# Rank-65561 over GF(16)

January 15, 2021

## The equation

The equation of the surface is:

$$X_1^3 + X_2^3 + X_0^2 X_1 + X_0 X_1 X_2 = 0$$

(0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)The point rank of the equation over GF(16) is 286396965

### General information

Number of lines	16
Number of points	257
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	256
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$17^{16}$
Type of lines on points	$16, 1^{256}$

#### Singular Points

The surface has 1 singular points:

$$0: P_3 = \mathbf{P}(0,0,0,1) = \mathbf{P}(0,0,0,1)$$

### The 16 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)_{289}$$

$$\ell_1 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{545} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{545} = \mathbf{Pl}(0, 0, 0, 1, 1, 0)_{785}$$

$$\ell_2 = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69921} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69921} = \mathbf{PI}(0,1,0,1,0,0)_{49}$$

$$\ell_3 = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4913} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4913} = \mathbf{PI}(0,1,0,1,1,0)_{801}$$

$$\ell_4 = \begin{bmatrix} 1 & \delta^{10} & \delta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{29210} = \begin{bmatrix} 1 & 10 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{29210} = \mathbf{PI}(0,6,0,10,1,0)_{1085}$$

$$\ell_5 = \begin{bmatrix} 1 & \delta^3 & \delta^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{67976} = \begin{bmatrix} 1 & 8 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{67976} = \mathbf{PI}(0,15,0,8,1,0)_{1032}$$

$$\ell_6 = \begin{bmatrix} 1 & \delta^6 & \delta^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17471} = \begin{bmatrix} 1 & 15 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17471} = \mathbf{PI}(0,3,0,15,1,0)_{1237}$$

$$\ell_7 = \begin{bmatrix} 1 & \delta^5 & \delta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{33578} = \begin{bmatrix} 1 & 11 & 13 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{33578} = \mathbf{PI}(0,13,0,11,1,0)_{1123}$$

$$\ell_8 = \begin{bmatrix} 1 & \delta^{10} & \delta^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{33578} = \begin{bmatrix} 1 & 10 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{32578} = \mathbf{PI}(0,7,0,10,1,0)_{1086}$$

$$\ell_9 = \begin{bmatrix} 1 & \delta^{12} & \delta^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{22931} = \begin{bmatrix} 1 & 3 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{22931} = \mathbf{PI}(0,5,0,3,1,0)_{867}$$

$$\ell_{10} = \begin{bmatrix} 0 & 1 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70091} = \begin{bmatrix} 0 & 1 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70091} = \mathbf{PI}(0,11,0,1,0,0)_{59}$$

$$\ell_{11} = \begin{bmatrix} 1 & \delta^{10} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7370} = \begin{bmatrix} 1 & 10 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70074} = \mathbf{PI}(0,10,0,1,0,0)_{58}$$

$$\ell_{12} = \begin{bmatrix} 0 & 1 & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7643} = \begin{bmatrix} 1 & 11 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7643} = \mathbf{PI}(0,10,0,1,0,1)_{1111}$$

$$\ell_{14} = \begin{bmatrix} 1 & \delta^5 & \delta^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{36581} = \begin{bmatrix} 1 & 11 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{36581} = \mathbf{PI}(0,8,0,5,1,0)_{932}$$

Rank of lines: (272, 545, 69921, 4913, 29210, 67976, 17471, 60059, 33578, 22931, 70091, 7370, 70074, 7643, 55691, 36581)

Rank of points on Klein quadric: (289, 785, 49, 801, 1085, 1032, 1237, 1123, 1086, 867, 59, 1080, 58, 1111, 1122, 932)

#### **Eckardt Points**

The surface has 0 Eckardt points:

#### **Double Points**

The surface has 0 Double points:

The double points on the surface are:

#### Single Points

The surface has 256 single points: The single points on the surface are:

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0: P_0 = (1,0,0,0) lies on line \ell_0
                                                                       48: P_{581} = (4, 3, 1, 1) lies on line \ell_4
1: P_4 = (1, 1, 1, 1) lies on line \ell_3
                                                                       49: P_{582} = (5, 3, 1, 1) lies on line \ell_5
2: P_5 = (1, 1, 0, 0) lies on line \ell_1
                                                                       50: P_{617} = (8, 5, 1, 1) lies on line \ell_6
3: P_{35} = (0, 1, 1, 0) lies on line \ell_2
                                                                       51: P_{618} = (9, 5, 1, 1) lies on line \ell_7
4: P_{36} = (1, 1, 1, 0) lies on line \ell_3
                                                                       52: P_{671} = (14, 8, 1, 1) lies on line \ell_8
5: P_{71} = (4, 3, 1, 0) lies on line \ell_4
                                                                       53: P_{672} = (15, 8, 1, 1) lies on line \ell_9
6: P_{72} = (5, 3, 1, 0) lies on line \ell_5
                                                                       54: P_{689} = (0, 10, 1, 1) lies on line \ell_{10}
7: P_{107} = (8, 5, 1, 0) lies on line \ell_6
                                                                       55: P_{690} = (1, 10, 1, 1) lies on line \ell_{11}
8: P_{108} = (9, 5, 1, 0) lies on line \ell_7
                                                                       56: P_{705} = (0, 11, 1, 1) lies on line \ell_{12}
9: P_{161} = (14, 8, 1, 0) lies on line \ell_8
                                                                       57: P_{706} = (1, 11, 1, 1) lies on line \ell_{13}
10: P_{162} = (15, 8, 1, 0) lies on line \ell_9
                                                                       58: P_{771} = (2, 15, 1, 1) lies on line \ell_{14}
11: P_{179} = (0, 10, 1, 0) lies on line \ell_{10}
                                                                       59: P_{772} = (3, 15, 1, 1) lies on line \ell_{15}
12: P_{180} = (1, 10, 1, 0) lies on line \ell_{11}
                                                                       60: P_{817} = (0, 2, 2, 1) lies on line \ell_2
13: P_{195} = (0, 11, 1, 0) lies on line \ell_{12}
                                                                       61: P_{819} = (2, 2, 2, 1) lies on line \ell_3
                                                                       62: P_{889} = (8, 6, 2, 1) lies on line \ell_4
14: P_{196} = (1, 11, 1, 0) lies on line \ell_{13}
15: P_{261} = (2, 15, 1, 0) lies on line \ell_{14}
                                                                       63: P_{891} = (10, 6, 2, 1) lies on line \ell_5
                                                                       64 : P_{901} = (4, 7, 2, 1) lies on line \ell_{14}
16: P_{262} = (3, 15, 1, 0) lies on line \ell_{15}
17: P_{275} = (1,0,0,1) lies on line \ell_0
                                                                       65: P_{903} = (6,7,2,1) lies on line \ell_{15}
18: P_{276} = (2, 0, 0, 1) lies on line \ell_0
                                                                       66: P_{934} = (5, 9, 2, 1) lies on line \ell_8
19: P_{277} = (3,0,0,1) lies on line \ell_0
                                                                       67: P_{936} = (7, 9, 2, 1) lies on line \ell_9
20: P_{278} = (4, 0, 0, 1) lies on line \ell_0
                                                                       68: P_{954} = (9, 10, 2, 1) lies on line \ell_6
21: P_{279} = (5, 0, 0, 1) lies on line \ell_0
                                                                       69: P_{956} = (11, 10, 2, 1) lies on line \ell_7
22: P_{280} = (6,0,0,1) lies on line \ell_0
                                                                       70: P_{993} = (0, 13, 2, 1) lies on line \ell_{10}
                                                                       71: P_{995} = (2, 13, 2, 1) lies on line \ell_{11}
23: P_{281} = (7,0,0,1) lies on line \ell_0
24: P_{282} = (8,0,0,1) lies on line \ell_0
                                                                       72: P_{1025} = (0, 15, 2, 1) lies on line \ell_{12}
25: P_{283} = (9, 0, 0, 1) lies on line \ell_0
                                                                       73: P_{1027} = (2, 15, 2, 1) lies on line \ell_{13}
26: P_{284} = (10, 0, 0, 1) lies on line \ell_0
                                                                       74: P_{1065} = (8, 1, 3, 1) lies on line \ell_9
27: P_{285} = (11, 0, 0, 1) lies on line \ell_0
                                                                       75: P_{1068} = (11, 1, 3, 1) lies on line \ell_8
28: P_{286} = (12, 0, 0, 1) lies on line \ell_0
                                                                       76: P_{1089} = (0, 3, 3, 1) lies on line \ell_2
                                                                       77 : P_{1092} = (3, 3, 3, 1) lies on line \ell_3
29: P_{287} = (13, 0, 0, 1) lies on line \ell_0
30: P_{288} = (14,0,0,1) lies on line \ell_0
                                                                       78: P_{1105} = (0, 4, 3, 1) lies on line \ell_{12}
31: P_{289} = (15,0,0,1) lies on line \ell_0
                                                                       79: P_{1108} = (3, 4, 3, 1) lies on line \ell_{13}
32: P_{291} = (1, 1, 0, 1) lies on line \ell_1
                                                                       80: P_{1133} = (12, 5, 3, 1) lies on line \ell_4
33: P_{308} = (2, 2, 0, 1) lies on line \ell_1
                                                                       81: P_{1136} = (15, 5, 3, 1) lies on line \ell_5
34: P_{325} = (3,3,0,1) lies on line \ell_1
                                                                       82: P_{1153} = (0, 7, 3, 1) lies on line \ell_{10}
35: P_{342} = (4, 4, 0, 1) lies on line \ell_1
                                                                       83: P_{1156} = (3, 7, 3, 1) lies on line \ell_{11}
36: P_{359} = (5, 5, 0, 1) lies on line \ell_1
                                                                       84: P_{1174} = (5, 8, 3, 1) lies on line \ell_{15}
37: P_{376} = (6, 6, 0, 1) lies on line \ell_1
                                                                       85: P_{1175} = (6, 8, 3, 1) lies on line \ell_{14}
38: P_{393} = (7,7,0,1) lies on line \ell_1
                                                                       86: P_{1282} = (1, 15, 3, 1) lies on line \ell_6
39: P_{410} = (8, 8, 0, 1) lies on line \ell_1
                                                                       87: P_{1283} = (2, 15, 3, 1) lies on line \ell_7
40 : P_{427} = (9, 9, 0, 1) lies on line \ell_1
                                                                       88: P_{1345} = (0, 3, 4, 1) lies on line \ell_{10}
41: P_{444} = (10, 10, 0, 1) lies on line \ell_1
                                                                       89: P_{1349} = (4, 3, 4, 1) lies on line \ell_{11}
42: P_{461} = (11, 11, 0, 1) lies on line \ell_1
                                                                       90: P_{1361} = (0, 4, 4, 1) lies on line \ell_2
                                                                       91 : P_{1365} = (4, 4, 4, 1) lies on line \ell_3
43: P_{478} = (12, 12, 0, 1) lies on line \ell_1
44: P_{495} = (13, 13, 0, 1) lies on line \ell_1
                                                                       92: P_{1409} = (0, 7, 4, 1) lies on line \ell_{12}
45: P_{512} = (14, 14, 0, 1) lies on line \ell_1
                                                                       93: P_{1413} = (4, 7, 4, 1) lies on line \ell_{13}
                                                                       94 : P_{1483} = (10, 11, 4, 1) lies on line \ell_8
46: P_{529} = (15, 15, 0, 1) lies on line \ell_1
47: P_{546} = (0, 1, 1, 1) lies on line \ell_2
                                                                       95: P_{1487} = (14, 11, 4, 1) lies on line \ell_9
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96: P_{1498} = (9, 12, 4, 1) lies on line \ell_4
                                                                      150: P_{2417} = (0, 6, 8, 1) lies on line \ell_{10}
97: P_{1502} = (13, 12, 4, 1) lies on line \ell_5
                                                                      151: P_{2425} = (8, 6, 8, 1) lies on line \ell_{11}
98: P_{1516} = (11, 13, 4, 1) lies on line \ell_6
                                                                      152: P_{2449} = (0, 8, 8, 1) lies on line \ell_2
                                                                      153: P_{2457} = (8, 8, 8, 1) lies on line \ell_3
99: P_{1520} = (15, 13, 4, 1) lies on line \ell_7
100: P_{1529} = (8, 14, 4, 1) lies on line \ell_{14}
                                                                      154: P_{2545} = (0, 14, 8, 1) lies on line \ell_{12}
101: P_{1533} = (12, 14, 4, 1) lies on line \ell_{15}
                                                                      155: P_{2553} = (8, 14, 8, 1) lies on line \ell_{13}
102: P_{1579} = (10, 1, 5, 1) lies on line \ell_{14}
                                                                      156: P_{2566} = (5, 15, 8, 1) lies on line \ell_9
103: P_{1584} = (15, 1, 5, 1) lies on line \ell_{15}
                                                                      157: P_{2574} = (13, 15, 8, 1) lies on line \ell_8
104: P_{1602} = (1, 3, 5, 1) lies on line \ell_9
                                                                      158: P_{2615} = (6, 2, 9, 1) lies on line \ell_5
105: P_{1605} = (4, 3, 5, 1) lies on line \ell_8
                                                                      159: P_{2624} = (15, 2, 9, 1) lies on line \ell_4
106: P_{1633} = (0, 5, 5, 1) lies on line \ell_2
                                                                      160: P_{2657} = (0, 5, 9, 1) lies on line \ell_{12}
107: P_{1638} = (5, 5, 5, 1) lies on line \ell_3
                                                                      161: P_{2666} = (9, 5, 9, 1) lies on line \ell_{13}
108: P_{1684} = (3, 8, 5, 1) lies on line \ell_6
                                                                      162: P_{2680} = (7, 6, 9, 1) lies on line \ell_6
109: P_{1687} = (6, 8, 5, 1) lies on line \ell_7
                                                                      163: P_{2687} = (14, 6, 9, 1) lies on line \ell_7
110: P_{1697} = (0, 9, 5, 1) lies on line \ell_{10}
                                                                      164 : P_{2692} = (3,7,9,1) lies on line \ell_8
111: P_{1702} = (5, 9, 5, 1) lies on line \ell_{11}
                                                                      165: P_{2699} = (10, 7, 9, 1) lies on line \ell_9
112: P_{1745} = (0, 12, 5, 1) lies on line \ell_{12}
                                                                      166: P_{2721} = (0, 9, 9, 1) lies on line \ell_2
113: P_{1750} = (5, 12, 5, 1) lies on line \ell_{13}
                                                                      167: P_{2730} = (9, 9, 9, 1) lies on line \ell_3
114: P_{1801} = (8, 15, 5, 1) lies on line \ell_5
                                                                      168: P_{2739} = (2, 10, 9, 1) lies on line \ell_{15}
115: P_{1806} = (13, 15, 5, 1) lies on line \ell_4
                                                                      169: P_{2748} = (11, 10, 9, 1) lies on line \ell_{14}
116: P_{1850} = (9, 2, 6, 1) lies on line \ell_9
                                                                      170: P_{2769} = (0, 12, 9, 1) lies on line \ell_{10}
117: P_{1856} = (15, 2, 6, 1) lies on line \ell_8
                                                                      171: P_{2778} = (9, 12, 9, 1) lies on line \ell_{11}
                                                                      172: P_{2849} = (0, 1, 10, 1) lies on line \ell_{12}
118: P_{1905} = (0, 6, 6, 1) lies on line \ell_2
                                                                      173: P_{2859} = (10, 1, 10, 1) lies on line \ell_{13}
119: P_{1911} = (6, 6, 6, 1) lies on line \ell_3
120: P_{1923} = (2, 7, 6, 1) lies on line \ell_6
                                                                      174: P_{2872} = (7, 2, 10, 1) lies on line \ell_{15}
121: P_{1925} = (4,7,6,1) lies on line \ell_7
                                                                      175: P_{2878} = (13, 2, 10, 1) lies on line \ell_{14}
122: P_{1937} = (0, 8, 6, 1) lies on line \ell_{12}
                                                                      176: P_{2931} = (2, 6, 10, 1) lies on line \ell_9
123: P_{1943} = (6, 8, 6, 1) lies on line \ell_{13}
                                                                      177: P_{2937} = (8, 6, 10, 1) lies on line \ell_8
124: P_{1963} = (10, 9, 6, 1) lies on line \ell_{15}
                                                                      178: P_{2948} = (3,7,10,1) lies on line \ell_4
125: P_{1965} = (12, 9, 6, 1) lies on line \ell_{14}
                                                                      179: P_{2954} = (9, 7, 10, 1) lies on line \ell_5
126: P_{1970} = (1, 10, 6, 1) lies on line \ell_4
                                                                      180: P_{2983} = (6, 9, 10, 1) lies on line \ell_6
127: P_{1976} = (7, 10, 6, 1) lies on line \ell_5
                                                                      181: P_{2989} = (12, 9, 10, 1) lies on line \ell_7
128: P_{2033} = (0, 14, 6, 1) lies on line \ell_{10}
                                                                      182: P_{2993} = (0, 10, 10, 1) lies on line \ell_2
129: P_{2039} = (6, 14, 6, 1) lies on line \ell_{11}
                                                                      183: P_{3003} = (10, 10, 10, 1) lies on line \ell_3
130: P_{2107} = (10, 2, 7, 1) lies on line \ell_6
                                                                      184: P_{3009} = (0, 11, 10, 1) lies on line \ell_{10}
131 : P_{2110} = (13, 2, 7, 1) lies on line \ell_7
                                                                      185: P_{3019} = (10, 11, 10, 1) lies on line \ell_{11}
132: P_{2113} = (0, 3, 7, 1) lies on line \ell_{12}
                                                                      186: P_{3105} = (0, 1, 11, 1) lies on line \ell_{10}
133 : P_{2120} = (7, 3, 7, 1) lies on line \ell_{13}
                                                                      187: P_{3116} = (11, 1, 11, 1) lies on line \ell_{11}
134 : P_{2129} = (0, 4, 7, 1) lies on line \ell_{10}
                                                                      188 : P_{3160} = (7, 4, 11, 1) lies on line \ell_4
135: P_{2136} = (7, 4, 7, 1) lies on line \ell_{11}
                                                                      189: P_{3165} = (12, 4, 11, 1) lies on line \ell_5
136: P_{2170} = (9, 6, 7, 1) lies on line \ell_{15}
                                                                      190: P_{3249} = (0, 10, 11, 1) lies on line \ell_{12}
137: P_{2175} = (14, 6, 7, 1) lies on line \ell_{14}
                                                                      191: P_{3260} = (11, 10, 11, 1) lies on line \ell_{13}
138 : P_{2177} = (0, 7, 7, 1) lies on line \ell_2
                                                                      192: P_{3265} = (0, 11, 11, 1) lies on line \ell_2
139: P_{2184} = (7,7,7,1) lies on line \ell_3
                                                                      193: P_{3276} = (11, 11, 11, 1) lies on line \ell_3
140: P_{2211} = (2, 9, 7, 1) lies on line \ell_5
                                                                      194: P_{3286} = (5, 12, 11, 1) lies on line \ell_7
                                                                      195 : P_{3295} = (14, 12, 11, 1) lies on line \ell_6
141: P_{2214} = (5, 9, 7, 1) lies on line \ell_4
142: P_{2226} = (1, 10, 7, 1) lies on line \ell_8
                                                                      196: P_{3301} = (4, 13, 11, 1) lies on line \ell_{15}
143: P_{2231} = (6, 10, 7, 1) lies on line \ell_9
                                                                      197: P_{3312} = (15, 13, 11, 1) lies on line \ell_{14}
144: P_{2340} = (3, 1, 8, 1) lies on line \ell_5
                                                                      198: P_{3319} = (6, 14, 11, 1) lies on line \ell_8
145: P_{2348} = (11, 1, 8, 1) lies on line \ell_4
                                                                      199: P_{3326} = (13, 14, 11, 1) lies on line \ell_9
146: P_{2376} = (7, 3, 8, 1) lies on line \ell_7
                                                                      200: P_{3416} = (7, 4, 12, 1) lies on line \ell_8
147: P_{2384} = (15, 3, 8, 1) lies on line \ell_6
                                                                      201: P_{3420} = (11, 4, 12, 1) lies on line \ell_9
148: P_{2402} = (1, 5, 8, 1) lies on line \ell_{15}
                                                                      202: P_{3425} = (0, 5, 12, 1) lies on line \ell_{10}
149: P_{2410} = (9, 5, 8, 1) lies on line \ell_{14}
                                                                      203: P_{3437} = (12, 5, 12, 1) lies on line \ell_{11}
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231 : P_{3967} = (14, 6, 14, 1) lies on line \ell_{13}
204: P_{3489} = (0, 9, 12, 1) lies on line \ell_{12}
205: P_{3501} = (12, 9, 12, 1) lies on line \ell_{13}
                                                                      232: P_{3985} = (0, 8, 14, 1) lies on line \ell_{10}
                                                                      233: P_{3999} = (14, 8, 14, 1) lies on line \ell_{11}
206: P_{3522} = (1, 11, 12, 1) lies on line \ell_{14}
207: P_{3534} = (13, 11, 12, 1) lies on line \ell_{15}
                                                                      234 : P_{4037} = (4, 11, 14, 1) lies on line \ell_5
208: P_{3537} = (0, 12, 12, 1) lies on line \ell_2
                                                                      235 : P_{4043} = (10, 11, 14, 1) lies on line \ell_4
209: P_{3549} = (12, 12, 12, 1) lies on line \ell_3
                                                                      236: P_{4054} = (5, 12, 14, 1) lies on line \ell_{14}
210: P_{3555} = (2, 13, 12, 1) lies on line \ell_4
                                                                      237: P_{4060} = (11, 12, 14, 1) lies on line \ell_{15}
211: P_{3567} = (14, 13, 12, 1) lies on line \ell_5
                                                                      238: P_{4067} = (2, 13, 14, 1) lies on line \ell_8
212 : P_{3573} = (4, 14, 12, 1) lies on line \ell_6
                                                                      239 : P_{4077} = (12, 13, 14, 1) lies on line \ell_9
213: P_{3577} = (8, 14, 12, 1) lies on line \ell_7
                                                                      240: P_{4081} = (0, 14, 14, 1) lies on line \ell_2
214: P_{3633} = (0, 2, 13, 1) lies on line \ell_{12}
                                                                      241: P_{4095} = (14, 14, 14, 1) lies on line \ell_3
215: P_{3646} = (13, 2, 13, 1) lies on line \ell_{13}
                                                                      242: P_{4134} = (5, 1, 15, 1) lies on line \ell_6
216: P_{3668} = (3, 4, 13, 1) lies on line \ell_{14}
                                                                      243: P_{4139} = (10, 1, 15, 1) lies on line \ell_7
217: P_{3679} = (14, 4, 13, 1) lies on line \ell_{15}
                                                                      244: P_{4145} = (0, 2, 15, 1) lies on line \ell_{10}
218 : P_{3778} = (1, 11, 13, 1) lies on line \ell_7
                                                                      245: P_{4160} = (15, 2, 15, 1) lies on line \ell_{11}
219: P_{3789} = (12, 11, 13, 1) lies on line \ell_6
                                                                      246: P_{4168} = (7, 3, 15, 1) lies on line \ell_{14}
220: P_{3797} = (4, 12, 13, 1) lies on line \ell_9
                                                                      247: P_{4169} = (8, 3, 15, 1) lies on line \ell_{15}
221: P_{3802} = (9, 12, 13, 1) lies on line \ell_8
                                                                      248: P_{4196} = (3, 5, 15, 1) lies on line \ell_9
222 : P_{3809} = (0, 13, 13, 1) lies on line \ell_2
                                                                      249: P_{4205} = (12, 5, 15, 1) lies on line \ell_8
223: P_{3822} = (13, 13, 13, 1) lies on line \ell_3
                                                                      250: P_{4242} = (1, 8, 15, 1) lies on line \ell_5
224: P_{3831} = (6, 14, 13, 1) lies on line \ell_4
                                                                      251: P_{4255} = (14, 8, 15, 1) lies on line \ell_4
225 : P_{3836} = (11, 14, 13, 1) lies on line \ell_5
                                                                      252: P_{4321} = (0, 13, 15, 1) lies on line \ell_{12}
226: P_{3841} = (0, 15, 13, 1) lies on line \ell_{10}
                                                                      253: P_{4336} = (15, 13, 15, 1) lies on line \ell_{13}
227 : P_{3854} = (13, 15, 13, 1) lies on line \ell_{11}
                                                                      254: P_{4353} = (0, 15, 15, 1) lies on line \ell_2
228: P_{3924} = (3, 4, 14, 1) lies on line \ell_7
                                                                      255: P_{4368} = (15, 15, 15, 1) lies on line \ell_3
229: P_{3934} = (13, 4, 14, 1) lies on line \ell_6
230: P_{3953} = (0, 6, 14, 1) lies on line \ell_{12}
```

The single points on the surface are:

### Points on surface but on no line

The surface has 0 points not on any line: The points on the surface but not on lines are:

# Line Intersection Graph

	0 1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	01	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1 0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	11	0	1	1	1	1	1	1	1	1	1	1	1	1	1
3	11	1	0	1	1	1	1	1	1	1	1	1	1	1	1
4	1 1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
5	1 1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
6	1 1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
7	11	1	1	1	1	1	0	1	1	1	1	1	1	1	1
8	1 1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
9	11	1	1	1	1	1	1	1	0	1	1	1	1	1	1
10	1 1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
11	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
12	1 1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
13	1 1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
14	1 1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
15	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 3 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

# ${\bf Line~4~intersects}$

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 5 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 6 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

## Line 7 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 8 intersects

	Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
ĺ	in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 9 intersects

	Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
i	n point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 10 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

#### Line 11 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

### ${\bf Line~12~intersects}$

	Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
ĺ	in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

### Line 13 intersects

Line	0	$\ell_1$									$\ell_{10}$			$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

### Line 14 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

### Line 15 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

The surface has 257 points:

The points on the surface are:

$0: P_0 = (1, 0, 0, 0)$	14: $P_{195} = (0, 11, 1, 0)$	$28: P_{285} = (11, 0, 0, 1)$
$1: P_3 = (0,0,0,1)$	15: $P_{196} = (1, 11, 1, 0)$	$29: P_{286} = (12, 0, 0, 1)$
$2: P_4 = (1, 1, 1, 1)$	$16: P_{261} = (2, 15, 1, 0)$	$30: P_{287} = (13, 0, 0, 1)$
$3: P_5 = (1, 1, 0, 0)$	$17: P_{262} = (3, 15, 1, 0)$	$31: P_{288} = (14, 0, 0, 1)$
$4: P_{35} = (0, 1, 1, 0)$	$18: P_{275} = (1, 0, 0, 1)$	$32: P_{289} = (15, 0, 0, 1)$
$5: P_{36} = (1, 1, 1, 0)$	$19: P_{276} = (2, 0, 0, 1)$	$33: P_{291} = (1, 1, 0, 1)$
$6: P_{71} = (4, 3, 1, 0)$	$20: P_{277} = (3, 0, 0, 1)$	$34: P_{308} = (2, 2, 0, 1)$
$7: P_{72} = (5, 3, 1, 0)$	$21: P_{278} = (4,0,0,1)$	$35: P_{325} = (3, 3, 0, 1)$
$8: P_{107} = (8, 5, 1, 0)$	$22: P_{279} = (5, 0, 0, 1)$	$36: P_{342} = (4, 4, 0, 1)$
$9: P_{108} = (9, 5, 1, 0)$	$23: P_{280} = (6,0,0,1)$	$37: P_{359} = (5, 5, 0, 1)$
$10: P_{161} = (14, 8, 1, 0)$	$24: P_{281} = (7, 0, 0, 1)$	$38: P_{376} = (6, 6, 0, 1)$
$11: P_{162} = (15, 8, 1, 0)$	$25: P_{282} = (8, 0, 0, 1)$	$39: P_{393} = (7,7,0,1)$
$12: P_{179} = (0, 10, 1, 0)$	$26: P_{283} = (9, 0, 0, 1)$	$40: P_{410} = (8, 8, 0, 1)$
13: $P_{180} = (1, 10, 1, 0)$	$27: P_{284} = (10, 0, 0, 1)$	$41: P_{427} = (9, 9, 0, 1)$

```
42: P_{444} = (10, 10, 0, 1)
                                                                                       150: P_{2410} = (9, 5, 8, 1)
                                           96: P_{1487} = (14, 11, 4, 1)
                                                                                       151: P_{2417} = (0, 6, 8, 1)
43: P_{461} = (11, 11, 0, 1)
                                           97: P_{1498} = (9, 12, 4, 1)
44: P_{478} = (12, 12, 0, 1)
                                           98: P_{1502} = (13, 12, 4, 1)
                                                                                       152: P_{2425} = (8, 6, 8, 1)
                                                                                       153: P_{2449} = (0, 8, 8, 1)
45: P_{495} = (13, 13, 0, 1)
                                           99: P_{1516} = (11, 13, 4, 1)
46: P_{512} = (14, 14, 0, 1)
                                           100: P_{1520} = (15, 13, 4, 1)
                                                                                       154: P_{2457} = (8, 8, 8, 1)
47: P_{529} = (15, 15, 0, 1)
                                           101: P_{1529} = (8, 14, 4, 1)
                                                                                       155: P_{2545} = (0, 14, 8, 1)
48: P_{546} = (0, 1, 1, 1)
                                           102: P_{1533} = (12, 14, 4, 1)
                                                                                       156: P_{2553} = (8, 14, 8, 1)
49: P_{581} = (4, 3, 1, 1)
                                           103: P_{1579} = (10, 1, 5, 1)
                                                                                       157: P_{2566} = (5, 15, 8, 1)
50: P_{582} = (5, 3, 1, 1)
                                           104: P_{1584} = (15, 1, 5, 1)
                                                                                       158: P_{2574} = (13, 15, 8, 1)
51: P_{617} = (8, 5, 1, 1)
                                           105: P_{1602} = (1, 3, 5, 1)
                                                                                       159: P_{2615} = (6, 2, 9, 1)
52: P_{618} = (9, 5, 1, 1)
                                           106: P_{1605} = (4, 3, 5, 1)
                                                                                       160: P_{2624} = (15, 2, 9, 1)
53: P_{671} = (14, 8, 1, 1)
                                           107: P_{1633} = (0, 5, 5, 1)
                                                                                       161: P_{2657} = (0, 5, 9, 1)
54: P_{672} = (15, 8, 1, 1)
                                           108: P_{1638} = (5, 5, 5, 1)
                                                                                       162: P_{2666} = (9, 5, 9, 1)
55: P_{689} = (0, 10, 1, 1)
                                           109: P_{1684} = (3, 8, 5, 1)
                                                                                       163: P_{2680} = (7, 6, 9, 1)
                                                                                       164: P_{2687} = (14, 6, 9, 1)
56: P_{690} = (1, 10, 1, 1)
                                           110: P_{1687} = (6, 8, 5, 1)
57: P_{705} = (0, 11, 1, 1)
                                           111: P_{1697} = (0, 9, 5, 1)
                                                                                       165: P_{2692} = (3,7,9,1)
                                           112: P_{1702} = (5, 9, 5, 1)
58: P_{706} = (1, 11, 1, 1)
                                                                                       166: P_{2699} = (10, 7, 9, 1)
                                           113: P_{1745} = (0, 12, 5, 1)
                                                                                       167: P_{2721} = (0, 9, 9, 1)
59: P_{771} = (2, 15, 1, 1)
60: P_{772} = (3, 15, 1, 1)
                                                                                       168: P_{2730} = (9, 9, 9, 1)
                                           114: P_{1750} = (5, 12, 5, 1)
61: P_{817} = (0, 2, 2, 1)
                                           115: P_{1801} = (8, 15, 5, 1)
                                                                                       169: P_{2739} = (2, 10, 9, 1)
62: P_{819} = (2, 2, 2, 1)
                                           116: P_{1806} = (13, 15, 5, 1)
                                                                                       170: P_{2748} = (11, 10, 9, 1)
63: P_{889} = (8, 6, 2, 1)
                                                                                       171: P_{2769} = (0, 12, 9, 1)
                                           117: P_{1850} = (9, 2, 6, 1)
                                                                                       172: P_{2778} = (9, 12, 9, 1)
64: P_{891} = (10, 6, 2, 1)
                                           118: P_{1856} = (15, 2, 6, 1)
65: P_{901} = (4,7,2,1)
                                           119: P_{1905} = (0, 6, 6, 1)
                                                                                       173: P_{2849} = (0, 1, 10, 1)
66: P_{903} = (6,7,2,1)
                                           120: P_{1911} = (6, 6, 6, 1)
                                                                                       174: P_{2859} = (10, 1, 10, 1)
67: P_{934} = (5, 9, 2, 1)
                                           121: P_{1923} = (2,7,6,1)
                                                                                       175: P_{2872} = (7, 2, 10, 1)
68: P_{936} = (7, 9, 2, 1)
                                           122: P_{1925} = (4,7,6,1)
                                                                                       176: P_{2878} = (13, 2, 10, 1)
69: P_{954} = (9, 10, 2, 1)
                                           123: P_{1937} = (0, 8, 6, 1)
                                                                                       177: P_{2931} = (2, 6, 10, 1)
                                                                                       178: P_{2937} = (8, 6, 10, 1)
70: P_{956} = (11, 10, 2, 1)
                                           124: P_{1943} = (6, 8, 6, 1)
71: P_{993} = (0, 13, 2, 1)
                                           125: P_{1963} = (10, 9, 6, 1)
                                                                                       179: P_{2948} = (3, 7, 10, 1)
72: P_{995} = (2, 13, 2, 1)
                                           126: P_{1965} = (12, 9, 6, 1)
                                                                                       180: P_{2954} = (9, 7, 10, 1)
                                                                                       181: P_{2983} = (6, 9, 10, 1)
73: P_{1025} = (0, 15, 2, 1)
                                           127: P_{1970} = (1, 10, 6, 1)
                                           128: P_{1976} = (7, 10, 6, 1)
74: P_{1027} = (2, 15, 2, 1)
                                                                                       182: P_{2989} = (12, 9, 10, 1)
75: P_{1065} = (8, 1, 3, 1)
                                           129: P_{2033} = (0, 14, 6, 1)
                                                                                       183: P_{2993} = (0, 10, 10, 1)
76: P_{1068} = (11, 1, 3, 1)
                                           130: P_{2039} = (6, 14, 6, 1)
                                                                                       184: P_{3003} = (10, 10, 10, 1)
                                           131: P_{2107} = (10, 2, 7, 1)
77: P_{1089} = (0, 3, 3, 1)
                                                                                       185: P_{3009} = (0, 11, 10, 1)
78: P_{1092} = (3, 3, 3, 1)
                                           132: P_{2110} = (13, 2, 7, 1)
                                                                                       186: P_{3019} = (10, 11, 10, 1)
                                                                                       187: P_{3105} = (0, 1, 11, 1)
79: P_{1105} = (0, 4, 3, 1)
                                           133: P_{2113} = (0, 3, 7, 1)
80: P_{1108} = (3,4,3,1)
                                           134: P_{2120} = (7, 3, 7, 1)
                                                                                       188: P_{3116} = (11, 1, 11, 1)
81: P_{1133} = (12, 5, 3, 1)
                                           135: P_{2129} = (0, 4, 7, 1)
                                                                                       189: P_{3160} = (7, 4, 11, 1)
82: P_{1136} = (15, 5, 3, 1)
                                           136: P_{2136} = (7,4,7,1)
                                                                                       190: P_{3165} = (12, 4, 11, 1)
                                           137: P_{2170} = (9, 6, 7, 1)
83: P_{1153} = (0,7,3,1)
                                                                                       191: P_{3249} = (0, 10, 11, 1)
84: P_{1156} = (3,7,3,1)
                                           138: P_{2175} = (14, 6, 7, 1)
                                                                                       192: P_{3260} = (11, 10, 11, 1)
85: P_{1174} = (5, 8, 3, 1)
                                           139: P_{2177} = (0,7,7,1)
                                                                                       193: P_{3265} = (0, 11, 11, 1)
86: P_{1175} = (6, 8, 3, 1)
                                           140: P_{2184} = (7,7,7,1)
                                                                                       194: P_{3276} = (11, 11, 11, 1)
                                                                                       195: P_{3286} = (5, 12, 11, 1)
                                           141: P_{2211} = (2, 9, 7, 1)
87: P_{1282} = (1, 15, 3, 1)
88: P_{1283} = (2, 15, 3, 1)
                                           142: P_{2214} = (5, 9, 7, 1)
                                                                                       196: P_{3295} = (14, 12, 11, 1)
89: P_{1345} = (0, 3, 4, 1)
                                           143: P_{2226} = (1, 10, 7, 1)
                                                                                       197: P_{3301} = (4, 13, 11, 1)
90: P_{1349} = (4, 3, 4, 1)
                                           144: P_{2231} = (6, 10, 7, 1)
                                                                                       198: P_{3312} = (15, 13, 11, 1)
91: P_{1361} = (0, 4, 4, 1)
                                           145: P_{2340} = (3, 1, 8, 1)
                                                                                       199: P_{3319} = (6, 14, 11, 1)
92: P_{1365} = (4, 4, 4, 1)
                                           146: P_{2348} = (11, 1, 8, 1)
                                                                                       200: P_{3326} = (13, 14, 11, 1)
                                           147: P_{2376} = (7, 3, 8, 1)
93: P_{1409} = (0,7,4,1)
                                                                                       201: P_{3416} = (7, 4, 12, 1)
94: P_{1413} = (4,7,4,1)
                                           148: P_{2384} = (15, 3, 8, 1)
                                                                                       202: P_{3420} = (11, 4, 12, 1)
95: P_{1483} = (10, 11, 4, 1)
                                           149: P_{2402} = (1, 5, 8, 1)
                                                                                       203: P_{3425} = (0, 5, 12, 1)
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204: P_{3437} = (12, 5, 12, 1)
                                           222: P_{3802} = (9, 12, 13, 1)
                                                                                      240: P_{4077} = (12, 13, 14, 1)
205: P_{3489} = (0, 9, 12, 1)
                                           223: P_{3809} = (0, 13, 13, 1)
                                                                                      241: P_{4081} = (0, 14, 14, 1)
206: P_{3501} = (12, 9, 12, 1)
                                           224: P_{3822} = (13, 13, 13, 1)
                                                                                      242: P_{4095} = (14, 14, 14, 1)
207: P_{3522} = (1, 11, 12, 1)
                                           225: P_{3831} = (6, 14, 13, 1)
                                                                                      243: P_{4134} = (5, 1, 15, 1)
208: P_{3534} = (13, 11, 12, 1)
                                           226: P_{3836} = (11, 14, 13, 1)
                                                                                      244: P_{4139} = (10, 1, 15, 1)
                                                                                      245: P_{4145} = (0, 2, 15, 1)
209: P_{3537} = (0, 12, 12, 1)
                                           227: P_{3841} = (0, 15, 13, 1)
                                                                                      246: P_{4160} = (15, 2, 15, 1)
210: P_{3549} = (12, 12, 12, 1)
                                           228: P_{3854} = (13, 15, 13, 1)
                                                                                      247: P_{4168} = (7, 3, 15, 1)
211: P_{3555} = (2, 13, 12, 1)
                                           229: P_{3924} = (3, 4, 14, 1)
212: P_{3567} = (14, 13, 12, 1)
                                           230: P_{3934} = (13, 4, 14, 1)
                                                                                      248: P_{4169} = (8, 3, 15, 1)
213: P_{3573} = (4, 14, 12, 1)
                                           231: P_{3953} = (0, 6, 14, 1)
                                                                                      249: P_{4196} = (3, 5, 15, 1)
214: P_{3577} = (8, 14, 12, 1)
                                           232: P_{3967} = (14, 6, 14, 1)
                                                                                      250: P_{4205} = (12, 5, 15, 1)
                                           233: P_{3985} = (0, 8, 14, 1)
215: P_{3633} = (0, 2, 13, 1)
                                                                                      251: P_{4242} = (1, 8, 15, 1)
216: P_{3646} = (13, 2, 13, 1)
                                           234: P_{3999} = (14, 8, 14, 1)
                                                                                      252: P_{4255} = (14, 8, 15, 1)
                                                                                      253: P_{4321} = (0, 13, 15, 1)
217: P_{3668} = (3, 4, 13, 1)
                                           235: P_{4037} = (4, 11, 14, 1)
218: P_{3679} = (14, 4, 13, 1)
                                           236: P_{4043} = (10, 11, 14, 1)
                                                                                      254: P_{4336} = (15, 13, 15, 1)
219: P_{3778} = (1, 11, 13, 1)
                                           237: P_{4054} = (5, 12, 14, 1)
                                                                                      255: P_{4353} = (0, 15, 15, 1)
                                                                                      256: P_{4368} = (15, 15, 15, 1)
220: P_{3789} = (12, 11, 13, 1)
                                           238: P_{4060} = (11, 12, 14, 1)
221: P_{3797} = (4, 12, 13, 1)
                                           239: P_{4067} = (2, 13, 14, 1)
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