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# Multi-Agent Design: Optimizing Agents with Better Prompts and Topologies

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Large language models, employed as multiple agents that interact and collaborate with each other, have excelled at solving complex tasks. The agents are programmed with *prompts* that declare their functionality, along with the *topologies* that orchestrate interactions across agents. Designing prompts and topologies for multi-agent systems (MAS) is inherently complex. To automate the entire design process, we first conduct an in-depth analysis of the design space aiming to understand the factors behind building effective MAS. We reveal that prompts together with topologies play critical roles in enabling more effective MAS design. Based on the insights, we propose Multi-Agent System Search (MASS), a MAS optimization framework that efficiently exploits the complex MAS design space by interleaving its optimization stages, from local to global, from prompts to topologies, over three stages: 1) block-level (*local*) prompt optimization; 2) workflow topology optimization; 3) workflow-level (*global*) prompt optimization, where each stage is conditioned on the iteratively optimized prompts/topologies from former stages. We show that MASS-optimized multi-agent systems outperform a spectrum of existing alternatives by a substantial margin. Based on the MASS-found systems, we finally propose design principles behind building effective multi-agent systems.

## 1. Introduction

Large language models (LLMs) have showcased extraordinary capabilities in understanding, reasoning, and generating coherent responses based on user prompts, revolutionizing a wide range of applications (Kojima et al., 2022; Ouyang et al., 2022). LLM-based agents enhance usability by autonomously handling complex tasks across diverse domains, including code generation and debugging (Jimenez et al., 2023), retrieval-augmented generation (Singh et al., 2025; Wang et al., 2024a), data analysis (Guo et al., 2024; Hu et al., 2024b), and interactive decision-making (Li et al., 2025; Su et al., 2025). These agents are typically programmed with prompts that reinforce them to interact with the environment, utilizing available tools, and approach their objectives over multiple turns (Yao et al., 2023). Beyond individual agents, LLMs can be orchestrated within complex topologies that coordinate multiple agents toward a shared objective. This type of multi-agent system (MAS) typically outperforms its single-agent counterpart by involving more diverse agentic perspectives or role profiles, such as agents as verifiers (Shinn et al., 2024) and multi-agent debate (Qian et al., 2024; Wang et al., 2024b).

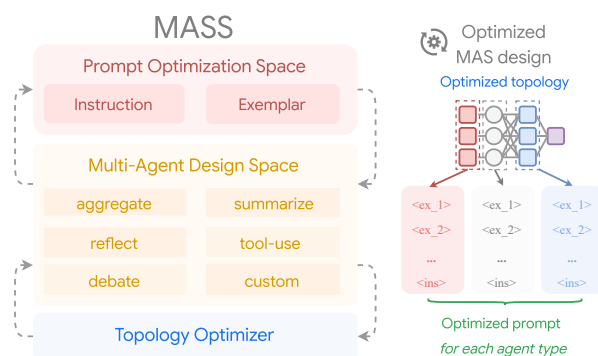


Figure 1 | Proposed Multi-Agent System Search (MASS) framework discovers effective multi-agent system designs (with both optimized *topology* and optimized *prompts*, right) via interleaved prompt optimization and topology optimization in a customizable multi-agent design space (key components illustrated on the left).

However, designing effective MAS for new domains often proves to be challenging. First, the single agent might suffer from prompt sensitivity (Verma et al., 2024), where simple modifications in the prompt can already exert significant but unexpected degradation of performance (Liu et al., 2024a; Zhou et al., 2024b). In MAS, when sensitive agents are cascaded, the compounding effect due to prompt sensitivity may be amplified. Together with the prompt design, crafting an effective topology might demand a substantial amount of manual experimentation, based on trial and error. The problem complexity is exacerbated by the overall combinatorial search space, over not only the unbounded space of prompt design but also the design decisions of what agent to integrate into the topology.

Although recent research has explored automating various aspects of agentic designs, there is still a gap in understanding of what matters most regarding improved MAS performance. For example, DSPy (Khatab et al., 2024) automates the process of designing exemplars for improved prompt programming. Li et al. (2024a) proposes to optimize MAS by scaling up the number of agents in majority voting. ADAS (Hu et al., 2024a) programs new topologies expressed in code via an LLM-based meta-agent. AFlow (Zhang et al., 2024b) searches better topologies using Monte Carlo Tree Search within a set of predefined operators. However, the interplay between multiple design spaces, including prompts and topologies, remains unclear.

In this paper, we first conduct in-depth analyses of common design spaces in MAS, examining the influence of various aspects such as optimizing the prompts, scaling the number of agents, and involving different types of topologies. Our analyses reveal that prompts frequently form an influential design component that yields strong-performing MAS, and influential topologies only represent a small fraction of the full search space. Based on these insights, we aim to distill the essence of influential MAS components into a pruned search space, thereby lowering the complexity of the overall search process. We propose Multi-Agent System Search (MASS), a novel multi-stage optimization framework that automates the optimization for MAS over an efficient search space. MASS integrates a plug-and-play prompt optimizer and workflow optimizer over a configurable topology space. It overcomes the complexity of joint optimization on MAS by interleaving the optimization stages, from local to global, from prompts to topologies, over three stages: 1) block-level (*local*) prompt ‘warm-up’ for each topology block; 2) workflow topology optimization in a *pruned* set of topology space; 3) workflow-level (*global*) prompt optimization given the best-found topology.

By optimizing over the identified influential components, MASS yields optimized MAS that achieves state-of-the-art performance, outperforming existing manually-crafted MAS baselines and automatically-generated alternatives, by a substantial margin, demonstrated across an extensive selection of tasks, including reasoning, multi-hop understanding, and code generation. Based on the strongest MAS found by MASS, we provide further insights and guidelines behind building effective MAS. Overall, our contributions can be summarized as follows: 1) we provide an in-depth analysis of the design factors that influence the performance of LLM-based MAS, highlighting the importance of prompts and identifying the influential topologies; 2) we propose MASS, a novel multi-stage optimizer that automates the MAS design by interleaving the optimization of prompts and topologies in an influential search space; 3) MASS shows significant performance improvement on various evaluation benchmarks, delivering guidelines for building effective multi-agent systems for the future.

## 2. Designing Multi-Agent Systems

In this section, we provide a formulation for designing MAS, followed by analyzing the influence of prompt and topology designs. We refer to the structural arrangements of agents (or equivalently, building blocks) as the topology of agents and define workflow  $\mathcal{W}$  as the logical sequence across

different topologies that builds the MAS. The design of a MAS can thus be broadly divided into two levels: block-level design and workflow-level orchestration. At the block level, we aim to design effective individual agents that best perform their intended role with better *prompt* design. On the other hand, at the workflow level, the optimization involves determining the *types* and *quantities* of agents to include and how to arrange them in the most effective way, referred to as the topology optimization. Formally, given a search space  $\mathcal{A}$  that defines all valid configurations  $a$  over the blocks (see Fig. 4), *workflow topology optimization* can be expressed as the following optimization problem with an objective function  $f(\cdot, \cdot)$  on a target input and output set  $(x, y) \sim \mathcal{D}$ :

$$\mathcal{W}^*(a) = \arg \max_{a \sim \mathcal{A}} \mathbb{E}_{(x,y) \sim \mathcal{D}} [f(\mathcal{W}(a(x)), y)]. \quad (1)$$

In the rest of this section, we provide an in-depth analysis of each component of MAS design.

### 2.1. Block-level: Prompt Design for Agents

At the block level, the primary “optimizable component” that significantly influences downstream performance is the *prompt*, which defines the role of the agent (e.g., “*You are an expert in reflecting on errors...*”), provides additional instructions to shape its behavior (e.g., “*You should think step by step...*”) and optionally, contains *few-shot demonstrations* (in-context examples) to guide the agent’s responses (Wan et al., 2024, 2025). For instance, a state-of-the-art prompt optimizer searches both instructions and few-shot demonstrations, where demonstrations are bootstrapped from the model’s own, correct predictions on the validation set based on a validation metric. Conditioned on the demonstrations, the prompt optimizer then proposes a few candidates for the instruction with a dataset summary or various hints to improve candidate diversity (Opsahl-Ong et al., 2024). The instructions and demonstrations are then jointly optimized.

Although it is well known that LLMs are sensitive to prompts (Verma et al., 2024; Zhou et al., 2024a), applying automatic prompt optimization (APO) techniques to MAS is rather non-trivial. Unlike single-turn tasks where APO can be easily performed by treating prompts as optimizable variables and performance over a validation set as the target. In MAS, APO becomes more complex due to the interdependence across agents (e.g., the output of one agent may be the input of another agent in a cascade with ground-truth responses for intermediate outputs not being available) and exponentially increasing complexity for combinatorial optimization with more number of agents  $n$  involved; The reward signals also become more sparse when  $n$  increases, preventing us from implementing APO directly on MAS in any manageable budget; as such, many prior works (Xia et al., 2024; Zhang et al., 2024f) in MAS still primarily use handcrafted prompts instead of including the prompts as optimizable components in the MAS design.

To systematically understand the influence of prompt design in MAS, we specifically and quantitatively analyze the effect of prompt optimization and compare its effectiveness to other operations common in MAS literature, such as scaling with more agents but with default prompts. We conduct

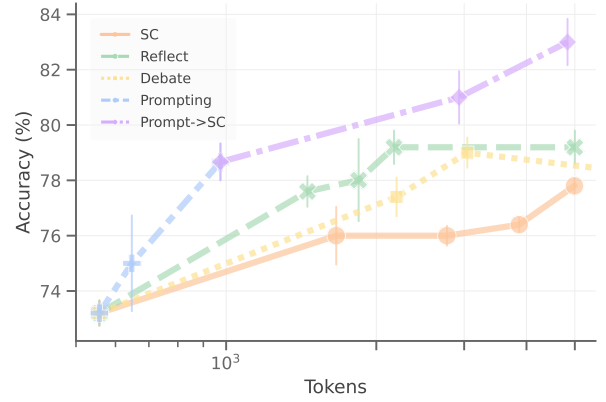


Figure 2 | Accuracy vs. the total token counts for prompt-optimized agents per question on MATH by Gemini 1.5 Pro compared to scaling agents with self-consistency (SC), self-refine (reflect), and multi-agent debate (debate) only. The error bar indicates 1 standard deviation. We show that by utilizing more compute, better accuracy can be obtained via more effective prompting.

APO on a chain-of-thought (Kojima et al., 2022) agent with both instruction optimization and 1-shot exemplar optimization via MIPRO (Opsahl-Ong et al., 2024), and fairly compare the total inference token cost with self-consistency (Kojima et al., 2022), self-refine (Madaan et al., 2024), and multi-agent debate (Du et al., 2024), where the specifications are provided in App. §B. In Fig. 2, prompting, which equips agents with more informative instructions and exemplars, demonstrates significant advantages in its token-effectiveness over other building blocks. Furthermore, by applying self-consistency on top of the prompt-optimized agent, we observe an improved scaling performance on the token cost, whereas standard approaches in scaling the number of agents (e.g. SC, or Reflect) saturate much earlier. This empirical observation sheds light on the importance of prompting while providing early evidence for designing effective MAS – *optimize agents locally before scaling their topology*.

## 2.2. Workflow-level Search Space Design

At the workflow level, the primary focus is on orchestrating agents to achieve the best performance effectively. As a relatively new concept specific to MAS, topology optimization has recently garnered significant attention (Li et al., 2024c; Zhang et al., 2024b). However, while much of the existing research emphasizes *search methods*—such as discovering the most efficient and effective way to identify the optimal configuration—there has been less focus on the design of *search spaces*, which determines the perimeter and the scope of any search algorithm. This imbalance draws a parallel to the historical development of *neural architecture search* (NAS) (White et al., 2023). Initially, the field concentrated on sophisticated search methods, such as Bayesian optimization (Kandasamy et al., 2018; Ru et al., 2021) and differentiable search (Liu et al., 2018). Follow-up works have highlighted the often-overlooked importance of search space design, arguing that it can be equally, if not more, critical (Wan et al., 2022; Zhou et al., 2023, 2024c). Inspired by this insight, we hypothesize that manually crafted topologies might be sub-optimal, and automatic topology optimization (potentially framed as a rigorous optimization problem) can play a similarly pivotal role via judiciously designing search space for MAS. To achieve so, we first define an expressive search space, similar to prior works, that consists of the connections between the following *building blocks*:

- **Aggregate:** Agents can collaborate in parallel with diversified predictions, which is then followed by an aggregation operator that obtains the most consistent prediction. The aggregate block can be parameterized by  $N_a$  agents acting in parallel. Majority vote (Li et al., 2024a) and self-consistency (Chen et al., 2024c) sits within this topology.
- **Reflect:** Agents can act as verifiers, providing critics and improvement suggestions based on former predictions. The feedback is then fed into the predictor or the reflector itself for an iterative improvement. Similarly, `reflect` can be parameterized by  $N_r$  that defines the number of rounds for self-reflection. The self-refine (Madaan et al., 2024) and Reflexion (Shinn et al., 2024) represent this block.
- **Debate:** Agents in debate can elicit more truthful predictions than single-agent prediction (Du et al., 2024; Liang et al., 2024), where each debating agent would collect opinions from all other agents

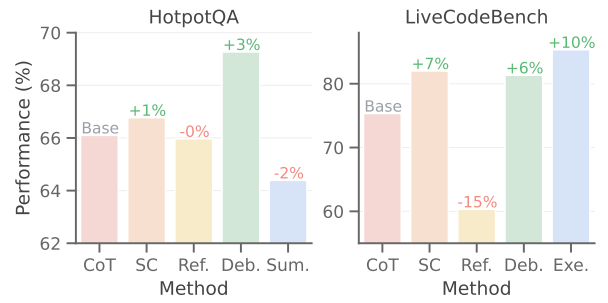


Figure 3 | The performance of different topologies with Gemini 1.5 Pro compared to the base agent with each topology being optimized with APO, where Sum. (Summarize) and Exe. (Executor) are task-specific topologies as illustrated in Fig. 4. We observe that not all topologies have a positive influence on the MAS design.

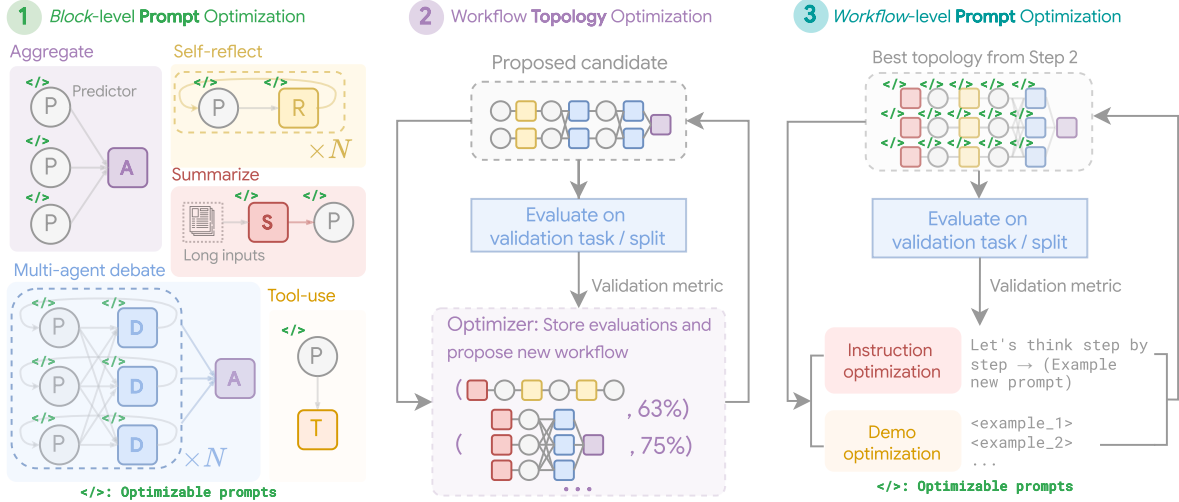


Figure 4 | Illustration of the MASS framework with its search space and the multi-stage optimization. The search space combines both prompts (Instruction, Demo) and configurable agentic building blocks (Aggregate, Reflect, Debate, Summarize, and Tool-use). 1) **Block-level Prompt Optimization**: we conduct *block-level* prompt optimization for each agentic module individually (denoted by `</>`); 2) **Workflow Topology Optimization**: conditioned on the best prompts found in Stage 1 on each agent block, MASS samples valid configurations from an influence-weighted design space while fusing the prompts of each building block from Stage 1; 3) **Workflow-level Prompt Optimization**: conditioned on the best workflow found in the Stage 2, we again conduct *workflow-level* prompt optimization on the best-found MAS (topologies visualized for *illustration only*).

and provides an updated response. This topology would involve a mixture of agents, and  $N_d$  defines the number of rounds for debating.

- **Custom Agents**: While the former three forms of agents represent the vast majority of agent topologies constructed as multiple parallel, serial, and mixture of agents, more versatile definitions of agents can be inserted into the MAS design space. For example, for task-specific use cases, we introduce an agent as *summarize* to improve the long-context capability in the customizable design space.
- **Tool-use**: Building towards an effective MAS, enabling agents to leverage tools to access external information is critical for system performance, such as using retriever for RAG (Lewis et al., 2020) and executor with test cases in coding (Chen et al., 2024d). We introduce tool-use as an optimizable binary ‘insertion’ decision  $N_T \in \{0, 1\}$ .

To understand the influence of individual topology, we report the performance of various topologies in Fig. 3. It is noticeable that not all topologies are beneficial to MAS design, whereas positively influenced topologies only represent a small fraction of the overall set, such that, in HotpotQA (Yang et al., 2018), only debate brings 3% gain while others fail to improve or even degrade systematic performance. We again observe similar trends in the test-output-prediction subtask of LiveCodeBench (Jain et al., 2024). It highlights the importance of searching in the influential set of search space, whereas including decremental building blocks may not only result in higher search complexity but also degrade the performance.

### 3. MASS: Multi-Agent System Search

Our analyses in Sec. 2 underscore the importance of well-designed prompts for individual agents and the careful definition of the search space to achieve effective MAS performance. Building on these, we



propose a multistage optimization algorithm, **Multi-Agent System Search (MASS)**, that surpasses prior arts that focused solely on optimizing workflow topology without appropriate prompt designs. Instead, our approach demonstrates the greater effectiveness of MAS design with properly optimized prompts and thoughtfully designed search spaces. MASS framework is illustrated in Algorithm 1 and Fig. 4, following an intuition from local to global, from block-level to workflow-level, that conquers the complexity of combinatorial optimization with effective per-stage optimization detailed below.

**1) Block-level prompt optimization.** Before composing agents, we first ensure that individual agents are thoroughly optimized at the block level, as highlighted in Sec. 2.1 and Fig. 2 – this step ensures that each agent is primed for its role with the most effective instructions in the most manageable computation budget. To further overcome the complexity of joint optimization on a large MAS space, we first warm up the initial predictor with single-agent APO,  $a_0^* \leftarrow \mathcal{O}_{\mathcal{D}}(a_0)$ , where both instruction and exemplars are jointly optimized with the modular prompt optimizer  $\mathcal{O}$ . Followed by conditioning on the warmed predictor, we continue optimizing each topology with a minimum number of agents,  $a_i^* \leftarrow \mathcal{O}_{\mathcal{D}}(a_i|a_0^*)$ , such that, 2 predictors paired with 1 debator form the minimum building block as the debate topology, thereby lowering the complexity for optimization, and this topology can be scaled up later with more predictors and debators but all equipped with optimized prompts. To measure the influence of each building block, we store the validation performance once the optimization is completed. It is important that though Stage (1) serves as the *warm-up* stage per building block, it is still a critical stage that guarantees the follow-up topology optimization is searching in an effective space, composing well-performing agents instead of suffering from the compounding impact from any ill-formed agents with manual prompts.

**2) Workflow topology optimization.** In this stage, we focus on optimizing the overall MAS structure, determining the most effective arrangement and connectivity between agents. The analysis in Fig. 3 shows that beneficial topologies only represent a small fraction of the full design space. Therefore, we aim to distill the essence of strong-performing topologies into a pruned space, thereby making the workflow-level topology search more efficient. Here, we propose to measure the incremental influence  $I_{a_i} = \mathcal{E}(a_i^*)/\mathcal{E}(a_0^*)$  that quantifies the relative gain for integrating the topology  $a_i$  over the initial agent  $a_0$ . Following the intuition that influential dimension comes with higher selection probability, we activate the corresponding topology dimension  $a$  if  $u > p_a$ , given  $u \sim \mathcal{U}(0, 1)$  and  $p_a = \text{Softmax}(I_a, t)$ . To compose diverse topologies into a unified space, we constrain the workflow with a rule-based order to reduce the optimization complexity, following a predefined sequence, such that [summarize, reflect, debate, aggregate]. We integrate rejection sampling over the pre-defined design space that rejects any deactivated dimension, or invalid topology compositions exceeding a maximum budget  $B$  on the number of agents. We refer to App. §B for the detailed search space per task.

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**Algorithm 1** MASS: Multi-Agent System Search

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- 1: **Input:** Agentic modules in the search space  $a_i \in \mathcal{A}$ , workflow of agents  $\mathcal{W}(a)$ , prompt optimizer  $\mathcal{O}$ , evaluator  $\mathcal{E}$ , validation set  $\mathcal{D}$ , temperature  $t$ , number of candidates  $N$ , budget  $B$ .
  - 2: **Output:** Optimized multi-agent system  $\mathcal{W}^*$ .
  - 3: [Block-level Prompt Optimization]
  - 4: Prompt optimization for the initial agent  $a_0^* \leftarrow \mathcal{O}_{\mathcal{D}}(a_0)$ .
  - 5: **for**  $a_i$  in  $\mathcal{A} \setminus \{a_0\}$  **do**
  - 6:   Local prompt optimization for each building block in the design space:  $a_i^* \leftarrow \mathcal{O}_{\mathcal{D}}(a_i|a_0^*)$
  - 7:   Obtain incremental Influence  $I_{a_i} \leftarrow \mathcal{E}(a_i^*)/\mathcal{E}(a_0^*)$ .
  - 8: **end for**
  - 9: [Workflow Topology Optimization]
  - 10: Obtain the selection probability  $p_a \leftarrow \text{Softmax}(I_a, t)$
  - 11: **while**  $n < N$  **do**
  - 12:   Reject invalid configurations  $c$  and cap a budget  $B$ . The design space is pruned by the selection probability  $p_a$ ,  $\mathcal{W}_c \leftarrow (a_i^*(\cdot), a_{i+1}^*(\cdot), \dots)$  with optimized prompts.
  - 13:   Store evaluations  $\mathcal{E}_{\mathcal{D}}(\mathcal{W}_c)$  and propose new  $\mathcal{W}$ .
  - 14: **end while**
  - 15: Obtain the best-performing  $\mathcal{W}_c^* \leftarrow \arg \max_{c \in \mathcal{C}} \mathcal{E}_{\mathcal{D}}(\mathcal{W}_c)$ .
  - 16: [Workflow-level Prompt Optimization]
  - 17: Workflow-level prompt optimization for the best-performing topology:  $\mathcal{W}^* \leftarrow \mathcal{O}_{\mathcal{D}}(\mathcal{W}_c^*)$ .
  - 18: **Return** optimized multi-agent system  $\mathcal{W}^*$ .
-

**3) Workflow-level prompt optimization.** As a final step, we treat the entire MAS design as an integrated entity and run an additional round of prompt optimization, conditioned on the best topology discovered in Stage (2),  $\mathcal{W}^* = \mathcal{O}_{\mathcal{D}}(\mathcal{W}_c^*)$ . It is worth noting that although prompts were optimized at the individual level in Stage (1), this stage acts as an adaptation or fine-tuning process, ensuring that prompts are tailored for orchestration within the MAS and that the interdependence between agents is optimized appropriately. Our experiments (Fig. 5 & 6) demonstrate that this stage often yields practical benefits.

## 4. Related Work

**Forms of LLM-based agentic systems.** The simplest form of an LLM-based agentic system involves a single agent that can dynamically interact and respond to the environment (Yao et al., 2023). Recent advances endow agents with diverse roles and tools (Wu et al., 2023), orchestrating multiple agents to cooperate with each other (Chen et al., 2024b). Standard forms of agent cooperation (i.e., topology) often involve parallel and serial flows of information. The parallel form usually diversifies the exploration among many agents in parallel (Li et al., 2024a), and self-consistency (SC) (Wang et al., 2023) is a representative way for scaling agents in parallel. The serial form aims to advance the exploitation of a task via a chain of agents, where LLMs can serve as reflective agents to self-justify and refine former predictions (Madaan et al., 2024; Shinn et al., 2024). Later, the opinions from multiple agents can be summarized to retrieve the most consistent answer by an aggregation agent (Chen et al., 2024c; Lin et al., 2024). Moreover, multi-agent debate consists of a more complex flow of information (Chen et al., 2024a; Wang et al., 2024c; Zhang et al., 2024c), and recent research shows that debating can elicit more truthful predictions (Du et al., 2024; Khan et al., 2024). Recent agent topology extends beyond the above connections (Qian et al., 2024; Wang et al., 2024b), and MASS can automatically search the best topology among the aforementioned spaces.

**Automatic optimization for MAS.** Recent research starts automating agent design by interpreting agent functions as learnable policies (Zhang et al., 2024d,e) and synthesizing trajectories for agent fine-tuning (Qiao et al., 2024). Going further from a single agent, automatic multi-agent optimization faces a higher level of complexity, thereby requiring a more sophisticated design of search space and algorithms. Among all recent advances in multi-agent optimization, the optimization space has spanned prompts (Khatab et al., 2024), tools (Zhou et al., 2024d), workflows (Li et al., 2024c), and thinking strategies (Shang et al., 2024). Aligning closer to our topology search space, DyLAN (Liu et al., 2024b) dynamically activates the composition of agents, and Archon (Saad-Falcon et al., 2024) frames MAS as a hyperparameter optimization problem. Neither of them has taken the important prompt space into account, where we demonstrated the importance of prompt optimization in Sec. 2.2. In addition, GPTSwarm (Zhuge et al., 2024) optimizes the connections between agentic nodes using a policy gradient algorithm. State-of-the-art automatic agent design methods, ADAS (Hu et al., 2024a) and AFlow (Zhang et al., 2024b), also attempt to optimize agentic workflows with advanced search algorithms and LLM as optimizers. However, we observe that the importance of proper prompt designs has been relatively under-studied in these prior works.

## 5. Experiments

**Models and evaluation data.** Aside from the common benchmarks used for automating MAS (Hu et al., 2024a; Zhang et al., 2024b), we conduct experiments on an extensive collection of tasks: 1) Hendryck’s MATH (Hendrycks et al., 2021) and DROP (Dua et al., 2019) for reasoning; HotpotQA (Yang et al., 2018), MuSiQue (Trivedi et al., 2022), 2WikiMultiHopQA (Ho et al., 2020) from LongBench (Bai et al., 2024) for long-context understanding; 3) MBPP (Austin et al., 2021),



Table 1 | Results on the evaluation set with Gemini 1.5 Pro and Gemini 1.5 Flash. We report the mean and standard deviation for all results with 3 runs of evaluations. We report the accuracy (%) for MATH and the test-output-prediction subtask of LiveCodeBench (LCB), F1 score for DROP, HotpotQA, MuSiQue, and 2WikiMQA, and pass@1 for MBPP and HumanEval. We note that the meta-prompt of AFlow<sup>\*</sup> only works properly with Claude 3.5 Sonnet. Therefore, we reproduce AFlow with Gemini 1.5 Pro as the executor and Claude 3.5 Sonnet as the optimizer, where <sup>\*</sup> indicates the results are only for reference. Number of agents in inference for all methods are below 10.

Gemini-1.5-pro-002									
Task	Reasoning		Multi-hop Long-context			Coding			
Method	MATH	DROP	HotpotQA	MuSiQue	2WikiMQA	MBPP	HumanEval	LCB	Avg.
CoT	71.67 <sub>3.30</sub>	70.59 <sub>1.67</sub>	57.43 <sub>0.52</sub>	37.81 <sub>1.43</sub>	63.39 <sub>1.12</sub>	68.33 <sub>0.47</sub>	86.67 <sub>0.94</sub>	66.33 <sub>0.62</sub>	65.28
Self-Consistency	77.33 <sub>1.25</sub>	74.06 <sub>0.90</sub>	58.60 <sub>2.19</sub>	41.81 <sub>1.00</sub>	67.79 <sub>1.19</sub>	69.50 <sub>0.71</sub>	86.00 <sub>0.82</sub>	70.33 <sub>0.94</sub>	68.18
Self-Refine	79.67 <sub>2.36</sub>	71.03 <sub>1.31</sub>	60.62 <sub>3.33</sub>	42.15 <sub>1.34</sub>	66.74 <sub>2.43</sub>	63.67 <sub>0.24</sub>	84.00 <sub>1.63</sub>	67.33 <sub>1.31</sub>	66.90
Multi-Agent Debate	78.67 <sub>0.94</sub>	71.78 <sub>0.71</sub>	64.87 <sub>0.23</sub>	46.00 <sub>0.80</sub>	71.78 <sub>0.63</sub>	68.67 <sub>0.85</sub>	86.67 <sub>1.25</sub>	73.67 <sub>1.65</sub>	70.26
ADAS	80.00 <sub>0.82</sub>	72.96 <sub>0.90</sub>	65.88 <sub>1.29</sub>	41.95 <sub>1.24</sub>	71.14 <sub>0.66</sub>	73.00 <sub>1.08</sub>	87.67 <sub>1.70</sub>	65.17 <sub>1.25</sub>	69.72
AFlow <sup>*</sup>	76.00 <sub>0.82</sub>	88.92 <sub>0.63</sub>	68.62 <sub>0.47</sub>	32.05 <sub>1.29</sub>	<b>76.51</b> <sub>1.05</sub>	-	88.00 <sub>0.00</sub>	-	-
MASS (Ours)	<b>84.67</b> <sub>0.47</sub>	<b>90.52</b> <sub>0.64</sub>	<b>69.91</b> <sub>1.11</sub>	<b>51.40</b> <sub>0.42</sub>	73.34 <sub>0.67</sub>	<b>86.50</b> <sub>0.41</sub>	<b>91.67</b> <sub>0.47</sub>	<b>82.33</b> <sub>0.85</sub>	<b>78.79</b>
Gemini-1.5-flash-002									
CoT	66.67 <sub>2.36</sub>	71.79 <sub>0.69</sub>	57.82 <sub>1.10</sub>	37.10 <sub>1.35</sub>	63.40 <sub>0.68</sub>	63.33 <sub>1.25</sub>	75.67 <sub>1.89</sub>	51.17 <sub>0.24</sub>	60.87
Self-Consistency	69.33 <sub>1.25</sub>	73.42 <sub>0.19</sub>	60.19 <sub>1.01</sub>	41.94 <sub>0.93</sub>	67.98 <sub>0.72</sub>	63.67 <sub>0.62</sub>	77.67 <sub>1.89</sub>	53.83 <sub>1.18</sub>	63.50
Self-Refine	71.33 <sub>0.94</sub>	73.71 <sub>1.09</sub>	58.84 <sub>3.04</sub>	41.21 <sub>1.99</sub>	65.56 <sub>1.57</sub>	63.33 <sub>1.25</sub>	81.67 <sub>1.89</sub>	52.00 <sub>1.41</sub>	63.46
Multi-Agent Debate	71.67 <sub>0.94</sub>	74.79 <sub>0.87</sub>	64.17 <sub>1.69</sub>	46.27 <sub>1.33</sub>	72.19 <sub>0.54</sub>	63.00 <sub>0.71</sub>	79.67 <sub>1.25</sub>	55.50 <sub>0.41</sub>	65.91
ADAS	68.00 <sub>1.41</sub>	75.95 <sub>1.18</sub>	61.36 <sub>2.89</sub>	<b>48.81</b> <sub>1.03</sub>	66.90 <sub>1.00</sub>	65.83 <sub>0.24</sub>	80.67 <sub>2.49</sub>	50.50 <sub>1.63</sub>	64.75
MASS (Ours)	<b>81.00</b> <sub>2.45</sub>	<b>91.68</b> <sub>0.14</sub>	<b>66.53</b> <sub>0.38</sub>	43.67 <sub>1.21</sub>	<b>76.69</b> <sub>0.50</sub>	<b>78.00</b> <sub>0.82</sub>	<b>84.67</b> <sub>0.47</sub>	<b>72.17</b> <sub>0.85</sub>	<b>74.30</b>

HumanEval (Chen et al., 2021), and LiveCodeBench (LCB) ‘test output prediction’ (Jain et al., 2024) for coding. We refer to App. §B & §D for details on data splits and prompt templates. We run all experiments primarily on two Gemini 1.5 model sizes (Reid et al., 2024) (gemini-1.5-pro-002 and gemini-1.5-flash-002) and further validate key findings on Claude 3.5 Sonnet (@20240620) (Anthropic, 2024).

**Baselines.** We consider the following baselines: 1) CoT (Kojima et al., 2022): direct chain-of-thought reasoning via zero-shot prompting; 2) CoT-SC (Wang et al., 2023): with self-consistency to find the most consistent answers from diversified reasoning traces; 3) Self-Refine (Madaan et al., 2024; Shinn et al., 2024): reflective agents to verify and self-refine predictions; 4) Multi-Agent Debate (Du et al., 2024; Liang et al., 2024): with agent justifying answers and aggregating information from other agents; 5) ADAS (Hu et al., 2024a): an automatic agent design framework, where an LLM-based meta-agent iteratively proposes new agents based on former evaluations; 6) AFlow (Zhang et al., 2024b): automatic workflow design via Monte-Carlo Tree Search over a set of pre-defined operators. We fairly compare all baselines by limiting the maximum number of agents to 10. We refer to App. §B for all specifications.

**Setup.** MASS integrates the state-of-the-art prompt optimizer, MIPRO (Opsahl-Ong et al., 2024), which optimizes both instructions and demonstrations for each agent via a Bayesian surrogate model. We limit the number of bootstrapped demonstrations to 3 and instruction candidates to 10, per agent in 10 rounds. In topology optimization for all tasks, we search for 10 different topologies via rejection sampling. Along with topology optimization, each topology is evaluated on the validation set 3 times to stabilize the prediction. The optimized MAS is then reported on the held-out test set over three

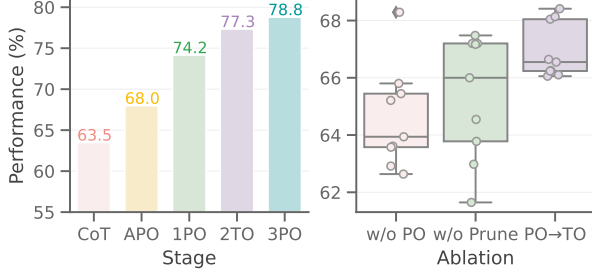


Figure 5 | **Left:** average performance per optimization stage of MASS over 8 evaluation tasks on Gemini 1.5 Pro. We compare MASS with a single agent (CoT) starting point as the reference and an APO baseline that optimizes over the single agent by MIPROv2 (Opsahl-Ong et al., 2024). Refer to App. §C for the detailed ablation per task. **Right:** a comparative ablation study on topology optimization (2TO) without pruning and without the former stage of prompt optimization (1PO) evaluated on HotpotQA.

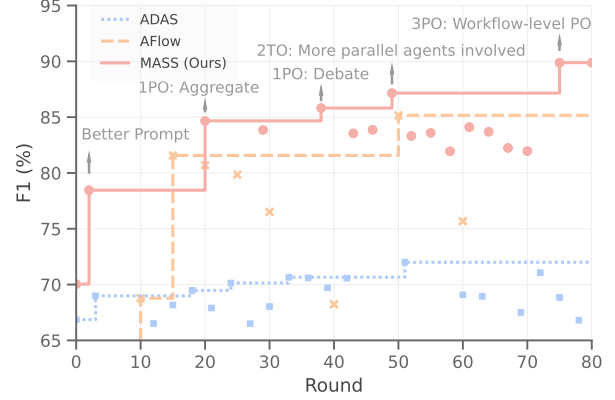


Figure 6 | The optimization trajectories of MASS compared to automatic agent design baselines per validation round on DROP. We note that, as a distinct advantage of MASS, the optimization within stages (1) & (2) of MASS can be completely parallelized, whereas ADAS and AFlow are iterative algorithms that have to wait to propose new agents until finishing earlier trajectories.

runs. We set model temperature  $T$  at 0.7, maximum output tokens at 4096, and the  $t$  in Softmax at 0.05 for sharpening the selection probability  $p_a$  for each search dimension. We implement the same LLM backbone as both evaluator and optimizer in all phases.

**Main results.** We present the main results of MASS compared to the baselines on the evaluation set in Table 1. MASS yields substantial gains over common forms of multi-agent systems, (e.g. self-consistency, self-refine, and multi-agent debate), that scale up without optimizing prompts for agents in collaboration. MASS leads to high-performing MAS: 78.8% and 74.3% on average on Gemini 1.5 Pro and Flash, respectively, where we observe consistent improvements on Claude 3.5 Sonnet as reported in Table 4. By comparing MASS with state-of-the-art automatic agent design baselines, ADAS and AFlow, we first notice that ADAS only brings subtle gains even by already conditioning its meta-agent generation based on the common forms of agents. The meta-agent keeps proposing complex topologies but without optimizing the prompt design. AFlow, on the other hand, demonstrates a competitive performance to MASS, especially on 2WikiMQA and HumanEval.

We attribute the performance of AFlow to: 1) its ‘expansion’ phase that generates new nodes based on an error log that contrasts the predictions with the ground truth, which provides implicit textual gradients (Pryzant et al., 2023) to reflect on any formatting errors in prompt design; 2) a more refined search space within a pre-defined set of operators. Though AFlow draws similar inspirations on the importance of search space design as MASS, it still lacks a phase of prompt optimization to *optimize* its pre-defined operators properly, resulting in under-performance for MAS search results at MATH and MuSiQue. Different from these baselines, the consistent improvements brought by MASS highlight the importance of searching in both prompt and topology design space.

**Ablating optimization stages.** To understand the incremental gain per MASS optimization stage, we provide a stage-by-stage ablation study in Fig. 5. We list the average performance of MASS from block-level to workflow-level optimization and compare it with a single agent APO baseline, where the block-level optimization performance indicates the best-performing building block  $a \in \mathcal{A}$  after APO. First, we notice that there is a large gain, 6% on average, between block-level optimization and single-agent optimization, showing that MAS benefits substantially from having its agents

### 1 Block-level Prompt Optimization (62% → 79%)

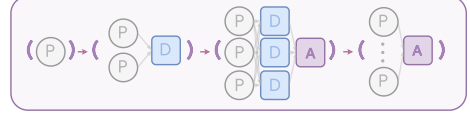
Debator:

You are a seasoned math professor specializing in clear and concise explanations. You are reviewing student solutions to math problems. Below, you will find the problem, followed by solutions from several students. Carefully examine each student's solution, identifying any errors in their logic or calculations. Provide a comprehensive rationale explaining your analysis of each student's work, clearly stating whether their final answer is correct or incorrect and why. Finally, provide your own definitive and simplified solution to the problem, ensuring its accuracy and clarity. Present your final answer bracketed between <answer> and </answer> at the end.

Question: Compute  $17^{-1} \pmod{83}$ .  
Solutions: Agent 0: 44\nAgent 1: 74  
Rationale: <Rationale>  
Answer: 44

<Task Demo: Exemplar\_2>  
<Task Demo: Exemplar\_3>

### 2 Workflow Topology Optimization (79% → 83%)



### 3 Workflow-level Prompt Optimization (83% → 85%)

Predictor:

Let's think step by step to solve the given problem. Clearly explain your reasoning process, showing all intermediate calculations and justifications. Express your final answer as a single numerical value or simplified expression enclosed within <answer></answer> tags. Avoid extraneous text or explanations outside of the core reasoning and final answer.  
<Task Demo: Exemplar\_1>

Figure 7 | A demonstration of the optimization trajectory of MASS on MATH. In (1) **block-level optimization**: multi-agent debate serves as the best-performing topology. In (2) **workflow topology optimization**, aggregating with more parallel agents outweighs the performance of agents in debate. Lastly, (3) **workflow-level optimization** discovers the optimal prompt conditioned on the best topology.

optimized inside the building block. In addition, going from Stage (1) to (2), another 3% gain can be achieved by composing influential topologies while searching the optimal configurations. Here, we provide an additional ablation on conducting Stage (2) without prompt optimization beforehand or without search space pruning. Fig. 5 (right) shows that both of them are critical for effective search space exploration. Lastly, MASS obtains further gains (~2%) by conducting workflow-level prompt optimization on the best-found topology, which indicates that optimizing the prompts towards modeling the interdependence of agents is beneficial in the MAS design.

**Cost-effectiveness of MASS.** We conduct analysis on the cost-effectiveness of MASS. In particular, we visualize the optimization trajectory of MASS as shown in Fig. 6. MASS's trajectory demonstrates a steady trend of optimization that gradually improves the validation performance via interleaving the search towards better prompts and topologies. However, when it comes to automatic design baselines without explicit prompt optimization stages, AFlow is exposed to a larger variance in its optimization due to the nature of MCTS, whereas ADAS gets trapped in discovering over-complex topologies that appear to be less effective than the prompt design space. Overall, the optimization trajectory of MASS highlights the importance of optimizing in an effective design space, where interleaved optimization further resolves the complexity with more consecutive rewards. Following Sec. 2.1, MASS also demonstrated advanced token-effectiveness, which we refer to Fig. 9.

**Best-found MAS architectures & Design principles.** We further inspect an example of optimized prompts and the trajectory of MASS in discovering more effective topologies in Fig. 7. The optimization starts from a zero-shot CoT agent, and soon MASS in Stage (1) identifies the high-performing topology in debate with its optimized prompt. However, as found in Stage (2), aggregating with more parallel agents actually outweighs the multi-agent debate. Workflow-level prompt optimization then leads to the best-performing predictor for aggregation. The overall optimization flow sheds light on our guidelines for building effective MAS: 1) optimizing individual agents properly is important before composing them into an MAS; 2) more effective MAS can be built by composing influential topologies; and 3) modeling the interdependence between agents is beneficial, and can be achieved via workflow-level joint optimization.

## 6. Conclusion

We approach designing effective MAS by first conducting a thorough analysis of the massive design space, revealing the crucial role of prompts, and identifying an influential subset of search space. Building on these findings, we introduce MASS, a novel multi-stage optimization framework that searches within a pruned design space, interleaving prompt and topology optimization to efficiently generate high-performing MAS. Our experiments demonstrate that MASS-optimized MAS significantly outperforms existing manual and automated approaches across an extensive set of tasks. Finally, based on the optimized systems discovered by MASS, we extract valuable design principles to guide the development of future effective LLM-based MAS.

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## A. Limitations and future work

MASS is a multi-agent design meta-framework also orthogonal to prompt and topology optimizers. MASS has brought substantial improvements over a single agent design by searching in a customizable topology space. Though our proposed topology space has covered the vast majority of effective MAS designs, including serial, parallel, and mixture of connections, it is still likely that incorporating other topologies may further improve the final performance of MASS, which is complementary to the development of MASS. For instance, the debate topology proposed in MASS involves a fully-connected topology across agents. Recent work has been identifying the sparsity of agent communications (Li et al., 2024b; Zhang et al., 2024a), and pruning redundant communications may further enhance the overall efficiency of the strongest MASS-found design. Though the topology optimizer in MASS already traverses efficiently in the proposed topology space, incorporating more advanced search algorithms, such as the Bayes optimizer (Kandasamy et al., 2018; Ru et al., 2021), may further improve the sample efficiency of MASS when faces a more complex design space. Similarly, the sample efficiency of the prompt optimizer may be further enhanced by conditioning on textual feedback from error logs (Pryzant et al., 2023; Wan et al., 2024), which we will endeavor to explore in future work.

## B. Implementation details

### B.1. Datasets

In this work, we included the following dataset: 1) Hendryck’s MATH (Hendrycks et al., 2021) consisting challenging competition-level mathematics problems, and DROP (Dua et al., 2019) requires discrete and symbolic reasoning over paragraphs; 2) HotpotQA (Yang et al., 2018), MuSiQue (Trivedi et al., 2022), and 2WikiMultiHopQA (Ho et al., 2020) to evaluate on information seeking from long-context with agentic systems, which we report from standardized versions in LongBench (Bai et al., 2024); 3) MBPP (Austin et al., 2021), HumanEval (Chen et al., 2021), and LiveCodeBench (Jain et al., 2024) as well-established coding benchmarks. Regarding LiveCodeBench, we use the ‘test output prediction’ task as an agent cooperative task. In line with AFlow (Zhang et al., 2024b), we use the public test cases of MBPP and HumanEval for the executor to retrieve reliable external feedback signals.

To save computation resources, we randomly sample a subset of the original validation and test splits to conduct all the experiments, where the specifications are reported in Table 2.

Table 2 | The specification of evaluation tasks: dataset split, topology search space, and the MASS-optimized MAS (on Gemini 1.5 Pro)

Task	Type	Val	Test	Topology Search Space	MASS
MATH	Mathematical Reasoning	60	100	{Aggregate, Reflect, Debate}	{9, 0, 0}
DROP	Discrete Reasoning	60	200	{Aggregate, Reflect, Debate}	{5, 0, 0}
HotpotQA	Long-context Understanding	50	100	{Summarize, Aggregate, Reflect, Debate}	{0, 5, 0, 1}
MuSiQue	Long-context Understanding	50	100	{Summarize, Aggregate, Reflect, Debate}	{0, 3, 0, 2}
2WikiMQA	Long-context Understanding	50	100	{Summarize, Aggregate, Reflect, Debate}	{0, 3, 0, 1}
MBPP	Coding	60	200	{Aggregate, Reflect, Debate, Executor}	{1, 4, 0, 1}
HumanEval	Coding	50	100	{Aggregate, Reflect, Debate, Executor}	{1, 3, 0, 1}
LiveCodeBench	Coding: test output prediction	100	200	{Aggregate, Reflect, Debate, Executor}	{3, 1, 1, 1}

Table 3 | The search dimension for each topology. The minimum topology defines the building block that MASS Stage (1) optimized.

Topology	Search Space	Minimum Topology Building Block	Specification
Summarize	{0, 1, 2, 3, 4}	{Summarizer, Predictor}	{1, 1}
Aggregate	{1, 3, 5, 7, 9}	{Predictor, Aggregator}	{3, 1}
Reflect	{0, 1, 2, 3, 4}	{Predictor, Reflector}	{1, 1}
Debate	{0, 1, 2, 3, 4}	{Predictor, Debator}	{2, 1}
Execute	{0, 1}	{Predictor, Executor, Reflector}	{1, 1, 1}

## B.2. Baselines

In this section, we report the specifications of all our baselines. We note that for the baselines: CoT, SC, Self-Refine, and Multi-Agent Debate, we follow the prompts given in ADAS (Hu et al., 2024a).

1) Chain-of-Thought (CoT) (Kojima et al., 2022). Direct chain-of-thought reasoning via zero-shot prompting: “Please think step by step and then solve the task.”

2) Self-Consistency (SC) (Wang et al., 2023). In self-consistency, we generate diverse chain-of-thought reasoning traces with a temperature of 0.8, followed by a rule-based majority vote that collects the most consistent answer. In Table 1, we report SC@9 to provide a fair comparison across baselines.

3) Self-Refine (Madaan et al., 2024): This baseline consists of one predictor that constantly takes feedback and a self-reflector that provides criticism. It involves a stop criterion whenever the self-reflector outputs “correct” in its prediction. We set the maximum number of rounds of reflections to 5, such that the worst case will involve 11 ( $1 + 2 \times 5$ ) calls.

4) Multi-Agent Debate (Du et al., 2024; Liang et al., 2024). In this baseline, it involves 3 agents that conduct reasoning and debating for 3 rounds. The opinions along the rounds of debating are finally judged by an aggregator that makes the final prediction. Hence, it contains 10 ( $3 \times 3 + 1$ ) agents.

5) Automated Design of Agentic Systems (ADAS) (Hu et al., 2024a). Consistent with our main experimental setups. We use Gemini 1.5 as both LLM optimizer and evaluator for reproducing all ADAS results. The generation of ADAS is conditioned on former evaluations of baselines, including CoT, SC, Self-Refine, and Multi-Agent Debate. We report ADAS with 30 rounds of search, and each round is evaluated on the validation set 3 times to stabilize the prediction.

6) AFlow (Zhang et al., 2024b). Automatic workflow design via Monte-Carlo Tree Search over a set of pre-defined operators. Similar to ADAS, AFlow also relies on an LLM optimizer to generate new nodes and topologies expressed in codes. However, we find the meta-prompt of AFlow does not generalize to other LLM backbones. Consequently, we report AFlow with its original LLM optimizer by Claude 3.5 Sonnet, and reproduce experiments with Gemini 1.5 Pro as the LLM executor. Therefore, the comparison is not completely fair, and we treat the results from AFlow as a good reference. We note that the ‘-’ in Table 1 refers to out-of-time errors, where the LLM executor has been trapped in executing accidental scripts with infinite loops. We still endeavored to report most results from AFlow as shown in Table 1 & Fig. 6 with the default experimental setup from AFlow: 20 rounds, 5 runs of validation per round, and k at 3.

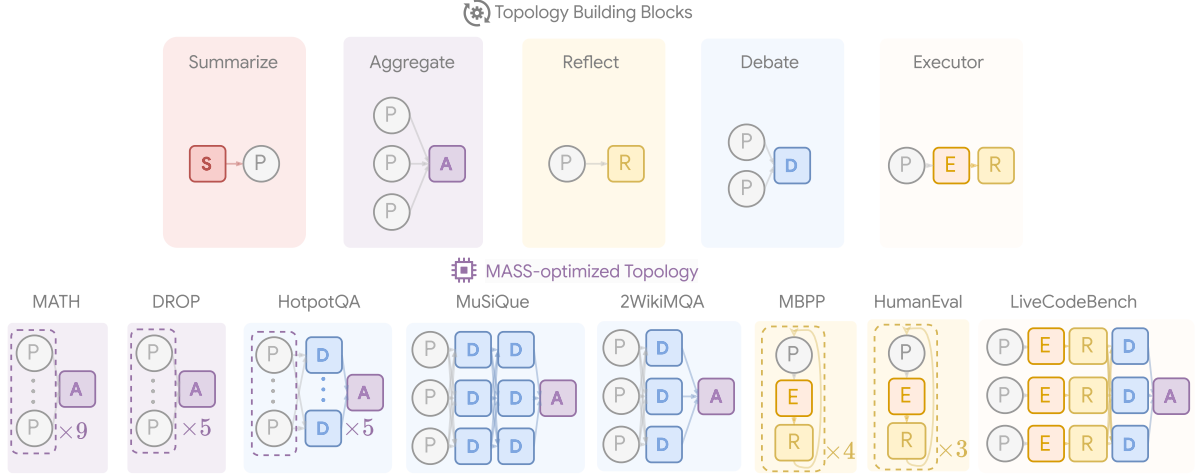


Figure 8 | Visualization of the topology building blocks and best MASS-discovered topologies from Gemini 1.5 Pro.

### B.3. MASS: Multi-Agent System Search

In this section, we provide additional details for MASS. The topology search space for each task is defined in Table 2. In addition, for Stage (1) block-level prompt optimization, the specification of the building block is defined in Table 3. We provide the visualization of both the minimum building blocks and the optimized topology in Fig. 8. We refer the reader to App. §D & §E for the prompt templates we used to define each type of agent and the best prompts discovered.

## C. Additional experiments

Table 4 | Results on the evaluation set with Claude 3.5 Sonnet. We keep the same experimental setup as Table 1. Since Claude 3.5 Sonnet does not support the same context window as Gemini, we report the standard HotpotQA instead of the LongBench. As we transfer the prompt template for each agent from Gemini to Claude, it is noticeable that the basic topology on some tasks may result in severe degradation of performance, and MASS successfully recovers the performance and brings significant improvements over the initial agent.

Claude-3.5-Sonnet							
Task	Reasoning		Multi-hop	Coding			Avg.
Method	MATH	DROP	HotpotQA	MBPP	HumanEval	LCB	
CoT	57.33 <sub>0.94</sub>	55.52 <sub>0.42</sub>	23.56 <sub>1.52</sub>	67.50 <sub>1.47</sub>	88.67 <sub>1.70</sub>	72.67 <sub>2.39</sub>	60.21
Self-Consistency	61.67 <sub>1.89</sub>	57.86 <sub>0.45</sub>	25.69 <sub>0.44</sub>	<b>69.17</b> <sub>0.62</sub>	90.00 <sub>0.82</sub>	72.67 <sub>2.39</sub>	62.84
Self-Refine	57.00 <sub>1.63</sub>	56.26 <sub>0.56</sub>	23.57 <sub>2.56</sub>	68.00 <sub>0.82</sub>	87.00 <sub>1.41</sub>	49.33 <sub>1.65</sub>	56.86
Multi-Agent Debate	45.00 <sub>3.74</sub>	26.62 <sub>0.11</sub>	31.41 <sub>3.30</sub>	00.00 <sub>0.00</sub>	84.33 <sub>3.30</sub>	72.82 <sub>1.84</sub>	43.36
MASS	<b>63.00</b> <sub>0.00</sub>	<b>68.93</b> <sub>0.38</sub>	<b>66.98</b> <sub>0.99</sub>	68.83 <sub>0.62</sub>	<b>93.00</b> <sub>0.82</sub>	<b>73.73</b> <sub>1.43</sub>	<b>72.43</b>

Table 5 | The detailed ablation results per optimization stage of MASS. Practical gains can be obtained by further conducting workflow-level prompt optimization (3PO) on the best-found topology.

Gemini-1.5-pro-002									
Task	Reasoning		Multi-hop Long-context			Coding			
Method	MATH	DROP	HotpotQA	MuSiQue	2WikiMQA	MBPP	HumanEval	LCB	Avg.
Base Agent	62.33 <sub>0.94</sub>	71.65 <sub>0.61</sub>	56.96 <sub>1.26</sub>	43.32 <sub>0.13</sub>	49.20 <sub>0.61</sub>	68.83 <sub>0.85</sub>	89.33 <sub>1.70</sub>	66.33 <sub>2.09</sub>	63.54
+ APO	79.33 <sub>1.89</sub>	77.51 <sub>0.38</sub>	59.72 <sub>0.00</sub>	43.97 <sub>0.00</sub>	61.49 <sub>0.24</sub>	67.00 <sub>1.08</sub>	86.33 <sub>1.25</sub>	68.50 <sub>1.22</sub>	67.44
+ 1PO	80.00 <sub>0.00</sub>	86.45 <sub>0.90</sub>	62.52 <sub>1.86</sub>	48.86 <sub>0.61</sub>	67.40 <sub>0.58</sub>	80.33 <sub>1.25</sub>	91.67 <sub>1.25</sub>	76.00 <sub>0.00</sub>	74.56
+ 2TO	83.00 <sub>1.63</sub>	86.75 <sub>1.32</sub>	65.22 <sub>1.34</sub>	52.61 <sub>0.52</sub>	72.82 <sub>0.86</sub>	85.00 <sub>1.08</sub>	92.00 <sub>0.82</sub>	81.33 <sub>0.00</sub>	77.55
+ 3PO	84.67 <sub>0.47</sub>	90.52 <sub>0.64</sub>	69.91 <sub>1.11</sub>	51.40 <sub>0.42</sub>	73.34 <sub>0.67</sub>	86.50 <sub>0.41</sub>	91.67 <sub>0.47</sub>	82.33 <sub>0.85</sub>	78.40

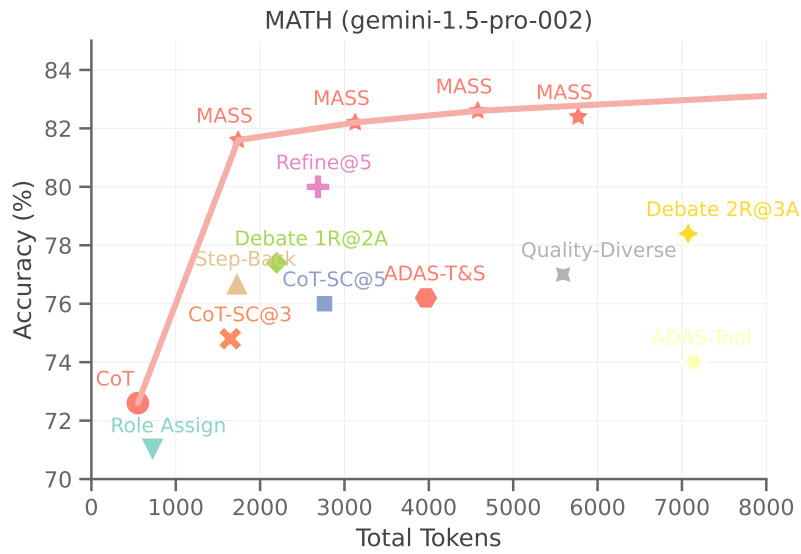


Figure 9 | The Pareto-front of MASS-optimized designs compared to multi-agent baselines. Total tokens include both inference input tokens and output tokens. Additional multi-agent baselines from ADAS (Hu et al., 2024a) and two best-found ADAS designs are included.

## D. Prompt template

We provide all prompt templates we used for defining the MASS search space. We use `<>` to enclose texts that have been skipped for presentation purposes. We follow the DSPy (Khatab et al., 2024) in constructing these agentic templates.

The general template for instruction, exemplar, and input/output fields:

```

1 <Instruction>
2
3
4 ---
5
6 Follow the following format.
7
8 Input: ${Input}
9 ...
10 Output: ${output}
11
12 ---
13
```

```

14 <example_1>
15
16 ---
17
18 Input: <Input>
19 ...
20 Output: <output>

```

#### MATH:

```

1 Predictor:
2
3 Let's think step by step.
4 ---
5 Question: ${question}
6 Reasoning: Let's think step by step in order to ${produce the answer}. We ...
7 Answer: ${answer}
8
9 -----
10 Reflector:
11
12 Please review the answer above and criticize on where might be wrong. If you are
    absolutely sure it is correct, output 'True' in 'correctness'.
13
14 ---
15 Question: ${question}
16 Text: ${text}
17 Reasoning: Let's think step by step in order to ${produce the correctness}. We ...
18 Feedback: ${feedback}
19 Correctness: True/False indicating if answer is correct given the question.
20
21 -----
22 Refiner:
23
24 Given previous attempts and feedback, carefully consider where you could go wrong in
    your latest attempt. Using insights from previous attempts, try to solve the
    task better. Show your final answer bracketed between <answer> and </answer> at
    the end.
25
26 ---
27 Question: ${question}
28 Previous answer: ${previous_answer}
29 Reflection: ${reflection}
30 Correctness: ${correctness}
31 Thinking: ${thinking}
32 Answer: ${answer}
33
34 -----
35
36 Debator:
37
38 These are the solutions to the question from other agents. Examine the solutions
    from other agents in your rationale, finish by giving an updated answer. Show
    your final answer bracketed between <answer> and </answer> at the end.
39
40 ---
41 Question: ${question}
42 Solutions: the solutions to the question from other agents
43 Reasoning: Let's think step by step in order to ${Examine the solutions from other
    agents}. We ...
44 Answer: The updated answer for the question. Do not repeat Answer:

```

#### DROP:

```

1 Predictor:
2
3 Please think step by step and then solve the task. # Your Task:
4 Please answer the following question based on the given context.
5 ---
6 Question: ${question}
7 Context: ${context}
8 Thinking: ${thinking}

```



```

9 Answer: Directly answer the question. Keep it very concise.
10
11 -----
12 Reflector:
13
14 Verify that the answer is based on the provided context. Give your reflection in the
   rationale.
15
16 ---
17 Question: ${question}
18 Context: ${context}
19 Text: ${text}
20 Reasoning: Let's think step by step in order to ${produce the correctness}. We ...
21 Correctness: True/False indicating if answer is correct given the observations and
   question.
22
23 -----
24 Refiner:
25
26 Please think step by step and then solve the task. # Your Task:
27 Based on the reflection, correctness of the previous answer, and the context again,
   give an updated answer.
28
29 ---
30 Question: ${question}
31 Context: ${context}
32 Previous answer: ${previous_answer}
33 Reflection: ${reflection}
34 Correctness: ${correctness}
35 Thinking: ${thinking}
36 Answer: Directly answer the question. Keep it very concise.
37
38 -----
39
40 Debator:
41
42 These are the solutions to the question from other agents. Based on the context,
   examine the solutions from other agents in your rationale, finish by giving an
   updated answer.
43
44 ---
45 Question: ${question}
46 Context: ${context}
47 Solutions: the solutions to the question from other agents
48 Reasoning: Let's think step by step in order to ${Examine the solutions from other
   agents}. We ...
49 Answer: The updated answer for the question. Do not repeat Answer:

```

#### HotpotQA, MuSiQue, and 2WikiMQA:

```

1 Predictor:
2
3 Answer the question with information based on the context. Only return the answer as
   your output.
4 ---
5 Question: ${question}
6 Context: ${context}
7 Answer: Only give me the answer. Do not output any other words.
8
9 -----
10 Summarizer:
11
12 Based on the question, retrieve relevant information from context that is ONLY
   helpful in answering the question. Include all key information. Do not repeat
   context.
13 ---
14 Question: ${question}
15 Context: ${context}
16 Summary: Only generate the summary. Start with Summary:
17
18 -----

```

```
19 Reflector:
20
21 Verify that the answer is based on the provided context.
22
23 ---
24 Question: ${question}
25 Context: ${context}
26 Text: ${text}
27 Reasoning: Let's think step by step in order to ${produce the correctness}. We ...
28 Correctness: True/False indicating if answer is correct given the observations and
    question.
29
30 -----
31
32 Debator:
33
34 These are the solutions to the question from other agents. Based on the context,
    examine the solutions from other agents in your rationale, finish by giving an
    updated answer.
35
36 ---
37 Question: ${question}
38 Context: ${context}
39 Solutions: the solutions to the question from other agents
40 Reasoning: Let's think step by step in order to ${Examine the solutions from other
    agents}. We ...
41 Answer: The updated answer for the question. Do not repeat Answer:
```

#### MBPP:

```
1 Predictor:
2
3 Let's think step by step. Provide a complete and correct code implementation in
    python.
4
5 ---
6 Question: ${question}
7 Thinking: ${thinking}
8 Answer: Only the code implementation. Do not include example usage or explanations.
9
10 -----
11 Reflector:
12
13 Please determine the correctness of the solution in passing all test cases. If it
    fails, based on the error message and traceback, think step by step, carefully
    propose an updated solution in the answer output with a correct code
    implementation in python.
14
15 ---
16 Question: ${question}
17 Previous solution: ${previous_solution}
18 Traceback: It contains the test cases, execution results, and ground truth. If there
    is an error, the relevant traceback is given.
19 Correctness: 'True/False' based on the correctness of executive feedback. If there
    is an error message, output 'False'
20 Thinking: ${thinking}
21 Answer: ${answer}
22
23 -----
24 Debator:
25
26 These are the solutions to the question from other agents. Examine the solutions
    from other agents in your rationale, finish by giving an updated answer. Let's
    think step by step. Provide a complete and correct code implementation in python
    .
27
28 ---
29 Question: ${question}
30 Solutions: the solutions to the question from other agents
31 Reasoning: Let's think step by step in order to ${Examine the solutions from other
    agents}. We ...
```

32 Answer: \${answer}

### HumanEval:

```

1 Predictor:
2
3 Let's think step by step. Provide a complete and correct code implementation in
  python.
4 ---
5 Question: ${question}
6 Thinking: ${thinking}
7 Answer: ${answer}
8
9 -----
10 Reflector:
11
12 Please determine the correctness of the solution in passing all test cases. If it
   fails, based on the error message and traceback, think step by step, carefully
   propose an updated solution in the answer output with a correct code
   implementation in python.
13
14 ---
15 Question: ${question}
16 Previous solution: ${previous_solution}
17 Traceback: ${traceback}
18 Thinking: ${thinking}
19 Answer: ${answer}
20
21 -----
22
23 Debator:
24
25 These are the solutions to the question from other agents. Examine the solutions
   from other agents in your rationale, finish by giving an updated answer. Let's
   think step by step. Provide a complete and correct code implementation in python
   .
26
27 ---
28 Question: ${question}
29 Solutions: the solutions to the question from other agents
30 Reasoning: Let's think step by step in order to ${Examine the solutions from other
   agents}. We ...
31 Answer: ${answer}

```

### LiveCodeBench:

```

1 Predictor:
2
3 You are a helpful programming assistant and an expert Python programmer. The user
  has written a input for the testcase. Think step by step. You will generate the
  code based on the problem requirepement. You will calculate the output of the
  testcase and write the whole assertion statement in the markdown code block with
  the correct output.
4 ---
5 Question: ${question}
6 Thinking: ${thinking}
7 Code: ${code}
8 Answer: complete the testcase with assertion.
9
10 -----
11 Reflector:
12
13 If there is an executive output in the traceback, parse the output into an assertion
   in the answer given the executive output.
14
15 ---
16 Question: ${question}
17 Previous solution: ${previous_solution}
18 Traceback: It contains the test cases, execution results, and ground truth. If there
   is an error, the relevant traceback is given.
19 Correctness: 'True/False' based on the correctness of executive feedback. If there
   is an error message, output 'False'

```

```

20 Thinking: ${thinking}
21 Answer: ${answer}
22
23 -----
24
25 Debator:
26
27 These are the solutions to the question from other agents. Examine the solutions
    from other agents in your rationale, finish by giving an updated answer.
28
29 ---
30 Question: ${question}
31 Solutions: the solutions to the question from other agents
32 Reasoning: Let's think step by step in order to ${Examine the solutions from other
    agents}. We ...
33 Answer: assert ${function(input)} == {executive_output}

```

## E. Best Prompts Discovered

In this section, we show a few typical prompts that have been discovered by MASS. Similarly, we indicate `<>` that skips some comments.

MATH:

```

1 Predictor:
2
3 Let's think step by step to solve the given problem. Clearly explain your reasoning
    process, showing all intermediate calculations and justifications. Express your
    final answer as a single numerical value or simplified expression enclosed
    within <answer></answer> tags. Avoid extraneous text or explanations outside of
    the core reasoning and final answer.
4
5 ---
6
7 Follow the following format.
8
9 Question: ${question}
10 Reasoning: Let's think step by step in order to ${produce the answer}. We ...
11 Answer: ${answer}
12
13 ---
14
15 Question: What is the average of the two smallest positive integer solutions to the
    congruence  $14u \equiv 46 \pmod{100}$ ?
16 Reasoning: Let's think step by step in order to find the average of the two smallest
    positive integer solutions to the congruence  $14u \equiv 46 \pmod{100}$ . We
    are looking for solutions to  $14u \equiv 46 \pmod{100}$ . We can divide the
    congruence by 2 to get  $7u \equiv 23 \pmod{50}$ . We want to find the inverse
    of 7 modulo 50. We use the Euclidean Algorithm: 
$$\begin{aligned} 50 &= 7 \cdot 7 + 1 \\ 7 &= 50 - 7 \cdot 7 \end{aligned}$$
 Thus,  $7(-7) \equiv 1 \pmod{50}$ ,
    so  $7^{-1} \equiv -7 \equiv 43 \pmod{50}$ . Multiplying  $7u \equiv 23 \pmod{50}$ 
    by 43 gives  $u \equiv 23 \cdot 43 \pmod{50}$ .  $23 \cdot 43 = 989 = 50 \cdot 19 + 39$ ,
    so  $23 \cdot 43 \equiv 39 \pmod{50}$ . Therefore,  $u \equiv 39 \pmod{50}$ .
    The two smallest positive integer solutions are  $u = 39$  and  $u = 39 + 50 = 89$ .
    The average of these two solutions is  $\frac{39 + 89}{2} = \frac{128}{2} = 64$ .
17 Answer: 64
18
19 ---

```

In the following prompts, interestingly, we observe that including the data summary, task demonstrations, and past instructions that have been used in MIPRO (Opsahl-Ong et al., 2024) to propose new candidates actually improves the final performance. Hence, we keep these prompts that lead to strong task performance.

DROP:

```

1 Predictor:

```

```

2
3 This dataset is designed for extractive question answering, focusing on retrieving
  concise, factual answers from short texts. Many questions involve extracting
  numerical information and performing simple calculations, suggesting
  applications in areas like sports analytics or financial data analysis. However,
  the dataset's Western cultural bias and lack of complex reasoning questions
  limit its generalizability and real-world applicability.
4
5 TASK DEMO(S):
6 <example_1>
7 Question: How many more points did the Spurs win by in Game 4 against the Mavericks?
8
9 Context:
10 The Mavericks finished 49-33, one game ahead of Phoenix for the eighth and final
   playoff spot, which meant that they would once again have to face their in-state
   rivals, the San Antonio Spurs, who were the top seed in the Western Conference
   with a 62-20 record. In Game 1 in San Antonio, Dallas had an 81-71 lead in the
   fourth quarter, but the Spurs rallied back and took Game 1, 85-90. However, the
   Mavs forced 22 turnovers in Game 2 to rout the Spurs 113-92, splitting the first
   two games before the series went to Dallas. In Game 3, Manu Gin\u00f3bili hit a
   shot that put the Spurs up 108-106 with 1.7 seconds left, but a buzzer-beater
   by Vince Carter gave the Mavs the victory, putting them up 2-1 in the series.
   The Spurs took Game 4 in Dallas 93-89 despite a late Dallas comeback after the
   Spurs at one point had a 20-point lead and later won Game 5 at home, 109-103,
   giving them a 3-2 series lead. The Mavs avoided elimination in Game 6 at home by
   rallying in the fourth quarter, winning 111-113. Game 7 was on the Spurs home
   court, and the Spurs beat the Mavericks 119-96, putting an end to the Mavericks
   season.
11
12 Thinking:
13 The Spurs scored 93 points in Game 4. The Mavericks scored 89 points in Game 4. The
   difference is  $93 - 89 = 4$ .
14 Answer: 4
15
16
17 BASIC INSTRUCTION:
18 '''
19 You are a highly specialized AI tasked with extracting critical numerical
   information for an urgent news report. A live broadcast is relying on your
   accuracy and speed. Think step-by-step, focusing on the numerical information
   provided in the context. Then, answer the question concisely with the extracted
   numerical answer. Failure to provide the correct numerical information will
   result in the broadcast being interrupted.
20
21 Question: {question}
22 Context: {context}
23 '''
24
25 TIP: Keep the instruction clear and concise.
26
27 PROPOSED INSTRUCTION:
28 '''
29
30 Extract the numerical answer to the following question. Show your reasoning by
   identifying the relevant numbers from the provided context and performing any
   necessary calculations. Respond with only the final numerical answer.
31
32 Question: {question}
33 Context: {context}
34 '''

```

### HotpotQA:

```

1 Predictor:
2
3 This multi-passage question answering dataset focuses on complex questions requiring
  synthesis of information from multiple Wikipedia-like sources, often involving
  named entities and temporal reasoning. It emphasizes integrating information,
  handling ambiguity, and leveraging real-world knowledge, posing a significant
  challenge for models relying solely on provided text. The dataset appears well-
  suited for evaluating advanced language models' reasoning abilities across

```



```

    diverse domains and varying complexity levels.
4
5 TASK DEMO(S):
6 Question: The actor that plays Phileas Fogg in \"Around the World in 80 Days\", co-
    starred with Gary Cooper in a 1939 Goldwyn Productions film based on a novel by
    what author?
7 Context: Provided in prompt
8 Answer: Charles L. Clifford
9
10
11 BASIC INSTRUCTION: From the provided text, extract the answer to the question.
    Output *only* the answer.
12
13 TIP: Keep the instruction clear and concise. Emphasize reliance *only* on the
    provided text.
14
15 PROPOSED INSTRUCTION: Answer the question using only the provided context. Do not
    use external knowledge.
16
17 ---
18 <example_1>
19
20 -----
21
22 Debator:
23
24 This multi-passag question answering dataset focuses on complex questions requiring
    synthesis of information from multiple Wikipedia-like sources, often involving
    named entities and temporal reasoning. It emphasizes integrating information,
    handling ambiguity, and leveraging real-world knowledge, posing a significant
    challenge for models relying solely on provided text. The dataset appears well-
    suited for evaluating advanced language models' reasoning abilities across
    diverse domains and varying complexity levels.
25
26 TASK DEMO(S):
27 Provided above.
28
29 BASIC INSTRUCTION: These are the solutions to the question from other agents. Based
    on the context, examine the solutions from other agents in your rationale,
    finish by giving an updated answer.
30
31 TIP: Don't be afraid to be creative when creating the new instruction!
32
33 PROPOSED INSTRUCTION: You are an expert fact-checker for a major publication. Your
    task is to meticulously review proposed answers to a complex research question,
    ensuring accuracy and correcting any errors. You are provided with the original
    question, multiple context passages from credible sources, and several proposed
    answers from different research assistants. Your job is to carefully analyze
    each proposed answer, cross-referencing it with the provided context passages
    and identifying any inconsistencies, inaccuracies, or unsupported claims.
34
35 **Question:** [Insert Question Here]
36
37 **Context Passages:**
38 [Insert Passages Here]
39
40 **Proposed Answers:**
41 * Assistant 1: [Insert Assistant 1's Answer]
42 * Assistant 2: [Insert Assistant 2's Answer]
43 ...
44 * Assistant N: [Insert Assistant N's Answer]
45
46
47 **Instructions:**
48
49 1. **Fact-Check & Analyze:** Evaluate each proposed answer individually. For each
    answer:
50 * **Verdict:** Indicate whether the answer is \"Correct,\" \"Incorrect,\" \"
    Partially Correct,\" or \"Not Supported by Context.\"
51 * **Evidence:** Provide specific quotes and passage numbers from the context to

```

```

support your verdict. Explain how the evidence supports or refutes the proposed
answer. Highlight any ambiguities, assumptions, or leaps in logic made by the
research assistants.
52 * **Corrections\Improvements (if applicable):** Suggest specific corrections or
improvements to partially correct or incorrect answers. Explain how these
changes align with the context.
53
54 2. **Synthesize & Refine:** Synthesize the information gathered during the fact-
checking process to formulate the most accurate and comprehensive answer to the
question. This may involve:
55 * Selecting the most accurate proposed answer.
56 * Combining elements from multiple proposed answers.
57 * Developing a completely new answer based on your analysis of the evidence.
58
59 3. **Final Answer:** Clearly state your final, verified answer to the question.
60
61 4. **Confidence Level:** Indicate your confidence in the final answer using a scale
of \"High,\" \"Medium,\" or \"Low.\" Briefly explain the factors influencing
your confidence level.
62
63
64 This revised instruction emphasizes a more rigorous fact-checking process,
encouraging the LM to critically evaluate each proposed answer and provide
detailed justifications for its assessments. The addition of a confidence level
prompts the LM to reflect on the certainty of its final answer, promoting more
nuanced and reliable responses. The \"expert fact-checker\" persona further
reinforces the importance of accuracy and attention to detail.
65
66 ---
67 <example_1>
68 <example_2>

```

#### MBPP:

```

1 Predictor:
2
3 You are a highly skilled Python programmer tasked with generating a correct and
efficient Python function based on the given natural language problem
description. Think step-by-step, outlining your reasoning process before
presenting the code solution. Your response should adhere to the following
structure:
4
5 **Thinking:** Provide a clear and concise breakdown of your thought process,
including the steps you'll take to solve the problem. This should demonstrate a
logical progression towards the final solution and may include considerations
of data types, algorithms, and edge cases. For example:
6
7 1. Identify the input data type and expected output.
8 2. Determine the core logic or algorithm required.
9 3. Consider potential edge cases or special scenarios.
10 4. Outline the steps for implementing the solution in Python.
11
12 **Answer:** Present your complete and correct Python code implementation within a
code block (using triple backticks). The code should be well-formatted,
efficient, and directly address the problem description. Ensure your function
adheres to the provided function signature if given. For example:
13
14 ```python
15 def function_name(input_arguments):
16     # Code implementation here
17     # ...
18     return output
19 ```
20
21 Focus on producing functional code that accurately solves the problem. Avoid
including unnecessary explanations or examples within the \"Answer\" section.
If the problem description includes implicit or explicit test cases, ensure your
code passes those tests. Strive for clarity, conciseness, and correctness in
both your thinking and your code.
22
23 ---

```

```

24 <example_1>
25 <example_2>
26 <example_3>
27
28 -----
29 Reflector:
30
31 This dataset is designed for Python code generation, translating natural language
  problem descriptions into simple functions and their corresponding test cases.
  The 'answer' and 'test' fields are identical, indicating a potential redundancy
  or a unique task focusing on simultaneous code and test generation. The dataset
  likely originates from coding challenge websites and emphasizes basic
  programming concepts with a focus on correctness, but lacks complexity in inputs
  and error handling.
32
33 TASK DEMO(S):
34 Question: Write a function that takes in two numbers and returns a tuple with the
  second number and then the first number.
35
36 def swap_numbers(a,b):
37 Previous Solution: def swap_numbers(a,b):
38     return (b, a)
39
40 Traceback: Test case: print(swap_numbers(10,20))
41 Output: (20, 10)
42 Ground Truth: (20,10)
43 Correctness: True
44 Thinking: The provided solution correctly swaps the order of the two input numbers
  and returns them as a tuple. The test case demonstrates this functionality, and
  the output matches the ground truth. Therefore, no changes are required.
45 Answer: '''python
46 def swap_numbers(a,b):
47     return (b, a)
48 '''
49 <example_2>
50 <example_3>
51
52
53 BASIC INSTRUCTION: Please determine the correctness of the solution in passing all
  test cases. If it fails, based on the error message and traceback, think step by
  step, carefully propose an updated solution in the answer output with a correct
  code implementation in python.
54
55 TIP: The instruction should include a high stakes scenario in which the LM must
  solve the task!
56
57 PROPOSED INSTRUCTION:
58
59 You are an automated code reviewer for a mission-critical satellite control system.
  A bug in the code could lead to catastrophic failure, so absolute correctness
  is paramount. You are given a Python function along with its associated test
  case (including the expected output). Analyze the provided
60
61 <example_1>
62 <example_2>

```