

Rank-24 over GF(16)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^3 + X_1^3 + X_2^3 = 0$$

(1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)

The point rank of the equation over GF(16) is 52

General information

Number of lines	9
Number of points	145
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	144
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17^9
Type of lines on points	$9, 1^{144}$

Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

The 9 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned} \ell_0 &= \left[\begin{array}{cccc} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{545} = \left[\begin{array}{cccc} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{545} = \mathbf{Pl}(0, 0, 0, 1, 1, 0)_{785} \\ \ell_1 &= \left[\begin{array}{cccc} 1 & \delta^5 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{3275} = \left[\begin{array}{cccc} 1 & 11 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{3275} = \mathbf{Pl}(0, 0, 0, 11, 1, 0)_{1095} \end{aligned}$$

$$\begin{aligned}
\ell_2 &= \begin{bmatrix} 1 & \delta^{10} & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3002} = \begin{bmatrix} 1 & 10 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3002} = \mathbf{Pl}(0, 0, 0, 10, 1, 0)_{1064} \\
\ell_3 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4640} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4640} = \mathbf{Pl}(0, 1, 0, 0, 1, 0)_{305} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{48320} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{48320} = \mathbf{Pl}(0, 11, 0, 0, 1, 0)_{315} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{43952} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{43952} = \mathbf{Pl}(0, 10, 0, 0, 1, 0)_{314} \\
\ell_6 &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69921} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69921} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{49} \\
\ell_7 &= \begin{bmatrix} 0 & 1 & \delta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70091} = \begin{bmatrix} 0 & 1 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70091} = \mathbf{Pl}(0, 11, 0, 1, 0, 0)_{59} \\
\ell_8 &= \begin{bmatrix} 0 & 1 & \delta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70074} = \begin{bmatrix} 0 & 1 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70074} = \mathbf{Pl}(0, 10, 0, 1, 0, 0)_{58}
\end{aligned}$$

Rank of lines: (545, 3275, 3002, 4640, 48320, 43952, 69921, 70091, 70074)

Rank of points on Klein quadric: (785, 1095, 1064, 305, 315, 314, 49, 59, 58)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 144 single points:

The single points on the surface are:

- | | |
|--|--|
| 0 : $P_5 = (1, 1, 0, 0)$ lies on line ℓ_0 | 14 : $P_{321} = (15, 2, 0, 1)$ lies on line ℓ_2 |
| 1 : $P_{14} = (10, 1, 0, 0)$ lies on line ℓ_1 | 15 : $P_{325} = (3, 3, 0, 1)$ lies on line ℓ_0 |
| 2 : $P_{15} = (11, 1, 0, 0)$ lies on line ℓ_2 | 16 : $P_{326} = (4, 3, 0, 1)$ lies on line ℓ_2 |
| 3 : $P_{20} = (1, 0, 1, 0)$ lies on line ℓ_3 | 17 : $P_{329} = (7, 3, 0, 1)$ lies on line ℓ_1 |
| 4 : $P_{29} = (10, 0, 1, 0)$ lies on line ℓ_4 | 18 : $P_{341} = (3, 4, 0, 1)$ lies on line ℓ_1 |
| 5 : $P_{30} = (11, 0, 1, 0)$ lies on line ℓ_5 | 19 : $P_{342} = (4, 4, 0, 1)$ lies on line ℓ_0 |
| 6 : $P_{35} = (0, 1, 1, 0)$ lies on line ℓ_6 | 20 : $P_{345} = (7, 4, 0, 1)$ lies on line ℓ_2 |
| 7 : $P_{179} = (0, 10, 1, 0)$ lies on line ℓ_7 | 21 : $P_{359} = (5, 5, 0, 1)$ lies on line ℓ_0 |
| 8 : $P_{195} = (0, 11, 1, 0)$ lies on line ℓ_8 | 22 : $P_{363} = (9, 5, 0, 1)$ lies on line ℓ_1 |
| 9 : $P_{291} = (1, 1, 0, 1)$ lies on line ℓ_0 | 23 : $P_{366} = (12, 5, 0, 1)$ lies on line ℓ_2 |
| 10 : $P_{300} = (10, 1, 0, 1)$ lies on line ℓ_1 | 24 : $P_{376} = (6, 6, 0, 1)$ lies on line ℓ_0 |
| 11 : $P_{301} = (11, 1, 0, 1)$ lies on line ℓ_2 | 25 : $P_{378} = (8, 6, 0, 1)$ lies on line ℓ_2 |
| 12 : $P_{308} = (2, 2, 0, 1)$ lies on line ℓ_0 | 26 : $P_{384} = (14, 6, 0, 1)$ lies on line ℓ_1 |
| 13 : $P_{319} = (13, 2, 0, 1)$ lies on line ℓ_1 | 27 : $P_{389} = (3, 7, 0, 1)$ lies on line ℓ_2 |

28 : $P_{390} = (4, 7, 0, 1)$ lies on line ℓ_1
 29 : $P_{393} = (7, 7, 0, 1)$ lies on line ℓ_0
 30 : $P_{408} = (6, 8, 0, 1)$ lies on line ℓ_1
 31 : $P_{410} = (8, 8, 0, 1)$ lies on line ℓ_0
 32 : $P_{416} = (14, 8, 0, 1)$ lies on line ℓ_2
 33 : $P_{423} = (5, 9, 0, 1)$ lies on line ℓ_2
 34 : $P_{427} = (9, 9, 0, 1)$ lies on line ℓ_0
 35 : $P_{430} = (12, 9, 0, 1)$ lies on line ℓ_1
 36 : $P_{435} = (1, 10, 0, 1)$ lies on line ℓ_2
 37 : $P_{444} = (10, 10, 0, 1)$ lies on line ℓ_0
 38 : $P_{445} = (11, 10, 0, 1)$ lies on line ℓ_1
 39 : $P_{451} = (1, 11, 0, 1)$ lies on line ℓ_1
 40 : $P_{460} = (10, 11, 0, 1)$ lies on line ℓ_2
 41 : $P_{461} = (11, 11, 0, 1)$ lies on line ℓ_0
 42 : $P_{471} = (5, 12, 0, 1)$ lies on line ℓ_1
 43 : $P_{475} = (9, 12, 0, 1)$ lies on line ℓ_2
 44 : $P_{478} = (12, 12, 0, 1)$ lies on line ℓ_0
 45 : $P_{484} = (2, 13, 0, 1)$ lies on line ℓ_2
 46 : $P_{495} = (13, 13, 0, 1)$ lies on line ℓ_0
 47 : $P_{497} = (15, 13, 0, 1)$ lies on line ℓ_1
 48 : $P_{504} = (6, 14, 0, 1)$ lies on line ℓ_2
 49 : $P_{506} = (8, 14, 0, 1)$ lies on line ℓ_1
 50 : $P_{512} = (14, 14, 0, 1)$ lies on line ℓ_0
 51 : $P_{516} = (2, 15, 0, 1)$ lies on line ℓ_1
 52 : $P_{527} = (13, 15, 0, 1)$ lies on line ℓ_2
 53 : $P_{529} = (15, 15, 0, 1)$ lies on line ℓ_0
 54 : $P_{531} = (1, 0, 1, 1)$ lies on line ℓ_3
 55 : $P_{540} = (10, 0, 1, 1)$ lies on line ℓ_4
 56 : $P_{541} = (11, 0, 1, 1)$ lies on line ℓ_5
 57 : $P_{546} = (0, 1, 1, 1)$ lies on line ℓ_6
 58 : $P_{689} = (0, 10, 1, 1)$ lies on line ℓ_7
 59 : $P_{705} = (0, 11, 1, 1)$ lies on line ℓ_8
 60 : $P_{787} = (2, 0, 2, 1)$ lies on line ℓ_3
 61 : $P_{798} = (13, 0, 2, 1)$ lies on line ℓ_4
 62 : $P_{800} = (15, 0, 2, 1)$ lies on line ℓ_5
 63 : $P_{817} = (0, 2, 2, 1)$ lies on line ℓ_6
 64 : $P_{993} = (0, 13, 2, 1)$ lies on line ℓ_7
 65 : $P_{1025} = (0, 15, 2, 1)$ lies on line ℓ_8
 66 : $P_{1044} = (3, 0, 3, 1)$ lies on line ℓ_3
 67 : $P_{1045} = (4, 0, 3, 1)$ lies on line ℓ_5
 68 : $P_{1048} = (7, 0, 3, 1)$ lies on line ℓ_4
 69 : $P_{1089} = (0, 3, 3, 1)$ lies on line ℓ_6
 70 : $P_{1105} = (0, 4, 3, 1)$ lies on line ℓ_8
 71 : $P_{1153} = (0, 7, 3, 1)$ lies on line ℓ_7
 72 : $P_{1300} = (3, 0, 4, 1)$ lies on line ℓ_4
 73 : $P_{1301} = (4, 0, 4, 1)$ lies on line ℓ_3
 74 : $P_{1304} = (7, 0, 4, 1)$ lies on line ℓ_5
 75 : $P_{1345} = (0, 3, 4, 1)$ lies on line ℓ_7
 76 : $P_{1361} = (0, 4, 4, 1)$ lies on line ℓ_6
 77 : $P_{1409} = (0, 7, 4, 1)$ lies on line ℓ_8
 78 : $P_{1558} = (5, 0, 5, 1)$ lies on line ℓ_3
 79 : $P_{1562} = (9, 0, 5, 1)$ lies on line ℓ_4
 80 : $P_{1565} = (12, 0, 5, 1)$ lies on line ℓ_5
 81 : $P_{1633} = (0, 5, 5, 1)$ lies on line ℓ_6

82 : $P_{1697} = (0, 9, 5, 1)$ lies on line ℓ_7
 83 : $P_{1745} = (0, 12, 5, 1)$ lies on line ℓ_8
 84 : $P_{1815} = (6, 0, 6, 1)$ lies on line ℓ_3
 85 : $P_{1817} = (8, 0, 6, 1)$ lies on line ℓ_5
 86 : $P_{1823} = (14, 0, 6, 1)$ lies on line ℓ_4
 87 : $P_{1905} = (0, 6, 6, 1)$ lies on line ℓ_6
 88 : $P_{1937} = (0, 8, 6, 1)$ lies on line ℓ_8
 89 : $P_{2033} = (0, 14, 6, 1)$ lies on line ℓ_7
 90 : $P_{2068} = (3, 0, 7, 1)$ lies on line ℓ_5
 91 : $P_{2069} = (4, 0, 7, 1)$ lies on line ℓ_4
 92 : $P_{2072} = (7, 0, 7, 1)$ lies on line ℓ_3
 93 : $P_{2113} = (0, 3, 7, 1)$ lies on line ℓ_8
 94 : $P_{2129} = (0, 4, 7, 1)$ lies on line ℓ_7
 95 : $P_{2177} = (0, 7, 7, 1)$ lies on line ℓ_6
 96 : $P_{2327} = (6, 0, 8, 1)$ lies on line ℓ_4
 97 : $P_{2329} = (8, 0, 8, 1)$ lies on line ℓ_3
 98 : $P_{2335} = (14, 0, 8, 1)$ lies on line ℓ_5
 99 : $P_{2417} = (0, 6, 8, 1)$ lies on line ℓ_7
 100 : $P_{2449} = (0, 8, 8, 1)$ lies on line ℓ_6
 101 : $P_{2545} = (0, 14, 8, 1)$ lies on line ℓ_8
 102 : $P_{2582} = (5, 0, 9, 1)$ lies on line ℓ_5
 103 : $P_{2586} = (9, 0, 9, 1)$ lies on line ℓ_3
 104 : $P_{2589} = (12, 0, 9, 1)$ lies on line ℓ_4
 105 : $P_{2657} = (0, 5, 9, 1)$ lies on line ℓ_8
 106 : $P_{2721} = (0, 9, 9, 1)$ lies on line ℓ_6
 107 : $P_{2769} = (0, 12, 9, 1)$ lies on line ℓ_7
 108 : $P_{2834} = (1, 0, 10, 1)$ lies on line ℓ_5
 109 : $P_{2843} = (10, 0, 10, 1)$ lies on line ℓ_3
 110 : $P_{2844} = (11, 0, 10, 1)$ lies on line ℓ_4
 111 : $P_{2849} = (0, 1, 10, 1)$ lies on line ℓ_8
 112 : $P_{2993} = (0, 10, 10, 1)$ lies on line ℓ_6
 113 : $P_{3009} = (0, 11, 10, 1)$ lies on line ℓ_7
 114 : $P_{3090} = (1, 0, 11, 1)$ lies on line ℓ_4
 115 : $P_{3099} = (10, 0, 11, 1)$ lies on line ℓ_5
 116 : $P_{3100} = (11, 0, 11, 1)$ lies on line ℓ_3
 117 : $P_{3105} = (0, 1, 11, 1)$ lies on line ℓ_7
 118 : $P_{3249} = (0, 10, 11, 1)$ lies on line ℓ_8
 119 : $P_{3265} = (0, 11, 11, 1)$ lies on line ℓ_6
 120 : $P_{3350} = (5, 0, 12, 1)$ lies on line ℓ_4
 121 : $P_{3354} = (9, 0, 12, 1)$ lies on line ℓ_5
 122 : $P_{3357} = (12, 0, 12, 1)$ lies on line ℓ_3
 123 : $P_{3425} = (0, 5, 12, 1)$ lies on line ℓ_7
 124 : $P_{3489} = (0, 9, 12, 1)$ lies on line ℓ_8
 125 : $P_{3537} = (0, 12, 12, 1)$ lies on line ℓ_6
 126 : $P_{3603} = (2, 0, 13, 1)$ lies on line ℓ_5
 127 : $P_{3614} = (13, 0, 13, 1)$ lies on line ℓ_3
 128 : $P_{3616} = (15, 0, 13, 1)$ lies on line ℓ_4
 129 : $P_{3633} = (0, 2, 13, 1)$ lies on line ℓ_8
 130 : $P_{3809} = (0, 13, 13, 1)$ lies on line ℓ_6
 131 : $P_{3841} = (0, 15, 13, 1)$ lies on line ℓ_7
 132 : $P_{3863} = (6, 0, 14, 1)$ lies on line ℓ_5
 133 : $P_{3865} = (8, 0, 14, 1)$ lies on line ℓ_4
 134 : $P_{3871} = (14, 0, 14, 1)$ lies on line ℓ_3
 135 : $P_{3953} = (0, 6, 14, 1)$ lies on line ℓ_8

136 : $P_{3985} = (0, 8, 14, 1)$ lies on line ℓ_7
137 : $P_{4081} = (0, 14, 14, 1)$ lies on line ℓ_6
138 : $P_{4115} = (2, 0, 15, 1)$ lies on line ℓ_4
139 : $P_{4126} = (13, 0, 15, 1)$ lies on line ℓ_5
140 : $P_{4128} = (15, 0, 15, 1)$ lies on line ℓ_3

141 : $P_{4145} = (0, 2, 15, 1)$ lies on line ℓ_7
142 : $P_{4321} = (0, 13, 15, 1)$ lies on line ℓ_8
143 : $P_{4353} = (0, 15, 15, 1)$ lies on line ℓ_6

The single points on the surface are:

Points on surface but on no line

The surface has 0 points not on any line:
The points on the surface but not on lines are:

Line Intersection Graph

	0	1	2	3	4	5	6	7	8
0	0	1	1	1	1	1	1	1	1
1	1	0	1	1	1	1	1	1	1
2	1	1	0	1	1	1	1	1	1
3	1	1	1	0	1	1	1	1	1
4	1	1	1	1	0	1	1	1	1
5	1	1	1	1	1	0	1	1	1
6	1	1	1	1	1	1	0	1	1
7	1	1	1	1	1	1	1	0	1
8	1	1	1	1	1	1	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 3 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 4 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 5 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_6	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 6 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_7	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 7 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_8
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 8 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

The surface has 145 points:

The points on the surface are:

0 : $P_3 = (0, 0, 0, 1)$	47 : $P_{495} = (13, 13, 0, 1)$	94 : $P_{2113} = (0, 3, 7, 1)$
1 : $P_5 = (1, 1, 0, 0)$	48 : $P_{497} = (15, 13, 0, 1)$	95 : $P_{2129} = (0, 4, 7, 1)$
2 : $P_{14} = (10, 1, 0, 0)$	49 : $P_{504} = (6, 14, 0, 1)$	96 : $P_{2177} = (0, 7, 7, 1)$
3 : $P_{15} = (11, 1, 0, 0)$	50 : $P_{506} = (8, 14, 0, 1)$	97 : $P_{2327} = (6, 0, 8, 1)$
4 : $P_{20} = (1, 0, 1, 0)$	51 : $P_{512} = (14, 14, 0, 1)$	98 : $P_{2329} = (8, 0, 8, 1)$
5 : $P_{29} = (10, 0, 1, 0)$	52 : $P_{516} = (2, 15, 0, 1)$	99 : $P_{2335} = (14, 0, 8, 1)$
6 : $P_{30} = (11, 0, 1, 0)$	53 : $P_{527} = (13, 15, 0, 1)$	100 : $P_{2417} = (0, 6, 8, 1)$
7 : $P_{35} = (0, 1, 1, 0)$	54 : $P_{529} = (15, 15, 0, 1)$	101 : $P_{2449} = (0, 8, 8, 1)$
8 : $P_{179} = (0, 10, 1, 0)$	55 : $P_{531} = (1, 0, 1, 1)$	102 : $P_{2545} = (0, 14, 8, 1)$
9 : $P_{195} = (0, 11, 1, 0)$	56 : $P_{540} = (10, 0, 1, 1)$	103 : $P_{2582} = (5, 0, 9, 1)$
10 : $P_{291} = (1, 1, 0, 1)$	57 : $P_{541} = (11, 0, 1, 1)$	104 : $P_{2586} = (9, 0, 9, 1)$
11 : $P_{300} = (10, 1, 0, 1)$	58 : $P_{546} = (0, 1, 1, 1)$	105 : $P_{2589} = (12, 0, 9, 1)$
12 : $P_{301} = (11, 1, 0, 1)$	59 : $P_{689} = (0, 10, 1, 1)$	106 : $P_{2657} = (0, 5, 9, 1)$
13 : $P_{308} = (2, 2, 0, 1)$	60 : $P_{705} = (0, 11, 1, 1)$	107 : $P_{2721} = (0, 9, 9, 1)$
14 : $P_{319} = (13, 2, 0, 1)$	61 : $P_{787} = (2, 0, 2, 1)$	108 : $P_{2769} = (0, 12, 9, 1)$
15 : $P_{321} = (15, 2, 0, 1)$	62 : $P_{798} = (13, 0, 2, 1)$	109 : $P_{2834} = (1, 0, 10, 1)$
16 : $P_{325} = (3, 3, 0, 1)$	63 : $P_{800} = (15, 0, 2, 1)$	110 : $P_{2843} = (10, 0, 10, 1)$
17 : $P_{326} = (4, 3, 0, 1)$	64 : $P_{817} = (0, 2, 2, 1)$	111 : $P_{2844} = (11, 0, 10, 1)$
18 : $P_{329} = (7, 3, 0, 1)$	65 : $P_{993} = (0, 13, 2, 1)$	112 : $P_{2849} = (0, 1, 10, 1)$
19 : $P_{341} = (3, 4, 0, 1)$	66 : $P_{1025} = (0, 15, 2, 1)$	113 : $P_{2993} = (0, 10, 10, 1)$
20 : $P_{342} = (4, 4, 0, 1)$	67 : $P_{1044} = (3, 0, 3, 1)$	114 : $P_{3009} = (0, 11, 10, 1)$
21 : $P_{345} = (7, 4, 0, 1)$	68 : $P_{1045} = (4, 0, 3, 1)$	115 : $P_{3090} = (1, 0, 11, 1)$
22 : $P_{359} = (5, 5, 0, 1)$	69 : $P_{1048} = (7, 0, 3, 1)$	116 : $P_{3099} = (10, 0, 11, 1)$
23 : $P_{363} = (9, 5, 0, 1)$	70 : $P_{1089} = (0, 3, 3, 1)$	117 : $P_{3100} = (11, 0, 11, 1)$
24 : $P_{366} = (12, 5, 0, 1)$	71 : $P_{1105} = (0, 4, 3, 1)$	118 : $P_{3105} = (0, 1, 11, 1)$
25 : $P_{376} = (6, 6, 0, 1)$	72 : $P_{1153} = (0, 7, 3, 1)$	119 : $P_{3249} = (0, 10, 11, 1)$
26 : $P_{378} = (8, 6, 0, 1)$	73 : $P_{1300} = (3, 0, 4, 1)$	120 : $P_{3265} = (0, 11, 11, 1)$
27 : $P_{384} = (14, 6, 0, 1)$	74 : $P_{1301} = (4, 0, 4, 1)$	121 : $P_{3350} = (5, 0, 12, 1)$
28 : $P_{389} = (3, 7, 0, 1)$	75 : $P_{1304} = (7, 0, 4, 1)$	122 : $P_{3354} = (9, 0, 12, 1)$
29 : $P_{390} = (4, 7, 0, 1)$	76 : $P_{1345} = (0, 3, 4, 1)$	123 : $P_{3357} = (12, 0, 12, 1)$
30 : $P_{393} = (7, 7, 0, 1)$	77 : $P_{1361} = (0, 4, 4, 1)$	124 : $P_{3425} = (0, 5, 12, 1)$
31 : $P_{408} = (6, 8, 0, 1)$	78 : $P_{1409} = (0, 7, 4, 1)$	125 : $P_{3489} = (0, 9, 12, 1)$
32 : $P_{410} = (8, 8, 0, 1)$	79 : $P_{1558} = (5, 0, 5, 1)$	126 : $P_{3537} = (0, 12, 12, 1)$
33 : $P_{416} = (14, 8, 0, 1)$	80 : $P_{1562} = (9, 0, 5, 1)$	127 : $P_{3603} = (2, 0, 13, 1)$
34 : $P_{423} = (5, 9, 0, 1)$	81 : $P_{1565} = (12, 0, 5, 1)$	128 : $P_{3614} = (13, 0, 13, 1)$
35 : $P_{427} = (9, 9, 0, 1)$	82 : $P_{1633} = (0, 5, 5, 1)$	129 : $P_{3616} = (15, 0, 13, 1)$
36 : $P_{430} = (12, 9, 0, 1)$	83 : $P_{1697} = (0, 9, 5, 1)$	130 : $P_{3633} = (0, 2, 13, 1)$
37 : $P_{435} = (1, 10, 0, 1)$	84 : $P_{1745} = (0, 12, 5, 1)$	131 : $P_{3809} = (0, 13, 13, 1)$
38 : $P_{444} = (10, 10, 0, 1)$	85 : $P_{1815} = (6, 0, 6, 1)$	132 : $P_{3841} = (0, 15, 13, 1)$
39 : $P_{445} = (11, 10, 0, 1)$	86 : $P_{1817} = (8, 0, 6, 1)$	133 : $P_{3863} = (6, 0, 14, 1)$
40 : $P_{451} = (1, 11, 0, 1)$	87 : $P_{1823} = (14, 0, 6, 1)$	134 : $P_{3865} = (8, 0, 14, 1)$
41 : $P_{460} = (10, 11, 0, 1)$	88 : $P_{1905} = (0, 6, 6, 1)$	135 : $P_{3871} = (14, 0, 14, 1)$
42 : $P_{461} = (11, 11, 0, 1)$	89 : $P_{1937} = (0, 8, 6, 1)$	136 : $P_{3953} = (0, 6, 14, 1)$
43 : $P_{471} = (5, 12, 0, 1)$	90 : $P_{2033} = (0, 14, 6, 1)$	137 : $P_{3985} = (0, 8, 14, 1)$
44 : $P_{475} = (9, 12, 0, 1)$	91 : $P_{2068} = (3, 0, 7, 1)$	138 : $P_{4081} = (0, 14, 14, 1)$
45 : $P_{478} = (12, 12, 0, 1)$	92 : $P_{2069} = (4, 0, 7, 1)$	139 : $P_{4115} = (2, 0, 15, 1)$
46 : $P_{484} = (2, 13, 0, 1)$	93 : $P_{2072} = (7, 0, 7, 1)$	140 : $P_{4126} = (13, 0, 15, 1)$

$$141 : P_{4128} = (15, 0, 15, 1)$$

$$142 : P_{4145} = (0, 2, 15, 1)$$

$$143 : P_{4321} = (0, 13, 15, 1)$$

$$144 : P_{4353} = (0, 15, 15, 1)$$