# Rank-74295 over GF(2)

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## The equation

The equation of the surface is:

$$X_2^3 + X_0^2 X_1 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(0, 0, 1, 0, 1, 1, 0, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 0)The point rank of the equation over GF(2) is 74295

## General information

Number of lines	2
Number of points	7
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	6
Number of points off lines	1
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$3^{2}$
Type of lines on points	$1^6, 0$

## Singular Points

The surface has 1 singular points:

0: 
$$P_6 = \mathbf{P}(1,0,1,0) = \mathbf{P}(1,0,1,0)$$

## The 2 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_7 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_7 = \mathbf{Pl}(1, 0, 0, 0, 0, 1)_{20}$$

$$\ell_1 = \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{array}\right]_3 = \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{array}\right]_3 = \mathbf{Pl}(1,0,1,0,1,0)_{13}$$

Rank of lines: (7, 3)

Rank of points on Klein quadric: (20, 13)

#### **Eckardt Points**

The surface has 0 Eckardt points:

#### **Double Points**

The surface has 0 Double points:

The double points on the surface are:

## Single Points

The surface has 6 single points:

The single points on the surface are:

$$0: P_0 = (1, 0, 0, 0)$$
 lies on line  $\ell_1$ 

1: 
$$P_1 = (0, 1, 0, 0)$$
 lies on line  $\ell_0$ 

$$2: P_4 = (1, 1, 1, 1)$$
 lies on line  $\ell_1$ 

$$3: P_6 = (1,0,1,0)$$
 lies on line  $\ell_0$ 

The single points on the surface are:

 $4: P_8 = (1, 1, 1, 0)$  lies on line  $\ell_0$ 

5:  $P_{14} = (0, 1, 1, 1)$  lies on line  $\ell_1$ 

# Points on surface but on no line

The surface has 1 points not on any line:

The points on the surface but not on lines are:

$$0: P_3 = (0, 0, 0, 1)$$

## Line Intersection Graph

 $\begin{array}{c|c} 0 \ 1 \\ \hline 0 \ 0 \ 0 \\ 1 \ 0 \ 0 \end{array}$ 

Neighbor sets in the line intersection graph:

Line 0 intersects

Line in point

Line 1 intersects

Line in point

The surface has 7 points:

The points on the surface are:

 $\begin{array}{lll} 0: \, P_0 = (1,0,0,0) & 3: \, P_4 = (1,1,1,1) \\ 1: \, P_1 = (0,1,0,0) & 4: \, P_6 = (1,0,1,0) \\ 2: \, P_3 = (0,0,0,1) & 5: \, P_8 = (1,1,1,0) \end{array}$