

Rank-487 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_3 + X_0 X_1^2 + X_1^2 X_2 = 0$$

(0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0)

The point rank of the equation over GF(32) is -2111764435

General information

Number of lines	1
Number of points	1089
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	33
Number of points off lines	1056
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33
Type of lines on points	$1^{33}, 0^{1056}$

Singular Points

The surface has 0 singular points:

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{2082} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{2082} = \mathbf{Pl}(0, 0, 1, 1, 1, 1)_{70562}$$

Rank of lines: (2082)

Rank of points on Klein quadric: (70562)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 33 single points:

The single points on the surface are:

- | | |
|--|--|
| 0 : $P_4 = (1, 1, 1, 1)$ lies on line ℓ_0 | 17 : $P_{2609} = (16, 16, 1, 1)$ lies on line ℓ_0 |
| 1 : $P_5 = (1, 1, 0, 0)$ lies on line ℓ_0 | 18 : $P_{2642} = (17, 17, 1, 1)$ lies on line ℓ_0 |
| 2 : $P_{2082} = (0, 0, 1, 1)$ lies on line ℓ_0 | 19 : $P_{2675} = (18, 18, 1, 1)$ lies on line ℓ_0 |
| 3 : $P_{2147} = (2, 2, 1, 1)$ lies on line ℓ_0 | 20 : $P_{2708} = (19, 19, 1, 1)$ lies on line ℓ_0 |
| 4 : $P_{2180} = (3, 3, 1, 1)$ lies on line ℓ_0 | 21 : $P_{2741} = (20, 20, 1, 1)$ lies on line ℓ_0 |
| 5 : $P_{2213} = (4, 4, 1, 1)$ lies on line ℓ_0 | 22 : $P_{2774} = (21, 21, 1, 1)$ lies on line ℓ_0 |
| 6 : $P_{2246} = (5, 5, 1, 1)$ lies on line ℓ_0 | 23 : $P_{2807} = (22, 22, 1, 1)$ lies on line ℓ_0 |
| 7 : $P_{2279} = (6, 6, 1, 1)$ lies on line ℓ_0 | 24 : $P_{2840} = (23, 23, 1, 1)$ lies on line ℓ_0 |
| 8 : $P_{2312} = (7, 7, 1, 1)$ lies on line ℓ_0 | 25 : $P_{2873} = (24, 24, 1, 1)$ lies on line ℓ_0 |
| 9 : $P_{2345} = (8, 8, 1, 1)$ lies on line ℓ_0 | 26 : $P_{2906} = (25, 25, 1, 1)$ lies on line ℓ_0 |
| 10 : $P_{2378} = (9, 9, 1, 1)$ lies on line ℓ_0 | 27 : $P_{2939} = (26, 26, 1, 1)$ lies on line ℓ_0 |
| 11 : $P_{2411} = (10, 10, 1, 1)$ lies on line ℓ_0 | 28 : $P_{2972} = (27, 27, 1, 1)$ lies on line ℓ_0 |
| 12 : $P_{2444} = (11, 11, 1, 1)$ lies on line ℓ_0 | 29 : $P_{3005} = (28, 28, 1, 1)$ lies on line ℓ_0 |
| 13 : $P_{2477} = (12, 12, 1, 1)$ lies on line ℓ_0 | 30 : $P_{3038} = (29, 29, 1, 1)$ lies on line ℓ_0 |
| 14 : $P_{2510} = (13, 13, 1, 1)$ lies on line ℓ_0 | 31 : $P_{3071} = (30, 30, 1, 1)$ lies on line ℓ_0 |
| 15 : $P_{2543} = (14, 14, 1, 1)$ lies on line ℓ_0 | 32 : $P_{3104} = (31, 31, 1, 1)$ lies on line ℓ_0 |
| 16 : $P_{2576} = (15, 15, 1, 1)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 1056 points not on any line:

Too many to print.

Line Intersection Graph

$$\begin{array}{c|c} & 0 \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line
in point

The surface has 1089 points:

Too many to print.