

# Rank-65617 over GF(64)

January 15, 2021

## The equation

The equation of the surface is :

$$X_1^3 + X_2^3 + X_3^3 + X_0^2 X_3 + X_0 X_1 X_2 = 0$$

( 0, 1, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0 )  
The point rank of the equation over GF(64) is 1091051653

## General information

Number of lines	21
Number of points	4481
Number of singular points	1
Number of Eckardt points	3
Number of double points	66
Number of single points	1218
Number of points off lines	3193
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$65^{21}$
Type of lines on points	$6, 3^3, 2^{66}, 1^{1218}, 0^{3193}$

## Singular Points

The surface has 1 singular points:

$$0 : P_{4163} = \mathbf{P}(1, 0, 0, 1) = \mathbf{P}(1, 0, 0, 1)$$

## The 21 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \left[ \begin{array}{cccc} 1 & 0 & 1 & \epsilon^9 \\ 0 & 1 & 1 & 0 \end{array} \right]_{12520450} = \left[ \begin{array}{cccc} 1 & 0 & 1 & 47 \\ 0 & 1 & 1 & 0 \end{array} \right]_{12520450} = \mathbf{Pl}(10, 47, 1, 47, 0, 1)_{469113}$$

$$\begin{aligned}
\ell_1 &= \begin{bmatrix} 1 & 0 & 1 & \epsilon^{18} \\ 0 & 1 & 1 & 0 \end{bmatrix}_{2933506} = \begin{bmatrix} 1 & 0 & 1 & 11 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{2933506} = \mathbf{Pl}(37, 11, 1, 11, 0, 1)_{326256} \\
\ell_2 &= \begin{bmatrix} 1 & 0 & 1 & \epsilon^{36} \\ 0 & 1 & 1 & 0 \end{bmatrix}_{9591106} = \begin{bmatrix} 1 & 0 & 1 & 36 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{9591106} = \mathbf{Pl}(46, 36, 1, 36, 0, 1)_{425490} \\
\ell_3 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \epsilon^{28} & \epsilon^{14} \end{bmatrix}_{270077} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 61 & 58 \end{bmatrix}_{270077} = \mathbf{Pl}(30, 58, 58, 30, 1, 0)_{139075} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & \epsilon^{35} & \epsilon^{21} \\ 0 & 1 & \epsilon^7 & \epsilon^{35} \end{bmatrix}_{15255413} = \begin{bmatrix} 1 & 0 & 18 & 57 \\ 0 & 1 & 35 & 18 \end{bmatrix}_{15255413} = \mathbf{Pl}(30, 58, 58, 30, 1, 1)_{778715} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \epsilon^{14} & \epsilon^7 \end{bmatrix}_{268602} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 58 & 35 \end{bmatrix}_{268602} = \mathbf{Pl}(40, 35, 35, 40, 1, 0)_{177326} \\
\ell_6 &= \begin{bmatrix} 1 & 0 & \epsilon^{49} & \epsilon^{42} \\ 0 & 1 & \epsilon^{35} & \epsilon^{49} \end{bmatrix}_{15039792} = \begin{bmatrix} 1 & 0 & 30 & 56 \\ 0 & 1 & 18 & 30 \end{bmatrix}_{15039792} = \mathbf{Pl}(40, 35, 35, 40, 1, 1)_{688824} \\
\ell_7 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \epsilon^{56} & \epsilon^{28} \end{bmatrix}_{270248} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 40 & 61 \end{bmatrix}_{270248} = \mathbf{Pl}(18, 61, 61, 18, 1, 0)_{91624} \\
\ell_8 &= \begin{bmatrix} 1 & 0 & \epsilon^7 & \epsilon^{42} \\ 0 & 1 & \epsilon^{14} & \epsilon^7 \end{bmatrix}_{15060957} = \begin{bmatrix} 1 & 0 & 35 & 56 \\ 0 & 1 & 58 & 35 \end{bmatrix}_{15060957} = \mathbf{Pl}(18, 61, 61, 18, 1, 1)_{790358} \\
\ell_9 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \epsilon^7 & \epsilon^{35} \end{bmatrix}_{267491} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 35 & 18 \end{bmatrix}_{267491} = \mathbf{Pl}(61, 18, 18, 61, 1, 0)_{259625} \\
\ell_{10} &= \begin{bmatrix} 1 & 0 & \epsilon^{56} & \epsilon^{21} \\ 0 & 1 & \epsilon^{49} & \epsilon^{56} \end{bmatrix}_{15348358} = \begin{bmatrix} 1 & 0 & 40 & 57 \\ 0 & 1 & 30 & 40 \end{bmatrix}_{15348358} = \mathbf{Pl}(61, 18, 18, 61, 1, 1)_{622506} \\
\ell_{11} &= \begin{bmatrix} 1 & 0 & \epsilon^{42} & \epsilon^{18} \\ 0 & 1 & \epsilon^{21} & 0 \end{bmatrix}_{3162417} = \begin{bmatrix} 1 & 0 & 56 & 11 \\ 0 & 1 & 57 & 0 \end{bmatrix}_{3162417} = \mathbf{Pl}(8, 12, 56, 7, 0, 1)_{313816} \\
\ell_{12} &= \begin{bmatrix} 1 & 0 & \epsilon^{42} & \epsilon^{36} \\ 0 & 1 & \epsilon^{21} & 0 \end{bmatrix}_{9820017} = \begin{bmatrix} 1 & 0 & 56 & 36 \\ 0 & 1 & 57 & 0 \end{bmatrix}_{9820017} = \mathbf{Pl}(15, 21, 56, 49, 0, 1)_{480521} \\
\ell_{13} &= \begin{bmatrix} 1 & 0 & \epsilon^{42} & \epsilon^9 \\ 0 & 1 & \epsilon^{21} & 0 \end{bmatrix}_{12749361} = \begin{bmatrix} 1 & 0 & 56 & 47 \\ 0 & 1 & 57 & 0 \end{bmatrix}_{12749361} = \mathbf{Pl}(62, 25, 56, 54, 0, 1)_{500413} \\
\ell_{14} &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & \epsilon^{36} \\ 0 & 1 & \epsilon^{42} & 0 \end{bmatrix}_{9824177} = \begin{bmatrix} 1 & 0 & 57 & 36 \\ 0 & 1 & 56 & 0 \end{bmatrix}_{9824177} = \mathbf{Pl}(33, 49, 57, 21, 0, 1)_{369470} \\
\ell_{15} &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & \epsilon^{18} \\ 0 & 1 & \epsilon^{42} & 0 \end{bmatrix}_{3166577} = \begin{bmatrix} 1 & 0 & 57 & 11 \\ 0 & 1 & 56 & 0 \end{bmatrix}_{3166577} = \mathbf{Pl}(45, 7, 57, 12, 0, 1)_{333761} \\
\ell_{16} &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & \epsilon^9 \\ 0 & 1 & \epsilon^{42} & 0 \end{bmatrix}_{12753521} = \begin{bmatrix} 1 & 0 & 57 & 47 \\ 0 & 1 & 56 & 0 \end{bmatrix}_{12753521} = \mathbf{Pl}(52, 54, 57, 25, 0, 1)_{385365} \\
\ell_{17} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \epsilon^{49} & \epsilon^{56} \end{bmatrix}_{268894} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 30 & 40 \end{bmatrix}_{268894} = \mathbf{Pl}(35, 40, 40, 35, 1, 0)_{157791} \\
\ell_{18} &= \begin{bmatrix} 1 & 0 & \epsilon^{14} & \epsilon^{21} \\ 0 & 1 & \epsilon^{28} & \epsilon^{14} \end{bmatrix}_{15424439} = \begin{bmatrix} 1 & 0 & 58 & 57 \\ 0 & 1 & 61 & 58 \end{bmatrix}_{15424439} = \mathbf{Pl}(35, 40, 40, 35, 1, 1)_{708412} \\
\ell_{19} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \epsilon^{35} & \epsilon^{49} \end{bmatrix}_{268242} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 18 & 30 \end{bmatrix}_{268242} = \mathbf{Pl}(58, 30, 30, 58, 1, 0)_{248471} \\
\ell_{20} &= \begin{bmatrix} 1 & 0 & \epsilon^{28} & \epsilon^{42} \\ 0 & 1 & \epsilon^{56} & \epsilon^{28} \end{bmatrix}_{15170789} = \begin{bmatrix} 1 & 0 & 61 & 56 \\ 0 & 1 & 40 & 61 \end{bmatrix}_{15170789} = \mathbf{Pl}(58, 30, 30, 58, 1, 1)_{669312}
\end{aligned}$$

Rank of lines: ( 12520450, 2933506, 9591106, 270077, 15255413, 268602, 15039792, 270248, 15060957, 267491, 15348358, 3162417, 9820017, 12749361, 9824177, 3166577, 12753521, 268894, 15424439, 268242, 15170789 )

Rank of points on Klein quadric: ( 469113, 326256, 425490, 139075, 778715, 177326, 688824, 91624, 790358, 259625, 622506, 313816, 480521, 500413, 369470, 333761, 385365, 157791, 708412, 248471, 669312 )

## Eckardt Points

The surface has 3 Eckardt points:

$$\begin{aligned} 0 : P_{131} &= \mathbf{P}(0, 1, 1, 0) = \mathbf{P}(0, 1, 1, 0), \\ 1 : P_{3651} &= \mathbf{P}(0, \epsilon^{42}, 1, 0) = \mathbf{P}(0, 56, 1, 0), \\ 2 : P_{3715} &= \mathbf{P}(0, \epsilon^{21}, 1, 0) = \mathbf{P}(0, 57, 1, 0). \end{aligned}$$

## Double Points

The surface has 66 Double points:

The double points on the surface are:

$$\begin{aligned} P_{111691} &= (10, 16, 26, 1) = \ell_0 \cap \ell_3 \\ P_{225291} &= (10, 63, 53, 1) = \ell_0 \cap \ell_8 \\ P_{265611} &= (10, 53, 63, 1) = \ell_0 \cap \ell_{10} \\ P_{261451} &= (10, 52, 62, 1) = \ell_0 \cap \ell_{13} \\ P_{221131} &= (10, 62, 52, 1) = \ell_0 \cap \ell_{16} \\ P_{71371} &= (10, 26, 16, 1) = \ell_0 \cap \ell_{19} \\ P_{184998} &= (37, 9, 44, 1) = \ell_1 \cap \ell_6 \\ P_{14886} &= (37, 39, 2, 1) = \ell_1 \cap \ell_7 \\ P_{164070} &= (37, 2, 39, 1) = \ell_1 \cap \ell_9 \\ P_{39846} &= (37, 45, 8, 1) = \ell_1 \cap \ell_{11} \\ P_{189030} &= (37, 8, 45, 1) = \ell_1 \cap \ell_{15} \\ P_{43878} &= (37, 44, 9, 1) = \ell_1 \cap \ell_{18} \\ P_{63599} &= (46, 32, 14, 1) = \ell_2 \cap \ell_4 \\ P_{176495} &= (46, 4, 42, 1) = \ell_2 \cap \ell_5 \\ P_{67759} &= (46, 33, 15, 1) = \ell_2 \cap \ell_{12} \\ P_{140335} &= (46, 15, 33, 1) = \ell_2 \cap \ell_{14} \\ P_{23279} &= (46, 42, 4, 1) = \ell_2 \cap \ell_{17} \\ P_{136175} &= (46, 14, 32, 1) = \ell_2 \cap \ell_{20} \\ P_{1249} &= (30, 18, 1, 0) = \ell_3 \cap \ell_4 \\ P_{251174} &= (37, 19, 60, 1) = \ell_3 \cap \ell_{11} \\ P_{160047} &= (46, 3, 38, 1) = \ell_3 \cap \ell_{14} \\ P_{243649} &= (0, 30, 58, 1) = \ell_3 \cap \ell_{18} \\ P_{221168} &= (47, 62, 52, 1) = \ell_4 \cap \ell_6 \\ P_{39820} &= (11, 45, 8, 1) = \ell_4 \cap \ell_8 \\ P_{81793} &= (0, 61, 18, 1) = \ell_4 \cap \ell_9 \\ P_{212235} &= (10, 51, 50, 1) = \ell_4 \cap \ell_{13} \\ P_{89190} &= (37, 48, 20, 1) = \ell_4 \cap \ell_{15} \\ P_{195557} &= (36, 46, 46, 1) = \ell_4 \cap \ell_{20} \\ P_{2027} &= (40, 30, 1, 0) = \ell_5 \cap \ell_6 \\ P_{150081} &= (0, 40, 35, 1) = \ell_5 \cap \ell_8 \\ P_{75558} &= (37, 27, 17, 1) = \ell_5 \cap \ell_{11} \\ P_{247819} &= (10, 31, 59, 1) = \ell_5 \cap \ell_{16} \\ P_{67749} &= (36, 33, 15, 1) = \ell_6 \cap \ell_{10} \\ P_{29579} &= (10, 13, 6, 1) = \ell_6 \cap \ell_{13} \end{aligned}$$

$$\begin{aligned} P_{99823} &= (46, 22, 23, 1) = \ell_6 \cap \ell_{14} \\ P_{158092} &= (11, 37, 37, 1) = \ell_6 \cap \ell_{18} \\ P_{130753} &= (0, 58, 30, 1) = \ell_6 \cap \ell_{19} \\ P_{2325} &= (18, 35, 1, 0) = \ell_7 \cap \ell_8 \\ P_{180619} &= (10, 5, 43, 1) = \ell_7 \cap \ell_{13} \\ P_{174319} &= (46, 34, 41, 1) = \ell_7 \cap \ell_{14} \\ P_{255169} &= (0, 18, 61, 1) = \ell_7 \cap \ell_{20} \\ P_{45808} &= (47, 10, 10, 1) = \ell_8 \cap \ell_{10} \\ P_{231023} &= (46, 24, 55, 1) = \ell_8 \cap \ell_{12} \\ P_{120742} &= (37, 29, 28, 1) = \ell_8 \cap \ell_{15} \\ P_{140325} &= (36, 15, 33, 1) = \ell_8 \cap \ell_{18} \\ P_{2688} &= (61, 40, 1, 0) = \ell_9 \cap \ell_{10} \\ P_{146095} &= (46, 41, 34, 1) = \ell_9 \cap \ell_{12} \\ P_{27403} &= (10, 43, 5, 1) = \ell_9 \cap \ell_{16} \\ P_{124774} &= (37, 28, 29, 1) = \ell_{10} \cap \ell_{11} \\ P_{106031} &= (46, 55, 24, 1) = \ell_{10} \cap \ell_{14} \\ P_{170241} &= (0, 35, 40, 1) = \ell_{10} \cap \ell_{17} \\ P_{189004} &= (11, 8, 45, 1) = \ell_{10} \cap \ell_{20} \\ P_{158118} &= (37, 37, 37, 1) = \ell_{11} \cap \ell_{15} \\ P_{202086} &= (37, 20, 48, 1) = \ell_{11} \cap \ell_{20} \\ P_{195567} &= (46, 46, 46, 1) = \ell_{12} \cap \ell_{14} \\ P_{95791} &= (46, 23, 22, 1) = \ell_{12} \cap \ell_{18} \\ P_{18927} &= (46, 38, 3, 1) = \ell_{12} \cap \ell_{19} \\ P_{45771} &= (10, 10, 10, 1) = \ell_{13} \cap \ell_{16} \\ P_{134923} &= (10, 59, 31, 1) = \ell_{13} \cap \ell_{17} \\ P_{115878} &= (37, 17, 27, 1) = \ell_{15} \cap \ell_{17} \\ P_{85862} &= (37, 60, 19, 1) = \ell_{15} \cap \ell_{19} \\ P_{57803} &= (10, 6, 13, 1) = \ell_{16} \cap \ell_{18} \\ P_{216267} &= (10, 50, 51, 1) = \ell_{16} \cap \ell_{20} \\ P_{3814} &= (35, 58, 1, 0) = \ell_{17} \cap \ell_{18} \\ P_{261488} &= (47, 52, 62, 1) = \ell_{18} \cap \ell_{20} \\ P_{4029} &= (58, 61, 1, 0) = \ell_{19} \cap \ell_{20} \end{aligned}$$

## Single Points

The surface has 1218 single points:

Too many to print.

### Points on surface but on no line

The surface has 3193 points not on any line:  
Too many to print.

### Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	0	1	1	1	0	0	0	0	1	0	1	0	0	1	0	0	1	0	0	1	0
1	1	0	1	0	0	0	1	1	0	1	0	1	0	0	0	1	0	0	1	0	0
2	1	1	0	0	1	1	0	0	0	0	0	1	0	1	0	0	1	0	0	1	0
3	1	0	0	0	1	1	0	1	0	1	0	0	1	0	0	1	0	1	1	1	0
4	0	0	1	1	0	0	1	0	1	1	0	0	0	1	0	1	0	0	0	0	1
5	0	0	1	1	0	0	1	1	1	1	0	1	0	0	0	0	1	1	0	1	0
6	0	1	0	0	1	1	0	0	0	0	1	0	0	1	1	0	0	0	1	1	0
7	0	1	0	1	0	1	0	0	1	1	0	0	0	1	1	0	0	1	0	1	1
8	1	0	0	0	1	1	0	1	0	0	1	0	0	1	0	0	1	0	0	1	0
9	0	1	0	1	1	1	0	1	0	0	1	0	0	0	1	1	0	1	0	1	0
10	1	0	0	0	0	0	1	0	1	1	0	1	0	0	1	0	0	1	0	0	1
11	0	1	0	1	0	1	0	0	0	0	1	0	1	1	0	1	0	0	0	0	1
12	0	0	1	0	0	0	0	0	1	1	0	1	0	1	1	0	0	0	1	1	0
13	1	0	0	0	1	0	1	1	0	0	0	0	1	1	0	0	0	1	0	0	0
14	0	0	1	1	0	0	1	1	0	0	1	0	0	1	1	0	0	0	0	0	0
15	0	1	0	0	1	0	0	0	1	0	0	1	0	0	1	0	1	1	0	1	0
16	1	0	0	0	0	1	0	0	0	1	1	1	0	1	1	0	0	1	0	1	0
17	0	0	1	1	0	1	0	1	0	1	0	0	1	0	1	0	0	1	1	0	0
18	0	1	0	1	0	0	1	0	1	0	0	0	1	0	0	0	1	1	0	0	1
19	1	0	0	1	0	1	1	1	0	1	0	0	1	0	0	1	0	1	0	0	1
20	0	0	1	0	1	0	0	1	0	0	1	1	0	0	0	0	1	0	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_8$	$\ell_{10}$	$\ell_{13}$	$\ell_{16}$	$\ell_{19}$
in point	$P_{131}$	$P_{131}$	$P_{111691}$	$P_{225291}$	$P_{265611}$	$P_{261451}$	$P_{221131}$	$P_{71371}$

Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{11}$	$\ell_{15}$	$\ell_{18}$
in point	$P_{131}$	$P_{131}$	$P_{184998}$	$P_{14886}$	$P_{164070}$	$P_{39846}$	$P_{189030}$	$P_{43878}$

Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_4$	$\ell_5$	$\ell_{12}$	$\ell_{14}$	$\ell_{17}$	$\ell_{20}$
in point	$P_{131}$	$P_{131}$	$P_{63599}$	$P_{176495}$	$P_{67759}$	$P_{140335}$	$P_{23279}$	$P_{136175}$

Line 3 intersects

Line	$\ell_0$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_9$	$\ell_{11}$	$\ell_{14}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$
in point	$P_{111691}$	$P_{1249}$	$P_{4163}$	$P_{4163}$	$P_{4163}$	$P_{251174}$	$P_{160047}$	$P_{4163}$	$P_{243649}$	$P_{4163}$

Line 4 intersects

Line	$\ell_2$	$\ell_3$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{13}$	$\ell_{15}$	$\ell_{20}$
in point	$P_{63599}$	$P_{1249}$	$P_{221168}$	$P_{39820}$	$P_{81793}$	$P_{212235}$	$P_{89190}$	$P_{195557}$

Line 5 intersects

Line	$\ell_2$	$\ell_3$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{16}$	$\ell_{17}$	$\ell_{19}$
in point	$P_{176495}$	$P_{4163}$	$P_{2027}$	$P_{4163}$	$P_{150081}$	$P_{4163}$	$P_{75558}$	$P_{247819}$	$P_{4163}$	$P_{4163}$

Line 6 intersects

Line	$\ell_1$	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{13}$	$\ell_{14}$	$\ell_{18}$	$\ell_{19}$
in point	$P_{184998}$	$P_{221168}$	$P_{2027}$	$P_{67749}$	$P_{29579}$	$P_{99823}$	$P_{158092}$	$P_{130753}$

Line 7 intersects

Line	$\ell_1$	$\ell_3$	$\ell_5$	$\ell_8$	$\ell_9$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$
in point	$P_{14886}$	$P_{4163}$	$P_{4163}$	$P_{2325}$	$P_{4163}$	$P_{180619}$	$P_{174319}$	$P_{4163}$	$P_{4163}$	$P_{255169}$

Line 8 intersects

Line	$\ell_0$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_{10}$	$\ell_{12}$	$\ell_{15}$	$\ell_{18}$
in point	$P_{225291}$	$P_{39820}$	$P_{150081}$	$P_{2325}$	$P_{45808}$	$P_{231023}$	$P_{120742}$	$P_{140325}$

Line 9 intersects

Line	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_{10}$	$\ell_{12}$	$\ell_{16}$	$\ell_{17}$	$\ell_{19}$
in point	$P_{164070}$	$P_{4163}$	$P_{81793}$	$P_{4163}$	$P_{4163}$	$P_{2688}$	$P_{146095}$	$P_{27403}$	$P_{4163}$	$P_{4163}$

Line 10 intersects

Line	$\ell_0$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{14}$	$\ell_{17}$	$\ell_{20}$
in point	$P_{265611}$	$P_{67749}$	$P_{45808}$	$P_{2688}$	$P_{124774}$	$P_{106031}$	$P_{170241}$	$P_{189004}$

Line 11 intersects

Line	$\ell_1$	$\ell_3$	$\ell_5$	$\ell_{10}$	$\ell_{12}$	$\ell_{13}$	$\ell_{15}$	$\ell_{20}$
in point	$P_{39846}$	$P_{251174}$	$P_{75558}$	$P_{124774}$	$P_{3651}$	$P_{3651}$	$P_{158118}$	$P_{202086}$

Line 12 intersects

Line	$\ell_2$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{18}$	$\ell_{19}$
in point	$P_{67759}$	$P_{231023}$	$P_{146095}$	$P_{3651}$	$P_{3651}$	$P_{195567}$	$P_{95791}$	$P_{18927}$

Line 13 intersects

Line	$\ell_0$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_{11}$	$\ell_{12}$	$\ell_{16}$	$\ell_{17}$
in point	$P_{261451}$	$P_{212235}$	$P_{29579}$	$P_{180619}$	$P_{3651}$	$P_{3651}$	$P_{45771}$	$P_{134923}$

Line 14 intersects

Line	$\ell_2$	$\ell_3$	$\ell_6$	$\ell_7$	$\ell_{10}$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$
in point	$P_{140335}$	$P_{160047}$	$P_{99823}$	$P_{174319}$	$P_{106031}$	$P_{195567}$	$P_{3715}$	$P_{3715}$

Line 15 intersects

Line	$\ell_1$	$\ell_4$	$\ell_8$	$\ell_{11}$	$\ell_{14}$	$\ell_{16}$	$\ell_{17}$	$\ell_{19}$
in point	$P_{189030}$	$P_{89190}$	$P_{120742}$	$P_{158118}$	$P_{3715}$	$P_{3715}$	$P_{115878}$	$P_{85862}$

Line 16 intersects

Line	$\ell_0$	$\ell_5$	$\ell_9$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{18}$	$\ell_{20}$
in point	$P_{221131}$	$P_{247819}$	$P_{27403}$	$P_{45771}$	$P_{3715}$	$P_{3715}$	$P_{57803}$	$P_{216267}$

Line 17 intersects

Line	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{13}$	$\ell_{15}$	$\ell_{18}$	$\ell_{19}$
in point	$P_{23279}$	$P_{4163}$	$P_{4163}$	$P_{4163}$	$P_{4163}$	$P_{170241}$	$P_{134923}$	$P_{115878}$	$P_{3814}$	$P_{4163}$

Line 18 intersects

Line	$\ell_1$	$\ell_3$	$\ell_6$	$\ell_8$	$\ell_{12}$	$\ell_{16}$	$\ell_{17}$	$\ell_{20}$
in point	$P_{43878}$	$P_{243649}$	$P_{158092}$	$P_{140325}$	$P_{95791}$	$P_{57803}$	$P_{3814}$	$P_{261488}$

Line 19 intersects

Line	$\ell_0$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{12}$	$\ell_{15}$	$\ell_{17}$	$\ell_{20}$
in point	$P_{71371}$	$P_{4163}$	$P_{4163}$	$P_{130753}$	$P_{4163}$	$P_{4163}$	$P_{18927}$	$P_{85862}$	$P_{4163}$	$P_{4029}$

Line 20 intersects

Line	$\ell_2$	$\ell_4$	$\ell_7$	$\ell_{10}$	$\ell_{11}$	$\ell_{16}$	$\ell_{18}$	$\ell_{19}$
in point	$P_{136175}$	$P_{195557}$	$P_{255169}$	$P_{189004}$	$P_{202086}$	$P_{216267}$	$P_{261488}$	$P_{4029}$

The surface has 4481 points:

Too many to print.