

# pst-3d basic three dimension functions

February 14, 2010

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Thanks to:		This	version	of pst-3d	uses th	e extended	keyval	handling	of pst-xkey	•
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# 1 PostScript functions SetMatrixThreeD,ProjThreeD, and SetMatrixEmbed

The viewpoint for 3D coordinates is given by three angles:  $\alpha$ ,  $\beta$  and  $\gamma$ .  $\alpha$  and  $\beta$  determine the direction from which one is looking.  $\gamma$  then determines the orientation of the observing.

When  $\alpha$ ,  $\beta$  and  $\gamma$  are all zero, the observer is looking from the negative part of the y-axis, and sees the xz-plane the way in 2D one sees the xy plan. Hence, to convert the 3D coordinates to their 2D project,  $\langle x, y, z \rangle$  map to  $\langle x, z \rangle$ .

When the orientation is different, we rotate the coordinates, and then perform the same projection.

We move up to latitude  $\beta$ , over to longitude  $\alpha$ , and then rotate by  $\gamma$ . This means that we first rotate around y-axis by  $\gamma$ , then around x-axis by  $\beta$ , and the around z-axis by  $\alpha$ .

Here are the matrices:

$$R_{z}(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R_{x}(\beta) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \beta & \sin \beta \\ 0 & -\sin \beta & \cos \beta \end{bmatrix}$$

$$R_{y}(\gamma) = \begin{bmatrix} \cos \gamma & 0 & -\sin \gamma \\ 0 & 1 & 0 \\ \sin \gamma & 0 & \cos \gamma \end{bmatrix}$$

The rotation of a coordinate is then performed by the matrix  $R_z(\alpha)R_x(\beta)R_y(\gamma)$ . The first and third columns of the matrix are the basis vectors of the plan upon which the 3D coordinates are project (the old basis vectors were <1,0,0> and <0,0,1>; rotating these gives the first and third columns of the matrix).

These new basis vectors are:

$$\tilde{x} = \begin{bmatrix} \cos \alpha \cos \gamma - \sin \beta \sin \alpha \sin \gamma \\ \sin \alpha \cos \gamma + \sin \beta \cos \alpha \sin \gamma \\ \cos \beta \sin \gamma \end{bmatrix}$$

$$\tilde{z} = \begin{bmatrix} -\cos \alpha \sin \gamma - \sin \beta \sin \alpha \cos \gamma \\ -\sin \alpha \sin \gamma + \sin \beta \cos \alpha \cos \gamma \\ \cos \beta \cos \gamma \end{bmatrix}$$

Rather than specifying the angles  $\alpha$  and  $\beta$ , the user gives a vector indicating where the viewpoint is. This new viewpoint is the rotation of the old viewpoint. The old viewpoint is <0,-1,0>, and so the new viewpoint is

$$R_z(\alpha)R_x(\beta) \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} \cos\beta\sin\alpha \\ -\cos\beta\cos\alpha \\ \sin\beta \end{bmatrix} = \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}$$

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Therefore,

```
\alpha = \arctan(v_1/-v_2)

\beta = \arctan(v_3 \sin \alpha/v_1)
```

Unless  $p_1 = p_2 = 0$ , in which case  $\alpha = 0$  and  $\beta = \text{sign}(p_3)90$ , or  $p_1 = p_3 = 0$ , in which case  $\beta = 0$ .

The syntax of SetMatrixThreeD is  $v_1$   $v_2$   $v_3$   $\gamma$  SetMatrixThreeD SetMatrixThreeD first computes

```
a = \sin \alpha b = \cos \alpha

c = \sin \beta d = \cos \beta

e = \sin \gamma f = \cos \gamma
```

and then sets Matrix3D to  $[\tilde{x}\ \tilde{z}].$ 

```
/SetMatrixThreeD {
   dup sin /e ED cos /f ED
   /p3 ED /p2 ED /p1 ED
   p1 0 eq
   { /a 0 def /b p2 0 le { 1 } { -1 } ifelse def
     p3 p2 abs
   { p2 0 eq
     { /a p1 0 lt { -1 } { 1 } ifelse def /b 0 def
      p3 p1 abs
11
     { p1 dup mul p2 dup mul add sqrt dup
      p1 exch div /a ED
13
      p2 exch div neg /b ED
      p3 p1 a div
15
16
     }
     ifelse
17
18
19
   ifelse
   atan dup sin /c ED cos /d ED
20
   /Matrix3D
21
22
     b f mul c a mul e mul sub
23
     a f mul c b mul e mul add
24
     d e mul
     b e mul neg c a mul f mul sub
26
     a e mul neg c b mul f mul add \,
     d f mul
28
   ] def
```

The syntax of ProjThreeD is  $x\ y\ z$  ProjThreeD  $x'\ y'$  where  $x'=< x,y,z>\cdot \tilde{x}$  and  $y'=< x,y,z>\cdot \tilde{z}.$ 

```
/ProjThreeD {
/z ED /y ED /x ED
```

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```
Matrix3D aload pop

z mul exch y mul add exch x mul add

4 1 roll

z mul exch y mul add exch x mul add

exch

exch

def
```

To embed 2D < x,y> coordinates in 3D, the user specifies the normal vector and an angle. If we decompose this normal vector into an angle, as when converting 3D coordinates to 2D coordinates, and let  $\hat{\alpha}$ ,  $\hat{\beta}$  and  $\hat{\gamma}$  be the three angles, then when these angles are all zero the coordinate < x,y> gets mapped to < x,0,y>, and otherwise < x,y> gets mapped to

$$R_z(\hat{\alpha})R_x(\hat{\beta})R_y(\hat{\gamma}) \begin{bmatrix} x \\ 0 \\ y \end{bmatrix} = \begin{bmatrix} \hat{x}_1x + \hat{z}_1y \\ \hat{x}_2x + \hat{z}_2y \\ \hat{x}_3x + \hat{z}_3y \end{bmatrix}$$

where  $\hat{x}$  and  $\hat{z}$  are the first and third columns of  $R_z(\hat{\alpha})R_x(\hat{\beta})R_y(\hat{\gamma})$ .

Now add on a 3D-origin:

$$\begin{bmatrix} \hat{x}_1 x + \hat{z}_1 y + x_0 \\ \hat{x}_2 x + \hat{z}_2 y + y_0 \\ \hat{x}_3 x + \hat{z}_3 y + z_0 \end{bmatrix}$$

Now when we project back onto 2D coordinates, we get

$$x' = \tilde{x}_{1}(\hat{x}_{1}x + \hat{z}_{1}y + x_{0}) + \tilde{x}_{2}(\hat{x}_{2}x + \hat{z}_{2}y + y_{0}) + \tilde{x}_{3}(\hat{x}_{3}x + \hat{z}_{3}y + z_{0})$$

$$= (\tilde{x}_{1}\hat{x}_{1} + \tilde{x}_{2}\hat{x}_{2} + \tilde{x}_{3}\hat{x}_{3})x$$

$$+(\tilde{x}_{1}\hat{z}_{1} + \tilde{x}_{2}\hat{z}_{2} + \tilde{x}_{3}\hat{z}_{3})y$$

$$+\tilde{x}_{1}x_{0} + \tilde{x}_{2}y_{0} + \tilde{z}_{3}z_{0}y' = \tilde{z}_{1}(\hat{x}_{1}x + \hat{z}_{1}y + x_{0}) + \tilde{z}_{2}(\hat{x}_{2}x + \hat{z}_{2}y + y_{0}) + \tilde{z}_{3}(\hat{x}_{3}x + \hat{z}_{3}y + z_{0})$$

$$= (\tilde{z}_{1}\hat{x}_{1} + \tilde{z}_{2}\hat{x}_{2} + \tilde{z}_{3}\hat{x}_{3})x$$

$$+(\tilde{z}_{1}\hat{z}_{1} + \tilde{z}_{2}\hat{z}_{2} + \tilde{z}_{3}\hat{z}_{3})y$$

$$+\tilde{z}_{1}x_{0} + \tilde{z}_{2}y_{0} + \tilde{z}_{3}z_{0}$$

Hence, the transformation matrix is:

$$\begin{bmatrix} \tilde{x}_{1}\hat{x}_{1} + \tilde{x}_{2}\hat{x}_{2} + \tilde{x}_{3}\hat{x}_{3}) \\ \tilde{z}_{1}\hat{x}_{1} + \tilde{z}_{2}\hat{x}_{2} + \tilde{z}_{3}\hat{x}_{3}) \\ \tilde{x}_{1}\hat{z}_{1} + \tilde{x}_{2}\hat{z}_{2} + \tilde{x}_{3}\hat{z}_{3}) \\ \tilde{z}_{1}\hat{z}_{1} + \tilde{z}_{2}\hat{z}_{2} + \tilde{z}_{3}\hat{z}_{3}) \\ \tilde{x}_{1}x_{0} + \tilde{x}_{2}y_{0} + \tilde{z}_{3}z_{0} \\ \tilde{z}_{1}x_{0} + \tilde{z}_{2}y_{0} + \tilde{z}_{3}z_{0} \end{bmatrix}$$

The syntax of SetMatrixEmbed is  $x_0$   $y_0$   $z_0$   $\hat{v_1}$   $\hat{v_2}$   $\hat{v_3}$   $\hat{\gamma}$   $v_1$   $v_2$   $v_3$   $\gamma$  SetMatrixEmbed

SetMatrixEmbed first sets <x1 x2 x3 y1 y2 y3> to the basis vectors for the view-point projection (the tilde stuff above). Then it sets Matrix3D to the basis vectors for the embedded plane. Finally, it sets the transformation matrix to the matrix given above.

```
1 /SetMatrixEmbed {
```

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```
SetMatrixThreeD
   Matrix3D aload pop
   /z3 ED /z2 ED /z1 ED /x3 ED /x2 ED /x1 ED
   SetMatrixThreeD
   Matrix3D aload pop
   z3 mul exch z2 mul add exch z1 mul add 4 1 roll
   z3 mul exch z2 mul add exch z1 mul add
   Matrix3D aload pop
   x3 mul exch x2 mul add exch x1 mul add 4 1 roll
11
   x3 mul exch x2 mul add exch x1 mul add
   3 -1 roll 3 -1 roll 4 -1 roll 8 -3 roll 3 copy
   x3 mul exch x2 mul add exch x1 mul add 4 1 roll
   z3 mul exch z2 mul add exch z1 mul add
   concat
 } def
```

# 2 Keywords

# 2.1 viewpoint

```
1  \let\pssetzlength\pssetylength
2  \define@key[psset]{pst-3d}{viewpoint}{%
3  \pst@expandafter\psset@eviewpoint#1 {} {} {} {} {} {}
4  \let\psk@viewpoint\pst@tempg}
5  \def\psset@eviewpoint#1 #2 #3 #4\@nil{%
6  \begingroup
7  \pssetxlength\pst@dima{#1}%
8  \pssetylength\pst@dimb{#2}%
9  \pssetzlength\pst@dimc{#3}%
10  \xdef\pst@tempg{%
11  \pst@number\pst@dima \pst@number\pst@dimb \pst@number\pst@dimc}%
12  \endgroup}
13  \psset[pst-3d]{viewpoint=1 -1 1}
```

# 2.2 viewangle

```
\define@key[psset]{pst-3d}{viewangle}{\pst@getangle{#1}\psk@viewangle}
\psset[pst-3d]{viewangle=0}
```

### 2.3 normal

```
1 \define@key[psset]{pst-3d}{normal}{%
2 \pst@expandafter\psset@@viewpoint#1 {} {} \@nil
3 \let\psk@normal\pst@tempg}
4 \psset[pst-3d]{normal=0 0 1}
```

2.4 embedangle

### 2.4 embedangle

```
\define@key[psset]{pst-3d}{embedangle}{\pst@getangle{#1}\psk@embedangle}
\psset[pst-3d]{embedangle=0}
```

# 3 Transformation matrix

```
/TMSave {

tx@Dict /TMatrix known not { /TMatrix { } def /RAngle { 0 } def } if end

/TMatrix [ TMatrix CM ] cvx def

def

/TMRestore { CP /TMatrix [ TMatrix setmatrix ] cvx def moveto } def

/TMChange {

TMSave

/cp [ currentpoint ] cvx def % Check this later.CM def
```

Set standard coor. system , with pt units and origin at currentpoint. This let's us rotate, or whatever, around  $T_E X$ 's current point, without having to worry about strange coordinate systems that the dvi-to-ps driver might be using.

```
1 CP T STV
```

Let  $M = old\ matrix$  (on stack), and M' equal current matrix. Then go from M' to M by applying  $M\ Inv(M')$ .

```
CM matrix invertmatrix % Inv(M')
matrix concatmatrix % M Inv(M')
```

Now modify transformation matrix:

```
1 exch exec
```

Now apply M Inv(M')

```
concat cp moveto
```

# 4 Macros

#### 4.1 \ThreeDput

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```
\pssetxlength\pst@dima{#1}%
   \pssetylength\pst@dimb{#2}%
11
   \pssetzlength\pst@dimc{#3}%
12
   \leavevmode
13
   \hbox{%
14
     \pst@Verb{%
15
        { \pst@number\pst@dima
          \pst@number\pst@dimb
17
          \pst@number\pst@dimc
          \psk@normal
19
          \psk@embedangle
          \psk@viewpoint
21
          \psk@viewangle
22
          \tx@SetMatrixEmbed
23
        } \tx@TMChange}%
     \box\pst@hbox
25
     \pst@Verb{\tx@TMRestore}}%
26
   \endgroup
27
   \ignorespaces}
```

# **5 Arithmetic**

\pst@divide This is adapted from Donald Arseneau's shapepar.sty. Syntax:

```
\pst@divide{<numerator>}{<denominator>}{<command>}
\pst@@divide{<numerator>}{<denominator>}
```

<numerator> and <denominator> should be dimensions. \pst@divide sets <command> to <num>/<den> (in points). \pst@divide sets \pst@dimg to <num>/<den>.

```
\def\pst@divide#1#2#3{%
\pst@divide{#1}{#2}%
\pst@dimtonum\pst@dimg{#3}}
\def\pst@divide#1#2{%
\pst@dimg=#1\relax
\pst@dimh=#2\relax
\pst@cntg=\pst@dimh
\pst@cnth=67108863
\pst@@divide\pst@@divide\pst@@@divide
\divide\pst@dimg\pst@cntg}
```

The number 16 is the level of uncertainty. Use a lower power of 2 for more accuracy (2 is most precise). But if you change it, you must change the repetions of \pst@@divide in \pst@@divide above:

```
precision^{repetitions} = 65536
```

```
(E.g., 16^4 = 65536).
```

```
1 \def\pst@@@divide{%
2 \ifnum
```

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```
\ifnum\pst@dimg<\z@-\fi\pst@dimg<\pst@cnth

unultiply\pst@dimg\sixt@en

else

divide\pst@cntg\sixt@en

fi}</pre>
```

\pst@pyth Syntax:

```
\pst@pyth{<dim1>}{<dim2>}{<dimen register>}
```

<dimen register> is set to  $((dim1)^2 + (dim2)^2)^{1/2}$ .

The algorithm is copied from PiCTeX, by Michael Wichura (with permission). Here is his description:

```
Suppose x>0, y>0. Put s=x+y. Let z=(x^2+y^2)^{1/2}. Then z=s\times f, where f=(t^2+(1-t)^2)^{1/2}=((1+\tau^2)/2)^{1/2} and t=x/s and \tau=2(t-1/2).
```

```
\def\pst@pyth#1#2#3{%
   \begingroup
     \pst@dima=#1\relax
     \ifnum\pst@dima<\z@\pst@dima=-\pst@dima\fi % dima=abs(x)
     \pst@dimb=#2\relax
     \ifnum\pst@dimb<\z@\pst@dimb=-\pst@dimb\fi % dimb=abs(y)</pre>
     \advance\pst@dimb\pst@dima % dimb=s=abs(x)+abs(y)
     % dimg=z=sqrt(x^2+y^2)
      \global\pst@dimg=\z@
     \else
      \multiply\pst@dima 8\relax
                                    % dima= 8abs(x)
      \pst@@divide\pst@dima\pst@dimb % dimg =8t=8abs(x)/s
      \advance\pst@dimg -4pt
                              % dimg = 4tau = (8t-4)
      \multiply\pst@dimg 2
      \pst@dimtonum\pst@dimg\pst@tempa
      \pst@dima=\pst@tempa\pst@dimg % dima=(8tau)^2
      \advance\pst@dima 64pt % dima=u=[64+(8tau)^2]/2
      \divide\pst@dima 2\relax
                                         % =(8f)^2
18
      \pst@dimd=7pt
                            % initial guess at sqrt(u)
      \pst@@pyth\pst@@pyth\pst@@pyth % dimd=sqrt(u)
20
      \pst@dimtonum\pst@dimd\pst@tempa
21
      \pst@dimg=\pst@tempa\pst@dimb
22
      \global\divide\pst@dimg 8
                                 % dimg=z=(8f)*s/8
23
     \fi
24
   \endgroup
25
   #3=\pst@dimg}
                              dimd = q < -- (q + u/q)/2
\def\pst@@pyth{%
   \pst@@divide\pst@dima\pst@dimd
   \advance\pst@dimd\pst@dimg
29
   \divide\pst@dimd 2\relax}
```

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```
\pst@sinandcos Syntax:
  \pst@sinandcos{<dim>}{<int>}
```

<dim>, in sp units, should equal 100,000 times the angle, in degrees between 0 and 90. <int> should equal the angle's quadrant (0, 1, 2 or 3). \pst@dimg is set to  $\sin(\theta)$  and \pst@dimh is set to  $\cos(\theta)$  (in pt's).

The algorithms uses the usual McLaurin expansion.

```
\def\pst@sinandcos#1{%
   \begingroup
     \pst@dima=#1\relax
     \pst@dima=.366022\pst@dima %Now 1pt=1/32rad
     \pst@dimb=\pst@dima % dimb->32sin(angle) in pts
     \pst@dimc=32\p@ % dimc->32cos(angle) in pts
     \pst@dimtonum\pst@dima\pst@tempa
     \pst@cntb=\tw@
     \pst@cntc=-\@ne
     \pst@cntg=32
     \loop
     \ifnum\pst@dima>\@cclvi % 256
      \pst@dima=\pst@tempa\pst@dima
13
      \divide\pst@dima\pst@cntg
      \divide\pst@dima\pst@cntb
      \ifodd\pst@cntb
        \advance\pst@dimb \pst@cntc\pst@dima
1
        \pst@cntc=-\pst@cntc
      \else
19
        \advance\pst@dimc by \pst@cntc\pst@dima
20
21
      \advance\pst@cntb\@ne
22
     \repeat
23
     \divide\pst@dimb\pst@cntg
24
     \divide\pst@dimc\pst@cntg
25
     \global\pst@dimg\pst@dimb
26
     \global\pst@dimh\pst@dimc
27
   \endgroup}
```

\pst@getsinandcos \pst@getsinandcos normalizes the angle to be in the first quadrant, sets \pst@quadrant to 0 for the first quadrant, 1 for the second, 2 for the third, and 3 for the fourth, invokes \pst@sinandcos, and sets \pst@sin to the sine and \pst@cos to the cosine.

```
1 \def\pst@getsinandcos#1{%
2 \pst@dimg=100000sp
3 \pst@dimg=#1\pst@dimg
4 \pst@dimh=36000000sp
5 \pst@cntg=0
6 \loop
7 \ifnum\pst@dimg<\z@
8 \advance\pst@dimg\pst@dimh</pre>
```

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```
\repeat
    \loop
10
    \ifnum\pst@dimg>\pst@dimh
11
     \advance\pst@dimg-\pst@dimh
12
    \repeat
13
    \protect\ \pst@dimh=9000000sp
14
    \def\pst@tempg{%
15
     \ifnum\pst@dimg<\pst@dimh\else
16
       \advance\pst@dimg-\pst@dimh
17
       \advance\pst@cntg\@ne
18
       \ifnum\pst@cntg>\thr@@ \advance\pst@cntg-4 \fi
       \expandafter\pst@tempg
20
     \fi}%
21
    \pst@tempg
22
    \chardef\pst@quadrant\pst@cntg
23
    \left\langle \int dim \right\rangle = \z@
24
      \def\pst@sin{0}%
25
     \def\pst@cos{1}%
26
27
    \else
      \pst@sinandcos\pst@dimg
28
      \pst@dimtonum\pst@dimg\pst@sin
29
30
      \pst@dimtonum\pst@dimh\pst@cos
    \fi}
```

# **6 Tilting**

#### \pstilt

```
\def\pstilt#1{\pst@makebox{\pstilt@{#1}}}
  \def\pstilt@#1{%
   \begingroup
     \leavevmode
     \pst@getsinandcos{#1}%
     \hbox{%
      \ifcase\pst@quadrant
        \kern\pst@cos\dp\pst@hbox
        \pst@dima=\pst@cos\ht\pst@hbox
        \ht\pst@hbox=\pst@sin\ht\pst@hbox
        \dp\pst@hbox=\pst@sin\dp\pst@hbox
      \or
12
        \kern\pst@sin\ht\pst@hbox
        \pst@dima=\pst@sin\dp\pst@hbox
        \ht\pst@hbox=\pst@cos\ht\pst@hbox
        \dp\pst@hbox=\pst@cos\dp\pst@hbox
16
      \or
17
        \kern\pst@cos\ht\pst@hbox
18
        \pst@dima=\pst@sin\dp\pst@hbox
19
        \pst@dimg=\pst@sin\ht\pst@hbox
20
        \ht\pst@hbox=\pst@sin\dp\pst@hbox
21
        \dp\pst@hbox=\pst@dimg
```

6 Tilting

```
\or
23
        \kern\pst@sin\dp\pst@hbox
24
        \pst@dima=\pst@sin\ht\pst@hbox
25
        \pst@dimg=\pst@cos\ht\pst@hbox
26
        \ht\pst@hbox=\pst@cos\dp\pst@hbox
27
        \dp\pst@hbox=\pst@dimg
28
29
       \pst@Verb{%
30
        { [ 1 0
31
            \pst@cos\space \ifnum\pst@quadrant>\@ne neg \fi
32
            \pst@sin\space
33
            \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
34
            \ifodd\pst@quadrant exch \fi
35
36
          ] concat
37
        } \tx@TMChange}%
38
       \box\pst@hbox
39
       \pst@Verb{\tx@TMRestore}%
40
41
       \kern\pst@dima}%
   \endgroup}
```

#### \psTilt

```
\def\psTilt#1{\pst@makebox{\psTilt@{#1}}}
  \def\psTilt@#1{%
    \begingroup
     \leavevmode
     \pst@getsinandcos{#1}%
     \hbox{%
       \ifodd\pst@quadrant
         \pst@@divide{\dp\pst@hbox}{\pst@cos\p@}%
         \ifnum\pst@quadrant=\thr@@\kern\else\pst@dima=\fi\pst@sin\pst@dimg
         \pst@divide{\ht\pst@hbox}{\pst@cos\p@}%
         \ifnum\pst@quadrant=\@ne\kern\else\pst@dima=\fi\pst@sin\pst@dimg
       \else
         \left( \int_{0}^{\infty} \left( \int_{0}^{\infty} dx \right) dx \right) dx
13
          \@pstrickserr{\string\psTilt\space angle cannot be 0 or 180}\@ehpa
          \def\pst@sin{.7071}%
15
          \def\pst@cos{.7071}%
16
1
         \pst@divide{\dp\pst@hbox}{\pst@sin\p@}%
18
         \ifnum\pst@quadrant=\z@\kern\else\pst@dima=\fi\pst@cos\pst@dimg
19
         \pst@@divide{\ht\pst@hbox}{\pst@sin\p@}%
20
         \ifnum\pst@quadrant=\tw@\kern\else\pst@dima=\fi\pst@cos\pst@dimg
21
       \fi
22
       \ifnum\pst@quadrant>\@ne
23
         \pst@dimg=\ht\pst@hbox
24
         \ht\pst@hbox=\dp\pst@hbox
25
        \dp\pst@hbox=\pst@dimg
26
27
       \fi
       \pst@Verb{%
28
        { [ 1 0
29
```

6 Tilting 14

```
\pst@cos\space \pst@sin\space
30
           \ifodd\pst@quadrant exch \fi
           \tx@Div
           \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
           \ifnum\pst@quadrant>\@ne -1 \else 1 \fi
34
         ] concat
36
        } \tx@TMChange}%
3
      \box\pst@hbox
38
      \pst@Verb{\tx@TMRestore}%
39
      \kern\pst@dima}%
   \endgroup}
```

# \psset@Tshadowsize,\psTshadowsize

```
1 \define@key[psset]{pst-3d}{Tshadowsize}{%
2 \pst@checknum{#1}\psTshadowsize}
3 \psset[pst-3d]{Tshadowsize=1}
```

# \psset@Tshadowangle,\psk@Tshadowangle

```
1 \define@key[psset]{pst-3d}{Tshadowangle}{%
2  \pst@getangle{#1}\psk@Tshadowangle}
3 \psset[pst-3d]{Tshadowangle=60}
```

# \psset@Tshadowcolor,\psTshadowcolor

```
1 \define@key[psset]{pst-3d}{Tshadowcolor}{%
2 \pst@getcolor{#1}\psTshadowcolor}
3 \psset[pst-3d]{Tshadowcolor=lightgray}
```

### \psshadow

```
\def\psshadow{\def\pst@par{}\pst@object{psshadow}}
  \def\psshadow@i{\pst@makebox{\psshadow@ii}}
  \def\psshadow@ii{%
   \begingroup
     \use@par
     \leavevmode
    \pst@getsinandcos{\psk@Tshadowangle}%
    \hbox{%
      \lower\dp\pst@hbox\hbox{%
       \pst@Verb{%
         { [ 1 0
            \pst@cos\space \psTshadowsize mul
            \ifnum\pst@quadrant>\@ne neg \fi
            \pst@sin\space \psTshadowsize mul
            \int \frac{1}{\pi} \left( \frac{1}{\pi} \right) = \frac{1}{\pi} \left( \frac{1}{\pi} \right)
            \ifodd\pst@quadrant exch \fi
            0 0
          ] concat
         } \tx@TMChange}}%
19
      20
      \pst@Verb{\tx@TMRestore}%
```

7 Affin Transformations 15

```
\box\pst@hbox}%
condgroup}
```

# 7 Affin Transformations

```
\verb|\psAffinTransform| [Options]| \{ transformation \ matrix \} \{ object \}
```

```
| \pspicture(3,6)\psset{linewidth=4pt,arrows=->}
| \psline(0,0)(1.5,0)(3,3)\rput*(2.25,1.5){foo}
| \psAffinTransform{0.5 0 0 2 0 0}{\color{red}%}
| \psline[linecolor=red](0,0)(1.5,0)(3,3)\rput*(2.25,1.5){foo}
| \}%
| \endpspicture
| foo
```

The transformation matrix must be a list of 6 values divided by a space. For a translation modify the last two values of 1001dxdy. The values for dx and dy must be of the unit pt! For a rotation we have the transformation matrix

$$\begin{bmatrix}
\cos(\alpha)\sin(\alpha) & 0 \\
-\sin(\alpha)\cos(\alpha) & 0 \\
00 & 1
\end{bmatrix}$$
(1)

For \psAffinT ransform the four values have to be modifies a cos a sin a sin neg a cos 0 0. Tilting can be done with sx00sy00. All effects can be combined.

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# 8 List of all optional arguments for pst-3d

Key	Type	Default
viewpoint	ordinary	1 -1 1
viewangle	ordinary	Θ
normal	ordinary	0 0 1
embedangle	ordinary	0
Tshadowsize	ordinary	1
Tshadowangle	ordinary	60
Tshadowcolor	ordinary	lightgray

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