Rank-76387 over GF(32)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^2 X_2 + X_0^2 X_3 + X_1^2 X_3 + X_1 X_2^2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 0, 0, 1, 1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is -2079292379

General information

Number of lines	4
Number of points	1089
Number of singular points	2
Number of Eckardt points	0
Number of double points	4
Number of single points	124
Number of points off lines	961
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^{4}
Type of lines on points	$2^4, 1^{124}, 0^{961}$

Singular Points

The surface has 2 singular points:

$$0: P_4 = \mathbf{P}(1, 1, 1, 1) = \mathbf{P}(1, 1, 1, 1) 1: P_5 = \mathbf{P}(1, 1, 0, 0) = \mathbf{P}(1, 1, 0, 0)$$

The 4 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{array} \right]_0 = \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{array} \right]_0 = \mathbf{Pl}(1,0,0,0,0,0)_0$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{33} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{33} = \mathbf{Pl}(1,0,1,0,1,0)_{1153}$$

$$\ell_2 = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1083424} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1083424} = \mathbf{Pl}(0,1,0,0,0,0)_{1}$$

$$\ell_3 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{2082} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{2082} = \mathbf{Pl}(0,0,1,1,1,1)_{70562}$$

Rank of lines: (0, 33, 1083424, 2082)

Rank of points on Klein quadric: (0, 1153, 1, 70562)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 4 Double points: The double points on the surface are:

$$P_0 = (1,0,0,0) = \ell_0 \cap \ell_1$$

$$P_5 = (1,1,0,0) = \ell_0 \cap \ell_3$$

$$P_4 = (1,1,1,1) = \ell_1 \cap \ell_3$$

$P_{2082} = (0, 0, 1, 1) = \ell_2 \cap \ell_3$

Single Points

The surface has 124 single points: The single points on the surface are:

 $0: P_1 = (0, 1, 0, 0)$ lies on line ℓ_0 22: $P_{25} = (21, 1, 0, 0)$ lies on line ℓ_0 1: $P_2 = (0,0,1,0)$ lies on line ℓ_2 23: $P_{26} = (22, 1, 0, 0)$ lies on line ℓ_0 2: $P_3 = (0,0,0,1)$ lies on line ℓ_2 24: $P_{27} = (23, 1, 0, 0)$ lies on line ℓ_0 $3: P_6 = (2, 1, 0, 0)$ lies on line ℓ_0 25: $P_{28} = (24, 1, 0, 0)$ lies on line ℓ_0 4: $P_7 = (3, 1, 0, 0)$ lies on line ℓ_0 26: $P_{29} = (25, 1, 0, 0)$ lies on line ℓ_0 5: $P_8 = (4, 1, 0, 0)$ lies on line ℓ_0 27: $P_{30} = (26, 1, 0, 0)$ lies on line ℓ_0 6: $P_9 = (5, 1, 0, 0)$ lies on line ℓ_0 28: $P_{31} = (27, 1, 0, 0)$ lies on line ℓ_0 29: $P_{32} = (28, 1, 0, 0)$ lies on line ℓ_0 7: $P_{10} = (6, 1, 0, 0)$ lies on line ℓ_0 8: $P_{11} = (7, 1, 0, 0)$ lies on line ℓ_0 $30: P_{33} = (29, 1, 0, 0)$ lies on line ℓ_0 9: $P_{12} = (8, 1, 0, 0)$ lies on line ℓ_0 $31: P_{34} = (30, 1, 0, 0)$ lies on line ℓ_0 10: $P_{13} = (9, 1, 0, 0)$ lies on line ℓ_0 $32: P_{35} = (31, 1, 0, 0)$ lies on line ℓ_0 11: $P_{14} = (10, 1, 0, 0)$ lies on line ℓ_0 $33: P_{2114} = (0, 1, 1, 1)$ lies on line ℓ_1 12 : $P_{15} = (11, 1, 0, 0)$ lies on line ℓ_0 $34: P_{2115} = (2, 1, 1, 1)$ lies on line ℓ_1 13: $P_{16} = (12, 1, 0, 0)$ lies on line ℓ_0 $35: P_{2116} = (3, 1, 1, 1)$ lies on line ℓ_1 14: $P_{17} = (13, 1, 0, 0)$ lies on line ℓ_0 $36: P_{2117} = (4, 1, 1, 1)$ lies on line ℓ_1 15: $P_{18} = (14, 1, 0, 0)$ lies on line ℓ_0 $37: P_{2118} = (5, 1, 1, 1)$ lies on line ℓ_1 16: $P_{19} = (15, 1, 0, 0)$ lies on line ℓ_0 $38: P_{2119} = (6, 1, 1, 1)$ lies on line ℓ_1 17: $P_{20} = (16, 1, 0, 0)$ lies on line ℓ_0 $39: P_{2120} = (7, 1, 1, 1)$ lies on line ℓ_1 18: $P_{21} = (17, 1, 0, 0)$ lies on line ℓ_0 $40: P_{2121} = (8, 1, 1, 1)$ lies on line ℓ_1 19 : $P_{22} = (18,1,0,0)$ lies on line ℓ_0 41: $P_{2122} = (9, 1, 1, 1)$ lies on line ℓ_1 20: $P_{23} = (19, 1, 0, 0)$ lies on line ℓ_0 42: $P_{2123} = (10, 1, 1, 1)$ lies on line ℓ_1 21: $P_{24} = (20, 1, 0, 0)$ lies on line ℓ_0 43: $P_{2124} = (11, 1, 1, 1)$ lies on line ℓ_1

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44: P_{2125} = (12, 1, 1, 1) lies on line \ell_1
                                                                      85: P_{2840} = (23, 23, 1, 1) lies on line \ell_3
45: P_{2126} = (13, 1, 1, 1) lies on line \ell_1
                                                                     86: P_{2873} = (24, 24, 1, 1) lies on line \ell_3
                                                                     87: P_{2906} = (25, 25, 1, 1) lies on line \ell_3
46: P_{2127} = (14, 1, 1, 1) lies on line \ell_1
47: P_{2128} = (15, 1, 1, 1) lies on line \ell_1
                                                                      88: P_{2939} = (26, 26, 1, 1) lies on line \ell_3
48: P_{2129} = (16, 1, 1, 1) lies on line \ell_1
                                                                     89: P_{2972} = (27, 27, 1, 1) lies on line \ell_3
                                                                     90: P_{3005} = (28, 28, 1, 1) lies on line \ell_3
49: P_{2130} = (17, 1, 1, 1) lies on line \ell_1
50: P_{2131} = (18, 1, 1, 1) lies on line \ell_1
                                                                     91: P_{3038} = (29, 29, 1, 1) lies on line \ell_3
51: P_{2132} = (19, 1, 1, 1) lies on line \ell_1
                                                                     92: P_{3071} = (30, 30, 1, 1) lies on line \ell_3
52: P_{2133} = (20, 1, 1, 1) lies on line \ell_1
                                                                     93: P_{3104} = (31, 31, 1, 1) lies on line \ell_3
53: P_{2134} = (21, 1, 1, 1) lies on line \ell_1
                                                                     94: P_{3105} = (0,0,2,1) lies on line \ell_2
54: P_{2135} = (22, 1, 1, 1) lies on line \ell_1
                                                                     95: P_{4129} = (0,0,3,1) lies on line \ell_2
55: P_{2136} = (23, 1, 1, 1) lies on line \ell_1
                                                                     96: P_{5153} = (0, 0, 4, 1) lies on line \ell_2
56: P_{2137} = (24, 1, 1, 1) lies on line \ell_1
                                                                     97: P_{6177} = (0, 0, 5, 1) lies on line \ell_2
57: P_{2138} = (25, 1, 1, 1) lies on line \ell_1
                                                                     98: P_{7201} = (0, 0, 6, 1) lies on line \ell_2
58: P_{2139} = (26, 1, 1, 1) lies on line \ell_1
                                                                      99: P_{8225} = (0, 0, 7, 1) lies on line \ell_2
59: P_{2140} = (27, 1, 1, 1) lies on line \ell_1
                                                                     100: P_{9249} = (0, 0, 8, 1) lies on line \ell_2
60: P_{2141} = (28, 1, 1, 1) lies on line \ell_1
                                                                     101: P_{10273} = (0, 0, 9, 1) lies on line \ell_2
61: P_{2142} = (29, 1, 1, 1) lies on line \ell_1
                                                                     102: P_{11297} = (0, 0, 10, 1) lies on line \ell_2
62: P_{2143} = (30, 1, 1, 1) lies on line \ell_1
                                                                     103: P_{12321} = (0, 0, 11, 1) lies on line \ell_2
63: P_{2144} = (31, 1, 1, 1) lies on line \ell_1
                                                                     104: P_{13345} = (0, 0, 12, 1) lies on line \ell_2
64: P_{2147} = (2, 2, 1, 1) lies on line \ell_3
                                                                     105: P_{14369} = (0, 0, 13, 1) lies on line \ell_2
65: P_{2180} = (3, 3, 1, 1) lies on line \ell_3
                                                                     106: P_{15393} = (0, 0, 14, 1) lies on line \ell_2
                                                                      107: P_{16417} = (0, 0, 15, 1) lies on line \ell_2
66: P_{2213} = (4, 4, 1, 1) lies on line \ell_3
67 : P_{2246} = (5, 5, 1, 1) lies on line \ell_3
                                                                     108 : P_{17441} = (0, 0, 16, 1) lies on line \ell_2
68: P_{2279} = (6, 6, 1, 1) lies on line \ell_3
                                                                      109: P_{18465} = (0, 0, 17, 1) lies on line \ell_2
69: P_{2312} = (7,7,1,1) lies on line \ell_3
                                                                     110: P_{19489} = (0, 0, 18, 1) lies on line \ell_2
70: P_{2345} = (8, 8, 1, 1) lies on line \ell_3
                                                                     111: P_{20513} = (0, 0, 19, 1) lies on line \ell_2
71: P_{2378} = (9, 9, 1, 1) lies on line \ell_3
                                                                     112: P_{21537} = (0, 0, 20, 1) lies on line \ell_2
                                                                     113: P_{22561} = (0, 0, 21, 1) lies on line \ell_2
72: P_{2411} = (10, 10, 1, 1) lies on line \ell_3
73: P_{2444} = (11, 11, 1, 1) lies on line \ell_3
                                                                     114: P_{23585} = (0, 0, 22, 1) lies on line \ell_2
74: P_{2477} = (12, 12, 1, 1) lies on line \ell_3
                                                                     115: P_{24609} = (0, 0, 23, 1) lies on line \ell_2
75: P_{2510} = (13, 13, 1, 1) lies on line \ell_3
                                                                     116: P_{25633} = (0, 0, 24, 1) lies on line \ell_2
76: P_{2543} = (14, 14, 1, 1) lies on line \ell_3
                                                                     117: P_{26657} = (0, 0, 25, 1) lies on line \ell_2
77: P_{2576} = (15, 15, 1, 1) lies on line \ell_3
                                                                     118: P_{27681} = (0, 0, 26, 1) lies on line \ell_2
78: P_{2609} = (16, 16, 1, 1) lies on line \ell_3
                                                                     119: P_{28705} = (0, 0, 27, 1) lies on line \ell_2
                                                                     120 : P_{29729} = (0, 0, 28, 1) lies on line \ell_2
79: P_{2642} = (17, 17, 1, 1) lies on line \ell_3
80: P_{2675} = (18, 18, 1, 1) lies on line \ell_3
                                                                     121: P_{30753} = (0, 0, 29, 1) lies on line \ell_2
81: P_{2708} = (19, 19, 1, 1) lies on line \ell_3
                                                                     122: P_{31777} = (0, 0, 30, 1) lies on line \ell_2
82: P_{2741} = (20, 20, 1, 1) lies on line \ell_3
                                                                     123: P_{32801} = (0, 0, 31, 1) lies on line \ell_2
83: P_{2774} = (21, 21, 1, 1) lies on line \ell_3
84: P_{2807} = (22, 22, 1, 1) lies on line \ell_3
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The single points on the surface are:

Points on surface but on no line

The surface has 961 points not on any line: The points on the surface but not on lines are:

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\begin{array}{lll} 0: \, P_{111} = (12,2,1,0) & 3: \, P_{193} = (30,4,1,0) \\ 1: \, P_{113} = (14,2,1,0) & 4: \, P_{298} = (7,8,1,0) \\ 2: \, P_{189} = (26,4,1,0) & 5: \, P_{306} = (15,8,1,0) \end{array}
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6: P_{339} = (16, 9, 1, 0)
                                                                  60: P_{2057} = (7, 31, 0, 1)
7: P_{348} = (25, 9, 1, 0)
                                                                  61: P_{3133} = (28, 0, 2, 1)
8: P_{376} = (21, 10, 1, 0)
                                                                  62: P_{3189} = (20, 2, 2, 1)
                                                                  63: P_{3192} = (23, 2, 2, 1)
9: P_{386} = (31, 10, 1, 0)
10: P_{393} = (6, 11, 1, 0)
                                                                  64: P_{3205} = (4, 3, 2, 1)
11: P_{400} = (13, 11, 1, 0)
                                                                  65: P_{3227} = (26, 3, 2, 1)
12: P_{456} = (5, 13, 1, 0)
                                                                  66: P_{3233} = (0, 4, 2, 1)
13: P_{459} = (8, 13, 1, 0)
                                                                  67: P_{3240} = (7, 4, 2, 1)
14: P_{501} = (18, 14, 1, 0)
                                                                  68: P_{3337} = (8, 7, 2, 1)
15: P_{511} = (28, 14, 1, 0)
                                                                  69: P_{3342} = (13, 7, 2, 1)
16: P_{535} = (20, 15, 1, 0)
                                                                  70: P_{3427} = (2, 10, 2, 1)
17: P_{542} = (27, 15, 1, 0)
                                                                  71: P_{3443} = (18, 10, 2, 1)
18: P_{550} = (3, 16, 1, 0)
                                                                  72: P_{3477} = (20, 11, 2, 1)
                                                                  73: P_{3482} = (25, 11, 2, 1)
19: P_{566} = (19, 16, 1, 0)
20: P_{615} = (4, 18, 1, 0)
                                                                  74: P_{3544} = (23, 13, 2, 1)
21: P_{633} = (22, 18, 1, 0)
                                                                  75: P_{3551} = (30, 13, 2, 1)
22: P_{654} = (11, 19, 1, 0)
                                                                  76: P_{3560} = (7, 14, 2, 1)
23: P_{667} = (24, 19, 1, 0)
                                                                  77: P_{3565} = (12, 14, 2, 1)
                                                                  78: P_{3589} = (4, 15, 2, 1)
24: P_{909} = (10, 27, 1, 0)
                                                                  79: P_{3603} = (18, 15, 2, 1)
25: P_{916} = (17, 27, 1, 0)
26: P_{1004} = (9, 30, 1, 0)
                                                                  80: P_{3618} = (1, 16, 2, 1)
27: P_{1018} = (23, 30, 1, 0)
                                                                  81: P_{3647} = (30, 16, 2, 1)
28: P_{1029} = (2, 31, 1, 0)
                                                                  82: P_{3693} = (12, 18, 2, 1)
29: P_{1056} = (29, 31, 1, 0)
                                                                  83: P_{3721} = (8, 19, 2, 1)
30: P_{1059} = (1,0,0,1)
                                                                  84: P_{3734} = (21, 19, 2, 1)
31: P_{1132} = (10, 2, 0, 1)
                                                                  85: P_{3810} = (1, 22, 2, 1)
                                                                  86: P_{3835} = (26, 22, 2, 1)
32: P_{1133} = (11, 2, 0, 1)
33: P_{1200} = (14, 4, 0, 1)
                                                                  87: P_{3894} = (21, 24, 2, 1)
34: P_{1201} = (15, 4, 0, 1)
                                                                  88: P_{3898} = (25, 24, 2, 1)
35: P_{1254} = (4, 6, 0, 1)
                                                                  89: P_{3918} = (13, 25, 2, 1)
36: P_{1255} = (5, 6, 0, 1)
                                                                  90: P_{3933} = (28, 25, 2, 1)
37: P_{1374} = (28, 9, 0, 1)
                                                                  91: P_{4147} = (18, 0, 3, 1)
38: P_{1375} = (29, 9, 0, 1)
                                                                  92: P_{4169} = (8, 1, 3, 1)
39: P_{1432} = (22, 11, 0, 1)
                                                                  93: P_{4170} = (9, 1, 3, 1)
40: P_{1433} = (23, 11, 0, 1)
                                                                  94: P_{4289} = (0, 5, 3, 1)
41: P_{1492} = (18, 13, 0, 1)
                                                                  95: P_{4296} = (7, 5, 3, 1)
42: P_{1493} = (19, 13, 0, 1)
                                                                  96: P_{4333} = (12, 6, 3, 1)
                                                                  97: P_{4348} = (27, 6, 3, 1)
43: P_{1562} = (24, 15, 0, 1)
44: P_{1563} = (25, 15, 0, 1)
                                                                  98: P_{4369} = (16, 7, 3, 1)
45: P_{1600} = (30, 16, 0, 1)
                                                                  99: P_{4373} = (20, 7, 3, 1)
46: P_{1601} = (31, 16, 0, 1)
                                                                  100: P_{4424} = (7, 9, 3, 1)
                                                                  101: P_{4427} = (10, 9, 3, 1)
47: P_{1654} = (20, 18, 0, 1)
48: P_{1655} = (21, 18, 0, 1)
                                                                  102: P_{4502} = (21, 11, 3, 1)
                                                                  103: P_{4508} = (27, 11, 3, 1)
49: P_{1714} = (16, 20, 0, 1)
50: P_{1715} = (17, 20, 0, 1)
                                                                  104: P_{4677} = (4, 17, 3, 1)
51: P_{1788} = (26, 22, 0, 1)
                                                                  105: P_{4702} = (29, 17, 3, 1)
52: P_{1789} = (27, 22, 0, 1)
                                                                  106: P_{4708} = (3, 18, 3, 1)
53: P_{1860} = (2, 25, 0, 1)
                                                                  107: P_{4715} = (10, 18, 3, 1)
54: P_{1861} = (3, 25, 0, 1)
                                                                  108: P_{4790} = (21, 20, 3, 1)
55: P_{1930} = (8, 27, 0, 1)
                                                                  109: P_{4794} = (25, 20, 3, 1)
56: P_{1931} = (9, 27, 0, 1)
                                                                  110: P_{4851} = (18, 22, 3, 1)
57: P_{1998} = (12, 29, 0, 1)
                                                                  111: P_{4862} = (29, 22, 3, 1)
58: P_{1999} = (13, 29, 0, 1)
                                                                  112: P_{4877} = (12, 23, 3, 1)
59: P_{2056} = (6, 31, 0, 1)
                                                                  113: P_{4881} = (16, 23, 3, 1)
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168: P_{6759} = (6, 18, 5, 1)
114: P_{4899} = (2, 24, 3, 1)
115: P_{4901} = (4, 24, 3, 1)
                                                                 169: P_{6764} = (11, 18, 5, 1)
116: P_{4995} = (2, 27, 3, 1)
                                                                 170: P_{6819} = (2, 20, 5, 1)
117: P_{5013} = (20, 27, 3, 1)
                                                                 171: P_{6843} = (26, 20, 5, 1)
118: P_{5033} = (8, 28, 3, 1)
                                                                 172: P_{6862} = (13, 21, 5, 1)
119: P_{5130} = (9, 31, 3, 1)
                                                                 173: P_{6878} = (29, 21, 5, 1)
120: P_{5146} = (25, 31, 3, 1)
                                                                 174: P_{6923} = (10, 23, 5, 1)
121: P_{5176} = (23, 0, 4, 1)
                                                                 175: P_{6958} = (13, 24, 5, 1)
122: P_{5305} = (24, 4, 4, 1)
                                                                 176: P_{6971} = (26, 24, 5, 1)
123: P_{5310} = (29, 4, 4, 1)
                                                                 177: P_{6986} = (9, 25, 5, 1)
124: P_{5316} = (3, 5, 4, 1)
                                                                 178: P_{6999} = (22, 25, 5, 1)
125: P_{5329} = (16, 5, 4, 1)
                                                                 179: P_{7111} = (6, 29, 5, 1)
126: P_{5368} = (23, 6, 4, 1)
                                                                 180: P_{7133} = (28, 29, 5, 1)
127: P_{5372} = (27, 6, 4, 1)
                                                                 181: P_{7213} = (12, 0, 6, 1)
                                                                 182: P_{7303} = (6, 3, 6, 1)
128: P_{5383} = (6, 7, 4, 1)
129: P_{5405} = (28, 7, 4, 1)
                                                                 183: P_{7326} = (29, 3, 6, 1)
130: P_{5419} = (10, 8, 4, 1)
                                                                 184: P_{7334} = (5, 4, 6, 1)
131: P_{5437} = (28, 8, 4, 1)
                                                                 185: P_{7353} = (24, 4, 6, 1)
132: P_{5467} = (26, 9, 4, 1)
                                                                 186: P_{7364} = (3, 5, 6, 1)
133: P_{5570} = (1, 13, 4, 1)
                                                                 187: P_{7380} = (19, 5, 6, 1)
134: P_{5588} = (19, 13, 4, 1)
                                                                 188: P_{7410} = (17, 6, 6, 1)
135: P_{5605} = (4, 14, 4, 1)
                                                                 189: P_{7415} = (22, 6, 6, 1)
                                                                 190: P_{7505} = (16, 9, 6, 1)
136: P_{5610} = (9, 14, 4, 1)
137: P_{5639} = (6, 15, 4, 1)
                                                                 191: P_{7511} = (22, 9, 6, 1)
138: P_{5662} = (29, 15, 4, 1)
                                                                 192: P_{7530} = (9, 10, 6, 1)
139: P_{5665} = (0, 16, 4, 1)
                                                                 193: P_{7545} = (24, 10, 6, 1)
140: P_{5686} = (21, 16, 4, 1)
                                                                 194: P_{7626} = (9, 13, 6, 1)
141: P_{5835} = (10, 21, 4, 1)
                                                                 195: P_{7647} = (30, 13, 6, 1)
142: P_{5852} = (27, 21, 4, 1)
                                                                 196: P_{7654} = (5, 14, 6, 1)
143: P_{5954} = (1, 25, 4, 1)
                                                                 197: P_{7785} = (8, 18, 6, 1)
144: P_{5956} = (3, 25, 4, 1)
                                                                 198: P_{7793} = (16, 18, 6, 1)
145: P_{6036} = (19, 27, 4, 1)
                                                                 199: P_{7817} = (8, 19, 6, 1)
146: P_{6041} = (24, 27, 4, 1)
                                                                 200: P_{7838} = (29, 19, 6, 1)
                                                                 201: P_{7841} = (0, 20, 6, 1)
147: P_{6134} = (21, 30, 4, 1)
148: P_{6139} = (26, 30, 4, 1)
                                                                 202: P_{7860} = (19, 20, 6, 1)
                                                                 203: P_{7877} = (4, 21, 6, 1)
149: P_{6154} = (9, 31, 4, 1)
150: P_{6161} = (16, 31, 4, 1)
                                                                 204: P_{7899} = (26, 21, 6, 1)
                                                                 205: P_{7963} = (26, 23, 6, 1)
151: P_{6186} = (9, 0, 5, 1)
152: P_{6219} = (10, 1, 5, 1)
                                                                 206: P_{7967} = (30, 23, 6, 1)
                                                                 207: P_{8005} = (4, 25, 6, 1)
153: P_{6220} = (11, 1, 5, 1)
154: P_{6245} = (4, 2, 5, 1)
                                                                 208: P_{8013} = (12, 25, 6, 1)
                                                                 209: P_{8068} = (3, 27, 6, 1)
155: P_{6270} = (29, 2, 5, 1)
156: P_{6405} = (4, 7, 5, 1)
                                                                 210: P_{8082} = (17, 27, 6, 1)
157: P_{6417} = (16, 7, 5, 1)
                                                                 211: P_{8239} = (14, 0, 7, 1)
158: P_{6470} = (5, 9, 5, 1)
                                                                 212: P_{8259} = (2, 1, 7, 1)
                                                                 213: P_{8260} = (3, 1, 7, 1)
159: P_{6479} = (14, 9, 5, 1)
160: P_{6543} = (14, 11, 5, 1)
                                                                 214: P_{8336} = (15, 3, 7, 1)
161: P_{6550} = (21, 11, 5, 1)
                                                                 215: P_{8337} = (16, 3, 7, 1)
162: P_{6577} = (16, 12, 5, 1)
                                                                 216: P_{8475} = (26, 7, 7, 1)
163: P_{6583} = (22, 12, 5, 1)
                                                                 217: P_{8477} = (28, 7, 7, 1)
                                                                 218: P_{8519} = (6, 9, 7, 1)
164: P_{6659} = (2, 15, 5, 1)
165: P_{6685} = (28, 15, 5, 1)
                                                                 219: P_{8529} = (16, 9, 7, 1)
                                                                 220: P_{8637} = (28, 12, 7, 1)
166: P_{6721} = (0, 17, 5, 1)
167: P_{6742} = (21, 17, 5, 1)
                                                                 221: P_{8679} = (6, 14, 7, 1)
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222: P_{8697} = (24, 14, 7, 1)
                                                                276: P_{10490} = (25, 6, 9, 1)
223: P_{8897} = (0, 21, 7, 1)
                                                                277: P_{10503} = (6, 7, 9, 1)
224: P_{8916} = (19, 21, 7, 1)
                                                                278: P_{10523} = (26, 7, 9, 1)
225: P_{8946} = (17, 22, 7, 1)
                                                                279: P_{10533} = (4, 8, 9, 1)
226: P_{8948} = (19, 22, 7, 1)
                                                                280: P_{10556} = (27, 8, 9, 1)
227: P_{8966} = (5, 23, 7, 1)
                                                                281: P_{10625} = (0, 11, 9, 1)
228: P_{8969} = (8, 23, 7, 1)
                                                                282: P_{10628} = (3, 11, 9, 1)
229: P_{9030} = (5, 25, 7, 1)
                                                                283: P_{10659} = (2, 12, 9, 1)
230: P_{9049} = (24, 25, 7, 1)
                                                                284: P_{10668} = (11, 12, 9, 1)
231: P_{9059} = (2, 26, 7, 1)
                                                                285: P_{10698} = (9, 13, 9, 1)
232: P_{9071} = (14, 26, 7, 1)
                                                                286: P_{10712} = (23, 13, 9, 1)
233: P_{9106} = (17, 27, 7, 1)
                                                                287: P_{10947} = (2, 21, 9, 1)
234: P_{9107} = (18, 27, 7, 1)
                                                                288: P_{10952} = (7, 21, 9, 1)
235: P_{9156} = (3, 29, 7, 1)
                                                                289: P_{11064} = (23, 24, 9, 1)
236: P_{9160} = (7, 29, 7, 1)
                                                                290: P_{11067} = (26, 24, 9, 1)
237: P_{9200} = (15, 30, 7, 1)
                                                                291: P_{11140} = (3, 27, 9, 1)
238: P_{9211} = (26, 30, 7, 1)
                                                                292: P_{11155} = (18, 27, 9, 1)
239: P_{9225} = (8, 31, 7, 1)
                                                                293: P_{11182} = (13, 28, 9, 1)
240: P_{9235} = (18, 31, 7, 1)
                                                                294: P_{11191} = (22, 28, 9, 1)
241: P_{9253} = (4,0,8,1)
                                                                295: P_{11202} = (1, 29, 9, 1)
242: P_{9301} = (20, 1, 8, 1)
                                                                296: P_{11214} = (13, 29, 9, 1)
243: P_{9302} = (21, 1, 8, 1)
                                                                297: P_{11244} = (11, 30, 9, 1)
244: P_{9383} = (6, 4, 8, 1)
                                                                298: P_{11260} = (27, 30, 9, 1)
245: P_{9399} = (22, 4, 8, 1)
                                                                299: P_{11266} = (1, 31, 9, 1)
246: P_{9451} = (10, 6, 8, 1)
                                                                300: P_{11271} = (6, 31, 9, 1)
247: P_{9457} = (16, 6, 8, 1)
                                                                301: P_{11313} = (16, 0, 10, 1)
248: P_{9569} = (0, 10, 8, 1)
                                                                302: P_{11357} = (28, 1, 10, 1)
249: P_{9572} = (3, 10, 8, 1)
                                                                303: P_{11358} = (29, 1, 10, 1)
250: P_{9733} = (4, 15, 8, 1)
                                                                304: P_{11364} = (3, 2, 10, 1)
251: P_{9751} = (22, 15, 8, 1)
                                                                305: P_{11381} = (20, 2, 10, 1)
252: P_{9762} = (1, 16, 8, 1)
                                                                306: P_{11420} = (27, 3, 10, 1)
253: P_{9792} = (31, 16, 8, 1)
                                                                307: P_{11422} = (29, 3, 10, 1)
254: P_{9802} = (9, 17, 8, 1)
                                                                308: P_{11500} = (11, 6, 10, 1)
255: P_{9811} = (18, 17, 8, 1)
                                                                309: P_{11507} = (18, 6, 10, 1)
256: P_{9826} = (1, 18, 8, 1)
                                                                310: P_{11526} = (5, 7, 10, 1)
257: P_{9846} = (21, 18, 8, 1)
                                                                311: P_{11534} = (13, 7, 10, 1)
258: P_{9963} = (10, 22, 8, 1)
                                                                312: P_{11586} = (1, 9, 10, 1)
259: P_{9993} = (8, 23, 8, 1)
                                                                313: P_{11613} = (28, 9, 10, 1)
260: P_{9998} = (13, 23, 8, 1)
                                                                314: P_{11690} = (9, 12, 10, 1)
261: P_{10020} = (3, 24, 8, 1)
                                                                315: P_{11692} = (11, 12, 10, 1)
262: P_{10033} = (16, 24, 8, 1)
                                                                316: P_{11714} = (1, 13, 10, 1)
263: P_{10058} = (9, 25, 8, 1)
                                                                317: P_{11731} = (18, 13, 10, 1)
264: P_{10080} = (31, 25, 8, 1)
                                                                318: P_{11745} = (0, 14, 10, 1)
265: P_{10094} = (13, 26, 8, 1)
                                                                319: P_{11750} = (5, 14, 10, 1)
266: P_{10101} = (20, 26, 8, 1)
                                                                320: P_{11829} = (20, 16, 10, 1)
267: P_{10119} = (6, 27, 8, 1)
                                                                321: P_{11834} = (25, 16, 10, 1)
268: P_{10139} = (26, 27, 8, 1)
                                                                322: P_{11876} = (3, 18, 10, 1)
269: P_{10259} = (18, 31, 8, 1)
                                                                323: P_{11882} = (9, 18, 10, 1)
270: P_{10267} = (26, 31, 8, 1)
                                                                324: P_{11950} = (13, 20, 10, 1)
271: P_{10295} = (22, 0, 9, 1)
                                                                325: P_{11951} = (14, 20, 10, 1)
272: P_{10341} = (4, 2, 9, 1)
                                                                326: P_{12075} = (10, 24, 10, 1)
273: P_{10362} = (25, 2, 9, 1)
                                                                327: P_{12092} = (27, 24, 10, 1)
274: P_{10408} = (7, 4, 9, 1)
                                                                328: P_{12111} = (14, 25, 10, 1)
275: P_{10483} = (18, 6, 9, 1)
                                                                329: P_{12305} = (16, 31, 10, 1)
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330: P_{12314} = (25, 31, 10, 1)
                                                                384: P_{14174} = (29, 25, 12, 1)
331: P_{12346} = (25, 0, 11, 1)
                                                                385: P_{14177} = (0, 26, 12, 1)
332: P_{12390} = (5, 2, 11, 1)
                                                                386: P_{14200} = (23, 26, 12, 1)
333: P_{12394} = (9, 2, 11, 1)
                                                                387: P_{14254} = (13, 28, 12, 1)
334: P_{12455} = (6, 4, 11, 1)
                                                                388: P_{14268} = (27, 28, 12, 1)
335: P_{12465} = (16, 4, 11, 1)
                                                                389: P_{14356} = (19, 31, 12, 1)
336: P_{12548} = (3, 7, 11, 1)
                                                                390: P_{14360} = (23, 31, 12, 1)
337: P_{12569} = (24, 7, 11, 1)
                                                                391: P_{14376} = (7, 0, 13, 1)
338: P_{12643} = (2, 10, 11, 1)
                                                                392: P_{14434} = (1, 2, 13, 1)
339: P_{12657} = (16, 10, 11, 1)
                                                                393: P_{14443} = (10, 2, 13, 1)
340: P_{12801} = (0, 15, 11, 1)
                                                                394: P_{14507} = (10, 4, 13, 1)
341: P_{12806} = (5, 15, 11, 1)
                                                                395: P_{14518} = (21, 4, 13, 1)
342: P_{12854} = (21, 16, 11, 1)
                                                                396: P_{14630} = (5, 8, 13, 1)
                                                                397: P_{14648} = (23, 8, 13, 1)
343: P_{12898} = (1, 18, 11, 1)
344: P_{12917} = (20, 18, 11, 1)
                                                                398: P_{14672} = (15, 9, 13, 1)
345: P_{12931} = (2, 19, 11, 1)
                                                                399: P_{14684} = (27, 9, 13, 1)
346: P_{12944} = (15, 19, 11, 1)
                                                                400: P_{14770} = (17, 12, 13, 1)
347: P_{12967} = (6, 20, 11, 1)
                                                                401: P_{14780} = (27, 12, 13, 1)
348: P_{12970} = (9, 20, 11, 1)
                                                                402: P_{14806} = (21, 13, 13, 1)
349: P_{12996} = (3, 21, 11, 1)
                                                                403: P_{14810} = (25, 13, 13, 1)
350: P_{13013} = (20, 21, 11, 1)
                                                                404: P_{14841} = (24, 14, 13, 1)
351: P_{13026} = (1, 22, 11, 1)
                                                                405: P_{14847} = (30, 14, 13, 1)
352: P_{13052} = (27, 22, 11, 1)
                                                                406: P_{14854} = (5, 15, 13, 1)
353: P_{13082} = (25, 23, 11, 1)
                                                                407: P_{14970} = (25, 18, 13, 1)
354: P_{13084} = (27, 23, 11, 1)
                                                                408: P_{14974} = (29, 18, 13, 1)
355: P_{13157} = (4, 26, 11, 1)
                                                                409: P_{14990} = (13, 19, 13, 1)
356: P_{13168} = (15, 26, 11, 1)
                                                                410: P_{14992} = (15, 19, 13, 1)
357: P_{13196} = (11, 27, 11, 1)
                                                                411: P_{15010} = (1, 20, 13, 1)
358: P_{13209} = (24, 27, 11, 1)
                                                                412: P_{15026} = (17, 20, 13, 1)
359: P_{13221} = (4, 28, 11, 1)
                                                                413: P_{15109} = (4, 23, 13, 1)
360: P_{13238} = (21, 28, 11, 1)
                                                                414: P_{15135} = (30, 23, 13, 1)
361: P_{13360} = (15, 0, 12, 1)
                                                                415: P_{15233} = (0, 27, 13, 1)
362: P_{13407} = (30, 1, 12, 1)
                                                                416: P_{15256} = (23, 27, 13, 1)
363: P_{13408} = (31, 1, 12, 1)
                                                                417: P_{15289} = (24, 28, 13, 1)
364: P_{13447} = (6, 3, 12, 1)
                                                                418: P_{15294} = (29, 28, 13, 1)
365: P_{13468} = (27, 3, 12, 1)
                                                                419: P_{15301} = (4, 29, 13, 1)
366: P_{13599} = (30, 7, 12, 1)
                                                                420: P_{15304} = (7, 29, 13, 1)
367: P_{13726} = (29, 11, 12, 1)
                                                                421: P_{15406} = (13, 0, 14, 1)
                                                                422: P_{15447} = (22, 1, 14, 1)
368: P_{13728} = (31, 11, 12, 1)
369: P_{13837} = (12, 15, 12, 1)
                                                                423: P_{15448} = (23, 1, 14, 1)
370: P_{13844} = (19, 15, 12, 1)
                                                                424: P_{15526} = (5, 4, 14, 1)
371: P_{13870} = (13, 16, 12, 1)
                                                                425: P_{15550} = (29, 4, 14, 1)
372: P_{13882} = (25, 16, 12, 1)
                                                                426: P_{15555} = (2, 5, 14, 1)
373: P_{13937} = (16, 18, 12, 1)
                                                                427: P_{15575} = (22, 5, 14, 1)
374: P_{13945} = (24, 18, 12, 1)
                                                                428: P_{15615} = (30, 6, 14, 1)
375: P_{13991} = (6, 20, 12, 1)
                                                                429: P_{15619} = (2, 7, 14, 1)
376: P_{14000} = (15, 20, 12, 1)
                                                                430: P_{15631} = (14, 7, 14, 1)
377: P_{14019} = (2, 21, 12, 1)
                                                                431: P_{15686} = (5, 9, 14, 1)
378: P_{14022} = (5, 21, 12, 1)
                                                                432: P_{15692} = (11, 9, 14, 1)
379: P_{14054} = (5, 22, 12, 1)
                                                                433: P_{15746} = (1, 11, 14, 1)
380: P_{14065} = (16, 22, 12, 1)
                                                                434: P_{15768} = (23, 11, 14, 1)
381: P_{14083} = (2, 23, 12, 1)
                                                                435: P_{15815} = (6, 13, 14, 1)
382: P_{14106} = (25, 23, 12, 1)
                                                                436: P_{15838} = (29, 13, 14, 1)
383: P_{14169} = (24, 25, 12, 1)
                                                                437: P_{15975} = (6, 18, 14, 1)
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492: P_{17975} = (22, 16, 16, 1)
438: P_{15982} = (13, 18, 14, 1)
439: P_{16042} = (9, 20, 14, 1)
                                                                493: P_{17990} = (5, 17, 16, 1)
440: P_{16048} = (15, 20, 14, 1)
                                                                494: P_{17998} = (13, 17, 16, 1)
441: P_{16082} = (17, 21, 14, 1)
                                                                495: P_{18028} = (11, 18, 16, 1)
442: P_{16092} = (27, 21, 14, 1)
                                                                496: P_{18030} = (13, 18, 16, 1)
443: P_{16236} = (11, 26, 14, 1)
                                                                497: P_{18052} = (3, 19, 16, 1)
444: P_{16240} = (15, 26, 14, 1)
                                                                498: P_{18077} = (28, 19, 16, 1)
445: P_{16258} = (1, 27, 14, 1)
                                                                499: P_{18083} = (2, 20, 16, 1)
446: P_{16266} = (9, 27, 14, 1)
                                                                500: P_{18105} = (24, 20, 16, 1)
447: P_{16348} = (27, 29, 14, 1)
                                                                501: P_{18133} = (20, 21, 16, 1)
448: P_{16351} = (30, 29, 14, 1)
                                                                502: P_{18136} = (23, 21, 16, 1)
449: P_{16353} = (0, 30, 14, 1)
                                                                503: P_{18306} = (1, 27, 16, 1)
450: P_{16370} = (17, 30, 14, 1)
                                                                504: P_{18313} = (8, 27, 16, 1)
451: P_{16423} = (6, 0, 15, 1)
                                                                505: P_{18339} = (2, 28, 16, 1)
452: P_{16488} = (7, 2, 15, 1)
                                                                506: P_{18351} = (14, 28, 16, 1)
453: P_{16496} = (15, 2, 15, 1)
                                                                507: P_{18412} = (11, 30, 16, 1)
                                                                508: P_{18417} = (16, 30, 16, 1)
454: P_{16529} = (16, 3, 15, 1)
                                                                509: P_{18453} = (20, 31, 16, 1)
455: P_{16544} = (31, 3, 15, 1)
456: P_{16556} = (11, 4, 15, 1)
                                                                510: P_{18455} = (22, 31, 16, 1)
457: P_{16562} = (17, 4, 15, 1)
                                                                511: P_{18476} = (11, 0, 17, 1)
458: P_{16677} = (4, 8, 15, 1)
                                                                512: P_{18511} = (14, 1, 17, 1)
459: P_{16704} = (31, 8, 15, 1)
                                                                513: P_{18512} = (15, 1, 17, 1)
460: P_{16706} = (1, 9, 15, 1)
                                                                514: P_{18609} = (16, 4, 17, 1)
461: P_{16734} = (29, 9, 15, 1)
                                                                515: P_{18615} = (22, 4, 17, 1)
462: P_{16861} = (28, 13, 15, 1)
                                                                516: P_{18668} = (11, 6, 17, 1)
463: P_{16869} = (4, 14, 15, 1)
                                                                517: P_{18682} = (25, 6, 17, 1)
464: P_{16878} = (13, 14, 15, 1)
                                                                518: P_{18692} = (3, 7, 17, 1)
465: P_{16942} = (13, 16, 15, 1)
                                                                519: P_{18716} = (27, 7, 17, 1)
466: P_{16949} = (20, 16, 15, 1)
                                                                520: P_{18768} = (15, 9, 17, 1)
467: P_{17094} = (5, 21, 15, 1)
                                                                521: P_{18773} = (20, 9, 17, 1)
468: P_{17096} = (7, 21, 15, 1)
                                                                522: P_{18834} = (17, 11, 17, 1)
469: P_{17169} = (16, 23, 15, 1)
                                                                523: P_{18847} = (30, 11, 17, 1)
470: P_{17181} = (28, 23, 15, 1)
                                                                524: P_{18849} = (0, 12, 17, 1)
471: P_{17187} = (2, 24, 15, 1)
                                                                525: P_{18877} = (28, 12, 17, 1)
                                                                526: P_{18973} = (28, 15, 17, 1)
472: P_{17191} = (6, 24, 15, 1)
                                                                527: P_{18975} = (30, 15, 17, 1)
473: P_{17218} = (1, 25, 15, 1)
474: P_{17219} = (2, 25, 15, 1)
                                                                528: P_{19150} = (13, 21, 17, 1)
475: P_{17318} = (5, 28, 15, 1)
                                                                529: P_{19153} = (16, 21, 17, 1)
                                                                530: P_{19189} = (20, 22, 17, 1)
476: P_{17342} = (29, 28, 15, 1)
477: P_{17356} = (11, 29, 15, 1)
                                                                531: P_{19192} = (23, 22, 17, 1)
478: P_{17365} = (20, 29, 15, 1)
                                                                532: P_{19247} = (14, 24, 17, 1)
479: P_{17409} = (0, 31, 15, 1)
                                                                533: P_{19310} = (13, 26, 17, 1)
480: P_{17426} = (17, 31, 15, 1)
                                                                534: P_{19322} = (25, 26, 17, 1)
481: P_{17465} = (24, 0, 16, 1)
                                                                535: P_{19383} = (22, 28, 17, 1)
482: P_{17512} = (7, 2, 16, 1)
                                                                536: P_{19388} = (27, 28, 17, 1)
483: P_{17513} = (8, 2, 16, 1)
                                                                537: P_{19396} = (3, 29, 17, 1)
484: P_{17634} = (1, 6, 16, 1)
                                                                538: P_{19397} = (4, 29, 17, 1)
485: P_{17638} = (5, 6, 16, 1)
                                                                539: P_{19461} = (4, 31, 17, 1)
486: P_{17775} = (14, 10, 16, 1)
                                                                540: P_{19480} = (23, 31, 17, 1)
487: P_{17784} = (23, 10, 16, 1)
                                                                541: P_{19518} = (29, 0, 18, 1)
488: P_{17796} = (3, 11, 16, 1)
                                                                542: P_{19577} = (24, 2, 18, 1)
489: P_{17857} = (0, 13, 16, 1)
                                                                543: P_{19737} = (24, 7, 18, 1)
490: P_{17885} = (28, 13, 16, 1)
                                                                544: P_{19740} = (27, 7, 18, 1)
491: P_{17960} = (7, 16, 16, 1)
                                                                545: P_{19777} = (0, 9, 18, 1)
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546: P_{19803} = (26, 9, 18, 1)
                                                                600: P_{21512} = (7, 31, 19, 1)
547: P_{19931} = (26, 13, 18, 1)
                                                                601: P_{21563} = (26, 0, 20, 1)
548: P_{19936} = (31, 13, 18, 1)
                                                                602: P_{21606} = (5, 2, 20, 1)
549: P_{19946} = (9, 14, 18, 1)
                                                                603: P_{21613} = (12, 2, 20, 1)
550: P_{19950} = (13, 14, 18, 1)
                                                                604: P_{21717} = (20, 5, 20, 1)
551: P_{19970} = (1, 15, 18, 1)
                                                                605: P_{21719} = (22, 5, 20, 1)
552: P_{19994} = (25, 15, 18, 1)
                                                                606: P_{21745} = (16, 6, 20, 1)
553: P_{20019} = (18, 16, 18, 1)
                                                                607: P_{21755} = (26, 6, 20, 1)
554: P_{20029} = (28, 16, 18, 1)
                                                                608: P_{21803} = (10, 8, 20, 1)
555: P_{20042} = (9, 17, 18, 1)
                                                                609: P_{21815} = (22, 8, 20, 1)
556: P_{20060} = (27, 17, 18, 1)
                                                                610: P_{21835} = (10, 9, 20, 1)
557: P_{20099} = (2, 19, 18, 1)
                                                                611: P_{21838} = (13, 9, 20, 1)
558: P_{20110} = (13, 19, 18, 1)
                                                                612: P_{21902} = (13, 11, 20, 1)
559: P_{20130} = (1, 20, 18, 1)
                                                                613: P_{21914} = (25, 11, 20, 1)
560: P_{20145} = (16, 20, 18, 1)
                                                                614: P_{21992} = (7, 14, 20, 1)
561: P_{20177} = (16, 21, 18, 1)
                                                                615: P_{21996} = (11, 14, 20, 1)
562: P_{20190} = (29, 21, 18, 1)
                                                                616: P_{22056} = (7, 16, 20, 1)
563: P_{20237} = (12, 23, 18, 1)
                                                                617: P_{22066} = (17, 16, 20, 1)
                                                                618: P_{22086} = (5, 17, 20, 1)
564: P_{20253} = (28, 23, 18, 1)
565: P_{20269} = (12, 24, 18, 1)
                                                                619: P_{22089} = (8, 17, 20, 1)
566: P_{20282} = (25, 24, 18, 1)
                                                                620: P_{22189} = (12, 20, 20, 1)
567: P_{20311} = (22, 25, 18, 1)
                                                                621: P_{22202} = (25, 20, 20, 1)
568: P_{20320} = (31, 25, 18, 1)
                                                                622: P_{22308} = (3, 24, 20, 1)
569: P_{20355} = (2, 27, 18, 1)
                                                                623: P_{22324} = (19, 24, 20, 1)
570: P_{20375} = (22, 27, 18, 1)
                                                                624: P_{22412} = (11, 27, 20, 1)
571: P_{20515} = (2, 0, 19, 1)
                                                                625: P_{22420} = (19, 27, 20, 1)
572: P_{20551} = (6, 1, 19, 1)
                                                                626: P_{22436} = (3, 28, 20, 1)
573: P_{20552} = (7, 1, 19, 1)
                                                                627: P_{22449} = (16, 28, 20, 1)
574: P_{20602} = (25, 2, 19, 1)
                                                                628: P_{22465} = (0, 29, 20, 1)
575: P_{20606} = (29, 2, 19, 1)
                                                                629: P_{22473} = (8, 29, 20, 1)
576: P_{20642} = (1, 4, 19, 1)
                                                                630: P_{22514} = (17, 30, 20, 1)
577: P_{20656} = (15, 4, 19, 1)
                                                                631: P_{22591} = (30, 0, 21, 1)
578: P_{20691} = (18, 5, 19, 1)
                                                                632: P_{22597} = (4, 1, 21, 1)
                                                                633: P_{22598} = (5, 1, 21, 1)
579: P_{20704} = (31, 5, 19, 1)
580: P_{20769} = (0, 8, 19, 1)
                                                                634: P_{22634} = (9, 2, 21, 1)
581: P_{20795} = (26, 8, 19, 1)
                                                                635: P_{22637} = (12, 2, 21, 1)
582: P_{20867} = (2, 11, 19, 1)
                                                                636: P_{22661} = (4, 3, 21, 1)
583: P_{20894} = (29, 11, 19, 1)
                                                                637: P_{22687} = (30, 3, 21, 1)
584: P_{20903} = (6, 12, 19, 1)
                                                                638: P_{22734} = (13, 5, 21, 1)
585: P_{20913} = (16, 12, 19, 1)
                                                                639: P_{22752} = (31, 5, 21, 1)
586: P_{20941} = (12, 13, 19, 1)
                                                                640: P_{22760} = (7, 6, 21, 1)
587: P_{20954} = (25, 13, 19, 1)
                                                                641: P_{22770} = (17, 6, 21, 1)
588: P_{21005} = (12, 15, 19, 1)
                                                                642: P_{22926} = (13, 11, 21, 1)
589: P_{21024} = (31, 15, 19, 1)
                                                                643: P_{22933} = (20, 11, 21, 1)
590: P_{21232} = (15, 22, 19, 1)
                                                                644: P_{23146} = (9, 18, 21, 1)
591: P_{21235} = (18, 22, 19, 1)
                                                                645: P_{23147} = (10, 18, 21, 1)
592: P_{21253} = (4, 23, 19, 1)
                                                                646: P_{23172} = (3, 19, 21, 1)
593: P_{21275} = (26, 23, 19, 1)
                                                                647: P_{23200} = (31, 19, 21, 1)
594: P_{21317} = (4, 25, 19, 1)
                                                                648: P_{23236} = (3, 21, 21, 1)
595: P_{21321} = (8, 25, 19, 1)
                                                                649: P_{23256} = (23, 21, 21, 1)
596: P_{21425} = (16, 28, 19, 1)
                                                                650: P_{23270} = (5, 22, 21, 1)
597: P_{21428} = (19, 28, 19, 1)
                                                                651: P_{23286} = (21, 22, 21, 1)
598: P_{21449} = (8, 29, 19, 1)
                                                                652: P_{23339} = (10, 24, 21, 1)
599: P_{21506} = (1, 31, 19, 1)
                                                                653: P_{23346} = (17, 24, 21, 1)
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708: P_{25166} = (13, 17, 23, 1)
654: P_{23369} = (8, 25, 21, 1)
655: P_{23373} = (12, 25, 21, 1)
                                                                709: P_{25252} = (3, 20, 23, 1)
656: P_{23416} = (23, 26, 21, 1)
                                                                710: P_{25263} = (14, 20, 23, 1)
                                                                711: P_{25307} = (26, 21, 23, 1)
657: P_{23457} = (0, 28, 21, 1)
658: P_{23465} = (8, 28, 21, 1)
                                                                712: P_{25311} = (30, 21, 23, 1)
659: P_{23528} = (7, 30, 21, 1)
                                                                713: P_{25352} = (7, 23, 23, 1)
660: P_{23541} = (20, 30, 21, 1)
                                                                714: P_{25362} = (17, 23, 23, 1)
661: P_{23590} = (5, 0, 22, 1)
                                                                715: P_{25377} = (0, 24, 23, 1)
662: P_{23723} = (10, 4, 22, 1)
                                                                716: P_{25391} = (14, 24, 23, 1)
663: P_{23744} = (31, 4, 22, 1)
                                                                717: P_{25563} = (26, 29, 23, 1)
664: P_{23867} = (26, 8, 22, 1)
                                                                718: P_{25565} = (28, 29, 23, 1)
665: P_{23975} = (6, 12, 22, 1)
                                                                719: P_{25603} = (2, 31, 23, 1)
666: P_{23991} = (22, 12, 22, 1)
                                                                720: P_{25623} = (22, 31, 23, 1)
                                                                721: P_{25643} = (10, 0, 24, 1)
667: P_{24039} = (6, 14, 22, 1)
668: P_{24063} = (30, 14, 22, 1)
                                                                722: P_{25691} = (26, 1, 24, 1)
669: P_{24067} = (2, 15, 22, 1)
                                                                723: P_{25692} = (27, 1, 24, 1)
                                                                724: P_{25857} = (0, 7, 24, 1)
670: P_{24095} = (30, 15, 22, 1)
671: P_{24100} = (3, 16, 22, 1)
                                                                725: P_{25887} = (30, 7, 24, 1)
672: P_{24109} = (12, 16, 22, 1)
                                                                726: P_{25976} = (23, 10, 24, 1)
673: P_{24221} = (28, 19, 22, 1)
                                                                727: P_{25978} = (25, 10, 24, 1)
674: P_{24224} = (31, 19, 22, 1)
                                                                728: P_{26027} = (10, 12, 24, 1)
675: P_{24267} = (10, 21, 22, 1)
                                                                729: P_{26044} = (27, 12, 24, 1)
676: P_{24274} = (17, 21, 22, 1)
                                                                730: P_{26054} = (5, 13, 24, 1)
677: P_{24292} = (3, 22, 22, 1)
                                                                731: P_{26080} = (31, 13, 24, 1)
678: P_{24309} = (20, 22, 22, 1)
                                                                732: P_{26092} = (11, 14, 24, 1)
679: P_{24370} = (17, 24, 22, 1)
                                                                733: P_{26093} = (12, 14, 24, 1)
680: P_{24380} = (27, 24, 22, 1)
                                                                734: P_{26132} = (19, 15, 24, 1)
681: P_{24385} = (0, 25, 22, 1)
                                                                735: P_{26144} = (31, 15, 24, 1)
682: P_{24399} = (14, 25, 22, 1)
                                                                736: P_{26198} = (21, 17, 24, 1)
683: P_{24429} = (12, 26, 22, 1)
                                                                737: P_{26213} = (4, 18, 24, 1)
684: P_{24431} = (14, 26, 22, 1)
                                                                738: P_{26234} = (25, 18, 24, 1)
685: P_{24475} = (26, 27, 22, 1)
                                                                739: P_{26297} = (24, 20, 24, 1)
686: P_{24477} = (28, 27, 22, 1)
                                                                740: P_{26299} = (26, 20, 24, 1)
687: P_{24518} = (5, 29, 22, 1)
                                                                741: P_{26340} = (3, 22, 24, 1)
688: P_{24540} = (27, 29, 22, 1)
                                                                742: P_{26360} = (23, 22, 24, 1)
689: P_{24579} = (2, 31, 22, 1)
                                                                743: P_{26413} = (12, 24, 24, 1)
690: P_{24597} = (20, 31, 22, 1)
                                                                744: P_{26422} = (21, 24, 24, 1)
691: P_{24617} = (8, 0, 23, 1)
                                                                745: P_{26469} = (4, 26, 24, 1)
692: P_{24653} = (12, 1, 23, 1)
                                                                746: P_{26476} = (11, 26, 24, 1)
693: P_{24654} = (13, 1, 23, 1)
                                                                747: P_{26532} = (3, 28, 24, 1)
694: P_{24776} = (7, 5, 23, 1)
                                                                748: P_{26548} = (19, 28, 24, 1)
695: P_{24813} = (12, 6, 23, 1)
                                                                749: P_{26566} = (5, 29, 24, 1)
696: P_{24824} = (23, 6, 23, 1)
                                                                750: P_{26591} = (30, 29, 24, 1)
697: P_{24887} = (22, 8, 23, 1)
                                                                751: P_{26674} = (17, 0, 25, 1)
698: P_{24893} = (28, 8, 23, 1)
                                                                752: P_{26724} = (3, 2, 25, 1)
699: P_{24938} = (9, 10, 23, 1)
                                                                753: P_{26744} = (23, 2, 25, 1)
700: P_{24946} = (17, 10, 23, 1)
                                                                754: P_{26779} = (26, 3, 25, 1)
701: P_{24976} = (15, 11, 23, 1)
                                                                755: P_{26783} = (30, 3, 25, 1)
702: P_{24991} = (30, 11, 23, 1)
                                                                756: P_{26849} = (0, 6, 25, 1)
703: P_{24995} = (2, 12, 23, 1)
                                                                757: P_{26879} = (30, 6, 25, 1)
704: P_{25002} = (9, 12, 23, 1)
                                                                758: P_{26883} = (2, 7, 25, 1)
705: P_{25124} = (3, 16, 23, 1)
                                                                759: P_{26893} = (12, 7, 25, 1)
706: P_{25136} = (15, 16, 23, 1)
                                                                760: P_{26931} = (18, 8, 25, 1)
707: P_{25161} = (8, 17, 23, 1)
                                                                761: P_{26936} = (23, 8, 25, 1)
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762: P_{26980} = (3, 10, 25, 1)
                                                                816: P_{28988} = (27, 8, 27, 1)
763: P_{27078} = (5, 13, 25, 1)
                                                                817: P_{28992} = (31, 8, 27, 1)
764: P_{27099} = (26, 13, 25, 1)
                                                                818: P_{28999} = (6, 9, 27, 1)
765: P_{27183} = (14, 16, 25, 1)
                                                                819: P_{29015} = (22, 9, 27, 1)
766: P_{27187} = (18, 16, 25, 1)
                                                                820: P_{29042} = (17, 10, 27, 1)
767: P_{27237} = (4, 18, 25, 1)
                                                                821: P_{29049} = (24, 10, 27, 1)
768: P_{27262} = (29, 18, 25, 1)
                                                                822: P_{29059} = (2, 11, 27, 1)
769: P_{27363} = (2, 22, 25, 1)
                                                                823: P_{29088} = (31, 11, 27, 1)
770: P_{27378} = (17, 22, 25, 1)
                                                                824: P_{29231} = (14, 16, 27, 1)
771: P_{27462} = (5, 25, 25, 1)
                                                                825: P_{29245} = (28, 16, 27, 1)
772: P_{27486} = (29, 25, 25, 1)
                                                                826: P_{29425} = (16, 22, 27, 1)
773: P_{27509} = (20, 26, 25, 1)
                                                                827: P_{29430} = (21, 22, 27, 1)
774: P_{27514} = (25, 26, 25, 1)
                                                                828: P_{29448} = (7, 23, 27, 1)
                                                                829: P_{29463} = (22, 23, 27, 1)
775: P_{27565} = (12, 28, 25, 1)
776: P_{27567} = (14, 28, 25, 1)
                                                                830: P_{29489} = (16, 24, 27, 1)
777: P_{27636} = (19, 30, 25, 1)
                                                                831: P_{29492} = (19, 24, 27, 1)
778: P_{27637} = (20, 30, 25, 1)
                                                                832: P_{29539} = (2, 26, 27, 1)
779: P_{27653} = (4, 31, 25, 1)
                                                                833: P_{29549} = (12, 26, 27, 1)
                                                                834: P_{29575} = (6, 27, 27, 1)
780: P_{27668} = (19, 31, 25, 1)
781: P_{27712} = (31, 0, 26, 1)
                                                                835: P_{29597} = (28, 27, 27, 1)
782: P_{27731} = (18, 1, 26, 1)
                                                                836: P_{29634} = (1, 29, 27, 1)
783: P_{27732} = (19, 1, 26, 1)
                                                                837: P_{29645} = (12, 29, 27, 1)
784: P_{27777} = (0, 3, 26, 1)
                                                                838: P_{29672} = (7, 30, 27, 1)
785: P_{27801} = (24, 3, 26, 1)
                                                                839: P_{29684} = (19, 30, 27, 1)
786: P_{27843} = (2, 5, 26, 1)
                                                                840: P_{29714} = (17, 31, 27, 1)
787: P_{27861} = (20, 5, 26, 1)
                                                                841: P_{29748} = (19, 0, 28, 1)
788: P_{27880} = (7, 6, 26, 1)
                                                                842: P_{29777} = (16, 1, 28, 1)
789: P_{27895} = (22, 6, 26, 1)
                                                                843: P_{29778} = (17, 1, 28, 1)
790: P_{27976} = (7, 9, 26, 1)
                                                                844: P_{29849} = (24, 3, 28, 1)
791: P_{27982} = (13, 9, 26, 1)
                                                                845: P_{29868} = (11, 4, 28, 1)
792: P_{28103} = (6, 13, 26, 1)
                                                                846: P_{29883} = (26, 4, 28, 1)
793: P_{28124} = (27, 13, 26, 1)
                                                                847: P_{29905} = (16, 5, 28, 1)
794: P_{28179} = (18, 15, 26, 1)
                                                                848: P_{29908} = (19, 5, 28, 1)
795: P_{28183} = (22, 15, 26, 1)
                                                                849: P_{29931} = (10, 6, 28, 1)
796: P_{28265} = (8, 18, 26, 1)
                                                                850: P_{29947} = (26, 6, 28, 1)
797: P_{28281} = (24, 18, 26, 1)
                                                                851: P_{29965} = (12, 7, 28, 1)
798: P_{28372} = (19, 21, 26, 1)
                                                                852: P_{29967} = (14, 7, 28, 1)
799: P_{28419} = (2, 23, 26, 1)
                                                                853: P_{29990} = (5, 8, 28, 1)
800: P_{28444} = (27, 23, 26, 1)
                                                                854: P_{30003} = (18, 8, 28, 1)
801: P_{28453} = (4, 24, 26, 1)
                                                                855: P_{30028} = (11, 9, 28, 1)
802: P_{28455} = (6, 24, 26, 1)
                                                                856: P_{30031} = (14, 9, 28, 1)
803: P_{28494} = (13, 25, 26, 1)
                                                                857: P_{30236} = (27, 15, 28, 1)
804: P_{28498} = (17, 25, 26, 1)
                                                                858: P_{30238} = (29, 15, 28, 1)
805: P_{28581} = (4, 28, 26, 1)
                                                                859: P_{30291} = (18, 17, 28, 1)
806: P_{28594} = (17, 28, 26, 1)
                                                                860: P_{30300} = (27, 17, 28, 1)
807: P_{28629} = (20, 29, 26, 1)
                                                                861: P_{30358} = (21, 19, 28, 1)
808: P_{28640} = (31, 29, 26, 1)
                                                                862: P_{30366} = (29, 19, 28, 1)
809: P_{28681} = (8, 31, 26, 1)
                                                                863: P_{30381} = (12, 20, 28, 1)
810: P_{28699} = (26, 31, 26, 1)
                                                                864: P_{30390} = (21, 20, 28, 1)
811: P_{28726} = (21, 0, 27, 1)
                                                                865: P_{30465} = (0, 23, 28, 1)
812: P_{28769} = (0, 2, 27, 1)
                                                                866: P_{30475} = (10, 23, 28, 1)
813: P_{28793} = (24, 2, 27, 1)
                                                                867: P_{30546} = (17, 25, 28, 1)
814: P_{28834} = (1, 4, 27, 1)
                                                                868: P_{30557} = (28, 25, 28, 1)
815: P_{28847} = (14, 4, 27, 1)
                                                                869: P_{30630} = (5, 28, 28, 1)
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$870: P_{30649} = (24, 28, 28, 1)$	$916: P_{32325} = (4, 17, 30, 1)$
$871: P_{30756} = (3, 0, 29, 1)$	$917: P_{32346} = (25, 17, 30, 1)$
$872: P_{30825} = (8, 2, 29, 1)$	$918: P_{32385} = (0, 19, 30, 1)$
$873: P_{30832} = (15, 2, 29, 1)$	919: $P_{32397} = (12, 19, 30, 1)$
$874: P_{30898} = (17, 4, 29, 1)$	$920: P_{32436} = (19, 20, 30, 1)$
$875: P_{30907} = (26, 4, 29, 1)$	$921: P_{32453} = (4, 21, 30, 1)$
$876: P_{30982} = (5,7,29,1)$	$922: P_{32479} = (30, 21, 30, 1)$
$877: P_{30985} = (8,7,29,1)$	$923: P_{32483} = (2, 22, 30, 1)$
$878: P_{31087} = (14, 10, 29, 1)$	$924: P_{32500} = (19, 22, 30, 1)$
$879: P_{31098} = (25, 10, 29, 1)$	$925: P_{32661} = (20, 27, 30, 1)$
$880: P_{31119} = (14, 11, 29, 1)$	$926: P_{32663} = (22, 27, 30, 1)$
$881: P_{31132} = (27, 11, 29, 1)$	$927: P_{32675} = (2, 28, 30, 1)$
$882: P_{31147} = (10, 12, 29, 1)$	$928: P_{32685} = (12, 28, 30, 1)$
$883: P_{31154} = (17, 12, 29, 1)$	929: $P_{32716} = (11, 29, 30, 1)$
$884: P_{31181} = (12, 13, 29, 1)$	930: $P_{32736} = (31, 29, 30, 1)$
$885: P_{31190} = (21, 13, 29, 1)$	$931: P_{32821} = (20, 0, 31, 1)$
$886: P_{31239} = (6, 15, 29, 1)$	$932: P_{32950} = (21, 4, 31, 1)$
$887: P_{31260} = (27, 15, 29, 1)$	$933: P_{32960} = (31, 4, 31, 1)$
$888: P_{31322} = (25, 17, 29, 1)$	$934: P_{32974} = (13, 5, 31, 1)$
$889: P_{31326} = (29, 17, 29, 1)$	$935: P_{32979} = (18, 5, 31, 1)$
$890: P_{31373} = (12, 19, 29, 1)$	$936: P_{32994} = (1, 6, 31, 1)$
$891: P_{31396} = (3, 20, 29, 1)$	$937: P_{32997} = (4, 6, 31, 1)$
$892: P_{31406} = (13, 20, 29, 1)$	938: $P_{33029} = (4, 7, 31, 1)$
$893: P_{31457} = (0, 22, 29, 1)$	$939: P_{33045} = (20, 7, 31, 1)$
$894: P_{31467} = (10, 22, 29, 1)$	$940: P_{33137} = (16, 10, 31, 1)$
$895: P_{31494} = (5, 23, 29, 1)$	
	$941: P_{33139} = (18, 10, 31, 1)$
$896: P_{31502} = (13, 23, 29, 1)$	$942: P_{33154} = (1, 11, 31, 1)$
$897: P_{31687} = (6, 29, 29, 1)$	$943: P_{33175} = (22, 11, 31, 1)$
$898: P_{31707} = (26, 29, 29, 1)$	$944: P_{33244} = (27, 13, 31, 1)$
$899: P_{31728} = (15, 30, 29, 1)$	$945: P_{33246} = (29, 13, 31, 1)$
$900: P_{31734} = (21, 30, 29, 1)$	$946: P_{33325} = (12, 16, 31, 1)$
$901: P_{31804} = (27, 0, 30, 1)$	$947: P_{33328} = (15, 16, 31, 1)$
$902: P_{31833} = (24, 1, 30, 1)$	$948: P_{33377} = (0, 18, 31, 1)$
$903: P_{31834} = (25, 1, 30, 1)$	$949: P_{33389} = (12, 18, 31, 1)$
$904: P_{31842} = (1, 2, 30, 1)$	$950: P_{33520} = (15, 22, 31, 1)$
$905: P_{31852} = (11, 2, 30, 1)$	951: $P_{33534} = (29, 22, 31, 1)$
$906: P_{31888} = (15, 3, 30, 1)$	$952: P_{33554} = (17, 23, 31, 1)$
$907: P_{31904} = (31, 3, 30, 1)$	$953: P_{33559} = (22, 23, 31, 1)$
$908: P_{32085} = (20, 9, 30, 1)$	$954: P_{33582} = (13, 24, 31, 1)$
$909: P_{32092} = (27, 9, 30, 1)$	$955: P_{33592} = (23, 24, 31, 1)$
$910: P_{32144} = (15, 11, 30, 1)$	$956: P_{33688} = (23, 27, 31, 1)$
$911: P_{32146} = (17, 11, 30, 1)$	$957: P_{33714} = (17, 28, 31, 1)$
$912: P_{32258} = (1, 15, 30, 1)$	$958: P_{33718} = (21, 28, 31, 1)$
$913: P_{32281} = (24, 15, 30, 1)$	$959: P_{33777} = (16, 30, 31, 1)$
$914: P_{32306} = (17, 16, 30, 1)$	$960: P_{33788} = (27, 30, 31, 1)$
$915: P_{32311} = (22, 16, 30, 1)$	
-= \ , , , ,	

Line Intersection Graph

	0	1	2	3
0 1 2	0	1	0	1
1	1	0	0	1
2	0	0	0	1
3	1	1	1	(

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_3
in point	P_0	P_5

 ${\bf Line~1~intersects}$

Line	ℓ_0	ℓ_3
in point	P_0	P_4

Line 2 intersects

Line	ℓ_3
in point	P_{2082}

Line 3 intersects

Line	ℓ_0	ℓ_1	ℓ_2
in point	P_5	P_4	P_{2082}

The surface has 1089 points:

Too many to print.