

Rank-66764 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^3 + X_3^3 + X_0^2 X_3 + X_0 X_1^2 + X_0 X_2^2 + X_0 X_1 X_2 = 0$$

(1, 0, 0, 1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is -2112814042

General information

Number of lines	1
Number of points	1089
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	33
Number of points off lines	1056
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33
Type of lines on points	$1^{33}, 0^{1056}$

Singular Points

The surface has 0 singular points:

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1082368} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1082368} = \mathbf{Pl}(0, 0, 0, 0, 0, 1)_{34849}$$

Rank of lines: (1082368)

Rank of points on Klein quadric: (34849)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 33 single points:

The single points on the surface are:

- | | |
|--|---|
| 0 : $P_1 = (0, 1, 0, 0)$ lies on line ℓ_0 | 17 : $P_{547} = (0, 16, 1, 0)$ lies on line ℓ_0 |
| 1 : $P_2 = (0, 0, 1, 0)$ lies on line ℓ_0 | 18 : $P_{579} = (0, 17, 1, 0)$ lies on line ℓ_0 |
| 2 : $P_{67} = (0, 1, 1, 0)$ lies on line ℓ_0 | 19 : $P_{611} = (0, 18, 1, 0)$ lies on line ℓ_0 |
| 3 : $P_{99} = (0, 2, 1, 0)$ lies on line ℓ_0 | 20 : $P_{643} = (0, 19, 1, 0)$ lies on line ℓ_0 |
| 4 : $P_{131} = (0, 3, 1, 0)$ lies on line ℓ_0 | 21 : $P_{675} = (0, 20, 1, 0)$ lies on line ℓ_0 |
| 5 : $P_{163} = (0, 4, 1, 0)$ lies on line ℓ_0 | 22 : $P_{707} = (0, 21, 1, 0)$ lies on line ℓ_0 |
| 6 : $P_{195} = (0, 5, 1, 0)$ lies on line ℓ_0 | 23 : $P_{739} = (0, 22, 1, 0)$ lies on line ℓ_0 |
| 7 : $P_{227} = (0, 6, 1, 0)$ lies on line ℓ_0 | 24 : $P_{771} = (0, 23, 1, 0)$ lies on line ℓ_0 |
| 8 : $P_{259} = (0, 7, 1, 0)$ lies on line ℓ_0 | 25 : $P_{803} = (0, 24, 1, 0)$ lies on line ℓ_0 |
| 9 : $P_{291} = (0, 8, 1, 0)$ lies on line ℓ_0 | 26 : $P_{835} = (0, 25, 1, 0)$ lies on line ℓ_0 |
| 10 : $P_{323} = (0, 9, 1, 0)$ lies on line ℓ_0 | 27 : $P_{867} = (0, 26, 1, 0)$ lies on line ℓ_0 |
| 11 : $P_{355} = (0, 10, 1, 0)$ lies on line ℓ_0 | 28 : $P_{899} = (0, 27, 1, 0)$ lies on line ℓ_0 |
| 12 : $P_{387} = (0, 11, 1, 0)$ lies on line ℓ_0 | 29 : $P_{931} = (0, 28, 1, 0)$ lies on line ℓ_0 |
| 13 : $P_{419} = (0, 12, 1, 0)$ lies on line ℓ_0 | 30 : $P_{963} = (0, 29, 1, 0)$ lies on line ℓ_0 |
| 14 : $P_{451} = (0, 13, 1, 0)$ lies on line ℓ_0 | 31 : $P_{995} = (0, 30, 1, 0)$ lies on line ℓ_0 |
| 15 : $P_{483} = (0, 14, 1, 0)$ lies on line ℓ_0 | 32 : $P_{1027} = (0, 31, 1, 0)$ lies on line ℓ_0 |
| 16 : $P_{515} = (0, 15, 1, 0)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 1056 points not on any line:

Too many to print.

Line Intersection Graph

$$\begin{array}{c|c} 0 & \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line
in point

The surface has 1089 points:

Too many to print.