

# Rank-24 over GF(64)

January 15, 2021

## The equation

The equation of the surface is :

$$X_0^3 + X_1^3 + X_2^3 = 0$$

( 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0 )

The point rank of the equation over GF(64) is 148

## General information

Number of lines	81
Number of points	5185
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	5184
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$65^{81}$
Type of lines on points	$81, 1^{5184}$

## Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

## The 81 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned} \ell_0 &= \left[ \begin{array}{cccc} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{8321} = \left[ \begin{array}{cccc} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{8321} = \mathbf{Pl}(0, 0, 0, 1, 1, 0)_{12353} \\ \ell_1 &= \left[ \begin{array}{cccc} 1 & \epsilon^{21} & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{241337} = \left[ \begin{array}{cccc} 1 & 57 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{241337} = \mathbf{Pl}(0, 0, 0, 57, 1, 0)_{19465} \end{aligned}$$

$$\begin{aligned}
\ell_2 &= \begin{bmatrix} 1 & \epsilon^{42} & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{237176} = \begin{bmatrix} 1 & 56 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{237176} = \mathbf{Pl}(0, 0, 0, 56, 1, 0)_{19338} \\
\ell_3 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{270464} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{270464} = \mathbf{Pl}(0, 1, 0, 0, 1, 0)_{4289} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15183488} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15183488} = \mathbf{Pl}(0, 57, 0, 0, 1, 0)_{4345} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14917184} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14917184} = \mathbf{Pl}(0, 56, 0, 0, 1, 0)_{4344} \\
\ell_6 &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043585} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043585} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{193} \\
\ell_7 &= \begin{bmatrix} 1 & \epsilon^{54} & \epsilon^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5638154} = \begin{bmatrix} 1 & 10 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5638154} = \mathbf{Pl}(0, 21, 0, 10, 1, 0)_{13580} \\
\ell_8 &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{57} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13269428} = \begin{bmatrix} 1 & 52 & 49 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13269428} = \mathbf{Pl}(0, 49, 0, 52, 1, 0)_{18942} \\
\ell_9 &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^{36} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9849086} = \begin{bmatrix} 1 & 62 & 36 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9849086} = \mathbf{Pl}(0, 36, 0, 62, 1, 0)_{20199} \\
\ell_{10} &= \begin{bmatrix} 1 & \epsilon^{15} & \epsilon^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16602389} = \begin{bmatrix} 1 & 21 & 62 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16602389} = \mathbf{Pl}(0, 62, 0, 21, 1, 0)_{15018} \\
\ell_{11} &= \begin{bmatrix} 1 & \epsilon^{57} & \epsilon^{54} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2871089} = \begin{bmatrix} 1 & 49 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2871089} = \mathbf{Pl}(0, 10, 0, 49, 1, 0)_{18522} \\
\ell_{12} &= \begin{bmatrix} 1 & \epsilon^{36} & \epsilon^{33} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14001764} = \begin{bmatrix} 1 & 36 & 52 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14001764} = \mathbf{Pl}(0, 52, 0, 36, 1, 0)_{16913} \\
\ell_{13} &= \begin{bmatrix} 1 & \epsilon^{39} & \epsilon^{48} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4027847} = \begin{bmatrix} 1 & 7 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4027847} = \mathbf{Pl}(0, 15, 0, 7, 1, 0)_{13193} \\
\ell_{14} &= \begin{bmatrix} 1 & \epsilon^{18} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12299915} = \begin{bmatrix} 1 & 11 & 46 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12299915} = \mathbf{Pl}(0, 46, 0, 11, 1, 0)_{13732} \\
\ell_{15} &= \begin{bmatrix} 1 & \epsilon^{60} & \epsilon^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8842124} = \begin{bmatrix} 1 & 12 & 33 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8842124} = \mathbf{Pl}(0, 33, 0, 12, 1, 0)_{13846} \\
\ell_{16} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5812916} = \begin{bmatrix} 1 & 52 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5812916} = \mathbf{Pl}(0, 21, 0, 52, 1, 0)_{18914} \\
\ell_{17} &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^{57} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13311038} = \begin{bmatrix} 1 & 62 & 49 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13311038} = \mathbf{Pl}(0, 49, 0, 62, 1, 0)_{20212} \\
\ell_{18} &= \begin{bmatrix} 1 & \epsilon^{54} & \epsilon^{36} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9632714} = \begin{bmatrix} 1 & 10 & 36 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9632714} = \mathbf{Pl}(0, 36, 0, 10, 1, 0)_{13595} \\
\ell_{19} &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5854526} = \begin{bmatrix} 1 & 62 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5854526} = \mathbf{Pl}(0, 21, 0, 62, 1, 0)_{20184} \\
\ell_{20} &= \begin{bmatrix} 1 & \epsilon^{54} & \epsilon^{57} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13094666} = \begin{bmatrix} 1 & 10 & 49 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13094666} = \mathbf{Pl}(0, 49, 0, 10, 1, 0)_{13608} \\
\ell_{21} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{36} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9807476} = \begin{bmatrix} 1 & 52 & 36 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9807476} = \mathbf{Pl}(0, 36, 0, 52, 1, 0)_{18929} \\
\ell_{22} &= \begin{bmatrix} 1 & \epsilon^9 & \epsilon^{24} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12183407} = \begin{bmatrix} 1 & 47 & 45 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12183407} = \mathbf{Pl}(0, 45, 0, 47, 1, 0)_{18303}
\end{aligned}$$

$$\begin{aligned}
\ell_{23} &= \begin{bmatrix} 1 & \epsilon^{30} & \epsilon^{45} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10082102} = \begin{bmatrix} 1 & 54 & 37 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10082102} = \mathbf{Pl}(0, 37, 0, 54, 1, 0)_{19184} \\
\ell_{24} &= \begin{bmatrix} 1 & \epsilon^{51} & \epsilon^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2238617} = \begin{bmatrix} 1 & 25 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2238617} = \mathbf{Pl}(0, 8, 0, 25, 1, 0)_{15472} \\
\ell_{25} &= \begin{bmatrix} 1 & \epsilon^{49} & \epsilon^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15574622} = \begin{bmatrix} 1 & 30 & 58 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15574622} = \mathbf{Pl}(0, 58, 0, 30, 1, 0)_{16157} \\
\ell_{26} &= \begin{bmatrix} 1 & \epsilon^{28} & \epsilon^{56} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10910141} = \begin{bmatrix} 1 & 61 & 40 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10910141} = \mathbf{Pl}(0, 40, 0, 61, 1, 0)_{20076} \\
\ell_{27} &= \begin{bmatrix} 1 & \epsilon^7 & \epsilon^{35} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4943267} = \begin{bmatrix} 1 & 35 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4943267} = \mathbf{Pl}(0, 18, 0, 35, 1, 0)_{16752} \\
\ell_{28} &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12707693} = \begin{bmatrix} 1 & 45 & 47 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12707693} = \mathbf{Pl}(0, 47, 0, 45, 1, 0)_{18051} \\
\ell_{29} &= \begin{bmatrix} 1 & \epsilon^{45} & \epsilon^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14538533} = \begin{bmatrix} 1 & 37 & 54 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14538533} = \mathbf{Pl}(0, 54, 0, 37, 1, 0)_{17042} \\
\ell_{30} &= \begin{bmatrix} 1 & \epsilon^3 & \epsilon^{51} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6695048} = \begin{bmatrix} 1 & 8 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6695048} = \mathbf{Pl}(0, 25, 0, 8, 1, 0)_{13330} \\
\ell_{31} &= \begin{bmatrix} 1 & \epsilon^{48} & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3262223} = \begin{bmatrix} 1 & 15 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3262223} = \mathbf{Pl}(0, 12, 0, 15, 1, 0)_{14206} \\
\ell_{32} &= \begin{bmatrix} 1 & \epsilon^6 & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3070817} = \begin{bmatrix} 1 & 33 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3070817} = \mathbf{Pl}(0, 11, 0, 33, 1, 0)_{16491} \\
\ell_{33} &= \begin{bmatrix} 1 & \epsilon^{27} & \epsilon^{39} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2059694} = \begin{bmatrix} 1 & 46 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2059694} = \mathbf{Pl}(0, 7, 0, 46, 1, 0)_{18138} \\
\ell_{34} &= \begin{bmatrix} 1 & \epsilon^{14} & \epsilon^{28} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16490042} = \begin{bmatrix} 1 & 58 & 61 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16490042} = \mathbf{Pl}(0, 61, 0, 58, 1, 0)_{19716} \\
\ell_{35} &= \begin{bmatrix} 1 & \epsilon^{56} & \epsilon^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9491240} = \begin{bmatrix} 1 & 40 & 35 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9491240} = \mathbf{Pl}(0, 35, 0, 40, 1, 0)_{17404} \\
\ell_{36} &= \begin{bmatrix} 1 & \epsilon^{35} & \epsilon^{49} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8068178} = \begin{bmatrix} 1 & 18 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8068178} = \mathbf{Pl}(0, 30, 0, 18, 1, 0)_{14605} \\
\ell_{37} &= \begin{bmatrix} 1 & \epsilon^{30} & \epsilon^{24} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12212534} = \begin{bmatrix} 1 & 54 & 45 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12212534} = \mathbf{Pl}(0, 45, 0, 54, 1, 0)_{19192} \\
\ell_{38} &= \begin{bmatrix} 1 & \epsilon^{51} & \epsilon^{45} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9961433} = \begin{bmatrix} 1 & 25 & 37 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9961433} = \mathbf{Pl}(0, 37, 0, 25, 1, 0)_{15501} \\
\ell_{39} &= \begin{bmatrix} 1 & \epsilon^9 & \epsilon^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2330159} = \begin{bmatrix} 1 & 47 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2330159} = \mathbf{Pl}(0, 8, 0, 47, 1, 0)_{18266} \\
\ell_{40} &= \begin{bmatrix} 1 & \epsilon^{35} & \epsilon^{28} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16323602} = \begin{bmatrix} 1 & 18 & 61 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16323602} = \mathbf{Pl}(0, 61, 0, 18, 1, 0)_{14636} \\
\ell_{41} &= \begin{bmatrix} 1 & \epsilon^{14} & \epsilon^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9566138} = \begin{bmatrix} 1 & 58 & 35 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9566138} = \mathbf{Pl}(0, 35, 0, 58, 1, 0)_{19690} \\
\ell_{42} &= \begin{bmatrix} 1 & \epsilon^{56} & \epsilon^{49} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8159720} = \begin{bmatrix} 1 & 40 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8159720} = \mathbf{Pl}(0, 30, 0, 40, 1, 0)_{17399} \\
\ell_{43} &= \begin{bmatrix} 1 & \epsilon^{45} & \epsilon^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12674405} = \begin{bmatrix} 1 & 37 & 47 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12674405} = \mathbf{Pl}(0, 47, 0, 37, 1, 0)_{17035}
\end{aligned}$$

$$\begin{aligned}
\ell_{44} &= \begin{bmatrix} 1 & \epsilon^3 & \epsilon^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14417864} = \begin{bmatrix} 1 & 8 & 54 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14417864} = \mathbf{Pl}(0, 54, 0, 8, 1, 0)_{13359} \\
\ell_{45} &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^{51} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6849005} = \begin{bmatrix} 1 & 45 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6849005} = \mathbf{Pl}(0, 25, 0, 45, 1, 0)_{18029} \\
\ell_{46} &= \begin{bmatrix} 1 & \epsilon^{57} & \epsilon^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16718897} = \begin{bmatrix} 1 & 49 & 62 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16718897} = \mathbf{Pl}(0, 62, 0, 49, 1, 0)_{18574} \\
\ell_{47} &= \begin{bmatrix} 1 & \epsilon^{36} & \epsilon^{54} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2816996} = \begin{bmatrix} 1 & 36 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2816996} = \mathbf{Pl}(0, 10, 0, 36, 1, 0)_{16871} \\
\ell_{48} &= \begin{bmatrix} 1 & \epsilon^{15} & \epsilon^{33} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13939349} = \begin{bmatrix} 1 & 21 & 52 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13939349} = \mathbf{Pl}(0, 52, 0, 21, 1, 0)_{15008} \\
\ell_{49} &= \begin{bmatrix} 1 & \epsilon^7 & \epsilon^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15595427} = \begin{bmatrix} 1 & 35 & 58 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15595427} = \mathbf{Pl}(0, 58, 0, 35, 1, 0)_{16792} \\
\ell_{50} &= \begin{bmatrix} 1 & \epsilon^{49} & \epsilon^{56} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10781150} = \begin{bmatrix} 1 & 30 & 40 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10781150} = \mathbf{Pl}(0, 40, 0, 30, 1, 0)_{16139} \\
\ell_{51} &= \begin{bmatrix} 1 & \epsilon^{28} & \epsilon^{35} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5051453} = \begin{bmatrix} 1 & 61 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5051453} = \mathbf{Pl}(0, 18, 0, 61, 1, 0)_{20054} \\
\ell_{52} &= \begin{bmatrix} 1 & \epsilon^{36} & \epsilon^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16664804} = \begin{bmatrix} 1 & 36 & 62 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16664804} = \mathbf{Pl}(0, 62, 0, 36, 1, 0)_{16923} \\
\ell_{53} &= \begin{bmatrix} 1 & \epsilon^{15} & \epsilon^{54} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2754581} = \begin{bmatrix} 1 & 21 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2754581} = \mathbf{Pl}(0, 10, 0, 21, 1, 0)_{14966} \\
\ell_{54} &= \begin{bmatrix} 1 & \epsilon^{57} & \epsilon^{33} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14055857} = \begin{bmatrix} 1 & 49 & 52 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14055857} = \mathbf{Pl}(0, 52, 0, 49, 1, 0)_{18564} \\
\ell_{55} &= \begin{bmatrix} 1 & \epsilon^{51} & \epsilon^{24} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12091865} = \begin{bmatrix} 1 & 25 & 45 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12091865} = \mathbf{Pl}(0, 45, 0, 25, 1, 0)_{15509} \\
\ell_{56} &= \begin{bmatrix} 1 & \epsilon^9 & \epsilon^{45} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10052975} = \begin{bmatrix} 1 & 47 & 37 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10052975} = \mathbf{Pl}(0, 37, 0, 47, 1, 0)_{18295} \\
\ell_{57} &= \begin{bmatrix} 1 & \epsilon^{30} & \epsilon^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2359286} = \begin{bmatrix} 1 & 54 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2359286} = \mathbf{Pl}(0, 8, 0, 54, 1, 0)_{19155} \\
\ell_{58} &= \begin{bmatrix} 1 & \epsilon^6 & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3337121} = \begin{bmatrix} 1 & 33 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3337121} = \mathbf{Pl}(0, 12, 0, 33, 1, 0)_{16492} \\
\ell_{59} &= \begin{bmatrix} 1 & \epsilon^{27} & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3124910} = \begin{bmatrix} 1 & 46 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3124910} = \mathbf{Pl}(0, 11, 0, 46, 1, 0)_{18142} \\
\ell_{60} &= \begin{bmatrix} 1 & \epsilon^{48} & \epsilon^{39} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1930703} = \begin{bmatrix} 1 & 15 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1930703} = \mathbf{Pl}(0, 7, 0, 15, 1, 0)_{14201} \\
\ell_{61} &= \begin{bmatrix} 1 & \epsilon^3 & \epsilon^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12553736} = \begin{bmatrix} 1 & 8 & 47 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12553736} = \mathbf{Pl}(0, 47, 0, 8, 1, 0)_{13352} \\
\ell_{62} &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14571821} = \begin{bmatrix} 1 & 45 & 54 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14571821} = \mathbf{Pl}(0, 54, 0, 45, 1, 0)_{18058} \\
\ell_{63} &= \begin{bmatrix} 1 & \epsilon^{45} & \epsilon^{51} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6815717} = \begin{bmatrix} 1 & 37 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6815717} = \mathbf{Pl}(0, 25, 0, 37, 1, 0)_{17013} \\
\ell_{64} &= \begin{bmatrix} 1 & \epsilon^{18} & \epsilon^{48} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4044491} = \begin{bmatrix} 1 & 11 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4044491} = \mathbf{Pl}(0, 15, 0, 11, 1, 0)_{13701}
\end{aligned}$$

$$\begin{aligned}
\ell_{65} &= \begin{bmatrix} 1 & \epsilon^{60} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12304076} = \begin{bmatrix} 1 & 12 & 46 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12304076} = \mathbf{Pl}(0, 46, 0, 12, 1, 0)_{13859} \\
\ell_{66} &= \begin{bmatrix} 1 & \epsilon^{39} & \epsilon^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8821319} = \begin{bmatrix} 1 & 7 & 33 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8821319} = \mathbf{Pl}(0, 33, 0, 7, 1, 0)_{13211} \\
\ell_{67} &= \begin{bmatrix} 1 & \epsilon^{27} & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3391214} = \begin{bmatrix} 1 & 46 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3391214} = \mathbf{Pl}(0, 12, 0, 46, 1, 0)_{18143} \\
\ell_{68} &= \begin{bmatrix} 1 & \epsilon^{48} & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2995919} = \begin{bmatrix} 1 & 15 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2995919} = \mathbf{Pl}(0, 11, 0, 15, 1, 0)_{14205} \\
\ell_{69} &= \begin{bmatrix} 1 & \epsilon^6 & \epsilon^{39} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2005601} = \begin{bmatrix} 1 & 33 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2005601} = \mathbf{Pl}(0, 7, 0, 33, 1, 0)_{16487} \\
\ell_{70} &= \begin{bmatrix} 0 & 1 & \epsilon^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047225} = \begin{bmatrix} 0 & 1 & 57 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047225} = \mathbf{Pl}(0, 57, 0, 1, 0, 0)_{249} \\
\ell_{71} &= \begin{bmatrix} 0 & 1 & \epsilon^{42} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047160} = \begin{bmatrix} 0 & 1 & 56 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047160} = \mathbf{Pl}(0, 56, 0, 1, 0, 0)_{248} \\
\ell_{72} &= \begin{bmatrix} 1 & \epsilon^{28} & \epsilon^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15703613} = \begin{bmatrix} 1 & 61 & 58 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15703613} = \mathbf{Pl}(0, 58, 0, 61, 1, 0)_{20094} \\
\ell_{73} &= \begin{bmatrix} 1 & \epsilon^7 & \epsilon^{56} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10801955} = \begin{bmatrix} 1 & 35 & 40 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10801955} = \mathbf{Pl}(0, 40, 0, 35, 1, 0)_{16774} \\
\ell_{74} &= \begin{bmatrix} 1 & \epsilon^{49} & \epsilon^{35} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4922462} = \begin{bmatrix} 1 & 30 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4922462} = \mathbf{Pl}(0, 18, 0, 30, 1, 0)_{16117} \\
\ell_{75} &= \begin{bmatrix} 1 & \epsilon^{56} & \epsilon^{28} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16415144} = \begin{bmatrix} 1 & 40 & 61 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16415144} = \mathbf{Pl}(0, 61, 0, 40, 1, 0)_{17430} \\
\ell_{76} &= \begin{bmatrix} 1 & \epsilon^{35} & \epsilon^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9399698} = \begin{bmatrix} 1 & 18 & 35 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9399698} = \mathbf{Pl}(0, 35, 0, 18, 1, 0)_{14610} \\
\ell_{77} &= \begin{bmatrix} 1 & \epsilon^{14} & \epsilon^{49} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8234618} = \begin{bmatrix} 1 & 58 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8234618} = \mathbf{Pl}(0, 30, 0, 58, 1, 0)_{19685} \\
\ell_{78} &= \begin{bmatrix} 1 & \epsilon^{60} & \epsilon^{48} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4048652} = \begin{bmatrix} 1 & 12 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4048652} = \mathbf{Pl}(0, 15, 0, 12, 1, 0)_{13828} \\
\ell_{79} &= \begin{bmatrix} 1 & \epsilon^{39} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12283271} = \begin{bmatrix} 1 & 7 & 46 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12283271} = \mathbf{Pl}(0, 46, 0, 7, 1, 0)_{13224} \\
\ell_{80} &= \begin{bmatrix} 1 & \epsilon^{18} & \epsilon^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8837963} = \begin{bmatrix} 1 & 11 & 33 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8837963} = \mathbf{Pl}(0, 33, 0, 11, 1, 0)_{13719}
\end{aligned}$$

Rank of lines: ( 8321, 241337, 237176, 270464, 15183488, 14917184, 17043585, 5638154, 13269428, 9849086, 16602389, 2871089, 14001764, 4027847, 12299915, 8842124, 5812916, 13311038, 9632714, 5854526, 13094666, 9807476, 12183407, 10082102, 2238617, 15574622, 10910141, 4943267, 12707693, 14538533, 6695048, 3262223, 3070817, 2059694, 16490042, 9491240, 8068178, 12212534, 9961433, 2330159, 16323602, 9566138, 8159720, 12674405, 14417864, 6849005, 16718897, 2816996, 13939349, 15595427, ...4048652, 12283271, 8837963 )

Rank of points on Klein quadric: ( 12353, 19465, 19338, 4289, 4345, 4344, 193, 13580, 18942, 20199, 15018, 18522, 16913, 13193, 13732, 13846, 18914, 20212, 13595, 20184, 13608, 18929, 18303, 19184, 15472, 16157, 20076, 16752, 18051, 17042, 13330, 14206, 16491, 18138, 19716, 17404, 14605, 19192, 15501, 18266, 14636, 19690, 17399, 17035, 13359, 18029, 18574, 16871, 15008, 16792, ...13828, 13224, 13719 )

**Eckardt Points**

The surface has 0 Eckardt points:

**Double Points**

The surface has 0 Double points:

The double points on the surface are:

**Single Points**

The surface has 5184 single points:

Too many to print.

**Points on surface but on no line**

The surface has 0 points not on any line:

The points on the surface but not on lines are:

## Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47		
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
3	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
4	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
5	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
6	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
7	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
8	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
9	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
10	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
11	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
12	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
13	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
14	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
15	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
16	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
17	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
18	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
19	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
20	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
21	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
22	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
23	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
24	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
25	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
26	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
27	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
28	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
29	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
30	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
31	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
32	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
33	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
34	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
35	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
36	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
37	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
38	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1																														

Line 0 intersects

Line 1 intersects

Line 2 intersects

Line 3 intersects

Line 4 intersects

Line 5 intersects

Line 6 intersects

Line 7 intersects

Line 8 intersects

Line 9 intersects

Line 10 intersects

Line 11 intersects

8



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Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$	$\ell_{45}$	$\ell_{46}$	$\ell_{47}$	$\ell_{48}$	$\ell_{49}$	$\ell_{50}$	$\ell_{51}$	$\ell_{52}$	$\ell_{53}$	$\ell_{54}$	$\ell_{55}$	$\ell_{56}$	$\ell_{57}$	$\ell_{58}$	$\ell_{59}$	$\ell_{60}$	$\ell_{61}$	$\ell_{62}$	$\ell_{63}$	$\ell_{64}$	$\ell_{65}$	$\ell_{66}$	$\ell_{67}$	$\ell_{68}$	$\ell_{69}$	$\ell_{70}$	$\ell_{71}$	$\ell_{72}$	$\ell_{73}$	$\ell_{74}$	$\ell_{75}$	$\ell_{76}$	$\ell_{77}$	$\ell_{78}$	$\ell_{79}$	$\ell_{80}$	$\ell_{81}$	$\ell_{82}$	$\ell_{83}$	$\ell_{84}$	$\ell_{85}$	$\ell_{86}$	$\ell_{87}$	$\ell_{88}$	$\ell_{89}$	$\ell_{90}$	$\ell_{91}$	$\ell_{92}$	$\ell_{93}$	$\ell_{94}$	$\ell_{95}$	$\ell_{96}$	$\ell_{97}$	$\ell_{98}$	$\ell_{99}$	$\ell_{100}$	$\ell_{101}$	$\ell_{102}$	$\ell_{103}$	$\ell_{104}$	$\ell_{105}$	$\ell_{106}$	$\ell_{107}$	$\ell_{108}$	$\ell_{109}$	$\ell_{110}$	$\ell_{111}$	$\ell_{112}$	$\ell_{113}$	$\ell_{114}$	$\ell_{115}$	$\ell_{116}$	$\ell_{117}$	$\ell_{118}$	$\ell_{119}$	$\ell_{120}$	$\ell_{121}$	$\ell_{122}$	$\ell_{123}$	$\ell_{124}$	$\ell_{125}$	$\ell_{126}$	$\ell_{127}$	$\ell_{128}$	$\ell_{129}$	$\ell_{130}$	$\ell_{131}$	$\ell_{132}$	$\ell_{133}$	$\ell_{134}$	$\ell_{135}$	$\ell_{136}$	$\ell_{137}$	$\ell_{138}$	$\ell_{139}$	$\ell_{140}$	$\ell_{141}$	$\ell_{142}$	$\ell_{143}$	$\ell_{144}$	$\ell_{145}$	$\ell_{146}$	$\ell_{147}$	$\ell_{148}$	$\ell_{149}$	$\ell_{150}$	$\ell_{151}$	$\ell_{152}$	$\ell_{153}$	$\ell_{154}$	$\ell_{155}$	$\ell_{156}$	$\ell_{157}$	$\ell_{158}$	$\ell_{159}$	$\ell_{160}$	$\ell_{161}$	$\ell_{162}$	$\ell_{163}$	$\ell_{164}$	$\ell_{165}$	$\ell_{166}$	$\ell_{167}$	$\ell_{168}$	$\ell_{169}$	$\ell_{170}$	$\ell_{171}$	$\ell_{172}$	$\ell_{173}$	$\ell_{174}$	$\ell_{175}$	$\ell_{176}$	$\ell_{177}$	$\ell_{178}$	$\ell_{179}$	$\ell_{180}$	$\ell_{181}$	$\ell_{182}$	$\ell_{183}$	$\ell_{184}$	$\ell_{185}$	$\ell_{186}$	$\ell_{187}$	$\ell_{188}$	$\ell_{189}$	$\ell_{190}$	$\ell_{191}$	$\ell_{192}$	$\ell_{193}$	$\ell_{194}$	$\ell_{195}$	$\ell_{196}$	$\ell_{197}$	$\ell_{198}$	$\ell_{199}$	$\ell_{200}$	$\ell_{201}$	$\ell_{202}$	$\ell_{203}$	$\ell_{204}$	$\ell_{205}$	$\ell_{206}$	$\ell_{207}$	$\ell_{208}$	$\ell_{209}$	$\ell_{210}$	$\ell_{211}$	$\ell_{212}$	$\ell_{213}$	$\ell_{214}$	$\ell_{215}$	$\ell_{216}$	$\ell_{217}$	$\ell_{218}$	$\ell_{219}$	$\ell_{220}$	$\ell_{221}$	$\ell_{222}$	$\ell_{223}$	$\ell_{224}$	$\ell_{225}$	$\ell_{226}$	$\ell_{227}$	$\ell_{228}$	$\ell_{229}$	$\ell_{230}$	$\ell_{231}$	$\ell_{232}$	$\ell_{233}$	$\ell_{234}$	$\ell_{235}$	$\ell_{236}$	$\ell_{237}$	$\ell_{238}$	$\ell_{239}$	$\ell_{240}$	$\ell_{241}$	$\ell_{242}$	$\ell_{243}$	$\ell_{244}$	$\ell_{245}$	$\ell_{246}$	$\ell_{247}$	$\ell_{248}$	$\ell_{249}$	$\ell_{250}$	$\ell_{251}$	$\ell_{252}$	$\ell_{253}$	$\ell_{254}$	$\ell_{255}$	$\ell_{256}$	$\ell_{257}$	$\ell_{258}$	$\ell_{259}$	$\ell_{260}$	$\ell_{261}$	$\ell_{262}$	$\ell_{263}$	$\ell_{264}$	$\ell_{265}$	$\ell_{266}$	$\ell_{267}$	$\ell_{268}$	$\ell_{269}$	$\ell_{270}$	$\ell_{271}$	$\ell_{272}$	$\ell_{273}$	$\ell_{274}$	$\ell_{275}$	$\ell_{276}$	$\ell_{277}$	$\ell_{278}$	$\ell_{279}$	$\ell_{280}$	$\ell_{281}$	$\ell_{282}$	$\ell_{283}$	$\ell_{284}$	$\ell_{285}$	$\ell_{286}$	$\ell_{287}$	$\ell_{288}$	$\ell_{289}$	$\ell_{290}$	$\ell_{291}$	$\ell_{292}$	$\ell_{293}$	$\ell_{294}$	$\ell_{295}$	$\ell_{296}$	$\ell_{297}$	$\ell_{298}$	$\ell_{299}$	$\$
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Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$	$\ell_{45}$	$\ell_{46}$	$\ell_{47}$	$\ell_{48}$	$\ell_{49}$	$\ell_{50}$	$\ell_{51}$	$\ell_{52}$	$\ell_{53}$	$\ell_{54}$	$\ell_{55}$	$\ell_{56}$	$\ell_{57}$	$\ell_{58}$	$\ell_{59}$	$\ell_{60}$	$\ell_{61}$	$\ell_{62}$	$\ell_{63}$	$\ell_{64}$	$\ell_{65}$	$\ell_{66}$	$\ell_{67}$	$\ell_{68}$	$\ell_{69}$	$\ell_{70}$	$\ell_{71}$	$\ell_{72}$	$\ell_{73}$	$\ell_{74}$	$\ell_{75}$	$\ell_{76}$	$\ell_{77}$	$\ell_{78}$	$\ell_{79}$	$\ell_{80}$	$\ell_{81}$	$\ell_{82}$	$\ell_{83}$	$\ell_{84}$	$\ell_{85}$	$\ell_{86}$	$\ell_{87}$	$\ell_{88}$	$\ell_{89}$	$\ell_{90}$	$\ell_{91}$	$\ell_{92}$	$\ell_{93}$	$\ell_{94}$	$\ell_{95}$	$\ell_{96}$	$\ell_{97}$	$\ell_{98}$	$\ell_{99}$	$\ell_{100}$	$\ell_{101}$	$\ell_{102}$	$\ell_{103}$	$\ell_{104}$	$\ell_{105}$	$\ell_{106}$	$\ell_{107}$	$\ell_{108}$	$\ell_{109}$	$\ell_{110}$	$\ell_{111}$	$\ell_{112}$	$\ell_{113}$	$\ell_{114}$	$\ell_{115}$	$\ell_{116}$	$\ell_{117}$	$\ell_{118}$	$\ell_{119}$	$\ell_{120}$	$\ell_{121}$	$\ell_{122}$	$\ell_{123}$	$\ell_{124}$	$\ell_{125}$	$\ell_{126}$	$\ell_{127}$	$\ell_{128}$	$\ell_{129}$	$\ell_{130}$	$\ell_{131}$	$\ell_{132}$	$\ell_{133}$	$\ell_{134}$	$\ell_{135}$	$\ell_{136}$	$\ell_{137}$	$\ell_{138}$	$\ell_{139}$	$\ell_{140}$	$\ell_{141}$	$\ell_{142}$	$\ell_{143}$	$\ell_{144}$	$\ell_{145}$	$\ell_{146}$	$\ell_{147}$	$\ell_{148}$	$\ell_{149}$	$\ell_{150}$	$\ell_{151}$	$\ell_{152}$	$\ell_{153}$	$\ell_{154}$	$\ell_{155}$	$\ell_{156}$	$\ell_{157}$	$\ell_{158}$	$\ell_{159}$	$\ell_{160}$	$\ell_{161}$	$\ell_{162}$	$\ell_{163}$	$\ell_{164}$	$\ell_{165}$	$\ell_{166}$	$\ell_{167}$	$\ell_{168}$	$\ell_{169}$	$\ell_{170}$	$\ell_{171}$	$\ell_{172}$	$\ell_{173}$	$\ell_{174}$	$\ell_{175}$	$\ell_{176}$	$\ell_{177}$	$\ell_{178}$	$\ell_{179}$	$\ell_{180}$	$\ell_{181}$	$\ell_{182}$	$\ell_{183}$	$\ell_{184}$	$\ell_{185}$	$\ell_{186}$	$\ell_{187}$	$\ell_{188}$	$\ell_{189}$	$\ell_{190}$	$\ell_{191}$	$\ell_{192}$	$\ell_{193}$	$\ell_{194}$	$\ell_{195}$	$\ell_{196}$	$\ell_{197}$	$\ell_{198}$	$\ell_{199}$	$\ell_{200}$	$\ell_{201}$	$\ell_{202}$	$\ell_{203}$	$\ell_{204}$	$\ell_{205}$	$\ell_{206}$	$\ell_{207}$	$\ell_{208}$	$\ell_{209}$	$\ell_{210}$	$\ell_{211}$	$\ell_{212}$	$\ell_{213}$	$\ell_{214}$	$\ell_{215}$	$\ell_{216}$	$\ell_{217}$	$\ell_{218}$	$\ell_{219}$	$\ell_{220}$	$\ell_{221}$	$\ell_{222}$	$\ell_{223}$	$\ell_{224}$	$\ell_{225}$	$\ell_{226}$	$\ell_{227}$	$\ell_{228}$	$\ell_{229}$	$\ell_{230}$	$\ell_{231}$	$\ell_{232}$	$\ell_{233}$	$\ell_{234}$	$\ell_{235}$	$\ell_{236}$	$\ell_{237}$	$\ell_{238}$	$\ell_{239}$	$\ell_{240}$	$\ell_{241}$	$\ell_{242}$	$\ell_{243}$	$\ell_{244}$	$\ell_{245}$	$\ell_{246}$	$\ell_{247}$	$\ell_{248}$	$\ell_{249}$	$\ell_{250}$	$\ell_{251}$	$\ell_{252}$	$\ell_{253}$	$\ell_{254}$	$\ell_{255}$	$\ell_{256}$	$\ell_{257}$	$\ell_{258}$	$\ell_{259}$	$\ell_{260}$	$\ell_{261}$	$\ell_{262}$	$\ell_{263}$	$\ell_{264}$	$\ell_{265}$	$\ell_{266}$	$\ell_{267}$	$\ell_{268}$	$\ell_{269}$	$\ell_{270}$	$\ell_{271}$	$\ell_{272}$	$\ell_{273}$	$\ell_{274}$	$\ell_{275}$	$\ell_{276}$	$\ell_{277}$	$\ell_{278}$	$\ell_{279}$	$\ell_{280}$	$\ell_{281}$	$\ell_{282}$	$\ell_{283}$	$\ell_{284}$	$\ell_{285}$	$\ell_{286}$	$\ell_{287}$	$\ell_{288}$	$\ell_{289}$	$\ell_{290}$	$\ell_{291}$	$\ell_{292}$	$\ell_{293}$	$\ell_{294}$	$\ell_{295}$	$\ell_{296}$	$\ell_{297}$	$\ell_{298}$	$\ell$
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Line 77 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 78 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 79 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

Line 80 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

The surface has 5185 points:

Too many to print.