Rank-65548 over GF(16)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_3^3 + X_0 X_1 X_2 = 0$$

(1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over GF(16) is 286335254

General information

Number of lines	7
Number of points	305
Number of singular points	2
Number of Eckardt points	0
Number of double points	3
Number of single points	105
Number of points off lines	195
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17 ⁷
Type of lines on points	$4^2, 2^3, 1^{105}, 0^{195}$

Singular Points

The surface has 2 singular points:

$$0: P_1 = \mathbf{P}(0, 1, 0, 0) = \mathbf{P}(0, 1, 0, 0) 1: P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0)$$

The 7 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69888} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69888} = \mathbf{Pl}(0, 0, 0, 0, 0, 1)_{4625}$$

$$\ell_{1} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{4368} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{4368} = \mathbf{Pl}(1,0,0,1,0,0)_{34}$$

$$\ell_{2} = \begin{bmatrix} 1 & 0 & 0 & \delta^{5} \\ 0 & 1 & 0 & 0 \end{bmatrix}_{48048} = \begin{bmatrix} 1 & 0 & 0 & 11 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{48048} = \mathbf{Pl}(10,0,0,1,0,0)_{43}$$

$$\ell_{3} = \begin{bmatrix} 1 & 0 & 0 & \delta^{10} \\ 0 & 1 & 0 & 0 \end{bmatrix}_{43680} = \begin{bmatrix} 1 & 0 & 0 & 10 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{43680} = \mathbf{Pl}(11,0,0,1,0,0)_{44}$$

$$\ell_{4} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4624} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4624} = \mathbf{Pl}(0,1,1,0,0,0)_{18}$$

$$\ell_{5} = \begin{bmatrix} 1 & 0 & 0 & \delta^{5} \\ 0 & 0 & 1 & 0 \end{bmatrix}_{48304} = \begin{bmatrix} 1 & 0 & 0 & 11 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{48304} = \mathbf{Pl}(0,11,1,0,0,0)_{28}$$

$$\ell_{6} = \begin{bmatrix} 1 & 0 & 0 & \delta^{10} \\ 0 & 0 & 1 & 0 \end{bmatrix}_{43936} = \begin{bmatrix} 1 & 0 & 0 & 10 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{43936} = \mathbf{Pl}(0,10,1,0,0,0)_{27}$$

Rank of lines: (69888, 4368, 48048, 43680, 4624, 48304, 43936) Rank of points on Klein quadric: (4625, 34, 43, 44, 18, 28, 27)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 3 Double points: The double points on the surface are:

$$P_{275} = (1, 0, 0, 1) = \ell_1 \cap \ell_4$$

$$P_{284} = (10, 0, 0, 1) = \ell_2 \cap \ell_5$$

 $P_{285} = (11, 0, 0, 1) = \ell_3 \cap \ell_6$

Single Points

The surface has 105 single points: The single points on the surface are:

$0: P_{35} = (0, 1, 1, 0)$ lies on line ℓ_0	15: $P_{291} = (1, 1, 0, 1)$ lies on line ℓ_1
1: $P_{51} = (0, 2, 1, 0)$ lies on line ℓ_0	16: $P_{300} = (10, 1, 0, 1)$ lies on line ℓ_2
2: $P_{67} = (0, 3, 1, 0)$ lies on line ℓ_0	17: $P_{301} = (11, 1, 0, 1)$ lies on line ℓ_3
$3: P_{83} = (0,4,1,0)$ lies on line ℓ_0	18: $P_{307} = (1, 2, 0, 1)$ lies on line ℓ_1
4: $P_{99} = (0, 5, 1, 0)$ lies on line ℓ_0	19: $P_{316} = (10, 2, 0, 1)$ lies on line ℓ_2
$5: P_{115} = (0, 6, 1, 0)$ lies on line ℓ_0	20: $P_{317} = (11, 2, 0, 1)$ lies on line ℓ_3
6: $P_{131} = (0, 7, 1, 0)$ lies on line ℓ_0	$21: P_{323} = (1, 3, 0, 1)$ lies on line ℓ_1
7: $P_{147} = (0, 8, 1, 0)$ lies on line ℓ_0	22: $P_{332} = (10, 3, 0, 1)$ lies on line ℓ_2
8: $P_{163} = (0, 9, 1, 0)$ lies on line ℓ_0	23: $P_{333} = (11, 3, 0, 1)$ lies on line ℓ_3
9: $P_{179} = (0, 10, 1, 0)$ lies on line ℓ_0	$24: P_{339} = (1, 4, 0, 1)$ lies on line ℓ_1
10: $P_{195} = (0, 11, 1, 0)$ lies on line ℓ_0	25: $P_{348} = (10, 4, 0, 1)$ lies on line ℓ_2
11: $P_{211} = (0, 12, 1, 0)$ lies on line ℓ_0	26: $P_{349} = (11, 4, 0, 1)$ lies on line ℓ_3
12: $P_{227} = (0, 13, 1, 0)$ lies on line ℓ_0	27: $P_{355} = (1, 5, 0, 1)$ lies on line ℓ_1
13: $P_{243} = (0, 14, 1, 0)$ lies on line ℓ_0	28: $P_{364} = (10, 5, 0, 1)$ lies on line ℓ_2
14: $P_{259} = (0, 15, 1, 0)$ lies on line ℓ_0	29: $P_{365} = (11, 5, 0, 1)$ lies on line ℓ_3

```
30: P_{371} = (1, 6, 0, 1) lies on line \ell_1
                                                                      68: P_{1052} = (11, 0, 3, 1) lies on line \ell_6
31: P_{380} = (10, 6, 0, 1) lies on line \ell_2
                                                                      69: P_{1298} = (1,0,4,1) lies on line \ell_4
                                                                      70: P_{1307} = (10, 0, 4, 1) lies on line \ell_5
32: P_{381} = (11, 6, 0, 1) lies on line \ell_3
33: P_{387} = (1, 7, 0, 1) lies on line \ell_1
                                                                      71: P_{1308} = (11, 0, 4, 1) lies on line \ell_6
34: P_{396} = (10, 7, 0, 1) lies on line \ell_2
                                                                      72: P_{1554} = (1, 0, 5, 1) lies on line \ell_4
35: P_{397} = (11,7,0,1) lies on line \ell_3
                                                                      73: P_{1563} = (10, 0, 5, 1) lies on line \ell_5
36: P_{403} = (1, 8, 0, 1) lies on line \ell_1
                                                                      74: P_{1564} = (11, 0, 5, 1) lies on line \ell_6
37: P_{412} = (10, 8, 0, 1) lies on line \ell_2
                                                                      75: P_{1810} = (1, 0, 6, 1) lies on line \ell_4
38: P_{413} = (11, 8, 0, 1) lies on line \ell_3
                                                                      76: P_{1819} = (10, 0, 6, 1) lies on line \ell_5
39: P_{419} = (1, 9, 0, 1) lies on line \ell_1
                                                                      77: P_{1820} = (11, 0, 6, 1) lies on line \ell_6
40: P_{428} = (10, 9, 0, 1) lies on line \ell_2
                                                                      78: P_{2066} = (1, 0, 7, 1) lies on line \ell_4
41: P_{429} = (11, 9, 0, 1) lies on line \ell_3
                                                                      79: P_{2075} = (10, 0, 7, 1) lies on line \ell_5
42: P_{435} = (1, 10, 0, 1) lies on line \ell_1
                                                                     80: P_{2076} = (11, 0, 7, 1) lies on line \ell_6
43: P_{444} = (10, 10, 0, 1) lies on line \ell_2
                                                                     81: P_{2322} = (1,0,8,1) lies on line \ell_4
44: P_{445} = (11, 10, 0, 1) lies on line \ell_3
                                                                     82: P_{2331} = (10, 0, 8, 1) lies on line \ell_5
45: P_{451} = (1, 11, 0, 1) lies on line \ell_1
                                                                     83: P_{2332} = (11, 0, 8, 1) lies on line \ell_6
46: P_{460} = (10, 11, 0, 1) lies on line \ell_2
                                                                     84: P_{2578} = (1,0,9,1) lies on line \ell_4
47: P_{461} = (11, 11, 0, 1) lies on line \ell_3
                                                                     85: P_{2587} = (10, 0, 9, 1) lies on line \ell_5
48: P_{467} = (1, 12, 0, 1) lies on line \ell_1
                                                                     86: P_{2588} = (11, 0, 9, 1) lies on line \ell_6
49: P_{476} = (10, 12, 0, 1) lies on line \ell_2
                                                                     87: P_{2834} = (1, 0, 10, 1) lies on line \ell_4
50: P_{477} = (11, 12, 0, 1) lies on line \ell_3
                                                                     88: P_{2843} = (10, 0, 10, 1) lies on line \ell_5
51: P_{483} = (1, 13, 0, 1) lies on line \ell_1
                                                                     89: P_{2844} = (11, 0, 10, 1) lies on line \ell_6
52: P_{492} = (10, 13, 0, 1) lies on line \ell_2
                                                                     90: P_{3090} = (1, 0, 11, 1) lies on line \ell_4
                                                                     91 : P_{3099} = (10, 0, 11, 1) lies on line \ell_5
53: P_{493} = (11, 13, 0, 1) lies on line \ell_3
54: P_{499} = (1, 14, 0, 1) lies on line \ell_1
                                                                     92: P_{3100} = (11, 0, 11, 1) lies on line \ell_6
55: P_{508} = (10, 14, 0, 1) lies on line \ell_2
                                                                     93: P_{3346} = (1, 0, 12, 1) lies on line \ell_4
56: P_{509} = (11, 14, 0, 1) lies on line \ell_3
                                                                     94: P_{3355} = (10, 0, 12, 1) lies on line \ell_5
57: P_{515} = (1, 15, 0, 1) lies on line \ell_1
                                                                     95: P_{3356} = (11, 0, 12, 1) lies on line \ell_6
58: P_{524} = (10, 15, 0, 1) lies on line \ell_2
                                                                     96: P_{3602} = (1, 0, 13, 1) lies on line \ell_4
59: P_{525} = (11, 15, 0, 1) lies on line \ell_3
                                                                     97: P_{3611} = (10, 0, 13, 1) lies on line \ell_5
60: P_{531} = (1,0,1,1) lies on line \ell_4
                                                                     98: P_{3612} = (11, 0, 13, 1) lies on line \ell_6
61: P_{540} = (10, 0, 1, 1) lies on line \ell_5
                                                                     99: P_{3858} = (1, 0, 14, 1) lies on line \ell_4
62: P_{541} = (11, 0, 1, 1) lies on line \ell_6
                                                                     100: P_{3867} = (10, 0, 14, 1) lies on line \ell_5
63: P_{786} = (1,0,2,1) lies on line \ell_4
                                                                     101: P_{3868} = (11, 0, 14, 1) lies on line \ell_6
64: P_{795} = (10, 0, 2, 1) lies on line \ell_5
                                                                     102: P_{4114} = (1, 0, 15, 1) lies on line \ell_4
65: P_{796} = (11, 0, 2, 1) lies on line \ell_6
                                                                     103: P_{4123} = (10, 0, 15, 1) lies on line \ell_5
66: P_{1042} = (1,0,3,1) lies on line \ell_4
                                                                     104: P_{4124} = (11, 0, 15, 1) lies on line \ell_6
67: P_{1051} = (10, 0, 3, 1) lies on line \ell_5
```

The single points on the surface are:

Points on surface but on no line

The surface has 195 points not on any line: The points on the surface but not on lines are:

```
\begin{array}{lll} 0: \, P_{36} = (1,1,1,0) & 6: \, P_{144} = (13,7,1,0) \\ 1: \, P_{65} = (14,2,1,0) & 7: \, P_{152} = (5,8,1,0) \\ 2: \, P_{82} = (15,3,1,0) & 8: \, P_{167} = (4,9,1,0) \\ 3: \, P_{85} = (2,4,1,0) & 9: \, P_{190} = (11,10,1,0) \\ 4: \, P_{102} = (3,5,1,0) & 10: \, P_{205} = (10,11,1,0) \\ 5: \, P_{127} = (12,6,1,0) & 11: \, P_{218} = (7,12,1,0) \end{array}
```

```
66: P_{1635} = (2, 5, 5, 1)
12: P_{233} = (6, 13, 1, 0)
13: P_{252} = (9, 14, 1, 0)
                                                                  67: P_{1654} = (5, 6, 5, 1)
14: P_{267} = (8, 15, 1, 0)
                                                                  68: P_{1672} = (7, 7, 5, 1)
15: P_{568} = (7, 2, 1, 1)
                                                                  69: P_{1690} = (9, 8, 5, 1)
                                                                  70: P_{1712} = (15, 9, 5, 1)
16: P_{586} = (9, 3, 1, 1)
                                                                  71: P_{1719} = (6, 10, 5, 1)
17: P_{605} = (12, 4, 1, 1)
18: P_{623} = (14, 5, 1, 1)
                                                                  72: P_{1737} = (8, 11, 5, 1)
19: P_{640} = (15, 6, 1, 1)
                                                                  73: P_{1758} = (13, 12, 5, 1)
20: P_{646} = (5,7,1,1)
                                                                  74: P_{1789} = (12, 14, 5, 1)
21: P_{659} = (2, 8, 1, 1)
                                                                  75: P_{1840} = (15, 1, 6, 1)
22: P_{679} = (6, 9, 1, 1)
                                                                  76: P_{1849} = (8, 2, 6, 1)
23: P_{729} = (8, 12, 1, 1)
                                                                  77: P_{1894} = (5, 5, 6, 1)
24: P_{740} = (3, 13, 1, 1)
                                                                  78: P_{1908} = (3, 6, 6, 1)
                                                                  79: P_{1944} = (7, 8, 6, 1)
25: P_{766} = (13, 14, 1, 1)
26: P_{773} = (4, 15, 1, 1)
                                                                  80: P_{1965} = (12, 9, 6, 1)
27: P_{808} = (7, 1, 2, 1)
                                                                  81: P_{1982} = (13, 10, 6, 1)
28: P_{829} = (12, 2, 2, 1)
                                                                  82: P_{1987} = (2, 11, 6, 1)
29: P_{848} = (15, 3, 2, 1)
                                                                  83: P_{2010} = (9, 12, 6, 1)
30: P_{851} = (2,4,2,1)
                                                                  84: P_{2031} = (14, 13, 6, 1)
                                                                  85: P_{2037} = (4, 14, 6, 1)
31: P_{889} = (8, 6, 2, 1)
32: P_{910} = (13, 7, 2, 1)
                                                                  86: P_{2055} = (6, 15, 6, 1)
33: P_{919} = (6, 8, 2, 1)
                                                                  87: P_{2086} = (5, 1, 7, 1)
34: P_{948} = (3, 10, 2, 1)
                                                                  88: P_{2110} = (13, 2, 7, 1)
35: P_{965} = (4, 11, 2, 1)
                                                                  89: P_{2119} = (6, 3, 7, 1)
36: P_{1002} = (9, 13, 2, 1)
                                                                  90: P_{2143} = (14, 4, 7, 1)
37: P_{1023} = (14, 14, 2, 1)
                                                                  91: P_{2152} = (7, 5, 7, 1)
                                                                  92: P_{2185} = (8, 7, 7, 1)
38: P_{1030} = (5, 15, 2, 1)
39: P_{1066} = (9, 1, 3, 1)
                                                                  93: P_{2212} = (3, 9, 7, 1)
40: P_{1088} = (15, 2, 3, 1)
                                                                  94: P_{2237} = (12, 10, 7, 1)
41: P_{1103} = (14, 3, 3, 1)
                                                                  95: P_{2250} = (9, 11, 7, 1)
42: P_{1113} = (8,4,3,1)
                                                                  96: P_{2261} = (4, 12, 7, 1)
43: P_{1125} = (4, 5, 3, 1)
                                                                  97: P_{2275} = (2, 13, 7, 1)
44: P_{1159} = (6,7,3,1)
                                                                  98: P_{2320} = (15, 15, 7, 1)
45: P_{1192} = (7, 9, 3, 1)
                                                                  99: P_{2339} = (2, 1, 8, 1)
46: P_{1206} = (5, 10, 3, 1)
                                                                  100: P_{2359} = (6, 2, 8, 1)
                                                                  101: P_{2410} = (9, 5, 8, 1)
47: P_{1229} = (12, 11, 3, 1)
48: P_{1236} = (3, 12, 3, 1)
                                                                  102: P_{2424} = (7, 6, 8, 1)
                                                                  103: P_{2453} = (4, 8, 8, 1)
49: P_{1262} = (13, 13, 3, 1)
50: P_{1283} = (2, 15, 3, 1)
                                                                  104: P_{2470} = (5, 9, 8, 1)
51: P_{1325} = (12, 1, 4, 1)
                                                                  105: P_{2496} = (15, 10, 8, 1)
52: P_{1331} = (2, 2, 4, 1)
                                                                  106: P_{2510} = (13, 11, 8, 1)
                                                                  107: P_{2525} = (12, 12, 8, 1)
53: P_{1353} = (8, 3, 4, 1)
54: P_{1367} = (6, 4, 4, 1)
                                                                  108: P_{2537} = (8, 13, 8, 1)
                                                                  109: P_{2548} = (3, 14, 8, 1)
55: P_{1380} = (3, 5, 4, 1)
56: P_{1423} = (14, 7, 4, 1)
                                                                  110: P_{2575} = (14, 15, 8, 1)
                                                                  111: P_{2599} = (6, 1, 9, 1)
57: P_{1445} = (4, 9, 4, 1)
58: P_{1466} = (9, 10, 4, 1)
                                                                  112: P_{2632} = (7, 3, 9, 1)
59: P_{1478} = (5, 11, 4, 1)
                                                                  113: P_{2645} = (4, 4, 9, 1)
60: P_{1496} = (7, 12, 4, 1)
                                                                  114: P_{2672} = (15, 5, 9, 1)
61: P_{1520} = (15, 13, 4, 1)
                                                                  115: P_{2685} = (12, 6, 9, 1)
62: P_{1550} = (13, 15, 4, 1)
                                                                  116: P_{2692} = (3, 7, 9, 1)
63: P_{1583} = (14, 1, 5, 1)
                                                                  117: P_{2710} = (5, 8, 9, 1)
64: P_{1605} = (4, 3, 5, 1)
                                                                  118: P_{2734} = (13, 9, 9, 1)
65: P_{1620} = (3, 4, 5, 1)
                                                                  119: P_{2745} = (8, 10, 9, 1)
```

```
120: P_{2767} = (14, 11, 9, 1)
                                                                 158: P_{3574} = (5, 14, 12, 1)
121: P_{2771} = (2, 12, 9, 1)
                                                                 159: P_{3620} = (3, 1, 13, 1)
                                                                 160: P_{3642} = (9, 2, 13, 1)
122: P_{2810} = (9, 14, 9, 1)
123: P_{2868} = (3, 2, 10, 1)
                                                                 161: P_{3662} = (13, 3, 13, 1)
124: P_{2886} = (5, 3, 10, 1)
                                                                 162: P_{3680} = (15, 4, 13, 1)
125: P_{2906} = (9, 4, 10, 1)
                                                                 163: P_{3711} = (14, 6, 13, 1)
126: P_{2919} = (6, 5, 10, 1)
                                                                 164: P_{3715} = (2, 7, 13, 1)
127: P_{2942} = (13, 6, 10, 1)
                                                                 165: P_{3737} = (8, 8, 13, 1)
128: P_{2957} = (12, 7, 10, 1)
                                                                 166: P_{3765} = (4, 10, 13, 1)
129: P_{2976} = (15, 8, 10, 1)
                                                                 167: P_{3784} = (7, 11, 13, 1)
130: P_{2985} = (8, 9, 10, 1)
                                                                 168: P_{3814} = (5, 13, 13, 1)
131: P_{3039} = (14, 12, 10, 1)
                                                                 169: P_{3831} = (6, 14, 13, 1)
                                                                 170: P_{3853} = (12, 15, 13, 1)
132: P_{3045} = (4, 13, 10, 1)
133: P_{3059} = (2, 14, 10, 1)
                                                                 171: P_{3886} = (13, 1, 14, 1)
134: P_{3080} = (7, 15, 10, 1)
                                                                 172: P_{3903} = (14, 2, 14, 1)
135: P_{3125} = (4, 2, 11, 1)
                                                                 173: P_{3949} = (12, 5, 14, 1)
136: P_{3149} = (12, 3, 11, 1)
                                                                 174: P_{3957} = (4, 6, 14, 1)
137: P_{3158} = (5, 4, 11, 1)
                                                                 175: P_{3988} = (3, 8, 14, 1)
138: P_{3177} = (8, 5, 11, 1)
                                                                 176: P_{4010} = (9, 9, 14, 1)
139: P_{3187} = (2, 6, 11, 1)
                                                                 177: P_{4019} = (2, 10, 14, 1)
140: P_{3210} = (9, 7, 11, 1)
                                                                 178: P_{4048} = (15, 11, 14, 1)
141: P_{3230} = (13, 8, 11, 1)
                                                                 179: P_{4054} = (5, 12, 14, 1)
142: P_{3247} = (14, 9, 11, 1)
                                                                 180: P_{4071} = (6, 13, 14, 1)
143: P_{3287} = (6, 12, 11, 1)
                                                                 181: P_{4088} = (7, 14, 14, 1)
144: P_{3304} = (7, 13, 11, 1)
                                                                 182: P_{4105} = (8, 15, 14, 1)
145: P_{3328} = (15, 14, 11, 1)
                                                                 183: P_{4133} = (4, 1, 15, 1)
146: P_{3332} = (3, 15, 11, 1)
                                                                 184: P_{4150} = (5, 2, 15, 1)
147: P_{3369} = (8, 1, 12, 1)
                                                                 185 : P_{4163} = (2, 3, 15, 1)
                                                                 186: P_{4190} = (13, 4, 15, 1)
148: P_{3396} = (3, 3, 12, 1)
149: P_{3416} = (7, 4, 12, 1)
                                                                 187: P_{4215} = (6, 6, 15, 1)
150: P_{3438} = (13, 5, 12, 1)
                                                                 188: P_{4240} = (15, 7, 15, 1)
151: P_{3450} = (9, 6, 12, 1)
                                                                 189: P_{4255} = (14, 8, 15, 1)
152: P_{3461} = (4, 7, 12, 1)
                                                                 190: P_{4280} = (7, 10, 15, 1)
                                                                 191: P_{4292} = (3, 11, 15, 1)
153: P_{3485} = (12, 8, 12, 1)
154: P_{3491} = (2, 9, 12, 1)
                                                                 192: P_{4333} = (12, 13, 15, 1)
155: P_{3519} = (14, 10, 12, 1)
                                                                 193: P_{4345} = (8, 14, 15, 1)
156: P_{3527} = (6, 11, 12, 1)
                                                                 194: P_{4362} = (9, 15, 15, 1)
157: P_{3552} = (15, 12, 12, 1)
```

Line Intersection Graph

	0123456
0	0111111
1	1011100
2	1101010
3	1110001
4	1100011
5	1010101
6	$\begin{array}{c} 3 & 2 & 3 & 3 \\ 0 & 1 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 1 & 1 & 0 \\ \end{array}$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6
in point	P_1	P_1	P_1	P_2	P_2	P_2

Line	1	intersects

Line	ℓ_0	ℓ_2	ℓ_3	ℓ_4
in point	P_1	P_1	P_1	P_{275}

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_3	ℓ_5
in point	P_1	P_1	P_1	P_{284}

Line 3 intersects $\frac{1}{2}$

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_6
in point	P_1	P_1	P_1	P_{285}

Line 4 intersects

Line	ℓ_0	ℓ_1	ℓ_5	ℓ_6
in point	P_2	P_{275}	P_2	P_2

Line 5 intersects

Line	ℓ_0	ℓ_2	ℓ_4	ℓ_6
in point	P_2	P_{284}	P_2	P_2

Line 6 intersects

Line	ℓ_0	ℓ_3	ℓ_4	ℓ_5
in point	P_2	P_{285}	P_2	P_2

The surface has 305 points: The points on the surface are:

2 7 (2 1 2 2)	(0.47.4.0)	(10.0.1)
$0: P_1 = (0, 1, 0, 0)$	$30: P_{259} = (0, 15, 1, 0)$	$60: P_{428} = (10, 9, 0, 1)$
$1: P_2 = (0, 0, 1, 0)$	$31: P_{267} = (8, 15, 1, 0)$	$61: P_{429} = (11, 9, 0, 1)$
$2: P_{35} = (0, 1, 1, 0)$	$32: P_{275} = (1, 0, 0, 1)$	$62: P_{435} = (1, 10, 0, 1)$
$3: P_{36} = (1, 1, 1, 0)$	$33: P_{284} = (10, 0, 0, 1)$	$63: P_{444} = (10, 10, 0, 1)$
$4: P_{51} = (0, 2, 1, 0)$	$34: P_{285} = (11, 0, 0, 1)$	$64: P_{445} = (11, 10, 0, 1)$
$5: P_{65} = (14, 2, 1, 0)$	$35: P_{291} = (1, 1, 0, 1)$	$65: P_{451} = (1, 11, 0, 1)$
$6: P_{67} = (0, 3, 1, 0)$	$36: P_{300} = (10, 1, 0, 1)$	$66: P_{460} = (10, 11, 0, 1)$
$7: P_{82} = (15, 3, 1, 0)$	$37: P_{301} = (11, 1, 0, 1)$	$67: P_{461} = (11, 11, 0, 1)$
$8: P_{83} = (0, 4, 1, 0)$	$38: P_{307} = (1, 2, 0, 1)$	$68: P_{467} = (1, 12, 0, 1)$
$9: P_{85} = (2, 4, 1, 0)$	$39: P_{316} = (10, 2, 0, 1)$	$69: P_{476} = (10, 12, 0, 1)$
$10: P_{99} = (0, 5, 1, 0)$	$40: P_{317} = (11, 2, 0, 1)$	$70: P_{477} = (11, 12, 0, 1)$
$11: P_{102} = (3, 5, 1, 0)$	$41: P_{323} = (1, 3, 0, 1)$	$71: P_{483} = (1, 13, 0, 1)$
$12: P_{115} = (0, 6, 1, 0)$	$42: P_{332} = (10, 3, 0, 1)$	$72: P_{492} = (10, 13, 0, 1)$
13: $P_{127} = (12, 6, 1, 0)$	$43: P_{333} = (11, 3, 0, 1)$	$73: P_{493} = (11, 13, 0, 1)$
$14: P_{131} = (0, 7, 1, 0)$	$44: P_{339} = (1, 4, 0, 1)$	$74: P_{499} = (1, 14, 0, 1)$
$15: P_{144} = (13, 7, 1, 0)$	$45: P_{348} = (10, 4, 0, 1)$	$75: P_{508} = (10, 14, 0, 1)$
$16: P_{147} = (0, 8, 1, 0)$	$46: P_{349} = (11, 4, 0, 1)$	$76: P_{509} = (11, 14, 0, 1)$
$17: P_{152} = (5, 8, 1, 0)$	$47: P_{355} = (1, 5, 0, 1)$	77: $P_{515} = (1, 15, 0, 1)$
$18: P_{163} = (0, 9, 1, 0)$	$48: P_{364} = (10, 5, 0, 1)$	$78: P_{524} = (10, 15, 0, 1)$
$19: P_{167} = (4, 9, 1, 0)$	$49: P_{365} = (11, 5, 0, 1)$	$79: P_{525} = (11, 15, 0, 1)$
$20: P_{179} = (0, 10, 1, 0)$	$50: P_{371} = (1, 6, 0, 1)$	$80: P_{531} = (1,0,1,1)$
$21: P_{190} = (11, 10, 1, 0)$	$51: P_{380} = (10, 6, 0, 1)$	$81: P_{540} = (10, 0, 1, 1)$
$22: P_{195} = (0, 11, 1, 0)$	$52: P_{381} = (11, 6, 0, 1)$	$82: P_{541} = (11, 0, 1, 1)$
$23: P_{205} = (10, 11, 1, 0)$	$53: P_{387} = (1,7,0,1)$	$83: P_{568} = (7, 2, 1, 1)$
$24: P_{211} = (0, 12, 1, 0)$	$54: P_{396} = (10, 7, 0, 1)$	$84: P_{586} = (9, 3, 1, 1)$
$25: P_{218} = (7, 12, 1, 0)$	$55: P_{397} = (11, 7, 0, 1)$	$85: P_{605} = (12, 4, 1, 1)$
$26: P_{227} = (0, 13, 1, 0)$	$56: P_{403} = (1, 8, 0, 1)$	$86: P_{623} = (14, 5, 1, 1)$
$27: P_{233} = (6, 13, 1, 0)$	$57: P_{412} = (10, 8, 0, 1)$	$87: P_{640} = (15, 6, 1, 1)$
$28: P_{243} = (0, 14, 1, 0)$	$58: P_{413} = (11, 8, 0, 1)$	$88: P_{646} = (5, 7, 1, 1)$
$ \begin{array}{l} 20: P_{243} = (0, 14, 1, 0) \\ 29: P_{252} = (9, 14, 1, 0) \end{array} $	$59: P_{419} = (1, 9, 0, 1)$ $59: P_{419} = (1, 9, 0, 1)$	$89: P_{659} = (2, 8, 1, 1)$
20. 1 202 - (0, 14, 1, 0)	00 . 1419 — (1,0,0,1)	$0.5 \cdot 1_{0.09} - (2, 0, 1, 1)$

```
198: P_{2548} = (3, 14, 8, 1)
90: P_{679} = (6, 9, 1, 1)
                                           144: P_{1605} = (4, 3, 5, 1)
                                                                                       199: P_{2575} = (14, 15, 8, 1)
91: P_{729} = (8, 12, 1, 1)
                                           145: P_{1620} = (3, 4, 5, 1)
92: P_{740} = (3, 13, 1, 1)
                                                                                       200: P_{2578} = (1, 0, 9, 1)
                                           146: P_{1635} = (2, 5, 5, 1)
                                                                                       201: P_{2587} = (10, 0, 9, 1)
93: P_{766} = (13, 14, 1, 1)
                                           147: P_{1654} = (5, 6, 5, 1)
94: P_{773} = (4, 15, 1, 1)
                                           148: P_{1672} = (7, 7, 5, 1)
                                                                                       202: P_{2588} = (11, 0, 9, 1)
95: P_{786} = (1,0,2,1)
                                           149: P_{1690} = (9, 8, 5, 1)
                                                                                       203: P_{2599} = (6, 1, 9, 1)
96: P_{795} = (10, 0, 2, 1)
                                           150: P_{1712} = (15, 9, 5, 1)
                                                                                       204: P_{2632} = (7, 3, 9, 1)
97: P_{796} = (11, 0, 2, 1)
                                           151: P_{1719} = (6, 10, 5, 1)
                                                                                       205: P_{2645} = (4, 4, 9, 1)
98: P_{808} = (7, 1, 2, 1)
                                           152: P_{1737} = (8, 11, 5, 1)
                                                                                       206: P_{2672} = (15, 5, 9, 1)
99: P_{829} = (12, 2, 2, 1)
                                           153: P_{1758} = (13, 12, 5, 1)
                                                                                       207: P_{2685} = (12, 6, 9, 1)
100: P_{848} = (15, 3, 2, 1)
                                           154: P_{1789} = (12, 14, 5, 1)
                                                                                       208: P_{2692} = (3,7,9,1)
101: P_{851} = (2,4,2,1)
                                           155: P_{1810} = (1, 0, 6, 1)
                                                                                       209: P_{2710} = (5, 8, 9, 1)
102: P_{889} = (8, 6, 2, 1)
                                           156: P_{1819} = (10, 0, 6, 1)
                                                                                       210: P_{2734} = (13, 9, 9, 1)
103: P_{910} = (13, 7, 2, 1)
                                           157: P_{1820} = (11, 0, 6, 1)
                                                                                       211: P_{2745} = (8, 10, 9, 1)
                                                                                       212: P_{2767} = (14, 11, 9, 1)
104: P_{919} = (6, 8, 2, 1)
                                           158: P_{1840} = (15, 1, 6, 1)
105: P_{948} = (3, 10, 2, 1)
                                           159: P_{1849} = (8, 2, 6, 1)
                                                                                       213: P_{2771} = (2, 12, 9, 1)
                                           160 : P_{1894} = (5, 5, 6, 1)
106: P_{965} = (4, 11, 2, 1)
                                                                                       214: P_{2810} = (9, 14, 9, 1)
                                           161: P_{1908} = (3, 6, 6, 1)
107: P_{1002} = (9, 13, 2, 1)
                                                                                       215: P_{2834} = (1, 0, 10, 1)
108: P_{1023} = (14, 14, 2, 1)
                                                                                       216: P_{2843} = (10, 0, 10, 1)
                                           162: P_{1944} = (7, 8, 6, 1)
109: P_{1030} = (5, 15, 2, 1)
                                           163: P_{1965} = (12, 9, 6, 1)
                                                                                       217: P_{2844} = (11, 0, 10, 1)
110: P_{1042} = (1, 0, 3, 1)
                                           164: P_{1982} = (13, 10, 6, 1)
                                                                                       218: P_{2868} = (3, 2, 10, 1)
                                                                                       219: P_{2886} = (5, 3, 10, 1)
111: P_{1051} = (10, 0, 3, 1)
                                           165: P_{1987} = (2, 11, 6, 1)
                                                                                       220: P_{2906} = (9, 4, 10, 1)
112: P_{1052} = (11, 0, 3, 1)
                                           166: P_{2010} = (9, 12, 6, 1)
113: P_{1066} = (9, 1, 3, 1)
                                           167: P_{2031} = (14, 13, 6, 1)
                                                                                       221: P_{2919} = (6, 5, 10, 1)
114: P_{1088} = (15, 2, 3, 1)
                                           168: P_{2037} = (4, 14, 6, 1)
                                                                                       222: P_{2942} = (13, 6, 10, 1)
115: P_{1103} = (14, 3, 3, 1)
                                           169: P_{2055} = (6, 15, 6, 1)
                                                                                       223: P_{2957} = (12, 7, 10, 1)
116: P_{1113} = (8, 4, 3, 1)
                                           170: P_{2066} = (1, 0, 7, 1)
                                                                                       224: P_{2976} = (15, 8, 10, 1)
117: P_{1125} = (4, 5, 3, 1)
                                           171: P_{2075} = (10, 0, 7, 1)
                                                                                       225: P_{2985} = (8, 9, 10, 1)
118: P_{1159} = (6, 7, 3, 1)
                                                                                       226: P_{3039} = (14, 12, 10, 1)
                                           172: P_{2076} = (11, 0, 7, 1)
                                           173: P_{2086} = (5, 1, 7, 1)
119: P_{1192} = (7, 9, 3, 1)
                                                                                       227: P_{3045} = (4, 13, 10, 1)
120: P_{1206} = (5, 10, 3, 1)
                                           174: P_{2110} = (13, 2, 7, 1)
                                                                                       228: P_{3059} = (2, 14, 10, 1)
121: P_{1229} = (12, 11, 3, 1)
                                           175: P_{2119} = (6, 3, 7, 1)
                                                                                       229: P_{3080} = (7, 15, 10, 1)
122: P_{1236} = (3, 12, 3, 1)
                                           176: P_{2143} = (14, 4, 7, 1)
                                                                                       230: P_{3090} = (1, 0, 11, 1)
123: P_{1262} = (13, 13, 3, 1)
                                           177: P_{2152} = (7, 5, 7, 1)
                                                                                       231: P_{3099} = (10, 0, 11, 1)
124: P_{1283} = (2, 15, 3, 1)
                                           178: P_{2185} = (8,7,7,1)
                                                                                       232: P_{3100} = (11, 0, 11, 1)
125: P_{1298} = (1, 0, 4, 1)
                                           179: P_{2212} = (3, 9, 7, 1)
                                                                                       233: P_{3125} = (4, 2, 11, 1)
126: P_{1307} = (10, 0, 4, 1)
                                           180: P_{2237} = (12, 10, 7, 1)
                                                                                       234: P_{3149} = (12, 3, 11, 1)
                                                                                       235: P_{3158} = (5, 4, 11, 1)
127: P_{1308} = (11, 0, 4, 1)
                                           181: P_{2250} = (9, 11, 7, 1)
128: P_{1325} = (12, 1, 4, 1)
                                           182: P_{2261} = (4, 12, 7, 1)
                                                                                       236: P_{3177} = (8, 5, 11, 1)
129: P_{1331} = (2, 2, 4, 1)
                                           183: P_{2275} = (2, 13, 7, 1)
                                                                                       237: P_{3187} = (2, 6, 11, 1)
130: P_{1353} = (8, 3, 4, 1)
                                           184: P_{2320} = (15, 15, 7, 1)
                                                                                       238: P_{3210} = (9, 7, 11, 1)
131: P_{1367} = (6, 4, 4, 1)
                                           185: P_{2322} = (1,0,8,1)
                                                                                       239: P_{3230} = (13, 8, 11, 1)
132: P_{1380} = (3, 5, 4, 1)
                                           186: P_{2331} = (10, 0, 8, 1)
                                                                                       240: P_{3247} = (14, 9, 11, 1)
133 : P_{1423} = (14, 7, 4, 1)
                                           187: P_{2332} = (11, 0, 8, 1)
                                                                                       241: P_{3287} = (6, 12, 11, 1)
134: P_{1445} = (4, 9, 4, 1)
                                           188: P_{2339} = (2, 1, 8, 1)
                                                                                       242: P_{3304} = (7, 13, 11, 1)
                                           189 : P_{2359} = (6, 2, 8, 1)
                                                                                       243: P_{3328} = (15, 14, 11, 1)
135: P_{1466} = (9, 10, 4, 1)
                                           190: P_{2410} = (9, 5, 8, 1)
136: P_{1478} = (5, 11, 4, 1)
                                                                                       244: P_{3332} = (3, 15, 11, 1)
137: P_{1496} = (7, 12, 4, 1)
                                           191: P_{2424} = (7, 6, 8, 1)
                                                                                       245: P_{3346} = (1, 0, 12, 1)
138: P_{1520} = (15, 13, 4, 1)
                                           192: P_{2453} = (4, 8, 8, 1)
                                                                                       246: P_{3355} = (10, 0, 12, 1)
139: P_{1550} = (13, 15, 4, 1)
                                           193: P_{2470} = (5, 9, 8, 1)
                                                                                       247: P_{3356} = (11, 0, 12, 1)
140: P_{1554} = (1, 0, 5, 1)
                                           194: P_{2496} = (15, 10, 8, 1)
                                                                                       248: P_{3369} = (8, 1, 12, 1)
                                           195: P_{2510} = (13, 11, 8, 1)
141: P_{1563} = (10, 0, 5, 1)
                                                                                       249: P_{3396} = (3, 3, 12, 1)
142: P_{1564} = (11, 0, 5, 1)
                                           196: P_{2525} = (12, 12, 8, 1)
                                                                                       250: P_{3416} = (7, 4, 12, 1)
143: P_{1583} = (14, 1, 5, 1)
                                           197: P_{2537} = (8, 13, 8, 1)
                                                                                       251: P_{3438} = (13, 5, 12, 1)
```

```
252: P_{3450} = (9, 6, 12, 1)
                                           270: P_{3765} = (4, 10, 13, 1)
                                                                                      288: P_{4088} = (7, 14, 14, 1)
253: P_{3461} = (4,7,12,1)
                                           271: P_{3784} = (7, 11, 13, 1)
                                                                                      289: P_{4105} = (8, 15, 14, 1)
254: P_{3485} = (12, 8, 12, 1)
                                           272: P_{3814} = (5, 13, 13, 1)
                                                                                      290: P_{4114} = (1, 0, 15, 1)
255: P_{3491} = (2, 9, 12, 1)
                                           273: P_{3831} = (6, 14, 13, 1)
                                                                                      291: P_{4123} = (10, 0, 15, 1)
256: P_{3519} = (14, 10, 12, 1)
                                           274: P_{3853} = (12, 15, 13, 1)
                                                                                      292: P_{4124} = (11, 0, 15, 1)
                                                                                      293: P_{4133} = (4, 1, 15, 1)
257: P_{3527} = (6, 11, 12, 1)
                                           275: P_{3858} = (1, 0, 14, 1)
                                                                                      294: P_{4150} = (5, 2, 15, 1)
258: P_{3552} = (15, 12, 12, 1)
                                           276: P_{3867} = (10, 0, 14, 1)
                                           277: P_{3868} = (11, 0, 14, 1)
                                                                                      295: P_{4163} = (2, 3, 15, 1)
259: P_{3574} = (5, 14, 12, 1)
260: P_{3602} = (1, 0, 13, 1)
                                           278: P_{3886} = (13, 1, 14, 1)
                                                                                      296: P_{4190} = (13, 4, 15, 1)
261: P_{3611} = (10, 0, 13, 1)
                                           279: P_{3903} = (14, 2, 14, 1)
                                                                                      297: P_{4215} = (6, 6, 15, 1)
262: P_{3612} = (11, 0, 13, 1)
                                           280: P_{3949} = (12, 5, 14, 1)
                                                                                      298: P_{4240} = (15, 7, 15, 1)
263: P_{3620} = (3, 1, 13, 1)
                                           281: P_{3957} = (4, 6, 14, 1)
                                                                                      299: P_{4255} = (14, 8, 15, 1)
264: P_{3642} = (9, 2, 13, 1)
                                           282: P_{3988} = (3, 8, 14, 1)
                                                                                      300: P_{4280} = (7, 10, 15, 1)
265: P_{3662} = (13, 3, 13, 1)
                                           283: P_{4010} = (9, 9, 14, 1)
                                                                                      301: P_{4292} = (3, 11, 15, 1)
266: P_{3680} = (15, 4, 13, 1)
                                           284: P_{4019} = (2, 10, 14, 1)
                                                                                      302: P_{4333} = (12, 13, 15, 1)
267: P_{3711} = (14, 6, 13, 1)
                                           285: P_{4048} = (15, 11, 14, 1)
                                                                                      303: P_{4345} = (8, 14, 15, 1)
268: P_{3715} = (2, 7, 13, 1)
                                           286: P_{4054} = (5, 12, 14, 1)
                                                                                      304: P_{4362} = (9, 15, 15, 1)
269: P_{3737} = (8, 8, 13, 1)
                                           287: P_{4071} = (6, 13, 14, 1)
```