

Nested sampling with peers



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Abstract

A nested sampling algorithm is a Bayesian approach to computing and comparing models and generating samples from posterior distributions. We introduce a general Monte Carlo method based on Nested Sampling, which name is Nested Sampling with peers, this method generates one particle above the threshold from the last iteration by querying the params from the server and updating it. We describe the new method over a test case and find that it has better accuracy than the original MCMC-based nested sampling with the same computational overhead. Put your abstract here. The abstract should contain a brief summary of the aim, methodologies, finding and conclusions of the dissertation. The abstract should normally be fewer than 350 words.

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Chapter 1

Introduction

1.1 Bayesian Analysis

The Bayesian Analysis problem is in fact a parameter estimation problem, The term *parameter* means *unknown quantity*, however in real world, we don't have enough information to decide a quantity, so we need Bayesian Analysis to help us. The parameter you interested in are denoted by θ , to estimate them, first of all, you need to model a probability distribution on the *hypothesis space*, a *hypothesis space* is the collection of possibilities, this means that you are modeling the initial assumptions, and the probability distribution is called the *prior*, it is the distribution of θ . The data set is called D , after that we can use Bayes' Theorem to determine the *posterior distribution*:

$$p(\theta|D) = \frac{p(\theta)p(D|\theta)}{p(D)} \quad (1.1)$$

in the above equation,

1. $p(\theta|D)$ is the posterior distribution, the conditional distribution of θ given the observed data, D .
2. $p(\theta)$ is prior distribution specified based on prior assumptions or information
3. $p(D|\theta)$ is the likelihood which refers to the conditional probability of observing the data
4. $p(D)$ is the marginal likelihood (or evidence) that refers to the probability of D regardless of the values of θ .

1.1.1 Marginal Likelihood**1.2 Nested Sampling****1.3 Distributed System****1.3.1 BONIC****1.4 Spakslab Problem**

Chapter 2

Implementation

We first show some simple examples of mathematical formulae using latex typesetting.

1. The basic functions: $\cos(x), \sin(x), \ln(x)$, (`\cos (x) , \sin (x) , \ln (x) $`).
2. Greek letters: $\alpha\beta\gamma\delta\epsilon\dots$ (`\alpha\beta\gamma\delta\epsilon\dots $`).
3. Mathematical symbols: $\int \oint \sum \lim \bigcup \bigcap$ (`\int \oint \sum \lim \bigcup \bigcap $`).
4. Fractions: $\frac{1}{2}, \frac{1}{2-x}$ (`\frac{1}{2} , \frac{1}{2-x} $`).

The following matrix

$$\begin{bmatrix} U_r & r & W_r \\ 0 & 1 & V_x \\ 0 & 0 & W_x \end{bmatrix}, \quad (2.1)$$

is generated using the `equarray` environment:

```
\begin{equarray}\label{eqn:matrix}
\left[
\begin{array}{ccc}
U_{r}& r & W_{r}\\
0 & 1 & V_{x}\\
0 & 0 & W_{x}
\end{array}
\right],
\end{equarray}
```

The `\label{eqn:matrix}` command labels the equation with `{eqn:matrix}` which can be referred to somewhere else in the text by using `\ref{eqn:matrix}` or `\eqref{eqn:matrix}`.

The command `\notag` eliminates the numbering of the first equation,

$$\begin{aligned}\lambda^{(1)} &= \text{tr}[T^{(1)}P], \\ \lambda^{(2)} &= \text{tr}[T^{(2)}P - T^{(1)}ST^{(1)}P].\end{aligned}\tag{2.2}$$

```
\begin{eqnarray} \label{eqn:lambda_trace} \\ \lambda^{(1)}&=&\text{tr}[T^{(1)}P], \notag \\ \lambda^{(2)}&=&\text{tr}[T^{(2)}P - T^{(1)}ST^{(1)}P]. \\ \end{eqnarray}
```

2.0.1 Itemized lists

Example of an itemized list:

- muscle and fat cells remove glucose from the blood,
- cells use glucose for protein synthesis.

```
\begin{itemize} \\ \item muscle and fat cells remove glucose from the blood, \\ \item cells use glucose for protein synthesis. \\ \end{itemize}
```

This can be done by an enumerated list:

1. muscle and fat cells remove glucose from the blood,
2. cells use glucose for protein synthesis.

```
\begin{enumerate} \\ \item muscle and fat cells remove glucose from the blood, \\ \item cells use glucose for protein synthesis. \\ \end{enumerate}
```

2.0.2 Inserting figures

You may save your Matlab figures as jpg files. Figures should be stored in the same folder as the latex files. For the graphicx package to work you usually need to ask latex to create a pdf file (e.g., command `pdflatex` or `latexpdf`).

An example of an inserted image is given in Figure 2.1.

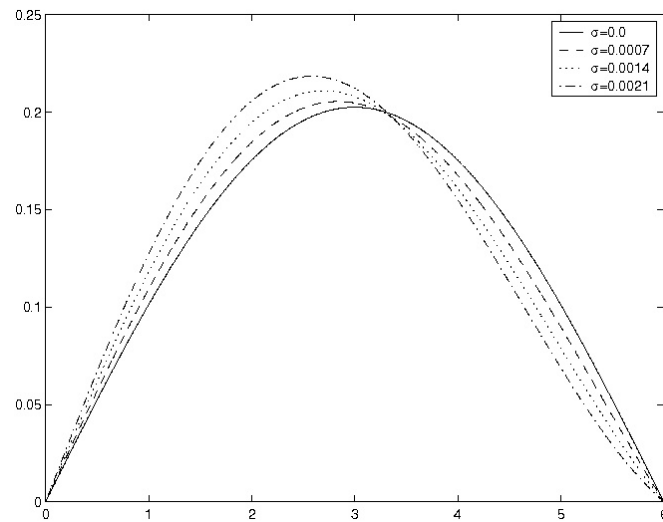


Figure 2.1: Mode shapes

2.0.3 Tables

Example of a table,

Gene	GeneID	Length
human latexin	1234	14.9 kbps
mouse latexin	2345	10.1 kbps
rat latexin	3456	9.6 kbps

Table 2.1: **title of table** - Overview of latexin genes.

```
\begin{table}[htp]
\centering
\begin{tabular}{ccc}
```

```
% ccc means 3 columns, all centered; alternatives are l, r
{\bf Gene} & {\bf GeneID} & {\bf Length} \\
\hline % draws a line under the column headers
human latexin & 1234 & 14.9 kbps \\
mouse latexin & 2345 & 10.1 kbps \\
rat latexin   & 3456 & 9.6 kbps \\
\end{tabular}
\caption[title of table]{\textbf{title of table} - Overview of latexin genes.}
\label{latexin_genes} % label for cross-links with \ref{latexin_genes}
\end{table}
```

See how to add two vertical lines in the table (Simply change {ccc} to {c|c|c})

Gene	GeneID	Length
human latexin	1234	14.9 kbps
mouse latexin	2345	10.1 kbps
rat latexin	3456	9.6 kbps

Table 2.2: **title of table** - Overview of latexin genes.

2.0.4 How to Refer to Equations, Sections, etc

- References can be linked to equations, figures, tables or sections using the command `\ref`: Equation (2.2), Figure 2.1, Table 2.2 and Section 2.0.3.
Equation~(\ref{eqn:lambda_trace}), Figure~\ref{modes},
Table~\ref{latexin_genes2} and Section~\ref{table}.
- Equations can be conveniently referred to using `\eqref`. See, for example, Equation (2.2).
Equation \eqref{eqn:lambda_trace}
Note that `\eqref` includes the round brackets by itself.
- Citations are in a similar way but using the command `\cite`:
[2], [3], and [4], or [2, 3, 4] .

```
\cite{Salmond}, \cite{Stull}, and \cite{TandC},
or \cite{Salmond,Stull,TandC} .
```

There are many different styles for writing citations – you should follow the norms for your subject area.

A more advanced way to do citations is to use `bibtex`. This is a powerful tool and we encourage you to try it. There is plenty of information about it on the web.

Chapter 3

Methodologies and analysis

3.1 Methodologies

3.2 Analysis

Chapter 4

Discussion

4.1 Main results

4.2 Discussion

Chapter 5

Conclusions

You may add more chapters as needed in the file.

References

- [1] Farge Marie, *Wavelet Transforms and Their Applications to Turbulence*, Ann. Rev. Fluid Mech. volume 24, pages 395-457, 1992.
- [2] Salmond Jennifer, *Vertical Mixing of Ozone in the Very Stable Nocturnal Boundary Layer*, PhD Thesis, University of British Columbia, 2001.
- [3] Stull B. Ronald, *Introduction to Boundary Layer Meteorology*, Dordrecht; Boston: Kluwer Academic Publishers, 1988.
- [4] Torrence Christopher, Compo Gilbert P., *A Practical Guide to Wavelet Analysis*, Bulletin of the American Meteorological Society volume 79, pages 61-78, 1998.

Appendix A

Some extra things

This is an optional chapter for any additional material that does not fit conveniently into the body of the text (e.g., data, copies of computer programmes). Note that appendices won't necessarily be marked.