

COMBINATIONS AND PERMUTATIONS

The Counting Principle

Also known as the **fundamental theorem of counting**.

If a job consists of k separate tasks and there are n_1 ways of doing the first task, n_2 ways of doing the second task, etc., there are $n_1 \times n_2 \times \dots \times n_k$ ways of completing the entire job.

Factorials

$n!$ is the number of ways to list a set of n objects.

Denote "n-factorial" or "factorial of n " as $n!$

$$n! = n \times (n-1) \times (n-2) \dots 2 \times 1$$

$$2! = 2 \times 1 = 2$$

$$3! = 3 \times 2 \times 1 = 6$$

Remember, $0! = 1$.

Definitions

Permutation: An arrangement of objects without repetition in which order matters.

Combination: An arrangement of objects without repetition in which order doesn't matter.

Permutation Formula

$P(n,k) = \frac{n!}{(n-k)!}$, where n is the total number of options and k is the number of options we want to choose.

Combination Formula

$C(n,k) = \frac{n!}{(n-k)!k!}$, where n is the total number of options and k is the number of options we want to choose.