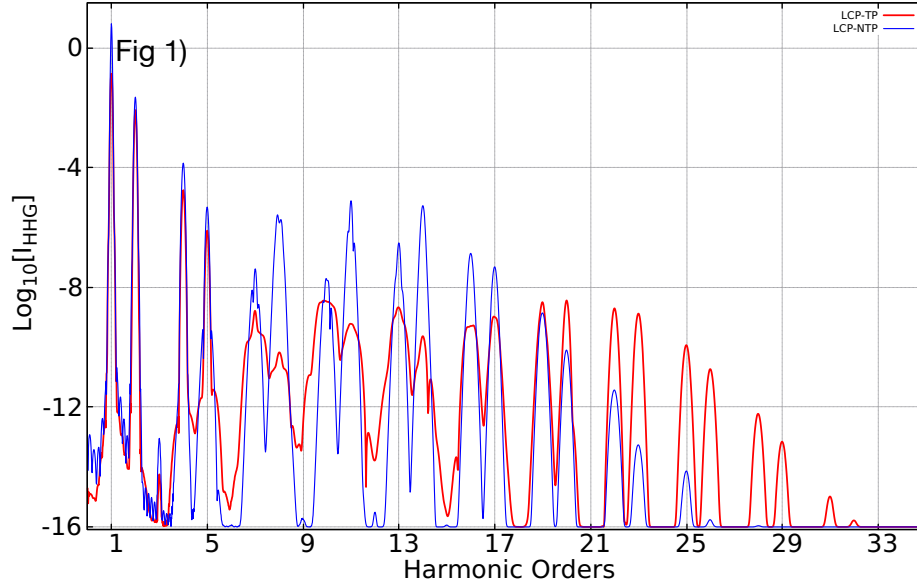


# Reports on topological phases and harmonic generation: circular polarized laser field driver

September 21, 2019

## Topological dependence of high-order harmonic generation

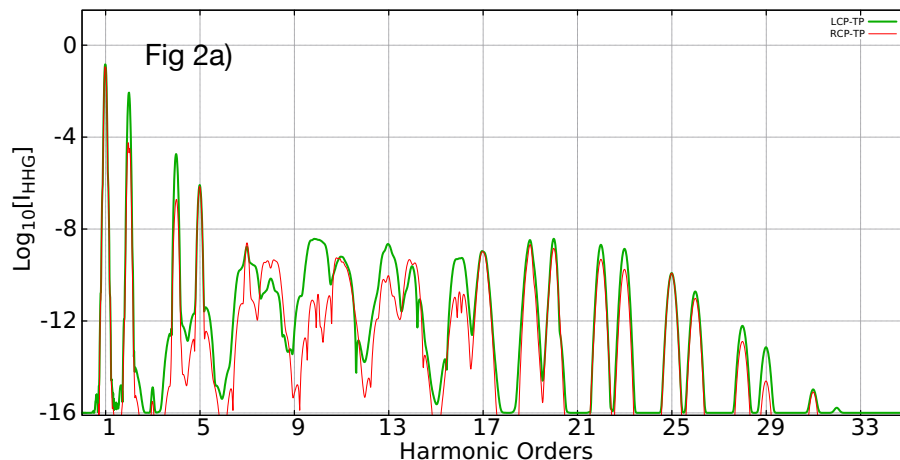


**Fig. 1)** Blue line (topological non-trivial phase) and red line (topological trivial phase) depict the high-order harmonic generation (HHG) for two different topological phases of Haldane model (HM) while a left-handed circularly polarized (LCP) driven laser of field strength  $E_0 =$

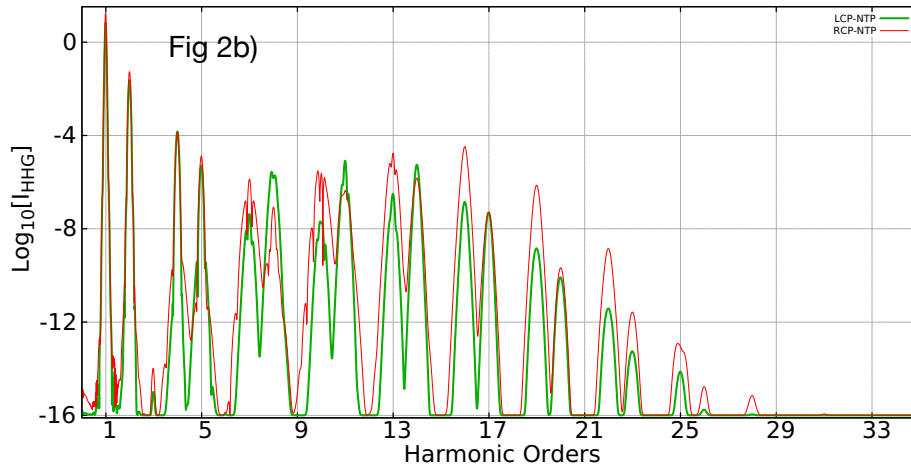
0.005 a.u. and the photon energy is  $w_0 = 0.015$  a.u. drives the crystalline Haldane lattice. The dephasing time was fixed to  $T_2 = 220$  a.u. and the band gap for both topological phase are equals,  $E_g = 0.112$  a.u. The Haldane model parameters are  $\phi_0 = 0.06$  rad for trivial phase,  $\phi_0 = 1.16$  rad for the topological phase, while  $M_0/t_2 = 2.54$  keep constants.

For this numerical results, we can appreciate a huge enhancement of the topological harmonic orders for the topological phase ( $C=+1$ , Chern No.) around the cut-off than those HOs corresponded to the trivial phase ( $C=0$ , Chern No.)

## Circular Dichroism for trivial and non trivial phase



**Fig 2a)** This figure shows the HHG spectra for LCP and Right-handed and circularly polarized (RCP) in green and red, respectively for similar parameters



of the trivial phase used in Fig 1) .

The HHG spectrum shows a remarkable **negative dichroism** for the plateau and cut-off around the  $3n+1$ , but positive in the cut-off for  $3n+2$ . Fig 2b) In green and red lines, we have the HHG spectra for LCP and RCP within a topological phase

where  $\phi_0 = 1.16$  rad. Laser field parameters used here are the same than those used in Fig 1) and the dephasing time too,  $T_2 = 220$  a.u.

## Topological phase transition using circular Dichroism (CD)

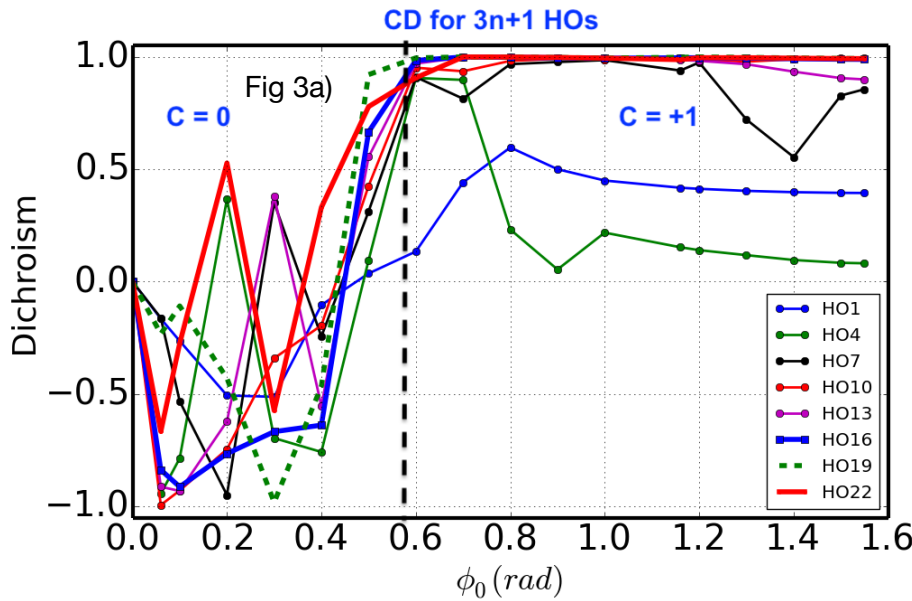


Fig 3a) Depicts the circular dichroism (CD) as a **function of the MAGNETIC FLUX PHASE,  $\phi_0$** , and  $M_0/t_2 = 2.54$  of Haldane Model for every harmonic order corresponding to  $3n + 1$ . The laser pulse is a large pulse of 36 cycles under a  $\cos^2$  envelope and with a laser field strength of  $E_0 = 0.0045$  a.u.

dashed vertical line approximately speaking. Chern No. is +1 for  $\phi_0 > 0.51$  (fully topological non-trivial phase).

First of all, one can notice from Fig3a), there is a potential to distinguish trivial phase from non-trivial phase by the CD, since CD is mostly negative for trivial phase while CD is positive for non-trivial phase in average for most of the  $3n+1$  HOs.

Secondly, for the trivial phase, the CD is fluctuating between positive and negative values. This is attributed mainly to time dephasing effects as the Fig. 4 will show.

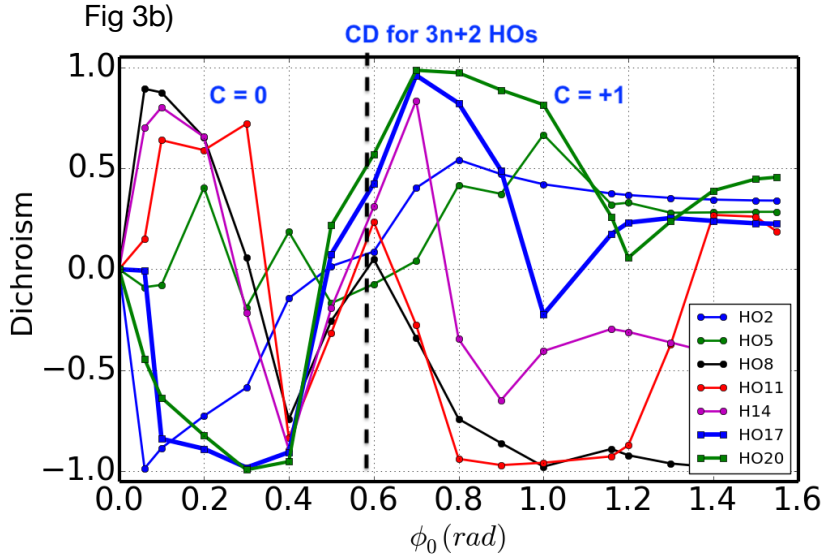


Fig 3b) CD as a function of the magnetic flux phase,  $\phi_0$ , corresponding to each HOs  $3n+2$ .

The CD of this  $3n+2$  harmonics are not really clear quantity to distinguish one topological phase from other.

This plot CD in 3b) is in contrast to what it is observed in 3a). There is a set of possible reasons or, 1) dephasing time, 2) nature of the breaking symmetries, Time-reversal symmetry and space-inversion symmetry sensitivity of those  $3n+2$  Harmonic orders. Perhaps, there exist another couple of reason why we have this chaotic behaviors on the HHG HOs, but so far, this two I suspect are the most reasonable one. however, I don't know.

## Dephasing Study

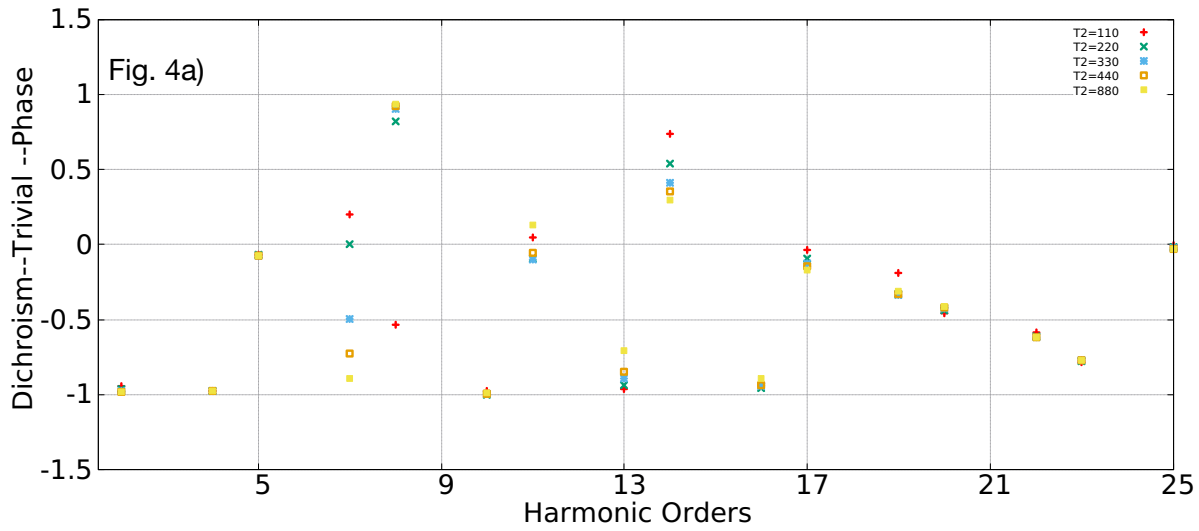


Fig 4a) Shows the CD of HHG spectrum for a trivial phase of Haldane model with  $M_0/t_2 = 2.54$  and  $\phi_0 = 0.06$  rad for each HO as a function of the dephasing time  $T_2$ . The CD for HOs>5th is **EXTREMELY SENSITIVE** to the choice of the Dephasing time in particular around the plateau and cut-off.

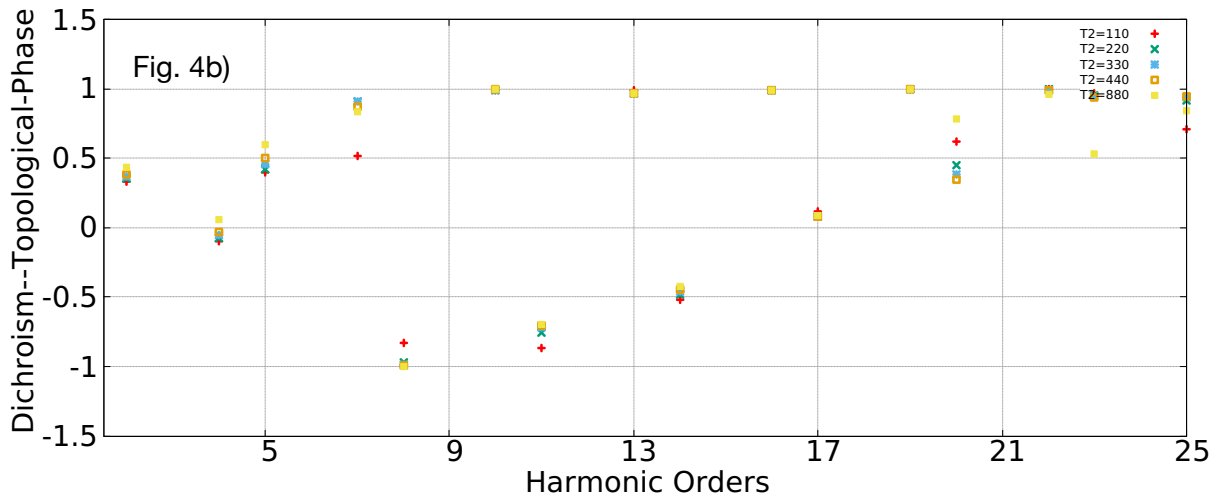


Fig 4b) shows the CD of the HHG spectrum for an non-trivial phase of HM with  $M_0/t_2 = 2.54$ , and  $\phi_0 = 1.16$  rads for each HO as a function of the dephasing time  $T_2$ .

These Fig 4a) — 4b) clearly show CD depends on the dephasing time for the HOs  $3n+2$  (some of them around  $3n+1$ ) around the plateau and cut-off. The most robust dichroism is observed for the nontrivial phase and HOs  $3n+1$ .

**One can infer easily or obviously than the  $3n+1$  CD** would be strongest one, once we try to scan topological phase transition along  $\phi_0$  axis of HM and its phase diagram. Additionally, Fig 3a) is showing that **this CD can potentially be sensitive to the respectively dephasing time used at each MAGNETIC FLUX PHASE,  $\phi_0$ .**

This dephasing time dependence of the harmonic yield with respect to  $\phi_0$  or min band-gap between conduction and valence band, is the main source of noise for the CD shown in Fig 3a) along the trivial phase. This is a clear hypothesis and obvious, since the dephasing time is a material dependent quantity, if you don't understand it, just, please go to literature and search by yourself.