Rank-355 over GF(32)

January 15, 2021

The equation

The equation of the surface is:

$$X_3^3 + X_0^2 X_1 + X_0^2 X_3 + X_1^2 X_2 = 0$$

(0, 0, 0, 1, 1, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0) The point rank of the equation over GF(32) is -2111765459

General information

Number of lines	3
Number of points	1089
Number of singular points	1
Number of Eckardt points	0
Number of double points	2
Number of single points	95
Number of points off lines	992
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^{3}
Type of lines on points	$2^2, 1^{95}, 0^{992}$

Singular Points

The surface has 1 singular points:

$$0: P_2 = \mathbf{P}(0,0,1,0) = \mathbf{P}(0,0,1,0)$$

The 3 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1024} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1024} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{33} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{33} = \mathbf{Pl}(1, 0, 1, 0, 1, 0)_{1153}$$

$$\ell_2 = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{34848} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{34848} = \mathbf{Pl}(0, 1, 1, 0, 0, 0)_{34}$$

Rank of lines: (1024, 33, 34848)

Rank of points on Klein quadric: (2, 1153, 34)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 2 Double points: The double points on the surface are:

$$P_0 = (1, 0, 0, 0) = \ell_0 \cap \ell_1$$

$$P_2 = (0, 0, 1, 0) = \ell_0 \cap \ell_2$$

Single Points

The surface has 95 single points: The single points on the surface are:

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0: P_4 = (1, 1, 1, 1) lies on line \ell_1
                                                                      26: P_{61} = (26, 0, 1, 0) lies on line \ell_0
1: P_{36} = (1, 0, 1, 0) lies on line \ell_0
                                                                      27: P_{62} = (27, 0, 1, 0) lies on line \ell_0
2: P_{37} = (2,0,1,0) lies on line \ell_0
                                                                      28: P_{63} = (28, 0, 1, 0) lies on line \ell_0
3: P_{38} = (3,0,1,0) lies on line \ell_0
                                                                      29: P_{64} = (29, 0, 1, 0) lies on line \ell_0
4: P_{39} = (4, 0, 1, 0) lies on line \ell_0
                                                                      30: P_{65} = (30, 0, 1, 0) lies on line \ell_0
5: P_{40} = (5, 0, 1, 0) lies on line \ell_0
                                                                      31: P_{66} = (31, 0, 1, 0) lies on line \ell_0
6: P_{41} = (6,0,1,0) lies on line \ell_0
                                                                      32: P_{1059} = (1,0,0,1) lies on line \ell_2
                                                                      33: P_{2083} = (1, 0, 1, 1) lies on line \ell_2
7: P_{42} = (7,0,1,0) lies on line \ell_0
8: P_{43} = (8,0,1,0) lies on line \ell_0
                                                                      34: P_{2114} = (0, 1, 1, 1) lies on line \ell_1
                                                                      35: P_{2115} = (2, 1, 1, 1) lies on line \ell_1
9: P_{44} = (9, 0, 1, 0) lies on line \ell_0
                                                                      36: P_{2116} = (3, 1, 1, 1) lies on line \ell_1
10: P_{45} = (10, 0, 1, 0) lies on line \ell_0
11: P_{46} = (11, 0, 1, 0) lies on line \ell_0
                                                                      37: P_{2117} = (4, 1, 1, 1) lies on line \ell_1
                                                                      38: P_{2118} = (5, 1, 1, 1) lies on line \ell_1
12: P_{47} = (12, 0, 1, 0) lies on line \ell_0
13: P_{48} = (13, 0, 1, 0) lies on line \ell_0
                                                                      39: P_{2119} = (6, 1, 1, 1) lies on line \ell_1
14 : P_{49} = (14, 0, 1, 0) lies on line \ell_0
                                                                      40: P_{2120} = (7, 1, 1, 1) lies on line \ell_1
15: P_{50} = (15, 0, 1, 0) lies on line \ell_0
                                                                      41: P_{2121} = (8, 1, 1, 1) lies on line \ell_1
                                                                      42 : P_{2122} = (9, 1, 1, 1) lies on line \ell_1
16: P_{51} = (16, 0, 1, 0) lies on line \ell_0
17: P_{52} = (17, 0, 1, 0) lies on line \ell_0
                                                                      43: P_{2123} = (10, 1, 1, 1) lies on line \ell_1
18: P_{53} = (18, 0, 1, 0) lies on line \ell_0
                                                                      44: P_{2124} = (11, 1, 1, 1) lies on line \ell_1
19 : P_{54} = (19, 0, 1, 0) lies on line \ell_0
                                                                      45: P_{2125} = (12, 1, 1, 1) lies on line \ell_1
20: P_{55} = (20, 0, 1, 0) lies on line \ell_0
                                                                      46: P_{2126} = (13, 1, 1, 1) lies on line \ell_1
                                                                      47: P_{2127} = (14, 1, 1, 1) lies on line \ell_1
21: P_{56} = (21, 0, 1, 0) lies on line \ell_0
22: P_{57} = (22, 0, 1, 0) lies on line \ell_0
                                                                      48: P_{2128} = (15, 1, 1, 1) lies on line \ell_1
23: P_{58} = (23, 0, 1, 0) lies on line \ell_0
                                                                      49: P_{2129} = (16, 1, 1, 1) lies on line \ell_1
24: P_{59} = (24, 0, 1, 0) lies on line \ell_0
                                                                      50: P_{2130} = (17, 1, 1, 1) lies on line \ell_1
25: P_{60} = (25, 0, 1, 0) lies on line \ell_0
                                                                      51: P_{2131} = (18, 1, 1, 1) lies on line \ell_1
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74 : P_{12322} = (1, 0, 11, 1) lies on line \ell_2
52: P_{2132} = (19, 1, 1, 1) lies on line \ell_1
                                                                      75: P_{13346} = (1, 0, 12, 1) lies on line \ell_2
53: P_{2133} = (20, 1, 1, 1) lies on line \ell_1
54: P_{2134} = (21, 1, 1, 1) lies on line \ell_1
                                                                      76: P_{14370} = (1, 0, 13, 1) lies on line \ell_2
                                                                      77: P_{15394} = (1, 0, 14, 1) lies on line \ell_2
55: P_{2135} = (22, 1, 1, 1) lies on line \ell_1
56 : P_{2136} = (23, 1, 1, 1) lies on line \ell_1
                                                                      78: P_{16418} = (1, 0, 15, 1) lies on line \ell_2
                                                                      79: P_{17442} = (1, 0, 16, 1) lies on line \ell_2
57: P_{2137} = (24, 1, 1, 1) lies on line \ell_1
58: P_{2138} = (25, 1, 1, 1) lies on line \ell_1
                                                                      80: P_{18466} = (1, 0, 17, 1) lies on line \ell_2
59: P_{2139} = (26, 1, 1, 1) lies on line \ell_1
                                                                      81: P_{19490} = (1, 0, 18, 1) lies on line \ell_2
60: P_{2140} = (27, 1, 1, 1) lies on line \ell_1
                                                                      82: P_{20514} = (1, 0, 19, 1) lies on line \ell_2
61: P_{2141} = (28, 1, 1, 1) lies on line \ell_1
                                                                      83: P_{21538} = (1, 0, 20, 1) lies on line \ell_2
62: P_{2142} = (29, 1, 1, 1) lies on line \ell_1
                                                                      84: P_{22562} = (1, 0, 21, 1) lies on line \ell_2
                                                                      85 : P_{23586} = (1, 0, 22, 1) lies on line \ell_2
63: P_{2143} = (30, 1, 1, 1) lies on line \ell_1
64: P_{2144} = (31, 1, 1, 1) lies on line \ell_1
                                                                      86: P_{24610} = (1, 0, 23, 1) lies on line \ell_2
                                                                      87: P_{25634} = (1, 0, 24, 1) lies on line \ell_2
65: P_{3106} = (1,0,2,1) lies on line \ell_2
66: P_{4130} = (1, 0, 3, 1) lies on line \ell_2
                                                                      88: P_{26658} = (1, 0, 25, 1) lies on line \ell_2
67: P_{5154} = (1, 0, 4, 1) lies on line \ell_2
                                                                      89: P_{27682} = (1, 0, 26, 1) lies on line \ell_2
68: P_{6178} = (1, 0, 5, 1) lies on line \ell_2
                                                                      90: P_{28706} = (1, 0, 27, 1) lies on line \ell_2
                                                                      91 : P_{29730} = (1, 0, 28, 1) lies on line \ell_2
69: P_{7202} = (1,0,6,1) lies on line \ell_2
70: P_{8226} = (1,0,7,1) lies on line \ell_2
                                                                      92: P_{30754} = (1, 0, 29, 1) lies on line \ell_2
71: P_{9250} = (1,0,8,1) lies on line \ell_2
                                                                      93: P_{31778} = (1, 0, 30, 1) lies on line \ell_2
72: P_{10274} = (1, 0, 9, 1) lies on line \ell_2
                                                                      94: P_{32802} = (1, 0, 31, 1) lies on line \ell_2
73: P_{11298} = (1, 0, 10, 1) lies on line \ell_2
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The single points on the surface are:

Points on surface but on no line

The surface has 992 points not on any line: The points on the surface but not on lines are:

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0: P_1 = (0, 1, 0, 0)
                                                                  22: P_{768} = (29, 22, 1, 0)
1: P_{68} = (1, 1, 1, 0)
                                                                  23: P_{799} = (28, 23, 1, 0)
2: P_{126} = (27, 2, 1, 0)
                                                                  24: P_{826} = (23, 24, 1, 0)
                                                                  25: P_{857} = (22, 25, 1, 0)
3: P_{157} = (26, 3, 1, 0)
4: P_{165} = (2, 4, 1, 0)
                                                                  26: P_{879} = (12, 26, 1, 0)
5: P_{198} = (3, 5, 1, 0)
                                                                  27: P_{912} = (13, 27, 1, 0)
6: P_{252} = (25, 6, 1, 0)
                                                                  28: P_{952} = (21, 28, 1, 0)
7: P_{283} = (24, 7, 1, 0)
                                                                  29: P_{983} = (20, 29, 1, 0)
                                                                  30: P_{1009} = (14, 30, 1, 0)
8: P_{310} = (19, 8, 1, 0)
9: P_{341} = (18, 9, 1, 0)
                                                                  31: P_{1042} = (15, 31, 1, 0)
10: P_{363} = (8, 10, 1, 0)
                                                                  32: P_{1143} = (21, 2, 0, 1)
11: P_{396} = (9, 11, 1, 0)
                                                                  33: P_{1185} = (31, 3, 0, 1)
12: P_{436} = (17, 12, 1, 0)
                                                                  34: P_{1214} = (28, 4, 0, 1)
13: P_{467} = (16, 13, 1, 0)
                                                                  35: P_{1236} = (18, 5, 0, 1)
14: P_{493} = (10, 14, 1, 0)
                                                                  36: P_{1267} = (17, 6, 0, 1)
15: P_{526} = (11, 15, 1, 0)
                                                                  37: P_{1292} = (10, 7, 0, 1)
16: P_{551} = (4, 16, 1, 0)
                                                                  38: P_{1316} = (2, 8, 0, 1)
                                                                  39: P_{1375} = (29, 9, 0, 1)
17: P_{584} = (5, 17, 1, 0)
18: P_{642} = (31, 18, 1, 0)
                                                                  40: P_{1382} = (4, 10, 0, 1)
19: P_{673} = (30, 19, 1, 0)
                                                                  41: P_{1432} = (22, 11, 0, 1)
20: P_{681} = (6, 20, 1, 0)
                                                                  42: P_{1453} = (11, 12, 0, 1)
21: P_{714} = (7, 21, 1, 0)
                                                                  43: P_{1498} = (24, 13, 0, 1)
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44: P_{1522} = (16, 14, 0, 1)
                                                                 98: P_{3375} = (14, 8, 2, 1)
45: P_{1563} = (25, 15, 0, 1)
                                                                 99: P_{3404} = (11, 9, 2, 1)
                                                                 100: P_{3451} = (26, 10, 2, 1)
46: P_{1593} = (23, 16, 0, 1)
47: P_{1611} = (9, 17, 0, 1)
                                                                 101: P_{3469} = (12, 11, 2, 1)
48: P_{1654} = (20, 18, 0, 1)
                                                                 102: P_{3498} = (9, 12, 2, 1)
49: P_{1693} = (27, 19, 0, 1)
                                                                 103: P_{3526} = (5, 13, 2, 1)
50: P_{1710} = (12, 20, 0, 1)
                                                                 104: P_{3571} = (18, 14, 2, 1)
51: P_{1744} = (14, 21, 0, 1)
                                                                 105: P_{3614} = (29, 15, 2, 1)
52: P_{1765} = (3, 22, 0, 1)
                                                                 106: P_{3625} = (8, 16, 2, 1)
53: P_{1813} = (19, 23, 0, 1)
                                                                 107: P_{3672} = (23, 17, 2, 1)
54: P_{1834} = (8, 24, 0, 1)
                                                                 108: P_{3682} = (1, 18, 2, 1)
55: P_{1863} = (5, 25, 0, 1)
                                                                 109: P_{3737} = (24, 19, 2, 1)
56: P_{1905} = (15, 26, 0, 1)
                                                                 110: P_{3747} = (2, 20, 2, 1)
57: P_{1929} = (7, 27, 0, 1)
                                                                 111: P_{3785} = (8, 21, 2, 1)
                                                                 112: P_{3811} = (2, 22, 2, 1)
58: P_{1984} = (30, 28, 0, 1)
59: P_{2012} = (26, 29, 0, 1)
                                                                 113: P_{3846} = (5, 23, 2, 1)
60: P_{2031} = (13, 30, 0, 1)
                                                                 114: P_{3891} = (18, 24, 2, 1)
61: P_{2056} = (6, 31, 0, 1)
                                                                 115: P_{3931} = (26, 25, 2, 1)
62: P_{2171} = (26, 2, 1, 1)
                                                                 116: P_{3965} = (28, 26, 2, 1)
                                                                 117: P_{3978} = (9, 27, 2, 1)
63: P_{2204} = (27, 3, 1, 1)
64: P_{2212} = (3, 4, 1, 1)
                                                                 118: P_{4012} = (11, 28, 2, 1)
65: P_{2243} = (2, 5, 1, 1)
                                                                 119: P_{4056} = (23, 29, 2, 1)
66: P_{2297} = (24, 6, 1, 1)
                                                                 120: P_{4095} = (30, 30, 2, 1)
67: P_{2330} = (25, 7, 1, 1)
                                                                 121: P_{4097} = (0, 31, 2, 1)
68: P_{2355} = (18, 8, 1, 1)
                                                                 122: P_{4216} = (23, 2, 3, 1)
69: P_{2388} = (19, 9, 1, 1)
                                                                 123: P_{4249} = (24, 3, 3, 1)
                                                                 124: P_{4259} = (2,4,3,1)
70: P_{2410} = (9, 10, 1, 1)
71: P_{2441} = (8, 11, 1, 1)
                                                                 125: P_{4303} = (14, 5, 3, 1)
                                                                 126: P_{4326} = (5, 6, 3, 1)
72: P_{2481} = (16, 12, 1, 1)
73: P_{2514} = (17, 13, 1, 1)
                                                                 127: P_{4382} = (29, 7, 3, 1)
74: P_{2540} = (11, 14, 1, 1)
                                                                 128: P_{4415} = (30, 8, 3, 1)
75: P_{2571} = (10, 15, 1, 1)
                                                                 129: P_{4422} = (5, 9, 3, 1)
76: P_{2598} = (5, 16, 1, 1)
                                                                 130: P_{4472} = (23, 10, 3, 1)
77: P_{2629} = (4, 17, 1, 1)
                                                                 131: P_{4499} = (18, 11, 3, 1)
78: P_{2687} = (30, 18, 1, 1)
                                                                 132: P_{4531} = (18, 12, 3, 1)
79: P_{2720} = (31, 19, 1, 1)
                                                                 133: P_{4557} = (12, 13, 3, 1)
80: P_{2728} = (7, 20, 1, 1)
                                                                 134: P_{4586} = (9, 14, 3, 1)
                                                                 135: P_{4623} = (14, 15, 3, 1)
81: P_{2759} = (6, 21, 1, 1)
82: P_{2813} = (28, 22, 1, 1)
                                                                 136: P_{4667} = (26, 16, 3, 1)
83: P_{2846} = (29, 23, 1, 1)
                                                                 137: P_{4699} = (26, 17, 3, 1)
84: P_{2871} = (22, 24, 1, 1)
                                                                 138: P_{4716} = (11, 18, 3, 1)
                                                                 139: P_{4765} = (28, 19, 3, 1)
85: P_{2904} = (23, 25, 1, 1)
86: P_{2926} = (13, 26, 1, 1)
                                                                 140: P_{4778} = (9, 20, 3, 1)
                                                                 141: P_{4801} = (0, 21, 3, 1)
87: P_{2957} = (12, 27, 1, 1)
88: P_{2997} = (20, 28, 1, 1)
                                                                 142: P_{4862} = (29, 22, 3, 1)
89: P_{3030} = (21, 29, 1, 1)
                                                                 143: P_{4876} = (11, 23, 3, 1)
90: P_{3056} = (15, 30, 1, 1)
                                                                 144: P_{4909} = (12, 24, 3, 1)
91: P_{3087} = (14, 31, 1, 1)
                                                                 145: P_{4937} = (8, 25, 3, 1)
92: P_{3193} = (24, 2, 2, 1)
                                                                 146: P_{4991} = (30, 26, 3, 1)
93: P_{3229} = (28, 3, 2, 1)
                                                                 147: P_{4995} = (2, 27, 3, 1)
94: P_{3262} = (29, 4, 2, 1)
                                                                 148: P_{5026} = (1, 28, 3, 1)
95: P_{3295} = (30, 5, 2, 1)
                                                                 149: P_{5081} = (24, 29, 3, 1)
96: P_{3309} = (12, 6, 2, 1)
                                                                 150: P_{5117} = (28, 30, 3, 1)
97: P_{3343} = (14, 7, 2, 1)
                                                                 151 : P_{5129} = (8, 31, 3, 1)
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206: P_{7018} = (9, 26, 5, 1)
152: P_{5228} = (11, 2, 4, 1)
153: P_{5272} = (23, 3, 4, 1)
                                                                 207: P_{7067} = (26, 27, 5, 1)
154: P_{5288} = (7, 4, 4, 1)
                                                                 208: P_{7073} = (0, 28, 5, 1)
                                                                 209: P_{7116} = (11, 29, 5, 1)
155: P_{5336} = (23, 5, 4, 1)
156: P_{5348} = (3, 6, 4, 1)
                                                                 210: P_{7148} = (11, 30, 5, 1)
157: P_{5386} = (9,7,4,1)
                                                                 211: P_{7199} = (30, 31, 5, 1)
158: P_{5416} = (7, 8, 4, 1)
                                                                 212: P_{7271} = (6, 2, 6, 1)
159: P_{5442} = (1, 9, 4, 1)
                                                                 213: P_{7317} = (20, 3, 6, 1)
160: P_{5503} = (30, 10, 4, 1)
                                                                 214: P_{7335} = (6, 4, 6, 1)
161: P_{5520} = (15, 11, 4, 1)
                                                                 215: P_{7388} = (27, 5, 6, 1)
162: P_{5561} = (24, 12, 4, 1)
                                                                 216: P_{7423} = (30, 6, 6, 1)
163: P_{5579} = (10, 13, 4, 1)
                                                                 217: P_{7438} = (13, 7, 6, 1)
164: P_{5604} = (3, 14, 4, 1)
                                                                 218: P_{7468} = (11, 8, 6, 1)
165: P_{5659} = (26, 15, 4, 1)
                                                                 219: P_{7512} = (23, 9, 6, 1)
                                                                 220:\ P_{7521}=(0,10,6,1)
166: P_{5687} = (22, 16, 4, 1)
167: P_{5716} = (19, 17, 4, 1)
                                                                 221: P_{7574} = (21, 11, 6, 1)
168: P_{5729} = (0, 18, 4, 1)
                                                                 222: P_{7611} = (26, 12, 6, 1)
                                                                 223: P_{7640} = (23, 13, 6, 1)
169: P_{5780} = (19, 19, 4, 1)
                                                                 224: P_{7650} = (1, 14, 6, 1)
170: P_{5819} = (26, 20, 4, 1)
171: P_{5855} = (30, 21, 4, 1)
                                                                 225: P_{7711} = (30, 15, 6, 1)
172: P_{5881} = (24, 22, 4, 1)
                                                                 226: P_{7722} = (9, 16, 6, 1)
                                                                 227: P_{7758} = (13, 17, 6, 1)
173: P_{5904} = (15, 23, 4, 1)
                                                                 228: P_{7798} = (21, 18, 6, 1)
174: P_{5938} = (17, 24, 4, 1)
175: P_{5957} = (4, 25, 4, 1)
                                                                 229: P_{7825} = (16, 19, 6, 1)
176: P_{5996} = (11, 26, 4, 1)
                                                                 230: P_{7861} = (20, 20, 6, 1)
177: P_{6034} = (17, 27, 4, 1)
                                                                 231: P_{7897} = (24, 21, 6, 1)
178: P_{6059} = (10, 28, 4, 1)
                                                                 232: P_{7930} = (25, 22, 6, 1)
179: P_{6085} = (4, 29, 4, 1)
                                                                 233: P_{7962} = (25, 23, 6, 1)
180: P_{6122} = (9, 30, 4, 1)
                                                                 234: P_{7980} = (11, 24, 6, 1)
181: P_{6167} = (22, 31, 4, 1)
                                                                 235: P_{8028} = (27, 25, 6, 1)
182: P_{6245} = (4, 2, 5, 1)
                                                                 236: P_{8057} = (24, 26, 6, 1)
183: P_{6292} = (19, 3, 5, 1)
                                                                 237: P_{8096} = (31, 27, 6, 1)
184: P_{6329} = (24, 4, 5, 1)
                                                                 238: P_{8128} = (31, 28, 6, 1)
185 : P_{6344} = (7, 5, 5, 1)
                                                                 239: P_{8138} = (9, 29, 6, 1)
                                                                 240: P_{8187} = (26, 30, 6, 1)
186: P_{6379} = (10, 6, 5, 1)
                                                                 241: P_{8209} = (16, 31, 6, 1)
187: P_{6427} = (26, 7, 5, 1)
188: P_{6456} = (23, 8, 5, 1)
                                                                 242: P_{8298} = (9, 2, 7, 1)
                                                                 243: P_{8337} = (16, 3, 7, 1)
189: P_{6480} = (15, 9, 5, 1)
190: P_{6516} = (19, 10, 5, 1)
                                                                 244: P_{8378} = (25, 4, 7, 1)
191: P_{6546} = (17, 11, 5, 1)
                                                                 245: P_{8396} = (11, 5, 7, 1)
192: P_{6564} = (3, 12, 5, 1)
                                                                 246: P_{8440} = (23, 6, 7, 1)
                                                                 247: P_{8479} = (30, 7, 7, 1)
193: P_{6596} = (3, 13, 5, 1)
194: P_{6649} = (24, 14, 5, 1)
                                                                 248: P_{8508} = (27, 8, 7, 1)
                                                                 249: P_{8538} = (25, 9, 7, 1)
195: P_{6666} = (9, 15, 5, 1)
196: P_{6693} = (4, 16, 5, 1)
                                                                 250: P_{8558} = (13, 10, 7, 1)
197: P_{6751} = (30, 17, 5, 1)
                                                                 251: P_{8588} = (11, 11, 7, 1)
198: P_{6763} = (10, 18, 5, 1)
                                                                 252: P_{8610} = (1, 12, 7, 1)
199: P_{6808} = (23, 19, 5, 1)
                                                                 253: P_{8671} = (30, 13, 7, 1)
200: P_{6834} = (17, 20, 5, 1)
                                                                 254: P_{8699} = (26, 14, 7, 1)
                                                                 255: P_{8718} = (13, 15, 7, 1)
201: P_{6871} = (22, 21, 5, 1)
                                                                 256: P_{8764} = (27, 16, 7, 1)
202: P_{6888} = (7, 22, 5, 1)
203: P_{6914} = (1, 23, 5, 1)
                                                                 257: P_{8769} = (0, 17, 7, 1)
204: P_{6960} = (15, 24, 5, 1)
                                                                 258: P_{8832} = (31, 18, 7, 1)
205: P_{6999} = (22, 25, 5, 1)
                                                                 259: P_{8853} = (20, 19, 7, 1)
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260: P_{8896} = (31, 20, 7, 1)
                                                                314: P_{10736} = (15, 14, 9, 1)
261: P_{8913} = (16, 21, 7, 1)
                                                                315: P_{10755} = (2, 15, 9, 1)
262: P_{8935} = (6, 22, 7, 1)
                                                                316: P_{10815} = (30, 16, 9, 1)
263: P_{8984} = (23, 23, 7, 1)
                                                                317: P_{10846} = (29, 17, 9, 1)
264: P_{9014} = (21, 24, 7, 1)
                                                                318: P_{10866} = (17, 18, 9, 1)
                                                                319: P_{10906} = (25, 19, 9, 1)
265: P_{9034} = (9, 25, 7, 1)
266: P_{9083} = (26, 26, 7, 1)
                                                                320: P_{10940} = (27, 20, 9, 1)
267: P_{9109} = (20, 27, 7, 1)
                                                                321: P_{10955} = (10, 21, 9, 1)
268: P_{9142} = (21, 28, 7, 1)
                                                                322: P_{11007} = (30, 22, 9, 1)
269: P_{9159} = (6, 29, 7, 1)
                                                                323: P_{11029} = (20, 23, 9, 1)
270: P_{9209} = (24, 30, 7, 1)
                                                                324: P_{11048} = (7, 24, 9, 1)
271: P_{9241} = (24, 31, 7, 1)
                                                                325: P_{11085} = (12, 25, 9, 1)
272: P_{9328} = (15, 2, 8, 1)
                                                                326: P_{11119} = (14, 26, 9, 1)
273: P_{9370} = (25, 3, 8, 1)
                                                                327: P_{11153} = (16, 27, 9, 1)
274: P_{9407} = (30, 4, 8, 1)
                                                                328: P_{11196} = (27, 28, 9, 1)
275: P_{9419} = (10, 5, 8, 1)
                                                                329: P_{11216} = (15, 29, 9, 1)
                                                                330: P_{11245} = (12, 30, 9, 1)
276: P_{9455} = (14, 6, 8, 1)
277: P_{9475} = (2,7,8,1)
                                                                331: P_{11267} = (2, 31, 9, 1)
278: P_{9531} = (26, 8, 8, 1)
                                                                332: P_{11363} = (2, 2, 10, 1)
279: P_{9557} = (20, 9, 8, 1)
                                                                333: P_{11419} = (26, 3, 10, 1)
280: P_{9598} = (29, 10, 8, 1)
                                                                334: P_{11456} = (31, 4, 10, 1)
281: P_{9608} = (7, 11, 8, 1)
                                                                335: P_{11463} = (6, 5, 10, 1)
282: P_{9648} = (15, 12, 8, 1)
                                                                336: P_{11508} = (19, 6, 10, 1)
283: P_{9672} = (7, 13, 8, 1)
                                                                337: P_{11527} = (6, 7, 10, 1)
284: P_{9717} = (20, 14, 8, 1)
                                                                338: P_{11575} = (22, 8, 10, 1)
285: P_{9746} = (17, 15, 8, 1)
                                                                339: P_{11587} = (2, 9, 10, 1)
286: P_{9773} = (12, 16, 8, 1)
                                                                340: P_{11620} = (3, 10, 10, 1)
287: P_{9809} = (16, 17, 8, 1)
                                                                341: P_{11678} = (29, 11, 10, 1)
288: P_{9852} = (27, 18, 8, 1)
                                                                342: P_{11694} = (13, 12, 10, 1)
289: P_{9886} = (29, 19, 8, 1)
                                                                343: P_{11739} = (26, 13, 10, 1)
290: P_{9905} = (16, 20, 8, 1)
                                                                344: P_{11767} = (22, 14, 10, 1)
291: P_{9923} = (2, 21, 8, 1)
                                                                345: P_{11798} = (21, 15, 10, 1)
292: P_{9954} = (1, 22, 8, 1)
                                                                346: P_{11828} = (19, 16, 10, 1)
293: P_{10011} = (26, 23, 8, 1)
                                                                347: P_{11855} = (14, 17, 10, 1)
294: P_{10042} = (25, 24, 8, 1)
                                                                348: P_{11887} = (14, 18, 10, 1)
                                                                349: P_{11935} = (30, 19, 10, 1)
295: P_{10079} = (30, 25, 8, 1)
296: P_{10093} = (12, 26, 8, 1)
                                                                350: P_{11967} = (30, 20, 10, 1)
297: P_{10140} = (27, 27, 8, 1)
                                                                351: P_{11973} = (4, 21, 10, 1)
298: P_{10162} = (17, 28, 8, 1)
                                                                352: P_{12001} = (0, 22, 10, 1)
299: P_{10177} = (0, 29, 8, 1)
                                                                353: P_{12045} = (12, 23, 10, 1)
300: P_{10223} = (14, 30, 8, 1)
                                                                354: P_{12068} = (3, 24, 10, 1)
301: P_{10251} = (10, 31, 8, 1)
                                                                355: P_{12098} = (1, 25, 10, 1)
302: P_{10337} = (0, 2, 9, 1)
                                                                356: P_{12160} = (31, 26, 10, 1)
303: P_{10398} = (29, 3, 9, 1)
                                                                357: P_{12182} = (21, 27, 10, 1)
304: P_{10402} = (1,4,9,1)
                                                                358: P_{12197} = (4, 28, 10, 1)
305: P_{10459} = (26, 5, 9, 1)
                                                                359: P_{12238} = (13, 29, 10, 1)
306: P_{10472} = (7, 6, 9, 1)
                                                                360: P_{12286} = (29, 30, 10, 1)
307: P_{10514} = (17, 7, 9, 1)
                                                                361: P_{12301} = (12, 31, 10, 1)
308: P_{10539} = (10, 8, 9, 1)
                                                                362: P_{12398} = (13, 2, 11, 1)
309: P_{10587} = (26, 9, 9, 1)
                                                                363: P_{12447} = (30, 3, 11, 1)
310: P_{10609} = (16, 10, 9, 1)
                                                                364: P_{12449} = (0, 4, 11, 1)
311: P_{10650} = (25, 11, 9, 1)
                                                                365: P_{12503} = (22, 5, 11, 1)
312: P_{10677} = (20, 12, 9, 1)
                                                                366: P_{12539} = (26, 6, 11, 1)
313: P_{10703} = (14, 13, 9, 1)
                                                                367: P_{12566} = (21, 7, 11, 1)
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422: P_{14463} = (30, 2, 13, 1)
368: P_{12583} = (6, 8, 11, 1)
369: P_{12621} = (12, 9, 11, 1)
                                                                423: P_{14486} = (21, 3, 13, 1)
370: P_{12655} = (14, 10, 11, 1)
                                                                424: P_{14523} = (26, 4, 13, 1)
371: P_{12676} = (3, 11, 11, 1)
                                                                425: P_{14560} = (31, 5, 13, 1)
372: P_{12727} = (22, 12, 11, 1)
                                                                426: P_{14582} = (21, 6, 13, 1)
373: P_{12756} = (19, 13, 11, 1)
                                                                427: P_{14611} = (18, 7, 13, 1)
374: P_{12782} = (13, 14, 11, 1)
                                                                428: P_{14640} = (15, 8, 13, 1)
375: P_{12807} = (6, 15, 11, 1)
                                                                429: P_{14663} = (6, 9, 13, 1)
376: P_{12834} = (1, 16, 11, 1)
                                                                430: P_{14699} = (10, 10, 13, 1)
377: P_{12868} = (3, 17, 11, 1)
                                                                431: P_{14721} = (0, 11, 13, 1)
378: P_{12901} = (4, 18, 11, 1)
                                                                432: P_{14760} = (7, 12, 13, 1)
379: P_{12955} = (26, 19, 11, 1)
                                                                433: P_{14813} = (28, 13, 13, 1)
380: P_{12982} = (21, 20, 11, 1)
                                                                434: P_{14845} = (28, 14, 13, 1)
381: P_{13005} = (12, 21, 11, 1)
                                                                435: P_{14850} = (1, 15, 13, 1)
382: P_{13056} = (31, 22, 11, 1)
                                                                436: P_{14912} = (31, 16, 13, 1)
383: P_{13059} = (2, 23, 11, 1)
                                                                437: P_{14920} = (7, 17, 13, 1)
384: P_{13118} = (29, 24, 11, 1)
                                                                438: P_{14950} = (5, 18, 13, 1)
385: P_{13140} = (19, 25, 11, 1)
                                                                439: P_{14994} = (17, 19, 13, 1)
386: P_{13182} = (29, 26, 11, 1)
                                                                440: P_{15022} = (13, 20, 13, 1)
387: P_{13215} = (30, 27, 11, 1)
                                                                441: P_{15067} = (26, 21, 13, 1)
388: P_{13231} = (14, 28, 11, 1)
                                                                442: P_{15078} = (5, 22, 13, 1)
389: P_{13251} = (2, 29, 11, 1)
                                                                443: P_{15113} = (8, 23, 13, 1)
390: P_{13312} = (31, 30, 11, 1)
                                                                444: P_{15167} = (30, 24, 13, 1)
391: P_{13317} = (4, 31, 11, 1)
                                                                445: P_{15182} = (13, 25, 13, 1)
392: P_{13426} = (17, 2, 12, 1)
                                                                446: P_{15211} = (10, 26, 13, 1)
393: P_{13458} = (17, 3, 12, 1)
                                                                447: P_{15239} = (6, 27, 13, 1)
394: P_{13478} = (5, 4, 12, 1)
                                                                448: P_{15280} = (15, 28, 13, 1)
395: P_{13520} = (15, 5, 12, 1)
                                                                449: P_{15314} = (17, 29, 13, 1)
396: P_{13565} = (28, 6, 12, 1)
                                                                450: P_{15337} = (8, 30, 13, 1)
397: P_{13570} = (1, 7, 12, 1)
                                                                451: P_{15379} = (18, 31, 13, 1)
398: P_{13632} = (31, 8, 12, 1)
                                                                452: P_{15485} = (28, 2, 14, 1)
399: P_{13641} = (8, 9, 12, 1)
                                                                453: P_{15507} = (18, 3, 14, 1)
400: P_{13672} = (7, 10, 12, 1)
                                                                454: P_{15525} = (4, 4, 14, 1)
401: P_{13727} = (30, 11, 12, 1)
                                                                455: P_{15556} = (3, 5, 14, 1)
402: P_{13757} = (28, 12, 12, 1)
                                                                456: P_{15586} = (1, 6, 14, 1)
403: P_{13782} = (21, 13, 12, 1)
                                                                457: P_{15622} = (5, 7, 14, 1)
404: P_{13800} = (7, 14, 12, 1)
                                                                458: P_{15668} = (19, 8, 14, 1)
405: P_{13843} = (18, 15, 12, 1)
                                                                459: P_{15711} = (30, 9, 14, 1)
                                                                460: P_{15738} = (25, 10, 14, 1)
406: P_{13870} = (13, 16, 12, 1)
407: P_{13899} = (10, 17, 12, 1)
                                                                461: P_{15749} = (4, 11, 14, 1)
408: P_{13936} = (15, 18, 12, 1)
                                                                462: P_{15807} = (30, 12, 14, 1)
409: P_{13974} = (21, 19, 12, 1)
                                                                463: P_{15817} = (8, 13, 14, 1)
410: P_{13991} = (6, 20, 12, 1)
                                                                464: P_{15846} = (5, 14, 14, 1)
411: P_{14035} = (18, 21, 12, 1)
                                                                465: P_{15895} = (22, 15, 14, 1)
412: P_{14075} = (26, 22, 12, 1)
                                                                466: P_{15923} = (18, 16, 14, 1)
413: P_{14087} = (6, 23, 12, 1)
                                                                467: P_{15957} = (20, 17, 14, 1)
414: P_{14113} = (0, 24, 12, 1)
                                                                468: P_{15995} = (26, 18, 14, 1)
415: P_{14176} = (31, 25, 12, 1)
                                                                469: P_{16023} = (22, 19, 14, 1)
416: P_{14185} = (8, 26, 12, 1)
                                                                470: P_{16041} = (8, 20, 14, 1)
417: P_{14222} = (13, 27, 12, 1)
                                                                471: P_{16085} = (20, 21, 14, 1)
418: P_{14246} = (5, 28, 12, 1)
                                                                472: P_{16124} = (27, 22, 14, 1)
419: P_{14303} = (30, 29, 12, 1)
                                                                473: P_{16145} = (16, 23, 14, 1)
420: P_{14315} = (10, 30, 12, 1)
                                                                474: P_{16187} = (26, 24, 14, 1)
421: P_{14363} = (26, 31, 12, 1)
                                                                475: P_{16193} = (0, 25, 14, 1)
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530: P_{18086} = (5, 20, 16, 1)
476: P_{16252} = (27, 26, 14, 1)
477: P_{16260} = (3, 27, 14, 1)
                                                                531: P_{18124} = (11, 21, 16, 1)
478: P_{16305} = (16, 28, 14, 1)
                                                                532: P_{18161} = (16, 22, 16, 1)
479: P_{16340} = (19, 29, 14, 1)
                                                                533: P_{18191} = (14, 23, 16, 1)
480: P_{16378} = (25, 30, 14, 1)
                                                                534: P_{18240} = (31, 24, 16, 1)
481: P_{16413} = (28, 31, 14, 1)
                                                                535: P_{18248} = (7, 25, 16, 1)
482: P_{16500} = (19, 2, 15, 1)
                                                                536: P_{18280} = (7, 26, 16, 1)
483: P_{16535} = (22, 3, 15, 1)
                                                                537: P_{18319} = (14, 27, 16, 1)
484: P_{16572} = (27, 4, 15, 1)
                                                                538: P_{18356} = (19, 28, 16, 1)
485: P_{16596} = (19, 5, 15, 1)
                                                                539: P_{18372} = (3, 29, 16, 1)
486: P_{16617} = (8, 6, 15, 1)
                                                                540: P_{18406} = (5, 30, 16, 1)
487: P_{16663} = (22, 7, 15, 1)
                                                                541: P_{18436} = (3, 31, 16, 1)
488: P_{16676} = (3, 8, 15, 1)
                                                                542: P_{18532} = (3, 2, 17, 1)
489: P_{16721} = (16, 9, 15, 1)
                                                                543: P_{18572} = (11, 3, 17, 1)
490: P_{16757} = (20, 10, 15, 1)
                                                                544: P_{18609} = (16, 4, 17, 1)
491: P_{16795} = (26, 11, 15, 1)
                                                                545: P_{18633} = (8, 5, 17, 1)
492: P_{16806} = (5, 12, 15, 1)
                                                                546: P_{18682} = (25, 6, 17, 1)
493: P_{16834} = (1, 13, 15, 1)
                                                                547: P_{18720} = (31, 7, 17, 1)
494: P_{16895} = (30, 14, 15, 1)
                                                                548: P_{18745} = (24, 8, 17, 1)
495: P_{16902} = (5, 15, 15, 1)
                                                                549: P_{18767} = (14, 9, 17, 1)
496: P_{16929} = (0, 16, 15, 1)
                                                                550: P_{18809} = (24, 10, 17, 1)
497: P_{16986} = (25, 17, 15, 1)
                                                                551: P_{18848} = (31, 11, 17, 1)
498: P_{17009} = (16, 18, 15, 1)
                                                                552: P_{18868} = (19, 12, 17, 1)
499: P_{17043} = (18, 19, 15, 1)
                                                                553: P_{18897} = (16, 13, 17, 1)
500: P_{17060} = (3, 20, 15, 1)
                                                                554: P_{18921} = (8, 14, 17, 1)
501: P_{17117} = (28, 21, 15, 1)
                                                                555: P_{18957} = (12, 15, 17, 1)
502: P_{17125} = (4, 22, 15, 1)
                                                                556: P_{18984} = (7, 16, 17, 1)
503: P_{17183} = (30, 23, 15, 1)
                                                                557: P_{19030} = (21, 17, 17, 1)
504: P_{17189} = (4, 24, 15, 1)
                                                                558: P_{19060} = (19, 18, 17, 1)
505: P_{17235} = (18, 25, 15, 1)
                                                                559: P_{19088} = (15, 19, 17, 1)
506: P_{17274} = (25, 26, 15, 1)
                                                                560: P_{19119} = (14, 20, 17, 1)
507: P_{17289} = (8, 27, 15, 1)
                                                                561: P_{19140} = (3, 21, 17, 1)
508: P_{17339} = (26, 28, 15, 1)
                                                                562: P_{19184} = (15, 22, 17, 1)
509: P_{17373} = (28, 29, 15, 1)
                                                                563: P_{19201} = (0, 23, 17, 1)
510: P_{17404} = (27, 30, 15, 1)
                                                                564: P_{19234} = (1, 24, 17, 1)
511: P_{17429} = (20, 31, 15, 1)
                                                                565: P_{19286} = (21, 25, 17, 1)
512: P_{17517} = (12, 2, 16, 1)
                                                                566: P_{19302} = (5, 26, 17, 1)
513: P_{17552} = (15, 3, 16, 1)
                                                                567: P_{19334} = (5, 27, 17, 1)
514: P_{17584} = (15, 4, 16, 1)
                                                                568: P_{19386} = (25, 28, 17, 1)
515: P_{17625} = (24, 5, 16, 1)
                                                                569: P_{19405} = (12, 29, 17, 1)
516: P_{17649} = (16, 6, 16, 1)
                                                                570: P_{19432} = (7, 30, 17, 1)
517: P_{17677} = (12, 7, 16, 1)
                                                                571: P_{19468} = (11, 31, 17, 1)
518: P_{17705} = (8, 8, 16, 1)
                                                                572: P_{19554} = (1, 2, 18, 1)
519: P_{17729} = (0, 9, 16, 1)
                                                                573: P_{19597} = (12, 3, 18, 1)
520: P_{17782} = (21, 10, 16, 1)
                                                                574: P_{19631} = (14, 4, 18, 1)
521: P_{17794} = (1, 11, 16, 1)
                                                                575: P_{19669} = (20, 5, 18, 1)
522: P_{17833} = (8, 12, 16, 1)
                                                                576: P_{19694} = (13, 6, 18, 1)
523: P_{17882} = (25, 13, 16, 1)
                                                                577: P_{19721} = (8, 7, 18, 1)
524: P_{17908} = (19, 14, 16, 1)
                                                                578: P_{19749} = (4, 8, 18, 1)
525: P_{17952} = (31, 15, 16, 1)
                                                                579: P_{19799} = (22, 9, 18, 1)
526: P_{17974} = (21, 16, 16, 1)
                                                                580: P_{19820} = (11, 10, 18, 1)
527: P_{18009} = (24, 17, 16, 1)
                                                                581: P_{19868} = (27, 11, 18, 1)
528: P_{18042} = (25, 18, 16, 1)
                                                                582: P_{19883} = (10, 12, 18, 1)
529: P_{18060} = (11, 19, 16, 1)
                                                                583: P_{19909} = (4, 13, 18, 1)
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584: P_{19954} = (17, 14, 18, 1)
                                                                638: P_{21806} = (13, 8, 20, 1)
585: P_{19996} = (27, 15, 18, 1)
                                                                639: P_{21853} = (28, 9, 20, 1)
586: P_{20011} = (10, 16, 18, 1)
                                                                640: P_{21872} = (15, 10, 20, 1)
587: P_{20039} = (6, 17, 18, 1)
                                                                641: P_{21913} = (24, 11, 20, 1)
588: P_{20077} = (12, 18, 18, 1)
                                                                642: P_{21948} = (27, 12, 20, 1)
589: P_{20105} = (8, 19, 18, 1)
                                                                643: P_{21964} = (11, 13, 20, 1)
590: P_{20140} = (11, 20, 18, 1)
                                                                644: P_{21985} = (0, 14, 20, 1)
591: P_{20174} = (13, 21, 18, 1)
                                                                645: P_{22045} = (28, 15, 20, 1)
592: P_{20210} = (17, 22, 18, 1)
                                                                646: P_{22069} = (20, 16, 20, 1)
593: P_{20249} = (24, 23, 18, 1)
                                                                647: P_{22083} = (2, 17, 20, 1)
594: P_{20262} = (5, 24, 18, 1)
                                                                648: P_{22126} = (13, 18, 20, 1)
595: P_{20313} = (24, 25, 18, 1)
                                                                649: P_{22148} = (3, 19, 20, 1)
596: P_{20341} = (20, 26, 18, 1)
                                                                650: P_{22196} = (19, 20, 20, 1)
597: P_{20353} = (0, 27, 18, 1)
                                                                651: P_{22236} = (27, 21, 20, 1)
598: P_{20391} = (6, 28, 18, 1)
                                                                652: P_{22252} = (11, 22, 20, 1)
599: P_{20431} = (14, 29, 18, 1)
                                                                653: P_{22291} = (18, 23, 20, 1)
600: P_{20471} = (22, 30, 18, 1)
                                                                654: P_{22311} = (6, 24, 20, 1)
                                                                655: P_{22343} = (6, 25, 20, 1)
601: P_{20486} = (5, 31, 18, 1)
602: P_{20591} = (14, 2, 19, 1)
                                                                656: P_{22372} = (3, 26, 20, 1)
603: P_{20617} = (8, 3, 19, 1)
                                                                657: P_{22425} = (24, 27, 20, 1)
604: P_{20658} = (17, 4, 19, 1)
                                                                658: P_{22440} = (7, 28, 20, 1)
605: P_{20677} = (4, 5, 19, 1)
                                                                659: P_{22494} = (29, 29, 20, 1)
606: P_{20709} = (4, 6, 19, 1)
                                                                660: P_{22498} = (1, 30, 20, 1)
607: P_{20764} = (27, 7, 19, 1)
                                                                661: P_{22548} = (19, 31, 20, 1)
608: P_{20789} = (20, 8, 19, 1)
                                                                662: P_{22654} = (29, 2, 21, 1)
609: P_{20825} = (24, 9, 19, 1)
                                                                663: P_{22660} = (3, 3, 21, 1)
610: P_{20839} = (6, 10, 19, 1)
                                                                664: P_{22700} = (11, 4, 21, 1)
611: P_{20870} = (5, 11, 19, 1)
                                                                665: P_{22734} = (13, 5, 21, 1)
612: P_{20914} = (17, 12, 19, 1)
                                                                666: P_{22764} = (11, 6, 21, 1)
613: P_{20942} = (13, 13, 19, 1)
                                                                667: P_{22813} = (28, 7, 21, 1)
614: P_{20971} = (10, 14, 19, 1)
                                                                668: P_{22846} = (29, 8, 21, 1)
615: P_{21001} = (8, 15, 19, 1)
                                                                669: P_{22867} = (18, 9, 21, 1)
616: P_{21049} = (24, 16, 19, 1)
                                                                670: P_{22883} = (2, 10, 21, 1)
                                                                671: P_{22919} = (6, 11, 21, 1)
617: P_{21068} = (11, 17, 19, 1)
                                                                672: P_{22945} = (0, 12, 21, 1)
618: P_{21095} = (6, 18, 19, 1)
619: P_{21133} = (12, 19, 19, 1)
                                                                673: P_{22979} = (2, 13, 21, 1)
620: P_{21153} = (0, 20, 19, 1)
                                                                674: P_{23036} = (27, 14, 21, 1)
621: P_{21190} = (5, 21, 19, 1)
                                                                675: P_{23056} = (15, 15, 21, 1)
622: P_{21231} = (14, 22, 19, 1)
                                                                676: P_{23079} = (6, 16, 21, 1)
623: P_{21271} = (22, 23, 19, 1)
                                                                677: P_{23120} = (15, 17, 21, 1)
624: P_{21308} = (27, 24, 19, 1)
                                                                678: P_{23144} = (7, 18, 21, 1)
625: P_{21323} = (10, 25, 19, 1)
                                                                679: P_{23176} = (7, 19, 21, 1)
626: P_{21367} = (22, 26, 19, 1)
                                                                680: P_{23225} = (24, 20, 21, 1)
627: P_{21388} = (11, 27, 19, 1)
                                                                681: P_{23252} = (19, 21, 21, 1)
628: P_{21421} = (12, 28, 19, 1)
                                                                682: P_{23285} = (20, 22, 21, 1)
629: P_{21442} = (1, 29, 19, 1)
                                                                683: P_{23325} = (28, 23, 21, 1)
630: P_{21493} = (20, 30, 19, 1)
                                                                684: P_{23353} = (24, 24, 21, 1)
631: P_{21518} = (13, 31, 19, 1)
                                                                685: P_{23381} = (20, 25, 21, 1)
632: P_{21619} = (18, 2, 20, 1)
                                                                686: P_{23394} = (1, 26, 21, 1)
633: P_{21640} = (7, 3, 20, 1)
                                                                687: P_{23444} = (19, 27, 21, 1)
634: P_{21685} = (20, 4, 20, 1)
                                                                688: P_{23470} = (13, 28, 21, 1)
635: P_{21726} = (29, 5, 20, 1)
                                                                689: P_{23507} = (18, 29, 21, 1)
636: P_{21731} = (2, 6, 20, 1)
                                                                690: P_{23524} = (3, 30, 21, 1)
637: P_{21776} = (15, 7, 20, 1)
                                                                691: P_{23580} = (27, 31, 21, 1)
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692: P_{23680} = (31, 2, 22, 1)
                                                                746: P_{25459} = (18, 26, 23, 1)
693: P_{23685} = (4, 3, 22, 1)
                                                                747: P_{25502} = (29, 27, 23, 1)
694: P_{23734} = (21, 4, 22, 1)
                                                                748: P_{25529} = (24, 28, 23, 1)
695: P_{23762} = (17, 5, 22, 1)
                                                                749: P_{25568} = (31, 29, 23, 1)
696: P_{23808} = (31, 6, 22, 1)
                                                                750: P_{25585} = (16, 30, 23, 1)
697: P_{23820} = (11, 7, 22, 1)
                                                                751: P_{25630} = (29, 31, 23, 1)
698: P_{23842} = (1, 8, 22, 1)
                                                                752: P_{25719} = (22, 2, 24, 1)
699: P_{23883} = (10, 9, 22, 1)
                                                                753: P_{25738} = (9, 3, 24, 1)
700: P_{23922} = (17, 10, 22, 1)
                                                                754: P_{25774} = (13, 4, 24, 1)
701: P_{23939} = (2, 11, 22, 1)
                                                                755: P_{25793} = (0, 5, 24, 1)
702: P_{23994} = (25, 12, 22, 1)
                                                                756: P_{25840} = (15, 6, 24, 1)
703: P_{24023} = (22, 13, 22, 1)
                                                                757: P_{25861} = (4, 7, 24, 1)
704: P_{24035} = (2, 14, 22, 1)
                                                                758: P_{25905} = (16, 8, 24, 1)
705: P_{24089} = (24, 15, 22, 1)
                                                                759: P_{25930} = (9, 9, 24, 1)
                                                                760: P_{25965} = (12, 10, 24, 1)
706: P_{24108} = (11, 16, 22, 1)
707: P_{24157} = (28, 17, 22, 1)
                                                                761: P_{26001} = (16, 11, 24, 1)
708: P_{24185} = (24, 18, 22, 1)
                                                                762: P_{26029} = (12, 12, 24, 1)
709: P_{24193} = (0, 19, 22, 1)
                                                                763: P_{26055} = (6, 13, 24, 1)
710: P_{24254} = (29, 20, 22, 1)
                                                                764: P_{26104} = (23, 14, 24, 1)
711: P_{24286} = (29, 21, 22, 1)
                                                                765: P_{26136} = (23, 15, 24, 1)
712: P_{24299} = (10, 22, 22, 1)
                                                                766: P_{26159} = (14, 16, 24, 1)
713: P_{24325} = (4, 23, 22, 1)
                                                                767: P_{26178} = (1, 17, 24, 1)
714: P_{24381} = (28, 24, 22, 1)
                                                                768: P_{26231} = (22, 18, 24, 1)
715: P_{24410} = (25, 25, 22, 1)
                                                                769: P_{26254} = (13, 19, 24, 1)
716: P_{24433} = (16, 26, 22, 1)
                                                                770: P_{26298} = (25, 20, 24, 1)
717: P_{24471} = (22, 27, 22, 1)
                                                                771: P_{26312} = (7, 21, 24, 1)
718: P_{24499} = (18, 28, 22, 1)
                                                                772: P_{26355} = (18, 22, 24, 1)
719: P_{24529} = (16, 29, 22, 1)
                                                                773: P_{26376} = (7, 23, 24, 1)
720: P_{24563} = (18, 30, 22, 1)
                                                                774: P_{26415} = (14, 24, 24, 1)
721: P_{24598} = (21, 31, 22, 1)
                                                                775: P_{26461} = (28, 25, 24, 1)
722: P_{24689} = (16, 2, 23, 1)
                                                                776: P_{26469} = (4, 26, 24, 1)
723: P_{24705} = (0, 3, 23, 1)
                                                                777: P_{26515} = (18, 27, 24, 1)
724: P_{24747} = (10, 4, 23, 1)
                                                                778: P_{26557} = (28, 28, 24, 1)
725: P_{24770} = (1, 5, 23, 1)
                                                                779: P_{26586} = (25, 29, 24, 1)
726: P_{24823} = (22, 6, 23, 1)
                                                                780: P_{26599} = (6, 30, 24, 1)
727: P_{24857} = (24, 7, 23, 1)
                                                                781: P_{26640} = (15, 31, 24, 1)
728: P_{24882} = (17, 8, 23, 1)
                                                                782: P_{26746} = (25, 2, 25, 1)
729: P_{24901} = (4, 9, 23, 1)
                                                                783: P_{26766} = (13, 3, 25, 1)
730: P_{24957} = (28, 10, 23, 1)
                                                                784: P_{26803} = (18, 4, 25, 1)
731: P_{24989} = (28, 11, 23, 1)
                                                                785: P_{26833} = (16, 5, 25, 1)
732: P_{24995} = (2, 12, 23, 1)
                                                                786: P_{26855} = (6, 6, 25, 1)
733: P_{25056} = (31, 13, 23, 1)
                                                                787: P_{26904} = (23, 7, 25, 1)
734: P_{25082} = (25, 14, 23, 1)
                                                                788: P_{26913} = (0, 8, 25, 1)
735: P_{25100} = (11, 15, 23, 1)
                                                                789: P_{26952} = (7, 9, 25, 1)
736: P_{25146} = (25, 16, 23, 1)
                                                                790: P_{26978} = (1, 10, 25, 1)
737: P_{25170} = (17, 17, 23, 1)
                                                                791: P_{27023} = (14, 11, 25, 1)
738: P_{25203} = (18, 18, 23, 1)
                                                                792: P_{27064} = (23, 12, 25, 1)
739: P_{25221} = (4, 19, 23, 1)
                                                                793: P_{27088} = (15, 13, 25, 1)
740: P_{25271} = (22, 20, 23, 1)
                                                                794: P_{27117} = (12, 14, 25, 1)
741: P_{25302} = (21, 21, 23, 1)
                                                                795: P_{27141} = (4, 15, 25, 1)
742: P_{25334} = (21, 22, 23, 1)
                                                                796: P_{27197} = (28, 16, 25, 1)
743: P_{25355} = (10, 23, 23, 1)
                                                                797: P_{27213} = (12, 17, 25, 1)
744: P_{25379} = (2, 24, 23, 1)
                                                                798: P_{27261} = (28, 18, 25, 1)
745: P_{25420} = (11, 25, 23, 1)
                                                                799: P_{27274} = (9, 19, 25, 1)
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800: P_{27315} = (18, 20, 25, 1)
                                                                854: P_{29167} = (14, 14, 27, 1)
801: P_{27344} = (15, 21, 25, 1)
                                                                855: P_{29185} = (0, 15, 27, 1)
802: P_{27374} = (13, 22, 25, 1)
                                                                856: P_{29220} = (3, 16, 27, 1)
803: P_{27402} = (9, 23, 25, 1)
                                                                857: P_{29267} = (18, 17, 27, 1)
804: P_{27441} = (16, 24, 25, 1)
                                                                858: P_{29290} = (9, 18, 27, 1)
805: P_{27471} = (14, 25, 25, 1)
                                                                859: P_{29323} = (10, 19, 27, 1)
806: P_{27495} = (6, 26, 25, 1)
                                                                860: P_{29373} = (28, 20, 27, 1)
807: P_{27546} = (25, 27, 25, 1)
                                                                861: P_{29386} = (9, 21, 27, 1)
808: P_{27575} = (22, 28, 25, 1)
                                                                862: P_{29421} = (12, 22, 27, 1)
809: P_{27607} = (22, 29, 25, 1)
                                                                863: P_{29472} = (31, 23, 27, 1)
810: P_{27621} = (4, 30, 25, 1)
                                                                864: P_{29483} = (10, 24, 27, 1)
811: P_{27656} = (7, 31, 25, 1)
                                                                865: P_{29522} = (17, 25, 27, 1)
812: P_{27772} = (27, 2, 26, 1)
                                                                866: P_{29558} = (21, 26, 27, 1)
                                                                867: P_{29592} = (23, 27, 27, 1)
813: P_{27787} = (10, 3, 26, 1)
814: P_{27821} = (12, 4, 26, 1)
                                                                868: P_{29604} = (3, 28, 27, 1)
815: P_{27853} = (12, 5, 26, 1)
                                                                869: P_{29660} = (27, 29, 27, 1)
                                                                870: P_{29688} = (23, 30, 27, 1)
816: P_{27891} = (18, 6, 26, 1)
817: P_{27905} = (0, 7, 26, 1)
                                                                871: P_{29698} = (1, 31, 27, 1)
818: P_{27965} = (28, 8, 26, 1)
                                                                872: P_{29801} = (8, 2, 28, 1)
819: P_{28000} = (31, 9, 26, 1)
                                                                873: P_{29826} = (1, 3, 28, 1)
820: P_{28019} = (18, 10, 26, 1)
                                                                874: P_{29879} = (22, 4, 28, 1)
821: P_{28043} = (10, 11, 26, 1)
                                                                875: P_{29894} = (5, 5, 28, 1)
822: P_{28079} = (14, 12, 26, 1)
                                                                876: P_{29950} = (29, 6, 28, 1)
823: P_{28124} = (27, 13, 26, 1)
                                                                877: P_{29960} = (7,7,28,1)
                                                                878: P_{30006} = (21, 8, 28, 1)
824: P_{28150} = (21, 14, 26, 1)
825: P_{28180} = (19, 15, 26, 1)
                                                                879: P_{30038} = (21, 9, 28, 1)
826: P_{28210} = (17, 16, 26, 1)
                                                                880: P_{30071} = (22, 10, 28, 1)
827: P_{28256} = (31, 17, 26, 1)
                                                                881: P_{30090} = (9, 11, 28, 1)
828: P_{28260} = (3, 18, 26, 1)
                                                                882: P_{30144} = (31, 12, 28, 1)
                                                                883: P_{30165} = (20, 13, 28, 1)
829: P_{28303} = (14, 19, 26, 1)
830: P_{28344} = (23, 20, 26, 1)
                                                                884: P_{30181} = (4, 14, 28, 1)
831: P_{28354} = (1, 21, 26, 1)
                                                                885: P_{30229} = (20, 15, 28, 1)
832: P_{28404} = (19, 22, 26, 1)
                                                                886: P_{30256} = (15, 16, 28, 1)
833: P_{28434} = (17, 23, 26, 1)
                                                                887: P_{30300} = (27, 17, 28, 1)
834: P_{28469} = (20, 24, 26, 1)
                                                                888: P_{30307} = (2, 18, 28, 1)
835: P_{28484} = (3, 25, 26, 1)
                                                                889: P_{30342} = (5, 19, 28, 1)
836: P_{28536} = (23, 26, 26, 1)
                                                                890: P_{30384} = (15, 20, 28, 1)
837: P_{28573} = (28, 27, 26, 1)
                                                                891: P_{30424} = (23, 21, 28, 1)
838: P_{28586} = (9, 28, 26, 1)
                                                                892: P_{30442} = (9, 22, 28, 1)
839: P_{28629} = (20, 29, 26, 1)
                                                                893: P_{30492} = (27, 23, 28, 1)
840: P_{28662} = (21, 30, 26, 1)
                                                                894: P_{30520} = (23, 24, 28, 1)
841: P_{28682} = (9, 31, 26, 1)
                                                                895: P_{30558} = (29, 25, 28, 1)
842: P_{28789} = (20, 2, 27, 1)
                                                                896: P_{30561} = (0, 26, 28, 1)
843: P_{28815} = (14, 3, 27, 1)
                                                                897: P_{30597} = (4, 27, 28, 1)
844: P_{28852} = (19, 4, 27, 1)
                                                                898: P_{30633} = (8, 28, 28, 1)
845: P_{28893} = (28, 5, 27, 1)
                                                                899: P_{30664} = (7, 29, 28, 1)
846: P_{28924} = (27, 6, 27, 1)
                                                                900: P_{30691} = (2, 30, 28, 1)
847: P_{28948} = (19, 7, 27, 1)
                                                                901: P_{30752} = (31, 31, 28, 1)
848: P_{28973} = (12, 8, 27, 1)
                                                                902: P_{30824} = (7, 2, 29, 1)
849: P_{29010} = (17, 9, 27, 1)
                                                                903: P_{30854} = (5, 3, 29, 1)
850: P_{29056} = (31, 10, 27, 1)
                                                                904: P_{30890} = (9, 4, 29, 1)
851: P_{29077} = (20, 11, 27, 1)
                                                                905: P_{30934} = (21, 5, 29, 1)
852: P_{29110} = (21, 12, 27, 1)
                                                                906: P_{30965} = (20, 6, 29, 1)
853: P_{29139} = (18, 13, 27, 1)
                                                                907: P_{30997} = (20, 7, 29, 1)
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951: P_{32466} = (17, 21, 30, 1)
908: P_{31014} = (5, 8, 29, 1)
909: P_{31068} = (27, 9, 29, 1)
                                                                952: P_{32489} = (8, 22, 30, 1)
910: P_{31100} = (27, 10, 29, 1)
                                                                953: P_{32526} = (13, 23, 30, 1)
911: P_{31128} = (23, 11, 29, 1)
                                                                954: P_{32558} = (13, 24, 30, 1)
912: P_{31141} = (4, 12, 29, 1)
                                                                955: P_{32579} = (2, 25, 30, 1)
913: P_{31198} = (29, 13, 29, 1)
                                                                956: P_{32628} = (19, 26, 30, 1)
914: P_{31232} = (31, 14, 29, 1)
                                                                957: P_{32651} = (10, 27, 30, 1)
915: P_{31240} = (7, 15, 29, 1)
                                                                958: P_{32702} = (29, 28, 30, 1)
916: P_{31294} = (29, 16, 29, 1)
                                                                959: P_{32715} = (10, 29, 30, 1)
917: P_{31319} = (22, 17, 29, 1)
                                                                960: P_{32754} = (17, 30, 30, 1)
918: P_{31337} = (8, 18, 29, 1)
                                                                961: P_{32794} = (25, 31, 30, 1)
919: P_{31362} = (1, 19, 29, 1)
                                                                962: P_{32875} = (10, 2, 31, 1)
920: P_{31397} = (4, 20, 29, 1)
                                                                963: P_{32903} = (6, 3, 31, 1)
921: P_{31456} = (31, 21, 29, 1)
                                                                964: P_{32937} = (8, 4, 31, 1)
922: P_{31479} = (22, 22, 29, 1)
                                                                965: P_{32986} = (25, 5, 31, 1)
923: P_{31510} = (21, 23, 29, 1)
                                                                966: P_{33002} = (9, 6, 31, 1)
                                                                967: P_{33041} = (16, 7, 31, 1)
924: P_{31530} = (9, 24, 29, 1)
925: P_{31568} = (15, 25, 29, 1)
                                                                968: P_{33066} = (9, 8, 31, 1)
926: P_{31587} = (2, 26, 29, 1)
                                                                969: P_{33102} = (13, 9, 31, 1)
927: P_{31632} = (15, 27, 29, 1)
                                                                970: P_{33126} = (5, 10, 31, 1)
928: P_{31651} = (2, 28, 29, 1)
                                                                971: P_{33166} = (13, 11, 31, 1)
929: P_{31689} = (8, 29, 29, 1)
                                                                972: P_{33191} = (6, 12, 31, 1)
930: P_{31713} = (0, 30, 29, 1)
                                                                973: P_{33217} = (0, 13, 31, 1)
931: P_{31768} = (23, 31, 29, 1)
                                                                974: P_{33278} = (29, 14, 31, 1)
932: P_{31846} = (5, 2, 30, 1)
                                                                975: P_{33284} = (3, 15, 31, 1)
933: P_{31875} = (2, 3, 30, 1)
                                                                976: P_{33315} = (2, 16, 31, 1)
934: P_{31928} = (23, 4, 30, 1)
                                                                977: P_{33353} = (8, 17, 31, 1)
935: P_{31946} = (9, 5, 30, 1)
                                                                978: P_{33406} = (29, 18, 31, 1)
936: P_{31969} = (0, 6, 30, 1)
                                                                979: P_{33411} = (2, 19, 31, 1)
937: P_{32004} = (3, 7, 30, 1)
                                                                980: P_{33451} = (10, 20, 31, 1)
938: P_{32058} = (25, 8, 30, 1)
                                                                981: P_{33498} = (25, 21, 31, 1)
939: P_{32068} = (3, 9, 30, 1)
                                                                982: P_{33528} = (23, 22, 31, 1)
940: P_{32105} = (8, 10, 30, 1)
                                                                983: P_{33540} = (3, 23, 31, 1)
941: P_{32148} = (19, 11, 30, 1)
                                                                984: P_{33588} = (19, 24, 31, 1)
942: P_{32190} = (29, 12, 30, 1)
                                                                985: P_{33617} = (16, 25, 31, 1)
943: P_{32202} = (9, 13, 30, 1)
                                                                986: P_{33650} = (17, 26, 31, 1)
944: P_{32231} = (6, 14, 30, 1)
                                                                987: P_{33666} = (1, 27, 31, 1)
                                                                988: P_{33720} = (23, 28, 31, 1)
945: P_{32273} = (16, 15, 30, 1)
946: P_{32305} = (16, 16, 30, 1)
                                                                989: P_{33734} = (5, 29, 31, 1)
947: P_{32326} = (5, 17, 30, 1)
                                                                990: P_{33780} = (19, 30, 31, 1)
948: P_{32376} = (23, 18, 30, 1)
                                                                991: P_{33810} = (17, 31, 31, 1)
949: P_{32391} = (6, 19, 30, 1)
950: P_{32418} = (1, 20, 30, 1)
```

Line Intersection Graph

 $\begin{array}{c|c}
 & 0 & 1 & 2 \\
\hline
0 & 0 & 1 & 1 \\
1 & 1 & 0 & 0 \\
2 & 1 & 0 & 0
\end{array}$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2
in point	P_0	P_2

Line 1 intersects

Line	ℓ_0
in point	P_0

Line 2 intersects

Line	ℓ_0
in point	P_2

The surface has 1089 points: Too many to print.