

# Rank-65687 over GF(16)

January 15, 2021

## The equation

The equation of the surface is :

$$X_2^3 + X_0^2 X_1 + X_0 X_1^2 + X_0 X_1 X_2 = 0$$

( 0, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0 )  
The point rank of the equation over GF(16) is 554832405

## General information

Number of lines	16
Number of points	257
Number of singular points	17
Number of Eckardt points	0
Number of double points	0
Number of single points	256
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$17^{16}$
Type of lines on points	$16, 1^{256}$

## Singular Points

The surface has 17 singular points:

- |  |  |
|--|--|
| 0 : $P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$                                    | 9 : $P_{2457} = \mathbf{P}(\delta^3, \delta^3, \delta^3, 1) = \mathbf{P}(8, 8, 8, 1)$              |
| 1 : $P_4 = \mathbf{P}(1, 1, 1, 1) = \mathbf{P}(1, 1, 1, 1)$                                    | 10 : $P_{2730} = \mathbf{P}(\delta^4, \delta^4, \delta^4, 1) = \mathbf{P}(9, 9, 9, 1)$             |
| 2 : $P_{36} = \mathbf{P}(1, 1, 1, 0) = \mathbf{P}(1, 1, 1, 0)$                                 | 11 : $P_{3003} = \mathbf{P}(\delta^{10}, \delta^{10}, \delta^{10}, 1) = \mathbf{P}(10, 10, 10, 1)$ |
| 3 : $P_{819} = \mathbf{P}(\delta, \delta, \delta, 1) = \mathbf{P}(2, 2, 2, 1)$                 | 12 : $P_{3276} = \mathbf{P}(\delta^5, \delta^5, \delta^5, 1) = \mathbf{P}(11, 11, 11, 1)$          |
| 4 : $P_{1092} = \mathbf{P}(\delta^{12}, \delta^{12}, \delta^{12}, 1) = \mathbf{P}(3, 3, 3, 1)$ | 13 : $P_{3549} = \mathbf{P}(\delta^{14}, \delta^{14}, \delta^{14}, 1) = \mathbf{P}(12, 12, 12, 1)$ |
| 5 : $P_{1365} = \mathbf{P}(\delta^2, \delta^2, \delta^2, 1) = \mathbf{P}(4, 4, 4, 1)$          | 14 : $P_{3822} = \mathbf{P}(\delta^{11}, \delta^{11}, \delta^{11}, 1) = \mathbf{P}(13, 13, 13, 1)$ |
| 6 : $P_{1638} = \mathbf{P}(\delta^9, \delta^9, \delta^9, 1) = \mathbf{P}(5, 5, 5, 1)$          | 15 : $P_{4095} = \mathbf{P}(\delta^8, \delta^8, \delta^8, 1) = \mathbf{P}(14, 14, 14, 1)$          |
| 7 : $P_{1911} = \mathbf{P}(\delta^{13}, \delta^{13}, \delta^{13}, 1) = \mathbf{P}(6, 6, 6, 1)$ | 16 : $P_{4368} = \mathbf{P}(\delta^6, \delta^6, \delta^6, 1) = \mathbf{P}(15, 15, 15, 1)$          |
| 8 : $P_{2184} = \mathbf{P}(\delta^7, \delta^7, \delta^7, 1) = \mathbf{P}(7, 7, 7, 1)$          |  |

## The 16 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned}
\ell_0 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)_{289} \\
\ell_1 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69904} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69904} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)_{33} \\
\ell_2 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{545} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{545} = \mathbf{Pl}(0, 0, 0, 1, 1, 0)_{785} \\
\ell_3 &= \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4913} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4913} = \mathbf{Pl}(0, 1, 0, 1, 1, 0)_{801} \\
\ell_4 &= \begin{bmatrix} 1 & \delta^{12} & \delta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{57875} = \begin{bmatrix} 1 & 3 & 13 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{57875} = \mathbf{Pl}(0, 13, 0, 3, 1, 0)_{875} \\
\ell_5 &= \begin{bmatrix} 1 & \delta^6 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{52415} = \begin{bmatrix} 1 & 15 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{52415} = \mathbf{Pl}(0, 11, 0, 15, 1, 0)_{1245} \\
\ell_6 &= \begin{bmatrix} 1 & \delta^{12} & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{44771} = \begin{bmatrix} 1 & 3 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{44771} = \mathbf{Pl}(0, 10, 0, 3, 1, 0)_{872} \\
\ell_7 &= \begin{bmatrix} 1 & \delta^9 & \delta^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{32213} = \begin{bmatrix} 1 & 5 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{32213} = \mathbf{Pl}(0, 7, 0, 5, 1, 0)_{931} \\
\ell_8 &= \begin{bmatrix} 1 & \delta^3 & \delta^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{54872} = \begin{bmatrix} 1 & 8 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{54872} = \mathbf{Pl}(0, 12, 0, 8, 1, 0)_{1029} \\
\ell_9 &= \begin{bmatrix} 1 & \delta^9 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{49685} = \begin{bmatrix} 1 & 5 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{49685} = \mathbf{Pl}(0, 11, 0, 5, 1, 0)_{935} \\
\ell_{10} &= \begin{bmatrix} 1 & \delta^9 & \delta^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{54053} = \begin{bmatrix} 1 & 5 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{54053} = \mathbf{Pl}(0, 12, 0, 5, 1, 0)_{936} \\
\ell_{11} &= \begin{bmatrix} 1 & \delta^6 & \delta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{61151} = \begin{bmatrix} 1 & 15 & 13 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{61151} = \mathbf{Pl}(0, 13, 0, 15, 1, 0)_{1247} \\
\ell_{12} &= \begin{bmatrix} 1 & \delta^3 & \delta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{28664} = \begin{bmatrix} 1 & 8 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{28664} = \mathbf{Pl}(0, 6, 0, 8, 1, 0)_{1023} \\
\ell_{13} &= \begin{bmatrix} 1 & \delta^{12} & \delta^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{31667} = \begin{bmatrix} 1 & 3 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{31667} = \mathbf{Pl}(0, 7, 0, 3, 1, 0)_{869} \\
\ell_{14} &= \begin{bmatrix} 1 & \delta^6 & \delta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30575} = \begin{bmatrix} 1 & 15 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30575} = \mathbf{Pl}(0, 6, 0, 15, 1, 0)_{1240} \\
\ell_{15} &= \begin{bmatrix} 1 & \delta^3 & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{46136} = \begin{bmatrix} 1 & 8 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{46136} = \mathbf{Pl}(0, 10, 0, 8, 1, 0)_{1027}
\end{aligned}$$

Rank of lines: ( 272, 69904, 545, 4913, 57875, 52415, 44771, 32213, 54872, 49685, 54053, 61151, 28664, 31667, 30575, 46136 )

Rank of points on Klein quadric: ( 289, 33, 785, 801, 875, 1245, 872, 931, 1029, 935, 936, 1247, 1023, 869, 1240, 1027 )

## Eckardt Points

The surface has 0 Eckardt points:

## Double Points

The surface has 0 Double points:  
The double points on the surface are:

## Single Points

The surface has 256 single points:  
The single points on the surface are:

- |  |  |
|--|--|
| 0 : $P_0 = (1, 0, 0, 0)$ lies on line $\ell_0$           | 41 : $P_{359} = (5, 5, 0, 1)$ lies on line $\ell_2$      |
| 1 : $P_1 = (0, 1, 0, 0)$ lies on line $\ell_1$           | 42 : $P_{370} = (0, 6, 0, 1)$ lies on line $\ell_1$      |
| 2 : $P_4 = (1, 1, 1, 1)$ lies on line $\ell_3$           | 43 : $P_{376} = (6, 6, 0, 1)$ lies on line $\ell_2$      |
| 3 : $P_5 = (1, 1, 0, 0)$ lies on line $\ell_2$           | 44 : $P_{386} = (0, 7, 0, 1)$ lies on line $\ell_1$      |
| 4 : $P_{36} = (1, 1, 1, 0)$ lies on line $\ell_3$        | 45 : $P_{393} = (7, 7, 0, 1)$ lies on line $\ell_2$      |
| 5 : $P_{60} = (9, 2, 1, 0)$ lies on line $\ell_4$        | 46 : $P_{402} = (0, 8, 0, 1)$ lies on line $\ell_1$      |
| 6 : $P_{61} = (10, 2, 1, 0)$ lies on line $\ell_5$       | 47 : $P_{410} = (8, 8, 0, 1)$ lies on line $\ell_2$      |
| 7 : $P_{94} = (11, 4, 1, 0)$ lies on line $\ell_6$       | 48 : $P_{418} = (0, 9, 0, 1)$ lies on line $\ell_1$      |
| 8 : $P_{97} = (14, 4, 1, 0)$ lies on line $\ell_7$       | 49 : $P_{427} = (9, 9, 0, 1)$ lies on line $\ell_2$      |
| 9 : $P_{165} = (2, 9, 1, 0)$ lies on line $\ell_8$       | 50 : $P_{434} = (0, 10, 0, 1)$ lies on line $\ell_1$     |
| 10 : $P_{173} = (10, 9, 1, 0)$ lies on line $\ell_9$     | 51 : $P_{444} = (10, 10, 0, 1)$ lies on line $\ell_2$    |
| 11 : $P_{181} = (2, 10, 1, 0)$ lies on line $\ell_{10}$  | 52 : $P_{450} = (0, 11, 0, 1)$ lies on line $\ell_1$     |
| 12 : $P_{188} = (9, 10, 1, 0)$ lies on line $\ell_{11}$  | 53 : $P_{461} = (11, 11, 0, 1)$ lies on line $\ell_2$    |
| 13 : $P_{199} = (4, 11, 1, 0)$ lies on line $\ell_{12}$  | 54 : $P_{466} = (0, 12, 0, 1)$ lies on line $\ell_1$     |
| 14 : $P_{209} = (14, 11, 1, 0)$ lies on line $\ell_{13}$ | 55 : $P_{478} = (12, 12, 0, 1)$ lies on line $\ell_2$    |
| 15 : $P_{247} = (4, 14, 1, 0)$ lies on line $\ell_{14}$  | 56 : $P_{482} = (0, 13, 0, 1)$ lies on line $\ell_1$     |
| 16 : $P_{254} = (11, 14, 1, 0)$ lies on line $\ell_{15}$ | 57 : $P_{495} = (13, 13, 0, 1)$ lies on line $\ell_2$    |
| 17 : $P_{275} = (1, 0, 0, 1)$ lies on line $\ell_0$      | 58 : $P_{498} = (0, 14, 0, 1)$ lies on line $\ell_1$     |
| 18 : $P_{276} = (2, 0, 0, 1)$ lies on line $\ell_0$      | 59 : $P_{512} = (14, 14, 0, 1)$ lies on line $\ell_2$    |
| 19 : $P_{277} = (3, 0, 0, 1)$ lies on line $\ell_0$      | 60 : $P_{514} = (0, 15, 0, 1)$ lies on line $\ell_1$     |
| 20 : $P_{278} = (4, 0, 0, 1)$ lies on line $\ell_0$      | 61 : $P_{529} = (15, 15, 0, 1)$ lies on line $\ell_2$    |
| 21 : $P_{279} = (5, 0, 0, 1)$ lies on line $\ell_0$      | 62 : $P_{570} = (9, 2, 1, 1)$ lies on line $\ell_4$      |
| 22 : $P_{280} = (6, 0, 0, 1)$ lies on line $\ell_0$      | 63 : $P_{571} = (10, 2, 1, 1)$ lies on line $\ell_5$     |
| 23 : $P_{281} = (7, 0, 0, 1)$ lies on line $\ell_0$      | 64 : $P_{604} = (11, 4, 1, 1)$ lies on line $\ell_6$     |
| 24 : $P_{282} = (8, 0, 0, 1)$ lies on line $\ell_0$      | 65 : $P_{607} = (14, 4, 1, 1)$ lies on line $\ell_7$     |
| 25 : $P_{283} = (9, 0, 0, 1)$ lies on line $\ell_0$      | 66 : $P_{675} = (2, 9, 1, 1)$ lies on line $\ell_8$      |
| 26 : $P_{284} = (10, 0, 0, 1)$ lies on line $\ell_0$     | 67 : $P_{683} = (10, 9, 1, 1)$ lies on line $\ell_9$     |
| 27 : $P_{285} = (11, 0, 0, 1)$ lies on line $\ell_0$     | 68 : $P_{691} = (2, 10, 1, 1)$ lies on line $\ell_{10}$  |
| 28 : $P_{286} = (12, 0, 0, 1)$ lies on line $\ell_0$     | 69 : $P_{698} = (9, 10, 1, 1)$ lies on line $\ell_{11}$  |
| 29 : $P_{287} = (13, 0, 0, 1)$ lies on line $\ell_0$     | 70 : $P_{709} = (4, 11, 1, 1)$ lies on line $\ell_{12}$  |
| 30 : $P_{288} = (14, 0, 0, 1)$ lies on line $\ell_0$     | 71 : $P_{719} = (14, 11, 1, 1)$ lies on line $\ell_{13}$ |
| 31 : $P_{289} = (15, 0, 0, 1)$ lies on line $\ell_0$     | 72 : $P_{757} = (4, 14, 1, 1)$ lies on line $\ell_{14}$  |
| 32 : $P_{290} = (0, 1, 0, 1)$ lies on line $\ell_1$      | 73 : $P_{764} = (11, 14, 1, 1)$ lies on line $\ell_{15}$ |
| 33 : $P_{291} = (1, 1, 0, 1)$ lies on line $\ell_2$      | 74 : $P_{819} = (2, 2, 2, 1)$ lies on line $\ell_3$      |
| 34 : $P_{306} = (0, 2, 0, 1)$ lies on line $\ell_1$      | 75 : $P_{860} = (11, 4, 2, 1)$ lies on line $\ell_4$     |
| 35 : $P_{308} = (2, 2, 0, 1)$ lies on line $\ell_2$      | 76 : $P_{862} = (13, 4, 2, 1)$ lies on line $\ell_5$     |
| 36 : $P_{322} = (0, 3, 0, 1)$ lies on line $\ell_1$      | 77 : $P_{873} = (8, 5, 2, 1)$ lies on line $\ell_{14}$   |
| 37 : $P_{325} = (3, 3, 0, 1)$ lies on line $\ell_2$      | 78 : $P_{880} = (15, 5, 2, 1)$ lies on line $\ell_{15}$  |
| 38 : $P_{338} = (0, 4, 0, 1)$ lies on line $\ell_1$      | 79 : $P_{918} = (5, 8, 2, 1)$ lies on line $\ell_7$      |
| 39 : $P_{342} = (4, 4, 0, 1)$ lies on line $\ell_2$      | 80 : $P_{928} = (15, 8, 2, 1)$ lies on line $\ell_6$     |
| 40 : $P_{354} = (0, 5, 0, 1)$ lies on line $\ell_1$      | 81 : $P_{965} = (4, 11, 2, 1)$ lies on line $\ell_8$     |

82 :  $P_{974} = (13, 11, 2, 1)$  lies on line  $\ell_9$   
 83 :  $P_{997} = (4, 13, 2, 1)$  lies on line  $\ell_{10}$   
 84 :  $P_{1004} = (11, 13, 2, 1)$  lies on line  $\ell_{11}$   
 85 :  $P_{1030} = (5, 15, 2, 1)$  lies on line  $\ell_{13}$   
 86 :  $P_{1033} = (8, 15, 2, 1)$  lies on line  $\ell_{12}$   
 87 :  $P_{1079} = (6, 2, 3, 1)$  lies on line  $\ell_8$   
 88 :  $P_{1080} = (7, 2, 3, 1)$  lies on line  $\ell_9$   
 89 :  $P_{1092} = (3, 3, 3, 1)$  lies on line  $\ell_3$   
 90 :  $P_{1116} = (11, 4, 3, 1)$  lies on line  $\ell_{13}$   
 91 :  $P_{1117} = (12, 4, 3, 1)$  lies on line  $\ell_{12}$   
 92 :  $P_{1139} = (2, 6, 3, 1)$  lies on line  $\ell_4$   
 93 :  $P_{1144} = (7, 6, 3, 1)$  lies on line  $\ell_5$   
 94 :  $P_{1155} = (2, 7, 3, 1)$  lies on line  $\ell_{11}$   
 95 :  $P_{1159} = (6, 7, 3, 1)$  lies on line  $\ell_{10}$   
 96 :  $P_{1221} = (4, 11, 3, 1)$  lies on line  $\ell_{15}$   
 97 :  $P_{1229} = (12, 11, 3, 1)$  lies on line  $\ell_{14}$   
 98 :  $P_{1237} = (4, 12, 3, 1)$  lies on line  $\ell_6$   
 99 :  $P_{1244} = (11, 12, 3, 1)$  lies on line  $\ell_7$   
 100 :  $P_{1353} = (8, 3, 4, 1)$  lies on line  $\ell_{10}$   
 101 :  $P_{1360} = (15, 3, 4, 1)$  lies on line  $\ell_{11}$   
 102 :  $P_{1365} = (4, 4, 4, 1)$  lies on line  $\ell_3$   
 103 :  $P_{1418} = (9, 7, 4, 1)$  lies on line  $\ell_{12}$   
 104 :  $P_{1419} = (10, 7, 4, 1)$  lies on line  $\ell_{13}$   
 105 :  $P_{1428} = (3, 8, 4, 1)$  lies on line  $\ell_5$   
 106 :  $P_{1440} = (15, 8, 4, 1)$  lies on line  $\ell_4$   
 107 :  $P_{1448} = (7, 9, 4, 1)$  lies on line  $\ell_6$   
 108 :  $P_{1451} = (10, 9, 4, 1)$  lies on line  $\ell_7$   
 109 :  $P_{1464} = (7, 10, 4, 1)$  lies on line  $\ell_{15}$   
 110 :  $P_{1466} = (9, 10, 4, 1)$  lies on line  $\ell_{14}$   
 111 :  $P_{1540} = (3, 15, 4, 1)$  lies on line  $\ell_9$   
 112 :  $P_{1545} = (8, 15, 4, 1)$  lies on line  $\ell_8$   
 113 :  $P_{1629} = (12, 4, 5, 1)$  lies on line  $\ell_{15}$   
 114 :  $P_{1630} = (13, 4, 5, 1)$  lies on line  $\ell_{14}$   
 115 :  $P_{1638} = (5, 5, 5, 1)$  lies on line  $\ell_3$   
 116 :  $P_{1658} = (9, 6, 5, 1)$  lies on line  $\ell_9$   
 117 :  $P_{1659} = (10, 6, 5, 1)$  lies on line  $\ell_8$   
 118 :  $P_{1703} = (6, 9, 5, 1)$  lies on line  $\ell_{11}$   
 119 :  $P_{1707} = (10, 9, 5, 1)$  lies on line  $\ell_{10}$   
 120 :  $P_{1719} = (6, 10, 5, 1)$  lies on line  $\ell_4$   
 121 :  $P_{1722} = (9, 10, 5, 1)$  lies on line  $\ell_5$   
 122 :  $P_{1749} = (4, 12, 5, 1)$  lies on line  $\ell_{13}$   
 123 :  $P_{1758} = (13, 12, 5, 1)$  lies on line  $\ell_{12}$   
 124 :  $P_{1765} = (4, 13, 5, 1)$  lies on line  $\ell_7$   
 125 :  $P_{1773} = (12, 13, 5, 1)$  lies on line  $\ell_6$   
 126 :  $P_{1833} = (8, 1, 6, 1)$  lies on line  $\ell_6$   
 127 :  $P_{1840} = (15, 1, 6, 1)$  lies on line  $\ell_7$   
 128 :  $P_{1885} = (12, 4, 6, 1)$  lies on line  $\ell_8$   
 129 :  $P_{1887} = (14, 4, 6, 1)$  lies on line  $\ell_9$   
 130 :  $P_{1911} = (6, 6, 6, 1)$  lies on line  $\ell_3$   
 131 :  $P_{1938} = (1, 8, 6, 1)$  lies on line  $\ell_{12}$   
 132 :  $P_{1952} = (15, 8, 6, 1)$  lies on line  $\ell_{13}$   
 133 :  $P_{2005} = (4, 12, 6, 1)$  lies on line  $\ell_4$   
 134 :  $P_{2015} = (14, 12, 6, 1)$  lies on line  $\ell_5$   
 135 :  $P_{2037} = (4, 14, 6, 1)$  lies on line  $\ell_{11}$

136 :  $P_{2045} = (12, 14, 6, 1)$  lies on line  $\ell_{10}$   
 137 :  $P_{2050} = (1, 15, 6, 1)$  lies on line  $\ell_{14}$   
 138 :  $P_{2057} = (8, 15, 6, 1)$  lies on line  $\ell_{15}$   
 139 :  $P_{2084} = (3, 1, 7, 1)$  lies on line  $\ell_{15}$   
 140 :  $P_{2086} = (5, 1, 7, 1)$  lies on line  $\ell_{14}$   
 141 :  $P_{2114} = (1, 3, 7, 1)$  lies on line  $\ell_{13}$   
 142 :  $P_{2118} = (5, 3, 7, 1)$  lies on line  $\ell_{12}$   
 143 :  $P_{2142} = (13, 4, 7, 1)$  lies on line  $\ell_{11}$   
 144 :  $P_{2143} = (14, 4, 7, 1)$  lies on line  $\ell_{10}$   
 145 :  $P_{2146} = (1, 5, 7, 1)$  lies on line  $\ell_7$   
 146 :  $P_{2148} = (3, 5, 7, 1)$  lies on line  $\ell_6$   
 147 :  $P_{2184} = (7, 7, 7, 1)$  lies on line  $\ell_3$   
 148 :  $P_{2277} = (4, 13, 7, 1)$  lies on line  $\ell_9$   
 149 :  $P_{2287} = (14, 13, 7, 1)$  lies on line  $\ell_8$   
 150 :  $P_{2293} = (4, 14, 7, 1)$  lies on line  $\ell_5$   
 151 :  $P_{2302} = (13, 14, 7, 1)$  lies on line  $\ell_4$   
 152 :  $P_{2424} = (7, 6, 8, 1)$  lies on line  $\ell_{11}$   
 153 :  $P_{2426} = (9, 6, 8, 1)$  lies on line  $\ell_{10}$   
 154 :  $P_{2439} = (6, 7, 8, 1)$  lies on line  $\ell_9$   
 155 :  $P_{2442} = (9, 7, 8, 1)$  lies on line  $\ell_8$   
 156 :  $P_{2457} = (8, 8, 8, 1)$  lies on line  $\ell_3$   
 157 :  $P_{2471} = (6, 9, 8, 1)$  lies on line  $\ell_5$   
 158 :  $P_{2472} = (7, 9, 8, 1)$  lies on line  $\ell_4$   
 159 :  $P_{2510} = (13, 11, 8, 1)$  lies on line  $\ell_7$   
 160 :  $P_{2511} = (14, 11, 8, 1)$  lies on line  $\ell_6$   
 161 :  $P_{2540} = (11, 13, 8, 1)$  lies on line  $\ell_{14}$   
 162 :  $P_{2543} = (14, 13, 8, 1)$  lies on line  $\ell_{15}$   
 163 :  $P_{2556} = (11, 14, 8, 1)$  lies on line  $\ell_{12}$   
 164 :  $P_{2558} = (13, 14, 8, 1)$  lies on line  $\ell_{13}$   
 165 :  $P_{2630} = (5, 3, 9, 1)$  lies on line  $\ell_{15}$   
 166 :  $P_{2640} = (15, 3, 9, 1)$  lies on line  $\ell_{14}$   
 167 :  $P_{2660} = (3, 5, 9, 1)$  lies on line  $\ell_{13}$   
 168 :  $P_{2672} = (15, 5, 9, 1)$  lies on line  $\ell_{12}$   
 169 :  $P_{2730} = (9, 9, 9, 1)$  lies on line  $\ell_3$   
 170 :  $P_{2765} = (12, 11, 9, 1)$  lies on line  $\ell_5$   
 171 :  $P_{2767} = (14, 11, 9, 1)$  lies on line  $\ell_4$   
 172 :  $P_{2780} = (11, 12, 9, 1)$  lies on line  $\ell_{10}$   
 173 :  $P_{2783} = (14, 12, 9, 1)$  lies on line  $\ell_{11}$   
 174 :  $P_{2812} = (11, 14, 9, 1)$  lies on line  $\ell_8$   
 175 :  $P_{2813} = (12, 14, 9, 1)$  lies on line  $\ell_9$   
 176 :  $P_{2820} = (3, 15, 9, 1)$  lies on line  $\ell_7$   
 177 :  $P_{2822} = (5, 15, 9, 1)$  lies on line  $\ell_6$   
 178 :  $P_{2852} = (3, 1, 10, 1)$  lies on line  $\ell_{12}$   
 179 :  $P_{2857} = (8, 1, 10, 1)$  lies on line  $\ell_{13}$   
 180 :  $P_{2882} = (1, 3, 10, 1)$  lies on line  $\ell_6$   
 181 :  $P_{2889} = (8, 3, 10, 1)$  lies on line  $\ell_7$   
 182 :  $P_{2962} = (1, 8, 10, 1)$  lies on line  $\ell_{15}$   
 183 :  $P_{2964} = (3, 8, 10, 1)$  lies on line  $\ell_{14}$   
 184 :  $P_{3003} = (10, 10, 10, 1)$  lies on line  $\ell_3$   
 185 :  $P_{3021} = (12, 11, 10, 1)$  lies on line  $\ell_{11}$   
 186 :  $P_{3022} = (13, 11, 10, 1)$  lies on line  $\ell_{10}$   
 187 :  $P_{3036} = (11, 12, 10, 1)$  lies on line  $\ell_9$   
 188 :  $P_{3038} = (13, 12, 10, 1)$  lies on line  $\ell_8$   
 189 :  $P_{3052} = (11, 13, 10, 1)$  lies on line  $\ell_5$

190 :  $P_{3053} = (12, 13, 10, 1)$  lies on line  $\ell_4$   
 191 :  $P_{3110} = (5, 1, 11, 1)$  lies on line  $\ell_{11}$   
 192 :  $P_{3120} = (15, 1, 11, 1)$  lies on line  $\ell_{10}$   
 193 :  $P_{3170} = (1, 5, 11, 1)$  lies on line  $\ell_9$   
 194 :  $P_{3184} = (15, 5, 11, 1)$  lies on line  $\ell_8$   
 195 :  $P_{3192} = (7, 6, 11, 1)$  lies on line  $\ell_{14}$   
 196 :  $P_{3195} = (10, 6, 11, 1)$  lies on line  $\ell_{15}$   
 197 :  $P_{3207} = (6, 7, 11, 1)$  lies on line  $\ell_7$   
 198 :  $P_{3211} = (10, 7, 11, 1)$  lies on line  $\ell_6$   
 199 :  $P_{3255} = (6, 10, 11, 1)$  lies on line  $\ell_{13}$   
 200 :  $P_{3256} = (7, 10, 11, 1)$  lies on line  $\ell_{12}$   
 201 :  $P_{3276} = (11, 11, 11, 1)$  lies on line  $\ell_3$   
 202 :  $P_{3330} = (1, 15, 11, 1)$  lies on line  $\ell_5$   
 203 :  $P_{3334} = (5, 15, 11, 1)$  lies on line  $\ell_4$   
 204 :  $P_{3366} = (5, 1, 12, 1)$  lies on line  $\ell_5$   
 205 :  $P_{3369} = (8, 1, 12, 1)$  lies on line  $\ell_4$   
 206 :  $P_{3384} = (7, 2, 12, 1)$  lies on line  $\ell_7$   
 207 :  $P_{3386} = (9, 2, 12, 1)$  lies on line  $\ell_6$   
 208 :  $P_{3426} = (1, 5, 12, 1)$  lies on line  $\ell_{10}$   
 209 :  $P_{3433} = (8, 5, 12, 1)$  lies on line  $\ell_{11}$   
 210 :  $P_{3459} = (2, 7, 12, 1)$  lies on line  $\ell_{14}$   
 211 :  $P_{3466} = (9, 7, 12, 1)$  lies on line  $\ell_{15}$   
 212 :  $P_{3474} = (1, 8, 12, 1)$  lies on line  $\ell_8$   
 213 :  $P_{3478} = (5, 8, 12, 1)$  lies on line  $\ell_9$   
 214 :  $P_{3491} = (2, 9, 12, 1)$  lies on line  $\ell_{12}$   
 215 :  $P_{3496} = (7, 9, 12, 1)$  lies on line  $\ell_{13}$   
 216 :  $P_{3549} = (12, 12, 12, 1)$  lies on line  $\ell_3$   
 217 :  $P_{3620} = (3, 1, 13, 1)$  lies on line  $\ell_8$   
 218 :  $P_{3632} = (15, 1, 13, 1)$  lies on line  $\ell_9$   
 219 :  $P_{3639} = (6, 2, 13, 1)$  lies on line  $\ell_{12}$   
 220 :  $P_{3642} = (9, 2, 13, 1)$  lies on line  $\ell_{13}$   
 221 :  $P_{3650} = (1, 3, 13, 1)$  lies on line  $\ell_4$   
 222 :  $P_{3664} = (15, 3, 13, 1)$  lies on line  $\ell_5$   
 223 :  $P_{3699} = (2, 6, 13, 1)$  lies on line  $\ell_6$

224 :  $P_{3706} = (9, 6, 13, 1)$  lies on line  $\ell_7$   
 225 :  $P_{3747} = (2, 9, 13, 1)$  lies on line  $\ell_{15}$   
 226 :  $P_{3751} = (6, 9, 13, 1)$  lies on line  $\ell_{14}$   
 227 :  $P_{3822} = (13, 13, 13, 1)$  lies on line  $\ell_3$   
 228 :  $P_{3842} = (1, 15, 13, 1)$  lies on line  $\ell_{11}$   
 229 :  $P_{3844} = (3, 15, 13, 1)$  lies on line  $\ell_{10}$   
 230 :  $P_{3895} = (6, 2, 14, 1)$  lies on line  $\ell_{15}$   
 231 :  $P_{3899} = (10, 2, 14, 1)$  lies on line  $\ell_{14}$   
 232 :  $P_{3910} = (5, 3, 14, 1)$  lies on line  $\ell_8$   
 233 :  $P_{3913} = (8, 3, 14, 1)$  lies on line  $\ell_9$   
 234 :  $P_{3940} = (3, 5, 14, 1)$  lies on line  $\ell_4$   
 235 :  $P_{3945} = (8, 5, 14, 1)$  lies on line  $\ell_5$   
 236 :  $P_{3955} = (2, 6, 14, 1)$  lies on line  $\ell_{13}$   
 237 :  $P_{3963} = (10, 6, 14, 1)$  lies on line  $\ell_{12}$   
 238 :  $P_{3988} = (3, 8, 14, 1)$  lies on line  $\ell_{11}$   
 239 :  $P_{3990} = (5, 8, 14, 1)$  lies on line  $\ell_{10}$   
 240 :  $P_{4019} = (2, 10, 14, 1)$  lies on line  $\ell_7$   
 241 :  $P_{4023} = (6, 10, 14, 1)$  lies on line  $\ell_6$   
 242 :  $P_{4095} = (14, 14, 14, 1)$  lies on line  $\ell_3$   
 243 :  $P_{4152} = (7, 2, 15, 1)$  lies on line  $\ell_{10}$   
 244 :  $P_{4155} = (10, 2, 15, 1)$  lies on line  $\ell_{11}$   
 245 :  $P_{4227} = (2, 7, 15, 1)$  lies on line  $\ell_5$   
 246 :  $P_{4235} = (10, 7, 15, 1)$  lies on line  $\ell_4$   
 247 :  $P_{4275} = (2, 10, 15, 1)$  lies on line  $\ell_9$   
 248 :  $P_{4280} = (7, 10, 15, 1)$  lies on line  $\ell_8$   
 249 :  $P_{4318} = (13, 12, 15, 1)$  lies on line  $\ell_{15}$   
 250 :  $P_{4319} = (14, 12, 15, 1)$  lies on line  $\ell_{14}$   
 251 :  $P_{4333} = (12, 13, 15, 1)$  lies on line  $\ell_{13}$   
 252 :  $P_{4335} = (14, 13, 15, 1)$  lies on line  $\ell_{12}$   
 253 :  $P_{4349} = (12, 14, 15, 1)$  lies on line  $\ell_7$   
 254 :  $P_{4350} = (13, 14, 15, 1)$  lies on line  $\ell_6$   
 255 :  $P_{4368} = (15, 15, 15, 1)$  lies on line  $\ell_3$

The single points on the surface are:

#### Points on surface but on no line

The surface has 0 points not on any line:

The points on the surface but not on lines are:

## Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
3	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1
4	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
5	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
6	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
7	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
8	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
9	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1
10	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
11	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
12	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
13	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
14	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
15	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 3 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 4 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 5 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 6 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 7 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 8 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 9 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 10 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 11 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 12 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 13 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 14 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 15 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

The surface has 257 points:

The points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$	14 : $P_{199} = (4, 11, 1, 0)$	28 : $P_{285} = (11, 0, 0, 1)$
1 : $P_1 = (0, 1, 0, 0)$	15 : $P_{209} = (14, 11, 1, 0)$	29 : $P_{286} = (12, 0, 0, 1)$
2 : $P_3 = (0, 0, 0, 1)$	16 : $P_{247} = (4, 14, 1, 0)$	30 : $P_{287} = (13, 0, 0, 1)$
3 : $P_4 = (1, 1, 1, 1)$	17 : $P_{254} = (11, 14, 1, 0)$	31 : $P_{288} = (14, 0, 0, 1)$
4 : $P_5 = (1, 1, 0, 0)$	18 : $P_{275} = (1, 0, 0, 1)$	32 : $P_{289} = (15, 0, 0, 1)$
5 : $P_{36} = (1, 1, 1, 0)$	19 : $P_{276} = (2, 0, 0, 1)$	33 : $P_{290} = (0, 1, 0, 1)$
6 : $P_{60} = (9, 2, 1, 0)$	20 : $P_{277} = (3, 0, 0, 1)$	34 : $P_{291} = (1, 1, 0, 1)$
7 : $P_{61} = (10, 2, 1, 0)$	21 : $P_{278} = (4, 0, 0, 1)$	35 : $P_{306} = (0, 2, 0, 1)$
8 : $P_{94} = (11, 4, 1, 0)$	22 : $P_{279} = (5, 0, 0, 1)$	36 : $P_{308} = (2, 2, 0, 1)$
9 : $P_{97} = (14, 4, 1, 0)$	23 : $P_{280} = (6, 0, 0, 1)$	37 : $P_{322} = (0, 3, 0, 1)$
10 : $P_{165} = (2, 9, 1, 0)$	24 : $P_{281} = (7, 0, 0, 1)$	38 : $P_{325} = (3, 3, 0, 1)$
11 : $P_{173} = (10, 9, 1, 0)$	25 : $P_{282} = (8, 0, 0, 1)$	39 : $P_{338} = (0, 4, 0, 1)$
12 : $P_{181} = (2, 10, 1, 0)$	26 : $P_{283} = (9, 0, 0, 1)$	40 : $P_{342} = (4, 4, 0, 1)$
13 : $P_{188} = (9, 10, 1, 0)$	27 : $P_{284} = (10, 0, 0, 1)$	41 : $P_{354} = (0, 5, 0, 1)$

42 : $P_{359} = (5, 5, 0, 1)$	96 : $P_{1159} = (6, 7, 3, 1)$	150 : $P_{2287} = (14, 13, 7, 1)$
43 : $P_{370} = (0, 6, 0, 1)$	97 : $P_{1221} = (4, 11, 3, 1)$	151 : $P_{2293} = (4, 14, 7, 1)$
44 : $P_{376} = (6, 6, 0, 1)$	98 : $P_{1229} = (12, 11, 3, 1)$	152 : $P_{2302} = (13, 14, 7, 1)$
45 : $P_{386} = (0, 7, 0, 1)$	99 : $P_{1237} = (4, 12, 3, 1)$	153 : $P_{2424} = (7, 6, 8, 1)$
46 : $P_{393} = (7, 7, 0, 1)$	100 : $P_{1244} = (11, 12, 3, 1)$	154 : $P_{2426} = (9, 6, 8, 1)$
47 : $P_{402} = (0, 8, 0, 1)$	101 : $P_{1353} = (8, 3, 4, 1)$	155 : $P_{2439} = (6, 7, 8, 1)$
48 : $P_{410} = (8, 8, 0, 1)$	102 : $P_{1360} = (15, 3, 4, 1)$	156 : $P_{2442} = (9, 7, 8, 1)$
49 : $P_{418} = (0, 9, 0, 1)$	103 : $P_{1365} = (4, 4, 4, 1)$	157 : $P_{2457} = (8, 8, 8, 1)$
50 : $P_{427} = (9, 9, 0, 1)$	104 : $P_{1418} = (9, 7, 4, 1)$	158 : $P_{2471} = (6, 9, 8, 1)$
51 : $P_{434} = (0, 10, 0, 1)$	105 : $P_{1419} = (10, 7, 4, 1)$	159 : $P_{2472} = (7, 9, 8, 1)$
52 : $P_{444} = (10, 10, 0, 1)$	106 : $P_{1428} = (3, 8, 4, 1)$	160 : $P_{2510} = (13, 11, 8, 1)$
53 : $P_{450} = (0, 11, 0, 1)$	107 : $P_{1440} = (15, 8, 4, 1)$	161 : $P_{2511} = (14, 11, 8, 1)$
54 : $P_{461} = (11, 11, 0, 1)$	108 : $P_{1448} = (7, 9, 4, 1)$	162 : $P_{2540} = (11, 13, 8, 1)$
55 : $P_{466} = (0, 12, 0, 1)$	109 : $P_{1451} = (10, 9, 4, 1)$	163 : $P_{2543} = (14, 13, 8, 1)$
56 : $P_{478} = (12, 12, 0, 1)$	110 : $P_{1464} = (7, 10, 4, 1)$	164 : $P_{2556} = (11, 14, 8, 1)$
57 : $P_{482} = (0, 13, 0, 1)$	111 : $P_{1466} = (9, 10, 4, 1)$	165 : $P_{2558} = (13, 14, 8, 1)$
58 : $P_{495} = (13, 13, 0, 1)$	112 : $P_{1540} = (3, 15, 4, 1)$	166 : $P_{2630} = (5, 3, 9, 1)$
59 : $P_{498} = (0, 14, 0, 1)$	113 : $P_{1545} = (8, 15, 4, 1)$	167 : $P_{2640} = (15, 3, 9, 1)$
60 : $P_{512} = (14, 14, 0, 1)$	114 : $P_{1629} = (12, 4, 5, 1)$	168 : $P_{2660} = (3, 5, 9, 1)$
61 : $P_{514} = (0, 15, 0, 1)$	115 : $P_{1630} = (13, 4, 5, 1)$	169 : $P_{2672} = (15, 5, 9, 1)$
62 : $P_{529} = (15, 15, 0, 1)$	116 : $P_{1638} = (5, 5, 5, 1)$	170 : $P_{2730} = (9, 9, 9, 1)$
63 : $P_{570} = (9, 2, 1, 1)$	117 : $P_{1658} = (9, 6, 5, 1)$	171 : $P_{2765} = (12, 11, 9, 1)$
64 : $P_{571} = (10, 2, 1, 1)$	118 : $P_{1659} = (10, 6, 5, 1)$	172 : $P_{2767} = (14, 11, 9, 1)$
65 : $P_{604} = (11, 4, 1, 1)$	119 : $P_{1703} = (6, 9, 5, 1)$	173 : $P_{2780} = (11, 12, 9, 1)$
66 : $P_{607} = (14, 4, 1, 1)$	120 : $P_{1707} = (10, 9, 5, 1)$	174 : $P_{2783} = (14, 12, 9, 1)$
67 : $P_{675} = (2, 9, 1, 1)$	121 : $P_{1719} = (6, 10, 5, 1)$	175 : $P_{2812} = (11, 14, 9, 1)$
68 : $P_{683} = (10, 9, 1, 1)$	122 : $P_{1722} = (9, 10, 5, 1)$	176 : $P_{2813} = (12, 14, 9, 1)$
69 : $P_{691} = (2, 10, 1, 1)$	123 : $P_{1749} = (4, 12, 5, 1)$	177 : $P_{2820} = (3, 15, 9, 1)$
70 : $P_{698} = (9, 10, 1, 1)$	124 : $P_{1758} = (13, 12, 5, 1)$	178 : $P_{2822} = (5, 15, 9, 1)$
71 : $P_{709} = (4, 11, 1, 1)$	125 : $P_{1765} = (4, 13, 5, 1)$	179 : $P_{2852} = (3, 1, 10, 1)$
72 : $P_{719} = (14, 11, 1, 1)$	126 : $P_{1773} = (12, 13, 5, 1)$	180 : $P_{2857} = (8, 1, 10, 1)$
73 : $P_{757} = (4, 14, 1, 1)$	127 : $P_{1833} = (8, 1, 6, 1)$	181 : $P_{2882} = (1, 3, 10, 1)$
74 : $P_{764} = (11, 14, 1, 1)$	128 : $P_{1840} = (15, 1, 6, 1)$	182 : $P_{2889} = (8, 3, 10, 1)$
75 : $P_{819} = (2, 2, 2, 1)$	129 : $P_{1885} = (12, 4, 6, 1)$	183 : $P_{2962} = (1, 8, 10, 1)$
76 : $P_{860} = (11, 4, 2, 1)$	130 : $P_{1887} = (14, 4, 6, 1)$	184 : $P_{2964} = (3, 8, 10, 1)$
77 : $P_{862} = (13, 4, 2, 1)$	131 : $P_{1911} = (6, 6, 6, 1)$	185 : $P_{3003} = (10, 10, 10, 1)$
78 : $P_{873} = (8, 5, 2, 1)$	132 : $P_{1938} = (1, 8, 6, 1)$	186 : $P_{3021} = (12, 11, 10, 1)$
79 : $P_{880} = (15, 5, 2, 1)$	133 : $P_{1952} = (15, 8, 6, 1)$	187 : $P_{3022} = (13, 11, 10, 1)$
80 : $P_{918} = (5, 8, 2, 1)$	134 : $P_{2005} = (4, 12, 6, 1)$	188 : $P_{3036} = (11, 12, 10, 1)$
81 : $P_{928} = (15, 8, 2, 1)$	135 : $P_{2015} = (14, 12, 6, 1)$	189 : $P_{3038} = (13, 12, 10, 1)$
82 : $P_{965} = (4, 11, 2, 1)$	136 : $P_{2037} = (4, 14, 6, 1)$	190 : $P_{3052} = (11, 13, 10, 1)$
83 : $P_{974} = (13, 11, 2, 1)$	137 : $P_{2045} = (12, 14, 6, 1)$	191 : $P_{3053} = (12, 13, 10, 1)$
84 : $P_{997} = (4, 13, 2, 1)$	138 : $P_{2050} = (1, 15, 6, 1)$	192 : $P_{3110} = (5, 1, 11, 1)$
85 : $P_{1004} = (11, 13, 2, 1)$	139 : $P_{2057} = (8, 15, 6, 1)$	193 : $P_{3120} = (15, 1, 11, 1)$
86 : $P_{1030} = (5, 15, 2, 1)$	140 : $P_{2084} = (3, 1, 7, 1)$	194 : $P_{3170} = (1, 5, 11, 1)$
87 : $P_{1033} = (8, 15, 2, 1)$	141 : $P_{2086} = (5, 1, 7, 1)$	195 : $P_{3184} = (15, 5, 11, 1)$
88 : $P_{1079} = (6, 2, 3, 1)$	142 : $P_{2114} = (1, 3, 7, 1)$	196 : $P_{3192} = (7, 6, 11, 1)$
89 : $P_{1080} = (7, 2, 3, 1)$	143 : $P_{2118} = (5, 3, 7, 1)$	197 : $P_{3195} = (10, 6, 11, 1)$
90 : $P_{1092} = (3, 3, 3, 1)$	144 : $P_{2142} = (13, 4, 7, 1)$	198 : $P_{3207} = (6, 7, 11, 1)$
91 : $P_{1116} = (11, 4, 3, 1)$	145 : $P_{2143} = (14, 4, 7, 1)$	199 : $P_{3211} = (10, 7, 11, 1)$
92 : $P_{1117} = (12, 4, 3, 1)$	146 : $P_{2146} = (1, 5, 7, 1)$	200 : $P_{3255} = (6, 10, 11, 1)$
93 : $P_{1139} = (2, 6, 3, 1)$	147 : $P_{2148} = (3, 5, 7, 1)$	201 : $P_{3256} = (7, 10, 11, 1)$
94 : $P_{1144} = (7, 6, 3, 1)$	148 : $P_{2184} = (7, 7, 7, 1)$	202 : $P_{3276} = (11, 11, 11, 1)$
95 : $P_{1155} = (2, 7, 3, 1)$	149 : $P_{2277} = (4, 13, 7, 1)$	203 : $P_{3330} = (1, 15, 11, 1)$



204 : $P_{3334} = (5, 15, 11, 1)$	222 : $P_{3650} = (1, 3, 13, 1)$	240 : $P_{3990} = (5, 8, 14, 1)$
205 : $P_{3366} = (5, 1, 12, 1)$	223 : $P_{3664} = (15, 3, 13, 1)$	241 : $P_{4019} = (2, 10, 14, 1)$
206 : $P_{3369} = (8, 1, 12, 1)$	224 : $P_{3699} = (2, 6, 13, 1)$	242 : $P_{4023} = (6, 10, 14, 1)$
207 : $P_{3384} = (7, 2, 12, 1)$	225 : $P_{3706} = (9, 6, 13, 1)$	243 : $P_{4095} = (14, 14, 14, 1)$
208 : $P_{3386} = (9, 2, 12, 1)$	226 : $P_{3747} = (2, 9, 13, 1)$	244 : $P_{4152} = (7, 2, 15, 1)$
209 : $P_{3426} = (1, 5, 12, 1)$	227 : $P_{3751} = (6, 9, 13, 1)$	245 : $P_{4155} = (10, 2, 15, 1)$
210 : $P_{3433} = (8, 5, 12, 1)$	228 : $P_{3822} = (13, 13, 13, 1)$	246 : $P_{4227} = (2, 7, 15, 1)$
211 : $P_{3459} = (2, 7, 12, 1)$	229 : $P_{3842} = (1, 15, 13, 1)$	247 : $P_{4235} = (10, 7, 15, 1)$
212 : $P_{3466} = (9, 7, 12, 1)$	230 : $P_{3844} = (3, 15, 13, 1)$	248 : $P_{4275} = (2, 10, 15, 1)$
213 : $P_{3474} = (1, 8, 12, 1)$	231 : $P_{3895} = (6, 2, 14, 1)$	249 : $P_{4280} = (7, 10, 15, 1)$
214 : $P_{3478} = (5, 8, 12, 1)$	232 : $P_{3899} = (10, 2, 14, 1)$	250 : $P_{4318} = (13, 12, 15, 1)$
215 : $P_{3491} = (2, 9, 12, 1)$	233 : $P_{3910} = (5, 3, 14, 1)$	251 : $P_{4319} = (14, 12, 15, 1)$
216 : $P_{3496} = (7, 9, 12, 1)$	234 : $P_{3913} = (8, 3, 14, 1)$	252 : $P_{4333} = (12, 13, 15, 1)$
217 : $P_{3549} = (12, 12, 12, 1)$	235 : $P_{3940} = (3, 5, 14, 1)$	253 : $P_{4335} = (14, 13, 15, 1)$
218 : $P_{3620} = (3, 1, 13, 1)$	236 : $P_{3945} = (8, 5, 14, 1)$	254 : $P_{4349} = (12, 14, 15, 1)$
219 : $P_{3632} = (15, 1, 13, 1)$	237 : $P_{3955} = (2, 6, 14, 1)$	255 : $P_{4350} = (13, 14, 15, 1)$
220 : $P_{3639} = (6, 2, 13, 1)$	238 : $P_{3963} = (10, 6, 14, 1)$	256 : $P_{4368} = (15, 15, 15, 1)$
221 : $P_{3642} = (9, 2, 13, 1)$	239 : $P_{3988} = (3, 8, 14, 1)$	