"Forecasting: Principles and Practice" Notes

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Contents

Chapter 1: Getting Started

Types of Quantitative Forecasts

- Cross-sectional Data
  - Given a set of parameters, try to *predict* an outcome based on data. For example, predict the house price based on number of bedrooms, bathrooms, etc.
- Time series Data
  - Forecast future outcome based on historical data

Basic Steps of Forecasting

1. Problem Definition
2. Gathering Information
3. Exploratory Analysis
4. Choosing and Fitting Models
5. Using and Evaluating Model

Chapter 2: Forecaster's Toolbox

Graphs

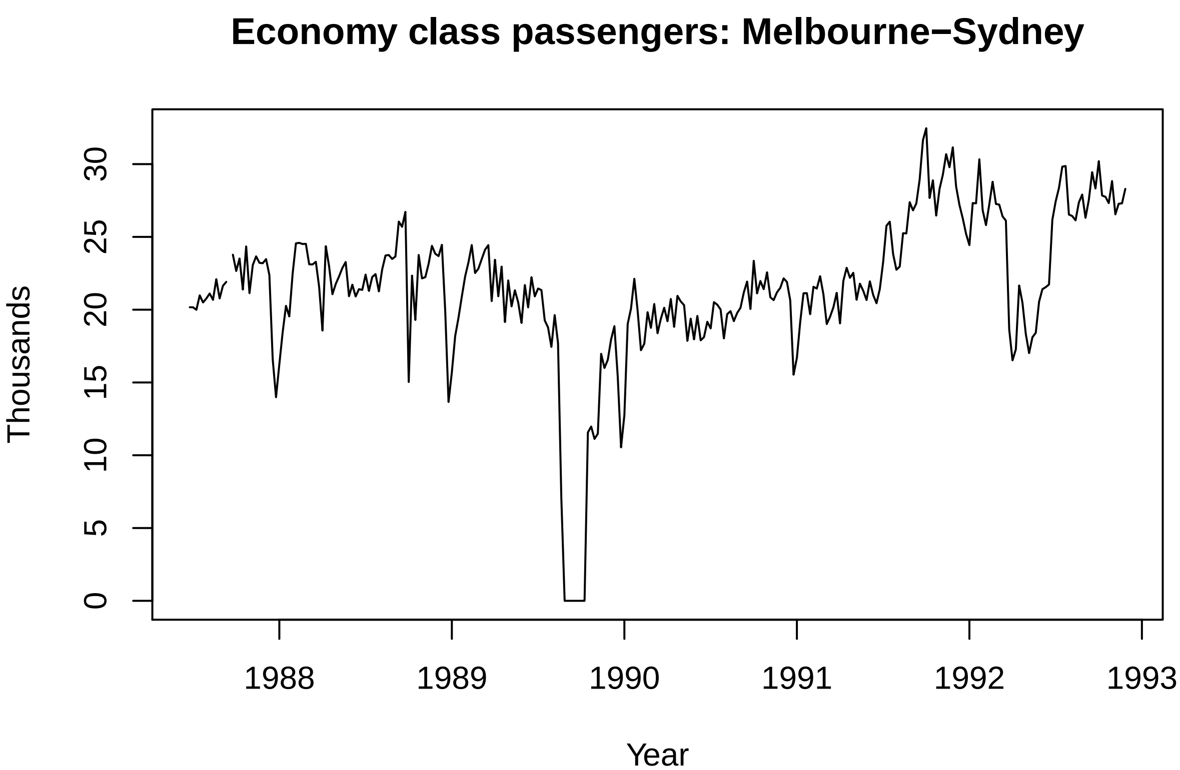
First thing to do for any forecasting exercise is to plot the data to look for patterns or any abnormalities.

Time Plots

aka Line graphs.

Example 1

```
data(melsyd)
plot(melsyd[,"Economy.Class"],
  main="Economy class passengers: Melbourne-Sydney",
  xlab="Year",ylab="Thousands")
```

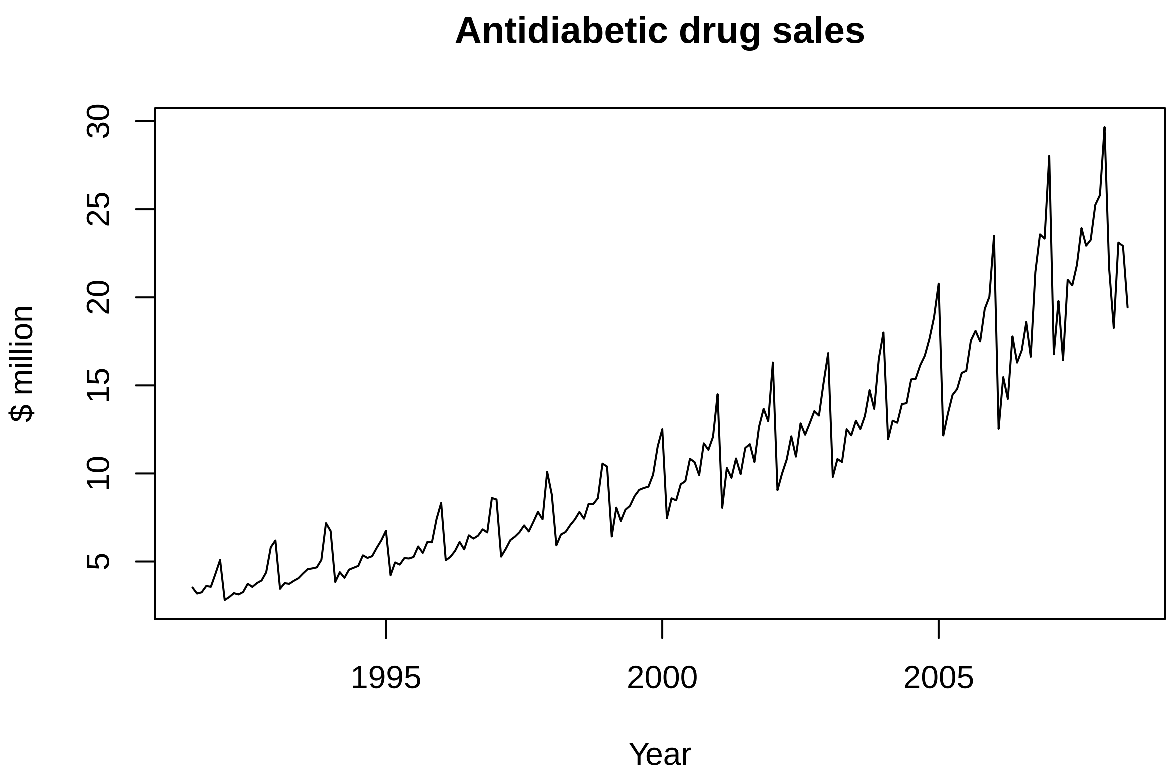


Notes:

- Missing data in 1989 – industrial dispute
- Dip in 1992 – trial which replaced some economy class seats with business class
- Large increase in 1991
- etc

Example 2

```
data(a10)
plot(a10, ylab="$ million", xlab="Year", main="Antidiabetic drug sales")
```



Notes:

- Seasonality
- Upward trend

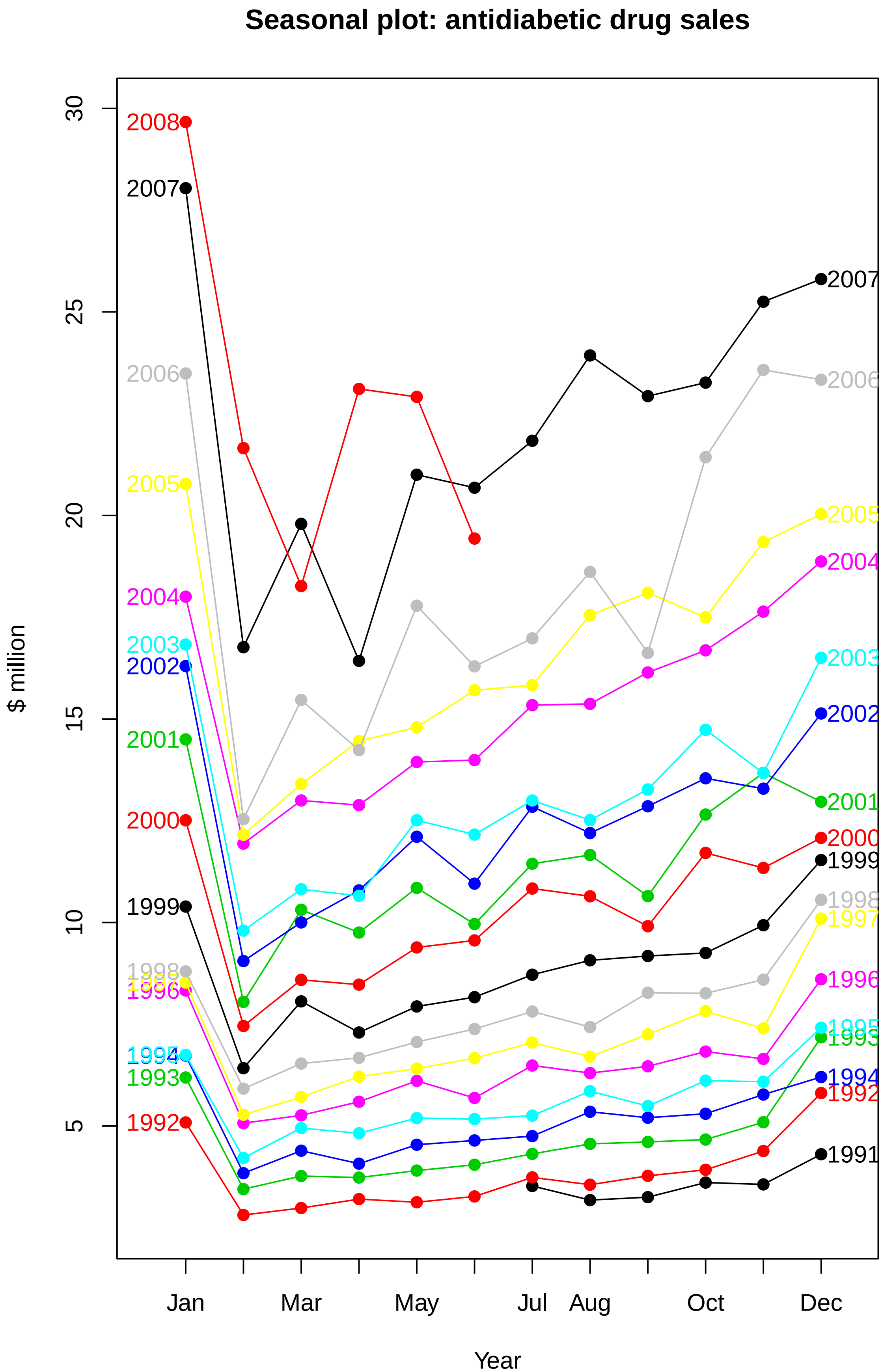
Common Time Series Patterns

- **Trend**
- **Seasonality**
- **Cycles** – rises and falls that are not of a fixed period

Seasonal Plots

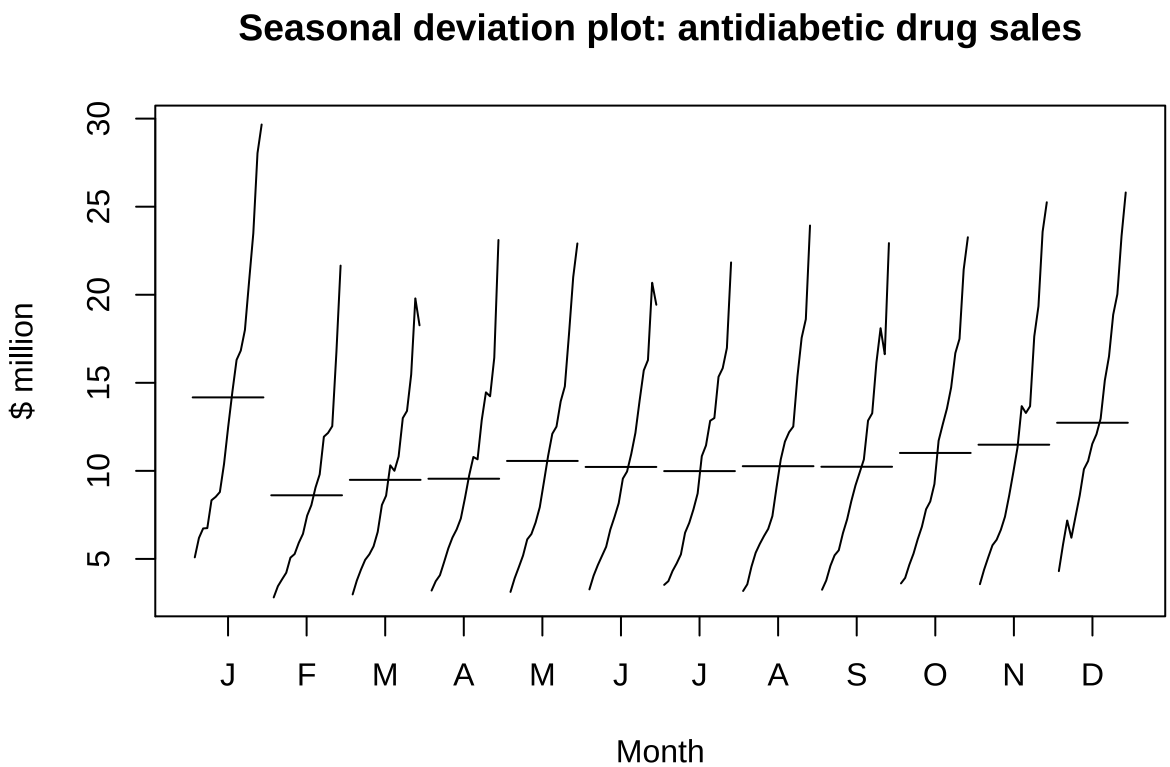
Line plots comparing each *season*.

```
seasonplot(a10,
           ylab='$ million',
           xlab='Year',
           main='Seasonal plot: antidiabetic drug sales',
           year.labels=TRUE,
           year.labels.left=TRUE,
           col=1:20,
           pch=19)
```



Seasonal plot: antidiabetic drug sales
$ million
Year
Jan
Mar
May
Jul
Aug
Oct
Dec
2008
2007
2006
2005
2004
2003
2002
2001
2000
1999
1998
1997
1996
1995
1994
1993
1992
1991

```r
monthplot(a10,
          ylab='$ million',
          xlab='Month',
          main='Seasonal deviation plot: antidiabetic drug sales')
```



Scatterplots

Useful for analyzing cross-sectional data

Summary Statistics

Univariate statistics

Can simply use *summary* function on the data.

Bivariate statistics

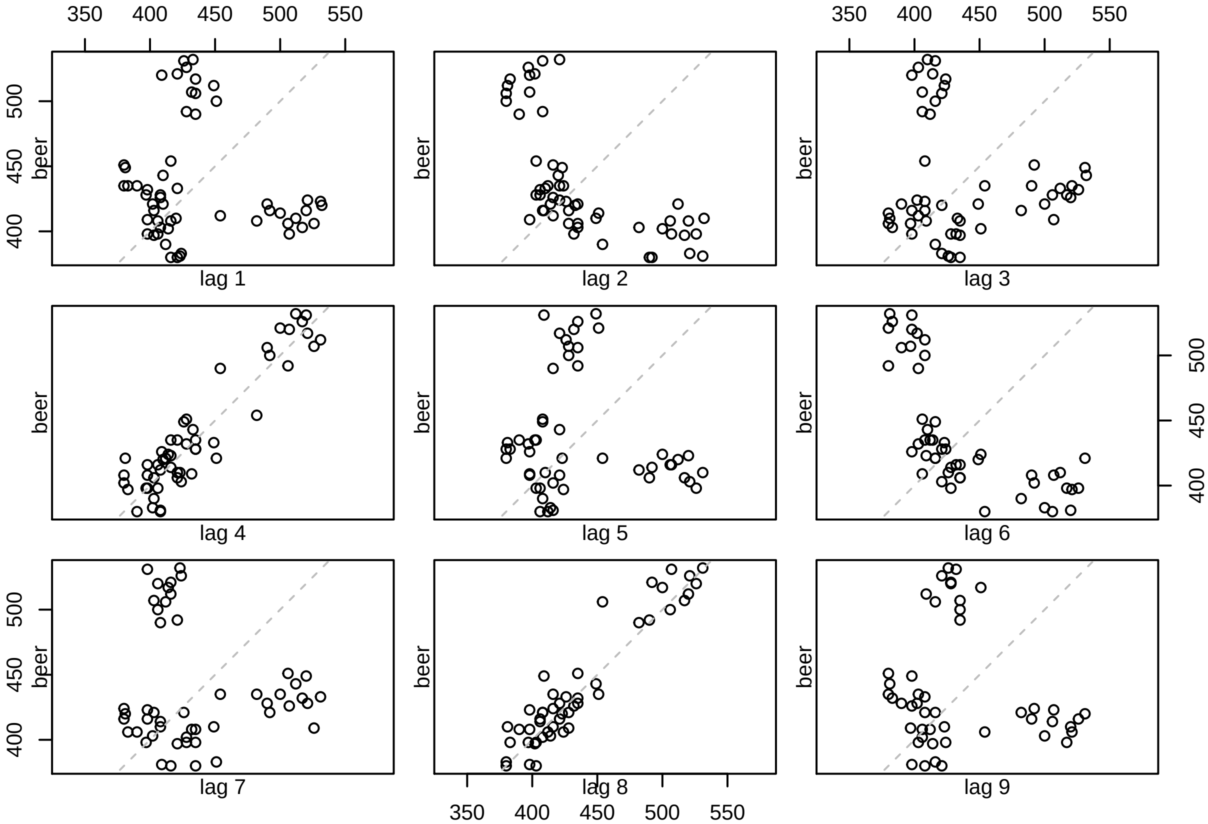
Correlation coefficient: r

$$r = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2}\sqrt{\sum (y_i - \overline{y})^2}}$$

Autocorrelation

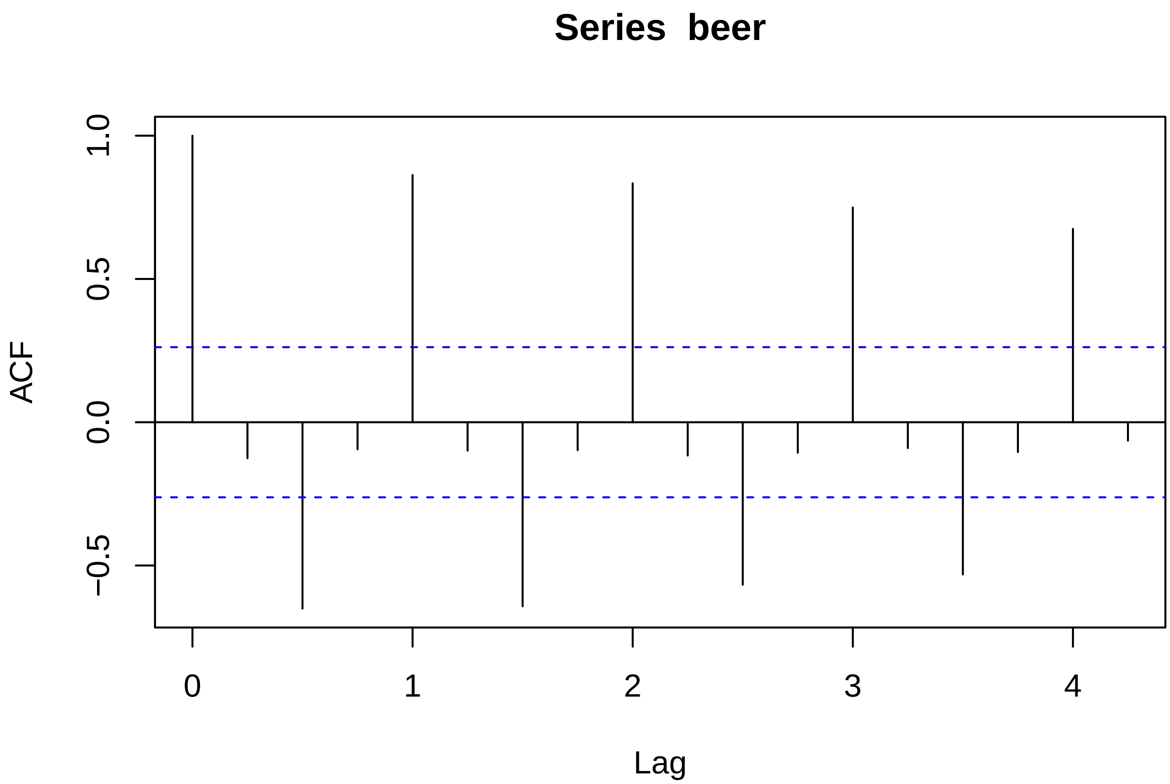
Used to test correlation on lag. r_1 tests correlation on lag 1, r_2 tests correlation on lag 2, etc.

```
data(ausbeer)
beer <- window(ausbeer, start=1992, end=2006-0.1)
lag.plot(beer, lags=9, do.lines=FALSE)
```



Each lag has a corresponding correlation value r. These correlation values are plotted to form an *autocorrelation function* or *ACF*. The plot is known as a *correlogram*.

```
acf(beer)
```



Notes:

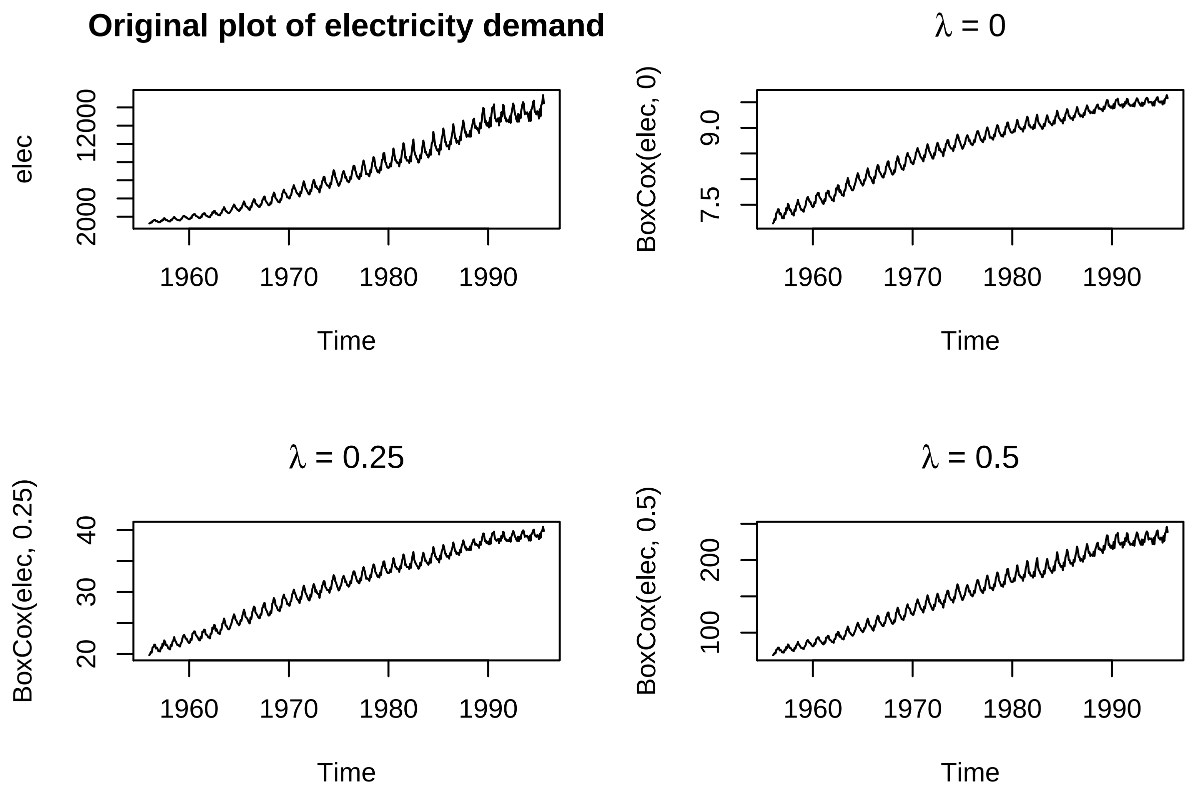
- r_4 at lag 4 has the highest correlation because seasonal patterns happen every four quarters
- Negative correlations happen two quarters after peaks

Time series that show no autocorrelation are called *white noise.*Acf plot will show no significant correlations for any lag periods.

Transformations

Log and power transformations are common. *Box-Cox Transformations* is a useful family of log and power transformations. If the coefficient λ is 0, it does a natural log, otherwise it does a power transformation. λ can be between 0 and 1. A good lambda will transform the data such that each seasonal swing is roughly equal. Running the function *BoxCox.lambda(data)* will choose a λ for you. In this case, it will choose 0.27.

```
data(elec)
par(mfrow=c(2, 2))
plot(elec, main='Original plot of electricity demand')
plot(BoxCox(elec, 0), main=expression(paste(lambda, ' = 0')))
plot(BoxCox(elec, 0.25), main=expression(paste(lambda, ' = 0.25')))
plot(BoxCox(elec, 0.5), main=expression(paste(lambda, ' = 0.5')))
```



After tranforming, we need to make a forecast on the transformed data. Then we need to *back transform* to obtain the forecast in the original scale.

Evaluating forecast accuracy

Scale-dependent errors

Forecast error is simply $e_i = y_i - \hat{y}_i$ where y_i is actual and $\hat{y}_i$ is forecast. Two common measures are:

$$\text{Mean absolute error: MAE} = mean(|e_i|)$$

$$\text{Root mean squared error: RMSE} = \sqrt{mean(e_i^2)}$$

MAE is most common, however can only be compared to values on the same scale, or on the same data set.

Percentage errors

Scale independent so can compare errors from different data sets. This can be calculated as $p_i = 100e_i/y_i$. The most commonly used measure is:

$$\text{Mean absolute percentage error: MAPE} = mean(|p_i|)$$

This can present the problem is any value y_i is 0 or close to 0.

Scaled errors

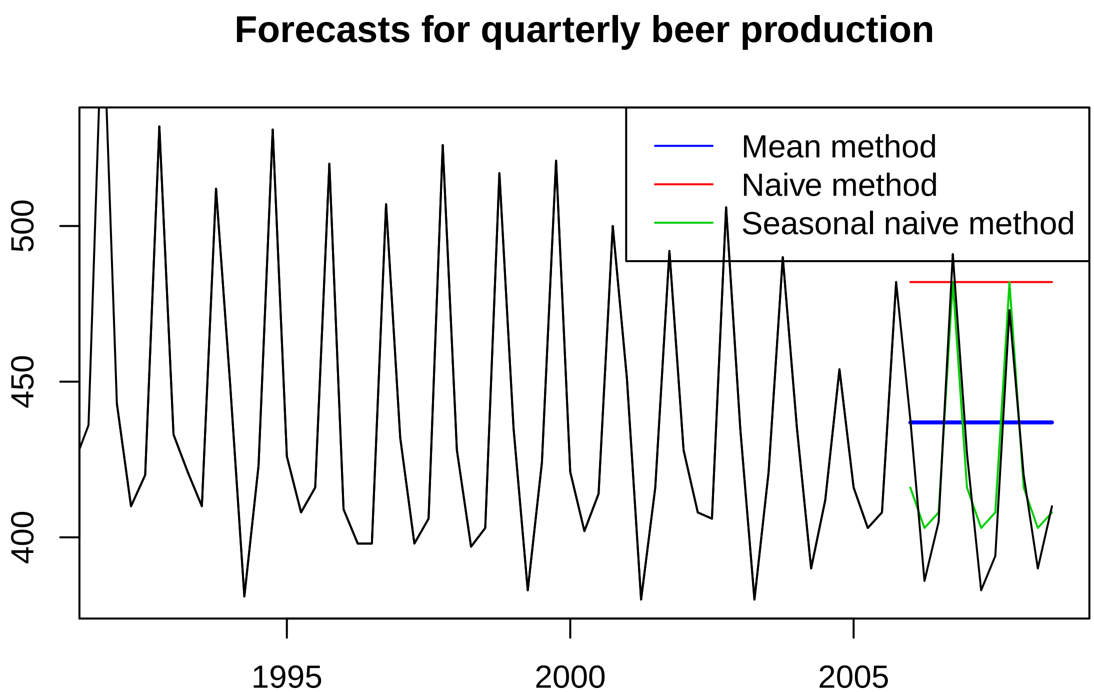
Scaled errors are used as an alternative to percentage errors. The *mean absolute scaled error* or *MASE* is a commonly used one (alternatively *mean squared scaled error* or *MSSE* is used).

Example

```
beer2 <- window(ausbeer,start=1992,end=2006-.1)

beerfit1 <- meanf(beer2,h=11)
beerfit2 <- rwf(beer2,h=11)
beerfit3 <- snaive(beer2,h=11)

plot(beerfit1, plot.conf=FALSE,
  main="Forecasts for quarterly beer production")
lines(beerfit2$mean,col=2)
lines(beerfit3$mean,col=3)
lines(ausbeer)
legend("topright", lty=1, col=c(4,2,3),
  legend=c("Mean method","Naive method","Seasonal naive method"))
```



The following shows the various error tests:

```
beer3 <- window(ausbeer, start=2006)
accuracy(beerfit1, beer3)
```

```
##                         ME     RMSE      MAE        MPE     MAPE     MASE
## Training set  8.121418e-15 44.17630 35.91135 -0.9510944 7.995509 2.444228
## Test set     -1.718344e+01 38.01454 33.77760 -4.7345524 8.169955 2.298999
##                     ACF1 Theil's U
## Training set -0.12566970        NA
## Test set     -0.08286364 0.7901651
```

```r
accuracy(beerfit2, beer3)
```

```
##                       ME     RMSE      MAE         MPE     MAPE     MASE
## Training set   0.7090909 66.60207 55.43636  -0.8987351 12.26632 3.773156
## Test set     -62.2727273 70.90647 63.90909 -15.5431822 15.87645 4.349833
##                     ACF1 Theil's U
## Training set -0.25475212        NA
## Test set     -0.08286364  1.428524
```

```r
accuracy(beerfit3, beer3)
```

```
##                     ME     RMSE      MAE        MPE     MAPE      MASE
## Training set -1.846154 17.24261 14.69231 -0.4803931 3.401224 1.0000000
## Test set     -2.545455 12.96849 11.27273 -0.7530978 2.729847 0.7672537
##                    ACF1 Theil's U
## Training set -0.3408329        NA
## Test set     -0.1786912   0.22573
```