Rank-65554 over GF(16)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0 X_1 X_2 = 0$$

(1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over $\mathrm{GF}(16)$ is 286335526

General information

Number of lines	3
Number of points	273
Number of singular points	3
Number of Eckardt points	0
Number of double points	3
Number of single points	45
Number of points off lines	225
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17^{3}
Type of lines on points	$2^3, 1^{45}, 0^{225}$

Singular Points

The surface has 3 singular points:

$$\begin{array}{ll} 0: \ P_{36} = \mathbf{P}(1,1,1,0) = \mathbf{P}(1,1,1,0) \\ 1: \ P_{190} = \mathbf{P}(\delta^5,\delta^{10},1,0) = \mathbf{P}(11,10,1,0) \end{array} \qquad \qquad 2: \ P_{205} = \mathbf{P}(\delta^{10},\delta^5,1,0) = \mathbf{P}(10,11,1,0)$$

The 3 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{274} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{274} = \mathbf{Pl}(1, 0, 1, 0, 0, 1)_{4657}$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 1 & \delta^{5} & 0 \end{bmatrix}_{2741} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{2741} = \mathbf{Pl}(11, 0, 10, 0, 0, 1)_{4946}$$

$$\ell_2 = \begin{bmatrix} 1 & 0 & \delta^{5} & 0 \\ 0 & 1 & \delta^{10} & 0 \end{bmatrix}_{3013} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 10 & 0 \end{bmatrix}_{3013} = \mathbf{Pl}(10, 0, 11, 0, 0, 1)_{4976}$$

Rank of lines: (274, 2741, 3013)

Rank of points on Klein quadric: (4657, 4946, 4976)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 3 Double points: The double points on the surface are:

$$P_{205} = (10, 11, 1, 0) = \ell_0 \cap \ell_1$$

$$P_{190} = (11, 10, 1, 0) = \ell_0 \cap \ell_2$$

 $P_{36} = (1, 1, 1, 0) = \ell_1 \cap \ell_2$

Single Points

The surface has 45 single points: The single points on the surface are:

 $0: P_5 = (1, 1, 0, 0)$ lies on line ℓ_0 1: $P_{14} = (10, 1, 0, 0)$ lies on line ℓ_1 2: $P_{15} = (11, 1, 0, 0)$ lies on line ℓ_2 $3: P_{20} = (1,0,1,0)$ lies on line ℓ_0 4: $P_{29} = (10, 0, 1, 0)$ lies on line ℓ_2 5: $P_{30} = (11, 0, 1, 0)$ lies on line ℓ_1 6: $P_{35} = (0, 1, 1, 0)$ lies on line ℓ_0 7: $P_{54} = (3, 2, 1, 0)$ lies on line ℓ_0 8: $P_{56} = (5, 2, 1, 0)$ lies on line ℓ_2 9: $P_{57} = (6, 2, 1, 0)$ lies on line ℓ_1 10: $P_{69} = (2, 3, 1, 0)$ lies on line ℓ_0 11: $P_{79} = (12, 3, 1, 0)$ lies on line ℓ_1 12: $P_{81} = (14, 3, 1, 0)$ lies on line ℓ_2 13: $P_{88} = (5, 4, 1, 0)$ lies on line ℓ_0 14 : $P_{91} = (8, 4, 1, 0)$ lies on line ℓ_1 15: $P_{96} = (13, 4, 1, 0)$ lies on line ℓ_2 16: $P_{101} = (2, 5, 1, 0)$ lies on line ℓ_1 17: $P_{103} = (4, 5, 1, 0)$ lies on line ℓ_0 18: $P_{105} = (6, 5, 1, 0)$ lies on line ℓ_2 19: $P_{117} = (2, 6, 1, 0)$ lies on line ℓ_2 20: $P_{120} = (5, 6, 1, 0)$ lies on line ℓ_1 21: $P_{122} = (7, 6, 1, 0)$ lies on line ℓ_0 22: $P_{137} = (6,7,1,0)$ lies on line ℓ_0

23: $P_{140} = (9,7,1,0)$ lies on line ℓ_2 24: $P_{146} = (15, 7, 1, 0)$ lies on line ℓ_1 25: $P_{151} = (4, 8, 1, 0)$ lies on line ℓ_2 26: $P_{156} = (9, 8, 1, 0)$ lies on line ℓ_0 27: $P_{160} = (13, 8, 1, 0)$ lies on line ℓ_1 28: $P_{170} = (7, 9, 1, 0)$ lies on line ℓ_1 29: $P_{171} = (8, 9, 1, 0)$ lies on line ℓ_0 $30: P_{178} = (15, 9, 1, 0)$ lies on line ℓ_2 31 : $P_{179} = (0, 10, 1, 0)$ lies on line ℓ_1 $32: P_{195} = (0, 11, 1, 0)$ lies on line ℓ_2 33: $P_{214} = (3, 12, 1, 0)$ lies on line ℓ_2 $34: P_{224} = (13, 12, 1, 0)$ lies on line ℓ_0 $35: P_{225} = (14, 12, 1, 0)$ lies on line ℓ_1 $36: P_{231} = (4, 13, 1, 0)$ lies on line ℓ_1 $37: P_{235} = (8, 13, 1, 0)$ lies on line ℓ_2 $38: P_{239} = (12, 13, 1, 0)$ lies on line ℓ_0 $39: P_{246} = (3, 14, 1, 0)$ lies on line ℓ_1 $40: P_{255} = (12, 14, 1, 0)$ lies on line ℓ_2 41: $P_{258} = (15, 14, 1, 0)$ lies on line ℓ_0 $42: P_{266} = (7, 15, 1, 0)$ lies on line ℓ_2 43: $P_{268} = (9, 15, 1, 0)$ lies on line ℓ_1 $44: P_{273} = (14, 15, 1, 0)$ lies on line ℓ_0

The single points on the surface are:

Points on surface but on no line

The surface has 225 points not on any line: The points on the surface but not on lines are:

```
0: P_{275} = (1,0,0,1)
                                                                  48: P_{1276} = (11, 14, 3, 1)
1: P_{284} = (10, 0, 0, 1)
                                                                  49: P_{1327} = (14, 1, 4, 1)
2: P_{285} = (11, 0, 0, 1)
                                                                  50: P_{1353} = (8, 3, 4, 1)
3: P_{290} = (0, 1, 0, 1)
                                                                  51: P_{1367} = (6, 4, 4, 1)
4: P_{434} = (0, 10, 0, 1)
                                                                  52: P_{1397} = (4, 6, 4, 1)
5: P_{450} = (0, 11, 0, 1)
                                                                  53: P_{1403} = (10, 6, 4, 1)
6: P_{530} = (0, 0, 1, 1)
                                                                  54: P_{1407} = (14, 6, 4, 1)
7: P_{570} = (9, 2, 1, 1)
                                                                  55: P_{1423} = (14, 7, 4, 1)
8: P_{583} = (6, 3, 1, 1)
                                                                  56: P_{1428} = (3, 8, 4, 1)
9: P_{607} = (14, 4, 1, 1)
                                                                  57: P_{1433} = (8, 8, 4, 1)
10: P_{622} = (13, 5, 1, 1)
                                                                  58: P_{1436} = (11, 8, 4, 1)
11: P_{628} = (3, 6, 1, 1)
                                                                  59: P_{1463} = (6, 10, 4, 1)
12: P_{649} = (8, 7, 1, 1)
                                                                  60: P_{1481} = (8, 11, 4, 1)
13: P_{664} = (7, 8, 1, 1)
                                                                  61: P_{1522} = (1, 14, 4, 1)
                                                                  62: P_{1527} = (6, 14, 4, 1)
14: P_{675} = (2, 9, 1, 1)
15: P_{736} = (15, 12, 1, 1)
                                                                  63: P_{1528} = (7, 14, 4, 1)
16: P_{742} = (5, 13, 1, 1)
                                                                  64: P_{1582} = (13, 1, 5, 1)
17: P_{757} = (4, 14, 1, 1)
                                                                  65: P_{1590} = (5, 2, 5, 1)
18: P_{781} = (12, 15, 1, 1)
                                                                  66: P_{1595} = (10, 2, 5, 1)
19: P_{810} = (9, 1, 2, 1)
                                                                  67: P_{1600} = (15, 2, 5, 1)
20: P_{829} = (12, 2, 2, 1)
                                                                  68: P_{1635} = (2, 5, 5, 1)
21: P_{870} = (5, 5, 2, 1)
                                                                  69: P_{1712} = (15, 9, 5, 1)
22: P_{875} = (10, 5, 2, 1)
                                                                  70: P_{1715} = (2, 10, 5, 1)
23: P_{880} = (15, 5, 2, 1)
                                                                  71: P_{1744} = (15, 11, 5, 1)
                                                                  72: P_{1758} = (13, 12, 5, 1)
24: P_{930} = (1, 9, 2, 1)
25: P_{941} = (12, 9, 2, 1)
                                                                  73: P_{1762} = (1, 13, 5, 1)
26: P_{942} = (13, 9, 2, 1)
                                                                  74: P_{1773} = (12, 13, 5, 1)
27: P_{950} = (5, 10, 2, 1)
                                                                  75: P_{1774} = (13, 13, 5, 1)
28: P_{973} = (12, 11, 2, 1)
                                                                  76: P_{1795} = (2, 15, 5, 1)
                                                                  77: P_{1802} = (9, 15, 5, 1)
29: P_{979} = (2, 12, 2, 1)
30: P_{986} = (9, 12, 2, 1)
                                                                  78: P_{1804} = (11, 15, 5, 1)
31: P_{988} = (11, 12, 2, 1)
                                                                  79: P_{1828} = (3, 1, 6, 1)
32: P_{1002} = (9, 13, 2, 1)
                                                                  80: P_{1858} = (1, 3, 6, 1)
33: P_{1030} = (5, 15, 2, 1)
                                                                  81: P_{1863} = (6, 3, 6, 1)
34: P_{1063} = (6, 1, 3, 1)
                                                                  82: P_{1864} = (7, 3, 6, 1)
                                                                  83: P_{1877} = (4, 4, 6, 1)
35: P_{1103} = (14, 3, 3, 1)
36: P_{1113} = (8,4,3,1)
                                                                  84: P_{1883} = (10, 4, 6, 1)
37: P_{1138} = (1, 6, 3, 1)
                                                                  85: P_{1887} = (14, 4, 6, 1)
38: P_{1143} = (6,6,3,1)
                                                                  86: P_{1908} = (3, 6, 6, 1)
39: P_{1144} = (7,6,3,1)
                                                                  87: P_{1924} = (3,7,6,1)
40: P_{1159} = (6,7,3,1)
                                                                  88: P_{1929} = (8,7,6,1)
41: P_{1173} = (4, 8, 3, 1)
                                                                  89: P_{1932} = (11, 7, 6, 1)
42: P_{1179} = (10, 8, 3, 1)
                                                                  90: P_{1944} = (7, 8, 6, 1)
43: P_{1183} = (14, 8, 3, 1)
                                                                  91: P_{1973} = (4, 10, 6, 1)
44: P_{1209} = (8, 10, 3, 1)
                                                                  92: P_{1992} = (7, 11, 6, 1)
45: P_{1231} = (14, 11, 3, 1)
                                                                  93: P_{2037} = (4, 14, 6, 1)
46: P_{1268} = (3, 14, 3, 1)
                                                                  94: P_{2089} = (8, 1, 7, 1)
47: P_{1273} = (8, 14, 3, 1)
                                                                  95: P_{2119} = (6, 3, 7, 1)
```

```
150: P_{3064} = (7, 14, 10, 1)
96: P_{2143} = (14, 4, 7, 1)
97: P_{2164} = (3,6,7,1)
                                                                 151: P_{3082} = (9, 15, 10, 1)
                                                                 152: P_{3089} = (0, 0, 11, 1)
98: P_{2169} = (8, 6, 7, 1)
99: P_{2172} = (11, 6, 7, 1)
                                                                 153: P_{3133} = (12, 2, 11, 1)
100: P_{2185} = (8,7,7,1)
                                                                 154: P_{3151} = (14, 3, 11, 1)
101: P_{2194} = (1, 8, 7, 1)
                                                                 155: P_{3161} = (8, 4, 11, 1)
102: P_{2199} = (6, 8, 7, 1)
                                                                 156: P_{3184} = (15, 5, 11, 1)
103: P_{2200} = (7, 8, 7, 1)
                                                                 157: P_{3192} = (7, 6, 11, 1)
104: P_{2239} = (14, 10, 7, 1)
                                                                 158: P_{3207} = (6, 7, 11, 1)
105: P_{2247} = (6, 11, 7, 1)
                                                                 159: P_{3221} = (4, 8, 11, 1)
106: P_{2293} = (4, 14, 7, 1)
                                                                 160: P_{3246} = (13, 9, 11, 1)
107: P_{2299} = (10, 14, 7, 1)
                                                                 161: P_{3283} = (2, 12, 11, 1)
108: P_{2303} = (14, 14, 7, 1)
                                                                 162: P_{3306} = (9, 13, 11, 1)
109: P_{2344} = (7, 1, 8, 1)
                                                                 163: P_{3316} = (3, 14, 11, 1)
                                                                 164: P_{3334} = (5, 15, 11, 1)
110: P_{2373} = (4,3,8,1)
111: P_{2379} = (10, 3, 8, 1)
                                                                 165: P_{3376} = (15, 1, 12, 1)
                                                                 166: P_{3379} = (2, 2, 12, 1)
112: P_{2383} = (14, 3, 8, 1)
                                                                 167: P_{3386} = (9, 2, 12, 1)
113: P_{2388} = (3, 4, 8, 1)
                                                                 168: P_{3388} = (11, 2, 12, 1)
114: P_{2393} = (8, 4, 8, 1)
115: P_{2396} = (11, 4, 8, 1)
                                                                 169: P_{3438} = (13, 5, 12, 1)
116: P_{2424} = (7, 6, 8, 1)
                                                                 170: P_{3491} = (2, 9, 12, 1)
117: P_{2434} = (1, 7, 8, 1)
                                                                 171: P_{3518} = (13, 10, 12, 1)
118: P_{2439} = (6, 7, 8, 1)
                                                                 172: P_{3523} = (2, 11, 12, 1)
119: P_{2440} = (7,7,8,1)
                                                                 173: P_{3552} = (15, 12, 12, 1)
120: P_{2453} = (4, 8, 8, 1)
                                                                 174: P_{3558} = (5, 13, 12, 1)
121: P_{2484} = (3, 10, 8, 1)
                                                                 175: P_{3563} = (10, 13, 12, 1)
122: P_{2501} = (4, 11, 8, 1)
                                                                 176: P_{3568} = (15, 13, 12, 1)
123: P_{2548} = (3, 14, 8, 1)
                                                                 177: P_{3586} = (1, 15, 12, 1)
124: P_{2595} = (2, 1, 9, 1)
                                                                 178: P_{3597} = (12, 15, 12, 1)
125: P_{2610} = (1, 2, 9, 1)
                                                                 179: P_{3598} = (13, 15, 12, 1)
126: P_{2621} = (12, 2, 9, 1)
                                                                 180: P_{3622} = (5, 1, 13, 1)
127: P_{2622} = (13, 2, 9, 1)
                                                                 181: P_{3642} = (9, 2, 13, 1)
128: P_{2672} = (15, 5, 9, 1)
                                                                 182: P_{3682} = (1, 5, 13, 1)
129: P_{2734} = (13, 9, 9, 1)
                                                                 183: P_{3693} = (12, 5, 13, 1)
                                                                 184: P_{3694} = (13, 5, 13, 1)
130: P_{2752} = (15, 10, 9, 1)
                                                                 185: P_{3747} = (2, 9, 13, 1)
131: P_{2766} = (13, 11, 9, 1)
132: P_{2771} = (2, 12, 9, 1)
                                                                 186: P_{3754} = (9, 9, 13, 1)
133: P_{2787} = (2, 13, 9, 1)
                                                                 187: P_{3756} = (11, 9, 13, 1)
134: P_{2794} = (9, 13, 9, 1)
                                                                 188: P_{3773} = (12, 10, 13, 1)
135: P_{2796} = (11, 13, 9, 1)
                                                                 189: P_{3786} = (9, 11, 13, 1)
136: P_{2822} = (5, 15, 9, 1)
                                                                 190: P_{3798} = (5, 12, 13, 1)
137: P_{2827} = (10, 15, 9, 1)
                                                                 191: P_{3803} = (10, 12, 13, 1)
138: P_{2832} = (15, 15, 9, 1)
                                                                 192: P_{3808} = (15, 12, 13, 1)
139: P_{2833} = (0, 0, 10, 1)
                                                                 193: P_{3814} = (5, 13, 13, 1)
140: P_{2870} = (5, 2, 10, 1)
                                                                 194: P_{3853} = (12, 15, 13, 1)
141: P_{2889} = (8, 3, 10, 1)
                                                                 195: P_{3877} = (4, 1, 14, 1)
142: P_{2903} = (6, 4, 10, 1)
                                                                 196: P_{3908} = (3, 3, 14, 1)
143: P_{2915} = (2, 5, 10, 1)
                                                                 197: P_{3913} = (8, 3, 14, 1)
144: P_{2933} = (4, 6, 10, 1)
                                                                 198: P_{3916} = (11, 3, 14, 1)
145: P_{2959} = (14, 7, 10, 1)
                                                                 199: P_{3922} = (1, 4, 14, 1)
146: P_{2964} = (3, 8, 10, 1)
                                                                 200: P_{3927} = (6, 4, 14, 1)
147: P_{2992} = (15, 9, 10, 1)
                                                                 201: P_{3928} = (7, 4, 14, 1)
148: P_{3038} = (13, 12, 10, 1)
                                                                 202: P_{3957} = (4, 6, 14, 1)
149: P_{3053} = (12, 13, 10, 1)
                                                                 203: P_{3973} = (4,7,14,1)
```

```
204: P_{3979} = (10, 7, 14, 1)
                                                                215: P_{4262} = (5, 9, 15, 1)
205: P_{3983} = (14, 7, 14, 1)
                                                                216: P_{4267} = (10, 9, 15, 1)
                                                                217: P_{4272} = (15, 9, 15, 1)
206: P_{3988} = (3, 8, 14, 1)
                                                                218: P_{4282} = (9, 10, 15, 1)
207: P_{4024} = (7, 10, 14, 1)
208: P_{4036} = (3, 11, 14, 1)
                                                                219: P_{4294} = (5, 11, 15, 1)
209: P_{4088} = (7, 14, 14, 1)
                                                                220: P_{4306} = (1, 12, 15, 1)
                                                                221: P_{4317} = (12, 12, 15, 1)
210: P_{4141} = (12, 1, 15, 1)
211: P_{4150} = (5, 2, 15, 1)
                                                                222: P_{4318} = (13, 12, 15, 1)
212: P_{4195} = (2, 5, 15, 1)
                                                                223: P_{4333} = (12, 13, 15, 1)
213: P_{4202} = (9, 5, 15, 1)
                                                                224: P_{4362} = (9, 15, 15, 1)
214: P_{4204} = (11, 5, 15, 1)
```

Line Intersection Graph

 $\begin{array}{c|c} 0 & 1 & 2 \\ \hline 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 2 & 1 & 1 & 0 \end{array}$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2
in point	P_{205}	P_{190}

Line 1 intersects

Line	ℓ_0	ℓ_2
in point	P_{205}	P_{36}

Line 2 intersects

Line	ℓ_0	ℓ_1
in point	P_{190}	P_{36}

The surface has 273 points:

The points on the surface are:

$0: P_5 = (1, 1, 0, 0)$	$21: P_{120} = (5, 6, 1, 0)$	$42: P_{246} = (3, 14, 1, 0)$
$1: P_{14} = (10, 1, 0, 0)$	$22: P_{122} = (7, 6, 1, 0)$	$43: P_{255} = (12, 14, 1, 0)$
$2: P_{15} = (11, 1, 0, 0)$	$23: P_{137} = (6,7,1,0)$	$44: P_{258} = (15, 14, 1, 0)$
$3: P_{20} = (1,0,1,0)$	$24: P_{140} = (9,7,1,0)$	$45: P_{266} = (7, 15, 1, 0)$
$4: P_{29} = (10, 0, 1, 0)$	$25: P_{146} = (15, 7, 1, 0)$	$46: P_{268} = (9, 15, 1, 0)$
$5: P_{30} = (11, 0, 1, 0)$	$26: P_{151} = (4, 8, 1, 0)$	$47: P_{273} = (14, 15, 1, 0)$
$6: P_{35} = (0, 1, 1, 0)$	$27: P_{156} = (9, 8, 1, 0)$	$48: P_{275} = (1, 0, 0, 1)$
$7: P_{36} = (1, 1, 1, 0)$	$28: P_{160} = (13, 8, 1, 0)$	$49: P_{284} = (10, 0, 0, 1)$
$8: P_{54} = (3, 2, 1, 0)$	$29: P_{170} = (7, 9, 1, 0)$	$50: P_{285} = (11, 0, 0, 1)$
$9: P_{56} = (5, 2, 1, 0)$	$30: P_{171} = (8, 9, 1, 0)$	$51: P_{290} = (0, 1, 0, 1)$
$10: P_{57} = (6, 2, 1, 0)$	$31: P_{178} = (15, 9, 1, 0)$	$52: P_{434} = (0, 10, 0, 1)$
$11: P_{69} = (2, 3, 1, 0)$	$32: P_{179} = (0, 10, 1, 0)$	$53: P_{450} = (0, 11, 0, 1)$
$12: P_{79} = (12, 3, 1, 0)$	$33: P_{190} = (11, 10, 1, 0)$	$54: P_{530} = (0, 0, 1, 1)$
$13: P_{81} = (14, 3, 1, 0)$	$34: P_{195} = (0, 11, 1, 0)$	$55: P_{570} = (9, 2, 1, 1)$
$14: P_{88} = (5, 4, 1, 0)$	$35: P_{205} = (10, 11, 1, 0)$	$56: P_{583} = (6, 3, 1, 1)$
$15: P_{91} = (8, 4, 1, 0)$	$36: P_{214} = (3, 12, 1, 0)$	$57: P_{607} = (14, 4, 1, 1)$
$16: P_{96} = (13, 4, 1, 0)$	$37: P_{224} = (13, 12, 1, 0)$	$58: P_{622} = (13, 5, 1, 1)$
$17: P_{101} = (2, 5, 1, 0)$	$38: P_{225} = (14, 12, 1, 0)$	$59: P_{628} = (3, 6, 1, 1)$
$18: P_{103} = (4, 5, 1, 0)$	$39: P_{231} = (4, 13, 1, 0)$	$60: P_{649} = (8,7,1,1)$
$19: P_{105} = (6, 5, 1, 0)$	$40: P_{235} = (8, 13, 1, 0)$	$61: P_{664} = (7, 8, 1, 1)$
$20: P_{117} = (2, 6, 1, 0)$	$41: P_{239} = (12, 13, 1, 0)$	$62: P_{675} = (2, 9, 1, 1)$

```
63: P_{736} = (15, 12, 1, 1)
                                           117: P_{1712} = (15, 9, 5, 1)
                                                                                       171: P_{2548} = (3, 14, 8, 1)
64: P_{742} = (5, 13, 1, 1)
                                           118: P_{1715} = (2, 10, 5, 1)
                                                                                       172: P_{2595} = (2, 1, 9, 1)
65: P_{757} = (4, 14, 1, 1)
                                           119: P_{1744} = (15, 11, 5, 1)
                                                                                       173: P_{2610} = (1, 2, 9, 1)
66: P_{781} = (12, 15, 1, 1)
                                                                                       174: P_{2621} = (12, 2, 9, 1)
                                           120: P_{1758} = (13, 12, 5, 1)
67: P_{810} = (9, 1, 2, 1)
                                           121: P_{1762} = (1, 13, 5, 1)
                                                                                       175: P_{2622} = (13, 2, 9, 1)
68: P_{829} = (12, 2, 2, 1)
                                           122: P_{1773} = (12, 13, 5, 1)
                                                                                       176: P_{2672} = (15, 5, 9, 1)
69: P_{870} = (5, 5, 2, 1)
                                           123: P_{1774} = (13, 13, 5, 1)
                                                                                       177: P_{2734} = (13, 9, 9, 1)
                                                                                       178: P_{2752} = (15, 10, 9, 1)
70: P_{875} = (10, 5, 2, 1)
                                           124: P_{1795} = (2, 15, 5, 1)
71: P_{880} = (15, 5, 2, 1)
                                           125: P_{1802} = (9, 15, 5, 1)
                                                                                       179: P_{2766} = (13, 11, 9, 1)
72: P_{930} = (1, 9, 2, 1)
                                           126: P_{1804} = (11, 15, 5, 1)
                                                                                       180: P_{2771} = (2, 12, 9, 1)
73: P_{941} = (12, 9, 2, 1)
                                           127: P_{1828} = (3, 1, 6, 1)
                                                                                       181: P_{2787} = (2, 13, 9, 1)
74: P_{942} = (13, 9, 2, 1)
                                           128: P_{1858} = (1, 3, 6, 1)
                                                                                       182: P_{2794} = (9, 13, 9, 1)
75: P_{950} = (5, 10, 2, 1)
                                           129: P_{1863} = (6, 3, 6, 1)
                                                                                       183: P_{2796} = (11, 13, 9, 1)
                                           130: P_{1864} = (7, 3, 6, 1)
                                                                                       184: P_{2822} = (5, 15, 9, 1)
76: P_{973} = (12, 11, 2, 1)
                                                                                       185: P_{2827} = (10, 15, 9, 1)
77: P_{979} = (2, 12, 2, 1)
                                           131: P_{1877} = (4, 4, 6, 1)
78: P_{986} = (9, 12, 2, 1)
                                           132: P_{1883} = (10, 4, 6, 1)
                                                                                       186: P_{2832} = (15, 15, 9, 1)
                                           133 : P_{1887} = (14, 4, 6, 1)
79: P_{988} = (11, 12, 2, 1)
                                                                                       187: P_{2833} = (0, 0, 10, 1)
80: P_{1002} = (9, 13, 2, 1)
                                           134: P_{1908} = (3, 6, 6, 1)
                                                                                       188: P_{2870} = (5, 2, 10, 1)
                                                                                       189: P_{2889} = (8, 3, 10, 1)
81: P_{1030} = (5, 15, 2, 1)
                                           135: P_{1924} = (3,7,6,1)
82: P_{1063} = (6, 1, 3, 1)
                                           136: P_{1929} = (8,7,6,1)
                                                                                       190: P_{2903} = (6, 4, 10, 1)
83: P_{1103} = (14, 3, 3, 1)
                                           137: P_{1932} = (11, 7, 6, 1)
                                                                                       191: P_{2915} = (2, 5, 10, 1)
                                                                                       192: P_{2933} = (4, 6, 10, 1)
84: P_{1113} = (8,4,3,1)
                                           138: P_{1944} = (7, 8, 6, 1)
85: P_{1138} = (1, 6, 3, 1)
                                           139: P_{1973} = (4, 10, 6, 1)
                                                                                       193: P_{2959} = (14, 7, 10, 1)
86: P_{1143} = (6, 6, 3, 1)
                                           140: P_{1992} = (7, 11, 6, 1)
                                                                                       194: P_{2964} = (3, 8, 10, 1)
87: P_{1144} = (7,6,3,1)
                                           141: P_{2037} = (4, 14, 6, 1)
                                                                                       195: P_{2992} = (15, 9, 10, 1)
88: P_{1159} = (6,7,3,1)
                                           142: P_{2089} = (8, 1, 7, 1)
                                                                                       196: P_{3038} = (13, 12, 10, 1)
89: P_{1173} = (4, 8, 3, 1)
                                           143: P_{2119} = (6, 3, 7, 1)
                                                                                       197: P_{3053} = (12, 13, 10, 1)
90: P_{1179} = (10, 8, 3, 1)
                                           144: P_{2143} = (14, 4, 7, 1)
                                                                                       198: P_{3064} = (7, 14, 10, 1)
                                                                                       199: P_{3082} = (9, 15, 10, 1)
91: P_{1183} = (14, 8, 3, 1)
                                           145: P_{2164} = (3, 6, 7, 1)
                                           146: P_{2169} = (8, 6, 7, 1)
92: P_{1209} = (8, 10, 3, 1)
                                                                                       200: P_{3089} = (0, 0, 11, 1)
93: P_{1231} = (14, 11, 3, 1)
                                           147: P_{2172} = (11, 6, 7, 1)
                                                                                       201: P_{3133} = (12, 2, 11, 1)
94: P_{1268} = (3, 14, 3, 1)
                                           148: P_{2185} = (8,7,7,1)
                                                                                       202: P_{3151} = (14, 3, 11, 1)
95: P_{1273} = (8, 14, 3, 1)
                                           149: P_{2194} = (1, 8, 7, 1)
                                                                                       203: P_{3161} = (8, 4, 11, 1)
                                           150: P_{2199} = (6, 8, 7, 1)
                                                                                       204: P_{3184} = (15, 5, 11, 1)
96: P_{1276} = (11, 14, 3, 1)
                                           151: P_{2200} = (7, 8, 7, 1)
97: P_{1327} = (14, 1, 4, 1)
                                                                                       205: P_{3192} = (7, 6, 11, 1)
                                           152: P_{2239} = (14, 10, 7, 1)
98: P_{1353} = (8, 3, 4, 1)
                                                                                       206: P_{3207} = (6,7,11,1)
99: P_{1367} = (6, 4, 4, 1)
                                           153: P_{2247} = (6, 11, 7, 1)
                                                                                       207: P_{3221} = (4, 8, 11, 1)
100: P_{1397} = (4, 6, 4, 1)
                                                                                       208: P_{3246} = (13, 9, 11, 1)
                                           154: P_{2293} = (4, 14, 7, 1)
101: P_{1403} = (10, 6, 4, 1)
                                           155: P_{2299} = (10, 14, 7, 1)
                                                                                       209: P_{3283} = (2, 12, 11, 1)
102: P_{1407} = (14, 6, 4, 1)
                                           156: P_{2303} = (14, 14, 7, 1)
                                                                                       210: P_{3306} = (9, 13, 11, 1)
103: P_{1423} = (14, 7, 4, 1)
                                           157: P_{2344} = (7, 1, 8, 1)
                                                                                       211: P_{3316} = (3, 14, 11, 1)
104: P_{1428} = (3, 8, 4, 1)
                                           158: P_{2373} = (4, 3, 8, 1)
                                                                                       212: P_{3334} = (5, 15, 11, 1)
105: P_{1433} = (8, 8, 4, 1)
                                           159: P_{2379} = (10, 3, 8, 1)
                                                                                       213: P_{3376} = (15, 1, 12, 1)
106: P_{1436} = (11, 8, 4, 1)
                                           160: P_{2383} = (14, 3, 8, 1)
                                                                                       214: P_{3379} = (2, 2, 12, 1)
107: P_{1463} = (6, 10, 4, 1)
                                           161: P_{2388} = (3,4,8,1)
                                                                                       215: P_{3386} = (9, 2, 12, 1)
                                           162: P_{2393} = (8, 4, 8, 1)
                                                                                       216: P_{3388} = (11, 2, 12, 1)
108: P_{1481} = (8, 11, 4, 1)
109: P_{1522} = (1, 14, 4, 1)
                                           163: P_{2396} = (11, 4, 8, 1)
                                                                                       217: P_{3438} = (13, 5, 12, 1)
110: P_{1527} = (6, 14, 4, 1)
                                           164: P_{2424} = (7, 6, 8, 1)
                                                                                       218: P_{3491} = (2, 9, 12, 1)
                                                                                       219: P_{3518} = (13, 10, 12, 1)
111: P_{1528} = (7, 14, 4, 1)
                                           165: P_{2434} = (1, 7, 8, 1)
112: P_{1582} = (13, 1, 5, 1)
                                           166: P_{2439} = (6, 7, 8, 1)
                                                                                       220: P_{3523} = (2, 11, 12, 1)
113: P_{1590} = (5, 2, 5, 1)
                                           167: P_{2440} = (7, 7, 8, 1)
                                                                                       221: P_{3552} = (15, 12, 12, 1)
114: P_{1595} = (10, 2, 5, 1)
                                           168: P_{2453} = (4, 8, 8, 1)
                                                                                       222: P_{3558} = (5, 13, 12, 1)
115: P_{1600} = (15, 2, 5, 1)
                                           169: P_{2484} = (3, 10, 8, 1)
                                                                                       223: P_{3563} = (10, 13, 12, 1)
116: P_{1635} = (2, 5, 5, 1)
                                           170: P_{2501} = (4, 11, 8, 1)
                                                                                       224: P_{3568} = (15, 13, 12, 1)
```

```
225: P_{3586} = (1, 15, 12, 1)
                                           242: P_{3853} = (12, 15, 13, 1)
                                                                                      259: P_{4150} = (5, 2, 15, 1)
226: P_{3597} = (12, 15, 12, 1)
                                           243: P_{3877} = (4, 1, 14, 1)
                                                                                      260: P_{4195} = (2, 5, 15, 1)
227: P_{3598} = (13, 15, 12, 1)
                                           244: P_{3908} = (3, 3, 14, 1)
                                                                                      261: P_{4202} = (9, 5, 15, 1)
                                                                                      262: P_{4204} = (11, 5, 15, 1)
228: P_{3622} = (5, 1, 13, 1)
                                           245: P_{3913} = (8, 3, 14, 1)
229: P_{3642} = (9, 2, 13, 1)
                                           246: P_{3916} = (11, 3, 14, 1)
                                                                                      263: P_{4262} = (5, 9, 15, 1)
                                                                                      264: P_{4267} = (10, 9, 15, 1)
230: P_{3682} = (1, 5, 13, 1)
                                           247: P_{3922} = (1, 4, 14, 1)
                                                                                      265: P_{4272} = (15, 9, 15, 1)
231: P_{3693} = (12, 5, 13, 1)
                                           248: P_{3927} = (6, 4, 14, 1)
                                           249: P_{3928} = (7, 4, 14, 1)
                                                                                      266: P_{4282} = (9, 10, 15, 1)
232: P_{3694} = (13, 5, 13, 1)
233: P_{3747} = (2, 9, 13, 1)
                                           250: P_{3957} = (4, 6, 14, 1)
                                                                                      267: P_{4294} = (5, 11, 15, 1)
234: P_{3754} = (9, 9, 13, 1)
                                           251: P_{3973} = (4,7,14,1)
                                                                                      268: P_{4306} = (1, 12, 15, 1)
235: P_{3756} = (11, 9, 13, 1)
                                           252: P_{3979} = (10, 7, 14, 1)
                                                                                      269: P_{4317} = (12, 12, 15, 1)
236: P_{3773} = (12, 10, 13, 1)
                                           253: P_{3983} = (14, 7, 14, 1)
                                                                                      270: P_{4318} = (13, 12, 15, 1)
237: P_{3786} = (9, 11, 13, 1)
                                           254: P_{3988} = (3, 8, 14, 1)
                                                                                      271: P_{4333} = (12, 13, 15, 1)
238: P_{3798} = (5, 12, 13, 1)
                                                                                      272: P_{4362} = (9, 15, 15, 1)
                                           255: P_{4024} = (7, 10, 14, 1)
239: P_{3803} = (10, 12, 13, 1)
                                           256: P_{4036} = (3, 11, 14, 1)
240: P_{3808} = (15, 12, 13, 1)
                                           257: P_{4088} = (7, 14, 14, 1)
241: P_{3814} = (5, 13, 13, 1)
                                           258: P_{4141} = (12, 1, 15, 1)
```