## Exercise session 0

## Topics: matrices and vectors manipulation, plots of functions and Matlab programming language

- 1. Define the vector x=[1:-0.1:0]. Type the following MATLAB instructions, understanding their meaning:
  - a) x([1 4 3]);
  - b) x([1:2:7 10])=zeros(1,5);
  - c)  $x([1 \ 2 \ 5])=[0.5*ones(1,2) \ -0.3];$
  - d) y=x(end:-1:1).
- 2. Define the matrix:

$$\mathbf{A} = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{pmatrix}$$

and type the following MATLAB instructions, understanding their meaning:

- a) size(A);
- b) A(1:2,4), A(:,3), A(1:2,:), A(:,[2,4]), A([2 3 3],:);
- c) A(3,2)=A(1,1);
- d) A(1:2,4)=zeros(2,1);
- e) A(2,:)=A(2,:)-A(2,1)/A(1,1)\*A(1,:).;
- 3. Define the matrix:

$$\mathbf{A} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 5 & 6 & 7 & 8 & 9 & 10 \\ 9 & 10 & 11 & 12 & 13 & 14 \\ 15 & 16 & 17 & 18 & 19 & 20 \end{pmatrix}$$

After that:

- a) assemble the matrix **B** made by the columns of **A** in reverse order (that is to say the first column of **B** is the  $6^{\text{th}}$  of **A**, the  $2^{\text{nd}}$  of **B** is the  $5^{\text{th}}$  of **A**, ...).
- b) assemble the matrix made by the even columns of A;
- c) assemble the matrix made by the odd rows of A;
- d) assemble the matrix made by rows 1,4,3 and columns 5,2 of A;
- e) assemble the vector made by the diagonal elements  $a_{kk}$ , k = 1, ..., 4 of **A**;
- 4. Use the MATLAB command diag to define a  $10 \times 10$ -tridiagonal matrix  $\mathbf{B}$  in which the main diagonal elements are all equal to 5 while the sub-diagonal elements are equal to -1 and the super-diagonal elements are equal to 3. Set the elements of the intersection between column 6 and 9 and rows 5 and 8 equal to 2.
- 5. Use the Matlab command plot to graphically represent the following mathematical functions:

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$$f(x) = \sin(x)$$
  $x \in [-\pi, \pi];$   
 $f(x) = e^x$   $x \in [-1, 1];$ 

$$f(x) = e^{-x^2} \qquad x \in [-\pi, \pi];$$

$$f(x) = \frac{\sin(x)}{x} \qquad x \in (0, 4\pi];$$
  
$$f(x) = x \sin(\frac{1}{x}) \qquad x \in (0, 2];$$

6. Graphically represent the mathematical function:

$$f(x) = \sqrt{\frac{100(1 - 0.01x^2)^2 + 0.02x^2}{(1 - x^2)^2 + 0.1x^2}} \quad x \in [0.1, \ 100],$$

using the MATLAB commands plot and loglog. Evaluate the function at sufficiently large number of points in the range of interest. Comment the results.

7. Write a MATLAB function which evaluates the mathematical function:

$$f(x) = \begin{cases} -2x, & x < 0, \\ 0, & x = 0, \\ 2x, & x > 0, \end{cases}$$

both at a generic point x and at each point of a vector. After that, graphically represent the function f in the interval [-1,1].

8. Write a MATLAB function in order to approximate the value of the function  $f(x) = e^x$  in a neighborhood of x = 0 by means of Taylor polynomial

$$e^x \approx 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!}$$

of degree n, 0-centered. Stop the summation when the term  $\frac{x^i}{i!}$  is less than a fixed tolerance tol. Run the function with x = 1, tol = 1.0e - 10 and compute the relative error linked to the value of the polynomial at x, using as exact value the one given by the Matlab function  $\exp(\mathbf{x})$ .