Rank-24 over GF(32)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 = 0$$

General information

Number of lines	33
Number of points	1057
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	1056
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^{33}
Type of lines on points	$33, 1^{1056}$

Singular Points

The surface has 1 singular points:

$$0: P_3 = \mathbf{P}(0,0,0,1) = \mathbf{P}(0,0,0,1)$$

The 33 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2113} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2113} = \mathbf{Pl}(0, 0, 0, 1, 1, 0)_{3105}$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{34880} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{34880} = \mathbf{Pl}(0, 1, 0, 0, 1, 0)_{1121}$$

$$\begin{split} \ell_2 &= \begin{bmatrix} 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082433} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082433} = \mathbf{PI}(0,1,0,1,0,0)_{97} \\ \ell_3 &= \begin{bmatrix} 1 & \eta^{12} & \eta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{252622} = \begin{bmatrix} 1 & 14 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{252622} = \mathbf{PI}(0,7,0,14,1,0)_{3962} \\ \ell_4 &= \begin{bmatrix} 1 & \eta^{14} & \eta^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{403773} = \begin{bmatrix} 1 & 29 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{403773} = \mathbf{PI}(0,11,0,29,1,0)_{4911} \\ \ell_5 &= \begin{bmatrix} 1 & \eta^{24} & \eta^{22} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{743070} = \begin{bmatrix} 1 & 30 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{743070} = \mathbf{PI}(0,21,0,30,1,0)_{4984} \\ \ell_6 &= \begin{bmatrix} 1 & \eta^{28} & \eta^{23} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{531670} = \begin{bmatrix} 1 & 22 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{34388} = \mathbf{PI}(0,21,0,30,1,0)_{4984} \\ \ell_7 &= \begin{bmatrix} 1 & \eta^{20} & \eta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{81388} = \begin{bmatrix} 1 & 12 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{81388} = \mathbf{PI}(0,2,0,12,1,0)_{3831} \\ \ell_8 &= \begin{bmatrix} 1 & \eta^{30} & \eta^{19} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{183917} = \begin{bmatrix} 1 & 18 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{183917} = \mathbf{PI}(0,5,0,13,1,0)_{3897} \\ \ell_{10} &= \begin{bmatrix} 1 & \eta^{2} & \eta^{24} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{183917} = \begin{bmatrix} 1 & 21 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{183917} = \mathbf{PI}(0,5,0,13,1,0)_{3897} \\ \ell_{11} &= \begin{bmatrix} 1 & \eta^{16} & \eta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1037973} = \begin{bmatrix} 1 & 21 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1037973} = \mathbf{PI}(0,30,0,21,1,0)_{4426} \\ \ell_{12} &= \begin{bmatrix} 1 & \eta^{13} & \eta^{17} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{673308} = \begin{bmatrix} 1 & 28 & 19 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{673308} = \mathbf{PI}(0,17,0,27,1,0)_{4791} \\ \ell_{12} &= \begin{bmatrix} 1 & \eta^{19} & \eta^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{673308} = \begin{bmatrix} 1 & 8 & 23 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{787464} = \mathbf{PI}(0,12,0,2,1,0)_{3211} \\ \ell_{15} &= \begin{bmatrix} 1 & \eta^{19} & \eta^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{399599} = \begin{bmatrix} 1 & 23 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{399521} = \mathbf{PI}(0,12,0,2,1,0)_{3211} \\ \ell_{16} &= \begin{bmatrix} 1 & \eta^{17} & \eta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{968211} = \begin{bmatrix} 1 & 19 & 28 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{968211} = \mathbf{PI}(0,30,0,16,1,0)_{4298} \\ \ell_{17} &= \begin{bmatrix} 1 & \eta^{17} & \eta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1076025} = \begin{bmatrix} 1 & 25 & 31 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1076025} = \mathbf{PI}(0,30,0,16,1,0)_{4094} \\ \ell_{19} &= \begin{bmatrix} 1 & \eta^{11} & \eta^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{119409} = \begin{bmatrix} 1 & 16 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{$$

$$\begin{split} \ell_{23} &= \begin{bmatrix} 1 & \eta^5 & \eta^8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{446053} = \begin{bmatrix} 1 & 5 & 13 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{446053} = \mathbf{Pl}(0,13,0,5,1,0)_{3401} \\ \ell_{24} &= \begin{bmatrix} 1 & \eta^{23} & \eta^{28} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{761039} = \begin{bmatrix} 1 & 15 & 22 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{761039} = \mathbf{Pl}(0,22,0,15,1,0)_{4040} \\ \ell_{25} &= \begin{bmatrix} 1 & \eta^{15} & \eta^{25} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{879423} = \begin{bmatrix} 1 & 31 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{879423} = \mathbf{Pl}(0,25,0,31,1,0)_{5051} \\ \ell_{26} &= \begin{bmatrix} 1 & \eta^{10} & \eta^{16} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{932273} = \begin{bmatrix} 1 & 17 & 27 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{932273} = \mathbf{Pl}(0,27,0,17,1,0)_{4171} \\ \ell_{27} &= \begin{bmatrix} 1 & \eta^7 & \eta^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{326612} = \begin{bmatrix} 1 & 20 & 9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{326612} = \mathbf{Pl}(0,9,0,20,1,0)_{4342} \\ \ell_{28} &= \begin{bmatrix} 1 & \eta^6 & \eta^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{823402} = \begin{bmatrix} 1 & 10 & 24 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{823402} = \mathbf{Pl}(0,24,0,10,1,0)_{3727} \\ \ell_{29} &= \begin{bmatrix} 1 & \eta^{27} & \eta^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{993579} = \begin{bmatrix} 1 & 11 & 29 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{993579} = \mathbf{Pl}(0,29,0,11,1,0)_{3795} \\ \ell_{30} &= \begin{bmatrix} 1 & \eta^{18} & \eta^4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{545411} = \begin{bmatrix} 1 & 3 & 16 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{545411} = \mathbf{Pl}(0,16,0,3,1,0)_{3278} \\ \ell_{31} &= \begin{bmatrix} 1 & \eta^2 & \eta^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{884708} = \begin{bmatrix} 1 & 4 & 26 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{884708} = \mathbf{Pl}(0,26,0,4,1,0)_{4595} \end{aligned}$$

Rank of lines: (2113, 34880, 1082433, 252622, 403773, 743070, 531670, 81388, 223026, 183917, 1037973, 604603, 673308, 616230, 787464, 409058, 295959, 968211, 1076025, 481991, 119440, 163834, 687049, 446053, 761039, 879423, 932273, 326612, 823402, 993579, 545411, 884708, 364664)

Rank of points on Klein quadric: (3105, 1121, 97, 3962, 4911, 4984, 4474, 3831, 4213, 3897, 4426, 4791, 4856, 3469, 3600, 3211, 4530, 4298, 4679, 3528, 4084, 4715, 3660, 3401, 4040, 5051, 4171, 4342, 3727, 3795, 3278, 3351, 4595)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 1056 single points: Too many to print.

Points on surface but on no line

The surface has 0 points not on any line: The points on the surface but not on lines are:

Line Intersection Graph

	0 1	2	3 4	1 5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30 3	31	32
0	01	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	10	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	11	0	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
3	11	1	0 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
4	11	1	1 () 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
5	11	1	1 1	1 (1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
6	11	1	1 1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
7	11	1	1 1	1	. 1	. 0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
8	11	1	1 1	1 1	. 1	. 1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
9	11	1	1 1	1	. 1	. 1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
10	11	1	1 1	1	. 1	. 1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
11	11	1	1 1	1	. 1	. 1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
12	11	1	1 1	1	. 1	. 1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
13	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
14	11	1	1 1	1	. 1	. 1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
15	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
16	11	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
17	11	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
18	11	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
19	11	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
20	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1
21	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
22	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
23	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
24	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
25	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
26	11	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1
27	11	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
28	1 1	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
29	1 1	1	1 1	1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
30	11	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
31	11	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
32	1 1	1	1 1	1 1	. 1	. 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3									

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}	_
in point	P_{2}	P_2	P_{2}	P_{2}	P_2	P_{2}	P_2	P_{2}	P_{2}	P_{3}	P_{3}	P_{2}	P_{2}	P_{3}	P_2	P_2	P_{2}	P_{2}	P_2	P_{2}	P_{2}	P_{2}	Γ

Line 2 intersects

ſ	т.	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	_
	Line	ℓ_0	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}	
	in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Π									

Line 3 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3									

Line 4 intersects
in point $\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Line 5 intersects
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
in point $ P_3 $ $ P_$
Line 6 intersects
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
Line 7 intersects
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
Line 8 intersects
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
Line 9 intersects
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
in point $ P_3 $ $ P_$
Line 10 intersects
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
in point P_3 P
Line 11 intersects
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
Line 12 intersects
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
Line 13 intersects
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
Line 14 intersects
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
in point $ P_3 $
Line 15 intersects
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
in point $ P_3 $
Line 16 intersects
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$

Line 17 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 18 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 19 int	ersec	cts																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 20 int	ersec	cts																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 21 int	ersec	cts																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 22 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 23 int		ets																				
Line	n point P3 P3 P3 P3 P3 P3 P3 P																					
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	$P_3 \mid .$
	ersec	ets																				
																ℓ_{15}	ℓ_{16}					
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .
			ℓ_2	ℓ_3			ℓ_6	ℓ_7		ℓ_9	ℓ_{10}							ℓ_{17}				
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
	-																					
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
		cts																				
												ℓ_{11}										
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
	ersec	ets																				
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .

Line 30 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	Ī
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Ī										

Line 31 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	Γ.
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Ĺ										

${\bf Line~32~intersects}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	-
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3											

The surface has 1057 points:

Too many to print.