Rank-65613 over GF(16)

January 15, 2021

The equation

The equation of the surface is:

$$X_1^3 + X_3^3 + X_0^2 X_3 + X_0 X_1 X_2 = 0$$

(0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over GF(16) is 303112485

General information

Number of lines	11
Number of points	321
Number of singular points	2
Number of Eckardt points	0
Number of double points	15
Number of single points	148
Number of points off lines	156
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17 ¹¹
Type of lines on points	$5, 4, 2^{15}, 1^{148}, 0^{156}$

Singular Points

The surface has 2 singular points:

$$\begin{aligned} 0: \ P_2 &= \mathbf{P}(0,0,1,0) = \mathbf{P}(0,0,1,0) \\ 1: \ P_{275} &= \mathbf{P}(1,0,0,1) = \mathbf{P}(1,0,0,1) \end{aligned}$$

The 11 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{256} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{256} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2$$

$$\ell_{1} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4624} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4624} = \mathbf{Pl}(0,1,1,0,0,0)_{18}$$

$$\ell_{2} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69905} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69905} = \mathbf{Pl}(0,1,0,0,0,1)_{4641}$$

$$\ell_{3} = \begin{bmatrix} 0 & 1 & 0 & \delta^{5} \\ 0 & 0 & 1 & 0 \end{bmatrix}_{70075} = \begin{bmatrix} 0 & 1 & 0 & 11 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{70075} = \mathbf{Pl}(0,11,0,0,0,1)_{4651}$$

$$\ell_{4} = \begin{bmatrix} 0 & 1 & 0 & \delta^{10} \\ 0 & 0 & 1 & 0 \end{bmatrix}_{70058} = \begin{bmatrix} 0 & 1 & 0 & 10 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{70058} = \mathbf{Pl}(0,10,0,0,0,1)_{4650}$$

$$\ell_{5} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{289} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{289} = \mathbf{Pl}(1,1,0,0,1,1)_{8961}$$

$$\ell_{6} = \begin{bmatrix} 1 & 0 & \delta^{5} & 0 \\ 0 & 1 & 0 & \delta^{5} \end{bmatrix}_{3179} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 0 & 11 \end{bmatrix}_{3179} = \mathbf{Pl}(10,11,0,0,1,1)_{8970}$$

$$\ell_{7} = \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 1 & 0 & \delta^{10} \end{bmatrix}_{2890} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 0 & 10 \end{bmatrix}_{2890} = \mathbf{Pl}(11,10,0,0,1,1)_{8971}$$

$$\ell_{8} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}_{4385} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{4385} = \mathbf{Pl}(11,10,10,11,1,0)_{3645}$$

$$\ell_{10} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \delta^{10} & \delta^{5} \end{bmatrix}_{4539} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 10 & 11 \end{bmatrix}_{4554} = \mathbf{Pl}(10,11,11,10,1,0)_{3434}$$

Rank of lines: (256, 4624, 69905, 70075, 70058, 289, 3179, 2890, 4385, 4539, 4554)
Rank of points on Klein quadric: (2, 18, 4641, 4651, 4650, 8961, 8970, 8971, 1250, 3645, 3434)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 15 Double points: The double points on the surface are:

$$\begin{split} P_{20} &= (1,0,1,0) = \ell_0 \cap \ell_5 \\ P_{29} &= (10,0,1,0) = \ell_0 \cap \ell_6 \\ P_{30} &= (11,0,1,0) = \ell_0 \cap \ell_7 \\ P_{290} &= (0,1,0,1) = \ell_2 \cap \ell_5 \\ P_{546} &= (0,1,1,1) = \ell_2 \cap \ell_8 \\ P_{434} &= (0,10,0,1) = \ell_3 \cap \ell_6 \\ P_{3249} &= (0,10,11,1) = \ell_3 \cap \ell_{10} \\ P_{450} &= (0,11,0,1) = \ell_4 \cap \ell_7 \end{split}$$

$$\begin{split} P_{3009} &= (0,11,10,1) = \ell_4 \cap \ell_9 \\ P_{3116} &= (11,1,11,1) = \ell_5 \cap \ell_9 \\ P_{2859} &= (10,1,10,1) = \ell_5 \cap \ell_{10} \\ P_{3004} &= (11,10,10,1) = \ell_6 \cap \ell_8 \\ P_{699} &= (10,10,1,1) = \ell_6 \cap \ell_9 \\ P_{3275} &= (10,11,11,1) = \ell_7 \cap \ell_8 \\ P_{716} &= (11,11,1,1) = \ell_7 \cap \ell_{10} \end{split}$$

Single Points

The surface has 148 single points: The single points on the surface are:

```
54: P_{1710} = (13, 9, 5, 1) lies on line \ell_9
0: P_0 = (1,0,0,0) lies on line \ell_0
1: P_4 = (1, 1, 1, 1) lies on line \ell_5
                                                                      55: P_{1713} = (0, 10, 5, 1) lies on line \ell_3
                                                                      56: P_{1722} = (9, 10, 5, 1) lies on line \ell_6
2: P_{21} = (2,0,1,0) lies on line \ell_0
3: P_{22} = (3,0,1,0) lies on line \ell_0
                                                                      57: P_{1729} = (0, 11, 5, 1) lies on line \ell_4
4: P_{23} = (4,0,1,0) lies on line \ell_0
                                                                      58: P_{1741} = (12, 11, 5, 1) lies on line \ell_7
5: P_{24} = (5,0,1,0) lies on line \ell_0
                                                                      59: P_{1753} = (8, 12, 5, 1) lies on line \ell_{10}
6: P_{25} = (6,0,1,0) lies on line \ell_0
                                                                      60: P_{1810} = (1, 0, 6, 1) lies on line \ell_1
7: P_{26} = (7,0,1,0) lies on line \ell_0
                                                                      61: P_{1825} = (0, 1, 6, 1) lies on line \ell_2
8: P_{27} = (8,0,1,0) lies on line \ell_0
                                                                      62: P_{1831} = (6, 1, 6, 1) lies on line \ell_5
9: P_{28} = (9,0,1,0) lies on line \ell_0
                                                                      63: P_{1912} = (7, 6, 6, 1) lies on line \ell_8
10: P_{31} = (12, 0, 1, 0) lies on line \ell_0
                                                                      64: P_{1952} = (15, 8, 6, 1) lies on line \ell_{10}
                                                                      65: P_{1969} = (0, 10, 6, 1) lies on line \ell_3
11: P_{32} = (13, 0, 1, 0) lies on line \ell_0
12: P_{33} = (14, 0, 1, 0) lies on line \ell_0
                                                                      66: P_{1983} = (14, 10, 6, 1) lies on line \ell_6
13: P_{34} = (15, 0, 1, 0) lies on line \ell_0
                                                                      67: P_{1985} = (0, 11, 6, 1) lies on line \ell_4
14: P_{36} = (1, 1, 1, 0) lies on line \ell_8
                                                                      68: P_{1993} = (8, 11, 6, 1) lies on line \ell_7
15: P_{190} = (11, 10, 1, 0) lies on line \ell_9
                                                                      69: P_{2042} = (9, 14, 6, 1) lies on line \ell_9
16: P_{205} = (10, 11, 1, 0) lies on line \ell_{10}
                                                                      70: P_{2066} = (1, 0, 7, 1) lies on line \ell_1
17: P_{531} = (1, 0, 1, 1) lies on line \ell_1
                                                                      71: P_{2081} = (0, 1, 7, 1) lies on line \ell_2
                                                                      72 : P_{2088} = (7, 1, 7, 1) lies on line \ell_5
18: P_{689} = (0, 10, 1, 1) lies on line \ell_3
19: P_{705} = (0, 11, 1, 1) lies on line \ell_4
                                                                      73: P_{2118} = (5, 3, 7, 1) lies on line \ell_{10}
20: P_{786} = (1, 0, 2, 1) lies on line \ell_1
                                                                      74: P_{2131} = (2, 4, 7, 1) lies on line \ell_9
21: P_{801} = (0, 1, 2, 1) lies on line \ell_2
                                                                      75: P_{2183} = (6,7,7,1) lies on line \ell_8
22: P_{803} = (2, 1, 2, 1) lies on line \ell_5
                                                                      76: P_{2225} = (0, 10, 7, 1) lies on line \ell_3
                                                                      77 : P_{2229} = (4, 10, 7, 1) lies on line \ell_6
23: P_{820} = (3, 2, 2, 1) lies on line \ell_8
24: P_{945} = (0, 10, 2, 1) lies on line \ell_3
                                                                      78: P_{2241} = (0, 11, 7, 1) lies on line \ell_4
25: P_{958} = (13, 10, 2, 1) lies on line \ell_6
                                                                      79: P_{2244} = (3, 11, 7, 1) lies on line \ell_7
26: P_{961} = (0, 11, 2, 1) lies on line \ell_4
                                                                      80: P_{2322} = (1,0,8,1) lies on line \ell_1
27: P_{976} = (15, 11, 2, 1) lies on line \ell_7
                                                                      81: P_{2337} = (0, 1, 8, 1) lies on line \ell_2
28: P_{1007} = (14, 13, 2, 1) lies on line \ell_9
                                                                      82: P_{2345} = (8, 1, 8, 1) lies on line \ell_5
29: P_{1037} = (12, 15, 2, 1) lies on line \ell_{10}
                                                                      83: P_{2432} = (15, 6, 8, 1) lies on line \ell_9
30: P_{1042} = (1,0,3,1) lies on line \ell_1
                                                                      84: P_{2458} = (9, 8, 8, 1) lies on line \ell_8
31: P_{1057} = (0, 1, 3, 1) lies on line \ell_2
                                                                      85: P_{2481} = (0, 10, 8, 1) lies on line \ell_3
32: P_{1060} = (3, 1, 3, 1) lies on line \ell_5
                                                                      86: P_{2487} = (6, 10, 8, 1) lies on line \ell_6
33: P_{1091} = (2, 3, 3, 1) lies on line \ell_8
                                                                      87: P_{2497} = (0, 11, 8, 1) lies on line \ell_4
34: P_{1111} = (6, 4, 3, 1) lies on line \ell_{10}
                                                                      88: P_{2511} = (14, 11, 8, 1) lies on line \ell_7
                                                                      89 : P_{2552} = (7, 14, 8, 1) lies on line \ell_{10}
35: P_{1158} = (5,7,3,1) lies on line \ell_9
36: P_{1201} = (0, 10, 3, 1) lies on line \ell_3
                                                                      90: P_{2578} = (1,0,9,1) lies on line \ell_1
37: P_{1208} = (7, 10, 3, 1) lies on line \ell_6
                                                                      91: P_{2593} = (0, 1, 9, 1) lies on line \ell_2
                                                                      92 : P_{2602} = (9, 1, 9, 1) lies on line \ell_5
38: P_{1217} = (0, 11, 3, 1) lies on line \ell_4
                                                                      93: P_{2670} = (13, 5, 9, 1) lies on line \ell_{10}
39: P_{1221} = (4,11,3,1) lies on line \ell_7
                                                                      94: P_{2729} = (8, 9, 9, 1) lies on line \ell_8
40: P_{1298} = (1,0,4,1) lies on line \ell_1
41: P_{1313} = (0, 1, 4, 1) lies on line \ell_2
                                                                      95: P_{2737} = (0, 10, 9, 1) lies on line \ell_3
                                                                      96 : P_{2749} = (12, 10, 9, 1) lies on line \ell_6
42: P_{1317} = (4, 1, 4, 1) lies on line \ell_5
43: P_{1351} = (6, 3, 4, 1) lies on line \ell_9
                                                                      97: P_{2753} = (0, 11, 9, 1) lies on line \ell_4
44: P_{1366} = (5, 4, 4, 1) lies on line \ell_8
                                                                      98: P_{2758} = (5, 11, 9, 1) lies on line \ell_7
45: P_{1411} = (2, 7, 4, 1) lies on line \ell_{10}
                                                                      99: P_{2773} = (4, 12, 9, 1) lies on line \ell_9
46: P_{1457} = (0, 10, 4, 1) lies on line \ell_3
                                                                      100: P_{2834} = (1, 0, 10, 1) lies on line \ell_1
47: P_{1460} = (3, 10, 4, 1) lies on line \ell_6
                                                                      101: P_{2849} = (0, 1, 10, 1) lies on line \ell_2
48: P_{1473} = (0, 11, 4, 1) lies on line \ell_4
                                                                      102: P_{2993} = (0, 10, 10, 1) lies on line \ell_3
49: P_{1480} = (7, 11, 4, 1) lies on line \ell_7
                                                                      103: P_{3010} = (1, 11, 10, 1) lies on line \ell_7
50: P_{1554} = (1,0,5,1) lies on line \ell_1
                                                                      104: P_{3090} = (1, 0, 11, 1) lies on line \ell_1
51: P_{1569} = (0, 1, 5, 1) lies on line \ell_2
                                                                      105: P_{3105} = (0, 1, 11, 1) lies on line \ell_2
                                                                      106 : P_{3250} = (1, 10, 11, 1) lies on line \ell_6
52: P_{1574} = (5, 1, 5, 1) lies on line \ell_5
53: P_{1637} = (4, 5, 5, 1) lies on line \ell_8
                                                                      107: P_{3265} = (0, 11, 11, 1) lies on line \ell_4
```

```
108: P_{3346} = (1, 0, 12, 1) lies on line \ell_1
                                                                     129: P_{3873} = (0, 1, 14, 1) lies on line \ell_2
109 : P_{3361} = (0, 1, 12, 1) lies on line \ell_2
                                                                     130: P_{3887} = (14, 1, 14, 1) lies on line \ell_5
110: P_{3373} = (12, 1, 12, 1) lies on line \ell_5
                                                                     131: P_{3962} = (9, 6, 14, 1) lies on line \ell_{10}
111: P_{3433} = (8, 5, 12, 1) lies on line \ell_9
                                                                     132: P_{3992} = (7, 8, 14, 1) lies on line \ell_9
112: P_{3493} = (4, 9, 12, 1) lies on line \ell_{10}
                                                                     133 : P_{4017} = (0, 10, 14, 1) lies on line \ell_3
113: P_{3505} = (0, 10, 12, 1) lies on line \ell_3
                                                                     134: P_{4025} = (8, 10, 14, 1) lies on line \ell_6
114: P_{3510} = (5, 10, 12, 1) lies on line \ell_6
                                                                     135: P_{4033} = (0, 11, 14, 1) lies on line \ell_4
115: P_{3521} = (0, 11, 12, 1) lies on line \ell_4
                                                                     136: P_{4039} = (6, 11, 14, 1) lies on line \ell_7
116: P_{3530} = (9, 11, 12, 1) lies on line \ell_7
                                                                     137: P_{4096} = (15, 14, 14, 1) lies on line \ell_8
117: P_{3550} = (13, 12, 12, 1) lies on line \ell_8
                                                                     138: P_{4114} = (1, 0, 15, 1) lies on line \ell_1
118: P_{3602} = (1, 0, 13, 1) lies on line \ell_1
                                                                     139: P_{4129} = (0, 1, 15, 1) lies on line \ell_2
119: P_{3617} = (0, 1, 13, 1) lies on line \ell_2
                                                                     140: P_{4144} = (15, 1, 15, 1) lies on line \ell_5
120: P_{3630} = (13, 1, 13, 1) lies on line \ell_5
                                                                     141: P_{4157} = (12, 2, 15, 1) lies on line \ell_9
121: P_{3647} = (14, 2, 13, 1) lies on line \ell_{10}
                                                                     142: P_{4273} = (0, 10, 15, 1) lies on line \ell_3
122: P_{3761} = (0, 10, 13, 1) lies on line \ell_3
                                                                     143: P_{4275} = (2, 10, 15, 1) lies on line \ell_6
123: P_{3776} = (15, 10, 13, 1) lies on line \ell_6
                                                                     144: P_{4289} = (0, 11, 15, 1) lies on line \ell_4
124: P_{3777} = (0, 11, 13, 1) lies on line \ell_4
                                                                     145: P_{4302} = (13, 11, 15, 1) lies on line \ell_7
125: P_{3779} = (2, 11, 13, 1) lies on line \ell_7
                                                                     146: P_{4324} = (3, 13, 15, 1) lies on line \ell_{10}
126: P_{3821} = (12, 13, 13, 1) lies on line \ell_8
                                                                     147: P_{4367} = (14, 15, 15, 1) lies on line \ell_8
127: P_{3844} = (3, 15, 13, 1) lies on line \ell_9
128: P_{3858} = (1, 0, 14, 1) lies on line \ell_1
```

The single points on the surface are:

Points on surface but on no line

The surface has 156 points not on any line: The points on the surface but not on lines are:

```
0: P_{55} = (4, 2, 1, 0)
                                                                  23: P_{518} = (4, 15, 0, 1)
1: P_{72} = (5, 3, 1, 0)
                                                                  24: P_{585} = (8, 3, 1, 1)
2: P_{92} = (9, 4, 1, 0)
                                                                  25: P_{588} = (11, 3, 1, 1)
3: P_{107} = (8, 5, 1, 0)
                                                                  26: P_{619} = (10, 5, 1, 1)
                                                                  27: P_{624} = (15, 5, 1, 1)
4: P_{128} = (13, 6, 1, 0)
5: P_{143} = (12, 7, 1, 0)
                                                                  28: P_{660} = (3, 8, 1, 1)
6: P_{162} = (15, 8, 1, 0)
                                                                  29: P_{668} = (11, 8, 1, 1)
7: P_{177} = (14, 9, 1, 0)
                                                                  30: P_{774} = (5, 15, 1, 1)
                                                                  31: P_{779} = (10, 15, 1, 1)
8: P_{217} = (6, 12, 1, 0)
9: P_{234} = (7, 13, 1, 0)
                                                                  32: P_{824} = (7, 2, 2, 1)
10: P_{245} = (2, 14, 1, 0)
                                                                  33: P_{868} = (3, 5, 2, 1)
                                                                  34: P_{874} = (9, 5, 2, 1)
11: P_{262} = (3, 15, 1, 0)
12: P_{310} = (4, 2, 0, 1)
                                                                  35: P_{900} = (3,7,2,1)
13: P_{331} = (9, 3, 0, 1)
                                                                  36: P_{910} = (13, 7, 2, 1)
14: P_{347} = (9, 4, 0, 1)
                                                                  37: P_{1006} = (13, 13, 2, 1)
15: P_{368} = (14, 5, 0, 1)
                                                                  38: P_{1010} = (1, 14, 2, 1)
16: P_{372} = (2, 6, 0, 1)
                                                                  39: P_{1013} = (4, 14, 2, 1)
17: P_{395} = (9, 7, 0, 1)
                                                                  40: P_{1036} = (11, 15, 2, 1)
18: P_{404} = (2, 8, 0, 1)
                                                                  41: P_{1096} = (7, 3, 3, 1)
19: P_{432} = (14, 9, 0, 1)
                                                                  42: P_{1115} = (10, 4, 3, 1)
20: P_{480} = (14, 12, 0, 1)
                                                                  43: P_{1165} = (12, 7, 3, 1)
21: P_{486} = (4, 13, 0, 1)
                                                                  44: P_{1190} = (5, 9, 3, 1)
22: P_{500} = (2, 14, 0, 1)
                                                                  45: P_{1192} = (7, 9, 3, 1)
```

```
46: P_{1270} = (5, 14, 3, 1)
                                                                 100: P_{2727} = (6, 9, 9, 1)
                                                                 101: P_{2781} = (12, 12, 9, 1)
47: P_{1279} = (14, 14, 3, 1)
                                                                 102: P_{2819} = (2, 15, 9, 1)
48: P_{1282} = (1, 15, 3, 1)
                                                                 103: P_{2825} = (8, 15, 9, 1)
49: P_{1290} = (9, 15, 3, 1)
50: P_{1330} = (1, 2, 4, 1)
                                                                 104: P_{2905} = (8, 4, 10, 1)
51: P_{1338} = (9, 2, 4, 1)
                                                                 105: P_{2908} = (11, 4, 10, 1)
52: P_{1355} = (10, 3, 4, 1)
                                                                 106: P_{3035} = (10, 12, 10, 1)
53: P_{1373} = (12, 4, 4, 1)
                                                                 107: P_{3040} = (15, 12, 10, 1)
54: P_{1416} = (7,7,4,1)
                                                                 108: P_{3046} = (5, 13, 10, 1)
55: P_{1430} = (5, 8, 4, 1)
                                                                 109: P_{3051} = (10, 13, 10, 1)
56: P_{1439} = (14, 8, 4, 1)
                                                                 110: P_{3060} = (3, 14, 10, 1)
57: P_{1494} = (5, 12, 4, 1)
                                                                 111: P_{3068} = (11, 14, 10, 1)
58: P_{1496} = (7, 12, 4, 1)
                                                                 112: P_{3126} = (5, 2, 11, 1)
59: P_{1587} = (2, 2, 5, 1)
                                                                 113: P_{3131} = (10, 2, 11, 1)
60: P_{1593} = (8, 2, 5, 1)
                                                                 114: P_{3188} = (3, 6, 11, 1)
61: P_{1602} = (1, 3, 5, 1)
                                                                 115: P_{3196} = (11, 6, 11, 1)
62: P_{1615} = (14, 3, 5, 1)
                                                                 116: P_{3209} = (8, 7, 11, 1)
                                                                 117: P_{3212} = (11, 7, 11, 1)
63: P_{1645} = (12, 5, 5, 1)
                                                                 118: P_{3243} = (10, 9, 11, 1)
64: P_{1708} = (11, 9, 5, 1)
65: P_{1751} = (6, 12, 5, 1)
                                                                 119: P_{3248} = (15, 9, 11, 1)
66: P_{1785} = (8, 14, 5, 1)
                                                                 120: P_{3431} = (6, 5, 12, 1)
                                                                 121: P_{3458} = (1, 7, 12, 1)
67: P_{1789} = (12, 14, 5, 1)
                                                                 122: P_{3471} = (14, 7, 12, 1)
68: P_{1915} = (10, 6, 6, 1)
69: P_{1925} = (4,7,6,1)
                                                                 123: P_{3481} = (8, 8, 12, 1)
70: P_{1936} = (15, 7, 6, 1)
                                                                 124: P_{3485} = (12, 8, 12, 1)
71: P_{1950} = (13, 8, 6, 1)
                                                                 125: P_{3501} = (12, 9, 12, 1)
                                                                 126: P_{3548} = (11, 12, 12, 1)
72: P_{2002} = (1, 12, 6, 1)
73: P_{2003} = (2, 12, 6, 1)
                                                                 127: P_{3555} = (2, 13, 12, 1)
74: P_{2039} = (6, 14, 6, 1)
                                                                 128: P_{3561} = (8, 13, 12, 1)
75: P_{2055} = (6, 15, 6, 1)
                                                                 129: P_{3646} = (13, 2, 13, 1)
76: P_{2064} = (15, 15, 6, 1)
                                                                 130: P_{3652} = (3, 3, 13, 1)
77: P_{2125} = (12, 3, 7, 1)
                                                                 131: P_{3662} = (13, 3, 13, 1)
78: P_{2136} = (7, 4, 7, 1)
                                                                 132: P_{3698} = (1, 6, 13, 1)
79: P_{2150} = (5, 5, 7, 1)
                                                                 133: P_{3701} = (4, 6, 13, 1)
                                                                 134: P_{3796} = (3, 12, 13, 1)
80: P_{2152} = (7, 5, 7, 1)
                                                                 135: P_{3802} = (9, 12, 13, 1)
81: P_{2166} = (5, 6, 7, 1)
82: P_{2175} = (14, 6, 7, 1)
                                                                 136: P_{3820} = (11, 13, 13, 1)
83: P_{2187} = (10, 7, 7, 1)
                                                                 137: P_{3848} = (7, 15, 13, 1)
84: P_{2274} = (1, 13, 7, 1)
                                                                 138: P_{3909} = (4, 3, 14, 1)
85: P_{2282} = (9, 13, 7, 1)
                                                                 139: P_{3920} = (15, 3, 14, 1)
86: P_{2359} = (6, 2, 8, 1)
                                                                 140: P_{3959} = (6, 6, 14, 1)
87: P_{2368} = (15, 2, 8, 1)
                                                                 141: P_{3995} = (10, 8, 14, 1)
88: P_{2389} = (4, 4, 8, 1)
                                                                 142: P_{4002} = (1, 9, 14, 1)
                                                                 143: P_{4003} = (2, 9, 14, 1)
89: P_{2400} = (15, 4, 8, 1)
90: P_{2402} = (1, 5, 8, 1)
                                                                 144: P_{4071} = (6, 13, 14, 1)
91: P_{2403} = (2,5,8,1)
                                                                 145: P_{4080} = (15, 13, 14, 1)
92: P_{2430} = (13, 6, 8, 1)
                                                                 146: P_{4094} = (13, 14, 14, 1)
93: P_{2455} = (6, 8, 8, 1)
                                                                 147: P_{4156} = (11, 2, 15, 1)
94: P_{2555} = (10, 14, 8, 1)
                                                                 148: P_{4180} = (3, 4, 15, 1)
95: P_{2642} = (1, 4, 9, 1)
                                                                 149: P_{4190} = (13, 4, 15, 1)
96: P_{2655} = (14, 4, 9, 1)
                                                                 150: P_{4242} = (1, 8, 15, 1)
97: P_{2668} = (11, 5, 9, 1)
                                                                 151: P_{4245} = (4, 8, 15, 1)
98: P_{2681} = (8, 6, 9, 1)
                                                                 152: P_{4260} = (3, 9, 15, 1)
99: P_{2685} = (12, 6, 9, 1)
                                                                 153: P_{4266} = (9, 9, 15, 1)
```

```
\begin{array}{l} 154:\ P_{4328} = (7,13,15,1) \\ 155:\ P_{4366} = (13,15,15,1) \end{array}
```

Line Intersection Graph

	0123456789	10
0	0111111100	0
1	1011100011	1
2	1101110010	0
3	1110101000	1
4	1111000101	0
5	1010000001	1
	1001000011	0
7	1000100010	1
8	0110001101	1
9	0100111010	1
10	0101010111	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7
in point	P_2	P_2	P_2	P_2	P_{20}	P_{29}	P_{30}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_3	ℓ_4	ℓ_8	ℓ_9	ℓ_{10}	
in point	P_2	P_2	P_2	P_2	P_{275}	P_{275}	P_{275}	

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_8
in point	P_2	P_2	P_2	P_2	P_{290}	P_{546}

Line 3 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_4	ℓ_6	ℓ_{10}
in point	P_2	P_2	P_2	P_2	P_{434}	P_{3249}

Line 4 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_7	ℓ_9
in point	P_2	P_2	P_2	P_2	P_{450}	P_{3009}

 ${\bf Line~5~intersects}$

Line	ℓ_0	ℓ_2	ℓ_9	ℓ_{10}
in point	P_{20}	P_{290}	P_{3116}	P_{2859}

Line 6 intersects

Line	ℓ_0	ℓ_3	ℓ_8	ℓ_9
in point	P_{29}	P_{434}	P_{3004}	P_{699}

Line 7 intersects

Line	ℓ_0	ℓ_4	ℓ_8	ℓ_{10}
in point	P_{30}	P_{450}	P_{3275}	P_{716}

 ${\bf Line~8~intersects}$

Line	ℓ_1	ℓ_2	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}
in point	P_{275}	P_{546}	P_{3004}	P_{3275}	P_{275}	P_{275}

Line 9 intersects

Line	ℓ_1	ℓ_4	ℓ_5	ℓ_6	ℓ_8	ℓ_{10}
in point	P_{275}	P_{3009}	P_{3116}	P_{699}	P_{275}	P_{275}

Line 10 intersects

Line	ℓ_1	ℓ_3	ℓ_5	ℓ_7	ℓ_8	ℓ_9
in point	P_{275}	P_{3249}	P_{2859}	P_{716}	P_{275}	P_{275}

The surface has 321 points: The points on the surface are:

```
0: P_0 = (1,0,0,0)
                                            50: P_{546} = (0, 1, 1, 1)
                                                                                        100: P_{1290} = (9, 15, 3, 1)
                                            51: P_{585} = (8, 3, 1, 1)
1: P_2 = (0,0,1,0)
                                                                                        101: P_{1298} = (1,0,4,1)
                                                                                        102: P_{1313} = (0, 1, 4, 1)
2: P_4 = (1, 1, 1, 1)
                                            52: P_{588} = (11, 3, 1, 1)
                                                                                        103: P_{1317} = (4, 1, 4, 1)
3: P_{20} = (1,0,1,0)
                                            53: P_{619} = (10, 5, 1, 1)
4: P_{21} = (2,0,1,0)
                                            54: P_{624} = (15, 5, 1, 1)
                                                                                        104: P_{1330} = (1, 2, 4, 1)
5: P_{22} = (3,0,1,0)
                                            55: P_{660} = (3, 8, 1, 1)
                                                                                        105: P_{1338} = (9, 2, 4, 1)
6: P_{23} = (4,0,1,0)
                                            56: P_{668} = (11, 8, 1, 1)
                                                                                        106: P_{1351} = (6, 3, 4, 1)
                                            57: P_{689} = (0, 10, 1, 1)
7: P_{24} = (5, 0, 1, 0)
                                                                                        107: P_{1355} = (10, 3, 4, 1)
8: P_{25} = (6,0,1,0)
                                            58: P_{699} = (10, 10, 1, 1)
                                                                                        108: P_{1366} = (5, 4, 4, 1)
                                                                                        109: P_{1373} = (12, 4, 4, 1)
9: P_{26} = (7,0,1,0)
                                            59: P_{705} = (0, 11, 1, 1)
10: P_{27} = (8, 0, 1, 0)
                                            60: P_{716} = (11, 11, 1, 1)
                                                                                        110: P_{1411} = (2,7,4,1)
11: P_{28} = (9, 0, 1, 0)
                                            61: P_{774} = (5, 15, 1, 1)
                                                                                        111: P_{1416} = (7,7,4,1)
12: P_{29} = (10, 0, 1, 0)
                                            62: P_{779} = (10, 15, 1, 1)
                                                                                        112: P_{1430} = (5, 8, 4, 1)
13: P_{30} = (11, 0, 1, 0)
                                            63: P_{786} = (1, 0, 2, 1)
                                                                                        113: P_{1439} = (14, 8, 4, 1)
14: P_{31} = (12, 0, 1, 0)
                                            64: P_{801} = (0, 1, 2, 1)
                                                                                        114: P_{1457} = (0, 10, 4, 1)
15: P_{32} = (13, 0, 1, 0)
                                            65: P_{803} = (2, 1, 2, 1)
                                                                                        115: P_{1460} = (3, 10, 4, 1)
16: P_{33} = (14, 0, 1, 0)
                                            66: P_{820} = (3, 2, 2, 1)
                                                                                        116: P_{1473} = (0, 11, 4, 1)
17: P_{34} = (15, 0, 1, 0)
                                            67: P_{824} = (7, 2, 2, 1)
                                                                                        117: P_{1480} = (7, 11, 4, 1)
18: P_{36} = (1, 1, 1, 0)
                                            68: P_{868} = (3, 5, 2, 1)
                                                                                        118: P_{1494} = (5, 12, 4, 1)
19: P_{55} = (4, 2, 1, 0)
                                            69: P_{874} = (9, 5, 2, 1)
                                                                                        119: P_{1496} = (7, 12, 4, 1)
20: P_{72} = (5, 3, 1, 0)
                                            70: P_{900} = (3,7,2,1)
                                                                                        120: P_{1554} = (1,0,5,1)
21: P_{92} = (9, 4, 1, 0)
                                            71: P_{910} = (13, 7, 2, 1)
                                                                                        121: P_{1569} = (0, 1, 5, 1)
22: P_{107} = (8, 5, 1, 0)
                                            72: P_{945} = (0, 10, 2, 1)
                                                                                        122: P_{1574} = (5, 1, 5, 1)
23: P_{128} = (13, 6, 1, 0)
                                            73: P_{958} = (13, 10, 2, 1)
                                                                                        123: P_{1587} = (2, 2, 5, 1)
                                            74: P_{961} = (0, 11, 2, 1)
                                                                                        124: P_{1593} = (8, 2, 5, 1)
24: P_{143} = (12, 7, 1, 0)
25: P_{162} = (15, 8, 1, 0)
                                            75: P_{976} = (15, 11, 2, 1)
                                                                                        125: P_{1602} = (1, 3, 5, 1)
26: P_{177} = (14, 9, 1, 0)
                                            76: P_{1006} = (13, 13, 2, 1)
                                                                                        126: P_{1615} = (14, 3, 5, 1)
27: P_{190} = (11, 10, 1, 0)
                                            77: P_{1007} = (14, 13, 2, 1)
                                                                                        127: P_{1637} = (4, 5, 5, 1)
28: P_{205} = (10, 11, 1, 0)
                                            78: P_{1010} = (1, 14, 2, 1)
                                                                                        128: P_{1645} = (12, 5, 5, 1)
                                                                                        129: P_{1708} = (11, 9, 5, 1)
29: P_{217} = (6, 12, 1, 0)
                                            79: P_{1013} = (4, 14, 2, 1)
30: P_{234} = (7, 13, 1, 0)
                                            80: P_{1036} = (11, 15, 2, 1)
                                                                                        130: P_{1710} = (13, 9, 5, 1)
31: P_{245} = (2, 14, 1, 0)
                                            81: P_{1037} = (12, 15, 2, 1)
                                                                                        131: P_{1713} = (0, 10, 5, 1)
32: P_{262} = (3, 15, 1, 0)
                                            82: P_{1042} = (1, 0, 3, 1)
                                                                                        132: P_{1722} = (9, 10, 5, 1)
33: P_{275} = (1,0,0,1)
                                            83: P_{1057} = (0, 1, 3, 1)
                                                                                        133: P_{1729} = (0, 11, 5, 1)
34: P_{290} = (0, 1, 0, 1)
                                                                                        134: P_{1741} = (12, 11, 5, 1)
                                            84: P_{1060} = (3, 1, 3, 1)
                                                                                        135: P_{1751} = (6, 12, 5, 1)
35: P_{310} = (4, 2, 0, 1)
                                            85: P_{1091} = (2, 3, 3, 1)
36: P_{331} = (9, 3, 0, 1)
                                            86: P_{1096} = (7, 3, 3, 1)
                                                                                        136: P_{1753} = (8, 12, 5, 1)
37: P_{347} = (9,4,0,1)
                                            87: P_{1111} = (6, 4, 3, 1)
                                                                                        137: P_{1785} = (8, 14, 5, 1)
38: P_{368} = (14, 5, 0, 1)
                                            88: P_{1115} = (10, 4, 3, 1)
                                                                                        138: P_{1789} = (12, 14, 5, 1)
                                            89: P_{1158} = (5,7,3,1)
                                                                                        139: P_{1810} = (1, 0, 6, 1)
39: P_{372} = (2, 6, 0, 1)
40: P_{395} = (9, 7, 0, 1)
                                            90: P_{1165} = (12, 7, 3, 1)
                                                                                        140: P_{1825} = (0, 1, 6, 1)
41: P_{404} = (2, 8, 0, 1)
                                            91: P_{1190} = (5, 9, 3, 1)
                                                                                        141: P_{1831} = (6, 1, 6, 1)
42: P_{432} = (14, 9, 0, 1)
                                            92: P_{1192} = (7, 9, 3, 1)
                                                                                        142: P_{1912} = (7, 6, 6, 1)
43: P_{434} = (0, 10, 0, 1)
                                            93: P_{1201} = (0, 10, 3, 1)
                                                                                        143: P_{1915} = (10, 6, 6, 1)
44: P_{450} = (0, 11, 0, 1)
                                            94: P_{1208} = (7, 10, 3, 1)
                                                                                        144: P_{1925} = (4, 7, 6, 1)
45: P_{480} = (14, 12, 0, 1)
                                            95: P_{1217} = (0, 11, 3, 1)
                                                                                        145: P_{1936} = (15, 7, 6, 1)
46: P_{486} = (4, 13, 0, 1)
                                            96: P_{1221} = (4, 11, 3, 1)
                                                                                        146: P_{1950} = (13, 8, 6, 1)
47: P_{500} = (2, 14, 0, 1)
                                            97: P_{1270} = (5, 14, 3, 1)
                                                                                        147: P_{1952} = (15, 8, 6, 1)
                                            98: P_{1279} = (14, 14, 3, 1)
48: P_{518} = (4, 15, 0, 1)
                                                                                        148: P_{1969} = (0, 10, 6, 1)
49: P_{531} = (1, 0, 1, 1)
                                            99: P_{1282} = (1, 15, 3, 1)
                                                                                        149: P_{1983} = (14, 10, 6, 1)
```

```
150: P_{1985} = (0, 11, 6, 1)
                                                                                       258: P_{3521} = (0, 11, 12, 1)
                                           204: P_{2685} = (12, 6, 9, 1)
                                                                                       259: P_{3530} = (9, 11, 12, 1)
151: P_{1993} = (8, 11, 6, 1)
                                           205: P_{2727} = (6, 9, 9, 1)
                                                                                       260: P_{3548} = (11, 12, 12, 1)
152: P_{2002} = (1, 12, 6, 1)
                                           206: P_{2729} = (8, 9, 9, 1)
                                           207: P_{2737} = (0, 10, 9, 1)
                                                                                       261: P_{3550} = (13, 12, 12, 1)
153: P_{2003} = (2, 12, 6, 1)
154: P_{2039} = (6, 14, 6, 1)
                                           208: P_{2749} = (12, 10, 9, 1)
                                                                                      262: P_{3555} = (2, 13, 12, 1)
155: P_{2042} = (9, 14, 6, 1)
                                           209: P_{2753} = (0, 11, 9, 1)
                                                                                      263: P_{3561} = (8, 13, 12, 1)
156: P_{2055} = (6, 15, 6, 1)
                                           210: P_{2758} = (5, 11, 9, 1)
                                                                                      264: P_{3602} = (1, 0, 13, 1)
157: P_{2064} = (15, 15, 6, 1)
                                           211: P_{2773} = (4, 12, 9, 1)
                                                                                       265: P_{3617} = (0, 1, 13, 1)
158: P_{2066} = (1, 0, 7, 1)
                                           212: P_{2781} = (12, 12, 9, 1)
                                                                                      266: P_{3630} = (13, 1, 13, 1)
159: P_{2081} = (0, 1, 7, 1)
                                           213: P_{2819} = (2, 15, 9, 1)
                                                                                       267: P_{3646} = (13, 2, 13, 1)
160: P_{2088} = (7, 1, 7, 1)
                                           214: P_{2825} = (8, 15, 9, 1)
                                                                                       268: P_{3647} = (14, 2, 13, 1)
161: P_{2118} = (5, 3, 7, 1)
                                           215: P_{2834} = (1, 0, 10, 1)
                                                                                       269: P_{3652} = (3, 3, 13, 1)
162: P_{2125} = (12, 3, 7, 1)
                                           216: P_{2849} = (0, 1, 10, 1)
                                                                                       270: P_{3662} = (13, 3, 13, 1)
163: P_{2131} = (2,4,7,1)
                                           217: P_{2859} = (10, 1, 10, 1)
                                                                                       271: P_{3698} = (1, 6, 13, 1)
                                                                                       272: P_{3701} = (4, 6, 13, 1)
164: P_{2136} = (7, 4, 7, 1)
                                           218: P_{2905} = (8, 4, 10, 1)
165: P_{2150} = (5, 5, 7, 1)
                                           219: P_{2908} = (11, 4, 10, 1)
                                                                                       273: P_{3761} = (0, 10, 13, 1)
                                           220: P_{2993} = (0, 10, 10, 1)
                                                                                       274: P_{3776} = (15, 10, 13, 1)
166: P_{2152} = (7, 5, 7, 1)
167: P_{2166} = (5, 6, 7, 1)
                                                                                       275: P_{3777} = (0, 11, 13, 1)
                                           221: P_{3004} = (11, 10, 10, 1)
168: P_{2175} = (14, 6, 7, 1)
                                                                                       276: P_{3779} = (2, 11, 13, 1)
                                           222: P_{3009} = (0, 11, 10, 1)
169: P_{2183} = (6,7,7,1)
                                           223: P_{3010} = (1, 11, 10, 1)
                                                                                       277: P_{3796} = (3, 12, 13, 1)
170: P_{2187} = (10, 7, 7, 1)
                                           224: P_{3035} = (10, 12, 10, 1)
                                                                                       278: P_{3802} = (9, 12, 13, 1)
171: P_{2225} = (0, 10, 7, 1)
                                           225: P_{3040} = (15, 12, 10, 1)
                                                                                       279: P_{3820} = (11, 13, 13, 1)
172: P_{2229} = (4, 10, 7, 1)
                                           226: P_{3046} = (5, 13, 10, 1)
                                                                                       280: P_{3821} = (12, 13, 13, 1)
173: P_{2241} = (0, 11, 7, 1)
                                           227: P_{3051} = (10, 13, 10, 1)
                                                                                      281: P_{3844} = (3, 15, 13, 1)
174: P_{2244} = (3, 11, 7, 1)
                                           228: P_{3060} = (3, 14, 10, 1)
                                                                                       282: P_{3848} = (7, 15, 13, 1)
175: P_{2274} = (1, 13, 7, 1)
                                           229: P_{3068} = (11, 14, 10, 1)
                                                                                       283: P_{3858} = (1, 0, 14, 1)
176: P_{2282} = (9, 13, 7, 1)
                                           230: P_{3090} = (1, 0, 11, 1)
                                                                                       284: P_{3873} = (0, 1, 14, 1)
177: P_{2322} = (1,0,8,1)
                                           231: P_{3105} = (0, 1, 11, 1)
                                                                                       285: P_{3887} = (14, 1, 14, 1)
178: P_{2337} = (0, 1, 8, 1)
                                           232: P_{3116} = (11, 1, 11, 1)
                                                                                       286: P_{3909} = (4, 3, 14, 1)
                                           233: P_{3126} = (5, 2, 11, 1)
179: P_{2345} = (8, 1, 8, 1)
                                                                                       287: P_{3920} = (15, 3, 14, 1)
180: P_{2359} = (6, 2, 8, 1)
                                           234: P_{3131} = (10, 2, 11, 1)
                                                                                       288: P_{3959} = (6, 6, 14, 1)
181: P_{2368} = (15, 2, 8, 1)
                                           235: P_{3188} = (3, 6, 11, 1)
                                                                                       289: P_{3962} = (9, 6, 14, 1)
                                           236: P_{3196} = (11, 6, 11, 1)
182: P_{2389} = (4, 4, 8, 1)
                                                                                       290: P_{3992} = (7, 8, 14, 1)
183: P_{2400} = (15, 4, 8, 1)
                                           237: P_{3209} = (8, 7, 11, 1)
                                                                                       291: P_{3995} = (10, 8, 14, 1)
                                           238: P_{3212} = (11, 7, 11, 1)
184: P_{2402} = (1, 5, 8, 1)
                                                                                       292: P_{4002} = (1, 9, 14, 1)
                                           239: P_{3243} = (10, 9, 11, 1)
185: P_{2403} = (2, 5, 8, 1)
                                                                                      293: P_{4003} = (2, 9, 14, 1)
186: P_{2430} = (13, 6, 8, 1)
                                           240: P_{3248} = (15, 9, 11, 1)
                                                                                       294: P_{4017} = (0, 10, 14, 1)
                                           241: P_{3249} = (0, 10, 11, 1)
                                                                                       295: P_{4025} = (8, 10, 14, 1)
187: P_{2432} = (15, 6, 8, 1)
188: P_{2455} = (6, 8, 8, 1)
                                           242: P_{3250} = (1, 10, 11, 1)
                                                                                       296: P_{4033} = (0, 11, 14, 1)
189: P_{2458} = (9, 8, 8, 1)
                                           243: P_{3265} = (0, 11, 11, 1)
                                                                                       297: P_{4039} = (6, 11, 14, 1)
190: P_{2481} = (0, 10, 8, 1)
                                           244: P_{3275} = (10, 11, 11, 1)
                                                                                       298: P_{4071} = (6, 13, 14, 1)
191: P_{2487} = (6, 10, 8, 1)
                                           245: P_{3346} = (1, 0, 12, 1)
                                                                                       299: P_{4080} = (15, 13, 14, 1)
192: P_{2497} = (0, 11, 8, 1)
                                           246: P_{3361} = (0, 1, 12, 1)
                                                                                       300: P_{4094} = (13, 14, 14, 1)
                                           247: P_{3373} = (12, 1, 12, 1)
                                                                                       301: P_{4096} = (15, 14, 14, 1)
193: P_{2511} = (14, 11, 8, 1)
194: P_{2552} = (7, 14, 8, 1)
                                           248: P_{3431} = (6, 5, 12, 1)
                                                                                       302: P_{4114} = (1, 0, 15, 1)
                                           249: P_{3433} = (8, 5, 12, 1)
                                                                                       303: P_{4129} = (0, 1, 15, 1)
195: P_{2555} = (10, 14, 8, 1)
                                                                                       304: P_{4144} = (15, 1, 15, 1)
196: P_{2578} = (1, 0, 9, 1)
                                           250: P_{3458} = (1,7,12,1)
197: P_{2593} = (0, 1, 9, 1)
                                           251: P_{3471} = (14, 7, 12, 1)
                                                                                       305: P_{4156} = (11, 2, 15, 1)
198: P_{2602} = (9, 1, 9, 1)
                                           252: P_{3481} = (8, 8, 12, 1)
                                                                                       306: P_{4157} = (12, 2, 15, 1)
                                           253: P_{3485} = (12, 8, 12, 1)
199: P_{2642} = (1, 4, 9, 1)
                                                                                       307: P_{4180} = (3, 4, 15, 1)
200: P_{2655} = (14, 4, 9, 1)
                                           254: P_{3493} = (4, 9, 12, 1)
                                                                                       308: P_{4190} = (13, 4, 15, 1)
201: P_{2668} = (11, 5, 9, 1)
                                           255: P_{3501} = (12, 9, 12, 1)
                                                                                       309: P_{4242} = (1, 8, 15, 1)
202: P_{2670} = (13, 5, 9, 1)
                                           256: P_{3505} = (0, 10, 12, 1)
                                                                                       310: P_{4245} = (4, 8, 15, 1)
203: P_{2681} = (8, 6, 9, 1)
                                           257: P_{3510} = (5, 10, 12, 1)
                                                                                       311: P_{4260} = (3, 9, 15, 1)
```

```
\begin{array}{lll} 312: \ P_{4266} = (9,9,15,1) & 316: \ P_{4302} = (13,11,15,1) \\ 313: \ P_{4273} = (0,10,15,1) & 317: \ P_{4324} = (3,13,15,1) \\ 314: \ P_{4275} = (2,10,15,1) & 318: \ P_{4328} = (7,13,15,1) \\ 315: \ P_{4289} = (0,11,15,1) & 319: \ P_{4366} = (13,15,15,1) \end{array}
```