

Rank-74279 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_2^3 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(0, 0, 1, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is 1141934117

General information

Number of lines	1
Number of points	1057
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	33
Number of points off lines	1024
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33
Type of lines on points	$1^{33}, 0^{1024}$

Singular Points

The surface has 0 singular points:

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0$$

Rank of lines: (0)

Rank of points on Klein quadric: (0)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 33 single points:

The single points on the surface are:

- | | |
|---|---|
| 0 : $P_0 = (1, 0, 0, 0)$ lies on line ℓ_0 | 17 : $P_{20} = (16, 1, 0, 0)$ lies on line ℓ_0 |
| 1 : $P_1 = (0, 1, 0, 0)$ lies on line ℓ_0 | 18 : $P_{21} = (17, 1, 0, 0)$ lies on line ℓ_0 |
| 2 : $P_5 = (1, 1, 0, 0)$ lies on line ℓ_0 | 19 : $P_{22} = (18, 1, 0, 0)$ lies on line ℓ_0 |
| 3 : $P_6 = (2, 1, 0, 0)$ lies on line ℓ_0 | 20 : $P_{23} = (19, 1, 0, 0)$ lies on line ℓ_0 |
| 4 : $P_7 = (3, 1, 0, 0)$ lies on line ℓ_0 | 21 : $P_{24} = (20, 1, 0, 0)$ lies on line ℓ_0 |
| 5 : $P_8 = (4, 1, 0, 0)$ lies on line ℓ_0 | 22 : $P_{25} = (21, 1, 0, 0)$ lies on line ℓ_0 |
| 6 : $P_9 = (5, 1, 0, 0)$ lies on line ℓ_0 | 23 : $P_{26} = (22, 1, 0, 0)$ lies on line ℓ_0 |
| 7 : $P_{10} = (6, 1, 0, 0)$ lies on line ℓ_0 | 24 : $P_{27} = (23, 1, 0, 0)$ lies on line ℓ_0 |
| 8 : $P_{11} = (7, 1, 0, 0)$ lies on line ℓ_0 | 25 : $P_{28} = (24, 1, 0, 0)$ lies on line ℓ_0 |
| 9 : $P_{12} = (8, 1, 0, 0)$ lies on line ℓ_0 | 26 : $P_{29} = (25, 1, 0, 0)$ lies on line ℓ_0 |
| 10 : $P_{13} = (9, 1, 0, 0)$ lies on line ℓ_0 | 27 : $P_{30} = (26, 1, 0, 0)$ lies on line ℓ_0 |
| 11 : $P_{14} = (10, 1, 0, 0)$ lies on line ℓ_0 | 28 : $P_{31} = (27, 1, 0, 0)$ lies on line ℓ_0 |
| 12 : $P_{15} = (11, 1, 0, 0)$ lies on line ℓ_0 | 29 : $P_{32} = (28, 1, 0, 0)$ lies on line ℓ_0 |
| 13 : $P_{16} = (12, 1, 0, 0)$ lies on line ℓ_0 | 30 : $P_{33} = (29, 1, 0, 0)$ lies on line ℓ_0 |
| 14 : $P_{17} = (13, 1, 0, 0)$ lies on line ℓ_0 | 31 : $P_{34} = (30, 1, 0, 0)$ lies on line ℓ_0 |
| 15 : $P_{18} = (14, 1, 0, 0)$ lies on line ℓ_0 | 32 : $P_{35} = (31, 1, 0, 0)$ lies on line ℓ_0 |
| 16 : $P_{19} = (15, 1, 0, 0)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 1024 points not on any line:

Too many to print.

Line Intersection Graph

$$\begin{array}{c|c} 0 & \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line
in point

The surface has 1057 points:

Too many to print.