

Rank-65735 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_2^3 + X_0^2 X_3 + X_0 X_1^2 + X_0 X_1 X_2 = 0$$

(0, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is -2112845787

General information

Number of lines	1
Number of points	1057
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	33
Number of points off lines	1024
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33
Type of lines on points	$1^{33}, 0^{1024}$

Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082400} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082400} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)_{65}$$

Rank of lines: (1082400)
Rank of points on Klein quadric: (65)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:
The double points on the surface are:

Single Points

The surface has 33 single points:
The single points on the surface are:

- | | |
|---|---|
| 0 : $P_1 = (0, 1, 0, 0)$ lies on line ℓ_0 | 17 : $P_{1570} = (0, 16, 0, 1)$ lies on line ℓ_0 |
| 1 : $P_3 = (0, 0, 0, 1)$ lies on line ℓ_0 | 18 : $P_{1602} = (0, 17, 0, 1)$ lies on line ℓ_0 |
| 2 : $P_{1090} = (0, 1, 0, 1)$ lies on line ℓ_0 | 19 : $P_{1634} = (0, 18, 0, 1)$ lies on line ℓ_0 |
| 3 : $P_{1122} = (0, 2, 0, 1)$ lies on line ℓ_0 | 20 : $P_{1666} = (0, 19, 0, 1)$ lies on line ℓ_0 |
| 4 : $P_{1154} = (0, 3, 0, 1)$ lies on line ℓ_0 | 21 : $P_{1698} = (0, 20, 0, 1)$ lies on line ℓ_0 |
| 5 : $P_{1186} = (0, 4, 0, 1)$ lies on line ℓ_0 | 22 : $P_{1730} = (0, 21, 0, 1)$ lies on line ℓ_0 |
| 6 : $P_{1218} = (0, 5, 0, 1)$ lies on line ℓ_0 | 23 : $P_{1762} = (0, 22, 0, 1)$ lies on line ℓ_0 |
| 7 : $P_{1250} = (0, 6, 0, 1)$ lies on line ℓ_0 | 24 : $P_{1794} = (0, 23, 0, 1)$ lies on line ℓ_0 |
| 8 : $P_{1282} = (0, 7, 0, 1)$ lies on line ℓ_0 | 25 : $P_{1826} = (0, 24, 0, 1)$ lies on line ℓ_0 |
| 9 : $P_{1314} = (0, 8, 0, 1)$ lies on line ℓ_0 | 26 : $P_{1858} = (0, 25, 0, 1)$ lies on line ℓ_0 |
| 10 : $P_{1346} = (0, 9, 0, 1)$ lies on line ℓ_0 | 27 : $P_{1890} = (0, 26, 0, 1)$ lies on line ℓ_0 |
| 11 : $P_{1378} = (0, 10, 0, 1)$ lies on line ℓ_0 | 28 : $P_{1922} = (0, 27, 0, 1)$ lies on line ℓ_0 |
| 12 : $P_{1410} = (0, 11, 0, 1)$ lies on line ℓ_0 | 29 : $P_{1954} = (0, 28, 0, 1)$ lies on line ℓ_0 |
| 13 : $P_{1442} = (0, 12, 0, 1)$ lies on line ℓ_0 | 30 : $P_{1986} = (0, 29, 0, 1)$ lies on line ℓ_0 |
| 14 : $P_{1474} = (0, 13, 0, 1)$ lies on line ℓ_0 | 31 : $P_{2018} = (0, 30, 0, 1)$ lies on line ℓ_0 |
| 15 : $P_{1506} = (0, 14, 0, 1)$ lies on line ℓ_0 | 32 : $P_{2050} = (0, 31, 0, 1)$ lies on line ℓ_0 |
| 16 : $P_{1538} = (0, 15, 0, 1)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 1024 points not on any line:
Too many to print.

Line Intersection Graph

$$\begin{array}{c|c} & 0 \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:
Line 0 intersects

Line
in point

The surface has 1057 points:
Too many to print.