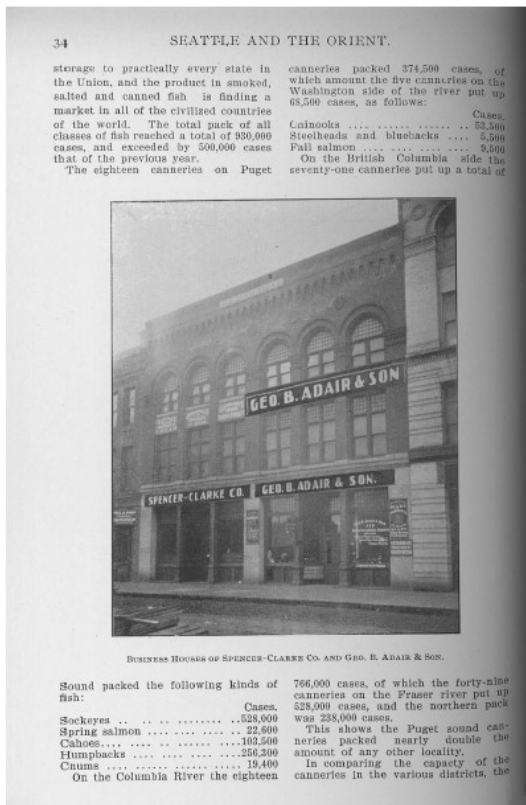


Sequence 5 exercises

1. Binarization of some scanned book pages (Homework)

Services like Internet Archive have digitized large collections of books. First, the book pages are scanned. Then, the scanned images are binarized and processed through an optical character recognition (OCR) engine. For modern books, the book spine can be removed to separate the book pages for more efficient scanning. For vintage books, however, destroying the original binding of the book is often undesirable. If a book is scanned with its spine left intact, the curvature of the pages causes uneven illumination in the resulting images. This effect can be observed in the following images.



Both images (*book_page_1.jpg* and *book_page_2.jpg*) are available in the *images* directory. Download the file *Sequence5_part1_code.py*.

- For each image, generate a binary image by performing a global thresholding. Use a threshold chosen by Otsu's method (cf. *threshold_otsu()* function). Display the binary image. Also, display the histogram of the original image and clearly mark the threshold of Otsu's method on this histogram. Comment on the quality of the binary image for text reading (do not take attention to the figures). What is the problem?
- Propose and implement a solution in order to improve the binarized image. Display the binary image by explaining your method to obtain it. Comment on the quality of the binary image for text reading compared to the result from part (a).

2. Kmean clustering (Classwork)

Download the file *Sequence5_part2_code.py*.

2.1 Kmean clustering based on luminance information

Proceed to the kmean segmentation of images *toyobjects.png*, *bacteria.tif* and *leopard.jpg*. In each case, guess the optimal number of clusters. Rmk: for the *bacteria.tif* image, we suppose there are two clusters only: bacteria and background.

Comment the obtained segmentations. Explain in each case why the kmean algorithm is efficient or not.

In order to post process the segmented image, apply some morphological operations. Explain your process.

2.2 Kmean clustering based on Gabor features

In order to improve the segmentation especially for the *leopard.jpg* image, let us consider Gabor filters. Gabor filters are filters sensitive to both frequency and orientation. They emphasize frequencies in a given orientation. Such a filter is defined by:

$$g_{\theta,f}(x,y) = \exp\left[-\frac{1}{2}\left(\frac{x_{\theta}^2}{\sigma_x^2} + \frac{y_{\theta}^2}{\sigma_y^2}\right)\right] \cos(2\pi f x_{\theta})$$

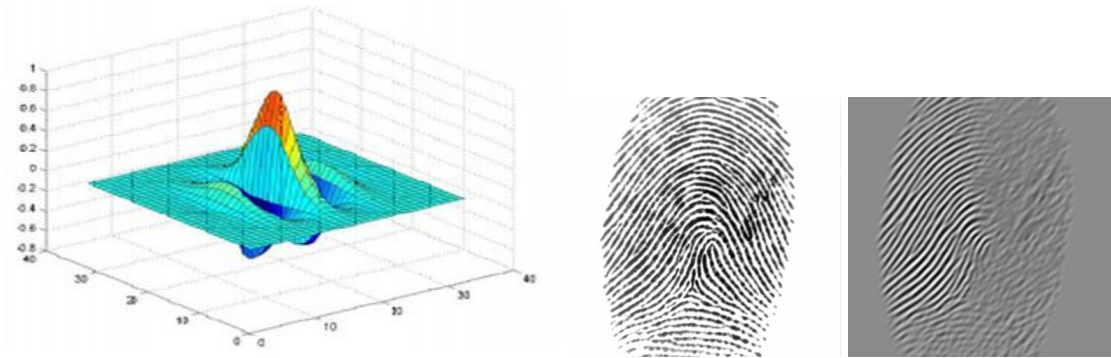
$$g_{\theta,f}(x,y) = \exp\left[-\frac{1}{2}\left(\frac{x_{\theta}^2}{\sigma_x^2} + \frac{y_{\theta}^2}{\sigma_y^2}\right)\right] \cos(2\pi f (x \sin \theta + y \cos \theta))$$

$$\begin{bmatrix} x_{\theta} \\ y_{\theta} \end{bmatrix} = \begin{bmatrix} \cos(90^{\circ} - \theta) & \sin(90^{\circ} - \theta) \\ -\sin(90^{\circ} - \theta) & \cos(90^{\circ} - \theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} \sin \theta & \cos \theta \\ -\cos \theta & \sin \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Where: θ is the filter orientation, f : is the sine filter frequency, σ_x , σ_y are the standard deviations of the exponential envelop.

Rmk: theoretically, the full expression of Gabor filter introduces also a complex term in the expression which is $i \cdot \sin(\dots)$ ($\exp[\dots] * (\cos(\dots) + i \cdot \sin(\dots))$) but here we have written the real part of the answer only.

The following figure presents an example of Gabor filter transfer function with the exponential envelop and the sine evolution. The figure shows the effect of such a filter tuned on 45° on a fingerprint image. It appears that the lines in the 45° orientation are highlighted.



Implement the Gabor filtering (cf. *skimage.filters* module) of the image to be segmented by considering the frequency=0.5 and 8 orientations ($0, \pi/8, \pi/4, \dots, 7\pi/8$). Filter the *leopard.jpg* image with the 8 oriented filters and compute the magnitude of the Gabor filter answer for each orientation. Before displaying the results, smooth each answer by applying a Gaussian filter with $\sigma = 3$ on each magnitude map.

In order to improve the segmentation result, the idea is to apply the kmean algorithm on the best Gabor map instead on the luminance map. If necessary, tune the Gabor filters parameters in order to obtain the best Gabor map (define first what a good Gabor map is in your opinion). Display the obtained segmentation.

In order to post process the segmented image, apply some morphological operations. Explain your process.