

Take $S_2 = \{1, 2, 3, 4\}$.

$$\begin{aligned}\delta(S_2, a) &= \text{followpos}(1) \cup \text{followpos}(3) = \{1, 2, 3, 4\} = S_2 \\ \delta(S_2, b) &= \text{followpos}(2) \cup \text{followpos}(4) = \{1, 2, 3, 5\} = \text{New state. Mark it as } S_3 \\ \delta(S_3, a) &= \text{followpos}(1) \cup \text{followpos}(3) = \{1, 2, 3, 4\} = S_2 \\ \delta(S_3, b) &= \text{followpos}(2) \cup \text{followpos}(5) = \{1, 2, 3, 6\} = \text{New state. Mark it as } S_4 \\ \delta(S_4, a) &= \text{followpos}(1) \cup \text{followpos}(3) = \{1, 2, 3, 4\} = S_2 \\ \delta(S_4, b) &= \text{followpos}(2) = \{1, 2, 3\} = S_1\end{aligned}$$

All the states are traversed, and no new state appears. Therefore, it is the final DFA. The transitional diagram of the DFA is given in Fig. 5.15.

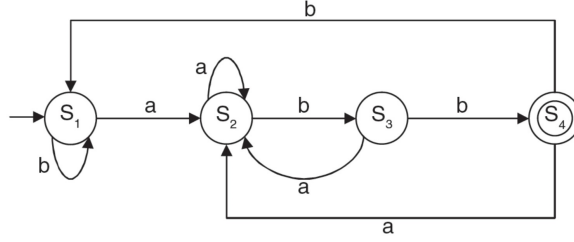


Fig. 5.15

5.6 NFA with ϵ Move and Conversion to DFA by ϵ -Closure Method

If any FA contains any $\epsilon(\text{null})$ move or transaction, then that FA is called an NFA with ϵ moves. An example is shown in Fig. 5.16.

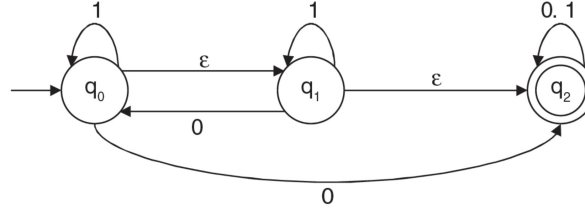


Fig. 5.16

The previous FA in Fig. 5.16 contains two null moves. So, the previous FA is an NFA with null move. From the definition of an NFA, we know that for an NFA from a single state for a single input the machine can go to more than one state, i.e., $Q \times \Sigma \rightarrow 2^Q$, where 2^Q is the power set of Q .

From a state by getting ϵ input, the machine is confined into that state. An FA with null move must contain at least one ϵ move. For this type of FA for input ϵ , the machine can go to more than one state. (One is that same state and the other is the ϵ -transaction next state). So, an FA with ϵ move can be called as an NFA.

For the previous FA,

$$\delta(q_0, \epsilon) \rightarrow q_0 \quad \text{and} \quad \delta(q_0, \epsilon) \rightarrow q_1$$

$$\delta(q_1, \epsilon) \rightarrow q_1 \quad \text{and} \quad \delta(q_1, \epsilon) \rightarrow q_2$$