

# Rank-74051 over GF(64)

January 15, 2021

## The equation

The equation of the surface is :

$$X_0^2 X_3 + X_1^2 X_2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

( 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0 )

The point rank of the equation over GF(64) is 1090785349

## General information

|                            |                                  |
|----------------------------|----------------------------------|
| Number of lines            | 10                               |
| Number of points           | 4353                             |
| Number of singular points  | 1                                |
| Number of Eckardt points   | 2                                |
| Number of double points    | 9                                |
| Number of single points    | 621                              |
| Number of points off lines | 3720                             |
| Number of Hesse planes     | 0                                |
| Number of axes             | 0                                |
| Type of points on lines    | $65^{10}$                        |
| Type of lines on points    | $5, 3^2, 2^9, 1^{621}, 0^{3720}$ |

## Singular Points

The surface has 1 singular points:

$$0 : P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0)$$

## The 10 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{PI}(1, 0, 0, 0, 0, 0)_0$$

$$\begin{aligned}
\ell_1 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4096} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4096} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2 \\
\ell_2 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{8257} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{8257} = \mathbf{Pl}(0, 0, 1, 0, 0, 1)_{270528} \\
\ell_3 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043520} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043520} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)_{129} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{266304} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{266304} = \mathbf{Pl}(1, 0, 0, 1, 0, 0)_{130} \\
\ell_5 &= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047616} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047616} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_1 \\
\ell_6 &= \begin{bmatrix} 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{274561} = \begin{bmatrix} 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{274561} = \mathbf{Pl}(0, 1, 1, 0, 0, 1)_{270592} \\
\ell_7 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{270400} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{270400} = \mathbf{Pl}(0, 1, 1, 0, 0, 0)_{66} \\
\ell_8 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{4225} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{4225} = \mathbf{Pl}(1, 1, 0, 0, 1, 1)_{536577} \\
\ell_9 &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{270529} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{270529} = \mathbf{Pl}(1, 1, 0, 1, 1, 1)_{540609}
\end{aligned}$$

Rank of lines: ( 0, 4096, 8257, 17043520, 266304, 17047616, 274561, 270400, 4225, 270529 )

Rank of points on Klein quadric: ( 0, 2, 270528, 129, 130, 1, 270592, 66, 536577, 540609 )

### Eckardt Points

The surface has 2 Eckardt points:

$$0 : P_1 = \mathbf{P}(0, 1, 0, 0) = \mathbf{P}(0, 1, 0, 0),$$

$$1 : P_{4226} = \mathbf{P}(0, 1, 0, 1) = \mathbf{P}(0, 1, 0, 1).$$

### Double Points

The surface has 9 Double points:

The double points on the surface are:

$$P_0 = (1, 0, 0, 0) = \ell_0 \cap \ell_1$$

$$P_5 = (1, 1, 0, 0) = \ell_0 \cap \ell_2$$

$$P_{68} = (1, 0, 1, 0) = \ell_1 \cap \ell_8$$

$$P_{132} = (1, 1, 1, 0) = \ell_2 \cap \ell_9$$

$$P_3 = (0, 0, 0, 1) = \ell_3 \cap \ell_5$$

$$P_{4227} = (1, 1, 0, 1) = \ell_4 \cap \ell_6$$

$$P_{4163} = (1, 0, 0, 1) = \ell_4 \cap \ell_7$$

$$P_4 = (1, 1, 1, 1) = \ell_6 \cap \ell_8$$

$$P_{8259} = (1, 0, 1, 1) = \ell_7 \cap \ell_9$$

### Single Points

The surface has 621 single points:

The single points on the surface are:



108 :  $P_{115} = (48, 0, 1, 0)$  lies on line  $\ell_1$   
 109 :  $P_{116} = (49, 0, 1, 0)$  lies on line  $\ell_1$   
 110 :  $P_{117} = (50, 0, 1, 0)$  lies on line  $\ell_1$   
 111 :  $P_{118} = (51, 0, 1, 0)$  lies on line  $\ell_1$   
 112 :  $P_{119} = (52, 0, 1, 0)$  lies on line  $\ell_1$   
 113 :  $P_{120} = (53, 0, 1, 0)$  lies on line  $\ell_1$   
 114 :  $P_{121} = (54, 0, 1, 0)$  lies on line  $\ell_1$   
 115 :  $P_{122} = (55, 0, 1, 0)$  lies on line  $\ell_1$   
 116 :  $P_{123} = (56, 0, 1, 0)$  lies on line  $\ell_1$   
 117 :  $P_{124} = (57, 0, 1, 0)$  lies on line  $\ell_1$   
 118 :  $P_{125} = (58, 0, 1, 0)$  lies on line  $\ell_1$   
 119 :  $P_{126} = (59, 0, 1, 0)$  lies on line  $\ell_1$   
 120 :  $P_{127} = (60, 0, 1, 0)$  lies on line  $\ell_1$   
 121 :  $P_{128} = (61, 0, 1, 0)$  lies on line  $\ell_1$   
 122 :  $P_{129} = (62, 0, 1, 0)$  lies on line  $\ell_1$   
 123 :  $P_{130} = (63, 0, 1, 0)$  lies on line  $\ell_1$   
 124 :  $P_{197} = (2, 2, 1, 0)$  lies on line  $\ell_2$   
 125 :  $P_{262} = (3, 3, 1, 0)$  lies on line  $\ell_2$   
 126 :  $P_{327} = (4, 4, 1, 0)$  lies on line  $\ell_2$   
 127 :  $P_{392} = (5, 5, 1, 0)$  lies on line  $\ell_2$   
 128 :  $P_{457} = (6, 6, 1, 0)$  lies on line  $\ell_2$   
 129 :  $P_{522} = (7, 7, 1, 0)$  lies on line  $\ell_2$   
 130 :  $P_{587} = (8, 8, 1, 0)$  lies on line  $\ell_2$   
 131 :  $P_{652} = (9, 9, 1, 0)$  lies on line  $\ell_2$   
 132 :  $P_{717} = (10, 10, 1, 0)$  lies on line  $\ell_2$   
 133 :  $P_{782} = (11, 11, 1, 0)$  lies on line  $\ell_2$   
 134 :  $P_{847} = (12, 12, 1, 0)$  lies on line  $\ell_2$   
 135 :  $P_{912} = (13, 13, 1, 0)$  lies on line  $\ell_2$   
 136 :  $P_{977} = (14, 14, 1, 0)$  lies on line  $\ell_2$   
 137 :  $P_{1042} = (15, 15, 1, 0)$  lies on line  $\ell_2$   
 138 :  $P_{1107} = (16, 16, 1, 0)$  lies on line  $\ell_2$   
 139 :  $P_{1172} = (17, 17, 1, 0)$  lies on line  $\ell_2$   
 140 :  $P_{1237} = (18, 18, 1, 0)$  lies on line  $\ell_2$   
 141 :  $P_{1302} = (19, 19, 1, 0)$  lies on line  $\ell_2$   
 142 :  $P_{1367} = (20, 20, 1, 0)$  lies on line  $\ell_2$   
 143 :  $P_{1432} = (21, 21, 1, 0)$  lies on line  $\ell_2$   
 144 :  $P_{1497} = (22, 22, 1, 0)$  lies on line  $\ell_2$   
 145 :  $P_{1562} = (23, 23, 1, 0)$  lies on line  $\ell_2$   
 146 :  $P_{1627} = (24, 24, 1, 0)$  lies on line  $\ell_2$   
 147 :  $P_{1692} = (25, 25, 1, 0)$  lies on line  $\ell_2$   
 148 :  $P_{1757} = (26, 26, 1, 0)$  lies on line  $\ell_2$   
 149 :  $P_{1822} = (27, 27, 1, 0)$  lies on line  $\ell_2$   
 150 :  $P_{1887} = (28, 28, 1, 0)$  lies on line  $\ell_2$   
 151 :  $P_{1952} = (29, 29, 1, 0)$  lies on line  $\ell_2$   
 152 :  $P_{2017} = (30, 30, 1, 0)$  lies on line  $\ell_2$   
 153 :  $P_{2082} = (31, 31, 1, 0)$  lies on line  $\ell_2$   
 154 :  $P_{2147} = (32, 32, 1, 0)$  lies on line  $\ell_2$   
 155 :  $P_{2212} = (33, 33, 1, 0)$  lies on line  $\ell_2$   
 156 :  $P_{2277} = (34, 34, 1, 0)$  lies on line  $\ell_2$   
 157 :  $P_{2342} = (35, 35, 1, 0)$  lies on line  $\ell_2$   
 158 :  $P_{2407} = (36, 36, 1, 0)$  lies on line  $\ell_2$   
 159 :  $P_{2472} = (37, 37, 1, 0)$  lies on line  $\ell_2$   
 160 :  $P_{2537} = (38, 38, 1, 0)$  lies on line  $\ell_2$   
 161 :  $P_{2602} = (39, 39, 1, 0)$  lies on line  $\ell_2$

162 :  $P_{2667} = (40, 40, 1, 0)$  lies on line  $\ell_2$   
 163 :  $P_{2732} = (41, 41, 1, 0)$  lies on line  $\ell_2$   
 164 :  $P_{2797} = (42, 42, 1, 0)$  lies on line  $\ell_2$   
 165 :  $P_{2862} = (43, 43, 1, 0)$  lies on line  $\ell_2$   
 166 :  $P_{2927} = (44, 44, 1, 0)$  lies on line  $\ell_2$   
 167 :  $P_{2992} = (45, 45, 1, 0)$  lies on line  $\ell_2$   
 168 :  $P_{3057} = (46, 46, 1, 0)$  lies on line  $\ell_2$   
 169 :  $P_{3122} = (47, 47, 1, 0)$  lies on line  $\ell_2$   
 170 :  $P_{3187} = (48, 48, 1, 0)$  lies on line  $\ell_2$   
 171 :  $P_{3252} = (49, 49, 1, 0)$  lies on line  $\ell_2$   
 172 :  $P_{3317} = (50, 50, 1, 0)$  lies on line  $\ell_2$   
 173 :  $P_{3382} = (51, 51, 1, 0)$  lies on line  $\ell_2$   
 174 :  $P_{3447} = (52, 52, 1, 0)$  lies on line  $\ell_2$   
 175 :  $P_{3512} = (53, 53, 1, 0)$  lies on line  $\ell_2$   
 176 :  $P_{3577} = (54, 54, 1, 0)$  lies on line  $\ell_2$   
 177 :  $P_{3642} = (55, 55, 1, 0)$  lies on line  $\ell_2$   
 178 :  $P_{3707} = (56, 56, 1, 0)$  lies on line  $\ell_2$   
 179 :  $P_{3772} = (57, 57, 1, 0)$  lies on line  $\ell_2$   
 180 :  $P_{3837} = (58, 58, 1, 0)$  lies on line  $\ell_2$   
 181 :  $P_{3902} = (59, 59, 1, 0)$  lies on line  $\ell_2$   
 182 :  $P_{3967} = (60, 60, 1, 0)$  lies on line  $\ell_2$   
 183 :  $P_{4032} = (61, 61, 1, 0)$  lies on line  $\ell_2$   
 184 :  $P_{4097} = (62, 62, 1, 0)$  lies on line  $\ell_2$   
 185 :  $P_{4162} = (63, 63, 1, 0)$  lies on line  $\ell_2$   
 186 :  $P_{4290} = (0, 2, 0, 1)$  lies on line  $\ell_3$   
 187 :  $P_{4291} = (1, 2, 0, 1)$  lies on line  $\ell_4$   
 188 :  $P_{4354} = (0, 3, 0, 1)$  lies on line  $\ell_3$   
 189 :  $P_{4355} = (1, 3, 0, 1)$  lies on line  $\ell_4$   
 190 :  $P_{4418} = (0, 4, 0, 1)$  lies on line  $\ell_3$   
 191 :  $P_{4419} = (1, 4, 0, 1)$  lies on line  $\ell_4$   
 192 :  $P_{4482} = (0, 5, 0, 1)$  lies on line  $\ell_3$   
 193 :  $P_{4483} = (1, 5, 0, 1)$  lies on line  $\ell_4$   
 194 :  $P_{4546} = (0, 6, 0, 1)$  lies on line  $\ell_3$   
 195 :  $P_{4547} = (1, 6, 0, 1)$  lies on line  $\ell_4$   
 196 :  $P_{4610} = (0, 7, 0, 1)$  lies on line  $\ell_3$   
 197 :  $P_{4611} = (1, 7, 0, 1)$  lies on line  $\ell_4$   
 198 :  $P_{4674} = (0, 8, 0, 1)$  lies on line  $\ell_3$   
 199 :  $P_{4675} = (1, 8, 0, 1)$  lies on line  $\ell_4$   
 200 :  $P_{4738} = (0, 9, 0, 1)$  lies on line  $\ell_3$   
 201 :  $P_{4739} = (1, 9, 0, 1)$  lies on line  $\ell_4$   
 202 :  $P_{4802} = (0, 10, 0, 1)$  lies on line  $\ell_3$   
 203 :  $P_{4803} = (1, 10, 0, 1)$  lies on line  $\ell_4$   
 204 :  $P_{4866} = (0, 11, 0, 1)$  lies on line  $\ell_3$   
 205 :  $P_{4867} = (1, 11, 0, 1)$  lies on line  $\ell_4$   
 206 :  $P_{4930} = (0, 12, 0, 1)$  lies on line  $\ell_3$   
 207 :  $P_{4931} = (1, 12, 0, 1)$  lies on line  $\ell_4$   
 208 :  $P_{4994} = (0, 13, 0, 1)$  lies on line  $\ell_3$   
 209 :  $P_{4995} = (1, 13, 0, 1)$  lies on line  $\ell_4$   
 210 :  $P_{5058} = (0, 14, 0, 1)$  lies on line  $\ell_3$   
 211 :  $P_{5059} = (1, 14, 0, 1)$  lies on line  $\ell_4$   
 212 :  $P_{5122} = (0, 15, 0, 1)$  lies on line  $\ell_3$   
 213 :  $P_{5123} = (1, 15, 0, 1)$  lies on line  $\ell_4$   
 214 :  $P_{5186} = (0, 16, 0, 1)$  lies on line  $\ell_3$   
 215 :  $P_{5187} = (1, 16, 0, 1)$  lies on line  $\ell_4$

216 :  $P_{5250} = (0, 17, 0, 1)$  lies on line  $\ell_3$   
 217 :  $P_{5251} = (1, 17, 0, 1)$  lies on line  $\ell_4$   
 218 :  $P_{5314} = (0, 18, 0, 1)$  lies on line  $\ell_3$   
 219 :  $P_{5315} = (1, 18, 0, 1)$  lies on line  $\ell_4$   
 220 :  $P_{5378} = (0, 19, 0, 1)$  lies on line  $\ell_3$   
 221 :  $P_{5379} = (1, 19, 0, 1)$  lies on line  $\ell_4$   
 222 :  $P_{5442} = (0, 20, 0, 1)$  lies on line  $\ell_3$   
 223 :  $P_{5443} = (1, 20, 0, 1)$  lies on line  $\ell_4$   
 224 :  $P_{5506} = (0, 21, 0, 1)$  lies on line  $\ell_3$   
 225 :  $P_{5507} = (1, 21, 0, 1)$  lies on line  $\ell_4$   
 226 :  $P_{5570} = (0, 22, 0, 1)$  lies on line  $\ell_3$   
 227 :  $P_{5571} = (1, 22, 0, 1)$  lies on line  $\ell_4$   
 228 :  $P_{5634} = (0, 23, 0, 1)$  lies on line  $\ell_3$   
 229 :  $P_{5635} = (1, 23, 0, 1)$  lies on line  $\ell_4$   
 230 :  $P_{5698} = (0, 24, 0, 1)$  lies on line  $\ell_3$   
 231 :  $P_{5699} = (1, 24, 0, 1)$  lies on line  $\ell_4$   
 232 :  $P_{5762} = (0, 25, 0, 1)$  lies on line  $\ell_3$   
 233 :  $P_{5763} = (1, 25, 0, 1)$  lies on line  $\ell_4$   
 234 :  $P_{5826} = (0, 26, 0, 1)$  lies on line  $\ell_3$   
 235 :  $P_{5827} = (1, 26, 0, 1)$  lies on line  $\ell_4$   
 236 :  $P_{5890} = (0, 27, 0, 1)$  lies on line  $\ell_3$   
 237 :  $P_{5891} = (1, 27, 0, 1)$  lies on line  $\ell_4$   
 238 :  $P_{5954} = (0, 28, 0, 1)$  lies on line  $\ell_3$   
 239 :  $P_{5955} = (1, 28, 0, 1)$  lies on line  $\ell_4$   
 240 :  $P_{6018} = (0, 29, 0, 1)$  lies on line  $\ell_3$   
 241 :  $P_{6019} = (1, 29, 0, 1)$  lies on line  $\ell_4$   
 242 :  $P_{6082} = (0, 30, 0, 1)$  lies on line  $\ell_3$   
 243 :  $P_{6083} = (1, 30, 0, 1)$  lies on line  $\ell_4$   
 244 :  $P_{6146} = (0, 31, 0, 1)$  lies on line  $\ell_3$   
 245 :  $P_{6147} = (1, 31, 0, 1)$  lies on line  $\ell_4$   
 246 :  $P_{6210} = (0, 32, 0, 1)$  lies on line  $\ell_3$   
 247 :  $P_{6211} = (1, 32, 0, 1)$  lies on line  $\ell_4$   
 248 :  $P_{6274} = (0, 33, 0, 1)$  lies on line  $\ell_3$   
 249 :  $P_{6275} = (1, 33, 0, 1)$  lies on line  $\ell_4$   
 250 :  $P_{6338} = (0, 34, 0, 1)$  lies on line  $\ell_3$   
 251 :  $P_{6339} = (1, 34, 0, 1)$  lies on line  $\ell_4$   
 252 :  $P_{6402} = (0, 35, 0, 1)$  lies on line  $\ell_3$   
 253 :  $P_{6403} = (1, 35, 0, 1)$  lies on line  $\ell_4$   
 254 :  $P_{6466} = (0, 36, 0, 1)$  lies on line  $\ell_3$   
 255 :  $P_{6467} = (1, 36, 0, 1)$  lies on line  $\ell_4$   
 256 :  $P_{6530} = (0, 37, 0, 1)$  lies on line  $\ell_3$   
 257 :  $P_{6531} = (1, 37, 0, 1)$  lies on line  $\ell_4$   
 258 :  $P_{6594} = (0, 38, 0, 1)$  lies on line  $\ell_3$   
 259 :  $P_{6595} = (1, 38, 0, 1)$  lies on line  $\ell_4$   
 260 :  $P_{6658} = (0, 39, 0, 1)$  lies on line  $\ell_3$   
 261 :  $P_{6659} = (1, 39, 0, 1)$  lies on line  $\ell_4$   
 262 :  $P_{6722} = (0, 40, 0, 1)$  lies on line  $\ell_3$   
 263 :  $P_{6723} = (1, 40, 0, 1)$  lies on line  $\ell_4$   
 264 :  $P_{6786} = (0, 41, 0, 1)$  lies on line  $\ell_3$   
 265 :  $P_{6787} = (1, 41, 0, 1)$  lies on line  $\ell_4$   
 266 :  $P_{6850} = (0, 42, 0, 1)$  lies on line  $\ell_3$   
 267 :  $P_{6851} = (1, 42, 0, 1)$  lies on line  $\ell_4$   
 268 :  $P_{6914} = (0, 43, 0, 1)$  lies on line  $\ell_3$   
 269 :  $P_{6915} = (1, 43, 0, 1)$  lies on line  $\ell_4$

270 :  $P_{6978} = (0, 44, 0, 1)$  lies on line  $\ell_3$   
 271 :  $P_{6979} = (1, 44, 0, 1)$  lies on line  $\ell_4$   
 272 :  $P_{7042} = (0, 45, 0, 1)$  lies on line  $\ell_3$   
 273 :  $P_{7043} = (1, 45, 0, 1)$  lies on line  $\ell_4$   
 274 :  $P_{7106} = (0, 46, 0, 1)$  lies on line  $\ell_3$   
 275 :  $P_{7107} = (1, 46, 0, 1)$  lies on line  $\ell_4$   
 276 :  $P_{7170} = (0, 47, 0, 1)$  lies on line  $\ell_3$   
 277 :  $P_{7171} = (1, 47, 0, 1)$  lies on line  $\ell_4$   
 278 :  $P_{7234} = (0, 48, 0, 1)$  lies on line  $\ell_3$   
 279 :  $P_{7235} = (1, 48, 0, 1)$  lies on line  $\ell_4$   
 280 :  $P_{7298} = (0, 49, 0, 1)$  lies on line  $\ell_3$   
 281 :  $P_{7299} = (1, 49, 0, 1)$  lies on line  $\ell_4$   
 282 :  $P_{7362} = (0, 50, 0, 1)$  lies on line  $\ell_3$   
 283 :  $P_{7363} = (1, 50, 0, 1)$  lies on line  $\ell_4$   
 284 :  $P_{7426} = (0, 51, 0, 1)$  lies on line  $\ell_3$   
 285 :  $P_{7427} = (1, 51, 0, 1)$  lies on line  $\ell_4$   
 286 :  $P_{7490} = (0, 52, 0, 1)$  lies on line  $\ell_3$   
 287 :  $P_{7491} = (1, 52, 0, 1)$  lies on line  $\ell_4$   
 288 :  $P_{7554} = (0, 53, 0, 1)$  lies on line  $\ell_3$   
 289 :  $P_{7555} = (1, 53, 0, 1)$  lies on line  $\ell_4$   
 290 :  $P_{7618} = (0, 54, 0, 1)$  lies on line  $\ell_3$   
 291 :  $P_{7619} = (1, 54, 0, 1)$  lies on line  $\ell_4$   
 292 :  $P_{7682} = (0, 55, 0, 1)$  lies on line  $\ell_3$   
 293 :  $P_{7683} = (1, 55, 0, 1)$  lies on line  $\ell_4$   
 294 :  $P_{7746} = (0, 56, 0, 1)$  lies on line  $\ell_3$   
 295 :  $P_{7747} = (1, 56, 0, 1)$  lies on line  $\ell_4$   
 296 :  $P_{7810} = (0, 57, 0, 1)$  lies on line  $\ell_3$   
 297 :  $P_{7811} = (1, 57, 0, 1)$  lies on line  $\ell_4$   
 298 :  $P_{7874} = (0, 58, 0, 1)$  lies on line  $\ell_3$   
 299 :  $P_{7875} = (1, 58, 0, 1)$  lies on line  $\ell_4$   
 300 :  $P_{7938} = (0, 59, 0, 1)$  lies on line  $\ell_3$   
 301 :  $P_{7939} = (1, 59, 0, 1)$  lies on line  $\ell_4$   
 302 :  $P_{8002} = (0, 60, 0, 1)$  lies on line  $\ell_3$   
 303 :  $P_{8003} = (1, 60, 0, 1)$  lies on line  $\ell_4$   
 304 :  $P_{8066} = (0, 61, 0, 1)$  lies on line  $\ell_3$   
 305 :  $P_{8067} = (1, 61, 0, 1)$  lies on line  $\ell_4$   
 306 :  $P_{8130} = (0, 62, 0, 1)$  lies on line  $\ell_3$   
 307 :  $P_{8131} = (1, 62, 0, 1)$  lies on line  $\ell_4$   
 308 :  $P_{8194} = (0, 63, 0, 1)$  lies on line  $\ell_3$   
 309 :  $P_{8195} = (1, 63, 0, 1)$  lies on line  $\ell_4$   
 310 :  $P_{8258} = (0, 0, 1, 1)$  lies on line  $\ell_5$   
 311 :  $P_{12353} = (0, 0, 2, 1)$  lies on line  $\ell_5$   
 312 :  $P_{12354} = (1, 0, 2, 1)$  lies on line  $\ell_7$   
 313 :  $P_{12418} = (1, 1, 2, 1)$  lies on line  $\ell_6$   
 314 :  $P_{12419} = (2, 1, 2, 1)$  lies on line  $\ell_8$   
 315 :  $P_{12547} = (2, 3, 2, 1)$  lies on line  $\ell_9$   
 316 :  $P_{16449} = (0, 0, 3, 1)$  lies on line  $\ell_5$   
 317 :  $P_{16450} = (1, 0, 3, 1)$  lies on line  $\ell_7$   
 318 :  $P_{16514} = (1, 1, 3, 1)$  lies on line  $\ell_6$   
 319 :  $P_{16516} = (3, 1, 3, 1)$  lies on line  $\ell_8$   
 320 :  $P_{16580} = (3, 2, 3, 1)$  lies on line  $\ell_9$   
 321 :  $P_{20545} = (0, 0, 4, 1)$  lies on line  $\ell_5$   
 322 :  $P_{20546} = (1, 0, 4, 1)$  lies on line  $\ell_7$   
 323 :  $P_{20610} = (1, 1, 4, 1)$  lies on line  $\ell_6$

324 :  $P_{20613} = (4, 1, 4, 1)$  lies on line  $\ell_8$   
 325 :  $P_{20869} = (4, 5, 4, 1)$  lies on line  $\ell_9$   
 326 :  $P_{24641} = (0, 0, 5, 1)$  lies on line  $\ell_5$   
 327 :  $P_{24642} = (1, 0, 5, 1)$  lies on line  $\ell_7$   
 328 :  $P_{24706} = (1, 1, 5, 1)$  lies on line  $\ell_6$   
 329 :  $P_{24710} = (5, 1, 5, 1)$  lies on line  $\ell_8$   
 330 :  $P_{24902} = (5, 4, 5, 1)$  lies on line  $\ell_9$   
 331 :  $P_{28737} = (0, 0, 6, 1)$  lies on line  $\ell_5$   
 332 :  $P_{28738} = (1, 0, 6, 1)$  lies on line  $\ell_7$   
 333 :  $P_{28802} = (1, 1, 6, 1)$  lies on line  $\ell_6$   
 334 :  $P_{28807} = (6, 1, 6, 1)$  lies on line  $\ell_8$   
 335 :  $P_{29191} = (6, 7, 6, 1)$  lies on line  $\ell_9$   
 336 :  $P_{32833} = (0, 0, 7, 1)$  lies on line  $\ell_5$   
 337 :  $P_{32834} = (1, 0, 7, 1)$  lies on line  $\ell_7$   
 338 :  $P_{32898} = (1, 1, 7, 1)$  lies on line  $\ell_6$   
 339 :  $P_{32904} = (7, 1, 7, 1)$  lies on line  $\ell_8$   
 340 :  $P_{33224} = (7, 6, 7, 1)$  lies on line  $\ell_9$   
 341 :  $P_{36929} = (0, 0, 8, 1)$  lies on line  $\ell_5$   
 342 :  $P_{36930} = (1, 0, 8, 1)$  lies on line  $\ell_7$   
 343 :  $P_{36994} = (1, 1, 8, 1)$  lies on line  $\ell_6$   
 344 :  $P_{37001} = (8, 1, 8, 1)$  lies on line  $\ell_8$   
 345 :  $P_{37513} = (8, 9, 8, 1)$  lies on line  $\ell_9$   
 346 :  $P_{41025} = (0, 0, 9, 1)$  lies on line  $\ell_5$   
 347 :  $P_{41026} = (1, 0, 9, 1)$  lies on line  $\ell_7$   
 348 :  $P_{41090} = (1, 1, 9, 1)$  lies on line  $\ell_6$   
 349 :  $P_{41098} = (9, 1, 9, 1)$  lies on line  $\ell_8$   
 350 :  $P_{41546} = (9, 8, 9, 1)$  lies on line  $\ell_9$   
 351 :  $P_{45121} = (0, 0, 10, 1)$  lies on line  $\ell_5$   
 352 :  $P_{45122} = (1, 0, 10, 1)$  lies on line  $\ell_7$   
 353 :  $P_{45186} = (1, 1, 10, 1)$  lies on line  $\ell_6$   
 354 :  $P_{45195} = (10, 1, 10, 1)$  lies on line  $\ell_8$   
 355 :  $P_{45835} = (10, 11, 10, 1)$  lies on line  $\ell_9$   
 356 :  $P_{49217} = (0, 0, 11, 1)$  lies on line  $\ell_5$   
 357 :  $P_{49218} = (1, 0, 11, 1)$  lies on line  $\ell_7$   
 358 :  $P_{49282} = (1, 1, 11, 1)$  lies on line  $\ell_6$   
 359 :  $P_{49292} = (11, 1, 11, 1)$  lies on line  $\ell_8$   
 360 :  $P_{49868} = (11, 10, 11, 1)$  lies on line  $\ell_9$   
 361 :  $P_{53313} = (0, 0, 12, 1)$  lies on line  $\ell_5$   
 362 :  $P_{53314} = (1, 0, 12, 1)$  lies on line  $\ell_7$   
 363 :  $P_{53378} = (1, 1, 12, 1)$  lies on line  $\ell_6$   
 364 :  $P_{53389} = (12, 1, 12, 1)$  lies on line  $\ell_8$   
 365 :  $P_{54157} = (12, 13, 12, 1)$  lies on line  $\ell_9$   
 366 :  $P_{57409} = (0, 0, 13, 1)$  lies on line  $\ell_5$   
 367 :  $P_{57410} = (1, 0, 13, 1)$  lies on line  $\ell_7$   
 368 :  $P_{57474} = (1, 1, 13, 1)$  lies on line  $\ell_6$   
 369 :  $P_{57486} = (13, 1, 13, 1)$  lies on line  $\ell_8$   
 370 :  $P_{58190} = (13, 12, 13, 1)$  lies on line  $\ell_9$   
 371 :  $P_{61505} = (0, 0, 14, 1)$  lies on line  $\ell_5$   
 372 :  $P_{61506} = (1, 0, 14, 1)$  lies on line  $\ell_7$   
 373 :  $P_{61570} = (1, 1, 14, 1)$  lies on line  $\ell_6$   
 374 :  $P_{61583} = (14, 1, 14, 1)$  lies on line  $\ell_8$   
 375 :  $P_{62479} = (14, 15, 14, 1)$  lies on line  $\ell_9$   
 376 :  $P_{65601} = (0, 0, 15, 1)$  lies on line  $\ell_5$   
 377 :  $P_{65602} = (1, 0, 15, 1)$  lies on line  $\ell_7$

378 :  $P_{65666} = (1, 1, 15, 1)$  lies on line  $\ell_6$   
 379 :  $P_{65680} = (15, 1, 15, 1)$  lies on line  $\ell_8$   
 380 :  $P_{66512} = (15, 14, 15, 1)$  lies on line  $\ell_9$   
 381 :  $P_{69697} = (0, 0, 16, 1)$  lies on line  $\ell_5$   
 382 :  $P_{69698} = (1, 0, 16, 1)$  lies on line  $\ell_7$   
 383 :  $P_{69762} = (1, 1, 16, 1)$  lies on line  $\ell_6$   
 384 :  $P_{69777} = (16, 1, 16, 1)$  lies on line  $\ell_8$   
 385 :  $P_{70801} = (16, 17, 16, 1)$  lies on line  $\ell_9$   
 386 :  $P_{73793} = (0, 0, 17, 1)$  lies on line  $\ell_5$   
 387 :  $P_{73794} = (1, 0, 17, 1)$  lies on line  $\ell_7$   
 388 :  $P_{73858} = (1, 1, 17, 1)$  lies on line  $\ell_6$   
 389 :  $P_{73874} = (17, 1, 17, 1)$  lies on line  $\ell_8$   
 390 :  $P_{74834} = (17, 16, 17, 1)$  lies on line  $\ell_9$   
 391 :  $P_{77889} = (0, 0, 18, 1)$  lies on line  $\ell_5$   
 392 :  $P_{77890} = (1, 0, 18, 1)$  lies on line  $\ell_7$   
 393 :  $P_{77954} = (1, 1, 18, 1)$  lies on line  $\ell_6$   
 394 :  $P_{77971} = (18, 1, 18, 1)$  lies on line  $\ell_8$   
 395 :  $P_{79123} = (18, 19, 18, 1)$  lies on line  $\ell_9$   
 396 :  $P_{81985} = (0, 0, 19, 1)$  lies on line  $\ell_5$   
 397 :  $P_{81986} = (1, 0, 19, 1)$  lies on line  $\ell_7$   
 398 :  $P_{82050} = (1, 1, 19, 1)$  lies on line  $\ell_6$   
 399 :  $P_{82068} = (19, 1, 19, 1)$  lies on line  $\ell_8$   
 400 :  $P_{83156} = (19, 18, 19, 1)$  lies on line  $\ell_9$   
 401 :  $P_{86081} = (0, 0, 20, 1)$  lies on line  $\ell_5$   
 402 :  $P_{86082} = (1, 0, 20, 1)$  lies on line  $\ell_7$   
 403 :  $P_{86146} = (1, 1, 20, 1)$  lies on line  $\ell_6$   
 404 :  $P_{86165} = (20, 1, 20, 1)$  lies on line  $\ell_8$   
 405 :  $P_{87445} = (20, 21, 20, 1)$  lies on line  $\ell_9$   
 406 :  $P_{90177} = (0, 0, 21, 1)$  lies on line  $\ell_5$   
 407 :  $P_{90178} = (1, 0, 21, 1)$  lies on line  $\ell_7$   
 408 :  $P_{90242} = (1, 1, 21, 1)$  lies on line  $\ell_6$   
 409 :  $P_{90262} = (21, 1, 21, 1)$  lies on line  $\ell_8$   
 410 :  $P_{91478} = (21, 20, 21, 1)$  lies on line  $\ell_9$   
 411 :  $P_{94273} = (0, 0, 22, 1)$  lies on line  $\ell_5$   
 412 :  $P_{94274} = (1, 0, 22, 1)$  lies on line  $\ell_7$   
 413 :  $P_{94338} = (1, 1, 22, 1)$  lies on line  $\ell_6$   
 414 :  $P_{94359} = (22, 1, 22, 1)$  lies on line  $\ell_8$   
 415 :  $P_{95767} = (22, 23, 22, 1)$  lies on line  $\ell_9$   
 416 :  $P_{98369} = (0, 0, 23, 1)$  lies on line  $\ell_5$   
 417 :  $P_{98370} = (1, 0, 23, 1)$  lies on line  $\ell_7$   
 418 :  $P_{98434} = (1, 1, 23, 1)$  lies on line  $\ell_6$   
 419 :  $P_{98456} = (23, 1, 23, 1)$  lies on line  $\ell_8$   
 420 :  $P_{99800} = (23, 22, 23, 1)$  lies on line  $\ell_9$   
 421 :  $P_{102465} = (0, 0, 24, 1)$  lies on line  $\ell_5$   
 422 :  $P_{102466} = (1, 0, 24, 1)$  lies on line  $\ell_7$   
 423 :  $P_{102530} = (1, 1, 24, 1)$  lies on line  $\ell_6$   
 424 :  $P_{102553} = (24, 1, 24, 1)$  lies on line  $\ell_8$   
 425 :  $P_{104089} = (24, 25, 24, 1)$  lies on line  $\ell_9$   
 426 :  $P_{106561} = (0, 0, 25, 1)$  lies on line  $\ell_5$   
 427 :  $P_{106562} = (1, 0, 25, 1)$  lies on line  $\ell_7$   
 428 :  $P_{106626} = (1, 1, 25, 1)$  lies on line  $\ell_6$   
 429 :  $P_{106650} = (25, 1, 25, 1)$  lies on line  $\ell_8$   
 430 :  $P_{108122} = (25, 24, 25, 1)$  lies on line  $\ell_9$   
 431 :  $P_{110657} = (0, 0, 26, 1)$  lies on line  $\ell_5$

432 :  $P_{110658} = (1, 0, 26, 1)$  lies on line  $\ell_7$   
 433 :  $P_{110722} = (1, 1, 26, 1)$  lies on line  $\ell_6$   
 434 :  $P_{110747} = (26, 1, 26, 1)$  lies on line  $\ell_8$   
 435 :  $P_{112411} = (26, 27, 26, 1)$  lies on line  $\ell_9$   
 436 :  $P_{114753} = (0, 0, 27, 1)$  lies on line  $\ell_5$   
 437 :  $P_{114754} = (1, 0, 27, 1)$  lies on line  $\ell_7$   
 438 :  $P_{114818} = (1, 1, 27, 1)$  lies on line  $\ell_6$   
 439 :  $P_{114844} = (27, 1, 27, 1)$  lies on line  $\ell_8$   
 440 :  $P_{116444} = (27, 26, 27, 1)$  lies on line  $\ell_9$   
 441 :  $P_{118849} = (0, 0, 28, 1)$  lies on line  $\ell_5$   
 442 :  $P_{118850} = (1, 0, 28, 1)$  lies on line  $\ell_7$   
 443 :  $P_{118914} = (1, 1, 28, 1)$  lies on line  $\ell_6$   
 444 :  $P_{118941} = (28, 1, 28, 1)$  lies on line  $\ell_8$   
 445 :  $P_{120733} = (28, 29, 28, 1)$  lies on line  $\ell_9$   
 446 :  $P_{122945} = (0, 0, 29, 1)$  lies on line  $\ell_5$   
 447 :  $P_{122946} = (1, 0, 29, 1)$  lies on line  $\ell_7$   
 448 :  $P_{123010} = (1, 1, 29, 1)$  lies on line  $\ell_6$   
 449 :  $P_{123038} = (29, 1, 29, 1)$  lies on line  $\ell_8$   
 450 :  $P_{124766} = (29, 28, 29, 1)$  lies on line  $\ell_9$   
 451 :  $P_{127041} = (0, 0, 30, 1)$  lies on line  $\ell_5$   
 452 :  $P_{127042} = (1, 0, 30, 1)$  lies on line  $\ell_7$   
 453 :  $P_{127106} = (1, 1, 30, 1)$  lies on line  $\ell_6$   
 454 :  $P_{127135} = (30, 1, 30, 1)$  lies on line  $\ell_8$   
 455 :  $P_{129055} = (30, 31, 30, 1)$  lies on line  $\ell_9$   
 456 :  $P_{131137} = (0, 0, 31, 1)$  lies on line  $\ell_5$   
 457 :  $P_{131138} = (1, 0, 31, 1)$  lies on line  $\ell_7$   
 458 :  $P_{131202} = (1, 1, 31, 1)$  lies on line  $\ell_6$   
 459 :  $P_{131232} = (31, 1, 31, 1)$  lies on line  $\ell_8$   
 460 :  $P_{133088} = (31, 30, 31, 1)$  lies on line  $\ell_9$   
 461 :  $P_{135233} = (0, 0, 32, 1)$  lies on line  $\ell_5$   
 462 :  $P_{135234} = (1, 0, 32, 1)$  lies on line  $\ell_7$   
 463 :  $P_{135298} = (1, 1, 32, 1)$  lies on line  $\ell_6$   
 464 :  $P_{135329} = (32, 1, 32, 1)$  lies on line  $\ell_8$   
 465 :  $P_{137377} = (32, 33, 32, 1)$  lies on line  $\ell_9$   
 466 :  $P_{139329} = (0, 0, 33, 1)$  lies on line  $\ell_5$   
 467 :  $P_{139330} = (1, 0, 33, 1)$  lies on line  $\ell_7$   
 468 :  $P_{139394} = (1, 1, 33, 1)$  lies on line  $\ell_6$   
 469 :  $P_{139426} = (33, 1, 33, 1)$  lies on line  $\ell_8$   
 470 :  $P_{141410} = (33, 32, 33, 1)$  lies on line  $\ell_9$   
 471 :  $P_{143425} = (0, 0, 34, 1)$  lies on line  $\ell_5$   
 472 :  $P_{143426} = (1, 0, 34, 1)$  lies on line  $\ell_7$   
 473 :  $P_{143490} = (1, 1, 34, 1)$  lies on line  $\ell_6$   
 474 :  $P_{143523} = (34, 1, 34, 1)$  lies on line  $\ell_8$   
 475 :  $P_{145699} = (34, 35, 34, 1)$  lies on line  $\ell_9$   
 476 :  $P_{147521} = (0, 0, 35, 1)$  lies on line  $\ell_5$   
 477 :  $P_{147522} = (1, 0, 35, 1)$  lies on line  $\ell_7$   
 478 :  $P_{147586} = (1, 1, 35, 1)$  lies on line  $\ell_6$   
 479 :  $P_{147620} = (35, 1, 35, 1)$  lies on line  $\ell_8$   
 480 :  $P_{149732} = (35, 34, 35, 1)$  lies on line  $\ell_9$   
 481 :  $P_{151617} = (0, 0, 36, 1)$  lies on line  $\ell_5$   
 482 :  $P_{151618} = (1, 0, 36, 1)$  lies on line  $\ell_7$   
 483 :  $P_{151682} = (1, 1, 36, 1)$  lies on line  $\ell_6$   
 484 :  $P_{151717} = (36, 1, 36, 1)$  lies on line  $\ell_8$   
 485 :  $P_{154021} = (36, 37, 36, 1)$  lies on line  $\ell_9$

486 :  $P_{155713} = (0, 0, 37, 1)$  lies on line  $\ell_5$   
 487 :  $P_{155714} = (1, 0, 37, 1)$  lies on line  $\ell_7$   
 488 :  $P_{155778} = (1, 1, 37, 1)$  lies on line  $\ell_6$   
 489 :  $P_{155814} = (37, 1, 37, 1)$  lies on line  $\ell_8$   
 490 :  $P_{158054} = (37, 36, 37, 1)$  lies on line  $\ell_9$   
 491 :  $P_{159809} = (0, 0, 38, 1)$  lies on line  $\ell_5$   
 492 :  $P_{159810} = (1, 0, 38, 1)$  lies on line  $\ell_7$   
 493 :  $P_{159874} = (1, 1, 38, 1)$  lies on line  $\ell_6$   
 494 :  $P_{159911} = (38, 1, 38, 1)$  lies on line  $\ell_8$   
 495 :  $P_{162343} = (38, 39, 38, 1)$  lies on line  $\ell_9$   
 496 :  $P_{163905} = (0, 0, 39, 1)$  lies on line  $\ell_5$   
 497 :  $P_{163906} = (1, 0, 39, 1)$  lies on line  $\ell_7$   
 498 :  $P_{163970} = (1, 1, 39, 1)$  lies on line  $\ell_6$   
 499 :  $P_{164008} = (39, 1, 39, 1)$  lies on line  $\ell_8$   
 500 :  $P_{166376} = (39, 38, 39, 1)$  lies on line  $\ell_9$   
 501 :  $P_{168001} = (0, 0, 40, 1)$  lies on line  $\ell_5$   
 502 :  $P_{168002} = (1, 0, 40, 1)$  lies on line  $\ell_7$   
 503 :  $P_{168066} = (1, 1, 40, 1)$  lies on line  $\ell_6$   
 504 :  $P_{168105} = (40, 1, 40, 1)$  lies on line  $\ell_8$   
 505 :  $P_{170665} = (40, 41, 40, 1)$  lies on line  $\ell_9$   
 506 :  $P_{172097} = (0, 0, 41, 1)$  lies on line  $\ell_5$   
 507 :  $P_{172098} = (1, 0, 41, 1)$  lies on line  $\ell_7$   
 508 :  $P_{172162} = (1, 1, 41, 1)$  lies on line  $\ell_6$   
 509 :  $P_{172202} = (41, 1, 41, 1)$  lies on line  $\ell_8$   
 510 :  $P_{174698} = (41, 40, 41, 1)$  lies on line  $\ell_9$   
 511 :  $P_{176193} = (0, 0, 42, 1)$  lies on line  $\ell_5$   
 512 :  $P_{176194} = (1, 0, 42, 1)$  lies on line  $\ell_7$   
 513 :  $P_{176258} = (1, 1, 42, 1)$  lies on line  $\ell_6$   
 514 :  $P_{176299} = (42, 1, 42, 1)$  lies on line  $\ell_8$   
 515 :  $P_{178987} = (42, 43, 42, 1)$  lies on line  $\ell_9$   
 516 :  $P_{180289} = (0, 0, 43, 1)$  lies on line  $\ell_5$   
 517 :  $P_{180290} = (1, 0, 43, 1)$  lies on line  $\ell_7$   
 518 :  $P_{180354} = (1, 1, 43, 1)$  lies on line  $\ell_6$   
 519 :  $P_{180396} = (43, 1, 43, 1)$  lies on line  $\ell_8$   
 520 :  $P_{183020} = (43, 42, 43, 1)$  lies on line  $\ell_9$   
 521 :  $P_{184385} = (0, 0, 44, 1)$  lies on line  $\ell_5$   
 522 :  $P_{184386} = (1, 0, 44, 1)$  lies on line  $\ell_7$   
 523 :  $P_{184450} = (1, 1, 44, 1)$  lies on line  $\ell_6$   
 524 :  $P_{184493} = (44, 1, 44, 1)$  lies on line  $\ell_8$   
 525 :  $P_{187309} = (44, 45, 44, 1)$  lies on line  $\ell_9$   
 526 :  $P_{188481} = (0, 0, 45, 1)$  lies on line  $\ell_5$   
 527 :  $P_{188482} = (1, 0, 45, 1)$  lies on line  $\ell_7$   
 528 :  $P_{188546} = (1, 1, 45, 1)$  lies on line  $\ell_6$   
 529 :  $P_{188590} = (45, 1, 45, 1)$  lies on line  $\ell_8$   
 530 :  $P_{191342} = (45, 44, 45, 1)$  lies on line  $\ell_9$   
 531 :  $P_{192577} = (0, 0, 46, 1)$  lies on line  $\ell_5$   
 532 :  $P_{192578} = (1, 0, 46, 1)$  lies on line  $\ell_7$   
 533 :  $P_{192642} = (1, 1, 46, 1)$  lies on line  $\ell_6$   
 534 :  $P_{192687} = (46, 1, 46, 1)$  lies on line  $\ell_8$   
 535 :  $P_{195631} = (46, 47, 46, 1)$  lies on line  $\ell_9$   
 536 :  $P_{196673} = (0, 0, 47, 1)$  lies on line  $\ell_5$   
 537 :  $P_{196674} = (1, 0, 47, 1)$  lies on line  $\ell_7$   
 538 :  $P_{196738} = (1, 1, 47, 1)$  lies on line  $\ell_6$   
 539 :  $P_{196784} = (47, 1, 47, 1)$  lies on line  $\ell_8$

540 :  $P_{199664} = (47, 46, 47, 1)$  lies on line  $\ell_9$   
 541 :  $P_{200769} = (0, 0, 48, 1)$  lies on line  $\ell_5$   
 542 :  $P_{200770} = (1, 0, 48, 1)$  lies on line  $\ell_7$   
 543 :  $P_{200834} = (1, 1, 48, 1)$  lies on line  $\ell_6$   
 544 :  $P_{200881} = (48, 1, 48, 1)$  lies on line  $\ell_8$   
 545 :  $P_{203953} = (48, 49, 48, 1)$  lies on line  $\ell_9$   
 546 :  $P_{204865} = (0, 0, 49, 1)$  lies on line  $\ell_5$   
 547 :  $P_{204866} = (1, 0, 49, 1)$  lies on line  $\ell_7$   
 548 :  $P_{204930} = (1, 1, 49, 1)$  lies on line  $\ell_6$   
 549 :  $P_{204978} = (49, 1, 49, 1)$  lies on line  $\ell_8$   
 550 :  $P_{207986} = (49, 48, 49, 1)$  lies on line  $\ell_9$   
 551 :  $P_{208961} = (0, 0, 50, 1)$  lies on line  $\ell_5$   
 552 :  $P_{208962} = (1, 0, 50, 1)$  lies on line  $\ell_7$   
 553 :  $P_{209026} = (1, 1, 50, 1)$  lies on line  $\ell_6$   
 554 :  $P_{209075} = (50, 1, 50, 1)$  lies on line  $\ell_8$   
 555 :  $P_{212275} = (50, 51, 50, 1)$  lies on line  $\ell_9$   
 556 :  $P_{213057} = (0, 0, 51, 1)$  lies on line  $\ell_5$   
 557 :  $P_{213058} = (1, 0, 51, 1)$  lies on line  $\ell_7$   
 558 :  $P_{213122} = (1, 1, 51, 1)$  lies on line  $\ell_6$   
 559 :  $P_{213172} = (51, 1, 51, 1)$  lies on line  $\ell_8$   
 560 :  $P_{216308} = (51, 50, 51, 1)$  lies on line  $\ell_9$   
 561 :  $P_{217153} = (0, 0, 52, 1)$  lies on line  $\ell_5$   
 562 :  $P_{217154} = (1, 0, 52, 1)$  lies on line  $\ell_7$   
 563 :  $P_{217218} = (1, 1, 52, 1)$  lies on line  $\ell_6$   
 564 :  $P_{217269} = (52, 1, 52, 1)$  lies on line  $\ell_8$   
 565 :  $P_{220597} = (52, 53, 52, 1)$  lies on line  $\ell_9$   
 566 :  $P_{221249} = (0, 0, 53, 1)$  lies on line  $\ell_5$   
 567 :  $P_{221250} = (1, 0, 53, 1)$  lies on line  $\ell_7$   
 568 :  $P_{221314} = (1, 1, 53, 1)$  lies on line  $\ell_6$   
 569 :  $P_{221366} = (53, 1, 53, 1)$  lies on line  $\ell_8$   
 570 :  $P_{224630} = (53, 52, 53, 1)$  lies on line  $\ell_9$   
 571 :  $P_{225345} = (0, 0, 54, 1)$  lies on line  $\ell_5$   
 572 :  $P_{225346} = (1, 0, 54, 1)$  lies on line  $\ell_7$   
 573 :  $P_{225410} = (1, 1, 54, 1)$  lies on line  $\ell_6$   
 574 :  $P_{225463} = (54, 1, 54, 1)$  lies on line  $\ell_8$   
 575 :  $P_{228919} = (54, 55, 54, 1)$  lies on line  $\ell_9$   
 576 :  $P_{229441} = (0, 0, 55, 1)$  lies on line  $\ell_5$   
 577 :  $P_{229442} = (1, 0, 55, 1)$  lies on line  $\ell_7$   
 578 :  $P_{229506} = (1, 1, 55, 1)$  lies on line  $\ell_6$   
 579 :  $P_{229560} = (55, 1, 55, 1)$  lies on line  $\ell_8$   
 580 :  $P_{232952} = (55, 54, 55, 1)$  lies on line  $\ell_9$   
 581 :  $P_{233537} = (0, 0, 56, 1)$  lies on line  $\ell_5$   
 582 :  $P_{233538} = (1, 0, 56, 1)$  lies on line  $\ell_7$   
 583 :  $P_{233602} = (1, 1, 56, 1)$  lies on line  $\ell_6$   
 584 :  $P_{233657} = (56, 1, 56, 1)$  lies on line  $\ell_8$   
 585 :  $P_{237241} = (56, 57, 56, 1)$  lies on line  $\ell_9$   
 586 :  $P_{237633} = (0, 0, 57, 1)$  lies on line  $\ell_5$   
 587 :  $P_{237634} = (1, 0, 57, 1)$  lies on line  $\ell_7$   
 588 :  $P_{237698} = (1, 1, 57, 1)$  lies on line  $\ell_6$   
 589 :  $P_{237754} = (57, 1, 57, 1)$  lies on line  $\ell_8$   
 590 :  $P_{241274} = (57, 56, 57, 1)$  lies on line  $\ell_9$   
 591 :  $P_{241729} = (0, 0, 58, 1)$  lies on line  $\ell_5$   
 592 :  $P_{241730} = (1, 0, 58, 1)$  lies on line  $\ell_7$   
 593 :  $P_{241794} = (1, 1, 58, 1)$  lies on line  $\ell_6$   
 594 :  $P_{241851} = (58, 1, 58, 1)$  lies on line  $\ell_8$   
 595 :  $P_{245563} = (58, 59, 58, 1)$  lies on line  $\ell_9$   
 596 :  $P_{245825} = (0, 0, 59, 1)$  lies on line  $\ell_5$   
 597 :  $P_{245826} = (1, 0, 59, 1)$  lies on line  $\ell_7$   
 598 :  $P_{245890} = (1, 1, 59, 1)$  lies on line  $\ell_6$   
 599 :  $P_{245948} = (59, 1, 59, 1)$  lies on line  $\ell_8$   
 600 :  $P_{249596} = (59, 58, 59, 1)$  lies on line  $\ell_9$   
 601 :  $P_{249921} = (0, 0, 60, 1)$  lies on line  $\ell_5$   
 602 :  $P_{249922} = (1, 0, 60, 1)$  lies on line  $\ell_7$   
 603 :  $P_{249986} = (1, 1, 60, 1)$  lies on line  $\ell_6$   
 604 :  $P_{250045} = (60, 1, 60, 1)$  lies on line  $\ell_8$   
 605 :  $P_{253885} = (60, 61, 60, 1)$  lies on line  $\ell_9$   
 606 :  $P_{254017} = (0, 0, 61, 1)$  lies on line  $\ell_5$   
 607 :  $P_{254018} = (1, 0, 61, 1)$  lies on line  $\ell_7$   
 608 :  $P_{254082} = (1, 1, 61, 1)$  lies on line  $\ell_6$   
 609 :  $P_{254142} = (61, 1, 61, 1)$  lies on line  $\ell_8$   
 610 :  $P_{257918} = (61, 60, 61, 1)$  lies on line  $\ell_9$   
 611 :  $P_{258113} = (0, 0, 62, 1)$  lies on line  $\ell_5$   
 612 :  $P_{258114} = (1, 0, 62, 1)$  lies on line  $\ell_7$   
 613 :  $P_{258178} = (1, 1, 62, 1)$  lies on line  $\ell_6$   
 614 :  $P_{258239} = (62, 1, 62, 1)$  lies on line  $\ell_8$   
 615 :  $P_{262207} = (62, 63, 62, 1)$  lies on line  $\ell_9$   
 616 :  $P_{262209} = (0, 0, 63, 1)$  lies on line  $\ell_5$   
 617 :  $P_{262210} = (1, 0, 63, 1)$  lies on line  $\ell_7$   
 618 :  $P_{262274} = (1, 1, 63, 1)$  lies on line  $\ell_6$   
 619 :  $P_{262336} = (63, 1, 63, 1)$  lies on line  $\ell_8$   
 620 :  $P_{266240} = (63, 62, 63, 1)$  lies on line  $\ell_9$

The single points on the surface are:

### Points on surface but on no line

The surface has 3720 points not on any line:  
Too many to print.



## Line Intersection Graph

|   | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|---|---|---|---|---|---|---|---|---|---|
| 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 0 |
| 2 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 |
| 3 | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 4 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 5 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 6 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 |
| 7 | 0 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 1 |
| 8 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 9 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 0 |

Neighbor sets in the line intersection graph:

Line 0 intersects

| Line     | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_4$ |
|----------|----------|----------|----------|----------|
| in point | $P_0$    | $P_5$    | $P_1$    | $P_1$    |

Line 1 intersects

| Line     | $\ell_0$ | $\ell_2$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_8$ |
|----------|----------|----------|----------|----------|----------|----------|
| in point | $P_0$    | $P_2$    | $P_2$    | $P_2$    | $P_2$    | $P_{68}$ |

Line 2 intersects

| Line     | $\ell_0$ | $\ell_1$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_9$  |
|----------|----------|----------|----------|----------|----------|-----------|
| in point | $P_5$    | $P_2$    | $P_2$    | $P_2$    | $P_2$    | $P_{132}$ |

Line 3 intersects

| Line     | $\ell_0$ | $\ell_4$ | $\ell_5$ | $\ell_8$   | $\ell_9$   |
|----------|----------|----------|----------|------------|------------|
| in point | $P_1$    | $P_1$    | $P_3$    | $P_{4226}$ | $P_{4226}$ |

Line 4 intersects

| Line     | $\ell_0$ | $\ell_3$ | $\ell_6$   | $\ell_7$   |
|----------|----------|----------|------------|------------|
| in point | $P_1$    | $P_1$    | $P_{4227}$ | $P_{4163}$ |

Line 5 intersects

| Line     | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_6$ | $\ell_7$ |
|----------|----------|----------|----------|----------|----------|
| in point | $P_2$    | $P_2$    | $P_3$    | $P_2$    | $P_2$    |

Line 6 intersects

| Line     | $\ell_1$ | $\ell_2$ | $\ell_4$   | $\ell_5$ | $\ell_7$ | $\ell_8$ |
|----------|----------|----------|------------|----------|----------|----------|
| in point | $P_2$    | $P_2$    | $P_{4227}$ | $P_2$    | $P_2$    | $P_4$    |

Line 7 intersects

| Line     | $\ell_1$ | $\ell_2$ | $\ell_4$   | $\ell_5$ | $\ell_6$ | $\ell_9$   |
|----------|----------|----------|------------|----------|----------|------------|
| in point | $P_2$    | $P_2$    | $P_{4163}$ | $P_2$    | $P_2$    | $P_{8259}$ |

Line 8 intersects

| Line     | $\ell_1$ | $\ell_3$   | $\ell_6$ | $\ell_9$   |
|----------|----------|------------|----------|------------|
| in point | $P_{68}$ | $P_{4226}$ | $P_4$    | $P_{4226}$ |

Line 9 intersects

| Line     | $\ell_2$  | $\ell_3$   | $\ell_7$   | $\ell_8$   |
|----------|-----------|------------|------------|------------|
| in point | $P_{132}$ | $P_{4226}$ | $P_{8259}$ | $P_{4226}$ |

The surface has 4353 points:

Too many to print.