Interdependent Evolution of Non-Spectral Opinions and Social Networks

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BACKGROUND AND MOTIVATION

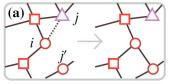
- ► Opinion Formation (e.g. voter models) is a common and very fundamental problem in the social sciences
- Goal: Modelling the coevolution of both opinions and the underlying social network
- Does our social network shape the opinion we hold or does our opinion determine who is part of our network?
- ► Preview: Analogies to statistical physics, e.g. *phase transitions* can be identified
- ► "Opinion" must be mutually exclusive and "non-spectral", e.g. brand preference, religious views...

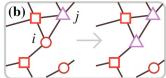
INITIAL SETUP

- ► Random graph with *N* nodes (opinion holder) and *M* edges (social connection)
- ▶ Random opinion g_i ∈ G assigned to node i
- Nodes exchange information (opinion) via undirected edges
- Externally set parameters:
 - ► *N* number of nodes
 - $\gamma = \frac{N}{G}$ average number of nodes per opinion
 - $k_{avg} = \frac{2M}{N}$ average degree
 - Φ reconnection probability

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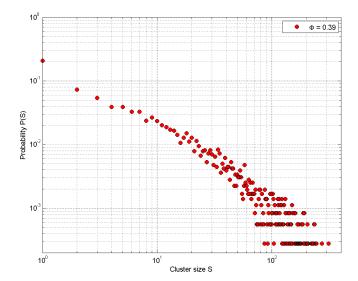
- 1. Pick a random node i with opinion g_i .
- 2. (a) With probability Φ select at random one of the nodes j that i is connected to.
 - ▶ If $g_i = g_i$, start over at step 1.
 - ▶ Otherwise, reconnect to a randomly chosen j' of same opinion, i.e. $g_{j'} = g_i$.
- 3. (**b**) Otherwise, with probability 1Φ randomly select one of the neighboring vertices j and change g_i to g_j .
- 4. Repeat until *consensus state* is achieved.





CLUSTER SIZE DISTRIBUTION

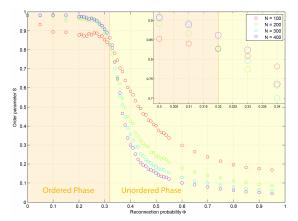
CONTINUOUS PHASE TRANSITION?



CLUSTER SIZE DISTRIBUTION

- ► Ordered phase
 - ▶ Low Φ , i.e. tendency to change opinion
 - ► Small clusters follow power law distribution
 - ► Existence of giant cluster
- ► Unordered phase
 - ▶ High Φ , i.e. tendency to keep opinion
 - ► Clusters follow Poisson-like distribution
 - No giant cluster!
- ► Phase transition
 - ▶ First guess: $\Phi_c = 0.39 \pm 0.05$
 - ► Power law behavior over the whole *s*-range
 - Order parameter $S = \frac{s_{max}}{N}$

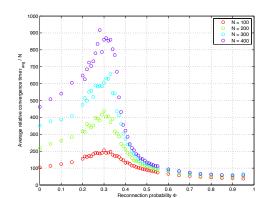
PHASE TRANSITION & CRITICAL POINT



- ► Really continuous phase transition
- ▶ Bigger N → more dramatic transition
- $\Phi_c = 0.32 \pm 0.02$ independent of system size *N*
- Weak agreement with $\Phi_c = 0.39 \pm 0.05$

CONVERGENCE TIME

- ▶ Iterations per node to reach consensus as function of Φ :
- ▶ "Divergence" at some Φ_c for different N
- ► Similar to divergent response functions in physics
- ► Supporting phase transition interpretation, but difficult to find direct analogy to τ_{avg}



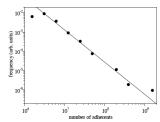


COMPARISONS TO EMPIRICAL DATA

- ▶ Idea: Compare distributions of some "opinion" in real world to the model \rightarrow identify and interpret corresponding Φ
- ► Religion:

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► Worldwide distribution of religions follows power law: Neither adaptation nor reconnection dominate in the formation?



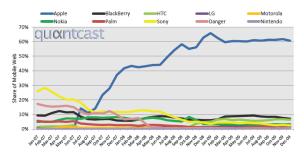
▶ Interpret Φ as an "intolerance indicator"?

COMPARISONS TO EMPIRICAL DATA

► Mobile Web Browsers:

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- ► An example for opinion = brand preference
- ► Contrast between giant cluster and "softer" distribution
- ▶ Note: Plot is not a cluster size histogram!



Interpret Φ as a "brand loyalty indicator"?





SUMMARY

- ▶ Interdependent evolution of opinions and networks, combining two mechanisms of adaption and reconnection determined by Φ
- ► Holme's and Newman's [5] work could be reproduced with more realistic assumptions
- ► Continuous phase transition
 - *N*-independent critical value $\Phi_c = 0.32 \pm 0.02$
 - ► Divergent consensus time at Φ_c

Outlook

- ▶ Variation of γ (diversity) and k_{avg} (density)
- Include analogue of "magnetic field" in model: "informed agents"?
- ► Make opinions *spectral*
- ► More detailed comparisons to empirical data





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