### CS1010X — Programming Methodology School of Computing National University of Singapore

# **Midterm Test**

26 March 2022				T	ime a	llowe	ed: 2 hou	ırs
Chu dont No.								
Student No:								

# Instructions (please read carefully):

- 1. Write down your student number on the **question paper**. DO NOT WRITE YOUR NAME ON THE QUESTION PAPER!
- 2. This is an open-book test.
- 3. Please switch off your mobile phone, and no laptop and no calculator. If found using any of these equipment any moment from now till your scripts have been collected, you will be given a zero mark.
- 4. This paper comprises **FIVE** (5) **questions** and **NINE** (9) **pages**. The time allowed for solving this test is 2 hours.
- 5. The maximum score of this test is **32 marks**. The weight of each question is given in square brackets beside the question number.
- 6. All questions must be answered in the space provided in this question paper. If you write something important as your answer outside the space provided, please make clear with some marking. At the end of the test, please submit your question paper only. No extra sheets will be accepted as answers.
- 7. You are allowed to use pencils. Please be sure your handwriting is legible and neat, and you have proper indentation as needed for your Python codes to avoid misinterpretation.

# **GOOD LUCK!**

Question	Marks
Q1	
Q2	
Q3	
Q4	
Q5	
Total	

## Question 1: Warming Up [5 marks]

**A.** For the following Python code (note that nested-if condition in a lambda function is valid still), write the output of the print statement. [2 marks]

```
z = lambda x: 1 if (x < 0 or x > 10) else (2 if x%2==0 else 3)
def f(a, b):
    sum = 0
    for i in range(a, b):
        sum += z(i)
    return sum

print(f(-6,16))
```

Ans:

**B.** For the following Python code, write the outputs (3 lines in total) of the print statements. [3 marks]

```
t = (1,2,3,4)
lst = [66, 77]
def gn(c):
    c[0] = [88]
    c[1][1] = 55
    return
def fn( a, b ):
    m = [ a, b ]
    a = b
    gn(m)
    return m

r = fn(t, lst)
print(t)
print(lst)
print(r)
```

Ans:	

# Question 2: Something familiar first [4 marks]

```
def compose(f, g):
     return lambda x:f(g(x))
 def twice(f):
     return compose(f, f)
def thrice(f):
     return compose(f, compose(f, f))
def repeated(f, n):
     if n == 0:
         return identity
         return compose(f, repeated(f, n - 1))
 add1 = lambda x: x + 1
 identity = lambda x: x
Given the above familiar codes, you are to write out the output of each given print
statement. Each part is 1 mark.
 print (twice (thrice) (add1) (1))
Ans:
print (twice (thrice) (twice) (add1) (1))
Ans:
print (thrice (twice) (thrice (add1)) (1))
Ans:
 print (twice (thrice) (repeated (thrice (add1), 100)) (1))
Ans:
```

### Question 3: Not really unfamiliar [10 marks]

**A.** You are given the following python code that works with input of two tuples s and t, of the same length.

Suppose we run the above code with the following 3 statements:

```
t = (0, 0, 0, 0, 1, 1, 1, 2, 3, 3, 4, 4, 4, 4, 4, 5, 5)

s = (1, 2, 1, 4, 2, 3, 4, 4, 2, 3, 4, 4, 4, 4, 4, 9, 10)

print(unknown(s, t))
```

What is the output from the print statement?

[3 marks]

Ans:

Explanation (if any to assist with understanding your thinking about the purpose of the code - good for receiving partial credit if your answer may not be completely correct):

What is the time and space complexity of the unknown function in terms of the length n of the tuple s and t. (Note that t is always in the form that  $t[i] \le t[j]$  for i < j. This information is not needed here for your analysis but just in case you have query on t.) A correct but too big an upper bound will not receive any credit. [3 marks]

```
Time:
Space:

Justification (for time and for space):
```

#### В.

What is the time and space complexity of the puzzle function in terms of the input n. A correct but too big an upper bound will not receive any credit. [4 marks]

Time:
Space:
Institution (for time and for one sa).
Justification (for time and for space):

## **Question 4: Counting Squares in Grid [4 marks]**

Given a square grid of size n by n, we want to write a program to count the total number of squares of size 1 by 1 (there are  $n \times n$  of them), size 2 by 2 (depending on n), and so on until size of n by n (just 1 such big square). This is in the same spirit as the familiar House of Cards problem we know: instead of counting triangles in House of Cards, we are counting squares here.

For a 1 by 1 grid, there is just 1 square in the grid.

For a 2 by 2 grid, there are 4 squares of size 1 by 1, and 1 square of size 2 by 2, for a total of 5 squares in the grid.

For a 3 by 3 grid, there are 9 squares of size 1 by 1, 4 squares of size 2 by 2, and 1 square of size 3 by 3, for a total of 14 squares in the grid.

For a 4 by 4 grid, what is the total number of squares we can find?	[1 marks]
Ans:	

Now you can write a recursive program to do the count on the total number of squares for a grid of size n by n. It is possible that there might be a closed form formula here to state the total number of squares, but you are not supposed to use any formula but simple recursive thinking to solve this question. Do provide simple explanation of your recursive thinking too. [3 marks]

<pre>def num_sq_given_grid_of(n):</pre>
Provide simple explanation of your recursive thinking here:

### **Question 5: Higher Order Functions [9 marks]**

You will be working with the following higher-order functions sumT and foldT which are similar to the sum and fold as given in our lessons but now working on tuples. (To simplify our questions to produce numbers, we set the base cases in both functions to return 0 instead of their usual tuple or f(0).)

```
def sumT(t, term, next):
    if t == ():
        return 0
    else:
        return term(t) + sumT( next(t), term, next)

def foldT(t, op, f):
    if t == ():
        return 0
    else:
        return op( f(t), foldT( t[:-1], op, f) )
```

**A.** The function alt\_sum\_sq takes an input tuple t (of numbers) to compute the alternating sum of the square of each term in t. That is, the output is:

$$\sum_{i=0}^{len(\texttt{t})-1} (\texttt{t}[i])^2 \cdot (-1)^i$$

Example execution:

```
>>> alt_sum_sq( (6,7,8) ) # = 6*6 - 7*7 + 8*8
51
>>> alt_sum_sq( (6,7,8,9) ) # = 6*6 - 7*7 + 8*8 - 9*9
-30
```

We can define alt\_sum\_sq with sumT as follows:

```
def alt_sum_sq( t ):
    return sumT( t, <T1>, <T2> )
```

Please provide possible lambda functions for <T1> and <T2>. We reserve the right to give no credit if your <T1> and <T2> do not match up to give a correct thinking to solve the problem. For example, no credit could be given when either <T1> or <T2> is left unanswered. [3 marks]

```
<T1>:
[2 marks]

<T2>:
[1 marks]
```

We can also define alt\_sum\_sq with foldT as follows:

```
def alt_sum_sq( t ):
    return foldT( t, <T1>, <T2> )
```

Please provide possible lambda functions for <T1> and <T2>. As in the above, we reserve the right to give no credit if your <T1> and <T2> do not match up to give a correct thinking to solve the problem. [3 marks]

```
<T1>:
[1 marks]

<T2>:
[2 marks]
```

**B.** Given two tuples of the same length, t and p, suppose we want to do the computation as follows:

```
def position_sum(t, p):
    result = 0
    for i in range(0, len(t)):
        result = result + t[i]*p[i]
    return result
```

Instead of the above simple code, we want to exercise our skill working with higher order functions to achieve the same computation. We need to do this in two parts where the first is a helper function to process the input t and p into a suitable format that you can use in <code>sumT</code> and <code>foldT</code> but you are NOT to do the calculation (this means multiplication) belonging to <code>sumT</code> and <code>foldT</code>. If you have trouble with writing this function, you should at least provide description on what your helper function is supposed to produce so that your solution in the next part can make some sense still. [1 marks]

```
def helper ( t, p ):
#
# IMPORTANT: You are to write simple iterative or recursive program WITHOUT
# the use of any other Python built-in functions (eg. accumulate, map, etc)
# You may use len function to check the length of a tuple. Also note that
# helper function is to arrange the items of t and p in some way without
# doing multiplication belonging to sumT and foldT.
```

The next step is the actual use of sumT or foldT. You can choose to do with either one. Please **DO NOT ANSWER BOTH** as we will only mark the first non-empty version if you do both.

The version with sumT is as follows:

```
def position_sum( t, p ):
    return sumT ( helper(t, p), <T1>, <T2> )
```

Please provide possible lambda functions for <T1> and <T2>. As before, we reserve the right to give no credit if your <T1> and <T2> plus the helper function do not match up to give a correct thinking to solve the problem. [2 marks]

<t1>: [1 marks]</t1>	
<t2>: [1 marks]</t2>	

If you have done the above with sumT for position\_sum, please ignore the following with foldT. Otherwise, please proceed to do the following with foldT:

```
def position_sum( t, p ):
    return foldT( helper(t, p), <T1>, <T2> )
```

Please provide possible lambda functions for <T1> and <T2>. As before, we reserve the right to give no credit if your <T1> and <T2> plus the helper function do not match up to give a correct thinking to solve the problem. [2 marks]

<t1>: [1 marks]</t1>	
<t2>: [1 marks]</t2>	

- END OF PAPER -