NOV 15, 2007

RM:= 3/ span of irred. characters
of sm

/ So:= 213

13:= DR M (So:= 213

product on R
Sn+m

 $f \cdot g = \operatorname{Ind}_{S_{m}^{m} \times S_{m}} (f \times g)$

fer, germ.

4. Sn -> 1/2 - Pi 1/2 ...

THM chi R -> 1 isomorphism

 $f \in \mathbb{R}^{n}$ $ch(f) := \langle f, \psi \rangle_{S_{N}}$

 $= \frac{1}{\sqrt{1-\alpha}} \frac{1}{\alpha \in S^{N}} f(\alpha) \beta^{\alpha}$

$$\begin{aligned}
&= \sum_{a \neq b} f(g) \, p \\
&$$

20 = 1 Stabs (8) 1

has cardinality conjugary class of type s

be the tainfal character of Sm

 $\sum_{p} \frac{1}{2} p_{p} = h_{m}$ ch (9m)=

nu + Ra

121= ~ $\lambda = (\lambda_1, \lambda_2, \dots)$

 $h_{\lambda} = h_{\lambda_1} h_{\lambda_2} \cdots$

hx = ch (7x, 7x2 ")

RM 7 Mind Shi "She " = Sm

Mind to Shithetic = Sm

Let $\chi^{\lambda} \in \mathbb{R}^{n}$ s.t. concretely $\chi^{\lambda} := det \left(\begin{array}{c} \chi^{\lambda} \\ \chi^{\lambda} := det \end{array} \right)$ Jawbi Trudi claim x à is an irreducible $u = |\lambda|$ character of Sa Pf we check $\cdot < \chi^{\lambda}, \lambda^{\lambda} > = 1$ $\chi^{\lambda}(1)>0$

 $\langle x^{\lambda}, x^{\mu} \rangle_{x} = \langle ch(x^{\lambda}), ch(x^{\mu}) \rangle$ $|\lambda| = |\mu| = n$ $\chi^{\lambda}, \chi^{\mu} \in R^{\mu} = \delta_{\lambda \mu}$

2 2h3 or thonormal basis (same cardinality as rank of R" i.e. p(m) = # partitions of m)

$$S_{\lambda} = ch(\chi^{\lambda})$$

$$= \sum_{s} \frac{1}{2^{s}} \chi_{s}^{\lambda} P_{s}^{s}$$

xx := value of xx at a of Sn of cycle type p

i.e. character table of Su gives
The transition matrix (charge of
basis) between pp and sh
want to show

X1m

2

$$\chi_{1m}^{\lambda} = \langle S_{\lambda}, h_{1m} \rangle$$

+ sort the relation

$$\int_{B_{g}} = \sum_{\lambda} \chi_{\lambda}^{\lambda} S_{\lambda}$$

$$p_1 = p_1^n = \sum_{\lambda} \chi_1^{\lambda} S_{\lambda}$$

$$S_{\lambda} = \frac{\alpha_{\lambda} + s/\alpha_{s}}{\alpha_{s}}$$

$$= \sum_{i=1}^{\infty} x_{i} \hat{x}_{i}^{*} = \sum_{\lambda} x_{i}^{\lambda} \hat{x}_{i}^{*} = \sum_{\lambda} x_{i}^{\lambda} \hat{x}_{i}^{*} = \sum_{\lambda} x_{i}^{*} \hat{x}$$

$$a_{\lambda + \delta} = \sum_{\sigma} \epsilon(\sigma) \times \delta(\lambda + \delta)$$

$$a_{\lambda + \delta} = \sum_{\sigma} \lambda + \delta + \cdots$$

$$\chi_{n}^{\lambda} = \left[\alpha_{s} \cdot \left(\sum_{i=1}^{n} x_{i} \right)^{n} \right]_{\lambda+s}$$

$$A=B$$

$$\sum_{k=0}^{\infty} (2^k)^k = (2^k)$$

$$(x + x^{-1})^{2^{4}} = (x + x^{-1})^{3} (x + x^{-1})^{3}$$

constant weff. 2n
$$R(2n) \times (2n-k)$$

lhs = $R=0$
 $R=0$
 $R=0$
 $R=2n-k$

$$K = 0$$

$$K = 2n - K$$

$$Const. term = {2n \choose n}$$

$$K = n$$

term.

$$\sum_{k=j}^{k} {\binom{n}{k}}^2$$

$$= \sum_{k=j}^{k} {\binom{n}{k}}^2$$

$$\chi_{i,m}^{l} = \left[\begin{array}{c} \omega & TT(x_{i},-x_{i},) \left(\sum\limits_{j=1}^{m} x_{i} \right)_{j} \right]^{\gamma+1} \\ \omega & \sum\limits_{j=1}^{m} \left(\sum\limits_{j=1}^{m} x_{i} \right)_{j} \end{array}$$

$$\left(\sum_{i=1}^{n} X_{i}^{i}\right)^{n} = \sum_{k=1}^{n} \frac{x_{1}^{i} \dots x_{m}^{k}}{x_{1}^{i} \dots x_{m}^{k}}$$

$$k_1,...,k_n > 0$$
 $k_1 + + k_n = m$
 $k = (k_1, k_2,...,k_n)$

$$\alpha^2 = \sum_{\epsilon(e)} \sum_{\alpha(g)}$$

$$\chi_{i}^{\lambda} = \frac{\sum_{i=1}^{N_i} \frac{M_i - M_i - K(i')}{\prod_{i=1}^{N_i} (M_i - M_i + \sigma(i'))!}$$

$$\mu! := \mu_1! \mu_2! \cdots \mu_n!$$

$$= \frac{n!}{\mu!} \det \left(\mu_i(\mu_{i-1}) \cdots (\mu_{i-n+j+1}) \right)$$

$$\frac{\mu_{i}!}{(\mu_{i}+m+j)!} = \mu_{i}(\mu_{i}-1)\cdots(\mu_{i}-m+j+1)$$

highest dog in pic is m-1

 $\chi_{1m}^{\lambda} = \frac{n!}{m!} TT(\mu_i - \mu_i)$ $\tauoking the malle the mall$

operations
to kill off
smaller des
terms in
each entry

 $-\chi^{(m)}=\eta_m$ tainial charof S_m

 $\chi^{(i^n)} = \epsilon_n$ sign repn.

TITO (taisial

目 59~

 $\chi^{\lambda'} = \varepsilon \chi^{\lambda}$

 $\chi_{\lambda'} = \langle S_{\lambda'}, \gamma_{\lambda} \rangle$

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i.e. w G/m corresponds to melyphication by sgm = &

- GC 50 26 (P1, P2,...) = ch (XG) XG = Indc (1)