

Ex 4 Session 0

First focus on the first part of the exercise, i.e. we have to construct a 10×10 tri-diagonal matrix B like this:

$$B = \begin{bmatrix} 5 & 3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 5 & 3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 5 & 3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 5 & 3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 5 & 3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 5 & 3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 & 5 & 3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -1 & 5 & 3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 5 & 3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 5 \end{bmatrix}$$

We can think to this matrix as the sum of 3 different matrices

$$D = \begin{bmatrix} 5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 5 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 5 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 5 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 5 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 5 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 5 \end{bmatrix}$$

→ How to construct this? Let's use **diag**

① I need this vector $[5, 5, \dots, 5] \rightarrow 5 * \text{ones}(10, 1)$
10 times

② **diag** of a vector is a matrix with this vector on the main diagonal → $D = \text{diag}(5 * \text{ones}(10, 1))$

$$C'S = \begin{bmatrix} 0 & 3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 3 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Like before this time I need of this vector:

$[3, 3, \dots, 3] \rightarrow 3 * \text{ones}(9, 1)$

3 times (think about the reason)

⇒ $C'S = \text{diag}(3 * \text{ones}(9, 1), 1)$

↑
because I want to put this vector in the first super-diagonal

$$C'L = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 \end{bmatrix}$$

Again $[-1, -1, \dots, -1] \rightarrow -1 * \text{ones}(9, 1)$

3 times

⇒ $C'L = \text{diag}(-1 * \text{ones}(9, 1), -1)$

↑
first sub-diagonal

$$\Rightarrow B = D + C'S + C'L$$

At the end the exercise asks to set the elements of the intersection between column 6, 9 and rows 5 and 8 equal to 2

→ use the indices: $B([5, 8], [6, 9]) = 2$