Rank-65540 over GF(8)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_0 X_1 X_2 = 0$$

General information

Number of lines	80
Number of points	129
Number of singular points	17
Number of Eckardt points	0
Number of double points	0
Number of single points	56
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	980
Type of lines on points	$16, 9^{72}, 1^{56}$

Singular Points

The surface has 17 singular points:

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\begin{array}{lll} 0: \ P_1 = \mathbf{P}(0,1,0,0) = \mathbf{P}(0,1,0,0) & 9: \ P_{130} = \mathbf{P}(0,\gamma^4,0,1) = \mathbf{P}(0,7,0,1) \\ 1: \ P_2 = \mathbf{P}(0,0,1,0) = \mathbf{P}(0,0,1,0) & 10: \ P_{138} = \mathbf{P}(0,0,1,1) = \mathbf{P}(0,0,1,1) \\ 2: \ P_3 = \mathbf{P}(0,0,0,1) = \mathbf{P}(0,0,0,1) & 11: \ P_{201} = \mathbf{P}(0,0,\gamma,1) = \mathbf{P}(0,0,2,1) \\ 3: \ P_{82} = \mathbf{P}(0,1,0,1) = \mathbf{P}(0,1,0,1) & 12: \ P_{265} = \mathbf{P}(0,0,\gamma^5,1) = \mathbf{P}(0,0,3,1) \\ 4: \ P_{90} = \mathbf{P}(0,\gamma,0,1) = \mathbf{P}(0,2,0,1) & 13: \ P_{329} = \mathbf{P}(0,0,\gamma^2,1) = \mathbf{P}(0,0,4,1) \\ 5: \ P_{98} = \mathbf{P}(0,\gamma^5,0,1) = \mathbf{P}(0,3,0,1) & 14: \ P_{393} = \mathbf{P}(0,0,\gamma^3,1) = \mathbf{P}(0,0,5,1) \\ 6: \ P_{106} = \mathbf{P}(0,\gamma^2,0,1) = \mathbf{P}(0,4,0,1) & 15: \ P_{457} = \mathbf{P}(0,0,\gamma^6,1) = \mathbf{P}(0,0,6,1) \\ 7: \ P_{114} = \mathbf{P}(0,\gamma^6,0,1) = \mathbf{P}(0,5,0,1) & 16: \ P_{521} = \mathbf{P}(0,0,\gamma^4,1) = \mathbf{P}(0,0,7,1) \end{array}
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The 80 Lines

The lines and their Pluecker coordinates are:

$$\begin{split} \ell_0 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4672} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4672} = \mathbf{PI}(0,0,0,0,0,1)_{649} \\ \ell_1 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4680} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4680} = \mathbf{PI}(0,0,0,1,0,0)_{17} \\ \ell_2 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4673} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4673} = \mathbf{PI}(0,0,0,1,0,1)_{769} \\ \ell_3 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \gamma^6 \end{bmatrix}_{4678} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4673} = \mathbf{PI}(0,0,0,6,0,1)_{844} \\ \ell_4 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \gamma^2 \end{bmatrix}_{4676} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4676} = \mathbf{PI}(0,0,0,4,0,1)_{814} \\ \ell_5 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4675} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4675} = \mathbf{PI}(0,0,0,3,0,1)_{799} \\ \ell_6 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \gamma^4 \end{bmatrix}_{4679} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{4679} = \mathbf{PI}(0,0,0,7,0,1)_{859} \\ \ell_7 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4677} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{4674} = \mathbf{PI}(0,0,0,5,0,1)_{829} \\ \ell_9 &= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4677} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4677} = \mathbf{PI}(0,0,0,5,0,1)_{829} \\ \ell_{10} &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4681} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4744} = \mathbf{PI}(0,1,0,0,0,1)_{657} \\ \ell_{11} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4681} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4744} = \mathbf{PI}(0,1,0,0,0,1)_{657} \\ \ell_{12} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4699} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4798} = \mathbf{PI}(0,4,0,0,0,1)_{660} \\ \ell_{13} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4735} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4735} = \mathbf{PI}(0,7,0,0,0,1)_{658} \\ \ell_{14} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4735} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4735} = \mathbf{PI}(0,5,0,0,0,1)_{661} \\ \ell_{17} &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4689} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4735} = \mathbf{PI}(0,1,0,1,0,1)_{777} \\ \ell_{19} &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4682} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4689} = \mathbf{PI}(0,5,0,0,0,1)_{661} \\ \ell_{17} &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4689} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 &$$

$$\begin{split} &\ell_{20} = \begin{bmatrix} 0 & 1 & 0 & \gamma^2 \\ 0 & 0 & 1 & \gamma^2 \end{bmatrix}_{4712} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4712} = \mathbf{PI}(0,4,0,4,0,1)_{825} \\ &\ell_{21} = \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4702} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4702} = \mathbf{PI}(0,3,0,3,0,1)_{809} \\ &\ell_{22} = \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & \gamma^4 \end{bmatrix}_{4422} = \begin{bmatrix} 0 & 1 & 0 & 7 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{4742} = \mathbf{PI}(0,7,0,7,0,1)_{873} \\ &\ell_{23} = \begin{bmatrix} 0 & 1 & 0 & \gamma \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4722} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4722} = \mathbf{PI}(0,5,0,5,0,1)_{841} \\ &\ell_{24} = \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4722} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4722} = \mathbf{PI}(0,1,0,1,1,0)_{209} \\ &\ell_{26} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{729} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{729} = \mathbf{PI}(0,1,0,1,1,0)_{209} \\ &\ell_{26} = \begin{bmatrix} 0 & 1 & \gamma^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4734} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4734} = \mathbf{PI}(0,6,0,1,0,0)_{30} \\ &\ell_{27} = \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4722} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4727} = \mathbf{PI}(0,6,0,1,0,1)_{792} \\ &\ell_{28} = \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4733} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4727} = \mathbf{PI}(0,6,0,1,0,1)_{782} \\ &\ell_{29} = \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^6 \end{bmatrix}_{4705} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4738} = \mathbf{PI}(0,3,0,6,0,1)_{840} \\ &\ell_{31} = \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4684} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4738} = \mathbf{PI}(0,7,0,3,0,1)_{813} \\ &\ell_{32} = \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4684} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4694} = \mathbf{PI}(0,5,0,7,0,1)_{813} \\ &\ell_{33} = \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4684} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4738} = \mathbf{PI}(0,5,0,7,0,1)_{823} \\ &\ell_{34} = \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4684} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4738} = \mathbf{PI}(0,5,0,7,0,1)_{823} \\ &\ell_{35} = \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4684} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4736} = \mathbf{PI}(0,4,0,1,0,0)_{28} \\ &\ell_{35} = \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4736} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4736} = \mathbf{PI}(0,4,0,1,0,1)_{780} \\ &\ell_{37} = \begin{bmatrix} 0 & 1 & 0$$

$$\begin{split} \ell_{41} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^6 \end{bmatrix}_{4696} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{4696} = \mathbf{PI}(0,2,0,6,0,1)_{853} \\ \ell_{42} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma \end{bmatrix}_{4719} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{4719} = \mathbf{PI}(0,5,0,2,0,1)_{796} \\ \ell_{43} &= \begin{bmatrix} 1 & \gamma^6 & \gamma & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1678} = \begin{bmatrix} 1 & 6 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1678} = \mathbf{PI}(0,2,0,6,1,0)_{285} \\ \ell_{44} &= \begin{bmatrix} 0 & 1 & \gamma^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4707} = \begin{bmatrix} 0 & 1 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4707} = \mathbf{PI}(0,3,0,1,0,0)_{27} \\ \ell_{45} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & \gamma^2 \end{bmatrix}_{4685} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4685} = \mathbf{PI}(0,1,0,4,0,1)_{822} \\ \ell_{46} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma \end{bmatrix}_{4728} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{4728} = \mathbf{PI}(0,6,0,2,0,1)_{797} \\ \ell_{47} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^2 \\ 0 & 0 & 1 & \gamma^4 \end{bmatrix}_{4715} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{4705} = \mathbf{PI}(0,3,0,1,0,1)_{770} \\ \ell_{48} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & \gamma^4 \end{bmatrix}_{4715} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4700} = \mathbf{PI}(0,3,0,1,0,1)_{770} \\ \ell_{49} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & \gamma^6 \end{bmatrix}_{4741} = \begin{bmatrix} 0 & 1 & 0 & 7 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{4741} = \mathbf{PI}(0,7,0,6,0,1)_{858} \\ \ell_{50} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4695} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4695} = \mathbf{PI}(0,2,0,5,0,1)_{838} \\ \ell_{51} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4720} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4720} = \mathbf{PI}(0,6,0,2,1,0)_{229} \\ \ell_{53} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3722} = \begin{bmatrix} 1 & 2 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3722} = \mathbf{PI}(0,6,0,2,1,0)_{31} \\ \ell_{54} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^2 \end{bmatrix}_{4730} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4686} = \mathbf{PI}(0,1,0,5,0,1)_{837} \\ \ell_{56} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4711} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4711} = \mathbf{PI}(0,4,0,3,0,1)_{104} \\ \ell_{58} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4711} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4711} = \mathbf{PI}(0,4,0,3,0,1)_{104} \\ \ell_{58} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4711} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4711} = \mathbf{PI}(0,5,0,6,0,1)_{856} \\ \ell_{60} &= \begin{bmatrix} 0 & 1 & 0 &$$

$$\begin{split} \ell_{62} &= \begin{bmatrix} 0 & 1 & \gamma & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4698} = \begin{bmatrix} 0 & 1 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4698} = \mathbf{PI}(0,2,0,1,0,0)_{26} \\ \ell_{63} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & \gamma^6 \end{bmatrix}_{4687} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{4687} = \mathbf{PI}(0,1,0,6,0,1)_{852} \\ \ell_{64} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4729} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4729} = \mathbf{PI}(0,6,0,3,0,1)_{812} \\ \ell_{65} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^2 \\ 0 & 0 & 1 & \gamma \end{bmatrix}_{4710} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{4710} = \mathbf{PI}(0,4,0,2,0,1)_{795} \\ \ell_{66} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & \gamma^4 \end{bmatrix}_{4706} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{4706} = \mathbf{PI}(0,3,0,7,0,1)_{869} \\ \ell_{67} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4740} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4691} = \mathbf{PI}(0,7,0,5,0,1)_{843} \\ \ell_{69} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^2 \end{bmatrix}_{4721} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 4 \end{bmatrix}_{4725} = \mathbf{PI}(0,5,0,4,0,1)_{826} \\ \ell_{70} &= \begin{bmatrix} 1 & \gamma^3 & \gamma^4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4525} = \begin{bmatrix} 1 & 5 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4725} = \mathbf{PI}(0,7,0,5,1,0,0)_{29} \\ \ell_{72} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4731} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{4688} = \mathbf{PI}(0,1,0,7,0,1)_{867} \\ \ell_{73} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^3 \end{bmatrix}_{4731} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 5 \end{bmatrix}_{4731} = \mathbf{PI}(0,4,0,6,0,1)_{824} \\ \ell_{74} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^6 \\ 0 & 0 & 1 & \gamma^6 \end{bmatrix}_{4714} = \begin{bmatrix} 0 & 1 & 0 & 6 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{4714} = \mathbf{PI}(0,4,0,6,0,1)_{824} \\ \ell_{75} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^5 \\ 0 & 0 & 1 & \gamma^2 \end{bmatrix}_{4703} = \begin{bmatrix} 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{4703} = \mathbf{PI}(0,7,0,2,0,1)_{798} \\ \ell_{77} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^4 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4693} = \begin{bmatrix} 0 & 1 & 0 & 7 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{4737} = \mathbf{PI}(0,5,0,1,0,1)_{791} \\ \ell_{79} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4693} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{4737} = \mathbf{PI}(0,5,0,1,0,1)_{791} \\ \ell_{79} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4693} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4693} = \mathbf{PI}(0,5,0,1,0,1)_{793} \\ \ell_{78} &= \begin{bmatrix} 0 & 1 & 0 & \gamma^3 \\ 0 & 0 & 1 & \gamma^5 \end{bmatrix}_{4733} = \begin{bmatrix} 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{4693} = \mathbf{PI}(0,5,0,1,0,1)_{793} \\ \ell_{79} &= \begin{bmatrix} 0 & 1 &$$

Rank of lines: (4672, 4680, 4673, 4678, 4676, 4675, 4679, 4674, 4677, 4744, 4681, 4726, 4708, 4699, 4735, 4690, 4717, 4689, 4682, 4732, 4712, 4702, 4742, 4692, 4722, 729, 4734, 4683, 4727, 4713, 4705, 4738, 4694, 4724, 3503, 4716, 4684, 4733, 4709, 4704, 4739, 4696, 4719, 1678, 4707, 4685, 4728, 4715, 4700, 4741, ...4693, 4718, 2116)

Rank of points on Klein quadric: (649, 17, 769, 844, 814, 799, 859, 784, 829, 1, 657, 662, 660, 659, 663, 658, 661, 25, 777, 857, 825, 809, 873, 793, 841, 209, 30, 792, 782, 840, 854, 813, 823, 871, 303, 28, 807, 872, 780, 839, 828, 853, 796, 285, 27, 822, 797, 870, 779, 858, ...808, 781, 256)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 56 single points: The single points on the surface are:

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0: P_4 = (1, 1, 1, 1) lies on line \ell_{25}
1: P_{20} = (1, 1, 1, 0) lies on line \ell_{25}
2: P_{34} = (7, 2, 1, 0) lies on line \ell_{34}
3: P_{41} = (6,3,1,0) lies on line \ell_{43}
4: P_{45} = (2, 4, 1, 0) lies on line \ell_{52}
5: P_{54} = (3, 5, 1, 0) lies on line \ell_{61}
6: P_{64} = (5, 6, 1, 0) lies on line \ell_{70}
7: P_{71} = (4, 7, 1, 0) lies on line \ell_{79}
8: P_{160} = (7, 2, 1, 1) lies on line \ell_{34}
9: P_{167} = (6, 3, 1, 1) lies on line \ell_{43}
10: P_{171} = (2, 4, 1, 1) lies on line \ell_{52}
11: P_{180} = (3, 5, 1, 1) lies on line \ell_{61}
12: P_{190} = (5, 6, 1, 1) lies on line \ell_{70}
13: P_{197} = (4,7,1,1) lies on line \ell_{79}
14: P_{216} = (7, 1, 2, 1) lies on line \ell_{70}
15: P_{219} = (2, 2, 2, 1) lies on line \ell_{25}
16: P_{230} = (5, 3, 2, 1) lies on line \ell_{79}
17: P_{236} = (3, 4, 2, 1) lies on line \ell_{34}
18: P_{245} = (4, 5, 2, 1) lies on line \ell_{52}
19: P_{250} = (1, 6, 2, 1) lies on line \ell_{43}
20: P_{263} = (6,7,2,1) lies on line \ell_{61}
21: P_{279} = (6, 1, 3, 1) lies on line \ell_{52}
22: P_{286} = (5, 2, 3, 1) lies on line \ell_{61}
23: P_{292} = (3, 3, 3, 1) lies on line \ell_{25}
24: P_{298} = (1, 4, 3, 1) lies on line \ell_{79}
25: P_{312} = (7, 5, 3, 1) lies on line \ell_{43}
26: P_{317} = (4, 6, 3, 1) lies on line \ell_{34}
27: P_{323} = (2,7,3,1) lies on line \ell_{70}
28: P_{339} = (2, 1, 4, 1) lies on line \ell_{43}
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The single points on the surface are:

Points on surface but on no line

The surface has 0 points not on any line: The points on the surface but not on lines are:

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29: P_{348} = (3, 2, 4, 1) lies on line \ell_{70}
30: P_{354} = (1, 3, 4, 1) lies on line \ell_{61}
31: P_{365} = (4, 4, 4, 1) lies on line \ell_{25}
32: P_{375} = (6, 5, 4, 1) lies on line \ell_{34}
33: P_{384} = (7, 6, 4, 1) lies on line \ell_{79}
34: P_{390} = (5,7,4,1) lies on line \ell_{52}
35: P_{404} = (3, 1, 5, 1) lies on line \ell_{79}
36: P_{413} = (4, 2, 5, 1) lies on line \ell_{43}
37: P_{424} = (7, 3, 5, 1) lies on line \ell_{52}
38: P_{431} = (6, 4, 5, 1) lies on line \ell_{70}
39: P_{438} = (5, 5, 5, 1) lies on line \ell_{25}
40: P_{443} = (2, 6, 5, 1) lies on line \ell_{61}
41: P_{450} = (1, 7, 5, 1) lies on line \ell_{34}
42: P_{470} = (5, 1, 6, 1) lies on line \ell_{34}
43: P_{474} = (1, 2, 6, 1) lies on line \ell_{52}
44: P_{485} = (4, 3, 6, 1) lies on line \ell_{70}
45: P_{496} = (7, 4, 6, 1) lies on line \ell_{61}
46: P_{499} = (2, 5, 6, 1) lies on line \ell_{79}
47: P_{511} = (6, 6, 6, 1) lies on line \ell_{25}
48: P_{516} = (3,7,6,1) lies on line \ell_{43}
49: P_{533} = (4, 1, 7, 1) lies on line \ell_{61}
50: P_{543} = (6, 2, 7, 1) lies on line \ell_{79}
51: P_{547} = (2, 3, 7, 1) lies on line \ell_{34}
52: P_{558} = (5, 4, 7, 1) lies on line \ell_{43}
53: P_{562} = (1, 5, 7, 1) lies on line \ell_{70}
54: P_{572} = (3, 6, 7, 1) lies on line \ell_{52}
55: P_{584} = (7,7,7,1) lies on line \ell_{25}
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Line Intersection Graph

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11	11	11	1 1	l 1	11	. 1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	0	1	1	1	1
12	11	11	11	l 1	11	. 1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	0	1	1	1	1
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24	11	11	11	l 1	11	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	0	1	1	1	1
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Neighbor sets in the line intersection graph:

т	:	Ω	intersects
н.	ıne	u	intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_1	P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_{19}	P_{19}	P_{19}	P_{19}	P_{19}	P_{1}							

Line 1 intersects

Lir	ie	ℓ_0	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ
in poir	nt	P_1	P_3	P_{82}	P_{90}	P_{98}	P_{106}	P_{114}	P_{122}	P_{130}	P_3	P_{82}	P_{90}	P_{98}	\overline{P}							

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
in point	P_1	P_{138}	P_{146}	P_{153}	P_{161}	P_{169}	P_{177}	P_{185}	P_{193}	P_{146}	P_{138}	P_{161}							

Line 3 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	
in point	P_1	P_{201}	P_{209}	P_{217}	P_{225}	P_{233}	P_{241}	P_{249}	P_{257}	P_{217}	P_{225}	P_{201}								

Line 4 intersects

ĺ	Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
	in point	P_1	P_{265}	P_{273}	P_{281}	P_{289}	P_{297}	P_{305}	P_{313}	P_{321}	P_{289}	P_{281}	P_{273}							

${\bf Line~5~intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
in point	P_1	P_{329}	P_{337}	P_{345}	P_{353}	P_{361}	P_{369}	P_{377}	P_{385}	P_{361}	P_{369}	P_{377}							

Line 6 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
in point	P_1	P_{393}	P_{401}	P_{409}	P_{417}	P_{425}	P_{433}	P_{441}	P_{449}	P_{433}	P_{425}	P_{449}							

Line 7 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
in point	P_1	P_{457}	P_{465}	P_{473}	P_{481}	P_{489}	P_{497}	P_{505}	P_{513}	P_{505}	P_{513}	P_{489}							

Line 8 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
in point	P_1	P_{521}	P_{529}	P_{537}	P_{545}	P_{553}	P_{561}	P_{569}	P_{577}	P_{577}	P_{569}	P_{561}							

Line 9 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	
in point	P_2	P_3	P_{138}	P_{201}	P_{265}	P_{329}	P_{393}	P_{457}	P_{521}	P_2	P_3	P_{138}	P_{201}							

${\rm Line}\ 10\ {\rm intersects}$

ĺ	$_{ m Line}$	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
Ī	in point	P_2	P_{82}	P_{146}	P_{209}	P_{273}	P_{337}	P_{401}	P_{465}	P_{529}	P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_{146}	P_{82}	P_{273}

Line 11 intersects

$\operatorname{Lin}\epsilon$	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}
in point	P_2	P_{90}	P_{153}	P_{217}	P_{281}	P_{345}	P_{409}	P_{473}	P_{537}	P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_{217}	P_{281}	P_{90}

Line 12 int	tersec	ets																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	$ \ell$	219
in point	P_2	P_{98}		P_{225}			P_{417}	P_{481}			P_2	P_2	P_2	P_2	P_2	P_2	P_{289}	P_{225}	$\frac{1}{5}$	161
Line 13 int	tersec																	1		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	.8 /	ℓ_{19}
in point	P_2	P_{106}	P_{169}	P_{233}	P_{297}	P_{361}	P_{425}	P_{489}		P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_{361}			P_{489}
Line 14 int	i ersec	:ts																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	.8	ℓ_{19}
in point	P_2	P_{114}	P_{177}	P_{241}	P_{305}	P_{369}	P_{433}	P_{497}	P_{561}	P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_{433}	P_{36}	₆₉ F	P_{561}
Line 15 int	- iersec	-:ts	_	_	_	_	_	_	_	_	_			_			_	_	_	
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}		ℓ_{14}			ℓ_{18}	.8/	ℓ_{19}
in point	P_2	P_{122}	P_{185}	P_{249}	P_{313}	P_{377}	P_{441}	P_{505}	P_{569}	P_2	P_2	P_2	P_2	P_2	P_2	P_2		P_{56}		P_{377}
Line 16 int			_		_															
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}			ℓ_{15}				ℓ_{19}
in point	P_2	P_{130}	P_{193}	P_{257}	P_{321}	P_{385}	P_{449}	P_{513}	P_{577}	P_2	P_2	P_2	P_2	P_2	P_2	P_2	P_{577}			P_{449}
Line 17 int																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}		ℓ_{12}	ℓ_{13}	ℓ_{14}		5 l	216	ℓ_{18}
in point	P_{19}	P_3	P_{146}	P_{217}	P_{289}	P_{361}	P_{433}	P_{505}	P_{577}	P_3	P_{146}	P_{21}	$\overline{}_{17} \mid P$	289	P_{361}	P_{433}	P_{50}	P_{5}	577	P_{19}
Line 18 int																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9		10 \(\ell \)	ℓ_{11}	ℓ_{12}	ℓ_{13}			ℓ_{15}	ℓ_{16}	ℓ
in point	P_{19}	P_{82}	P_{138}	P_{225}	P_{281}	P_{369}	P_{425}	P_{513}	P_{569}	P_{138}	$8 \mid P$	$P_{82} \mid P$	P ₂₈₁	P_{225}	P_{425}	P_3	$_{369} \mid P$	569	P_{513}	$\mid P$
Line 19 int																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9			ℓ_{11}	ℓ_{12}	ℓ_{13}				ℓ_{16}	ℓ
in point	P_{19}	P_{90}	P_{161}	P_{201}	P_{273}	P_{377}	P_{449}	P_{489}	P_{561}	P_{201}	$1 \mid P$	P_{273}	P_{90}	P_{161}	P_{489}	P_5	$_{61} \mid P$	377	P_{449}	P
Line 20 int					<u>. </u>		· · · ·													
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9			ℓ_{11}	ℓ_{12}				ℓ_{15}	ℓ_{16}	1
in point	P_{19}	P_{98}	P_{153}	P_{209}	P_{265}	P_{385}	P_{441}	P_{497}	P_{553}	P_{265}	$5 \mid P$	209	P_{153}	P_{98}	P_{553}	$3 \mid P_4$	$P_{497} \mid P$	9441	P_{385}	P
Line 21 int																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9		ℓ_{10}	ℓ_{11}	ℓ_{12}			ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{19}	P_{106}	P_{177}	P_{249}	P_{321}	P_{329}	P_{401}	P_{473}	$_{3} \mid P_{545}$	P_{32}	29 <i>I</i>	P_{401}	P_{473}	P_{54}	$_{15} \mid P$	106	P_{177}	P_{249}	P_{32}	21
Line 22 int																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9		ℓ_{10}	ℓ_{11}	ℓ_{12}			ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{19}	P_{114}	P_{169}	P_{257}	P_{313}	P_{337}	P_{393}	P_{481}	P_{537}	P_{39}	$93 \mid I$	P_{337}	P_{537}	P_{48}	P	169	P_{114}	P_{313}	P_{25}	57

in point $ P_{19} P_{130} P_{185} P_{241} P_{297} P_{353} P_{409} P_{465} P_{521} P_{521} P_{465} P_{409} P_{353} P_{297} P_{241} P_{185} P_{130} P_{185} P_{130} P_{185} P_{18$	Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
	in point	P_{19}	P_{130}	P_{185}	P_{241}		P_{353}	P_{409}		P_{521}	P_{521}			P_{353}	1 1)	I /)	P_{185}	

 ℓ_7

 P_{457}

 ℓ_8

 P_{529}

 ℓ_9

 P_{457}

 ℓ_{10}

 P_{529}

 ℓ_{11}

 P_{345}

 ℓ_{12}

 P_{417}

 ℓ_{13}

 P_{233}

 ℓ_{14}

 P_{305}

 ℓ_{15}

 ℓ_{16}

 ℓ_6

 P_{417}

 ℓ_4

 ℓ_3

 P_{193} P_{233}

 ℓ_5

 P_{305} P_{345}

 ${\bf Line~23~intersects}$

in point P_{19}

 ${\bf Line~24~intersects}$

 ℓ_1

 P_{122}

 ℓ_2

Line 25 intersects

Line	ℓ_1	ℓ_9	ℓ_{17}	ℓ_{26}	ℓ_{34}	ℓ_{35}	ℓ_{43}	ℓ_{44}	ℓ_{52}	ℓ_{53}	ℓ_{61}	ℓ_{62}	ℓ_{70}	ℓ_{71}	ℓ_{79}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 26 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}
in point	P_{27}	P_3	P_{153}	P_{233}	P_{313}	P_{369}	P_{449}	P_{465}	P_{545}	P_3	P_{465}	P_{153}	P_{545}	P_{233}	P_{369}	P_{313}	P_{449}	P_3

${\rm Line}\ 27\ {\rm intersects}$

_																			
	Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
	in point	P_{27}	P_{82}	P_{161}	P_{241}	P_{321}	P_{361}	P_{441}	P_{457}	P_{537}	P_{457}	P_{82}	P_{537}	P_{161}	P_{361}	P_{241}	P_{441}	P_{321}	P

${\rm Line}\ 28\ {\rm intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in point	P_{27}	P_{90}	P_{138}	P_{249}	P_{297}	P_{385}	P_{433}	P_{481}	P_{529}	P_{138}	P_{529}	P_{90}	P_{481}	P_{297}	P_{433}	P_{249}	P_{385}	P

Line 29 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in point	P_{27}	P_{98}	P_{146}	P_{257}	P_{305}	P_{377}	P_{425}	P_{473}	P_{521}	P_{521}	P_{146}	P_{473}	P_{98}	P_{425}	P_{305}	P_{377}	P_{257}	P

Line 30 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{27}	P_{106}	P_{185}	P_{201}	P_{281}	P_{337}	P_{417}	P_{497}	P_{577}	P_{201}	P_{337}	P_{281}	P_{417}	P_{106}	P_{497}	P_{185}	P_{577}

Line 31 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{27}	P_{114}	P_{193}	P_{209}	P_{289}	P_{329}	P_{409}	P_{489}	P_{569}	P_{329}	P_{209}	P_{409}	P_{289}	P_{489}	P_{114}	P_{569}	P_{193}

${\rm Line}~32~{\rm intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{27}	P_{122}	P_{169}	P_{217}	P_{265}	P_{353}	P_{401}	P_{513}	P_{561}	P_{265}	P_{401}	P_{217}	P_{353}	P_{169}	P_{561}	P_{122}	P_{513}

Line 33 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{27}	P_{130}	P_{177}	P_{225}	P_{273}	P_{345}	P_{393}	P_{505}	P_{553}	P_{393}	P_{273}	P_{345}	P_{225}	P_{553}	P_{177}	P_{505}	P_{130}

Line 34 intersects

Line	ℓ_1	ℓ_9	ℓ_{17}	ℓ_{25}	ℓ_{26}	ℓ_{35}	ℓ_{43}	ℓ_{44}	ℓ_{52}	ℓ_{53}	ℓ_{61}	ℓ_{62}	ℓ_{70}	ℓ_{71}	ℓ_{79}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

${\bf Line~35~intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}
in point	P_{35}	P_3	P_{161}	P_{249}	P_{305}	P_{337}	P_{409}	P_{513}	P_{553}	P_3	P_{337}	P_{409}	P_{161}	P_{553}	P_{305}	P_{249}	P_{513}	P_3

Line 36 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	- (
in point	P_{35}	P_{82}	P_{153}	P_{257}	P_{297}	P_{329}	P_{417}	P_{505}	P_{561}	P_{329}	P_{82}	P_{153}	P_{417}	P_{297}	P_{561}	P_{505}	P_{257}	F

${\bf Line~37~intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in point	P_{35}	P_{90}	P_{146}	P_{233}	P_{321}	P_{353}	P_{393}	P_{497}	P_{569}	P_{393}	P_{146}	P_{90}	P_{353}	P_{233}	P_{497}	P_{569}	P_{321}	P

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	l
in point	P_{35}	P_{98}	P_{138}	P_{241}	P_{313}	P_{345}	P_{401}	P_{489}	P_{577}	P_{138}	P_{401}	P_{345}	P_{98}	P_{489}	P_{241}	P_{313}	P_{577}	P
Line 39 in	tersec	ts																
Line in point	ℓ_0 P_{35}	ℓ_1 P_{106}	ℓ_2 P_{193}	ℓ_3 P_{217}	ℓ_4 P_{273}	ℓ_5 P_{369}	ℓ_6 P_{441}	ℓ_7 P_{481}	ℓ_8 P_{521}	ℓ_9 P_{521}	ℓ_{10} P_{273}	ℓ_{11} P_{217}	ℓ_{12} P_{481}	$\ell_{13} = \ell_{106}$	$\ell_{14} = P_{369}$	ℓ_{15} P_{441}	ℓ_{16} P_{19}	
Line 40 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2 P_{185}	ℓ_3	ℓ_4	ℓ_5 P_{361}	ℓ_6 P_{449}	ℓ_7 P_{473}	ℓ_8 P_{529}	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point Line 41 in	P_{35}	P_{114}	F ₁₈₅	P_{225}	P_{265}	P ₃₆₁	P ₄₄₉	F ₄₇₃	F ₅₂₉	P_{265}	P_{529}	P_{473}	P_{225}	P_{361}	P ₁₁₄	P_{185}	P_{449})
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	\dashv
in point	P_{35}	P_{122}	P_{177}	P_{201}	P_{289}	P_{385}	P_{425}	P_{465}	P_{537}	P_{201}	P_{465}	P_{537}	P_{289}	P_{425}		P_{122}		
Line 42 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{35}	P_{130}	P_{169}	P_{209}	P_{281}	P_{377}	P_{433}	P_{457}	P_{545}	P_{457}	P_{209}	P_{281}	P_{545}	P_{169}	P_{433}	P_{377}	P_{130})
Line 43 in	tersec	ts																
	Li	ne ℓ	$1 \ell_9$	ℓ_{17}	ℓ_{25} ℓ	ℓ_{26} ℓ_{34}	ℓ_{35}	ℓ_{44}	$\ell_{52} \mid \ell_{5}$	ℓ_{63} ℓ_{61}	ℓ_{62}	ℓ_{70}	ℓ_{71} ℓ_{7}	79				
	in po				P_3 I	P_3 P_3			P_3 P	P_3 P_3	P_3	P_3	P_3 P	23				
Line 44 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7		ℓ_9 ℓ_2						15		17
in point	P_{43}	P_3	P_{169} .	P_{241} .	P_{273}	P_{385}	P_{417}	P_{473}	P_{569} .	$P_3 \mid P_2$	$_{273} \mid P_{4}$	P_{2}	$_{117} \mid P$	$P_{169} \mid F$	$P_{241} \mid P$	2 ₅₆₉ I	385 -	P_3
Line 45 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ł
in point	P_{43}	P_{82}	P_{177}	P_{233}	P_{265}	P_{377}	P_{409}	P_{481}	P_{577}	P_{265}	P_{82}	P_{409}	P_{481}	P_{233}	P_{177}	P_{377}	P_{577}	F
Line 46 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in point	P_{43}	P_{90}	P_{185}	P_{257}	P_{289}	P_{369}	P_{401}	P_{457}	P_{553}	P_{457}	P_{401}	P_{90}	P_{289}	P_{553}	P_{369}	P_{185}	P_{257}	F
Line 47 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	l
in point	P_{43}	P_{98}	P_{193}	P_{249}	P_{281}	P_{361}	P_{393}	P_{465}	P_{561}	P_{393}	P_{465}	P_{281}	P_{98}	P_{361}	P_{561}	P_{249}	P_{193}	F
Line 48 in	tersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{43}	P_{106}	P_{138}	P_{209}	P_{305}	P_{353}	P_{449}	P_{505}	P_{537}	P_{138}	P_{209}	P_{537}	P_{353}	P_{106}	P_{305}	P_{505}	P_{449})
Line 49 in	tersec	ts																
	0	ℓ_1	0	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
Line	ℓ_0		ℓ_2															
Line in point	P_{43}	P_{114}	P_{146}	P_{201}	P_{297}	P_{345}	P_{441}	P_{513}	P_{545}	P_{201}	P_{146}	P_{345}	P_{545}	P_{297}		P_{441}		

 ℓ_6

 P_{433}

 ℓ_7 P_{489}

 ℓ_8 P_{521}

 ℓ_9

 P_{521}

 ℓ_{11} P_{153}

 ℓ_{12}

 P_{225}

 ℓ_{13}

 P_{489}

 ℓ_{10} P_{337}

 $\begin{array}{c|cc} \ell_{14} & \ell_{15} \\ \hline P_{433} & P_{122} \\ \end{array}$

 ℓ_{16}

 P_{321}

 ℓ_2 P_{153}

 P_{43} P_{122}

Line

in point

 $\begin{array}{|c|c|c|}\hline \ell_3 \\ P_{225} \end{array}$

 ℓ_4 P_{321}

 ℓ_5 P_{337}

Line 51 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{43}	P_{130}	P_{161}	P_{217}	P_{313}	P_{329}	P_{425}	P_{497}	P_{529}	P_{329}	P_{529}	P_{217}	P_{161}	P_{425}	P_{497}	P_{313}	P_{130}

Line 52 intersects

Line	ℓ_1	ℓ_9	ℓ_{17}	ℓ_{25}	ℓ_{26}	ℓ_{34}	ℓ_{35}	ℓ_{43}	ℓ_{44}	ℓ_{53}	ℓ_{61}	ℓ_{62}	ℓ_{70}	ℓ_{71}	ℓ_{79}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 53 intersects

$_{ m Line}$	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}
in point	P_{51}	P_3	P_{177}	P_{257}	P_{281}	P_{353}	P_{441}	P_{489}	P_{529}	P_3	P_{529}	P_{281}	P_{353}	P_{489}	P_{177}	P_{441}	P_{257}	P_3

${\bf Line~54~intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	_
in point	P_{51}	P_{82}	P_{169}	P_{249}	P_{289}	P_{345}	P_{449}	P_{497}	P_{521}	P_{521}	P_{82}	P_{345}	P_{289}	P_{169}	P_{497}	P_{249}	P_{449}	I

Line 55 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in point	P_{51}	P_{90}	P_{193}	P_{241}	P_{265}	P_{337}	P_{425}	P_{505}	P_{545}	P_{265}	P_{337}	P_{90}	P_{545}	P_{425}	P_{241}	P_{505}	P_{193}	\overline{P}

Line 56 intersects

L	ine	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in po	int	P_{51}	P_{98}	P_{185}	P_{233}	P_{273}	P_{329}	P_{433}	P_{513}	P_{537}	P_{329}	P_{273}	P_{537}	P_{98}	P_{233}	P_{433}	P_{185}	P_{513}	P

Line 57 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{51}	P_{106}	P_{146}	P_{225}	P_{313}	P_{385}	P_{409}	P_{457}	P_{561}	P_{457}	P_{146}	P_{409}	P_{225}	P_{106}	P_{561}	P_{313}	P_{385}

${\rm Line}~58~{\rm intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{51}	P_{114}	P_{138}	P_{217}	P_{321}	P_{377}	P_{417}	P_{465}	P_{553}	P_{138}	P_{465}	P_{217}	P_{417}	P_{553}	P_{114}	P_{377}	P_{321}

Line 59 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{51}	P_{122}	P_{161}	P_{209}	P_{297}	P_{369}	P_{393}	P_{473}	P_{577}	P_{393}	P_{209}	P_{473}	P_{161}	P_{297}	P_{369}	P_{122}	P_{577}

Line 60 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{51}	P_{130}	P_{153}	P_{201}	P_{305}	P_{361}	P_{401}	P_{481}	P_{569}	P_{201}	P_{401}	P_{153}	P_{481}	P_{361}	P_{305}	P_{569}	P_{130}

Line 61 intersects

Line	ℓ_1	ℓ_9	ℓ_{17}	ℓ_{25}	ℓ_{26}	ℓ_{34}	ℓ_{35}	ℓ_{43}	ℓ_{44}	ℓ_{52}	ℓ_{53}	ℓ_{62}	ℓ_{70}	ℓ_{71}	ℓ_{79}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 62 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}
in point	P_{59}	P_3	P_{185}	P_{209}	P_{321}	P_{345}	P_{425}	P_{481}	P_{561}	P_3	P_{209}	P_{345}	P_{481}	P_{425}	P_{561}	P_{185}	P_{321}	P_3

${\rm Line}~63~{\rm intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ
in point	P_{59}	P_{82}	P_{193}	P_{201}	P_{313}	P_{353}	P_{433}	P_{473}	P_{553}	P_{201}	P_{82}	P_{473}	P_{353}	P_{553}	P_{433}	P_{313}	P_{193}	F

Line 64 int	ersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{59}	P_{90}	P_{169}	P_{225}	P_{305}	P_{329}	P_{441}	P_{465}	P_{577}	P_{329}	P_{465}	P_{90}	P_{225}	P_{169}	P_{305}	P_{441}	P_{577}	I
Line 65 int	ersect	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{59}	P_{98}	P_{177}	P_{217}	P_{297}	P_{337}	P_{449}	P_{457}	P_{569}	P_{457}	P_{337}	P_{217}	P_{98}	P_{297}	P_{177}	P_{569}	P_{449}	I
Line 66 int																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}				
in point	P_{59}	P_{106}	P_{153}	P_{241}	P_{289}	P_{377}	P_{393}	P_{513}	P_{529}	P_{393}	P_{529}	P_{153}	P_{289}	P_{100}	P_{24}	P_{37}	$_{7} \mid P_{51}$.3
Line 67 int																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}				
in point	P_{59}	P_{114}	P_{161}	P_{233}	P_{281}	P_{385}	P_{401}	P_{505}	P_{521}	P_{521}	P_{401}	P_{281}	P_{161}	P_{233}	$ P_{11} $	$_{4} \mid P_{50}$	$_{5} \mid P_{38}$	35
Line 68 int																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}				
in point	P_{59}	P_{122}	P_{138}	P_{257}	P_{273}	P_{361}	P_{409}	P_{497}	P_{545}	P_{138}	P_{273}	P_{409}	P_{545}	P_{363}	P_{49}	$_{7} \mid P_{12}$	$_2 \mid P_{25}$	57
Line 69 int																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}				
in point	P_{59}	P_{130}	P_{146}	P_{249}	P_{265}	P_{369}	P_{417}	P_{489}	P_{537}	P_{265}	P_{146}	P_{537}	P_{417}	P_{489}	P_{36}	P_{24}	$_{9} \mid P_{13}$	30
Line 70 int		ine ℓ	$\begin{array}{c cccc} P_1 & \ell_9 \\ \hline P_3 & P_3 \end{array}$	$egin{array}{ c c c c c c c c c c c c c c c c c c c$		$\begin{array}{c c} P_{26} & \ell_{34} \\ \hline P_{3} & P_{3} \end{array}$				$\begin{array}{c cccc} P_{52} & \ell_{53} \\ \hline P_{3} & P_{3} \end{array}$		ℓ_{62} P_3		79 D ₃				
Line 71 int	-		3 - 3	- 3	- 3 -	3 - 3	- 1 - 3	- 3	- 3 -	3 - 3	- 3	- 3	- 3 -	3				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9 ℓ	10 \ \ell \	11	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}
in point	P_{67}		P_{193}		P_{297}						2 ₄₀₁ P			297				P_3
Line 72 int	ersec	ts	,	•	•	,		•			•		•	•	·	•	•	
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	
in point	P_{67}	P_{82}	P_{185}	P_{217}	P_{305}	P_{385}	P_{393}	P_{489}	P_{545}	P_{393}		P_{217}	P_{545}	P_{489}	P_{305}	P_{185}	P_{385}	F
Line 73 int																		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	l
in point	P_{67}	P_{90}	P_{177}	P_{209}	P_{313}	P_{361}	P_{417}	P_{513}	P_{521}	P_{521}	P_{209}	P_{90}	P_{417}	P_{361}	P_{177}	P_{313}	P_{513}	P
Line 74 int	ersec	ts																
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	l
in point	P_{67}	P_{98}	P_{169}	P_{201}	P_{321}	P_{369}	P_{409}	P_{505}	P_{529}	P_{201}	P_{529}	P_{409}	P_{98}	P_{169}	P_{369}	P_{505}	P_{321}	F
Line 75 int																		
Line	ℓ_0	ℓ_1	0	0	0		0	0		1 0	1 0		0	0	0	1 0	0	,
in point	P_{67}	P_{106}	$\frac{\ell_2}{P_{161}}$	ℓ_3 P_{257}	ℓ_4 P_{265}	ℓ_5 P_{345}	ℓ_6 P_{433}	$\frac{\ell_7}{P_{465}}$	ℓ_8 P_{569}	l_9 P_{265}	ℓ_{10} P_{465}	ℓ_{11} P_{345}	$\frac{\ell_{12}}{P_{161}}$	$\frac{\ell_{13}}{P_{106}}$				_

 ℓ_6

 P_{425}

 ℓ_7

 P_{457}

 ℓ_8

 P_{577}

 ℓ_9

 P_{457}

 ℓ_{11}

 P_{153}

 ℓ_{10}

 P_{273}

 ℓ_{12}

 P_{353}

 ℓ_{13}

 P_{425}

 ℓ_{14}

 ℓ_{15}

 P_{114} P_{249}

 ℓ_{16}

 ${\rm Line}~76~{\rm intersects}$

 P_{67} P_{114}

Line

in point

 ℓ_2

 ℓ_3

 P_{153} P_{249} P_{273} P_{353}

 ℓ_4

 ℓ_5

Line 77 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{67}	P_{122}	P_{146}	P_{241}	P_{281}	P_{329}	P_{449}	P_{481}	P_{553}	P_{329}	P_{146}	P_{281}	P_{481}	P_{553}	P_{241}	P_{122}	P_{449}

Line 78 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}
in point	P_{67}	P_{130}	P_{138}	P_{233}	P_{289}	P_{337}	P_{441}	P_{473}	P_{561}	P_{138}	P_{337}	P_{473}	P_{289}	P_{233}	P_{561}	P_{441}	P_{130}

Line 79 intersects

Line	ℓ_1	ℓ_9	ℓ_{17}	ℓ_{25}	ℓ_{26}	ℓ_{34}	ℓ_{35}	ℓ_{43}	ℓ_{44}	ℓ_{52}	ℓ_{53}	ℓ_{61}	ℓ_{62}	ℓ_{70}	ℓ_{71}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

The surface has 129 points:

The points on the surface are:

```
0: P_1 = (0, 1, 0, 0)
                                            36: P_{190} = (5, 6, 1, 1)
                                                                                        72: P_{345} = (0, 2, 4, 1)
1: P_2 = (0,0,1,0)
                                            37: P_{193} = (0,7,1,1)
                                                                                        73: P_{348} = (3, 2, 4, 1)
2: P_3 = (0,0,0,1)
                                            38: P_{197} = (4, 7, 1, 1)
                                                                                        74: P_{353} = (0, 3, 4, 1)
3: P_4 = (1, 1, 1, 1)
                                            39: P_{201} = (0,0,2,1)
                                                                                        75: P_{354} = (1, 3, 4, 1)
                                            40: P_{209} = (0, 1, 2, 1)
4: P_{19} = (0, 1, 1, 0)
                                                                                        76: P_{361} = (0, 4, 4, 1)
5: P_{20} = (1, 1, 1, 0)
                                            41: P_{216} = (7, 1, 2, 1)
                                                                                        77: P_{365} = (4, 4, 4, 1)
6: P_{27} = (0, 2, 1, 0)
                                            42: P_{217} = (0, 2, 2, 1)
                                                                                        78: P_{369} = (0, 5, 4, 1)
7: P_{34} = (7, 2, 1, 0)
                                            43: P_{219} = (2, 2, 2, 1)
                                                                                        79: P_{375} = (6, 5, 4, 1)
8: P_{35} = (0, 3, 1, 0)
                                            44: P_{225} = (0, 3, 2, 1)
                                                                                        80: P_{377} = (0,6,4,1)
9: P_{41} = (6, 3, 1, 0)
                                            45: P_{230} = (5, 3, 2, 1)
                                                                                        81: P_{384} = (7, 6, 4, 1)
10: P_{43} = (0, 4, 1, 0)
                                            46: P_{233} = (0, 4, 2, 1)
                                                                                        82: P_{385} = (0,7,4,1)
11: P_{45} = (2, 4, 1, 0)
                                            47: P_{236} = (3, 4, 2, 1)
                                                                                        83: P_{390} = (5,7,4,1)
12: P_{51} = (0, 5, 1, 0)
                                            48: P_{241} = (0, 5, 2, 1)
                                                                                        84: P_{393} = (0,0,5,1)
13: P_{54} = (3, 5, 1, 0)
                                            49: P_{245} = (4, 5, 2, 1)
                                                                                        85: P_{401} = (0, 1, 5, 1)
14: P_{59} = (0, 6, 1, 0)
                                            50: P_{249} = (0, 6, 2, 1)
                                                                                        86: P_{404} = (3, 1, 5, 1)
15: P_{64} = (5, 6, 1, 0)
                                                                                        87: P_{409} = (0, 2, 5, 1)
                                            51: P_{250} = (1, 6, 2, 1)
16: P_{67} = (0, 7, 1, 0)
                                            52: P_{257} = (0,7,2,1)
                                                                                        88: P_{413} = (4, 2, 5, 1)
17: P_{71} = (4,7,1,0)
                                            53: P_{263} = (6,7,2,1)
                                                                                        89: P_{417} = (0, 3, 5, 1)
18: P_{82} = (0, 1, 0, 1)
                                            54: P_{265} = (0, 0, 3, 1)
                                                                                        90: P_{424} = (7, 3, 5, 1)
19: P_{90} = (0, 2, 0, 1)
                                            55: P_{273} = (0, 1, 3, 1)
                                                                                        91: P_{425} = (0,4,5,1)
20: P_{98} = (0, 3, 0, 1)
                                            56: P_{279} = (6, 1, 3, 1)
                                                                                        92: P_{431} = (6, 4, 5, 1)
21: P_{106} = (0, 4, 0, 1)
                                            57: P_{281} = (0, 2, 3, 1)
                                                                                        93: P_{433} = (0, 5, 5, 1)
22: P_{114} = (0, 5, 0, 1)
                                            58: P_{286} = (5, 2, 3, 1)
                                                                                        94: P_{438} = (5,5,5,1)
23: P_{122} = (0, 6, 0, 1)
                                            59: P_{289} = (0, 3, 3, 1)
                                                                                        95: P_{441} = (0, 6, 5, 1)
24: P_{130} = (0,7,0,1)
                                            60: P_{292} = (3, 3, 3, 1)
                                                                                        96: P_{443} = (2, 6, 5, 1)
25: P_{138} = (0,0,1,1)
                                            61: P_{297} = (0,4,3,1)
                                                                                        97: P_{449} = (0,7,5,1)
26: P_{146} = (0, 1, 1, 1)
                                            62: P_{298} = (1,4,3,1)
                                                                                        98: P_{450} = (1,7,5,1)
27: P_{153} = (0, 2, 1, 1)
                                                                                        99: P_{457} = (0,0,6,1)
                                            63: P_{305} = (0, 5, 3, 1)
28: P_{160} = (7, 2, 1, 1)
                                            64: P_{312} = (7, 5, 3, 1)
                                                                                        100: P_{465} = (0, 1, 6, 1)
                                            65: P_{313} = (0, 6, 3, 1)
                                                                                        101: P_{470} = (5, 1, 6, 1)
29: P_{161} = (0, 3, 1, 1)
30: P_{167} = (6, 3, 1, 1)
                                            66: P_{317} = (4, 6, 3, 1)
                                                                                        102: P_{473} = (0, 2, 6, 1)
                                            67: P_{321} = (0,7,3,1)
                                                                                        103: P_{474} = (1, 2, 6, 1)
31: P_{169} = (0,4,1,1)
32: P_{171} = (2,4,1,1)
                                            68: P_{323} = (2,7,3,1)
                                                                                        104: P_{481} = (0, 3, 6, 1)
33: P_{177} = (0, 5, 1, 1)
                                            69: P_{329} = (0,0,4,1)
                                                                                        105: P_{485} = (4, 3, 6, 1)
34: P_{180} = (3, 5, 1, 1)
                                            70: P_{337} = (0, 1, 4, 1)
                                                                                        106: P_{489} = (0, 4, 6, 1)
35: P_{185} = (0, 6, 1, 1)
                                            71: P_{339} = (2, 1, 4, 1)
                                                                                        107: P_{496} = (7, 4, 6, 1)
```

$108: P_{497} = (0, 5, 6, 1)$	$116: P_{533} = (4, 1, 7, 1)$	$124: P_{562} = (1, 5, 7, 1)$
$109: P_{499} = (2, 5, 6, 1)$	$117: P_{537} = (0, 2, 7, 1)$	$125: P_{569} = (0, 6, 7, 1)$
$110: P_{505} = (0, 6, 6, 1)$	$118: P_{543} = (6, 2, 7, 1)$	$126: P_{572} = (3, 6, 7, 1)$
$111: P_{511} = (6, 6, 6, 1)$	$119: P_{545} = (0, 3, 7, 1)$	$127: P_{577} = (0,7,7,1)$
$112: P_{513} = (0,7,6,1)$	$120: P_{547} = (2, 3, 7, 1)$	$128: P_{584} = (7,7,7,1)$
$113: P_{516} = (3,7,6,1)$	$121: P_{553} = (0,4,7,1)$	
$114: P_{521} = (0,0,7,1)$	$122: P_{558} = (5, 4, 7, 1)$	
$115: P_{529} = (0, 1, 7, 1)$	$123: P_{561} = (0, 5, 7, 1)$	