Rank-74053 over GF(32)

January 15, 2021

The equation

The equation of the surface is:

$$X_1^3 + X_0^2 X_3 + X_1^2 X_2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0) The point rank of the equation over GF(32) is -2112846779

General information

Number of lines	4
Number of points	1089
Number of singular points	1
Number of Eckardt points	1
Number of double points	1
Number of single points	127
Number of points off lines	960
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^{4}
Type of lines on points	$3, 2, 1^{127}, 0^{960}$

Singular Points

The surface has 1 singular points:

$$0: P_2 = \mathbf{P}(0,0,1,0) = \mathbf{P}(0,0,1,0)$$

The 4 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1024} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1024} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2$$

$$\ell_{1} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1083424} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1083424} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_{1}$$

$$\ell_{2} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{34848} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{34848} = \mathbf{Pl}(0, 1, 1, 0, 0, 0)_{34}$$

$$\ell_{3} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082433} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082433} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{97}$$

Rank of lines: (1024, 1083424, 34848, 1082433) Rank of points on Klein quadric: (2, 1, 34, 97)

Eckardt Points

The surface has 1 Eckardt points: $0: P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0).$

Double Points

The surface has 1 Double points: The double points on the surface are:

$$P_3 = (0,0,0,1) = \ell_1 \cap \ell_3$$

Single Points

The surface has 127 single points: The single points on the surface are:

$0: P_0 = (1,0,0,0)$ lies on line ℓ_0	23: $P_{58} = (23, 0, 1, 0)$ lies on line ℓ_0
1: $P_{36} = (1,0,1,0)$ lies on line ℓ_0	24: $P_{59} = (24, 0, 1, 0)$ lies on line ℓ_0
2: $P_{37} = (2,0,1,0)$ lies on line ℓ_0	25: $P_{60} = (25, 0, 1, 0)$ lies on line ℓ_0
$3: P_{38} = (3,0,1,0)$ lies on line ℓ_0	26: $P_{61} = (26, 0, 1, 0)$ lies on line ℓ_0
4: $P_{39} = (4,0,1,0)$ lies on line ℓ_0	27: $P_{62} = (27, 0, 1, 0)$ lies on line ℓ_0
5: $P_{40} = (5, 0, 1, 0)$ lies on line ℓ_0	28: $P_{63} = (28, 0, 1, 0)$ lies on line ℓ_0
6: $P_{41} = (6, 0, 1, 0)$ lies on line ℓ_0	29: $P_{64} = (29, 0, 1, 0)$ lies on line ℓ_0
7: $P_{42} = (7, 0, 1, 0)$ lies on line ℓ_0	$30: P_{65} = (30, 0, 1, 0)$ lies on line ℓ_0
8: $P_{43} = (8,0,1,0)$ lies on line ℓ_0	$31: P_{66} = (31, 0, 1, 0)$ lies on line ℓ_0
9: $P_{44} = (9, 0, 1, 0)$ lies on line ℓ_0	$32: P_{67} = (0, 1, 1, 0)$ lies on line ℓ_3
10: $P_{45} = (10, 0, 1, 0)$ lies on line ℓ_0	33: $P_{1059} = (1, 0, 0, 1)$ lies on line ℓ_2
11: $P_{46} = (11, 0, 1, 0)$ lies on line ℓ_0	$34: P_{2082} = (0,0,1,1)$ lies on line ℓ_1
12: $P_{47} = (12, 0, 1, 0)$ lies on line ℓ_0	$35: P_{2083} = (1,0,1,1)$ lies on line ℓ_2
13: $P_{48} = (13, 0, 1, 0)$ lies on line ℓ_0	$36: P_{2114} = (0, 1, 1, 1)$ lies on line ℓ_3
14: $P_{49} = (14, 0, 1, 0)$ lies on line ℓ_0	$37: P_{3105} = (0,0,2,1)$ lies on line ℓ_1
15: $P_{50} = (15, 0, 1, 0)$ lies on line ℓ_0	38: $P_{3106} = (1,0,2,1)$ lies on line ℓ_2
16: $P_{51} = (16, 0, 1, 0)$ lies on line ℓ_0	39: $P_{3169} = (0, 2, 2, 1)$ lies on line ℓ_3
17: $P_{52} = (17, 0, 1, 0)$ lies on line ℓ_0	40: $P_{4129} = (0,0,3,1)$ lies on line ℓ_1
18: $P_{53} = (18, 0, 1, 0)$ lies on line ℓ_0	41: $P_{4130} = (1,0,3,1)$ lies on line ℓ_2
19: $P_{54} = (19, 0, 1, 0)$ lies on line ℓ_0	$42: P_{4225} = (0, 3, 3, 1)$ lies on line ℓ_3
20: $P_{55} = (20, 0, 1, 0)$ lies on line ℓ_0	43: $P_{5153} = (0, 0, 4, 1)$ lies on line ℓ_1
21: $P_{56} = (21, 0, 1, 0)$ lies on line ℓ_0	44: $P_{5154} = (1, 0, 4, 1)$ lies on line ℓ_2
22: $P_{57} = (22, 0, 1, 0)$ lies on line ℓ_0	$45: P_{5281} = (0, 4, 4, 1)$ lies on line ℓ_3

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87: P_{20065} = (0, 18, 18, 1) lies on line \ell_3
46: P_{6177} = (0,0,5,1) lies on line \ell_1
                                                                     88: P_{20513} = (0, 0, 19, 1) lies on line \ell_1
47: P_{6178} = (1, 0, 5, 1) lies on line \ell_2
48: P_{6337} = (0, 5, 5, 1) lies on line \ell_3
                                                                     89: P_{20514} = (1, 0, 19, 1) lies on line \ell_2
49: P_{7201} = (0,0,6,1) lies on line \ell_1
                                                                     90: P_{21121} = (0, 19, 19, 1) lies on line \ell_3
50: P_{7202} = (1,0,6,1) lies on line \ell_2
                                                                     91: P_{21537} = (0, 0, 20, 1) lies on line \ell_1
51: P_{7393} = (0,6,6,1) lies on line \ell_3
                                                                     92: P_{21538} = (1, 0, 20, 1) lies on line \ell_2
                                                                     93: P_{22177} = (0, 20, 20, 1) lies on line \ell_3
52: P_{8225} = (0,0,7,1) lies on line \ell_1
53: P_{8226} = (1,0,7,1) lies on line \ell_2
                                                                     94: P_{22561} = (0, 0, 21, 1) lies on line \ell_1
54: P_{8449} = (0,7,7,1) lies on line \ell_3
                                                                     95: P_{22562} = (1, 0, 21, 1) lies on line \ell_2
55: P_{9249} = (0,0,8,1) lies on line \ell_1
                                                                     96: P_{23233} = (0, 21, 21, 1) lies on line \ell_3
56: P_{9250} = (1,0,8,1) lies on line \ell_2
                                                                     97: P_{23585} = (0, 0, 22, 1) lies on line \ell_1
57: P_{9505} = (0, 8, 8, 1) lies on line \ell_3
                                                                     98: P_{23586} = (1, 0, 22, 1) lies on line \ell_2
58: P_{10273} = (0, 0, 9, 1) lies on line \ell_1
                                                                     99: P_{24289} = (0, 22, 22, 1) lies on line \ell_3
59: P_{10274} = (1,0,9,1) lies on line \ell_2
                                                                     100: P_{24609} = (0, 0, 23, 1) lies on line \ell_1
60: P_{10561} = (0, 9, 9, 1) lies on line \ell_3
                                                                     101: P_{24610} = (1, 0, 23, 1) lies on line \ell_2
61: P_{11297} = (0, 0, 10, 1) lies on line \ell_1
                                                                     102: P_{25345} = (0, 23, 23, 1) lies on line \ell_3
62: P_{11298} = (1, 0, 10, 1) lies on line \ell_2
                                                                     103: P_{25633} = (0, 0, 24, 1) lies on line \ell_1
63: P_{11617} = (0, 10, 10, 1) lies on line \ell_3
                                                                     104: P_{25634} = (1, 0, 24, 1) lies on line \ell_2
64: P_{12321} = (0, 0, 11, 1) lies on line \ell_1
                                                                     105: P_{26401} = (0, 24, 24, 1) lies on line \ell_3
65: P_{12322} = (1, 0, 11, 1) lies on line \ell_2
                                                                     106: P_{26657} = (0, 0, 25, 1) lies on line \ell_1
66: P_{12673} = (0, 11, 11, 1) lies on line \ell_3
                                                                     107: P_{26658} = (1, 0, 25, 1) lies on line \ell_2
67: P_{13345} = (0, 0, 12, 1) lies on line \ell_1
                                                                     108: P_{27457} = (0, 25, 25, 1) lies on line \ell_3
68: P_{13346} = (1, 0, 12, 1) lies on line \ell_2
                                                                     109: P_{27681} = (0, 0, 26, 1) lies on line \ell_1
69: P_{13729} = (0, 12, 12, 1) lies on line \ell_3
                                                                     110 : P_{27682} = (1, 0, 26, 1) lies on line \ell_2
70: P_{14369} = (0, 0, 13, 1) lies on line \ell_1
                                                                     111: P_{28513} = (0, 26, 26, 1) lies on line \ell_3
                                                                     112 : P_{28705} = (0, 0, 27, 1) lies on line \ell_1
71: P_{14370} = (1, 0, 13, 1) lies on line \ell_2
72: P_{14785} = (0, 13, 13, 1) lies on line \ell_3
                                                                     113: P_{28706} = (1, 0, 27, 1) lies on line \ell_2
73: P_{15393} = (0, 0, 14, 1) lies on line \ell_1
                                                                     114: P_{29569} = (0, 27, 27, 1) lies on line \ell_3
74: P_{15394} = (1, 0, 14, 1) lies on line \ell_2
                                                                     115: P_{29729} = (0, 0, 28, 1) lies on line \ell_1
75: P_{15841} = (0, 14, 14, 1) lies on line \ell_3
                                                                     116: P_{29730} = (1, 0, 28, 1) lies on line \ell_2
76: P_{16417} = (0, 0, 15, 1) lies on line \ell_1
                                                                     117: P_{30625} = (0, 28, 28, 1) lies on line \ell_3
77: P_{16418} = (1, 0, 15, 1) lies on line \ell_2
                                                                     118: P_{30753} = (0, 0, 29, 1) lies on line \ell_1
78: P_{16897} = (0, 15, 15, 1) lies on line \ell_3
                                                                     119: P_{30754} = (1, 0, 29, 1) lies on line \ell_2
79 : P_{17441} = (0, 0, 16, 1) lies on line \ell_1
                                                                     120: P_{31681} = (0, 29, 29, 1) lies on line \ell_3
80: P_{17442} = (1, 0, 16, 1) lies on line \ell_2
                                                                     121: P_{31777} = (0, 0, 30, 1) lies on line \ell_1
81 : P_{17953} = (0, 16, 16, 1) lies on line \ell_3
                                                                     122: P_{31778} = (1, 0, 30, 1) lies on line \ell_2
82: P_{18465} = (0, 0, 17, 1) lies on line \ell_1
                                                                     123: P_{32737} = (0, 30, 30, 1) lies on line \ell_3
83: P_{18466} = (1, 0, 17, 1) lies on line \ell_2
                                                                     124: P_{32801} = (0, 0, 31, 1) lies on line \ell_1
                                                                     125 : P_{32802} = (1, 0, 31, 1) lies on line \ell_2
84: P_{19009} = (0, 17, 17, 1) lies on line \ell_3
85: P_{19489} = (0, 0, 18, 1) lies on line \ell_1
                                                                     126: P_{33793} = (0, 31, 31, 1) lies on line \ell_3
86: P_{19490} = (1, 0, 18, 1) lies on line \ell_2
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The single points on the surface are:

Points on surface but on no line

The surface has 960 points not on any line: The points on the surface but not on lines are:

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\begin{array}{lll} 0: \, P_{105} = (6,2,1,0) & 3: \, P_{215} = (20,5,1,0) \\ 1: \, P_{137} = (6,3,1,0) & 4: \, P_{245} = (18,6,1,0) \\ 2: \, P_{183} = (20,4,1,0) & 5: \, P_{277} = (18,7,1,0) \end{array}
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60: P_{2158} = (13, 2, 1, 1)
6: P_{293} = (2, 8, 1, 0)
7: P_{325} = (2, 9, 1, 0)
                                                                  61: P_{2159} = (14, 2, 1, 1)
8: P_{359} = (4, 10, 1, 0)
                                                                  62: P_{2205} = (28, 3, 1, 1)
9: P_{391} = (4, 11, 1, 0)
                                                                  63: P_{2207} = (30, 3, 1, 1)
10: P_{441} = (22, 12, 1, 0)
                                                                  64: P_{2236} = (27, 4, 1, 1)
11: P_{473} = (22, 13, 1, 0)
                                                                  65: P_{2239} = (30, 4, 1, 1)
12: P_{499} = (16, 14, 1, 0)
                                                                  66: P_{2260} = (19, 5, 1, 1)
13: P_{531} = (16, 15, 1, 0)
                                                                  67: P_{2264} = (23, 5, 1, 1)
14: P_{576} = (29, 16, 1, 0)
                                                                  68: P_{2298} = (25, 6, 1, 1)
15: P_{608} = (29, 17, 1, 0)
                                                                  69: P_{2303} = (30, 6, 1, 1)
16: P_{638} = (27, 18, 1, 0)
                                                                  70: P_{2358} = (21, 8, 1, 1)
17: P_{670} = (27, 19, 1, 0)
                                                                  71: P_{2365} = (28, 8, 1, 1)
18: P_{684} = (9, 20, 1, 0)
                                                                  72: P_{2424} = (23, 10, 1, 1)
19: P_{716} = (9, 21, 1, 0)
                                                                  73: P_{2429} = (28, 10, 1, 1)
20: P_{754} = (15, 22, 1, 0)
                                                                  74: P_{2472} = (7, 12, 1, 1)
21: P_{786} = (15, 23, 1, 0)
                                                                  75: P_{2475} = (10, 12, 1, 1)
22: P_{834} = (31, 24, 1, 0)
                                                                  76: P_{2501} = (4, 13, 1, 1)
23: P_{866} = (31, 25, 1, 0)
                                                                  77: P_{2505} = (8, 13, 1, 1)
24: P_{892} = (25, 26, 1, 0)
                                                                  78: P_{2552} = (23, 14, 1, 1)
25: P_{924} = (25, 27, 1, 0)
                                                                  79: P_{2553} = (24, 14, 1, 1)
26: P_{942} = (11, 28, 1, 0)
                                                                  80: P_{2595} = (2, 16, 1, 1)
27: P_{974} = (11, 29, 1, 0)
                                                                  81: P_{2612} = (19, 16, 1, 1)
28: P_{1008} = (13, 30, 1, 0)
                                                                  82: P_{2633} = (8, 17, 1, 1)
29: P_{1040} = (13, 31, 1, 0)
                                                                  83: P_{2649} = (24, 17, 1, 1)
30: P_{1176} = (22, 3, 0, 1)
                                                                  84: P_{2696} = (7, 19, 1, 1)
31: P_{1177} = (23, 3, 0, 1)
                                                                  85: P_{2710} = (21, 19, 1, 1)
32: P_{1242} = (24, 5, 0, 1)
                                                                  86: P_{2727} = (6, 20, 1, 1)
33: P_{1243} = (25, 5, 0, 1)
                                                                  87: P_{2740} = (19, 20, 1, 1)
34: P_{1292} = (10, 7, 0, 1)
                                                                  88: P_{2795} = (10, 22, 1, 1)
35: P_{1293} = (11, 7, 0, 1)
                                                                  89: P_{2814} = (29, 22, 1, 1)
36: P_{1372} = (26, 9, 0, 1)
                                                                  90: P_{2895} = (14, 25, 1, 1)
37: P_{1373} = (27, 9, 0, 1)
                                                                  91: P_{2903} = (22, 25, 1, 1)
38: P_{1412} = (2, 11, 0, 1)
                                                                  92: P_{2927} = (14, 26, 1, 1)
                                                                  93: P_{2934} = (21, 26, 1, 1)
39: P_{1413} = (3, 11, 0, 1)
40: P_{1462} = (20, 12, 0, 1)
                                                                  94: P_{2955} = (10, 27, 1, 1)
41: P_{1463} = (21, 12, 0, 1)
                                                                  95: P_{2961} = (16, 27, 1, 1)
42: P_{1542} = (4, 15, 0, 1)
                                                                  96: P_{3017} = (8, 29, 1, 1)
                                                                  97: P_{3029} = (20, 29, 1, 1)
43: P_{1543} = (5, 15, 0, 1)
44: P_{1608} = (6, 17, 0, 1)
                                                                  98: P_{3048} = (7, 30, 1, 1)
45: P_{1609} = (7, 17, 0, 1)
                                                                  99: P_{3065} = (24, 30, 1, 1)
46: P_{1646} = (12, 18, 0, 1)
                                                                  100: P_{3174} = (5, 2, 2, 1)
                                                                  101: P_{3225} = (24, 3, 2, 1)
47: P_{1647} = (13, 18, 0, 1)
48: P_{1744} = (14, 21, 0, 1)
                                                                  102: P_{3232} = (31, 3, 2, 1)
                                                                  103: P_{3240} = (7, 4, 2, 1)
49: P_{1745} = (15, 21, 0, 1)
50: P_{1812} = (18, 23, 0, 1)
                                                                  104: P_{3247} = (14, 4, 2, 1)
                                                                  105: P_{3268} = (3, 5, 2, 1)
51: P_{1813} = (19, 23, 0, 1)
52: P_{1834} = (8, 24, 0, 1)
                                                                  106: P_{3273} = (8, 5, 2, 1)
53: P_{1835} = (9, 24, 0, 1)
                                                                  107: P_{3366} = (5, 8, 2, 1)
                                                                  108: P_{3381} = (20, 8, 2, 1)
54: P_{1918} = (28, 26, 0, 1)
55: P_{1919} = (29, 26, 0, 1)
                                                                  109: P_{3428} = (3, 10, 2, 1)
56: P_{1984} = (30, 28, 0, 1)
                                                                  110: P_{3447} = (22, 10, 2, 1)
57: P_{1985} = (31, 28, 0, 1)
                                                                  111: P_{3490} = (1, 12, 2, 1)
58: P_{2066} = (16, 31, 0, 1)
                                                                  112: P_{3513} = (24, 12, 2, 1)
59: P_{2067} = (17, 31, 0, 1)
                                                                  113: P_{3524} = (3, 13, 2, 1)
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114: P_{3545} = (24, 13, 2, 1)
                                                                 168: P_{5702} = (5, 17, 4, 1)
115: P_{3554} = (1, 14, 2, 1)
                                                                 169: P_{5707} = (10, 17, 4, 1)
116: P_{3581} = (28, 14, 2, 1)
                                                                 170: P_{5788} = (27, 19, 4, 1)
                                                                 171: P_{5789} = (28, 19, 4, 1)
117: P_{3667} = (18, 17, 2, 1)
118: P_{3669} = (20, 17, 2, 1)
                                                                 172: P_{5986} = (1, 26, 4, 1)
119: P_{3683} = (2, 18, 2, 1)
                                                                 173: P_{5992} = (7, 26, 4, 1)
120: P_{3768} = (23, 20, 2, 1)
                                                                 174: P_{6022} = (5, 27, 4, 1)
121: P_{3772} = (27, 20, 2, 1)
                                                                 175: P_{6024} = (7, 27, 4, 1)
122: P_{3781} = (4, 21, 2, 1)
                                                                 176: P_{6063} = (14, 28, 4, 1)
123: P_{3787} = (10, 21, 2, 1)
                                                                 177: P_{6065} = (16, 28, 4, 1)
124: P_{3975} = (6, 27, 2, 1)
                                                                 178: P_{6083} = (2, 29, 4, 1)
125: P_{3989} = (20, 27, 2, 1)
                                                                 179: P_{6105} = (24, 29, 4, 1)
126: P_{4078} = (13, 30, 2, 1)
                                                                 180: P_{6114} = (1, 30, 4, 1)
127: P_{4086} = (21, 30, 2, 1)
                                                                 181: P_{6136} = (23, 30, 4, 1)
128: P_{4173} = (12, 1, 3, 1)
                                                                 182: P_{6235} = (26, 1, 5, 1)
129: P_{4175} = (14, 1, 3, 1)
                                                                 183: P_{6239} = (30, 1, 5, 1)
130: P_{4229} = (4, 3, 3, 1)
                                                                 184 : P_{6353} = (16, 5, 5, 1)
                                                                 185: P_{6508} = (11, 10, 5, 1)
131: P_{4263} = (6, 4, 3, 1)
132: P_{4268} = (11, 4, 3, 1)
                                                                 186: P_{6510} = (13, 10, 5, 1)
133: P_{4394} = (9, 8, 3, 1)
                                                                 187: P_{6538} = (9, 11, 5, 1)
134: P_{4401} = (16, 8, 3, 1)
                                                                 188: P_{6539} = (10, 11, 5, 1)
135: P_{4425} = (8, 9, 3, 1)
                                                                 189: P_{6569} = (8, 12, 5, 1)
136: P_{4435} = (18, 9, 3, 1)
                                                                 190: P_{6577} = (16, 12, 5, 1)
137: P_{4528} = (15, 12, 3, 1)
                                                                 191: P_{6704} = (15, 16, 5, 1)
138: P_{4539} = (26, 12, 3, 1)
                                                                 192: P_{6709} = (20, 16, 5, 1)
139: P_{4590} = (13, 14, 3, 1)
                                                                 193: P_{6757} = (4, 18, 5, 1)
140: P_{4607} = (30, 14, 3, 1)
                                                                 194: P_{6774} = (21, 18, 5, 1)
141: P_{4612} = (3, 15, 3, 1)
                                                                 195: P_{6889} = (8, 22, 5, 1)
142: P_{4628} = (19, 15, 3, 1)
                                                                 196: P_{6894} = (13, 22, 5, 1)
143 : P_{4677} = (4, 17, 3, 1)
                                                                 197: P_{6930} = (17, 23, 5, 1)
144: P_{4692} = (19, 17, 3, 1)
                                                                 198: P_{6990} = (13, 25, 5, 1)
145: P_{4783} = (14, 20, 3, 1)
                                                                 199: P_{7007} = (30, 25, 5, 1)
146: P_{4791} = (22, 20, 3, 1)
                                                                 200: P_{7012} = (3, 26, 5, 1)
147: P_{4847} = (14, 22, 3, 1)
                                                                 201: P_{7040} = (31, 26, 5, 1)
                                                                 202: P_{7130} = (25, 29, 5, 1)
148: P_{4849} = (16, 22, 3, 1)
                                                                 203: P_{7135} = (30, 29, 5, 1)
149: P_{5030} = (5, 28, 3, 1)
150: P_{5073} = (16, 29, 3, 1)
                                                                 204: P_{7156} = (19, 30, 5, 1)
                                                                 205: P_{7164} = (27, 30, 5, 1)
151: P_{5076} = (19, 29, 3, 1)
152: P_{5123} = (2, 31, 3, 1)
                                                                 206: P_{7174} = (5, 31, 5, 1)
153: P_{5128} = (7, 31, 3, 1)
                                                                 207: P_{7177} = (8, 31, 5, 1)
154: P_{5237} = (20, 2, 4, 1)
                                                                 208: P_{7288} = (23, 2, 6, 1)
155: P_{5246} = (29, 2, 4, 1)
                                                                 209: P_{7291} = (26, 2, 6, 1)
156: P_{5298} = (17, 4, 4, 1)
                                                                 210: P_{7371} = (10, 5, 6, 1)
                                                                 211: P_{7382} = (21, 5, 6, 1)
157: P_{5320} = (7, 5, 4, 1)
158: P_{5331} = (18, 5, 4, 1)
                                                                 212: P_{7414} = (21, 6, 6, 1)
159: P_{5445} = (4, 9, 4, 1)
                                                                 213: P_{7428} = (3,7,6,1)
160: P_{5490} = (17, 10, 4, 1)
                                                                 214: P_{7441} = (16, 7, 6, 1)
161: P_{5502} = (29, 10, 4, 1)
                                                                 215: P_{7463} = (6, 8, 6, 1)
                                                                 216: P_{7475} = (18, 8, 6, 1)
162: P_{5546} = (9, 12, 4, 1)
163: P_{5566} = (29, 12, 4, 1)
                                                                 217: P_{7561} = (8, 11, 6, 1)
                                                                 218: P_{7575} = (22, 11, 6, 1)
164: P_{5606} = (5, 14, 4, 1)
165: P_{5626} = (25, 14, 4, 1)
                                                                 219: P_{7658} = (9, 14, 6, 1)
166: P_{5686} = (21, 16, 4, 1)
                                                                 220: P_{7850} = (9, 20, 6, 1)
167: P_{5695} = (30, 16, 4, 1)
                                                                 221: P_{7872} = (31, 20, 6, 1)
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222: P_{8106} = (9, 28, 6, 1)
                                                                 276: P_{9910} = (21, 20, 8, 1)
223: P_{8107} = (10, 28, 6, 1)
                                                                 277: P_{9933} = (12, 21, 8, 1)
224: P_{8164} = (3, 30, 6, 1)
                                                                 278: P_{9941} = (20, 21, 8, 1)
225: P_{8173} = (12, 30, 6, 1)
                                                                 279: P_{9979} = (26, 22, 8, 1)
226: P_{8196} = (3, 31, 6, 1)
                                                                 280: P_{10006} = (21, 23, 8, 1)
227: P_{8203} = (10, 31, 6, 1)
                                                                 281: P_{10014} = (29, 23, 8, 1)
228: P_{8292} = (3, 2, 7, 1)
                                                                 282: P_{10019} = (2, 24, 8, 1)
229: P_{8301} = (12, 2, 7, 1)
                                                                 283: P_{10046} = (29, 24, 8, 1)
230: P_{8323} = (2, 3, 7, 1)
                                                                 284: P_{10055} = (6, 25, 8, 1)
231: P_{8331} = (10, 3, 7, 1)
                                                                 285: P_{10066} = (17, 25, 8, 1)
232: P_{8368} = (15, 4, 7, 1)
                                                                 286: P_{10087} = (6, 26, 8, 1)
233: P_{8371} = (18, 4, 7, 1)
                                                                 287: P_{10090} = (9, 26, 8, 1)
234: P_{8426} = (9, 6, 7, 1)
                                                                 288: P_{10138} = (25, 27, 8, 1)
                                                                 289: P_{10143} = (30, 27, 8, 1)
235: P_{8443} = (26, 6, 7, 1)
236: P_{8469} = (20, 7, 7, 1)
                                                                 290: P_{10153} = (8, 28, 8, 1)
237: P_{8516} = (3, 9, 7, 1)
                                                                 291: P_{10163} = (18, 28, 8, 1)
238: P_{8537} = (24, 9, 7, 1)
                                                                 292: P_{10213} = (4, 30, 8, 1)
239: P_{8581} = (4, 11, 7, 1)
                                                                 293: P_{10223} = (14, 30, 8, 1)
                                                                 294: P_{10250} = (9, 31, 8, 1)
240: P_{8594} = (17, 11, 7, 1)
241: P_{8612} = (3, 12, 7, 1)
                                                                 295: P_{10252} = (11, 31, 8, 1)
242: P_{8679} = (6, 14, 7, 1)
                                                                 296: P_{10312} = (7, 1, 9, 1)
243: P_{8681} = (8, 14, 7, 1)
                                                                 297: P_{10320} = (15, 1, 9, 1)
244: P_{8771} = (2, 17, 7, 1)
                                                                 298: P_{10411} = (10, 4, 9, 1)
245: P_{8796} = (27, 17, 7, 1)
                                                                 299: P_{10469} = (4, 6, 9, 1)
246: P_{8878} = (13, 20, 7, 1)
                                                                 300: P_{10487} = (22, 6, 9, 1)
247: P_{8880} = (15, 20, 7, 1)
                                                                 301: P_{10511} = (14, 7, 9, 1)
248: P_{8899} = (2, 21, 7, 1)
                                                                 302: P_{10518} = (21, 7, 9, 1)
249: P_{8904} = (7, 21, 7, 1)
                                                                 303: P_{10553} = (24, 8, 9, 1)
250: P_{8965} = (4, 23, 7, 1)
                                                                 304: P_{10556} = (27, 8, 9, 1)
251: P_{8976} = (15, 23, 7, 1)
                                                                 305: P_{10571} = (10, 9, 9, 1)
252: P_{9044} = (19, 25, 7, 1)
                                                                 306: P_{10724} = (3, 14, 9, 1)
253: P_{9048} = (23, 25, 7, 1)
                                                                 307: P_{10740} = (19, 14, 9, 1)
254: P_{9077} = (20, 26, 7, 1)
                                                                 308: P_{10759} = (6, 15, 9, 1)
255: P_{9082} = (25, 26, 7, 1)
                                                                 309: P_{10784} = (31, 15, 9, 1)
256: P_{9093} = (4, 27, 7, 1)
                                                                 310: P_{10786} = (1, 16, 9, 1)
257: P_{9103} = (14, 27, 7, 1)
                                                                 311: P_{10789} = (4, 16, 9, 1)
258: P_{9297} = (16, 1, 8, 1)
                                                                 312: P_{10820} = (3, 17, 9, 1)
259: P_{9306} = (25, 1, 8, 1)
                                                                 313: P_{10832} = (15, 17, 9, 1)
260: P_{9320} = (7, 2, 8, 1)
                                                                 314: P_{10980} = (3, 22, 9, 1)
261: P_{9335} = (22, 2, 8, 1)
                                                                 315: P_{10998} = (21, 22, 9, 1)
262: P_{9474} = (1,7,8,1)
                                                                 316: P_{11014} = (5, 23, 9, 1)
263: P_{9502} = (29, 7, 8, 1)
                                                                 317: P_{11035} = (26, 23, 9, 1)
264: P_{9516} = (11, 8, 8, 1)
                                                                 318: P_{11059} = (18, 24, 9, 1)
265: P_{9607} = (6, 11, 8, 1)
                                                                 319: P_{11062} = (21, 24, 9, 1)
266: P_{9622} = (21, 11, 8, 1)
                                                                 320: P_{11074} = (1, 25, 9, 1)
267: P_{9674} = (9, 13, 8, 1)
                                                                 321: P_{11088} = (15, 25, 9, 1)
268: P_{9680} = (15, 13, 8, 1)
                                                                 322: P_{11242} = (9, 30, 9, 1)
269: P_{9730} = (1, 15, 8, 1)
                                                                 323: P_{11262} = (29, 30, 9, 1)
270: P_{9752} = (23, 15, 8, 1)
                                                                 324: P_{11269} = (4, 31, 9, 1)
271: P_{9774} = (13, 16, 8, 1)
                                                                 325: P_{11290} = (25, 31, 9, 1)
272: P_{9785} = (24, 16, 8, 1)
                                                                 326: P_{11335} = (6, 1, 10, 1)
273: P_{9850} = (25, 18, 8, 1)
                                                                 327: P_{11342} = (13, 1, 10, 1)
274: P_{9853} = (28, 18, 8, 1)
                                                                 328: P_{11367} = (6, 2, 10, 1)
275: P_{9894} = (5, 20, 8, 1)
                                                                 329: P_{11380} = (19, 2, 10, 1)
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384: P_{13021} = (28, 21, 11, 1)
330: P_{11404} = (11, 3, 10, 1)
331: P_{11413} = (20, 3, 10, 1)
                                                                385: P_{13023} = (30, 21, 11, 1)
332: P_{11446} = (21, 4, 10, 1)
                                                                386: P_{13092} = (3, 24, 11, 1)
333: P_{11450} = (25, 4, 10, 1)
                                                                387: P_{13106} = (17, 24, 11, 1)
334: P_{11501} = (12, 6, 10, 1)
                                                                388: P_{13126} = (5, 25, 11, 1)
335: P_{11509} = (20, 6, 10, 1)
                                                                389: P_{13149} = (28, 25, 11, 1)
336: P_{11525} = (4, 7, 10, 1)
                                                                390: P_{13286} = (5, 30, 11, 1)
337: P_{11543} = (22, 7, 10, 1)
                                                                391: P_{13289} = (8, 30, 11, 1)
338: P_{11591} = (6, 9, 10, 1)
                                                                392: P_{13331} = (18, 31, 11, 1)
339: P_{11608} = (23, 9, 10, 1)
                                                                393: P_{13333} = (20, 31, 11, 1)
340: P_{11632} = (15, 10, 10, 1)
                                                                394: P_{13382} = (5, 1, 12, 1)
341: P_{11720} = (7, 13, 10, 1)
                                                                395: P_{13385} = (8, 1, 12, 1)
342: P_{11740} = (27, 13, 10, 1)
                                                                396: P_{13455} = (14, 3, 12, 1)
343: P_{11797} = (20, 15, 10, 1)
                                                                397: P_{13468} = (27, 3, 12, 1)
344: P_{11805} = (28, 15, 10, 1)
                                                                398: P_{13514} = (9, 5, 12, 1)
345: P_{11884} = (11, 18, 10, 1)
                                                                399: P_{13522} = (17, 5, 12, 1)
346: P_{11888} = (15, 18, 10, 1)
                                                                400: P_{13539} = (2, 6, 12, 1)
347: P_{11921} = (16, 19, 10, 1)
                                                                401: P_{13551} = (14, 6, 12, 1)
348: P_{11935} = (30, 19, 10, 1)
                                                                402: P_{13595} = (26, 7, 12, 1)
349: P_{11970} = (1, 21, 10, 1)
                                                                403: P_{13605} = (4, 8, 12, 1)
350: P_{11991} = (22, 21, 10, 1)
                                                                404: P_{13611} = (10, 8, 12, 1)
351: P_{12042} = (9, 23, 10, 1)
                                                                405: P_{13645} = (12, 9, 12, 1)
352: P_{12043} = (10, 23, 10, 1)
                                                                406: P_{13647} = (14, 9, 12, 1)
353: P_{12087} = (22, 24, 10, 1)
                                                                407: P_{13710} = (13, 11, 12, 1)
354: P_{12093} = (28, 24, 10, 1)
                                                                408: P_{13720} = (23, 11, 12, 1)
355: P_{12100} = (3, 25, 10, 1)
                                                                409: P_{13756} = (27, 12, 12, 1)
356: P_{12172} = (11, 27, 10, 1)
                                                                410: P_{13987} = (2, 20, 12, 1)
357: P_{12192} = (31, 27, 10, 1)
                                                                411: P_{13993} = (8, 20, 12, 1)
358: P_{12219} = (26, 28, 10, 1)
                                                                412: P_{14153} = (8, 25, 12, 1)
359: P_{12222} = (29, 28, 10, 1)
                                                                413: P_{14165} = (20, 25, 12, 1)
360: P_{12242} = (17, 29, 10, 1)
                                                                414: P_{14227} = (18, 27, 12, 1)
361: P_{12253} = (28, 29, 10, 1)
                                                                415: P_{14231} = (22, 27, 12, 1)
362: P_{12290} = (1, 31, 10, 1)
                                                                416: P_{14307} = (2, 30, 12, 1)
363: P_{12313} = (24, 31, 10, 1)
                                                                417: P_{14336} = (31, 30, 12, 1)
                                                                418: P_{14352} = (15, 31, 12, 1)
364: P_{12374} = (21, 1, 11, 1)
365: P_{12384} = (31, 1, 11, 1)
                                                                419: P_{14367} = (30, 31, 12, 1)
366: P_{12514} = (1, 6, 11, 1)
                                                                420: P_{14480} = (15, 3, 13, 1)
                                                                421: P_{14490} = (25, 3, 13, 1)
367: P_{12544} = (31, 6, 11, 1)
368: P_{12554} = (9, 7, 11, 1)
                                                                422: P_{14509} = (12, 4, 13, 1)
369: P_{12573} = (28, 7, 11, 1)
                                                                423: P_{14525} = (28, 4, 13, 1)
370: P_{12643} = (2, 10, 11, 1)
                                                                424: P_{14530} = (1, 5, 13, 1)
371: P_{12648} = (7, 10, 11, 1)
                                                                425: P_{14557} = (28, 5, 13, 1)
372: P_{12687} = (14, 11, 11, 1)
                                                                426: P_{14626} = (1, 8, 13, 1)
373: P_{12710} = (5, 12, 11, 1)
                                                                427: P_{14632} = (7, 8, 13, 1)
374: P_{12736} = (31, 12, 11, 1)
                                                                428: P_{14693} = (4, 10, 13, 1)
375: P_{12738} = (1, 13, 11, 1)
                                                                429: P_{14713} = (24, 10, 13, 1)
376: P_{12753} = (16, 13, 11, 1)
                                                                430: P_{14764} = (11, 12, 13, 1)
377: P_{12847} = (14, 16, 11, 1)
                                                                431: P_{14781} = (28, 12, 13, 1)
378: P_{12903} = (6, 18, 11, 1)
                                                                432: P_{14811} = (26, 13, 13, 1)
379: P_{12913} = (16, 18, 11, 1)
                                                                433: P_{14862} = (13, 15, 13, 1)
380: P_{12940} = (11, 19, 11, 1)
                                                                434: P_{14903} = (22, 16, 13, 1)
381: P_{12951} = (22, 19, 11, 1)
                                                                435: P_{14906} = (25, 16, 13, 1)
382: P_{12977} = (16, 20, 11, 1)
                                                                436: P_{14989} = (12, 19, 13, 1)
383: P_{12986} = (25, 20, 11, 1)
                                                                437: P_{14997} = (20, 19, 13, 1)
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438: P_{15156} = (19, 24, 13, 1)
                                                                492: P_{16688} = (15, 8, 15, 1)
439: P_{15164} = (27, 24, 13, 1)
                                                                493: P_{16698} = (25, 8, 15, 1)
440: P_{15185} = (16, 25, 13, 1)
                                                                494: P_{16718} = (13, 9, 15, 1)
441: P_{15190} = (21, 25, 13, 1)
                                                                495: P_{16725} = (20, 9, 15, 1)
442: P_{15213} = (12, 26, 13, 1)
                                                                496: P_{16863} = (30, 13, 15, 1)
443: P_{15231} = (30, 26, 13, 1)
                                                                497: P_{16869} = (4, 14, 15, 1)
444: P_{15241} = (8, 27, 13, 1)
                                                                498: P_{16886} = (21, 14, 15, 1)
445: P_{15256} = (23, 27, 13, 1)
                                                                499: P_{16927} = (30, 15, 15, 1)
446: P_{15354} = (25, 30, 13, 1)
                                                                500: P_{17002} = (9, 18, 15, 1)
447: P_{15355} = (26, 30, 13, 1)
                                                                501: P_{17022} = (29, 18, 15, 1)
448: P_{15445} = (20, 1, 14, 1)
                                                                502: P_{17035} = (10, 19, 15, 1)
449: P_{15452} = (27, 1, 14, 1)
                                                                503: P_{17042} = (17, 19, 15, 1)
450: P_{15472} = (15, 2, 14, 1)
                                                                504: P_{17058} = (1, 20, 15, 1)
451: P_{15475} = (18, 2, 14, 1)
                                                                505: P_{17075} = (18, 20, 15, 1)
452: P_{15529} = (8, 4, 14, 1)
                                                                506: P_{17100} = (11, 21, 15, 1)
453: P_{15541} = (20, 4, 14, 1)
                                                                507: P_{17112} = (23, 21, 15, 1)
                                                                508: P_{17266} = (17, 26, 15, 1)
454: P_{15568} = (15, 5, 14, 1)
455: P_{15582} = (29, 5, 14, 1)
                                                                509: P_{17267} = (18, 26, 15, 1)
                                                                510: P_{17282} = (1, 27, 15, 1)
456: P_{15590} = (5, 6, 14, 1)
457: P_{15640} = (23, 7, 14, 1)
                                                                511: P_{17294} = (13, 27, 15, 1)
458: P_{15642} = (25, 7, 14, 1)
                                                                512: P_{17332} = (19, 28, 15, 1)
459: P_{15662} = (13, 8, 14, 1)
                                                                513: P_{17336} = (23, 28, 15, 1)
460: P_{15668} = (19, 8, 14, 1)
                                                                514: P_{17351} = (6, 29, 15, 1)
461: P_{15696} = (15, 9, 14, 1)
                                                                515: P_{17358} = (13, 29, 15, 1)
462: P_{15712} = (31, 9, 14, 1)
                                                                516: P_{17522} = (17, 2, 16, 1)
463: P_{15765} = (20, 11, 14, 1)
                                                                517: P_{17526} = (21, 2, 16, 1)
464: P_{15769} = (24, 11, 14, 1)
                                                                518: P_{17538} = (1, 3, 16, 1)
465: P_{15872} = (31, 14, 14, 1)
                                                                519: P_{17558} = (21, 3, 16, 1)
466: P_{15911} = (6, 16, 14, 1)
                                                                520: P_{17591} = (22, 4, 16, 1)
                                                                521: P_{17598} = (29, 4, 16, 1)
467: P_{15933} = (28, 16, 14, 1)
468: P_{15970} = (1, 18, 14, 1)
                                                                522: P_{17699} = (2, 8, 16, 1)
469: P_{15976} = (7, 18, 14, 1)
                                                                523: P_{17720} = (23, 8, 16, 1)
470: P_{16059} = (26, 20, 14, 1)
                                                                524: P_{17809} = (16, 11, 16, 1)
471: P_{16062} = (29, 20, 14, 1)
                                                                525: P_{17839} = (14, 12, 16, 1)
472: P_{16081} = (16, 21, 14, 1)
                                                                526: P_{17842} = (17, 12, 16, 1)
473: P_{16090} = (25, 21, 14, 1)
                                                                527: P_{17876} = (19, 13, 16, 1)
474: P_{16109} = (12, 22, 14, 1)
                                                                528: P_{17885} = (28, 13, 16, 1)
475: P_{16120} = (23, 22, 14, 1)
                                                                529: P_{17901} = (12, 14, 16, 1)
                                                                530: P_{17911} = (22, 14, 16, 1)
476: P_{16132} = (3, 23, 14, 1)
477: P_{16151} = (22, 23, 14, 1)
                                                                531: P_{17965} = (12, 16, 16, 1)
478: P_{16172} = (11, 24, 14, 1)
                                                                532: P_{17994} = (9, 17, 16, 1)
                                                                533: P_{18006} = (21, 17, 16, 1)
479: P_{16175} = (14, 24, 14, 1)
480: P_{16259} = (2, 27, 14, 1)
                                                                534: P_{18050} = (1, 19, 16, 1)
481: P_{16278} = (21, 27, 14, 1)
                                                                535: P_{18073} = (24, 19, 16, 1)
482: P_{16290} = (1, 28, 14, 1)
                                                                536: P_{18149} = (4, 22, 16, 1)
483: P_{16314} = (25, 28, 14, 1)
                                                                537: P_{18152} = (7, 22, 16, 1)
484: P_{16408} = (23, 31, 14, 1)
                                                                538: P_{18190} = (13, 23, 16, 1)
485: P_{16414} = (29, 31, 14, 1)
                                                                539: P_{18207} = (30, 23, 16, 1)
486: P_{16467} = (18, 1, 15, 1)
                                                                540: P_{18284} = (11, 26, 16, 1)
487: P_{16477} = (28, 1, 15, 1)
                                                                541: P_{18295} = (22, 26, 16, 1)
488: P_{16626} = (17, 6, 15, 1)
                                                                542: P_{18407} = (6, 30, 16, 1)
489: P_{16632} = (23, 6, 15, 1)
                                                                543: P_{18418} = (17, 30, 16, 1)
490: P_{16646} = (5, 7, 15, 1)
                                                                544: P_{18500} = (3, 1, 17, 1)
491: P_{16653} = (12, 7, 15, 1)
                                                                545: P_{18516} = (19, 1, 17, 1)
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546: P_{18566} = (5, 3, 17, 1)
                                                                600: P_{20549} = (4, 1, 19, 1)
547: P_{18579} = (18, 3, 17, 1)
                                                                601: P_{20567} = (22, 1, 19, 1)
548: P_{18676} = (19, 6, 17, 1)
                                                                602: P_{20657} = (16, 4, 19, 1)
549: P_{18684} = (27, 6, 17, 1)
                                                                603: P_{20664} = (23, 4, 19, 1)
550: P_{18769} = (16, 9, 17, 1)
                                                                604: P_{20708} = (3, 6, 19, 1)
551: P_{18781} = (28, 9, 17, 1)
                                                                605: P_{20712} = (7, 6, 19, 1)
552: P_{18910} = (29, 13, 17, 1)
                                                                606: P_{20743} = (6, 7, 19, 1)
553: P_{18912} = (31, 13, 17, 1)
                                                                607: P_{20754} = (17, 7, 19, 1)
554: P_{18928} = (15, 14, 17, 1)
                                                                608: P_{20808} = (7, 9, 19, 1)
555: P_{18940} = (27, 14, 17, 1)
                                                                609: P_{20826} = (25, 9, 19, 1)
556: P_{18956} = (11, 15, 17, 1)
                                                                610: P_{20866} = (1, 11, 19, 1)
557: P_{18959} = (14, 15, 17, 1)
                                                                611: P_{20893} = (28, 11, 19, 1)
558: P_{19022} = (13, 17, 17, 1)
                                                                612: P_{20915} = (18, 12, 19, 1)
559: P_{19051} = (10, 18, 17, 1)
                                                                613: P_{20922} = (25, 12, 19, 1)
560: P_{19058} = (17, 18, 17, 1)
                                                                614: P_{20943} = (14, 13, 19, 1)
561: P_{19075} = (2, 19, 17, 1)
                                                                615: P_{20951} = (22, 13, 19, 1)
562: P_{19081} = (8, 19, 17, 1)
                                                                616: P_{20963} = (2, 14, 19, 1)
563: P_{19175} = (6, 22, 17, 1)
                                                                617: P_{20971} = (10, 14, 19, 1)
564: P_{19188} = (19, 22, 17, 1)
                                                                618: P_{21002} = (9, 15, 19, 1)
565: P_{19245} = (12, 24, 17, 1)
                                                                619: P_{21011} = (18, 15, 19, 1)
566: P_{19275} = (10, 25, 17, 1)
                                                                620: P_{21036} = (11, 16, 19, 1)
567: P_{19292} = (27, 25, 17, 1)
                                                                621: P_{21043} = (18, 16, 19, 1)
568: P_{19307} = (10, 26, 17, 1)
                                                                622: P_{21130} = (9, 19, 19, 1)
569: P_{19310} = (13, 26, 17, 1)
                                                                623: P_{21204} = (19, 21, 19, 1)
570: P_{19532} = (11, 1, 18, 1)
                                                                624: P_{21216} = (31, 21, 19, 1)
571: P_{19545} = (24, 1, 18, 1)
                                                                625: P_{21222} = (5, 22, 19, 1)
                                                                626: P_{21242} = (25, 22, 19, 1)
572: P_{19561} = (8, 2, 18, 1)
573: P_{19618} = (1, 4, 18, 1)
                                                                627: P_{21269} = (20, 23, 19, 1)
574: P_{19619} = (2, 4, 18, 1)
                                                                628: P_{21276} = (27, 23, 19, 1)
575: P_{19660} = (11, 5, 18, 1)
                                                                629: P_{21282} = (1, 24, 19, 1)
576: P_{19675} = (26, 5, 18, 1)
                                                                630: P_{21301} = (20, 24, 19, 1)
577: P_{19835} = (26, 10, 18, 1)
                                                                631: P_{21401} = (24, 27, 19, 1)
578: P_{19839} = (30, 10, 18, 1)
                                                                632: P_{21406} = (29, 27, 19, 1)
579: P_{19856} = (15, 11, 18, 1)
                                                                633: P_{21416} = (7, 28, 19, 1)
580: P_{19866} = (25, 11, 18, 1)
                                                                634: P_{21429} = (20, 28, 19, 1)
581: P_{19955} = (18, 14, 18, 1)
                                                                635: P_{21453} = (12, 29, 19, 1)
582: P_{19957} = (20, 14, 18, 1)
                                                                636: P_{21526} = (21, 31, 19, 1)
583: P_{19971} = (2, 15, 18, 1)
                                                                637: P_{21527} = (22, 31, 19, 1)
584: P_{19991} = (22, 15, 18, 1)
                                                                638: P_{21668} = (3, 4, 20, 1)
585: P_{20073} = (8, 18, 18, 1)
                                                                639: P_{21689} = (24, 4, 20, 1)
586: P_{20110} = (13, 19, 18, 1)
                                                                640: P_{21866} = (9, 10, 20, 1)
587: P_{20120} = (23, 19, 18, 1)
                                                                641: P_{21877} = (20, 10, 20, 1)
588: P_{20194} = (1, 22, 18, 1)
                                                                642: P_{22027} = (10, 15, 20, 1)
                                                                643: P_{22042} = (25, 15, 20, 1)
589: P_{20204} = (11, 22, 18, 1)
590: P_{20232} = (7, 23, 18, 1)
                                                                644: P_{22095} = (14, 17, 20, 1)
591: P_{20256} = (31, 23, 18, 1)
                                                                645: P_{22109} = (28, 17, 20, 1)
592: P_{20264} = (7, 24, 18, 1)
                                                                646: P_{22118} = (5, 18, 20, 1)
593: P_{20267} = (10, 24, 18, 1)
                                                                647: P_{22127} = (14, 18, 20, 1)
594: P_{20291} = (2, 25, 18, 1)
                                                                648: P_{22150} = (5, 19, 20, 1)
595: P_{20318} = (29, 25, 18, 1)
                                                                649: P_{22171} = (26, 19, 20, 1)
596: P_{20388} = (3, 28, 18, 1)
                                                                650: P_{22205} = (28, 20, 20, 1)
597: P_{20397} = (12, 28, 18, 1)
                                                                651: P_{22214} = (5, 21, 20, 1)
598: P_{20424} = (7, 29, 18, 1)
                                                                652: P_{22222} = (13, 21, 20, 1)
599: P_{20443} = (26, 29, 18, 1)
                                                                653: P_{22284} = (11, 23, 20, 1)
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654: P_{22287} = (14, 23, 20, 1)
                                                                708: P_{24718} = (13, 3, 23, 1)
655: P_{22476} = (11, 29, 20, 1)
                                                                709: P_{24721} = (16, 3, 23, 1)
656: P_{22483} = (18, 29, 20, 1)
                                                                710: P_{24781} = (12, 5, 23, 1)
657: P_{22508} = (11, 30, 20, 1)
                                                                711: P_{24887} = (22, 8, 23, 1)
658: P_{22641} = (16, 2, 21, 1)
                                                                712: P_{24895} = (30, 8, 23, 1)
659: P_{22655} = (30, 2, 21, 1)
                                                                713: P_{25006} = (13, 12, 23, 1)
660: P_{22663} = (6, 3, 21, 1)
                                                                714: P_{25012} = (19, 12, 23, 1)
661: P_{22686} = (29, 3, 21, 1)
                                                                715: P_{25030} = (5, 13, 23, 1)
662: P_{22694} = (5, 4, 21, 1)
                                                                716: P_{25037} = (12, 13, 23, 1)
663: P_{22715} = (26, 4, 21, 1)
                                                                717: P_{25129} = (8, 16, 23, 1)
664: P_{22725} = (4, 5, 21, 1)
                                                                718: P_{25148} = (27, 16, 23, 1)
665: P_{22735} = (14, 5, 21, 1)
                                                                719: P_{25178} = (25, 17, 23, 1)
666: P_{22761} = (8, 6, 21, 1)
                                                                720: P_{25182} = (29, 17, 23, 1)
667: P_{22777} = (24, 6, 21, 1)
                                                                721: P_{25188} = (3, 18, 23, 1)
668: P_{22918} = (5, 11, 21, 1)
                                                                722: P_{25212} = (27, 18, 23, 1)
669: P_{22920} = (7, 11, 21, 1)
                                                                723: P_{25290} = (9, 21, 23, 1)
670: P_{22947} = (2, 12, 21, 1)
                                                                724: P_{25308} = (27, 21, 23, 1)
                                                                725: P_{25330} = (17, 22, 23, 1)
671: P_{22949} = (4, 12, 21, 1)
                                                                726: P_{25344} = (31, 22, 23, 1)
672: P_{23053} = (12, 15, 21, 1)
673: P_{23057} = (16, 15, 21, 1)
                                                                727: P_{25370} = (25, 23, 23, 1)
674: P_{23082} = (9, 16, 21, 1)
                                                                728: P_{25390} = (13, 24, 23, 1)
675: P_{23104} = (31, 16, 21, 1)
                                                                729: P_{25400} = (23, 24, 23, 1)
676: P_{23204} = (3, 20, 21, 1)
                                                                730: P_{25413} = (4, 25, 23, 1)
677: P_{23212} = (11, 20, 21, 1)
                                                                731: P_{25418} = (9, 25, 23, 1)
678: P_{23262} = (29, 21, 21, 1)
                                                                732: P_{25482} = (9, 27, 23, 1)
679: P_{23345} = (16, 24, 21, 1)
                                                                733: P_{25488} = (15, 27, 23, 1)
680: P_{23360} = (31, 24, 21, 1)
                                                                734: P_{25551} = (14, 29, 23, 1)
681: P_{23398} = (5, 26, 21, 1)
                                                                735: P_{25558} = (21, 29, 23, 1)
682: P_{23461} = (4, 28, 21, 1)
                                                                736: P_{25613} = (12, 31, 23, 1)
683: P_{23478} = (21, 28, 21, 1)
                                                                737: P_{25629} = (28, 31, 23, 1)
684: P_{23516} = (27, 29, 21, 1)
                                                                738: P_{25708} = (11, 2, 24, 1)
685: P_{23520} = (31, 29, 21, 1)
                                                                739: P_{25728} = (31, 2, 24, 1)
686: P_{23531} = (10, 30, 21, 1)
                                                                740: P_{25806} = (13, 5, 24, 1)
687: P_{23541} = (20, 30, 21, 1)
                                                                741: P_{25820} = (27, 5, 24, 1)
688: P_{23828} = (19, 7, 22, 1)
                                                                742: P_{25836} = (11, 6, 24, 1)
689: P_{23840} = (31, 7, 22, 1)
                                                                743: P_{25841} = (16, 6, 24, 1)
690: P_{23872} = (31, 8, 22, 1)
                                                                744: P_{25881} = (24, 7, 24, 1)
                                                                745: P_{25884} = (27, 7, 24, 1)
691: P_{23910} = (5, 10, 22, 1)
692: P_{23917} = (12, 10, 22, 1)
                                                                746: P_{25923} = (2, 9, 24, 1)
693: P_{23949} = (12, 11, 22, 1)
                                                                747: P_{25926} = (5, 9, 24, 1)
694: P_{23956} = (19, 11, 22, 1)
                                                                748: P_{25972} = (19, 10, 24, 1)
                                                                749: P_{25978} = (25, 10, 24, 1)
695: P_{24018} = (17, 13, 22, 1)
696: P_{24022} = (21, 13, 22, 1)
                                                                750: P_{26023} = (6, 12, 24, 1)
697: P_{24181} = (20, 18, 22, 1)
                                                                751: P_{26039} = (22, 12, 24, 1)
698: P_{24191} = (30, 18, 22, 1)
                                                                752: P_{26051} = (2, 13, 24, 1)
699: P_{24313} = (24, 22, 22, 1)
                                                                753: P_{26059} = (10, 13, 24, 1)
700: P_{24323} = (2, 23, 22, 1)
                                                                754: P_{26203} = (26, 17, 24, 1)
701: P_{24333} = (12, 23, 22, 1)
                                                                755: P_{26232} = (23, 18, 24, 1)
702: P_{24396} = (11, 25, 22, 1)
                                                                756: P_{26235} = (26, 18, 24, 1)
703: P_{24416} = (31, 25, 22, 1)
                                                                757: P_{26365} = (28, 22, 24, 1)
                                                                758: P_{26367} = (30, 22, 24, 1)
704: P_{24436} = (19, 26, 22, 1)
705: P_{24441} = (24, 26, 22, 1)
                                                                759: P_{26407} = (6, 24, 24, 1)
706: P_{24560} = (15, 30, 22, 1)
                                                                760: P_{26445} = (12, 25, 24, 1)
707: P_{24567} = (22, 30, 22, 1)
                                                                761: P_{26451} = (18, 25, 24, 1)
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816: P_{28820} = (19, 3, 27, 1)
762: P_{26473} = (8, 26, 24, 1)
763: P_{26492} = (27, 26, 24, 1)
                                                                817: P_{28827} = (26, 3, 27, 1)
764: P_{26514} = (17, 27, 24, 1)
                                                                818: P_{28871} = (6, 5, 27, 1)
765: P_{26523} = (26, 27, 24, 1)
                                                                819: P_{28896} = (31, 5, 27, 1)
766: P_{26531} = (2, 28, 24, 1)
                                                                820: P_{28910} = (13, 6, 27, 1)
767: P_{26540} = (11, 28, 24, 1)
                                                                821: P_{28925} = (28, 6, 27, 1)
768: P_{26760} = (7, 3, 25, 1)
                                                                822: P_{28931} = (2,7,27,1)
769: P_{26761} = (8, 3, 25, 1)
                                                                823: P_{28937} = (8, 7, 27, 1)
770: P_{26864} = (15, 6, 25, 1)
                                                                824: P_{28987} = (26, 8, 27, 1)
771: P_{26867} = (18, 6, 25, 1)
                                                                825: P_{28990} = (29, 8, 27, 1)
772: P_{26964} = (19, 9, 25, 1)
                                                                826: P_{29026} = (1, 10, 27, 1)
773: P_{26974} = (29, 9, 25, 1)
                                                                827: P_{29046} = (21, 10, 27, 1)
774: P_{26995} = (18, 10, 25, 1)
                                                                828: P_{29127} = (6, 13, 27, 1)
775: P_{27122} = (17, 14, 25, 1)
                                                                829: P_{29146} = (25, 13, 27, 1)
776: P_{27131} = (26, 14, 25, 1)
                                                                830: P_{29160} = (7, 14, 27, 1)
777: P_{27145} = (8, 15, 25, 1)
                                                                831: P_{29169} = (16, 14, 27, 1)
778: P_{27163} = (26, 15, 25, 1)
                                                                832: P_{29240} = (23, 16, 27, 1)
779: P_{27290} = (25, 19, 25, 1)
                                                                833: P_{29243} = (26, 16, 27, 1)
780: P_{27296} = (31, 19, 25, 1)
                                                                834: P_{29250} = (1, 17, 27, 1)
781: P_{27337} = (8, 21, 25, 1)
                                                                835: P_{29272} = (23, 17, 27, 1)
782: P_{27347} = (18, 21, 25, 1)
                                                                836: P_{29316} = (3, 19, 27, 1)
783: P_{27429} = (4, 24, 25, 1)
                                                                837: P_{29319} = (6, 19, 27, 1)
784: P_{27451} = (26, 24, 25, 1)
                                                                838: P_{29552} = (15, 26, 27, 1)
785: P_{27464} = (7, 25, 25, 1)
                                                                839: P_{29560} = (23, 26, 27, 1)
786: P_{27533} = (12, 27, 25, 1)
                                                                840: P_{29572} = (3, 27, 27, 1)
787: P_{27549} = (28, 27, 25, 1)
                                                                841: P_{29724} = (27, 31, 27, 1)
788: P_{27723} = (10, 1, 26, 1)
                                                                842: P_{29842} = (17, 3, 28, 1)
789: P_{27730} = (17, 1, 26, 1)
                                                                843: P_{29870} = (13, 4, 28, 1)
790: P_{27754} = (9, 2, 26, 1)
                                                                844: P_{29876} = (19, 4, 28, 1)
791: P_{27770} = (25, 2, 26, 1)
                                                                845: P_{29909} = (20, 5, 28, 1)
792: P_{27843} = (2, 5, 26, 1)
                                                                846: P_{29911} = (22, 5, 28, 1)
793: P_{27871} = (30, 5, 26, 1)
                                                                847: P_{29966} = (13, 7, 28, 1)
794: P_{27883} = (10, 6, 26, 1)
                                                                848: P_{29971} = (18, 7, 28, 1)
795: P_{27902} = (29, 6, 26, 1)
                                                                849: P_{30156} = (11, 13, 28, 1)
                                                                850: P_{30163} = (18, 13, 28, 1)
796: P_{28015} = (14, 10, 26, 1)
797: P_{28017} = (16, 10, 26, 1)
                                                                851: P_{30226} = (17, 15, 28, 1)
798: P_{28059} = (26, 11, 26, 1)
                                                                852: P_{30230} = (21, 15, 28, 1)
799: P_{28063} = (30, 11, 26, 1)
                                                                853: P_{30244} = (3, 16, 28, 1)
800: P_{28185} = (24, 15, 26, 1)
                                                                854: P_{30258} = (17, 16, 28, 1)
801: P_{28188} = (27, 15, 26, 1)
                                                                855: P_{30289} = (16, 17, 28, 1)
802: P_{28236} = (11, 17, 26, 1)
                                                                856: P_{30303} = (30, 17, 28, 1)
803: P_{28237} = (12, 17, 26, 1)
                                                                857: P_{30351} = (14, 19, 28, 1)
804: P_{28276} = (19, 18, 26, 1)
                                                                858: P_{30366} = (29, 19, 28, 1)
805: P_{28288} = (31, 18, 26, 1)
                                                                859: P_{30376} = (7, 20, 28, 1)
806: P_{28293} = (4, 19, 26, 1)
                                                                860: P_{30379} = (10, 20, 28, 1)
807: P_{28307} = (18, 19, 26, 1)
                                                                861: P_{30435} = (2, 22, 28, 1)
808: P_{28325} = (4, 20, 26, 1)
                                                                862: P_{30451} = (18, 22, 28, 1)
809: P_{28351} = (30, 20, 26, 1)
                                                                863: P_{30481} = (16, 23, 28, 1)
810: P_{28356} = (3, 21, 26, 1)
                                                                864: P_{30493} = (28, 23, 28, 1)
811: P_{28515} = (2, 26, 26, 1)
                                                                865: P_{30565} = (4, 26, 28, 1)
812: P_{28613} = (4, 29, 26, 1)
                                                                866: P_{30577} = (16, 26, 28, 1)
813: P_{28619} = (10, 29, 26, 1)
                                                                867: P_{30647} = (22, 28, 28, 1)
814: P_{28779} = (10, 2, 27, 1)
                                                                868: P_{30662} = (5, 29, 28, 1)
815: P_{28793} = (24, 2, 27, 1)
                                                                869: P_{30672} = (15, 29, 28, 1)
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916: P_{32434} = (17, 20, 30, 1)
870: P_{30734} = (13, 31, 28, 1)
871: P_{30747} = (26, 31, 28, 1)
                                                                917: P_{32455} = (6, 21, 30, 1)
872: P_{31012} = (3, 8, 29, 1)
                                                                918: P_{32473} = (24, 21, 30, 1)
873: P_{31026} = (17, 8, 29, 1)
                                                                919: P_{32514} = (1, 23, 30, 1)
874: P_{31058} = (17, 9, 29, 1)
                                                                920: P_{32519} = (6, 23, 30, 1)
875: P_{31071} = (30, 9, 29, 1)
                                                                921: P_{32550} = (5, 24, 30, 1)
876: P_{31160} = (23, 12, 29, 1)
                                                                922: P_{32570} = (25, 24, 30, 1)
877: P_{31167} = (30, 12, 29, 1)
                                                                923: P_{32601} = (24, 25, 30, 1)
878: P_{31212} = (11, 14, 29, 1)
                                                                924: P_{32603} = (26, 25, 30, 1)
879: P_{31230} = (29, 14, 29, 1)
                                                                925: P_{32679} = (6, 28, 30, 1)
880: P_{31270} = (5, 16, 29, 1)
                                                                926: P_{32686} = (13, 28, 30, 1)
881: P_{31272} = (7, 16, 29, 1)
                                                                927: P_{32708} = (3, 29, 30, 1)
882: P_{31376} = (15, 19, 29, 1)
                                                                928: P_{32727} = (22, 29, 30, 1)
883: P_{31466} = (9, 22, 29, 1)
                                                                929: P_{32755} = (18, 30, 30, 1)
884: P_{31472} = (15, 22, 29, 1)
                                                                930: P_{32842} = (9, 1, 31, 1)
885: P_{31536} = (15, 24, 29, 1)
                                                                931: P_{32856} = (23, 1, 31, 1)
886: P_{31551} = (30, 24, 29, 1)
                                                                932: P_{32866} = (1, 2, 31, 1)
887: P_{31666} = (17, 28, 29, 1)
                                                                933: P_{32892} = (27, 2, 31, 1)
888: P_{31676} = (27, 28, 29, 1)
                                                                934: P_{32906} = (9, 3, 31, 1)
889: P_{31704} = (23, 29, 29, 1)
                                                                935: P_{32909} = (12, 3, 31, 1)
890: P_{31751} = (6, 31, 29, 1)
                                                                936: P_{33069} = (12, 8, 31, 1)
891: P_{31759} = (14, 31, 29, 1)
                                                                937: P_{33071} = (14, 8, 31, 1)
892: P_{31811} = (2, 1, 30, 1)
                                                                938: P_{33100} = (11, 9, 31, 1)
893: P_{31838} = (29, 1, 30, 1)
                                                                939: P_{33111} = (22, 9, 31, 1)
894: P_{31845} = (4, 2, 30, 1)
                                                                940: P_{33127} = (6, 10, 31, 1)
895: P_{31869} = (28, 2, 30, 1)
                                                                941: P_{33152} = (31, 10, 31, 1)
896: P_{31914} = (9, 4, 30, 1)
                                                                942: P_{33180} = (27, 11, 31, 1)
897: P_{31936} = (31, 4, 30, 1)
                                                                943: P_{33182} = (29, 11, 31, 1)
898: P_{32016} = (15, 7, 30, 1)
                                                                944: P_{33453} = (12, 20, 31, 1)
899: P_{32031} = (30, 7, 30, 1)
                                                                945: P_{33465} = (24, 20, 31, 1)
900: P_{32066} = (1, 9, 30, 1)
                                                                946: P_{33490} = (17, 21, 31, 1)
901: P_{32086} = (21, 9, 30, 1)
                                                                947: P_{33499} = (26, 21, 31, 1)
902: P_{32105} = (8, 10, 30, 1)
                                                                948: P_{33525} = (20, 22, 31, 1)
903: P_{32124} = (27, 10, 30, 1)
                                                                949: P_{33532} = (27, 22, 31, 1)
                                                                950: P_{33545} = (8, 23, 31, 1)
904: P_{32147} = (18, 11, 30, 1)
905: P_{32160} = (31, 11, 30, 1)
                                                                951: P_{33561} = (24, 23, 31, 1)
906: P_{32213} = (20, 13, 30, 1)
                                                                952: P_{33684} = (19, 27, 31, 1)
907: P_{32216} = (23, 13, 30, 1)
                                                                953: P_{33712} = (15, 28, 31, 1)
908: P_{32264} = (7, 15, 30, 1)
                                                                954: P_{33721} = (24, 28, 31, 1)
909: P_{32286} = (29, 15, 30, 1)
                                                                955: P_{33730} = (1, 29, 31, 1)
910: P_{32299} = (10, 16, 30, 1)
                                                                956: P_{33738} = (9, 29, 31, 1)
911: P_{32318} = (29, 16, 30, 1)
                                                                957: P_{33777} = (16, 30, 31, 1)
912: P_{32343} = (22, 17, 30, 1)
                                                                958: P_{33789} = (28, 30, 31, 1)
                                                                959: P_{33812} = (19, 31, 31, 1)
913: P_{32352} = (31, 17, 30, 1)
914: P_{32375} = (22, 18, 30, 1)
915: P_{32377} = (24, 18, 30, 1)
```

Line Intersection Graph

	Ψ	1	2	٠
0	0	1	1	(
1	1	0	1	1
2	1	1	0	(
1 2 3	0	1	0	(

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2
in point	P_2	P_2

 ${\bf Line~1~intersects}$

Line	ℓ_0	ℓ_2	ℓ_3
in point	P_2	P_2	P_3

Line 2 intersects

Line	ℓ_0	ℓ_1
in point	P_2	P_2

Line 3 intersects

Line	ℓ_1
in point	P_3

The surface has 1089 points:

Too many to print.