# Rank-65562 over GF(16)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_0^2 X_1 + X_0 X_1 X_2 = 0$$

( 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0 ) The point rank of the equation over  $\mathrm{GF}(16)$  is 286396966

# General information

Number of lines	16
Number of points	257
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	256
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$17^{16}$
Type of lines on points	$16, 1^{256}$

# Singular Points

The surface has 1 singular points:

$$0: P_3 = \mathbf{P}(0,0,0,1) = \mathbf{P}(0,0,0,1)$$

# The 16 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4640} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4640} = \mathbf{Pl}(0, 1, 0, 0, 1, 0)_{305}$$

$$\begin{split} \ell_1 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{48320} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{48320} = \mathbf{Pl}(0,11,0,0,1,0)_{315} \\ \ell_2 &= \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{43952} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{43952} = \mathbf{Pl}(0,10,0,0,1,0)_{314} \\ \ell_3 &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69921} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69921} = \mathbf{Pl}(0,1,0,1,0,0)_{49} \\ \ell_4 &= \begin{bmatrix} 1 & \delta^5 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{51323} = \begin{bmatrix} 1 & 11 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{51323} = \mathbf{Pl}(0,11,0,11,1,0)_{1121} \\ \ell_5 &= \begin{bmatrix} 1 & \delta^{10} & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{46682} = \begin{bmatrix} 1 & 10 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{46682} = \mathbf{Pl}(0,10,0,10,1,0)_{1084} \\ \ell_6 &= \begin{bmatrix} 1 & \delta^{10} & \delta^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{24842} = \begin{bmatrix} 1 & 10 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{24842} = \mathbf{Pl}(0,5,0,10,1,0)_{1084} \\ \ell_7 &= \begin{bmatrix} 1 & \delta^5 & \delta^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{38219} = \begin{bmatrix} 1 & 11 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{38219} = \mathbf{Pl}(0,8,0,11,1,0)_{1118} \\ \ell_8 &= \begin{bmatrix} 1 & \delta^{10} & \delta^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{68522} = \begin{bmatrix} 1 & 10 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30091} = \mathbf{Pl}(0,15,0,10,1,0)_{1094} \\ \ell_9 &= \begin{bmatrix} 0 & 1 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30302} = \begin{bmatrix} 1 & 14 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30302} = \mathbf{Pl}(0,6,0,14,1,0)_{1209} \\ \ell_{11} &= \begin{bmatrix} 1 & \delta^8 & \delta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{31940} = \begin{bmatrix} 1 & 4 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{31940} = \mathbf{Pl}(0,7,0,4,1,0)_{900} \\ \ell_{12} &= \begin{bmatrix} 0 & 1 & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{55145} = \begin{bmatrix} 1 & 9 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{55145} = \mathbf{Pl}(0,12,0,9,1,0)_{1060} \\ \ell_{14} &= \begin{bmatrix} 1 & \delta & \delta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16370} = \begin{bmatrix} 1 & 11 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16370} = \mathbf{Pl}(0,3,0,11,1,0)_{1113} \\ \ell_{15} &= \begin{bmatrix} 1 & \delta^5 & \delta^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16370} = \begin{bmatrix} 1 & 11 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16370} = \mathbf{Pl}(0,3,0,11,1,0)_{1113} \end{aligned}$$

Rank of lines: ( 4640, 48320, 43952, 69921, 51323, 46682, 24842, 38219, 68522, 70091, 30302, 31940, 70074, 55145, 57602, 16379 )

Rank of points on Klein quadric: ( 305, 315, 314, 49, 1121, 1089, 1084, 1118, 1094, 59, 1209, 900, 58, 1060, 844, 1113 )

### **Eckardt Points**

The surface has 0 Eckardt points:

### **Double Points**

The surface has 0 Double points:

The double points on the surface are:

### Single Points

The surface has 256 single points: The single points on the surface are:

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0: P_{20} = (1,0,1,0) lies on line \ell_0
                                                                       48: P_{1044} = (3,0,3,1) lies on line \ell_0
1: P_{29} = (10, 0, 1, 0) lies on line \ell_1
                                                                       49: P_{1045} = (4,0,3,1) lies on line \ell_2
2: P_{30} = (11, 0, 1, 0) lies on line \ell_2
                                                                       50: P_{1048} = (7,0,3,1) lies on line \ell_1
3: P_{35} = (0, 1, 1, 0) lies on line \ell_3
                                                                       51: P_{1088} = (15, 2, 3, 1) lies on line \ell_8
4: P_{45} = (10, 1, 1, 0) lies on line \ell_4
                                                                       52: P_{1089} = (0, 3, 3, 1) lies on line \ell_3
                                                                       53: P_{1093} = (4, 3, 3, 1) lies on line \ell_5
5: P_{46} = (11, 1, 1, 0) lies on line \ell_5
6: P_{66} = (15, 2, 1, 0) lies on line \ell_6
                                                                       54: P_{1096} = (7,3,3,1) lies on line \ell_4
7: P_{86} = (3, 4, 1, 0) lies on line \ell_7
                                                                       55: P_{1105} = (0, 4, 3, 1) lies on line \ell_{12}
8: P_{168} = (5, 9, 1, 0) lies on line \ell_8
                                                                       56: P_{1107} = (2, 4, 3, 1) lies on line \ell_{14}
9: P_{179} = (0, 10, 1, 0) lies on line \ell_9
                                                                       57: P_{1111} = (6, 4, 3, 1) lies on line \ell_{13}
10: P_{183} = (4, 10, 1, 0) lies on line \ell_{10}
                                                                       58: P_{1145} = (8, 6, 3, 1) lies on line \ell_6
11: P_{193} = (14, 10, 1, 0) lies on line \ell_{11}
                                                                       59: P_{1153} = (0,7,3,1) lies on line \ell_9
12: P_{195} = (0, 11, 1, 0) lies on line \ell_{12}
                                                                       60: P_{1164} = (11, 7, 3, 1) lies on line \ell_{11}
13: P_{197} = (2, 11, 1, 0) lies on line \ell_{13}
                                                                       61: P_{1165} = (12, 7, 3, 1) lies on line \ell_{10}
                                                                       62: P_{1218} = (1, 11, 3, 1) lies on line \ell_{15}
14: P_{204} = (9, 11, 1, 0) lies on line \ell_{14}
15: P_{251} = (8, 14, 1, 0) lies on line \ell_{15}
                                                                       63: P_{1238} = (5, 12, 3, 1) lies on line \ell_7
16: P_{531} = (1,0,1,1) lies on line \ell_0
                                                                       64: P_{1300} = (3, 0, 4, 1) lies on line \ell_1
17: P_{540} = (10, 0, 1, 1) lies on line \ell_1
                                                                       65: P_{1301} = (4, 0, 4, 1) lies on line \ell_0
18: P_{541} = (11, 0, 1, 1) lies on line \ell_2
                                                                       66: P_{1304} = (7, 0, 4, 1) lies on line \ell_2
                                                                       67: P_{1345} = (0, 3, 4, 1) lies on line \ell_9
19: P_{546} = (0, 1, 1, 1) lies on line \ell_3
20: P_{555} = (10, 1, 1, 1) lies on line \ell_4
                                                                       68: P_{1354} = (9, 3, 4, 1) lies on line \ell_{10}
21: P_{556} = (11, 1, 1, 1) lies on line \ell_5
                                                                       69: P_{1355} = (10, 3, 4, 1) lies on line \ell_{11}
22: P_{576} = (15, 2, 1, 1) lies on line \ell_6
                                                                       70: P_{1361} = (0, 4, 4, 1) lies on line \ell_3
23: P_{596} = (3, 4, 1, 1) lies on line \ell_7
                                                                       71: P_{1364} = (3, 4, 4, 1) lies on line \ell_4
24: P_{678} = (5, 9, 1, 1) lies on line \ell_8
                                                                       72: P_{1368} = (7, 4, 4, 1) lies on line \ell_5
25: P_{689} = (0, 10, 1, 1) lies on line \ell_9
                                                                       73: P_{1409} = (0, 7, 4, 1) lies on line \ell_{12}
26: P_{693} = (4, 10, 1, 1) lies on line \ell_{10}
                                                                       74: P_{1417} = (8, 7, 4, 1) lies on line \ell_{13}
27: P_{703} = (14, 10, 1, 1) lies on line \ell_{11}
                                                                       75: P_{1424} = (15, 7, 4, 1) lies on line \ell_{14}
28 : P_{705} = (0, 11, 1, 1) lies on line \ell_{12}
                                                                       76: P_{1439} = (14, 8, 4, 1) lies on line \ell_6
29: P_{707} = (2, 11, 1, 1) lies on line \ell_{13}
                                                                       77: P_{1453} = (12, 9, 4, 1) lies on line \ell_7
30: P_{714} = (9, 11, 1, 1) lies on line \ell_{14}
                                                                       78: P_{1468} = (11, 10, 4, 1) lies on line \ell_{15}
31: P_{761} = (8, 14, 1, 1) lies on line \ell_{15}
                                                                       79: P_{1550} = (13, 15, 4, 1) lies on line \ell_8
32: P_{787} = (2,0,2,1) lies on line \ell_0
                                                                       80: P_{1558} = (5, 0, 5, 1) lies on line \ell_0
33: P_{798} = (13, 0, 2, 1) lies on line \ell_1
                                                                       81: P_{1562} = (9, 0, 5, 1) lies on line \ell_1
34: P_{800} = (15, 0, 2, 1) lies on line \ell_2
                                                                       82: P_{1565} = (12, 0, 5, 1) lies on line \ell_2
35: P_{817} = (0, 2, 2, 1) lies on line \ell_3
                                                                       83: P_{1620} = (3, 4, 5, 1) lies on line \ell_{15}
                                                                       84 : P_{1633} = (0, 5, 5, 1) lies on line \ell_3
36: P_{830} = (13, 2, 2, 1) lies on line \ell_4
37: P_{832} = (15, 2, 2, 1) lies on line \ell_5
                                                                       85: P_{1642} = (9, 5, 5, 1) lies on line \ell_4
38: P_{856} = (7, 4, 2, 1) lies on line \ell_6
                                                                       86: P_{1645} = (12, 5, 5, 1) lies on line \ell_5
39: P_{874} = (9, 5, 2, 1) lies on line \ell_{15}
                                                                       87: P_{1657} = (8, 6, 5, 1) lies on line \ell_8
40 : P_{919} = (6, 8, 2, 1) lies on line \ell_7
                                                                       88 : P_{1697} = (0, 9, 5, 1) lies on line \ell_9
41: P_{971} = (10, 11, 2, 1) lies on line \ell_8
                                                                       89: P_{1701} = (4, 9, 5, 1) lies on line \ell_{11}
42: P_{993} = (0, 13, 2, 1) lies on line \ell_9
                                                                       90: P_{1710} = (13, 9, 5, 1) lies on line \ell_{10}
43: P_{998} = (5, 13, 2, 1) lies on line \ell_{11}
                                                                       91: P_{1714} = (1, 10, 5, 1) lies on line \ell_6
44: P_{1001} = (8, 13, 2, 1) lies on line \ell_{10}
                                                                       92: P_{1745} = (0, 12, 5, 1) lies on line \ell_{12}
45: P_{1025} = (0, 15, 2, 1) lies on line \ell_{12}
                                                                       93: P_{1751} = (6, 12, 5, 1) lies on line \ell_{14}
46: P_{1029} = (4, 15, 2, 1) lies on line \ell_{13}
                                                                       94: P_{1755} = (10, 12, 5, 1) lies on line \ell_{13}
47: P_{1036} = (11, 15, 2, 1) lies on line \ell_{14}
                                                                       95: P_{1776} = (15, 13, 5, 1) lies on line \ell_7
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96: P_{1815} = (6,0,6,1) lies on line \ell_0
                                                                      150: P_{2671} = (14, 5, 9, 1) lies on line \ell_{14}
                                                                      151: P_{2721} = (0, 9, 9, 1) lies on line \ell_3
97: P_{1817} = (8,0,6,1) lies on line \ell_2
                                                                      152 : P_{2726} = (5, 9, 9, 1) lies on line \ell_5
98: P_{1823} = (14, 0, 6, 1) lies on line \ell_1
99: P_{1835} = (10, 1, 6, 1) lies on line \ell_7
                                                                      153: P_{2733} = (12, 9, 9, 1) lies on line \ell_4
100: P_{1880} = (7, 4, 6, 1) lies on line \ell_8
                                                                      154: P_{2763} = (10, 11, 9, 1) lies on line \ell_6
101: P_{1905} = (0, 6, 6, 1) lies on line \ell_3
                                                                      155: P_{2769} = (0, 12, 9, 1) lies on line \ell_9
102: P_{1913} = (8, 6, 6, 1) lies on line \ell_5
                                                                      156: P_{2772} = (3, 12, 9, 1) lies on line \ell_{11}
103: P_{1919} = (14, 6, 6, 1) lies on line \ell_4
                                                                      157: P_{2784} = (15, 12, 9, 1) lies on line \ell_{10}
104: P_{1937} = (0, 8, 6, 1) lies on line \ell_{12}
                                                                      158: P_{2807} = (6, 14, 9, 1) lies on line \ell_8
105: P_{1941} = (4, 8, 6, 1) lies on line \ell_{14}
                                                                      159: P_{2819} = (2, 15, 9, 1) lies on line \ell_7
106: P_{1949} = (12, 8, 6, 1) lies on line \ell_{13}
                                                                      160: P_{2834} = (1, 0, 10, 1) lies on line \ell_2
107: P_{2010} = (9, 12, 6, 1) lies on line \ell_6
                                                                      161: P_{2843} = (10, 0, 10, 1) lies on line \ell_0
108: P_{2033} = (0, 14, 6, 1) lies on line \ell_9
                                                                      162: P_{2844} = (11, 0, 10, 1) lies on line \ell_1
                                                                      163: P_{2849} = (0, 1, 10, 1) lies on line \ell_{12}
109: P_{2034} = (1, 14, 6, 1) lies on line \ell_{10}
110: P_{2048} = (15, 14, 6, 1) lies on line \ell_{11}
                                                                      164: P_{2861} = (12, 1, 10, 1) lies on line \ell_{14}
111: P_{2051} = (2, 15, 6, 1) lies on line \ell_{15}
                                                                      165: P_{2862} = (13, 1, 10, 1) lies on line \ell_{13}
112: P_{2068} = (3, 0, 7, 1) lies on line \ell_2
                                                                      166: P_{2888} = (7, 3, 10, 1) lies on line \ell_7
113: P_{2069} = (4, 0, 7, 1) lies on line \ell_1
                                                                      167: P_{2967} = (6, 8, 10, 1) lies on line \ell_{15}
114: P_{2072} = (7,0,7,1) lies on line \ell_0
                                                                      168: P_{2993} = (0, 10, 10, 1) lies on line \ell_3
115: P_{2091} = (10, 1, 7, 1) lies on line \ell_{15}
                                                                      169: P_{2994} = (1, 10, 10, 1) lies on line \ell_5
116: P_{2113} = (0, 3, 7, 1) lies on line \ell_{12}
                                                                      170: P_{3004} = (11, 10, 10, 1) lies on line \ell_4
                                                                      171: P_{3009} = (0, 11, 10, 1) lies on line \ell_9
117: P_{2126} = (13, 3, 7, 1) lies on line \ell_{14}
118: P_{2127} = (14, 3, 7, 1) lies on line \ell_{13}
                                                                      172: P_{3012} = (3, 11, 10, 1) lies on line \ell_{10}
                                                                      173: P_{3017} = (8, 11, 10, 1) lies on line \ell_{11}
119: P_{2129} = (0, 4, 7, 1) lies on line \ell_9
120: P_{2130} = (1, 4, 7, 1) lies on line \ell_{11}
                                                                      174: P_{3034} = (9, 12, 10, 1) lies on line \ell_8
121: P_{2134} = (5, 4, 7, 1) lies on line \ell_{10}
                                                                      175: P_{3043} = (2, 13, 10, 1) lies on line \ell_6
122: P_{2154} = (9, 5, 7, 1) lies on line \ell_7
                                                                      176: P_{3090} = (1, 0, 11, 1) lies on line \ell_1
123: P_{2177} = (0,7,7,1) lies on line \ell_3
                                                                      177: P_{3099} = (10, 0, 11, 1) lies on line \ell_2
124: P_{2180} = (3,7,7,1) lies on line \ell_5
                                                                      178: P_{3100} = (11, 0, 11, 1) lies on line \ell_0
125: P_{2181} = (4,7,7,1) lies on line \ell_4
                                                                      179: P_{3105} = (0, 1, 11, 1) lies on line \ell_9
126: P_{2275} = (2, 13, 7, 1) lies on line \ell_8
                                                                      180: P_{3111} = (6, 1, 11, 1) lies on line \ell_{11}
127: P_{2295} = (6, 14, 7, 1) lies on line \ell_6
                                                                      181: P_{3112} = (7, 1, 11, 1) lies on line \ell_{10}
128: P_{2327} = (6,0,8,1) lies on line \ell_1
                                                                      182: P_{3181} = (12, 5, 11, 1) lies on line \ell_8
129: P_{2329} = (8,0,8,1) lies on line \ell_0
                                                                      183: P_{3199} = (14, 6, 11, 1) lies on line \ell_{15}
130: P_{2335} = (14, 0, 8, 1) lies on line \ell_2
                                                                      184: P_{3205} = (4,7,11,1) lies on line \ell_7
131: P_{2417} = (0, 6, 8, 1) lies on line \ell_9
                                                                      185: P_{3249} = (0, 10, 11, 1) lies on line \ell_{12}
132: P_{2428} = (11, 6, 8, 1) lies on line \ell_{10}
                                                                      186: P_{3254} = (5, 10, 11, 1) lies on line \ell_{14}
133 : P_{2430} = (13, 6, 8, 1) lies on line \ell_{11}
                                                                      187: P_{3264} = (15, 10, 11, 1) lies on line \ell_{13}
134 : P_{2436} = (3, 7, 8, 1) lies on line \ell_8
                                                                      188: P_{3265} = (0, 11, 11, 1) lies on line \ell_3
135: P_{2449} = (0, 8, 8, 1) lies on line \ell_3
                                                                      189: P_{3266} = (1, 11, 11, 1) lies on line \ell_4
136: P_{2455} = (6, 8, 8, 1) lies on line \ell_4
                                                                      190: P_{3275} = (10, 11, 11, 1) lies on line \ell_5
137: P_{2463} = (14, 8, 8, 1) lies on line \ell_5
                                                                      191: P_{3342} = (13, 15, 11, 1) lies on line \ell_6
138: P_{2470} = (5, 9, 8, 1) lies on line \ell_6
                                                                      192: P_{3350} = (5, 0, 12, 1) lies on line \ell_1
139: P_{2498} = (1, 11, 8, 1) lies on line \ell_7
                                                                      193: P_{3354} = (9, 0, 12, 1) lies on line \ell_2
140: P_{2544} = (15, 13, 8, 1) lies on line \ell_{15}
                                                                      194: P_{3357} = (12, 0, 12, 1) lies on line \ell_0
141: P_{2545} = (0, 14, 8, 1) lies on line \ell_{12}
                                                                      195: P_{3372} = (11, 1, 12, 1) lies on line \ell_6
142: P_{2552} = (7, 14, 8, 1) lies on line \ell_{14}
                                                                      196: P_{3390} = (13, 2, 12, 1) lies on line \ell_7
143: P_{2554} = (9, 14, 8, 1) lies on line \ell_{13}
                                                                      197: P_{3425} = (0, 5, 12, 1) lies on line \ell_9
144: P_{2582} = (5, 0, 9, 1) lies on line \ell_2
                                                                      198: P_{3427} = (2, 5, 12, 1) lies on line \ell_{10}
145: P_{2586} = (9, 0, 9, 1) lies on line \ell_0
                                                                      199: P_{3432} = (7, 5, 12, 1) lies on line \ell_{11}
146: P_{2589} = (12, 0, 9, 1) lies on line \ell_1
                                                                      200: P_{3461} = (4, 7, 12, 1) lies on line \ell_{15}
147: P_{2632} = (7, 3, 9, 1) lies on line \ell_{15}
                                                                      201: P_{3487} = (14, 8, 12, 1) lies on line \ell_8
148: P_{2657} = (0, 5, 9, 1) lies on line \ell_{12}
                                                                      202: P_{3489} = (0, 9, 12, 1) lies on line \ell_{12}
149: P_{2668} = (11, 5, 9, 1) lies on line \ell_{13}
                                                                      203: P_{3490} = (1, 9, 12, 1) lies on line \ell_{13}
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204: P_{3497} = (8, 9, 12, 1) lies on line \ell_{14}
                                                                      231: P_{3956} = (3, 6, 14, 1) lies on line \ell_{14}
205: P_{3537} = (0, 12, 12, 1) lies on line \ell_3
                                                                      232: P_{3958} = (5, 6, 14, 1) lies on line \ell_{13}
                                                                      233: P_{3985} = (0, 8, 14, 1) lies on line \ell_9
206: P_{3542} = (5, 12, 12, 1) lies on line \ell_4
207: P_{3546} = (9, 12, 12, 1) lies on line \ell_5
                                                                      234 : P_{3987} = (2, 8, 14, 1) lies on line \ell_{11}
208 : P_{3603} = (2, 0, 13, 1) lies on line \ell_2
                                                                      235: P_{3995} = (10, 8, 14, 1) lies on line \ell_{10}
209 : P_{3614} = (13, 0, 13, 1) lies on line \ell_0
                                                                      236: P_{4028} = (11, 10, 14, 1) lies on line \ell_7
210: P_{3616} = (15, 0, 13, 1) lies on line \ell_1
                                                                      237: P_{4081} = (0, 14, 14, 1) lies on line \ell_3
211: P_{3628} = (11, 1, 13, 1) lies on line \ell_8
                                                                      238: P_{4087} = (6, 14, 14, 1) lies on line \ell_5
212: P_{3633} = (0, 2, 13, 1) lies on line \ell_{12}
                                                                      239 : P_{4089} = (8, 14, 14, 1) lies on line \ell_4
213: P_{3634} = (1, 2, 13, 1) lies on line \ell_{14}
                                                                      240: P_{4115} = (2, 0, 15, 1) lies on line \ell_1
214: P_{3636} = (3, 2, 13, 1) lies on line \ell_{13}
                                                                      241: P_{4126} = (13, 0, 15, 1) lies on line \ell_2
215: P_{3653} = (4, 3, 13, 1) lies on line \ell_6
                                                                      242: P_{4128} = (15, 0, 15, 1) lies on line \ell_0
216: P_{3711} = (14, 6, 13, 1) lies on line \ell_7
                                                                      243: P_{4145} = (0, 2, 15, 1) lies on line \ell_9
217: P_{3757} = (12, 9, 13, 1) lies on line \ell_{15}
                                                                      244: P_{4157} = (12, 2, 15, 1) lies on line \ell_{11}
218 : P_{3809} = (0, 13, 13, 1) lies on line \ell_3
                                                                      245: P_{4159} = (14, 2, 15, 1) lies on line \ell_{10}
219: P_{3811} = (2, 13, 13, 1) lies on line \ell_5
                                                                      246: P_{4228} = (3, 7, 15, 1) lies on line \ell_6
220: P_{3824} = (15, 13, 13, 1) lies on line \ell_4
                                                                      247: P_{4274} = (1, 10, 15, 1) lies on line \ell_8
221: P_{3841} = (0, 15, 13, 1) lies on line \ell_9
                                                                      248: P_{4310} = (5, 12, 15, 1) lies on line \ell_{15}
222 : P_{3847} = (6, 15, 13, 1) lies on line \ell_{10}
                                                                      249: P_{4321} = (0, 13, 15, 1) lies on line \ell_{12}
223: P_{3850} = (9, 15, 13, 1) lies on line \ell_{11}
                                                                      250: P_{4328} = (7, 13, 15, 1) lies on line \ell_{13}
224 : P_{3863} = (6, 0, 14, 1) lies on line \ell_2
                                                                      251: P_{4331} = (10, 13, 15, 1) lies on line \ell_{14}
225 : P_{3865} = (8, 0, 14, 1) lies on line \ell_1
                                                                      252 : P_{4345} = (8, 14, 15, 1) lies on line \ell_7
226: P_{3871} = (14, 0, 14, 1) lies on line \ell_0
                                                                      253: P_{4353} = (0, 15, 15, 1) lies on line \ell_3
227: P_{3902} = (13, 2, 14, 1) lies on line \ell_{15}
                                                                      254: P_{4355} = (2, 15, 15, 1) lies on line \ell_4
228: P_{3909} = (4, 3, 14, 1) lies on line \ell_8
                                                                      255: P_{4366} = (13, 15, 15, 1) lies on line \ell_5
229: P_{3949} = (12, 5, 14, 1) lies on line \ell_6
230: P_{3953} = (0, 6, 14, 1) lies on line \ell_{12}
```

The single points on the surface are:

# Points on surface but on no line

The surface has 0 points not on any line: The points on the surface but not on lines are:

# Line Intersection Graph

	0 1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	01	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1 0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	11	0	1	1	1	1	1	1	1	1	1	1	1	1	1
3	11	1	0	1	1	1	1	1	1	1	1	1	1	1	1
4	1 1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
5	1 1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
6	1 1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
7	11	1	1	1	1	1	0	1	1	1	1	1	1	1	1
8	1 1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
9	11	1	1	1	1	1	1	1	0	1	1	1	1	1	1
10	1 1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
11	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
12	1 1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
13	1 1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
14	1 1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
15	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

# Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

# Line 3 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

# ${\bf Line~4~intersects}$

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 5 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

# Line 6 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

# Line 7 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

#### Line 8 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

#### Line 9 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$									

### Line 10 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

#### Line 11 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

#### Line 12 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

#### Line 13 intersects

Line	0	$\ell_1$									$\ell_{10}$			$\ell_{14}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$

### Line 14 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{15}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

### Line 15 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$
in point	$P_3$	$P_3$	$P_3$	$P_3$	$P_3$										

The surface has 257 points:

The points on the surface are:

```
0: P_3 = (0,0,0,1)
                                            14: P_{197} = (2, 11, 1, 0)
                                                                                        28: P_{703} = (14, 10, 1, 1)
1: P_{20} = (1, 0, 1, 0)
                                            15: P_{204} = (9, 11, 1, 0)
                                                                                        29: P_{705} = (0, 11, 1, 1)
2: P_{29} = (10, 0, 1, 0)
                                                                                        30: P_{707} = (2, 11, 1, 1)
                                            16: P_{251} = (8, 14, 1, 0)
                                            17: P_{531} = (1, 0, 1, 1)
3: P_{30} = (11, 0, 1, 0)
                                                                                        31: P_{714} = (9, 11, 1, 1)
4: P_{35} = (0, 1, 1, 0)
                                            18: P_{540} = (10, 0, 1, 1)
                                                                                        32: P_{761} = (8, 14, 1, 1)
5: P_{45} = (10, 1, 1, 0)
                                            19: P_{541} = (11, 0, 1, 1)
                                                                                        33: P_{787} = (2,0,2,1)
6: P_{46} = (11, 1, 1, 0)
                                            20: P_{546} = (0, 1, 1, 1)
                                                                                        34: P_{798} = (13, 0, 2, 1)
7: P_{66} = (15, 2, 1, 0)
                                            21: P_{555} = (10, 1, 1, 1)
                                                                                        35: P_{800} = (15, 0, 2, 1)
8: P_{86} = (3, 4, 1, 0)
                                            22: P_{556} = (11, 1, 1, 1)
                                                                                        36: P_{817} = (0, 2, 2, 1)
9: P_{168} = (5, 9, 1, 0)
                                            23: P_{576} = (15, 2, 1, 1)
                                                                                        37: P_{830} = (13, 2, 2, 1)
10: P_{179} = (0, 10, 1, 0)
                                            24: P_{596} = (3, 4, 1, 1)
                                                                                        38: P_{832} = (15, 2, 2, 1)
11: P_{183} = (4, 10, 1, 0)
                                            25: P_{678} = (5, 9, 1, 1)
                                                                                        39: P_{856} = (7,4,2,1)
12: P_{193} = (14, 10, 1, 0)
                                            26: P_{689} = (0, 10, 1, 1)
                                                                                        40: P_{874} = (9, 5, 2, 1)
13: P_{195} = (0, 11, 1, 0)
                                            27: P_{693} = (4, 10, 1, 1)
                                                                                        41: P_{919} = (6, 8, 2, 1)
```

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42: P_{971} = (10, 11, 2, 1)
                                           96: P_{1776} = (15, 13, 5, 1)
                                                                                       150: P_{2668} = (11, 5, 9, 1)
                                                                                       151: P_{2671} = (14, 5, 9, 1)
43: P_{993} = (0, 13, 2, 1)
                                           97: P_{1815} = (6, 0, 6, 1)
44: P_{998} = (5, 13, 2, 1)
                                           98: P_{1817} = (8, 0, 6, 1)
                                                                                       152: P_{2721} = (0, 9, 9, 1)
                                                                                       153: P_{2726} = (5, 9, 9, 1)
45: P_{1001} = (8, 13, 2, 1)
                                           99: P_{1823} = (14, 0, 6, 1)
46: P_{1025} = (0, 15, 2, 1)
                                           100: P_{1835} = (10, 1, 6, 1)
                                                                                       154: P_{2733} = (12, 9, 9, 1)
47: P_{1029} = (4, 15, 2, 1)
                                           101: P_{1880} = (7, 4, 6, 1)
                                                                                       155: P_{2763} = (10, 11, 9, 1)
48: P_{1036} = (11, 15, 2, 1)
                                           102: P_{1905} = (0, 6, 6, 1)
                                                                                       156: P_{2769} = (0, 12, 9, 1)
49: P_{1044} = (3,0,3,1)
                                           103: P_{1913} = (8, 6, 6, 1)
                                                                                       157: P_{2772} = (3, 12, 9, 1)
50: P_{1045} = (4,0,3,1)
                                           104: P_{1919} = (14, 6, 6, 1)
                                                                                       158: P_{2784} = (15, 12, 9, 1)
51: P_{1048} = (7,0,3,1)
                                           105: P_{1937} = (0, 8, 6, 1)
                                                                                       159: P_{2807} = (6, 14, 9, 1)
52: P_{1088} = (15, 2, 3, 1)
                                           106: P_{1941} = (4, 8, 6, 1)
                                                                                       160: P_{2819} = (2, 15, 9, 1)
53: P_{1089} = (0,3,3,1)
                                           107: P_{1949} = (12, 8, 6, 1)
                                                                                       161: P_{2834} = (1, 0, 10, 1)
54: P_{1093} = (4, 3, 3, 1)
                                           108: P_{2010} = (9, 12, 6, 1)
                                                                                       162: P_{2843} = (10, 0, 10, 1)
55: P_{1096} = (7, 3, 3, 1)
                                                                                       163: P_{2844} = (11, 0, 10, 1)
                                           109: P_{2033} = (0, 14, 6, 1)
56: P_{1105} = (0, 4, 3, 1)
                                                                                       164: P_{2849} = (0, 1, 10, 1)
                                           110: P_{2034} = (1, 14, 6, 1)
57: P_{1107} = (2,4,3,1)
                                           111: P_{2048} = (15, 14, 6, 1)
                                                                                       165: P_{2861} = (12, 1, 10, 1)
                                                                                       166: P_{2862} = (13, 1, 10, 1)
58: P_{1111} = (6,4,3,1)
                                           112: P_{2051} = (2, 15, 6, 1)
                                           113: P_{2068} = (3, 0, 7, 1)
59: P_{1145} = (8, 6, 3, 1)
                                                                                       167: P_{2888} = (7, 3, 10, 1)
                                                                                       168: P_{2967} = (6, 8, 10, 1)
60: P_{1153} = (0,7,3,1)
                                           114: P_{2069} = (4, 0, 7, 1)
61: P_{1164} = (11, 7, 3, 1)
                                           115: P_{2072} = (7, 0, 7, 1)
                                                                                       169: P_{2993} = (0, 10, 10, 1)
62: P_{1165} = (12, 7, 3, 1)
                                           116: P_{2091} = (10, 1, 7, 1)
                                                                                       170: P_{2994} = (1, 10, 10, 1)
63: P_{1218} = (1, 11, 3, 1)
                                           117: P_{2113} = (0, 3, 7, 1)
                                                                                       171: P_{3004} = (11, 10, 10, 1)
64: P_{1238} = (5, 12, 3, 1)
                                           118: P_{2126} = (13, 3, 7, 1)
                                                                                       172: P_{3009} = (0, 11, 10, 1)
65: P_{1300} = (3, 0, 4, 1)
                                           119: P_{2127} = (14, 3, 7, 1)
                                                                                       173: P_{3012} = (3, 11, 10, 1)
66: P_{1301} = (4, 0, 4, 1)
                                           120: P_{2129} = (0,4,7,1)
                                                                                       174: P_{3017} = (8, 11, 10, 1)
67: P_{1304} = (7, 0, 4, 1)
                                           121: P_{2130} = (1, 4, 7, 1)
                                                                                       175: P_{3034} = (9, 12, 10, 1)
                                           122: P_{2134} = (5, 4, 7, 1)
68: P_{1345} = (0, 3, 4, 1)
                                                                                       176: P_{3043} = (2, 13, 10, 1)
69: P_{1354} = (9, 3, 4, 1)
                                           123: P_{2154} = (9, 5, 7, 1)
                                                                                       177: P_{3090} = (1, 0, 11, 1)
                                           124: P_{2177} = (0,7,7,1)
                                                                                       178: P_{3099} = (10, 0, 11, 1)
70: P_{1355} = (10, 3, 4, 1)
                                           125: P_{2180} = (3, 7, 7, 1)
71: P_{1361} = (0, 4, 4, 1)
                                                                                       179: P_{3100} = (11, 0, 11, 1)
72: P_{1364} = (3,4,4,1)
                                           126: P_{2181} = (4,7,7,1)
                                                                                       180: P_{3105} = (0, 1, 11, 1)
                                                                                       181: P_{3111} = (6, 1, 11, 1)
73: P_{1368} = (7, 4, 4, 1)
                                           127: P_{2275} = (2, 13, 7, 1)
74: P_{1409} = (0,7,4,1)
                                           128: P_{2295} = (6, 14, 7, 1)
                                                                                       182: P_{3112} = (7, 1, 11, 1)
75: P_{1417} = (8, 7, 4, 1)
                                           129: P_{2327} = (6,0,8,1)
                                                                                       183: P_{3181} = (12, 5, 11, 1)
76: P_{1424} = (15, 7, 4, 1)
                                           130 : P_{2329} = (8, 0, 8, 1)
                                                                                       184: P_{3199} = (14, 6, 11, 1)
77: P_{1439} = (14, 8, 4, 1)
                                           131: P_{2335} = (14, 0, 8, 1)
                                                                                       185: P_{3205} = (4,7,11,1)
78: P_{1453} = (12, 9, 4, 1)
                                           132: P_{2417} = (0, 6, 8, 1)
                                                                                       186: P_{3249} = (0, 10, 11, 1)
                                                                                       187: P_{3254} = (5, 10, 11, 1)
79: P_{1468} = (11, 10, 4, 1)
                                           133: P_{2428} = (11, 6, 8, 1)
80: P_{1550} = (13, 15, 4, 1)
                                           134: P_{2430} = (13, 6, 8, 1)
                                                                                       188: P_{3264} = (15, 10, 11, 1)
81: P_{1558} = (5,0,5,1)
                                           135: P_{2436} = (3,7,8,1)
                                                                                       189: P_{3265} = (0, 11, 11, 1)
82: P_{1562} = (9, 0, 5, 1)
                                           136: P_{2449} = (0, 8, 8, 1)
                                                                                       190: P_{3266} = (1, 11, 11, 1)
83: P_{1565} = (12, 0, 5, 1)
                                           137: P_{2455} = (6, 8, 8, 1)
                                                                                       191: P_{3275} = (10, 11, 11, 1)
84: P_{1620} = (3,4,5,1)
                                           138: P_{2463} = (14, 8, 8, 1)
                                                                                       192: P_{3342} = (13, 15, 11, 1)
85: P_{1633} = (0, 5, 5, 1)
                                           139: P_{2470} = (5, 9, 8, 1)
                                                                                       193: P_{3350} = (5, 0, 12, 1)
86: P_{1642} = (9, 5, 5, 1)
                                           140: P_{2498} = (1, 11, 8, 1)
                                                                                       194: P_{3354} = (9, 0, 12, 1)
                                                                                       195: P_{3357} = (12, 0, 12, 1)
87: P_{1645} = (12, 5, 5, 1)
                                           141: P_{2544} = (15, 13, 8, 1)
88: P_{1657} = (8, 6, 5, 1)
                                           142: P_{2545} = (0, 14, 8, 1)
                                                                                       196: P_{3372} = (11, 1, 12, 1)
89: P_{1697} = (0, 9, 5, 1)
                                           143: P_{2552} = (7, 14, 8, 1)
                                                                                       197: P_{3390} = (13, 2, 12, 1)
                                                                                       198: P_{3425} = (0, 5, 12, 1)
90: P_{1701} = (4, 9, 5, 1)
                                           144: P_{2554} = (9, 14, 8, 1)
91: P_{1710} = (13, 9, 5, 1)
                                           145: P_{2582} = (5, 0, 9, 1)
                                                                                       199: P_{3427} = (2, 5, 12, 1)
92: P_{1714} = (1, 10, 5, 1)
                                           146: P_{2586} = (9, 0, 9, 1)
                                                                                       200: P_{3432} = (7, 5, 12, 1)
93: P_{1745} = (0, 12, 5, 1)
                                           147: P_{2589} = (12, 0, 9, 1)
                                                                                       201: P_{3461} = (4,7,12,1)
94: P_{1751} = (6, 12, 5, 1)
                                           148: P_{2632} = (7, 3, 9, 1)
                                                                                       202: P_{3487} = (14, 8, 12, 1)
95: P_{1755} = (10, 12, 5, 1)
                                           149: P_{2657} = (0, 5, 9, 1)
                                                                                       203: P_{3489} = (0, 9, 12, 1)
```

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204: P_{3490} = (1, 9, 12, 1)
                                           222: P_{3841} = (0, 15, 13, 1)
                                                                                      240: P_{4089} = (8, 14, 14, 1)
205: P_{3497} = (8, 9, 12, 1)
                                           223: P_{3847} = (6, 15, 13, 1)
                                                                                      241: P_{4115} = (2, 0, 15, 1)
206: P_{3537} = (0, 12, 12, 1)
                                           224: P_{3850} = (9, 15, 13, 1)
                                                                                      242: P_{4126} = (13, 0, 15, 1)
207: P_{3542} = (5, 12, 12, 1)
                                           225: P_{3863} = (6, 0, 14, 1)
                                                                                      243: P_{4128} = (15, 0, 15, 1)
208: P_{3546} = (9, 12, 12, 1)
                                           226: P_{3865} = (8, 0, 14, 1)
                                                                                      244: P_{4145} = (0, 2, 15, 1)
                                                                                      245: P_{4157} = (12, 2, 15, 1)
209: P_{3603} = (2, 0, 13, 1)
                                           227: P_{3871} = (14, 0, 14, 1)
                                                                                      246: P_{4159} = (14, 2, 15, 1)
210: P_{3614} = (13, 0, 13, 1)
                                           228: P_{3902} = (13, 2, 14, 1)
                                                                                      247: P_{4228} = (3, 7, 15, 1)
                                           229: P_{3909} = (4, 3, 14, 1)
211: P_{3616} = (15, 0, 13, 1)
212: P_{3628} = (11, 1, 13, 1)
                                           230: P_{3949} = (12, 5, 14, 1)
                                                                                      248: P_{4274} = (1, 10, 15, 1)
213: P_{3633} = (0, 2, 13, 1)
                                           231: P_{3953} = (0, 6, 14, 1)
                                                                                      249: P_{4310} = (5, 12, 15, 1)
214: P_{3634} = (1, 2, 13, 1)
                                           232: P_{3956} = (3, 6, 14, 1)
                                                                                      250: P_{4321} = (0, 13, 15, 1)
                                           233: P_{3958} = (5, 6, 14, 1)
                                                                                      251: P_{4328} = (7, 13, 15, 1)
215: P_{3636} = (3, 2, 13, 1)
216: P_{3653} = (4, 3, 13, 1)
                                           234: P_{3985} = (0, 8, 14, 1)
                                                                                      252: P_{4331} = (10, 13, 15, 1)
217: P_{3711} = (14, 6, 13, 1)
                                           235: P_{3987} = (2, 8, 14, 1)
                                                                                      253: P_{4345} = (8, 14, 15, 1)
218: P_{3757} = (12, 9, 13, 1)
                                           236: P_{3995} = (10, 8, 14, 1)
                                                                                      254: P_{4353} = (0, 15, 15, 1)
219: P_{3809} = (0, 13, 13, 1)
                                           237: P_{4028} = (11, 10, 14, 1)
                                                                                      255: P_{4355} = (2, 15, 15, 1)
                                                                                      256: P_{4366} = (13, 15, 15, 1)
220: P_{3811} = (2, 13, 13, 1)
                                           238: P_{4081} = (0, 14, 14, 1)
221: P_{3824} = (15, 13, 13, 1)
                                           239: P_{4087} = (6, 14, 14, 1)
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