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1 Function Make-Fibonacci-Heap()
2    $n[H] := 0$ 
3    $min[H] := NIL$ 
4   return  $H$ 

1 Function Fibonacci-Heap-Minimum( $H$ )
2   return  $min[H]$ 

1 Function Fibonacci-Heap-Link( $H, y, x$ )
2   remove  $y$  from the root list of  $H$ 
3   make  $y$  a child of  $x$ 
4    $degree[x] := degree[x] + 1$ 
5    $mark[y] := FALSE$ 

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1 Function Consolidate( $H$ )
2   for  $i : 0$  to  $D(n[H])$  do
3      $A[i] := NIL$ 
4   foreach node  $x$  in the root list of  $H$  do
5      $x := w$ 
6      $d := degree[x]$ 
7     while  $A[i] \neq NIL$  do
8        $y := A[d]$ 
9       if  $key[x] > key[y]$  then
10        exchange  $x \longleftrightarrow y$ 
11      Fibonacci-Heap-Link( $H, y, x$ )
12       $A[d] := NIL$ 
13       $d := d + 1$ 
14     $A[d] := x$ 
15   $min[H] := NIL$ 
16  for  $i := 0$  to  $D(n[H])$  do
17    if  $A[i] \neq NIL$  then
18      add  $A[i]$  to the root list of  $H$ 
19    if  $min[H] = NIL$  or  $key[A[i]] < key[min[H]]$  then
20       $min[H] := A[i]$ 

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1 Function Fibonacci-Heap-Union( $H1, H2$ )
2    $H := \text{Make-Fibonacci-Heap}()$ 
3    $min[H] := min[H1]$ 
4   Concatenate the root list of  $H2$  with the root list of  $H$ 
5   if ( $min[H1] = NIL$ ) or ( $min[H2] \neq NIL$  and
6      $min[H2] < min[H1]$ ) then
7      $min[H] := min[H2]$ 
7    $n[H] := n[H1] + n[H2]$ 
8   free the objects  $H1$  and  $H2$ 
9   return  $H$ 

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1 Function Fibonacci-Heap-Insert( $H, x$ )
2    $degree[x] := 0$ 
3    $p[x] := NIL$ 
4    $child[x] := NIL$ 
5    $left[x] := x$ 
6    $right[x] := x$ 
7    $mark[x] := FALSE$ 
8   concatenate the root list containing  $x$  with root list  $H$ 
9   if  $min[H] = NIL$  or  $key[x] < key[min[H]]$  then
10      $min[H] := x$ 
11    $n[H] = n[H] + 1$ 

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1 Function Fibonacci-Heap-Extract-Min( $H$ )
2    $z := min[H]$ 
3   if  $x \neq NIL$  then
4     foreach  $child\ x\ of\ z$  do
5       add  $x$  to the root list of  $H$ 
6        $p[x] := NIL$ 
7     remove  $z$  from the root list of  $H$ 
8     if  $z = right[z]$  then
9        $min[H] := NIL$ 
10    else
11       $min[H] := right[z]$ 
12      Consolidate( $H$ )
13     $n[H] := n[H] - 1$ 
14  return  $z$ 

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1 Function Fibonacci-Heap-Decrease-Key( $H, x, k$ )
2   if  $k > key[x]$  then
3     error "new key is greater than the current key"
4    $key[x] := k$ 
5    $y := p[x]$ 
6   if  $y \neq NIL$  and  $key[x] < key[y]$  then
7     Cut( $H, x, y$ )
8     Cascading-Cut( $H, y$ )
9   if  $key[x] < key[min[H]]$  then
10     $min[H] := x$ 

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1 Function Cut( $H, x, y$ )
2   remove  $x$  from the root list of  $y$ , decrementing  $degree[y]$ 
3   add  $x$  to the root list of  $H$ 
4    $p[x] := NIL$ 
5    $mark[x] := FALSE$ 

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1 Function CascadingCut( $H, y$ )
2    $z := p[y]$ 
3   if  $z \neq NIL$  then
4     if  $mark[y] = FALSE$  then
5        $mark[y] := TRUE$ 
6     else
7       Cut( $H, y, z$ )
8       Cascading-Cut( $H, z$ )

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1 Function Fibonacci-Heap-Delete( $H, x$ )
2   Fibonacci-Heap-Decrease-Key( $H, x, -\infty$ )
3   Fibonacci-Heap-Extract-Min( $H$ )

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