

Rank-65915 over GF(8)

January 15, 2021

The equation

The equation of the surface is :

$$X_3^3 + X_0^2 X_1 + X_0^2 X_2 + X_0^2 X_3 + X_1^2 X_2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(8) is 1244210253

General information

Number of lines	1
Number of points	73
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	9
Number of points off lines	64
Number of Hesse planes	0
Number of axes	0
Type of points on lines	9
Type of lines on points	$1^9, 0^{64}$

Singular Points

The surface has 1 singular points:

$$0 : P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0)$$

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \left[\begin{array}{cccc} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 \end{array} \right]_{593} = \left[\begin{array}{cccc} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 \end{array} \right]_{593} = \mathbf{Pl}(1, 1, 1, 1, 1, 0)_{306}$$

Rank of lines: (593)

Rank of points on Klein quadric: (306)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 9 single points:

The single points on the surface are:

- 0 : $P_{20} = (1, 1, 1, 0)$ lies on line ℓ_0
- 1 : $P_{75} = (1, 0, 0, 1)$ lies on line ℓ_0
- 2 : $P_{146} = (0, 1, 1, 1)$ lies on line ℓ_0
- 3 : $P_{220} = (3, 2, 2, 1)$ lies on line ℓ_0
- 4 : $P_{291} = (2, 3, 3, 1)$ lies on line ℓ_0

- 5 : $P_{366} = (5, 4, 4, 1)$ lies on line ℓ_0
- 6 : $P_{437} = (4, 5, 5, 1)$ lies on line ℓ_0
- 7 : $P_{512} = (7, 6, 6, 1)$ lies on line ℓ_0
- 8 : $P_{583} = (6, 7, 7, 1)$ lies on line ℓ_0

The single points on the surface are:

Points on surface but on no line

The surface has 64 points not on any line:

The points on the surface but not on lines are:

- | | |
|-------------------------------|-------------------------------|
| 0 : $P_0 = (1, 0, 0, 0)$ | 18 : $P_{226} = (1, 3, 2, 1)$ |
| 1 : $P_1 = (0, 1, 0, 0)$ | 19 : $P_{234} = (1, 4, 2, 1)$ |
| 2 : $P_2 = (0, 0, 1, 0)$ | 20 : $P_{240} = (7, 4, 2, 1)$ |
| 3 : $P_4 = (1, 1, 1, 1)$ | 21 : $P_{241} = (0, 5, 2, 1)$ |
| 4 : $P_{30} = (3, 2, 1, 0)$ | 22 : $P_{244} = (3, 5, 2, 1)$ |
| 5 : $P_{33} = (6, 2, 1, 0)$ | 23 : $P_{270} = (5, 0, 3, 1)$ |
| 6 : $P_{46} = (3, 4, 1, 0)$ | 24 : $P_{279} = (6, 1, 3, 1)$ |
| 7 : $P_{48} = (5, 4, 1, 0)$ | 25 : $P_{280} = (7, 1, 3, 1)$ |
| 8 : $P_{72} = (5, 7, 1, 0)$ | 26 : $P_{281} = (0, 2, 3, 1)$ |
| 9 : $P_{73} = (6, 7, 1, 0)$ | 27 : $P_{296} = (7, 3, 3, 1)$ |
| 10 : $P_{92} = (2, 2, 0, 1)$ | 28 : $P_{315} = (2, 6, 3, 1)$ |
| 11 : $P_{103} = (5, 3, 0, 1)$ | 29 : $P_{319} = (6, 6, 3, 1)$ |
| 12 : $P_{110} = (4, 4, 0, 1)$ | 30 : $P_{324} = (3, 7, 3, 1)$ |
| 13 : $P_{120} = (6, 5, 0, 1)$ | 31 : $P_{326} = (5, 7, 3, 1)$ |
| 14 : $P_{125} = (3, 6, 0, 1)$ | 32 : $P_{333} = (4, 0, 4, 1)$ |
| 15 : $P_{137} = (7, 7, 0, 1)$ | 33 : $P_{363} = (2, 4, 4, 1)$ |
| 16 : $P_{203} = (2, 0, 2, 1)$ | 34 : $P_{370} = (1, 5, 4, 1)$ |
| 17 : $P_{224} = (7, 2, 2, 1)$ | 35 : $P_{377} = (0, 6, 4, 1)$ |

36 : $P_{382} = (5, 6, 4, 1)$
 37 : $P_{386} = (1, 7, 4, 1)$
 38 : $P_{387} = (2, 7, 4, 1)$
 39 : $P_{399} = (6, 0, 5, 1)$
 40 : $P_{403} = (2, 1, 5, 1)$
 41 : $P_{404} = (3, 1, 5, 1)$
 42 : $P_{414} = (5, 2, 5, 1)$
 43 : $P_{415} = (6, 2, 5, 1)$
 44 : $P_{420} = (3, 3, 5, 1)$
 45 : $P_{421} = (4, 3, 5, 1)$
 46 : $P_{425} = (0, 4, 5, 1)$
 47 : $P_{435} = (2, 5, 5, 1)$
 48 : $P_{460} = (3, 0, 6, 1)$
 49 : $P_{469} = (4, 1, 6, 1)$
 50 : $P_{470} = (5, 1, 6, 1)$

51 : $P_{492} = (3, 4, 6, 1)$
 52 : $P_{495} = (6, 4, 6, 1)$
 53 : $P_{502} = (5, 5, 6, 1)$
 54 : $P_{504} = (7, 5, 6, 1)$
 55 : $P_{509} = (4, 6, 6, 1)$
 56 : $P_{513} = (0, 7, 6, 1)$
 57 : $P_{528} = (7, 0, 7, 1)$
 58 : $P_{538} = (1, 2, 7, 1)$
 59 : $P_{541} = (4, 2, 7, 1)$
 60 : $P_{545} = (0, 3, 7, 1)$
 61 : $P_{551} = (6, 3, 7, 1)$
 62 : $P_{570} = (1, 6, 7, 1)$
 63 : $P_{581} = (4, 7, 7, 1)$

Line Intersection Graph

$$\begin{array}{c|c} & 0 \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line
in point

The surface has 73 points:

The points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$
 1 : $P_1 = (0, 1, 0, 0)$
 2 : $P_2 = (0, 0, 1, 0)$
 3 : $P_4 = (1, 1, 1, 1)$
 4 : $P_{20} = (1, 1, 1, 0)$
 5 : $P_{30} = (3, 2, 1, 0)$
 6 : $P_{33} = (6, 2, 1, 0)$
 7 : $P_{46} = (3, 4, 1, 0)$
 8 : $P_{48} = (5, 4, 1, 0)$
 9 : $P_{72} = (5, 7, 1, 0)$
 10 : $P_{73} = (6, 7, 1, 0)$
 11 : $P_{75} = (1, 0, 0, 1)$
 12 : $P_{92} = (2, 2, 0, 1)$
 13 : $P_{103} = (5, 3, 0, 1)$
 14 : $P_{110} = (4, 4, 0, 1)$
 15 : $P_{120} = (6, 5, 0, 1)$
 16 : $P_{125} = (3, 6, 0, 1)$
 17 : $P_{137} = (7, 7, 0, 1)$
 18 : $P_{146} = (0, 1, 1, 1)$
 19 : $P_{203} = (2, 0, 2, 1)$
 20 : $P_{220} = (3, 2, 2, 1)$
 21 : $P_{224} = (7, 2, 2, 1)$
 22 : $P_{226} = (1, 3, 2, 1)$
 23 : $P_{234} = (1, 4, 2, 1)$
 24 : $P_{240} = (7, 4, 2, 1)$

25 : $P_{241} = (0, 5, 2, 1)$
 26 : $P_{244} = (3, 5, 2, 1)$
 27 : $P_{270} = (5, 0, 3, 1)$
 28 : $P_{279} = (6, 1, 3, 1)$
 29 : $P_{280} = (7, 1, 3, 1)$
 30 : $P_{281} = (0, 2, 3, 1)$
 31 : $P_{291} = (2, 3, 3, 1)$
 32 : $P_{296} = (7, 3, 3, 1)$
 33 : $P_{315} = (2, 6, 3, 1)$
 34 : $P_{319} = (6, 6, 3, 1)$
 35 : $P_{324} = (3, 7, 3, 1)$
 36 : $P_{326} = (5, 7, 3, 1)$
 37 : $P_{333} = (4, 0, 4, 1)$
 38 : $P_{363} = (2, 4, 4, 1)$
 39 : $P_{366} = (5, 4, 4, 1)$
 40 : $P_{370} = (1, 5, 4, 1)$
 41 : $P_{377} = (0, 6, 4, 1)$
 42 : $P_{382} = (5, 6, 4, 1)$
 43 : $P_{386} = (1, 7, 4, 1)$
 44 : $P_{387} = (2, 7, 4, 1)$
 45 : $P_{399} = (6, 0, 5, 1)$
 46 : $P_{403} = (2, 1, 5, 1)$
 47 : $P_{404} = (3, 1, 5, 1)$
 48 : $P_{414} = (5, 2, 5, 1)$
 49 : $P_{415} = (6, 2, 5, 1)$

50 : $P_{420} = (3, 3, 5, 1)$
 51 : $P_{421} = (4, 3, 5, 1)$
 52 : $P_{425} = (0, 4, 5, 1)$
 53 : $P_{435} = (2, 5, 5, 1)$
 54 : $P_{437} = (4, 5, 5, 1)$
 55 : $P_{460} = (3, 0, 6, 1)$
 56 : $P_{469} = (4, 1, 6, 1)$
 57 : $P_{470} = (5, 1, 6, 1)$
 58 : $P_{492} = (3, 4, 6, 1)$
 59 : $P_{495} = (6, 4, 6, 1)$
 60 : $P_{502} = (5, 5, 6, 1)$
 61 : $P_{504} = (7, 5, 6, 1)$
 62 : $P_{509} = (4, 6, 6, 1)$
 63 : $P_{512} = (7, 6, 6, 1)$
 64 : $P_{513} = (0, 7, 6, 1)$
 65 : $P_{528} = (7, 0, 7, 1)$
 66 : $P_{538} = (1, 2, 7, 1)$
 67 : $P_{541} = (4, 2, 7, 1)$
 68 : $P_{545} = (0, 3, 7, 1)$
 69 : $P_{551} = (6, 3, 7, 1)$
 70 : $P_{570} = (1, 6, 7, 1)$
 71 : $P_{581} = (4, 7, 7, 1)$
 72 : $P_{583} = (6, 7, 7, 1)$