

“Forecasting: Principles and Practice” Notes

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Chapter 1: Getting Started

Types of Quantitative Forecasts

- Cross-sectional Data
 - Given a set of parameters, try to *predict* an outcome based on data. For example, predict the house price based on number of bedrooms, bathrooms, etc.
- Time series Data
 - Forecast future outcome based on historical data

Basic Steps of Forecasting

1. Problem Definition
2. Gathering Information
3. Exploratory Analysis
4. Choosing and Fitting Models
5. Using and Evaluating Model

Chapter 2: Forecaster's Toolbox

Graphs

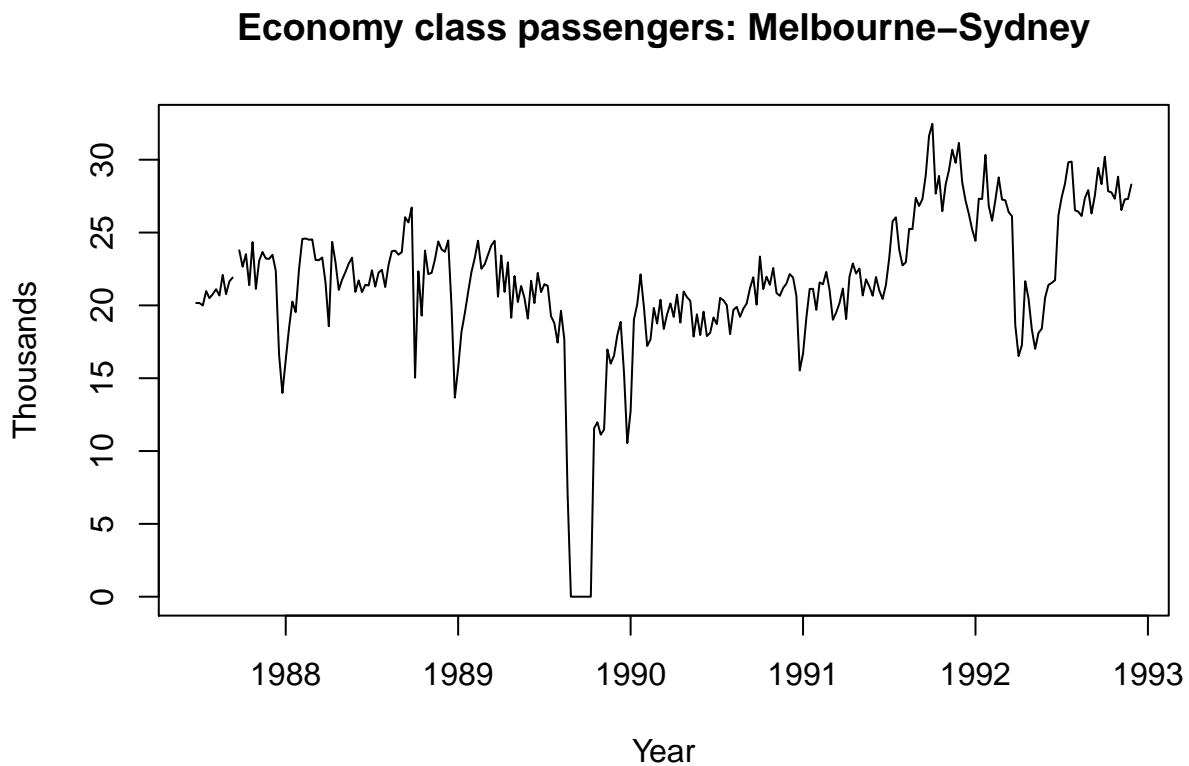
First thing to do for any forecasting exercise is to plot the data to look for patterns or any abnormalities.

Time Plots

aka Line graphs.

Example 1

```
data(melsyd)
plot(melsyd[, "Economy.Class"],
     main="Economy class passengers: Melbourne-Sydney",
     xlab="Year", ylab="Thousands")
```



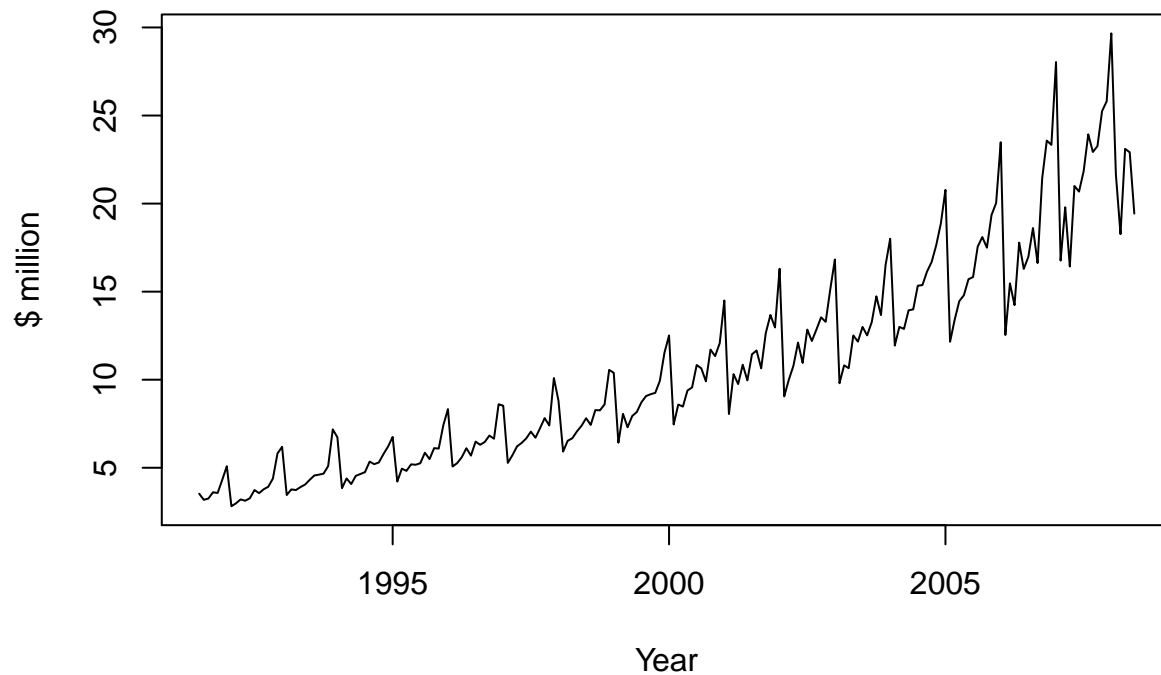
Notes:

- Missing data in 1989 – industrial dispute
- Dip in 1992 – trial which replaced some economy class seats with business class
- Large increase in 1991
- etc

Example 2

```
data(a10)
plot(a10, ylab="$ million", xlab="Year", main="Antidiabetic drug sales")
```

Antidiabetic drug sales



Notes:

- Seasonality
- Upward trend

Common Time Series Patterns

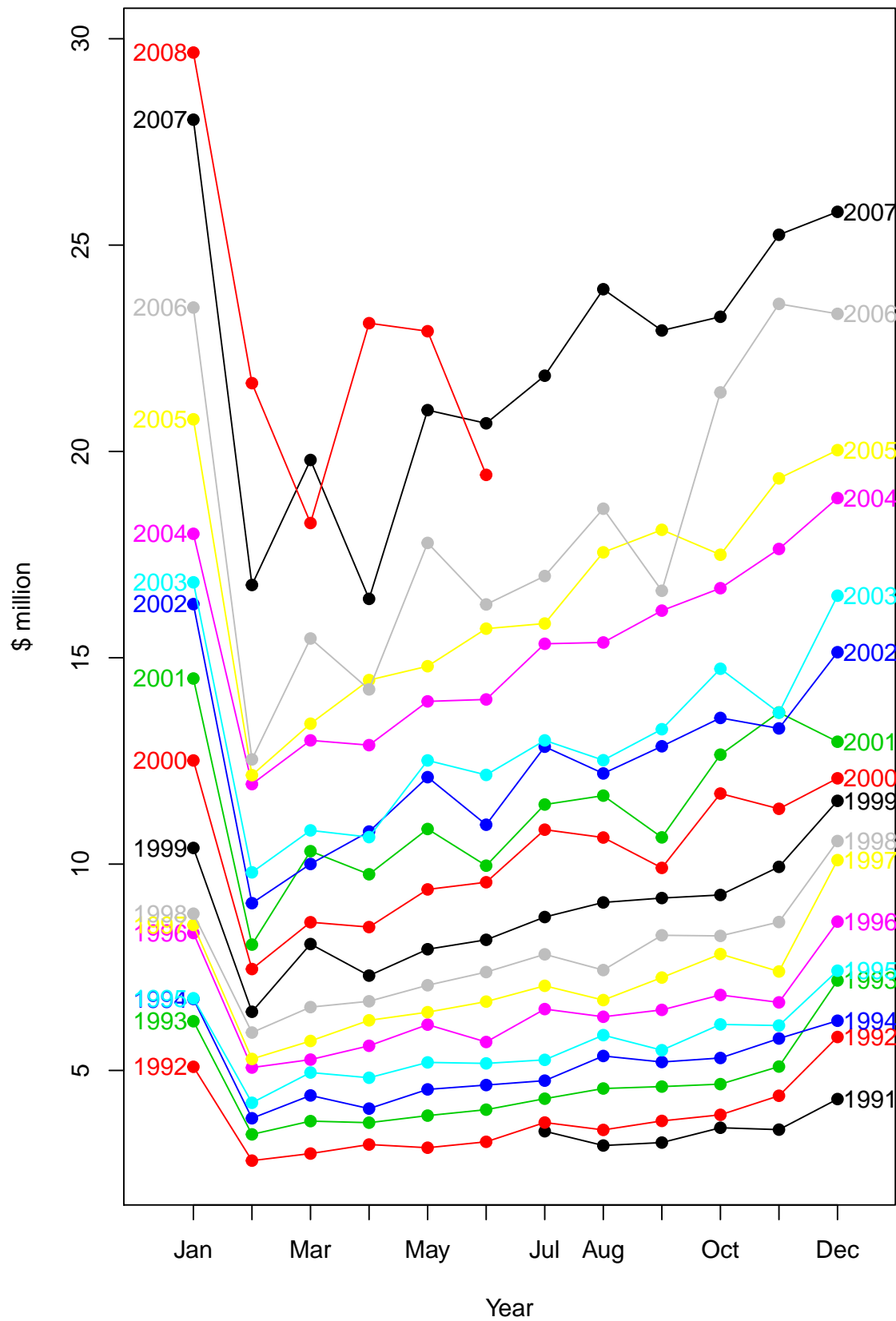
- **Trend**
- **Seasonality**
- **Cycles** – rises and falls that are not of a fixed period

Seasonal Plots

Line plots comparing each *season*.

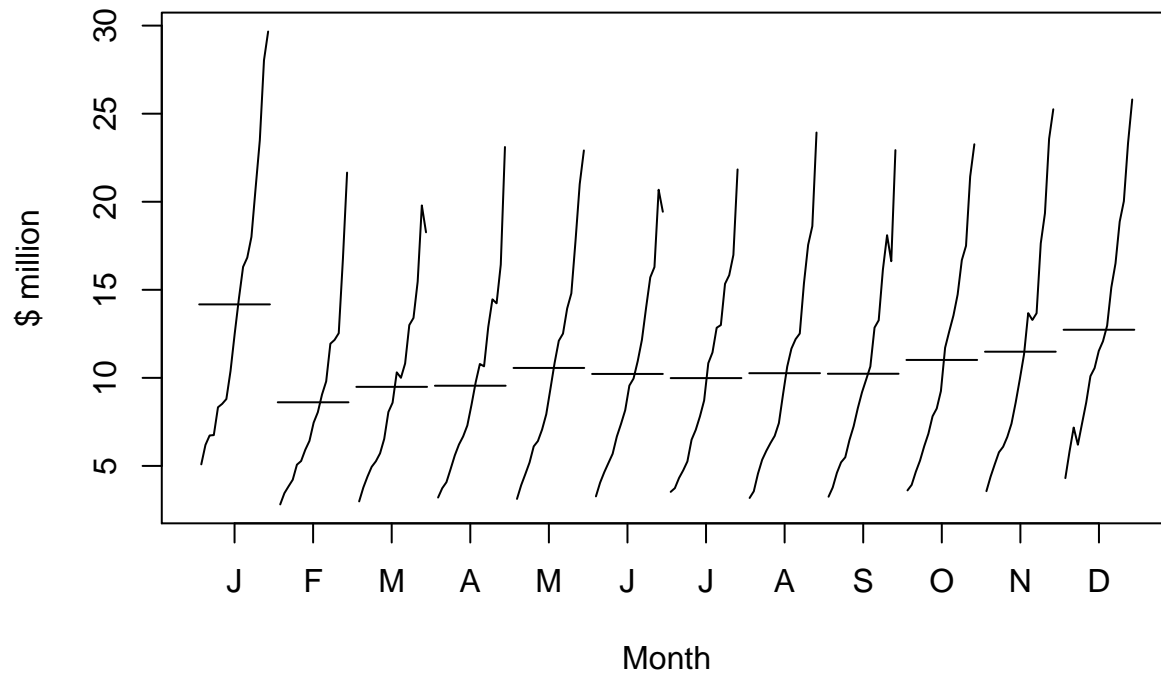
```
seasonplot(a10,  
           ylab='$ million',  
           xlab='Year',  
           main='Seasonal plot: antidiabetic drug sales',  
           year.labels=TRUE,  
           year.labels.left=TRUE,  
           col=1:20,  
           pch=19)
```

Seasonal plot: antidiabetic drug sales



```
monthplot(a10,
          ylab='$ million',
          xlab='Month',
          main='Seasonal deviation plot: antidiabetic drug sales')
```

Seasonal deviation plot: antidiabetic drug sales



Scatterplots

Useful for analyzing cross-sectional data

Summary Statistics

Univariate statistics

Can simply use *summary* function on the data.

Bivariate statistics

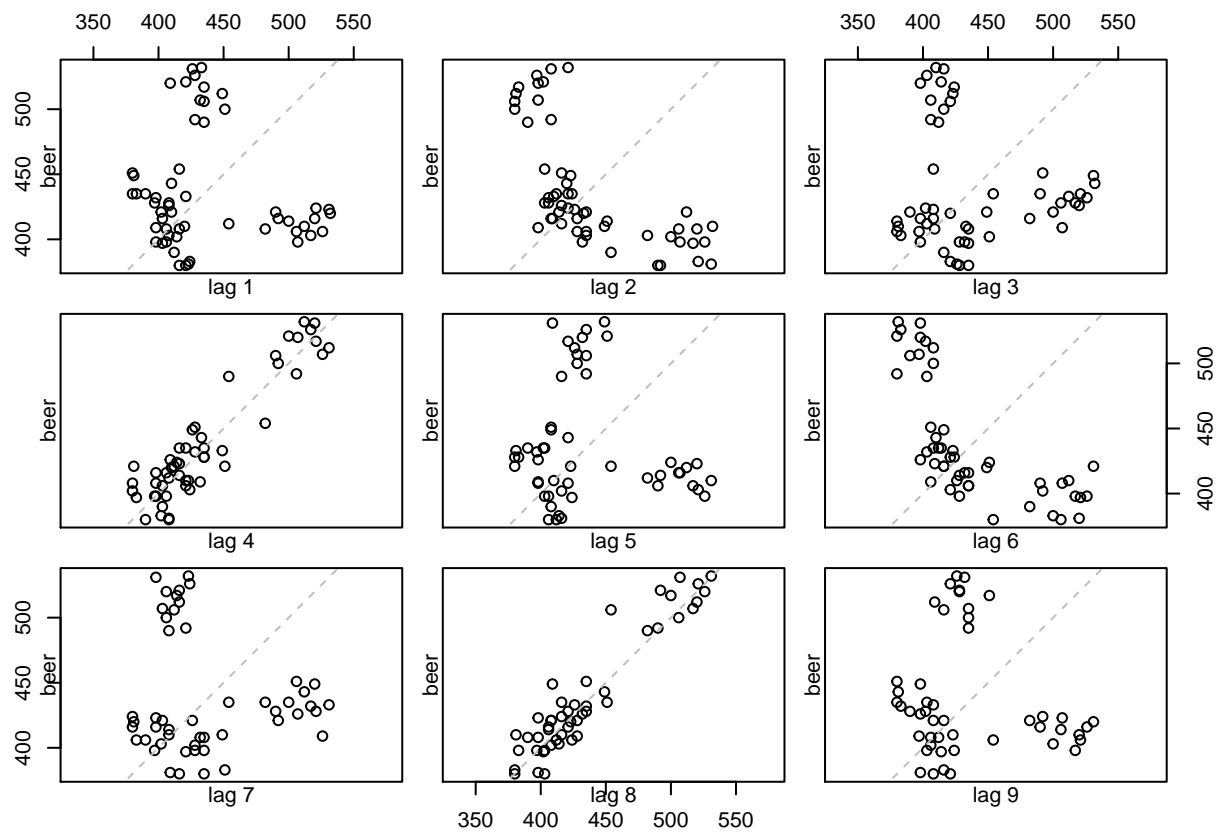
Correlation coefficient: r

$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2} \sqrt{\sum (y_i - \bar{y})^2}}$$

Autocorrelation

Used to test correlation on lag. r_1 tests correlation on lag 1, r_2 tests correlation on lag 2, etc.

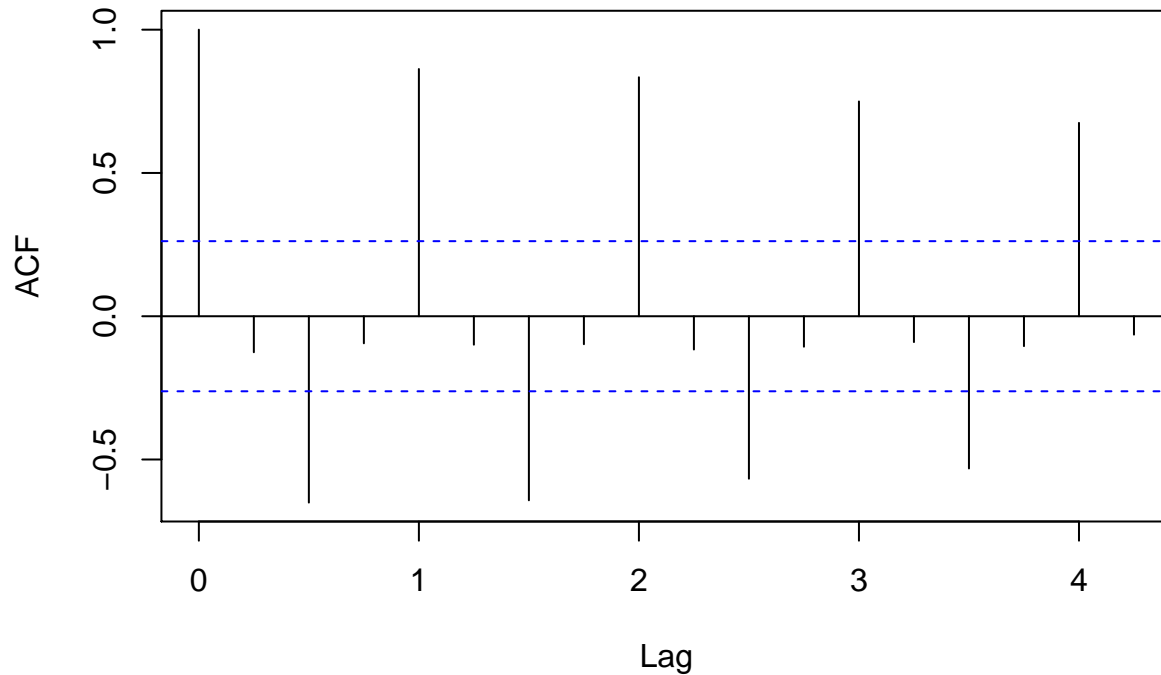
```
data(ausbeer)
beer <- window(ausbeer, start=1992, end=2006-0.1)
lag.plot(beer, lags=9, do.lines=FALSE)
```



Each lag has a corresponding correlation value r . These correlation values are plotted to form an *autocorrelation function* or *ACF*. The plot is known as a *correlogram*.

```
acf(beer)
```

Series beer



Notes:

- r_4 at lag 4 has the highest correlation because seasonal patterns happen every four quarters
- Negative correlations happen two quarters after peaks

Time series that show no autocorrelation are called *white noise*. Acf plot will show no significant correlations for any lag periods.

Simple forecasting methods

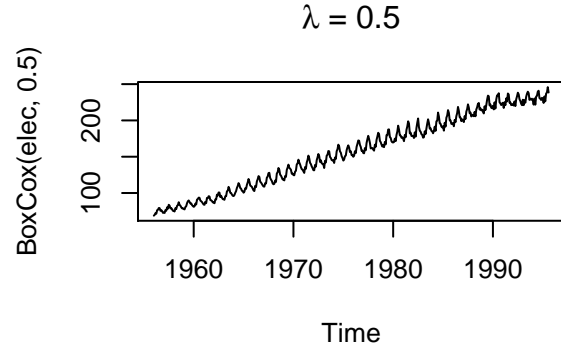
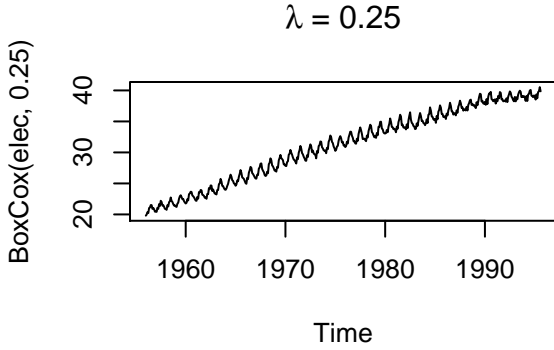
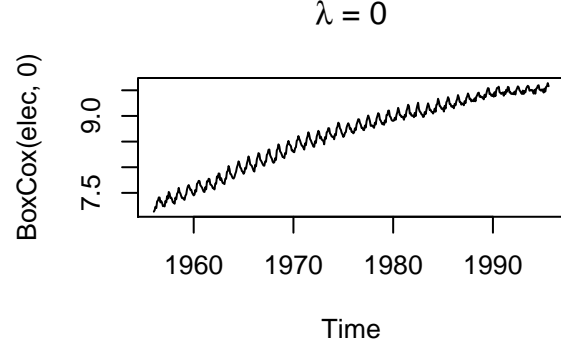
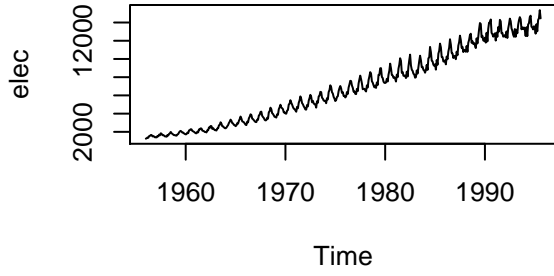
- **Mean** – just the mean of historical values for all forecasted values.
- **Naive** – just the last actual value for all forecasted values.
- **Seasonal Naive** – variation of naive. Uses the last value of some period last season.
- **Drift** – variation of naive. Allows forecast to increase or decrease over time (the *drift*) based on average change.

Transformations

Log and power transformations are common. *Box-Cox Transformations* is a useful family of log and power transformations. If the coefficient λ is 0, it does a natural log, otherwise it does a power transformation. λ can be between 0 and 1. A good lambda will transform the data such that each seasonal swing is roughly equal. Running the function `BoxCox.lambda(data)` will choose a λ for you. In this case, it will choose 0.27.

```
data(elec)
par(mfrow=c(2, 2))
plot(elec, main='Original plot of electricity demand')
plot(BoxCox(elec, 0), main=expression(paste(lambda, ' = 0')))
plot(BoxCox(elec, 0.25), main=expression(paste(lambda, ' = 0.25')))
plot(BoxCox(elec, 0.5), main=expression(paste(lambda, ' = 0.5')))
```


Original plot of electricity demand



After transforming, we need to make a forecast on the transformed data. Then we need to *back transform* to obtain the forecast in the original scale.

Evaluating forecast accuracy

Scale-dependent errors

Forecast error is simply $e_i = y_i - \hat{y}_i$ where y_i is actual and \hat{y}_i is forecast. Two common measures are:

$$\text{Mean absolute error: MAE} = \text{mean}(|e_i|)$$

$$\text{Root mean squared error: RMSE} = \sqrt{\text{mean}(e_i^2)}$$

MAE is most common, however can only be compared to values on the same scale, or on the same data set.

Percentage errors

Scale independent so can compare errors from different data sets. This can be calculated as $p_i = 100e_i/y_i$. The most commonly used measure is:

$$\text{Mean absolute percentage error: MAPE} = \text{mean}(|p_i|)$$

This can present the problem is any value y_i is 0 or close to 0.

Scaled errors

Scaled errors are used as an alternative to percentage errors. The *mean absolute scaled error* or *MASE* is a commonly used one (alternatively *mean squared scaled error* or *MSSE* is used).

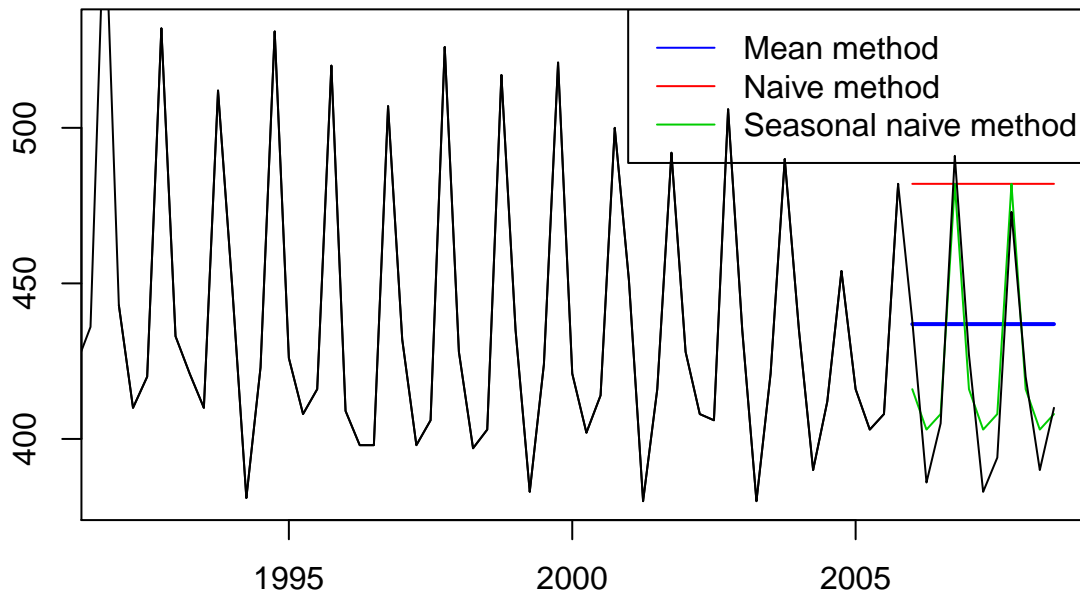
Example

```
beer2 <- window(ausbeer,start=1992,end=2006-.1)

beerfit1 <- meanf(beer2,h=11)
beerfit2 <- rwf(beer2,h=11)
beerfit3 <- snaive(beer2,h=11)

plot(beerfit1, plot.conf=FALSE,
     main="Forecasts for quarterly beer production")
lines(beerfit2$mean,col=2)
lines(beerfit3$mean,col=3)
lines(ausbeer)
legend("topright", lty=1, col=c(4,2,3),
     legend=c("Mean method","Naive method","Seasonal naive method"))
```

Forecasts for quarterly beer production



The following shows the various error tests:

```
beer3 <- window(ausbeer, start=2006)
accuracy(beerfit1, beer3)
```

```
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set  8.121418e-15 44.17630 35.91135 -0.9510944 7.995509 2.444228
## Test set     -1.718344e+01 38.01454 33.77760 -4.7345524 8.169955 2.298999
##              ACF1 Theil's U
## Training set -0.12566970      NA
## Test set     -0.08286364 0.7901651
```

```
accuracy(beerfit2, beer3)
```

```
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set  0.7090909 66.60207 55.43636 -0.8987351 12.26632 3.773156
## Test set     -62.2727273 70.90647 63.90909 -15.5431822 15.87645 4.349833
##              ACF1 Theil's U
## Training set -0.25475212      NA
## Test set     -0.08286364  1.428524
```

```
accuracy(beerfit3, beer3)
```

```
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -1.846154 17.24261 14.69231 -0.4803931 3.401224 1.0000000
## Test set     -2.545455 12.96849 11.27273 -0.7530978 2.729847 0.7672537
##              ACF1 Theil's U
## Training set -0.3408329      NA
## Test set     -0.1786912  0.22573
```

Here we see that the seasonal naive method is best.

Residual diagnostics

Residuals are simply the difference between the forecast and actual value $e_i = y_i - \hat{y}_i$. A good forecast will yield residuals with the following properties:

- Residuals are uncorrelated. If you find correlations then there was something not included in the forecasting model.
- Residuals have zero mean. A non-zero mean means forecast is biased.

If the above properties are not satisfied, then forecast can be improved. If residuals have a mean m , then simply adding m to all forecasts will solve the problem. Fixing the correlation problem will be explained in **Chapter 8**.

The following two properties are not required, but useful:

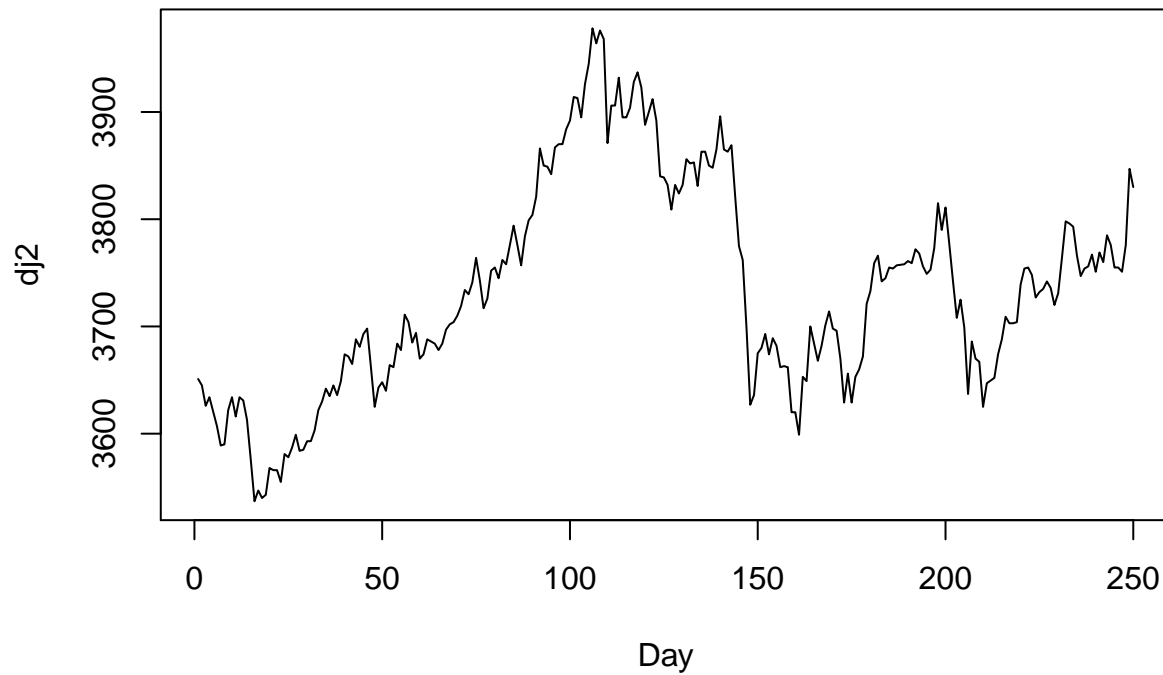
- Residuals have constant variance.
- Residuals are normally distributed.

Example: Dow Jones

Naive method is usually best for stocks. Therefore, residuals are simply the difference between consecutive observations.

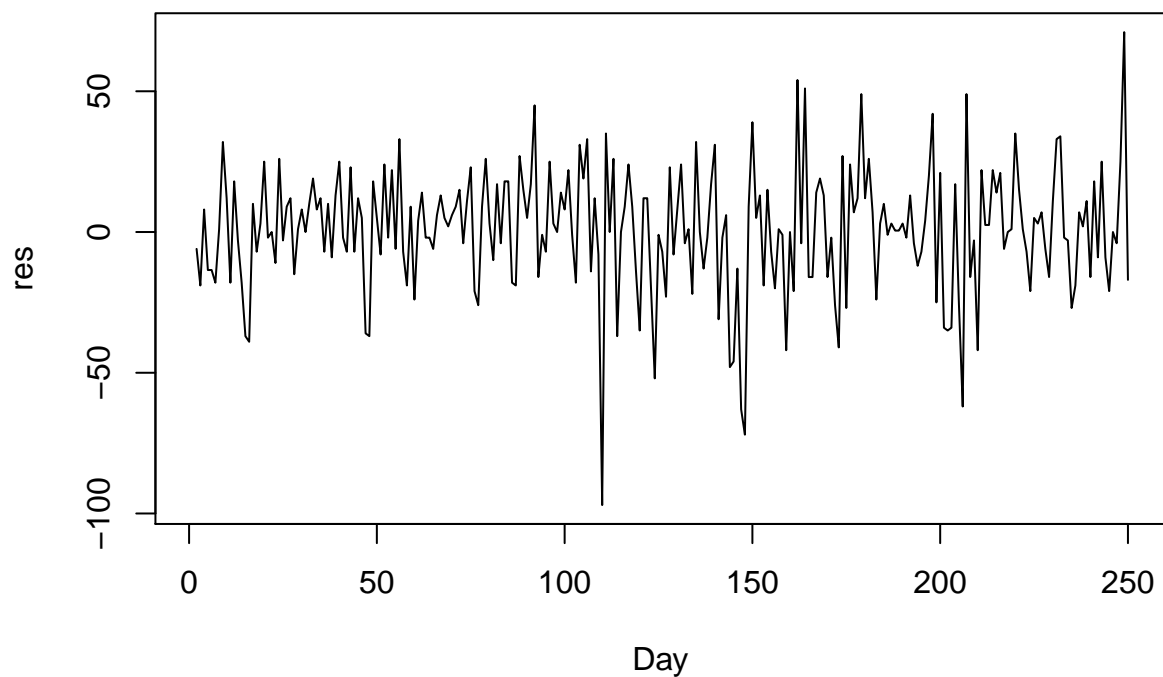
```
data(dj)
# par(mfrow=c(4, 1))
dj2 <- window(dj, end=250)
plot(dj2,
     main='Dow Jones Index (daily ending 1994-07-15)',
     xlab='Day')
```

Dow Jones Index (daily ending 1994-07-15)

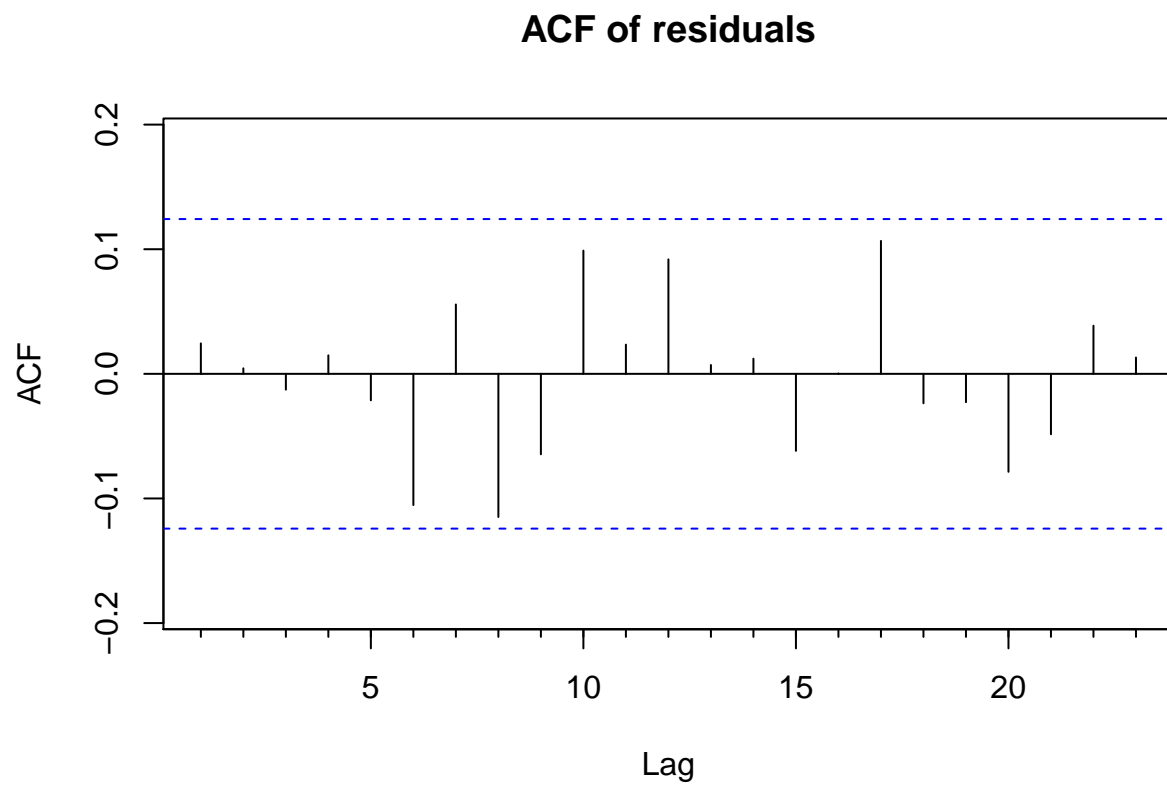


```
res <- residuals(naive(dj2))
plot(res,
      main='Residuals from naive method',
      xlab='Day')
```

Residuals from naive method

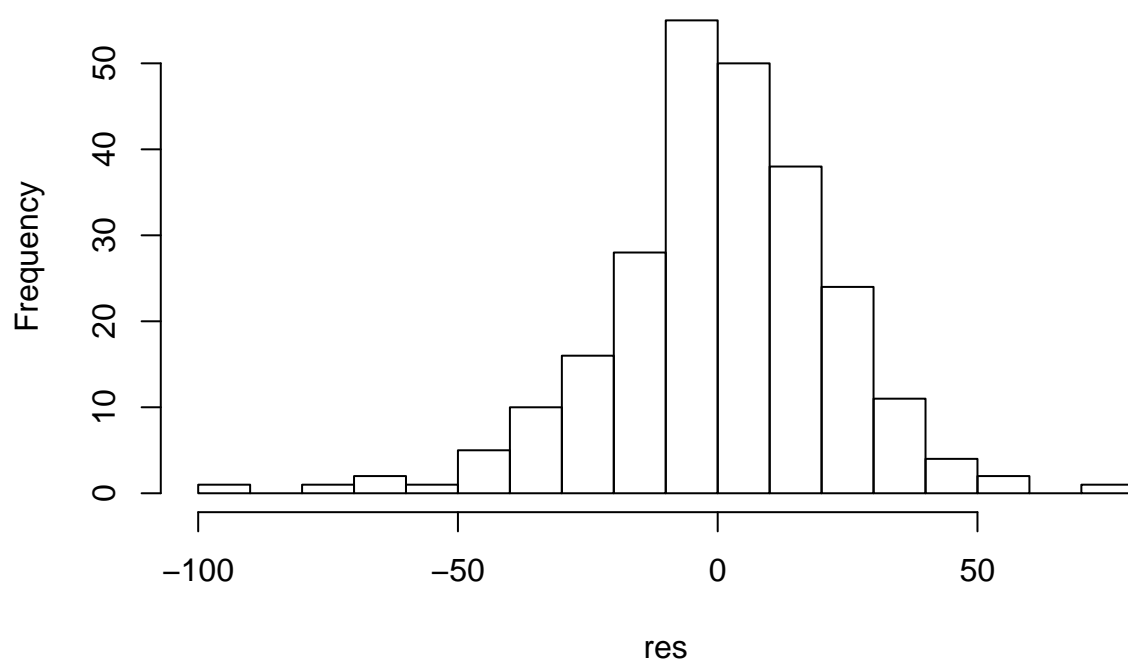


```
Acf(res,  
     main='ACF of residuals')
```



```
hist(res,  
     nclass='FD',  
     main='Histogram of residuals')
```

Histogram of residuals



Notes:

- [x] Residuals are not correlated.
- [x] Residuals are close to zero.
- [x] Residuals have constant variance.
- [] Not quite normally distributed so prediction intervals may be inaccurate.