Rank-74279 over GF(8)

January 15, 2021

The equation

The equation of the surface is:

$$X_2^3 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

 $(\ 0,\ 0,\ 1,\ 0,\ 0,\ 1,\ 0,\ 0,\ 1,\ 0,\ 0,\ 1,\ 0,\ 0,\ 1,\ 0,\ 0,\ 0)$

The point rank of the equation over GF(8) is 1361384077

General information

Number of lines	1
Number of points	73
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	9
Number of points off lines	64
Number of Hesse planes	0
Number of axes	0
Type of points on lines	9
Type of lines on points	$1^9, 0^{64}$

Singular Points

The surface has 0 singular points:

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0$$

Rank of lines: (0)

Rank of points on Klein quadric: (0)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 9 single points: The single points on the surface are:

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\begin{array}{lll} 0: \ P_0 = (1,0,0,0) \ \mbox{lies on line} \ \ell_0 \\ 1: \ P_1 = (0,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 2: \ P_5 = (1,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 3: \ P_6 = (2,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 4: \ P_7 = (3,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ \end{array}
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The single points on the surface are:

Points on surface but on no line

The surface has 64 points not on any line: The points on the surface but not on lines are:

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0: P_3 = (0,0,0,1)
                                                                 22: P_{264} = (7,7,2,1)
1: P_{12} = (1, 0, 1, 0)
                                                                 23: P_{266} = (1,0,3,1)
2: P_{32} = (5, 2, 1, 0)
                                                                 24: P_{270} = (5,0,3,1)
3: P_{34} = (7, 2, 1, 0)
                                                                 25: P_{284} = (3, 2, 3, 1)
4: P_{45} = (2, 4, 1, 0)
                                                                 26: P_{286} = (5, 2, 3, 1)
5: P_{49} = (6, 4, 1, 0)
                                                                 27: P_{290} = (1, 3, 3, 1)
6: P_{70} = (3, 7, 1, 0)
                                                                 28: P_{295} = (6, 3, 3, 1)
7: P_{71} = (4, 7, 1, 0)
                                                                 29: P_{303} = (6, 4, 3, 1)
8: P_{83} = (1, 1, 0, 1)
                                                                 30: P_{321} = (0,7,3,1)
9: P_{94} = (4, 2, 0, 1)
                                                                 31: P_{324} = (3,7,3,1)
10: P_{103} = (5, 3, 0, 1)
                                                                 32: P_{347} = (2, 2, 4, 1)
                                                                 33: P_{348} = (3, 2, 4, 1)
11: P_{113} = (7, 4, 0, 1)
12: P_{120} = (6, 5, 0, 1)
                                                                 34: P_{356} = (3, 3, 4, 1)
13: P_{125} = (3, 6, 0, 1)
                                                                 35: P_{369} = (0, 5, 4, 1)
14: P_{132} = (2,7,0,1)
                                                                 36: P_{375} = (6, 5, 4, 1)
15: P_{146} = (0, 1, 1, 1)
                                                                 37: P_{387} = (2,7,4,1)
16: P_{225} = (0, 3, 2, 1)
                                                                 38: P_{391} = (6,7,4,1)
17: P_{230} = (5, 3, 2, 1)
                                                                 39: P_{394} = (1,0,5,1)
18: P_{238} = (5, 4, 2, 1)
                                                                 40: P_{399} = (6,0,5,1)
19: P_{240} = (7, 4, 2, 1)
                                                                 41: P_{409} = (0, 2, 5, 1)
20: P_{255} = (6, 6, 2, 1)
                                                                 42: P_{414} = (5, 2, 5, 1)
21: P_{263} = (6,7,2,1)
                                                                 43: P_{430} = (5, 4, 5, 1)
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44: P_{431} = (6, 4, 5, 1)
                                                                   55: P_{516} = (3, 7, 6, 1)
45: P_{434} = (1, 5, 5, 1)
                                                                   56: P_{519} = (6,7,6,1)
46: P_{436} = (3, 5, 5, 1)
                                                                   57: P_{540} = (3, 2, 7, 1)
47: P_{452} = (3, 7, 5, 1)
                                                                   58: P_{541} = (4, 2, 7, 1)
                                                                  59: P_{557} = (4, 4, 7, 1)
48: P_{458} = (1, 0, 6, 1)
49: P_{460} = (3, 0, 6, 1)
                                                                   60: P_{558} = (5, 4, 7, 1)
50: P_{478} = (5, 2, 6, 1)
                                                                   61: P_{566} = (5, 5, 7, 1)
51: P_{489} = (0, 4, 6, 1)
                                                                  62: P_{569} = (0, 6, 7, 1)
52: P_{495} = (6, 4, 6, 1)
                                                                   63: P_{572} = (3, 6, 7, 1)
53: P_{506} = (1, 6, 6, 1)
54: P_{510} = (5, 6, 6, 1)
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Line Intersection Graph

 $\begin{array}{c|c} 0 \\ \hline 0 & 0 \end{array}$

Neighbor sets in the line intersection graph: Line 0 intersects

Line in point

The surface has 73 points:

The points on the surface are:

$0: P_0 = (1,0,0,0)$	$25: P_{225} = (0, 3, 2, 1)$	$50: P_{409} = (0, 2, 5, 1)$
$1: P_1 = (0, 1, 0, 0)$	$26: P_{230} = (5, 3, 2, 1)$	$51: P_{414} = (5, 2, 5, 1)$
$2: P_3 = (0,0,0,1)$	$27: P_{238} = (5, 4, 2, 1)$	$52: P_{430} = (5, 4, 5, 1)$
$3: P_5 = (1, 1, 0, 0)$	$28: P_{240} = (7, 4, 2, 1)$	$53: P_{431} = (6, 4, 5, 1)$
$4: P_6 = (2, 1, 0, 0)$	$29: P_{255} = (6, 6, 2, 1)$	$54: P_{434} = (1, 5, 5, 1)$
$5: P_7 = (3, 1, 0, 0)$	$30: P_{263} = (6,7,2,1)$	$55: P_{436} = (3, 5, 5, 1)$
$6: P_8 = (4, 1, 0, 0)$	$31: P_{264} = (7,7,2,1)$	$56: P_{452} = (3,7,5,1)$
$7: P_9 = (5, 1, 0, 0)$	$32: P_{266} = (1,0,3,1)$	$57: P_{458} = (1,0,6,1)$
$8: P_{10} = (6, 1, 0, 0)$	$33: P_{270} = (5,0,3,1)$	$58: P_{460} = (3,0,6,1)$
$9: P_{11} = (7, 1, 0, 0)$	$34: P_{284} = (3, 2, 3, 1)$	$59: P_{478} = (5, 2, 6, 1)$
$10: P_{12} = (1, 0, 1, 0)$	$35: P_{286} = (5, 2, 3, 1)$	$60: P_{489} = (0, 4, 6, 1)$
$11: P_{32} = (5, 2, 1, 0)$	$36: P_{290} = (1, 3, 3, 1)$	$61: P_{495} = (6, 4, 6, 1)$
$12: P_{34} = (7, 2, 1, 0)$	$37: P_{295} = (6, 3, 3, 1)$	$62: P_{506} = (1, 6, 6, 1)$
$13: P_{45} = (2, 4, 1, 0)$	$38: P_{303} = (6,4,3,1)$	$63: P_{510} = (5, 6, 6, 1)$
$14: P_{49} = (6, 4, 1, 0)$	$39: P_{321} = (0,7,3,1)$	$64: P_{516} = (3, 7, 6, 1)$
$15: P_{70} = (3, 7, 1, 0)$	$40: P_{324} = (3,7,3,1)$	$65: P_{519} = (6, 7, 6, 1)$
$16: P_{71} = (4, 7, 1, 0)$	$41: P_{347} = (2, 2, 4, 1)$	$66: P_{540} = (3, 2, 7, 1)$
$17: P_{83} = (1, 1, 0, 1)$	$42: P_{348} = (3, 2, 4, 1)$	$67: P_{541} = (4, 2, 7, 1)$
$18: P_{94} = (4, 2, 0, 1)$	$43: P_{356} = (3, 3, 4, 1)$	$68: P_{557} = (4, 4, 7, 1)$
19: $P_{103} = (5, 3, 0, 1)$	$44 : P_{369} = (0, 5, 4, 1)$	$69: P_{558} = (5, 4, 7, 1)$
$20: P_{113} = (7, 4, 0, 1)$	$45: P_{375} = (6, 5, 4, 1)$	$70: P_{566} = (5, 5, 7, 1)$
$21: P_{120} = (6, 5, 0, 1)$	$46: P_{387} = (2,7,4,1)$	$71: P_{569} = (0, 6, 7, 1)$
$22: P_{125} = (3, 6, 0, 1)$	$47: P_{391} = (6,7,4,1)$	$72: P_{572} = (3, 6, 7, 1)$
$23: P_{132} = (2,7,0,1)$	$48: P_{394} = (1, 0, 5, 1)$	
$24: P_{146} = (0, 1, 1, 1)$	$49: P_{399} = (6,0,5,1)$	
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