

# Rank-65546 over GF(4)

January 15, 2021

## The equation

The equation of the surface is :

$$X_0^3 + X_1^3 + X_2^3 + X_0X_1X_2 = 0$$

( 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0 )

The point rank of the equation over GF(4) is 1431655790

## General information

Number of lines	60
Number of points	49
Number of singular points	13
Number of Eckardt points	0
Number of double points	0
Number of single points	0
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$5^{60}$
Type of lines on points	$12, 9^{12}, 5^{36}$

## Singular Points

The surface has 13 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

$$1 : P_4 = \mathbf{P}(1, 1, 1, 1) = \mathbf{P}(1, 1, 1, 1)$$

$$2 : P_{12} = \mathbf{P}(1, 1, 1, 0) = \mathbf{P}(1, 1, 1, 0)$$

$$3 : P_{18} = \mathbf{P}(\omega^2, \omega, 1, 0) = \mathbf{P}(3, 2, 1, 0)$$

$$4 : P_{21} = \mathbf{P}(\omega, \omega^2, 1, 0) = \mathbf{P}(2, 3, 1, 0)$$

$$5 : P_{48} = \mathbf{P}(\omega^2, \omega, 1, 1) = \mathbf{P}(3, 2, 1, 1)$$

$$6 : P_{51} = \mathbf{P}(\omega, \omega^2, 1, 1) = \mathbf{P}(2, 3, 1, 1)$$

$$7 : P_{60} = \mathbf{P}(\omega^2, 1, \omega, 1) = \mathbf{P}(3, 1, 2, 1)$$

$$8 : P_{63} = \mathbf{P}(\omega, \omega, \omega, 1) = \mathbf{P}(2, 2, 2, 1)$$

$$9 : P_{66} = \mathbf{P}(1, \omega^2, \omega, 1) = \mathbf{P}(1, 3, 2, 1)$$

$$10 : P_{75} = \mathbf{P}(\omega, 1, \omega^2, 1) = \mathbf{P}(2, 1, 3, 1)$$

$$11 : P_{78} = \mathbf{P}(1, \omega, \omega^2, 1) = \mathbf{P}(1, 2, 3, 1)$$

$$12 : P_{84} = \mathbf{P}(\omega^2, \omega^2, \omega^2, 1) = \mathbf{P}(3, 3, 3, 1)$$

## The 60 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned}
\ell_0 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{22} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{22} = \mathbf{Pl}(1, 0, 1, 0, 0, 1)_{109} \\
\ell_1 &= \begin{bmatrix} 1 & 0 & \omega & 0 \\ 0 & 1 & \omega^2 & 0 \end{bmatrix}_{45} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 3 & 0 \end{bmatrix}_{45} = \mathbf{Pl}(3, 0, 2, 0, 0, 1)_{118} \\
\ell_2 &= \begin{bmatrix} 1 & 0 & \omega^2 & 0 \\ 0 & 1 & \omega & 0 \end{bmatrix}_{65} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 1 & 2 & 0 \end{bmatrix}_{65} = \mathbf{Pl}(2, 0, 3, 0, 0, 1)_{124} \\
\ell_3 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{41} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{41} = \mathbf{Pl}(0, 0, 0, 1, 1, 0)_{53} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{110} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{110} = \mathbf{Pl}(1, 0, 1, 1, 1, 1)_{199} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & 1 & \omega^2 \\ 0 & 1 & 1 & \omega^2 \end{bmatrix}_{286} = \begin{bmatrix} 1 & 0 & 1 & 3 \\ 0 & 1 & 1 & 3 \end{bmatrix}_{286} = \mathbf{Pl}(2, 0, 2, 3, 3, 1)_{327} \\
\ell_6 &= \begin{bmatrix} 1 & 0 & 1 & \omega \\ 0 & 1 & 1 & \omega \end{bmatrix}_{198} = \begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 1 & 2 \end{bmatrix}_{198} = \mathbf{Pl}(3, 0, 3, 2, 2, 1)_{275} \\
\ell_7 &= \begin{bmatrix} 1 & \omega^2 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{83} = \begin{bmatrix} 1 & 3 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{83} = \mathbf{Pl}(0, 0, 0, 3, 1, 0)_{67} \\
\ell_8 &= \begin{bmatrix} 1 & 0 & \omega & \omega \\ 0 & 1 & \omega^2 & \omega^2 \end{bmatrix}_{225} = \begin{bmatrix} 1 & 0 & 2 & 2 \\ 0 & 1 & 3 & 3 \end{bmatrix}_{225} = \mathbf{Pl}(2, 0, 1, 1, 2, 1)_{260} \\
\ell_9 &= \begin{bmatrix} 1 & 0 & \omega & 1 \\ 0 & 1 & \omega^2 & \omega \end{bmatrix}_{137} = \begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 3 & 2 \end{bmatrix}_{137} = \mathbf{Pl}(3, 0, 2, 3, 1, 1)_{208} \\
\ell_{10} &= \begin{bmatrix} 1 & 0 & \omega & \omega^2 \\ 0 & 1 & \omega^2 & 1 \end{bmatrix}_{301} = \begin{bmatrix} 1 & 0 & 2 & 3 \\ 0 & 1 & 3 & 1 \end{bmatrix}_{301} = \mathbf{Pl}(1, 0, 3, 2, 3, 1)_{333} \\
\ell_{11} &= \begin{bmatrix} 1 & \omega & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{62} = \begin{bmatrix} 1 & 2 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{62} = \mathbf{Pl}(0, 0, 0, 2, 1, 0)_{60} \\
\ell_{12} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega^2 \\ 0 & 1 & \omega & \omega \end{bmatrix}_{325} = \begin{bmatrix} 1 & 0 & 3 & 3 \\ 0 & 1 & 2 & 2 \end{bmatrix}_{325} = \mathbf{Pl}(3, 0, 1, 1, 3, 1)_{321} \\
\ell_{13} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega \\ 0 & 1 & \omega & 1 \end{bmatrix}_{237} = \begin{bmatrix} 1 & 0 & 3 & 2 \\ 0 & 1 & 2 & 1 \end{bmatrix}_{237} = \mathbf{Pl}(1, 0, 2, 3, 2, 1)_{266} \\
\ell_{14} &= \begin{bmatrix} 1 & 0 & \omega^2 & 1 \\ 0 & 1 & \omega & \omega^2 \end{bmatrix}_{161} = \begin{bmatrix} 1 & 0 & 3 & 1 \\ 0 & 1 & 2 & 3 \end{bmatrix}_{161} = \mathbf{Pl}(2, 0, 3, 2, 1, 1)_{214} \\
\ell_{15} &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{104} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{104} = \mathbf{Pl}(0, 1, 0, 0, 1, 0)_{29} \\
\ell_{16} &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{26} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{26} = \mathbf{Pl}(1, 1, 1, 0, 1, 1)_{180} \\
\ell_{17} &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & \omega^2 \end{bmatrix}_{34} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 3 \end{bmatrix}_{34} = \mathbf{Pl}(2, 3, 2, 0, 3, 1)_{304} \\
\ell_{18} &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & \omega \end{bmatrix}_{30} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 2 \end{bmatrix}_{30} = \mathbf{Pl}(3, 2, 3, 0, 2, 1)_{248} \\
\ell_{19} &= \begin{bmatrix} 1 & 0 & \omega^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{272} = \mathbf{Pl}(0, 3, 0, 0, 1, 0)_{31}
\end{aligned}$$

$$\begin{aligned}
\ell_{20} &= \begin{bmatrix} 1 & 0 & \omega^2 & 0 \\ 0 & 1 & \omega & 1 \end{bmatrix}_{69} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 1 & 2 & 1 \end{bmatrix}_{69} = \mathbf{Pl}(1, 1, 2, 0, 2, 1)_{243} \\
\ell_{21} &= \begin{bmatrix} 1 & 0 & \omega^2 & 0 \\ 0 & 1 & \omega & \omega^2 \end{bmatrix}_{77} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 1 & 2 & 3 \end{bmatrix}_{77} = \mathbf{Pl}(2, 3, 3, 0, 1, 1)_{187} \\
\ell_{22} &= \begin{bmatrix} 1 & 0 & \omega^2 & 0 \\ 0 & 1 & \omega & \omega \end{bmatrix}_{73} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 1 & 2 & 2 \end{bmatrix}_{73} = \mathbf{Pl}(3, 2, 1, 0, 3, 1)_{302} \\
\ell_{23} &= \begin{bmatrix} 1 & 0 & \omega & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{188} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{188} = \mathbf{Pl}(0, 2, 0, 0, 1, 0)_{30} \\
\ell_{24} &= \begin{bmatrix} 1 & 0 & \omega & 0 \\ 0 & 1 & \omega^2 & 1 \end{bmatrix}_{49} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 3 & 1 \end{bmatrix}_{49} = \mathbf{Pl}(1, 1, 3, 0, 3, 1)_{306} \\
\ell_{25} &= \begin{bmatrix} 1 & 0 & \omega & 0 \\ 0 & 1 & \omega^2 & \omega^2 \end{bmatrix}_{57} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 3 & 3 \end{bmatrix}_{57} = \mathbf{Pl}(2, 3, 1, 0, 2, 1)_{241} \\
\ell_{26} &= \begin{bmatrix} 1 & 0 & \omega & 0 \\ 0 & 1 & \omega^2 & \omega \end{bmatrix}_{53} = \begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 3 & 2 \end{bmatrix}_{53} = \mathbf{Pl}(3, 2, 2, 0, 1, 1)_{185} \\
\ell_{27} &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{345} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{345} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{13} \\
\ell_{28} &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{106} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{106} = \mathbf{Pl}(1, 1, 1, 1, 0, 1)_{150} \\
\ell_{29} &= \begin{bmatrix} 1 & 0 & 1 & \omega^2 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{274} = \begin{bmatrix} 1 & 0 & 1 & 3 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{274} = \mathbf{Pl}(2, 3, 1, 3, 0, 1)_{169} \\
\ell_{30} &= \begin{bmatrix} 1 & 0 & 1 & \omega \\ 0 & 1 & 1 & 0 \end{bmatrix}_{190} = \begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{190} = \mathbf{Pl}(3, 2, 1, 2, 0, 1)_{161} \\
\ell_{31} &= \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{125} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{125} = \mathbf{Pl}(0, 1, 0, 1, 1, 0)_{57} \\
\ell_{32} &= \begin{bmatrix} 1 & 0 & \omega & \omega \\ 0 & 1 & \omega^2 & \omega \end{bmatrix}_{221} = \begin{bmatrix} 1 & 0 & 2 & 2 \\ 0 & 1 & 3 & 2 \end{bmatrix}_{221} = \mathbf{Pl}(1, 1, 1, 1, 1, 1)_{219} \\
\ell_{33} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega^2 \\ 0 & 1 & \omega & \omega^2 \end{bmatrix}_{329} = \begin{bmatrix} 1 & 0 & 3 & 3 \\ 0 & 1 & 2 & 3 \end{bmatrix}_{329} = \mathbf{Pl}(1, 1, 1, 1, 1, 1)_{222} \\
\ell_{34} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega \\ 0 & 1 & \omega & \omega \end{bmatrix}_{241} = \begin{bmatrix} 1 & 0 & 3 & 2 \\ 0 & 1 & 2 & 2 \end{bmatrix}_{241} = \mathbf{Pl}(2, 3, 2, 3, 3, 1)_{349} \\
\ell_{35} &= \begin{bmatrix} 1 & 0 & \omega & 1 \\ 0 & 1 & \omega^2 & 1 \end{bmatrix}_{133} = \begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 3 & 1 \end{bmatrix}_{133} = \mathbf{Pl}(2, 3, 2, 3, 3, 1)_{346} \\
\ell_{36} &= \begin{bmatrix} 1 & 0 & \omega & \omega^2 \\ 0 & 1 & \omega^2 & \omega^2 \end{bmatrix}_{309} = \begin{bmatrix} 1 & 0 & 2 & 3 \\ 0 & 1 & 3 & 3 \end{bmatrix}_{309} = \mathbf{Pl}(3, 2, 3, 2, 2, 1)_{293} \\
\ell_{37} &= \begin{bmatrix} 1 & 0 & \omega^2 & 1 \\ 0 & 1 & \omega & 1 \end{bmatrix}_{153} = \begin{bmatrix} 1 & 0 & 3 & 1 \\ 0 & 1 & 2 & 1 \end{bmatrix}_{153} = \mathbf{Pl}(3, 2, 3, 2, 2, 1)_{296} \\
\ell_{38} &= \begin{bmatrix} 0 & 1 & \omega^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{355} = \begin{bmatrix} 0 & 1 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{355} = \mathbf{Pl}(0, 3, 0, 1, 0, 0)_{15} \\
\ell_{39} &= \begin{bmatrix} 1 & 0 & \omega & 1 \\ 0 & 1 & \omega^2 & 0 \end{bmatrix}_{129} = \begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 3 & 0 \end{bmatrix}_{129} = \mathbf{Pl}(3, 2, 2, 3, 0, 1)_{173} \\
\ell_{40} &= \begin{bmatrix} 1 & 0 & \omega & \omega^2 \\ 0 & 1 & \omega^2 & 0 \end{bmatrix}_{297} = \begin{bmatrix} 1 & 0 & 2 & 3 \\ 0 & 1 & 3 & 0 \end{bmatrix}_{297} = \mathbf{Pl}(1, 1, 2, 2, 0, 1)_{162}
\end{aligned}$$

$$\begin{aligned}
\ell_{41} &= \begin{bmatrix} 1 & 0 & \omega & \omega \\ 0 & 1 & \omega^2 & 0 \end{bmatrix}_{213} = \begin{bmatrix} 1 & 0 & 2 & 2 \\ 0 & 1 & 3 & 0 \end{bmatrix}_{213} = \mathbf{Pl}(2, 3, 2, 1, 0, 1)_{154} \\
\ell_{42} &= \begin{bmatrix} 1 & \omega^2 & \omega & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{251} = \begin{bmatrix} 1 & 3 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{251} = \mathbf{Pl}(0, 2, 0, 3, 1, 0)_{72} \\
\ell_{43} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega \\ 0 & 1 & \omega & \omega^2 \end{bmatrix}_{245} = \begin{bmatrix} 1 & 0 & 3 & 2 \\ 0 & 1 & 2 & 3 \end{bmatrix}_{245} = \mathbf{Pl}(3, 2, 2, 3, 1, 1)_{227} \\
\ell_{44} &= \begin{bmatrix} 1 & 0 & 1 & \omega \\ 0 & 1 & 1 & \omega^2 \end{bmatrix}_{202} = \begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 1 & 3 \end{bmatrix}_{202} = \mathbf{Pl}(1, 1, 3, 2, 3, 1)_{354} \\
\ell_{45} &= \begin{bmatrix} 1 & 0 & \omega^2 & 1 \\ 0 & 1 & \omega & \omega \end{bmatrix}_{157} = \begin{bmatrix} 1 & 0 & 3 & 1 \\ 0 & 1 & 2 & 2 \end{bmatrix}_{157} = \mathbf{Pl}(1, 1, 3, 2, 3, 1)_{351} \\
\ell_{46} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega^2 \\ 0 & 1 & \omega & 1 \end{bmatrix}_{321} = \begin{bmatrix} 1 & 0 & 3 & 3 \\ 0 & 1 & 2 & 1 \end{bmatrix}_{321} = \mathbf{Pl}(2, 3, 1, 1, 2, 1)_{280} \\
\ell_{47} &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & \omega \end{bmatrix}_{114} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 2 \end{bmatrix}_{114} = \mathbf{Pl}(2, 3, 1, 1, 2, 1)_{283} \\
\ell_{48} &= \begin{bmatrix} 1 & 0 & 1 & \omega^2 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{278} = \begin{bmatrix} 1 & 0 & 1 & 3 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{278} = \mathbf{Pl}(3, 2, 2, 3, 1, 1)_{230} \\
\ell_{49} &= \begin{bmatrix} 0 & 1 & \omega & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{350} = \begin{bmatrix} 0 & 1 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{350} = \mathbf{Pl}(0, 2, 0, 1, 0, 0)_{14} \\
\ell_{50} &= \begin{bmatrix} 1 & 0 & \omega^2 & 1 \\ 0 & 1 & \omega & 0 \end{bmatrix}_{149} = \begin{bmatrix} 1 & 0 & 3 & 1 \\ 0 & 1 & 2 & 0 \end{bmatrix}_{149} = \mathbf{Pl}(2, 3, 3, 2, 0, 1)_{166} \\
\ell_{51} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega \\ 0 & 1 & \omega & 0 \end{bmatrix}_{233} = \begin{bmatrix} 1 & 0 & 3 & 2 \\ 0 & 1 & 2 & 0 \end{bmatrix}_{233} = \mathbf{Pl}(1, 1, 3, 3, 0, 1)_{174} \\
\ell_{52} &= \begin{bmatrix} 1 & 0 & \omega^2 & \omega^2 \\ 0 & 1 & \omega & 0 \end{bmatrix}_{317} = \begin{bmatrix} 1 & 0 & 3 & 3 \\ 0 & 1 & 2 & 0 \end{bmatrix}_{317} = \mathbf{Pl}(3, 2, 3, 1, 0, 1)_{158} \\
\ell_{53} &= \begin{bmatrix} 1 & \omega & \omega^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{314} = \begin{bmatrix} 1 & 2 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{314} = \mathbf{Pl}(0, 3, 0, 2, 1, 0)_{66} \\
\ell_{54} &= \begin{bmatrix} 1 & 0 & \omega & \omega^2 \\ 0 & 1 & \omega^2 & \omega \end{bmatrix}_{305} = \begin{bmatrix} 1 & 0 & 2 & 3 \\ 0 & 1 & 3 & 2 \end{bmatrix}_{305} = \mathbf{Pl}(2, 3, 3, 2, 1, 1)_{235} \\
\ell_{55} &= \begin{bmatrix} 1 & 0 & 1 & \omega^2 \\ 0 & 1 & 1 & \omega \end{bmatrix}_{282} = \begin{bmatrix} 1 & 0 & 1 & 3 \\ 0 & 1 & 1 & 2 \end{bmatrix}_{282} = \mathbf{Pl}(1, 1, 2, 3, 2, 1)_{285} \\
\ell_{56} &= \begin{bmatrix} 1 & 0 & \omega & 1 \\ 0 & 1 & \omega^2 & \omega^2 \end{bmatrix}_{141} = \begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 3 & 3 \end{bmatrix}_{141} = \mathbf{Pl}(1, 1, 2, 3, 2, 1)_{288} \\
\ell_{57} &= \begin{bmatrix} 1 & 0 & 1 & \omega \\ 0 & 1 & 1 & 1 \end{bmatrix}_{194} = \begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{194} = \mathbf{Pl}(2, 3, 3, 2, 1, 1)_{232} \\
\ell_{58} &= \begin{bmatrix} 1 & 0 & \omega & \omega \\ 0 & 1 & \omega^2 & 1 \end{bmatrix}_{217} = \begin{bmatrix} 1 & 0 & 2 & 2 \\ 0 & 1 & 3 & 1 \end{bmatrix}_{217} = \mathbf{Pl}(3, 2, 1, 1, 3, 1)_{344} \\
\ell_{59} &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & \omega^2 \end{bmatrix}_{118} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 3 \end{bmatrix}_{118} = \mathbf{Pl}(3, 2, 1, 1, 3, 1)_{341}
\end{aligned}$$

Rank of lines: ( 22, 45, 65, 41, 110, 286, 198, 83, 225, 137, 301, 62, 325, 237, 161, 104, 26, 34, 30, 272, 69, 77, 73, 188, 49, 57, 53, 345, 106, 274, 190, 125, 221, 329, 241, 133, 309, 153, 355, 129, 297, 213, 251, 245, 202, 157, 321, 114, 278, 350, ...194, 217, 118 )

Rank of points on Klein quadric: ( 109, 118, 124, 53, 199, 327, 275, 67, 260, 208, 333, 60, 321, 266, 214, 29, 180, 304, 248, 31, 243, 187, 302, 30, 306, 241, 185, 13, 150, 169, 161, 57, 219, 222, 349, 346, 293, 296, 15, 173, 162, 154, 72, 227, 354, 351, 280, 283, 230, 14, ...232, 344, 341 )

**Eckardt Points**

The surface has 0 Eckardt points:

**Double Points**

The surface has 0 Double points:

The double points on the surface are:

**Single Points**

The surface has 0 single points:

The single points on the surface are:

The single points on the surface are:

**Points on surface but on no line**

The surface has 0 points not on any line:

The points on the surface but not on lines are:

# Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47		
0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1		
1	1	0	1	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	
2	1	1	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	0	0	0	0	1	1	1	1	1	
3	1	0	0	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	1	1	1	1	1	1	0	0	0	0	0	0	1	0	0	0	1	0	1	0	0	1	
4	1	0	0	1	0	1	0	0	1	1	1	1	1	1	1	0	0	1	0	0	1	0	0	0	0	1	1	1	1	1	1	0	0	0	0	1	0	1	0	0	1	0	1	0	1	0	0	1		
5	1	0	0	1	1	0	1	0	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	1	0	0	1	1	1	1	1	0	0	1	0	0	1	0	0	0	0	1	1	0	1	0	0	1	
6	1	0	0	1	1	1	0	0	1	1	1	1	1	1	1	1	0	1	0	0	0	0	0	1	0	1	1	1	1	1	0	1	0	1	0	0	0	0	0	1	0	0	1	0	1	0	0	1		
7	0	1	0	1	0	0	0	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	0	0	0	1	1	0	0	1	1	0	1	1	1	1	1	1	1	0	0	0	0	
8	0	1	0	0	1	0	0	0	0	0	0	1	0	1	0	0	1	0	1	0	0	1	1	1	1	1	0	0	1	0	1	1	0	0	1	1	0	1	1	1	1	1	0	1	1	0	0	0		
9	0	1	0	0	0	1	0	1	0	0	1	0	0	0	0	1	0	1	0	0	0	1	0	1	1	1	1	0	0	0	1	1	1	0	0	1	1	0	1	1	1	1	1	0	0	0	1	0	1	
10	0	1	0	0	0	0	1	1	1	0	0	1	0	0	1	0	0	0	0	1	1	1	1	1	1	1	0	1	0	0	1	1	0	0	1	1	0	1	1	1	1	1	0	0	0	0	1	0		
11	0	0	1	1	0	0	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	1	1	0	0	1	1	0	0	0	1	1	0	1	1	0			
12	0	0	1	0	1	0	0	1	0	1	1	1	1	1	1	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	1	1	0	1	1	0	0	1	0	1	0	0	1	1	0	1	1	0		
13	0	0	1	0	1	0	0	0	1	1	1	1	1	1	1	1	0	0	1	1	1	1	1	0	0	1	0	0	1	0	0	1	0	1	1	0	0	1	0	0	1	0	1	1	0	1	1	0		
14	0	0	1	0	0	1	0	0	1	1	1	1	1	1	1	1	0	0	1	1	1	1	1	0	0	0	1	0	0	1	0	1	0	1	1	0	0	1	0	0	0	1	1	1	0	1	1	0		
15	1	0	0	1	1	1	0	0	0	1	1	1	1	1	1	0	0	0	1	1	1	1	0	0	0	1	0	0	0	1	1	1	1	0	0	0	0	0	0	1	0	0	0	1	0	1	0	0	1	
16	1	0	0	1	1	1	0	0	1	1	0	1	1	0	1	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	0	0	0	1	0	1	0	0	0	0	1	1	0	1	0	0	1		
17	1	0	0	1	1	1	0	0	1	1	0	1	1	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	1	1	1	1	0	1	0	0	0	0	1	0	1	0	0	1	0	1	0	0	1	
18	1	0	0	1	1	1	0	0	1	1	1	0	0	0	0	1	0	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	0	0	1	0	1	0	0	0	0	1	0	1	0	1	0	0	1	
19	0	0	1	1	0	0	1	1	1	0	0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	0	1	0	0	0	1	0	1	1	0	0	1	1	0	0	0	1	1	0	1	1	0		
20	0	0	1	0	0	1	0	1	0	0	1	0	1	1	0	1	0	0	1	0	1	1	0	1	0	0	0	0	1	0	1	0	1	1	0	0	1	0	1	0	0	1	1	0	1	1	0			
21	0	0	1	0	0	0	1	0	1	0	1	1	0	1	0	1	0	0	1	0	1	1	0	1	0	0	1	0	0	0	1	1	0	1	1	0	0	1	0	0	1	0	1	1	0	1	1	0		
22	0	0	1	0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	0	0	1	0	0	0	0	1	0	1	0	0	1	0	1	1	0	0	1	0	0	0	1	1	1	0	1	1	0		
23	0	1	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0	0	1	1	1	1	0	0	0	1	1	0	0	1	1	0	1	1	1	1	1	1	1	0	0	0	0	
24	0	1	0	0	1	0	0	0	1	0	0	0	1	0	0	1	0	0	1	0	0	1	0	1	1	0	0	0	1	1	1	0	0	0	1	1	0	0	1	1	0	1	1	1	1	0	1	0	0	1
25	0	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	1	0	1	1	0	1	0	1	0	1	0	1	0	0	1	1	0	0	1	1	0	0	1	1	0	1	1	1	1	0	0	0	1	
26	0	1	0	0	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	0	0	0	1	1	1	0	0	0	1	0	1	1	0	0	1	1	0	1	1	1	1	1	1	0	0	1	0	1	
27	1	0	0	1	0	0	0	1	1	1	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	1	0	0	0	1	0	1	0	0	1	
28	1	0	0	1	0	1	1	1	1	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	1	0	1	0	1	1	0	1	1	0	0	0	0	0	0	0	1	0	0	1	0	1	0	0	1	
29	1	0	0	1	0	1	1	1	1	1	0	1	1	1	1	0	1	0	0	0	0	0	0	0	1	1	1	0	1	0	0	0	1	1	0	0	0	0	0	0	1	0	1	0	1	0	0	1		
30	1	0	0	1	0	0	1	1	1	1	1	0	0	1	1	1	0	0	1	0	0	1	0	0	1	1	1	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	1	1	0	1	0	0	1	
31	0	1	1	1	0	0	0	1	1	1	1	1	1	1	1	0	0	0	1	1	1	1	1	1	1	1	1	1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	
32	0	1	1	0	0	0	0	0	0	0	1	0	0	0	0	0	1	0	0	0	0	0	0	1	1	1	1	0	1	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	
33	0	1	1	0	1	0	0	0	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	1	0	0	1	1	0	1	1	1	0	0	1	1	1	1	1	0	0	0	0	1	1	0	1	1	
34	0	1	1	0	0	1	0	0	0	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1	1	1	0	1	1	1	0	0	0	0	0	0	0	1	1	0	1	1	0	
35	0	1	1	0	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1	1	1	1	0	0	1	0	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	0	0	0	
36	0	1	1	0	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	1	1	1	1	1	0	1	1	1	1	1	1	1	1	0	0	0	1	
37	0	1	1	0	1	0	0	0	0	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	
38	0	1	1	0	0	0	1	0	0	0	1	0	0	0	1	1	1	1	1	0	0	0	1	1	1	1	1	0	0	0	1	1	0	0	1	1	0	0	1	1	1	1	1	1	0	0	0	0	0	
39	0	1	0	0	0	1	1	1	0	0	0	1	0	0	1	0	0	1	0	0	1	1	1</																											

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$	$\ell_{45}$	$\ell_{46}$	$\ell_{47}$	$\ell_{48}$
in point	$P_{21}$	$P_{18}$	$P_5$	$P_5$	$P_5$	$P_5$	$P_8$	$P_8$	$P_8$	$P_8$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$
in point	$P_{21}$	$P_{12}$	$P_6$	$P_6$	$P_6$	$P_6$	$P_{10}$	$P_{10}$	$P_{10}$	$P_{10}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$	$\ell_{45}$
in point	$P_{18}$	$P_{12}$	$P_7$	$P_7$	$P_7$	$P_7$	$P_9$	$P_9$	$P_9$	$P_9$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 3 intersects

Line	$\ell_0$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_{11}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{23}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{38}$	$\ell_{42}$	$\ell_{44}$	$\ell_{47}$
in point	$P_5$	$P_5$	$P_5$	$P_5$	$P_3$	$P_3$	$P_3$	$P_{27}$	$P_{32}$	$P_{37}$	$P_3$	$P_3$	$P_3$	$P_{27}$	$P_{32}$	$P_{37}$	$P_3$	$P_3$	$P_3$	$P_{27}$	$P_{32}$

Line 4 intersects

Line	$\ell_0$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{21}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{35}$	$\ell_{37}$	$\ell_{40}$	$\ell_{42}$	$\ell_{43}$
in point	$P_5$	$P_5$	$P_5$	$P_5$	$P_{51}$	$P_{48}$	$P_{39}$	$P_{42}$	$P_{48}$	$P_{51}$	$P_{48}$	$P_{51}$	$P_{42}$	$P_{39}$	$P_{51}$	$P_{48}$	$P_{51}$	$P_{48}$	$P_{51}$	$P_{48}$	$P_{48}$

Line 5 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_6$	$\ell_9$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{22}$	$\ell_{24}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{33}$	$\ell_{36}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$
in point	$P_5$	$P_5$	$P_5$	$P_5$	$P_{60}$	$P_{66}$	$P_{55}$	$P_{60}$	$P_{61}$	$P_{66}$	$P_{66}$	$P_{60}$	$P_{61}$	$P_{66}$	$P_{55}$	$P_{60}$	$P_{66}$	$P_{60}$	$P_{60}$	$P_{66}$	$P_{66}$

Line 6 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{25}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{32}$	$\ell_{34}$	$\ell_{39}$	$\ell_{42}$	$\ell_{43}$
in point	$P_5$	$P_5$	$P_5$	$P_5$	$P_{78}$	$P_{75}$	$P_{72}$	$P_{75}$	$P_{78}$	$P_{81}$	$P_{75}$	$P_{78}$	$P_{81}$	$P_{78}$	$P_{75}$	$P_{72}$	$P_{78}$	$P_{75}$	$P_{78}$	$P_{75}$	$P_{75}$

Line 7 intersects

Line	$\ell_1$	$\ell_3$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{15}$	$\ell_{19}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$
in point	$P_6$	$P_3$	$P_6$	$P_6$	$P_6$	$P_3$	$P_3$	$P_3$	$P_3$	$P_{28}$	$P_{33}$	$P_{35}$	$P_3$	$P_3$	$P_{28}$	$P_{33}$	$P_{35}$	$P_3$	$P_{35}$	$P_{28}$	$P_{33}$

Line 8 intersects

Line	$\ell_1$	$\ell_4$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{18}$	$\ell_{20}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{29}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$
in point	$P_6$	$P_{51}$	$P_6$	$P_6$	$P_6$	$P_4$	$P_{51}$	$P_4$	$P_{41}$	$P_4$	$P_{45}$	$P_{51}$	$P_{51}$	$P_4$	$P_{41}$	$P_{51}$	$P_{45}$	$P_{45}$	$P_4$	$P_{51}$	$P_{41}$

Line 9 intersects

Line	$\ell_1$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_{10}$	$\ell_{13}$	$\ell_{16}$	$\ell_{21}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$
in point	$P_6$	$P_{60}$	$P_6$	$P_6$	$P_6$	$P_{63}$	$P_{60}$	$P_{63}$	$P_{54}$	$P_{60}$	$P_{63}$	$P_{65}$	$P_{60}$	$P_{63}$	$P_{65}$	$P_{54}$	$P_{60}$	$P_{65}$	$P_{54}$	$P_{63}$	$P_{63}$

Line 10 intersects

Line	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{14}$	$\ell_{17}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{28}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$
in point	$P_6$	$P_{78}$	$P_6$	$P_6$	$P_6$	$P_{84}$	$P_{78}$	$P_{84}$	$P_{71}$	$P_{73}$	$P_{78}$	$P_{84}$	$P_{78}$	$P_{84}$	$P_{78}$	$P_{73}$	$P_{71}$	$P_{73}$	$P_{78}$	$P_{71}$	$P_{71}$

Line 11 intersects

Line	$\ell_2$	$\ell_3$	$\ell_7$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{27}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{38}$	$\ell_{42}$	$\ell_{43}$	$\ell_{45}$
in point	$P_7$	$P_3$	$P_3$	$P_7$	$P_7$	$P_7$	$P_3$	$P_3$	$P_{29}$	$P_{31}$	$P_{36}$	$P_3$	$P_3$	$P_3$	$P_{29}$	$P_{31}$	$P_{36}$	$P_3$	$P_3$	$P_{36}$	$P_{29}$

Line 12 intersects

Line	$\ell_2$	$\ell_4$	$\ell_8$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$	$\ell_{30}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{39}$	$\ell_{42}$	$\ell_{43}$	$\ell_{45}$
in point	$P_7$	$P_{48}$	$P_4$	$P_7$	$P_7$	$P_7$	$P_{48}$	$P_{40}$	$P_4$	$P_{48}$	$P_{49}$	$P_4$	$P_{48}$	$P_4$	$P_{40}$	$P_{49}$	$P_{48}$	$P_4$	$P_{48}$	$P_4$	$P_{48}$

Line 13 intersects

Line	$\ell_2$	$\ell_5$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{14}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{25}$	$\ell_{28}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{40}$	$\ell_{42}$	$\ell_{43}$
in point	$P_7$	$P_{66}$	$P_{63}$	$P_7$	$P_7$	$P_7$	$P_{66}$	$P_{56}$	$P_{57}$	$P_{63}$	$P_{66}$	$P_{63}$	$P_{66}$	$P_{63}$	$P_{66}$	$P_{56}$	$P_{57}$	$P_{63}$	$P_{66}$	$P_{56}$

Line 14 intersects

Line	$\ell_2$	$\ell_6$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{16}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{26}$	$\ell_{29}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$
in point	$P_7$	$P_{75}$	$P_{84}$	$P_7$	$P_7$	$P_7$	$P_{75}$	$P_{70}$	$P_{75}$	$P_{77}$	$P_{84}$	$P_{84}$	$P_{75}$	$P_{84}$	$P_{77}$	$P_{75}$	$P_{70}$	$P_{84}$	$P_{75}$	$P_{77}$

Line 15 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_{11}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{23}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{38}$	$\ell_{42}$	$\ell_{44}$	$\ell_{47}$
in point	$P_8$	$P_3$	$P_{39}$	$P_{55}$	$P_{72}$	$P_3$	$P_3$	$P_8$	$P_8$	$P_8$	$P_3$	$P_3$	$P_3$	$P_{39}$	$P_{55}$	$P_{72}$	$P_3$	$P_3$	$P_3$	$P_{72}$	$P_{39}$

Line 16 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_9$	$\ell_{14}$	$\ell_{15}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{24}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{34}$	$\ell_{36}$	$\ell_{41}$	$\ell_{42}$
in point	$P_8$	$P_{27}$	$P_{42}$	$P_{60}$	$P_{75}$	$P_{60}$	$P_{75}$	$P_8$	$P_8$	$P_8$	$P_{75}$	$P_{60}$	$P_{42}$	$P_{27}$	$P_{75}$	$P_{60}$	$P_{75}$	$P_{60}$	$P_{60}$	$P_{75}$

Line 17 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$	$\ell_{18}$	$\ell_{21}$	$\ell_{25}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{32}$	$\ell_{37}$	$\ell_{39}$	$\ell_{42}$
in point	$P_8$	$P_{32}$	$P_{48}$	$P_{61}$	$P_{78}$	$P_{78}$	$P_{48}$	$P_8$	$P_8$	$P_8$	$P_{48}$	$P_{78}$	$P_{61}$	$P_{78}$	$P_{32}$	$P_{48}$	$P_{78}$	$P_{48}$	$P_{78}$	$P_{48}$

Line 18 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{22}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{33}$	$\ell_{35}$	$\ell_{40}$	$\ell_{42}$
in point	$P_8$	$P_{37}$	$P_{51}$	$P_{66}$	$P_{81}$	$P_{51}$	$P_{66}$	$P_8$	$P_8$	$P_8$	$P_{66}$	$P_{51}$	$P_{81}$	$P_{66}$	$P_{51}$	$P_{37}$	$P_{66}$	$P_{51}$	$P_{51}$	$P_{66}$

Line 19 intersects

Line	$\ell_2$	$\ell_3$	$\ell_7$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{27}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{38}$	$\ell_{42}$	$\ell_{43}$	$\ell_{45}$
in point	$P_9$	$P_3$	$P_3$	$P_3$	$P_{40}$	$P_{56}$	$P_{70}$	$P_3$	$P_9$	$P_9$	$P_9$	$P_3$	$P_3$	$P_3$	$P_{40}$	$P_{56}$	$P_{70}$	$P_3$	$P_3$	$P_{56}$	$P_{70}$

Line 20 intersects

Line	$\ell_2$	$\ell_6$	$\ell_8$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{16}$	$\ell_{19}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$	$\ell_{29}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{39}$	$\ell_{42}$	$\ell_{43}$	$\ell_{45}$
in point	$P_9$	$P_{75}$	$P_4$	$P_{29}$	$P_4$	$P_{57}$	$P_{75}$	$P_{75}$	$P_9$	$P_9$	$P_9$	$P_4$	$P_{75}$	$P_4$	$P_{29}$	$P_{75}$	$P_{57}$	$P_4$	$P_{75}$	$P_4$	$P_{29}$

Line 21 intersects

Line	$\ell_2$	$\ell_4$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{22}$	$\ell_{25}$	$\ell_{30}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{40}$	$\ell_{42}$	$\ell_{43}$
in point	$P_9$	$P_{48}$	$P_{63}$	$P_{31}$	$P_{48}$	$P_{63}$	$P_{77}$	$P_{48}$	$P_9$	$P_9$	$P_9$	$P_{63}$	$P_{48}$	$P_{63}$	$P_{77}$	$P_{31}$	$P_{48}$	$P_{63}$	$P_{48}$	$P_{77}$

Line 22 intersects

Line	$\ell_2$	$\ell_5$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{26}$	$\ell_{28}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$
in point	$P_9$	$P_{66}$	$P_{84}$	$P_{36}$	$P_{49}$	$P_{66}$	$P_{84}$	$P_{66}$	$P_9$	$P_9$	$P_9$	$P_{84}$	$P_{66}$	$P_{84}$	$P_{66}$	$P_{49}$	$P_{36}$	$P_{84}$	$P_{66}$	$P_{36}$

Line 23 intersects

Line	$\ell_1$	$\ell_3$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{15}$	$\ell_{19}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{42}$
in point	$P_{10}$	$P_3$	$P_3$	$P_{41}$	$P_{54}$	$P_{71}$	$P_3$	$P_3$	$P_3$	$P_{10}$	$P_{10}$	$P_{10}$	$P_3$	$P_3$	$P_{41}$	$P_{54}$	$P_{71}$	$P_3$	$P_{54}$	$P_{71}$	$P_{41}$

Line 24 intersects

Line	$\ell_1$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{16}$	$\ell_{20}$	$\ell_{23}$	$\ell_{25}$	$\ell_{26}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{42}$
in point	$P_{10}$	$P_{60}$	$P_{28}$	$P_4$	$P_{60}$	$P_{73}$	$P_4$	$P_{60}$	$P_4$	$P_{10}$	$P_{10}$	$P_{10}$	$P_{60}$	$P_4$	$P_{28}$	$P_{73}$	$P_{60}$	$P_{73}$	$P_4$	$P_{28}$	$P_{73}$



Line 25 intersects

Line	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{13}$	$\ell_{17}$	$\ell_{21}$	$\ell_{23}$	$\ell_{24}$	$\ell_{26}$	$\ell_{28}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$
in point	$P_{10}$	$P_{78}$	$P_{33}$	$P_{45}$	$P_{63}$	$P_{78}$	$P_{63}$	$P_{78}$	$P_{63}$	$P_{10}$	$P_{10}$	$P_{10}$	$P_{78}$	$P_{63}$	$P_{78}$	$P_{33}$	$P_{45}$	$P_{45}$	$P_{78}$	$P_{63}$

Line 26 intersects

Line	$\ell_1$	$\ell_4$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{18}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{29}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$
in point	$P_{10}$	$P_{51}$	$P_{35}$	$P_{51}$	$P_{65}$	$P_{84}$	$P_{84}$	$P_{51}$	$P_{84}$	$P_{10}$	$P_{10}$	$P_{10}$	$P_{51}$	$P_{84}$	$P_{65}$	$P_{51}$	$P_{35}$	$P_{65}$	$P_{35}$	$P_{51}$

Line 27 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_{11}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{23}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{31}$	$\ell_{38}$	$\ell_{42}$	$\ell_{44}$	$\ell_{45}$
in point	$P_{11}$	$P_3$	$P_{42}$	$P_{61}$	$P_{81}$	$P_3$	$P_3$	$P_3$	$P_{42}$	$P_{61}$	$P_{81}$	$P_3$	$P_3$	$P_{11}$	$P_{11}$	$P_{11}$	$P_3$	$P_3$	$P_3$	$P_{61}$	$P_{81}$

Line 28 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{22}$	$\ell_{25}$	$\ell_{27}$	$\ell_{29}$	$\ell_{30}$	$\ell_{32}$	$\ell_{33}$	$\ell_{39}$	$\ell_{42}$
in point	$P_{11}$	$P_{27}$	$P_{39}$	$P_{66}$	$P_{78}$	$P_{78}$	$P_{66}$	$P_{39}$	$P_{27}$	$P_{78}$	$P_{66}$	$P_{66}$	$P_{78}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{78}$	$P_{66}$	$P_{78}$	$P_{66}$

Line 29 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$	$\ell_{30}$	$\ell_{34}$	$\ell_{35}$	$\ell_{40}$	$\ell_{42}$
in point	$P_{11}$	$P_{32}$	$P_{51}$	$P_{55}$	$P_{75}$	$P_{51}$	$P_{75}$	$P_{55}$	$P_{75}$	$P_{32}$	$P_{51}$	$P_{75}$	$P_{51}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{75}$	$P_{51}$	$P_{51}$	$P_{75}$

Line 30 intersects

Line	$\ell_0$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_9$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{21}$	$\ell_{24}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{36}$	$\ell_{37}$	$\ell_{41}$	$\ell_{42}$
in point	$P_{11}$	$P_{37}$	$P_{48}$	$P_{60}$	$P_{72}$	$P_{60}$	$P_{48}$	$P_{72}$	$P_{60}$	$P_{48}$	$P_{37}$	$P_{48}$	$P_{60}$	$P_{11}$	$P_{11}$	$P_{11}$	$P_{60}$	$P_{48}$	$P_{60}$	$P_{48}$

Line 31 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$
in point	$P_{12}$	$P_{12}$	$P_3$	$P_3$	$P_4$	$P_{63}$	$P_{84}$	$P_3$	$P_4$	$P_{63}$	$P_{84}$	$P_3$	$P_3$	$P_4$	$P_{63}$	$P_{84}$	$P_3$	$P_4$	$P_{63}$	$P_{84}$	$P_3$

Line 32 intersects

Line	$\ell_1$	$\ell_2$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{17}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{28}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{38}$
in point	$P_{12}$	$P_{12}$	$P_{78}$	$P_{28}$	$P_{41}$	$P_{65}$	$P_{78}$	$P_{78}$	$P_{41}$	$P_{28}$	$P_{78}$	$P_{65}$	$P_{78}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{65}$

Line 33 intersects

Line	$\ell_1$	$\ell_2$	$\ell_5$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{28}$	$\ell_{31}$	$\ell_{32}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{42}$
in point	$P_{12}$	$P_{12}$	$P_{66}$	$P_{29}$	$P_{40}$	$P_{66}$	$P_{77}$	$P_{66}$	$P_{40}$	$P_{29}$	$P_{77}$	$P_{66}$	$P_{66}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{66}$

Line 34 intersects

Line	$\ell_1$	$\ell_2$	$\ell_6$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{16}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{29}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{35}$	$\ell_{36}$	$\ell_{37}$	$\ell_{42}$
in point	$P_{12}$	$P_{12}$	$P_{75}$	$P_{31}$	$P_{49}$	$P_{56}$	$P_{75}$	$P_{75}$	$P_{56}$	$P_{75}$	$P_{31}$	$P_{49}$	$P_{75}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{75}$

Line 35 intersects

Line	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{18}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{29}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{36}$	$\ell_{37}$	$\ell_{38}$
in point	$P_{12}$	$P_{12}$	$P_{51}$	$P_{33}$	$P_{51}$	$P_{54}$	$P_{73}$	$P_{51}$	$P_{54}$	$P_{73}$	$P_{33}$	$P_{51}$	$P_{51}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{73}$

Line 36 intersects

Line	$\ell_1$	$\ell_2$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{16}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{37}$	$\ell_{38}$
in point	$P_{12}$	$P_{12}$	$P_{60}$	$P_{35}$	$P_{45}$	$P_{60}$	$P_{71}$	$P_{60}$	$P_{71}$	$P_{60}$	$P_{45}$	$P_{35}$	$P_{60}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{45}$

Line 37 intersects

Line	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{33}$	$\ell_{34}$	$\ell_{35}$	$\ell_{36}$	$\ell_{42}$
in point	$P_{12}$	$P_{12}$	$P_{48}$	$P_{36}$	$P_{48}$	$P_{57}$	$P_{70}$	$P_{48}$	$P_{70}$	$P_{57}$	$P_{48}$	$P_{36}$	$P_{48}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{12}$	$P_{48}$

Line 38 intersects

Line	$\ell_1$	$\ell_3$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{15}$	$\ell_{19}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$
in point	$P_{15}$	$P_3$	$P_3$	$P_{45}$	$P_{65}$	$P_{73}$	$P_3$	$P_3$	$P_3$	$P_3$	$P_{73}$	$P_{45}$	$P_{65}$	$P_3$	$P_3$	$P_{65}$	$P_{73}$	$P_{45}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 39 intersects

Line	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{17}$	$\ell_{20}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{28}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{40}$	$\ell_{41}$
in point	$P_{15}$	$P_{78}$	$P_{35}$	$P_4$	$P_{54}$	$P_{78}$	$P_4$	$P_{78}$	$P_4$	$P_{54}$	$P_4$	$P_{78}$	$P_{35}$	$P_{78}$	$P_4$	$P_{78}$	$P_{54}$	$P_{35}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 40 intersects

Line	$\ell_1$	$\ell_4$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{13}$	$\ell_{18}$	$\ell_{21}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{29}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$
in point	$P_{15}$	$P_{51}$	$P_{28}$	$P_{51}$	$P_{63}$	$P_{71}$	$P_{63}$	$P_{51}$	$P_{63}$	$P_{71}$	$P_{28}$	$P_{63}$	$P_{51}$	$P_{51}$	$P_{63}$	$P_{28}$	$P_{51}$	$P_{71}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 41 intersects

Line	$\ell_1$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{16}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{30}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$
in point	$P_{15}$	$P_{60}$	$P_{33}$	$P_{41}$	$P_{60}$	$P_{84}$	$P_{84}$	$P_{60}$	$P_{84}$	$P_{41}$	$P_{60}$	$P_{33}$	$P_{84}$	$P_{60}$	$P_{84}$	$P_{41}$	$P_{33}$	$P_{60}$	$P_{15}$	$P_{15}$	$P_{15}$

Line 42 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$
in point	$P_{18}$	$P_{18}$	$P_3$	$P_{48}$	$P_{66}$	$P_{75}$	$P_3$	$P_3$	$P_{48}$	$P_{66}$	$P_{75}$	$P_3$	$P_{75}$	$P_{48}$	$P_{66}$	$P_3$	$P_{75}$	$P_{48}$	$P_{66}$	$P_3$	$P_{48}$

Line 43 intersects

Line	$\ell_0$	$\ell_2$	$\ell_8$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{39}$	$\ell_{42}$	$\ell_{44}$	$\ell_{45}$	$\ell_{46}$
in point	$P_{18}$	$P_{18}$	$P_4$	$P_{36}$	$P_4$	$P_{56}$	$P_{77}$	$P_{56}$	$P_4$	$P_{77}$	$P_{36}$	$P_4$	$P_4$	$P_{77}$	$P_{56}$	$P_{36}$	$P_4$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 44 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{26}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{35}$	$\ell_{40}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$
in point	$P_{18}$	$P_{18}$	$P_{27}$	$P_{51}$	$P_{61}$	$P_{72}$	$P_{51}$	$P_{72}$	$P_{27}$	$P_{61}$	$P_{51}$	$P_{51}$	$P_{61}$	$P_{27}$	$P_{51}$	$P_{72}$	$P_{51}$	$P_{51}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 45 intersects

Line	$\ell_0$	$\ell_2$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{25}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{40}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$	$\ell_{45}$
in point	$P_{18}$	$P_{18}$	$P_{63}$	$P_{29}$	$P_{49}$	$P_{63}$	$P_{70}$	$P_{70}$	$P_{29}$	$P_{63}$	$P_{49}$	$P_{63}$	$P_{63}$	$P_{29}$	$P_{49}$	$P_{70}$	$P_{63}$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 46 intersects

Line	$\ell_0$	$\ell_2$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{26}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$	$\ell_{45}$
in point	$P_{18}$	$P_{18}$	$P_{84}$	$P_{31}$	$P_{40}$	$P_{57}$	$P_{84}$	$P_{40}$	$P_{57}$	$P_{31}$	$P_{84}$	$P_{84}$	$P_{84}$	$P_{40}$	$P_{31}$	$P_{57}$	$P_{84}$	$P_{18}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 47 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_9$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{24}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{36}$	$\ell_{41}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$
in point	$P_{18}$	$P_{18}$	$P_{32}$	$P_{39}$	$P_{60}$	$P_{81}$	$P_{60}$	$P_{39}$	$P_{60}$	$P_{32}$	$P_{81}$	$P_{60}$	$P_{81}$	$P_{39}$	$P_{32}$	$P_{60}$	$P_{60}$	$P_{60}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 48 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{10}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{25}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{32}$	$\ell_{39}$	$\ell_{42}$	$\ell_{43}$	$\ell_{44}$
in point	$P_{18}$	$P_{18}$	$P_{37}$	$P_{42}$	$P_{55}$	$P_{78}$	$P_{78}$	$P_{55}$	$P_{42}$	$P_{78}$	$P_{37}$	$P_{78}$	$P_{42}$	$P_{78}$	$P_{55}$	$P_{37}$	$P_{78}$	$P_{78}$	$P_{18}$	$P_{18}$	$P_{18}$

Line 49 intersects

Line	$\ell_2$	$\ell_3$	$\ell_7$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{27}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{38}$	$\ell_{42}$	$\ell_{43}$
in point	$P_{19}$	$P_3$	$P_3$	$P_3$	$P_{49}$	$P_{57}$	$P_{77}$	$P_3$	$P_3$	$P_{57}$	$P_{77}$	$P_{49}$	$P_3$	$P_3$	$P_3$	$P_{77}$	$P_{49}$	$P_{57}$	$P_3$	$P_3$	$P_{77}$

Line 50 intersects

Line	$\ell_2$	$\ell_5$	$\ell_8$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$	$\ell_{28}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{39}$	$\ell_{42}$	$\ell_{43}$
in point	$P_{19}$	$P_{66}$	$P_4$	$P_{31}$	$P_4$	$P_{66}$	$P_{70}$	$P_{66}$	$P_{70}$	$P_4$	$P_{31}$	$P_{66}$	$P_4$	$P_{66}$	$P_4$	$P_{66}$	$P_{31}$	$P_{70}$	$P_4$	$P_{66}$	$P_{66}$

Line 51 intersects

Line	$\ell_2$	$\ell_4$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{26}$	$\ell_{30}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{41}$	$\ell_{42}$
in point	$P_{19}$	$P_{48}$	$P_{84}$	$P_{29}$	$P_{48}$	$P_{56}$	$P_{84}$	$P_{48}$	$P_{56}$	$P_{29}$	$P_{48}$	$P_{84}$	$P_{84}$	$P_{48}$	$P_{84}$	$P_{29}$	$P_{56}$	$P_{48}$	$P_{84}$	$P_{48}$

Line 52 intersects

Line	$\ell_2$	$\ell_6$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{16}$	$\ell_{19}$	$\ell_{20}$	$\ell_{21}$	$\ell_{22}$	$\ell_{25}$	$\ell_{29}$	$\ell_{31}$	$\ell_{33}$	$\ell_{34}$	$\ell_{37}$	$\ell_{40}$	$\ell_{42}$
in point	$P_{19}$	$P_{75}$	$P_{63}$	$P_{36}$	$P_{40}$	$P_{63}$	$P_{75}$	$P_{75}$	$P_{40}$	$P_{75}$	$P_{63}$	$P_{36}$	$P_{63}$	$P_{75}$	$P_{63}$	$P_{40}$	$P_{75}$	$P_{36}$	$P_{63}$	$P_{75}$

Line 53 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{27}$
in point	$P_{21}$	$P_{21}$	$P_3$	$P_{51}$	$P_{60}$	$P_{78}$	$P_3$	$P_{51}$	$P_{60}$	$P_{78}$	$P_3$	$P_3$	$P_{60}$	$P_{78}$	$P_{51}$	$P_3$	$P_3$	$P_{60}$	$P_{78}$	$P_{51}$	$P_3$

Line 54 intersects

Line	$\ell_0$	$\ell_1$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{20}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$	$\ell_{42}$
in point	$P_{21}$	$P_{21}$	$P_{33}$	$P_4$	$P_{65}$	$P_{71}$	$P_4$	$P_4$	$P_{71}$	$P_4$	$P_{33}$	$P_{65}$	$P_4$	$P_{65}$	$P_{33}$	$P_{71}$	$P_{65}$	$P_4$	$P_{71}$	$P_{33}$	$P_4$

Line 55 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{21}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{37}$	$\ell_{42}$	$\ell_{44}$	$\ell_{47}$
in point	$P_{21}$	$P_{21}$	$P_{27}$	$P_{48}$	$P_{55}$	$P_{81}$	$P_{48}$	$P_{55}$	$P_{27}$	$P_{48}$	$P_{81}$	$P_{48}$	$P_{81}$	$P_{27}$	$P_{55}$	$P_{48}$	$P_{48}$	$P_{48}$	$P_{27}$	$P_8$

Line 56 intersects

Line	$\ell_0$	$\ell_1$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{14}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$	$\ell_{42}$
in point	$P_{21}$	$P_{21}$	$P_{28}$	$P_{45}$	$P_{54}$	$P_{84}$	$P_{84}$	$P_{84}$	$P_{54}$	$P_{28}$	$P_{45}$	$P_{84}$	$P_{84}$	$P_{28}$	$P_{54}$	$P_{45}$	$P_{45}$	$P_{54}$	$P_{28}$	$P_8$	$P_8$

Line 57 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{22}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{33}$	$\ell_{42}$	$\ell_{44}$	$\ell_{47}$
in point	$P_{21}$	$P_{21}$	$P_{32}$	$P_{42}$	$P_{66}$	$P_{72}$	$P_{66}$	$P_{72}$	$P_{42}$	$P_{32}$	$P_{66}$	$P_{66}$	$P_{42}$	$P_{66}$	$P_{32}$	$P_{72}$	$P_{66}$	$P_{66}$	$P_{72}$	$P_3$

Line 58 intersects

Line	$\ell_0$	$\ell_1$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{13}$	$\ell_{21}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$	$\ell_{31}$	$\ell_{32}$	$\ell_{35}$	$\ell_{36}$	$\ell_{38}$	$\ell_{39}$	$\ell_{40}$	$\ell_{41}$	$\ell_{42}$
in point	$P_{21}$	$P_{21}$	$P_{35}$	$P_{41}$	$P_{63}$	$P_{73}$	$P_{63}$	$P_{63}$	$P_{41}$	$P_{73}$	$P_{63}$	$P_{35}$	$P_{63}$	$P_{41}$	$P_{73}$	$P_{35}$	$P_{73}$	$P_{35}$	$P_{63}$	$P_4$	$P_4$

Line 59 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{27}$	$\ell_{28}$	$\ell_{29}$	$\ell_{30}$	$\ell_{34}$	$\ell_{42}$	$\ell_{44}$	$\ell_{47}$
in point	$P_{21}$	$P_{21}$	$P_{37}$	$P_{39}$	$P_{61}$	$P_{75}$	$P_{75}$	$P_{39}$	$P_{75}$	$P_{61}$	$P_{37}$	$P_{75}$	$P_{61}$	$P_{39}$	$P_{75}$	$P_{37}$	$P_{75}$	$P_{75}$	$P_{61}$	$P_3$

The surface has 49 points:

The points on the surface are:

$$0 : P_3 = (0, 0, 0, 1)$$

$$1 : P_4 = (1, 1, 1, 1)$$

$$2 : P_5 = (1, 1, 0, 0)$$

$$3 : P_6 = (2, 1, 0, 0)$$

$$4 : P_7 = (3, 1, 0, 0)$$

$$5 : P_8 = (1, 0, 1, 0)$$

$$6 : P_9 = (2, 0, 1, 0)$$

$$7 : P_{10} = (3, 0, 1, 0)$$

$$8 : P_{11} = (0, 1, 1, 0)$$

$$9 : P_{12} = (1, 1, 1, 0)$$

$$10 : P_{15} = (0, 2, 1, 0)$$

$$11 : P_{18} = (3, 2, 1, 0)$$

$$12 : P_{19} = (0, 3, 1, 0)$$

$$13 : P_{21} = (2, 3, 1, 0)$$

$$14 : P_{27} = (1, 1, 0, 1)$$

$$15 : P_{28} = (2, 1, 0, 1)$$

$$16 : P_{29} = (3, 1, 0, 1)$$

$$17 : P_{31} = (1, 2, 0, 1)$$

$$18 : P_{32} = (2, 2, 0, 1)$$

$$19 : P_{33} = (3, 2, 0, 1)$$

$$20 : P_{35} = (1, 3, 0, 1)$$

$$21 : P_{36} = (2, 3, 0, 1)$$

$$22 : P_{37} = (3, 3, 0, 1)$$

$$23 : P_{39} = (1, 0, 1, 1)$$

$$24 : P_{40} = (2, 0, 1, 1)$$

$$25 : P_{41} = (3, 0, 1, 1)$$

$$26 : P_{42} = (0, 1, 1, 1)$$

27 :  $P_{45} = (0, 2, 1, 1)$   
 28 :  $P_{48} = (3, 2, 1, 1)$   
 29 :  $P_{49} = (0, 3, 1, 1)$   
 30 :  $P_{51} = (2, 3, 1, 1)$   
 31 :  $P_{54} = (1, 0, 2, 1)$   
 32 :  $P_{55} = (2, 0, 2, 1)$   
 33 :  $P_{56} = (3, 0, 2, 1)$   
 34 :  $P_{57} = (0, 1, 2, 1)$

35 :  $P_{60} = (3, 1, 2, 1)$   
 36 :  $P_{61} = (0, 2, 2, 1)$   
 37 :  $P_{63} = (2, 2, 2, 1)$   
 38 :  $P_{65} = (0, 3, 2, 1)$   
 39 :  $P_{66} = (1, 3, 2, 1)$   
 40 :  $P_{70} = (1, 0, 3, 1)$   
 41 :  $P_{71} = (2, 0, 3, 1)$   
 42 :  $P_{72} = (3, 0, 3, 1)$

43 :  $P_{73} = (0, 1, 3, 1)$   
 44 :  $P_{75} = (2, 1, 3, 1)$   
 45 :  $P_{77} = (0, 2, 3, 1)$   
 46 :  $P_{78} = (1, 2, 3, 1)$   
 47 :  $P_{81} = (0, 3, 3, 1)$   
 48 :  $P_{84} = (3, 3, 3, 1)$