

# Cheat Sheet PG(3, 4)

January 16, 2021

## The projective space PG(3, 4)

$$q = 4$$

$$p = 2$$

$$e = 2$$

$$n = 3$$

Number of points = 85

Number of lines = 357

Number of lines on a point = 21

Number of points on a line = 5

## The points of PG(3, 4)

PG(3, 4) has 85 points:

$$P_0 = (1, 0, 0, 0) = (1, 0, 0, 0)$$

$$P_1 = (0, 1, 0, 0) = (0, 1, 0, 0)$$

$$P_2 = (0, 0, 1, 0) = (0, 0, 1, 0)$$

$$P_3 = (0, 0, 0, 1) = (0, 0, 0, 1)$$

$$P_4 = (1, 1, 1, 1) = (1, 1, 1, 1)$$

$$P_5 = (1, 1, 0, 0) = (1, 1, 0, 0)$$

$$P_6 = (2, 1, 0, 0) = (\alpha, 1, 0, 0)$$

$$P_7 = (3, 1, 0, 0) = (\alpha^2, 1, 0, 0)$$

$$P_8 = (1, 0, 1, 0) = (1, 0, 1, 0)$$

$$P_9 = (2, 0, 1, 0) = (\alpha, 0, 1, 0)$$

$$P_{10} = (3, 0, 1, 0) = (\alpha^2, 0, 1, 0)$$

$$P_{11} = (0, 1, 1, 0) = (0, 1, 1, 0)$$

$$P_{12} = (1, 1, 1, 0) = (1, 1, 1, 0)$$

$$P_{13} = (2, 1, 1, 0) = (\alpha, 1, 1, 0)$$

$$P_{14} = (3, 1, 1, 0) = (\alpha^2, 1, 1, 0)$$

$$P_{15} = (0, 2, 1, 0) = (0, \alpha, 1, 0)$$

$$P_{16} = (1, 2, 1, 0) = (1, \alpha, 1, 0)$$

$$P_{17} = (2, 2, 1, 0) = (\alpha, \alpha, 1, 0)$$

$$P_{18} = (3, 2, 1, 0) = (\alpha^2, \alpha, 1, 0)$$

$$P_{19} = (0, 3, 1, 0) = (0, \alpha^2, 1, 0)$$

$$P_{20} = (1, 3, 1, 0) = (1, \alpha^2, 1, 0)$$

$$P_{21} = (2, 3, 1, 0) = (\alpha, \alpha^2, 1, 0)$$

$$P_{22} = (3, 3, 1, 0) = (\alpha^2, \alpha^2, 1, 0)$$

$$P_{23} = (1, 0, 0, 1) = (1, 0, 0, 1)$$

$$P_{24} = (2, 0, 0, 1) = (\alpha, 0, 0, 1)$$

$$P_{25} = (3, 0, 0, 1) = (\alpha^2, 0, 0, 1)$$

$$P_{26} = (0, 1, 0, 1) = (0, 1, 0, 1)$$

$$P_{27} = (1, 1, 0, 1) = (1, 1, 0, 1)$$

$$P_{28} = (2, 1, 0, 1) = (\alpha, 1, 0, 1)$$

$$P_{29} = (3, 1, 0, 1) = (\alpha^2, 1, 0, 1)$$

$$P_{30} = (0, 2, 0, 1) = (0, \alpha, 0, 1)$$

$$P_{31} = (1, 2, 0, 1) = (1, \alpha, 0, 1)$$

$$P_{32} = (2, 2, 0, 1) = (\alpha, \alpha, 0, 1)$$

$$P_{33} = (3, 2, 0, 1) = (\alpha^2, \alpha, 0, 1)$$

$$\begin{aligned}
P_{34} &= (0, 3, 0, 1) = (0, \alpha^2, 0, 1) \\
P_{35} &= (1, 3, 0, 1) = (1, \alpha^2, 0, 1) \\
P_{36} &= (2, 3, 0, 1) = (\alpha, \alpha^2, 0, 1) \\
P_{37} &= (3, 3, 0, 1) = (\alpha^2, \alpha^2, 0, 1) \\
P_{38} &= (0, 0, 1, 1) = (0, 0, 1, 1) \\
P_{39} &= (1, 0, 1, 1) = (1, 0, 1, 1) \\
P_{40} &= (2, 0, 1, 1) = (\alpha, 0, 1, 1) \\
P_{41} &= (3, 0, 1, 1) = (\alpha^2, 0, 1, 1) \\
P_{42} &= (0, 1, 1, 1) = (0, 1, 1, 1) \\
P_{43} &= (2, 1, 1, 1) = (\alpha, 1, 1, 1) \\
P_{44} &= (3, 1, 1, 1) = (\alpha^2, 1, 1, 1) \\
P_{45} &= (0, 2, 1, 1) = (0, \alpha, 1, 1) \\
P_{46} &= (1, 2, 1, 1) = (1, \alpha, 1, 1) \\
P_{47} &= (2, 2, 1, 1) = (\alpha, \alpha, 1, 1) \\
P_{48} &= (3, 2, 1, 1) = (\alpha^2, \alpha, 1, 1) \\
P_{49} &= (0, 3, 1, 1) = (0, \alpha^2, 1, 1) \\
P_{50} &= (1, 3, 1, 1) = (1, \alpha^2, 1, 1) \\
P_{51} &= (2, 3, 1, 1) = (\alpha, \alpha^2, 1, 1) \\
P_{52} &= (3, 3, 1, 1) = (\alpha^2, \alpha^2, 1, 1) \\
P_{53} &= (0, 0, 2, 1) = (0, 0, \alpha, 1) \\
P_{54} &= (1, 0, 2, 1) = (1, 0, \alpha, 1) \\
P_{55} &= (2, 0, 2, 1) = (\alpha, 0, \alpha, 1) \\
P_{56} &= (3, 0, 2, 1) = (\alpha^2, 0, \alpha, 1) \\
P_{57} &= (0, 1, 2, 1) = (0, 1, \alpha, 1) \\
P_{58} &= (1, 1, 2, 1) = (1, 1, \alpha, 1) \\
P_{59} &= (2, 1, 2, 1) = (\alpha, 1, \alpha, 1)
\end{aligned}$$

$$\begin{aligned}
P_{60} &= (3, 1, 2, 1) = (\alpha^2, 1, \alpha, 1) \\
P_{61} &= (0, 2, 2, 1) = (0, \alpha, \alpha, 1) \\
P_{62} &= (1, 2, 2, 1) = (1, \alpha, \alpha, 1) \\
P_{63} &= (2, 2, 2, 1) = (\alpha, \alpha, \alpha, 1) \\
P_{64} &= (3, 2, 2, 1) = (\alpha^2, \alpha, \alpha, 1) \\
P_{65} &= (0, 3, 2, 1) = (0, \alpha^2, \alpha, 1) \\
P_{66} &= (1, 3, 2, 1) = (1, \alpha^2, \alpha, 1) \\
P_{67} &= (2, 3, 2, 1) = (\alpha, \alpha^2, \alpha, 1) \\
P_{68} &= (3, 3, 2, 1) = (\alpha^2, \alpha^2, \alpha, 1) \\
P_{69} &= (0, 0, 3, 1) = (0, 0, \alpha^2, 1) \\
P_{70} &= (1, 0, 3, 1) = (1, 0, \alpha^2, 1) \\
P_{71} &= (2, 0, 3, 1) = (\alpha, 0, \alpha^2, 1) \\
P_{72} &= (3, 0, 3, 1) = (\alpha^2, 0, \alpha^2, 1) \\
P_{73} &= (0, 1, 3, 1) = (0, 1, \alpha^2, 1) \\
P_{74} &= (1, 1, 3, 1) = (1, 1, \alpha^2, 1) \\
P_{75} &= (2, 1, 3, 1) = (\alpha, 1, \alpha^2, 1) \\
P_{76} &= (3, 1, 3, 1) = (\alpha^2, 1, \alpha^2, 1) \\
P_{77} &= (0, 2, 3, 1) = (0, \alpha, \alpha^2, 1) \\
P_{78} &= (1, 2, 3, 1) = (1, \alpha, \alpha^2, 1) \\
P_{79} &= (2, 2, 3, 1) = (\alpha, \alpha, \alpha^2, 1) \\
P_{80} &= (3, 2, 3, 1) = (\alpha^2, \alpha, \alpha^2, 1) \\
P_{81} &= (0, 3, 3, 1) = (0, \alpha^2, \alpha^2, 1) \\
P_{82} &= (1, 3, 3, 1) = (1, \alpha^2, \alpha^2, 1) \\
P_{83} &= (2, 3, 3, 1) = (\alpha, \alpha^2, \alpha^2, 1) \\
P_{84} &= (3, 3, 3, 1) = (\alpha^2, \alpha^2, \alpha^2, 1)
\end{aligned}$$

Baer subgeometry:

$$\begin{array}{llll}
P_0 = (1, 0, 0, 0) & P_4 = (1, 1, 1, 1) & P_{12} = (1, 1, 1, 0) & P_{38} = (0, 0, 1, 1) \\
P_1 = (0, 1, 0, 0) & P_5 = (1, 1, 0, 0) & P_{23} = (1, 0, 0, 1) & P_{39} = (1, 0, 1, 1) \\
P_2 = (0, 0, 1, 0) & P_8 = (1, 0, 1, 0) & P_{26} = (0, 1, 0, 1) & P_{42} = (0, 1, 1, 1) \\
P_3 = (0, 0, 0, 1) & P_{11} = (0, 1, 1, 0) & P_{27} = (1, 1, 0, 1) &
\end{array}$$

There are 15 elements in the Baer subgeometry.

Normalized from the left:

$$\begin{array}{llll}
P_0 = (1, 0, 0, 0) & P_6 = (1, 3, 0, 0) & P_{12} = (1, 1, 1, 0) & P_{18} = (1, 3, 2, 0) \\
P_1 = (0, 1, 0, 0) & P_7 = (1, 2, 0, 0) & P_{13} = (1, 3, 3, 0) & P_{19} = (0, 1, 2, 0) \\
P_2 = (0, 0, 1, 0) & P_8 = (1, 0, 1, 0) & P_{14} = (1, 2, 2, 0) & P_{20} = (1, 3, 1, 0) \\
P_3 = (0, 0, 0, 1) & P_9 = (1, 0, 3, 0) & P_{15} = (0, 1, 3, 0) & P_{21} = (1, 2, 3, 0) \\
P_4 = (1, 1, 1, 1) & P_{10} = (1, 0, 2, 0) & P_{16} = (1, 2, 1, 0) & P_{22} = (1, 1, 2, 0) \\
P_5 = (1, 1, 0, 0) & P_{11} = (0, 1, 1, 0) & P_{17} = (1, 1, 3, 0) & P_{23} = (1, 0, 0, 1)
\end{array}$$

$P_{24} = (1, 0, 0, 3)$	$P_{40} = (1, 0, 3, 3)$	$P_{56} = (1, 0, 3, 2)$	$P_{72} = (1, 0, 1, 2)$
$P_{25} = (1, 0, 0, 2)$	$P_{41} = (1, 0, 2, 2)$	$P_{57} = (0, 1, 2, 1)$	$P_{73} = (0, 1, 3, 1)$
$P_{26} = (0, 1, 0, 1)$	$P_{42} = (0, 1, 1, 1)$	$P_{58} = (1, 1, 2, 1)$	$P_{74} = (1, 1, 3, 1)$
$P_{27} = (1, 1, 0, 1)$	$P_{43} = (1, 3, 3, 3)$	$P_{59} = (1, 3, 1, 3)$	$P_{75} = (1, 3, 2, 3)$
$P_{28} = (1, 3, 0, 3)$	$P_{44} = (1, 2, 2, 2)$	$P_{60} = (1, 2, 3, 2)$	$P_{76} = (1, 2, 1, 2)$
$P_{29} = (1, 2, 0, 2)$	$P_{45} = (0, 1, 3, 3)$	$P_{61} = (0, 1, 1, 3)$	$P_{77} = (0, 1, 2, 3)$
$P_{30} = (0, 1, 0, 3)$	$P_{46} = (1, 2, 1, 1)$	$P_{62} = (1, 2, 2, 1)$	$P_{78} = (1, 2, 3, 1)$
$P_{31} = (1, 2, 0, 1)$	$P_{47} = (1, 1, 3, 3)$	$P_{63} = (1, 1, 1, 3)$	$P_{79} = (1, 1, 2, 3)$
$P_{32} = (1, 1, 0, 3)$	$P_{48} = (1, 3, 2, 2)$	$P_{64} = (1, 3, 3, 2)$	$P_{80} = (1, 3, 1, 2)$
$P_{33} = (1, 3, 0, 2)$	$P_{49} = (0, 1, 2, 2)$	$P_{65} = (0, 1, 3, 2)$	$P_{81} = (0, 1, 1, 2)$
$P_{34} = (0, 1, 0, 2)$	$P_{50} = (1, 3, 1, 1)$	$P_{66} = (1, 3, 2, 1)$	$P_{82} = (1, 3, 3, 1)$
$P_{35} = (1, 3, 0, 1)$	$P_{51} = (1, 2, 3, 3)$	$P_{67} = (1, 2, 1, 3)$	$P_{83} = (1, 2, 2, 3)$
$P_{36} = (1, 2, 0, 3)$	$P_{52} = (1, 1, 2, 2)$	$P_{68} = (1, 1, 3, 2)$	$P_{84} = (1, 1, 1, 2)$
$P_{37} = (1, 1, 0, 2)$	$P_{53} = (0, 0, 1, 3)$	$P_{69} = (0, 0, 1, 2)$	
$P_{38} = (0, 0, 1, 1)$	$P_{54} = (1, 0, 2, 1)$	$P_{70} = (1, 0, 3, 1)$	
$P_{39} = (1, 0, 1, 1)$	$P_{55} = (1, 0, 1, 3)$	$P_{71} = (1, 0, 2, 3)$	

## The lines of $\text{PG}(3, 4)$

$\text{PG}(3, 4)$  has 357 1-subspaces:

$$\begin{aligned}
L_0 &= \begin{bmatrix} 1000 \\ 0100 \end{bmatrix} = \mathbf{Pl}(1, 0, 0, 0, 0, 0) \\
L_1 &= \begin{bmatrix} 1000 \\ 0110 \end{bmatrix} = \mathbf{Pl}(1, 0, 1, 0, 0, 0) \\
L_2 &= \begin{bmatrix} 1000 \\ 0120 \end{bmatrix} = \mathbf{Pl}(1, 0, 2, 0, 0, 0) \\
L_3 &= \begin{bmatrix} 1000 \\ 0130 \end{bmatrix} = \mathbf{Pl}(1, 0, 3, 0, 0, 0) \\
L_4 &= \begin{bmatrix} 1000 \\ 0101 \end{bmatrix} = \mathbf{Pl}(1, 0, 0, 0, 1, 0) \\
L_5 &= \begin{bmatrix} 1000 \\ 0111 \end{bmatrix} = \mathbf{Pl}(1, 0, 1, 0, 1, 0) \\
L_6 &= \begin{bmatrix} 1000 \\ 0121 \end{bmatrix} = \mathbf{Pl}(1, 0, 2, 0, 1, 0) \\
L_7 &= \begin{bmatrix} 1000 \\ 0131 \end{bmatrix} = \mathbf{Pl}(1, 0, 3, 0, 1, 0) \\
L_8 &= \begin{bmatrix} 1000 \\ 0102 \end{bmatrix} = \mathbf{Pl}(1, 0, 0, 0, 2, 0) \\
L_9 &= \begin{bmatrix} 1000 \\ 0112 \end{bmatrix} = \mathbf{Pl}(1, 0, 1, 0, 2, 0) \\
L_{10} &= \begin{bmatrix} 1000 \\ 0122 \end{bmatrix} = \mathbf{Pl}(1, 0, 2, 0, 2, 0) \\
L_{11} &= \begin{bmatrix} 1000 \\ 0132 \end{bmatrix} = \mathbf{Pl}(1, 0, 3, 0, 2, 0) \\
L_{12} &= \begin{bmatrix} 1000 \\ 0103 \end{bmatrix} = \mathbf{Pl}(1, 0, 0, 0, 3, 0) \\
L_{13} &= \begin{bmatrix} 1000 \\ 0113 \end{bmatrix} = \mathbf{Pl}(1, 0, 1, 0, 3, 0) \\
L_{14} &= \begin{bmatrix} 1000 \\ 0123 \end{bmatrix} = \mathbf{Pl}(1, 0, 2, 0, 3, 0) \\
L_{15} &= \begin{bmatrix} 1000 \\ 0133 \end{bmatrix} = \mathbf{Pl}(1, 0, 3, 0, 3, 0) \\
L_{16} &= \begin{bmatrix} 1000 \\ 0010 \end{bmatrix} = \mathbf{Pl}(0, 0, 1, 0, 0, 0) \\
L_{17} &= \begin{bmatrix} 1000 \\ 0011 \end{bmatrix} = \mathbf{Pl}(0, 0, 1, 0, 1, 0) \\
L_{18} &= \begin{bmatrix} 1000 \\ 0012 \end{bmatrix} = \mathbf{Pl}(0, 0, 1, 0, 2, 0) \\
L_{19} &= \begin{bmatrix} 1000 \\ 0013 \end{bmatrix} = \mathbf{Pl}(0, 0, 1, 0, 3, 0)
\end{aligned}$$

$$\begin{aligned}
L_{20} &= \begin{bmatrix} 1000 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 0, 1, 0) \\
L_{21} &= \begin{bmatrix} 1010 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 0, 0, 1) \\
L_{22} &= \begin{bmatrix} 1010 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 0, 0, 1) \\
L_{23} &= \begin{bmatrix} 1010 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 0, 0, 1) \\
L_{24} &= \begin{bmatrix} 1010 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 0, 0, 1) \\
L_{25} &= \begin{bmatrix} 1010 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 0, 1, 1) \\
L_{26} &= \begin{bmatrix} 1010 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 0, 1, 1) \\
L_{27} &= \begin{bmatrix} 1010 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 0, 1, 1) \\
L_{28} &= \begin{bmatrix} 1010 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 0, 1, 1) \\
L_{29} &= \begin{bmatrix} 1010 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 0, 2, 1) \\
L_{30} &= \begin{bmatrix} 1010 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 0, 2, 1) \\
L_{31} &= \begin{bmatrix} 1010 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 0, 2, 1) \\
L_{32} &= \begin{bmatrix} 1010 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 0, 2, 1) \\
L_{33} &= \begin{bmatrix} 1010 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 0, 3, 1) \\
L_{34} &= \begin{bmatrix} 1010 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 0, 3, 1) \\
L_{35} &= \begin{bmatrix} 1010 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 0, 3, 1) \\
L_{36} &= \begin{bmatrix} 1010 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 0, 3, 1) \\
L_{37} &= \begin{bmatrix} 1100 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 0, 0, 1) \\
L_{38} &= \begin{bmatrix} 1100 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 1, 1, 1) \\
L_{39} &= \begin{bmatrix} 1100 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 2, 2, 1) \\
L_{40} &= \begin{bmatrix} 1100 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 3, 3, 1)
\end{aligned}$$

$$\begin{aligned}
L_{41} &= \begin{bmatrix} 1100 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 1, 1, 0) \\
L_{42} &= \begin{bmatrix} 1020 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 0, 0, 2) \\
L_{43} &= \begin{bmatrix} 1020 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 0, 0, 2) \\
L_{44} &= \begin{bmatrix} 1020 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 0, 0, 2) \\
L_{45} &= \begin{bmatrix} 1020 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 0, 0, 2) \\
L_{46} &= \begin{bmatrix} 1020 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 0, 1, 2) \\
L_{47} &= \begin{bmatrix} 1020 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 0, 1, 2) \\
L_{48} &= \begin{bmatrix} 1020 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 0, 1, 2) \\
L_{49} &= \begin{bmatrix} 1020 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 0, 1, 2) \\
L_{50} &= \begin{bmatrix} 1020 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 0, 2, 2) \\
L_{51} &= \begin{bmatrix} 1020 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 0, 2, 2) \\
L_{52} &= \begin{bmatrix} 1020 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 0, 2, 2) \\
L_{53} &= \begin{bmatrix} 1020 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 0, 2, 2) \\
L_{54} &= \begin{bmatrix} 1020 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 0, 3, 2) \\
L_{55} &= \begin{bmatrix} 1020 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 0, 3, 2) \\
L_{56} &= \begin{bmatrix} 1020 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 0, 3, 2) \\
L_{57} &= \begin{bmatrix} 1020 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 0, 3, 2) \\
L_{58} &= \begin{bmatrix} 1200 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 0, 0, 2) \\
L_{59} &= \begin{bmatrix} 1200 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 2, 1, 2) \\
L_{60} &= \begin{bmatrix} 1200 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 3, 2, 2) \\
L_{61} &= \begin{bmatrix} 1200 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 1, 3, 2)
\end{aligned}$$

$$\begin{aligned}
L_{62} &= \begin{bmatrix} 1200 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 2, 1, 0) \\
L_{63} &= \begin{bmatrix} 1030 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 0, 0, 3) \\
L_{64} &= \begin{bmatrix} 1030 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 0, 0, 3) \\
L_{65} &= \begin{bmatrix} 1030 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 0, 0, 3) \\
L_{66} &= \begin{bmatrix} 1030 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 0, 0, 3) \\
L_{67} &= \begin{bmatrix} 1030 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 0, 1, 3) \\
L_{68} &= \begin{bmatrix} 1030 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 0, 1, 3) \\
L_{69} &= \begin{bmatrix} 1030 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 0, 1, 3) \\
L_{70} &= \begin{bmatrix} 1030 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 0, 1, 3) \\
L_{71} &= \begin{bmatrix} 1030 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 0, 2, 3) \\
L_{72} &= \begin{bmatrix} 1030 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 0, 2, 3) \\
L_{73} &= \begin{bmatrix} 1030 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 0, 2, 3) \\
L_{74} &= \begin{bmatrix} 1030 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 0, 2, 3) \\
L_{75} &= \begin{bmatrix} 1030 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 0, 3, 3) \\
L_{76} &= \begin{bmatrix} 1030 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 0, 3, 3) \\
L_{77} &= \begin{bmatrix} 1030 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 0, 3, 3) \\
L_{78} &= \begin{bmatrix} 1030 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 0, 3, 3) \\
L_{79} &= \begin{bmatrix} 1300 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 0, 0, 3) \\
L_{80} &= \begin{bmatrix} 1300 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 3, 1, 3) \\
L_{81} &= \begin{bmatrix} 1300 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 1, 2, 3) \\
L_{82} &= \begin{bmatrix} 1300 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 0, 1, 2, 3, 3)
\end{aligned}$$

$$\begin{aligned}
L_{83} &= \begin{bmatrix} 1300 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 3, 1, 0) \\
L_{84} &= \begin{bmatrix} 1001 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 0, 0) \\
L_{85} &= \begin{bmatrix} 1001 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 0, 0) \\
L_{86} &= \begin{bmatrix} 1001 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 0, 0) \\
L_{87} &= \begin{bmatrix} 1001 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 0, 0) \\
L_{88} &= \begin{bmatrix} 1001 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 1, 0) \\
L_{89} &= \begin{bmatrix} 1001 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 1, 0) \\
L_{90} &= \begin{bmatrix} 1001 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 1, 0) \\
L_{91} &= \begin{bmatrix} 1001 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 1, 0) \\
L_{92} &= \begin{bmatrix} 1001 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 2, 0) \\
L_{93} &= \begin{bmatrix} 1001 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 2, 0) \\
L_{94} &= \begin{bmatrix} 1001 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 2, 0) \\
L_{95} &= \begin{bmatrix} 1001 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 2, 0) \\
L_{96} &= \begin{bmatrix} 1001 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 3, 0) \\
L_{97} &= \begin{bmatrix} 1001 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 3, 0) \\
L_{98} &= \begin{bmatrix} 1001 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 3, 0) \\
L_{99} &= \begin{bmatrix} 1001 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 3, 0) \\
L_{100} &= \begin{bmatrix} 1001 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 0, 0) \\
L_{101} &= \begin{bmatrix} 1001 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 1, 0) \\
L_{102} &= \begin{bmatrix} 1001 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 2, 0) \\
L_{103} &= \begin{bmatrix} 1001 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 3, 0)
\end{aligned}$$



$$\begin{aligned}
L_{104} &= \begin{bmatrix} 1010 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 0, 1, 0) \\
L_{105} &= \begin{bmatrix} 1011 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 0, 1) \\
L_{106} &= \begin{bmatrix} 1011 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 0, 1) \\
L_{107} &= \begin{bmatrix} 1011 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 0, 1) \\
L_{108} &= \begin{bmatrix} 1011 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 0, 1) \\
L_{109} &= \begin{bmatrix} 1011 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 1, 1, 1) \\
L_{110} &= \begin{bmatrix} 1011 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 1, 1, 1) \\
L_{111} &= \begin{bmatrix} 1011 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 1, 1, 1) \\
L_{112} &= \begin{bmatrix} 1011 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 1, 1, 1) \\
L_{113} &= \begin{bmatrix} 1011 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 1, 2, 1) \\
L_{114} &= \begin{bmatrix} 1011 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 1, 2, 1) \\
L_{115} &= \begin{bmatrix} 1011 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 1, 2, 1) \\
L_{116} &= \begin{bmatrix} 1011 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 1, 2, 1) \\
L_{117} &= \begin{bmatrix} 1011 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 1, 3, 1) \\
L_{118} &= \begin{bmatrix} 1011 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 1, 3, 1) \\
L_{119} &= \begin{bmatrix} 1011 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 1, 3, 1) \\
L_{120} &= \begin{bmatrix} 1011 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 1, 3, 1) \\
L_{121} &= \begin{bmatrix} 1101 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 0, 1) \\
L_{122} &= \begin{bmatrix} 1101 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 1, 1, 1) \\
L_{123} &= \begin{bmatrix} 1101 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 2, 2, 1) \\
L_{124} &= \begin{bmatrix} 1101 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 3, 3, 1)
\end{aligned}$$

$$\begin{aligned}
L_{125} &= \begin{bmatrix} 1110 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 1, 1, 0) \\
L_{126} &= \begin{bmatrix} 1021 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 0, 2) \\
L_{127} &= \begin{bmatrix} 1021 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 0, 2) \\
L_{128} &= \begin{bmatrix} 1021 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 0, 2) \\
L_{129} &= \begin{bmatrix} 1021 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 0, 2) \\
L_{130} &= \begin{bmatrix} 1021 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 1, 1, 2) \\
L_{131} &= \begin{bmatrix} 1021 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 1, 1, 2) \\
L_{132} &= \begin{bmatrix} 1021 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 1, 1, 2) \\
L_{133} &= \begin{bmatrix} 1021 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 1, 1, 2) \\
L_{134} &= \begin{bmatrix} 1021 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 1, 2, 2) \\
L_{135} &= \begin{bmatrix} 1021 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 1, 2, 2) \\
L_{136} &= \begin{bmatrix} 1021 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 1, 2, 2) \\
L_{137} &= \begin{bmatrix} 1021 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 1, 2, 2) \\
L_{138} &= \begin{bmatrix} 1021 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 1, 3, 2) \\
L_{139} &= \begin{bmatrix} 1021 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 1, 3, 2) \\
L_{140} &= \begin{bmatrix} 1021 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 1, 3, 2) \\
L_{141} &= \begin{bmatrix} 1021 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 1, 3, 2) \\
L_{142} &= \begin{bmatrix} 1201 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 0, 2) \\
L_{143} &= \begin{bmatrix} 1201 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 2, 1, 2) \\
L_{144} &= \begin{bmatrix} 1201 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 3, 2, 2) \\
L_{145} &= \begin{bmatrix} 1201 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 1, 3, 2)
\end{aligned}$$

$$\begin{aligned}
L_{146} &= \begin{bmatrix} 1210 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 2, 1, 0) \\
L_{147} &= \begin{bmatrix} 1031 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 1, 0, 3) \\
L_{148} &= \begin{bmatrix} 1031 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 1, 0, 3) \\
L_{149} &= \begin{bmatrix} 1031 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 1, 0, 3) \\
L_{150} &= \begin{bmatrix} 1031 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 1, 0, 3) \\
L_{151} &= \begin{bmatrix} 1031 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 1, 1, 3) \\
L_{152} &= \begin{bmatrix} 1031 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 1, 1, 3) \\
L_{153} &= \begin{bmatrix} 1031 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 1, 1, 3) \\
L_{154} &= \begin{bmatrix} 1031 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 1, 1, 3) \\
L_{155} &= \begin{bmatrix} 1031 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 1, 2, 3) \\
L_{156} &= \begin{bmatrix} 1031 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 1, 2, 3) \\
L_{157} &= \begin{bmatrix} 1031 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 1, 2, 3) \\
L_{158} &= \begin{bmatrix} 1031 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 1, 2, 3) \\
L_{159} &= \begin{bmatrix} 1031 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 1, 3, 3) \\
L_{160} &= \begin{bmatrix} 1031 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 1, 3, 3) \\
L_{161} &= \begin{bmatrix} 1031 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 1, 3, 3) \\
L_{162} &= \begin{bmatrix} 1031 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 1, 3, 3) \\
L_{163} &= \begin{bmatrix} 1301 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 0, 0, 3) \\
L_{164} &= \begin{bmatrix} 1301 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 3, 1, 3) \\
L_{165} &= \begin{bmatrix} 1301 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 1, 2, 3) \\
L_{166} &= \begin{bmatrix} 1301 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 1, 1, 2, 3, 3)
\end{aligned}$$

$$\begin{aligned}
L_{167} &= \begin{bmatrix} 1310 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 3, 1, 0) \\
L_{168} &= \begin{bmatrix} 1002 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 0, 0) \\
L_{169} &= \begin{bmatrix} 1002 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 0, 0) \\
L_{170} &= \begin{bmatrix} 1002 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 0, 0) \\
L_{171} &= \begin{bmatrix} 1002 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 0, 0) \\
L_{172} &= \begin{bmatrix} 1002 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 1, 0) \\
L_{173} &= \begin{bmatrix} 1002 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 1, 0) \\
L_{174} &= \begin{bmatrix} 1002 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 1, 0) \\
L_{175} &= \begin{bmatrix} 1002 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 1, 0) \\
L_{176} &= \begin{bmatrix} 1002 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 2, 0) \\
L_{177} &= \begin{bmatrix} 1002 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 2, 0) \\
L_{178} &= \begin{bmatrix} 1002 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 2, 0) \\
L_{179} &= \begin{bmatrix} 1002 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 2, 0) \\
L_{180} &= \begin{bmatrix} 1002 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 3, 0) \\
L_{181} &= \begin{bmatrix} 1002 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 3, 0) \\
L_{182} &= \begin{bmatrix} 1002 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 3, 0) \\
L_{183} &= \begin{bmatrix} 1002 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 3, 0) \\
L_{184} &= \begin{bmatrix} 1002 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 0, 0) \\
L_{185} &= \begin{bmatrix} 1002 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 1, 0) \\
L_{186} &= \begin{bmatrix} 1002 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 2, 0) \\
L_{187} &= \begin{bmatrix} 1002 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 3, 0)
\end{aligned}$$

$$\begin{aligned}
L_{188} &= \begin{bmatrix} 1020 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 0, 1, 0) \\
L_{189} &= \begin{bmatrix} 1012 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 0, 1) \\
L_{190} &= \begin{bmatrix} 1012 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 0, 1) \\
L_{191} &= \begin{bmatrix} 1012 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 0, 1) \\
L_{192} &= \begin{bmatrix} 1012 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 0, 1) \\
L_{193} &= \begin{bmatrix} 1012 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 2, 1, 1) \\
L_{194} &= \begin{bmatrix} 1012 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 2, 1, 1) \\
L_{195} &= \begin{bmatrix} 1012 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 2, 1, 1) \\
L_{196} &= \begin{bmatrix} 1012 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 2, 1, 1) \\
L_{197} &= \begin{bmatrix} 1012 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 2, 2, 1) \\
L_{198} &= \begin{bmatrix} 1012 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 2, 2, 1) \\
L_{199} &= \begin{bmatrix} 1012 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 2, 2, 1) \\
L_{200} &= \begin{bmatrix} 1012 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 2, 2, 1) \\
L_{201} &= \begin{bmatrix} 1012 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 2, 3, 1) \\
L_{202} &= \begin{bmatrix} 1012 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 2, 3, 1) \\
L_{203} &= \begin{bmatrix} 1012 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 2, 3, 1) \\
L_{204} &= \begin{bmatrix} 1012 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 2, 3, 1) \\
L_{205} &= \begin{bmatrix} 1102 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 0, 1) \\
L_{206} &= \begin{bmatrix} 1102 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 1, 1, 1) \\
L_{207} &= \begin{bmatrix} 1102 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 2, 2, 1) \\
L_{208} &= \begin{bmatrix} 1102 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 3, 3, 1)
\end{aligned}$$

$$\begin{aligned}
L_{209} &= \begin{bmatrix} 1120 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 1, 1, 0) \\
L_{210} &= \begin{bmatrix} 1022 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 0, 2) \\
L_{211} &= \begin{bmatrix} 1022 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 0, 2) \\
L_{212} &= \begin{bmatrix} 1022 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 0, 2) \\
L_{213} &= \begin{bmatrix} 1022 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 0, 2) \\
L_{214} &= \begin{bmatrix} 1022 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 2, 1, 2) \\
L_{215} &= \begin{bmatrix} 1022 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 2, 1, 2) \\
L_{216} &= \begin{bmatrix} 1022 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 2, 1, 2) \\
L_{217} &= \begin{bmatrix} 1022 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 2, 1, 2) \\
L_{218} &= \begin{bmatrix} 1022 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 2, 2, 2) \\
L_{219} &= \begin{bmatrix} 1022 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 2, 2, 2) \\
L_{220} &= \begin{bmatrix} 1022 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 2, 2, 2) \\
L_{221} &= \begin{bmatrix} 1022 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 2, 2, 2) \\
L_{222} &= \begin{bmatrix} 1022 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 2, 3, 2) \\
L_{223} &= \begin{bmatrix} 1022 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 2, 3, 2) \\
L_{224} &= \begin{bmatrix} 1022 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 2, 3, 2) \\
L_{225} &= \begin{bmatrix} 1022 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 2, 3, 2) \\
L_{226} &= \begin{bmatrix} 1202 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 0, 2) \\
L_{227} &= \begin{bmatrix} 1202 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 2, 1, 2) \\
L_{228} &= \begin{bmatrix} 1202 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 3, 2, 2) \\
L_{229} &= \begin{bmatrix} 1202 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 1, 3, 2)
\end{aligned}$$

$$\begin{aligned}
L_{230} &= \begin{bmatrix} 1220 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 2, 1, 0) \\
L_{231} &= \begin{bmatrix} 1032 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 2, 0, 3) \\
L_{232} &= \begin{bmatrix} 1032 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 2, 0, 3) \\
L_{233} &= \begin{bmatrix} 1032 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 2, 0, 3) \\
L_{234} &= \begin{bmatrix} 1032 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 2, 0, 3) \\
L_{235} &= \begin{bmatrix} 1032 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 2, 1, 3) \\
L_{236} &= \begin{bmatrix} 1032 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 2, 1, 3) \\
L_{237} &= \begin{bmatrix} 1032 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 2, 1, 3) \\
L_{238} &= \begin{bmatrix} 1032 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 2, 1, 3) \\
L_{239} &= \begin{bmatrix} 1032 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 2, 2, 3) \\
L_{240} &= \begin{bmatrix} 1032 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 2, 2, 3) \\
L_{241} &= \begin{bmatrix} 1032 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 2, 2, 3) \\
L_{242} &= \begin{bmatrix} 1032 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 2, 2, 3) \\
L_{243} &= \begin{bmatrix} 1032 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 2, 3, 3) \\
L_{244} &= \begin{bmatrix} 1032 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 2, 3, 3) \\
L_{245} &= \begin{bmatrix} 1032 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 2, 3, 3) \\
L_{246} &= \begin{bmatrix} 1032 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 2, 3, 3) \\
L_{247} &= \begin{bmatrix} 1302 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 0, 0, 3) \\
L_{248} &= \begin{bmatrix} 1302 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 3, 1, 3) \\
L_{249} &= \begin{bmatrix} 1302 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 1, 2, 3) \\
L_{250} &= \begin{bmatrix} 1302 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 2, 1, 2, 3, 3)
\end{aligned}$$

$$\begin{aligned}
L_{251} &= \begin{bmatrix} 1320 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 3, 1, 0) \\
L_{252} &= \begin{bmatrix} 1003 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 0, 0) \\
L_{253} &= \begin{bmatrix} 1003 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 0, 0) \\
L_{254} &= \begin{bmatrix} 1003 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 0, 0) \\
L_{255} &= \begin{bmatrix} 1003 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 0, 0) \\
L_{256} &= \begin{bmatrix} 1003 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 1, 0) \\
L_{257} &= \begin{bmatrix} 1003 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 1, 0) \\
L_{258} &= \begin{bmatrix} 1003 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 1, 0) \\
L_{259} &= \begin{bmatrix} 1003 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 1, 0) \\
L_{260} &= \begin{bmatrix} 1003 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 2, 0) \\
L_{261} &= \begin{bmatrix} 1003 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 2, 0) \\
L_{262} &= \begin{bmatrix} 1003 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 2, 0) \\
L_{263} &= \begin{bmatrix} 1003 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 2, 0) \\
L_{264} &= \begin{bmatrix} 1003 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 3, 0) \\
L_{265} &= \begin{bmatrix} 1003 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 3, 0) \\
L_{266} &= \begin{bmatrix} 1003 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 3, 0) \\
L_{267} &= \begin{bmatrix} 1003 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 3, 0) \\
L_{268} &= \begin{bmatrix} 1003 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 0, 0) \\
L_{269} &= \begin{bmatrix} 1003 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 1, 0) \\
L_{270} &= \begin{bmatrix} 1003 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 2, 0) \\
L_{271} &= \begin{bmatrix} 1003 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 3, 0)
\end{aligned}$$



$$\begin{aligned}
L_{272} &= \begin{bmatrix} 1030 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 0, 1, 0) \\
L_{273} &= \begin{bmatrix} 1013 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 0, 1) \\
L_{274} &= \begin{bmatrix} 1013 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 0, 1) \\
L_{275} &= \begin{bmatrix} 1013 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 0, 1) \\
L_{276} &= \begin{bmatrix} 1013 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 0, 1) \\
L_{277} &= \begin{bmatrix} 1013 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 3, 1, 1) \\
L_{278} &= \begin{bmatrix} 1013 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 3, 1, 1) \\
L_{279} &= \begin{bmatrix} 1013 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 3, 1, 1) \\
L_{280} &= \begin{bmatrix} 1013 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 3, 1, 1) \\
L_{281} &= \begin{bmatrix} 1013 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 3, 2, 1) \\
L_{282} &= \begin{bmatrix} 1013 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 3, 2, 1) \\
L_{283} &= \begin{bmatrix} 1013 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 3, 2, 1) \\
L_{284} &= \begin{bmatrix} 1013 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 3, 2, 1) \\
L_{285} &= \begin{bmatrix} 1013 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 3, 3, 1) \\
L_{286} &= \begin{bmatrix} 1013 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 3, 3, 1) \\
L_{287} &= \begin{bmatrix} 1013 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 3, 3, 1) \\
L_{288} &= \begin{bmatrix} 1013 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 3, 3, 1) \\
L_{289} &= \begin{bmatrix} 1103 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 0, 1) \\
L_{290} &= \begin{bmatrix} 1103 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 1, 1, 1) \\
L_{291} &= \begin{bmatrix} 1103 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 2, 2, 1) \\
L_{292} &= \begin{bmatrix} 1103 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 3, 3, 1)
\end{aligned}$$

$$\begin{aligned}
L_{293} &= \begin{bmatrix} 1130 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 1, 1, 0) \\
L_{294} &= \begin{bmatrix} 1023 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 0, 2) \\
L_{295} &= \begin{bmatrix} 1023 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 0, 2) \\
L_{296} &= \begin{bmatrix} 1023 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 0, 2) \\
L_{297} &= \begin{bmatrix} 1023 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 0, 2) \\
L_{298} &= \begin{bmatrix} 1023 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 3, 1, 2) \\
L_{299} &= \begin{bmatrix} 1023 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 3, 1, 2) \\
L_{300} &= \begin{bmatrix} 1023 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 3, 1, 2) \\
L_{301} &= \begin{bmatrix} 1023 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 3, 1, 2) \\
L_{302} &= \begin{bmatrix} 1023 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 3, 2, 2) \\
L_{303} &= \begin{bmatrix} 1023 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 3, 2, 2) \\
L_{304} &= \begin{bmatrix} 1023 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 3, 2, 2) \\
L_{305} &= \begin{bmatrix} 1023 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 3, 2, 2) \\
L_{306} &= \begin{bmatrix} 1023 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 3, 3, 2) \\
L_{307} &= \begin{bmatrix} 1023 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 3, 3, 2) \\
L_{308} &= \begin{bmatrix} 1023 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 3, 3, 2) \\
L_{309} &= \begin{bmatrix} 1023 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 3, 3, 2) \\
L_{310} &= \begin{bmatrix} 1203 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 0, 2) \\
L_{311} &= \begin{bmatrix} 1203 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 2, 1, 2) \\
L_{312} &= \begin{bmatrix} 1203 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 3, 2, 2) \\
L_{313} &= \begin{bmatrix} 1203 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 1, 3, 2)
\end{aligned}$$

$$\begin{aligned}
L_{314} &= \begin{bmatrix} 1230 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 2, 1, 0) \\
L_{315} &= \begin{bmatrix} 1033 \\ 0100 \end{bmatrix} = \mathbf{PI}(1, 0, 0, 3, 0, 3) \\
L_{316} &= \begin{bmatrix} 1033 \\ 0110 \end{bmatrix} = \mathbf{PI}(1, 3, 1, 3, 0, 3) \\
L_{317} &= \begin{bmatrix} 1033 \\ 0120 \end{bmatrix} = \mathbf{PI}(1, 1, 2, 3, 0, 3) \\
L_{318} &= \begin{bmatrix} 1033 \\ 0130 \end{bmatrix} = \mathbf{PI}(1, 2, 3, 3, 0, 3) \\
L_{319} &= \begin{bmatrix} 1033 \\ 0101 \end{bmatrix} = \mathbf{PI}(1, 3, 0, 3, 1, 3) \\
L_{320} &= \begin{bmatrix} 1033 \\ 0111 \end{bmatrix} = \mathbf{PI}(1, 0, 1, 3, 1, 3) \\
L_{321} &= \begin{bmatrix} 1033 \\ 0121 \end{bmatrix} = \mathbf{PI}(1, 2, 2, 3, 1, 3) \\
L_{322} &= \begin{bmatrix} 1033 \\ 0131 \end{bmatrix} = \mathbf{PI}(1, 1, 3, 3, 1, 3) \\
L_{323} &= \begin{bmatrix} 1033 \\ 0102 \end{bmatrix} = \mathbf{PI}(1, 1, 0, 3, 2, 3) \\
L_{324} &= \begin{bmatrix} 1033 \\ 0112 \end{bmatrix} = \mathbf{PI}(1, 2, 1, 3, 2, 3) \\
L_{325} &= \begin{bmatrix} 1033 \\ 0122 \end{bmatrix} = \mathbf{PI}(1, 0, 2, 3, 2, 3) \\
L_{326} &= \begin{bmatrix} 1033 \\ 0132 \end{bmatrix} = \mathbf{PI}(1, 3, 3, 3, 2, 3) \\
L_{327} &= \begin{bmatrix} 1033 \\ 0103 \end{bmatrix} = \mathbf{PI}(1, 2, 0, 3, 3, 3) \\
L_{328} &= \begin{bmatrix} 1033 \\ 0113 \end{bmatrix} = \mathbf{PI}(1, 1, 1, 3, 3, 3) \\
L_{329} &= \begin{bmatrix} 1033 \\ 0123 \end{bmatrix} = \mathbf{PI}(1, 3, 2, 3, 3, 3) \\
L_{330} &= \begin{bmatrix} 1033 \\ 0133 \end{bmatrix} = \mathbf{PI}(1, 0, 3, 3, 3, 3) \\
L_{331} &= \begin{bmatrix} 1303 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 0, 0, 3) \\
L_{332} &= \begin{bmatrix} 1303 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 3, 1, 3) \\
L_{333} &= \begin{bmatrix} 1303 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 1, 2, 3) \\
L_{334} &= \begin{bmatrix} 1303 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 3, 1, 2, 3, 3)
\end{aligned}$$

$$\begin{aligned}
L_{335} &= \begin{bmatrix} 1330 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 3, 1, 0) \\
L_{336} &= \begin{bmatrix} 0100 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 0, 0, 1) \\
L_{337} &= \begin{bmatrix} 0100 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 1, 0, 1) \\
L_{338} &= \begin{bmatrix} 0100 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 2, 0, 1) \\
L_{339} &= \begin{bmatrix} 0100 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 3, 0, 1) \\
L_{340} &= \begin{bmatrix} 0100 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 0, 0, 1, 0, 0) \\
L_{341} &= \begin{bmatrix} 0101 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 0, 0, 1) \\
L_{342} &= \begin{bmatrix} 0101 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 1, 0, 1) \\
L_{343} &= \begin{bmatrix} 0101 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 2, 0, 1) \\
L_{344} &= \begin{bmatrix} 0101 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 3, 0, 1) \\
L_{345} &= \begin{bmatrix} 0110 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 1, 0, 0) \\
L_{346} &= \begin{bmatrix} 0102 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 0, 0, 1) \\
L_{347} &= \begin{bmatrix} 0102 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 1, 0, 1) \\
L_{348} &= \begin{bmatrix} 0102 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 2, 0, 1) \\
L_{349} &= \begin{bmatrix} 0102 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 3, 0, 1) \\
L_{350} &= \begin{bmatrix} 0120 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 2, 0, 1, 0, 0) \\
L_{351} &= \begin{bmatrix} 0103 \\ 0010 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 0, 0, 1) \\
L_{352} &= \begin{bmatrix} 0103 \\ 0011 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 1, 0, 1) \\
L_{353} &= \begin{bmatrix} 0103 \\ 0012 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 2, 0, 1) \\
L_{354} &= \begin{bmatrix} 0103 \\ 0013 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 3, 0, 1) \\
L_{355} &= \begin{bmatrix} 0130 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 3, 0, 1, 0, 0)
\end{aligned}$$

$$L_{356} = \begin{bmatrix} 0010 \\ 0001 \end{bmatrix} = \mathbf{PI}(0, 1, 0, 0, 0, 0)$$

Lines sorted by Pluecker coordinates

$$0 = \mathbf{PI}(1, 0, 0, 0, 0, 0) = L_0 = \begin{bmatrix} 1000 \\ 0100 \end{bmatrix}$$

$$1 = \mathbf{PI}(0, 1, 0, 0, 0, 0) = L_{356} = \begin{bmatrix} 0010 \\ 0001 \end{bmatrix}$$

$$2 = \mathbf{PI}(0, 0, 1, 0, 0, 0) = L_{16} = \begin{bmatrix} 1000 \\ 0010 \end{bmatrix}$$

$$3 = \mathbf{PI}(0, 0, 0, 1, 0, 0) = L_{340} = \begin{bmatrix} 0100 \\ 0001 \end{bmatrix}$$

$$4 = \mathbf{PI}(0, 0, 0, 0, 1, 0) = L_{20} = \begin{bmatrix} 1000 \\ 0001 \end{bmatrix}$$

$$5 = \mathbf{PI}(0, 0, 0, 0, 0, 1) = L_{336} = \begin{bmatrix} 0100 \\ 0010 \end{bmatrix}$$

$$6 = \mathbf{PI}(1, 0, 1, 0, 0, 0) = L_1 = \begin{bmatrix} 1000 \\ 0110 \end{bmatrix}$$

$$7 = \mathbf{PI}(2, 0, 1, 0, 0, 0) = L_3 = \begin{bmatrix} 1000 \\ 0130 \end{bmatrix}$$

$$8 = \mathbf{PI}(3, 0, 1, 0, 0, 0) = L_2 = \begin{bmatrix} 1000 \\ 0120 \end{bmatrix}$$

$$9 = \mathbf{PI}(0, 1, 1, 0, 0, 0) = L_{100} = \begin{bmatrix} 1001 \\ 0010 \end{bmatrix}$$

$$10 = \mathbf{PI}(0, 2, 1, 0, 0, 0) = L_{184} = \begin{bmatrix} 1002 \\ 0010 \end{bmatrix}$$

$$11 = \mathbf{PI}(0, 3, 1, 0, 0, 0) = L_{268} = \begin{bmatrix} 1003 \\ 0010 \end{bmatrix}$$

$$12 = \mathbf{PI}(1, 0, 0, 1, 0, 0) = L_{84} = \begin{bmatrix} 1001 \\ 0100 \end{bmatrix}$$

$$13 = \mathbf{PI}(2, 0, 0, 1, 0, 0) = L_{252} = \begin{bmatrix} 1003 \\ 0100 \end{bmatrix}$$

$$14 = \mathbf{PI}(3, 0, 0, 1, 0, 0) = L_{168} = \begin{bmatrix} 1002 \\ 0100 \end{bmatrix}$$

$$15 = \mathbf{PI}(0, 1, 0, 1, 0, 0) = L_{345} = \begin{bmatrix} 0110 \\ 0001 \end{bmatrix}$$

$$16 = \mathbf{PI}(0, 2, 0, 1, 0, 0) = L_{350} = \begin{bmatrix} 0120 \\ 0001 \end{bmatrix}$$

$$17 = \mathbf{PI}(0, 3, 0, 1, 0, 0) = L_{355} = \begin{bmatrix} 0130 \\ 0001 \end{bmatrix}$$

$$18 = \mathbf{PI}(1, 1, 1, 1, 0, 0) = L_{85} = \begin{bmatrix} 1001 \\ 0110 \end{bmatrix}$$

$$19 = \mathbf{PI}(3, 2, 1, 1, 0, 0) = L_{170} = \begin{bmatrix} 1002 \\ 0120 \end{bmatrix}$$

$$\begin{aligned}
20 &= \mathbf{PI}(2, 3, 1, 1, 0, 0) = L_{255} = \begin{bmatrix} 1003 \\ 0130 \end{bmatrix} \\
21 &= \mathbf{PI}(2, 1, 2, 1, 0, 0) = L_{253} = \begin{bmatrix} 1003 \\ 0110 \end{bmatrix} \\
22 &= \mathbf{PI}(1, 2, 2, 1, 0, 0) = L_{86} = \begin{bmatrix} 1001 \\ 0120 \end{bmatrix} \\
23 &= \mathbf{PI}(3, 3, 2, 1, 0, 0) = L_{171} = \begin{bmatrix} 1002 \\ 0130 \end{bmatrix} \\
24 &= \mathbf{PI}(3, 1, 3, 1, 0, 0) = L_{169} = \begin{bmatrix} 1002 \\ 0110 \end{bmatrix} \\
25 &= \mathbf{PI}(2, 2, 3, 1, 0, 0) = L_{254} = \begin{bmatrix} 1003 \\ 0120 \end{bmatrix} \\
26 &= \mathbf{PI}(1, 3, 3, 1, 0, 0) = L_{87} = \begin{bmatrix} 1001 \\ 0130 \end{bmatrix} \\
27 &= \mathbf{PI}(1, 0, 0, 0, 1, 0) = L_4 = \begin{bmatrix} 1000 \\ 0101 \end{bmatrix} \\
28 &= \mathbf{PI}(2, 0, 0, 0, 1, 0) = L_{12} = \begin{bmatrix} 1000 \\ 0103 \end{bmatrix} \\
29 &= \mathbf{PI}(3, 0, 0, 0, 1, 0) = L_8 = \begin{bmatrix} 1000 \\ 0102 \end{bmatrix} \\
30 &= \mathbf{PI}(0, 1, 0, 0, 1, 0) = L_{104} = \begin{bmatrix} 1010 \\ 0001 \end{bmatrix} \\
31 &= \mathbf{PI}(0, 2, 0, 0, 1, 0) = L_{188} = \begin{bmatrix} 1020 \\ 0001 \end{bmatrix} \\
32 &= \mathbf{PI}(0, 3, 0, 0, 1, 0) = L_{272} = \begin{bmatrix} 1030 \\ 0001 \end{bmatrix} \\
33 &= \mathbf{PI}(0, 0, 1, 0, 1, 0) = L_{17} = \begin{bmatrix} 1000 \\ 0011 \end{bmatrix} \\
34 &= \mathbf{PI}(1, 0, 1, 0, 1, 0) = L_5 = \begin{bmatrix} 1000 \\ 0111 \end{bmatrix} \\
35 &= \mathbf{PI}(2, 0, 1, 0, 1, 0) = L_{15} = \begin{bmatrix} 1000 \\ 0133 \end{bmatrix} \\
36 &= \mathbf{PI}(3, 0, 1, 0, 1, 0) = L_{10} = \begin{bmatrix} 1000 \\ 0122 \end{bmatrix} \\
37 &= \mathbf{PI}(0, 1, 1, 0, 1, 0) = L_{101} = \begin{bmatrix} 1001 \\ 0011 \end{bmatrix} \\
38 &= \mathbf{PI}(0, 2, 1, 0, 1, 0) = L_{185} = \begin{bmatrix} 1002 \\ 0011 \end{bmatrix} \\
39 &= \mathbf{PI}(0, 3, 1, 0, 1, 0) = L_{269} = \begin{bmatrix} 1003 \\ 0011 \end{bmatrix} \\
40 &= \mathbf{PI}(0, 0, 2, 0, 1, 0) = L_{19} = \begin{bmatrix} 1000 \\ 0013 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
41 &= \mathbf{PI}(1, 0, 2, 0, 1, 0) = L_6 = \begin{bmatrix} 1000 \\ 0121 \end{bmatrix} \\
42 &= \mathbf{PI}(2, 0, 2, 0, 1, 0) = L_{13} = \begin{bmatrix} 1000 \\ 0113 \end{bmatrix} \\
43 &= \mathbf{PI}(3, 0, 2, 0, 1, 0) = L_{11} = \begin{bmatrix} 1000 \\ 0132 \end{bmatrix} \\
44 &= \mathbf{PI}(0, 1, 2, 0, 1, 0) = L_{271} = \begin{bmatrix} 1003 \\ 0013 \end{bmatrix} \\
45 &= \mathbf{PI}(0, 2, 2, 0, 1, 0) = L_{103} = \begin{bmatrix} 1001 \\ 0013 \end{bmatrix} \\
46 &= \mathbf{PI}(0, 3, 2, 0, 1, 0) = L_{187} = \begin{bmatrix} 1002 \\ 0013 \end{bmatrix} \\
47 &= \mathbf{PI}(0, 0, 3, 0, 1, 0) = L_{18} = \begin{bmatrix} 1000 \\ 0012 \end{bmatrix} \\
48 &= \mathbf{PI}(1, 0, 3, 0, 1, 0) = L_7 = \begin{bmatrix} 1000 \\ 0131 \end{bmatrix} \\
49 &= \mathbf{PI}(2, 0, 3, 0, 1, 0) = L_{14} = \begin{bmatrix} 1000 \\ 0123 \end{bmatrix} \\
50 &= \mathbf{PI}(3, 0, 3, 0, 1, 0) = L_9 = \begin{bmatrix} 1000 \\ 0112 \end{bmatrix} \\
51 &= \mathbf{PI}(0, 1, 3, 0, 1, 0) = L_{186} = \begin{bmatrix} 1002 \\ 0012 \end{bmatrix} \\
52 &= \mathbf{PI}(0, 2, 3, 0, 1, 0) = L_{270} = \begin{bmatrix} 1003 \\ 0012 \end{bmatrix} \\
53 &= \mathbf{PI}(0, 3, 3, 0, 1, 0) = L_{102} = \begin{bmatrix} 1001 \\ 0012 \end{bmatrix} \\
54 &= \mathbf{PI}(0, 0, 0, 1, 1, 0) = L_{41} = \begin{bmatrix} 1100 \\ 0001 \end{bmatrix} \\
55 &= \mathbf{PI}(1, 0, 0, 1, 1, 0) = L_{88} = \begin{bmatrix} 1001 \\ 0101 \end{bmatrix} \\
56 &= \mathbf{PI}(2, 0, 0, 1, 1, 0) = L_{264} = \begin{bmatrix} 1003 \\ 0103 \end{bmatrix} \\
57 &= \mathbf{PI}(3, 0, 0, 1, 1, 0) = L_{176} = \begin{bmatrix} 1002 \\ 0102 \end{bmatrix} \\
58 &= \mathbf{PI}(0, 1, 0, 1, 1, 0) = L_{125} = \begin{bmatrix} 1110 \\ 0001 \end{bmatrix} \\
59 &= \mathbf{PI}(0, 2, 0, 1, 1, 0) = L_{209} = \begin{bmatrix} 1120 \\ 0001 \end{bmatrix} \\
60 &= \mathbf{PI}(0, 3, 0, 1, 1, 0) = L_{293} = \begin{bmatrix} 1130 \\ 0001 \end{bmatrix} \\
61 &= \mathbf{PI}(1, 1, 1, 1, 1, 0) = L_{89} = \begin{bmatrix} 1001 \\ 0111 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
62 &= \mathbf{PI}(3, 2, 1, 1, 1, 0) = L_{178} = \begin{bmatrix} 1002 \\ 0122 \end{bmatrix} \\
63 &= \mathbf{PI}(2, 3, 1, 1, 1, 0) = L_{267} = \begin{bmatrix} 1003 \\ 0133 \end{bmatrix} \\
64 &= \mathbf{PI}(2, 1, 2, 1, 1, 0) = L_{265} = \begin{bmatrix} 1003 \\ 0113 \end{bmatrix} \\
65 &= \mathbf{PI}(1, 2, 2, 1, 1, 0) = L_{90} = \begin{bmatrix} 1001 \\ 0121 \end{bmatrix} \\
66 &= \mathbf{PI}(3, 3, 2, 1, 1, 0) = L_{179} = \begin{bmatrix} 1002 \\ 0132 \end{bmatrix} \\
67 &= \mathbf{PI}(3, 1, 3, 1, 1, 0) = L_{177} = \begin{bmatrix} 1002 \\ 0112 \end{bmatrix} \\
68 &= \mathbf{PI}(2, 2, 3, 1, 1, 0) = L_{266} = \begin{bmatrix} 1003 \\ 0123 \end{bmatrix} \\
69 &= \mathbf{PI}(1, 3, 3, 1, 1, 0) = L_{91} = \begin{bmatrix} 1001 \\ 0131 \end{bmatrix} \\
70 &= \mathbf{PI}(0, 0, 0, 2, 1, 0) = L_{62} = \begin{bmatrix} 1200 \\ 0001 \end{bmatrix} \\
71 &= \mathbf{PI}(1, 0, 0, 2, 1, 0) = L_{172} = \begin{bmatrix} 1002 \\ 0101 \end{bmatrix} \\
72 &= \mathbf{PI}(2, 0, 0, 2, 1, 0) = L_{96} = \begin{bmatrix} 1001 \\ 0103 \end{bmatrix} \\
73 &= \mathbf{PI}(3, 0, 0, 2, 1, 0) = L_{260} = \begin{bmatrix} 1003 \\ 0102 \end{bmatrix} \\
74 &= \mathbf{PI}(0, 1, 0, 2, 1, 0) = L_{146} = \begin{bmatrix} 1210 \\ 0001 \end{bmatrix} \\
75 &= \mathbf{PI}(0, 2, 0, 2, 1, 0) = L_{230} = \begin{bmatrix} 1220 \\ 0001 \end{bmatrix} \\
76 &= \mathbf{PI}(0, 3, 0, 2, 1, 0) = L_{314} = \begin{bmatrix} 1230 \\ 0001 \end{bmatrix} \\
77 &= \mathbf{PI}(2, 1, 1, 2, 1, 0) = L_{99} = \begin{bmatrix} 1001 \\ 0133 \end{bmatrix} \\
78 &= \mathbf{PI}(1, 2, 1, 2, 1, 0) = L_{173} = \begin{bmatrix} 1002 \\ 0111 \end{bmatrix} \\
79 &= \mathbf{PI}(3, 3, 1, 2, 1, 0) = L_{262} = \begin{bmatrix} 1003 \\ 0122 \end{bmatrix} \\
80 &= \mathbf{PI}(3, 1, 2, 2, 1, 0) = L_{263} = \begin{bmatrix} 1003 \\ 0132 \end{bmatrix} \\
81 &= \mathbf{PI}(2, 2, 2, 2, 1, 0) = L_{97} = \begin{bmatrix} 1001 \\ 0113 \end{bmatrix} \\
82 &= \mathbf{PI}(1, 3, 2, 2, 1, 0) = L_{174} = \begin{bmatrix} 1002 \\ 0121 \end{bmatrix}
\end{aligned}$$



$$\begin{aligned}
83 &= \mathbf{PI}(1, 1, 3, 2, 1, 0) = L_{175} = \begin{bmatrix} 1002 \\ 0131 \end{bmatrix} \\
84 &= \mathbf{PI}(3, 2, 3, 2, 1, 0) = L_{261} = \begin{bmatrix} 1003 \\ 0112 \end{bmatrix} \\
85 &= \mathbf{PI}(2, 3, 3, 2, 1, 0) = L_{98} = \begin{bmatrix} 1001 \\ 0123 \end{bmatrix} \\
86 &= \mathbf{PI}(0, 0, 0, 3, 1, 0) = L_{83} = \begin{bmatrix} 1300 \\ 0001 \end{bmatrix} \\
87 &= \mathbf{PI}(1, 0, 0, 3, 1, 0) = L_{256} = \begin{bmatrix} 1003 \\ 0101 \end{bmatrix} \\
88 &= \mathbf{PI}(2, 0, 0, 3, 1, 0) = L_{180} = \begin{bmatrix} 1002 \\ 0103 \end{bmatrix} \\
89 &= \mathbf{PI}(3, 0, 0, 3, 1, 0) = L_{92} = \begin{bmatrix} 1001 \\ 0102 \end{bmatrix} \\
90 &= \mathbf{PI}(0, 1, 0, 3, 1, 0) = L_{167} = \begin{bmatrix} 1310 \\ 0001 \end{bmatrix} \\
91 &= \mathbf{PI}(0, 2, 0, 3, 1, 0) = L_{251} = \begin{bmatrix} 1320 \\ 0001 \end{bmatrix} \\
92 &= \mathbf{PI}(0, 3, 0, 3, 1, 0) = L_{335} = \begin{bmatrix} 1330 \\ 0001 \end{bmatrix} \\
93 &= \mathbf{PI}(3, 1, 1, 3, 1, 0) = L_{94} = \begin{bmatrix} 1001 \\ 0122 \end{bmatrix} \\
94 &= \mathbf{PI}(2, 2, 1, 3, 1, 0) = L_{183} = \begin{bmatrix} 1002 \\ 0133 \end{bmatrix} \\
95 &= \mathbf{PI}(1, 3, 1, 3, 1, 0) = L_{257} = \begin{bmatrix} 1003 \\ 0111 \end{bmatrix} \\
96 &= \mathbf{PI}(1, 1, 2, 3, 1, 0) = L_{258} = \begin{bmatrix} 1003 \\ 0121 \end{bmatrix} \\
97 &= \mathbf{PI}(3, 2, 2, 3, 1, 0) = L_{95} = \begin{bmatrix} 1001 \\ 0132 \end{bmatrix} \\
98 &= \mathbf{PI}(2, 3, 2, 3, 1, 0) = L_{181} = \begin{bmatrix} 1002 \\ 0113 \end{bmatrix} \\
99 &= \mathbf{PI}(2, 1, 3, 3, 1, 0) = L_{182} = \begin{bmatrix} 1002 \\ 0123 \end{bmatrix} \\
100 &= \mathbf{PI}(1, 2, 3, 3, 1, 0) = L_{259} = \begin{bmatrix} 1003 \\ 0131 \end{bmatrix} \\
101 &= \mathbf{PI}(3, 3, 3, 3, 1, 0) = L_{93} = \begin{bmatrix} 1001 \\ 0112 \end{bmatrix} \\
102 &= \mathbf{PI}(1, 0, 0, 0, 0, 1) = L_{21} = \begin{bmatrix} 1010 \\ 0100 \end{bmatrix} \\
103 &= \mathbf{PI}(2, 0, 0, 0, 0, 1) = L_{63} = \begin{bmatrix} 1030 \\ 0100 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
104 &= \mathbf{PI}(3, 0, 0, 0, 0, 1) = L_{42} = \begin{bmatrix} 1020 \\ 0100 \end{bmatrix} \\
105 &= \mathbf{PI}(0, 1, 0, 0, 0, 1) = L_{341} = \begin{bmatrix} 0101 \\ 0010 \end{bmatrix} \\
106 &= \mathbf{PI}(0, 2, 0, 0, 0, 1) = L_{346} = \begin{bmatrix} 0102 \\ 0010 \end{bmatrix} \\
107 &= \mathbf{PI}(0, 3, 0, 0, 0, 1) = L_{351} = \begin{bmatrix} 0103 \\ 0010 \end{bmatrix} \\
108 &= \mathbf{PI}(0, 0, 1, 0, 0, 1) = L_{37} = \begin{bmatrix} 1100 \\ 0010 \end{bmatrix} \\
109 &= \mathbf{PI}(1, 0, 1, 0, 0, 1) = L_{22} = \begin{bmatrix} 1010 \\ 0110 \end{bmatrix} \\
110 &= \mathbf{PI}(2, 0, 1, 0, 0, 1) = L_{66} = \begin{bmatrix} 1030 \\ 0130 \end{bmatrix} \\
111 &= \mathbf{PI}(3, 0, 1, 0, 0, 1) = L_{44} = \begin{bmatrix} 1020 \\ 0120 \end{bmatrix} \\
112 &= \mathbf{PI}(0, 1, 1, 0, 0, 1) = L_{121} = \begin{bmatrix} 1101 \\ 0010 \end{bmatrix} \\
113 &= \mathbf{PI}(0, 2, 1, 0, 0, 1) = L_{205} = \begin{bmatrix} 1102 \\ 0010 \end{bmatrix} \\
114 &= \mathbf{PI}(0, 3, 1, 0, 0, 1) = L_{289} = \begin{bmatrix} 1103 \\ 0010 \end{bmatrix} \\
115 &= \mathbf{PI}(0, 0, 2, 0, 0, 1) = L_{79} = \begin{bmatrix} 1300 \\ 0010 \end{bmatrix} \\
116 &= \mathbf{PI}(1, 0, 2, 0, 0, 1) = L_{23} = \begin{bmatrix} 1010 \\ 0120 \end{bmatrix} \\
117 &= \mathbf{PI}(2, 0, 2, 0, 0, 1) = L_{64} = \begin{bmatrix} 1030 \\ 0110 \end{bmatrix} \\
118 &= \mathbf{PI}(3, 0, 2, 0, 0, 1) = L_{45} = \begin{bmatrix} 1020 \\ 0130 \end{bmatrix} \\
119 &= \mathbf{PI}(0, 1, 2, 0, 0, 1) = L_{331} = \begin{bmatrix} 1303 \\ 0010 \end{bmatrix} \\
120 &= \mathbf{PI}(0, 2, 2, 0, 0, 1) = L_{163} = \begin{bmatrix} 1301 \\ 0010 \end{bmatrix} \\
121 &= \mathbf{PI}(0, 3, 2, 0, 0, 1) = L_{247} = \begin{bmatrix} 1302 \\ 0010 \end{bmatrix} \\
122 &= \mathbf{PI}(0, 0, 3, 0, 0, 1) = L_{58} = \begin{bmatrix} 1200 \\ 0010 \end{bmatrix} \\
123 &= \mathbf{PI}(1, 0, 3, 0, 0, 1) = L_{24} = \begin{bmatrix} 1010 \\ 0130 \end{bmatrix} \\
124 &= \mathbf{PI}(2, 0, 3, 0, 0, 1) = L_{65} = \begin{bmatrix} 1030 \\ 0120 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
125 &= \mathbf{PI}(3, 0, 3, 0, 0, 1) = L_{43} = \begin{bmatrix} 1020 \\ 0110 \end{bmatrix} \\
126 &= \mathbf{PI}(0, 1, 3, 0, 0, 1) = L_{226} = \begin{bmatrix} 1202 \\ 0010 \end{bmatrix} \\
127 &= \mathbf{PI}(0, 2, 3, 0, 0, 1) = L_{310} = \begin{bmatrix} 1203 \\ 0010 \end{bmatrix} \\
128 &= \mathbf{PI}(0, 3, 3, 0, 0, 1) = L_{142} = \begin{bmatrix} 1201 \\ 0010 \end{bmatrix} \\
129 &= \mathbf{PI}(0, 0, 0, 1, 0, 1) = L_{337} = \begin{bmatrix} 0100 \\ 0011 \end{bmatrix} \\
130 &= \mathbf{PI}(1, 0, 0, 1, 0, 1) = L_{105} = \begin{bmatrix} 1011 \\ 0100 \end{bmatrix} \\
131 &= \mathbf{PI}(2, 0, 0, 1, 0, 1) = L_{315} = \begin{bmatrix} 1033 \\ 0100 \end{bmatrix} \\
132 &= \mathbf{PI}(3, 0, 0, 1, 0, 1) = L_{210} = \begin{bmatrix} 1022 \\ 0100 \end{bmatrix} \\
133 &= \mathbf{PI}(0, 1, 0, 1, 0, 1) = L_{342} = \begin{bmatrix} 0101 \\ 0011 \end{bmatrix} \\
134 &= \mathbf{PI}(0, 2, 0, 1, 0, 1) = L_{347} = \begin{bmatrix} 0102 \\ 0011 \end{bmatrix} \\
135 &= \mathbf{PI}(0, 3, 0, 1, 0, 1) = L_{352} = \begin{bmatrix} 0103 \\ 0011 \end{bmatrix} \\
136 &= \mathbf{PI}(1, 1, 1, 1, 0, 1) = L_{106} = \begin{bmatrix} 1011 \\ 0110 \end{bmatrix} \\
137 &= \mathbf{PI}(3, 2, 1, 1, 0, 1) = L_{212} = \begin{bmatrix} 1022 \\ 0120 \end{bmatrix} \\
138 &= \mathbf{PI}(2, 3, 1, 1, 0, 1) = L_{318} = \begin{bmatrix} 1033 \\ 0130 \end{bmatrix} \\
139 &= \mathbf{PI}(2, 1, 2, 1, 0, 1) = L_{316} = \begin{bmatrix} 1033 \\ 0110 \end{bmatrix} \\
140 &= \mathbf{PI}(1, 2, 2, 1, 0, 1) = L_{107} = \begin{bmatrix} 1011 \\ 0120 \end{bmatrix} \\
141 &= \mathbf{PI}(3, 3, 2, 1, 0, 1) = L_{213} = \begin{bmatrix} 1022 \\ 0130 \end{bmatrix} \\
142 &= \mathbf{PI}(3, 1, 3, 1, 0, 1) = L_{211} = \begin{bmatrix} 1022 \\ 0110 \end{bmatrix} \\
143 &= \mathbf{PI}(2, 2, 3, 1, 0, 1) = L_{317} = \begin{bmatrix} 1033 \\ 0120 \end{bmatrix} \\
144 &= \mathbf{PI}(1, 3, 3, 1, 0, 1) = L_{108} = \begin{bmatrix} 1011 \\ 0130 \end{bmatrix} \\
145 &= \mathbf{PI}(0, 0, 0, 2, 0, 1) = L_{338} = \begin{bmatrix} 0100 \\ 0012 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
146 &= \mathbf{PI}(1, 0, 0, 2, 0, 1) = L_{189} = \begin{bmatrix} 1012 \\ 0100 \end{bmatrix} \\
147 &= \mathbf{PI}(2, 0, 0, 2, 0, 1) = L_{147} = \begin{bmatrix} 1031 \\ 0100 \end{bmatrix} \\
148 &= \mathbf{PI}(3, 0, 0, 2, 0, 1) = L_{294} = \begin{bmatrix} 1023 \\ 0100 \end{bmatrix} \\
149 &= \mathbf{PI}(0, 1, 0, 2, 0, 1) = L_{343} = \begin{bmatrix} 0101 \\ 0012 \end{bmatrix} \\
150 &= \mathbf{PI}(0, 2, 0, 2, 0, 1) = L_{348} = \begin{bmatrix} 0102 \\ 0012 \end{bmatrix} \\
151 &= \mathbf{PI}(0, 3, 0, 2, 0, 1) = L_{353} = \begin{bmatrix} 0103 \\ 0012 \end{bmatrix} \\
152 &= \mathbf{PI}(2, 1, 1, 2, 0, 1) = L_{150} = \begin{bmatrix} 1031 \\ 0130 \end{bmatrix} \\
153 &= \mathbf{PI}(1, 2, 1, 2, 0, 1) = L_{190} = \begin{bmatrix} 1012 \\ 0110 \end{bmatrix} \\
154 &= \mathbf{PI}(3, 3, 1, 2, 0, 1) = L_{296} = \begin{bmatrix} 1023 \\ 0120 \end{bmatrix} \\
155 &= \mathbf{PI}(3, 1, 2, 2, 0, 1) = L_{297} = \begin{bmatrix} 1023 \\ 0130 \end{bmatrix} \\
156 &= \mathbf{PI}(2, 2, 2, 2, 0, 1) = L_{148} = \begin{bmatrix} 1031 \\ 0110 \end{bmatrix} \\
157 &= \mathbf{PI}(1, 3, 2, 2, 0, 1) = L_{191} = \begin{bmatrix} 1012 \\ 0120 \end{bmatrix} \\
158 &= \mathbf{PI}(1, 1, 3, 2, 0, 1) = L_{192} = \begin{bmatrix} 1012 \\ 0130 \end{bmatrix} \\
159 &= \mathbf{PI}(3, 2, 3, 2, 0, 1) = L_{295} = \begin{bmatrix} 1023 \\ 0110 \end{bmatrix} \\
160 &= \mathbf{PI}(2, 3, 3, 2, 0, 1) = L_{149} = \begin{bmatrix} 1031 \\ 0120 \end{bmatrix} \\
161 &= \mathbf{PI}(0, 0, 0, 3, 0, 1) = L_{339} = \begin{bmatrix} 0100 \\ 0013 \end{bmatrix} \\
162 &= \mathbf{PI}(1, 0, 0, 3, 0, 1) = L_{273} = \begin{bmatrix} 1013 \\ 0100 \end{bmatrix} \\
163 &= \mathbf{PI}(2, 0, 0, 3, 0, 1) = L_{231} = \begin{bmatrix} 1032 \\ 0100 \end{bmatrix} \\
164 &= \mathbf{PI}(3, 0, 0, 3, 0, 1) = L_{126} = \begin{bmatrix} 1021 \\ 0100 \end{bmatrix} \\
165 &= \mathbf{PI}(0, 1, 0, 3, 0, 1) = L_{344} = \begin{bmatrix} 0101 \\ 0013 \end{bmatrix} \\
166 &= \mathbf{PI}(0, 2, 0, 3, 0, 1) = L_{349} = \begin{bmatrix} 0102 \\ 0013 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
167 &= \mathbf{PI}(0, 3, 0, 3, 0, 1) = L_{354} = \begin{bmatrix} 0103 \\ 0013 \end{bmatrix} \\
168 &= \mathbf{PI}(3, 1, 1, 3, 0, 1) = L_{128} = \begin{bmatrix} 1021 \\ 0120 \end{bmatrix} \\
169 &= \mathbf{PI}(2, 2, 1, 3, 0, 1) = L_{234} = \begin{bmatrix} 1032 \\ 0130 \end{bmatrix} \\
170 &= \mathbf{PI}(1, 3, 1, 3, 0, 1) = L_{274} = \begin{bmatrix} 1013 \\ 0110 \end{bmatrix} \\
171 &= \mathbf{PI}(1, 1, 2, 3, 0, 1) = L_{275} = \begin{bmatrix} 1013 \\ 0120 \end{bmatrix} \\
172 &= \mathbf{PI}(3, 2, 2, 3, 0, 1) = L_{129} = \begin{bmatrix} 1021 \\ 0130 \end{bmatrix} \\
173 &= \mathbf{PI}(2, 3, 2, 3, 0, 1) = L_{232} = \begin{bmatrix} 1032 \\ 0110 \end{bmatrix} \\
174 &= \mathbf{PI}(2, 1, 3, 3, 0, 1) = L_{233} = \begin{bmatrix} 1032 \\ 0120 \end{bmatrix} \\
175 &= \mathbf{PI}(1, 2, 3, 3, 0, 1) = L_{276} = \begin{bmatrix} 1013 \\ 0130 \end{bmatrix} \\
176 &= \mathbf{PI}(3, 3, 3, 3, 0, 1) = L_{127} = \begin{bmatrix} 1021 \\ 0110 \end{bmatrix} \\
177 &= \mathbf{PI}(1, 1, 0, 0, 1, 1) = L_{25} = \begin{bmatrix} 1010 \\ 0101 \end{bmatrix} \\
178 &= \mathbf{PI}(3, 2, 0, 0, 1, 1) = L_{50} = \begin{bmatrix} 1020 \\ 0102 \end{bmatrix} \\
179 &= \mathbf{PI}(2, 3, 0, 0, 1, 1) = L_{75} = \begin{bmatrix} 1030 \\ 0103 \end{bmatrix} \\
180 &= \mathbf{PI}(1, 1, 1, 0, 1, 1) = L_{26} = \begin{bmatrix} 1010 \\ 0111 \end{bmatrix} \\
181 &= \mathbf{PI}(3, 2, 1, 0, 1, 1) = L_{52} = \begin{bmatrix} 1020 \\ 0122 \end{bmatrix} \\
182 &= \mathbf{PI}(2, 3, 1, 0, 1, 1) = L_{78} = \begin{bmatrix} 1030 \\ 0133 \end{bmatrix} \\
183 &= \mathbf{PI}(1, 1, 2, 0, 1, 1) = L_{27} = \begin{bmatrix} 1010 \\ 0121 \end{bmatrix} \\
184 &= \mathbf{PI}(3, 2, 2, 0, 1, 1) = L_{53} = \begin{bmatrix} 1020 \\ 0132 \end{bmatrix} \\
185 &= \mathbf{PI}(2, 3, 2, 0, 1, 1) = L_{76} = \begin{bmatrix} 1030 \\ 0113 \end{bmatrix} \\
186 &= \mathbf{PI}(1, 1, 3, 0, 1, 1) = L_{28} = \begin{bmatrix} 1010 \\ 0131 \end{bmatrix} \\
187 &= \mathbf{PI}(3, 2, 3, 0, 1, 1) = L_{51} = \begin{bmatrix} 1020 \\ 0112 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
188 &= \mathbf{PI}(2, 3, 3, 0, 1, 1) = L_{77} = \begin{bmatrix} 1030 \\ 0123 \end{bmatrix} \\
189 &= \mathbf{PI}(1, 1, 0, 1, 1, 1) = L_{109} = \begin{bmatrix} 1011 \\ 0101 \end{bmatrix} \\
190 &= \mathbf{PI}(3, 2, 0, 1, 1, 1) = L_{218} = \begin{bmatrix} 1022 \\ 0102 \end{bmatrix} \\
191 &= \mathbf{PI}(2, 3, 0, 1, 1, 1) = L_{327} = \begin{bmatrix} 1033 \\ 0103 \end{bmatrix} \\
192 &= \mathbf{PI}(0, 0, 1, 1, 1, 1) = L_{38} = \begin{bmatrix} 1100 \\ 0011 \end{bmatrix} \\
193 &= \mathbf{PI}(1, 0, 1, 1, 1, 1) = L_{110} = \begin{bmatrix} 1011 \\ 0111 \end{bmatrix} \\
194 &= \mathbf{PI}(2, 0, 1, 1, 1, 1) = L_{330} = \begin{bmatrix} 1033 \\ 0133 \end{bmatrix} \\
195 &= \mathbf{PI}(3, 0, 1, 1, 1, 1) = L_{220} = \begin{bmatrix} 1022 \\ 0122 \end{bmatrix} \\
196 &= \mathbf{PI}(0, 1, 1, 1, 1, 1) = L_{122} = \begin{bmatrix} 1101 \\ 0011 \end{bmatrix} \\
197 &= \mathbf{PI}(0, 2, 1, 1, 1, 1) = L_{206} = \begin{bmatrix} 1102 \\ 0011 \end{bmatrix} \\
198 &= \mathbf{PI}(0, 3, 1, 1, 1, 1) = L_{290} = \begin{bmatrix} 1103 \\ 0011 \end{bmatrix} \\
199 &= \mathbf{PI}(3, 1, 2, 1, 1, 1) = L_{221} = \begin{bmatrix} 1022 \\ 0132 \end{bmatrix} \\
200 &= \mathbf{PI}(2, 2, 2, 1, 1, 1) = L_{328} = \begin{bmatrix} 1033 \\ 0113 \end{bmatrix} \\
201 &= \mathbf{PI}(1, 3, 2, 1, 1, 1) = L_{111} = \begin{bmatrix} 1011 \\ 0121 \end{bmatrix} \\
202 &= \mathbf{PI}(2, 1, 3, 1, 1, 1) = L_{329} = \begin{bmatrix} 1033 \\ 0123 \end{bmatrix} \\
203 &= \mathbf{PI}(1, 2, 3, 1, 1, 1) = L_{112} = \begin{bmatrix} 1011 \\ 0131 \end{bmatrix} \\
204 &= \mathbf{PI}(3, 3, 3, 1, 1, 1) = L_{219} = \begin{bmatrix} 1022 \\ 0112 \end{bmatrix} \\
205 &= \mathbf{PI}(1, 1, 0, 2, 1, 1) = L_{193} = \begin{bmatrix} 1012 \\ 0101 \end{bmatrix} \\
206 &= \mathbf{PI}(3, 2, 0, 2, 1, 1) = L_{302} = \begin{bmatrix} 1023 \\ 0102 \end{bmatrix} \\
207 &= \mathbf{PI}(2, 3, 0, 2, 1, 1) = L_{159} = \begin{bmatrix} 1031 \\ 0103 \end{bmatrix} \\
208 &= \mathbf{PI}(3, 1, 1, 2, 1, 1) = L_{304} = \begin{bmatrix} 1023 \\ 0122 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
209 &= \mathbf{PI}(2, 2, 1, 2, 1, 1) = L_{162} = \begin{bmatrix} 1031 \\ 0133 \end{bmatrix} \\
210 &= \mathbf{PI}(1, 3, 1, 2, 1, 1) = L_{194} = \begin{bmatrix} 1012 \\ 0111 \end{bmatrix} \\
211 &= \mathbf{PI}(2, 1, 2, 2, 1, 1) = L_{160} = \begin{bmatrix} 1031 \\ 0113 \end{bmatrix} \\
212 &= \mathbf{PI}(1, 2, 2, 2, 1, 1) = L_{195} = \begin{bmatrix} 1012 \\ 0121 \end{bmatrix} \\
213 &= \mathbf{PI}(3, 3, 2, 2, 1, 1) = L_{305} = \begin{bmatrix} 1023 \\ 0132 \end{bmatrix} \\
214 &= \mathbf{PI}(0, 0, 3, 2, 1, 1) = L_{60} = \begin{bmatrix} 1200 \\ 0012 \end{bmatrix} \\
215 &= \mathbf{PI}(1, 0, 3, 2, 1, 1) = L_{196} = \begin{bmatrix} 1012 \\ 0131 \end{bmatrix} \\
216 &= \mathbf{PI}(2, 0, 3, 2, 1, 1) = L_{161} = \begin{bmatrix} 1031 \\ 0123 \end{bmatrix} \\
217 &= \mathbf{PI}(3, 0, 3, 2, 1, 1) = L_{303} = \begin{bmatrix} 1023 \\ 0112 \end{bmatrix} \\
218 &= \mathbf{PI}(0, 1, 3, 2, 1, 1) = L_{228} = \begin{bmatrix} 1202 \\ 0012 \end{bmatrix} \\
219 &= \mathbf{PI}(0, 2, 3, 2, 1, 1) = L_{312} = \begin{bmatrix} 1203 \\ 0012 \end{bmatrix} \\
220 &= \mathbf{PI}(0, 3, 3, 2, 1, 1) = L_{144} = \begin{bmatrix} 1201 \\ 0012 \end{bmatrix} \\
221 &= \mathbf{PI}(1, 1, 0, 3, 1, 1) = L_{277} = \begin{bmatrix} 1013 \\ 0101 \end{bmatrix} \\
222 &= \mathbf{PI}(3, 2, 0, 3, 1, 1) = L_{134} = \begin{bmatrix} 1021 \\ 0102 \end{bmatrix} \\
223 &= \mathbf{PI}(2, 3, 0, 3, 1, 1) = L_{243} = \begin{bmatrix} 1032 \\ 0103 \end{bmatrix} \\
224 &= \mathbf{PI}(2, 1, 1, 3, 1, 1) = L_{246} = \begin{bmatrix} 1032 \\ 0133 \end{bmatrix} \\
225 &= \mathbf{PI}(1, 2, 1, 3, 1, 1) = L_{278} = \begin{bmatrix} 1013 \\ 0111 \end{bmatrix} \\
226 &= \mathbf{PI}(3, 3, 1, 3, 1, 1) = L_{136} = \begin{bmatrix} 1021 \\ 0122 \end{bmatrix} \\
227 &= \mathbf{PI}(0, 0, 2, 3, 1, 1) = L_{82} = \begin{bmatrix} 1300 \\ 0013 \end{bmatrix} \\
228 &= \mathbf{PI}(1, 0, 2, 3, 1, 1) = L_{279} = \begin{bmatrix} 1013 \\ 0121 \end{bmatrix} \\
229 &= \mathbf{PI}(2, 0, 2, 3, 1, 1) = L_{244} = \begin{bmatrix} 1032 \\ 0113 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
230 &= \mathbf{PI}(3, 0, 2, 3, 1, 1) = L_{137} = \begin{bmatrix} 1021 \\ 0132 \end{bmatrix} \\
231 &= \mathbf{PI}(0, 1, 2, 3, 1, 1) = L_{334} = \begin{bmatrix} 1303 \\ 0013 \end{bmatrix} \\
232 &= \mathbf{PI}(0, 2, 2, 3, 1, 1) = L_{166} = \begin{bmatrix} 1301 \\ 0013 \end{bmatrix} \\
233 &= \mathbf{PI}(0, 3, 2, 3, 1, 1) = L_{250} = \begin{bmatrix} 1302 \\ 0013 \end{bmatrix} \\
234 &= \mathbf{PI}(3, 1, 3, 3, 1, 1) = L_{135} = \begin{bmatrix} 1021 \\ 0112 \end{bmatrix} \\
235 &= \mathbf{PI}(2, 2, 3, 3, 1, 1) = L_{245} = \begin{bmatrix} 1032 \\ 0123 \end{bmatrix} \\
236 &= \mathbf{PI}(1, 3, 3, 3, 1, 1) = L_{280} = \begin{bmatrix} 1013 \\ 0131 \end{bmatrix} \\
237 &= \mathbf{PI}(2, 1, 0, 0, 2, 1) = L_{67} = \begin{bmatrix} 1030 \\ 0101 \end{bmatrix} \\
238 &= \mathbf{PI}(1, 2, 0, 0, 2, 1) = L_{29} = \begin{bmatrix} 1010 \\ 0102 \end{bmatrix} \\
239 &= \mathbf{PI}(3, 3, 0, 0, 2, 1) = L_{54} = \begin{bmatrix} 1020 \\ 0103 \end{bmatrix} \\
240 &= \mathbf{PI}(2, 1, 1, 0, 2, 1) = L_{70} = \begin{bmatrix} 1030 \\ 0131 \end{bmatrix} \\
241 &= \mathbf{PI}(1, 2, 1, 0, 2, 1) = L_{30} = \begin{bmatrix} 1010 \\ 0112 \end{bmatrix} \\
242 &= \mathbf{PI}(3, 3, 1, 0, 2, 1) = L_{56} = \begin{bmatrix} 1020 \\ 0123 \end{bmatrix} \\
243 &= \mathbf{PI}(2, 1, 2, 0, 2, 1) = L_{68} = \begin{bmatrix} 1030 \\ 0111 \end{bmatrix} \\
244 &= \mathbf{PI}(1, 2, 2, 0, 2, 1) = L_{31} = \begin{bmatrix} 1010 \\ 0122 \end{bmatrix} \\
245 &= \mathbf{PI}(3, 3, 2, 0, 2, 1) = L_{57} = \begin{bmatrix} 1020 \\ 0133 \end{bmatrix} \\
246 &= \mathbf{PI}(2, 1, 3, 0, 2, 1) = L_{69} = \begin{bmatrix} 1030 \\ 0121 \end{bmatrix} \\
247 &= \mathbf{PI}(1, 2, 3, 0, 2, 1) = L_{32} = \begin{bmatrix} 1010 \\ 0132 \end{bmatrix} \\
248 &= \mathbf{PI}(3, 3, 3, 0, 2, 1) = L_{55} = \begin{bmatrix} 1020 \\ 0113 \end{bmatrix} \\
249 &= \mathbf{PI}(2, 1, 0, 1, 2, 1) = L_{319} = \begin{bmatrix} 1033 \\ 0101 \end{bmatrix} \\
250 &= \mathbf{PI}(1, 2, 0, 1, 2, 1) = L_{113} = \begin{bmatrix} 1011 \\ 0102 \end{bmatrix}
\end{aligned}$$



$$\begin{aligned}
251 &= \mathbf{PI}(3, 3, 0, 1, 2, 1) = L_{222} = \begin{bmatrix} 1022 \\ 0103 \end{bmatrix} \\
252 &= \mathbf{PI}(3, 1, 1, 1, 2, 1) = L_{224} = \begin{bmatrix} 1022 \\ 0123 \end{bmatrix} \\
253 &= \mathbf{PI}(2, 2, 1, 1, 2, 1) = L_{322} = \begin{bmatrix} 1033 \\ 0131 \end{bmatrix} \\
254 &= \mathbf{PI}(1, 3, 1, 1, 2, 1) = L_{114} = \begin{bmatrix} 1011 \\ 0112 \end{bmatrix} \\
255 &= \mathbf{PI}(0, 0, 2, 1, 2, 1) = L_{80} = \begin{bmatrix} 1300 \\ 0011 \end{bmatrix} \\
256 &= \mathbf{PI}(1, 0, 2, 1, 2, 1) = L_{115} = \begin{bmatrix} 1011 \\ 0122 \end{bmatrix} \\
257 &= \mathbf{PI}(2, 0, 2, 1, 2, 1) = L_{320} = \begin{bmatrix} 1033 \\ 0111 \end{bmatrix} \\
258 &= \mathbf{PI}(3, 0, 2, 1, 2, 1) = L_{225} = \begin{bmatrix} 1022 \\ 0133 \end{bmatrix} \\
259 &= \mathbf{PI}(0, 1, 2, 1, 2, 1) = L_{332} = \begin{bmatrix} 1303 \\ 0011 \end{bmatrix} \\
260 &= \mathbf{PI}(0, 2, 2, 1, 2, 1) = L_{164} = \begin{bmatrix} 1301 \\ 0011 \end{bmatrix} \\
261 &= \mathbf{PI}(0, 3, 2, 1, 2, 1) = L_{248} = \begin{bmatrix} 1302 \\ 0011 \end{bmatrix} \\
262 &= \mathbf{PI}(1, 1, 3, 1, 2, 1) = L_{116} = \begin{bmatrix} 1011 \\ 0132 \end{bmatrix} \\
263 &= \mathbf{PI}(3, 2, 3, 1, 2, 1) = L_{223} = \begin{bmatrix} 1022 \\ 0113 \end{bmatrix} \\
264 &= \mathbf{PI}(2, 3, 3, 1, 2, 1) = L_{321} = \begin{bmatrix} 1033 \\ 0121 \end{bmatrix} \\
265 &= \mathbf{PI}(2, 1, 0, 2, 2, 1) = L_{151} = \begin{bmatrix} 1031 \\ 0101 \end{bmatrix} \\
266 &= \mathbf{PI}(1, 2, 0, 2, 2, 1) = L_{197} = \begin{bmatrix} 1012 \\ 0102 \end{bmatrix} \\
267 &= \mathbf{PI}(3, 3, 0, 2, 2, 1) = L_{306} = \begin{bmatrix} 1023 \\ 0103 \end{bmatrix} \\
268 &= \mathbf{PI}(0, 0, 1, 2, 2, 1) = L_{39} = \begin{bmatrix} 1100 \\ 0012 \end{bmatrix} \\
269 &= \mathbf{PI}(1, 0, 1, 2, 2, 1) = L_{198} = \begin{bmatrix} 1012 \\ 0112 \end{bmatrix} \\
270 &= \mathbf{PI}(2, 0, 1, 2, 2, 1) = L_{154} = \begin{bmatrix} 1031 \\ 0131 \end{bmatrix} \\
271 &= \mathbf{PI}(3, 0, 1, 2, 2, 1) = L_{308} = \begin{bmatrix} 1023 \\ 0123 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
272 &= \mathbf{PI}(0, 1, 1, 2, 2, 1) = L_{123} = \begin{bmatrix} 1101 \\ 0012 \end{bmatrix} \\
273 &= \mathbf{PI}(0, 2, 1, 2, 2, 1) = L_{207} = \begin{bmatrix} 1102 \\ 0012 \end{bmatrix} \\
274 &= \mathbf{PI}(0, 3, 1, 2, 2, 1) = L_{291} = \begin{bmatrix} 1103 \\ 0012 \end{bmatrix} \\
275 &= \mathbf{PI}(1, 1, 2, 2, 2, 1) = L_{199} = \begin{bmatrix} 1012 \\ 0122 \end{bmatrix} \\
276 &= \mathbf{PI}(3, 2, 2, 2, 2, 1) = L_{309} = \begin{bmatrix} 1023 \\ 0133 \end{bmatrix} \\
277 &= \mathbf{PI}(2, 3, 2, 2, 2, 1) = L_{152} = \begin{bmatrix} 1031 \\ 0111 \end{bmatrix} \\
278 &= \mathbf{PI}(3, 1, 3, 2, 2, 1) = L_{307} = \begin{bmatrix} 1023 \\ 0113 \end{bmatrix} \\
279 &= \mathbf{PI}(2, 2, 3, 2, 2, 1) = L_{153} = \begin{bmatrix} 1031 \\ 0121 \end{bmatrix} \\
280 &= \mathbf{PI}(1, 3, 3, 2, 2, 1) = L_{200} = \begin{bmatrix} 1012 \\ 0132 \end{bmatrix} \\
281 &= \mathbf{PI}(2, 1, 0, 3, 2, 1) = L_{235} = \begin{bmatrix} 1032 \\ 0101 \end{bmatrix} \\
282 &= \mathbf{PI}(1, 2, 0, 3, 2, 1) = L_{281} = \begin{bmatrix} 1013 \\ 0102 \end{bmatrix} \\
283 &= \mathbf{PI}(3, 3, 0, 3, 2, 1) = L_{138} = \begin{bmatrix} 1021 \\ 0103 \end{bmatrix} \\
284 &= \mathbf{PI}(1, 1, 1, 3, 2, 1) = L_{282} = \begin{bmatrix} 1013 \\ 0112 \end{bmatrix} \\
285 &= \mathbf{PI}(3, 2, 1, 3, 2, 1) = L_{140} = \begin{bmatrix} 1021 \\ 0123 \end{bmatrix} \\
286 &= \mathbf{PI}(2, 3, 1, 3, 2, 1) = L_{238} = \begin{bmatrix} 1032 \\ 0131 \end{bmatrix} \\
287 &= \mathbf{PI}(3, 1, 2, 3, 2, 1) = L_{141} = \begin{bmatrix} 1021 \\ 0133 \end{bmatrix} \\
288 &= \mathbf{PI}(2, 2, 2, 3, 2, 1) = L_{236} = \begin{bmatrix} 1032 \\ 0111 \end{bmatrix} \\
289 &= \mathbf{PI}(1, 3, 2, 3, 2, 1) = L_{283} = \begin{bmatrix} 1013 \\ 0122 \end{bmatrix} \\
290 &= \mathbf{PI}(0, 0, 3, 3, 2, 1) = L_{61} = \begin{bmatrix} 1200 \\ 0013 \end{bmatrix} \\
291 &= \mathbf{PI}(1, 0, 3, 3, 2, 1) = L_{284} = \begin{bmatrix} 1013 \\ 0132 \end{bmatrix} \\
292 &= \mathbf{PI}(2, 0, 3, 3, 2, 1) = L_{237} = \begin{bmatrix} 1032 \\ 0121 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
293 &= \mathbf{PI}(3, 0, 3, 3, 2, 1) = L_{139} = \begin{bmatrix} 1021 \\ 0113 \end{bmatrix} \\
294 &= \mathbf{PI}(0, 1, 3, 3, 2, 1) = L_{229} = \begin{bmatrix} 1202 \\ 0013 \end{bmatrix} \\
295 &= \mathbf{PI}(0, 2, 3, 3, 2, 1) = L_{313} = \begin{bmatrix} 1203 \\ 0013 \end{bmatrix} \\
296 &= \mathbf{PI}(0, 3, 3, 3, 2, 1) = L_{145} = \begin{bmatrix} 1201 \\ 0013 \end{bmatrix} \\
297 &= \mathbf{PI}(3, 1, 0, 0, 3, 1) = L_{46} = \begin{bmatrix} 1020 \\ 0101 \end{bmatrix} \\
298 &= \mathbf{PI}(2, 2, 0, 0, 3, 1) = L_{71} = \begin{bmatrix} 1030 \\ 0102 \end{bmatrix} \\
299 &= \mathbf{PI}(1, 3, 0, 0, 3, 1) = L_{33} = \begin{bmatrix} 1010 \\ 0103 \end{bmatrix} \\
300 &= \mathbf{PI}(3, 1, 1, 0, 3, 1) = L_{48} = \begin{bmatrix} 1020 \\ 0121 \end{bmatrix} \\
301 &= \mathbf{PI}(2, 2, 1, 0, 3, 1) = L_{74} = \begin{bmatrix} 1030 \\ 0132 \end{bmatrix} \\
302 &= \mathbf{PI}(1, 3, 1, 0, 3, 1) = L_{34} = \begin{bmatrix} 1010 \\ 0113 \end{bmatrix} \\
303 &= \mathbf{PI}(3, 1, 2, 0, 3, 1) = L_{49} = \begin{bmatrix} 1020 \\ 0131 \end{bmatrix} \\
304 &= \mathbf{PI}(2, 2, 2, 0, 3, 1) = L_{72} = \begin{bmatrix} 1030 \\ 0112 \end{bmatrix} \\
305 &= \mathbf{PI}(1, 3, 2, 0, 3, 1) = L_{35} = \begin{bmatrix} 1010 \\ 0123 \end{bmatrix} \\
306 &= \mathbf{PI}(3, 1, 3, 0, 3, 1) = L_{47} = \begin{bmatrix} 1020 \\ 0111 \end{bmatrix} \\
307 &= \mathbf{PI}(2, 2, 3, 0, 3, 1) = L_{73} = \begin{bmatrix} 1030 \\ 0122 \end{bmatrix} \\
308 &= \mathbf{PI}(1, 3, 3, 0, 3, 1) = L_{36} = \begin{bmatrix} 1010 \\ 0133 \end{bmatrix} \\
309 &= \mathbf{PI}(3, 1, 0, 1, 3, 1) = L_{214} = \begin{bmatrix} 1022 \\ 0101 \end{bmatrix} \\
310 &= \mathbf{PI}(2, 2, 0, 1, 3, 1) = L_{323} = \begin{bmatrix} 1033 \\ 0102 \end{bmatrix} \\
311 &= \mathbf{PI}(1, 3, 0, 1, 3, 1) = L_{117} = \begin{bmatrix} 1011 \\ 0103 \end{bmatrix} \\
312 &= \mathbf{PI}(2, 1, 1, 1, 3, 1) = L_{326} = \begin{bmatrix} 1033 \\ 0132 \end{bmatrix} \\
313 &= \mathbf{PI}(1, 2, 1, 1, 3, 1) = L_{118} = \begin{bmatrix} 1011 \\ 0113 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
314 &= \mathbf{PI}(3, 3, 1, 1, 3, 1) = L_{216} = \begin{bmatrix} 1022 \\ 0121 \end{bmatrix} \\
315 &= \mathbf{PI}(1, 1, 2, 1, 3, 1) = L_{119} = \begin{bmatrix} 1011 \\ 0123 \end{bmatrix} \\
316 &= \mathbf{PI}(3, 2, 2, 1, 3, 1) = L_{217} = \begin{bmatrix} 1022 \\ 0131 \end{bmatrix} \\
317 &= \mathbf{PI}(2, 3, 2, 1, 3, 1) = L_{324} = \begin{bmatrix} 1033 \\ 0112 \end{bmatrix} \\
318 &= \mathbf{PI}(0, 0, 3, 1, 3, 1) = L_{59} = \begin{bmatrix} 1200 \\ 0011 \end{bmatrix} \\
319 &= \mathbf{PI}(1, 0, 3, 1, 3, 1) = L_{120} = \begin{bmatrix} 1011 \\ 0133 \end{bmatrix} \\
320 &= \mathbf{PI}(2, 0, 3, 1, 3, 1) = L_{325} = \begin{bmatrix} 1033 \\ 0122 \end{bmatrix} \\
321 &= \mathbf{PI}(3, 0, 3, 1, 3, 1) = L_{215} = \begin{bmatrix} 1022 \\ 0111 \end{bmatrix} \\
322 &= \mathbf{PI}(0, 1, 3, 1, 3, 1) = L_{227} = \begin{bmatrix} 1202 \\ 0011 \end{bmatrix} \\
323 &= \mathbf{PI}(0, 2, 3, 1, 3, 1) = L_{311} = \begin{bmatrix} 1203 \\ 0011 \end{bmatrix} \\
324 &= \mathbf{PI}(0, 3, 3, 1, 3, 1) = L_{143} = \begin{bmatrix} 1201 \\ 0011 \end{bmatrix} \\
325 &= \mathbf{PI}(3, 1, 0, 2, 3, 1) = L_{298} = \begin{bmatrix} 1023 \\ 0101 \end{bmatrix} \\
326 &= \mathbf{PI}(2, 2, 0, 2, 3, 1) = L_{155} = \begin{bmatrix} 1031 \\ 0102 \end{bmatrix} \\
327 &= \mathbf{PI}(1, 3, 0, 2, 3, 1) = L_{201} = \begin{bmatrix} 1012 \\ 0103 \end{bmatrix} \\
328 &= \mathbf{PI}(1, 1, 1, 2, 3, 1) = L_{202} = \begin{bmatrix} 1012 \\ 0113 \end{bmatrix} \\
329 &= \mathbf{PI}(3, 2, 1, 2, 3, 1) = L_{300} = \begin{bmatrix} 1023 \\ 0121 \end{bmatrix} \\
330 &= \mathbf{PI}(2, 3, 1, 2, 3, 1) = L_{158} = \begin{bmatrix} 1031 \\ 0132 \end{bmatrix} \\
331 &= \mathbf{PI}(0, 0, 2, 2, 3, 1) = L_{81} = \begin{bmatrix} 1300 \\ 0012 \end{bmatrix} \\
332 &= \mathbf{PI}(1, 0, 2, 2, 3, 1) = L_{203} = \begin{bmatrix} 1012 \\ 0123 \end{bmatrix} \\
333 &= \mathbf{PI}(2, 0, 2, 2, 3, 1) = L_{156} = \begin{bmatrix} 1031 \\ 0112 \end{bmatrix} \\
334 &= \mathbf{PI}(3, 0, 2, 2, 3, 1) = L_{301} = \begin{bmatrix} 1023 \\ 0131 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
335 &= \mathbf{PI}(0, 1, 2, 2, 3, 1) = L_{333} = \begin{bmatrix} 1303 \\ 0012 \end{bmatrix} \\
336 &= \mathbf{PI}(0, 2, 2, 2, 3, 1) = L_{165} = \begin{bmatrix} 1301 \\ 0012 \end{bmatrix} \\
337 &= \mathbf{PI}(0, 3, 2, 2, 3, 1) = L_{249} = \begin{bmatrix} 1302 \\ 0012 \end{bmatrix} \\
338 &= \mathbf{PI}(2, 1, 3, 2, 3, 1) = L_{157} = \begin{bmatrix} 1031 \\ 0122 \end{bmatrix} \\
339 &= \mathbf{PI}(1, 2, 3, 2, 3, 1) = L_{204} = \begin{bmatrix} 1012 \\ 0133 \end{bmatrix} \\
340 &= \mathbf{PI}(3, 3, 3, 2, 3, 1) = L_{299} = \begin{bmatrix} 1023 \\ 0111 \end{bmatrix} \\
341 &= \mathbf{PI}(3, 1, 0, 3, 3, 1) = L_{130} = \begin{bmatrix} 1021 \\ 0101 \end{bmatrix} \\
342 &= \mathbf{PI}(2, 2, 0, 3, 3, 1) = L_{239} = \begin{bmatrix} 1032 \\ 0102 \end{bmatrix} \\
343 &= \mathbf{PI}(1, 3, 0, 3, 3, 1) = L_{285} = \begin{bmatrix} 1013 \\ 0103 \end{bmatrix} \\
344 &= \mathbf{PI}(0, 0, 1, 3, 3, 1) = L_{40} = \begin{bmatrix} 1100 \\ 0013 \end{bmatrix} \\
345 &= \mathbf{PI}(1, 0, 1, 3, 3, 1) = L_{286} = \begin{bmatrix} 1013 \\ 0113 \end{bmatrix} \\
346 &= \mathbf{PI}(2, 0, 1, 3, 3, 1) = L_{242} = \begin{bmatrix} 1032 \\ 0132 \end{bmatrix} \\
347 &= \mathbf{PI}(3, 0, 1, 3, 3, 1) = L_{132} = \begin{bmatrix} 1021 \\ 0121 \end{bmatrix} \\
348 &= \mathbf{PI}(0, 1, 1, 3, 3, 1) = L_{124} = \begin{bmatrix} 1101 \\ 0013 \end{bmatrix} \\
349 &= \mathbf{PI}(0, 2, 1, 3, 3, 1) = L_{208} = \begin{bmatrix} 1102 \\ 0013 \end{bmatrix} \\
350 &= \mathbf{PI}(0, 3, 1, 3, 3, 1) = L_{292} = \begin{bmatrix} 1103 \\ 0013 \end{bmatrix} \\
351 &= \mathbf{PI}(2, 1, 2, 3, 3, 1) = L_{240} = \begin{bmatrix} 1032 \\ 0112 \end{bmatrix} \\
352 &= \mathbf{PI}(1, 2, 2, 3, 3, 1) = L_{287} = \begin{bmatrix} 1013 \\ 0123 \end{bmatrix} \\
353 &= \mathbf{PI}(3, 3, 2, 3, 3, 1) = L_{133} = \begin{bmatrix} 1021 \\ 0131 \end{bmatrix} \\
354 &= \mathbf{PI}(1, 1, 3, 3, 3, 1) = L_{288} = \begin{bmatrix} 1013 \\ 0133 \end{bmatrix} \\
355 &= \mathbf{PI}(3, 2, 3, 3, 3, 1) = L_{131} = \begin{bmatrix} 1021 \\ 0111 \end{bmatrix}
\end{aligned}$$

$$356 = \mathbf{Pl}(2, 3, 3, 3, 3, 1) = L_{241} = \begin{bmatrix} 1032 \\ 0122 \end{bmatrix}$$

$\text{PG}(3, 4)$  has the following low weight Pluecker lines:

$$L_0 = \begin{bmatrix} 1000 \\ 0100 \end{bmatrix} = \mathbf{Pl}(1, 0, 0, 0, 0, 0)$$

$$L_{16} = \begin{bmatrix} 1000 \\ 0010 \end{bmatrix} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)$$

$$L_{20} = \begin{bmatrix} 1000 \\ 0001 \end{bmatrix} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)$$

$$L_{336} = \begin{bmatrix} 0100 \\ 0010 \end{bmatrix} = \mathbf{Pl}(0, 0, 0, 0, 0, 1)$$

$$L_{340} = \begin{bmatrix} 0100 \\ 0001 \end{bmatrix} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)$$

$$L_{356} = \begin{bmatrix} 0010 \\ 0001 \end{bmatrix} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)$$

## The planes of $\text{PG}(3, 4)$

$\text{PG}(3, 4)$  has 85 2-subspaces:

$$\begin{aligned}
 L_0 &= \begin{bmatrix} 1000 \\ 0100 \\ 0010 \end{bmatrix} \\
 L_1 &= \begin{bmatrix} 1000 \\ 0100 \\ 0011 \end{bmatrix} \\
 L_2 &= \begin{bmatrix} 1000 \\ 0100 \\ 0012 \end{bmatrix} \\
 L_3 &= \begin{bmatrix} 1000 \\ 0100 \\ 0013 \end{bmatrix} \\
 L_4 &= \begin{bmatrix} 1000 \\ 0100 \\ 0001 \end{bmatrix} \\
 L_5 &= \begin{bmatrix} 1000 \\ 0101 \\ 0010 \end{bmatrix} \\
 L_6 &= \begin{bmatrix} 1000 \\ 0101 \\ 0011 \end{bmatrix} \\
 L_7 &= \begin{bmatrix} 1000 \\ 0101 \\ 0012 \end{bmatrix} \\
 L_8 &= \begin{bmatrix} 1000 \\ 0101 \\ 0013 \end{bmatrix} \\
 L_9 &= \begin{bmatrix} 1000 \\ 0110 \\ 0001 \end{bmatrix} \\
 L_{10} &= \begin{bmatrix} 1000 \\ 0102 \\ 0010 \end{bmatrix} \\
 L_{11} &= \begin{bmatrix} 1000 \\ 0102 \\ 0011 \end{bmatrix} \\
 L_{12} &= \begin{bmatrix} 1000 \\ 0102 \\ 0012 \end{bmatrix}
 \end{aligned}$$

$$\begin{aligned}
L_{13} &= \begin{bmatrix} 1000 \\ 0102 \\ 0013 \end{bmatrix} \\
L_{14} &= \begin{bmatrix} 1000 \\ 0120 \\ 0001 \end{bmatrix} \\
L_{15} &= \begin{bmatrix} 1000 \\ 0103 \\ 0010 \end{bmatrix} \\
L_{16} &= \begin{bmatrix} 1000 \\ 0103 \\ 0011 \end{bmatrix} \\
L_{17} &= \begin{bmatrix} 1000 \\ 0103 \\ 0012 \end{bmatrix} \\
L_{18} &= \begin{bmatrix} 1000 \\ 0103 \\ 0013 \end{bmatrix} \\
L_{19} &= \begin{bmatrix} 1000 \\ 0130 \\ 0001 \end{bmatrix} \\
L_{20} &= \begin{bmatrix} 1000 \\ 0010 \\ 0001 \end{bmatrix} \\
L_{21} &= \begin{bmatrix} 1001 \\ 0100 \\ 0010 \end{bmatrix} \\
L_{22} &= \begin{bmatrix} 1001 \\ 0100 \\ 0011 \end{bmatrix} \\
L_{23} &= \begin{bmatrix} 1001 \\ 0100 \\ 0012 \end{bmatrix} \\
L_{24} &= \begin{bmatrix} 1001 \\ 0100 \\ 0013 \end{bmatrix} \\
L_{25} &= \begin{bmatrix} 1010 \\ 0100 \\ 0001 \end{bmatrix} \\
L_{26} &= \begin{bmatrix} 1001 \\ 0101 \\ 0010 \end{bmatrix}
\end{aligned}$$



$$\begin{aligned}
L_{27} &= \begin{bmatrix} 1001 \\ 0101 \\ 0011 \end{bmatrix} \\
L_{28} &= \begin{bmatrix} 1001 \\ 0101 \\ 0012 \end{bmatrix} \\
L_{29} &= \begin{bmatrix} 1001 \\ 0101 \\ 0013 \end{bmatrix} \\
L_{30} &= \begin{bmatrix} 1010 \\ 0110 \\ 0001 \end{bmatrix} \\
L_{31} &= \begin{bmatrix} 1001 \\ 0102 \\ 0010 \end{bmatrix} \\
L_{32} &= \begin{bmatrix} 1001 \\ 0102 \\ 0011 \end{bmatrix} \\
L_{33} &= \begin{bmatrix} 1001 \\ 0102 \\ 0012 \end{bmatrix} \\
L_{34} &= \begin{bmatrix} 1001 \\ 0102 \\ 0013 \end{bmatrix} \\
L_{35} &= \begin{bmatrix} 1010 \\ 0120 \\ 0001 \end{bmatrix} \\
L_{36} &= \begin{bmatrix} 1001 \\ 0103 \\ 0010 \end{bmatrix} \\
L_{37} &= \begin{bmatrix} 1001 \\ 0103 \\ 0011 \end{bmatrix} \\
L_{38} &= \begin{bmatrix} 1001 \\ 0103 \\ 0012 \end{bmatrix} \\
L_{39} &= \begin{bmatrix} 1001 \\ 0103 \\ 0013 \end{bmatrix} \\
L_{40} &= \begin{bmatrix} 1010 \\ 0130 \\ 0001 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
L_{41} &= \begin{bmatrix} 1100 \\ 0010 \\ 0001 \end{bmatrix} \\
L_{42} &= \begin{bmatrix} 1002 \\ 0100 \\ 0010 \end{bmatrix} \\
L_{43} &= \begin{bmatrix} 1002 \\ 0100 \\ 0011 \end{bmatrix} \\
L_{44} &= \begin{bmatrix} 1002 \\ 0100 \\ 0012 \end{bmatrix} \\
L_{45} &= \begin{bmatrix} 1002 \\ 0100 \\ 0013 \end{bmatrix} \\
L_{46} &= \begin{bmatrix} 1020 \\ 0100 \\ 0001 \end{bmatrix} \\
L_{47} &= \begin{bmatrix} 1002 \\ 0101 \\ 0010 \end{bmatrix} \\
L_{48} &= \begin{bmatrix} 1002 \\ 0101 \\ 0011 \end{bmatrix} \\
L_{49} &= \begin{bmatrix} 1002 \\ 0101 \\ 0012 \end{bmatrix} \\
L_{50} &= \begin{bmatrix} 1002 \\ 0101 \\ 0013 \end{bmatrix} \\
L_{51} &= \begin{bmatrix} 1020 \\ 0110 \\ 0001 \end{bmatrix} \\
L_{52} &= \begin{bmatrix} 1002 \\ 0102 \\ 0010 \end{bmatrix} \\
L_{53} &= \begin{bmatrix} 1002 \\ 0102 \\ 0011 \end{bmatrix} \\
L_{54} &= \begin{bmatrix} 1002 \\ 0102 \\ 0012 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
L_{55} &= \begin{bmatrix} 1002 \\ 0102 \\ 0013 \end{bmatrix} \\
L_{56} &= \begin{bmatrix} 1020 \\ 0120 \\ 0001 \end{bmatrix} \\
L_{57} &= \begin{bmatrix} 1002 \\ 0103 \\ 0010 \end{bmatrix} \\
L_{58} &= \begin{bmatrix} 1002 \\ 0103 \\ 0011 \end{bmatrix} \\
L_{59} &= \begin{bmatrix} 1002 \\ 0103 \\ 0012 \end{bmatrix} \\
L_{60} &= \begin{bmatrix} 1002 \\ 0103 \\ 0013 \end{bmatrix} \\
L_{61} &= \begin{bmatrix} 1020 \\ 0130 \\ 0001 \end{bmatrix} \\
L_{62} &= \begin{bmatrix} 1200 \\ 0010 \\ 0001 \end{bmatrix} \\
L_{63} &= \begin{bmatrix} 1003 \\ 0100 \\ 0010 \end{bmatrix} \\
L_{64} &= \begin{bmatrix} 1003 \\ 0100 \\ 0011 \end{bmatrix} \\
L_{65} &= \begin{bmatrix} 1003 \\ 0100 \\ 0012 \end{bmatrix} \\
L_{66} &= \begin{bmatrix} 1003 \\ 0100 \\ 0013 \end{bmatrix} \\
L_{67} &= \begin{bmatrix} 1030 \\ 0100 \\ 0001 \end{bmatrix} \\
L_{68} &= \begin{bmatrix} 1003 \\ 0101 \\ 0010 \end{bmatrix}
\end{aligned}$$

$$\begin{aligned}
L_{69} &= \begin{bmatrix} 1003 \\ 0101 \\ 0011 \end{bmatrix} \\
L_{70} &= \begin{bmatrix} 1003 \\ 0101 \\ 0012 \end{bmatrix} \\
L_{71} &= \begin{bmatrix} 1003 \\ 0101 \\ 0013 \end{bmatrix} \\
L_{72} &= \begin{bmatrix} 1030 \\ 0110 \\ 0001 \end{bmatrix} \\
L_{73} &= \begin{bmatrix} 1003 \\ 0102 \\ 0010 \end{bmatrix} \\
L_{74} &= \begin{bmatrix} 1003 \\ 0102 \\ 0011 \end{bmatrix} \\
L_{75} &= \begin{bmatrix} 1003 \\ 0102 \\ 0012 \end{bmatrix} \\
L_{76} &= \begin{bmatrix} 1003 \\ 0102 \\ 0013 \end{bmatrix} \\
L_{77} &= \begin{bmatrix} 1030 \\ 0120 \\ 0001 \end{bmatrix} \\
L_{78} &= \begin{bmatrix} 1003 \\ 0103 \\ 0010 \end{bmatrix} \\
L_{79} &= \begin{bmatrix} 1003 \\ 0103 \\ 0011 \end{bmatrix} \\
L_{80} &= \begin{bmatrix} 1003 \\ 0103 \\ 0012 \end{bmatrix} \\
L_{81} &= \begin{bmatrix} 1003 \\ 0103 \\ 0013 \end{bmatrix} \\
L_{82} &= \begin{bmatrix} 1030 \\ 0130 \\ 0001 \end{bmatrix}
\end{aligned}$$

$$L_{83} = \begin{bmatrix} 1300 \\ 0010 \\ 0001 \end{bmatrix}$$

$$L_{84} = \begin{bmatrix} 0100 \\ 0010 \\ 0001 \end{bmatrix}$$

# **The polynomial rings associated with $\text{PG}(3, 4)$**

$h$	monomial	vector
0	$X_0$	$(1, 0, 0, 0)$
1	$X_1$	$(0, 1, 0, 0)$
2	$X_2$	$(0, 0, 1, 0)$
3	$X_3$	$(0, 0, 0, 1)$

$h$	monomial	vector
0	$X_0^2$	$(2, 0, 0, 0)$
1	$X_1^2$	$(0, 2, 0, 0)$
2	$X_2^2$	$(0, 0, 2, 0)$
3	$X_3^2$	$(0, 0, 0, 2)$
4	$X_0X_1$	$(1, 1, 0, 0)$
5	$X_0X_2$	$(1, 0, 1, 0)$
6	$X_0X_3$	$(1, 0, 0, 1)$
7	$X_1X_2$	$(0, 1, 1, 0)$
8	$X_1X_3$	$(0, 1, 0, 1)$
9	$X_2X_3$	$(0, 0, 1, 1)$

$h$	monomial	vector
0	$X_0^3$	$(3, 0, 0, 0)$
1	$X_1^3$	$(0, 3, 0, 0)$
2	$X_2^3$	$(0, 0, 3, 0)$
3	$X_3^3$	$(0, 0, 0, 3)$
4	$X_0^2 X_1$	$(2, 1, 0, 0)$
5	$X_0^2 X_2$	$(2, 0, 1, 0)$
6	$X_0^2 X_3$	$(2, 0, 0, 1)$
7	$X_0 X_1^2$	$(1, 2, 0, 0)$
8	$X_1^2 X_2$	$(0, 2, 1, 0)$
9	$X_1^2 X_3$	$(0, 2, 0, 1)$
10	$X_0 X_2^2$	$(1, 0, 2, 0)$
11	$X_1 X_2^2$	$(0, 1, 2, 0)$
12	$X_2^2 X_3$	$(0, 0, 2, 1)$
13	$X_0 X_3^2$	$(1, 0, 0, 2)$
14	$X_1 X_3^2$	$(0, 1, 0, 2)$
15	$X_2 X_3^2$	$(0, 0, 1, 2)$
16	$X_0 X_1 X_2$	$(1, 1, 1, 0)$
17	$X_0 X_1 X_3$	$(1, 1, 0, 1)$
18	$X_0 X_2 X_3$	$(1, 0, 1, 1)$
19	$X_1 X_2 X_3$	$(0, 1, 1, 1)$



$h$	monomial	vector
0	$X_0^4$	(4, 0, 0, 0)
1	$X_1^4$	(0, 4, 0, 0)
2	$X_2^4$	(0, 0, 4, 0)
3	$X_3^4$	(0, 0, 0, 4)
4	$X_0^3 X_1$	(3, 1, 0, 0)
5	$X_0^3 X_2$	(3, 0, 1, 0)
6	$X_0^3 X_3$	(3, 0, 0, 1)
7	$X_0 X_1^3$	(1, 3, 0, 0)
8	$X_1^3 X_2$	(0, 3, 1, 0)
9	$X_1^3 X_3$	(0, 3, 0, 1)
10	$X_0 X_2^3$	(1, 0, 3, 0)
11	$X_1 X_2^3$	(0, 1, 3, 0)
12	$X_2^3 X_3$	(0, 0, 3, 1)
13	$X_0 X_3^3$	(1, 0, 0, 3)
14	$X_1 X_3^3$	(0, 1, 0, 3)
15	$X_2 X_3^3$	(0, 0, 1, 3)
16	$X_0^2 X_1^2$	(2, 2, 0, 0)
17	$X_0^2 X_2^2$	(2, 0, 2, 0)
18	$X_0^2 X_3^2$	(2, 0, 0, 2)
19	$X_1^2 X_2^2$	(0, 2, 2, 0)
20	$X_1^2 X_3^2$	(0, 2, 0, 2)
21	$X_2^2 X_3^2$	(0, 0, 2, 2)
22	$X_0^2 X_1 X_2$	(2, 1, 1, 0)
23	$X_0^2 X_1 X_3$	(2, 1, 0, 1)
24	$X_0^2 X_2 X_3$	(2, 0, 1, 1)

$h$	monomial	vector
25	$X_0X_1^2X_2$	$(1, 2, 1, 0)$
26	$X_0X_1^2X_3$	$(1, 2, 0, 1)$
27	$X_1^2X_2X_3$	$(0, 2, 1, 1)$
28	$X_0X_1X_2^2$	$(1, 1, 2, 0)$
29	$X_0X_2^2X_3$	$(1, 0, 2, 1)$
30	$X_1X_2^2X_3$	$(0, 1, 2, 1)$
31	$X_0X_1X_3^2$	$(1, 1, 0, 2)$
32	$X_0X_2X_3^2$	$(1, 0, 1, 2)$
33	$X_1X_2X_3^2$	$(0, 1, 1, 2)$
34	$X_0X_1X_2X_3$	$(1, 1, 1, 1)$