

CSE 208 Online on Hashing

Scenario:

You're building a permission database where each `group_id` maps to users (`user_id`) with access rights (like `"read"`, `"write"`). Use a **two-layer hash table** with **open addressing** for both levels.

Structure:

- **Outer Table** (size `N`): Each element of this table contains a pointer/reference to another hash table on the second layer having size `N`. So, it stores (`group_id`, `pointer_to_inner_table`).
- **Inner Table** (size `N`): stores (`user_id`, `permission`)

Hashing:

- **Hash function for outer table:**
Use the `Hash1` function from your offline.
- **Hash function for Inner table:**
Use the `Hash2` function from your offline.

Operations:

`INSERT(group_id, user_id, permission)`

- Use `hash1` + linear probing to insert/find `group_id` in the outer table.
Linear probing:
$$\text{Index} = (\text{hash1}(\text{group_id}) + i) \bmod N$$
- Use `hash2` + quadratic probing to insert (`user_id`, `permission`) in the inner table.

Quadratic probing:

$$\text{Index} = (\text{hash2}(\text{user_id}) + i^2) \bmod N$$

`SEARCH(group_id, user_id)`

- Probe outer table for `group_id`.
- If found, probe the inner table for `user_id`.

- Print value if found; otherwise, report not found.

SEARCH(group_id)

- Return all (user_id, permission) in the inner table.
- If a group is not found, report it.

Input Format:

1. The first line contains two integers: N and Q
 - N: Size of both the outer and inner hash tables.
 - Q: Number of operations (commands) to process.
2. Each of the next Q lines contains one of the following operations:

Insert Operation

INSERT <group_id> <user_id> <permission>

- group_id: The key for the outer table.
- user_id: The key for the inner table under that group.
- permission: A string (e.g., "read", "write") representing access rights
- You don't need to provide any output for this operation.

Search with Two Keys

SEARCH <group_id> <user_id>

Searches for a specific user_id under a given group_id and prints its permission.

Search with One Key

SEARCH <group_id>

Prints all (user_id, permission) pairs for the given group_id.

DELETE

DELETE <group_id> <user_id>

Deletes and prints (user_id, permission) pair for the given group_id.

Output Format:

For each Search keyword, print the values if found. For each DELETE keyword, print the (user_id, permission) that is deleted.

Sample Input:

```
10 10
INSERT 101 1 read
INSERT 101 2 write
INSERT 111 2 read-write
SEARCH 101 1
SEARCH 101
DELETE 101 1
SEARCH 101
SEARCH 999
SEARCH 101 2
SEARCH 101 5
```

Sample Output:

```
read
(1, read), (2, write)
(1, read) deleted
(2, write)
Group not found
write
User not found in group 101
```