"Forecasting: Principles and Practice" Notes

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Chapter 1: Getting Started

Types of Quantitative Forecasts

- Cross-sectional Data
 - Given a set of parameters, try to *predict* an outcome based on data. For example, predict the house price based on number of bedrooms, bathrooms, etc.
- Time series Data
 - Forecast future outcome based on historical data

Basic Steps of Forecasting

- 1. Problem Definition
- 2. Gathering Information
- 3. Exploratory Analysis
- 4. Choosing and Fitting Models
- 5. Using and Evaluating Model

Chapter 2: Forecaster's Toolbox

Graphs

First thing to do for any forecasting exercise is to plot the data to look for patterns or any abnormalities.

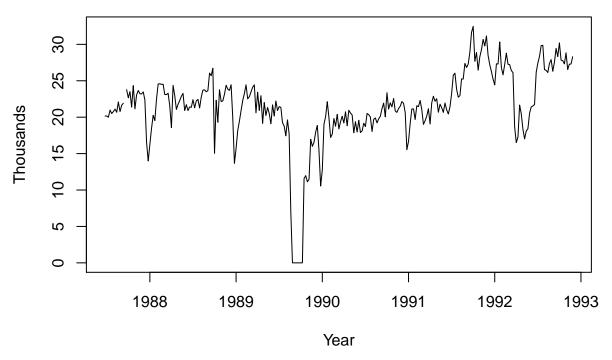
Time Plots

aka Line graphs.

Example 1

```
data(melsyd)
plot(melsyd[,"Economy.Class"],
   main="Economy class passengers: Melbourne-Sydney",
   xlab="Year",ylab="Thousands")
```

Economy class passengers: Melbourne-Sydney



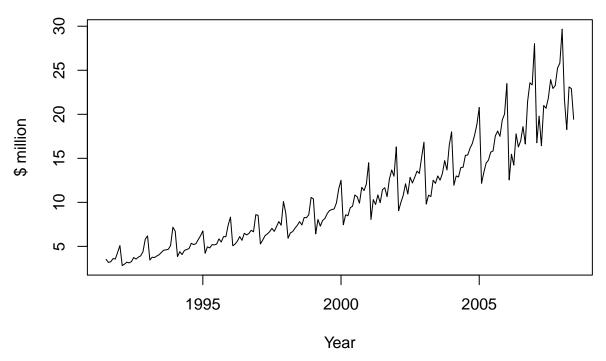
Notes:

- Missing data in 1989 industrial dispute
- Dip in 1992 trial which replaced some economy class seats with business class
- Large increase in 1991
- etc

Example 2

```
data(a10)
plot(a10, ylab="$ million", xlab="Year", main="Antidiabetic drug sales")
```

Antidiabetic drug sales



Notes:

- Seasonality
- Upward trend

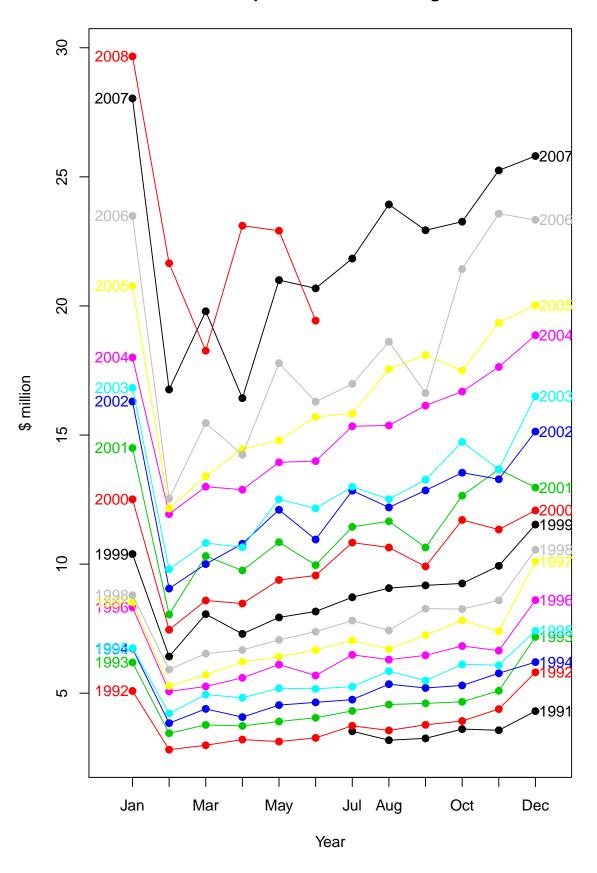
Common Time Series Patterns

- Trend
- Seasonality
- \bullet $\,$ Cycles rises and falls that are not of a fixed period

Seasonal Plots

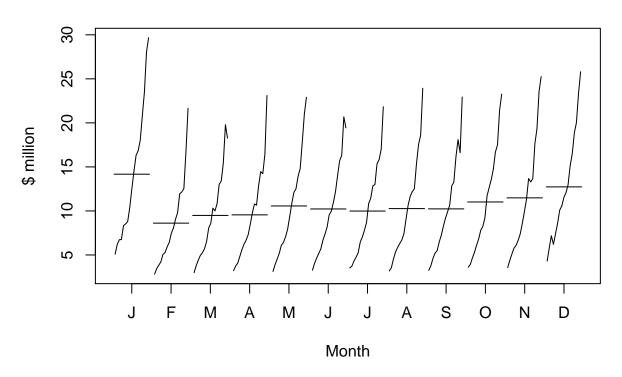
Line plots comparing each season.

Seasonal plot: antidiabetic drug sales



```
monthplot(a10,
   ylab='$ million',
   xlab='Month',
   main='Seasonal deviation plot: antidiabetic drug sales')
```

Seasonal deviation plot: antidiabetic drug sales



Scatterplots

Useful for analyzing cross-sectional data

Summary Statistics

Univariate statistics

Can simply use *summary* function on the data.

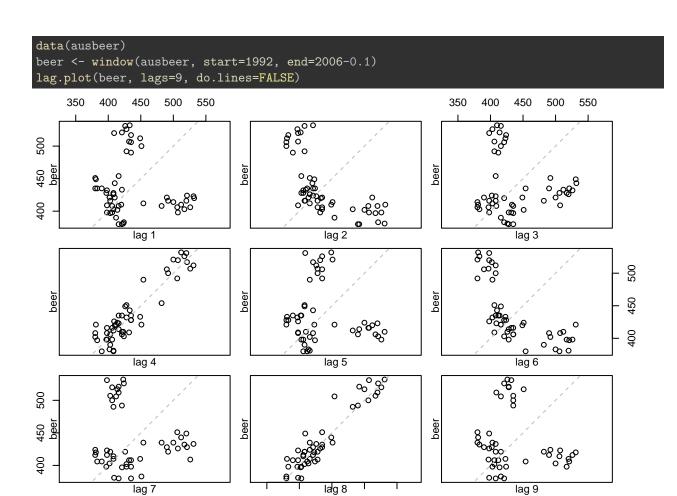
Bivariate statistics

Correlation coefficient: r

$$r = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2} \sqrt{\sum (y_i - \overline{y})^2}}$$

Autocorrelation

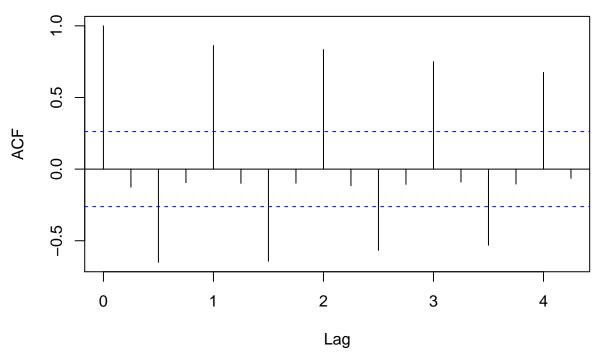
Used to test correlation on lag r_1 tests correlation on lag r_2 tests correlation on lag r_2 , etc.



Each lag has a corresponding correlation value r. These correlation values are plotted to form an *autocorrelation* function or ACF. The plot is known as a correlogram.

acf(beer)

Series beer



Notes:

- r_4 at lag 4 has the highest correlation because seasonal patterns happen every four quarters
- Negative correlations happen two quarters after peaks

Time series that show no autocorrelation are called *white noise*. Acf plot will show no significant correlations for any lag periods.

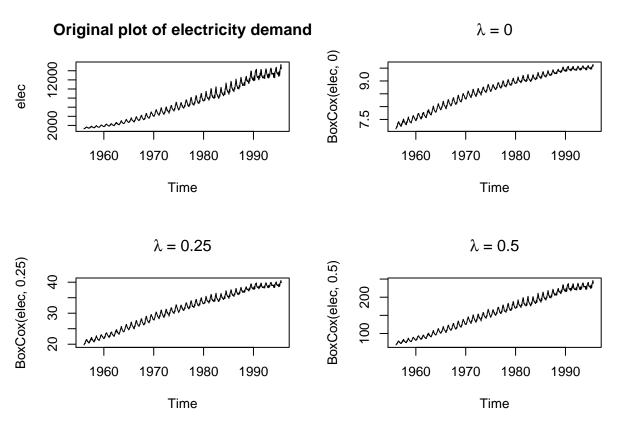
Simple forecasting methods

- ullet Mean just the mean of historical values for all forecasted values.
- Naive just the last actual value for all forecasted values.
- Seasonal Naive variation of naive. Uses the last value of some period last season.
- **Drift** variation of naive. Allows forecast to increase or decrease over time (the *drift*) based on average change.

Transformations

Log and power transformations are common. Box-Cox Transformations is a useful family of log and power transformations. If the coefficient λ is 0, it does a natural log, otherwise it does a power transformation. λ can be between 0 and 1. A good lambda will transform the data such that each seasonal swing is roughly equal. Running the function BoxCox.lambda(data) will choose a λ for you. In this case, it will choose 0.27.

```
data(elec)
par(mfrow=c(2, 2))
plot(elec, main='Original plot of electricity demand')
plot(BoxCox(elec, 0), main=expression(paste(lambda, ' = 0')))
plot(BoxCox(elec, 0.25), main=expression(paste(lambda, ' = 0.25')))
plot(BoxCox(elec, 0.5), main=expression(paste(lambda, ' = 0.5')))
```



After transforming, we need to make a forecast on the transformed data. Then we need to *back transform* to obtain the forecast in the original scale.

Evaluating forecast accuracy

Scale-dependent errors

Forecast error is simply $e_i = y_i - \hat{y}_i$ where y_i is actual and \hat{y}_i is forecast. Two common measures are:

Mean absolute error: MAE =
$$mean(|e_i|)$$

Root mean squared error: RMSE = $\sqrt{mean(e_i^2)}$

MAE is most common, however can only be compared to values on the same scale, or on the same data set.

Percentage errors

Scale independent so can compare errors from different data sets. This can be calculated as $p_i = 100e_i/y_i$. The most commonly used measure is:

Mean absolute percentage error: MAPE = $mean(|p_i|)$

This can present the problem is any value y_i is 0 or close to 0.

Scaled errors

Scaled errors are used as an alternative to percentage errors. The mean absolute scaled error or MASE is a commonly used one (alternatively mean squared scaled error or MSSE is used).

Example

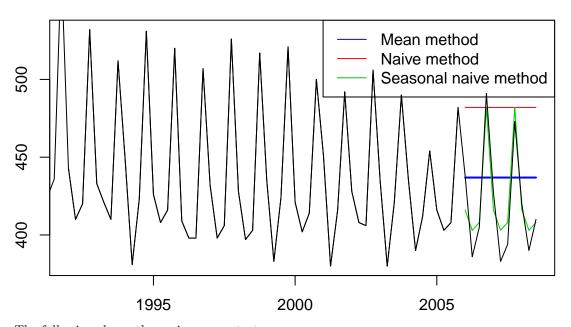
```
beer2 <- window(ausbeer,start=1992,end=2006-.1)

beerfit1 <- meanf(beer2,h=11)
beerfit2 <- rwf(beer2,h=11)

plot(beerfit3 <- snaive(beer2,h=11)

plot(beerfit1, plot.conf=FALSE,
    main="Forecasts for quarterly beer production")
lines(beerfit2$mean,col=2)
lines(beerfit3$mean,col=3)
lines(ausbeer)
legend("topright", lty=1, col=c(4,2,3),
    legend=c("Mean method","Naive method","Seasonal naive method"))</pre>
```

Forecasts for quarterly beer production



The following shows the various error tests:

```
beer3 <- window(ausbeer, start=2006)</pre>
accuracy(beerfit1, beer3)
                                                                 MAPE
                            ME
                                   RMSE
                                              MAE
                                                         MPE
                                                                           MASE
## Training set 8.121418e-15 44.17630 35.91135 -0.9510944 7.995509 2.444228
                 -1.718344e+01 38.01454 33.77760 -4.7345524 8.169955 2.298999
## Test set
##
                        ACF1 Theil's U
## Training set -0.12566970
                                    NA
## Test set
                -0.08286364 0.7901651
```

accuracy(beerfit2, beer3)

```
##
                         ME
                                 RMSE
                                           MAE
                                                       MPE
                                                                MAPE
                                                                         MASE
                  0.7090909 66.60207 55.43636
## Training set
                                                -0.8987351 12.26632 3.773156
## Test set
                -62.2727273 70.90647 63.90909 -15.5431822 15.87645 4.349833
##
                       ACF1 Theil's U
## Training set -0.25475212
## Test set
                -0.08286364
                             1.428524
```

accuracy(beerfit3, beer3)

```
##
                               RMSE
                                                    MPE
                                                             MAPE
                                                                       MASE
                       ME
                                         MAE
## Training set -1.846154 17.24261 14.69231 -0.4803931 3.401224 1.0000000
                -2.545455 12.96849 11.27273 -0.7530978 2.729847 0.7672537
## Test set
                      ACF1 Theil's U
## Training set -0.3408329
                                   NA
## Test set
                -0.1786912
                              0.22573
```

Here we see that the seasonal naive method is best.

Residual diagnostics

Residuals are simply the difference between the forecast and actual value $e_i = y_i - \hat{y}_i$. A good forecast will yield residuals with the following properties:

- Residuals are uncorrelated. If you find correlations then there was something not included in the forecasting model.
- Residuals have zero mean. A non-zero mean means forecast is biased.

If the above properties are not satisfied, then forecast can be improved. If residuals have a mean m, then simply adding m to all forecasts will solve the problem. Fixing the correlation problem will be explained in **Chapter 8**.

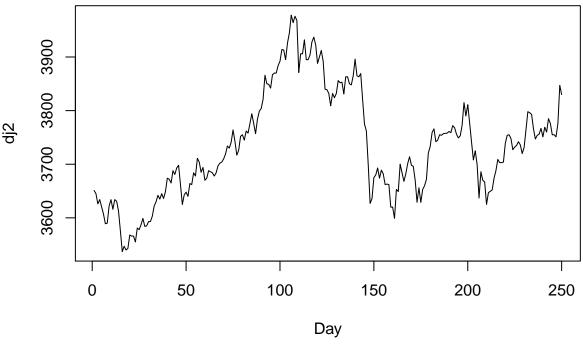
The following two properties are not required, but useful:

- Residuals have constant variance.
- Residuals are normally distributed.

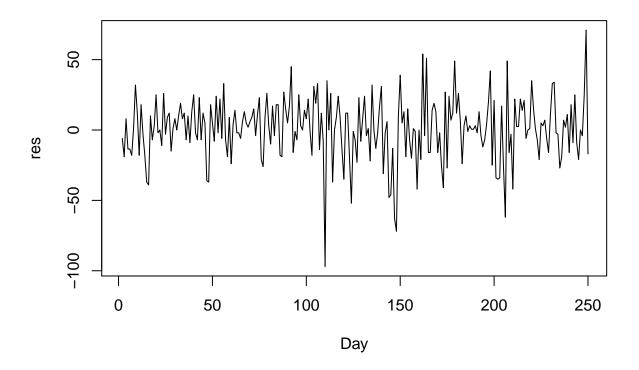
Example: Dow Jones

Naive method is usually best for stocks. Therefore, residuals are simply the difference between consecutive observations.

Dow Jones Index (daily ending 1994-07-15)

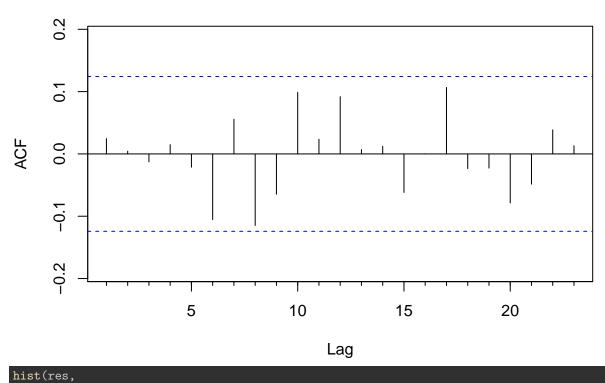


Residuals from naive method



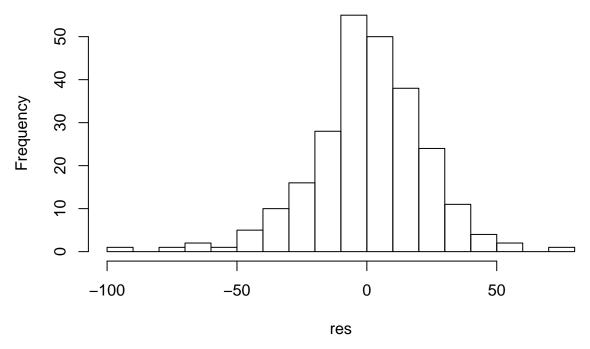
Acf(res,
 main='ACF of residuals')

ACF of residuals



```
nist(res,
    nclass='FD',
    main='Histogram of residuals')
```

Histogram of residuals



Notes:

- [x] Residuals are not correlated.
- [x] Residuals are close to zero.
- [x] Residuals have constant variance.
- [] Not quite normally distributed so prediction intervals may be inaccurate.

Portmanteau tests for autocorrelation

Test if autocorrelation is the result of white noise. Portmanteau test

Simple regression

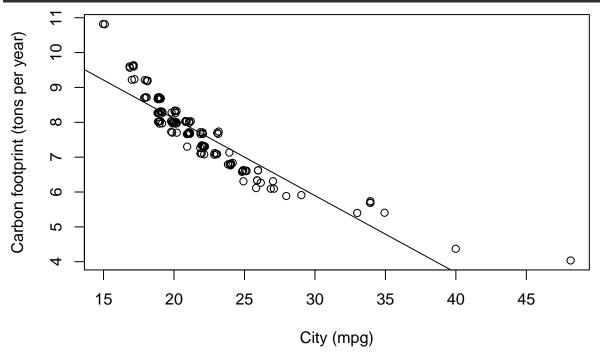
Fit a line over observations where it minimizes the sum of square errors:

$$\sum_{i=1}^{N} \epsilon_i^2$$

The correlation coefficient r shows how much x predicts y.

Example: Car emission

fit <- lm(Carbon ~ City, data=fuel) abline(fit)</pre>

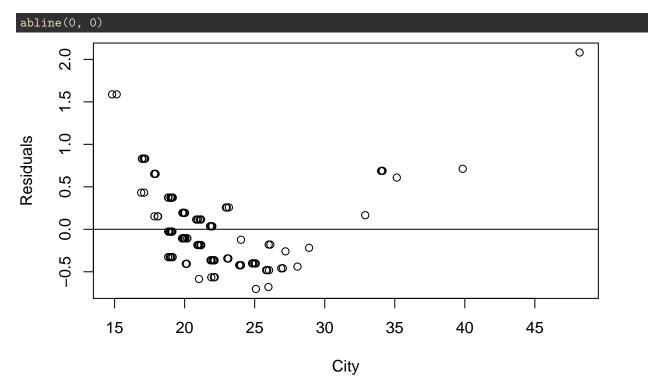


summary(fit)

```
##
## Call:
## lm(formula = Carbon ~ City, data = fuel)
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
## -0.7014 -0.3643 -0.1062 0.1938 2.0809
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 12.525647
                          0.199232
                                     62.87
                                             <2e-16 ***
                          0.008878
## City
              -0.220970
                                    -24.89
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4703 on 132 degrees of freedom
## Multiple R-squared: 0.8244, Adjusted R-squared: 0.823
## F-statistic: 619.5 on 1 and 132 DF, p-value: < 2.2e-16
```

Evaluating regression models

```
res <- residuals(fit)
plot(jitter(res) ~ jitter(City),
     ylab='Residuals',
     xlab='City',
     data=fuel)</pre>
```



We see that there is a U-shaped pattern and therefore a simple linear model may not be appropriate.

Outliers

An outlier is considered an influential observation if it has a large impact on the regression model

Example: Predicting weight from height

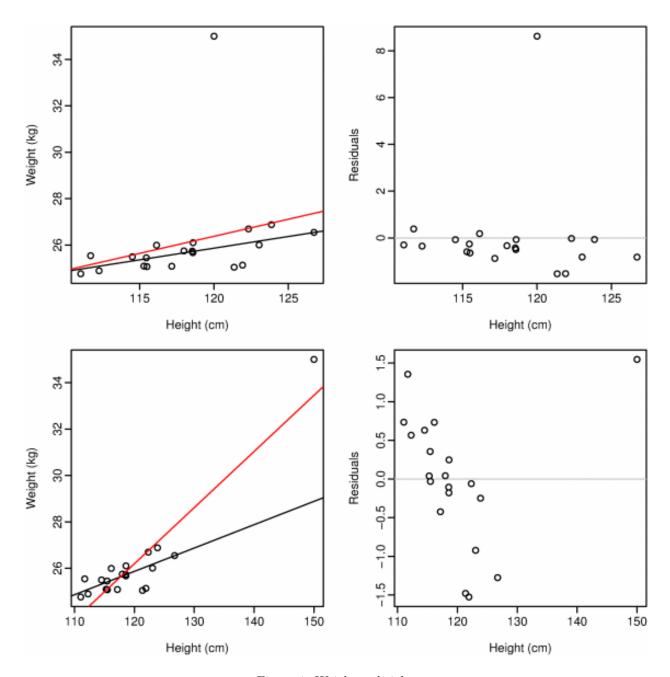


Figure 1: Weight vs height