



The Transformer Architecture

Olmo Zavala-Romero and ChatGPT





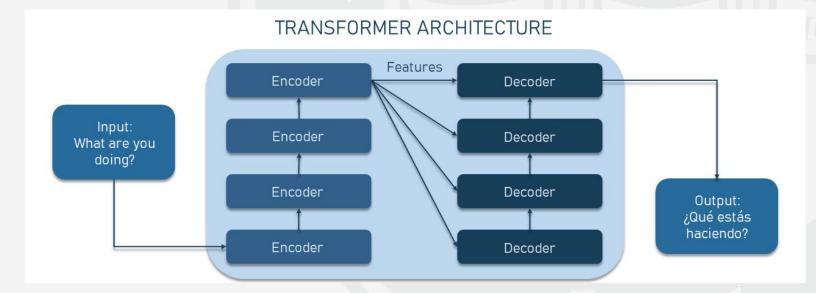
- Objective
 - Good understanding of the architecture
- Outline
 - Motivation
 - Evolution of Sequence Models
 - Need of Transformers
 - Transformers architecture components
 - Embedding
 - Positional encoding
 - Attention
 - Multi-head attention



What is the transformer architecture?



The Transformer architecture is a type of neural network architecture introduced in the paper "Attention Is All You Need" by Vaswani et al. in 2017. It's primarily designed for sequence-to-sequence tasks like machine translation but has been successfully adapted for a variety of other tasks. The architecture consists of an Encoder-Decoder framework, although variations like BERT use just the Encoder, and GPT uses just the Decoder for specific tasks.



https://proceedings.neurips.cc/paper/2017/file/3f5ee243547dee91fbd053c1c4a845aa-Paper.pdf



Motivation



Natural Language Processing (NLP):

- 1. Machine Translation: Transformers were initially proposed for this task and have become the state-of-the-art here.
- Text Summarization: Automatic generation of concise summaries from long articles. **Graph-based Learning:**
- answering questions based on a
- 4. Named Entity Recognition (NER) locations, and organizations in te
- Sentiment Analysis: Classifying t data.
- Language Modeling: Models like Transformer) are often used in te
- Speech Recognition: Transforme converting spoken language into

3. Question Answering: Models like 1. Molecular Design: Predicting molecular p. Social Network Analysis: Analyzing relati

Time-Series Analysis:

- 1. Financial Forecasting: Using transformer predicting stock prices.
- 2. Anomaly Detection: Detecting anomalies

Bioinformatics:

Protein Folding: AlphaFold 2, which has re folding prediction, employs transformer-like architectures.

Computer Vision:

- Image Classification: Vision Transformer (ViT) is a notable application of the transformer architecture in computer vision.
- 2. Object Detection: Transformers have been used in frameworks like DETR for object detection tasks.
- 3. Semantic Segmentation: Segmenting parts of images based on semantic categories.

Multi-modal Learning:

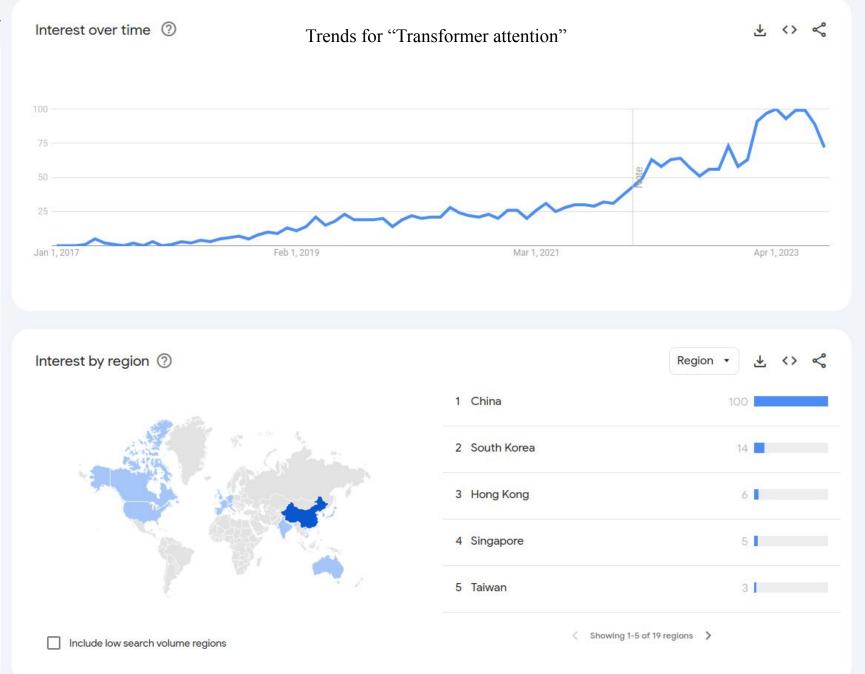
- Image Captioning: Generating textual descriptions of images.
- Visual Question Answering: Answering questions about an image or a series of images.

Reinforcement Learning:

- Game Playing: Transformers have been used in learning policies for complex games.
- 2. Multi-Agent Systems: Utilized in coordinating the behavior of multiple agents.

Audio and Speech:

- 1. Music Generation: Transformers have been adapted to generate musical sequences.
- 2. Speech Synthesis: Text-to-Speech systems like Tacotron 2 have started integrating transformer architectures.





Transformers (sources by Tom)



High-level, easy to read intro:

https://www.altexsoft.com/blog/language-models-gpt/

Paper introducing the Transformer Model:

https://arxiv.org/pdf/1706.03762.pdf

Detailed/annotated implementation:

http://nlp.seas.harvard.edu/annotated-transformer/

In my view accessible explanation of the workings of the model:

https://e2eml.school/transformers.html



History of Sequence models



Original objectives

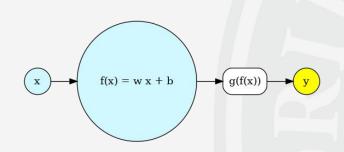
- Temporal/Order Dependencies
- Variable-Length Sequences

"Anita lava la tina" --> "la tina lava a Anita"

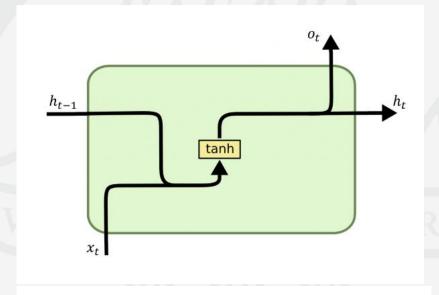


Recurrent Neural Networks





$$L = \frac{1}{n} \sum_{i=1}^{n} (y_i - g(f(x_i)))^2$$



$$h_t = anh(x_tW_{ih}^T + b_{ih} + h_{t-1}W_{hh}^T + b_{hh})$$

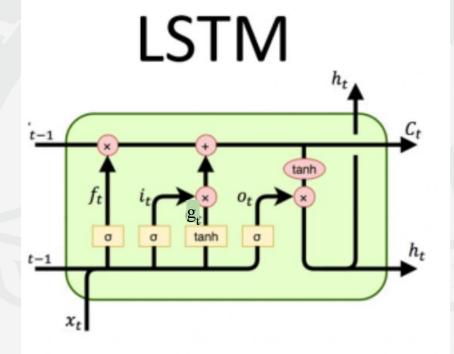
Torch RNN

http://dprogrammer.org/rnn-lstm-gru

LSTM



- Handling Long-Range Dependencies
- Avoid vanishing gradient



- $i \rightarrow input$
- $f \rightarrow forget$
- $g \rightarrow cell$
- $o \rightarrow output$
- $c \rightarrow context$
- $h \rightarrow hidden state$

$$i_t = \sigma(W_{ii}x_t + b_{ii} + W_{hi}h_{t-1} + b_{hi}) \ f_t = \sigma(W_{if}x_t + b_{if} + W_{hf}h_{t-1} + b_{hf}) \ g_t = anh(W_{ig}x_t + b_{ig} + W_{hg}h_{t-1} + b_{hg}) \ o_t = \sigma(W_{io}x_t + b_{io} + W_{ho}h_{t-1} + b_{ho}) \ c_t = f_t \odot c_{t-1} + i_t \odot g_t \ h_t = o_t \odot anh(c_t)$$

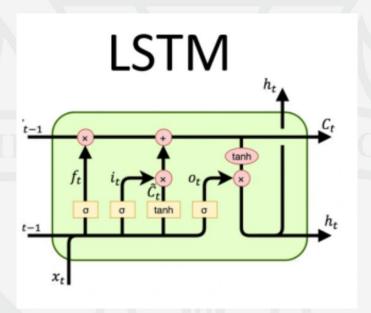


Need for Transformers



Limitations (RNNs, LSTMs, GRUs)

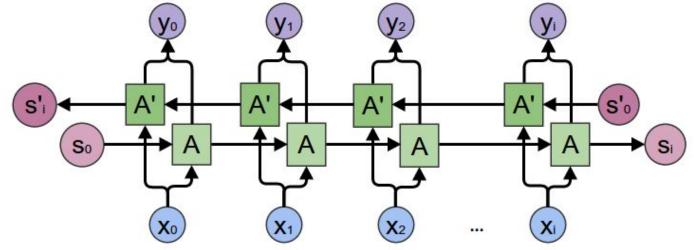
- Parallelization
- Handling Long Sequences
- Computational Complexity





BIRNN



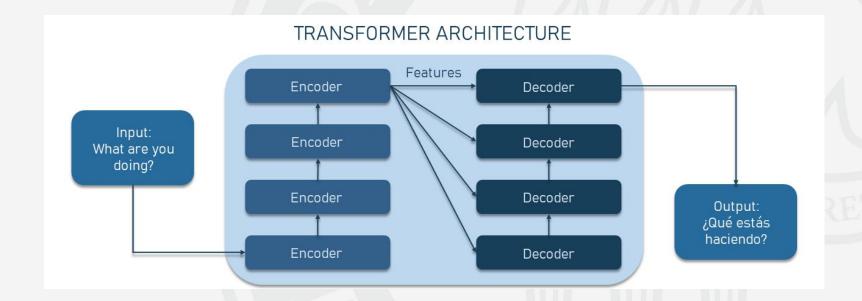


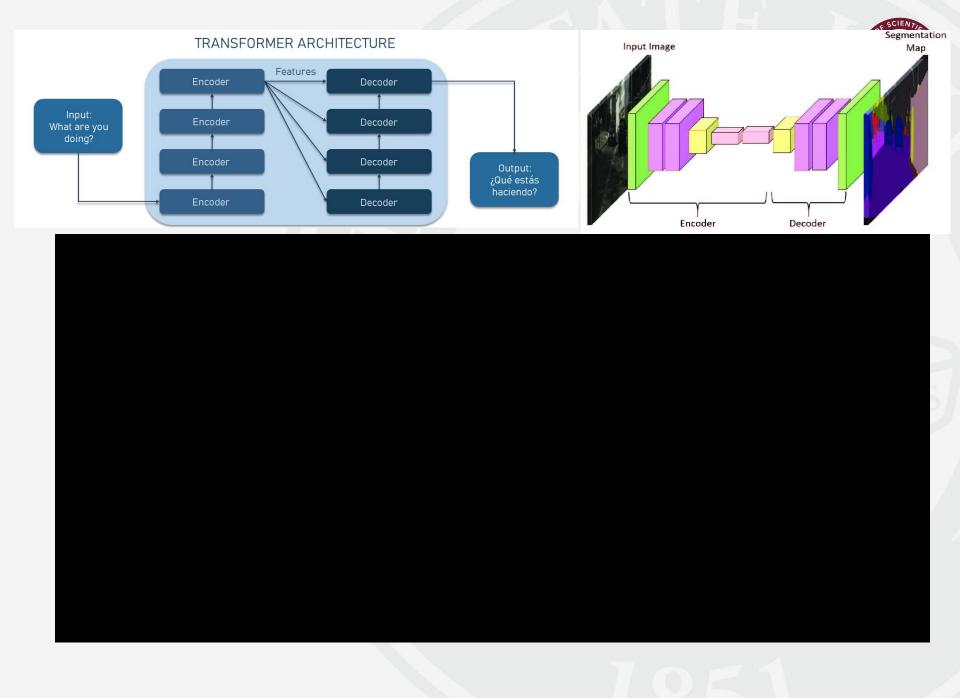
- Context awareness
- Improved accuracy



Transformer Architecture



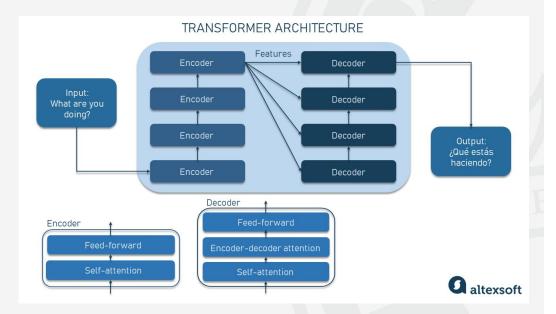






Transformer





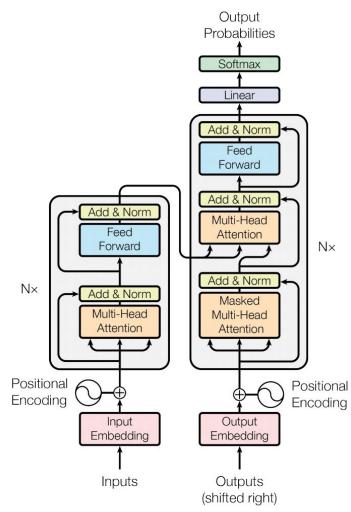


Figure 1: The Transformer - model architecture.



Main components



- Encoder Decoder
- Feed forward networks
- Embeddings
- Positional encoding
- Attention
 - Multi-head attention
 - Masked Multi-Head Attention

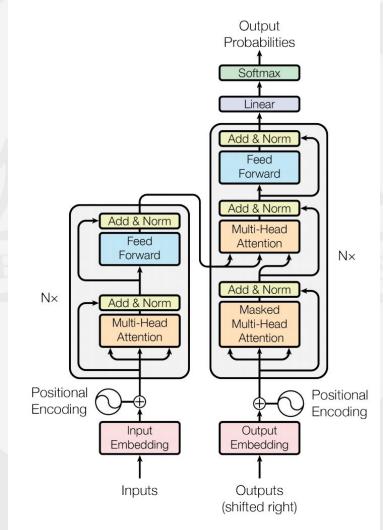


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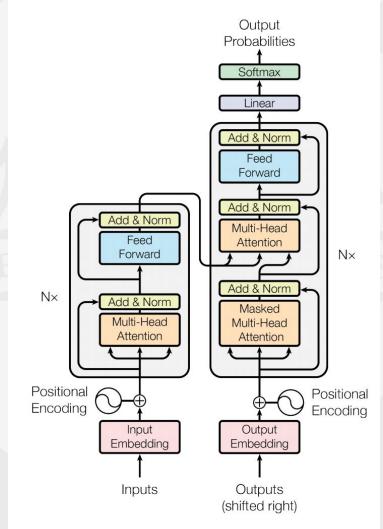


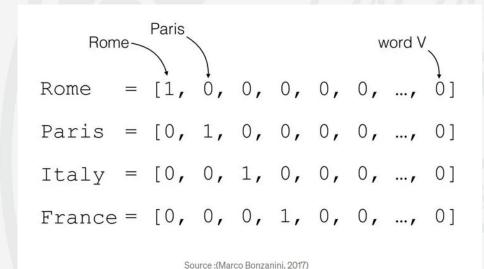
Figure 1: The Transformer - model architecture.



Word Representations



One hot encoding





Word Representations



Word embedding

	Man (5391)	Woman (9853)	King (4914)	Queen (7157)	Apple (456)	Orange (6257)
Gender	- (l	-0.95	0.97	0.00	0.01
Royal	0.01	0.62	0.93	0.95	-0.01	0.00
Age	0.03	0.02	0.7	0.69	0.03	-0.02
Food	6.09	5.01	0.02	0.01	0.95 Ac	tivate 0.97 low: to Settings to activa

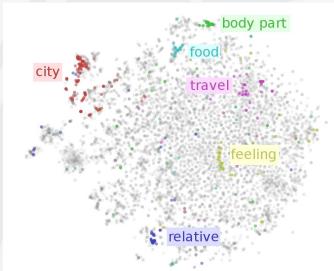
Represent your vocabulary as an N dimensional vector where 'related' words are 'closer' together.

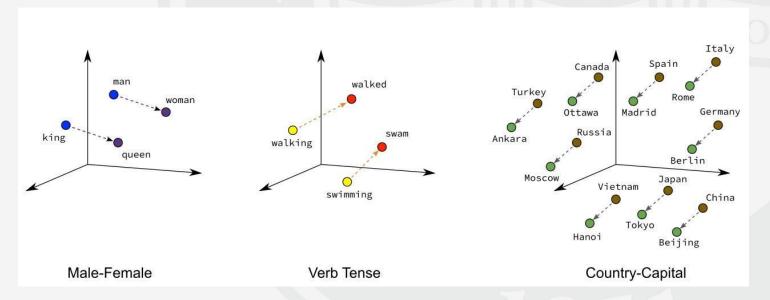
Example file to show the learning of embeddings



Word embeddings









How to learn embeddings?



The objective is to maximize the following likelihood function:

$$L = \sum_{t=1}^T \sum_{-c \leq j \leq c, j
eq 0} \log p(w_{t+j}|w_t)$$

Where $p(w_o|w_i)$ is defined as:

$$p(w_o|w_i) = rac{\exp(v_{w_o}' \cdot v_{w_i})}{\sum_{w=1}^V \exp(v_w' \cdot v_{w_i})}$$

- Initialize word vectors randomly.
- 2. Iterate through each word in the corpus and use surrounding words as context.
- Update the word vectors by optimizing the objective function, typically using SGD or some variant.



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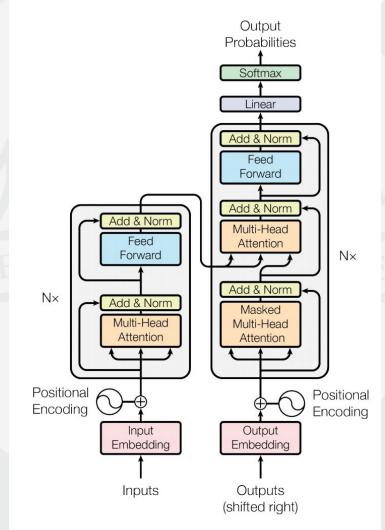


Figure 1: The Transformer - model architecture.



Positional Encoding

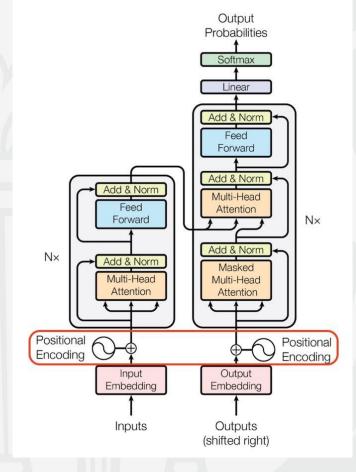


Why?

• Transformers doesn't know the order of the words (embeddings)

What do we want?

- Unique encoding for each location-word combination
- Distance *between* locations should be consistent
- Generalize to longer sentences



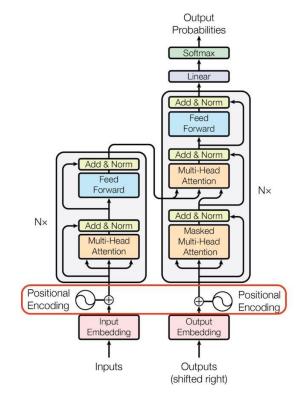
https://e2eml.school/transformers.html

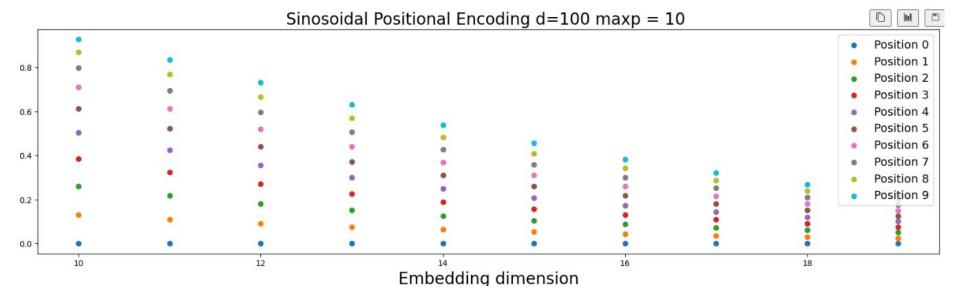
How?

1. Sinusoidal Positional Embeddings: One popular method involves using sinusoidal functions to generate these embeddings. Given a position p in the sequence and a dimension i in the embedding, the sinusoidal positional encoding for that entry is computed as:

$$PE_{(p,2i)} = \sin\left(rac{p}{10000^{2i/d}}
ight) \ PE_{(p,2i+1)} = \cos\left(rac{p}{10000^{2i/d}}
ight)$$

where PE is the positional encoding matrix, p is the position, i ranges over the dimensions, and d is the embedding dimension. This method is easy to compute and can be scaled for sequences of variable lengths.



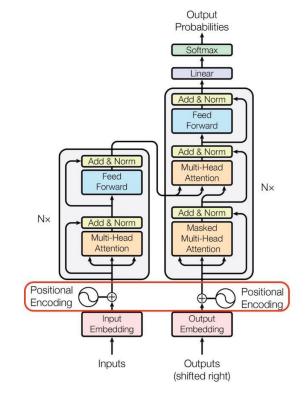


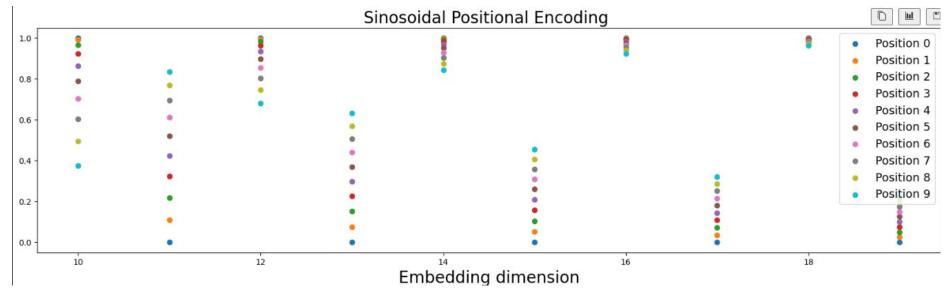
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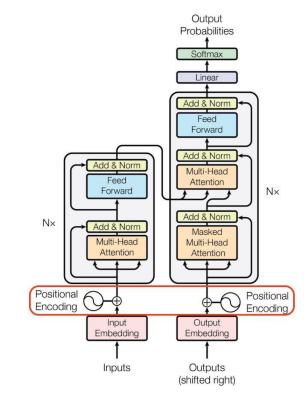
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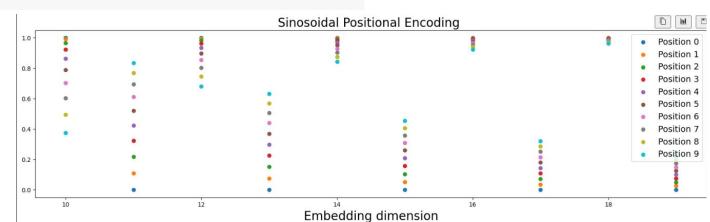
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$$E' = E + PE$$

Here E^\prime is the enhanced embedding, E is the original word embedding, and PE is the positional embedding.







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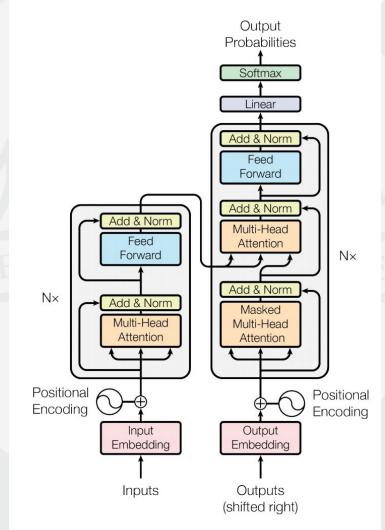


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Concept of Attention

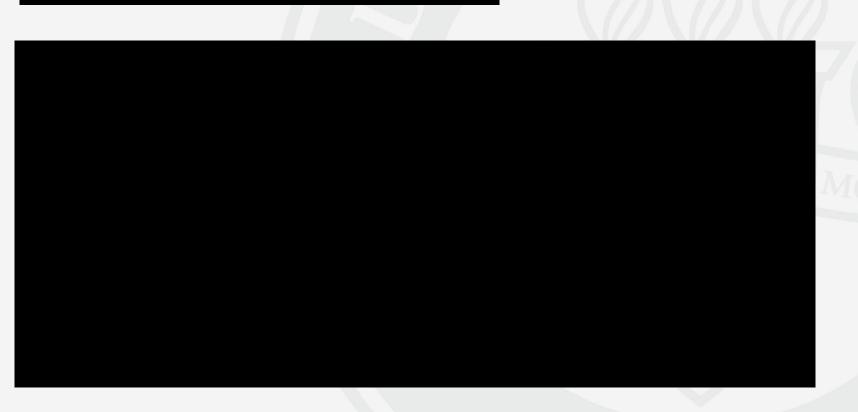


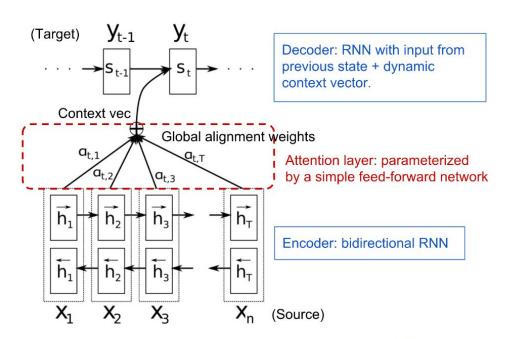


https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seg2seg-models-with-attention/

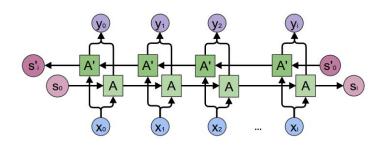
Attention







Attention



The decoder network has hidden state $s_t = f(s_{t-1}, y_{t-1}, \mathbf{c}_t)$ for the output word at position t, $t = 1, \ldots, m$, where the context vector \mathbf{c}_t is a sum of hidden states of the input sequence, weighted by alignment scores:

$$\begin{aligned} \mathbf{c}_t &= \sum_{i=1}^n \alpha_{t,i} \boldsymbol{h}_i & \boldsymbol{h}_i &= [\overrightarrow{\boldsymbol{h}}_i^\top; \overleftarrow{\boldsymbol{h}}_i^\top]^\top, i = 1, \dots, n & ; \text{Context vector for output } y_t \\ \alpha_{t,i} &= \operatorname{align}(y_t, x_i) & ; \text{How well two words } y_t \text{ and } x_i \text{ are aligned.} \\ &= \frac{\exp(\operatorname{score}(\boldsymbol{s}_{t-1}, \boldsymbol{h}_i))}{\sum_{i'=1}^n \exp(\operatorname{score}(\boldsymbol{s}_{t-1}, \boldsymbol{h}_{i'}))} & ; \text{Softmax of some predefined alignment score..} \end{aligned}$$

$$\operatorname{score}({m s}_t,{m h}_i) = {m v}_a^ op anh({f W}_a[{m s}_t;{m h}_i])$$

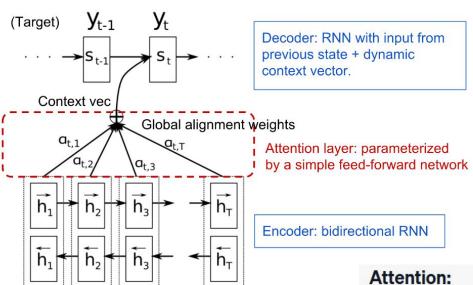
where both \mathbf{v}_a and \mathbf{W}_a are weight matrices to be learned in the alignment model.



Attention mechanisms



Name	Alignment score function	Citation
Content-base attention	$ ext{score}(oldsymbol{s}_t, oldsymbol{h}_i) = ext{cosine}[oldsymbol{s}_t, oldsymbol{h}_i]$	Graves2014
Additive(*)	$\mathrm{score}(\boldsymbol{s}_t,\boldsymbol{h}_i) = \mathbf{v}_a^\top \tanh(\mathbf{W}_a[\boldsymbol{s}_{t-1};\boldsymbol{h}_i])$	Bahdanau2015
Location-Base	$lpha_{t,i} = \mathrm{softmax}(\mathbf{W}_a \mathbf{s}_t)$ Note: This simplifies the softmax alignment to only depend on the target position.	Luong2015
General	$ ext{score}(m{s}_t, m{h}_i) = m{s}_t^{ op} \mathbf{W}_a m{h}_i$ where \mathbf{W}_a is a trainable weight matrix in the attention layer.	Luong2015
Dot-Product	$\operatorname{score}(oldsymbol{s}_t,oldsymbol{h}_i) = oldsymbol{s}_t^ op oldsymbol{h}_i$	Luong2015
Scaled Dot- Product(^)	$\operatorname{score}(\boldsymbol{s}_t, \boldsymbol{h}_i) = \frac{\boldsymbol{s}_t^{\scriptscriptstyle \top} \boldsymbol{h}_i}{\sqrt{n}}$ Note: very similar to the dot-product attention except for a scaling factor; where n is the dimension of the source hidden state.	Vaswani2017



(Source)

Attention

In general, attention mechanisms allow a model to focus on certain parts of the input when producing the output. The basic idea is to take a set of queries (Q), keys (K), and values (V) as input and produce weighted combinations of the values as output.

The attention function is generally formulated as:

$$\operatorname{Attention}(Q,K,V) = \operatorname{softmax}\left(rac{QK^T}{\sqrt{d_k}}
ight) imes V$$

In sequence-to-sequence models like those used in machine translation, "attention" often refers to the mechanism where the decoder pays attention to different parts of the encoder's output while generating each element of the decoded sequence. In this case, Q usually comes from the decoder, and K and V come from the encoder.

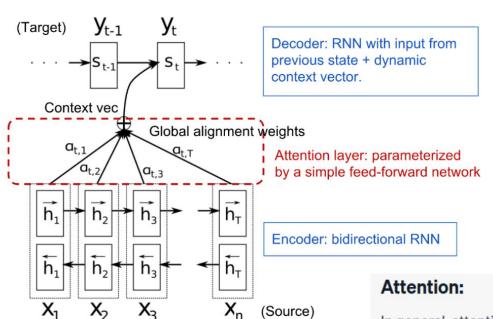
$$egin{aligned} \mathbf{c}_t &= \sum_{i=1}^n lpha_{t,i} oldsymbol{h}_i \ lpha_{t,i} &= \operatorname{align}(y_t, x_i) \ &= rac{\exp(\operatorname{score}(oldsymbol{s}_{t-1}, oldsymbol{h}_i))}{\sum_{i'=1}^n \exp(\operatorname{score}(oldsymbol{s}_{t-1}, oldsymbol{h}_{i'}))} \end{aligned}$$

 X_3

 X_2

 X_1

Dot-Product
$$\operatorname{score}(\boldsymbol{s}_t, \boldsymbol{h}_i) = \boldsymbol{s}_t^{\top} \boldsymbol{h}_i$$



Attention

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The attention function is generally formulated as:

$$Attention(Q, K, V) = softmax \begin{pmatrix} QK^T \\ \sqrt{d_k} \end{pmatrix} \times V$$

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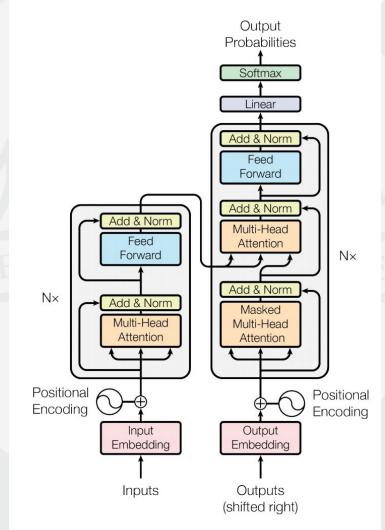


Figure 1: The Transformer - model architecture.



Attention vs Self-attention



Differences:

- 1. Source of Q, K, V:
 - Attention: Q, K, V can come from different sequences.
 - Self-Attention: Q, K, V are from the same sequence.

2. Use-Cases:

- Attention: Often used in encoder-decoder architectures where the decoder attends to the encoder's output.
- Self-Attention: Commonly used within either the encoder or the decoder to consider other positions in the same sequence for each position.

3. Range of Application:

- Attention: Between different sequences (e.g., source and target in machine translation).
- Self-Attention: Within the same sequence.

4. Types of Tasks:

- Attention: Sequence-to-sequence tasks like machine translation, text summarization, etc.
- Self-Attention: Tasks that require understanding the context in a single sequence, such as language modeling, text classification, etc.



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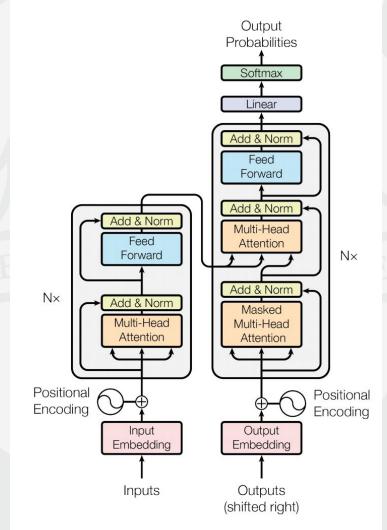
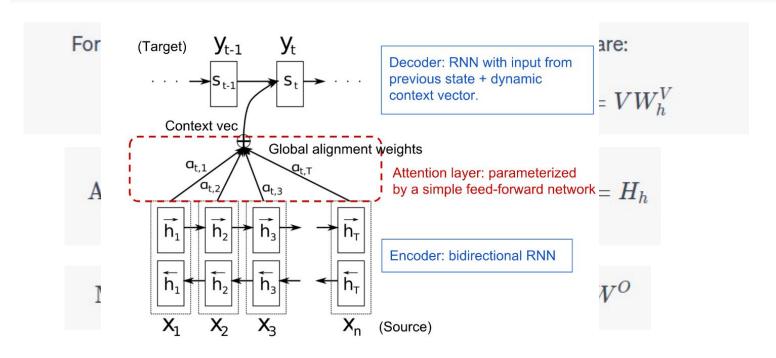


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Multi-Head Attention

Multi-head attention is an extension of the standard attention mechanism that allows the model to focus on different parts of the input for different tasks or reasoning, all in parallel. It's a cornerstone of transformer models and has found applications in various domains like NLP, computer vision, and even scientific disciplines like your fields of oceanography and medical imaging when sequential or structured data are involved.





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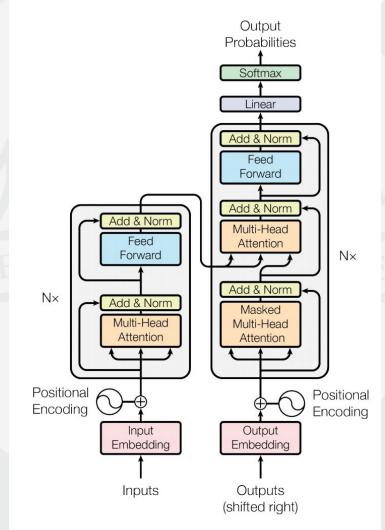


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Didn't have more time ... but

- Encoder Decoder
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- Skip connections
- Softmax in the output

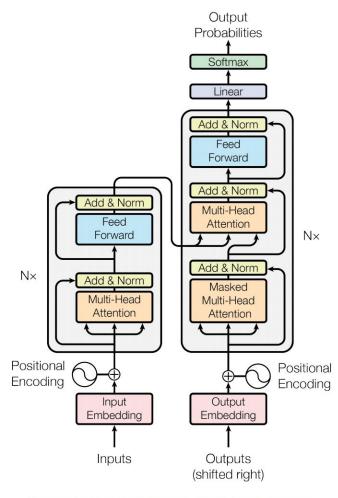


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Summary



Innovations:

- Self-Attention
- Multi-Head Attention
- Positional Embeddings

Relevance:

- NLP
- Computer Vision
- Etc.

Limitations:

- Computational cost
- Interpretability
- Lack of Recurrence
- Risk of Overfitting



Questions?



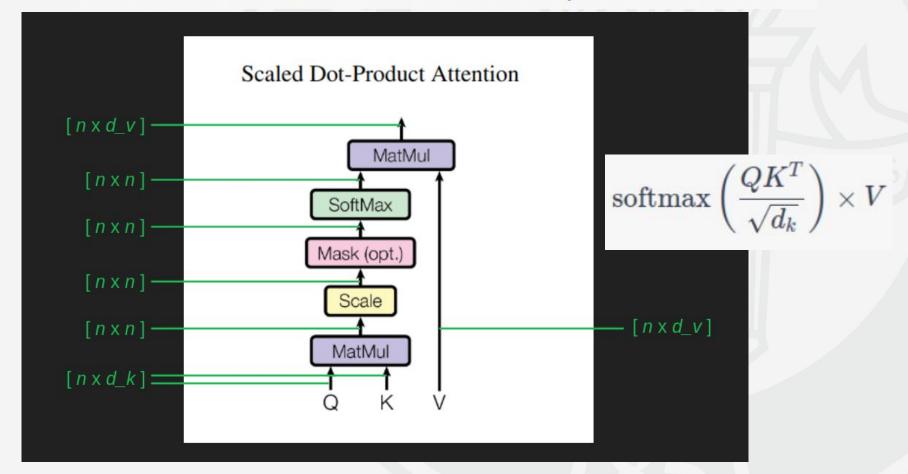




Scaled Dot-Product Attention



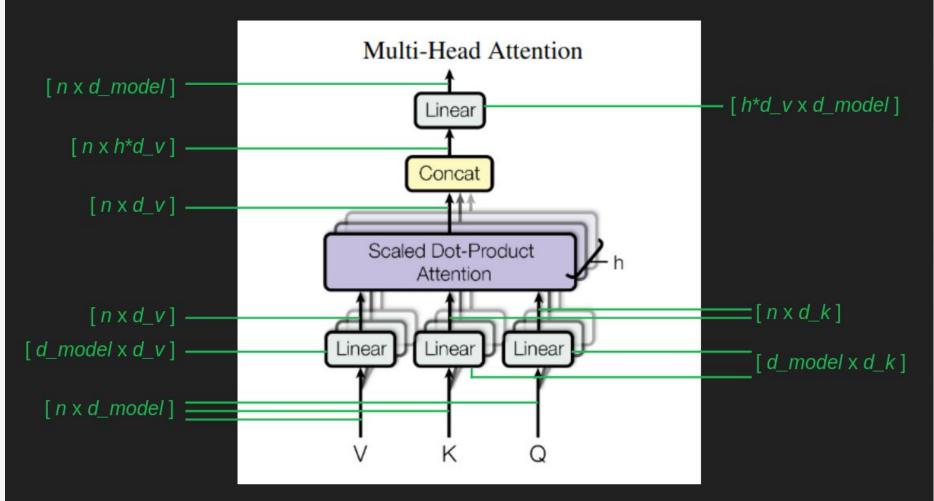
The Scaled Dot-Product Attention is a type of attention mechanism that calculates the importance of different parts in a sequence relative to each part. It's primarily used in Transformer models. The main components are Queries Q, Keys K, and Values V.





Multi-head Self-attention







Transformer Decoder



