

Rank-65609 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_1^3 + X_2^3 + X_0^2 X_3 + X_0 X_1 X_2 = 0$$

(0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is -2112845755

General information

Number of lines	2
Number of points	1057
Number of singular points	1
Number of Eckardt points	0
Number of double points	1
Number of single points	64
Number of points off lines	992
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^2
Type of lines on points	$2, 1^{64}, 0^{992}$

Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

The 2 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned} \ell_0 &= \left[\begin{array}{cccc} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{1082433} = \left[\begin{array}{cccc} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{1082433} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{97} \\ \ell_1 &= \left[\begin{array}{cccc} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{array} \right]_{34882} = \left[\begin{array}{cccc} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{array} \right]_{34882} = \mathbf{Pl}(1, 1, 1, 1, 0, 1)_{38818} \end{aligned}$$

Rank of lines: (1082433, 34882)
Rank of points on Klein quadric: (97, 38818)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 1 Double points:
The double points on the surface are:

$$P_{67} = (0, 1, 1, 0) = \ell_0 \cap \ell_1$$

Single Points

The surface has 64 single points:
The single points on the surface are:

- | | |
|---|---|
| 0 : $P_3 = (0, 0, 0, 1)$ lies on line ℓ_0 | 33 : $P_{17986} = (1, 17, 16, 1)$ lies on line ℓ_1 |
| 1 : $P_{1091} = (1, 1, 0, 1)$ lies on line ℓ_1 | 34 : $P_{18978} = (1, 16, 17, 1)$ lies on line ℓ_1 |
| 2 : $P_{2083} = (1, 0, 1, 1)$ lies on line ℓ_1 | 35 : $P_{19009} = (0, 17, 17, 1)$ lies on line ℓ_0 |
| 3 : $P_{2114} = (0, 1, 1, 1)$ lies on line ℓ_0 | 36 : $P_{20065} = (0, 18, 18, 1)$ lies on line ℓ_0 |
| 4 : $P_{3169} = (0, 2, 2, 1)$ lies on line ℓ_0 | 37 : $P_{20098} = (1, 19, 18, 1)$ lies on line ℓ_1 |
| 5 : $P_{3202} = (1, 3, 2, 1)$ lies on line ℓ_1 | 38 : $P_{21090} = (1, 18, 19, 1)$ lies on line ℓ_1 |
| 6 : $P_{4194} = (1, 2, 3, 1)$ lies on line ℓ_1 | 39 : $P_{21121} = (0, 19, 19, 1)$ lies on line ℓ_0 |
| 7 : $P_{4225} = (0, 3, 3, 1)$ lies on line ℓ_0 | 40 : $P_{22177} = (0, 20, 20, 1)$ lies on line ℓ_0 |
| 8 : $P_{5281} = (0, 4, 4, 1)$ lies on line ℓ_0 | 41 : $P_{22210} = (1, 21, 20, 1)$ lies on line ℓ_1 |
| 9 : $P_{5314} = (1, 5, 4, 1)$ lies on line ℓ_1 | 42 : $P_{23202} = (1, 20, 21, 1)$ lies on line ℓ_1 |
| 10 : $P_{6306} = (1, 4, 5, 1)$ lies on line ℓ_1 | 43 : $P_{23233} = (0, 21, 21, 1)$ lies on line ℓ_0 |
| 11 : $P_{6337} = (0, 5, 5, 1)$ lies on line ℓ_0 | 44 : $P_{24289} = (0, 22, 22, 1)$ lies on line ℓ_0 |
| 12 : $P_{7393} = (0, 6, 6, 1)$ lies on line ℓ_0 | 45 : $P_{24322} = (1, 23, 22, 1)$ lies on line ℓ_1 |
| 13 : $P_{7426} = (1, 7, 6, 1)$ lies on line ℓ_1 | 46 : $P_{25314} = (1, 22, 23, 1)$ lies on line ℓ_1 |
| 14 : $P_{8418} = (1, 6, 7, 1)$ lies on line ℓ_1 | 47 : $P_{25345} = (0, 23, 23, 1)$ lies on line ℓ_0 |
| 15 : $P_{8449} = (0, 7, 7, 1)$ lies on line ℓ_0 | 48 : $P_{26401} = (0, 24, 24, 1)$ lies on line ℓ_0 |
| 16 : $P_{9505} = (0, 8, 8, 1)$ lies on line ℓ_0 | 49 : $P_{26434} = (1, 25, 24, 1)$ lies on line ℓ_1 |
| 17 : $P_{9538} = (1, 9, 8, 1)$ lies on line ℓ_1 | 50 : $P_{27426} = (1, 24, 25, 1)$ lies on line ℓ_1 |
| 18 : $P_{10530} = (1, 8, 9, 1)$ lies on line ℓ_1 | 51 : $P_{27457} = (0, 25, 25, 1)$ lies on line ℓ_0 |
| 19 : $P_{10561} = (0, 9, 9, 1)$ lies on line ℓ_0 | 52 : $P_{28513} = (0, 26, 26, 1)$ lies on line ℓ_0 |
| 20 : $P_{11617} = (0, 10, 10, 1)$ lies on line ℓ_0 | 53 : $P_{28546} = (1, 27, 26, 1)$ lies on line ℓ_1 |
| 21 : $P_{11650} = (1, 11, 10, 1)$ lies on line ℓ_1 | 54 : $P_{29538} = (1, 26, 27, 1)$ lies on line ℓ_1 |
| 22 : $P_{12642} = (1, 10, 11, 1)$ lies on line ℓ_1 | 55 : $P_{29569} = (0, 27, 27, 1)$ lies on line ℓ_0 |
| 23 : $P_{12673} = (0, 11, 11, 1)$ lies on line ℓ_0 | 56 : $P_{30625} = (0, 28, 28, 1)$ lies on line ℓ_0 |
| 24 : $P_{13729} = (0, 12, 12, 1)$ lies on line ℓ_0 | 57 : $P_{30658} = (1, 29, 28, 1)$ lies on line ℓ_1 |
| 25 : $P_{13762} = (1, 13, 12, 1)$ lies on line ℓ_1 | 58 : $P_{31650} = (1, 28, 29, 1)$ lies on line ℓ_1 |
| 26 : $P_{14754} = (1, 12, 13, 1)$ lies on line ℓ_1 | 59 : $P_{31681} = (0, 29, 29, 1)$ lies on line ℓ_0 |
| 27 : $P_{14785} = (0, 13, 13, 1)$ lies on line ℓ_0 | 60 : $P_{32737} = (0, 30, 30, 1)$ lies on line ℓ_0 |
| 28 : $P_{15841} = (0, 14, 14, 1)$ lies on line ℓ_0 | 61 : $P_{32770} = (1, 31, 30, 1)$ lies on line ℓ_1 |
| 29 : $P_{15874} = (1, 15, 14, 1)$ lies on line ℓ_1 | 62 : $P_{33762} = (1, 30, 31, 1)$ lies on line ℓ_1 |
| 30 : $P_{16866} = (1, 14, 15, 1)$ lies on line ℓ_1 | 63 : $P_{33793} = (0, 31, 31, 1)$ lies on line ℓ_0 |
| 31 : $P_{16897} = (0, 15, 15, 1)$ lies on line ℓ_0 | |
| 32 : $P_{17953} = (0, 16, 16, 1)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 992 points not on any line:

The points on the surface but not on lines are:

0 : $P_0 = (1, 0, 0, 0)$	45 : $P_{1544} = (6, 15, 0, 1)$
1 : $P_4 = (1, 1, 1, 1)$	46 : $P_{1580} = (10, 16, 0, 1)$
2 : $P_{121} = (22, 2, 1, 0)$	47 : $P_{1633} = (31, 17, 0, 1)$
3 : $P_{156} = (25, 3, 1, 0)$	48 : $P_{1663} = (29, 18, 0, 1)$
4 : $P_{188} = (25, 4, 1, 0)$	49 : $P_{1683} = (17, 19, 0, 1)$
5 : $P_{201} = (6, 5, 1, 0)$	50 : $P_{1721} = (23, 20, 0, 1)$
6 : $P_{253} = (26, 6, 1, 0)$	51 : $P_{1734} = (4, 21, 0, 1)$
7 : $P_{284} = (25, 7, 1, 0)$	52 : $P_{1769} = (7, 22, 0, 1)$
8 : $P_{319} = (28, 8, 1, 0)$	53 : $P_{1807} = (13, 23, 0, 1)$
9 : $P_{338} = (15, 9, 1, 0)$	54 : $P_{1853} = (27, 24, 0, 1)$
10 : $P_{378} = (23, 10, 1, 0)$	55 : $P_{1879} = (21, 25, 0, 1)$
11 : $P_{418} = (31, 11, 1, 0)$	56 : $P_{1899} = (9, 26, 0, 1)$
12 : $P_{448} = (29, 12, 1, 0)$	57 : $P_{1952} = (30, 27, 0, 1)$
13 : $P_{471} = (20, 13, 1, 0)$	58 : $P_{1970} = (16, 28, 0, 1)$
14 : $P_{507} = (24, 14, 1, 0)$	59 : $P_{2010} = (24, 29, 0, 1)$
15 : $P_{533} = (18, 15, 1, 0)$	60 : $P_{2023} = (5, 30, 0, 1)$
16 : $P_{553} = (6, 16, 1, 0)$	61 : $P_{2070} = (20, 31, 0, 1)$
17 : $P_{599} = (20, 17, 1, 0)$	62 : $P_{2174} = (29, 2, 1, 1)$
18 : $P_{622} = (11, 18, 1, 0)$	63 : $P_{2176} = (31, 2, 1, 1)$
19 : $P_{664} = (21, 19, 1, 0)$	64 : $P_{2189} = (12, 3, 1, 1)$
20 : $P_{678} = (3, 20, 1, 0)$	65 : $P_{2192} = (15, 3, 1, 1)$
21 : $P_{713} = (6, 21, 1, 0)$	66 : $P_{2227} = (18, 4, 1, 1)$
22 : $P_{756} = (17, 22, 1, 0)$	67 : $P_{2231} = (22, 4, 1, 1)$
23 : $P_{800} = (29, 23, 1, 0)$	68 : $P_{2267} = (26, 5, 1, 1)$
24 : $P_{825} = (22, 24, 1, 0)$	69 : $P_{2272} = (31, 5, 1, 1)$
25 : $P_{847} = (12, 25, 1, 0)$	70 : $P_{2329} = (24, 7, 1, 1)$
26 : $P_{889} = (22, 26, 1, 0)$	71 : $P_{2336} = (31, 7, 1, 1)$
27 : $P_{928} = (29, 27, 1, 0)$	72 : $P_{2389} = (20, 9, 1, 1)$
28 : $P_{951} = (20, 28, 1, 0)$	73 : $P_{2398} = (29, 9, 1, 1)$
29 : $P_{968} = (5, 29, 1, 0)$	74 : $P_{2455} = (22, 11, 1, 1)$
30 : $P_{1002} = (7, 30, 1, 0)$	75 : $P_{2462} = (29, 11, 1, 1)$
31 : $P_{1036} = (9, 31, 1, 0)$	76 : $P_{2470} = (5, 12, 1, 1)$
32 : $P_{1141} = (19, 2, 0, 1)$	77 : $P_{2474} = (9, 12, 1, 1)$
33 : $P_{1165} = (11, 3, 0, 1)$	78 : $P_{2503} = (6, 13, 1, 1)$
34 : $P_{1194} = (8, 4, 0, 1)$	79 : $P_{2508} = (11, 13, 1, 1)$
35 : $P_{1233} = (15, 5, 0, 1)$	80 : $P_{2583} = (22, 15, 1, 1)$
36 : $P_{1278} = (28, 6, 0, 1)$	81 : $P_{2586} = (25, 15, 1, 1)$
37 : $P_{1284} = (2, 7, 0, 1)$	82 : $P_{2602} = (9, 16, 1, 1)$
38 : $P_{1326} = (12, 8, 0, 1)$	83 : $P_{2618} = (25, 16, 1, 1)$
39 : $P_{1368} = (22, 9, 0, 1)$	84 : $P_{2628} = (3, 17, 1, 1)$
40 : $P_{1404} = (26, 10, 0, 1)$	85 : $P_{2643} = (18, 17, 1, 1)$
41 : $P_{1435} = (25, 11, 0, 1)$	86 : $P_{2663} = (6, 18, 1, 1)$
42 : $P_{1460} = (18, 12, 0, 1)$	87 : $P_{2677} = (20, 18, 1, 1)$
43 : $P_{1488} = (14, 13, 0, 1)$	88 : $P_{2760} = (7, 21, 1, 1)$
44 : $P_{1509} = (3, 14, 0, 1)$	89 : $P_{2771} = (18, 21, 1, 1)$

90 : $P_{2828} = (11, 23, 1, 1)$	144 : $P_{4998} = (5, 27, 3, 1)$
91 : $P_{2845} = (28, 23, 1, 1)$	145 : $P_{5006} = (13, 27, 3, 1)$
92 : $P_{2864} = (15, 24, 1, 1)$	146 : $P_{5033} = (8, 28, 3, 1)$
93 : $P_{2872} = (23, 24, 1, 1)$	147 : $P_{5034} = (9, 28, 3, 1)$
94 : $P_{2924} = (11, 26, 1, 1)$	148 : $P_{5073} = (16, 29, 3, 1)$
95 : $P_{2930} = (17, 26, 1, 1)$	149 : $P_{5075} = (18, 29, 3, 1)$
96 : $P_{2960} = (15, 27, 1, 1)$	150 : $P_{5108} = (19, 30, 3, 1)$
97 : $P_{2965} = (20, 27, 1, 1)$	151 : $P_{5109} = (20, 30, 3, 1)$
98 : $P_{2986} = (9, 28, 1, 1)$	152 : $P_{5161} = (8, 0, 4, 1)$
99 : $P_{2998} = (21, 28, 1, 1)$	153 : $P_{5203} = (18, 1, 4, 1)$
100 : $P_{3079} = (6, 31, 1, 1)$	154 : $P_{5207} = (22, 1, 4, 1)$
101 : $P_{3098} = (25, 31, 1, 1)$	155 : $P_{5253} = (4, 3, 4, 1)$
102 : $P_{3124} = (19, 0, 2, 1)$	156 : $P_{5257} = (8, 3, 4, 1)$
103 : $P_{3166} = (29, 1, 2, 1)$	157 : $P_{5297} = (16, 4, 4, 1)$
104 : $P_{3168} = (31, 1, 2, 1)$	158 : $P_{5334} = (21, 5, 4, 1)$
105 : $P_{3173} = (4, 2, 2, 1)$	159 : $P_{5433} = (24, 8, 4, 1)$
106 : $P_{3208} = (7, 3, 2, 1)$	160 : $P_{5438} = (29, 8, 4, 1)$
107 : $P_{3282} = (17, 5, 2, 1)$	161 : $P_{5699} = (2, 17, 4, 1)$
108 : $P_{3292} = (27, 5, 2, 1)$	162 : $P_{5709} = (12, 17, 4, 1)$
109 : $P_{3352} = (23, 7, 2, 1)$	163 : $P_{5831} = (6, 21, 4, 1)$
110 : $P_{3354} = (25, 7, 2, 1)$	164 : $P_{5849} = (24, 21, 4, 1)$
111 : $P_{3595} = (10, 15, 2, 1)$	165 : $P_{5900} = (11, 23, 4, 1)$
112 : $P_{3605} = (20, 15, 2, 1)$	166 : $P_{5918} = (29, 23, 4, 1)$
113 : $P_{3733} = (20, 19, 2, 1)$	167 : $P_{5938} = (17, 24, 4, 1)$
114 : $P_{3736} = (23, 19, 2, 1)$	168 : $P_{5951} = (30, 24, 4, 1)$
115 : $P_{3768} = (23, 20, 2, 1)$	169 : $P_{6084} = (3, 29, 4, 1)$
116 : $P_{3771} = (26, 20, 2, 1)$	170 : $P_{6105} = (24, 29, 4, 1)$
117 : $P_{3846} = (5, 23, 2, 1)$	171 : $P_{6159} = (14, 31, 4, 1)$
118 : $P_{3855} = (14, 23, 2, 1)$	172 : $P_{6174} = (29, 31, 4, 1)$
119 : $P_{3939} = (2, 26, 2, 1)$	173 : $P_{6192} = (15, 0, 5, 1)$
120 : $P_{3956} = (19, 26, 2, 1)$	174 : $P_{6235} = (26, 1, 5, 1)$
121 : $P_{4010} = (9, 28, 2, 1)$	175 : $P_{6240} = (31, 1, 5, 1)$
122 : $P_{4021} = (20, 28, 2, 1)$	176 : $P_{6258} = (17, 2, 5, 1)$
123 : $P_{4140} = (11, 0, 3, 1)$	177 : $P_{6268} = (27, 2, 5, 1)$
124 : $P_{4173} = (12, 1, 3, 1)$	178 : $P_{6326} = (21, 4, 5, 1)$
125 : $P_{4176} = (15, 1, 3, 1)$	179 : $P_{6354} = (17, 5, 5, 1)$
126 : $P_{4200} = (7, 2, 3, 1)$	180 : $P_{6411} = (10, 7, 5, 1)$
127 : $P_{4230} = (5, 3, 3, 1)$	181 : $P_{6418} = (17, 7, 5, 1)$
128 : $P_{4261} = (4, 4, 3, 1)$	182 : $P_{6538} = (9, 11, 5, 1)$
129 : $P_{4265} = (8, 4, 3, 1)$	183 : $P_{6540} = (11, 11, 5, 1)$
130 : $P_{4426} = (9, 9, 3, 1)$	184 : $P_{6665} = (8, 15, 5, 1)$
131 : $P_{4435} = (18, 9, 3, 1)$	185 : $P_{6687} = (30, 15, 5, 1)$
132 : $P_{4495} = (14, 11, 3, 1)$	186 : $P_{6699} = (10, 16, 5, 1)$
133 : $P_{4500} = (19, 11, 3, 1)$	187 : $P_{6705} = (16, 16, 5, 1)$
134 : $P_{4592} = (15, 14, 3, 1)$	188 : $P_{6793} = (8, 19, 5, 1)$
135 : $P_{4606} = (29, 14, 3, 1)$	189 : $P_{6814} = (29, 19, 5, 1)$
136 : $P_{4624} = (15, 15, 3, 1)$	190 : $P_{6890} = (9, 22, 5, 1)$
137 : $P_{4639} = (30, 15, 3, 1)$	191 : $P_{6894} = (13, 22, 5, 1)$
138 : $P_{4780} = (11, 20, 3, 1)$	192 : $P_{6923} = (10, 23, 5, 1)$
139 : $P_{4787} = (18, 20, 3, 1)$	193 : $P_{6924} = (11, 23, 5, 1)$
140 : $P_{4810} = (9, 21, 3, 1)$	194 : $P_{7081} = (8, 28, 5, 1)$
141 : $P_{4820} = (19, 21, 3, 1)$	195 : $P_{7084} = (11, 28, 5, 1)$
142 : $P_{4902} = (5, 24, 3, 1)$	196 : $P_{7114} = (9, 29, 5, 1)$
143 : $P_{4905} = (8, 24, 3, 1)$	197 : $P_{7120} = (15, 29, 5, 1)$

198 : $P_{7159} = (22, 30, 5, 1)$
 199 : $P_{7168} = (31, 30, 5, 1)$
 200 : $P_{7188} = (19, 31, 5, 1)$
 201 : $P_{7200} = (31, 31, 5, 1)$
 202 : $P_{7229} = (28, 0, 6, 1)$
 203 : $P_{7413} = (20, 6, 6, 1)$
 204 : $P_{7444} = (19, 7, 6, 1)$
 205 : $P_{7535} = (14, 10, 6, 1)$
 206 : $P_{7544} = (23, 10, 6, 1)$
 207 : $P_{7587} = (2, 12, 6, 1)$
 208 : $P_{7600} = (15, 12, 6, 1)$
 209 : $P_{7655} = (6, 14, 6, 1)$
 210 : $P_{7656} = (7, 14, 6, 1)$
 211 : $P_{7706} = (25, 15, 6, 1)$
 212 : $P_{7711} = (30, 15, 6, 1)$
 213 : $P_{7843} = (2, 20, 6, 1)$
 214 : $P_{7862} = (21, 20, 6, 1)$
 215 : $P_{7944} = (7, 23, 6, 1)$
 216 : $P_{7963} = (26, 23, 6, 1)$
 217 : $P_{7971} = (2, 24, 6, 1)$
 218 : $P_{7993} = (24, 24, 6, 1)$
 219 : $P_{8008} = (7, 25, 6, 1)$
 220 : $P_{8028} = (27, 25, 6, 1)$
 221 : $P_{8042} = (9, 26, 6, 1)$
 222 : $P_{8064} = (31, 26, 6, 1)$
 223 : $P_{8077} = (12, 27, 6, 1)$
 224 : $P_{8093} = (28, 27, 6, 1)$
 225 : $P_{8105} = (8, 28, 6, 1)$
 226 : $P_{8107} = (10, 28, 6, 1)$
 227 : $P_{8227} = (2, 0, 7, 1)$
 228 : $P_{8281} = (24, 1, 7, 1)$
 229 : $P_{8288} = (31, 1, 7, 1)$
 230 : $P_{8312} = (23, 2, 7, 1)$
 231 : $P_{8314} = (25, 2, 7, 1)$
 232 : $P_{8395} = (10, 5, 7, 1)$
 233 : $P_{8402} = (17, 5, 7, 1)$
 234 : $P_{8436} = (19, 6, 7, 1)$
 235 : $P_{8470} = (21, 7, 7, 1)$
 236 : $P_{8492} = (11, 8, 7, 1)$
 237 : $P_{8503} = (22, 8, 7, 1)$
 238 : $P_{8528} = (15, 9, 7, 1)$
 239 : $P_{8534} = (21, 9, 7, 1)$
 240 : $P_{8547} = (2, 10, 7, 1)$
 241 : $P_{8562} = (17, 10, 7, 1)$
 242 : $P_{8639} = (30, 12, 7, 1)$
 243 : $P_{8640} = (31, 12, 7, 1)$
 244 : $P_{8666} = (25, 13, 7, 1)$
 245 : $P_{8672} = (31, 13, 7, 1)$
 246 : $P_{8694} = (21, 14, 7, 1)$
 247 : $P_{8699} = (26, 14, 7, 1)$
 248 : $P_{8722} = (17, 15, 7, 1)$
 249 : $P_{8730} = (25, 15, 7, 1)$
 250 : $P_{8749} = (12, 16, 7, 1)$
 251 : $P_{8756} = (19, 16, 7, 1)$

252 : $P_{8869} = (4, 20, 7, 1)$
 253 : $P_{8872} = (7, 20, 7, 1)$
 254 : $P_{8948} = (19, 22, 7, 1)$
 255 : $P_{8959} = (30, 22, 7, 1)$
 256 : $P_{9075} = (18, 26, 7, 1)$
 257 : $P_{9087} = (30, 26, 7, 1)$
 258 : $P_{9158} = (5, 29, 7, 1)$
 259 : $P_{9181} = (28, 29, 7, 1)$
 260 : $P_{9198} = (13, 30, 7, 1)$
 261 : $P_{9214} = (29, 30, 7, 1)$
 262 : $P_{9220} = (3, 31, 7, 1)$
 263 : $P_{9237} = (20, 31, 7, 1)$
 264 : $P_{9261} = (12, 0, 8, 1)$
 265 : $P_{9401} = (24, 4, 8, 1)$
 266 : $P_{9406} = (29, 4, 8, 1)$
 267 : $P_{9484} = (11, 7, 8, 1)$
 268 : $P_{9495} = (22, 7, 8, 1)$
 269 : $P_{9515} = (10, 8, 8, 1)$
 270 : $P_{9540} = (3, 9, 8, 1)$
 271 : $P_{9576} = (7, 10, 8, 1)$
 272 : $P_{9598} = (29, 10, 8, 1)$
 273 : $P_{9613} = (12, 11, 8, 1)$
 274 : $P_{9631} = (30, 11, 8, 1)$
 275 : $P_{9639} = (6, 12, 8, 1)$
 276 : $P_{9642} = (9, 12, 8, 1)$
 277 : $P_{9699} = (2, 14, 8, 1)$
 278 : $P_{9726} = (29, 14, 8, 1)$
 279 : $P_{9803} = (10, 17, 8, 1)$
 280 : $P_{9815} = (22, 17, 8, 1)$
 281 : $P_{9827} = (2, 18, 8, 1)$
 282 : $P_{9831} = (6, 18, 8, 1)$
 283 : $P_{9877} = (20, 19, 8, 1)$
 284 : $P_{9881} = (24, 19, 8, 1)$
 285 : $P_{9975} = (22, 22, 8, 1)$
 286 : $P_{9976} = (23, 22, 8, 1)$
 287 : $P_{10002} = (17, 23, 8, 1)$
 288 : $P_{10009} = (24, 23, 8, 1)$
 289 : $P_{10022} = (5, 24, 8, 1)$
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 694 : $P_{23839} = (30, 7, 22, 1)$
 695 : $P_{23863} = (22, 8, 22, 1)$
 696 : $P_{23864} = (23, 8, 22, 1)$
 697 : $P_{23883} = (10, 9, 22, 1)$
 698 : $P_{23902} = (29, 9, 22, 1)$
 699 : $P_{24102} = (5, 16, 22, 1)$
 700 : $P_{24104} = (7, 16, 22, 1)$
 701 : $P_{24140} = (11, 17, 22, 1)$
 702 : $P_{24160} = (31, 17, 22, 1)$
 703 : $P_{24201} = (8, 19, 22, 1)$
 704 : $P_{24214} = (21, 19, 22, 1)$
 705 : $P_{24274} = (17, 21, 22, 1)$
 706 : $P_{24280} = (23, 21, 22, 1)$
 707 : $P_{24314} = (25, 22, 22, 1)$
 708 : $P_{24335} = (14, 23, 22, 1)$
 709 : $P_{24398} = (13, 25, 22, 1)$
 710 : $P_{24409} = (24, 25, 22, 1)$
 711 : $P_{24494} = (13, 28, 22, 1)$
 712 : $P_{24509} = (28, 28, 22, 1)$
 713 : $P_{24529} = (16, 29, 22, 1)$
 714 : $P_{24536} = (23, 29, 22, 1)$
 715 : $P_{24622} = (13, 0, 23, 1)$
 716 : $P_{24652} = (11, 1, 23, 1)$
 717 : $P_{24669} = (28, 1, 23, 1)$
 718 : $P_{24678} = (5, 2, 23, 1)$
 719 : $P_{24687} = (14, 2, 23, 1)$
 720 : $P_{24748} = (11, 4, 23, 1)$
 721 : $P_{24766} = (29, 4, 23, 1)$
 722 : $P_{24779} = (10, 5, 23, 1)$
 723 : $P_{24780} = (11, 5, 23, 1)$
 724 : $P_{24808} = (7, 6, 23, 1)$
 725 : $P_{24827} = (26, 6, 23, 1)$
 726 : $P_{24882} = (17, 8, 23, 1)$
 727 : $P_{24889} = (24, 8, 23, 1)$
 728 : $P_{24900} = (3, 9, 23, 1)$
 729 : $P_{24926} = (29, 9, 23, 1)$
 730 : $P_{24933} = (4, 10, 23, 1)$
 731 : $P_{24935} = (6, 10, 23, 1)$
 732 : $P_{24973} = (12, 11, 23, 1)$
 733 : $P_{24986} = (25, 11, 23, 1)$
 734 : $P_{25046} = (21, 13, 23, 1)$
 735 : $P_{25054} = (29, 13, 23, 1)$
 736 : $P_{25163} = (10, 17, 23, 1)$
 737 : $P_{25168} = (15, 17, 23, 1)$

738 : $P_{25220} = (3, 19, 23, 1)$	792 : $P_{26923} = (10, 8, 25, 1)$
739 : $P_{25230} = (13, 19, 23, 1)$	793 : $P_{26941} = (28, 8, 25, 1)$
740 : $P_{25259} = (10, 20, 23, 1)$	794 : $P_{27001} = (24, 10, 25, 1)$
741 : $P_{25263} = (14, 20, 23, 1)$	795 : $P_{27002} = (25, 10, 25, 1)$
742 : $P_{25327} = (14, 22, 23, 1)$	796 : $P_{27023} = (14, 11, 25, 1)$
743 : $P_{25369} = (24, 23, 23, 1)$	797 : $P_{27031} = (22, 11, 25, 1)$
744 : $P_{25432} = (23, 25, 23, 1)$	798 : $P_{27056} = (15, 12, 25, 1)$
745 : $P_{25436} = (27, 25, 23, 1)$	799 : $P_{27059} = (18, 12, 25, 1)$
746 : $P_{25444} = (3, 26, 23, 1)$	800 : $P_{27090} = (17, 13, 25, 1)$
747 : $P_{25460} = (19, 26, 23, 1)$	801 : $P_{27094} = (21, 13, 25, 1)$
748 : $P_{25587} = (18, 30, 23, 1)$	802 : $P_{27212} = (11, 17, 25, 1)$
749 : $P_{25589} = (20, 30, 23, 1)$	803 : $P_{27228} = (27, 17, 25, 1)$
750 : $P_{25610} = (9, 31, 23, 1)$	804 : $P_{27337} = (8, 21, 25, 1)$
751 : $P_{25625} = (24, 31, 23, 1)$	805 : $P_{27348} = (19, 21, 25, 1)$
752 : $P_{25660} = (27, 0, 24, 1)$	806 : $P_{27374} = (13, 22, 25, 1)$
753 : $P_{25680} = (15, 1, 24, 1)$	807 : $P_{27385} = (24, 22, 25, 1)$
754 : $P_{25688} = (23, 1, 24, 1)$	808 : $P_{27416} = (23, 23, 25, 1)$
755 : $P_{25734} = (5, 3, 24, 1)$	809 : $P_{27420} = (27, 23, 25, 1)$
756 : $P_{25737} = (8, 3, 24, 1)$	810 : $P_{27455} = (30, 24, 25, 1)$
757 : $P_{25778} = (17, 4, 24, 1)$	811 : $P_{27463} = (6, 25, 25, 1)$
758 : $P_{25791} = (30, 4, 24, 1)$	812 : $P_{27565} = (12, 28, 25, 1)$
759 : $P_{25827} = (2, 6, 24, 1)$	813 : $P_{27577} = (24, 28, 25, 1)$
760 : $P_{25849} = (24, 6, 24, 1)$	814 : $P_{27690} = (9, 0, 26, 1)$
761 : $P_{25894} = (5, 8, 24, 1)$	815 : $P_{27724} = (11, 1, 26, 1)$
762 : $P_{25916} = (27, 8, 24, 1)$	816 : $P_{27730} = (17, 1, 26, 1)$
763 : $P_{25960} = (7, 10, 24, 1)$	817 : $P_{27747} = (2, 2, 26, 1)$
764 : $P_{25965} = (12, 10, 24, 1)$	818 : $P_{27764} = (19, 2, 26, 1)$
765 : $P_{25990} = (5, 11, 24, 1)$	819 : $P_{27882} = (9, 6, 26, 1)$
766 : $P_{26007} = (22, 11, 24, 1)$	820 : $P_{27904} = (31, 6, 26, 1)$
767 : $P_{26031} = (14, 12, 24, 1)$	821 : $P_{27923} = (18, 7, 26, 1)$
768 : $P_{26048} = (31, 12, 24, 1)$	822 : $P_{27935} = (30, 7, 26, 1)$
769 : $P_{26097} = (16, 14, 24, 1)$	823 : $P_{27979} = (10, 9, 26, 1)$
770 : $P_{26101} = (20, 14, 24, 1)$	824 : $P_{27999} = (30, 9, 26, 1)$
771 : $P_{26119} = (6, 15, 24, 1)$	825 : $P_{28012} = (11, 10, 26, 1)$
772 : $P_{26139} = (26, 15, 24, 1)$	826 : $P_{28021} = (20, 10, 26, 1)$
773 : $P_{26160} = (15, 16, 24, 1)$	827 : $P_{28044} = (11, 11, 26, 1)$
774 : $P_{26167} = (22, 16, 24, 1)$	828 : $P_{28047} = (14, 11, 26, 1)$
775 : $P_{26191} = (14, 17, 24, 1)$	829 : $P_{28100} = (3, 13, 26, 1)$
776 : $P_{26192} = (15, 17, 24, 1)$	830 : $P_{28113} = (16, 13, 26, 1)$
777 : $P_{26216} = (7, 18, 24, 1)$	831 : $P_{28135} = (6, 14, 26, 1)$
778 : $P_{26220} = (11, 18, 24, 1)$	832 : $P_{28159} = (30, 14, 26, 1)$
779 : $P_{26250} = (9, 19, 24, 1)$	833 : $P_{28275} = (18, 18, 26, 1)$
780 : $P_{26270} = (29, 19, 24, 1)$	834 : $P_{28288} = (31, 18, 26, 1)$
781 : $P_{26276} = (3, 20, 24, 1)$	835 : $P_{28325} = (4, 20, 26, 1)$
782 : $P_{26294} = (21, 20, 24, 1)$	836 : $P_{28352} = (31, 20, 26, 1)$
783 : $P_{26408} = (7, 24, 24, 1)$	837 : $P_{28371} = (18, 21, 26, 1)$
784 : $P_{26463} = (30, 25, 24, 1)$	838 : $P_{28372} = (19, 21, 26, 1)$
785 : $P_{26519} = (22, 27, 24, 1)$	839 : $P_{28420} = (3, 23, 26, 1)$
786 : $P_{26525} = (28, 27, 24, 1)$	840 : $P_{28436} = (19, 23, 26, 1)$
787 : $P_{26575} = (14, 29, 24, 1)$	841 : $P_{28516} = (3, 26, 26, 1)$
788 : $P_{26591} = (30, 29, 24, 1)$	842 : $P_{28569} = (24, 27, 26, 1)$
789 : $P_{26678} = (21, 0, 25, 1)$	843 : $P_{28735} = (30, 0, 27, 1)$
790 : $P_{26856} = (7, 6, 25, 1)$	844 : $P_{28752} = (15, 1, 27, 1)$
791 : $P_{26876} = (27, 6, 25, 1)$	845 : $P_{28757} = (20, 1, 27, 1)$

846 : $P_{28806} = (5, 3, 27, 1)$	900 : $P_{30715} = (26, 30, 28, 1)$
847 : $P_{28814} = (13, 3, 27, 1)$	901 : $P_{30777} = (24, 0, 29, 1)$
848 : $P_{28909} = (12, 6, 27, 1)$	902 : $P_{30865} = (16, 3, 29, 1)$
849 : $P_{28925} = (28, 6, 27, 1)$	903 : $P_{30867} = (18, 3, 29, 1)$
850 : $P_{29063} = (6, 11, 27, 1)$	904 : $P_{30884} = (3, 4, 29, 1)$
851 : $P_{29065} = (8, 11, 27, 1)$	905 : $P_{30905} = (24, 4, 29, 1)$
852 : $P_{29116} = (27, 12, 27, 1)$	906 : $P_{30922} = (9, 5, 29, 1)$
853 : $P_{29119} = (30, 12, 27, 1)$	907 : $P_{30928} = (15, 5, 29, 1)$
854 : $P_{29383} = (6, 21, 27, 1)$	908 : $P_{30982} = (5, 7, 29, 1)$
855 : $P_{29395} = (18, 21, 27, 1)$	909 : $P_{31005} = (28, 7, 29, 1)$
856 : $P_{29495} = (22, 24, 27, 1)$	910 : $P_{31337} = (8, 18, 29, 1)$
857 : $P_{29501} = (28, 24, 27, 1)$	911 : $P_{31349} = (20, 18, 29, 1)$
858 : $P_{29561} = (24, 26, 27, 1)$	912 : $P_{31389} = (28, 19, 29, 1)$
859 : $P_{29571} = (2, 27, 27, 1)$	913 : $P_{31390} = (29, 19, 29, 1)$
860 : $P_{29604} = (3, 28, 27, 1)$	914 : $P_{31397} = (4, 20, 29, 1)$
861 : $P_{29611} = (10, 28, 27, 1)$	915 : $P_{31421} = (28, 20, 29, 1)$
862 : $P_{29671} = (6, 30, 27, 1)$	916 : $P_{31441} = (16, 21, 29, 1)$
863 : $P_{29693} = (28, 30, 27, 1)$	917 : $P_{31446} = (21, 21, 29, 1)$
864 : $P_{29745} = (16, 0, 28, 1)$	918 : $P_{31473} = (16, 22, 29, 1)$
865 : $P_{29770} = (9, 1, 28, 1)$	919 : $P_{31480} = (23, 22, 29, 1)$
866 : $P_{29782} = (21, 1, 28, 1)$	920 : $P_{31535} = (14, 24, 29, 1)$
867 : $P_{29802} = (9, 2, 28, 1)$	921 : $P_{31551} = (30, 24, 29, 1)$
868 : $P_{29813} = (20, 2, 28, 1)$	922 : $P_{31659} = (10, 28, 29, 1)$
869 : $P_{29833} = (8, 3, 28, 1)$	923 : $P_{31703} = (22, 29, 29, 1)$
870 : $P_{29834} = (9, 3, 28, 1)$	924 : $P_{31720} = (7, 30, 29, 1)$
871 : $P_{29897} = (8, 5, 28, 1)$	925 : $P_{31732} = (19, 30, 29, 1)$
872 : $P_{29900} = (11, 5, 28, 1)$	926 : $P_{31782} = (5, 0, 30, 1)$
873 : $P_{29929} = (8, 6, 28, 1)$	927 : $P_{31892} = (19, 3, 30, 1)$
874 : $P_{29931} = (10, 6, 28, 1)$	928 : $P_{31893} = (20, 3, 30, 1)$
875 : $P_{29987} = (2, 8, 28, 1)$	929 : $P_{31959} = (22, 5, 30, 1)$
876 : $P_{30010} = (25, 8, 28, 1)$	930 : $P_{31968} = (31, 5, 30, 1)$
877 : $P_{30034} = (17, 9, 28, 1)$	931 : $P_{32014} = (13, 7, 30, 1)$
878 : $P_{30039} = (22, 9, 28, 1)$	932 : $P_{32030} = (29, 7, 30, 1)$
879 : $P_{30139} = (26, 12, 28, 1)$	933 : $P_{32039} = (6, 8, 30, 1)$
880 : $P_{30143} = (30, 12, 28, 1)$	934 : $P_{32046} = (13, 8, 30, 1)$
881 : $P_{30183} = (6, 14, 28, 1)$	935 : $P_{32101} = (4, 10, 30, 1)$
882 : $P_{30208} = (31, 14, 28, 1)$	936 : $P_{32119} = (22, 10, 30, 1)$
883 : $P_{30227} = (18, 15, 28, 1)$	937 : $P_{32250} = (25, 14, 30, 1)$
884 : $P_{30232} = (23, 15, 28, 1)$	938 : $P_{32253} = (28, 14, 30, 1)$
885 : $P_{30248} = (7, 16, 28, 1)$	939 : $P_{32270} = (13, 15, 30, 1)$
886 : $P_{30261} = (20, 16, 28, 1)$	940 : $P_{32279} = (22, 15, 30, 1)$
887 : $P_{30325} = (20, 18, 28, 1)$	941 : $P_{32358} = (5, 18, 30, 1)$
888 : $P_{30331} = (26, 18, 28, 1)$	942 : $P_{32363} = (10, 18, 30, 1)$
889 : $P_{30342} = (5, 19, 28, 1)$	943 : $P_{32391} = (6, 19, 30, 1)$
890 : $P_{30360} = (23, 19, 28, 1)$	944 : $P_{32408} = (23, 19, 30, 1)$
891 : $P_{30446} = (13, 22, 28, 1)$	945 : $P_{32437} = (20, 20, 30, 1)$
892 : $P_{30461} = (28, 22, 28, 1)$	946 : $P_{32438} = (21, 20, 30, 1)$
893 : $P_{30541} = (12, 25, 28, 1)$	947 : $P_{32452} = (3, 21, 30, 1)$
894 : $P_{30553} = (24, 25, 28, 1)$	948 : $P_{32477} = (28, 21, 30, 1)$
895 : $P_{30596} = (3, 27, 28, 1)$	949 : $P_{32531} = (18, 23, 30, 1)$
896 : $P_{30603} = (10, 27, 28, 1)$	950 : $P_{32533} = (20, 23, 30, 1)$
897 : $P_{30648} = (23, 28, 28, 1)$	951 : $P_{32647} = (6, 27, 30, 1)$
898 : $P_{30667} = (10, 29, 28, 1)$	952 : $P_{32669} = (28, 27, 30, 1)$
899 : $P_{30705} = (16, 30, 28, 1)$	953 : $P_{32689} = (16, 28, 30, 1)$

954 : $P_{32699} = (26, 28, 30, 1)$
 955 : $P_{32712} = (7, 29, 30, 1)$
 956 : $P_{32724} = (19, 29, 30, 1)$
 957 : $P_{32756} = (19, 30, 30, 1)$
 958 : $P_{32781} = (12, 31, 30, 1)$
 959 : $P_{32821} = (20, 0, 31, 1)$
 960 : $P_{32839} = (6, 1, 31, 1)$
 961 : $P_{32858} = (25, 1, 31, 1)$
 962 : $P_{32943} = (14, 4, 31, 1)$
 963 : $P_{32958} = (29, 4, 31, 1)$
 964 : $P_{32980} = (19, 5, 31, 1)$
 965 : $P_{32992} = (31, 5, 31, 1)$
 966 : $P_{33028} = (3, 7, 31, 1)$
 967 : $P_{33045} = (20, 7, 31, 1)$
 968 : $P_{33092} = (3, 9, 31, 1)$
 969 : $P_{33120} = (31, 9, 31, 1)$
 970 : $P_{33164} = (11, 11, 31, 1)$
 971 : $P_{33165} = (12, 11, 31, 1)$
 972 : $P_{33200} = (15, 12, 31, 1)$
 973 : $P_{33216} = (31, 12, 31, 1)$

974 : $P_{33252} = (3, 14, 31, 1)$
 975 : $P_{33257} = (8, 14, 31, 1)$
 976 : $P_{33283} = (2, 15, 31, 1)$
 977 : $P_{33303} = (22, 15, 31, 1)$
 978 : $P_{33355} = (10, 17, 31, 1)$
 979 : $P_{33364} = (19, 17, 31, 1)$
 980 : $P_{33381} = (4, 18, 31, 1)$
 981 : $P_{33402} = (25, 18, 31, 1)$
 982 : $P_{33434} = (25, 19, 31, 1)$
 983 : $P_{33436} = (27, 19, 31, 1)$
 984 : $P_{33447} = (6, 20, 31, 1)$
 985 : $P_{33460} = (19, 20, 31, 1)$
 986 : $P_{33479} = (6, 21, 31, 1)$
 987 : $P_{33485} = (12, 21, 31, 1)$
 988 : $P_{33546} = (9, 23, 31, 1)$
 989 : $P_{33561} = (24, 23, 31, 1)$
 990 : $P_{33773} = (12, 30, 31, 1)$
 991 : $P_{33811} = (18, 31, 31, 1)$

Line Intersection Graph

	0 1
0	0 1
1	1 0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1
in point	P_{67}

Line 1 intersects

Line	ℓ_0
in point	P_{67}

The surface has 1057 points:

Too many to print.