Rank-76307 over GF(64)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^2 X_1 + X_1^2 X_3 + X_1 X_2^2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0) The point rank of the equation over $\mathrm{GF}(64)$ is 1107562565

General information

Number of lines	16
Number of points	4417
Number of singular points	2
Number of Eckardt points	3
Number of double points	29
Number of single points	963
Number of points off lines	3420
Number of Hesse planes	0
Number of axes	0
Type of points on lines	65 ¹⁶
Type of lines on points	$5^2, 3^3, 2^{29}, 1^{963}, 0^{3420}$

Singular Points

The surface has 2 singular points:

$$0: P_{123} = \mathbf{P}(\epsilon^{42}, 0, 1, 0) = \mathbf{P}(56, 0, 1, 0) 1: P_{124} = \mathbf{P}(\epsilon^{21}, 0, 1, 0) = \mathbf{P}(57, 0, 1, 0)$$

The 16 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4096} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4096} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{233016} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{233016} = \mathbf{PI}(57,0,0,0,0,1)_{270458}$$

$$\ell_2 = \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{237177} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{237177} = \mathbf{PI}(56,0,0,0,0,1)_{270457}$$

$$\ell_3 = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047616} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17047616} = \mathbf{PI}(0,1,0,0,0,0)_{1}$$

$$\ell_4 = \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{237242} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 1 & 57 & 0 \\ 0 & 1 & 56 & 57 \end{bmatrix}_{240881} = \mathbf{PI}(1,1,1,0,56,1)_{14951040}$$

$$\ell_5 = \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 1 & \epsilon^{21} & \epsilon^{21} \end{bmatrix}_{240881} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 1 & 56 & 57 \end{bmatrix}_{240881} = \mathbf{PI}(56,57,57,0,1,1)_{540223}$$

$$\ell_6 = \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 1 & \epsilon^{21} & \epsilon^{42} \end{bmatrix}_{240818} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 1 & 57 & 56 \end{bmatrix}_{240818} = \mathbf{PI}(57,56,56,0,57,1)_{15216641}$$

$$\ell_7 = \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{233081} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 1 & 57 & 56 \end{bmatrix}_{240818} = \mathbf{PI}(1,1,1,0,57,1)_{15213120}$$

$$\ell_8 = \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 1 & \epsilon^{42} & \epsilon^{21} \end{bmatrix}_{236720} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 1 & 56 & 57 \end{bmatrix}_{236720} = \mathbf{PI}(56,57,57,0,56,1)_{14954623}$$

$$\ell_9 = \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 1 & \epsilon^{21} & \epsilon^{42} \end{bmatrix}_{236657} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 1 & 57 & 56 \end{bmatrix}_{236657} = \mathbf{PI}(0,56,57,56,57,1)_{15228289}$$

$$\ell_{11} = \begin{bmatrix} 1 & \epsilon^{42} & 0 & 1 \\ 0 & 0 & 1 & \epsilon^{42} \end{bmatrix}_{507633} = \begin{bmatrix} 1 & 56 & 0 & 1 \\ 0 & 0 & 1 & 57 \end{bmatrix}_{503473} = \mathbf{PI}(0,56,57,56,57,1)_{14966083}$$

$$\ell_{12} = \begin{bmatrix} 1 & 1 & 0 & \epsilon^{21} \\ 0 & 0 & 1 & \epsilon^{22} \end{bmatrix}_{15187586} = \begin{bmatrix} 1 & 57 & 0 & 57 \\ 0 & 0 & 1 & 57 \end{bmatrix}_{15187586} = \mathbf{PI}(0,1,57,56,57,1)_{15228234}$$

$$\ell_{14} = \begin{bmatrix} 1 & \epsilon^{42} & 0 & \epsilon^{42} \\ 0 & 0 & 1 & \epsilon^{42} \end{bmatrix}_{1518093} = \begin{bmatrix} 1 & 56 & 0 & 56 \\ 0 & 0 & 1 & 57 \end{bmatrix}_{15150193} = \mathbf{PI}(0,1,56,57,56,1)_{14966027}$$

$$\ell_{15} = \begin{bmatrix} 1 & 1 & 0 & \epsilon^{42} \\ 0 & 0 & 1 & \epsilon^{21} \end{bmatrix}_{1518093} = \begin{bmatrix} 1 & 56 & 0 & 56 \\ 0 & 0 & 1 & 57 \end{bmatrix}_{15150193} = \mathbf{PI}(0,56,1,1,1,1)_{544697}$$

Rank of lines: (4096, 233016, 237177, 17047616, 237242, 240881, 240818, 233081, 236720, 236657, 507633, 503473, 15187586, 15420657, 15150193, 14921282)

Rank of points on Klein quadric: (2, 270458, 270457, 1, 14951040, 540223, 15216641, 15213120, 14954623, 540161, 15228289, 14966083, 544698, 15228234, 14966027, 544697)

Eckardt Points

The surface has 3 Eckardt points:

 $0: P_{8258} = \mathbf{P}(0,0,1,1) = \mathbf{P}(0,0,1,1),$

1: $P_{233537} = \mathbf{P}(0, 0, \epsilon^{42}, 1) = \mathbf{P}(0, 0, 56, 1),$ 2: $P_{237633} = \mathbf{P}(0, 0, \epsilon^{21}, 1) = \mathbf{P}(0, 0, 57, 1).$

Double Points

The surface has 29 Double points:

The double points on the surface are:

$P_2 = (0,0,1,0) = \ell_0 \cap \ell_3$
$P_1 = (0, 1, 0, 0) = \ell_1 \cap \ell_2$
$P_{188} = (57, 1, 1, 0) = \ell_1 \cap \ell_{11}$
$P_{3708} = (57, 56, 1, 0) = \ell_1 \cap \ell_{13}$
$P_{3772} = (57, 57, 1, 0) = \ell_1 \cap \ell_{15}$
$P_{187} = (56, 1, 1, 0) = \ell_2 \cap \ell_{10}$
$P_{3707} = (56, 56, 1, 0) = \ell_2 \cap \ell_{12}$
$P_{3771} = (56, 57, 1, 0) = \ell_2 \cap \ell_{14}$
$P_{8322} = (0, 1, 1, 1) = \ell_4 \cap \ell_7$
$P_{237754} = (57, 1, 57, 1) = \ell_4 \cap \ell_{11}$
$P_{233602} = (1, 1, 56, 1) = \ell_4 \cap \ell_{12}$
$P_{4282} = (56, 1, 0, 1) = \ell_4 \cap \ell_{13}$
$P_{241217} = (0, 56, 57, 1) = \ell_5 \cap \ell_8$
$P_{11898} = (57, 56, 1, 1) = \ell_5 \cap \ell_{10}$
$P_{7747} = (1, 56, 0, 1) = \ell_5 \cap \ell_{11}$

$$\begin{split} P_{237177} &= (56, 56, 56, 1) = \ell_5 \cap \ell_{15} \\ P_{237185} &= (0, 57, 56, 1) = \ell_6 \cap \ell_9 \\ P_{11906} &= (1, 57, 1, 1) = \ell_6 \cap \ell_{13} \\ P_{241337} &= (56, 57, 57, 1) = \ell_6 \cap \ell_{14} \\ P_{7867} &= (57, 57, 0, 1) = \ell_6 \cap \ell_{15} \\ P_{233657} &= (56, 1, 56, 1) = \ell_7 \cap \ell_{10} \\ P_{4283} &= (57, 1, 0, 1) = \ell_7 \cap \ell_{14} \\ P_{237698} &= (1, 1, 57, 1) = \ell_7 \cap \ell_{15} \\ P_{7802} &= (56, 56, 0, 1) = \ell_8 \cap \ell_{12} \\ P_{237178} &= (57, 56, 56, 1) = \ell_8 \cap \ell_{13} \\ P_{11842} &= (1, 56, 1, 1) = \ell_8 \cap \ell_{14} \\ P_{7811} &= (1, 57, 0, 1) = \ell_9 \cap \ell_{10} \\ P_{11961} &= (56, 57, 1, 1) = \ell_9 \cap \ell_{11} \\ P_{241338} &= (57, 57, 57, 1) = \ell_9 \cap \ell_{12} \end{split}$$

Single Points

The surface has 963 single points: The single points on the surface are:

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0: P_0 = (1,0,0,0) lies on line \ell_0
1: P_3 = (0,0,0,1) lies on line \ell_3
2: P_{68} = (1, 0, 1, 0) lies on line \ell_0
3: P_{69} = (2,0,1,0) lies on line \ell_0
4: P_{70} = (3,0,1,0) lies on line \ell_0
5: P_{71} = (4,0,1,0) lies on line \ell_0
6: P_{72} = (5, 0, 1, 0) lies on line \ell_0
7: P_{73} = (6,0,1,0) lies on line \ell_0
8: P_{74} = (7, 0, 1, 0) lies on line \ell_0
9: P_{75} = (8, 0, 1, 0) lies on line \ell_0
10: P_{76} = (9, 0, 1, 0) lies on line \ell_0
11: P_{77} = (10, 0, 1, 0) lies on line \ell_0
12: P_{78} = (11, 0, 1, 0) lies on line \ell_0
13: P_{79} = (12, 0, 1, 0) lies on line \ell_0
14: P_{80} = (13, 0, 1, 0) lies on line \ell_0
15: P_{81} = (14, 0, 1, 0) lies on line \ell_0
16: P_{82} = (15, 0, 1, 0) lies on line \ell_0
17: P_{83} = (16, 0, 1, 0) lies on line \ell_0
18: P_{84} = (17, 0, 1, 0) lies on line \ell_0
19: P_{85} = (18, 0, 1, 0) lies on line \ell_0
20: P_{86} = (19, 0, 1, 0) lies on line \ell_0
21: P_{87} = (20, 0, 1, 0) lies on line \ell_0
22: P_{88} = (21, 0, 1, 0) lies on line \ell_0
23: P_{89} = (22, 0, 1, 0) lies on line \ell_0
24: P_{90} = (23, 0, 1, 0) lies on line \ell_0
25 : P_{91} = (24, 0, 1, 0) lies on line \ell_0
26: P_{92} = (25, 0, 1, 0) lies on line \ell_0
27: P_{93} = (26, 0, 1, 0) lies on line \ell_0
28: P_{94} = (27, 0, 1, 0) lies on line \ell_0
29 : P_{95}=(28,0,1,0) lies on line \ell_0
30: P_{96} = (29, 0, 1, 0) lies on line \ell_0
31: P_{97} = (30, 0, 1, 0) lies on line \ell_0
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32: P_{98} = (31, 0, 1, 0) lies on line \ell_0
33: P_{99} = (32, 0, 1, 0) lies on line \ell_0
34: P_{100} = (33, 0, 1, 0) lies on line \ell_0
35: P_{101} = (34, 0, 1, 0) lies on line \ell_0
36: P_{102} = (35, 0, 1, 0) lies on line \ell_0
37: P_{103} = (36,0,1,0) lies on line \ell_0
38: P_{104} = (37, 0, 1, 0) lies on line \ell_0
39: P_{105} = (38, 0, 1, 0) lies on line \ell_0
40: P_{106} = (39, 0, 1, 0) lies on line \ell_0
41: P_{107} = (40, 0, 1, 0) lies on line \ell_0
42: P_{108} = (41, 0, 1, 0) lies on line \ell_0
43: P_{109} = (42, 0, 1, 0) lies on line \ell_0
44: P_{110} = (43, 0, 1, 0) lies on line \ell_0
45: P_{111} = (44, 0, 1, 0) lies on line \ell_0
46: P_{112} = (45, 0, 1, 0) lies on line \ell_0
47: P_{113} = (46, 0, 1, 0) lies on line \ell_0
48: P_{114} = (47, 0, 1, 0) lies on line \ell_0
49: P_{115} = (48, 0, 1, 0) lies on line \ell_0
50: P_{116} = (49, 0, 1, 0) lies on line \ell_0
51: P_{117} = (50, 0, 1, 0) lies on line \ell_0
52: P_{118} = (51, 0, 1, 0) lies on line \ell_0
53: P_{119} = (52, 0, 1, 0) lies on line \ell_0
54: P_{120} = (53, 0, 1, 0) lies on line \ell_0
55: P_{121} = (54, 0, 1, 0) lies on line \ell_0
56: P_{122} = (55, 0, 1, 0) lies on line \ell_0
57: P_{125} = (58, 0, 1, 0) lies on line \ell_0
58: P_{126} = (59, 0, 1, 0) lies on line \ell_0
59: P_{127} = (60, 0, 1, 0) lies on line \ell_0
60: P_{128} = (61, 0, 1, 0) lies on line \ell_0
61: P_{129} = (62, 0, 1, 0) lies on line \ell_0
62: P_{130} = (63, 0, 1, 0) lies on line \ell_0
63: P_{251} = (56, 2, 1, 0) lies on line \ell_2
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64: P_{252} = (57, 2, 1, 0) lies on line \ell_1
                                                                     118: P_{1980} = (57, 29, 1, 0) lies on line \ell_1
65: P_{315} = (56, 3, 1, 0) lies on line \ell_2
                                                                     119: P_{2043} = (56, 30, 1, 0) lies on line \ell_2
66: P_{316} = (57, 3, 1, 0) lies on line \ell_1
                                                                     120: P_{2044} = (57, 30, 1, 0) lies on line \ell_1
67: P_{379} = (56, 4, 1, 0) lies on line \ell_2
                                                                     121: P_{2107} = (56, 31, 1, 0) lies on line \ell_2
68: P_{380} = (57, 4, 1, 0) lies on line \ell_1
                                                                     122: P_{2108} = (57, 31, 1, 0) lies on line \ell_1
69: P_{443} = (56, 5, 1, 0) lies on line \ell_2
                                                                     123: P_{2171} = (56, 32, 1, 0) lies on line \ell_2
                                                                     124: P_{2172} = (57, 32, 1, 0) lies on line \ell_1
70: P_{444} = (57, 5, 1, 0) lies on line \ell_1
71: P_{507} = (56, 6, 1, 0) lies on line \ell_2
                                                                     125: P_{2235} = (56, 33, 1, 0) lies on line \ell_2
72: P_{508} = (57, 6, 1, 0) lies on line \ell_1
                                                                     126: P_{2236} = (57, 33, 1, 0) lies on line \ell_1
73: P_{571} = (56, 7, 1, 0) lies on line \ell_2
                                                                     127: P_{2299} = (56, 34, 1, 0) lies on line \ell_2
74: P_{572} = (57, 7, 1, 0) lies on line \ell_1
                                                                     128: P_{2300} = (57, 34, 1, 0) lies on line \ell_1
75: P_{635} = (56, 8, 1, 0) lies on line \ell_2
                                                                     129: P_{2363} = (56, 35, 1, 0) lies on line \ell_2
76: P_{636} = (57, 8, 1, 0) lies on line \ell_1
                                                                     130: P_{2364} = (57, 35, 1, 0) lies on line \ell_1
                                                                     131: P_{2427} = (56, 36, 1, 0) lies on line \ell_2
77: P_{699} = (56, 9, 1, 0) lies on line \ell_2
                                                                     132 : P_{2428} = (57, 36, 1, 0) lies on line \ell_1
78: P_{700} = (57, 9, 1, 0) lies on line \ell_1
79: P_{763} = (56, 10, 1, 0) lies on line \ell_2
                                                                     133: P_{2491} = (56, 37, 1, 0) lies on line \ell_2
80: P_{764} = (57, 10, 1, 0) lies on line \ell_1
                                                                     134: P_{2492} = (57, 37, 1, 0) lies on line \ell_1
81: P_{827} = (56, 11, 1, 0) lies on line \ell_2
                                                                     135: P_{2555} = (56, 38, 1, 0) lies on line \ell_2
                                                                     136: P_{2556} = (57, 38, 1, 0) lies on line \ell_1
82: P_{828} = (57, 11, 1, 0) lies on line \ell_1
83: P_{891} = (56, 12, 1, 0) lies on line \ell_2
                                                                     137: P_{2619} = (56, 39, 1, 0) lies on line \ell_2
84: P_{892} = (57, 12, 1, 0) lies on line \ell_1
                                                                     138: P_{2620} = (57, 39, 1, 0) lies on line \ell_1
85: P_{955} = (56, 13, 1, 0) lies on line \ell_2
                                                                     139: P_{2683} = (56, 40, 1, 0) lies on line \ell_2
86: P_{956} = (57, 13, 1, 0) lies on line \ell_1
                                                                     140: P_{2684} = (57, 40, 1, 0) lies on line \ell_1
                                                                     141 : P_{2747} = (56, 41, 1, 0) lies on line \ell_2
87: P_{1019} = (56, 14, 1, 0) lies on line \ell_2
88: P_{1020} = (57, 14, 1, 0) lies on line \ell_1
                                                                     142: P_{2748} = (57, 41, 1, 0) lies on line \ell_1
89: P_{1083} = (56, 15, 1, 0) lies on line \ell_2
                                                                     143: P_{2811} = (56, 42, 1, 0) lies on line \ell_2
90: P_{1084} = (57, 15, 1, 0) lies on line \ell_1
                                                                     144: P_{2812} = (57, 42, 1, 0) lies on line \ell_1
91: P_{1147} = (56, 16, 1, 0) lies on line \ell_2
                                                                     145: P_{2875} = (56, 43, 1, 0) lies on line \ell_2
92: P_{1148} = (57, 16, 1, 0) lies on line \ell_1
                                                                     146: P_{2876} = (57, 43, 1, 0) lies on line \ell_1
93: P_{1211} = (56, 17, 1, 0) lies on line \ell_2
                                                                     147: P_{2939} = (56, 44, 1, 0) lies on line \ell_2
94: P_{1212} = (57, 17, 1, 0) lies on line \ell_1
                                                                     148: P_{2940} = (57, 44, 1, 0) lies on line \ell_1
95: P_{1275} = (56, 18, 1, 0) lies on line \ell_2
                                                                     149: P_{3003} = (56, 45, 1, 0) lies on line \ell_2
96: P_{1276} = (57, 18, 1, 0) lies on line \ell_1
                                                                     150: P_{3004} = (57, 45, 1, 0) lies on line \ell_1
97: P_{1339} = (56, 19, 1, 0) lies on line \ell_2
                                                                     151: P_{3067} = (56, 46, 1, 0) lies on line \ell_2
98: P_{1340} = (57, 19, 1, 0) lies on line \ell_1
                                                                     152: P_{3068} = (57, 46, 1, 0) lies on line \ell_1
99: P_{1403} = (56, 20, 1, 0) lies on line \ell_2
                                                                     153: P_{3131} = (56, 47, 1, 0) lies on line \ell_2
100: P_{1404} = (57, 20, 1, 0) lies on line \ell_1
                                                                     154: P_{3132} = (57, 47, 1, 0) lies on line \ell_1
101 : P_{1467} = (56, 21, 1, 0) lies on line \ell_2
                                                                     155: P_{3195} = (56, 48, 1, 0) lies on line \ell_2
102: P_{1468} = (57, 21, 1, 0) lies on line \ell_1
                                                                     156: P_{3196} = (57, 48, 1, 0) lies on line \ell_1
103: P_{1531} = (56, 22, 1, 0) lies on line \ell_2
                                                                     157: P_{3259} = (56, 49, 1, 0) lies on line \ell_2
104 : P_{1532} = (57, 22, 1, 0) lies on line \ell_1
                                                                     158: P_{3260} = (57, 49, 1, 0) lies on line \ell_1
105: P_{1595} = (56, 23, 1, 0) lies on line \ell_2
                                                                     159: P_{3323} = (56, 50, 1, 0) lies on line \ell_2
106: P_{1596} = (57, 23, 1, 0) lies on line \ell_1
                                                                     160: P_{3324} = (57, 50, 1, 0) lies on line \ell_1
107: P_{1659} = (56, 24, 1, 0) lies on line \ell_2
                                                                     161: P_{3387} = (56, 51, 1, 0) lies on line \ell_2
108: P_{1660} = (57, 24, 1, 0) lies on line \ell_1
                                                                     162: P_{3388} = (57, 51, 1, 0) lies on line \ell_1
109: P_{1723} = (56, 25, 1, 0) lies on line \ell_2
                                                                     163: P_{3451} = (56, 52, 1, 0) lies on line \ell_2
110: P_{1724} = (57, 25, 1, 0) lies on line \ell_1
                                                                     164: P_{3452} = (57, 52, 1, 0) lies on line \ell_1
111: P_{1787} = (56, 26, 1, 0) lies on line \ell_2
                                                                     165: P_{3515} = (56, 53, 1, 0) lies on line \ell_2
112: P_{1788} = (57, 26, 1, 0) lies on line \ell_1
                                                                     166: P_{3516} = (57, 53, 1, 0) lies on line \ell_1
113: P_{1851} = (56, 27, 1, 0) lies on line \ell_2
                                                                     167: P_{3579} = (56, 54, 1, 0) lies on line \ell_2
114: P_{1852} = (57, 27, 1, 0) lies on line \ell_1
                                                                     168: P_{3580} = (57, 54, 1, 0) lies on line \ell_1
115: P_{1915} = (56, 28, 1, 0) lies on line \ell_2
                                                                     169: P_{3643} = (56, 55, 1, 0) lies on line \ell_2
116: P_{1916} = (57, 28, 1, 0) lies on line \ell_1
                                                                     170: P_{3644} = (57, 55, 1, 0) lies on line \ell_1
117: P_{1979} = (56, 29, 1, 0) lies on line \ell_2
                                                                     171: P_{3835} = (56, 58, 1, 0) lies on line \ell_2
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172 : P_{3836} = (57, 58, 1, 0) lies on line \ell_1
                                                                      226: P_{26596} = (35, 30, 5, 1) lies on line \ell_{14}
                                                                      227: P_{26851} = (34, 34, 5, 1) lies on line \ell_{12}
173: P_{3899} = (56, 59, 1, 0) lies on line \ell_2
                                                                      228: P_{27111} = (38, 38, 5, 1) lies on line \ell_{15}
174: P_{3900} = (57, 59, 1, 0) lies on line \ell_1
175: P_{3963} = (56, 60, 1, 0) lies on line \ell_2
                                                                      229: P_{28252} = (27, 56, 5, 1) lies on line \ell_5
176: P_{3964} = (57, 60, 1, 0) lies on line \ell_1
                                                                      230: P_{28264} = (39, 56, 5, 1) lies on line \ell_8
177: P_{4027} = (56, 61, 1, 0) lies on line \ell_2
                                                                      231: P_{28319} = (30, 57, 5, 1) lies on line \ell_9
178: P_{4028} = (57, 61, 1, 0) lies on line \ell_1
                                                                      232: P_{28324} = (35, 57, 5, 1) lies on line \ell_6
179: P_{4091} = (56, 62, 1, 0) lies on line \ell_2
                                                                      233: P_{28508} = (27, 60, 5, 1) lies on line \ell_{10}
180 : P_{4092} = (57, 62, 1, 0) lies on line \ell_1
                                                                      234: P_{28575} = (30, 61, 5, 1) lies on line \ell_{11}
181: P_{4155} = (56, 63, 1, 0) lies on line \ell_2
                                                                      235: P_{28737} = (0,0,6,1) lies on line \ell_3
182: P_{4156} = (57, 63, 1, 0) lies on line \ell_1
                                                                      236: P_{28812} = (11, 1, 6, 1) lies on line \ell_4
183: P_{12353} = (0, 0, 2, 1) lies on line \ell_3
                                                                      237: P_{28813} = (12, 1, 6, 1) lies on line \ell_7
184: P_{12458} = (41, 1, 2, 1) lies on line \ell_4
                                                                      238: P_{29452} = (11, 11, 6, 1) lies on line \ell_{12}
185: P_{12459} = (42, 1, 2, 1) lies on line \ell_7
                                                                      239: P_{29517} = (12, 12, 6, 1) lies on line \ell_{15}
                                                                      240: P_{31950} = (13, 50, 6, 1) lies on line \ell_{13}
186: P_{13420} = (43, 16, 2, 1) lies on line \ell_{13}
187: P_{13545} = (40, 18, 2, 1) lies on line \ell_{14}
                                                                      241: P_{32075} = (10, 52, 6, 1) lies on line \ell_{14}
188: P_{15018} = (41, 41, 2, 1) lies on line \ell_{12}
                                                                      242: P_{32334} = (13, 56, 6, 1) lies on line \ell_8
189 : P_{15083} = (42, 42, 2, 1) lies on line \ell_{15}
                                                                      243: P_{32371} = (50, 56, 6, 1) lies on line \ell_5
190 : P_{15953} = (16, 56, 2, 1) lies on line \ell_5
                                                                      244: P_{32395} = (10, 57, 6, 1) lies on line \ell_6
191: P_{15980} = (43, 56, 2, 1) lies on line \ell_8
                                                                      245: P_{32437} = (52, 57, 6, 1) lies on line \ell_9
192: P_{16019} = (18, 57, 2, 1) lies on line \ell_9
                                                                      246: P_{32757} = (52, 62, 6, 1) lies on line \ell_{11}
193 : P_{16041} = (40, 57, 2, 1) lies on line \ell_6
                                                                      247: P_{32819} = (50, 63, 6, 1) lies on line \ell_{10}
194: P_{16083} = (18, 58, 2, 1) lies on line \ell_{11}
                                                                      248: P_{32833} = (0,0,7,1) lies on line \ell_3
195 : P_{16145} = (16, 59, 2, 1) lies on line \ell_{10}
                                                                      249 : P_{32948} = (51, 1, 7, 1) lies on line \ell_4
196: P_{16449} = (0,0,3,1) lies on line \ell_3
                                                                      250: P_{32950} = (53, 1, 7, 1) lies on line \ell_7
197: P_{16530} = (17, 1, 3, 1) lies on line \ell_4
                                                                      251: P_{33525} = (52, 10, 7, 1) lies on line \ell_{13}
198: P_{16532} = (19, 1, 3, 1) lies on line \ell_7
                                                                      252: P_{33715} = (50, 13, 7, 1) lies on line \ell_{14}
199: P_{17554} = (17, 17, 3, 1) lies on line \ell_{12}
                                                                      253: P_{36148} = (51, 51, 7, 1) lies on line \ell_{12}
200: P_{17684} = (19, 19, 3, 1) lies on line \ell_{15}
                                                                      254: P_{36278} = (53, 53, 7, 1) lies on line \ell_{15}
201: P_{19027} = (18, 40, 3, 1) lies on line \ell_{13}
                                                                      255: P_{36427} = (10, 56, 7, 1) lies on line \ell_5
202: P_{19217} = (16, 43, 3, 1) lies on line \ell_{14}
                                                                      256: P_{36469} = (52, 56, 7, 1) lies on line \ell_8
203: P_{20051} = (18, 56, 3, 1) lies on line \ell_8
                                                                      257: P_{36494} = (13, 57, 7, 1) lies on line \ell_9
204: P_{20073} = (40, 56, 3, 1) lies on line \ell_5
                                                                      258: P_{36531} = (50, 57, 7, 1) lies on line \ell_6
205 : P_{20113} = (16, 57, 3, 1) lies on line \ell_6
                                                                      259 : P_{36811} = (10, 62, 7, 1) lies on line \ell_{10}
206: P_{20140} = (43, 57, 3, 1) lies on line \ell_9
                                                                      260: P_{36878} = (13, 63, 7, 1) lies on line \ell_{11}
207: P_{20201} = (40, 58, 3, 1) lies on line \ell_{10}
                                                                      261: P_{36929} = (0, 0, 8, 1) lies on line \ell_3
208: P_{20268} = (43, 59, 3, 1) lies on line \ell_{11}
                                                                      262: P_{37013} = (20, 1, 8, 1) lies on line \ell_7
209 : P_{20545} = (0, 0, 4, 1) lies on line \ell_3
                                                                      263: P_{37022} = (29, 1, 8, 1) lies on line \ell_4
210: P_{20635} = (26, 1, 4, 1) lies on line \ell_4
                                                                      264: P_{38229} = (20, 20, 8, 1) lies on line \ell_{15}
                                                                      265: P_{38814} = (29, 29, 8, 1) lies on line \ell_{12}
211: P_{20640} = (31, 1, 4, 1) lies on line \ell_7
212: P_{22235} = (26, 26, 4, 1) lies on line \ell_{12}
                                                                      266: P_{39254} = (21, 36, 8, 1) lies on line \ell_{13}
213: P_{22560} = (31, 31, 4, 1) lies on line \ell_{15}
                                                                      267: P_{39773} = (28, 44, 8, 1) lies on line \ell_{14}
214: P_{22815} = (30, 35, 4, 1) lies on line \ell_{13}
                                                                      268: P_{40045} = (44, 48, 8, 1) lies on line \ell_{11}
215: P_{23068} = (27, 39, 4, 1) lies on line \ell_{14}
                                                                      269: P_{40101} = (36, 49, 8, 1) lies on line \ell_{10}
216: P_{24159} = (30, 56, 4, 1) lies on line \ell_8
                                                                      270: P_{40534} = (21, 56, 8, 1) lies on line \ell_8
217: P_{24164} = (35, 56, 4, 1) lies on line \ell_5
                                                                      271: P_{40549} = (36, 56, 8, 1) lies on line \ell_5
218: P_{24220} = (27, 57, 4, 1) lies on line \ell_6
                                                                      272: P_{40605} = (28, 57, 8, 1) lies on line \ell_6
219: P_{24232} = (39, 57, 4, 1) lies on line \ell_9
                                                                      273: P_{40621} = (44, 57, 8, 1) lies on line \ell_9
220: P_{24424} = (39, 60, 4, 1) lies on line \ell_{11}
                                                                      274: P_{41025} = (0, 0, 9, 1) lies on line \ell_3
221: P_{24484} = (35, 61, 4, 1) lies on line \ell_{10}
                                                                      275: P_{41126} = (37, 1, 9, 1) lies on line \ell_4
222: P_{24641} = (0, 0, 5, 1) lies on line \ell_3
                                                                      276: P_{41134} = (45, 1, 9, 1) lies on line \ell_7
223: P_{24739} = (34, 1, 5, 1) lies on line \ell_4
                                                                      277: P_{42405} = (36, 21, 9, 1) lies on line \ell_{14}
                                                                      278 : P_{42861} = (44, 28, 9, 1) lies on line \ell_{13}
224: P_{24743} = (38, 1, 5, 1) lies on line \ell_7
225: P_{26408} = (39, 27, 5, 1) lies on line \ell_{13}
                                                                      279: P_{43430} = (37, 37, 9, 1) lies on line \ell_{12}
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280 : P_{43950} = (45, 45, 9, 1) lies on line \ell_{15}
                                                                     334 : P_{61003} = (10, 56, 13, 1) lies on line \ell_8
281: P_{44125} = (28, 48, 9, 1) lies on line \ell_{10}
                                                                     335: P_{61055} = (62, 56, 13, 1) lies on line \ell_5
282 : P_{44182} = (21, 49, 9, 1) lies on line \ell_{11}
                                                                     336: P_{61063} = (6, 57, 13, 1) lies on line \ell_6
283 : P_{44637} = (28, 56, 9, 1) lies on line \ell_5
                                                                     337: P_{61108} = (51, 57, 13, 1) lies on line \ell_9
284 : P_{44653} = (44, 56, 9, 1) lies on line \ell_8
                                                                     338: P_{61387} = (10, 62, 13, 1) lies on line \ell_{13}
285 : P_{44694} = (21, 57, 9, 1) lies on line \ell_9
                                                                     339: P_{61505} = (0, 0, 14, 1) lies on line \ell_3
286: P_{44709} = (36, 57, 9, 1) lies on line \ell_6
                                                                     340: P_{61602} = (33, 1, 14, 1) lies on line \ell_7
287: P_{45121} = (0, 0, 10, 1) lies on line \ell_3
                                                                     341: P_{61615} = (46, 1, 14, 1) lies on line \ell_4
288: P_{45192} = (7, 1, 10, 1) lies on line \ell_7
                                                                     342: P_{63009} = (32, 23, 14, 1) lies on line \ell_{13}
289: P_{45197} = (12, 1, 10, 1) lies on line \ell_4
                                                                     343: P_{63152} = (47, 25, 14, 1) lies on line \ell_{14}
290: P_{45576} = (7, 7, 10, 1) lies on line \ell_{15}
                                                                     344: P_{63650} = (33, 33, 14, 1) lies on line \ell_{15}
291: P_{45901} = (12, 12, 10, 1) lies on line \ell_{12}
                                                                     345: P_{64495} = (46, 46, 14, 1) lies on line \ell_{12}
292: P_{48384} = (63, 50, 10, 1) lies on line \ell_{11}
                                                                     346: P_{64986} = (25, 54, 14, 1) lies on line \ell_{11}
293: P_{48438} = (53, 51, 10, 1) lies on line \ell_{10}
                                                                     347: P_{65048} = (23, 55, 14, 1) lies on line \ell_{10}
                                                                     348: P_{65112} = (23, 56, 14, 1) lies on line \ell_5
294: P_{48519} = (6, 53, 10, 1) lies on line \ell_{13}
295: P_{48711} = (6, 56, 10, 1) lies on line \ell_8
                                                                     349: P_{65121} = (32, 56, 14, 1) lies on line \ell_8
296: P_{48758} = (53, 56, 10, 1) lies on line \ell_5
                                                                     350: P_{65178} = (25, 57, 14, 1) lies on line \ell_9
297: P_{48782} = (13, 57, 10, 1) lies on line \ell_6
                                                                     351: P_{65200} = (47, 57, 14, 1) lies on line \ell_6
298: P_{48832} = (63, 57, 10, 1) lies on line \ell_9
                                                                     352: P_{65601} = (0, 0, 15, 1) lies on line \ell_3
299: P_{49166} = (13, 63, 10, 1) lies on line \ell_{14}
                                                                     353: P_{65687} = (22, 1, 15, 1) lies on line \ell_4
300: P_{49217} = (0, 0, 11, 1) lies on line \ell_3
                                                                     354 : P_{65689} = (24, 1, 15, 1) lies on line \ell_7
301: P_{49333} = (52, 1, 11, 1) lies on line \ell_4
                                                                     355: P_{67031} = (22, 22, 15, 1) lies on line \ell_{12}
302 : P_{49343} = (62, 1, 11, 1) lies on line \ell_7
                                                                     356: P_{67161} = (24, 24, 15, 1) lies on line \ell_{15}
303 : P_{49654} = (53, 6, 11, 1) lies on line \ell_{14}
                                                                     357: P_{67672} = (23, 32, 15, 1) lies on line \ell_{14}
304: P_{50112} = (63, 13, 11, 1) lies on line \ell_{13}
                                                                     358: P_{68634} = (25, 47, 15, 1) lies on line \ell_{13}
305: P_{52430} = (13, 50, 11, 1) lies on line \ell_{10}
                                                                     359: P_{69104} = (47, 54, 15, 1) lies on line \ell_{10}
306: P_{52487} = (6, 51, 11, 1) lies on line \ell_{11}
                                                                     360: P_{69153} = (32, 55, 15, 1) lies on line \ell_{11}
307: P_{52597} = (52, 52, 11, 1) lies on line \ell_{12}
                                                                     361: P_{69210} = (25, 56, 15, 1) lies on line \ell_8
308: P_{52814} = (13, 56, 11, 1) lies on line \ell_5
                                                                     362: P_{69232} = (47, 56, 15, 1) lies on line \ell_5
309: P_{52864} = (63, 56, 11, 1) lies on line \ell_8
                                                                     363: P_{69272} = (23, 57, 15, 1) lies on line \ell_6
310: P_{52871} = (6, 57, 11, 1) lies on line \ell_9
                                                                     364: P_{69281} = (32, 57, 15, 1) lies on line \ell_9
311: P_{52918} = (53, 57, 11, 1) lies on line \ell_6
                                                                     365: P_{69697} = (0, 0, 16, 1) lies on line \ell_3
312: P_{53247} = (62, 62, 11, 1) lies on line \ell_{15}
                                                                     366: P_{69763} = (2, 1, 16, 1) lies on line \ell_7
313: P_{53313} = (0, 0, 12, 1) lies on line \ell_3
                                                                     367: P_{69780} = (19, 1, 16, 1) lies on line \ell_4
314: P_{53427} = (50, 1, 12, 1) lies on line \ell_7
                                                                     368: P_{69827} = (2, 2, 16, 1) lies on line \ell_{15}
315: P_{53440} = (63, 1, 12, 1) lies on line \ell_4
                                                                     369: P_{70932} = (19, 19, 16, 1) lies on line \ell_{12}
316: P_{53748} = (51, 6, 12, 1) lies on line \ell_{13}
                                                                     370: P_{72315} = (58, 40, 16, 1) lies on line \ell_{11}
317: P_{54015} = (62, 10, 12, 1) lies on line \ell_{14}
                                                                     371: P_{72363} = (42, 41, 16, 1) lies on line \ell_{10}
318: P_{56563} = (50, 50, 12, 1) lies on line \ell_{15}
                                                                     372: P_{72388} = (3, 42, 16, 1) lies on line \ell_{13}
319: P_{56651} = (10, 52, 12, 1) lies on line \ell_{11}
                                                                     373: P_{73284} = (3, 56, 16, 1) lies on line \ell_8
                                                                     374: P_{73323} = (42, 56, 16, 1) lies on line \ell_5
320: P_{56711} = (6, 53, 12, 1) lies on line \ell_{10}
321: P_{56903} = (6, 56, 12, 1) lies on line \ell_5
                                                                     375: P_{73363} = (18, 57, 16, 1) lies on line \ell_6
322: P_{56948} = (51, 56, 12, 1) lies on line \ell_8
                                                                     376: P_{73403} = (58, 57, 16, 1) lies on line \ell_9
323: P_{56971} = (10, 57, 12, 1) lies on line \ell_9
                                                                     377: P_{73427} = (18, 58, 16, 1) lies on line \ell_{14}
324: P_{57023} = (62, 57, 12, 1) lies on line \ell_6
                                                                     378: P_{73793} = (0, 0, 17, 1) lies on line \ell_3
325: P_{57408} = (63, 63, 12, 1) lies on line \ell_{12}
                                                                     379: P_{73900} = (43, 1, 17, 1) lies on line \ell_4
326: P_{57409} = (0, 0, 13, 1) lies on line \ell_3
                                                                     380: P_{73916} = (59, 1, 17, 1) lies on line \ell_7
327: P_{57480} = (7, 1, 13, 1) lies on line \ell_4
                                                                     381: P_{74027} = (42, 3, 17, 1) lies on line \ell_{14}
328: P_{57484} = (11, 1, 13, 1) lies on line \ell_7
                                                                     382: P_{75003} = (58, 18, 17, 1) lies on line \ell_{13}
329: P_{57864} = (7, 7, 13, 1) lies on line \ell_{12}
                                                                     383: P_{76371} = (18, 40, 17, 1) lies on line \ell_{10}
                                                                     384: P_{76420} = (3, 41, 17, 1) lies on line \ell_{11}
330: P_{58124} = (11, 11, 13, 1) lies on line \ell_{15}
331: P_{60679} = (6, 51, 13, 1) lies on line \ell_{14}
                                                                     385: P_{76588} = (43, 43, 17, 1) lies on line \ell_{12}
                                                                     386 : P_{77395} = (18, 56, 17, 1) lies on line \ell_5
332: P_{60799} = (62, 52, 13, 1) lies on line \ell_{10}
333: P_{60852} = (51, 53, 13, 1) lies on line \ell_{11}
                                                                     387: P_{77435} = (58, 56, 17, 1) lies on line \ell_8
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442 : P_{93862} = (37, 57, 21, 1) lies on line \ell_9
388: P_{77444} = (3, 57, 17, 1) lies on line \ell_9
                                                                     443: P_{94273} = (0, 0, 22, 1) lies on line \ell_3
389: P_{77483} = (42, 57, 17, 1) lies on line \ell_6
                                                                     444: P_{94369} = (32, 1, 22, 1) lies on line \ell_4
390: P_{77628} = (59, 59, 17, 1) lies on line \ell_{15}
391: P_{77889} = (0, 0, 18, 1) lies on line \ell_3
                                                                     445: P_{94392} = (55, 1, 22, 1) lies on line \ell_7
392: P_{77955} = (2, 1, 18, 1) lies on line \ell_4
                                                                     446: P_{95266} = (33, 15, 22, 1) lies on line \ell_{14}
393 : P_{77970} = (17, 1, 18, 1) lies on line \ell_7
                                                                     447: P_{95927} = (54, 25, 22, 1) lies on line \ell_{13}
394: P_{78019} = (2, 2, 18, 1) lies on line \ell_{12}
                                                                     448: P_{96353} = (32, 32, 22, 1) lies on line \ell_{12}
395: P_{78994} = (17, 17, 18, 1) lies on line \ell_{15}
                                                                     449: P_{97232} = (15, 46, 22, 1) lies on line \ell_{11}
396: P_{80516} = (3, 41, 18, 1) lies on line \ell_{14}
                                                                     450: P_{97306} = (25, 47, 22, 1) lies on line \ell_{10}
397: P_{80618} = (41, 42, 18, 1) lies on line \ell_{11}
                                                                     451: P_{97848} = (55, 55, 22, 1) lies on line \ell_{15}
398: P_{80700} = (59, 43, 18, 1) lies on line \ell_{10}
                                                                     452: P_{97882} = (25, 56, 22, 1) lies on line \ell_5
399: P_{81489} = (16, 56, 18, 1) lies on line \ell_8
                                                                     453: P_{97911} = (54, 56, 22, 1) lies on line \ell_8
400: P_{81532} = (59, 56, 18, 1) lies on line \ell_5
                                                                     454: P_{97936} = (15, 57, 22, 1) lies on line \ell_9
401: P_{81540} = (3, 57, 18, 1) lies on line \ell_6
                                                                     455: P_{97954} = (33, 57, 22, 1) lies on line \ell_6
402: P_{81578} = (41, 57, 18, 1) lies on line \ell_9
                                                                     456: P_{98369} = (0, 0, 23, 1) lies on line \ell_3
403: P_{81681} = (16, 59, 18, 1) lies on line \ell_{13}
                                                                     457: P_{98447} = (14, 1, 23, 1) lies on line \ell_7
404: P_{81985} = (0, 0, 19, 1) lies on line \ell_3
                                                                     458: P_{98457} = (24, 1, 23, 1) lies on line \ell_4
405: P_{82089} = (40, 1, 19, 1) lies on line \ell_7
                                                                     459: P_{99279} = (14, 14, 23, 1) lies on line \ell_{15}
406 : P_{82107} = (58, 1, 19, 1) lies on line \ell_4
                                                                     460: P_{99929} = (24, 24, 23, 1) lies on line \ell_{12}
                                                                     461: P_{100496} = (15, 33, 23, 1) lies on line \ell_{13}
407: P_{82218} = (41, 3, 19, 1) lies on line \ell_{13}
408: P_{83068} = (59, 16, 19, 1) lies on line \ell_{14}
                                                                     462: P_{101346} = (33, 46, 23, 1) lies on line \ell_{10}
409: P_{84585} = (40, 40, 19, 1) lies on line \ell_{15}
                                                                     463: P_{101431} = (54, 47, 23, 1) lies on line \ell_{11}
410 : P_{84676} = (3, 42, 19, 1) lies on line \ell_{10}
                                                                     464: P_{101850} = (25, 54, 23, 1) lies on line \ell_{14}
411: P_{84753} = (16, 43, 19, 1) lies on line \ell_{11}
                                                                     465: P_{101968} = (15, 56, 23, 1) lies on line \ell_8
412: P_{85572} = (3, 56, 19, 1) lies on line \ell_5
                                                                     466: P_{101986} = (33, 56, 23, 1) lies on line \ell_5
413: P_{85610} = (41, 56, 19, 1) lies on line \ell_8
                                                                     467: P_{102042} = (25, 57, 23, 1) lies on line \ell_6
414: P_{85649} = (16, 57, 19, 1) lies on line \ell_9
                                                                     468: P_{102071} = (54, 57, 23, 1) lies on line \ell_9
415: P_{85692} = (59, 57, 19, 1) lies on line \ell_6
                                                                     469: P_{102465} = (0, 0, 24, 1) lies on line \ell_3
416: P_{85755} = (58, 58, 19, 1) lies on line \ell_{12}
                                                                     470: P_{102576} = (47, 1, 24, 1) lies on line \ell_7
417: P_{86081} = (0, 0, 20, 1) lies on line \ell_3
                                                                     471: P_{102583} = (54, 1, 24, 1) lies on line \ell_4
418: P_{86181} = (36, 1, 20, 1) lies on line \ell_7
                                                                     472: P_{103471} = (46, 15, 24, 1) lies on line \ell_{13}
419: P_{86194} = (49, 1, 20, 1) lies on line \ell_4
                                                                     473: P_{103992} = (55, 23, 24, 1) lies on line \ell_{14}
420: P_{86630} = (37, 8, 20, 1) lies on line \ell_{13}
                                                                     474: P_{104536} = (23, 32, 24, 1) lies on line \ell_{11}
421 : P_{87921} = (48, 28, 20, 1) lies on line \ell_{14}
                                                                     475: P_{104592} = (15, 33, 24, 1) lies on line \ell_{10}
422: P_{88421} = (36, 36, 20, 1) lies on line \ell_{15}
                                                                     476: P_{105520} = (47, 47, 24, 1) lies on line \ell_{15}
                                                                     477 : P_{105975} = (54, 54, 24, 1) lies on line \ell_{12}
423: P_{88925} = (28, 44, 20, 1) lies on line \ell_{11}
424: P_{88969} = (8, 45, 20, 1) lies on line \ell_{10}
                                                                     478: P_{106064} = (15, 56, 24, 1) lies on line \ell_5
425: P_{89266} = (49, 49, 20, 1) lies on line \ell_{12}
                                                                     479: P_{106095} = (46, 56, 24, 1) lies on line \ell_8
426: P_{89673} = (8, 56, 20, 1) lies on line \ell_5
                                                                     480 : P_{106136} = (23, 57, 24, 1) lies on line \ell_9
427: P_{89702} = (37, 56, 20, 1) lies on line \ell_8
                                                                     481 : P_{106168} = (55, 57, 24, 1) lies on line \ell_6
428 : P_{89757} = (28, 57, 20, 1) lies on line \ell_9
                                                                     482: P_{106561} = (0, 0, 25, 1) lies on line \ell_3
429: P_{89777} = (48, 57, 20, 1) lies on line \ell_6
                                                                     483: P_{106639} = (14, 1, 25, 1) lies on line \ell_4
                                                                     484: P_{106647} = (22, 1, 25, 1) lies on line \ell_7
430: P_{90177} = (0, 0, 21, 1) lies on line \ell_3
431: P_{90250} = (9, 1, 21, 1) lies on line \ell_4
                                                                     485: P_{107471} = (14, 14, 25, 1) lies on line \ell_{12}
432 : P_{90270} = (29, 1, 21, 1) lies on line \ell_7
                                                                     486: P_{107991} = (22, 22, 25, 1) lies on line \ell_{15}
433: P_{90762} = (9, 9, 21, 1) lies on line \ell_{12}
                                                                     487: P_{108664} = (55, 32, 25, 1) lies on line \ell_{10}
434: P_{92062} = (29, 29, 21, 1) lies on line \ell_{15}
                                                                     488: P_{108719} = (46, 33, 25, 1) lies on line \ell_{11}
435: P_{92553} = (8, 37, 21, 1) lies on line \ell_{14}
                                                                     489: P_{109520} = (15, 46, 25, 1) lies on line \ell_{14}
436: P_{93041} = (48, 44, 21, 1) lies on line \ell_{10}
                                                                     490: P_{110104} = (23, 55, 25, 1) lies on line \ell_{13}
437: P_{93094} = (37, 45, 21, 1) lies on line \ell_{11}
                                                                     491: P_{110168} = (23, 56, 25, 1) lies on line \ell_8
438 : P_{93277} = (28, 48, 21, 1) lies on line \ell_{13}
                                                                     492: P_{110200} = (55, 56, 25, 1) lies on line \ell_5
439: P_{93789} = (28, 56, 21, 1) lies on line \ell_8
                                                                     493: P_{110224} = (15, 57, 25, 1) lies on line \ell_6
440: P_{93809} = (48, 56, 21, 1) lies on line \ell_5
                                                                     494: P_{110255} = (46, 57, 25, 1) lies on line \ell_9
441: P_{93833} = (8, 57, 21, 1) lies on line \ell_6
                                                                     495: P_{110657} = (0, 0, 26, 1) lies on line \ell_3
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496: P_{110760} = (39, 1, 26, 1) lies on line \ell_4
                                                                     550: P_{127366} = (5, 5, 30, 1) lies on line \ell_{12}
497: P_{110781} = (60, 1, 26, 1) lies on line \ell_7
                                                                     551: P_{128731} = (26, 26, 30, 1) lies on line \ell_{15}
                                                                     552: P_{129221} = (4, 34, 30, 1) lies on line \ell_{14}
498: P_{110951} = (38, 4, 26, 1) lies on line \ell_{14}
499: P_{112638} = (61, 30, 26, 1) lies on line \ell_{13}
                                                                     553: P_{129507} = (34, 38, 30, 1) lies on line \ell_{11}
                                                                     554: P_{129597} = (60, 39, 30, 1) lies on line \ell_{10}
500: P_{112837} = (4, 34, 26, 1) lies on line \ell_{11}
501: P_{112927} = (30, 35, 26, 1) lies on line \ell_{10}
                                                                     555: P_{130652} = (27, 56, 30, 1) lies on line \ell_8
502: P_{113192} = (39, 39, 26, 1) lies on line \ell_{12}
                                                                     556: P_{130685} = (60, 56, 30, 1) lies on line \ell_5
503: P_{114271} = (30, 56, 26, 1) lies on line \ell_5
                                                                     557: P_{130693} = (4, 57, 30, 1) lies on line \ell_6
                                                                     558 : P_{130723} = (34, 57, 30, 1) lies on line \ell_9
504: P_{114302} = (61, 56, 26, 1) lies on line \ell_8
505: P_{114309} = (4, 57, 26, 1) lies on line \ell_9
                                                                     559: P_{130908} = (27, 60, 30, 1) lies on line \ell_{13}
506: P_{114343} = (38, 57, 26, 1) lies on line \ell_6
                                                                     560: P_{131137} = (0,0,31,1) lies on line \ell_3
                                                                     561: P_{131236} = (35, 1, 31, 1) lies on line \ell_7
507: P_{114557} = (60, 60, 26, 1) lies on line \ell_{15}
508: P_{114753} = (0, 0, 27, 1) lies on line \ell_3
                                                                     562: P_{131262} = (61, 1, 31, 1) lies on line \ell_4
509: P_{114822} = (5, 1, 27, 1) lies on line \ell_7
                                                                     563: P_{131427} = (34, 4, 31, 1) lies on line \ell_{13}
510: P_{114848} = (31, 1, 27, 1) lies on line \ell_4
                                                                     564: P_{132925} = (60, 27, 31, 1) lies on line \ell_{14}
511: P_{115078} = (5, 5, 27, 1) lies on line \ell_{15}
                                                                     565: P_{133412} = (35, 35, 31, 1) lies on line \ell_{15}
                                                                     566: P_{133573} = (4, 38, 31, 1) lies on line \ell_{10}
512: P_{116768} = (31, 31, 27, 1) lies on line \ell_{12}
                                                                     567: P_{133660} = (27, 39, 31, 1) lies on line \ell_{11}
513: P_{116967} = (38, 34, 27, 1) lies on line \ell_{10}
514: P_{117054} = (61, 35, 27, 1) lies on line \ell_{11}
                                                                     568: P_{134725} = (4, 56, 31, 1) lies on line \ell_5
515: P_{117189} = (4, 38, 27, 1) lies on line \ell_{13}
                                                                     569: P_{134755} = (34, 56, 31, 1) lies on line \ell_8
516: P_{118341} = (4, 56, 27, 1) lies on line \ell_8
                                                                     570: P_{134812} = (27, 57, 31, 1) lies on line \ell_9
517: P_{118375} = (38, 56, 27, 1) lies on line \ell_5
                                                                     571: P_{134845} = (60, 57, 31, 1) lies on line \ell_6
518: P_{118431} = (30, 57, 27, 1) lies on line \ell_6
                                                                     572: P_{135102} = (61, 61, 31, 1) lies on line \ell_{12}
519: P_{118462} = (61, 57, 27, 1) lies on line \ell_9
                                                                     573: P_{135233} = (0,0,32,1) lies on line \ell_3
520: P_{118687} = (30, 61, 27, 1) lies on line \ell_{14}
                                                                     574: P_{135312} = (15, 1, 32, 1) lies on line \ell_4
521: P_{118849} = (0, 0, 28, 1) lies on line \ell_3
                                                                     575: P_{135343} = (46, 1, 32, 1) lies on line \ell_7
522: P_{118922} = (9, 1, 28, 1) lies on line \ell_7
                                                                     576: P_{136208} = (15, 15, 32, 1) lies on line \ell_{12}
523: P_{118933} = (20, 1, 28, 1) lies on line \ell_4
                                                                     577: P_{136655} = (14, 22, 32, 1) lies on line \ell_{14}
524: P_{119434} = (9, 9, 28, 1) lies on line \ell_{15}
                                                                     578: P_{136791} = (22, 24, 32, 1) lies on line \ell_{11}
525: P_{120149} = (20, 20, 28, 1) lies on line \ell_{12}
                                                                     579: P_{136887} = (54, 25, 32, 1) lies on line \ell_{10}
526: P_{121202} = (49, 36, 28, 1) lies on line \ell_{11}
                                                                     580: P_{138223} = (46, 46, 32, 1) lies on line \ell_{15}
527: P_{121262} = (45, 37, 28, 1) lies on line \ell_{10}
                                                                     581: P_{138736} = (47, 54, 32, 1) lies on line \ell_{13}
528: P_{121737} = (8, 45, 28, 1) lies on line \ell_{13}
                                                                     582: P_{138864} = (47, 56, 32, 1) lies on line \ell_8
                                                                     583 : P_{138871} = (54, 56, 32, 1) lies on line \ell_5
529: P_{122006} = (21, 49, 28, 1) lies on line \ell_{14}
530: P_{122441} = (8, 56, 28, 1) lies on line \ell_8
                                                                     584: P_{138895} = (14, 57, 32, 1) lies on line \ell_6
531: P_{122478} = (45, 56, 28, 1) lies on line \ell_5
                                                                     585: P_{138903} = (22, 57, 32, 1) lies on line \ell_9
532: P_{122518} = (21, 57, 28, 1) lies on line \ell_6
                                                                     586: P_{139329} = (0,0,33,1) lies on line \ell_3
533: P_{122546} = (49, 57, 28, 1) lies on line \ell_9
                                                                     587: P_{139416} = (23, 1, 33, 1) lies on line \ell_7
                                                                     588: P_{139448} = (55, 1, 33, 1) lies on line \ell_4
534: P_{122945} = (0, 0, 29, 1) lies on line \ell_3
535: P_{123053} = (44, 1, 29, 1) lies on line \ell_4
                                                                     589: P_{140247} = (22, 14, 33, 1) lies on line \ell_{13}
536 : P_{123057} = (48, 1, 29, 1) lies on line \ell_7
                                                                     590: P_{140824} = (23, 23, 33, 1) lies on line \ell_{15}
537: P_{123502} = (45, 8, 29, 1) lies on line \ell_{14}
                                                                     591: P_{140879} = (14, 24, 33, 1) lies on line \ell_{10}
538: P_{124338} = (49, 21, 29, 1) lies on line \ell_{13}
                                                                     592: P_{140976} = (47, 25, 33, 1) lies on line \ell_{11}
539: P_{125270} = (21, 36, 29, 1) lies on line \ell_{10}
                                                                     593: P_{142391} = (54, 47, 33, 1) lies on line \ell_{14}
540: P_{125321} = (8, 37, 29, 1) lies on line \ell_{11}
                                                                     594: P_{142904} = (55, 55, 33, 1) lies on line \ell_{12}
541 : P_{125805} = (44, 44, 29, 1) lies on line \ell_{12}
                                                                     595: P_{142927} = (14, 56, 33, 1) lies on line \ell_5
542: P_{126065} = (48, 48, 29, 1) lies on line \ell_{15}
                                                                     596: P_{142935} = (22, 56, 33, 1) lies on line \ell_8
543: P_{126550} = (21, 56, 29, 1) lies on line \ell_5
                                                                     597: P_{143024} = (47, 57, 33, 1) lies on line \ell_9
544: P_{126578} = (49, 56, 29, 1) lies on line \ell_8
                                                                     598: P_{143031} = (54, 57, 33, 1) lies on line \ell_6
545: P_{126601} = (8, 57, 29, 1) lies on line \ell_9
                                                                     599: P_{143425} = (0, 0, 34, 1) lies on line \ell_3
546: P_{126638} = (45, 57, 29, 1) lies on line \ell_6
                                                                     600: P_{143519} = (30, 1, 34, 1) lies on line \ell_4
547: P_{127041} = (0,0,30,1) lies on line \ell_3
                                                                     601: P_{143550} = (61, 1, 34, 1) lies on line \ell_7
548: P_{127110} = (5, 1, 30, 1) lies on line \ell_4
                                                                     602: P_{143776} = (31, 5, 34, 1) lies on line \ell_{14}
549: P_{127131} = (26, 1, 30, 1) lies on line \ell_7
                                                                     603: P_{145094} = (5, 26, 34, 1) lies on line \ell_{11}
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658: P_{162110} = (61, 35, 38, 1) lies on line \ell_{14}
604: P_{145192} = (39, 27, 34, 1) lies on line \ell_{10}
605: P_{145375} = (30, 30, 34, 1) lies on line \ell_{12}
                                                                     659: P_{163398} = (5, 56, 38, 1) lies on line \ell_5
606: P_{145981} = (60, 39, 34, 1) lies on line \ell_{13}
                                                                     660: P_{163419} = (26, 56, 38, 1) lies on line \ell_8
607: P_{147048} = (39, 56, 34, 1) lies on line \ell_5
                                                                     661: P_{163492} = (35, 57, 38, 1) lies on line \ell_9
                                                                     662: P_{163518} = (61, 57, 38, 1) lies on line \ell_6
608: P_{147069} = (60, 56, 34, 1) lies on line \ell_8
609: P_{147078} = (5, 57, 34, 1) lies on line \ell_9
                                                                     663: P_{163709} = (60, 60, 38, 1) lies on line \ell_{12}
610: P_{147104} = (31, 57, 34, 1) lies on line \ell_6
                                                                     664: P_{163905} = (0, 0, 39, 1) lies on line \ell_3
611: P_{147390} = (61, 61, 34, 1) lies on line \ell_{15}
                                                                     665: P_{163973} = (4, 1, 39, 1) lies on line \ell_4
612: P_{147521} = (0, 0, 35, 1) lies on line \ell_3
                                                                     666: P_{164003} = (34, 1, 39, 1) lies on line \ell_7
613 : P_{147589} = (4, 1, 35, 1) lies on line \ell_7
                                                                     667: P_{164165} = (4, 4, 39, 1) lies on line \ell_{12}
614: P_{147623} = (38, 1, 35, 1) lies on line \ell_4
                                                                     668: P_{165574} = (5, 26, 39, 1) lies on line \ell_{14}
615: P_{147781} = (4, 4, 35, 1) lies on line \ell_{15}
                                                                     669: P_{165886} = (61, 30, 39, 1) lies on line \ell_{10}
616: P_{149216} = (31, 26, 35, 1) lies on line \ell_{10}
                                                                     670: P_{165915} = (26, 31, 39, 1) lies on line \ell_{11}
617: P_{149309} = (60, 27, 35, 1) lies on line \ell_{11}
                                                                     671: P_{166115} = (34, 34, 39, 1) lies on line \ell_{15}
                                                                     672: P_{167524} = (35, 56, 39, 1) lies on line \ell_8
618: P_{149510} = (5, 31, 35, 1) lies on line \ell_{13}
619: P_{149991} = (38, 38, 35, 1) lies on line \ell_{12}
                                                                     673: P_{167550} = (61, 56, 39, 1) lies on line \ell_5
620: P_{151110} = (5, 56, 35, 1) lies on line \ell_8
                                                                     674: P_{167558} = (5, 57, 39, 1) lies on line \ell_6
621: P_{151136} = (31, 56, 35, 1) lies on line \ell_5
                                                                     675: P_{167579} = (26, 57, 39, 1) lies on line \ell_9
622: P_{151208} = (39, 57, 35, 1) lies on line \ell_6
                                                                     676: P_{167844} = (35, 61, 39, 1) lies on line \ell_{13}
                                                                     677 : P_{168001} = (0, 0, 40, 1) lies on line \ell_3
623: P_{151229} = (60, 57, 35, 1) lies on line \ell_9
624: P_{151400} = (39, 60, 35, 1) lies on line \ell_{14}
                                                                     678: P_{168068} = (3, 1, 40, 1) lies on line \ell_7
625: P_{151617} = (0, 0, 36, 1) lies on line \ell_3
                                                                     679: P_{168107} = (42, 1, 40, 1) lies on line \ell_4
626: P_{151689} = (8, 1, 36, 1) lies on line \ell_7
                                                                     680: P_{168196} = (3, 3, 40, 1) lies on line \ell_{15}
627 : P_{151726} = (45, 1, 36, 1) lies on line \ell_4
                                                                     681: P_{169084} = (59, 16, 40, 1) lies on line \ell_{11}
628: P_{152137} = (8, 8, 36, 1) lies on line \ell_{15}
                                                                     682: P_{169108} = (19, 17, 40, 1) lies on line \ell_{10}
629: P_{152906} = (9, 20, 36, 1) lies on line \ell_{13}
                                                                     683: P_{169219} = (2, 19, 40, 1) lies on line \ell_{13}
630: P_{153457} = (48, 28, 36, 1) lies on line \ell_{11}
                                                                     684: P_{170731} = (42, 42, 40, 1) lies on line \ell_{12}
631: P_{153493} = (20, 29, 36, 1) lies on line \ell_{10}
                                                                     685: P_{171587} = (2, 56, 40, 1) lies on line \ell_8
632: P_{154542} = (45, 45, 36, 1) lies on line \ell_{12}
                                                                     686: P_{171604} = (19, 56, 40, 1) lies on line \ell_5
633: P_{154733} = (44, 48, 36, 1) lies on line \ell_{14}
                                                                     687: P_{171692} = (43, 57, 40, 1) lies on line \ell_6
634: P_{155210} = (9, 56, 36, 1) lies on line \ell_8
                                                                     688: P_{171708} = (59, 57, 40, 1) lies on line \ell_9
635: P_{155221} = (20, 56, 36, 1) lies on line \ell_5
                                                                     689: P_{171820} = (43, 59, 40, 1) lies on line \ell_{14}
636: P_{155309} = (44, 57, 36, 1) lies on line \ell_6
                                                                     690: P_{172097} = (0, 0, 41, 1) lies on line \ell_3
637 : P_{155313} = (48, 57, 36, 1) lies on line \ell_9
                                                                     691: P_{172179} = (18, 1, 41, 1) lies on line \ell_4
638: P_{155713} = (0, 0, 37, 1) lies on line \ell_3
                                                                     692: P_{172219} = (58, 1, 41, 1) lies on line \ell_7
                                                                     693 : P_{172244} = (19, 2, 41, 1) lies on line \ell_{14}
639: P_{155798} = (21, 1, 37, 1) lies on line \ell_4
640: P_{155826} = (49, 1, 37, 1) lies on line \ell_7
                                                                     694: P_{173164} = (43, 16, 41, 1) lies on line \ell_{10}
641: P_{156309} = (20, 9, 37, 1) lies on line \ell_{14}
                                                                     695: P_{173187} = (2, 17, 41, 1) lies on line \ell_{11}
                                                                     696: P_{173267} = (18, 18, 41, 1) lies on line \ell_{12}
642: P_{157078} = (21, 21, 37, 1) lies on line \ell_{12}
643: P_{157549} = (44, 28, 37, 1) lies on line \ell_{10}
                                                                     697: P_{174908} = (59, 43, 41, 1) lies on line \ell_{13}
644: P_{157578} = (9, 29, 37, 1) lies on line \ell_{11}
                                                                     698: P_{175724} = (43, 56, 41, 1) lies on line \ell_5
645: P_{158577} = (48, 44, 37, 1) lies on line \ell_{13}
                                                                     699: P_{175740} = (59, 56, 41, 1) lies on line \ell_8
646 : P_{158898} = (49, 49, 37, 1) lies on line \ell_{15}
                                                                     700: P_{175747} = (2, 57, 41, 1) lies on line \ell_9
647: P_{159341} = (44, 56, 37, 1) lies on line \ell_5
                                                                     701: P_{175764} = (19, 57, 41, 1) lies on line \ell_6
648: P_{159345} = (48, 56, 37, 1) lies on line \ell_8
                                                                     702: P_{175867} = (58, 58, 41, 1) lies on line \ell_{15}
649 : P_{159370} = (9, 57, 37, 1) lies on line \ell_9
                                                                     703: P_{176193} = (0, 0, 42, 1) lies on line \ell_3
650: P_{159381} = (20, 57, 37, 1) lies on line \ell_6
                                                                     704: P_{176273} = (16, 1, 42, 1) lies on line \ell_7
651: P_{159809} = (0, 0, 38, 1) lies on line \ell_3
                                                                     705: P_{176316} = (59, 1, 42, 1) lies on line \ell_4
652: P_{159900} = (27, 1, 38, 1) lies on line \ell_7
                                                                     706: P_{176338} = (17, 2, 42, 1) lies on line \ell_{13}
653: P_{159933} = (60, 1, 38, 1) lies on line \ell_4
                                                                     707: P_{177233} = (16, 16, 42, 1) lies on line \ell_{15}
654: P_{160155} = (26, 5, 38, 1) lies on line \ell_{13}
                                                                     708: P_{177385} = (40, 18, 42, 1) lies on line \ell_{11}
655: P_{161564} = (27, 27, 38, 1) lies on line \ell_{15}
                                                                     709: P_{177411} = (2, 19, 42, 1) lies on line \ell_{10}
656 : P_{161764} = (35, 30, 38, 1) lies on line \ell_{11}
                                                                     710 : P_{178811} = (58, 40, 42, 1) lies on line \ell_{14}
657: P_{161798} = (5, 31, 38, 1) lies on line \ell_{10}
                                                                     711: P_{179779} = (2, 56, 42, 1) lies on line \ell_5
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712 : P_{179794} = (17, 56, 42, 1) lies on line \ell_8
                                                                      766: P_{196239} = (14, 57, 46, 1) lies on line \ell_9
713: P_{179881} = (40, 57, 42, 1) lies on line \ell_9
                                                                      767: P_{196249} = (24, 57, 46, 1) lies on line \ell_6
                                                                      768 : P_{196673} = (0, 0, 47, 1) lies on line \ell_3
714: P_{179899} = (58, 57, 42, 1) lies on line \ell_6
715: P_{180028} = (59, 59, 42, 1) lies on line \ell_{12}
                                                                      769: P_{196752} = (15, 1, 47, 1) lies on line \ell_7
                                                                      770 : P_{196770} = (33, 1, 47, 1) lies on line \ell_4
716: P_{180289} = (0, 0, 43, 1) lies on line \ell_3
717: P_{180356} = (3, 1, 43, 1) lies on line \ell_4
                                                                      771: P_{197648} = (15, 15, 47, 1) lies on line \ell_{15}
                                                                      772: P_{198105} = (24, 22, 47, 1) lies on line \ell_{10}
718: P_{180394} = (41, 1, 43, 1) lies on line \ell_7
719: P_{180484} = (3, 3, 43, 1) lies on line \ell_{12}
                                                                      773: P_{198200} = (55, 23, 47, 1) lies on line \ell_{11}
720: P_{181379} = (2, 17, 43, 1) lies on line \ell_{14}
                                                                      774: P_{198223} = (14, 24, 47, 1) lies on line \ell_{13}
721: P_{181499} = (58, 18, 43, 1) lies on line \ell_{10}
                                                                      775: P_{198818} = (33, 33, 47, 1) lies on line \ell_{12}
722: P_{181522} = (17, 19, 43, 1) lies on line \ell_{11}
                                                                      776: P_{200225} = (32, 55, 47, 1) lies on line \ell_{14}
723 : P_{182954} = (41, 41, 43, 1) lies on line \ell_{15}
                                                                      777: P_{200271} = (14, 56, 47, 1) lies on line \ell_8
724: P_{183913} = (40, 56, 43, 1) lies on line \ell_8
                                                                      778: P_{200281} = (24, 56, 47, 1) lies on line \ell_5
725: P_{183931} = (58, 56, 43, 1) lies on line \ell_5
                                                                      779: P_{200353} = (32, 57, 47, 1) lies on line \ell_6
726: P_{183939} = (2, 57, 43, 1) lies on line \ell_6
                                                                      780 : P_{200376} = (55, 57, 47, 1) lies on line \ell_9
727: P_{183954} = (17, 57, 43, 1) lies on line \ell_9
                                                                      781: P_{200769} = (0, 0, 48, 1) lies on line \ell_3
                                                                      782 : P_{200854} = (21, 1, 48, 1) lies on line \ell_7
728: P_{184041} = (40, 58, 43, 1) lies on line \ell_{13}
729 : P_{184385} = (0, 0, 44, 1) lies on line \ell_3
                                                                      783: P_{200869} = (36, 1, 48, 1) lies on line \ell_4
730 : P_{184457} = (8, 1, 44, 1) lies on line \ell_4
                                                                      784: P_{201326} = (45, 8, 48, 1) lies on line \ell_{11}
731: P_{184486} = (37, 1, 44, 1) lies on line \ell_7
                                                                      785: P_{201374} = (29, 9, 48, 1) lies on line \ell_{10}
732: P_{184905} = (8, 8, 44, 1) lies on line \ell_{12}
                                                                      786: P_{202134} = (21, 21, 48, 1) lies on line \ell_{15}
733: P_{185694} = (29, 20, 44, 1) lies on line \ell_{11}
                                                                      787: P_{202645} = (20, 29, 48, 1) lies on line \ell_{13}
734: P_{185778} = (49, 21, 44, 1) lies on line \ell_{10}
                                                                      788: P_{203109} = (36, 36, 48, 1) lies on line \ell_{12}
                                                                      789 : P_{203686} = (37, 45, 48, 1) lies on line \ell_{14}
735 : P_{186250} = (9, 29, 44, 1) lies on line \ell_{14}
736: P_{186790} = (37, 37, 44, 1) lies on line \ell_{15}
                                                                      790: P_{204373} = (20, 56, 48, 1) lies on line \ell_8
737: P_{187557} = (36, 49, 44, 1) lies on line \ell_{13}
                                                                      791 : P_{204382} = (29, 56, 48, 1) lies on line \ell_5
738: P_{188005} = (36, 56, 44, 1) lies on line \ell_8
                                                                      792: P_{204454} = (37, 57, 48, 1) lies on line \ell_6
739: P_{188018} = (49, 56, 44, 1) lies on line \ell_5
                                                                      793: P_{204462} = (45, 57, 48, 1) lies on line \ell_9
740: P_{188042} = (9, 57, 44, 1) lies on line \ell_6
                                                                      794: P_{204865} = (0, 0, 49, 1) lies on line \ell_3
741: P_{188062} = (29, 57, 44, 1) lies on line \ell_9
                                                                      795: P_{204957} = (28, 1, 49, 1) lies on line \ell_4
742: P_{188481} = (0, 0, 45, 1) lies on line \ell_3
                                                                      796: P_{204973} = (44, 1, 49, 1) lies on line \ell_7
743: P_{188573} = (28, 1, 45, 1) lies on line \ell_7
                                                                      797: P_{205414} = (37, 8, 49, 1) lies on line \ell_{10}
744: P_{188593} = (48, 1, 45, 1) lies on line \ell_4
                                                                      798: P_{205461} = (20, 9, 49, 1) lies on line \ell_{11}
                                                                      799 : P_{206174} = (29, 20, 49, 1) lies on line \ell_{14}
745: P_{189086} = (29, 9, 45, 1) lies on line \ell_{13}
746: P_{189770} = (9, 20, 45, 1) lies on line \ell_{10}
                                                                     800: P_{206685} = (28, 28, 49, 1) lies on line \ell_{12}
                                                                     801 : P_{207278} = (45, 37, 49, 1) lies on line \ell_{13}
747: P_{189861} = (36, 21, 45, 1) lies on line \ell_{11}
748: P_{190301} = (28, 28, 45, 1) lies on line \ell_{15}
                                                                      802: P_{207725} = (44, 44, 49, 1) lies on line \ell_{15}
749 : P_{190834} = (49, 36, 45, 1) lies on line \ell_{14}
                                                                      803 : P_{208486} = (37, 56, 49, 1) lies on line \ell_5
750: P_{191601} = (48, 48, 45, 1) lies on line \ell_{12}
                                                                     804 : P_{208494} = (45, 56, 49, 1) lies on line \ell_8
                                                                     805: P_{208533} = (20, 57, 49, 1) lies on line \ell_9
751: P_{192074} = (9, 56, 45, 1) lies on line \ell_5
752 : P_{192094} = (29, 56, 45, 1) lies on line \ell_8
                                                                     806: P_{208542} = (29, 57, 49, 1) lies on line \ell_6
753: P_{192165} = (36, 57, 45, 1) lies on line \ell_9
                                                                     807: P_{208961} = (0, 0, 50, 1) lies on line \ell_3
754 : P_{192178} = (49, 57, 45, 1) lies on line \ell_6
                                                                     808: P_{209031} = (6, 1, 50, 1) lies on line \ell_7
755: P_{192577} = (0, 0, 46, 1) lies on line \ell_3
                                                                     809: P_{209078} = (53, 1, 50, 1) lies on line \ell_4
756: P_{192666} = (25, 1, 46, 1) lies on line \ell_4
                                                                     810: P_{209351} = (6, 6, 50, 1) lies on line \ell_{15}
757: P_{192695} = (54, 1, 46, 1) lies on line \ell_7
                                                                      811: P_{209663} = (62, 10, 50, 1) lies on line \ell_{11}
758: P_{193497} = (24, 14, 46, 1) lies on line \ell_{14}
                                                                     812: P_{209677} = (12, 11, 50, 1) lies on line \ell_{10}
759: P_{193999} = (14, 22, 46, 1) lies on line \ell_{11}
                                                                     813: P_{209736} = (7, 12, 50, 1) lies on line \ell_{13}
760: P_{194081} = (32, 23, 46, 1) lies on line \ell_{10}
                                                                     814: P_{212406} = (53, 53, 50, 1) lies on line \ell_{12}
761: P_{194202} = (25, 25, 46, 1) lies on line \ell_{12}
                                                                     815: P_{212552} = (7, 56, 50, 1) lies on line \ell_8
                                                                     816: P_{212557} = (12, 56, 50, 1) lies on line \ell_5
762: P_{194680} = (55, 32, 46, 1) lies on line \ell_{13}
763: P_{196087} = (54, 54, 46, 1) lies on line \ell_{15}
                                                                     817: P_{212661} = (52, 57, 50, 1) lies on line \ell_6
764 : P_{196193} = (32, 56, 46, 1) lies on line \ell_5
                                                                     818: P_{212671} = (62, 57, 50, 1) lies on line \ell_9
765: P_{196216} = (55, 56, 46, 1) lies on line \ell_8
                                                                     819: P_{212981} = (52, 62, 50, 1) lies on line \ell_{14}
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820: P_{213057} = (0, 0, 51, 1) lies on line \ell_3
                                                                     874: P_{229552} = (47, 1, 55, 1) lies on line \ell_4
821: P_{213134} = (13, 1, 51, 1) lies on line \ell_4
                                                                     875: P_{230359} = (22, 14, 55, 1) lies on line \ell_{10}
822: P_{213184} = (63, 1, 51, 1) lies on line \ell_7
                                                                     876: P_{230434} = (33, 15, 55, 1) lies on line \ell_{11}
823: P_{213517} = (12, 7, 51, 1) lies on line \ell_{14}
                                                                     877: P_{230873} = (24, 22, 55, 1) lies on line \ell_{13}
824: P_{213749} = (52, 10, 51, 1) lies on line \ell_{10}
                                                                     878: P_{231066} = (25, 25, 55, 1) lies on line \ell_{15}
825: P_{213768} = (7, 11, 51, 1) lies on line \ell_{11}
                                                                     879: P_{231599} = (46, 33, 55, 1) lies on line \ell_{14}
                                                                     880: P_{232496} = (47, 47, 55, 1) lies on line \ell_{12}
826: P_{213902} = (13, 13, 51, 1) lies on line \ell_{12}
827: P_{216447} = (62, 52, 51, 1) lies on line \ell_{13}
                                                                     881: P_{233047} = (22, 56, 55, 1) lies on line \ell_5
828: P_{216693} = (52, 56, 51, 1) lies on line \ell_5
                                                                     882 : P_{233049} = (24, 56, 55, 1) lies on line \ell_8
829: P_{216703} = (62, 56, 51, 1) lies on line \ell_8
                                                                     883: P_{233122} = (33, 57, 55, 1) lies on line \ell_9
830: P_{216712} = (7, 57, 51, 1) lies on line \ell_9
                                                                     884: P_{233135} = (46, 57, 55, 1) lies on line \ell_6
831 : P_{216717} = (12, 57, 51, 1) lies on line \ell_6
                                                                     885: P_{241729} = (0, 0, 58, 1) lies on line \ell_3
832: P_{217152} = (63, 63, 51, 1) lies on line \ell_{15}
                                                                     886: P_{241809} = (16, 1, 58, 1) lies on line \ell_4
833: P_{217153} = (0, 0, 52, 1) lies on line \ell_3
                                                                     887: P_{241836} = (43, 1, 58, 1) lies on line \ell_7
                                                                     888: P_{241876} = (19, 2, 58, 1) lies on line \ell_{11}
834 : P_{217223} = (6, 1, 52, 1) lies on line \ell_4
835: P_{217268} = (51, 1, 52, 1) lies on line \ell_7
                                                                     889: P_{241962} = (41, 3, 58, 1) lies on line \ell_{10}
836: P_{217543} = (6, 6, 52, 1) lies on line \ell_{12}
                                                                     890: P_{242769} = (16, 16, 58, 1) lies on line \ell_{12}
837: P_{217864} = (7, 11, 52, 1) lies on line \ell_{14}
                                                                     891: P_{242962} = (17, 19, 58, 1) lies on line \ell_{14}
838: P_{217932} = (11, 12, 52, 1) lies on line \ell_{11}
                                                                     892: P_{244395} = (42, 41, 58, 1) lies on line \ell_{13}
839: P_{218048} = (63, 13, 52, 1) lies on line \ell_{10}
                                                                     893: P_{244524} = (43, 43, 58, 1) lies on line \ell_{15}
840: P_{220468} = (51, 51, 52, 1) lies on line \ell_{15}
                                                                     894 : P_{245354} = (41, 56, 58, 1) lies on line \ell_5
841 : P_{220787} = (50, 56, 52, 1) lies on line \ell_8
                                                                     895: P_{245355} = (42, 56, 58, 1) lies on line \ell_8
842: P_{220800} = (63, 56, 52, 1) lies on line \ell_5
                                                                     896: P_{245394} = (17, 57, 58, 1) lies on line \ell_6
843 : P_{220808} = (7, 57, 52, 1) lies on line \ell_6
                                                                     897: P_{245396} = (19, 57, 58, 1) lies on line \ell_9
844: P_{220812} = (11, 57, 52, 1) lies on line \ell_9
                                                                     898: P_{245825} = (0, 0, 59, 1) lies on line \ell_3
845: P_{221235} = (50, 63, 52, 1) lies on line \ell_{13}
                                                                     899: P_{245907} = (18, 1, 59, 1) lies on line \ell_7
846: P_{221249} = (0, 0, 53, 1) lies on line \ell_3
                                                                     900: P_{245929} = (40, 1, 59, 1) lies on line \ell_4
847: P_{221323} = (10, 1, 53, 1) lies on line \ell_7
                                                                     901: P_{245970} = (17, 2, 59, 1) lies on line \ell_{10}
848: P_{221375} = (62, 1, 53, 1) lies on line \ell_4
                                                                     902: P_{246059} = (42, 3, 59, 1) lies on line \ell_{11}
849: P_{221708} = (11, 7, 53, 1) lies on line \ell_{13}
                                                                     903: P_{246932} = (19, 17, 59, 1) lies on line \ell_{13}
850: P_{221899} = (10, 10, 53, 1) lies on line \ell_{15}
                                                                     904: P_{246995} = (18, 18, 59, 1) lies on line \ell_{15}
851: P_{222024} = (7, 12, 53, 1) lies on line \ell_{10}
                                                                     905: P_{248425} = (40, 40, 59, 1) lies on line \ell_{12}
852: P_{222131} = (50, 13, 53, 1) lies on line \ell_{11}
                                                                     906: P_{248554} = (41, 42, 59, 1) lies on line \ell_{14}
853: P_{224512} = (63, 50, 53, 1) lies on line \ell_{14}
                                                                     907: P_{249426} = (17, 56, 59, 1) lies on line \ell_5
854: P_{224840} = (7, 56, 53, 1) lies on line \ell_5
                                                                     908: P_{249428} = (19, 56, 59, 1) lies on line \ell_8
855: P_{224844} = (11, 56, 53, 1) lies on line \ell_8
                                                                     909: P_{249514} = (41, 57, 59, 1) lies on line \ell_6
856: P_{224947} = (50, 57, 53, 1) lies on line \ell_9
                                                                     910: P_{249515} = (42, 57, 59, 1) lies on line \ell_9
857: P_{224960} = (63, 57, 53, 1) lies on line \ell_6
                                                                     911: P_{249921} = (0, 0, 60, 1) lies on line \ell_3
                                                                     912 : P_{250015} = (30, 1, 60, 1) lies on line \ell_7
858: P_{225279} = (62, 62, 53, 1) lies on line \ell_{12}
859: P_{225345} = (0, 0, 54, 1) lies on line \ell_3
                                                                     913: P_{250020} = (35, 1, 60, 1) lies on line \ell_4
860: P_{225432} = (23, 1, 54, 1) lies on line \ell_4
                                                                     914: P_{250215} = (38, 4, 60, 1) lies on line \ell_{11}
861: P_{225441} = (32, 1, 54, 1) lies on line \ell_7
                                                                     915: P_{250267} = (26, 5, 60, 1) lies on line \ell_{10}
862 : P_{226265} = (24, 14, 54, 1) lies on line \ell_{11}
                                                                     916 : P_{251616} = (31, 26, 60, 1) lies on line \ell_{13}
863: P_{226351} = (46, 15, 54, 1) lies on line \ell_{10}
                                                                     917: P_{251871} = (30, 30, 60, 1) lies on line \ell_{15}
864: P_{226840} = (23, 23, 54, 1) lies on line \ell_{12}
                                                                     918: P_{252196} = (35, 35, 60, 1) lies on line \ell_{12}
865 : P_{226903} = (22, 24, 54, 1) lies on line \ell_{14}
                                                                     919: P_{252387} = (34, 38, 60, 1) lies on line \ell_{14}
866: P_{227425} = (32, 32, 54, 1) lies on line \ell_{15}
                                                                     920: P_{253531} = (26, 56, 60, 1) lies on line \ell_5
867: P_{228322} = (33, 46, 54, 1) lies on line \ell_{13}
                                                                     921: P_{253536} = (31, 56, 60, 1) lies on line \ell_8
868: P_{228962} = (33, 56, 54, 1) lies on line \ell_8
                                                                     922: P_{253603} = (34, 57, 60, 1) lies on line \ell_6
869: P_{228975} = (46, 56, 54, 1) lies on line \ell_5
                                                                     923: P_{253607} = (38, 57, 60, 1) lies on line \ell_9
870: P_{229015} = (22, 57, 54, 1) lies on line \ell_6
                                                                     924: P_{254017} = (0, 0, 61, 1) lies on line \ell_3
871: P_{229017} = (24, 57, 54, 1) lies on line \ell_9
                                                                     925: P_{254108} = (27, 1, 61, 1) lies on line \ell_4
872: P_{229441} = (0, 0, 55, 1) lies on line \ell_3
                                                                     926: P_{254120} = (39, 1, 61, 1) lies on line \ell_7
873: P_{229530} = (25, 1, 55, 1) lies on line \ell_7
                                                                     927: P_{254307} = (34, 4, 61, 1) lies on line \ell_{10}
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928: P_{254368} = (31, 5, 61, 1) lies on line \ell_{11}
                                                                     946: P_{261708} = (11, 56, 62, 1) lies on line \ell_5
929 : P_{255772} = (27, 27, 61, 1) lies on line \ell_{12}
                                                                     947: P_{261709} = (12, 56, 62, 1) lies on line \ell_8
                                                                     948: P_{261812} = (51, 57, 62, 1) lies on line \ell_6
930: P_{256027} = (26, 31, 61, 1) lies on line \ell_{14}
931: P_{256231} = (38, 34, 61, 1) lies on line \ell_{13}
                                                                     949: P_{261814} = (53, 57, 62, 1) lies on line \ell_9
932: P_{256552} = (39, 39, 61, 1) lies on line \ell_{15}
                                                                     950: P_{262209} = (0, 0, 63, 1) lies on line \ell_3
933: P_{257635} = (34, 56, 61, 1) lies on line \ell_5
                                                                     951: P_{262283} = (10, 1, 63, 1) lies on line \ell_4
                                                                     952 : P_{262325} = (52, 1, 63, 1) lies on line \ell_7
934: P_{257639} = (38, 56, 61, 1) lies on line \ell_8
935: P_{257691} = (26, 57, 61, 1) lies on line \ell_6
                                                                     953: P_{262644} = (51, 6, 63, 1) lies on line \ell_{10}
936: P_{257696} = (31, 57, 61, 1) lies on line \ell_9
                                                                     954: P_{262669} = (12, 7, 63, 1) lies on line \ell_{11}
937: P_{258113} = (0, 0, 62, 1) lies on line \ell_3
                                                                     955: P_{262859} = (10, 10, 63, 1) lies on line \ell_{12}
938: P_{258190} = (13, 1, 62, 1) lies on line \ell_7
                                                                     956: P_{262988} = (11, 12, 63, 1) lies on line \ell_{14}
939: P_{258227} = (50, 1, 62, 1) lies on line \ell_4
                                                                     957: P_{265526} = (53, 51, 63, 1) lies on line \ell_{13}
940: P_{258550} = (53, 6, 62, 1) lies on line \ell_{11}
                                                                     958: P_{265589} = (52, 52, 63, 1) lies on line \ell_{15}
941: P_{258572} = (11, 7, 62, 1) lies on line \ell_{10}
                                                                     959: P_{265844} = (51, 56, 63, 1) lies on line \ell_5
942 : P_{258829} = (12, 11, 62, 1) lies on line \ell_{13}
                                                                     960: P_{265846} = (53, 56, 63, 1) lies on line \ell_8
943: P_{258958} = (13, 13, 62, 1) lies on line \ell_{15}
                                                                     961: P_{265868} = (11, 57, 63, 1) lies on line \ell_6
944: P_{261363} = (50, 50, 62, 1) lies on line \ell_{12}
                                                                     962: P_{265869} = (12, 57, 63, 1) lies on line \ell_9
945: P_{261556} = (51, 53, 62, 1) lies on line \ell_{14}
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The single points on the surface are:

Points on surface but on no line

The surface has 3420 points not on any line: Too many to print.

Line Intersection Graph

	0 1	2	2	1	5	6	7	Q	a	10	11	19	12	11	15
	_								9	10	11	14	10	14	10
0	0 1	1	1	1	1	1	1	1	1	0	0	0	0	0	0
1	10	1	0	0	0	0	1	1	1	0	1	0	1	0	1
2	11	0	0	1	1	1	0	0	0	1	0	1	0	1	0
3	10	0	0	0	0	0	0	0	0	1	1	1	1	1	1
4	10	1	0	0	1	1	1	0	0	0	1	1	1	0	0
5	10	1	0	1	0	1	0	1	0	1	1	0	0	0	1
6	10	1	0	1	1	0	0	0	1	0	0	0	1	1	1
7	11	0	0	1	0	0	0	1	1	1	0	0	0	1	1
8	11	0	0	0	1	0	1	0	1	0	0	1	1	1	0
9	11	0	0	0	0	1	1	1	0	1	1	1	0	0	0
10	00	1	1	0	1	0	1	0	1	0	0	0	1	0	0
11	0.1	0	1	1	1	0	0	0	1	0	0	0	0	1	0
12	0 0	1	1	1	0	0	0	1	1	0	0	0	0	0	1
13	0.1	0	1	1	0	1	0	1	0	1	0	0	0	0	0
14	0 0	1	1	0	0	1	1	1	0	0	1	0	0	0	0
15	0.1	0	1	0	1	1	1	0	0	0	0	1	0	0	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9
in point	P_{124}	P_{123}	P_2	P_{123}	P_{123}	P_{123}	P_{124}	P_{124}	P_{124}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_7	ℓ_8	ℓ_9	ℓ_{11}	ℓ_{13}	ℓ_{15}
in point	P_{124}	P_1	P_{124}	P_{124}	P_{124}	P_{188}	P_{3708}	P_{3772}

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_4	ℓ_5	ℓ_6	ℓ_{10}	ℓ_{12}	ℓ_{14}
in point	P_{123}	P_1	P_{123}	P_{123}	P_{123}	P_{187}	P_{3707}	P_{3771}

Line 3 intersects

Line	ℓ_0	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}
in point	P_2	P_{237633}	P_{233537}	P_{8258}	P_{237633}	P_{233537}	P_{8258}

Line 4 intersects

Line	ℓ_0	ℓ_2	ℓ_5	ℓ_6	ℓ_7	ℓ_{11}	ℓ_{12}	ℓ_{13}
in point	P_{123}	P_{123}	P_{123}	P_{123}	P_{8322}	P_{237754}	P_{233602}	P_{4282}

Line 5 intersects

Line	ℓ_0	ℓ_2	ℓ_4	ℓ_6	ℓ_8	ℓ_{10}	ℓ_{11}	ℓ_{15}
in point	P_{123}	P_{123}	P_{123}	P_{123}	P_{241217}	P_{11898}	P_{7747}	P_{237177}

 ${\bf Line~6~intersects}$

Line	ℓ_0	ℓ_2	ℓ_4	ℓ_5	ℓ_9	ℓ_{13}	ℓ_{14}	ℓ_{15}
in point	P_{123}	P_{123}	P_{123}	P_{123}	P_{237185}	P_{11906}	P_{241337}	P_{7867}

Line 7 intersects

Line	ℓ_0	ℓ_1	ℓ_4	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{14}	ℓ_{15}
in point	P_{124}	P_{124}	P_{8322}	P_{124}	P_{124}	P_{233657}	P_{4283}	P_{237698}

Line 8 intersects

Line	ℓ_0	ℓ_1	ℓ_5	ℓ_7	ℓ_9	ℓ_{12}	ℓ_{13}	ℓ_{14}
in point	P_{124}	P_{124}	P_{241217}	P_{124}	P_{124}	P_{7802}	P_{237178}	P_{11842}

Line 9 intersects $\frac{1}{2}$

Line	ℓ_0	ℓ_1	ℓ_6	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}	ℓ_{12}
in point	P_{124}	P_{124}	P_{237185}	P_{124}	P_{124}	P_{7811}	P_{11961}	P_{241338}

Line 10 intersects

Line	ℓ_2	ℓ_3	ℓ_5	ℓ_7	ℓ_9	ℓ_{13}
in point	P_{187}	P_{237633}	P_{11898}	P_{233657}	P_{7811}	P_{237633}

 ${\bf Line~11~intersects}$

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_9	ℓ_{14}
in point	P_{188}	P_{233537}	P_{237754}	P_{7747}	P_{11961}	P_{233537}

 ${\rm Line}\ 12\ {\rm intersects}$

Line	ℓ_2	ℓ_3	ℓ_4	ℓ_8	ℓ_9	ℓ_{15}
in point	P_{3707}	P_{8258}	P_{233602}	P_{7802}	P_{241338}	P_{8258}

Line 13 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_6	ℓ_8	ℓ_{10}
in point	P_{3708}	P_{237633}	P_{4282}	P_{11906}	P_{237178}	P_{237633}

 ${\bf Line~14~intersects}$

Line	ℓ_2	ℓ_3	ℓ_6	ℓ_7	ℓ_8	ℓ_{11}
in point	P_{3771}	P_{233537}	P_{241337}	P_{4283}	P_{11842}	P_{233537}

 ${\rm Line}\ 15\ {\rm intersects}$

Line	ℓ_1	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_{12}
in point	P_{3772}	P_{8258}	P_{237177}	P_{7867}	P_{237698}	P_{8258}

The surface has 4417 points:

Too many to print.