

# Modelling Complex Systems

## Genetic Algorithms

This lecture includes adapted slides of David Sumpter and Yu Liu, and work of Charitini Stavropoulou and Katarzyna Kowalczyk



# Evolution

- ▶ Evolution solves “problems”
- ▶ But there is no specific problem needed to be solved, only one general problem: increasing fitness
- ▶ We have specific problems

# Evolution

- ▶ e.g., eye
- ▶ Large solution space
- ▶ Open-ended
- ▶ Natural selection (adaptation):
  1. reproduction
  2. mutation
  3. competition (e.g., limited resources)



# Genetic Algorithm (GA)

- ▶ Large solution space, hard to check every possibility
- ▶ Not open-ended (should stop)
- ▶ Natural selection in computer:
  1. reproduction?
  2. mutation?
  3. competition?



# Genetic Algorithm (GA)

- ▶ John Henry Holland, 1970s
- ▶ Computer programs that evolve over generations to find (some of) the "fittest" out of a very large number



# Basic GA Recipe

- ▶ 1. Define a format (a string) to represent different strategies.  
We call one strategy as one chromosome.
- ▶ 2. Give a population of some random chromosomes
- ▶ 3. Calculate each chromosome's fitness
- ▶ 4. Evolution: cross-over and mutate
- ▶ 6. Repeat from step 3 for enough generations



# Basic GA Recipe

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# GA Evolving Robot: Strategy Format

Situations					Action
North	East	South	West	Here	
-	-	-	-	-	Move north
-	-	-	-	can	Move east
-	-	-	-	wall	Pick up can
-	-	-	can	-	Move
.....					
wall	-	can	wall	-	Stay still
.....					
wall	wall	wall	wall	wall	Move east



# GA Evolving Robot: Strategy Format

Situations					Action
North	East	South	West	Here	
-	-	-	-	-	0
-	-	-	-	can	1
-	-	-	-	wall	6
-	-	-	can	-	4
.....					
wall	-	can	wall	-	5
.....					
wall	wall	wall	wall	wall	1



# GA Evolving Robot: Strategy Format

- ▶  $3^5 = 243$  situations
- ▶ Move north  
Move east  
Move south  
Move west  
Move randomly  
Stay still  
Pick up can



# GA Evolving Robot: Strategy Format

- ▶ Each chromosome is a string of 243 digits, each of which is between 0 and 6.
- ▶ There are  $6^{243} = 1.23e189$  possible chromosomes.
- ▶  $3^5 = 243$  situations
- ▶ Move north  
Move east  
Move south  
Move west  
Move randomly  
Stay still  
Pick up can

23300323421630343530546006102562515114162260435654334066511514  
15650220640642051006643216161521652022364433363346013326503000  
40622050243165006111305146664232401245633345524126143441361020  
150630642551654043264463156164510543665346310551646005164



# GA Evolving Robot: Measure Fitness

- ▶ Given a finite time, the number of cans it picks up.
- ▶ The minimum time to pick all cans up.
- ▶ **Pick up can correctly +10;  
Try to pick up but no can -1;  
Crash to the wall -5;  
Otherwise 0.**

The fitness should be an average measured in many cases  
(e.g., 100 cases)

23300323421630343530546006102562515114162260435654334066511514  
15650220640642051006643216161521652022364433363346013326503000  
40622050243165006111305146664232401245633345524126143441361020  
150630642551654043264463156164510543665346310551646005164



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# GA Evolving Robot: Cross-Over



16411343121025360340361241431201104235462525304202044516433665  
61035322153105131440622120614631432154610256523644422025340345  
30502005620634026331002453416430151631210012214400664012665246  
351650154123113132453304433212634555005314213064423311000

23300323421630343530546006102562515114162260435654334066511514  
15650220640642051006643216161521652022364433363346013326503000  
40622050243165006111305146664232401245633345524126143441361020  
150630642551654043264463156164510543665346310551646005164



# GA Evolving Robot

- ▶ 1. Define a format (a string) to represent different strategies.  
We call one strategy as one chromosome.
- ▶ 2. Give a population of some random chromosomes
- ▶ 3. Calculate each chromosome's fitness
- ▶ 4. Evolution: cross-over and mutate
- ▶ 6. Repeat from step 3 for enough generations



# GA Evolving Robot

- ▶ 1. Define a format (a string) to represent different strategies.  
We call one strategy as one chromosome.
- ▶ 2. Give a population of some random chromosomes (200)
- ▶ 3. Calculate each chromosome's fitness (100 random cases)
- ▶ **4. Evolution: cross-over and mutate**
- ▶ 6. Repeat from step 3 for 1000 generations





# GA Evolving Robot

- ▶ **4. Evolution: cross-over and mutate**
- ▶ 4.1 Randomly select chromosome A and B based on their fitness
- ▶ 4.2 Randomly select a position and cross-over
- ▶ 4.3 By small probability (e.g.,  $p = 0.05$ ), mutate one gene
- ▶ 4.4 Repeat from 4.1 until you get 200 chromosomes



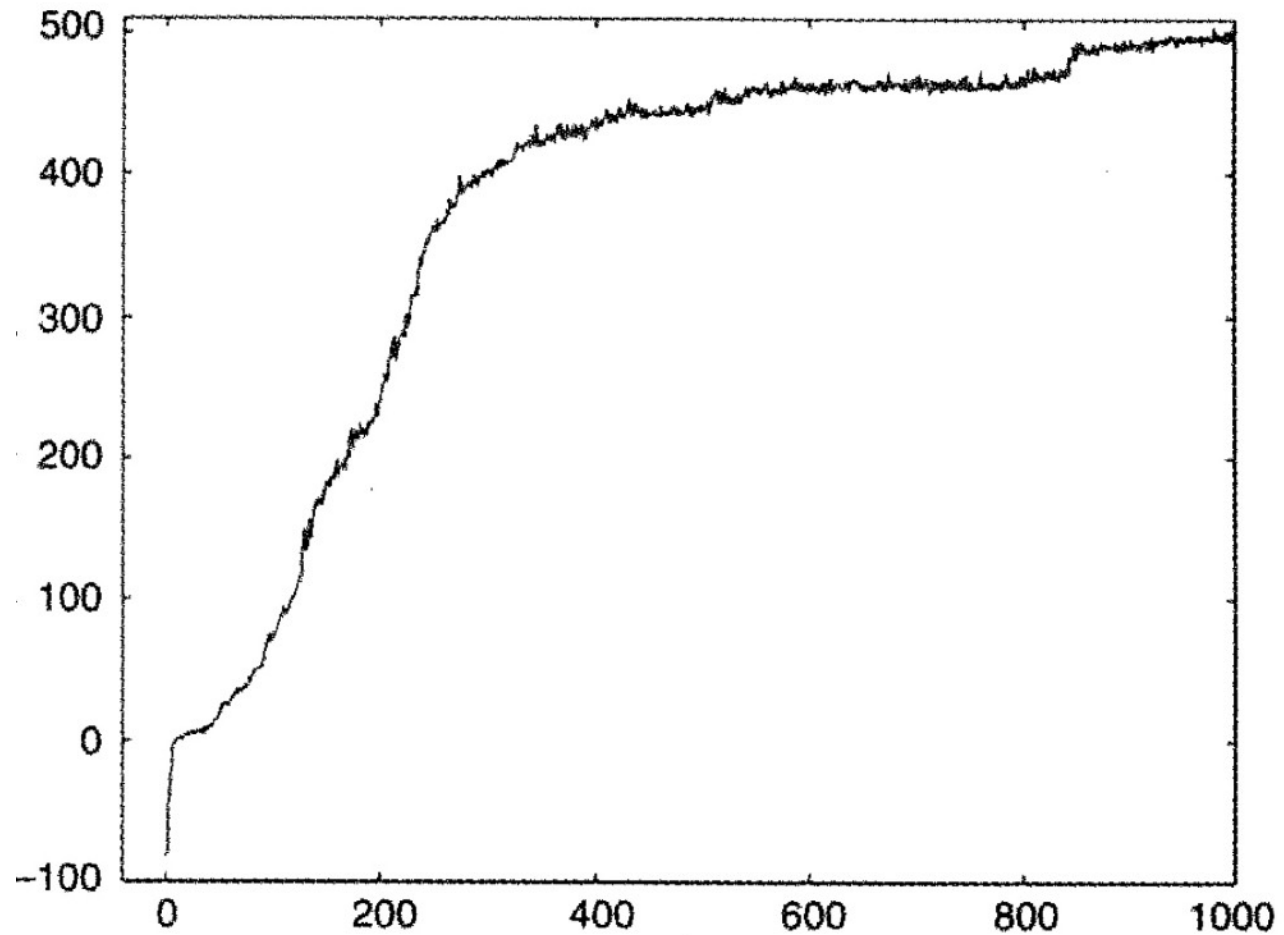
# GA Evolving Robot

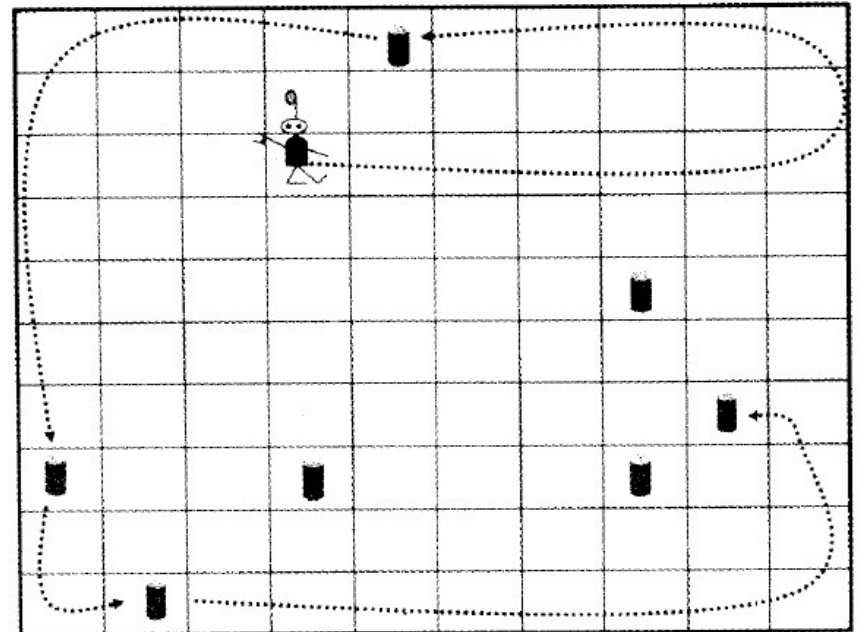
- ▶ What parameters do we have in this case?
- ▶ 1. fixed population of chromosomes (200)
- ▶ 2. number of repeats to calculate average fitness (100)
- ▶ 3. mutation rate per chromosome (0.05)
- ▶ 4. number of generations (1000)



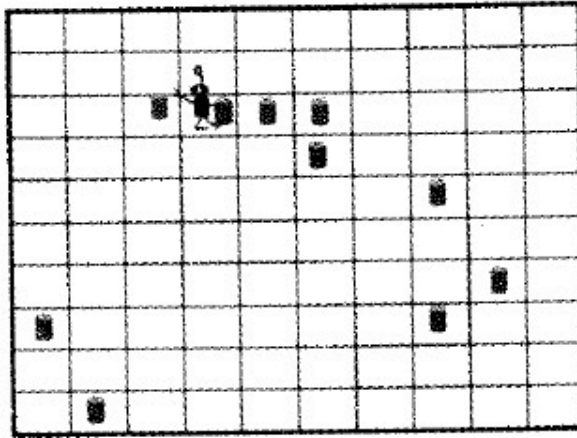
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# GA Evolving Robot

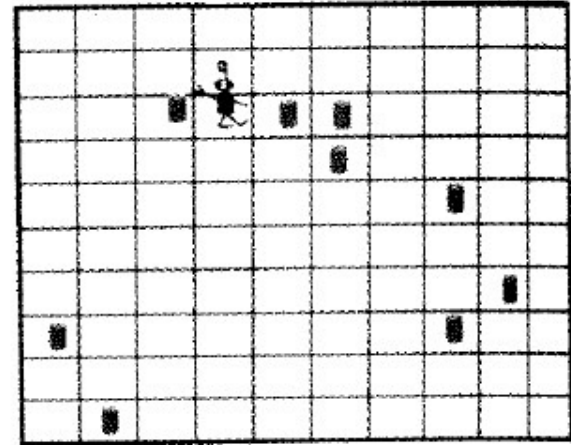




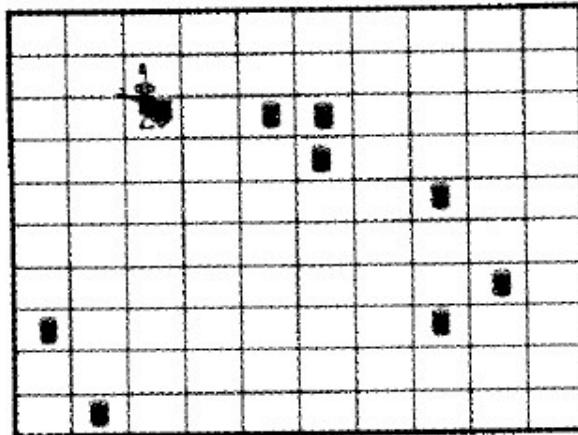
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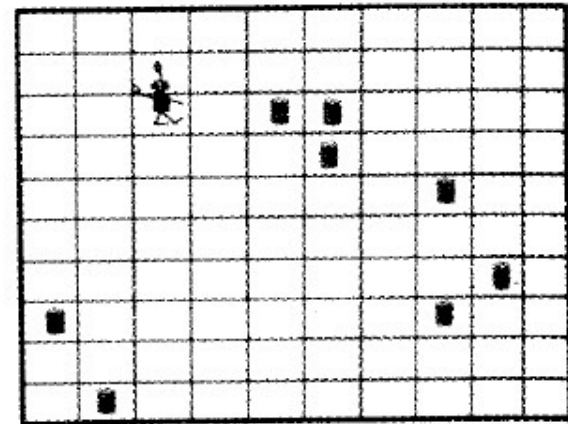
(a)



(b)

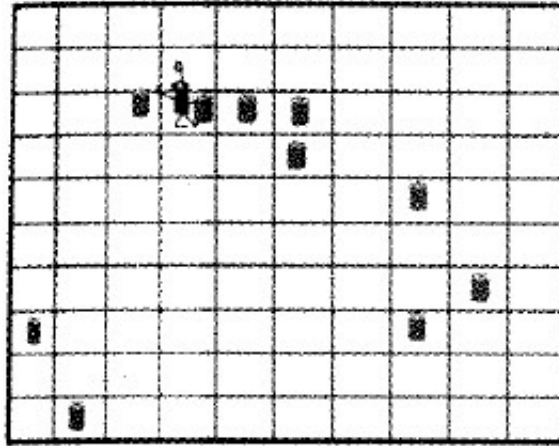


(c)

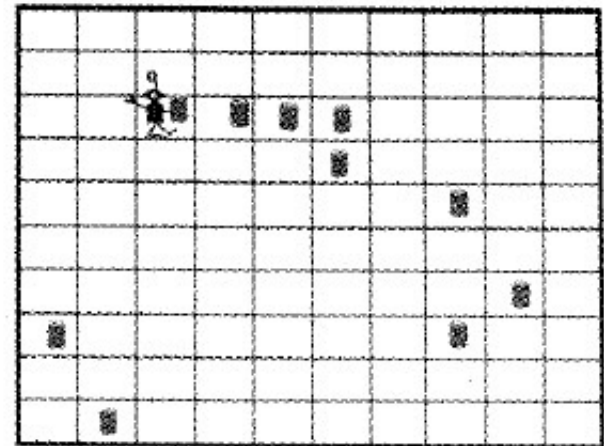


(d)

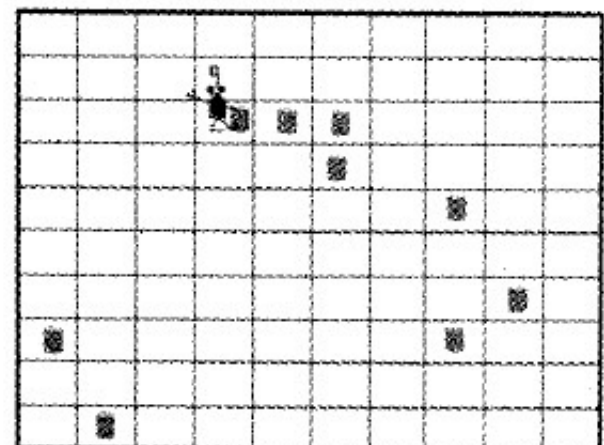
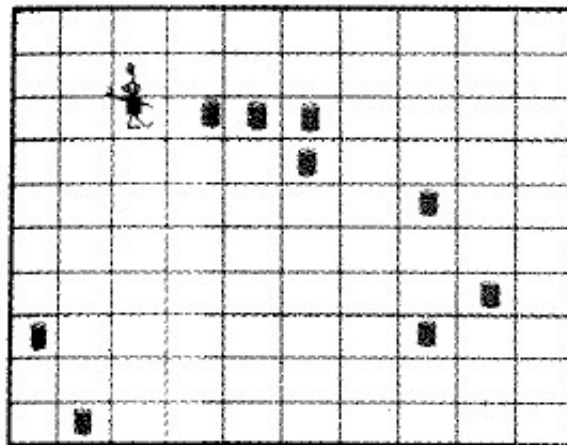
# GA Evolving Robot



(a)

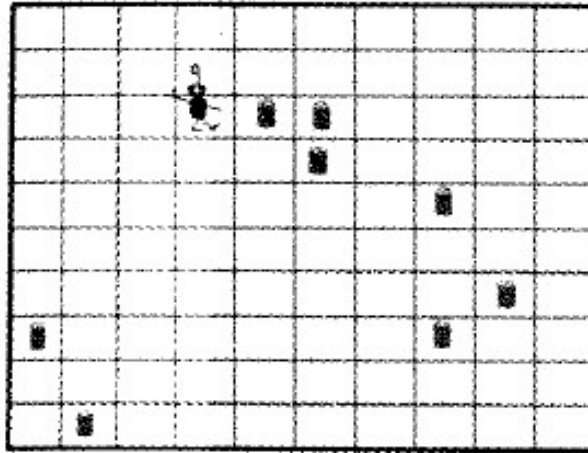


(b)

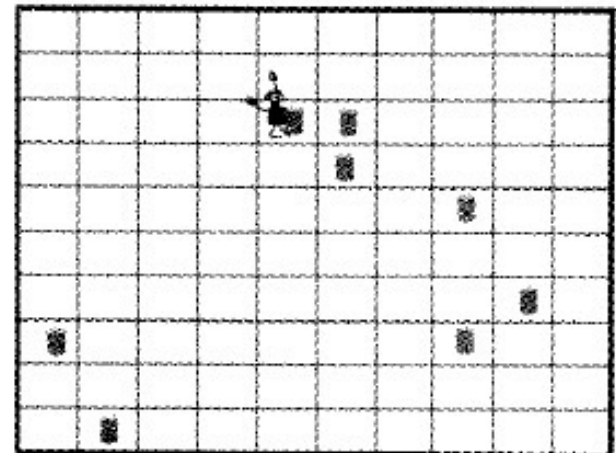




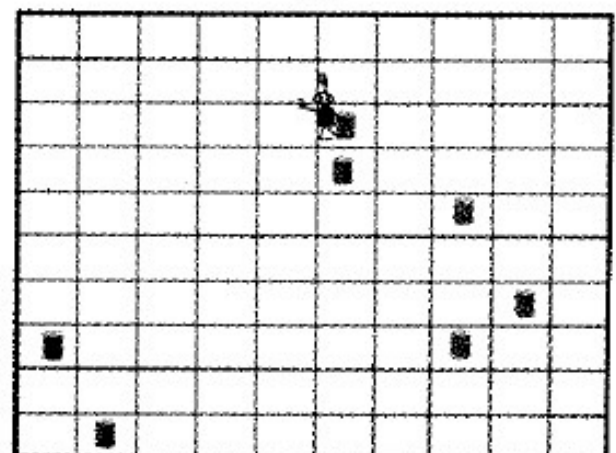
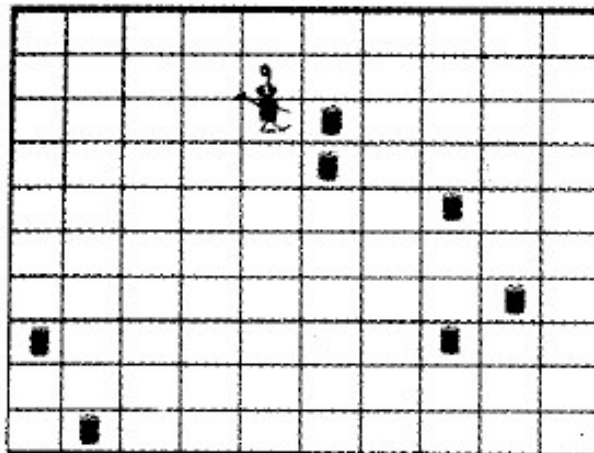
# GA Evolving Robot



(e)

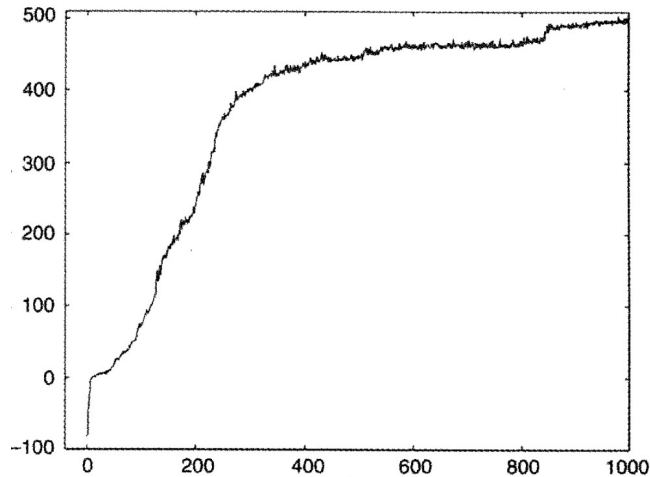


(f)





# GA Evolving Robot



- ▶ Independent good genes are easy to appear.
- ▶ Cooperative genes are difficult to appear but also very important.





# GA Evolving Robot

- ▶ Why does GA work?
- ▶ A balance between selection, mutation and cross-over.
- ▶ 1. Low mutation rate make sure that 1) genes are not easy to be wiped out (both good and bad genes), and 2) there is chance of good innovations.
- ▶ 2. Good strategies can always be made of groups of good gene modulars. The cross-over can assemble modulars.
- ▶ 3. Selection picks the good genes and good gene modulars.



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# GA Cellular Automata Computer

- ▶ Tell whether there are more black grids or not, based on local information.

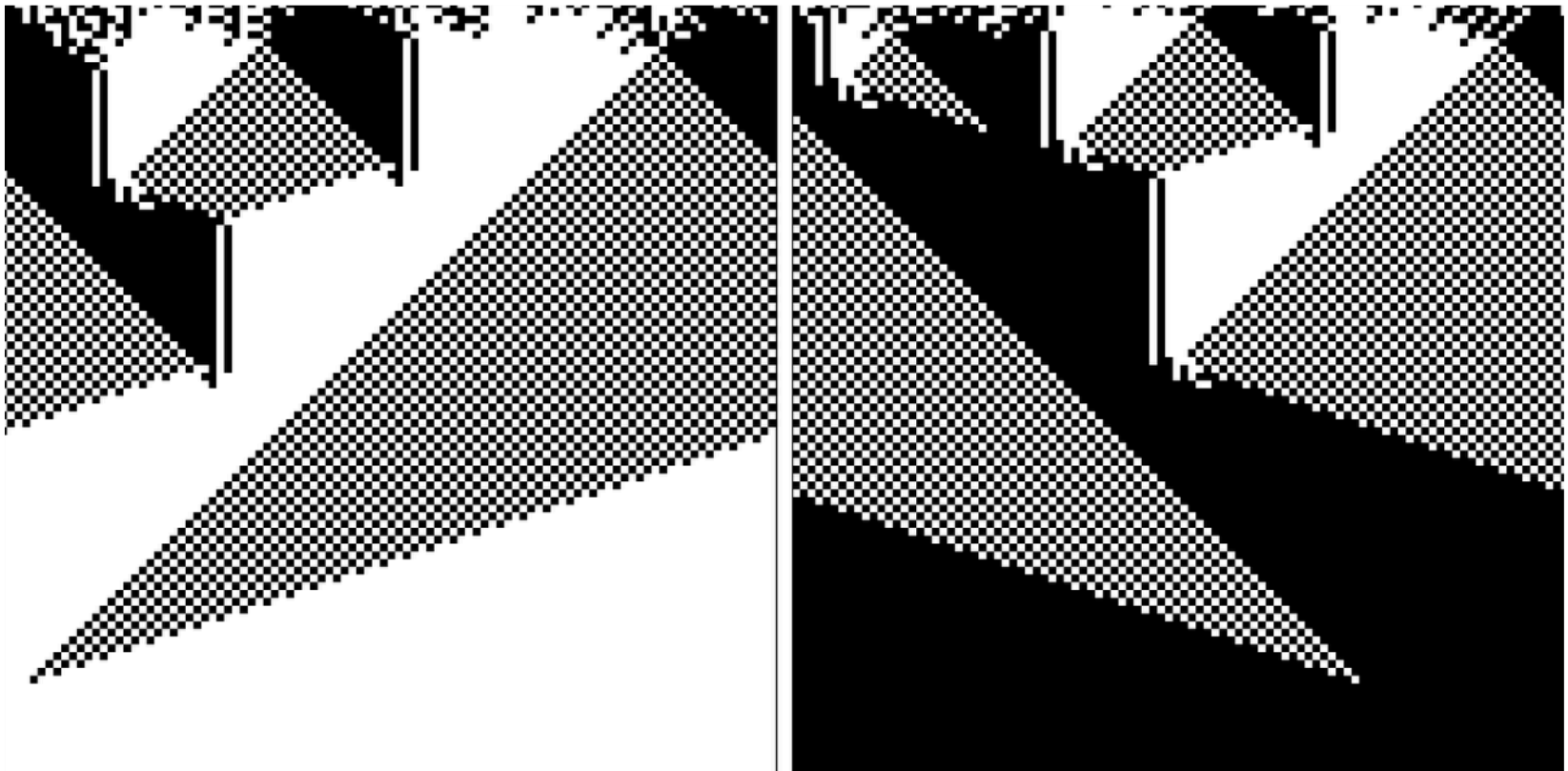


# GA Cellular Automata Computer

- ▶ Given a string of 0 and 1, tell whether there are more 1s or not, based on local information.
- ▶  $2^5 = 32$  situations;  
Each situation has 2 possible actions, so there are  $2^{32} = 4.295e9$  strategies.

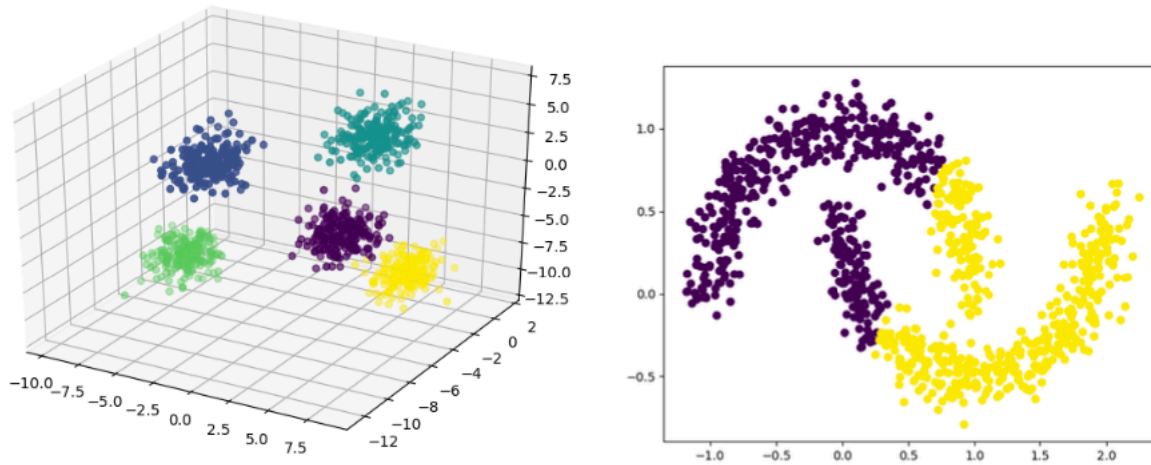
# GA Cellular Automata Computer

- ▶ Given a string of 0 and 1, tell whether there are more 1s or not, based on local information.



# Example: GA K-Means

- ▶ K-means - way to cluster pts in n-dimensions into k clusters



$$\mathcal{M}(C_1, \dots, C_K) = \sum_{i=1}^K \sum_{\mathbf{x}_j \in C_i} \|\mathbf{x}_j - \mathbf{c}_i\|$$

Charitini Stavropoulou

Katarzyna Kowalczyk

# Example: G A K-Means

- K-means - way to cluster pts in n-dimensions into k clusters



$$\mathcal{M}(C_1, \dots, C_K) = \sum_{i=1}^K \sum_{\mathbf{x}_j \in C_i} \|\mathbf{x}_j - \mathbf{c}_i\|$$

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# Dataset To Cluster -

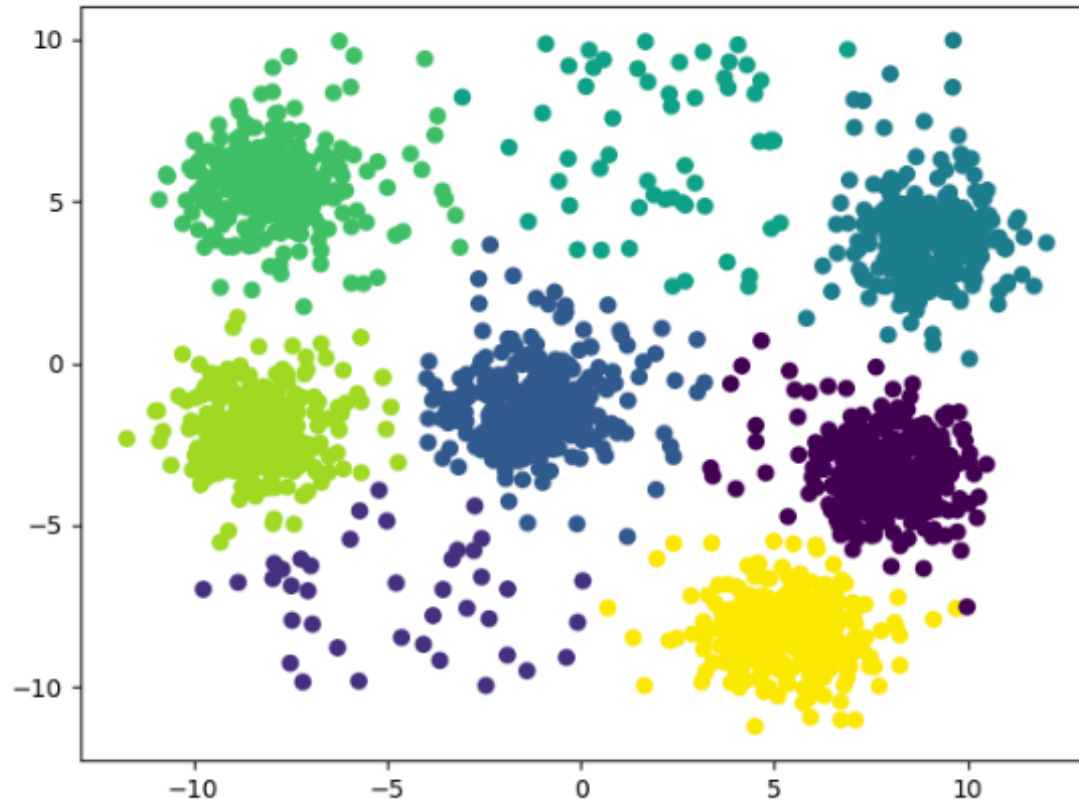


Figure 2: Data set used in the experiments.

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Katarzyna Kowalczyk



# Selecting Which Chromosomes Breed...

- ▶ Tournament - pick groups of  $s$  individuals and return individual with highest fitness.

e.g. if  $s = 2$  and chromosomes  $i, j$  chosen then return  $\arg \max \{f_i, f_j\}$

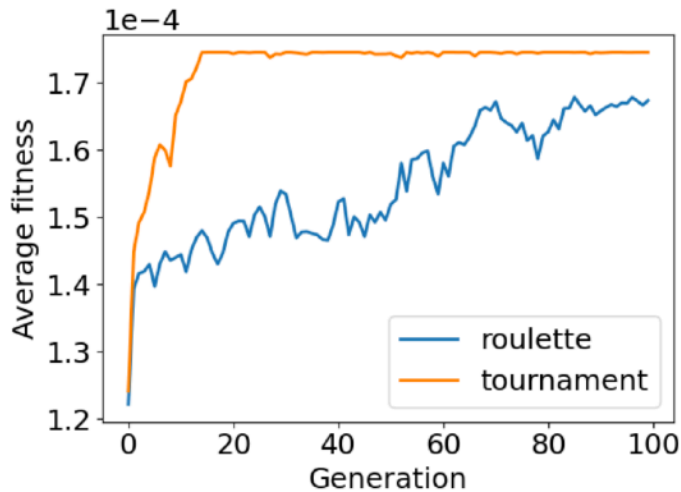
- ▶ Roulette wheel - each chromosome  $i$  chosen with probability proportional to fitness  $f_i$ .

$$\text{Probability of choosing } i = \frac{f_i}{\sum_j f_j}$$

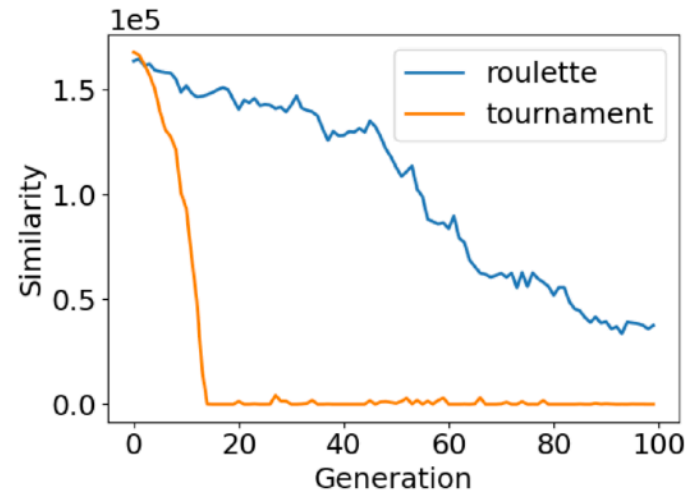
- ▶ Fitness - calculated to be  $\sim 1/\mathcal{M}$



# Selection Matters



(a) Average fitness



(b) Generation similarity

Figure 6: Comparison of two selection strategies for the same data set and GA parameters: 100 generations, population of 100,  $\mu_c = 0.8$ ,  $\mu_m = 0.01$ .

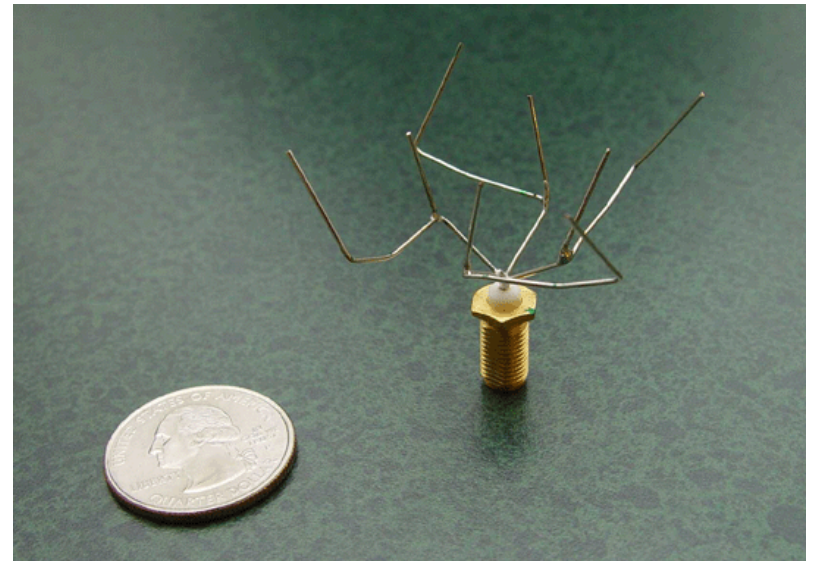
- ▶ **Generational similarity.** Treat each chromosome as a point in  $\mathbb{R}^{kn}$  and define to be sum of pairwise distances of chromosomes in generation.

Charitini Stavropoulou

Katarzyna Kowalczyk

# Comments On GA

- ▶ Automated design (e.g., Shape of the plane, antenna)
- ▶ Analyse satellite images
- ▶ Animations in film (e.g., horses in The Lord of the Rings III)
- ▶ Develop new drugs
- ▶ Protein folding
- ▶ .....





## Comments On GA

- ▶ GA always cannot get the best solution (there may be not a best solution), but can be good enough.
- ▶ Biological evolution is open-ended, while we define an end for GA.
- ▶ For biological evolution, the whole solution space is not fixed; while for GA generally, the whole solution space is actually fixed.



# GA Vs Machine Learning

- ▶ The common part is the ability to learn or 'fit' to data for predictions.
- ▶ Both have a fitness function - to determine how well the algorithm is performing
- ▶ GA is an example of reinforcement learning
- ▶ GA group of algorithms, rather than a single algorithm.
- ▶ Update rules from group of algorithms to group of algorithms in GA, very different to how one updates algorithms in other machine learning contexts.
- ▶ Nice example of reinforcement learning, (but not a GA!) is: arxiv:1707.02286

-see videos here - [https://www.youtube.com/watch?v=hx\\_bgoTF7bs](https://www.youtube.com/watch?v=hx_bgoTF7bs)