# Rank-76355 over GF(32)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^2 X_3 + X_1^2 X_3 + X_1 X_2^2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

( 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0 ) The point rank of the equation over GF(32) is -2112846811

# General information

Number of lines	5
Number of points	1121
Number of singular points	0
Number of Eckardt points	1
Number of double points	3
Number of single points	156
Number of points off lines	961
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$33^{5}$
Type of lines on points	$3, 2^3, 1^{156}, 0^{961}$

### Singular Points

The surface has 0 singular points:

# The 5 Lines

The lines and their Pluecker coordinates are:

$$\begin{split} \ell_0 &= \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{array} \right]_0 = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{array} \right]_0 = \mathbf{Pl}(1,0,0,0,0,0)_0 \\ \ell_1 &= \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]_{1024} = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]_{1024} = \mathbf{Pl}(0,0,1,0,0,0)_2 \end{split}$$

$$\ell_{2} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{1057} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{1057} = \mathbf{Pl}(1, 0, 0, 0, 0, 1)_{34850}$$

$$\ell_{3} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1083424} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1083424} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_{1}$$

$$\ell_{4} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{34848} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{34848} = \mathbf{Pl}(0, 1, 1, 0, 0, 0)_{34}$$

Rank of lines: (0, 1024, 1057, 1083424, 34848) Rank of points on Klein quadric: (0, 2, 34850, 1, 34)

### **Eckardt Points**

The surface has 1 Eckardt points:  $0: P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0).$ 

#### **Double Points**

The surface has 3 Double points: The double points on the surface are:

$$P_0 = (1, 0, 0, 0) = \ell_0 \cap \ell_1$$
  

$$P_1 = (0, 1, 0, 0) = \ell_0 \cap \ell_2$$

# $P_{36} = (1,0,1,0) = \ell_1 \cap \ell_2$

### Single Points

The surface has 156 single points: The single points on the surface are:

$0: P_3 = (0,0,0,1)$ lies on line $\ell_3$	$22: P_{26} = (22, 1, 0, 0)$ lies on line $\ell_0$
$1: P_5 = (1, 1, 0, 0)$ lies on line $\ell_0$	23: $P_{27} = (23, 1, 0, 0)$ lies on line $\ell_0$
$2: P_6 = (2, 1, 0, 0)$ lies on line $\ell_0$	24: $P_{28} = (24, 1, 0, 0)$ lies on line $\ell_0$
$3: P_7 = (3, 1, 0, 0)$ lies on line $\ell_0$	25: $P_{29} = (25, 1, 0, 0)$ lies on line $\ell_0$
$4: P_8 = (4, 1, 0, 0)$ lies on line $\ell_0$	26: $P_{30} = (26, 1, 0, 0)$ lies on line $\ell_0$
$5: P_9 = (5, 1, 0, 0)$ lies on line $\ell_0$	27: $P_{31} = (27, 1, 0, 0)$ lies on line $\ell_0$
$6: P_{10} = (6, 1, 0, 0)$ lies on line $\ell_0$	28: $P_{32} = (28, 1, 0, 0)$ lies on line $\ell_0$
7: $P_{11} = (7, 1, 0, 0)$ lies on line $\ell_0$	29: $P_{33} = (29, 1, 0, 0)$ lies on line $\ell_0$
$8: P_{12} = (8, 1, 0, 0)$ lies on line $\ell_0$	$30: P_{34} = (30, 1, 0, 0)$ lies on line $\ell_0$
$9: P_{13} = (9, 1, 0, 0)$ lies on line $\ell_0$	$31: P_{35} = (31, 1, 0, 0)$ lies on line $\ell_0$
10: $P_{14} = (10, 1, 0, 0)$ lies on line $\ell_0$	$32: P_{37} = (2,0,1,0)$ lies on line $\ell_1$
11: $P_{15} = (11, 1, 0, 0)$ lies on line $\ell_0$	33: $P_{38} = (3,0,1,0)$ lies on line $\ell_1$
12: $P_{16} = (12, 1, 0, 0)$ lies on line $\ell_0$	$34: P_{39} = (4,0,1,0)$ lies on line $\ell_1$
13: $P_{17} = (13, 1, 0, 0)$ lies on line $\ell_0$	$35: P_{40} = (5,0,1,0)$ lies on line $\ell_1$
14: $P_{18} = (14, 1, 0, 0)$ lies on line $\ell_0$	36: $P_{41} = (6, 0, 1, 0)$ lies on line $\ell_1$
15: $P_{19} = (15, 1, 0, 0)$ lies on line $\ell_0$	$37: P_{42} = (7,0,1,0)$ lies on line $\ell_1$
16: $P_{20} = (16, 1, 0, 0)$ lies on line $\ell_0$	38: $P_{43} = (8, 0, 1, 0)$ lies on line $\ell_1$
17: $P_{21} = (17, 1, 0, 0)$ lies on line $\ell_0$	39: $P_{44} = (9,0,1,0)$ lies on line $\ell_1$
18: $P_{22} = (18, 1, 0, 0)$ lies on line $\ell_0$	40: $P_{45} = (10, 0, 1, 0)$ lies on line $\ell_1$
19: $P_{23} = (19, 1, 0, 0)$ lies on line $\ell_0$	41: $P_{46} = (11, 0, 1, 0)$ lies on line $\ell_1$
20: $P_{24} = (20, 1, 0, 0)$ lies on line $\ell_0$	42: $P_{47} = (12, 0, 1, 0)$ lies on line $\ell_1$
$21: P_{25} = (21, 1, 0, 0)$ lies on line $\ell_0$	43: $P_{48} = (13, 0, 1, 0)$ lies on line $\ell_1$

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44: P_{49} = (14, 0, 1, 0) lies on line \ell_1
                                                                     98: P_{4129} = (0,0,3,1) lies on line \ell_3
45: P_{50} = (15, 0, 1, 0) lies on line \ell_1
                                                                     99: P_{4130} = (1,0,3,1) lies on line \ell_4
46: P_{51} = (16, 0, 1, 0) lies on line \ell_1
                                                                     100: P_{5153} = (0, 0, 4, 1) lies on line \ell_3
47: P_{52} = (17, 0, 1, 0) lies on line \ell_1
                                                                     101: P_{5154} = (1, 0, 4, 1) lies on line \ell_4
48: P_{53} = (18, 0, 1, 0) lies on line \ell_1
                                                                     102: P_{6177} = (0, 0, 5, 1) lies on line \ell_3
49: P_{54} = (19, 0, 1, 0) lies on line \ell_1
                                                                     103: P_{6178} = (1, 0, 5, 1) lies on line \ell_4
50: P_{55} = (20, 0, 1, 0) lies on line \ell_1
                                                                     104: P_{7201} = (0, 0, 6, 1) lies on line \ell_3
51: P_{56} = (21, 0, 1, 0) lies on line \ell_1
                                                                      105: P_{7202} = (1, 0, 6, 1) lies on line \ell_4
52: P_{57} = (22, 0, 1, 0) lies on line \ell_1
                                                                     106: P_{8225} = (0, 0, 7, 1) lies on line \ell_3
53: P_{58} = (23, 0, 1, 0) lies on line \ell_1
                                                                     107: P_{8226} = (1, 0, 7, 1) lies on line \ell_4
54: P_{59} = (24, 0, 1, 0) lies on line \ell_1
                                                                     108: P_{9249} = (0,0,8,1) lies on line \ell_3
55: P_{60} = (25, 0, 1, 0) lies on line \ell_1
                                                                     109: P_{9250} = (1,0,8,1) lies on line \ell_4
56: P_{61} = (26, 0, 1, 0) lies on line \ell_1
                                                                     110: P_{10273} = (0, 0, 9, 1) lies on line \ell_3
57: P_{62} = (27, 0, 1, 0) lies on line \ell_1
                                                                     111: P_{10274} = (1, 0, 9, 1) lies on line \ell_4
58: P_{63} = (28, 0, 1, 0) lies on line \ell_1
                                                                     112 : P_{11297} = (0, 0, 10, 1) lies on line \ell_3
59: P_{64} = (29, 0, 1, 0) lies on line \ell_1
                                                                     113: P_{11298} = (1, 0, 10, 1) lies on line \ell_4
60: P_{65} = (30, 0, 1, 0) lies on line \ell_1
                                                                     114: P_{12321} = (0, 0, 11, 1) lies on line \ell_3
61: P_{66} = (31, 0, 1, 0) lies on line \ell_1
                                                                     115: P_{12322} = (1, 0, 11, 1) lies on line \ell_4
62: P_{68} = (1, 1, 1, 0) lies on line \ell_2
                                                                     116: P_{13345} = (0, 0, 12, 1) lies on line \ell_3
63: P_{100} = (1, 2, 1, 0) lies on line \ell_2
                                                                     117: P_{13346} = (1, 0, 12, 1) lies on line \ell_4
64: P_{132} = (1, 3, 1, 0) lies on line \ell_2
                                                                     118: P_{14369} = (0, 0, 13, 1) lies on line \ell_3
65: P_{164} = (1, 4, 1, 0) lies on line \ell_2
                                                                     119: P_{14370} = (1, 0, 13, 1) lies on line \ell_4
66: P_{196} = (1, 5, 1, 0) lies on line \ell_2
                                                                      120: P_{15393} = (0, 0, 14, 1) lies on line \ell_3
                                                                     121 : P_{15394} = (1, 0, 14, 1) lies on line \ell_4
67: P_{228} = (1, 6, 1, 0) lies on line \ell_2
68: P_{260} = (1,7,1,0) lies on line \ell_2
                                                                     122: P_{16417} = (0, 0, 15, 1) lies on line \ell_3
69: P_{292} = (1, 8, 1, 0) lies on line \ell_2
                                                                     123: P_{16418} = (1, 0, 15, 1) lies on line \ell_4
70: P_{324} = (1, 9, 1, 0) lies on line \ell_2
                                                                     124: P_{17441} = (0, 0, 16, 1) lies on line \ell_3
71: P_{356} = (1, 10, 1, 0) lies on line \ell_2
                                                                     125: P_{17442} = (1, 0, 16, 1) lies on line \ell_4
72: P_{388} = (1, 11, 1, 0) lies on line \ell_2
                                                                     126: P_{18465} = (0, 0, 17, 1) lies on line \ell_3
73: P_{420} = (1, 12, 1, 0) lies on line \ell_2
                                                                     127: P_{18466} = (1, 0, 17, 1) lies on line \ell_4
74: P_{452} = (1, 13, 1, 0) lies on line \ell_2
                                                                     128: P_{19489} = (0, 0, 18, 1) lies on line \ell_3
75: P_{484} = (1, 14, 1, 0) lies on line \ell_2
                                                                     129: P_{19490} = (1, 0, 18, 1) lies on line \ell_4
76: P_{516} = (1, 15, 1, 0) lies on line \ell_2
                                                                     130: P_{20513} = (0, 0, 19, 1) lies on line \ell_3
77: P_{548} = (1, 16, 1, 0) lies on line \ell_2
                                                                     131: P_{20514} = (1, 0, 19, 1) lies on line \ell_4
78: P_{580} = (1, 17, 1, 0) lies on line \ell_2
                                                                     132: P_{21537} = (0, 0, 20, 1) lies on line \ell_3
79: P_{612} = (1, 18, 1, 0) lies on line \ell_2
                                                                     133: P_{21538} = (1, 0, 20, 1) lies on line \ell_4
80: P_{644} = (1, 19, 1, 0) lies on line \ell_2
                                                                     134: P_{22561} = (0, 0, 21, 1) lies on line \ell_3
81: P_{676} = (1, 20, 1, 0) lies on line \ell_2
                                                                     135: P_{22562} = (1, 0, 21, 1) lies on line \ell_4
82: P_{708} = (1, 21, 1, 0) lies on line \ell_2
                                                                     136: P_{23585} = (0, 0, 22, 1) lies on line \ell_3
                                                                     137 : P_{23586} = (1, 0, 22, 1) lies on line \ell_4
83: P_{740} = (1, 22, 1, 0) lies on line \ell_2
84 : P_{772} = (1, 23, 1, 0) lies on line \ell_2
                                                                     138: P_{24609} = (0, 0, 23, 1) lies on line \ell_3
85: P_{804} = (1, 24, 1, 0) lies on line \ell_2
                                                                     139: P_{24610} = (1, 0, 23, 1) lies on line \ell_4
                                                                     140 : P_{25633} = (0, 0, 24, 1) lies on line \ell_3
86: P_{836} = (1, 25, 1, 0) lies on line \ell_2
87: P_{868} = (1, 26, 1, 0) lies on line \ell_2
                                                                     141: P_{25634} = (1, 0, 24, 1) lies on line \ell_4
88: P_{900} = (1, 27, 1, 0) lies on line \ell_2
                                                                     142: P_{26657} = (0, 0, 25, 1) lies on line \ell_3
89: P_{932} = (1, 28, 1, 0) lies on line \ell_2
                                                                     143: P_{26658} = (1, 0, 25, 1) lies on line \ell_4
90: P_{964} = (1, 29, 1, 0) lies on line \ell_2
                                                                     144: P_{27681} = (0, 0, 26, 1) lies on line \ell_3
91: P_{996} = (1, 30, 1, 0) lies on line \ell_2
                                                                     145: P_{27682} = (1, 0, 26, 1) lies on line \ell_4
92: P_{1028} = (1, 31, 1, 0) lies on line \ell_2
                                                                     146: P_{28705} = (0, 0, 27, 1) lies on line \ell_3
93: P_{1059} = (1,0,0,1) lies on line \ell_4
                                                                     147: P_{28706} = (1, 0, 27, 1) lies on line \ell_4
94: P_{2082} = (0,0,1,1) lies on line \ell_3
                                                                     148: P_{29729} = (0, 0, 28, 1) lies on line \ell_3
95: P_{2083} = (1,0,1,1) lies on line \ell_4
                                                                     149: P_{29730} = (1, 0, 28, 1) lies on line \ell_4
                                                                     150 : P_{30753} = (0, 0, 29, 1) lies on line \ell_3
96: P_{3105} = (0,0,2,1) lies on line \ell_3
97: P_{3106} = (1,0,2,1) lies on line \ell_4
                                                                     151: P_{30754} = (1, 0, 29, 1) lies on line \ell_4
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152 : P_{31777} = (0,0,30,1) lies on line \ell_3
153 : P_{31778} = (1,0,30,1) lies on line \ell_4
154 : P_{32801} = (0,0,31,1) lies on line \ell_3
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The single points on the surface are:

#### Points on surface but on no line

The surface has 961 points not on any line: The points on the surface but not on lines are:

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0: P_{1132} = (10, 2, 0, 1)
                                                                  41: P_{2599} = (6, 16, 1, 1)
1: P_{1133} = (11, 2, 0, 1)
                                                                  42: P_{2616} = (23, 16, 1, 1)
2: P_{1200} = (14, 4, 0, 1)
                                                                  43: P_{2734} = (13, 20, 1, 1)
3: P_{1201} = (15, 4, 0, 1)
                                                                  44: P_{2745} = (24, 20, 1, 1)
4: P_{1254} = (4, 6, 0, 1)
                                                                  45: P_{2755} = (2, 21, 1, 1)
5: P_{1255} = (5, 6, 0, 1)
                                                                  46: P_{2775} = (22, 21, 1, 1)
6: P_{1374} = (28, 9, 0, 1)
                                                                  47: P_{2787} = (2, 22, 1, 1)
7: P_{1375} = (29, 9, 0, 1)
                                                                  48: P_{2806} = (21, 22, 1, 1)
8: P_{1432} = (22, 11, 0, 1)
                                                                  49: P_{2823} = (6, 23, 1, 1)
9: P_{1433} = (23, 11, 0, 1)
                                                                  50: P_{2833} = (16, 23, 1, 1)
10: P_{1492} = (18, 13, 0, 1)
                                                                  51: P_{2862} = (13, 24, 1, 1)
11: P_{1493} = (19, 13, 0, 1)
                                                                  52: P_{2869} = (20, 24, 1, 1)
12: P_{1562} = (24, 15, 0, 1)
                                                                  53: P_{2885} = (4, 25, 1, 1)
13: P_{1563} = (25, 15, 0, 1)
                                                                  54: P_{2909} = (28, 25, 1, 1)
14: P_{1600} = (30, 16, 0, 1)
                                                                  55: P_{2952} = (7, 27, 1, 1)
15: P_{1601} = (31, 16, 0, 1)
                                                                  56: P_{2974} = (29, 27, 1, 1)
16: P_{1654} = (20, 18, 0, 1)
                                                                  57: P_{2981} = (4, 28, 1, 1)
17: P_{1655} = (21, 18, 0, 1)
                                                                  58: P_{3002} = (25, 28, 1, 1)
18: P_{1714} = (16, 20, 0, 1)
                                                                  59: P_{3016} = (7, 29, 1, 1)
19: P_{1715} = (17, 20, 0, 1)
                                                                  60: P_{3036} = (27, 29, 1, 1)
20: P_{1788} = (26, 22, 0, 1)
                                                                  61: P_{3228} = (27, 3, 2, 1)
                                                                  62: P_{3229} = (28, 3, 2, 1)
21: P_{1789} = (27, 22, 0, 1)
22: P_{1860} = (2, 25, 0, 1)
                                                                  63: P_{3233} = (0,4,2,1)
23: P_{1861} = (3, 25, 0, 1)
                                                                  64: P_{3242} = (9, 4, 2, 1)
24: P_{1930} = (8, 27, 0, 1)
                                                                  65: P_{3298} = (1, 6, 2, 1)
                                                                  66: P_{3309} = (12, 6, 2, 1)
25: P_{1931} = (9, 27, 0, 1)
26: P_{1998} = (12, 29, 0, 1)
                                                                  67: P_{3333} = (4,7,2,1)
                                                                  68: P_{3340} = (11, 7, 2, 1)
27: P_{1999} = (13, 29, 0, 1)
28: P_{2056} = (6, 31, 0, 1)
                                                                  69: P_{3461} = (4, 11, 2, 1)
29: P_{2057} = (7, 31, 0, 1)
                                                                  70: P_{3476} = (19, 11, 2, 1)
30: P_{2114} = (0, 1, 1, 1)
                                                                  71: P_{3499} = (10, 12, 2, 1)
31: P_{2166} = (21, 2, 1, 1)
                                                                  72: P_{3508} = (19, 12, 2, 1)
32: P_{2167} = (22, 2, 1, 1)
                                                                  73: P_{3633} = (16, 16, 2, 1)
33: P_{2234} = (25, 4, 1, 1)
                                                                  74: P_{3637} = (20, 16, 2, 1)
34: P_{2237} = (28, 4, 1, 1)
                                                                  75: P_{3665} = (16, 17, 2, 1)
35: P_{2289} = (16, 6, 1, 1)
                                                                  76: P_{3671} = (22, 17, 2, 1)
36: P_{2296} = (23, 6, 1, 1)
                                                                  77: P_{3690} = (9, 18, 2, 1)
37: P_{2332} = (27, 7, 1, 1)
                                                                  78: P_{3768} = (23, 20, 2, 1)
38: P_{2334} = (29, 7, 1, 1)
                                                                  79: P_{3772} = (27, 20, 2, 1)
39: P_{2517} = (20, 13, 1, 1)
                                                                  80: P_{3782} = (5, 21, 2, 1)
40: P_{2521} = (24, 13, 1, 1)
                                                                  81: P_{3788} = (11, 21, 2, 1)
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82: P_{3907} = (2, 25, 2, 1)
                                                                 136: P_{5665} = (0, 16, 4, 1)
83: P_{3925} = (20, 25, 2, 1)
                                                                 137: P_{5676} = (11, 16, 4, 1)
84: P_{3949} = (12, 26, 2, 1)
                                                                 138: P_{5794} = (1, 20, 4, 1)
85: P_{3965} = (28, 26, 2, 1)
                                                                 139: P_{5819} = (26, 20, 4, 1)
86: P_{3974} = (5, 27, 2, 1)
                                                                 140: P_{5840} = (15, 21, 4, 1)
87: P_{3992} = (23, 27, 2, 1)
                                                                 141: P_{5841} = (16, 21, 4, 1)
88: P_{4011} = (10, 28, 2, 1)
                                                                 142: P_{5903} = (14, 23, 4, 1)
89: P_{4023} = (22, 28, 2, 1)
                                                                 143: P_{5914} = (25, 23, 4, 1)
90: P_{4234} = (9, 3, 3, 1)
                                                                 144: P_{5993} = (8, 26, 4, 1)
91: P_{4238} = (13, 3, 3, 1)
                                                                 145: P_{5999} = (14, 26, 4, 1)
92: P_{4289} = (0, 5, 3, 1)
                                                                 146: P_{6064} = (15, 28, 4, 1)
93: P_{4303} = (14, 5, 3, 1)
                                                                 147: P_{6066} = (17, 28, 4, 1)
                                                                 148: P_{6083} = (2, 29, 4, 1)
94: P_{4322} = (1, 6, 3, 1)
95: P_{4331} = (10, 6, 3, 1)
                                                                 149: P_{6105} = (24, 29, 4, 1)
96: P_{4397} = (12, 8, 3, 1)
                                                                 150: P_{6348} = (11, 5, 5, 1)
97: P_{4406} = (21, 8, 3, 1)
                                                                 151: P_{6364} = (27, 5, 5, 1)
                                                                 152: P_{6374} = (5, 6, 5, 1)
98: P_{4457} = (8, 10, 3, 1)
                                                                 153: P_{6395} = (26, 6, 5, 1)
99: P_{4472} = (23, 10, 3, 1)
100: P_{4686} = (13, 17, 3, 1)
                                                                 154: P_{6453} = (20, 8, 5, 1)
101: P_{4699} = (26, 17, 3, 1)
                                                                 155: P_{6457} = (24, 8, 5, 1)
102: P_{4719} = (14, 18, 3, 1)
                                                                 156: P_{6488} = (23, 9, 5, 1)
103: P_{4733} = (28, 18, 3, 1)
                                                                 157: P_{6495} = (30, 9, 5, 1)
104: P_{4743} = (6, 19, 3, 1)
                                                                 158: P_{6523} = (26, 10, 5, 1)
105: P_{4760} = (23, 19, 3, 1)
                                                                 159: P_{6525} = (28, 10, 5, 1)
106: P_{4803} = (2, 21, 3, 1)
                                                                 160: P_{6564} = (3, 12, 5, 1)
107: P_{4826} = (25, 21, 3, 1)
                                                                 161: P_{6588} = (27, 12, 5, 1)
108: P_{4835} = (2, 22, 3, 1)
                                                                 162: P_{6635} = (10, 14, 5, 1)
109: P_{4861} = (28, 22, 3, 1)
                                                                 163: P_{6649} = (24, 14, 5, 1)
110: P_{4873} = (8, 23, 3, 1)
                                                                 164: P_{6721} = (0, 17, 5, 1)
111: P_{4886} = (21, 23, 3, 1)
                                                                 165: P_{6751} = (30, 17, 5, 1)
112: P_{4932} = (3, 25, 3, 1)
                                                                 166: P_{6756} = (3, 18, 5, 1)
113: P_{4941} = (12, 25, 3, 1)
                                                                 167: P_{6771} = (18, 18, 5, 1)
114: P_{5031} = (6, 28, 3, 1)
                                                                 168: P_{6791} = (6, 19, 5, 1)
115: P_{5066} = (9, 29, 3, 1)
                                                                 169: P_{6803} = (18, 19, 5, 1)
116: P_{5067} = (10, 29, 3, 1)
                                                                 170: P_{6818} = (1, 20, 5, 1)
117: P_{5114} = (25, 30, 3, 1)
                                                                 171: P_{6831} = (14, 20, 5, 1)
118: P_{5120} = (31, 30, 3, 1)
                                                                 172: P_{6892} = (11, 22, 5, 1)
119: P_{5147} = (26, 31, 3, 1)
                                                                 173: P_{6895} = (14, 22, 5, 1)
120: P_{5152} = (31, 31, 3, 1)
                                                                 174: P_{6933} = (20, 23, 5, 1)
121: P_{5234} = (17, 2, 4, 1)
                                                                 175: P_{6955} = (10, 24, 5, 1)
122: P_{5241} = (24, 2, 4, 1)
                                                                 176: P_{6973} = (28, 24, 5, 1)
123: P_{5272} = (23, 3, 4, 1)
                                                                 177: P_{6981} = (4, 25, 5, 1)
124: P_{5275} = (26, 3, 4, 1)
                                                                 178: P_{7000} = (23, 25, 5, 1)
125: P_{5315} = (2, 5, 4, 1)
                                                                 179: P_{7077} = (4, 28, 5, 1)
126: P_{5336} = (23, 5, 4, 1)
                                                                 180: P_{7079} = (6, 28, 5, 1)
                                                                 181: P_{7363} = (2, 5, 6, 1)
127: P_{5349} = (4, 6, 4, 1)
128: P_{5374} = (29, 6, 4, 1)
                                                                 182: P_{7390} = (29, 5, 6, 1)
129: P_{5452} = (11, 9, 4, 1)
                                                                 183: P_{7429} = (4, 7, 6, 1)
                                                                 184: P_{7448} = (23, 7, 6, 1)
130: P_{5550} = (13, 12, 4, 1)
131: P_{5562} = (25, 12, 4, 1)
                                                                 185: P_{7465} = (8, 8, 6, 1)
                                                                 186: P_{7485} = (28, 8, 6, 1)
132: P_{5582} = (13, 13, 4, 1)
133: P_{5598} = (29, 13, 4, 1)
                                                                 187: P_{7497} = (8, 9, 6, 1)
134: P_{5641} = (8, 15, 4, 1)
                                                                 188: P_{7515} = (26, 9, 6, 1)
135: P_{5649} = (16, 15, 4, 1)
                                                                 189: P_{7534} = (13, 10, 6, 1)
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190: P_{7542} = (21, 10, 6, 1)
                                                                 244: P_{9329} = (16, 2, 8, 1)
191: P_{7557} = (4, 11, 6, 1)
                                                                 245: P_{9349} = (4, 3, 8, 1)
                                                                 246: P_{9374} = (29, 3, 8, 1)
192: P_{7579} = (26, 11, 6, 1)
193: P_{7588} = (3, 12, 6, 1)
                                                                 247: P_{9429} = (20, 5, 8, 1)
194: P_{7600} = (15, 12, 6, 1)
                                                                 248: P_{9433} = (24, 5, 8, 1)
195: P_{7672} = (23, 14, 6, 1)
                                                                 249: P_{9456} = (15, 6, 8, 1)
196: P_{7700} = (19, 15, 6, 1)
                                                                 250: P_{9468} = (27, 6, 8, 1)
197: P_{7702} = (21, 15, 6, 1)
                                                                 251: P_{9569} = (0, 10, 8, 1)
198: P_{7778} = (1, 18, 6, 1)
                                                                 252: P_{9596} = (27, 10, 8, 1)
199: P_{7780} = (3, 18, 6, 1)
                                                                 253: P_{9637} = (4, 12, 8, 1)
200: P_{7841} = (0, 20, 6, 1)
                                                                 254: P_{9643} = (10, 12, 8, 1)
201: P_{7863} = (22, 20, 6, 1)
                                                                 255: P_{9699} = (2, 14, 8, 1)
202: P_{7886} = (13, 21, 6, 1)
                                                                 256: P_{9725} = (28, 14, 8, 1)
203: P_{7902} = (29, 21, 6, 1)
                                                                 257: P_{9798} = (5, 17, 8, 1)
204: P_{8072} = (7, 27, 6, 1)
                                                                 258: P_{9817} = (24, 17, 8, 1)
205: P_{8087} = (22, 27, 6, 1)
                                                                 259: P_{9891} = (2, 20, 8, 1)
                                                                 260: P_{9907} = (18, 20, 8, 1)
206: P_{8131} = (2, 29, 6, 1)
                                                                 261: P_{9958} = (5, 22, 8, 1)
207: P_{8136} = (7, 29, 6, 1)
                                                                 262: P_{10099} = (18, 26, 8, 1)
208: P_{8180} = (19, 30, 6, 1)
209: P_{8189} = (28, 30, 6, 1)
                                                                 263: P_{10110} = (29, 26, 8, 1)
210: P_{8199} = (6, 31, 6, 1)
                                                                 264: P_{10121} = (8, 27, 8, 1)
211: P_{8208} = (15, 31, 6, 1)
                                                                 265: P_{10128} = (15, 27, 8, 1)
212: P_{8366} = (13, 4, 7, 1)
                                                                 266: P_{10155} = (10, 28, 8, 1)
213: P_{8369} = (16, 4, 7, 1)
                                                                 267: P_{10161} = (16, 28, 8, 1)
214: P_{8432} = (15, 6, 7, 1)
                                                                 268: P_{10229} = (20, 30, 8, 1)
215: P_{8445} = (28, 6, 7, 1)
                                                                 269: P_{10239} = (30, 30, 8, 1)
216: P_{8461} = (12, 7, 7, 1)
                                                                 270: P_{10269} = (28, 31, 8, 1)
217: P_{8473} = (24, 7, 7, 1)
                                                                 271: P_{10271} = (30, 31, 8, 1)
218: P_{8556} = (11, 10, 7, 1)
                                                                 272: P_{10338} = (1, 2, 9, 1)
                                                                 273: P_{10355} = (18, 2, 9, 1)
219: P_{8570} = (25, 10, 7, 1)
220: P_{8588} = (11, 11, 7, 1)
                                                                 274: P_{10423} = (22, 4, 9, 1)
221: P_{8607} = (30, 11, 7, 1)
                                                                 275: P_{10475} = (10, 6, 9, 1)
222: P_{8629} = (20, 12, 7, 1)
                                                                 276: P_{10489} = (24, 6, 9, 1)
223: P_{8668} = (27, 13, 7, 1)
                                                                 277: P_{10508} = (11, 7, 9, 1)
224: P_{8669} = (28, 13, 7, 1)
                                                                 278: P_{10513} = (16, 7, 9, 1)
225: P_{8689} = (16, 14, 7, 1)
                                                                 279: P_{10545} = (16, 8, 9, 1)
226: P_{8703} = (30, 14, 7, 1)
                                                                 280: P_{10548} = (19, 8, 9, 1)
227: P_{8743} = (6, 16, 7, 1)
                                                                 281: P_{10625} = (0, 11, 9, 1)
228: P_{8761} = (24, 16, 7, 1)
                                                                 282: P_{10649} = (24, 11, 9, 1)
                                                                 283: P_{10670} = (13, 12, 9, 1)
229: P_{8802} = (1, 18, 7, 1)
230: P_{8818} = (17, 18, 7, 1)
                                                                 284: P_{10672} = (15, 12, 9, 1)
231: P_{8845} = (12, 19, 7, 1)
                                                                 285: P_{10695} = (6, 13, 9, 1)
232: P_{8860} = (27, 19, 7, 1)
                                                                 286: P_{10702} = (13, 13, 9, 1)
233: P_{8897} = (0, 21, 7, 1)
                                                                 287: P_{10951} = (6, 21, 9, 1)
234: P_{8902} = (5, 21, 7, 1)
                                                                 288: P_{10956} = (11, 21, 9, 1)
235: P_{8967} = (6, 23, 7, 1)
                                                                 289: P_{11058} = (17, 24, 9, 1)
236: P_{8974} = (13, 23, 7, 1)
                                                                 290: P_{11063} = (22, 24, 9, 1)
237: P_{9077} = (20, 26, 7, 1)
                                                                 291: P_{11146} = (9, 27, 9, 1)
238: P_{9082} = (25, 26, 7, 1)
                                                                 292: P_{11158} = (21, 27, 9, 1)
239: P_{9094} = (5, 27, 7, 1)
                                                                 293: P_{11188} = (19, 28, 9, 1)
240: P_{9104} = (15, 27, 7, 1)
                                                                 294: P_{11190} = (21, 28, 9, 1)
241: P_{9224} = (7, 31, 7, 1)
                                                                 295: P_{11206} = (5, 29, 9, 1)
242: P_{9234} = (17, 31, 7, 1)
                                                                 296: P_{11211} = (10, 29, 9, 1)
243: P_{9314} = (1, 2, 8, 1)
                                                                 297: P_{11238} = (5, 30, 9, 1)
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298: P_{11250} = (17, 30, 9, 1)
                                                                352: P_{13085} = (28, 23, 11, 1)
                                                                353: P_{13180} = (27, 26, 11, 1)
299: P_{11280} = (15, 31, 9, 1)
300: P_{11283} = (18, 31, 9, 1)
                                                                354: P_{13184} = (31, 26, 11, 1)
301: P_{11371} = (10, 2, 10, 1)
                                                                355: P_{13205} = (20, 27, 11, 1)
302: P_{11392} = (31, 2, 10, 1)
                                                                356: P_{13212} = (27, 27, 11, 1)
303: P_{11402} = (9, 3, 10, 1)
                                                                357: P_{13232} = (15, 28, 11, 1)
304: P_{11415} = (22, 3, 10, 1)
                                                                358: P_{13237} = (20, 28, 11, 1)
305: P_{11426} = (1, 4, 10, 1)
                                                                359: P_{13445} = (4, 3, 12, 1)
306: P_{11438} = (13, 4, 10, 1)
                                                                360: P_{13458} = (17, 3, 12, 1)
307: P_{11473} = (16, 5, 10, 1)
                                                                361: P_{13556} = (19, 6, 12, 1)
308: P_{11479} = (22, 5, 10, 1)
                                                                362: P_{13568} = (31, 6, 12, 1)
309: P_{11688} = (7, 12, 10, 1)
                                                                363: P_{13591} = (22, 7, 12, 1)
310: P_{11698} = (17, 12, 10, 1)
                                                                364: P_{13676} = (11, 10, 12, 1)
311: P_{11745} = (0, 14, 10, 1)
                                                                365: P_{13694} = (29, 10, 12, 1)
312: P_{11747} = (2, 14, 10, 1)
                                                                366: P_{13708} = (11, 11, 12, 1)
313: P_{11848} = (7, 17, 10, 1)
                                                                367: P_{13714} = (17, 11, 12, 1)
314: P_{11870} = (29, 17, 10, 1)
                                                                368: P_{13733} = (4, 12, 12, 1)
315: P_{11892} = (19, 18, 10, 1)
                                                                369: P_{13760} = (31, 12, 12, 1)
316: P_{11896} = (23, 18, 10, 1)
                                                                370: P_{13814} = (21, 14, 12, 1)
317: P_{11924} = (19, 19, 10, 1)
                                                                371: P_{13815} = (22, 14, 12, 1)
318: P_{11934} = (29, 19, 10, 1)
                                                                372: P_{13832} = (7, 15, 12, 1)
319: P_{11939} = (2, 20, 10, 1)
                                                                373: P_{13833} = (8, 15, 12, 1)
320: P_{11968} = (31, 20, 10, 1)
                                                                374: P_{13974} = (21, 19, 12, 1)
321: P_{12046} = (13, 23, 10, 1)
                                                                375: P_{13983} = (30, 19, 12, 1)
322: P_{12047} = (14, 23, 10, 1)
                                                                376: P_{13992} = (7, 20, 12, 1)
323: P_{12114} = (17, 25, 10, 1)
                                                                377: P_{13998} = (13, 20, 12, 1)
324: P_{12143} = (14, 26, 10, 1)
                                                                378: P_{14041} = (24, 21, 12, 1)
325: P_{12145} = (16, 26, 10, 1)
                                                                379: P_{14047} = (30, 21, 12, 1)
326: P_{12229} = (4, 29, 10, 1)
                                                                380: P_{14050} = (1, 22, 12, 1)
                                                                381: P_{14068} = (19, 22, 12, 1)
327: P_{12234} = (9, 29, 10, 1)
328: P_{12261} = (4, 30, 10, 1)
                                                                382: P_{14126} = (13, 24, 12, 1)
329: P_{12280} = (23, 30, 10, 1)
                                                                383: P_{14142} = (29, 24, 12, 1)
330: P_{12396} = (11, 2, 11, 1)
                                                                384: P_{14177} = (0, 26, 12, 1)
331: P_{12413} = (28, 2, 11, 1)
                                                                385: P_{14185} = (8, 26, 12, 1)
332: P_{12450} = (1, 4, 11, 1)
                                                                386: P_{14278} = (5, 29, 12, 1)
                                                                387: P_{14285} = (12, 29, 12, 1)
333: P_{12458} = (9, 4, 11, 1)
334: P_{12557} = (12, 7, 11, 1)
                                                                388: P_{14310} = (5, 30, 12, 1)
335: P_{12570} = (25, 7, 11, 1)
                                                                389: P_{14329} = (24, 30, 12, 1)
336: P_{12649} = (8, 10, 11, 1)
                                                                390: P_{14435} = (2, 2, 13, 1)
337: P_{12654} = (13, 10, 11, 1)
                                                                391: P_{14458} = (25, 2, 13, 1)
338: P_{12801} = (0, 15, 11, 1)
                                                                392: P_{14467} = (2, 3, 13, 1)
339: P_{12808} = (7, 15, 11, 1)
                                                                393: P_{14485} = (20, 3, 13, 1)
340: P_{12858} = (25, 16, 11, 1)
                                                                394: P_{14543} = (14, 5, 13, 1)
341: P_{12906} = (9, 18, 11, 1)
                                                                395: P_{14548} = (19, 5, 13, 1)
342: P_{12928} = (31, 18, 11, 1)
                                                                396: P_{14612} = (19, 7, 13, 1)
343: P_{12941} = (12, 19, 11, 1)
                                                                397: P_{14613} = (20, 7, 13, 1)
344: P_{12946} = (17, 19, 11, 1)
                                                                398: P_{14760} = (7, 12, 13, 1)
345: P_{12968} = (7, 20, 11, 1)
                                                                399: P_{14769} = (16, 12, 13, 1)
346: P_{12975} = (14, 20, 11, 1)
                                                                400: P_{14880} = (31, 15, 13, 1)
347: P_{13006} = (13, 21, 11, 1)
                                                                401: P_{14902} = (21, 16, 13, 1)
348: P_{13008} = (15, 21, 11, 1)
                                                                402: P_{14907} = (26, 16, 13, 1)
349: P_{13039} = (14, 22, 11, 1)
                                                                403: P_{14918} = (5, 17, 13, 1)
350: P_{13042} = (17, 22, 11, 1)
                                                                404: P_{14920} = (7, 17, 13, 1)
351: P_{13065} = (8, 23, 11, 1)
                                                                405: P_{14959} = (14, 18, 13, 1)
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406: P_{14972} = (27, 18, 13, 1)
                                                                460: P_{16892} = (27, 14, 15, 1)
407: P_{15074} = (1, 22, 13, 1)
                                                                461: P_{16930} = (1, 16, 15, 1)
408: P_{15078} = (5, 22, 13, 1)
                                                                462: P_{16940} = (11, 16, 15, 1)
409: P_{15123} = (18, 23, 13, 1)
                                                                463: P_{17095} = (6, 21, 15, 1)
410: P_{15132} = (27, 23, 13, 1)
                                                                464: P_{17115} = (26, 21, 15, 1)
411: P_{15155} = (18, 24, 13, 1)
                                                                465: P_{17182} = (29, 23, 15, 1)
412: P_{15163} = (26, 24, 13, 1)
                                                                466: P_{17184} = (31, 23, 15, 1)
413: P_{15185} = (16, 25, 13, 1)
                                                                467: P_{17195} = (10, 24, 15, 1)
414: P_{15190} = (21, 25, 13, 1)
                                                                468: P_{17208} = (23, 24, 15, 1)
415: P_{15233} = (0, 27, 13, 1)
                                                                469: P_{17229} = (12, 25, 15, 1)
416: P_{15264} = (31, 27, 13, 1)
                                                                470: P_{17247} = (30, 25, 15, 1)
417: P_{15310} = (13, 29, 13, 1)
                                                                471: P_{17340} = (27, 28, 15, 1)
418: P_{15322} = (25, 29, 13, 1)
                                                                472: P_{17344} = (31, 28, 15, 1)
419: P_{15502} = (13, 3, 14, 1)
                                                                473: P_{17366} = (21, 29, 15, 1)
420: P_{15519} = (30, 3, 14, 1)
                                                                474: P_{17375} = (30, 29, 15, 1)
421: P_{15535} = (14, 4, 14, 1)
                                                                475: P_{17409} = (0, 31, 15, 1)
422: P_{15539} = (18, 4, 14, 1)
                                                                476: P_{17430} = (21, 31, 15, 1)
423: P_{15564} = (11, 5, 14, 1)
                                                                477: P_{17547} = (10, 3, 16, 1)
424: P_{15578} = (25, 5, 14, 1)
                                                                478: P_{17567} = (30, 3, 16, 1)
425: P_{15597} = (12, 6, 14, 1)
                                                                479: P_{17576} = (7, 4, 16, 1)
426: P_{15657} = (8, 8, 14, 1)
                                                                480: P_{17581} = (12, 4, 16, 1)
427: P_{15671} = (22, 8, 14, 1)
                                                                481: P_{17604} = (3, 5, 16, 1)
428: P_{15689} = (8, 9, 14, 1)
                                                                482: P_{17625} = (24, 5, 16, 1)
429: P_{15705} = (24, 9, 14, 1)
                                                                483: P_{17808} = (15, 11, 16, 1)
430: P_{15798} = (21, 12, 14, 1)
                                                                484: P_{17857} = (0, 13, 16, 1)
431: P_{15799} = (22, 12, 14, 1)
                                                                485: P_{17872} = (15, 13, 16, 1)
432: P_{15906} = (1, 16, 14, 1)
                                                                486: P_{17989} = (4, 17, 16, 1)
433: P_{15932} = (27, 16, 14, 1)
                                                                487: P_{18009} = (24, 17, 16, 1)
434: P_{15950} = (13, 17, 14, 1)
                                                                488: P_{18097} = (16, 20, 16, 1)
                                                                489: P_{18103} = (22, 20, 16, 1)
435: P_{15962} = (25, 17, 14, 1)
436: P_{16017} = (16, 19, 14, 1)
                                                                490: P_{18149} = (4, 22, 16, 1)
437: P_{16025} = (24, 19, 14, 1)
                                                                491: P_{18152} = (7, 22, 16, 1)
438: P_{16108} = (11, 22, 14, 1)
                                                                492: P_{18189} = (12, 23, 16, 1)
439: P_{16113} = (16, 22, 14, 1)
                                                                493: P_{18208} = (31, 23, 16, 1)
                                                                494: P_{18215} = (6, 24, 16, 1)
440: P_{16188} = (27, 24, 14, 1)
441: P_{16191} = (30, 24, 14, 1)
                                                                495: P_{18239} = (30, 24, 16, 1)
442: P_{16237} = (12, 26, 14, 1)
                                                                496: P_{18279} = (6, 26, 16, 1)
443: P_{16246} = (21, 26, 14, 1)
                                                                497: P_{18300} = (27, 26, 16, 1)
                                                                498: P_{18327} = (22, 27, 16, 1)
444: P_{16325} = (4, 29, 14, 1)
445: P_{16339} = (18, 29, 14, 1)
                                                                499: P_{18332} = (27, 27, 16, 1)
446: P_{16353} = (0, 30, 14, 1)
                                                                500: P_{18350} = (13, 28, 16, 1)
447: P_{16357} = (4, 30, 14, 1)
                                                                501: P_{18368} = (31, 28, 16, 1)
448: P_{16483} = (2, 2, 15, 1)
                                                                502: P_{18370} = (1, 29, 16, 1)
449: P_{16510} = (29, 2, 15, 1)
                                                                503: P_{18372} = (3, 29, 16, 1)
450: P_{16515} = (2, 3, 15, 1)
                                                                504: P_{18443} = (10, 31, 16, 1)
451: P_{16531} = (18, 3, 15, 1)
                                                                505: P_{18446} = (13, 31, 16, 1)
452: P_{16560} = (15, 4, 15, 1)
                                                                506: P_{18673} = (16, 6, 17, 1)
453: P_{16568} = (23, 4, 15, 1)
                                                                507: P_{18681} = (24, 6, 17, 1)
454: P_{16685} = (12, 8, 15, 1)
                                                                508: P_{18703} = (14, 7, 17, 1)
455: P_{16699} = (26, 8, 15, 1)
                                                                509: P_{18712} = (23, 7, 17, 1)
456: P_{16716} = (11, 9, 15, 1)
                                                                510: P_{18730} = (9, 8, 17, 1)
457: P_{16723} = (18, 9, 15, 1)
                                                                511: P_{18741} = (20, 8, 17, 1)
458: P_{16839} = (6, 13, 15, 1)
                                                                512: P_{18758} = (5, 9, 17, 1)
459: P_{16875} = (10, 14, 15, 1)
                                                                513: P_{18762} = (9, 9, 17, 1)
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514: P_{18792} = (7, 10, 17, 1)
                                                                568: P_{20676} = (3, 5, 19, 1)
515: P_{18814} = (29, 10, 17, 1)
                                                                569: P_{20696} = (23, 5, 19, 1)
516: P_{18836} = (19, 11, 17, 1)
                                                                570: P_{20732} = (27, 6, 19, 1)
517: P_{18841} = (24, 11, 17, 1)
                                                                571: P_{20736} = (31, 6, 19, 1)
518: P_{18849} = (0, 12, 17, 1)
                                                                572: P_{20769} = (0, 8, 19, 1)
519: P_{18868} = (19, 12, 17, 1)
                                                                573: P_{20782} = (13, 8, 19, 1)
520: P_{18916} = (3, 14, 17, 1)
                                                                574: P_{20854} = (21, 10, 19, 1)
521: P_{18936} = (23, 14, 17, 1)
                                                                575: P_{20860} = (27, 10, 19, 1)
522: P_{19011} = (2, 17, 17, 1)
                                                                576: P_{20917} = (20, 12, 19, 1)
523: P_{19024} = (15, 17, 17, 1)
                                                                577: P_{20928} = (31, 12, 19, 1)
524: P_{19108} = (3, 20, 17, 1)
                                                                578: P_{20940} = (11, 13, 19, 1)
525: P_{19122} = (17, 20, 17, 1)
                                                                579: P_{20948} = (19, 13, 19, 1)
526: P_{19217} = (16, 23, 17, 1)
                                                                580: P_{20967} = (6, 14, 19, 1)
527: P_{19221} = (20, 23, 17, 1)
                                                                581: P_{20975} = (14, 14, 19, 1)
528: P_{19262} = (29, 24, 17, 1)
                                                                582: P_{21007} = (14, 15, 19, 1)
529: P_{19280} = (15, 25, 17, 1)
                                                                583: P_{21014} = (21, 15, 19, 1)
530: P_{19295} = (30, 25, 17, 1)
                                                                584: P_{21059} = (2, 17, 19, 1)
531: P_{19299} = (2, 26, 17, 1)
                                                                585: P_{21065} = (8, 17, 19, 1)
                                                                586: P_{21189} = (4, 21, 19, 1)
532: P_{19302} = (5, 26, 17, 1)
533: P_{19394} = (1, 29, 17, 1)
                                                                587: P_{21193} = (8, 21, 19, 1)
534: P_{19423} = (30, 29, 17, 1)
                                                                588: P_{21324} = (11, 25, 19, 1)
535: P_{19432} = (7, 30, 17, 1)
                                                                589: P_{21326} = (13, 25, 19, 1)
536: P_{19439} = (14, 30, 17, 1)
                                                                590: P_{21347} = (2, 26, 19, 1)
537: P_{19582} = (29, 2, 18, 1)
                                                                591: P_{21365} = (20, 26, 19, 1)
538: P_{19722} = (9, 7, 18, 1)
                                                                592: P_{21378} = (1, 27, 19, 1)
539: P_{19738} = (25, 7, 18, 1)
                                                                593: P_{21381} = (4, 27, 19, 1)
540: P_{19777} = (0, 9, 18, 1)
                                                                594: P_{21444} = (3, 29, 19, 1)
541: P_{19800} = (23, 9, 18, 1)
                                                                595: P_{21622} = (21, 2, 20, 1)
542: P_{19912} = (7, 13, 18, 1)
                                                                596: P_{21626} = (25, 2, 20, 1)
543: P_{19923} = (18, 13, 18, 1)
                                                                597: P_{21826} = (1, 9, 20, 1)
544: P_{19940} = (3, 14, 18, 1)
                                                                598: P_{21830} = (5, 9, 20, 1)
545: P_{19942} = (5, 14, 18, 1)
                                                                599: P_{21867} = (10, 10, 20, 1)
546: P_{19980} = (11, 15, 18, 1)
                                                                600: P_{21880} = (23, 10, 20, 1)
547: P_{20000} = (31, 15, 18, 1)
                                                                601: P_{21892} = (3, 11, 20, 1)
548: P_{20017} = (16, 16, 18, 1)
                                                                602: P_{21899} = (10, 11, 20, 1)
                                                                603: P_{22012} = (27, 14, 20, 1)
549: P_{20026} = (25, 16, 18, 1)
550: P_{20044} = (11, 17, 18, 1)
                                                                604: P_{22013} = (28, 14, 20, 1)
551: P_{20049} = (16, 17, 18, 1)
                                                                605: P_{22020} = (3, 15, 20, 1)
552: P_{20101} = (4, 19, 18, 1)
                                                                606: P_{22033} = (16, 15, 20, 1)
553: P_{20127} = (30, 19, 18, 1)
                                                                607: P_{22085} = (4, 17, 20, 1)
554: P_{20132} = (3, 20, 18, 1)
                                                                608: P_{22103} = (22, 17, 20, 1)
555: P_{20137} = (8, 20, 18, 1)
                                                                609: P_{22133} = (20, 18, 20, 1)
556: P_{20168} = (7, 21, 18, 1)
                                                                610: P_{22144} = (31, 18, 20, 1)
                                                                611: P_{22153} = (8, 19, 20, 1)
557: P_{20191} = (30, 21, 18, 1)
558: P_{20230} = (5, 23, 18, 1)
                                                                612: P_{22168} = (23, 19, 20, 1)
559: P_{20254} = (29, 23, 18, 1)
                                                                613: P_{22225} = (16, 21, 20, 1)
560: P_{20261} = (4, 24, 18, 1)
                                                                614: P_{22233} = (24, 21, 20, 1)
561: P_{20266} = (9, 24, 18, 1)
                                                                615: P_{22245} = (4, 22, 20, 1)
562: P_{20297} = (8, 25, 18, 1)
                                                                616: P_{22262} = (21, 22, 20, 1)
563: P_{20312} = (23, 25, 18, 1)
                                                                617: P_{22374} = (5, 26, 20, 1)
564: P_{20354} = (1, 27, 18, 1)
                                                                618: P_{22400} = (31, 26, 20, 1)
565: P_{20384} = (31, 27, 18, 1)
                                                                619: P_{22455} = (22, 28, 20, 1)
                                                                620: P_{22460} = (27, 28, 20, 1)
566: P_{20615} = (6, 3, 19, 1)
567: P_{20632} = (23, 3, 19, 1)
                                                                621: P_{22465} = (0, 29, 20, 1)
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622: P_{22490} = (25, 29, 20, 1)
                                                                676: P_{24342} = (21, 23, 22, 1)
623: P_{22521} = (24, 30, 20, 1)
                                                                677: P_{24348} = (27, 23, 22, 1)
624: P_{22537} = (8, 31, 20, 1)
                                                                678: P_{24357} = (4, 24, 22, 1)
625: P_{22557} = (28, 31, 20, 1)
                                                                679: P_{24359} = (6, 24, 22, 1)
626: P_{22642} = (17, 2, 21, 1)
                                                                680: P_{24385} = (0, 25, 22, 1)
627: P_{22656} = (31, 2, 21, 1)
                                                                681: P_{24405} = (20, 25, 22, 1)
628: P_{22663} = (6, 3, 21, 1)
                                                                682: P_{24423} = (6, 26, 22, 1)
629: P_{22686} = (29, 3, 21, 1)
                                                                683: P_{24430} = (13, 26, 22, 1)
630: P_{22819} = (2, 8, 21, 1)
                                                                684: P_{24552} = (7, 30, 22, 1)
631: P_{22843} = (26, 8, 21, 1)
                                                                685: P_{24575} = (30, 30, 22, 1)
632: P_{22850} = (1, 9, 21, 1)
                                                                686: P_{24594} = (17, 31, 22, 1)
633: P_{22861} = (12, 9, 21, 1)
                                                                687: P_{24607} = (30, 31, 22, 1)
634: P_{22984} = (7, 13, 21, 1)
                                                                688: P_{24695} = (22, 2, 23, 1)
635: P_{22997} = (20, 13, 21, 1)
                                                                689: P_{24701} = (28, 2, 23, 1)
                                                                690: P_{24744} = (7, 4, 23, 1)
636: P_{23015} = (6, 14, 21, 1)
637: P_{23024} = (15, 14, 21, 1)
                                                                691: P_{24753} = (16, 4, 23, 1)
638: P_{23056} = (15, 15, 21, 1)
                                                                692: P_{24794} = (25, 5, 23, 1)
639: P_{23060} = (19, 15, 21, 1)
                                                                693: P_{24867} = (2, 8, 23, 1)
640: P_{23086} = (13, 16, 21, 1)
                                                                694: P_{24875} = (10, 8, 23, 1)
641: P_{23100} = (27, 16, 21, 1)
                                                                695: P_{24964} = (3, 11, 23, 1)
642: P_{23149} = (12, 18, 21, 1)
                                                                696: P_{24984} = (23, 11, 23, 1)
643: P_{23158} = (21, 18, 21, 1)
                                                                697: P_{25062} = (5, 14, 23, 1)
644: P_{23224} = (23, 20, 21, 1)
                                                                698: P_{25073} = (16, 14, 23, 1)
645: P_{23232} = (31, 20, 21, 1)
                                                                699: P_{25090} = (1, 15, 23, 1)
646: P_{23240} = (7, 21, 21, 1)
                                                                700: P_{25092} = (3, 15, 23, 1)
647: P_{23259} = (26, 21, 21, 1)
                                                                701: P_{25130} = (9, 16, 23, 1)
648: P_{23349} = (20, 24, 21, 1)
                                                                702: P_{25147} = (26, 16, 23, 1)
649: P_{23356} = (27, 24, 21, 1)
                                                                703: P_{25178} = (25, 17, 23, 1)
650: P_{23422} = (29, 26, 21, 1)
                                                                704: P_{25182} = (29, 17, 23, 1)
651: P_{23427} = (2, 27, 21, 1)
                                                                705: P_{25195} = (10, 18, 23, 1)
652: P_{23448} = (23, 27, 21, 1)
                                                                706: P_{25203} = (18, 18, 23, 1)
653: P_{23457} = (0, 28, 21, 1)
                                                                707: P_{25235} = (18, 19, 23, 1)
654: P_{23474} = (17, 28, 21, 1)
                                                                708: P_{25246} = (29, 19, 23, 1)
655: P_{23534} = (13, 30, 21, 1)
                                                                709: P_{25285} = (4, 21, 23, 1)
656: P_{23540} = (19, 30, 21, 1)
                                                                710: P_{25303} = (22, 21, 23, 1)
                                                                711: P_{25320} = (7, 22, 23, 1)
657: P_{23754} = (9, 5, 22, 1)
658: P_{23757} = (12, 5, 22, 1)
                                                                712: P_{25322} = (9, 22, 23, 1)
659: P_{23790} = (13, 6, 22, 1)
                                                                713: P_{25350} = (5, 23, 23, 1)
660: P_{23800} = (23, 6, 22, 1)
                                                                714: P_{25373} = (28, 23, 23, 1)
661: P_{23862} = (21, 8, 22, 1)
                                                                715: P_{25377} = (0, 24, 23, 1)
662: P_{23887} = (14, 9, 22, 1)
                                                                716: P_{25403} = (26, 24, 23, 1)
663: P_{23897} = (24, 9, 22, 1)
                                                                717: P_{25475} = (2, 27, 23, 1)
664: P_{23912} = (7, 10, 22, 1)
                                                                718: P_{25477} = (4, 27, 23, 1)
665: P_{23919} = (14, 10, 22, 1)
                                                                719: P_{25701} = (4, 2, 24, 1)
666: P_{23946} = (9, 11, 22, 1)
                                                                720: P_{25713} = (16, 2, 24, 1)
667: P_{23959} = (22, 11, 22, 1)
                                                                721: P_{25784} = (23, 4, 24, 1)
668: P_{24066} = (1, 15, 22, 1)
                                                                722: P_{25786} = (25, 4, 24, 1)
669: P_{24077} = (12, 15, 22, 1)
                                                                723: P_{25857} = (0, 7, 24, 1)
670: P_{24117} = (20, 16, 22, 1)
                                                                724: P_{25860} = (3, 7, 24, 1)
671: P_{24120} = (23, 16, 22, 1)
                                                                725: P_{25898} = (9, 8, 24, 1)
672: P_{24178} = (17, 18, 22, 1)
                                                                726: P_{25911} = (22, 8, 24, 1)
673: P_{24188} = (27, 18, 22, 1)
                                                                727: P_{25930} = (9, 9, 24, 1)
674: P_{24197} = (4, 19, 22, 1)
                                                                728: P_{25935} = (14, 9, 24, 1)
675: P_{24217} = (24, 19, 22, 1)
                                                                729: P_{25957} = (4, 10, 24, 1)
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730: P_{25967} = (14, 10, 24, 1)
                                                                784: P_{27857} = (16, 5, 26, 1)
                                                                785: P_{27927} = (22, 7, 26, 1)
731: P_{26023} = (6, 12, 24, 1)
732: P_{26039} = (22, 12, 24, 1)
                                                                786: P_{27932} = (27, 7, 26, 1)
733: P_{26052} = (3, 13, 24, 1)
                                                                787: P_{27956} = (19, 8, 26, 1)
734: P_{26060} = (11, 13, 24, 1)
                                                                788: P_{27965} = (28, 8, 26, 1)
735: P_{26118} = (5, 15, 24, 1)
                                                                789: P_{28144} = (15, 14, 26, 1)
736: P_{26137} = (24, 15, 24, 1)
                                                                790: P_{28151} = (22, 14, 26, 1)
737: P_{26158} = (13, 16, 24, 1)
                                                                791: P_{28173} = (12, 15, 26, 1)
738: P_{26166} = (21, 16, 24, 1)
                                                                792: P_{28176} = (15, 15, 26, 1)
739: P_{26183} = (6, 17, 24, 1)
                                                                793: P_{28296} = (7, 19, 26, 1)
740: P_{26418} = (17, 24, 24, 1)
                                                                794: P_{28306} = (17, 19, 26, 1)
741: P_{26424} = (23, 24, 24, 1)
                                                                795: P_{28329} = (8, 20, 26, 1)
742: P_{26444} = (11, 25, 24, 1)
                                                                796: P_{28339} = (18, 20, 26, 1)
743: P_{26454} = (21, 25, 24, 1)
                                                                797: P_{28378} = (25, 21, 26, 1)
744: P_{26545} = (16, 28, 24, 1)
                                                                798: P_{28402} = (17, 22, 26, 1)
745: P_{26554} = (25, 28, 24, 1)
                                                                799: P_{28411} = (26, 22, 26, 1)
746: P_{26606} = (13, 30, 24, 1)
                                                                800: P_{28482} = (1, 25, 26, 1)
747: P_{26610} = (17, 30, 24, 1)
                                                                801: P_{28489} = (8, 25, 26, 1)
748: P_{26626} = (1, 31, 24, 1)
                                                                802: P_{28529} = (16, 26, 26, 1)
749: P_{26630} = (5, 31, 24, 1)
                                                                803: P_{28531} = (18, 26, 26, 1)
750: P_{26773} = (20, 3, 25, 1)
                                                                804: P_{28584} = (7, 28, 26, 1)
751: P_{26780} = (27, 3, 25, 1)
                                                                805: P_{28596} = (19, 28, 26, 1)
752: P_{26849} = (0, 6, 25, 1)
                                                                806: P_{28630} = (21, 29, 26, 1)
753: P_{26878} = (29, 6, 25, 1)
                                                                807: P_{28636} = (27, 29, 26, 1)
754: P_{26897} = (16, 7, 25, 1)
                                                                808: P_{28666} = (25, 30, 26, 1)
755: P_{26901} = (20, 7, 25, 1)
                                                                809: P_{28669} = (28, 30, 26, 1)
756: P_{26920} = (7, 8, 25, 1)
                                                                810: P_{28683} = (10, 31, 26, 1)
757: P_{26929} = (16, 8, 25, 1)
                                                                811: P_{28694} = (21, 31, 26, 1)
758: P_{26947} = (2, 9, 25, 1)
                                                                812: P_{28769} = (0, 2, 27, 1)
759: P_{26957} = (12, 9, 25, 1)
                                                                813: P_{28787} = (18, 2, 27, 1)
760: P_{27005} = (28, 10, 25, 1)
                                                                814: P_{28837} = (4, 4, 27, 1)
761: P_{27016} = (7, 11, 25, 1)
                                                                815: P_{28839} = (6, 4, 27, 1)
762: P_{27039} = (30, 11, 25, 1)
                                                                816: P_{28869} = (4, 5, 27, 1)
763: P_{27097} = (24, 13, 25, 1)
                                                                817: P_{28894} = (29, 5, 27, 1)
764: P_{27102} = (29, 13, 25, 1)
                                                                818: P_{28910} = (13, 6, 27, 1)
765: P_{27126} = (21, 14, 25, 1)
                                                                819: P_{28925} = (28, 6, 27, 1)
766: P_{27135} = (30, 14, 25, 1)
                                                                820: P_{28932} = (3, 7, 27, 1)
                                                                821: P_{28938} = (9, 7, 27, 1)
767: P_{27148} = (11, 15, 25, 1)
768: P_{27162} = (25, 15, 25, 1)
                                                                822: P_{28995} = (2, 9, 27, 1)
769: P_{27212} = (11, 17, 25, 1)
                                                                823: P_{29023} = (30, 9, 27, 1)
770: P_{27227} = (26, 17, 25, 1)
                                                                824: P_{29106} = (17, 12, 27, 1)
771: P_{27245} = (12, 18, 25, 1)
                                                                825: P_{29110} = (21, 12, 27, 1)
772: P_{27252} = (19, 18, 25, 1)
                                                                826: P_{29124} = (3, 13, 27, 1)
773: P_{27284} = (19, 19, 25, 1)
                                                                827: P_{29149} = (28, 13, 27, 1)
774: P_{27286} = (21, 19, 25, 1)
                                                                828: P_{29257} = (8, 17, 27, 1)
775: P_{27321} = (24, 20, 25, 1)
                                                                829: P_{29279} = (30, 17, 27, 1)
776: P_{27324} = (27, 20, 25, 1)
                                                                830: P_{29385} = (8, 21, 27, 1)
777: P_{27427} = (2, 24, 25, 1)
                                                                831: P_{29406} = (29, 21, 27, 1)
                                                                832: P_{29415} = (6, 22, 27, 1)
778: P_{27453} = (28, 24, 25, 1)
779: P_{27650} = (1, 31, 25, 1)
                                                                833: P_{29436} = (27, 22, 27, 1)
780: P_{27675} = (26, 31, 25, 1)
                                                                834: P_{29475} = (2, 24, 27, 1)
781: P_{27777} = (0, 3, 26, 1)
                                                                835: P_{29482} = (9, 24, 27, 1)
782: P_{27787} = (10, 3, 26, 1)
                                                                836: P_{29506} = (1, 25, 27, 1)
783: P_{27853} = (12, 5, 26, 1)
                                                                837: P_{29522} = (17, 25, 27, 1)
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838: P_{29550} = (13, 26, 27, 1)
                                                                892: P_{31463} = (6, 22, 29, 1)
839: P_{29558} = (21, 26, 27, 1)
                                                                893: P_{31491} = (2, 23, 29, 1)
840: P_{29715} = (18, 31, 27, 1)
                                                                894: P_{31514} = (25, 23, 29, 1)
841: P_{29797} = (4, 2, 28, 1)
                                                                895: P_{31569} = (16, 25, 29, 1)
842: P_{29817} = (24, 2, 28, 1)
                                                                896: P_{31581} = (28, 25, 29, 1)
843: P_{29847} = (22, 3, 28, 1)
                                                                897: P_{31656} = (7, 28, 29, 1)
844: P_{29869} = (12, 4, 28, 1)
                                                                898: P_{31662} = (13, 28, 29, 1)
845: P_{29875} = (18, 4, 28, 1)
                                                                899: P_{31715} = (2, 30, 29, 1)
846: P_{29909} = (20, 5, 28, 1)
                                                                900: P_{31736} = (23, 30, 29, 1)
847: P_{29911} = (22, 5, 28, 1)
                                                                901: P_{31750} = (5, 31, 29, 1)
848: P_{29955} = (2,7,28,1)
                                                                902: P_{31758} = (13, 31, 29, 1)
849: P_{29982} = (29, 7, 28, 1)
                                                                903: P_{31899} = (26, 3, 30, 1)
850: P_{30043} = (26, 9, 28, 1)
                                                                904: P_{31901} = (28, 3, 30, 1)
851: P_{30045} = (28, 9, 28, 1)
                                                                905: P_{31956} = (19, 5, 30, 1)
852: P_{30052} = (3, 10, 28, 1)
                                                                906: P_{31964} = (27, 5, 30, 1)
853: P_{30053} = (4, 10, 28, 1)
                                                                907: P_{32003} = (2, 7, 30, 1)
854: P_{30082} = (1, 11, 28, 1)
                                                                908: P_{32020} = (19, 7, 30, 1)
855: P_{30107} = (26, 11, 28, 1)
                                                                909: P_{32040} = (7, 8, 30, 1)
856: P_{30147} = (2, 13, 28, 1)
                                                                910: P_{32046} = (13, 8, 30, 1)
857: P_{30172} = (27, 13, 28, 1)
                                                                911: P_{32107} = (10, 10, 30, 1)
858: P_{30345} = (8, 19, 28, 1)
                                                                912: P_{32122} = (25, 10, 30, 1)
859: P_{30364} = (27, 19, 28, 1)
                                                                913: P_{32136} = (7, 11, 30, 1)
860: P_{30465} = (0, 23, 28, 1)
                                                                914: P_{32139} = (10, 11, 30, 1)
861: P_{30477} = (12, 23, 28, 1)
                                                                915: P_{32167} = (6, 12, 30, 1)
862: P_{30614} = (21, 27, 28, 1)
                                                                916: P_{32188} = (27, 12, 30, 1)
863: P_{30622} = (29, 27, 28, 1)
                                                                917: P_{32194} = (1, 13, 30, 1)
864: P_{30628} = (3, 28, 28, 1)
                                                                918: P_{32195} = (2, 13, 30, 1)
865: P_{30646} = (21, 28, 28, 1)
                                                                919: P_{32298} = (9, 16, 30, 1)
866: P_{30675} = (18, 29, 28, 1)
                                                                920: P_{32319} = (30, 16, 30, 1)
867: P_{30681} = (24, 29, 28, 1)
                                                                921: P_{32327} = (6, 17, 30, 1)
868: P_{30709} = (20, 30, 28, 1)
                                                                922: P_{32336} = (15, 17, 30, 1)
869: P_{30720} = (31, 30, 28, 1)
                                                                923: P_{32385} = (0, 19, 30, 1)
870: P_{30729} = (8, 31, 28, 1)
                                                                924: P_{32401} = (16, 19, 30, 1)
871: P_{30752} = (31, 31, 28, 1)
                                                                925: P_{32443} = (26, 20, 30, 1)
872: P_{30866} = (17, 3, 29, 1)
                                                                926: P_{32490} = (9, 22, 30, 1)
873: P_{30867} = (18, 3, 29, 1)
                                                                927: P_{32497} = (16, 22, 30, 1)
874: P_{30887} = (6, 4, 29, 1)
                                                                928: P_{32590} = (13, 25, 30, 1)
875: P_{30909} = (28, 4, 29, 1)
                                                                929: P_{32592} = (15, 25, 30, 1)
876: P_{31019} = (10, 8, 29, 1)
                                                                930: P_{32634} = (25, 26, 30, 1)
877: P_{31033} = (24, 8, 29, 1)
                                                                931: P_{32637} = (28, 26, 30, 1)
878: P_{31059} = (18, 9, 29, 1)
                                                                932: P_{32933} = (4, 4, 31, 1)
879: P_{31070} = (29, 9, 29, 1)
                                                                933: P_{32951} = (22, 4, 31, 1)
880: P_{31106} = (1, 11, 29, 1)
                                                                934: P_{32965} = (4, 5, 31, 1)
                                                                935: P_{32970} = (9, 5, 31, 1)
881: P_{31122} = (17, 11, 29, 1)
882: P_{31153} = (16, 12, 29, 1)
                                                                936: P_{33012} = (19, 6, 31, 1)
                                                                937: P_{33019} = (26, 6, 31, 1)
883: P_{31162} = (25, 12, 29, 1)
884: P_{31215} = (14, 14, 29, 1)
                                                                938: P_{33039} = (14, 7, 31, 1)
885: P_{31225} = (24, 14, 29, 1)
                                                                939: P_{33049} = (24, 7, 31, 1)
886: P_{31238} = (5, 15, 29, 1)
                                                                940: P_{33124} = (3, 10, 31, 1)
887: P_{31247} = (14, 15, 29, 1)
                                                                941: P_{33147} = (26, 10, 31, 1)
888: P_{31339} = (10, 18, 29, 1)
                                                                942: P_{33162} = (9, 11, 31, 1)
889: P_{31352} = (23, 18, 29, 1)
                                                                943: P_{33168} = (15, 11, 31, 1)
890: P_{31368} = (7, 19, 29, 1)
                                                                944: P_{33218} = (1, 13, 31, 1)
891: P_{31457} = (0, 22, 29, 1)
                                                                945: P_{33232} = (15, 13, 31, 1)
```

```
\begin{array}{lll} 946: \ P_{33337} = (24,16,31,1) & 954: \ P_{33587} = (18,24,31,1) \\ 947: \ P_{33344} = (31,16,31,1) & 955: \ P_{33591} = (22,24,31,1) \\ 948: \ P_{33377} = (0,18,31,1) & 956: \ P_{33685} = (20,27,31,1) \\ 949: \ P_{33405} = (28,18,31,1) & 957: \ P_{33700} = (3,28,31,1) \\ 950: \ P_{33524} = (19,22,31,1) & 958: \ P_{33717} = (20,28,31,1) \\ 951: \ P_{33533} = (28,22,31,1) & 959: \ P_{33763} = (2,30,31,1) \\ 952: \ P_{33539} = (2,23,31,1) & 960: \ P_{33775} = (14,30,31,1) \\ 953: \ P_{33555} = (18,23,31,1) & 960: \ P_{33775} = (14,30,31,1) \end{array}
```

# Line Intersection Graph

	01234
0	01100
1	10111
2	11000
3	01001
4	$\begin{array}{c} 0 & 1 & 2 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ \end{array}$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$
in point	$P_0$	$P_1$

Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$
in point	$P_0$	$P_{36}$	$P_2$	$P_2$

Line 2 intersects

Line	$\ell_0$	$\ell_1$
in point	$P_1$	$P_{36}$

Line 3 intersects

Line	$\ell_1$	$\ell_4$
in point	$P_2$	$P_2$

Line 4 intersects

Line	$\ell_1$	$\ell_3$
in point	$P_2$	$P_2$

The surface has 1121 points:

Too many to print.