

Rank-65562 over GF(2)

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The equation

The equation of the surface is :

$$X_0^3 + X_1^3 + X_2^3 + X_0^2 X_1 + X_0 X_1 X_2 = 0$$

(1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(2) is 65562

General information

Number of lines	2
Number of points	5
Number of singular points	1
Number of Eckardt points	0
Number of double points	1
Number of single points	4
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	3^2
Type of lines on points	2, 1^4

Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0,0,0,1) = \mathbf{P}(0,0,0,1)$$

The 2 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{20} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{20} = \mathbf{Pl}(0,1,0,0,1,0)_{11}$$

$$\ell_1 = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{33} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{33} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_7$$

Rank of lines: (20, 33)

Rank of points on Klein quadric: (11, 7)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 1 Double points:

The double points on the surface are:

$$P_3 = (0, 0, 0, 1) = \ell_0 \cap \ell_1$$

Single Points

The surface has 4 single points:

The single points on the surface are:

0 : $P_6 = (1, 0, 1, 0)$ lies on line ℓ_0

1 : $P_7 = (0, 1, 1, 0)$ lies on line ℓ_1

2 : $P_{13} = (1, 0, 1, 1)$ lies on line ℓ_0

3 : $P_{14} = (0, 1, 1, 1)$ lies on line ℓ_1

The single points on the surface are:

Points on surface but on no line

The surface has 0 points not on any line:

The points on the surface but not on lines are:

Line Intersection Graph

$$\begin{array}{c|c} & 0 \ 1 \\ \hline 0 & 0 \ 1 \\ 1 & 1 \ 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1
in point	P_3

Line 1 intersects

Line	ℓ_0
in point	P_3

The surface has 5 points:

The points on the surface are:

$$\begin{aligned} 0 : P_3 &= (0, 0, 0, 1) \\ 1 : P_6 &= (1, 0, 1, 0) \end{aligned}$$

$$\begin{aligned} 2 : P_7 &= (0, 1, 1, 0) \\ 3 : P_{13} &= (1, 0, 1, 1) \end{aligned}$$

$$4 : P_{14} = (0, 1, 1, 1)$$