Rank-65618 over GF(64)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0^2 X_3 + X_0 X_1 X_2 = 0$$

(1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over $\mathrm{GF}(64)$ is 1091051654

General information

Number of lines	12
Number of points	4353
Number of singular points	3
Number of Eckardt points	0
Number of double points	18
Number of single points	732
Number of points off lines	3600
Number of Hesse planes	0
Number of axes	0
Type of points on lines	65^{12}
Type of lines on points	$4^3, 2^{18}, 1^{732}, 0^{3600}$

Singular Points

The surface has 3 singular points:

$$\begin{array}{ll} 0: \ P_4 = \mathbf{P}(1,1,1,1) = \mathbf{P}(1,1,1,1) \\ 1: \ P_{237186} = \mathbf{P}(1,\epsilon^{21},\epsilon^{42},1) = \mathbf{P}(1,57,56,1) \end{array} \\ \end{array} \\ \begin{array}{ll} 2: \ P_{241218} = \mathbf{P}(1,\epsilon^{42},\epsilon^{21},1) = \mathbf{P}(1,56,57,1) \\ \end{array}$$

The 12 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4162} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4162} = \mathbf{Pl}(1, 0, 1, 0, 0, 1)_{270529}$$

$$\begin{split} \ell_1 &= \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 1 & \epsilon^{21} & 0 \end{bmatrix}_{233073} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 1 & 57 & 0 \end{bmatrix}_{233073} = \mathbf{PI}(57, 0, 56, 0, 0, 1)_{277570} \\ \ell_2 &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 1 & \epsilon^{42} & 0 \end{bmatrix}_{237233} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 1 & 56 & 0 \end{bmatrix}_{237233} = \mathbf{PI}(56, 0, 57, 0, 0, 1)_{277696} \\ \ell_3 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{8258} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{8258} = \mathbf{PI}(0, 0, 1, 1, 1, 1)_{544578} \\ \ell_4 &= \begin{bmatrix} 1 & \epsilon^{21} & 0 & 0 \\ 0 & 0 & 1 & \epsilon^{21} \end{bmatrix}_{241330} = \begin{bmatrix} 1 & 57 & 0 & 0 \\ 0 & 0 & 1 & 57 \end{bmatrix}_{241330} = \mathbf{PI}(0, 0, 56, 57, 1, 1)_{551563} \\ \ell_5 &= \begin{bmatrix} 1 & \epsilon^{42} & 0 & 0 \\ 0 & 0 & 1 & \epsilon^{42} \end{bmatrix}_{237168} = \begin{bmatrix} 1 & 56 & 0 & 0 \\ 0 & 0 & 1 & 56 \end{bmatrix}_{237168} = \mathbf{PI}(0, 0, 57, 56, 1, 1)_{551690} \\ \ell_6 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{4225} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{4225} = \mathbf{PI}(1, 1, 0, 0, 1, 1)_{536577} \\ \ell_7 &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & 0 \\ 0 & 1 & 0 & \epsilon^{21} \end{bmatrix}_{240825} = \begin{bmatrix} 1 & 0 & 57 & 0 \\ 0 & 1 & 0 & 57 \end{bmatrix}_{240825} = \mathbf{PI}(56, 57, 0, 0, 1, 1)_{536632} \\ \ell_8 &= \begin{bmatrix} 1 & 0 & \epsilon^{42} & 0 \\ 0 & 1 & 0 & \epsilon^{42} \end{bmatrix}_{236600} = \begin{bmatrix} 1 & 0 & 56 & 0 \\ 0 & 1 & 0 & 56 \end{bmatrix}_{236600} = \mathbf{PI}(57, 56, 0, 0, 1, 1)_{536633} \\ \ell_9 &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{270466} = \begin{bmatrix} 1 & 0 & 56 & 1 \\ 0 & 1 & 57 & 0 \end{bmatrix}_{499377} = \mathbf{PI}(57, 56, 56, 57, 0, 1)_{512315} \\ \ell_{11} &= \begin{bmatrix} 1 & 0 & \epsilon^{21} & 1 \\ 0 & 1 & \epsilon^{42} & 0 \end{bmatrix}_{503537} = \begin{bmatrix} 1 & 0 & 57 & 1 \\ 0 & 1 & 56 & 0 \end{bmatrix}_{503537} = \mathbf{PI}(56, 57, 57, 56, 0, 1)_{508408} \end{aligned}$$

Rank of lines: (4162, 233073, 237233, 8258, 241330, 237168, 4225, 240825, 236600, 270466, 499377, 503537)

Rank of points on Klein quadric: (270529, 277570, 277696, 544578, 551563, 551690, 536577, 536632, 536633, 286530, 512315, 508408)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 18 Double points: The double points on the surface are:

$$\begin{split} P_{3771} &= (56, 57, 1, 0) = \ell_0 \cap \ell_1 \\ P_{3708} &= (57, 56, 1, 0) = \ell_0 \cap \ell_2 \\ P_5 &= (1, 1, 0, 0) = \ell_0 \cap \ell_3 \\ P_{68} &= (1, 0, 1, 0) = \ell_0 \cap \ell_6 \\ P_{131} &= (0, 1, 1, 0) = \ell_0 \cap \ell_9 \\ P_{132} &= (1, 1, 1, 0) = \ell_1 \cap \ell_2 \\ P_{60} &= (56, 1, 0, 0) = \ell_1 \cap \ell_4 \\ P_{124} &= (57, 0, 1, 0) = \ell_1 \cap \ell_8 \\ P_{3651} &= (0, 56, 1, 0) = \ell_1 \cap \ell_{10} \\ P_{61} &= (57, 1, 0, 0) = \ell_2 \cap \ell_5 \end{split}$$

$$P_{123} = (56, 0, 1, 0) = \ell_2 \cap \ell_7$$

$$P_{3715} = (0, 57, 1, 0) = \ell_2 \cap \ell_{11}$$

$$P_{11897} = (56, 56, 1, 1) = \ell_3 \cap \ell_7$$

$$P_{11962} = (57, 57, 1, 1) = \ell_3 \cap \ell_8$$

$$P_{233657} = (56, 1, 56, 1) = \ell_4 \cap \ell_6$$

$$P_{237178} = (57, 56, 56, 1) = \ell_4 \cap \ell_7$$

$$P_{237754} = (57, 1, 57, 1) = \ell_5 \cap \ell_6$$

$$P_{241337} = (56, 57, 57, 1) = \ell_5 \cap \ell_8$$

Single Points

The surface has 732 single points: The single points on the surface are:

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0: P_{198} = (3, 2, 1, 0) lies on line \ell_0
                                                                      48: P_{1222} = (3, 18, 1, 0) lies on line \ell_1
1: P_{235} = (40, 2, 1, 0) lies on line \ell_1
                                                                      49: P_{1235} = (16, 18, 1, 0) lies on line \ell_2
2: P_{238} = (43, 2, 1, 0) lies on line \ell_2
                                                                      50: P_{1238} = (19, 18, 1, 0) lies on line \ell_0
                                                                      51: P_{1301} = (18, 19, 1, 0) lies on line \ell_0
3: P_{261} = (2,3,1,0) lies on line \ell_0
4: P_{275} = (16, 3, 1, 0) lies on line \ell_1
                                                                      52: P_{1324} = (41, 19, 1, 0) lies on line \ell_2
5: P_{277} = (18, 3, 1, 0) lies on line \ell_2
                                                                      53: P_{1342} = (59, 19, 1, 0) lies on line \ell_1
6: P_{328} = (5, 4, 1, 0) lies on line \ell_0
                                                                      54: P_{1368} = (21, 20, 1, 0) lies on line \ell_0
7: P_{350} = (27, 4, 1, 0) lies on line \ell_1
                                                                      55: P_{1384} = (37, 20, 1, 0) lies on line \ell_2
8: P_{353} = (30, 4, 1, 0) lies on line \ell_2
                                                                      56: P_{1395} = (48, 20, 1, 0) lies on line \ell_1
9: P_{391} = (4, 5, 1, 0) lies on line \ell_0
                                                                      57: P_{1419} = (8, 21, 1, 0) lies on line \ell_1
10: P_{422} = (35, 5, 1, 0) lies on line \ell_1
                                                                      58: P_{1431} = (20, 21, 1, 0) lies on line \ell_0
11: P_{426} = (39, 5, 1, 0) lies on line \ell_2
                                                                      59: P_{1439} = (28, 21, 1, 0) lies on line \ell_2
12: P_{458} = (7, 6, 1, 0) lies on line \ell_0
                                                                      60: P_{1498} = (23, 22, 1, 0) lies on line \ell_0
13: P_{461} = (10, 6, 1, 0) lies on line \ell_1
                                                                      61: P_{1508} = (33, 22, 1, 0) lies on line \ell_1
14: P_{464} = (13, 6, 1, 0) lies on line \ell_2
                                                                      62: P_{1529} = (54, 22, 1, 0) lies on line \ell_2
15: P_{521} = (6, 7, 1, 0) lies on line \ell_0
                                                                      63: P_{1554} = (15, 23, 1, 0) lies on line \ell_2
16 : P_{565} = (50, 7, 1, 0) lies on line \ell_1
                                                                      64: P_{1561} = (22, 23, 1, 0) lies on line \ell_0
17: P_{567} = (52, 7, 1, 0) lies on line \ell_2
                                                                      65: P_{1564} = (25, 23, 1, 0) lies on line \ell_1
18: P_{588} = (9, 8, 1, 0) lies on line \ell_0
                                                                      66: P_{1628} = (25, 24, 1, 0) lies on line \ell_0
19: P_{600} = (21, 8, 1, 0) lies on line \ell_2
                                                                      67: P_{1649} = (46, 24, 1, 0) lies on line \ell_2
20: P_{607} = (28, 8, 1, 0) lies on line \ell_1
                                                                      68: P_{1658} = (55, 24, 1, 0) lies on line \ell_1
21: P_{651} = (8, 9, 1, 0) lies on line \ell_0
                                                                      69: P_{1682} = (15, 25, 1, 0) lies on line \ell_1
22: P_{679} = (36, 9, 1, 0) lies on line \ell_1
                                                                      70: P_{1690} = (23, 25, 1, 0) lies on line \ell_2
23: P_{687} = (44, 9, 1, 0) lies on line \ell_2
                                                                      71: P_{1691} = (24, 25, 1, 0) lies on line \ell_0
24: P_{713} = (6, 10, 1, 0) lies on line \ell_2
                                                                      72: P_{1758} = (27, 26, 1, 0) lies on line \ell_0
25: P_{718} = (11, 10, 1, 0) lies on line \ell_0
                                                                      73: P_{1769} = (38, 26, 1, 0) lies on line \ell_1
26: P_{720} = (13, 10, 1, 0) lies on line \ell_1
                                                                      74: P_{1792} = (61, 26, 1, 0) lies on line \ell_2
27: P_{781} = (10, 11, 1, 0) lies on line \ell_0
                                                                      75: P_{1799} = (4, 27, 1, 0) lies on line \ell_2
                                                                      76: P_{1821} = (26, 27, 1, 0) lies on line \ell_0
28: P_{824} = (53, 11, 1, 0) lies on line \ell_1
29: P_{834} = (63, 11, 1, 0) lies on line \ell_2
                                                                      77: P_{1825} = (30, 27, 1, 0) lies on line \ell_1
30: P_{848} = (13, 12, 1, 0) lies on line \ell_0
                                                                      78: P_{1867} = (8, 28, 1, 0) lies on line \ell_2
                                                                      79: P_{1880} = (21, 28, 1, 0) lies on line \ell_1
31: P_{886} = (51, 12, 1, 0) lies on line \ell_2
32: P_{897} = (62, 12, 1, 0) lies on line \ell_1
                                                                      80: P_{1888} = (29, 28, 1, 0) lies on line \ell_0
33: P_{905} = (6, 13, 1, 0) lies on line \ell_1
                                                                      81: P_{1951} = (28, 29, 1, 0) lies on line \ell_0
34: P_{909} = (10, 13, 1, 0) lies on line \ell_2
                                                                      82: P_{1968} = (45, 29, 1, 0) lies on line \ell_1
35: P_{911} = (12, 13, 1, 0) lies on line \ell_0
                                                                      83: P_{1972} = (49, 29, 1, 0) lies on line \ell_2
36: P_{978} = (15, 14, 1, 0) lies on line \ell_0
                                                                      84: P_{1991} = (4, 30, 1, 0) lies on line \ell_1
37: P_{995} = (32, 14, 1, 0) lies on line \ell_2
                                                                      85: P_{2014} = (27, 30, 1, 0) lies on line \ell_2
38: P_{1010} = (47, 14, 1, 0) lies on line \ell_1
                                                                      86: P_{2018} = (31, 30, 1, 0) lies on line \ell_0
                                                                      87: P_{2081} = (30, 31, 1, 0) lies on line \ell_0
39: P_{1041} = (14, 15, 1, 0) lies on line \ell_0
40: P_{1050} = (23, 15, 1, 0) lies on line \ell_1
                                                                      88: P_{2085} = (34, 31, 1, 0) lies on line \ell_2
41: P_{1052} = (25, 15, 1, 0) lies on line \ell_2
                                                                      89: P_{2111} = (60, 31, 1, 0) lies on line \ell_1
42: P_{1094} = (3, 16, 1, 0) lies on line \ell_2
                                                                      90: P_{2129} = (14, 32, 1, 0) lies on line \ell_1
                                                                      91 : P_{2148} = (33, 32, 1, 0) lies on line \ell_0
43: P_{1108} = (17, 16, 1, 0) lies on line \ell_0
44: P_{1109} = (18, 16, 1, 0) lies on line \ell_1
                                                                      92: P_{2162} = (47, 32, 1, 0) lies on line \ell_2
45: P_{1171} = (16, 17, 1, 0) lies on line \ell_0
                                                                      93: P_{2201} = (22, 33, 1, 0) lies on line \ell_2
46: P_{1197} = (42, 17, 1, 0) lies on line \ell_1
                                                                      94: P_{2211} = (32, 33, 1, 0) lies on line \ell_0
47: P_{1213} = (58, 17, 1, 0) lies on line \ell_2
                                                                      95: P_{2233} = (54, 33, 1, 0) lies on line \ell_1
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96: P_{2274} = (31, 34, 1, 0) lies on line \ell_1
                                                                     150: P_{3402} = (7, 52, 1, 0) lies on line \ell_1
97: P_{2278} = (35, 34, 1, 0) lies on line \ell_0
                                                                     151: P_{3445} = (50, 52, 1, 0) lies on line \ell_2
98: P_{2303} = (60, 34, 1, 0) lies on line \ell_2
                                                                     152: P_{3448} = (53, 52, 1, 0) lies on line \ell_0
99: P_{2312} = (5, 35, 1, 0) lies on line \ell_2
                                                                     153: P_{3470} = (11, 53, 1, 0) lies on line \ell_2
100: P_{2341} = (34, 35, 1, 0) lies on line \ell_0
                                                                     154: P_{3511} = (52, 53, 1, 0) lies on line \ell_0
101: P_{2346} = (39, 35, 1, 0) lies on line \ell_1
                                                                     155: P_{3522} = (63, 53, 1, 0) lies on line \ell_1
102: P_{2380} = (9, 36, 1, 0) lies on line \ell_2
                                                                     156: P_{3545} = (22, 54, 1, 0) lies on line \ell_1
103: P_{2408} = (37, 36, 1, 0) lies on line \ell_0
                                                                     157: P_{3556} = (33, 54, 1, 0) lies on line \ell_2
104: P_{2415} = (44, 36, 1, 0) lies on line \ell_1
                                                                     158: P_{3578} = (55, 54, 1, 0) lies on line \ell_0
105: P_{2455} = (20, 37, 1, 0) lies on line \ell_1
                                                                     159: P_{3611} = (24, 55, 1, 0) lies on line \ell_2
106: P_{2471} = (36, 37, 1, 0) lies on line \ell_0
                                                                     160: P_{3633} = (46, 55, 1, 0) lies on line \ell_1
107: P_{2483} = (48, 37, 1, 0) lies on line \ell_2
                                                                     161: P_{3641} = (54, 55, 1, 0) lies on line \ell_0
108: P_{2525} = (26, 38, 1, 0) lies on line \ell_2
                                                                     162: P_{3796} = (17, 58, 1, 0) lies on line \ell_1
109: P_{2538} = (39, 38, 1, 0) lies on line \ell_0
                                                                     163: P_{3821} = (42, 58, 1, 0) lies on line \ell_2
110: P_{2560} = (61, 38, 1, 0) lies on line \ell_1
                                                                     164: P_{3838} = (59, 58, 1, 0) lies on line \ell_0
111: P_{2568} = (5, 39, 1, 0) lies on line \ell_1
                                                                     165: P_{3862} = (19, 59, 1, 0) lies on line \ell_2
                                                                     166: P_{3884} = (41, 59, 1, 0) lies on line \ell_1
112: P_{2598} = (35, 39, 1, 0) lies on line \ell_2
113: P_{2601} = (38, 39, 1, 0) lies on line \ell_0
                                                                     167: P_{3901} = (58, 59, 1, 0) lies on line \ell_0
114: P_{2629} = (2, 40, 1, 0) lies on line \ell_2
                                                                     168: P_{3938} = (31, 60, 1, 0) lies on line \ell_2
                                                                     169 : P_{3941} = (34, 60, 1, 0) lies on line \ell_1
115: P_{2668} = (41, 40, 1, 0) lies on line \ell_0
116: P_{2670} = (43, 40, 1, 0) lies on line \ell_1
                                                                     170: P_{3968} = (61, 60, 1, 0) lies on line \ell_0
                                                                     171: P_{3997} = (26, 61, 1, 0) lies on line \ell_1
117: P_{2710} = (19, 41, 1, 0) lies on line \ell_1
118: P_{2731} = (40, 41, 1, 0) lies on line \ell_0
                                                                     172: P_{4009} = (38, 61, 1, 0) lies on line \ell_2
119: P_{2750} = (59, 41, 1, 0) lies on line \ell_2
                                                                     173: P_{4031} = (60, 61, 1, 0) lies on line \ell_0
120: P_{2772} = (17, 42, 1, 0) lies on line \ell_2
                                                                     174: P_{4047} = (12, 62, 1, 0) lies on line \ell_2
121: P_{2798} = (43, 42, 1, 0) lies on line \ell_0
                                                                     175: P_{4086} = (51, 62, 1, 0) lies on line \ell_1
122: P_{2813} = (58, 42, 1, 0) lies on line \ell_1
                                                                     176: P_{4098} = (63, 62, 1, 0) lies on line \ell_0
123: P_{2821} = (2, 43, 1, 0) lies on line \ell_1
                                                                     177: P_{4110} = (11, 63, 1, 0) lies on line \ell_1
                                                                     178: P_{4152} = (53, 63, 1, 0) lies on line \ell_2
124: P_{2859} = (40, 43, 1, 0) lies on line \ell_2
125: P_{2861} = (42, 43, 1, 0) lies on line \ell_0
                                                                     179: P_{4161} = (62, 63, 1, 0) lies on line \ell_0
126: P_{2892} = (9, 44, 1, 0) lies on line \ell_1
                                                                     180: P_{4226} = (0, 1, 0, 1) lies on line \ell_6
127: P_{2919} = (36, 44, 1, 0) lies on line \ell_2
                                                                     181: P_{4227} = (1, 1, 0, 1) lies on line \ell_9
128: P_{2928} = (45, 44, 1, 0) lies on line \ell_0
                                                                     182: P_{7746} = (0, 56, 0, 1) lies on line \ell_7
129: P_{2976} = (29, 45, 1, 0) lies on line \ell_2
                                                                     183: P_{7747} = (1, 56, 0, 1) lies on line \ell_{11}
130: P_{2991} = (44, 45, 1, 0) lies on line \ell_0
                                                                     184: P_{7810} = (0, 57, 0, 1) lies on line \ell_8
131: P_{2996} = (49, 45, 1, 0) lies on line \ell_1
                                                                     185: P_{7811} = (1, 57, 0, 1) lies on line \ell_{10}
132: P_{3035} = (24, 46, 1, 0) lies on line \ell_1
                                                                     186: P_{8258} = (0, 0, 1, 1) lies on line \ell_3
133 : P_{3058} = (47, 46, 1, 0) lies on line \ell_0
                                                                     187: P_{8259} = (1, 0, 1, 1) lies on line \ell_9
134 : P_{3066} = (55, 46, 1, 0) lies on line \ell_2
                                                                     188: P_{8387} = (2, 2, 1, 1) lies on line \ell_3
135: P_{3089} = (14, 47, 1, 0) lies on line \ell_2
                                                                     189: P_{8452} = (3, 3, 1, 1) lies on line \ell_3
136: P_{3107} = (32, 47, 1, 0) lies on line \ell_1
                                                                     190: P_{8517} = (4, 4, 1, 1) lies on line \ell_3
137: P_{3121} = (46, 47, 1, 0) lies on line \ell_0
                                                                     191: P_{8582} = (5, 5, 1, 1) lies on line \ell_3
138: P_{3159} = (20, 48, 1, 0) lies on line \ell_2
                                                                     192: P_{8647} = (6, 6, 1, 1) lies on line \ell_3
139: P_{3176} = (37, 48, 1, 0) lies on line \ell_1
                                                                     193: P_{8712} = (7,7,1,1) lies on line \ell_3
140: P_{3188} = (49, 48, 1, 0) lies on line \ell_0
                                                                     194: P_{8777} = (8, 8, 1, 1) lies on line \ell_3
141: P_{3232} = (29, 49, 1, 0) lies on line \ell_1
                                                                     195: P_{8842} = (9, 9, 1, 1) lies on line \ell_3
142: P_{3248} = (45, 49, 1, 0) lies on line \ell_2
                                                                     196: P_{8907} = (10, 10, 1, 1) lies on line \ell_3
143: P_{3251} = (48, 49, 1, 0) lies on line \ell_0
                                                                     197: P_{8972} = (11, 11, 1, 1) lies on line \ell_3
144: P_{3274} = (7, 50, 1, 0) lies on line \ell_2
                                                                     198: P_{9037} = (12, 12, 1, 1) lies on line \ell_3
145: P_{3318} = (51, 50, 1, 0) lies on line \ell_0
                                                                     199: P_{9102} = (13, 13, 1, 1) lies on line \ell_3
146: P_{3319} = (52, 50, 1, 0) lies on line \ell_1
                                                                     200: P_{9167} = (14, 14, 1, 1) lies on line \ell_3
147: P_{3343} = (12, 51, 1, 0) lies on line \ell_1
                                                                     201: P_{9232} = (15, 15, 1, 1) lies on line \ell_3
148: P_{3381} = (50, 51, 1, 0) lies on line \ell_0
                                                                     202: P_{9297} = (16, 16, 1, 1) lies on line \ell_3
149: P_{3393} = (62, 51, 1, 0) lies on line \ell_2
                                                                     203: P_{9362} = (17, 17, 1, 1) lies on line \ell_3
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204: P_{9427} = (18, 18, 1, 1) lies on line \ell_3
                                                                     258: P_{20074} = (41, 56, 3, 1) lies on line \ell_7
205: P_{9492} = (19, 19, 1, 1) lies on line \ell_3
                                                                     259: P_{20139} = (42, 57, 3, 1) lies on line \ell_8
206: P_{9557} = (20, 20, 1, 1) lies on line \ell_3
                                                                     260: P_{20613} = (4, 1, 4, 1) lies on line \ell_6
207: P_{9622} = (21, 21, 1, 1) lies on line \ell_3
                                                                     261: P_{20866} = (1, 5, 4, 1) lies on line \ell_9
208: P_{9687} = (22, 22, 1, 1) lies on line \ell_3
                                                                     262: P_{22274} = (1, 27, 4, 1) lies on line \ell_{10}
                                                                     263: P_{22466} = (1, 30, 4, 1) lies on line \ell_{11}
209: P_{9752} = (23, 23, 1, 1) lies on line \ell_3
210: P_{9817} = (24, 24, 1, 1) lies on line \ell_3
                                                                     264: P_{24163} = (34, 56, 4, 1) lies on line \ell_7
211: P_{9882} = (25, 25, 1, 1) lies on line \ell_3
                                                                     265: P_{24231} = (38, 57, 4, 1) lies on line \ell_8
212 : P_{9947} = (26, 26, 1, 1) lies on line \ell_3
                                                                     266: P_{24710} = (5, 1, 5, 1) lies on line \ell_6
213: P_{10012} = (27, 27, 1, 1) lies on line \ell_3
                                                                     267: P_{24898} = (1, 4, 5, 1) lies on line \ell_9
214: P_{10077} = (28, 28, 1, 1) lies on line \ell_3
                                                                     268: P_{26882} = (1, 35, 5, 1) lies on line \ell_{10}
215: P_{10142} = (29, 29, 1, 1) lies on line \ell_3
                                                                     269: P_{27138} = (1, 39, 5, 1) lies on line \ell_{11}
216: P_{10207} = (30, 30, 1, 1) lies on line \ell_3
                                                                     270: P_{28251} = (26, 56, 5, 1) lies on line \ell_7
217: P_{10272} = (31, 31, 1, 1) lies on line \ell_3
                                                                     271: P_{28320} = (31, 57, 5, 1) lies on line \ell_8
218: P_{10337} = (32, 32, 1, 1) lies on line \ell_3
                                                                     272: P_{28807} = (6, 1, 6, 1) lies on line \ell_6
219: P_{10402} = (33, 33, 1, 1) lies on line \ell_3
                                                                     273: P_{29186} = (1, 7, 6, 1) lies on line \ell_9
220: P_{10467} = (34, 34, 1, 1) lies on line \ell_3
                                                                     274: P_{29378} = (1, 10, 6, 1) lies on line \ell_{10}
221: P_{10532} = (35, 35, 1, 1) lies on line \ell_3
                                                                     275: P_{29570} = (1, 13, 6, 1) lies on line \ell_{11}
222: P_{10597} = (36, 36, 1, 1) lies on line \ell_3
                                                                     276: P_{32372} = (51, 56, 6, 1) lies on line \ell_7
223: P_{10662} = (37, 37, 1, 1) lies on line \ell_3
                                                                     277: P_{32438} = (53, 57, 6, 1) lies on line \ell_8
224 : P_{10727} = (38, 38, 1, 1) lies on line \ell_3
                                                                     278: P_{32904} = (7, 1, 7, 1) lies on line \ell_6
225 : P_{10792} = (39, 39, 1, 1) lies on line \ell_3
                                                                     279: P_{33218} = (1, 6, 7, 1) lies on line \ell_9
226: P_{10857} = (40, 40, 1, 1) lies on line \ell_3
                                                                     280: P_{36034} = (1, 50, 7, 1) lies on line \ell_{10}
227 : P_{10922} = (41, 41, 1, 1) lies on line \ell_3
                                                                     281: P_{36162} = (1, 52, 7, 1) lies on line \ell_{11}
228: P_{10987} = (42, 42, 1, 1) lies on line \ell_3
                                                                     282: P_{36428} = (11, 56, 7, 1) lies on line \ell_7
229: P_{11052} = (43, 43, 1, 1) lies on line \ell_3
                                                                     283: P_{36493} = (12, 57, 7, 1) lies on line \ell_8
230 : P_{11117} = (44, 44, 1, 1) lies on line \ell_3
                                                                     284: P_{37001} = (8, 1, 8, 1) lies on line \ell_6
231 : P_{11182} = (45, 45, 1, 1) lies on line \ell_3
                                                                     285: P_{37506} = (1, 9, 8, 1) lies on line \ell_9
232: P_{11247} = (46, 46, 1, 1) lies on line \ell_3
                                                                     286: P_{38274} = (1, 21, 8, 1) lies on line \ell_{11}
233: P_{11312} = (47, 47, 1, 1) lies on line \ell_3
                                                                     287: P_{38722} = (1, 28, 8, 1) lies on line \ell_{10}
234: P_{11377} = (48, 48, 1, 1) lies on line \ell_3
                                                                     288: P_{40550} = (37, 56, 8, 1) lies on line \ell_7
235 : P_{11442} = (49, 49, 1, 1) lies on line \ell_3
                                                                     289: P_{40622} = (45, 57, 8, 1) lies on line \ell_8
236: P_{11507} = (50, 50, 1, 1) lies on line \ell_3
                                                                     290: P_{41098} = (9, 1, 9, 1) lies on line \ell_6
237: P_{11572} = (51, 51, 1, 1) lies on line \ell_3
                                                                     291: P_{41538} = (1, 8, 9, 1) lies on line \ell_9
238: P_{11637} = (52, 52, 1, 1) lies on line \ell_3
                                                                     292: P_{43330} = (1, 36, 9, 1) lies on line \ell_{10}
                                                                     293: P_{43842} = (1, 44, 9, 1) lies on line \ell_{11}
239: P_{11702} = (53, 53, 1, 1) lies on line \ell_3
240: P_{11767} = (54, 54, 1, 1) lies on line \ell_3
                                                                     294: P_{44638} = (29, 56, 9, 1) lies on line \ell_7
241 : P_{11832} = (55, 55, 1, 1) lies on line \ell_3
                                                                     295 : P_{44693} = (20, 57, 9, 1) lies on line \ell_8
242 : P_{12027} = (58, 58, 1, 1) lies on line \ell_3
                                                                     296: P_{45195} = (10, 1, 10, 1) lies on line \ell_6
243: P_{12092} = (59, 59, 1, 1) lies on line \ell_3
                                                                     297: P_{45506} = (1, 6, 10, 1) lies on line \ell_{11}
                                                                     298 : P_{45826} = (1, 11, 10, 1) lies on line \ell_9
244: P_{12157} = (60, 60, 1, 1) lies on line \ell_3
245: P_{12222} = (61, 61, 1, 1) lies on line \ell_3
                                                                     299: P_{45954} = (1, 13, 10, 1) lies on line \ell_{10}
246: P_{12287} = (62, 62, 1, 1) lies on line \ell_3
                                                                     300: P_{48757} = (52, 56, 10, 1) lies on line \ell_7
247: P_{12352} = (63, 63, 1, 1) lies on line \ell_3
                                                                     301: P_{48831} = (62, 57, 10, 1) lies on line \ell_8
248: P_{12419} = (2, 1, 2, 1) lies on line \ell_6
                                                                     302: P_{49292} = (11, 1, 11, 1) lies on line \ell_6
249: P_{12546} = (1, 3, 2, 1) lies on line \ell_9
                                                                     303: P_{49858} = (1, 10, 11, 1) lies on line \ell_9
250: P_{14914} = (1, 40, 2, 1) lies on line \ell_{10}
                                                                     304: P_{52610} = (1, 53, 11, 1) lies on line \ell_{10}
251: P_{15106} = (1, 43, 2, 1) lies on line \ell_{11}
                                                                     305: P_{52813} = (12, 56, 11, 1) lies on line \ell_7
252: P_{15954} = (17, 56, 2, 1) lies on line \ell_7
                                                                     306: P_{52872} = (7, 57, 11, 1) lies on line \ell_8
253: P_{16020} = (19, 57, 2, 1) lies on line \ell_8
                                                                     307: P_{53250} = (1, 63, 11, 1) lies on line \ell_{11}
254: P_{16516} = (3, 1, 3, 1) lies on line \ell_6
                                                                     308: P_{53389} = (12, 1, 12, 1) lies on line \ell_6
255: P_{16578} = (1, 2, 3, 1) lies on line \ell_9
                                                                     309: P_{54146} = (1, 13, 12, 1) lies on line \ell_9
256: P_{17474} = (1, 16, 3, 1) lies on line \ell_{10}
                                                                     310: P_{56578} = (1, 51, 12, 1) lies on line \ell_{11}
257: P_{17602} = (1, 18, 3, 1) lies on line \ell_{11}
                                                                     311: P_{56904} = (7, 56, 12, 1) lies on line \ell_7
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312: P_{56972} = (11, 57, 12, 1) lies on line \ell_8
                                                                     366: P_{93810} = (49, 56, 21, 1) lies on line \ell_7
313: P_{57282} = (1, 62, 12, 1) lies on line \ell_{10}
                                                                     367: P_{93861} = (36, 57, 21, 1) lies on line \ell_8
                                                                     368: P_{94359} = (22, 1, 22, 1) lies on line \ell_6
314: P_{57486} = (13, 1, 13, 1) lies on line \ell_6
315: P_{57794} = (1, 6, 13, 1) lies on line \ell_{10}
                                                                     369: P_{95746} = (1, 23, 22, 1) lies on line \ell_9
316: P_{58050} = (1, 10, 13, 1) lies on line \ell_{11}
                                                                     370: P_{96386} = (1, 33, 22, 1) lies on line \ell_{10}
317: P_{58178} = (1, 12, 13, 1) lies on line \ell_9
                                                                     371: P_{97730} = (1, 54, 22, 1) lies on line \ell_{11}
318: P_{61056} = (63, 56, 13, 1) lies on line \ell_7
                                                                     372: P_{97881} = (24, 56, 22, 1) lies on line \ell_7
                                                                     373: P_{97935} = (14, 57, 22, 1) lies on line \ell_8
319: P_{61107} = (50, 57, 13, 1) lies on line \ell_8
320 : P_{61583} = (14, 1, 14, 1) lies on line \ell_6
                                                                     374: P_{98456} = (23, 1, 23, 1) lies on line \ell_6
321: P_{62466} = (1, 15, 14, 1) lies on line \ell_9
                                                                     375: P_{99330} = (1, 15, 23, 1) lies on line \ell_{11}
322: P_{63554} = (1, 32, 14, 1) lies on line \ell_{11}
                                                                     376: P_{99778} = (1, 22, 23, 1) lies on line \ell_9
323: P_{64514} = (1, 47, 14, 1) lies on line \ell_{10}
                                                                     377: P_{99970} = (1, 25, 23, 1) lies on line \ell_{10}
324: P_{65111} = (22, 56, 14, 1) lies on line \ell_7
                                                                     378: P_{101985} = (32, 56, 23, 1) lies on line \ell_7
325: P_{65177} = (24, 57, 14, 1) lies on line \ell_8
                                                                     379: P_{102072} = (55, 57, 23, 1) lies on line \ell_8
                                                                     380: P_{102553} = (24, 1, 24, 1) lies on line \ell_6
326: P_{65680} = (15, 1, 15, 1) lies on line \ell_6
327: P_{66498} = (1, 14, 15, 1) lies on line \ell_9
                                                                     381: P_{104066} = (1, 25, 24, 1) lies on line \ell_9
                                                                     382 : P_{105410} = (1, 46, 24, 1) lies on line \ell_{11}
328: P_{67074} = (1, 23, 15, 1) lies on line \ell_{10}
                                                                     383 : P_{105986} = (1, 55, 24, 1) lies on line \ell_{10}
329: P_{67202} = (1, 25, 15, 1) lies on line \ell_{11}
330 : P_{69231} = (46, 56, 15, 1) lies on line \ell_7
                                                                     384: P_{106063} = (14, 56, 24, 1) lies on line \ell_7
331: P_{69282} = (33, 57, 15, 1) lies on line \ell_8
                                                                     385: P_{106135} = (22, 57, 24, 1) lies on line \ell_8
                                                                     386: P_{106650} = (25, 1, 25, 1) lies on line \ell_6
332 : P_{69777} = (16, 1, 16, 1) lies on line \ell_6
                                                                     387: P_{107522} = (1, 15, 25, 1) lies on line \ell_{10}
333: P_{69890} = (1, 3, 16, 1) lies on line \ell_{11}
334: P_{70786} = (1, 17, 16, 1) lies on line \ell_9
                                                                     388: P_{108034} = (1, 23, 25, 1) lies on line \ell_{11}
335 : P_{70850} = (1, 18, 16, 1) lies on line \ell_{10}
                                                                     389: P_{108098} = (1, 24, 25, 1) lies on line \ell_9
336: P_{73324} = (43, 56, 16, 1) lies on line \ell_7
                                                                     390: P_{110199} = (54, 56, 25, 1) lies on line \ell_7
                                                                     391 : P_{110256} = (47, 57, 25, 1) lies on line \ell_8
337: P_{73404} = (59, 57, 16, 1) lies on line \ell_8
338 : P_{73874} = (17, 1, 17, 1) lies on line \ell_6
                                                                     392: P_{110747} = (26, 1, 26, 1) lies on line \ell_6
339: P_{74818} = (1, 16, 17, 1) lies on line \ell_9
                                                                     393: P_{112386} = (1, 27, 26, 1) lies on line \ell_9
340: P_{76482} = (1, 42, 17, 1) lies on line \ell_{10}
                                                                     394: P_{113090} = (1, 38, 26, 1) lies on line \ell_{10}
341: P_{77396} = (19, 56, 17, 1) lies on line \ell_7
                                                                     395: P_{114272} = (31, 56, 26, 1) lies on line \ell_7
342: P_{77443} = (2, 57, 17, 1) lies on line \ell_8
                                                                     396: P_{114310} = (5, 57, 26, 1) lies on line \ell_8
343: P_{77506} = (1, 58, 17, 1) lies on line \ell_{11}
                                                                     397: P_{114562} = (1, 61, 26, 1) lies on line \ell_{11}
344: P_{77971} = (18, 1, 18, 1) lies on line \ell_6
                                                                     398: P_{114844} = (27, 1, 27, 1) lies on line \ell_6
345: P_{78082} = (1, 3, 18, 1) lies on line \ell_{10}
                                                                     399 : P_{115010} = (1, 4, 27, 1) lies on line \ell_{11}
346: P_{78914} = (1, 16, 18, 1) lies on line \ell_{11}
                                                                     400: P_{116418} = (1, 26, 27, 1) lies on line \ell_9
347: P_{79106} = (1, 19, 18, 1) lies on line \ell_9
                                                                     401: P_{116674} = (1, 30, 27, 1) lies on line \ell_{10}
348: P_{81531} = (58, 56, 18, 1) lies on line \ell_7
                                                                     402: P_{118376} = (39, 56, 27, 1) lies on line \ell_7
349: P_{81577} = (40, 57, 18, 1) lies on line \ell_8
                                                                     403: P_{118461} = (60, 57, 27, 1) lies on line \ell_8
350: P_{82068} = (19, 1, 19, 1) lies on line \ell_6
                                                                     404: P_{118941} = (28, 1, 28, 1) lies on line \ell_6
351 : P_{83138} = (1, 18, 19, 1) lies on line \ell_9
                                                                     405: P_{119362} = (1, 8, 28, 1) lies on line \ell_{11}
                                                                     406: P_{120194} = (1, 21, 28, 1) lies on line \ell_{10}
352: P_{84610} = (1, 41, 19, 1) lies on line \ell_{11}
353: P_{85571} = (2, 56, 19, 1) lies on line \ell_7
                                                                     407: P_{120706} = (1, 29, 28, 1) lies on line \ell_9
354: P_{85650} = (17, 57, 19, 1) lies on line \ell_8
                                                                     408 : P_{122477} = (44, 56, 28, 1) lies on line \ell_7
355: P_{85762} = (1, 59, 19, 1) lies on line \ell_{10}
                                                                     409: P_{122545} = (48, 57, 28, 1) lies on line \ell_8
356: P_{86165} = (20, 1, 20, 1) lies on line \ell_6
                                                                     410: P_{123038} = (29, 1, 29, 1) lies on line \ell_6
357: P_{87426} = (1, 21, 20, 1) lies on line \ell_9
                                                                     411: P_{124738} = (1, 28, 29, 1) lies on line \ell_9
358: P_{88450} = (1, 37, 20, 1) lies on line \ell_{11}
                                                                     412: P_{125826} = (1, 45, 29, 1) lies on line \ell_{10}
359: P_{89154} = (1, 48, 20, 1) lies on line \ell_{10}
                                                                     413: P_{126082} = (1, 49, 29, 1) lies on line \ell_{11}
360: P_{89674} = (9, 56, 20, 1) lies on line \ell_7
                                                                     414: P_{126549} = (20, 56, 29, 1) lies on line \ell_7
361: P_{89758} = (29, 57, 20, 1) lies on line \ell_8
                                                                     415: P_{126602} = (9, 57, 29, 1) lies on line \ell_8
362: P_{90262} = (21, 1, 21, 1) lies on line \ell_6
                                                                     416: P_{127135} = (30, 1, 30, 1) lies on line \ell_6
363: P_{90690} = (1, 8, 21, 1) lies on line \ell_{10}
                                                                     417: P_{127298} = (1, 4, 30, 1) lies on line \ell_{10}
364: P_{91458} = (1, 20, 21, 1) lies on line \ell_9
                                                                     418: P_{128770} = (1, 27, 30, 1) lies on line \ell_{11}
365: P_{91970} = (1, 28, 21, 1) lies on line \ell_{11}
                                                                     419: P_{129026} = (1, 31, 30, 1) lies on line \ell_9
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420 : P_{130686} = (61, 56, 30, 1) lies on line \ell_7
                                                                     474: P_{167549} = (60, 56, 39, 1) lies on line \ell_7
                                                                     475: P_{167580} = (27, 57, 39, 1) lies on line \ell_8
421: P_{130724} = (35, 57, 30, 1) lies on line \ell_8
                                                                     476: P_{168105} = (40, 1, 40, 1) lies on line \ell_6
422: P_{131232} = (31, 1, 31, 1) lies on line \ell_6
423: P_{133058} = (1, 30, 31, 1) lies on line \ell_9
                                                                     477: P_{168130} = (1, 2, 40, 1) lies on line \ell_{11}
424: P_{133314} = (1, 34, 31, 1) lies on line \ell_{11}
                                                                     478: P_{170626} = (1, 41, 40, 1) lies on line \ell_9
425: P_{134726} = (5, 56, 31, 1) lies on line \ell_7
                                                                     479: P_{170754} = (1, 43, 40, 1) lies on line \ell_{10}
426: P_{134811} = (26, 57, 31, 1) lies on line \ell_8
                                                                     480: P_{171603} = (18, 56, 40, 1) lies on line \ell_7
427: P_{134978} = (1,60,31,1) lies on line \ell_{10}
                                                                     481: P_{171707} = (58, 57, 40, 1) lies on line \ell_8
428: P_{135329} = (32, 1, 32, 1) lies on line \ell_6
                                                                     482: P_{172202} = (41, 1, 41, 1) lies on line \ell_6
429: P_{136130} = (1, 14, 32, 1) lies on line \ell_{10}
                                                                     483: P_{173314} = (1, 19, 41, 1) lies on line \ell_{10}
430: P_{137346} = (1, 33, 32, 1) lies on line \ell_9
                                                                     484: P_{174658} = (1, 40, 41, 1) lies on line \ell_9
431: P_{138242} = (1, 47, 32, 1) lies on line \ell_{11}
                                                                     485: P_{175723} = (42, 56, 41, 1) lies on line \ell_7
432: P_{138872} = (55, 56, 32, 1) lies on line \ell_7
                                                                     486: P_{175748} = (3, 57, 41, 1) lies on line \ell_8
433: P_{138904} = (23, 57, 32, 1) lies on line \ell_8
                                                                     487: P_{175874} = (1, 59, 41, 1) lies on line \ell_{11}
434: P_{139426} = (33, 1, 33, 1) lies on line \ell_6
                                                                     488: P_{176299} = (42, 1, 42, 1) lies on line \ell_6
435: P_{140738} = (1, 22, 33, 1) lies on line \ell_{11}
                                                                     489: P_{177282} = (1, 17, 42, 1) lies on line \ell_{11}
436: P_{141378} = (1, 32, 33, 1) lies on line \ell_9
                                                                     490: P_{178946} = (1, 43, 42, 1) lies on line \ell_9
437: P_{142786} = (1, 54, 33, 1) lies on line \ell_{10}
                                                                     491: P_{179780} = (3, 56, 42, 1) lies on line \ell_7
                                                                     492: P_{179882} = (41, 57, 42, 1) lies on line \ell_8
438: P_{142928} = (15, 56, 33, 1) lies on line \ell_7
                                                                     493: P_{179906} = (1, 58, 42, 1) lies on line \ell_{10}
439: P_{143023} = (46, 57, 33, 1) lies on line \ell_8
440: P_{143523} = (34, 1, 34, 1) lies on line \ell_6
                                                                     494: P_{180396} = (43, 1, 43, 1) lies on line \ell_6
441: P_{145410} = (1, 31, 34, 1) lies on line \ell_{10}
                                                                     495 : P_{180418} = (1, 2, 43, 1) lies on line \ell_{10}
442: P_{145666} = (1, 35, 34, 1) lies on line \ell_9
                                                                     496: P_{182850} = (1, 40, 43, 1) lies on line \ell_{11}
443 : P_{147047} = (38, 56, 34, 1) lies on line \ell_7
                                                                     497: P_{182978} = (1, 42, 43, 1) lies on line \ell_9
444: P_{147077} = (4, 57, 34, 1) lies on line \ell_8
                                                                     498: P_{183932} = (59, 56, 43, 1) lies on line \ell_7
445: P_{147266} = (1, 60, 34, 1) lies on line \ell_{11}
                                                                     499: P_{183953} = (16, 57, 43, 1) lies on line \ell_8
446: P_{147620} = (35, 1, 35, 1) lies on line \ell_6
                                                                     500: P_{184493} = (44, 1, 44, 1) lies on line \ell_6
447: P_{147842} = (1, 5, 35, 1) lies on line \ell_{11}
                                                                     501: P_{184962} = (1, 9, 44, 1) lies on line \ell_{10}
448: P_{149698} = (1, 34, 35, 1) lies on line \ell_9
                                                                     502: P_{186690} = (1, 36, 44, 1) lies on line \ell_{11}
449: P_{150018} = (1, 39, 35, 1) lies on line \ell_{10}
                                                                     503: P_{187266} = (1, 45, 44, 1) lies on line \ell_9
450: P_{151135} = (30, 56, 35, 1) lies on line \ell_7
                                                                     504: P_{188017} = (48, 56, 44, 1) lies on line \ell_7
451: P_{151230} = (61, 57, 35, 1) lies on line \ell_8
                                                                     505: P_{188061} = (28, 57, 44, 1) lies on line \ell_8
452: P_{151717} = (36, 1, 36, 1) lies on line \ell_6
                                                                     506: P_{188590} = (45, 1, 45, 1) lies on line \ell_6
453 : P_{152194} = (1, 9, 36, 1) lies on line \ell_{11}
                                                                     507: P_{190338} = (1, 29, 45, 1) lies on line \ell_{11}
454: P_{153986} = (1, 37, 36, 1) lies on line \ell_9
                                                                     508: P_{191298} = (1, 44, 45, 1) lies on line \ell_9
                                                                     509: P_{191618} = (1, 49, 45, 1) lies on line \ell_{10}
455: P_{154434} = (1, 44, 36, 1) lies on line \ell_{10}
                                                                     510 : P_{192073} = (8, 56, 45, 1) lies on line \ell_7
456: P_{155222} = (21, 56, 36, 1) lies on line \ell_7
457: P_{155314} = (49, 57, 36, 1) lies on line \ell_8
                                                                     511: P_{192166} = (37, 57, 45, 1) lies on line \ell_8
458: P_{155814} = (37, 1, 37, 1) lies on line \ell_6
                                                                     512: P_{192687} = (46, 1, 46, 1) lies on line \ell_6
459: P_{156994} = (1, 20, 37, 1) lies on line \ell_{10}
                                                                     513: P_{194114} = (1, 24, 46, 1) lies on line \ell_{10}
460: P_{158018} = (1, 36, 37, 1) lies on line \ell_9
                                                                     514: P_{195586} = (1, 47, 46, 1) lies on line \ell_9
461: P_{158786} = (1, 48, 37, 1) lies on line \ell_{11}
                                                                     515: P_{196098} = (1, 55, 46, 1) lies on line \ell_{11}
462 : P_{159342} = (45, 56, 37, 1) lies on line \ell_7
                                                                     516: P_{196194} = (33, 56, 46, 1) lies on line \ell_7
463: P_{159369} = (8, 57, 37, 1) lies on line \ell_8
                                                                     517: P_{196240} = (15, 57, 46, 1) lies on line \ell_8
464: P_{159911} = (38, 1, 38, 1) lies on line \ell_6
                                                                     518: P_{196784} = (47, 1, 47, 1) lies on line \ell_6
465: P_{161474} = (1, 26, 38, 1) lies on line \ell_{11}
                                                                     519: P_{197570} = (1, 14, 47, 1) lies on line \ell_{11}
466: P_{162306} = (1, 39, 38, 1) lies on line \ell_9
                                                                     520: P_{198722} = (1, 32, 47, 1) lies on line \ell_{10}
467: P_{163397} = (4, 56, 38, 1) lies on line \ell_7
                                                                     521: P_{199618} = (1, 46, 47, 1) lies on line \ell_9
468: P_{163491} = (34, 57, 38, 1) lies on line \ell_8
                                                                     522: P_{200282} = (25, 56, 47, 1) lies on line \ell_7
469: P_{163714} = (1, 61, 38, 1) lies on line \ell_{10}
                                                                     523: P_{200375} = (54, 57, 47, 1) lies on line \ell_8
                                                                     524: P_{200881} = (48, 1, 48, 1) lies on line \ell_6
470: P_{164008} = (39, 1, 39, 1) lies on line \ell_6
471: P_{164226} = (1, 5, 39, 1) lies on line \ell_{10}
                                                                     525: P_{202050} = (1, 20, 48, 1) lies on line \ell_{11}
472 : P_{166146} = (1, 35, 39, 1) lies on line \ell_{11}
                                                                     526: P_{203138} = (1, 37, 48, 1) lies on line \ell_{10}
473: P_{166338} = (1, 38, 39, 1) lies on line \ell_9
                                                                     527: P_{203906} = (1, 49, 48, 1) lies on line \ell_9
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582: P_{234229} = (52, 10, 56, 1) lies on line \ell_4
528: P_{204381} = (28, 56, 48, 1) lies on line \ell_7
529: P_{204461} = (44, 57, 48, 1) lies on line \ell_8
                                                                    583: P_{234253} = (12, 11, 56, 1) lies on line \ell_4
530: P_{204978} = (49, 1, 49, 1) lies on line \ell_6
                                                                     584: P_{234312} = (7, 12, 56, 1) lies on line \ell_4
531: P_{206722} = (1, 29, 49, 1) lies on line \ell_{10}
                                                                    585: P_{234432} = (63, 13, 56, 1) lies on line \ell_4
532 : P_{207746} = (1, 45, 49, 1) lies on line \ell_{11}
                                                                    586: P_{234455} = (22, 14, 56, 1) lies on line \ell_4
533: P_{207938} = (1, 48, 49, 1) lies on line \ell_9
                                                                    587: P_{234543} = (46, 15, 56, 1) lies on line \ell_4
534: P_{208485} = (36, 56, 49, 1) lies on line \ell_7
                                                                    588: P_{234604} = (43, 16, 56, 1) lies on line \ell_4
535: P_{208534} = (21, 57, 49, 1) lies on line \ell_8
                                                                    589: P_{234644} = (19, 17, 56, 1) lies on line \ell_4
536: P_{209075} = (50, 1, 50, 1) lies on line \ell_6
                                                                    590: P_{234747} = (58, 18, 56, 1) lies on line \ell_4
537: P_{209410} = (1, 7, 50, 1) lies on line \ell_{11}
                                                                    591: P_{234755} = (2, 19, 56, 1) lies on line \ell_4
538: P_{212226} = (1, 51, 50, 1) lies on line \ell_9
                                                                    592: P_{234826} = (9, 20, 56, 1) lies on line \ell_4
539: P_{212290} = (1, 52, 50, 1) lies on line \ell_{10}
                                                                    593: P_{234930} = (49, 21, 56, 1) lies on line \ell_4
540: P_{212558} = (13, 56, 50, 1) lies on line \ell_7
                                                                    594: P_{234969} = (24, 22, 56, 1) lies on line \ell_4
541: P_{212672} = (63, 57, 50, 1) lies on line \ell_8
                                                                    595: P_{235041} = (32, 23, 56, 1) lies on line \ell_4
542: P_{213172} = (51, 1, 51, 1) lies on line \ell_6
                                                                    596: P_{235087} = (14, 24, 56, 1) lies on line \ell_4
543: P_{213826} = (1, 12, 51, 1) lies on line \ell_{10}
                                                                    597: P_{235191} = (54, 25, 56, 1) lies on line \ell_4
544: P_{216258} = (1, 50, 51, 1) lies on line \ell_9
                                                                    598: P_{235232} = (31, 26, 56, 1) lies on line \ell_4
545: P_{216694} = (53, 56, 51, 1) lies on line \ell_7
                                                                    599: P_{235304} = (39, 27, 56, 1) lies on line \ell_4
546: P_{216711} = (6, 57, 51, 1) lies on line \ell_8
                                                                    600: P_{235373} = (44, 28, 56, 1) lies on line \ell_4
547: P_{217026} = (1, 62, 51, 1) lies on line \ell_{11}
                                                                    601: P_{235413} = (20, 29, 56, 1) lies on line \ell_4
548: P_{217269} = (52, 1, 52, 1) lies on line \ell_6
                                                                    602: P_{235518} = (61, 30, 56, 1) lies on line \ell_4
549: P_{217602} = (1, 7, 52, 1) lies on line \ell_{10}
                                                                     603: P_{235526} = (5, 31, 56, 1) lies on line \ell_4
550: P_{220354} = (1, 50, 52, 1) lies on line \ell_{11}
                                                                     604: P_{235640} = (55, 32, 56, 1) lies on line \ell_4
551 : P_{220546} = (1, 53, 52, 1) lies on line \ell_9
                                                                    605: P_{235664} = (15, 33, 56, 1) lies on line \ell_4
552: P_{220799} = (62, 56, 52, 1) lies on line \ell_7
                                                                     606: P_{235751} = (38, 34, 56, 1) lies on line \ell_4
553 : P_{220811} = (10, 57, 52, 1) lies on line \ell_8
                                                                    607: P_{235807} = (30, 35, 56, 1) lies on line \ell_4
554: P_{221366} = (53, 1, 53, 1) lies on line \ell_6
                                                                    608: P_{235862} = (21, 36, 56, 1) lies on line \ell_4
555: P_{221954} = (1, 11, 53, 1) lies on line \ell_{11}
                                                                    609: P_{235950} = (45, 37, 56, 1) lies on line \ell_4
556: P_{224578} = (1, 52, 53, 1) lies on line \ell_9
                                                                    610: P_{235973} = (4, 38, 56, 1) lies on line \ell_4
557: P_{224839} = (6, 56, 53, 1) lies on line \ell_7
                                                                    611: P_{236093} = (60, 39, 56, 1) lies on line \ell_4
558: P_{224948} = (51, 57, 53, 1) lies on line \ell_8
                                                                    612: P_{236115} = (18, 40, 56, 1) lies on line \ell_4
559: P_{225282} = (1, 63, 53, 1) lies on line \ell_{10}
                                                                    613: P_{236203} = (42, 41, 56, 1) lies on line \ell_4
560: P_{225463} = (54, 1, 54, 1) lies on line \ell_6
                                                                     614: P_{236228} = (3, 42, 56, 1) lies on line \ell_4
561: P_{226754} = (1, 22, 54, 1) lies on line \ell_{10}
                                                                    615: P_{236348} = (59, 43, 56, 1) lies on line \ell_4
562: P_{227458} = (1, 33, 54, 1) lies on line \ell_{11}
                                                                    616: P_{236401} = (48, 44, 56, 1) lies on line \ell_4
563: P_{228866} = (1, 55, 54, 1) lies on line \ell_9
                                                                    617: P_{236425} = (8, 45, 56, 1) lies on line \ell_4
564: P_{228976} = (47, 56, 54, 1) lies on line \ell_7
                                                                     618: P_{236514} = (33, 46, 56, 1) lies on line \ell_4
565: P_{229018} = (25, 57, 54, 1) lies on line \ell_8
                                                                    619: P_{236570} = (25, 47, 56, 1) lies on line \ell_4
566: P_{229560} = (55, 1, 55, 1) lies on line \ell_6
                                                                    620: P_{236637} = (28, 48, 56, 1) lies on line \ell_4
567 : P_{230978} = (1, 24, 55, 1) lies on line \ell_{11}
                                                                    621: P_{236709} = (36, 49, 56, 1) lies on line \ell_4
568: P_{232386} = (1, 46, 55, 1) lies on line \ell_{10}
                                                                    622: P_{236750} = (13, 50, 56, 1) lies on line \ell_4
569: P_{232898} = (1, 54, 55, 1) lies on line \ell_9
                                                                    623: P_{236854} = (53, 51, 56, 1) lies on line \ell_4
570: P_{233048} = (23, 56, 55, 1) lies on line \ell_7
                                                                    624: P_{236927} = (62, 52, 56, 1) lies on line \ell_4
571: P_{233121} = (32, 57, 55, 1) lies on line \ell_8
                                                                    625: P_{236935} = (6, 53, 56, 1) lies on line \ell_4
572: P_{233537} = (0, 0, 56, 1) lies on line \ell_4
                                                                     626: P_{237040} = (47, 54, 56, 1) lies on line \ell_4
573: P_{233538} = (1, 0, 56, 1) lies on line \ell_{10}
                                                                    627: P_{237080} = (23, 55, 56, 1) lies on line \ell_4
574: P_{233682} = (17, 2, 56, 1) lies on line \ell_4
                                                                    628: P_{237289} = (40, 58, 56, 1) lies on line \ell_4
575: P_{233770} = (41, 3, 56, 1) lies on line \ell_4
                                                                     629: P_{237329} = (16, 59, 56, 1) lies on line \ell_4
576: P_{233827} = (34, 4, 56, 1) lies on line \ell_4
                                                                    630: P_{237404} = (27, 60, 56, 1) lies on line \ell_4
577 : P_{233883} = (26, 5, 56, 1) lies on line \ell_4
                                                                    631: P_{237476} = (35, 61, 56, 1) lies on line \ell_4
578: P_{233972} = (51, 6, 56, 1) lies on line \ell_4
                                                                    632: P_{237515} = (10, 62, 56, 1) lies on line \ell_4
579: P_{233996} = (11, 7, 56, 1) lies on line \ell_4
                                                                    633: P_{237619} = (50, 63, 56, 1) lies on line \ell_4
580 : P_{234086} = (37, 8, 56, 1) lies on line \ell_4
                                                                    634: P_{237633} = (0, 0, 57, 1) lies on line \ell_5
581: P_{234142} = (29, 9, 56, 1) lies on line \ell_4
                                                                     635: P_{237634} = (1, 0, 57, 1) lies on line \ell_{11}
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636 : P_{237780} = (19, 2, 57, 1) lies on line \ell_5
                                                                     685: P_{240903} = (6, 51, 57, 1) lies on line \ell_5
637: P_{237867} = (42, 3, 57, 1) lies on line \ell_5
                                                                     686: P_{240971} = (10, 52, 57, 1) lies on line \ell_5
                                                                     687: P_{241076} = (51, 53, 57, 1) lies on line \ell_5
638: P_{237927} = (38, 4, 57, 1) lies on line \ell_5
639: P_{237984} = (31, 5, 57, 1) lies on line \ell_5
                                                                    688: P_{241114} = (25, 54, 57, 1) lies on line \ell_5
640: P_{238070} = (53, 6, 57, 1) lies on line \ell_5
                                                                    689: P_{241185} = (32, 55, 57, 1) lies on line \ell_5
641: P_{238093} = (12, 7, 57, 1) lies on line \ell_5
                                                                    690: P_{241363} = (18, 58, 57, 1) lies on line \ell_5
642: P_{238190} = (45, 8, 57, 1) lies on line \ell_5
                                                                     691: P_{241452} = (43, 59, 57, 1) lies on line \ell_5
643: P_{238229} = (20, 9, 57, 1) lies on line \ell_5
                                                                     692: P_{241512} = (39, 60, 57, 1) lies on line \ell_5
644: P_{238335} = (62, 10, 57, 1) lies on line \ell_5
                                                                    693: P_{241567} = (30, 61, 57, 1) lies on line \ell_5
645: P_{238344} = (7, 11, 57, 1) lies on line \ell_5
                                                                     694: P_{241653} = (52, 62, 57, 1) lies on line \ell_5
646: P_{238412} = (11, 12, 57, 1) lies on line \ell_5
                                                                    695: P_{241678} = (13, 63, 57, 1) lies on line \ell_5
                                                                    696: P_{241851} = (58, 1, 58, 1) lies on line \ell_6
647: P_{238515} = (50, 13, 57, 1) lies on line \ell_5
648: P_{238553} = (24, 14, 57, 1) lies on line \ell_5
                                                                    697: P_{242818} = (1, 17, 58, 1) lies on line \ell_{10}
                                                                    698: P_{244418} = (1, 42, 58, 1) lies on line \ell_{11}
649: P_{238626} = (33, 15, 57, 1) lies on line \ell_5
650: P_{238716} = (59, 16, 57, 1) lies on line \ell_5
                                                                     699: P_{245353} = (40, 56, 58, 1) lies on line \ell_7
651: P_{238723} = (2, 17, 57, 1) lies on line \ell_5
                                                                     700: P_{245395} = (18, 57, 58, 1) lies on line \ell_8
652: P_{238825} = (40, 18, 57, 1) lies on line \ell_5
                                                                     701: P_{245506} = (1, 59, 58, 1) lies on line \ell_9
653: P_{238866} = (17, 19, 57, 1) lies on line \ell_5
                                                                     702: P_{245948} = (59, 1, 59, 1) lies on line \ell_6
654: P_{238942} = (29, 20, 57, 1) lies on line \ell_5
                                                                     703: P_{247042} = (1, 19, 59, 1) lies on line \ell_{11}
                                                                     704 : P_{248450} = (1, 41, 59, 1) lies on line \ell_{10}
655: P_{239013} = (36, 21, 57, 1) lies on line \ell_5
656: P_{239055} = (14, 22, 57, 1) lies on line \ell_5
                                                                     705: P_{249425} = (16, 56, 59, 1) lies on line \ell_7
657: P_{239160} = (55, 23, 57, 1) lies on line \ell_5
                                                                     706: P_{249516} = (43, 57, 59, 1) lies on line \ell_8
                                                                     707 : P_{249538} = (1, 58, 59, 1) lies on line \ell_9
658: P_{239191} = (22, 24, 57, 1) lies on line \ell_5
659 : P_{239280} = (47, 25, 57, 1) lies on line \ell_5
                                                                     708: P_{250045} = (60, 1, 60, 1) lies on line \ell_6
660: P_{239302} = (5, 26, 57, 1) lies on line \ell_5
                                                                     709: P_{251906} = (1, 31, 60, 1) lies on line \ell_{11}
661: P_{239421} = (60, 27, 57, 1) lies on line \ell_5
                                                                     710: P_{252098} = (1, 34, 60, 1) lies on line \ell_{10}
662: P_{239473} = (48, 28, 57, 1) lies on line \ell_5
                                                                     711: P_{253532} = (27, 56, 60, 1) lies on line \ell_7
663: P_{239498} = (9, 29, 57, 1) lies on line \ell_5
                                                                    712: P_{253608} = (39, 57, 60, 1) lies on line \ell_8
664 : P_{239588} = (35, 30, 57, 1) lies on line \ell_5
                                                                     713: P_{253826} = (1, 61, 60, 1) lies on line \ell_9
665: P_{239643} = (26, 31, 57, 1) lies on line \ell_5
                                                                     714: P_{254142} = (61, 1, 61, 1) lies on line \ell_6
666: P_{239704} = (23, 32, 57, 1) lies on line \ell_5
                                                                     715: P_{255682} = (1, 26, 61, 1) lies on line \ell_{10}
667: P_{239791} = (46, 33, 57, 1) lies on line \ell_5
                                                                    716: P_{256450} = (1, 38, 61, 1) lies on line \ell_{11}
668: P_{239813} = (4, 34, 57, 1) lies on line \ell_5
                                                                     717: P_{257636} = (35, 56, 61, 1) lies on line \ell_7
669 : P_{239934} = (61, 35, 57, 1) lies on line \ell_5
                                                                     718: P_{257695} = (30, 57, 61, 1) lies on line \ell_8
670: P_{239986} = (49, 36, 57, 1) lies on line \ell_5
                                                                     719: P_{257858} = (1, 60, 61, 1) lies on line \ell_9
671 : P_{240009} = (8, 37, 57, 1) lies on line \ell_5
                                                                    720: P_{258239} = (62, 1, 62, 1) lies on line \ell_6
672: P_{240099} = (34, 38, 57, 1) lies on line \ell_5
                                                                     721: P_{258882} = (1, 12, 62, 1) lies on line \ell_{11}
673: P_{240156} = (27, 39, 57, 1) lies on line \ell_5
                                                                     722 : P_{261378} = (1, 51, 62, 1) lies on line \ell_{10}
674: P_{240251} = (58, 40, 57, 1) lies on line \ell_5
                                                                     723: P_{261707} = (10, 56, 62, 1) lies on line \ell_7
675 : P_{240260} = (3, 41, 57, 1) lies on line \ell_5
                                                                     724 : P_{261813} = (52, 57, 62, 1) lies on line \ell_8
676 : P_{240362} = (41, 42, 57, 1) lies on line \ell_5
                                                                     725: P_{262146} = (1, 63, 62, 1) lies on line \ell_9
677: P_{240401} = (16, 43, 57, 1) lies on line \ell_5
                                                                     726: P_{262336} = (63, 1, 63, 1) lies on line \ell_6
678: P_{240477} = (28, 44, 57, 1) lies on line \ell_5
                                                                    727: P_{262914} = (1, 11, 63, 1) lies on line \ell_{10}
679: P_{240550} = (37, 45, 57, 1) lies on line \ell_5
                                                                     728: P_{265602} = (1, 53, 63, 1) lies on line \ell_{11}
680: P_{240592} = (15, 46, 57, 1) lies on line \ell_5
                                                                     729: P_{265843} = (50, 56, 63, 1) lies on line \ell_7
681 : P_{240695} = (54, 47, 57, 1) lies on line \ell_5
                                                                     730: P_{265870} = (13, 57, 63, 1) lies on line \ell_8
682: P_{240749} = (44, 48, 57, 1) lies on line \ell_5
                                                                    731: P_{266178} = (1, 62, 63, 1) lies on line \ell_9
683: P_{240790} = (21, 49, 57, 1) lies on line \ell_5
684: P_{240896} = (63, 50, 57, 1) lies on line \ell_5
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The single points on the surface are:

Points on surface but on no line

The surface has 3600 points not on any line: Too many to print.

Line Intersection Graph

	0123456789	10	11
0	0111001001	0	0
1	1010100010	1	0
2	1100010100	0	1
3	1000001110	1	1
4	0100001111	0	1
5	0010001111	1	0
6	1001110000	1	1
7	0011110001	1	0
8	0101110001	0	1
9	1000110110	1	1
10	0101011101	0	1
11	0011101011	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_6	ℓ_9
in point	P_{3771}	P_{3708}	P_5	P_{68}	P_{131}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_4	ℓ_8	ℓ_{10}
in point	P_{3771}	P_{132}	P_{60}	P_{124}	P_{3651}

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_5	ℓ_7	ℓ_{11}
in point	P_{3708}	P_{132}	P_{61}	P_{123}	P_{3715}

Line 3 intersects

Line	ℓ_0	ℓ_6	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}
in point	P_5	P_4	P_{11897}	P_{11962}	P_4	P_4

 ${\bf Line~4~intersects}$

Line	ℓ_1	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{11}
in point	P_{60}	P_{233657}	P_{237178}	P_{237186}	P_{237186}	P_{237186}

 ${\bf Line~5~intersects}$

Line	ℓ_2	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}
in point	P_{61}	P_{237754}	P_{241218}	P_{241337}	P_{241218}	P_{241218}

 $Line\ 6\ intersects$

Line	ℓ_0	ℓ_3	ℓ_4	ℓ_5	ℓ_{10}	ℓ_{11}
in point	P_{68}	P_4	P_{233657}	P_{237754}	P_4	P_4

Line 7 intersects

Line	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_9	ℓ_{10}
in point	P_{123}	P_{11897}	P_{237178}	P_{241218}	P_{241218}	P_{241218}

Line 8 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_9	ℓ_{11}
in point	P_{124}	P_{11962}	P_{237186}	P_{241337}	P_{237186}	P_{237186}

Line 9 intersects

Line	ℓ_0	ℓ_4	ℓ_5	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}
in point	P_{131}	P_{237186}	P_{241218}	P_{241218}	P_{237186}	P_{241218}	P_{237186}

Line 10 intersects

Line	ℓ_1	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_9	ℓ_{11}
in point	P_{3651}	P_4	P_{241218}	P_4	P_{241218}	P_{241218}	P_4

 ${\bf Line~11~intersects}$

Line	ℓ_2	ℓ_3	ℓ_4	ℓ_6	ℓ_8	ℓ_9	ℓ_{10}
in point	P_{3715}	P_4	P_{237186}	P_4	P_{237186}	P_{237186}	P_4

The surface has 4353 points:

Too many to print.