# Rank-65634 over GF(32)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_3 + X_0 X_1 X_2 = 0$$

 $(\ 1,\ 1,\ 1,\ 1,\ 1,\ 0,\ 1,\ 0,\ 0,\ 0,\ 0,\ 0,\ 0,\ 0,\ 0,\ 0,\ 1,\ 0,\ 0,\ 0)$ 

The point rank of the equation over GF(32) is -2111764410

## General information

| Number of lines            | 15                         |
|----------------------------|----------------------------|
| Number of points           | 1185                       |
| Number of singular points  | 0                          |
| Number of Eckardt points   | 0                          |
| Number of double points    | 45                         |
| Number of single points    | 405                        |
| Number of points off lines | 735                        |
| Number of Hesse planes     | 0                          |
| Number of axes             | 0                          |
| Type of points on lines    | $33^{15}$                  |
| Type of lines on points    | $2^{45}, 1^{405}, 0^{735}$ |

### Singular Points

The surface has 0 singular points:

### The 15 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & \eta^{20} & \eta^{16} \\ 0 & 1 & \eta^{29} & \eta^7 \end{bmatrix}_{926581} = \begin{bmatrix} 1 & 0 & 12 & 27 \\ 0 & 1 & 9 & 20 \end{bmatrix}_{926581} = \mathbf{Pl}(15, 13, 16, 11, 3, 1)_{151982}$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & \eta^6 & \eta^{15} \\ 0 & 1 & \eta^{21} & \eta^6 \end{bmatrix}_{1059458} = \begin{bmatrix} 1 & 0 & 10 & 31 \\ 0 & 1 & 24 & 10 \end{bmatrix}_{1059458} = \mathbf{Pl}(17, 24, 21, 26, 1, 1)_{91999}$$

$$\begin{split} \ell_2 &= \begin{bmatrix} 1 & 0 & \eta^{13} & \eta^7 \\ 0 & 1 & \eta^{21} & \eta^6 \end{bmatrix}_{706420} = \begin{bmatrix} 1 & 0 & 28 & 20 \\ 0 & 1 & 24 & 10 \end{bmatrix}_{706420} = \mathbf{Pl}(26, 21, 10, 25, 30, 1)_{1030998} \\ \ell_3 &= \begin{bmatrix} 1 & 0 & \eta^{26} & \eta^{14} \\ 0 & 1 & \eta^{11} & \eta^{12} \end{bmatrix}_{1005662} = \begin{bmatrix} 1 & 0 & 23 & 29 \\ 0 & 1 & 7 & 14 \end{bmatrix}_{1005662} = \mathbf{Pl}(3, 28, 14, 6, 19, 1)_{673866} \\ \ell_4 &= \begin{bmatrix} 1 & 0 & \eta^{21} & \eta^{28} \\ 0 & 1 & \eta^{22} & \eta^{24} \end{bmatrix}_{770477} = \begin{bmatrix} 1 & 0 & 24 & 22 \\ 0 & 1 & 21 & 30 \end{bmatrix}_{770477} = \mathbf{Pl}(5, 23, 30, 20, 8, 1)_{328734} \\ \ell_5 &= \begin{bmatrix} 1 & 0 & \eta^{22} & \eta^{19} \\ 0 & 1 & \eta^{26} & \eta^3 \end{bmatrix}_{225420} = \begin{bmatrix} 1 & 0 & 21 & 6 \\ 0 & 1 & 23 & 8 \end{bmatrix}_{225420} = \mathbf{Pl}(12, 7, 8, 22, 14, 1)_{504914} \\ \ell_6 &= \begin{bmatrix} 1 & 0 & \eta^{12} & \eta^{30} \\ 0 & 1 & \eta^{11} & \eta^{12} \end{bmatrix}_{624085} = \begin{bmatrix} 1 & 0 & 14 & 18 \\ 0 & 1 & 7 & 14 \end{bmatrix}_{624085} = \mathbf{Pl}(12, 7, 28, 3, 1, 1)_{98163} \\ \ell_7 &= \begin{bmatrix} 1 & 0 & \eta^9 & \eta \\ 0 & 1 & \eta^{27} & \eta^{14} \end{bmatrix}_{96069} = \begin{bmatrix} 1 & 0 & 26 & 2 \\ 0 & 1 & 11 & 29 \end{bmatrix}_{96069} = \mathbf{Pl}(31, 27, 13, 15, 5, 1)_{214742} \\ \ell_8 &= \begin{bmatrix} 1 & 0 & \eta^{17} & \eta^{27} \\ 0 & 1 & \eta^{13} & \eta^{17} \end{bmatrix}_{392783} = \begin{bmatrix} 1 & 0 & 19 & 11 \\ 0 & 1 & 28 & 19 \end{bmatrix}_{392783} = \mathbf{Pl}(3, 28, 24, 17, 1, 1)_{94155} \\ \ell_9 &= \begin{bmatrix} 1 & 0 & \eta^5 & \eta^4 \\ 0 & 1 & \eta^{15} & \eta^{25} \end{bmatrix}_{547300} = \begin{bmatrix} 1 & 0 & 8 & 15 \\ 0 & 1 & 23 & 8 \end{bmatrix}_{516095} = \mathbf{Pl}(9, 4, 2, 18, 12, 1)_{433859} \\ \ell_{10} &= \begin{bmatrix} 1 & 0 & \eta^{10} & \eta^8 \\ 0 & 1 & \eta^{20} & \eta^3 \end{bmatrix}_{457891} = \begin{bmatrix} 1 & 0 & 17 & 13 \\ 0 & 1 & 18 & 6 \end{bmatrix}_{457891} = \mathbf{Pl}(11, 16, 4, 9, 26, 1)_{894459} \\ \ell_{12} &= \begin{bmatrix} 1 & 0 & \eta^{18} & \eta^2 \\ 0 & 1 & \eta^{23} & \eta^{28} \end{bmatrix}_{139186} = \begin{bmatrix} 1 & 0 & 3 & 4 \\ 0 & 1 & 21 & 30 \end{bmatrix}_{337107} = \mathbf{Pl}(26, 21, 23, 5, 1, 1)_{93186} \\ \ell_{14} &= \begin{bmatrix} 1 & 0 & \eta^{11} & \eta^{25} \\ 0 & 1 & \eta^{13} & \eta^{17} \end{bmatrix}_{853635} = \begin{bmatrix} 1 & 0 & 7 & 25 \\ 0 & 1 & 28 & 19 \end{bmatrix}_{853635} = \mathbf{Pl}(17, 24, 19, 29, 10, 1)_{384360} \\ \mathbf{Pl}(14 &= \begin{bmatrix} 1 & 0 & \eta^{11} & \eta^{25} \\ 0 & 1 & \eta^{13} & \eta^{17} \end{bmatrix}_{853635} = \begin{bmatrix} 1 & 0 & 7 & 25 \\ 0 & 1 & 28 & 19 \end{bmatrix}_{853635} = \mathbf{Pl}(17, 24, 19, 29, 10, 1)_{384360} \\ \mathbf{Pl}(14 &= \begin{bmatrix} 1 & 0 & \eta^{11} & \eta^{25} \\ 0 & 1 & \eta^{13} & \eta^{17} \end{bmatrix}_{853635} = \begin{bmatrix} 1 & 0 & 7 & 25 \\ 0 & 1 & 28 & 19 \end{bmatrix}_{853635} = \mathbf{Pl}(17, 24, 19, 29, 10, 1)_{384360$$

Rank of lines: ( 926581, 1059458, 706420, 1005662, 770477, 225420, 624085, 96069, 392783, 547300, 516095, 457891, 139186, 337107, 853635)

Rank of points on Klein quadric: (151982, 91999, 1030998, 673886, 328734, 504914, 98163, 214742, 94155, 433859, 78471, 894459, 620953, 93186, 384360)

#### **Eckardt Points**

The surface has 0 Eckardt points:

#### **Double Points**

The surface has 45 Double points: The double points on the surface are:

$$\begin{array}{ll} P_{244} = (17,6,1,0) = \ell_0 \cap \ell_1 & P_{29718} = (21,31,27,1) = \ell_0 \cap \ell_8 \\ P_{12841} = (8,16,11,1) = \ell_0 \cap \ell_5 & P_{4309} = (20,5,3,1) = \ell_0 \cap \ell_{11} \\ P_{8076} = (11,27,6,1) = \ell_0 \cap \ell_6 & P_{33601} = (0,25,31,1) = \ell_1 \cap \ell_2 \\ P_{6750} = (29,17,5,1) = \ell_0 \cap \ell_7 & P_{19254} = (21,24,17,1) = \ell_1 \cap \ell_3 \end{array}$$

| $P_{18405} = (4, 30, 16, 1) = \ell_1 \cap \ell_4$     |
|---|
| $P_{27082} = (9, 13, 25, 1) = \ell_1 \cap \ell_{11}$  |
| $P_{5464} = (23, 9, 4, 1) = \ell_1 \cap \ell_{12}$    |
| $P_{12603} = (26, 8, 11, 1) = \ell_2 \cap \ell_4$     |
| $P_{16843} = (10, 13, 15, 1) = \ell_2 \cap \ell_7$    |
| $P_{3452} = (27, 10, 2, 1) = \ell_2 \cap \ell_8$      |
| $P_{6920} = (7, 23, 5, 1) = \ell_2 \cap \ell_{10}$    |
| $P_{20466} = (17, 30, 18, 1) = \ell_2 \cap \ell_{14}$ |
| $P_{10893} = (12, 19, 9, 1) = \ell_3 \cap \ell_5$     |
| $P_{19681} = (0, 6, 18, 1) = \ell_3 \cap \ell_6$      |
| $P_{5603} = (2, 14, 4, 1) = \ell_3 \cap \ell_{10}$    |
| $P_{33679} = (14, 27, 31, 1) = \ell_3 \cap \ell_{12}$ |
| $P_{16740} = (3, 10, 15, 1) = \ell_3 \cap \ell_{14}$  |
| $P_{33254} = (5, 14, 31, 1) = \ell_4 \cap \ell_5$     |
| $P_{13597} = (28, 7, 12, 1) = \ell_4 \cap \ell_6$     |
| $P_{19583} = (30, 2, 18, 1) = \ell_4 \cap \ell_9$     |
| $P_{10913} = (0, 20, 9, 1) = \ell_4 \cap \ell_{13}$   |
| $P_{5049} = (24, 28, 3, 1) = \ell_5 \cap \ell_8$      |
| $P_{17121} = (0, 22, 15, 1) = \ell_5 \cap \ell_{10}$  |

## $P_{28974} = (13, 8, 27, 1) = \ell_5 \cap \ell_{13}$ $P_{687} = (12, 20, 1, 0) = \ell_6 \cap \ell_7$ $P_{17817} = (24, 11, 16, 1) = \ell_6 \cap \ell_9$ $P_{14993} = (16, 19, 13, 1) = \ell_6 \cap \ell_{14}$ $P_{3709} = (28, 18, 2, 1) = \ell_7 \cap \ell_{10}$ $P_{18871} = (22, 12, 17, 1) = \ell_7 \cap \ell_{12}$ $P_{21616} = (15, 2, 20, 1) = \ell_7 \cap \ell_{13}$ $P_{742} = (3, 22, 1, 0) = \ell_8 \cap \ell_9$ $P_{30912} = (31, 4, 29, 1) = \ell_8 \cap \ell_{12}$ $P_{13249} = (0, 29, 11, 1) = \ell_8 \cap \ell_{14}$ $P_{24115} = (18, 16, 22, 1) = \ell_9 \cap \ell_{10}$ $P_{27783} = (6, 3, 26, 1) = \ell_9 \cap \ell_{11}$ $P_{14202} = (25, 26, 12, 1) = \ell_9 \cap \ell_{12}$ $P_{840} = (5, 25, 1, 0) = \ell_{10} \cap \ell_{11}$ $P_{14856} = (7, 15, 13, 1) = \ell_{11} \cap \ell_{13}$ $P_{10420} = (19, 4, 9, 1) = \ell_{11} \cap \ell_{14}$ $P_{989} = (26, 29, 1, 0) = \ell_{12} \cap \ell_{13}$ $P_{28376} = (23, 21, 26, 1) = \ell_{13} \cap \ell_{14}$

## Single Points

The surface has 405 single points: The single points on the surface are:

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0: P_{295} = (4, 8, 1, 0) lies on line \ell_2
1: P_{371} = (16, 10, 1, 0) lies on line \ell_3
2: P_{496} = (13, 14, 1, 0) lies on line \ell_4
3: P_{645} = (2, 19, 1, 0) lies on line \ell_5
4: P_{1022} = (27, 30, 1, 0) lies on line \ell_{14}
5: P_{1162} = (8, 3, 0, 1) lies on line \ell_3
6: P_{1183} = (29, 3, 0, 1) lies on line \ell_8
7: P_{1228} = (10, 5, 0, 1) lies on line \ell_4
8: P_{1240} = (22, 5, 0, 1) lies on line \ell_{10}
9: P_{1359} = (13, 9, 0, 1) lies on line \ell_9
10: P_{1437} = (27, 11, 0, 1) lies on line \ell_{11}
11: P_{1448} = (6, 12, 0, 1) lies on line \ell_6
12: P_{1472} = (30, 12, 0, 1) lies on line \ell_5
13: P_{1540} = (2, 15, 0, 1) lies on line \ell_0
14: P_{1616} = (14, 17, 0, 1) lies on line \ell_{14}
15: P_{1627} = (25, 17, 0, 1) lies on line \ell_1
16: P_{1650} = (16, 18, 0, 1) lies on line \ell_{12}
17: P_{1909} = (19, 26, 0, 1) lies on line \ell_2
18: P_{1910} = (20, 26, 0, 1) lies on line \ell_{13}
19: P_{2054} = (4, 31, 0, 1) lies on line \ell_7
20: P_{2319} = (14, 7, 1, 1) lies on line \ell_{13}
21: P_{2388} = (19, 9, 1, 1) lies on line \ell_0
22: P_{2393} = (24, 9, 1, 1) lies on line \ell_3
23: P_{2440} = (7, 11, 1, 1) lies on line \ell_4
24: P_{2441} = (8, 11, 1, 1) lies on line \ell_7
25: P_{2571} = (10, 15, 1, 1) lies on line \ell_{12}
26: P_{2582} = (21, 15, 1, 1) lies on line \ell_{14}
27: P_{2680} = (23, 18, 1, 1) lies on line \ell_2
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28: P_{2687} = (30, 18, 1, 1) lies on line \ell_{11}
29: P_{2783} = (30, 21, 1, 1) lies on line \ell_8
30: P_{2825} = (8, 23, 1, 1) lies on line \ell_1
31: P_{2859} = (10, 24, 1, 1) lies on line \ell_6
32: P_{2996} = (19, 28, 1, 1) lies on line \ell_{10}
33: P_{3087} = (14, 31, 1, 1) lies on line \ell_9
34: P_{3101} = (28, 31, 1, 1) lies on line \ell_5
35: P_{3116} = (11, 0, 2, 1) lies on line \ell_9
36: P_{3167} = (30, 1, 2, 1) lies on line \ell_6
37: P_{3206} = (5, 3, 2, 1) lies on line \ell_0
38: P_{3270} = (5, 5, 2, 1) lies on line \ell_{13}
39: P_{3390} = (29, 8, 2, 1) lies on line \ell_{14}
40: P_{3522} = (1, 13, 2, 1) lies on line \ell_{12}
41: P_{3611} = (26, 15, 2, 1) lies on line \ell_5
42: P_{3854} = (13, 23, 2, 1) lies on line \ell_3
43: P_{3921} = (16, 25, 2, 1) lies on line \ell_4
44: P_{4018} = (17, 28, 2, 1) lies on line \ell_{11}
45: P_{4063} = (30, 29, 2, 1) lies on line \ell_1
46: P_{4224} = (31, 2, 3, 1) lies on line \ell_2
47: P_{4337} = (16, 6, 3, 1) lies on line \ell_7
48: P_{4506} = (25, 11, 3, 1) lies on line \ell_{10}
49: P_{4668} = (27, 16, 3, 1) lies on line \ell_{12}
50: P_{4819} = (18, 21, 3, 1) lies on line \ell_6
51: P_{4839} = (6, 22, 3, 1) lies on line \ell_{14}
52: P_{4841} = (8, 22, 3, 1) lies on line \ell_9
53: P_{4894} = (29, 23, 3, 1) lies on line \ell_4
54: P_{4928} = (31, 24, 3, 1) lies on line \ell_{13}
55: P_{5008} = (15, 27, 3, 1) lies on line \ell_1
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56: P_{5086} = (29, 29, 3, 1) lies on line \ell_3
                                                                      110: P_{9382} = (5, 4, 8, 1) lies on line \ell_1
57: P_{5168} = (15, 0, 4, 1) lies on line \ell_{11}
                                                                      111: P_{9526} = (21, 8, 8, 1) lies on line \ell_9
58: P_{5204} = (19, 1, 4, 1) lies on line \ell_{13}
                                                                      112: P_{9563} = (26, 9, 8, 1) lies on line \ell_{13}
59: P_{5330} = (17, 5, 4, 1) lies on line \ell_7
                                                                      113: P_{9708} = (11, 14, 8, 1) lies on line \ell_7
60: P_{5358} = (13, 6, 4, 1) lies on line \ell_{14}
                                                                      114: P_{9783} = (22, 16, 8, 1) lies on line \ell_2
61: P_{5495} = (22, 10, 4, 1) lies on line \ell_5
                                                                      115: P_{9884} = (27, 19, 8, 1) lies on line \ell_{10}
62: P_{5714} = (17, 17, 4, 1) lies on line \ell_8
                                                                      116: P_{10077} = (28, 25, 8, 1) lies on line \ell_3
63: P_{5876} = (19, 22, 4, 1) lies on line \ell_6
                                                                      117: P_{10089} = (8, 26, 8, 1) lies on line \ell_{14}
64: P_{5901} = (12, 23, 4, 1) lies on line \ell_0
                                                                      118: P_{10094} = (13, 26, 8, 1) lies on line \ell_4
65: P_{5948} = (27, 24, 4, 1) lies on line \ell_4
                                                                      119: P_{10111} = (30, 26, 8, 1) lies on line \ell_0
66: P_{6018} = (1, 27, 4, 1) lies on line \ell_9
                                                                      120: P_{10186} = (9, 29, 8, 1) lies on line \ell_6
                                                                      121: P_{10199} = (22, 29, 8, 1) lies on line \ell_{11}
67: P_{6148} = (3, 31, 4, 1) lies on line \ell_2
68: P_{6272} = (31, 2, 5, 1) lies on line \ell_6
                                                                      122: P_{10357} = (20, 2, 9, 1) lies on line \ell_1
69: P_{6323} = (18, 4, 5, 1) lies on line \ell_3
                                                                      123: P_{10566} = (5, 9, 9, 1) lies on line \ell_6
70: P_{6419} = (18, 7, 5, 1) lies on line \ell_8
                                                                      124: P_{10623} = (30, 10, 9, 1) lies on line \ell_{10}
71: P_{6595} = (2, 13, 5, 1) lies on line \ell_9
                                                                      125: P_{10919} = (6, 20, 9, 1) lies on line \ell_8
72: P_{6663} = (6, 15, 5, 1) lies on line \ell_1
                                                                      126: P_{11059} = (18, 24, 9, 1) lies on line \ell_2
73: P_{6830} = (13, 20, 5, 1) lies on line \ell_{12}
                                                                      127: P_{11112} = (7, 26, 9, 1) lies on line \ell_7
                                                                      128: P_{11173} = (4, 28, 9, 1) lies on line \ell_{12}
74: P_{6903} = (22, 22, 5, 1) lies on line \ell_4
75: P_{6967} = (22, 24, 5, 1) lies on line \ell_{14}
                                                                      129: P_{11184} = (15, 28, 9, 1) lies on line \ell_0
76: P_{6987} = (10, 25, 5, 1) lies on line \ell_{11}
                                                                      130: P_{11255} = (22, 30, 9, 1) lies on line \ell_9
77: P_{6997} = (20, 25, 5, 1) lies on line \ell_5
                                                                      131: P_{11327} = (30, 0, 10, 1) lies on line \ell_2
78: P_{7082} = (9, 28, 5, 1) lies on line \ell_{13}
                                                                      132: P_{11348} = (19, 1, 10, 1) lies on line \ell_9
                                                                      133: P_{11403} = (10, 3, 10, 1) lies on line \ell_5
79: P_{7330} = (1, 4, 6, 1) lies on line \ell_4
80: P_{7377} = (16, 5, 6, 1) lies on line \ell_1
                                                                      134: P_{11412} = (19, 3, 10, 1) lies on line \ell_7
81: P_{7466} = (9, 8, 6, 1) lies on line \ell_7
                                                                      135: P_{11420} = (27, 3, 10, 1) lies on line \ell_{14}
82: P_{7507} = (18, 9, 6, 1) lies on line \ell_5
                                                                      136: P_{11442} = (17, 4, 10, 1) lies on line \ell_{10}
83: P_{7692} = (11, 15, 6, 1) lies on line \ell_2
                                                                      137: P_{11512} = (23, 6, 10, 1) lies on line \ell_4
84: P_{7784} = (7, 18, 6, 1) lies on line \ell_9
                                                                      138: P_{11555} = (2, 8, 10, 1) lies on line \ell_1
85: P_{7911} = (6, 22, 6, 1) lies on line \ell_{12}
                                                                      139: P_{11645} = (28, 10, 10, 1) lies on line \ell_{11}
86: P_{7942} = (5, 23, 6, 1) lies on line \ell_{11}
                                                                      140: P_{11652} = (3, 11, 10, 1) lies on line \ell_8
87: P_{7992} = (23, 24, 6, 1) lies on line \ell_8
                                                                      141: P_{11738} = (25, 13, 10, 1) lies on line \ell_3
88: P_{8009} = (8, 25, 6, 1) lies on line \ell_{10}
                                                                      142: P_{11826} = (17, 16, 10, 1) lies on line \ell_6
89: P_{8040} = (7, 26, 6, 1) lies on line \ell_3
                                                                      143: P_{12012} = (11, 22, 10, 1) lies on line \ell_{13}
90: P_{8163} = (2, 30, 6, 1) lies on line \ell_{13}
                                                                      144: P_{12026} = (25, 22, 10, 1) lies on line \ell_0
                                                                      145: P_{12272} = (15, 30, 10, 1) lies on line \ell_{12}
91: P_{8223} = (30, 31, 6, 1) lies on line \ell_{14}
92: P_{8238} = (13, 0, 7, 1) lies on line \ell_{10}
                                                                      146: P_{12438} = (21, 3, 11, 1) lies on line \ell_{12}
93: P_{8262} = (5, 1, 7, 1) lies on line \ell_{14}
                                                                      147: P_{12478} = (29, 4, 11, 1) lies on line \ell_6
94: P_{8322} = (1, 3, 7, 1) lies on line \ell_1
                                                                      148: P_{12554} = (9, 7, 11, 1) lies on line \ell_3
95: P_{8345} = (24, 3, 7, 1) lies on line \ell_{13}
                                                                      149: P_{12690} = (17, 11, 11, 1) lies on line \ell_{13}
96: P_{8357} = (4, 4, 7, 1) lies on line \ell_9
                                                                      150: P_{12788} = (19, 14, 11, 1) lies on line \ell_1
97: P_{8464} = (15, 7, 7, 1) lies on line \ell_2
                                                                      151: P_{12954} = (25, 19, 11, 1) lies on line \ell_{11}
                                                                      152 : P_{13073} = (16, 23, 11, 1) lies on line \ell_9
98: P_{8557} = (12, 10, 7, 1) lies on line \ell_4
99: P_{8605} = (28, 11, 7, 1) lies on line \ell_{12}
                                                                      153: P_{13088} = (31, 23, 11, 1) lies on line \ell_7
100: P_{8673} = (0, 14, 7, 1) lies on line \ell_{11}
                                                                      154: P_{13269} = (20, 29, 11, 1) lies on line \ell_{10}
                                                                      155 : P_{13425} = (16, 2, 12, 1) lies on line \ell_0
101: P_{8693} = (20, 14, 7, 1) lies on line \ell_8
102: P_{8712} = (7, 15, 7, 1) lies on line \ell_6
                                                                      156: P_{13543} = (6, 6, 12, 1) lies on line \ell_5
103: P_{8760} = (23, 16, 7, 1) lies on line \ell_3
                                                                      157: P_{13772} = (11, 13, 12, 1) lies on line \ell_{14}
104: P_{9073} = (16, 26, 7, 1) lies on line \ell_5
                                                                      158: P_{13866} = (9, 16, 12, 1) lies on line \ell_8
105: P_{9126} = (5, 28, 7, 1) lies on line \ell_7
                                                                      159: P_{13950} = (29, 18, 12, 1) lies on line \ell_{13}
106: P_{9179} = (26, 29, 7, 1) lies on line \ell_0
                                                                      160: P_{14007} = (22, 20, 12, 1) lies on line \ell_3
107: P_{9263} = (14, 0, 8, 1) lies on line \ell_5
                                                                      161: P_{14015} = (30, 20, 12, 1) lies on line \ell_7
                                                                      162 : P_{14023} = (6, 21, 12, 1) lies on line \ell_2
108: P_{9311} = (30, 1, 8, 1) lies on line \ell_{12}
109: P_{9318} = (5, 2, 8, 1) lies on line \ell_8
                                                                      163: P_{14051} = (2, 22, 12, 1) lies on line \ell_{11}
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164: P_{14128} = (15, 24, 12, 1) lies on line \ell_{10}
                                                                     218: P_{19212} = (11, 23, 17, 1) lies on line \ell_8
165: P_{14252} = (11, 28, 12, 1) lies on line \ell_1
                                                                     219: P_{19290} = (25, 25, 17, 1) lies on line \ell_{14}
                                                                     220: P_{19333} = (4, 27, 17, 1) lies on line \ell_{11}
166: P_{14387} = (18, 0, 13, 1) lies on line \ell_7
167: P_{14411} = (10, 1, 13, 1) lies on line \ell_{10}
                                                                     221: P_{19420} = (27, 29, 17, 1) lies on line \ell_9
168: P_{14498} = (1, 4, 13, 1) lies on line \ell_0
                                                                     222: P_{19477} = (20, 31, 17, 1) lies on line \ell_6
169: P_{14571} = (10, 6, 13, 1) lies on line \ell_8
                                                                     223: P_{19706} = (25, 6, 18, 1) lies on line \ell_{13}
170: P_{14596} = (3, 7, 13, 1) lies on line \ell_{12}
                                                                     224: P_{19759} = (14, 8, 18, 1) lies on line \ell_8
171: P_{14674} = (17, 9, 13, 1) lies on line \ell_4
                                                                     225: P_{19897} = (24, 12, 18, 1) lies on line \ell_0
172: P_{14779} = (26, 12, 13, 1) lies on line \ell_9
                                                                     226: P_{19966} = (29, 14, 18, 1) lies on line \ell_{12}
173: P_{15045} = (4, 21, 13, 1) lies on line \ell_5
                                                                     227: P_{20068} = (3, 18, 18, 1) lies on line \ell_1
174: P_{15227} = (26, 26, 13, 1) lies on line \ell_1
                                                                     228: P_{20163} = (2, 21, 18, 1) lies on line \ell_7
175: P_{15299} = (2, 29, 13, 1) lies on line \ell_2
                                                                     229: P_{20172} = (11, 21, 18, 1) lies on line \ell_{11}
176: P_{15335} = (6, 30, 13, 1) lies on line \ell_3
                                                                     230: P_{20256} = (31, 23, 18, 1) lies on line \ell_5
177: P_{15412} = (19, 0, 14, 1) lies on line \ell_3
                                                                     231: P_{20359} = (6, 27, 18, 1) lies on line \ell_{10}
178: P_{15433} = (8, 1, 14, 1) lies on line \ell_{11}
                                                                     232: P_{20523} = (10, 0, 19, 1) lies on line \ell_{14}
179: P_{15555} = (2, 5, 14, 1) lies on line \ell_5
                                                                     233: P_{20559} = (14, 1, 19, 1) lies on line \ell_7
180: P_{15561} = (8, 5, 14, 1) lies on line \ell_{12}
                                                                     234 : P_{20580} = (3, 2, 19, 1) lies on line \ell_{10}
181: P_{15567} = (14, 5, 14, 1) lies on line \ell_2
                                                                     235: P_{20670} = (29, 4, 19, 1) lies on line \ell_5
182: P_{15717} = (4, 10, 14, 1) lies on line \ell_6
                                                                     236: P_{20842} = (9, 10, 19, 1) lies on line \ell_0
                                                                     237: P_{20911} = (14, 12, 19, 1) lies on line \ell_{11}
183: P_{15821} = (12, 13, 14, 1) lies on line \ell_{13}
184 : P_{15864} = (23, 14, 14, 1) lies on line \ell_0
                                                                     238: P_{20913} = (16, 12, 19, 1) lies on line \ell_3
185: P_{15878} = (5, 15, 14, 1) lies on line \ell_{10}
                                                                     239 : P_{20916} = (19, 12, 19, 1) lies on line \ell_4
186: P_{15917} = (12, 16, 14, 1) lies on line \ell_1
                                                                     240: P_{21101} = (12, 18, 19, 1) lies on line \ell_6
187: P_{16032} = (31, 19, 14, 1) lies on line \ell_9
                                                                     241: P_{21128} = (7, 19, 19, 1) lies on line \ell_{12}
188: P_{16057} = (24, 20, 14, 1) lies on line \ell_{14}
                                                                     242: P_{21171} = (18, 20, 19, 1) lies on line \ell_1
189 : P_{16199} = (6, 25, 14, 1) lies on line \ell_7
                                                                     243: P_{21182} = (29, 20, 19, 1) lies on line \ell_9
190: P_{16208} = (15, 25, 14, 1) lies on line \ell_8
                                                                     244: P_{21238} = (21, 22, 19, 1) lies on line \ell_2
191: P_{16263} = (6, 27, 14, 1) lies on line \ell_4
                                                                     245: P_{21380} = (3, 27, 19, 1) lies on line \ell_{13}
192: P_{16605} = (28, 5, 15, 1) lies on line \ell_9
                                                                     246: P_{21486} = (13, 30, 19, 1) lies on line \ell_8
193: P_{16679} = (6, 8, 15, 1) lies on line \ell_0
                                                                     247: P_{21654} = (21, 3, 20, 1) lies on line \ell_4
194: P_{16909} = (12, 15, 15, 1) lies on line \ell_8
                                                                     248: P_{21739} = (10, 6, 20, 1) lies on line \ell_1
195: P_{16951} = (22, 16, 15, 1) lies on line \ell_{13}
                                                                     249: P_{21785} = (24, 7, 20, 1) lies on line \ell_{10}
196: P_{17100} = (11, 21, 15, 1) lies on line \ell_4
                                                                     250: P_{21846} = (21, 9, 20, 1) lies on line \ell_{11}
197: P_{17150} = (29, 22, 15, 1) lies on line \ell_1
                                                                     251: P_{21868} = (11, 10, 20, 1) lies on line \ell_{12}
198: P_{17198} = (13, 24, 15, 1) lies on line \ell_{11}
                                                                     252: P_{21898} = (9, 11, 20, 1) lies on line \ell_2
199: P_{17203} = (18, 24, 15, 1) lies on line \ell_{12}
                                                                     253: P_{22050} = (1, 16, 20, 1) lies on line \ell_{14}
200: P_{17385} = (8, 30, 15, 1) lies on line \ell_6
                                                                     254: P_{22094} = (13, 17, 20, 1) lies on line \ell_6
201 : P_{17472} = (31, 0, 16, 1) lies on line \ell_0
                                                                     255: P_{22132} = (19, 18, 20, 1) lies on line \ell_5
202 : P_{17481} = (8, 1, 16, 1) lies on line \ell_8
                                                                     256: P_{22149} = (4, 19, 20, 1) lies on line \ell_8
203: P_{17506} = (1, 2, 16, 1) lies on line \ell_{11}
                                                                     257: P_{22322} = (17, 24, 20, 1) lies on line \ell_0
204 : P_{17667} = (2, 7, 16, 1) lies on line \ell_{14}
                                                                     258: P_{22357} = (20, 25, 20, 1) lies on line \ell_9
205: P_{17837} = (12, 12, 16, 1) lies on line \ell_{10}
                                                                     259: P_{22544} = (15, 31, 20, 1) lies on line \ell_3
206: P_{17914} = (25, 14, 16, 1) lies on line \ell_2
                                                                     260: P_{22588} = (27, 0, 21, 1) lies on line \ell_1
207: P_{17997} = (12, 17, 16, 1) lies on line \ell_{12}
                                                                     261: P_{22610} = (17, 1, 21, 1) lies on line \ell_5
208: P_{18022} = (5, 18, 16, 1) lies on line \ell_3
                                                                     262: P_{22670} = (13, 3, 21, 1) lies on line \ell_2
                                                                     263 : P_{22722} = (1, 5, 21, 1) lies on line \ell_6
209: P_{18108} = (27, 20, 16, 1) lies on line \ell_5
210: P_{18235} = (26, 24, 16, 1) lies on line \ell_7
                                                                     264: P_{22728} = (7, 5, 21, 1) lies on line \ell_8
211: P_{18249} = (8, 25, 16, 1) lies on line \ell_{13}
                                                                     265: P_{23001} = (24, 13, 21, 1) lies on line \ell_4
212: P_{18611} = (18, 4, 17, 1) lies on line \ell_{13}
                                                                     266: P_{23035} = (26, 14, 21, 1) lies on line \ell_{14}
213: P_{18671} = (14, 6, 17, 1) lies on line \ell_0
                                                                     267: P_{23064} = (23, 15, 21, 1) lies on line \ell_9
214: P_{18686} = (29, 6, 17, 1) lies on line \ell_2
                                                                     268: P_{23089} = (16, 16, 21, 1) lies on line \ell_{11}
215: P_{18714} = (25, 7, 17, 1) lies on line \ell_5
                                                                     269: P_{23264} = (31, 21, 21, 1) lies on line \ell_3
216 : P_{18986} = (9, 16, 17, 1) lies on line \ell_4
                                                                     270 : P_{23268} = (3, 22, 21, 1) lies on line \ell_7
217: P_{19146} = (9, 21, 17, 1) lies on line \ell_{10}
                                                                     271: P_{23314} = (17, 23, 21, 1) lies on line \ell_{12}
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272 : P_{23521} = (0, 30, 21, 1) lies on line \ell_0
                                                                     326: P_{27380} = (19, 22, 25, 1) lies on line \ell_8
273: P_{23550} = (29, 30, 21, 1) lies on line \ell_{10}
                                                                     327: P_{27421} = (28, 23, 25, 1) lies on line \ell_{13}
                                                                     328: P_{27556} = (3, 28, 25, 1) lies on line \ell_9
274: P_{23574} = (21, 31, 21, 1) lies on line \ell_{13}
275: P_{23891} = (18, 9, 22, 1) lies on line \ell_{14}
                                                                     329: P_{27610} = (25, 29, 25, 1) lies on line \ell_7
276: P_{23918} = (13, 10, 22, 1) lies on line \ell_1
                                                                     330: P_{27673} = (24, 31, 25, 1) lies on line \ell_{12}
277: P_{23947} = (10, 11, 22, 1) lies on line \ell_3
                                                                     331: P_{27822} = (13, 4, 26, 1) lies on line \ell_7
278: P_{24088} = (23, 15, 22, 1) lies on line \ell_7
                                                                     332: P_{27936} = (31, 7, 26, 1) lies on line \ell_1
279: P_{24152} = (23, 17, 22, 1) lies on line \ell_5
                                                                     333: P_{27991} = (22, 9, 26, 1) lies on line \ell_8
280 : P_{24247} = (22, 20, 22, 1) lies on line \ell_0
                                                                     334: P_{28108} = (11, 13, 26, 1) lies on line \ell_{10}
281: P_{24283} = (26, 21, 22, 1) lies on line \ell_{12}
                                                                     335: P_{28341} = (20, 20, 26, 1) lies on line \ell_2
282 : P_{24419} = (2, 26, 22, 1) lies on line \ell_8
                                                                     336: P_{28432} = (15, 23, 26, 1) lies on line \ell_6
283: P_{24450} = (1, 27, 22, 1) lies on line \ell_2
                                                                     337: P_{28485} = (4, 25, 26, 1) lies on line \ell_0
284: P_{24502} = (21, 28, 22, 1) lies on line \ell_6
                                                                     338: P_{28560} = (15, 27, 26, 1) lies on line \ell_5
285: P_{24543} = (30, 29, 22, 1) lies on line \ell_{13}
                                                                     339: P_{28597} = (20, 28, 26, 1) lies on line \ell_3
286 : P_{24576} = (31, 30, 22, 1) lies on line \ell_{11}
                                                                     340: P_{28628} = (19, 29, 26, 1) lies on line \ell_{12}
287: P_{24592} = (15, 31, 22, 1) lies on line \ell_4
                                                                     341: P_{28634} = (25, 29, 26, 1) lies on line \ell_4
288: P_{24613} = (4, 0, 23, 1) lies on line \ell_{13}
                                                                     342: P_{28714} = (9, 0, 27, 1) lies on line \ell_{12}
289: P_{24667} = (26, 1, 23, 1) lies on line \ell_3
                                                                     343: P_{28751} = (14, 1, 27, 1) lies on line \ell_1
290 : P_{24694} = (21, 2, 23, 1) lies on line \ell_5
                                                                     344: P_{28804} = (3, 3, 27, 1) lies on line \ell_6
291: P_{24818} = (17, 6, 23, 1) lies on line \ell_9
                                                                     345: P_{29069} = (12, 11, 27, 1) lies on line \ell_{14}
292: P_{24859} = (26, 7, 23, 1) lies on line \ell_{11}
                                                                     346: P_{29218} = (1, 16, 27, 1) lies on line \ell_7
293: P_{24865} = (0, 8, 23, 1) lies on line \ell_{12}
                                                                     347: P_{29333} = (20, 19, 27, 1) lies on line \ell_4
294: P_{24890} = (25, 8, 23, 1) lies on line \ell_6
                                                                     348: P_{29359} = (14, 20, 27, 1) lies on line \ell_{10}
295: P_{24920} = (23, 9, 23, 1) lies on line \ell_{10}
                                                                     349: P_{29382} = (5, 21, 27, 1) lies on line \ell_9
296: P_{24994} = (1, 12, 23, 1) lies on line \ell_8
                                                                     350: P_{29413} = (4, 22, 27, 1) lies on line \ell_3
297: P_{25021} = (28, 12, 23, 1) lies on line \ell_1
                                                                     351: P_{29540} = (3, 26, 27, 1) lies on line \ell_{11}
298: P_{25155} = (2, 17, 23, 1) lies on line \ell_4
                                                                     352: P_{29617} = (16, 28, 27, 1) lies on line \ell_2
299: P_{25192} = (7, 18, 23, 1) lies on line \ell_0
                                                                     353: P_{29731} = (2, 0, 28, 1) lies on line \ell_6
300: P_{25222} = (5, 19, 23, 1) lies on line \ell_2
                                                                     354: P_{29773} = (12, 1, 28, 1) lies on line \ell_2
301: P_{25354} = (9, 23, 23, 1) lies on line \ell_{14}
                                                                     355: P_{29916} = (27, 5, 28, 1) lies on line \ell_3
302: P_{25500} = (27, 27, 23, 1) lies on line \ell_7
                                                                     356: P_{30158} = (13, 13, 28, 1) lies on line \ell_0
303: P_{25649} = (16, 0, 24, 1) lies on line \ell_8
                                                                     357: P_{30274} = (1, 17, 28, 1) lies on line \ell_{13}
304: P_{25668} = (3, 1, 24, 1) lies on line \ell_4
                                                                     358: P_{30294} = (21, 17, 28, 1) lies on line \ell_{10}
305: P_{25699} = (2, 2, 24, 1) lies on line \ell_{12}
                                                                     359 : P_{30333} = (28, 18, 28, 1) lies on line \ell_8
306: P_{25789} = (28, 4, 24, 1) lies on line \ell_2
                                                                     360: P_{30337} = (0, 19, 28, 1) lies on line \ell_7
307: P_{25906} = (17, 8, 24, 1) lies on line \ell_3
                                                                     361: P_{30359} = (22, 19, 28, 1) lies on line \ell_1
308: P_{25942} = (21, 9, 24, 1) lies on line \ell_7
                                                                     362: P_{30509} = (12, 24, 28, 1) lies on line \ell_9
309: P_{25953} = (0, 10, 24, 1) lies on line \ell_9
                                                                     363: P_{30534} = (5, 25, 28, 1) lies on line \ell_{12}
310: P_{25959} = (6, 10, 24, 1) lies on line \ell_{13}
                                                                     364: P_{30600} = (7, 27, 28, 1) lies on line \ell_{14}
311: P_{26009} = (24, 11, 24, 1) lies on line \ell_1
                                                                     365: P_{30643} = (18, 28, 28, 1) lies on line \ell_4
312: P_{26021} = (4, 12, 24, 1) lies on line \ell_{14}
                                                                     366: P_{30692} = (3, 30, 28, 1) lies on line \ell_5
313: P_{26285} = (12, 20, 24, 1) lies on line \ell_{11}
                                                                     367: P_{30745} = (24, 31, 28, 1) lies on line \ell_{11}
314: P_{26308} = (3, 21, 24, 1) lies on line \ell_0
                                                                     368: P_{30941} = (28, 5, 29, 1) lies on line \ell_{14}
315: P_{26412} = (11, 24, 24, 1) lies on line \ell_5
                                                                     369: P_{30974} = (29, 6, 29, 1) lies on line \ell_{11}
                                                                     370 : P_{30989} = (12, 7, 29, 1) lies on line \ell_7
316: P_{26466} = (1, 26, 24, 1) lies on line \ell_{10}
317: P_{26488} = (23, 26, 24, 1) lies on line \ell_6
                                                                     371: P_{31025} = (16, 8, 29, 1) lies on line \ell_{10}
318: P_{26722} = (1, 2, 25, 1) lies on line \ell_3
                                                                     372: P_{31049} = (8, 9, 29, 1) lies on line \ell_2
319: P_{26757} = (4, 3, 25, 1) lies on line \ell_{10}
                                                                     373: P_{31133} = (28, 11, 29, 1) lies on line \ell_0
320: P_{27018} = (9, 11, 25, 1) lies on line \ell_5
                                                                     374: P_{31164} = (27, 12, 29, 1) lies on line \ell_{13}
321: P_{27065} = (24, 12, 25, 1) lies on line \ell_2
                                                                     375: P_{31170} = (1, 13, 29, 1) lies on line \ell_5
                                                                     376: P_{31216} = (15, 14, 29, 1) lies on line \ell_9
322: P_{27132} = (27, 14, 25, 1) lies on line \ell_6
323: P_{27151} = (14, 15, 25, 1) lies on line \ell_4
                                                                     377: P_{31244} = (11, 15, 29, 1) lies on line \ell_3
                                                                     378 : P_{31360} = (31, 18, 29, 1) lies on line \ell_4
324: P_{27264} = (31, 18, 25, 1) lies on line \ell_{14}
325: P_{27283} = (18, 19, 25, 1) lies on line \ell_0
                                                                     379: P_{31407} = (14, 20, 29, 1) lies on line \ell_6
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380: P_{31432} = (7, 21, 29, 1) lies on line \ell_1
                                                                     393: P_{32712} = (7, 29, 30, 1) lies on line \ell_5
381 : P_{31785} = (8, 0, 30, 1) lies on line \ell_4
                                                                     394: P_{32761} = (24, 30, 30, 1) lies on line \ell_7
382: P_{31819} = (10, 1, 30, 1) lies on line \ell_0
                                                                     395: P_{32786} = (17, 31, 30, 1) lies on line \ell_1
383: P_{31861} = (20, 2, 30, 1) lies on line \ell_{14}
                                                                     396: P_{33034} = (9,7,31,1) lies on line \ell_9
384: P_{31989} = (20, 6, 30, 1) lies on line \ell_{12}
                                                                     397: P_{33052} = (27, 7, 31, 1) lies on line \ell_0
385: P_{32000} = (31, 6, 30, 1) lies on line \ell_{10}
                                                                     398: P_{33141} = (20, 10, 31, 1) lies on line \ell_7
386: P_{32051} = (18, 8, 30, 1) lies on line \ell_{11}
                                                                     399: P_{33242} = (25, 13, 31, 1) lies on line \ell_8
387: P_{32219} = (26, 13, 30, 1) lies on line \ell_6
                                                                     400: P_{33368} = (23, 17, 31, 1) lies on line \ell_{11}
388: P_{32241} = (16, 14, 30, 1) lies on line \ell_{13}
                                                                     401: P_{33419} = (10, 19, 31, 1) lies on line \ell_{13}
389: P_{32325} = (4, 17, 30, 1) lies on line \ell_2
                                                                     402: P_{33623} = (22, 25, 31, 1) lies on line \ell_6
390: P_{32331} = (10, 17, 30, 1) lies on line \ell_9
                                                                     403: P_{33712} = (15, 28, 31, 1) lies on line \ell_{14}
391 : P_{32351} = (30, 17, 30, 1) lies on line \ell_3
                                                                     404: P_{33819} = (26, 31, 31, 1) lies on line \ell_{10}
392: P_{32667} = (26, 27, 30, 1) lies on line \ell_8
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The single points on the surface are:

#### Points on surface but on no line

The surface has 735 points not on any line: The points on the surface but not on lines are:

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0: P_{36} = (1,0,1,0)
                                                                  31: P_{1830} = (4, 24, 0, 1)
1: P_{67} = (0, 1, 1, 0)
                                                                  32: P_{1857} = (31, 24, 0, 1)
2: P_{235} = (8, 6, 1, 0)
                                                                  33: P_{1918} = (28, 26, 0, 1)
3: P_{258} = (31, 6, 1, 0)
                                                                  34: P_{1925} = (3, 27, 0, 1)
4: P_{685} = (10, 20, 1, 0)
                                                                  35: P_{1965} = (11, 28, 0, 1)
5: P_{693} = (18, 20, 1, 0)
                                                                  36: P_{1967} = (13, 28, 0, 1)
6: P_{750} = (11, 22, 1, 0)
                                                                  37: P_{1981} = (27, 28, 0, 1)
7: P_{769} = (30, 22, 1, 0)
                                                                  38: P_{2082} = (0, 0, 1, 1)
8: P_{850} = (15, 25, 1, 0)
                                                                  39: P_{2083} = (1,0,1,1)
9: P_{854} = (19, 25, 1, 0)
                                                                  40: P_{2327} = (22, 7, 1, 1)
10: P_{972} = (9, 29, 1, 0)
                                                                  41: P_{2335} = (30, 7, 1, 1)
11: P_{977} = (14, 29, 1, 0)
                                                                  42: P_{2372} = (3, 9, 1, 1)
12: P_{1090} = (0, 1, 0, 1)
                                                                  43: P_{2438} = (5, 11, 1, 1)
13: P_{1127} = (5, 2, 0, 1)
                                                                  44: P_{2578} = (17, 15, 1, 1)
14: P_{1177} = (23, 3, 0, 1)
                                                                  45: P_{2683} = (26, 18, 1, 1)
                                                                  46: P_{2772} = (19, 21, 1, 1)
15: P_{1203} = (17, 4, 0, 1)
16: P_{1242} = (24, 5, 0, 1)
                                                                  47: P_{2778} = (25, 21, 1, 1)
17: P_{1286} = (4,7,0,1)
                                                                  48: P_{2827} = (10, 23, 1, 1)
18: P_{1298} = (16, 7, 0, 1)
                                                                  49: P_{2837} = (20, 23, 1, 1)
19: P_{1300} = (18, 7, 0, 1)
                                                                  50: P_{2863} = (14, 24, 1, 1)
                                                                  51: P_{2878} = (29, 24, 1, 1)
20: P_{1463} = (21, 12, 0, 1)
21: P_{1500} = (26, 13, 0, 1)
                                                                  52: P_{2983} = (6, 28, 1, 1)
22: P_{1582} = (12, 16, 0, 1)
                                                                  53: P_{2985} = (8, 28, 1, 1)
23: P_{1609} = (7, 17, 0, 1)
                                                                  54: P_{3085} = (12, 31, 1, 1)
24: P_{1739} = (9, 21, 0, 1)
                                                                  55: P_{3177} = (8, 2, 2, 1)
25: P_{1743} = (13, 21, 0, 1)
                                                                  56: P_{3211} = (10, 3, 2, 1)
                                                                  57: P_{3214} = (13, 3, 2, 1)
26: P_{1746} = (16, 21, 0, 1)
27: P_{1796} = (2, 23, 0, 1)
                                                                  58: P_{3287} = (22, 5, 2, 1)
28: P_{1809} = (15, 23, 0, 1)
                                                                  59: P_{3288} = (23, 5, 2, 1)
29: P_{1821} = (27, 23, 0, 1)
                                                                  60: P_{3302} = (5, 6, 2, 1)
30: P_{1828} = (2, 24, 0, 1)
                                                                  61: P_{3489} = (0, 12, 2, 1)
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62: P_{3555} = (2, 14, 2, 1)
                                                                 116: P_{6291} = (18, 3, 5, 1)
63: P_{3642} = (25, 16, 2, 1)
                                                                 117: P_{6363} = (26, 5, 5, 1)
                                                                 118: P_{6413} = (12, 7, 5, 1)
64: P_{3653} = (4, 17, 2, 1)
65: P_{3758} = (13, 20, 2, 1)
                                                                 119: P_{6425} = (24, 7, 5, 1)
66: P_{3820} = (11, 22, 2, 1)
                                                                 120: P_{6464} = (31, 8, 5, 1)
67: P_{3949} = (12, 26, 2, 1)
                                                                 121: P_{6507} = (10, 10, 5, 1)
68: P_{3993} = (24, 27, 2, 1)
                                                                 122: P_{6527} = (30, 10, 5, 1)
69: P_{4019} = (18, 28, 2, 1)
                                                                 123: P_{6528} = (31, 10, 5, 1)
70: P_{4031} = (30, 28, 2, 1)
                                                                 124: P_{6593} = (0, 13, 5, 1)
71: P_{4112} = (15, 31, 2, 1)
                                                                 125: P_{6607} = (14, 13, 5, 1)
72: P_{4134} = (5,0,3,1)
                                                                 126: P_{6647} = (22, 14, 5, 1)
73: P_{4185} = (24, 1, 3, 1)
                                                                 127: P_{6693} = (4, 16, 5, 1)
74: P_{4237} = (12, 3, 3, 1)
                                                                 128: P_{6795} = (10, 19, 5, 1)
75: P_{4259} = (2, 4, 3, 1)
                                                                 129: P_{6854} = (5, 21, 5, 1)
76: P_{4356} = (3,7,3,1)
                                                                 130: P_{6887} = (6, 22, 5, 1)
77: P_{4393} = (8, 8, 3, 1)
                                                                 131: P_{6888} = (7, 22, 5, 1)
78: P_{4399} = (14, 8, 3, 1)
                                                                 132: P_{6968} = (23, 24, 5, 1)
79: P_{4400} = (15, 8, 3, 1)
                                                                 133: P_{6969} = (24, 24, 5, 1)
                                                                 134: P_{6983} = (6, 25, 5, 1)
80: P_{4478} = (29, 10, 3, 1)
81: P_{4539} = (26, 12, 3, 1)
                                                                 135: P_{7012} = (3, 26, 5, 1)
82: P_{4582} = (5, 14, 3, 1)
                                                                 136: P_{7121} = (16, 29, 5, 1)
                                                                 137: P_{7154} = (17, 30, 5, 1)
83: P_{4632} = (23, 15, 3, 1)
                                                                 138: P_{7193} = (24, 31, 5, 1)
84: P_{4641} = (0, 16, 3, 1)
85: P_{4651} = (10, 16, 3, 1)
                                                                 139: P_{7280} = (15, 2, 6, 1)
86: P_{4752} = (15, 19, 3, 1)
                                                                 140: P_{7284} = (19, 2, 6, 1)
87: P_{4773} = (4, 20, 3, 1)
                                                                 141: P_{7296} = (31, 2, 6, 1)
                                                                 142: P_{7417} = (24, 6, 6, 1)
88: P_{4858} = (25, 22, 3, 1)
89: P_{4888} = (23, 23, 3, 1)
                                                                 143: P_{7464} = (7, 8, 6, 1)
90: P_{4893} = (28, 23, 3, 1)
                                                                 144: P_{7645} = (28, 13, 6, 1)
91: P_{4914} = (17, 24, 3, 1)
                                                                 145: P_{7651} = (2, 14, 6, 1)
92: P_{4920} = (23, 24, 3, 1)
                                                                 146: P_{7715} = (2, 16, 6, 1)
93: P_{4992} = (31, 26, 3, 1)
                                                                 147: P_{7761} = (16, 17, 6, 1)
94: P_{5081} = (24, 29, 3, 1)
                                                                 148: P_{7763} = (18, 17, 6, 1)
95: P_{5082} = (25, 29, 3, 1)
                                                                 149: P_{7777} = (0, 18, 6, 1)
96: P_{5097} = (8, 30, 3, 1)
                                                                 150: P_{7797} = (20, 18, 6, 1)
97: P_{5224} = (7, 2, 4, 1)
                                                                 151: P_{7852} = (11, 20, 6, 1)
98: P_{5275} = (26, 3, 4, 1)
                                                                 152: P_{7855} = (14, 20, 6, 1)
                                                                 153: P_{7857} = (16, 20, 6, 1)
99: P_{5291} = (10, 4, 4, 1)
100: P_{5327} = (14, 5, 4, 1)
                                                                 154: P_{7901} = (28, 21, 6, 1)
101: P_{5340} = (27, 5, 4, 1)
                                                                 155: P_{7987} = (18, 24, 6, 1)
102: P_{5553} = (16, 12, 4, 1)
                                                                 156: P_{7997} = (28, 24, 6, 1)
103: P_{5575} = (6, 13, 4, 1)
                                                                 157: P_{8043} = (10, 26, 6, 1)
104: P_{5721} = (24, 17, 4, 1)
                                                                 158: P_{8055} = (22, 26, 6, 1)
                                                                 159: P_{8148} = (19, 29, 6, 1)
105: P_{5722} = (25, 17, 4, 1)
106: P_{5760} = (31, 18, 4, 1)
                                                                 160: P_{8212} = (19, 31, 6, 1)
                                                                 161: P_{8245} = (20, 0, 7, 1)
107: P_{5810} = (17, 20, 4, 1)
108: P_{5898} = (9, 23, 4, 1)
                                                                 162: P_{8249} = (24, 0, 7, 1)
109: P_{5908} = (19, 23, 4, 1)
                                                                 163: P_{8348} = (27, 3, 7, 1)
                                                                 164: P_{8431} = (14, 6, 7, 1)
110: P_{5968} = (15, 25, 4, 1)
111: P_{5985} = (0, 26, 4, 1)
                                                                 165: P_{8507} = (26, 8, 7, 1)
112: P_{6108} = (27, 29, 4, 1)
                                                                 166: P_{8515} = (2, 9, 7, 1)
113: P_{6117} = (4, 30, 4, 1)
                                                                 167: P_{8561} = (16, 10, 7, 1)
114: P_{6194} = (17, 0, 5, 1)
                                                                 168: P_{8568} = (23, 10, 7, 1)
115: P_{6216} = (7, 1, 5, 1)
                                                                 169: P_{8620} = (11, 12, 7, 1)
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170: P_{8668} = (27, 13, 7, 1)
                                                                224: P_{10892} = (11, 19, 9, 1)
171: P_{8700} = (27, 14, 7, 1)
                                                                225: P_{10902} = (21, 19, 9, 1)
172: P_{8753} = (16, 16, 7, 1)
                                                                226: P_{10932} = (19, 20, 9, 1)
173: P_{8759} = (22, 16, 7, 1)
                                                                227: P_{10957} = (12, 21, 9, 1)
174: P_{8771} = (2, 17, 7, 1)
                                                                228: P_{11002} = (25, 22, 9, 1)
175: P_{8783} = (14, 17, 7, 1)
                                                                229: P_{11011} = (2, 23, 9, 1)
176: P_{8797} = (28, 17, 7, 1)
                                                                230: P_{11099} = (26, 25, 9, 1)
177: P_{8819} = (18, 18, 7, 1)
                                                                231: P_{11191} = (22, 28, 9, 1)
178: P_{8878} = (13, 20, 7, 1)
                                                                232: P_{11272} = (7, 31, 9, 1)
179: P_{8923} = (26, 21, 7, 1)
                                                                233: P_{11342} = (13, 1, 10, 1)
180: P_{8967} = (6, 23, 7, 1)
                                                                234: P_{11359} = (30, 1, 10, 1)
181: P_{8975} = (14, 23, 7, 1)
                                                                235: P_{11380} = (19, 2, 10, 1)
182: P_{8991} = (30, 23, 7, 1)
                                                                236: P_{11471} = (14, 5, 10, 1)
                                                                237: P_{11494} = (5, 6, 10, 1)
183: P_{8995} = (2, 24, 7, 1)
184: P_{9080} = (23, 26, 7, 1)
                                                                238: P_{11510} = (21, 6, 10, 1)
185: P_{9085} = (28, 26, 7, 1)
                                                                239: P_{11536} = (15, 7, 10, 1)
186: P_{9156} = (3, 29, 7, 1)
                                                                240: P_{11569} = (16, 8, 10, 1)
                                                                241: P_{11580} = (27, 8, 10, 1)
187: P_{9158} = (5, 29, 7, 1)
188: P_{9295} = (14, 1, 8, 1)
                                                                242: P_{11625} = (8, 10, 10, 1)
189: P_{9297} = (16, 1, 8, 1)
                                                                243: P_{11648} = (31, 10, 10, 1)
190: P_{9355} = (10, 3, 8, 1)
                                                                244: P_{11667} = (18, 11, 10, 1)
191: P_{9380} = (3, 4, 8, 1)
                                                                245: P_{11676} = (27, 11, 10, 1)
192: P_{9426} = (17, 5, 8, 1)
                                                                246: P_{11769} = (24, 14, 10, 1)
193: P_{9446} = (5, 6, 8, 1)
                                                                247: P_{11784} = (7, 15, 10, 1)
194: P_{9520} = (15, 8, 8, 1)
                                                                248: P_{11814} = (5, 16, 10, 1)
195: P_{9524} = (19, 8, 8, 1)
                                                                249: P_{11853} = (12, 17, 10, 1)
196: P_{9550} = (13, 9, 8, 1)
                                                                250: P_{11908} = (3, 19, 10, 1)
197: P_{9568} = (31, 9, 8, 1)
                                                                251: P_{11954} = (17, 20, 10, 1)
198: P_{9592} = (23, 10, 8, 1)
                                                                252: P_{12006} = (5, 22, 10, 1)
199: P_{9625} = (24, 11, 8, 1)
                                                                253: P_{12065} = (0, 24, 10, 1)
200: P_{9687} = (22, 13, 8, 1)
                                                                254: P_{12068} = (3, 24, 10, 1)
201: P_{9861} = (4, 19, 8, 1)
                                                                255: P_{12091} = (26, 24, 10, 1)
202: P_{9870} = (13, 19, 8, 1)
                                                                256: P_{12112} = (15, 25, 10, 1)
203: P_{9964} = (11, 22, 8, 1)
                                                                257: P_{12186} = (25, 27, 10, 1)
204: P_{9985} = (0, 23, 8, 1)
                                                                258: P_{12450} = (1, 4, 11, 1)
205: P_{9997} = (12, 23, 8, 1)
                                                                259: P_{12474} = (25, 4, 11, 1)
206: P_{10011} = (26, 23, 8, 1)
                                                                260: P_{12516} = (3, 6, 11, 1)
207: P_{10028} = (11, 24, 8, 1)
                                                                261: P_{12592} = (15, 8, 11, 1)
208: P_{10052} = (3, 25, 8, 1)
                                                                262: P_{12605} = (28, 8, 11, 1)
209: P_{10056} = (7, 25, 8, 1)
                                                                263: P_{12639} = (30, 9, 11, 1)
210: P_{10143} = (30, 27, 8, 1)
                                                                264: P_{12729} = (24, 12, 11, 1)
211: P_{10180} = (3, 29, 8, 1)
                                                                265: P_{12745} = (8, 13, 11, 1)
212: P_{10235} = (26, 30, 8, 1)
                                                                266: P_{12844} = (11, 16, 11, 1)
213: P_{10338} = (1, 2, 9, 1)
                                                                267: P_{12851} = (18, 16, 11, 1)
214: P_{10359} = (22, 2, 9, 1)
                                                                268: P_{12886} = (21, 17, 11, 1)
215: P_{10410} = (9, 4, 9, 1)
                                                                269: P_{12918} = (21, 18, 11, 1)
216: P_{10432} = (31, 4, 9, 1)
                                                                270: P_{12987} = (26, 20, 11, 1)
217: P_{10440} = (7, 5, 9, 1)
                                                                271: P_{13082} = (25, 23, 11, 1)
218: P_{10477} = (12, 6, 9, 1)
                                                                272: P_{13093} = (4, 24, 11, 1)
219: P_{10667} = (10, 12, 9, 1)
                                                                273: P_{13127} = (6, 25, 11, 1)
220: P_{10702} = (13, 13, 9, 1)
                                                                274: P_{13167} = (14, 26, 11, 1)
221: P_{10804} = (19, 16, 9, 1)
                                                                275: P_{13212} = (27, 27, 11, 1)
222: P_{10840} = (23, 17, 9, 1)
                                                                276: P_{13243} = (26, 28, 11, 1)
223: P_{10863} = (14, 18, 9, 1)
                                                                277: P_{13257} = (8, 29, 11, 1)
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332: P_{15826} = (17, 13, 14, 1)
278: P_{13371} = (26, 0, 12, 1)
279: P_{13405} = (28, 1, 12, 1)
                                                                333: P_{15851} = (10, 14, 14, 1)
280: P_{13409} = (0, 2, 12, 1)
                                                                334: P_{15859} = (18, 14, 14, 1)
281: P_{13428} = (19, 2, 12, 1)
                                                                335: P_{15875} = (2, 15, 14, 1)
282: P_{13522} = (17, 5, 12, 1)
                                                                336: P_{15882} = (9, 15, 14, 1)
283: P_{13565} = (28, 6, 12, 1)
                                                                337: P_{15967} = (30, 17, 14, 1)
284: P_{13566} = (29, 6, 12, 1)
                                                                338: P_{16050} = (17, 20, 14, 1)
285: P_{13627} = (26, 8, 12, 1)
                                                                339: P_{16061} = (28, 20, 14, 1)
286: P_{13654} = (21, 9, 12, 1)
                                                                340: P_{16096} = (31, 21, 14, 1)
287: P_{13695} = (30, 10, 12, 1)
                                                                341: P_{16210} = (17, 25, 14, 1)
288: P_{13734} = (5, 12, 12, 1)
                                                                342: P_{16333} = (12, 29, 14, 1)
289: P_{13802} = (9, 14, 12, 1)
                                                                343: P_{16360} = (7, 30, 14, 1)
290: P_{13900} = (11, 17, 12, 1)
                                                                344: P_{16406} = (21, 31, 14, 1)
291: P_{13959} = (6, 19, 12, 1)
                                                                345: P_{16483} = (2, 2, 15, 1)
292: P_{14014} = (29, 20, 12, 1)
                                                                346: P_{16543} = (30, 3, 15, 1)
293: P_{14024} = (7, 21, 12, 1)
                                                                347: P_{16629} = (20, 6, 15, 1)
294: P_{14038} = (21, 21, 12, 1)
                                                                348: P_{16657} = (16, 7, 15, 1)
295: P_{14093} = (12, 23, 12, 1)
                                                                349: P_{16733} = (28, 9, 15, 1)
296: P_{14172} = (27, 25, 12, 1)
                                                                350: P_{16760} = (23, 10, 15, 1)
                                                                351: P_{16768} = (31, 10, 15, 1)
297: P_{14222} = (13, 27, 12, 1)
298: P_{14244} = (3, 28, 12, 1)
                                                                352: P_{16788} = (19, 11, 15, 1)
299: P_{14262} = (21, 28, 12, 1)
                                                                353: P_{16829} = (28, 12, 15, 1)
300: P_{14313} = (8, 30, 12, 1)
                                                                354: P_{16842} = (9, 13, 15, 1)
301: P_{14314} = (9, 30, 12, 1)
                                                                355: P_{16848} = (15, 13, 15, 1)
302: P_{14335} = (30, 30, 12, 1)
                                                                356: P_{16930} = (1, 16, 15, 1)
303: P_{14462} = (29, 2, 13, 1)
                                                                357: P_{16935} = (6, 16, 15, 1)
304: P_{14492} = (27, 3, 13, 1)
                                                                358: P_{17062} = (5, 20, 15, 1)
305: P_{14529} = (0, 5, 13, 1)
                                                                359: P_{17131} = (10, 22, 15, 1)
306: P_{14603} = (10, 7, 13, 1)
                                                                360: P_{17156} = (3, 23, 15, 1)
307: P_{14608} = (15, 7, 13, 1)
                                                                361: P_{17191} = (6, 24, 15, 1)
308: P_{14638} = (13, 8, 13, 1)
                                                                362: P_{17256} = (7, 26, 15, 1)
309: P_{14730} = (9, 11, 13, 1)
                                                                363: P_{17291} = (10, 27, 15, 1)
310: P_{14757} = (4, 12, 13, 1)
                                                                364: P_{17348} = (3, 29, 15, 1)
311: P_{14772} = (19, 12, 13, 1)
                                                                365: P_{17537} = (0, 3, 16, 1)
312: P_{14815} = (30, 13, 13, 1)
                                                                366: P_{17590} = (21, 4, 16, 1)
313: P_{14909} = (28, 16, 13, 1)
                                                                367: P_{17604} = (3, 5, 16, 1)
314: P_{14918} = (5, 17, 13, 1)
                                                                368: P_{17664} = (31, 6, 16, 1)
315: P_{15027} = (18, 20, 13, 1)
                                                                369: P_{17747} = (18, 9, 16, 1)
316: P_{15099} = (26, 22, 13, 1)
                                                                370: P_{17831} = (6, 12, 16, 1)
317: P_{15173} = (4, 25, 13, 1)
                                                                371: P_{17832} = (7, 12, 16, 1)
318: P_{15221} = (20, 26, 13, 1)
                                                                372: P_{17967} = (14, 16, 16, 1)
                                                                373: P_{17987} = (2, 17, 16, 1)
319: P_{15222} = (21, 26, 13, 1)
320: P_{15444} = (19, 1, 14, 1)
                                                                374: P_{18015} = (30, 17, 16, 1)
321: P_{15452} = (27, 1, 14, 1)
                                                                375: P_{18065} = (16, 19, 16, 1)
322: P_{15463} = (6, 2, 14, 1)
                                                                376: P_{18147} = (2, 22, 16, 1)
323: P_{15529} = (8, 4, 14, 1)
                                                                377: P_{18217} = (8, 24, 16, 1)
324: P_{15616} = (31, 6, 14, 1)
                                                                378: P_{18220} = (11, 24, 16, 1)
325: P_{15617} = (0, 7, 14, 1)
                                                                379: P_{18286} = (13, 26, 16, 1)
326: P_{15620} = (3, 7, 14, 1)
                                                                380: P_{18325} = (20, 27, 16, 1)
327: P_{15622} = (5, 7, 14, 1)
                                                                381: P_{18381} = (12, 29, 16, 1)
328: P_{15654} = (5, 8, 14, 1)
                                                                382: P_{18477} = (12, 0, 17, 1)
329: P_{15715} = (2, 10, 14, 1)
                                                                383: P_{18518} = (21, 1, 17, 1)
330: P_{15726} = (13, 10, 14, 1)
                                                                384: P_{18566} = (5, 3, 17, 1)
331: P_{15803} = (26, 12, 14, 1)
                                                                385: P_{18634} = (9, 5, 17, 1)
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386: P_{18677} = (20, 6, 17, 1)
                                                                440: P_{21179} = (26, 20, 19, 1)
                                                                441: P_{21241} = (24, 22, 19, 1)
387: P_{18696} = (7,7,17,1)
388: P_{18713} = (24, 7, 17, 1)
                                                                442: P_{21243} = (26, 22, 19, 1)
389: P_{18735} = (14, 8, 17, 1)
                                                                443: P_{21258} = (9, 23, 19, 1)
390: P_{18803} = (18, 10, 17, 1)
                                                                444: P_{21316} = (3, 25, 19, 1)
391: P_{18897} = (16, 13, 17, 1)
                                                                445: P_{21353} = (8, 26, 19, 1)
392: P_{18927} = (14, 14, 17, 1)
                                                                446: P_{21409} = (0, 28, 19, 1)
393: P_{18931} = (18, 14, 17, 1)
                                                                447: P_{21421} = (12, 28, 19, 1)
394: P_{18932} = (19, 14, 17, 1)
                                                                448: P_{21426} = (17, 28, 19, 1)
395: P_{19012} = (3, 17, 17, 1)
                                                                449: P_{21450} = (9, 29, 19, 1)
396: P_{19048} = (7, 18, 17, 1)
                                                                450: P_{21475} = (2, 30, 19, 1)
397: P_{19085} = (12, 19, 17, 1)
                                                                451: P_{21489} = (16, 30, 19, 1)
                                                                452: P_{21647} = (14, 3, 20, 1)
398: P_{19144} = (7, 21, 17, 1)
399: P_{19163} = (26, 21, 17, 1)
                                                                453: P_{21658} = (25, 3, 20, 1)
400: P_{19182} = (13, 22, 17, 1)
                                                                454: P_{21673} = (8, 4, 20, 1)
401: P_{19285} = (20, 25, 17, 1)
                                                                455: P_{21683} = (18, 4, 20, 1)
402: P_{19286} = (21, 25, 17, 1)
                                                                456: P_{21696} = (31, 4, 20, 1)
403: P_{19329} = (0, 27, 17, 1)
                                                                457: P_{21770} = (9, 7, 20, 1)
404: P_{19359} = (30, 27, 17, 1)
                                                                458: P_{21784} = (23, 7, 20, 1)
405: P_{19378} = (17, 28, 17, 1)
                                                                459: P_{21825} = (0, 9, 20, 1)
406: P_{19450} = (25, 30, 17, 1)
                                                                460: P_{21854} = (29, 9, 20, 1)
407: P_{19568} = (15, 2, 18, 1)
                                                                461: P_{21878} = (21, 10, 20, 1)
408: P_{19571} = (18, 2, 18, 1)
                                                                462: P_{21930} = (9, 12, 20, 1)
409: P_{19609} = (24, 3, 18, 1)
                                                                463: P_{21934} = (13, 12, 20, 1)
410: P_{19647} = (30, 4, 18, 1)
                                                                464: P_{21957} = (4, 13, 20, 1)
411: P_{19677} = (28, 5, 18, 1)
                                                                465: P_{22121} = (8, 18, 20, 1)
412: P_{19711} = (30, 6, 18, 1)
                                                                466: P_{22184} = (7, 20, 20, 1)
413: P_{19730} = (17, 7, 18, 1)
                                                                467: P_{22249} = (8, 22, 20, 1)
414: P_{19993} = (24, 15, 18, 1)
                                                                468: P_{22424} = (23, 27, 20, 1)
                                                                469: P_{22456} = (23, 28, 20, 1)
415: P_{20017} = (16, 16, 18, 1)
416: P_{20041} = (8, 17, 18, 1)
                                                                470: P_{22478} = (13, 29, 20, 1)
417: P_{20190} = (29, 21, 18, 1)
                                                                471: P_{22480} = (15, 29, 20, 1)
418: P_{20205} = (12, 22, 18, 1)
                                                                472: P_{22495} = (30, 29, 20, 1)
419: P_{20306} = (17, 25, 18, 1)
                                                                473: P_{22501} = (4, 30, 20, 1)
420: P_{20354} = (1, 27, 18, 1)
                                                                474: P_{22568} = (7, 0, 21, 1)
421: P_{20382} = (29, 27, 18, 1)
                                                                475: P_{22590} = (29, 0, 21, 1)
422: P_{20412} = (27, 28, 18, 1)
                                                                476: P_{22680} = (23, 3, 21, 1)
423: P_{20439} = (22, 29, 18, 1)
                                                                477: P_{22681} = (24, 3, 21, 1)
424: P_{20456} = (7, 30, 18, 1)
                                                                478: P_{22723} = (2, 5, 21, 1)
425: P_{20458} = (9, 30, 18, 1)
                                                                479: P_{22789} = (4,7,21,1)
426: P_{20491} = (10, 31, 18, 1)
                                                                480: P_{22858} = (9, 9, 21, 1)
427: P_{20549} = (4, 1, 19, 1)
                                                                481: P_{22884} = (3, 10, 21, 1)
428: P_{20555} = (10, 1, 19, 1)
                                                                482: P_{22917} = (4, 11, 21, 1)
429: P_{20603} = (26, 2, 19, 1)
                                                                483: P_{22949} = (4, 12, 21, 1)
430: P_{20614} = (5, 3, 19, 1)
                                                                484: P_{22968} = (23, 12, 21, 1)
431: P_{20797} = (28, 8, 19, 1)
                                                                485: P_{22975} = (30, 12, 21, 1)
432: P_{20824} = (23, 9, 19, 1)
                                                                486: P_{22990} = (13, 13, 21, 1)
433: P_{20943} = (14, 13, 19, 1)
                                                                487: P_{23002} = (25, 13, 21, 1)
434: P_{20973} = (12, 14, 19, 1)
                                                                488: P_{23022} = (13, 14, 21, 1)
435: P_{21054} = (29, 16, 19, 1)
                                                                489: P_{23033} = (24, 14, 21, 1)
436: P_{21104} = (15, 18, 19, 1)
                                                                490: P_{23231} = (30, 20, 21, 1)
437: P_{21105} = (16, 18, 19, 1)
                                                                491: P_{23270} = (5, 22, 21, 1)
438: P_{21132} = (11, 19, 19, 1)
                                                                492: P_{23282} = (17, 22, 21, 1)
439: P_{21151} = (30, 19, 19, 1)
                                                                493: P_{23348} = (19, 24, 21, 1)
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548: P_{25586} = (17, 30, 23, 1)
494: P_{23349} = (20, 24, 21, 1)
495: P_{23359} = (30, 24, 21, 1)
                                                                549: P_{25614} = (13, 31, 23, 1)
496: P_{23408} = (15, 26, 21, 1)
                                                                550: P_{25639} = (6, 0, 24, 1)
497: P_{23427} = (2, 27, 21, 1)
                                                                551: P_{25656} = (23, 0, 24, 1)
498: P_{23460} = (3, 28, 21, 1)
                                                                552: P_{25765} = (4, 4, 24, 1)
499: P_{23516} = (27, 29, 21, 1)
                                                                553: P_{25790} = (29, 4, 24, 1)
500: P_{23523} = (2, 30, 21, 1)
                                                                554: P_{25803} = (10, 5, 24, 1)
501: P_{23662} = (13, 2, 22, 1)
                                                                555: P_{25814} = (21, 5, 24, 1)
502: P_{23683} = (2, 3, 22, 1)
                                                                556: P_{25820} = (27, 5, 24, 1)
503: P_{23696} = (15, 3, 22, 1)
                                                                557: P_{25841} = (16, 6, 24, 1)
504: P_{23720} = (7, 4, 22, 1)
                                                                558: P_{25869} = (12, 7, 24, 1)
505: P_{23791} = (14, 6, 22, 1)
                                                                559: P_{25893} = (4, 8, 24, 1)
506: P_{23854} = (13, 8, 22, 1)
                                                                560: P_{25917} = (28, 8, 24, 1)
507: P_{23951} = (14, 11, 22, 1)
                                                                561: P_{25966} = (13, 10, 24, 1)
508: P_{24010} = (9, 13, 22, 1)
                                                                562: P_{26038} = (21, 12, 24, 1)
509: P_{24012} = (11, 13, 22, 1)
                                                                563: P_{26045} = (28, 12, 24, 1)
510: P_{24015} = (14, 13, 22, 1)
                                                                564: P_{26158} = (13, 16, 24, 1)
                                                                565: P_{26186} = (9, 17, 24, 1)
511: P_{24065} = (0, 15, 22, 1)
                                                                566: P_{26236} = (27, 18, 24, 1)
512: P_{24090} = (25, 15, 22, 1)
513: P_{24148} = (19, 17, 22, 1)
                                                                567: P_{26253} = (12, 19, 24, 1)
514: P_{24149} = (20, 17, 22, 1)
                                                                568: P_{26276} = (3, 20, 24, 1)
515: P_{24317} = (28, 22, 22, 1)
                                                                569: P_{26299} = (26, 20, 24, 1)
516: P_{24360} = (7, 24, 22, 1)
                                                                570: P_{26396} = (27, 23, 24, 1)
517: P_{24387} = (2, 25, 22, 1)
                                                                571: P_{26443} = (10, 25, 24, 1)
518: P_{24393} = (8, 25, 22, 1)
                                                                572: P_{26478} = (13, 26, 24, 1)
519: P_{24403} = (18, 25, 22, 1)
                                                                573: P_{26539} = (10, 28, 24, 1)
520: P_{24488} = (7, 28, 22, 1)
                                                                574: P_{26543} = (14, 28, 24, 1)
521: P_{24496} = (15, 28, 22, 1)
                                                                575: P_{26554} = (25, 28, 24, 1)
522: P_{24568} = (23, 30, 22, 1)
                                                                576: P_{26656} = (31, 31, 24, 1)
523: P_{24634} = (25, 0, 23, 1)
                                                                577: P_{26812} = (27, 4, 25, 1)
524: P_{24637} = (28, 0, 23, 1)
                                                                578: P_{26821} = (4, 5, 25, 1)
525: P_{24675} = (2, 2, 23, 1)
                                                                579: P_{26848} = (31, 5, 25, 1)
526: P_{24693} = (20, 2, 23, 1)
                                                                580: P_{26853} = (4, 6, 25, 1)
527: P_{24712} = (7, 3, 23, 1)
                                                                581: P_{26858} = (9, 6, 25, 1)
528: P_{24713} = (8, 3, 23, 1)
                                                                582: P_{26859} = (10, 6, 25, 1)
529: P_{24718} = (13, 3, 23, 1)
                                                                583: P_{26902} = (21, 7, 25, 1)
530: P_{24753} = (16, 4, 23, 1)
                                                                584: P_{27004} = (27, 10, 25, 1)
531: P_{24787} = (18, 5, 23, 1)
                                                                585: P_{27049} = (8, 12, 25, 1)
532: P_{24813} = (12, 6, 23, 1)
                                                                586: P_{27070} = (29, 12, 25, 1)
533: P_{24827} = (26, 6, 23, 1)
                                                                587: P_{27167} = (30, 15, 25, 1)
534: P_{24881} = (16, 8, 23, 1)
                                                                588: P_{27190} = (21, 16, 25, 1)
                                                                589: P_{27289} = (24, 19, 25, 1)
535: P_{25009} = (16, 12, 23, 1)
536: P_{25104} = (15, 15, 23, 1)
                                                                590: P_{27327} = (30, 20, 25, 1)
537: P_{25160} = (7, 17, 23, 1)
                                                                591: P_{27414} = (21, 23, 25, 1)
538: P_{25174} = (21, 17, 23, 1)
                                                                592: P_{27424} = (31, 23, 25, 1)
539: P_{25219} = (2, 19, 23, 1)
                                                                593: P_{27480} = (23, 25, 25, 1)
540: P_{25238} = (21, 19, 23, 1)
                                                                594: P_{27532} = (11, 27, 25, 1)
541: P_{25289} = (8, 21, 23, 1)
                                                                595: P_{27536} = (15, 27, 25, 1)
542: P_{25291} = (10, 21, 23, 1)
                                                                596: P_{27551} = (30, 27, 25, 1)
543: P_{25303} = (22, 21, 23, 1)
                                                                597: P_{27649} = (0, 31, 25, 1)
544: P_{25321} = (8, 22, 23, 1)
                                                                598: P_{27655} = (6, 31, 25, 1)
545: P_{25394} = (17, 24, 23, 1)
                                                                599: P_{27684} = (3, 0, 26, 1)
546: P_{25413} = (4, 25, 23, 1)
                                                                600: P_{27736} = (23, 1, 26, 1)
547: P_{25518} = (13, 28, 23, 1)
                                                                601: P_{27772} = (27, 2, 26, 1)
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602: P_{27809} = (0, 4, 26, 1)
                                                                656: P_{30435} = (2, 22, 28, 1)
603: P_{27817} = (8, 4, 26, 1)
                                                                657: P_{30470} = (5, 23, 28, 1)
604: P_{27875} = (2, 6, 26, 1)
                                                                658: P_{30541} = (12, 25, 28, 1)
605: P_{27957} = (20, 8, 26, 1)
                                                                659: P_{30546} = (17, 25, 28, 1)
606: P_{28004} = (3, 10, 26, 1)
                                                                660: P_{30577} = (16, 26, 28, 1)
607: P_{28061} = (28, 11, 26, 1)
                                                                661: P_{30580} = (19, 26, 28, 1)
608: P_{28080} = (15, 12, 26, 1)
                                                                662: P_{30585} = (24, 26, 28, 1)
609: P_{28148} = (19, 14, 26, 1)
                                                                663: P_{30599} = (6, 27, 28, 1)
610: P_{28237} = (12, 17, 26, 1)
                                                                664: P_{30620} = (27, 27, 28, 1)
611: P_{28299} = (10, 19, 26, 1)
                                                                665: P_{30676} = (19, 29, 28, 1)
612: P_{28300} = (11, 19, 26, 1)
                                                                666: P_{30696} = (7, 30, 28, 1)
613: P_{28308} = (19, 19, 26, 1)
                                                                667: P_{30716} = (27, 30, 28, 1)
614: P_{28343} = (22, 20, 26, 1)
                                                                668: P_{30841} = (24, 2, 29, 1)
615: P_{28344} = (23, 20, 26, 1)
                                                                669: P_{30919} = (6, 5, 29, 1)
                                                                670: P_{30943} = (30, 5, 29, 1)
616: P_{28422} = (5, 23, 26, 1)
617: P_{28445} = (28, 23, 26, 1)
                                                                671: P_{31051} = (10, 9, 29, 1)
618: P_{28475} = (26, 24, 26, 1)
                                                                672: P_{31105} = (0, 11, 29, 1)
619: P_{28530} = (17, 26, 26, 1)
                                                                673: P_{31127} = (22, 11, 29, 1)
620: P_{28598} = (21, 28, 26, 1)
                                                                674: P_{31229} = (28, 14, 29, 1)
621: P_{28605} = (28, 28, 26, 1)
                                                                675: P_{31274} = (9, 16, 29, 1)
622: P_{28631} = (22, 29, 26, 1)
                                                                676: P_{31275} = (10, 16, 29, 1)
623: P_{28652} = (11, 30, 26, 1)
                                                                677: P_{31283} = (18, 16, 29, 1)
624: P_{28829} = (28, 3, 27, 1)
                                                                678: P_{31377} = (16, 19, 29, 1)
625: P_{28830} = (29, 3, 27, 1)
                                                                679: P_{31436} = (11, 21, 29, 1)
626: P_{28855} = (22, 4, 27, 1)
                                                                680: P_{31449} = (24, 21, 29, 1)
627: P_{28867} = (2, 5, 27, 1)
                                                                681: P_{31476} = (19, 22, 29, 1)
                                                                682: P_{31484} = (27, 22, 29, 1)
628: P_{28913} = (16, 6, 27, 1)
629: P_{29052} = (27, 10, 27, 1)
                                                                683: P_{31488} = (31, 22, 29, 1)
630: P_{29106} = (17, 12, 27, 1)
                                                                684: P_{31513} = (24, 23, 29, 1)
631: P_{29144} = (23, 13, 27, 1)
                                                                685: P_{31563} = (10, 25, 29, 1)
632: P_{29196} = (11, 15, 27, 1)
                                                                686: P_{31596} = (11, 26, 29, 1)
633: P_{29249} = (0, 17, 27, 1)
                                                                687: P_{31612} = (27, 26, 29, 1)
634: P_{29391} = (14, 21, 27, 1)
                                                                688: P_{31633} = (16, 27, 29, 1)
635: P_{29408} = (31, 21, 27, 1)
                                                                689: P_{31702} = (21, 29, 29, 1)
                                                                690: P_{31811} = (2, 1, 30, 1)
636: P_{29508} = (3, 25, 27, 1)
637: P_{29545} = (8, 26, 27, 1)
                                                                691: P_{31817} = (8, 1, 30, 1)
638: P_{29553} = (16, 26, 27, 1)
                                                                692: P_{31925} = (20, 4, 30, 1)
639: P_{29588} = (19, 27, 27, 1)
                                                                693: P_{31981} = (12, 6, 30, 1)
640: P_{29642} = (9, 29, 27, 1)
                                                                694: P_{32114} = (17, 10, 30, 1)
641: P_{29750} = (21, 0, 28, 1)
                                                                695: P_{32180} = (19, 12, 30, 1)
642: P_{29751} = (22, 0, 28, 1)
                                                                696: P_{32229} = (4, 14, 30, 1)
                                                                697: P_{32252} = (27, 14, 30, 1)
643: P_{29797} = (4, 2, 28, 1)
644: P_{29856} = (31, 3, 28, 1)
                                                                698: P_{32299} = (10, 16, 30, 1)
                                                                699: P_{32381} = (28, 18, 30, 1)
645: P_{29896} = (7, 5, 28, 1)
646: P_{29913} = (24, 5, 28, 1)
                                                                700: P_{32406} = (21, 19, 30, 1)
                                                                701: P_{32435} = (18, 20, 30, 1)
647: P_{29961} = (8, 7, 28, 1)
648: P_{29972} = (19, 7, 28, 1)
                                                                702: P_{32449} = (0, 21, 30, 1)
649: P_{29982} = (29, 7, 28, 1)
                                                                703: P_{32454} = (5, 21, 30, 1)
650: P_{30092} = (11, 11, 28, 1)
                                                                704: P_{32466} = (17, 21, 30, 1)
651: P_{30182} = (5, 14, 28, 1)
                                                                705: P_{32507} = (26, 22, 30, 1)
652: P_{30225} = (16, 15, 28, 1)
                                                                706: P_{32612} = (3, 26, 30, 1)
653: P_{30277} = (4, 17, 28, 1)
                                                                707: P_{32653} = (12, 27, 30, 1)
654: P_{30341} = (4, 19, 28, 1)
                                                                708: P_{32691} = (18, 28, 30, 1)
655: P_{30417} = (16, 21, 28, 1)
                                                                709: P_{32717} = (12, 29, 30, 1)
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710: P_{32728} = (23, 29, 30, 1)
                                                               723: P_{33267} = (18, 14, 31, 1)
711: P_{32746} = (9, 30, 30, 1)
                                                               724: P_{33273} = (24, 14, 31, 1)
712: P_{32751} = (14, 30, 30, 1)
                                                               725: P_{33289} = (8, 15, 31, 1)
713: P_{32773} = (4, 31, 30, 1)
                                                               726: P_{33470} = (29, 20, 31, 1)
714: P_{32780} = (11, 31, 30, 1)
                                                               727: P_{33486} = (13, 21, 31, 1)
715: P_{32879} = (14, 2, 31, 1)
                                                               728: P_{33510} = (5, 22, 31, 1)
716: P_{32918} = (21, 3, 31, 1)
                                                               729: P_{33574} = (5, 24, 31, 1)
                                                               730: P_{33615} = (14, 25, 31, 1)
717: P_{32933} = (4, 4, 31, 1)
718: P_{32980} = (19, 5, 31, 1)
                                                               731: P_{33656} = (23, 26, 31, 1)
719: P_{33045} = (20, 7, 31, 1)
                                                               732: P_{33676} = (11, 27, 31, 1)
720: P_{33176} = (23, 11, 31, 1)
                                                               733: P_{33696} = (31, 27, 31, 1)
721:\,P_{33218}=(1,13,31,1)
                                                               734: P_{33746} = (17, 29, 31, 1)
722: P_{33237} = (20, 13, 31, 1)
```

## Line Intersection Graph

|    | 0 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 1 | 2 | 13 | 14 |
|----|-----|---|---|---|---|---|---|---|---|----|----|---|---|----|----|
| 0  | 01  | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0  | 1  |   | 0 | 0  | 0  |
| 1  | 10  | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0  | 1  |   | 1 | 0  | 0  |
| 2  | 0 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 1  | 0  |   | 0 | 0  | 1  |
| 3  | 0 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1  | 0  |   | 1 | 0  | 1  |
| 4  | 0 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 0  | 0  |   | 0 | 1  | 0  |
| 5  | 10  | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1  | 0  |   | 0 | 1  | 0  |
| 6  | 10  | 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0  | 0  |   | 0 | 0  | 1  |
| 7  | 10  | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1  | 0  |   | 1 | 1  | 0  |
| 8  | 10  | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0  | 0  |   | 1 | 0  | 1  |
| 9  | 0 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1  | 1  |   | 1 | 0  | 0  |
| 10 | 0 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0  | 1  |   | 0 | 0  | 0  |
| 11 | 11  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1  | 0  |   | 0 | 1  | 1  |
| 12 | 0 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0  | 0  |   | 0 | 1  | 0  |
| 13 | 0 0 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0  | 1  |   | 1 | 0  | 1  |
| 14 | 0 0 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0  | 1  |   | 0 | 1  | 0  |

Neighbor sets in the line intersection graph:

Line 0 intersects

| Line     | $\ell_1$  | $\ell_5$    | $\ell_6$   | $\ell_7$   | $\ell_8$    | $\ell_{11}$ |
|----------|-----------|-------------|------------|------------|-------------|-------------|
| in point | $P_{244}$ | $P_{12841}$ | $P_{8076}$ | $P_{6750}$ | $P_{29718}$ | $P_{4309}$  |

Line 1 intersects

| Line     | $\ell_0$  | $\ell_2$    | $\ell_3$    | $\ell_4$    | $\ell_{11}$ | $\ell_{12}$ |
|----------|-----------|-------------|-------------|-------------|-------------|-------------|
| in point | $P_{244}$ | $P_{33601}$ | $P_{19254}$ | $P_{18405}$ | $P_{27082}$ | $P_{5464}$  |

Line 2 intersects

| Line     | $\ell_1$    | $\ell_4$    | $\ell_7$    | $\ell_8$   | $\ell_{10}$ | $\ell_{14}$ |
|----------|-------------|-------------|-------------|------------|-------------|-------------|
| in point | $P_{33601}$ | $P_{12603}$ | $P_{16843}$ | $P_{3452}$ | $P_{6920}$  | $P_{20466}$ |

Line 3 intersects

| Line     | $\ell_1$    | $\ell_5$    | $\ell_6$    | $\ell_{10}$ | $\ell_{12}$ | $\ell_{14}$ |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|
| in point | $P_{19254}$ | $P_{10893}$ | $P_{19681}$ | $P_{5603}$  | $P_{33679}$ | $P_{16740}$ |

Line 4 intersects

| Line     | $\ell_1$ $\ell_2$ |             | $\ell_5$    | $\ell_6$    | $\ell_9$    | $\ell_{13}$ |
|----------|-------------------|-------------|-------------|-------------|-------------|-------------|
| in point | $P_{18405}$       | $P_{12603}$ | $P_{33254}$ | $P_{13597}$ | $P_{19583}$ | $P_{10913}$ |

Line 5 intersects

| Line     | $\ell_0$ $\ell_3$ |             | $\ell_4$    | $\ell_8$   | $\ell_{10}$ | $\ell_{13}$ |
|----------|-------------------|-------------|-------------|------------|-------------|-------------|
| in point | $P_{12841}$       | $P_{10893}$ | $P_{33254}$ | $P_{5049}$ | $P_{17121}$ | $P_{28974}$ |

| Line 6 intersects     |          |             |             |             |             |             |             |
|-----------------------|----------|-------------|-------------|-------------|-------------|-------------|-------------|
|                       | Line     | $\ell_0$    | $\ell_3$    | $\ell_4$    | $\ell_7$    | $\ell_9$    | $\ell_{14}$ |
|                       | in point | $P_{8076}$  | $P_{19681}$ | $P_{13597}$ | $P_{687}$   | $P_{17817}$ | $P_{14993}$ |
| Line 7 intersects     |          |             |             |             |             | •           |             |
| Ziiio i iiitoriscotti | Line     | $\ell_0$    | $\ell_2$    | $\ell_6$    | $\ell_{10}$ | $\ell_{12}$ | $\ell_{13}$ |
|                       | in point | $P_{6750}$  | $P_{16843}$ | $P_{687}$   | $P_{3709}$  | $P_{18871}$ | $P_{21616}$ |
| Line 8 intersects     |          |             |             |             |             |             |             |
| Line o microccio      | Line     | $\ell_0$    | $\ell_2$    | $\ell_5$    | $\ell_9$    | $\ell_{12}$ | $\ell_{14}$ |
|                       | in point | $P_{29718}$ | $P_{3452}$  | $P_{5049}$  | $P_{742}$   | $P_{30912}$ | $P_{13249}$ |
| Line 9 intersects     |          | •           | '           | •           |             |             | ,           |
| Line 5 intersects     | Line     | $\ell_4$    | $\ell_6$    | $\ell_8$    | $\ell_{10}$ | $\ell_{11}$ | $\ell_{12}$ |
|                       | in point | $P_{19583}$ | $P_{17817}$ | $P_{742}$   | $P_{24115}$ | $P_{27783}$ | $P_{14202}$ |
| Line 10 intersects    |          |             |             |             |             |             |             |
| Line 10 intersects    | Line     | $\ell_2$    | $\ell_3$    | $\ell_5$    | $\ell_7$    | $\ell_9$    | $\ell_{11}$ |
|                       | in point | $P_{6920}$  | $P_{5603}$  | $P_{17121}$ | $P_{3709}$  | $P_{24115}$ | $P_{840}$   |
| Line 11 intersects    |          |             | "           |             |             | 1           |             |
| Line 11 intersects    | Line     | $\ell_0$    | $\ell_1$    | $\ell_9$    | $\ell_{10}$ | $\ell_{13}$ | $\ell_{14}$ |
|                       | in point | $P_{4309}$  | $P_{27082}$ | $P_{27783}$ | $P_{840}$   | $P_{14856}$ | $P_{10420}$ |
| Line 12 intersects    |          | 2000        |             |             | 0.20        |             |             |
| Line 12 intersects    | Line     | $\ell_1$    | $\ell_3$    | $\ell_7$    | $\ell_8$    | $\ell_9$    | $\ell_{13}$ |
|                       | in point | $P_{5464}$  | $P_{33679}$ | $P_{18871}$ | $P_{30912}$ |             |             |
| Line 13 intersects    |          | 0 20 2      |             |             |             |             |             |
| Line 13 intersects    | Line     | $\ell_4$    | $\ell_5$    | $\ell_7$    | $\ell_{11}$ | $\ell_{12}$ | $\ell_{14}$ |
|                       | in point | $P_{10913}$ | $P_{28974}$ | $P_{21616}$ | $P_{14856}$ |             | $P_{28376}$ |
| Line 14 intersects    |          | 10010       |             |             | 1 11000     | - 1 000     | 200.0       |
| Line 14 intersects    | Line     | $\ell_2$    | $\ell_3$    | $\ell_6$    | $\ell_8$    | $\ell_{11}$ | $\ell_{13}$ |
|                       |          | $P_{20466}$ | $P_{16740}$ | $P_{14993}$ | $P_{13249}$ | $P_{10420}$ | $P_{28376}$ |
|                       | I        | 20400       | 10140       | 14000       | 10249       | 10420       | 20010       |

The surface has 1185 points:

Too many to print.