.df.', h), aes(x, y)) +
194 | # labs(title = "Density of birthweights estimated using \n propensity score
        -weighted kernel regression", x = "Birthweight (grams)", y = "Density")
195 | #}
196
197|\, {\tt \#kerndensity.plot.bws}
```

ps1b.R

```
1 \ \# Econometrics helper functions for [R] 2 \ \#
```