

# Rank-4 over GF(4)

January 14, 2021

## General information

Points on lines:

$$5^{41}$$

Lines on points:

$$9^5, 5^{32}$$

## Singular Points

The surface has 21 singular points:

$$\begin{aligned} S_0 = P_1 &= \mathbf{P}(0, 1, 0, 0) = \mathbf{P}(0, 1, 0, 0) \\ S_1 = P_2 &= \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0) \\ S_2 = P_3 &= \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1) \\ S_3 = P_{11} &= \mathbf{P}(0, 1, 1, 0) = \mathbf{P}(0, 1, 1, 0) \\ S_4 = P_{15} &= \mathbf{P}(0, \omega, 1, 0) = \mathbf{P}(0, 2, 1, 0) \\ S_5 = P_{19} &= \mathbf{P}(0, \omega^2, 1, 0) = \mathbf{P}(0, 3, 1, 0) \\ S_6 = P_{26} &= \mathbf{P}(0, 1, 0, 1) = \mathbf{P}(0, 1, 0, 1) \\ S_7 = P_{30} &= \mathbf{P}(0, \omega, 0, 1) = \mathbf{P}(0, 2, 0, 1) \\ S_8 = P_{34} &= \mathbf{P}(0, \omega^2, 0, 1) = \mathbf{P}(0, 3, 0, 1) \\ S_9 = P_{38} &= \mathbf{P}(0, 0, 1, 1) = \mathbf{P}(0, 0, 1, 1) \\ S_{10} = P_{42} &= \mathbf{P}(0, 1, 1, 1) = \mathbf{P}(0, 1, 1, 1) \\ S_{11} = P_{45} &= \mathbf{P}(0, \omega, 1, 1) = \mathbf{P}(0, 2, 1, 1) \\ S_{12} = P_{49} &= \mathbf{P}(0, \omega^2, 1, 1) = \mathbf{P}(0, 3, 1, 1) \\ S_{13} = P_{53} &= \mathbf{P}(0, 0, \omega, 1) = \mathbf{P}(0, 0, 2, 1) \\ S_{14} = P_{57} &= \mathbf{P}(0, 1, \omega, 1) = \mathbf{P}(0, 1, 2, 1) \\ S_{15} = P_{61} &= \mathbf{P}(0, \omega, \omega, 1) = \mathbf{P}(0, 2, 2, 1) \\ S_{16} = P_{65} &= \mathbf{P}(0, \omega^2, \omega, 1) = \mathbf{P}(0, 3, 2, 1) \\ S_{17} = P_{69} &= \mathbf{P}(0, 0, \omega^2, 1) = \mathbf{P}(0, 0, 3, 1) \\ S_{18} = P_{73} &= \mathbf{P}(0, 1, \omega^2, 1) = \mathbf{P}(0, 1, 3, 1) \\ S_{19} = P_{77} &= \mathbf{P}(0, \omega, \omega^2, 1) = \mathbf{P}(0, 2, 3, 1) \\ S_{20} = P_{81} &= \mathbf{P}(0, \omega^2, \omega^2, 1) = \mathbf{P}(0, 3, 3, 1) \end{aligned}$$

## The 41 Lines

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{16} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{16} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2$$

$$\begin{aligned}
\ell_1 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{336} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{336} = \mathbf{Pl}(0, 0, 0, 0, 0, 1)_{101} \\
\ell_2 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{20} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{20} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)_{25} \\
\ell_3 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{17} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{17} = \mathbf{Pl}(0, 0, 1, 0, 1, 0)_{32} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{19} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{19} = \mathbf{Pl}(0, 0, 2, 0, 1, 0)_{39} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \omega \end{bmatrix}_{18} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{18} = \mathbf{Pl}(0, 0, 3, 0, 1, 0)_{46} \\
\ell_6 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{340} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{340} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)_9 \\
\ell_7 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{337} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{337} = \mathbf{Pl}(0, 0, 0, 1, 0, 1)_{129} \\
\ell_8 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{339} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{339} = \mathbf{Pl}(0, 0, 0, 3, 0, 1)_{143} \\
\ell_9 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & \omega \end{bmatrix}_{338} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{338} = \mathbf{Pl}(0, 0, 0, 2, 0, 1)_{136} \\
\ell_{10} &= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{356} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{356} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_1 \\
\ell_{11} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{100} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{100} = \mathbf{Pl}(0, 1, 1, 0, 0, 0)_6 \\
\ell_{12} &= \begin{bmatrix} 1 & 0 & 0 & \omega^2 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{268} = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{268} = \mathbf{Pl}(0, 3, 1, 0, 0, 0)_8 \\
\ell_{13} &= \begin{bmatrix} 1 & 0 & 0 & \omega \\ 0 & 0 & 1 & 0 \end{bmatrix}_{184} = \begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{184} = \mathbf{Pl}(0, 2, 1, 0, 0, 0)_7 \\
\ell_{14} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{341} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{341} = \mathbf{Pl}(0, 1, 0, 0, 0, 1)_{105} \\
\ell_{15} &= \begin{bmatrix} 0 & 1 & 0 & \omega^2 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{351} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{351} = \mathbf{Pl}(0, 3, 0, 0, 0, 1)_{107} \\
\ell_{16} &= \begin{bmatrix} 0 & 1 & 0 & \omega \\ 0 & 0 & 1 & 0 \end{bmatrix}_{346} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{346} = \mathbf{Pl}(0, 2, 0, 0, 0, 1)_{106} \\
\ell_{17} &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{104} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{104} = \mathbf{Pl}(0, 1, 0, 0, 1, 0)_{29} \\
\ell_{18} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{101} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{101} = \mathbf{Pl}(0, 1, 1, 0, 1, 0)_{36} \\
\ell_{19} &= \begin{bmatrix} 1 & 0 & 0 & \omega^2 \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{271} = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{271} = \mathbf{Pl}(0, 1, 2, 0, 1, 0)_{43} \\
\ell_{20} &= \begin{bmatrix} 1 & 0 & 0 & \omega \\ 0 & 0 & 1 & \omega \end{bmatrix}_{186} = \begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{186} = \mathbf{Pl}(0, 1, 3, 0, 1, 0)_{50} \\
\ell_{21} &= \begin{bmatrix} 1 & 0 & \omega^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \mathbf{Pl}(0, 3, 0, 0, 1, 0)_{31}
\end{aligned}$$

$$\begin{aligned}
\ell_{22} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & \omega \end{bmatrix}_{102} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{102} = \mathbf{Pl}(0, 3, 3, 0, 1, 0)_{52} \\
\ell_{23} &= \begin{bmatrix} 1 & 0 & 0 & \omega^2 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{269} = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{269} = \mathbf{Pl}(0, 3, 1, 0, 1, 0)_{38} \\
\ell_{24} &= \begin{bmatrix} 1 & 0 & 0 & \omega \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{187} = \begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{187} = \mathbf{Pl}(0, 3, 2, 0, 1, 0)_{45} \\
\ell_{25} &= \begin{bmatrix} 1 & 0 & \omega & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{188} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{188} = \mathbf{Pl}(0, 2, 0, 0, 1, 0)_{30} \\
\ell_{26} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{103} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{103} = \mathbf{Pl}(0, 2, 2, 0, 1, 0)_{44} \\
\ell_{27} &= \begin{bmatrix} 1 & 0 & 0 & \omega^2 \\ 0 & 0 & 1 & \omega \end{bmatrix}_{270} = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{270} = \mathbf{Pl}(0, 2, 3, 0, 1, 0)_{51} \\
\ell_{28} &= \begin{bmatrix} 1 & 0 & 0 & \omega \\ 0 & 0 & 1 & 1 \end{bmatrix}_{185} = \begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{185} = \mathbf{Pl}(0, 2, 1, 0, 1, 0)_{37} \\
\ell_{29} &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{345} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{345} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{13} \\
\ell_{30} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{342} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{342} = \mathbf{Pl}(0, 1, 0, 1, 0, 1)_{133} \\
\ell_{31} &= \begin{bmatrix} 0 & 1 & 0 & \omega^2 \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{354} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{354} = \mathbf{Pl}(0, 3, 0, 3, 0, 1)_{149} \\
\ell_{32} &= \begin{bmatrix} 0 & 1 & 0 & \omega \\ 0 & 0 & 1 & \omega \end{bmatrix}_{348} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{348} = \mathbf{Pl}(0, 2, 0, 2, 0, 1)_{141} \\
\ell_{33} &= \begin{bmatrix} 0 & 1 & \omega^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{355} = \begin{bmatrix} 0 & 1 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{355} = \mathbf{Pl}(0, 3, 0, 1, 0, 0)_{15} \\
\ell_{34} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & \omega \end{bmatrix}_{343} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{343} = \mathbf{Pl}(0, 1, 0, 2, 0, 1)_{140} \\
\ell_{35} &= \begin{bmatrix} 0 & 1 & 0 & \omega^2 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{352} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{352} = \mathbf{Pl}(0, 3, 0, 1, 0, 1)_{135} \\
\ell_{36} &= \begin{bmatrix} 0 & 1 & 0 & \omega \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{349} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{349} = \mathbf{Pl}(0, 2, 0, 3, 0, 1)_{148} \\
\ell_{37} &= \begin{bmatrix} 0 & 1 & \omega & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{350} = \begin{bmatrix} 0 & 1 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{350} = \mathbf{Pl}(0, 2, 0, 1, 0, 0)_{14} \\
\ell_{38} &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & \omega^2 \end{bmatrix}_{344} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 3 \end{bmatrix}_{344} = \mathbf{Pl}(0, 1, 0, 3, 0, 1)_{147} \\
\ell_{39} &= \begin{bmatrix} 0 & 1 & 0 & \omega^2 \\ 0 & 0 & 1 & \omega \end{bmatrix}_{353} = \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 2 \end{bmatrix}_{353} = \mathbf{Pl}(0, 3, 0, 2, 0, 1)_{142} \\
\ell_{40} &= \begin{bmatrix} 0 & 1 & 0 & \omega \\ 0 & 0 & 1 & 1 \end{bmatrix}_{347} = \begin{bmatrix} 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{347} = \mathbf{Pl}(0, 2, 0, 1, 0, 1)_{134}
\end{aligned}$$

Rank of lines: ( 16, 336, 20, 17, 19, 18, 340, 337, 339, 338, 356, 100, 268, 184, 341, 351, 346, 104, 101, 271, 186, 272, 102, 269, 187, 188, 103, 270, 185, 345, 342, 354, 348, 355, 343, 352, 349, 350, 344, 353, 347 )

Rank of points on Klein quadric: ( 2, 101, 25, 32, 39, 46, 9, 129, 143, 136, 1, 6, 8, 7, 105, 107, 106, 29, 36, 43, 50, 31, 52, 38, 45, 30, 44, 51, 37, 13, 133, 149, 141, 15, 140, 135, 148, 14, 147, 142, 134 )

### **Eckardt Points**

The surface has 0 Eckardt points:

### **Double Points**

The surface has 0 Double points:

The double points on the surface are:

### **Single Points**

The surface has 0 single points:

The single points on the surface are:

The single points on the surface are:

### **Points on surface but on no line**

The surface has 0 points not on any line:

	0	1	2	3	4	5	6	7	8	9
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The points on the surface but not on lines are:

## Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40							
0	0	1	1	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0						
1	1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1					
2	1	0	0	1	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0				
3	1	0	1	0	1	1	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1			
4	1	0	1	1	0	1	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	1	0	0	0	0	1	0	1	0	1	0	0	0				
5	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	0	0	1	0			
6	0	1	1	0	0	0	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
7	0	1	0	1	0	0	1	1	1	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
8	0	1	0	0	1	0	1	1	1	0	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
9	0	1	0	0	0	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	1	0	0	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
10	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
11	1	1	1	1	1	0	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
12	1	1	1	1	1	0	0	0	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
13	1	1	1	1	1	0	0	0	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
14	1	1	0	0	0	1	1	1	1	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
15	1	1	0	0	0	1	1	1	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
16	1	1	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1		
17	1	0	1	1	1	1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	0		
18	1	0	1	1	1	0	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1			
19	1	0	1	1	1	0	0	0	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	1	0	0	0	0	1	0	1	0	0	0	1	0	0	0		
20	1	0	1	1	1	0	0	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	0	0	1	0	0		
21	1	0	1	1	1	0	0	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	
22	1	0	1	1	1	0	0	0	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	0	0	1	0	0		
23	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1	0	0	
24	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	0	0	0	0	1	0	1	0	0	0	1	0	0	0		
25	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	
26	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	0	0	1	0	0	0	0	1	0	1	0	0	0	1	0	0	
27	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	0	0	0	1	0	1	0	0	0	0	1	0	0	0	1	0	0	
28	1	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1		
29	0	1	1	0	0	1	1	1	1	0	0	0	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
30	0	1	0	1	0	1	1	1	1	0	0	0	1	1	1	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
31	0	1	0	0	1	0	0	0	1	1	1	0	0	1	0	0	0	0	1	0	0	0	0	1	0	1	0	0	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
32	0	1	0	0	0	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	1	0	0	0	0	1	0	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
33	0	1	1	0	0	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
34	0	1	0	0	0	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	1	0	0	0	0	1	0	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	
35	0	1	0	1	0	1	1	1	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
36	0	1	0	0	1	0	0	0	1	1	1	0	0	1	0	0	0	0	1	0	0	0	0	1	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
37	0	1	1	0	0	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
38	0	1	0	0	1	0	0	0	1	1	1	0	0	1	0	0	0	0	1	0	0	0	0	1	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
39	0	1	0	0	0	1	1	1	0	0	0	1	0	1	0	0	0	0	1	0	1	0	0	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
40	0	1	0	1	0	0	1	1	1	0	1	0	0	0	0	1	0	0	0	0	0	0	0	1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{10}</$
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Line 2 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_0$	$P_0$	$P_0$	$P_0$	$P_3$	$P_3$	$P_{23}$	$P_{24}$	$P_{25}$	$P_3$	$P_{23}$	$P_{24}$	$P_{25}$	$P_3$	$P_{23}$	$P_{24}$	$P_{25}$	$P_3$	$P_{23}$	$P_{24}$	$P_{25}$

Line 3 intersects

Line	$\ell_0$	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_0$	$P_0$	$P_0$	$P_0$	$P_{38}$	$P_{38}$	$P_{39}$	$P_{40}$	$P_{41}$	$P_{39}$	$P_{38}$	$P_{41}$	$P_{40}$	$P_{40}$	$P_{41}$	$P_{38}$	$P_{39}$	$P_{41}$	$P_{40}$	$P_{39}$	$P_{41}$

Line 4 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_0$	$P_0$	$P_0$	$P_0$	$P_{53}$	$P_{53}$	$P_{54}$	$P_{55}$	$P_{56}$	$P_{55}$	$P_{56}$	$P_{53}$	$P_{54}$	$P_{56}$	$P_{55}$	$P_{54}$	$P_{53}$	$P_{54}$	$P_{53}$	$P_{56}$	$P_{54}$

Line 5 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_0$	$P_0$	$P_0$	$P_0$	$P_{69}$	$P_{69}$	$P_{70}$	$P_{71}$	$P_{72}$	$P_{72}$	$P_{71}$	$P_{70}$	$P_{69}$	$P_{70}$	$P_{69}$	$P_{72}$	$P_{71}$	$P_{71}$	$P_{72}$	$P_{69}$	$P_{71}$

Line 6 intersects

Line	$\ell_1$	$\ell_2$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{21}$	$\ell_{25}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_1$	$P_3$	$P_1$	$P_1$	$P_1$	$P_3$	$P_{26}$	$P_{30}$	$P_{34}$	$P_3$	$P_3$	$P_3$	$P_3$	$P_{26}$	$P_{30}$	$P_{34}$	$P_3$	$P_{26}$	$P_{30}$	$P_{34}$	$P_3$

Line 7 intersects

Line	$\ell_1$	$\ell_3$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{18}$	$\ell_{23}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_1$	$P_{38}$	$P_1$	$P_1$	$P_1$	$P_{38}$	$P_{42}$	$P_{45}$	$P_{49}$	$P_{38}$	$P_{38}$	$P_{38}$	$P_{42}$	$P_{38}$	$P_{49}$	$P_{45}$	$P_{45}$	$P_{49}$	$P_{38}$	$P_{42}$	$P_{45}$

Line 8 intersects

Line	$\ell_1$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{19}$	$\ell_{24}$	$\ell_{26}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_1$	$P_{53}$	$P_1$	$P_1$	$P_1$	$P_{53}$	$P_{57}$	$P_{61}$	$P_{65}$	$P_{53}$	$P_{53}$	$P_{53}$	$P_{61}$	$P_{65}$	$P_{53}$	$P_{57}$	$P_{65}$	$P_{61}$	$P_{57}$	$P_{53}$	$P_{61}$

Line 9 intersects

Line	$\ell_1$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{20}$	$\ell_{22}$	$\ell_{27}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_1$	$P_{69}$	$P_1$	$P_1$	$P_1$	$P_{69}$	$P_{73}$	$P_{77}$	$P_{81}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{81}$	$P_{77}$	$P_{73}$	$P_{69}$	$P_{73}$	$P_{69}$	$P_{81}$	$P_{77}$	$P_{73}$

Line 10 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$
in point	$P_2$	$P_2$	$P_3$	$P_{38}$	$P_{53}$	$P_{69}$	$P_3$	$P_{38}$	$P_{53}$	$P_{69}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_3$	$P_{38}$	$P_{53}$	$P_{69}$	$P_3$

Line 11 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$
in point	$P_2$	$P_2$	$P_{23}$	$P_{39}$	$P_{54}$	$P_{70}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_{39}$	$P_{23}$	$P_{70}$	$P_{54}$	$P_{70}$	$P_{23}$	$P_{54}$	$P_{39}$	$P_{70}$

Line 12 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$
in point	$P_2$	$P_2$	$P_{24}$	$P_{40}$	$P_{55}$	$P_{71}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_{55}$	$P_{71}$	$P_{24}$	$P_{40}$	$P_{40}$	$P_{55}$	$P_{24}$	$P_{71}$	$P_{55}$

Line 13 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$
in point	$P_2$	$P_2$	$P_{25}$	$P_{41}$	$P_{56}$	$P_{72}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_{72}$	$P_{56}$	$P_{41}$	$P_{25}$	$P_{56}$	$P_{41}$	$P_{72}$	$P_{25}$	$P_{56}$

Line 14 intersects

Line	$\ell_0$	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_2$	$P_2$	$P_{26}$	$P_{42}$	$P_{57}$	$P_{73}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_{42}$	$P_{26}$	$P_{73}$	$P_{57}$	$P_{73}$	$P_{26}$	$P_{57}$	$P_{42}$	$P_{73}$

Line 15 intersects

Line	$\ell_0$	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{16}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_2$	$P_2$	$P_{30}$	$P_{45}$	$P_{61}$	$P_{77}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_{61}$	$P_{77}$	$P_{30}$	$P_{45}$	$P_{45}$	$P_{61}$	$P_{30}$	$P_{77}$	$P_{30}$

Line 16 intersects

Line	$\ell_0$	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_2$	$P_2$	$P_{34}$	$P_{49}$	$P_{65}$	$P_{81}$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_2$	$P_{81}$	$P_{65}$	$P_{49}$	$P_{34}$	$P_{65}$	$P_{49}$	$P_{81}$	$P_{34}$	$P_{34}$

Line 17 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_8$	$P_3$	$P_{39}$	$P_{55}$	$P_{72}$	$P_3$	$P_3$	$P_{39}$	$P_{55}$	$P_{72}$	$P_8$	$P_8$	$P_8$	$P_3$	$P_{55}$	$P_{72}$	$P_{39}$	$P_3$	$P_{72}$	$P_{39}$	$P_{55}$

Line 18 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_8$	$P_{23}$	$P_{38}$	$P_{56}$	$P_{71}$	$P_{38}$	$P_{38}$	$P_{23}$	$P_{71}$	$P_{56}$	$P_8$	$P_8$	$P_8$	$P_{56}$	$P_{23}$	$P_{38}$	$P_{71}$	$P_{71}$	$P_{23}$	$P_{56}$	$P_{56}$

Line 19 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_8$	$P_{24}$	$P_{41}$	$P_{53}$	$P_{70}$	$P_{53}$	$P_{53}$	$P_{70}$	$P_{24}$	$P_{41}$	$P_8$	$P_8$	$P_8$	$P_{70}$	$P_{41}$	$P_{24}$	$P_{53}$	$P_{41}$	$P_{53}$	$P_{24}$	$P_{24}$

Line 20 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_8$	$P_{25}$	$P_{40}$	$P_{54}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{54}$	$P_{40}$	$P_{25}$	$P_8$	$P_8$	$P_8$	$P_{40}$	$P_{69}$	$P_{54}$	$P_{25}$	$P_{54}$	$P_{40}$	$P_{69}$	$P_{69}$

Line 21 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_9$	$P_3$	$P_{40}$	$P_{56}$	$P_{70}$	$P_3$	$P_3$	$P_{70}$	$P_{40}$	$P_{56}$	$P_3$	$P_{56}$	$P_{70}$	$P_{40}$	$P_9$	$P_9$	$P_9$	$P_3$	$P_{40}$	$P_{56}$	$P_{70}$

Line 22 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_9$	$P_{23}$	$P_{41}$	$P_{55}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{23}$	$P_{55}$	$P_{41}$	$P_{55}$	$P_{23}$	$P_{41}$	$P_{69}$	$P_9$	$P_9$	$P_9$	$P_{41}$	$P_{23}$	$P_{69}$	$P_{69}$

Line 23 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_9$	$P_{24}$	$P_{38}$	$P_{54}$	$P_{72}$	$P_{38}$	$P_{38}$	$P_{54}$	$P_{24}$	$P_{72}$	$P_{72}$	$P_{38}$	$P_{24}$	$P_{54}$	$P_9$	$P_9$	$P_9$	$P_{54}$	$P_{72}$	$P_{24}$	$P_{24}$

Line 24 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_9$	$P_{25}$	$P_{39}$	$P_{53}$	$P_{71}$	$P_{53}$	$P_{53}$	$P_{39}$	$P_{71}$	$P_{25}$	$P_{39}$	$P_{71}$	$P_{53}$	$P_{25}$	$P_9$	$P_9$	$P_9$	$P_{71}$	$P_{53}$	$P_{39}$	$P_{39}$

Line 25 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$
in point	$P_{10}$	$P_3$	$P_{41}$	$P_{54}$	$P_{71}$	$P_3$	$P_3$	$P_{54}$	$P_{71}$	$P_{41}$	$P_3$	$P_{71}$	$P_{41}$	$P_{54}$	$P_3$	$P_{41}$	$P_{54}$	$P_{71}$	$P_{10}$	$P_{10}$	$P_{10}$

Line 26 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{27}$	$\ell_{28}$
in point	$P_{10}$	$P_{23}$	$P_{40}$	$P_{53}$	$P_{72}$	$P_{53}$	$P_{53}$	$P_{23}$	$P_{40}$	$P_{72}$	$P_{72}$	$P_{23}$	$P_{53}$	$P_{40}$	$P_{40}$	$P_{23}$	$P_{72}$	$P_{53}$	$P_{10}$	$P_{10}$	$P_{10}$

Line 27 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{27}$	$\ell_{28}$
in point	$P_{10}$	$P_{24}$	$P_{39}$	$P_{56}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{39}$	$P_{24}$	$P_{56}$	$P_{39}$	$P_{56}$	$P_{24}$	$P_{69}$	$P_{56}$	$P_{69}$	$P_{24}$	$P_{39}$	$P_{10}$	$P_{10}$	$P_{10}$

Line 28 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{10}$	$P_{25}$	$P_{38}$	$P_{55}$	$P_{70}$	$P_{38}$	$P_{38}$	$P_{70}$	$P_{55}$	$P_{25}$	$P_{55}$	$P_{38}$	$P_{70}$	$P_{25}$	$P_{70}$	$P_{55}$	$P_{38}$	$P_{25}$	$P_{10}$	$P_{10}$

Line 29 intersects

Line	$\ell_1$	$\ell_2$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{21}$	$\ell_{25}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{11}$	$P_3$	$P_3$	$P_{42}$	$P_{61}$	$P_{81}$	$P_3$	$P_{42}$	$P_{61}$	$P_{81}$	$P_3$	$P_3$	$P_3$	$P_{11}$	$P_{11}$	$P_{11}$	$P_3$	$P_{61}$	$P_{81}$	$P_{42}$	$P_{11}$

Line 30 intersects

Line	$\ell_1$	$\ell_3$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{18}$	$\ell_{23}$	$\ell_{28}$	$\ell_{29}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{11}$	$P_{38}$	$P_{26}$	$P_{38}$	$P_{65}$	$P_{77}$	$P_{38}$	$P_{26}$	$P_{77}$	$P_{65}$	$P_{38}$	$P_{38}$	$P_{38}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{65}$	$P_{26}$	$P_{38}$	$P_{77}$	$P_{38}$

Line 31 intersects

Line	$\ell_1$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{19}$	$\ell_{24}$	$\ell_{26}$	$\ell_{29}$	$\ell_{30}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{11}$	$P_{53}$	$P_{30}$	$P_{49}$	$P_{53}$	$P_{73}$	$P_{53}$	$P_{73}$	$P_{30}$	$P_{49}$	$P_{53}$	$P_{53}$	$P_{53}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{73}$	$P_{49}$	$P_{30}$	$P_{53}$	$P_{73}$

Line 32 intersects

Line	$\ell_1$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{20}$	$\ell_{22}$	$\ell_{27}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{11}$	$P_{69}$	$P_{34}$	$P_{45}$	$P_{57}$	$P_{69}$	$P_{69}$	$P_{57}$	$P_{45}$	$P_{34}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{45}$	$P_{69}$	$P_{57}$	$P_{34}$

Line 33 intersects

Line	$\ell_1$	$\ell_2$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{21}$	$\ell_{25}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{15}$	$P_3$	$P_3$	$P_{45}$	$P_{65}$	$P_{73}$	$P_3$	$P_{73}$	$P_{45}$	$P_{65}$	$P_3$	$P_3$	$P_3$	$P_3$	$P_{65}$	$P_{73}$	$P_{45}$	$P_{15}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 34 intersects

Line	$\ell_1$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{20}$	$\ell_{22}$	$\ell_{27}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{15}$	$P_{69}$	$P_{26}$	$P_{49}$	$P_{61}$	$P_{69}$	$P_{69}$	$P_{26}$	$P_{61}$	$P_{49}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{61}$	$P_{26}$	$P_{49}$	$P_{69}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 35 intersects

Line	$\ell_1$	$\ell_3$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{18}$	$\ell_{23}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{15}$	$P_{38}$	$P_{30}$	$P_{38}$	$P_{57}$	$P_{81}$	$P_{38}$	$P_{57}$	$P_{30}$	$P_{81}$	$P_{38}$	$P_{38}$	$P_{38}$	$P_{81}$	$P_{38}$	$P_{30}$	$P_{57}$	$P_{15}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 36 intersects

Line	$\ell_1$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{19}$	$\ell_{24}$	$\ell_{26}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{15}$	$P_{53}$	$P_{34}$	$P_{42}$	$P_{53}$	$P_{77}$	$P_{53}$	$P_{42}$	$P_{77}$	$P_{34}$	$P_{53}$	$P_{53}$	$P_{53}$	$P_{42}$	$P_{77}$	$P_{53}$	$P_{34}$	$P_{15}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 37 intersects

Line	$\ell_1$	$\ell_2$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{21}$	$\ell_{25}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{37}$
in point	$P_{19}$	$P_3$	$P_3$	$P_{49}$	$P_{57}$	$P_{77}$	$P_3$	$P_{57}$	$P_{77}$	$P_{49}$	$P_3$	$P_3$	$P_3$	$P_3$	$P_{77}$	$P_{49}$	$P_{57}$	$P_3$	$P_{49}$	$P_{57}$	$P_{77}$

Line 38 intersects

Line	$\ell_1$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{19}$	$\ell_{24}$	$\ell_{26}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{19}$	$P_{53}$	$P_{26}$	$P_{45}$	$P_{53}$	$P_{81}$	$P_{53}$	$P_{26}$	$P_{45}$	$P_{81}$	$P_{53}$	$P_{53}$	$P_{53}$	$P_{81}$	$P_{26}$	$P_{53}$	$P_{45}$	$P_{45}$	$P_{26}$	$P_{81}$	$P_{53}$

Line 39 intersects

Line	$\ell_1$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{20}$	$\ell_{22}$	$\ell_{27}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{19}$	$P_{69}$	$P_{30}$	$P_{42}$	$P_{65}$	$P_{69}$	$P_{69}$	$P_{42}$	$P_{30}$	$P_{65}$	$P_{69}$	$P_{69}$	$P_{69}$	$P_{42}$	$P_{65}$	$P_{30}$	$P_{69}$	$P_{65}$	$P_{69}$	$P_{30}$	$P_{69}$

Line 40 intersects

Line	$\ell_1$	$\ell_3$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{18}$	$\ell_{23}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{36}$	$\ell_{37}$
in point	$P_{19}$	$P_{38}$	$P_{34}$	$P_{38}$	$P_{61}$	$P_{73}$	$P_{38}$	$P_{73}$	$P_{61}$	$P_{34}$	$P_{38}$	$P_{38}$	$P_{38}$	$P_{61}$	$P_{38}$	$P_{73}$	$P_{34}$	$P_{73}$	$P_{61}$	$P_{38}$	$P_{73}$

The surface has 37 points:

The points on the surface are:



0 :  $P_0 = (1, 0, 0, 0)$   
 1 :  $P_1 = (0, 1, 0, 0)$   
 2 :  $P_2 = (0, 0, 1, 0)$   
 3 :  $P_3 = (0, 0, 0, 1)$   
 4 :  $P_8 = (1, 0, 1, 0)$   
 5 :  $P_9 = (2, 0, 1, 0)$   
 6 :  $P_{10} = (3, 0, 1, 0)$   
 7 :  $P_{11} = (0, 1, 1, 0)$   
 8 :  $P_{15} = (0, 2, 1, 0)$   
 9 :  $P_{19} = (0, 3, 1, 0)$   
 10 :  $P_{23} = (1, 0, 0, 1)$   
 11 :  $P_{24} = (2, 0, 0, 1)$   
 12 :  $P_{25} = (3, 0, 0, 1)$

13 :  $P_{26} = (0, 1, 0, 1)$   
 14 :  $P_{30} = (0, 2, 0, 1)$   
 15 :  $P_{34} = (0, 3, 0, 1)$   
 16 :  $P_{38} = (0, 0, 1, 1)$   
 17 :  $P_{39} = (1, 0, 1, 1)$   
 18 :  $P_{40} = (2, 0, 1, 1)$   
 19 :  $P_{41} = (3, 0, 1, 1)$   
 20 :  $P_{42} = (0, 1, 1, 1)$   
 21 :  $P_{45} = (0, 2, 1, 1)$   
 22 :  $P_{49} = (0, 3, 1, 1)$   
 23 :  $P_{53} = (0, 0, 2, 1)$   
 24 :  $P_{54} = (1, 0, 2, 1)$   
 25 :  $P_{55} = (2, 0, 2, 1)$

26 :  $P_{56} = (3, 0, 2, 1)$   
 27 :  $P_{57} = (0, 1, 2, 1)$   
 28 :  $P_{61} = (0, 2, 2, 1)$   
 29 :  $P_{65} = (0, 3, 2, 1)$   
 30 :  $P_{69} = (0, 0, 3, 1)$   
 31 :  $P_{70} = (1, 0, 3, 1)$   
 32 :  $P_{71} = (2, 0, 3, 1)$   
 33 :  $P_{72} = (3, 0, 3, 1)$   
 34 :  $P_{73} = (0, 1, 3, 1)$   
 35 :  $P_{77} = (0, 2, 3, 1)$   
 36 :  $P_{81} = (0, 3, 3, 1)$