

Rank-76307 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^2 X_1 + X_1^2 X_3 + X_1 X_2^2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is 1109427237

General information

Number of lines	2
Number of points	1057
Number of singular points	0
Number of Eckardt points	0
Number of double points	1
Number of single points	64
Number of points off lines	992
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^2
Type of lines on points	$2, 1^{64}, 0^{992}$

Singular Points

The surface has 0 singular points:

The 2 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned}\ell_0 &= \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]_{1024} = \left[\begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]_{1024} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2 \\ \ell_1 &= \left[\begin{array}{cccc} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{1083424} = \left[\begin{array}{cccc} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{1083424} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_1\end{aligned}$$

Rank of lines: (1024, 1083424)
Rank of points on Klein quadric: (2, 1)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 1 Double points:
The double points on the surface are:

$$P_2 = (0, 0, 1, 0) = \ell_0 \cap \ell_1$$

Single Points

The surface has 64 single points:
The single points on the surface are:

- | | |
|---|--|
| 0 : $P_0 = (1, 0, 0, 0)$ lies on line ℓ_0 | 33 : $P_{2082} = (0, 0, 1, 1)$ lies on line ℓ_1 |
| 1 : $P_3 = (0, 0, 0, 1)$ lies on line ℓ_1 | 34 : $P_{3105} = (0, 0, 2, 1)$ lies on line ℓ_1 |
| 2 : $P_{36} = (1, 0, 1, 0)$ lies on line ℓ_0 | 35 : $P_{4129} = (0, 0, 3, 1)$ lies on line ℓ_1 |
| 3 : $P_{37} = (2, 0, 1, 0)$ lies on line ℓ_0 | 36 : $P_{5153} = (0, 0, 4, 1)$ lies on line ℓ_1 |
| 4 : $P_{38} = (3, 0, 1, 0)$ lies on line ℓ_0 | 37 : $P_{6177} = (0, 0, 5, 1)$ lies on line ℓ_1 |
| 5 : $P_{39} = (4, 0, 1, 0)$ lies on line ℓ_0 | 38 : $P_{7201} = (0, 0, 6, 1)$ lies on line ℓ_1 |
| 6 : $P_{40} = (5, 0, 1, 0)$ lies on line ℓ_0 | 39 : $P_{8225} = (0, 0, 7, 1)$ lies on line ℓ_1 |
| 7 : $P_{41} = (6, 0, 1, 0)$ lies on line ℓ_0 | 40 : $P_{9249} = (0, 0, 8, 1)$ lies on line ℓ_1 |
| 8 : $P_{42} = (7, 0, 1, 0)$ lies on line ℓ_0 | 41 : $P_{10273} = (0, 0, 9, 1)$ lies on line ℓ_1 |
| 9 : $P_{43} = (8, 0, 1, 0)$ lies on line ℓ_0 | 42 : $P_{11297} = (0, 0, 10, 1)$ lies on line ℓ_1 |
| 10 : $P_{44} = (9, 0, 1, 0)$ lies on line ℓ_0 | 43 : $P_{12321} = (0, 0, 11, 1)$ lies on line ℓ_1 |
| 11 : $P_{45} = (10, 0, 1, 0)$ lies on line ℓ_0 | 44 : $P_{13345} = (0, 0, 12, 1)$ lies on line ℓ_1 |
| 12 : $P_{46} = (11, 0, 1, 0)$ lies on line ℓ_0 | 45 : $P_{14369} = (0, 0, 13, 1)$ lies on line ℓ_1 |
| 13 : $P_{47} = (12, 0, 1, 0)$ lies on line ℓ_0 | 46 : $P_{15393} = (0, 0, 14, 1)$ lies on line ℓ_1 |
| 14 : $P_{48} = (13, 0, 1, 0)$ lies on line ℓ_0 | 47 : $P_{16417} = (0, 0, 15, 1)$ lies on line ℓ_1 |
| 15 : $P_{49} = (14, 0, 1, 0)$ lies on line ℓ_0 | 48 : $P_{17441} = (0, 0, 16, 1)$ lies on line ℓ_1 |
| 16 : $P_{50} = (15, 0, 1, 0)$ lies on line ℓ_0 | 49 : $P_{18465} = (0, 0, 17, 1)$ lies on line ℓ_1 |
| 17 : $P_{51} = (16, 0, 1, 0)$ lies on line ℓ_0 | 50 : $P_{19489} = (0, 0, 18, 1)$ lies on line ℓ_1 |
| 18 : $P_{52} = (17, 0, 1, 0)$ lies on line ℓ_0 | 51 : $P_{20513} = (0, 0, 19, 1)$ lies on line ℓ_1 |
| 19 : $P_{53} = (18, 0, 1, 0)$ lies on line ℓ_0 | 52 : $P_{21537} = (0, 0, 20, 1)$ lies on line ℓ_1 |
| 20 : $P_{54} = (19, 0, 1, 0)$ lies on line ℓ_0 | 53 : $P_{22561} = (0, 0, 21, 1)$ lies on line ℓ_1 |
| 21 : $P_{55} = (20, 0, 1, 0)$ lies on line ℓ_0 | 54 : $P_{23585} = (0, 0, 22, 1)$ lies on line ℓ_1 |
| 22 : $P_{56} = (21, 0, 1, 0)$ lies on line ℓ_0 | 55 : $P_{24609} = (0, 0, 23, 1)$ lies on line ℓ_1 |
| 23 : $P_{57} = (22, 0, 1, 0)$ lies on line ℓ_0 | 56 : $P_{25633} = (0, 0, 24, 1)$ lies on line ℓ_1 |
| 24 : $P_{58} = (23, 0, 1, 0)$ lies on line ℓ_0 | 57 : $P_{26657} = (0, 0, 25, 1)$ lies on line ℓ_1 |
| 25 : $P_{59} = (24, 0, 1, 0)$ lies on line ℓ_0 | 58 : $P_{27681} = (0, 0, 26, 1)$ lies on line ℓ_1 |
| 26 : $P_{60} = (25, 0, 1, 0)$ lies on line ℓ_0 | 59 : $P_{28705} = (0, 0, 27, 1)$ lies on line ℓ_1 |
| 27 : $P_{61} = (26, 0, 1, 0)$ lies on line ℓ_0 | 60 : $P_{29729} = (0, 0, 28, 1)$ lies on line ℓ_1 |
| 28 : $P_{62} = (27, 0, 1, 0)$ lies on line ℓ_0 | 61 : $P_{30753} = (0, 0, 29, 1)$ lies on line ℓ_1 |
| 29 : $P_{63} = (28, 0, 1, 0)$ lies on line ℓ_0 | 62 : $P_{31777} = (0, 0, 30, 1)$ lies on line ℓ_1 |
| 30 : $P_{64} = (29, 0, 1, 0)$ lies on line ℓ_0 | 63 : $P_{32801} = (0, 0, 31, 1)$ lies on line ℓ_1 |
| 31 : $P_{65} = (30, 0, 1, 0)$ lies on line ℓ_0 | |
| 32 : $P_{66} = (31, 0, 1, 0)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 992 points not on any line:

The points on the surface but not on lines are:

0 : $P_1 = (0, 1, 0, 0)$	45 : $P_{2421} = (20, 10, 1, 1)$
1 : $P_{1167} = (13, 3, 0, 1)$	46 : $P_{2484} = (19, 12, 1, 1)$
2 : $P_{1171} = (17, 3, 0, 1)$	47 : $P_{2486} = (21, 12, 1, 1)$
3 : $P_{1230} = (12, 5, 0, 1)$	48 : $P_{2520} = (23, 13, 1, 1)$
4 : $P_{1245} = (27, 5, 0, 1)$	49 : $P_{2522} = (25, 13, 1, 1)$
5 : $P_{1305} = (23, 7, 0, 1)$	50 : $P_{2555} = (26, 14, 1, 1)$
6 : $P_{1309} = (27, 7, 0, 1)$	51 : $P_{2558} = (29, 14, 1, 1)$
7 : $P_{1349} = (3, 9, 0, 1)$	52 : $P_{2615} = (22, 16, 1, 1)$
8 : $P_{1353} = (7, 9, 0, 1)$	53 : $P_{2621} = (28, 16, 1, 1)$
9 : $P_{1415} = (5, 11, 0, 1)$	54 : $P_{2632} = (7, 17, 1, 1)$
10 : $P_{1431} = (21, 11, 0, 1)$	55 : $P_{2655} = (30, 17, 1, 1)$
11 : $P_{1445} = (3, 12, 0, 1)$	56 : $P_{2694} = (5, 19, 1, 1)$
12 : $P_{1446} = (4, 12, 0, 1)$	57 : $P_{2714} = (25, 19, 1, 1)$
13 : $P_{1555} = (17, 15, 0, 1)$	58 : $P_{2735} = (14, 20, 1, 1)$
14 : $P_{1566} = (28, 15, 0, 1)$	59 : $P_{2738} = (17, 20, 1, 1)$
15 : $P_{1604} = (2, 17, 0, 1)$	60 : $P_{2804} = (19, 22, 1, 1)$
16 : $P_{1628} = (26, 17, 0, 1)$	61 : $P_{2811} = (26, 22, 1, 1)$
17 : $P_{1658} = (24, 18, 0, 1)$	62 : $P_{2884} = (3, 25, 1, 1)$
18 : $P_{1660} = (26, 18, 0, 1)$	63 : $P_{2889} = (8, 25, 1, 1)$
19 : $P_{1732} = (2, 21, 0, 1)$	64 : $P_{2921} = (8, 26, 1, 1)$
20 : $P_{1754} = (24, 21, 0, 1)$	65 : $P_{2941} = (28, 26, 1, 1)$
21 : $P_{1810} = (16, 23, 0, 1)$	66 : $P_{2951} = (6, 27, 1, 1)$
22 : $P_{1815} = (21, 23, 0, 1)$	67 : $P_{2969} = (24, 27, 1, 1)$
23 : $P_{1839} = (13, 24, 0, 1)$	68 : $P_{3021} = (12, 29, 1, 1)$
24 : $P_{1854} = (28, 24, 0, 1)$	69 : $P_{3039} = (30, 29, 1, 1)$
25 : $P_{1895} = (5, 26, 0, 1)$	70 : $P_{3044} = (3, 30, 1, 1)$
26 : $P_{1906} = (16, 26, 0, 1)$	71 : $P_{3063} = (22, 30, 1, 1)$
27 : $P_{1958} = (4, 28, 0, 1)$	72 : $P_{3205} = (4, 3, 2, 1)$
28 : $P_{1961} = (7, 28, 0, 1)$	73 : $P_{3227} = (26, 3, 2, 1)$
29 : $P_{2062} = (12, 31, 0, 1)$	74 : $P_{3233} = (0, 4, 2, 1)$
30 : $P_{2073} = (23, 31, 0, 1)$	75 : $P_{3244} = (11, 4, 2, 1)$
31 : $P_{2114} = (0, 1, 1, 1)$	76 : $P_{3316} = (19, 6, 2, 1)$
32 : $P_{2152} = (7, 2, 1, 1)$	77 : $P_{3328} = (31, 6, 2, 1)$
33 : $P_{2165} = (20, 2, 1, 1)$	78 : $P_{3351} = (22, 7, 2, 1)$
34 : $P_{2187} = (10, 3, 1, 1)$	79 : $P_{3353} = (24, 7, 2, 1)$
35 : $P_{2200} = (23, 3, 1, 1)$	80 : $P_{3412} = (19, 9, 2, 1)$
36 : $P_{2230} = (21, 4, 1, 1)$	81 : $P_{3414} = (21, 9, 2, 1)$
37 : $P_{2238} = (29, 4, 1, 1)$	82 : $P_{3470} = (13, 11, 2, 1)$
38 : $P_{2255} = (14, 5, 1, 1)$	83 : $P_{3488} = (31, 11, 2, 1)$
39 : $P_{2265} = (24, 5, 1, 1)$	84 : $P_{3562} = (9, 14, 2, 1)$
40 : $P_{2278} = (5, 6, 1, 1)$	85 : $P_{3566} = (13, 14, 2, 1)$
41 : $P_{2283} = (10, 6, 1, 1)$	86 : $P_{3651} = (2, 17, 2, 1)$
42 : $P_{2343} = (6, 8, 1, 1)$	87 : $P_{3673} = (24, 17, 2, 1)$
43 : $P_{2354} = (17, 8, 1, 1)$	88 : $P_{3710} = (29, 18, 2, 1)$
44 : $P_{2413} = (12, 10, 1, 1)$	89 : $P_{3722} = (9, 19, 2, 1)$

90 : $P_{3735} = (22, 19, 2, 1)$	144 : $P_{5789} = (28, 19, 4, 1)$
91 : $P_{3779} = (2, 21, 2, 1)$	145 : $P_{5801} = (8, 20, 4, 1)$
92 : $P_{3803} = (26, 21, 2, 1)$	146 : $P_{5811} = (18, 20, 4, 1)$
93 : $P_{3908} = (3, 25, 2, 1)$	147 : $P_{5832} = (7, 21, 4, 1)$
94 : $P_{3916} = (11, 25, 2, 1)$	148 : $P_{5850} = (25, 21, 4, 1)$
95 : $P_{4068} = (3, 30, 2, 1)$	149 : $P_{6052} = (3, 28, 4, 1)$
96 : $P_{4086} = (21, 30, 2, 1)$	150 : $P_{6053} = (4, 28, 4, 1)$
97 : $P_{4101} = (4, 31, 2, 1)$	151 : $P_{6124} = (11, 30, 4, 1)$
98 : $P_{4126} = (29, 31, 2, 1)$	152 : $P_{6140} = (27, 30, 4, 1)$
99 : $P_{4277} = (20, 4, 3, 1)$	153 : $P_{6254} = (13, 2, 5, 1)$
100 : $P_{4287} = (30, 4, 3, 1)$	154 : $P_{6267} = (26, 2, 5, 1)$
101 : $P_{4289} = (0, 5, 3, 1)$	155 : $P_{6403} = (2, 7, 5, 1)$
102 : $P_{4309} = (20, 5, 3, 1)$	156 : $P_{6412} = (11, 7, 5, 1)$
103 : $P_{4337} = (16, 6, 3, 1)$	157 : $P_{6534} = (5, 11, 5, 1)$
104 : $P_{4350} = (29, 6, 3, 1)$	158 : $P_{6545} = (16, 11, 5, 1)$
105 : $P_{4420} = (3, 9, 3, 1)$	159 : $P_{6609} = (16, 13, 5, 1)$
106 : $P_{4421} = (4, 9, 3, 1)$	160 : $P_{6619} = (26, 13, 5, 1)$
107 : $P_{4516} = (3, 12, 3, 1)$	161 : $P_{6708} = (19, 16, 5, 1)$
108 : $P_{4520} = (7, 12, 3, 1)$	162 : $P_{6718} = (29, 16, 5, 1)$
109 : $P_{4550} = (5, 13, 3, 1)$	163 : $P_{6721} = (0, 17, 5, 1)$
110 : $P_{4554} = (9, 13, 3, 1)$	164 : $P_{6750} = (29, 17, 5, 1)$
111 : $P_{4645} = (4, 16, 3, 1)$	165 : $P_{6778} = (25, 18, 5, 1)$
112 : $P_{4653} = (12, 16, 3, 1)$	166 : $P_{6783} = (30, 18, 5, 1)$
113 : $P_{4808} = (7, 21, 3, 1)$	167 : $P_{6830} = (13, 20, 5, 1)$
114 : $P_{4831} = (30, 21, 3, 1)$	168 : $P_{6839} = (22, 20, 5, 1)$
115 : $P_{4838} = (5, 22, 3, 1)$	169 : $P_{6938} = (25, 23, 5, 1)$
116 : $P_{4847} = (14, 22, 3, 1)$	170 : $P_{6947} = (2, 24, 5, 1)$
117 : $P_{4892} = (27, 23, 3, 1)$	171 : $P_{6967} = (22, 24, 5, 1)$
118 : $P_{4894} = (29, 23, 3, 1)$	172 : $P_{6994} = (17, 25, 5, 1)$
119 : $P_{4906} = (9, 24, 3, 1)$	173 : $P_{7007} = (30, 25, 5, 1)$
120 : $P_{4924} = (27, 24, 3, 1)$	174 : $P_{7014} = (5, 26, 5, 1)$
121 : $P_{5005} = (12, 27, 3, 1)$	175 : $P_{7030} = (21, 26, 5, 1)$
122 : $P_{5009} = (16, 27, 3, 1)$	176 : $P_{7052} = (11, 27, 5, 1)$
123 : $P_{5047} = (22, 28, 3, 1)$	177 : $P_{7058} = (17, 27, 5, 1)$
124 : $P_{5135} = (14, 31, 3, 1)$	178 : $P_{7092} = (19, 28, 5, 1)$
125 : $P_{5143} = (22, 31, 3, 1)$	179 : $P_{7094} = (21, 28, 5, 1)$
126 : $P_{5316} = (3, 5, 4, 1)$	180 : $P_{7272} = (7, 2, 6, 1)$
127 : $P_{5329} = (16, 5, 4, 1)$	181 : $P_{7284} = (19, 2, 6, 1)$
128 : $P_{5350} = (5, 6, 4, 1)$	182 : $P_{7301} = (4, 3, 6, 1)$
129 : $P_{5360} = (15, 6, 4, 1)$	183 : $P_{7327} = (30, 3, 6, 1)$
130 : $P_{5420} = (11, 8, 4, 1)$	184 : $P_{7522} = (1, 10, 6, 1)$
131 : $P_{5434} = (25, 8, 4, 1)$	185 : $P_{7551} = (30, 10, 6, 1)$
132 : $P_{5463} = (22, 9, 4, 1)$	186 : $P_{7622} = (5, 13, 6, 1)$
133 : $P_{5513} = (8, 11, 4, 1)$	187 : $P_{7629} = (12, 13, 6, 1)$
134 : $P_{5533} = (28, 11, 4, 1)$	188 : $P_{7661} = (12, 14, 6, 1)$
135 : $P_{5541} = (4, 12, 4, 1)$	189 : $P_{7752} = (7, 17, 6, 1)$
136 : $P_{5544} = (7, 12, 4, 1)$	190 : $P_{7770} = (25, 17, 6, 1)$
137 : $P_{5651} = (18, 15, 4, 1)$	191 : $P_{7788} = (11, 18, 6, 1)$
138 : $P_{5660} = (27, 15, 4, 1)$	192 : $P_{7792} = (15, 18, 6, 1)$
139 : $P_{5665} = (0, 16, 4, 1)$	193 : $P_{7841} = (0, 20, 6, 1)$
140 : $P_{5680} = (15, 16, 4, 1)$	194 : $P_{7865} = (24, 20, 6, 1)$
141 : $P_{5745} = (16, 18, 4, 1)$	195 : $P_{7910} = (5, 22, 6, 1)$
142 : $P_{5751} = (22, 18, 4, 1)$	196 : $P_{7916} = (11, 22, 6, 1)$
143 : $P_{5766} = (5, 19, 4, 1)$	197 : $P_{7979} = (10, 24, 6, 1)$

198 : $P_{7998} = (29, 24, 6, 1)$
 199 : $P_{8002} = (1, 25, 6, 1)$
 200 : $P_{8014} = (13, 25, 6, 1)$
 201 : $P_{8075} = (10, 27, 6, 1)$
 202 : $P_{8084} = (19, 27, 6, 1)$
 203 : $P_{8142} = (13, 29, 6, 1)$
 204 : $P_{8153} = (24, 29, 6, 1)$
 205 : $P_{8176} = (15, 30, 6, 1)$
 206 : $P_{8190} = (29, 30, 6, 1)$
 207 : $P_{8197} = (4, 31, 6, 1)$
 208 : $P_{8218} = (25, 31, 6, 1)$
 209 : $P_{8330} = (9, 3, 7, 1)$
 210 : $P_{8339} = (18, 3, 7, 1)$
 211 : $P_{8388} = (3, 5, 7, 1)$
 212 : $P_{8404} = (19, 5, 7, 1)$
 213 : $P_{8451} = (2, 7, 7, 1)$
 214 : $P_{8458} = (9, 7, 7, 1)$
 215 : $P_{8487} = (6, 8, 7, 1)$
 216 : $P_{8504} = (23, 8, 7, 1)$
 217 : $P_{8517} = (4, 9, 7, 1)$
 218 : $P_{8520} = (7, 9, 7, 1)$
 219 : $P_{8546} = (1, 10, 7, 1)$
 220 : $P_{8576} = (31, 10, 7, 1)$
 221 : $P_{8631} = (22, 12, 7, 1)$
 222 : $P_{8663} = (22, 13, 7, 1)$
 223 : $P_{8671} = (30, 13, 7, 1)$
 224 : $P_{8691} = (18, 14, 7, 1)$
 225 : $P_{8692} = (19, 14, 7, 1)$
 226 : $P_{8728} = (23, 15, 7, 1)$
 227 : $P_{8734} = (29, 15, 7, 1)$
 228 : $P_{8741} = (4, 16, 7, 1)$
 229 : $P_{8745} = (8, 16, 7, 1)$
 230 : $P_{8809} = (8, 18, 7, 1)$
 231 : $P_{8814} = (13, 18, 7, 1)$
 232 : $P_{8847} = (14, 19, 7, 1)$
 233 : $P_{8853} = (20, 19, 7, 1)$
 234 : $P_{8897} = (0, 21, 7, 1)$
 235 : $P_{8926} = (29, 21, 7, 1)$
 236 : $P_{8973} = (12, 23, 7, 1)$
 237 : $P_{8975} = (14, 23, 7, 1)$
 238 : $P_{8995} = (2, 24, 7, 1)$
 239 : $P_{9013} = (20, 24, 7, 1)$
 240 : $P_{9026} = (1, 25, 7, 1)$
 241 : $P_{9037} = (12, 25, 7, 1)$
 242 : $P_{9070} = (13, 26, 7, 1)$
 243 : $P_{9088} = (31, 26, 7, 1)$
 244 : $P_{9095} = (6, 27, 7, 1)$
 245 : $P_{9119} = (30, 27, 7, 1)$
 246 : $P_{9124} = (3, 28, 7, 1)$
 247 : $P_{9128} = (7, 28, 7, 1)$
 248 : $P_{9326} = (13, 2, 8, 1)$
 249 : $P_{9336} = (23, 2, 8, 1)$
 250 : $P_{9347} = (2, 3, 8, 1)$
 251 : $P_{9367} = (22, 3, 8, 1)$

252 : $P_{9498} = (25, 7, 8, 1)$
 253 : $P_{9502} = (29, 7, 8, 1)$
 254 : $P_{9508} = (3, 8, 8, 1)$
 255 : $P_{9534} = (29, 8, 8, 1)$
 256 : $P_{9569} = (0, 10, 8, 1)$
 257 : $P_{9586} = (17, 10, 8, 1)$
 258 : $P_{9649} = (16, 12, 8, 1)$
 259 : $P_{9664} = (31, 12, 8, 1)$
 260 : $P_{9778} = (17, 16, 8, 1)$
 261 : $P_{9779} = (18, 16, 8, 1)$
 262 : $P_{9799} = (6, 17, 8, 1)$
 263 : $P_{9815} = (22, 17, 8, 1)$
 264 : $P_{9902} = (13, 20, 8, 1)$
 265 : $P_{9916} = (27, 20, 8, 1)$
 266 : $P_{9974} = (21, 22, 8, 1)$
 267 : $P_{10003} = (18, 23, 8, 1)$
 268 : $P_{10016} = (31, 23, 8, 1)$
 269 : $P_{10070} = (21, 25, 8, 1)$
 270 : $P_{10072} = (23, 25, 8, 1)$
 271 : $P_{10087} = (6, 26, 8, 1)$
 272 : $P_{10108} = (27, 26, 8, 1)$
 273 : $P_{10179} = (2, 29, 8, 1)$
 274 : $P_{10202} = (25, 29, 8, 1)$
 275 : $P_{10244} = (3, 31, 8, 1)$
 276 : $P_{10257} = (16, 31, 8, 1)$
 277 : $P_{10342} = (5, 2, 9, 1)$
 278 : $P_{10367} = (30, 2, 9, 1)$
 279 : $P_{10412} = (11, 4, 9, 1)$
 280 : $P_{10533} = (4, 8, 9, 1)$
 281 : $P_{10556} = (27, 8, 9, 1)$
 282 : $P_{10581} = (20, 9, 9, 1)$
 283 : $P_{10586} = (25, 9, 9, 1)$
 284 : $P_{10595} = (2, 10, 9, 1)$
 285 : $P_{10611} = (18, 10, 9, 1)$
 286 : $P_{10625} = (0, 11, 9, 1)$
 287 : $P_{10650} = (25, 11, 9, 1)$
 288 : $P_{10779} = (26, 15, 9, 1)$
 289 : $P_{10783} = (30, 15, 9, 1)$
 290 : $P_{10790} = (5, 16, 9, 1)$
 291 : $P_{10792} = (7, 16, 9, 1)$
 292 : $P_{10853} = (4, 18, 9, 1)$
 293 : $P_{10864} = (15, 18, 9, 1)$
 294 : $P_{10895} = (14, 19, 9, 1)$
 295 : $P_{10907} = (26, 19, 9, 1)$
 296 : $P_{10920} = (7, 20, 9, 1)$
 297 : $P_{10929} = (16, 20, 9, 1)$
 298 : $P_{10993} = (16, 22, 9, 1)$
 299 : $P_{10994} = (17, 22, 9, 1)$
 300 : $P_{11011} = (2, 23, 9, 1)$
 301 : $P_{11023} = (14, 23, 9, 1)$
 302 : $P_{11081} = (8, 25, 9, 1)$
 303 : $P_{11084} = (11, 25, 9, 1)$
 304 : $P_{11113} = (8, 26, 9, 1)$
 305 : $P_{11125} = (20, 26, 9, 1)$

306 : $P_{11186} = (17, 28, 9, 1)$
 307 : $P_{11196} = (27, 28, 9, 1)$
 308 : $P_{11248} = (15, 30, 9, 1)$
 309 : $P_{11251} = (18, 30, 9, 1)$
 310 : $P_{11395} = (2, 3, 10, 1)$
 311 : $P_{11413} = (20, 3, 10, 1)$
 312 : $P_{11449} = (24, 4, 10, 1)$
 313 : $P_{11452} = (27, 4, 10, 1)$
 314 : $P_{11461} = (4, 5, 10, 1)$
 315 : $P_{11482} = (25, 5, 10, 1)$
 316 : $P_{11513} = (24, 6, 10, 1)$
 317 : $P_{11517} = (28, 6, 10, 1)$
 318 : $P_{11622} = (5, 10, 10, 1)$
 319 : $P_{11639} = (22, 10, 10, 1)$
 320 : $P_{11701} = (20, 12, 10, 1)$
 321 : $P_{11706} = (25, 12, 10, 1)$
 322 : $P_{11722} = (9, 13, 10, 1)$
 323 : $P_{11725} = (12, 13, 10, 1)$
 324 : $P_{11745} = (0, 14, 10, 1)$
 325 : $P_{11757} = (12, 14, 10, 1)$
 326 : $P_{11878} = (5, 18, 10, 1)$
 327 : $P_{11886} = (13, 18, 10, 1)$
 328 : $P_{11975} = (6, 21, 10, 1)$
 329 : $P_{11991} = (22, 21, 10, 1)$
 330 : $P_{12005} = (4, 22, 10, 1)$
 331 : $P_{12007} = (6, 22, 10, 1)$
 332 : $P_{12074} = (9, 24, 10, 1)$
 333 : $P_{12083} = (18, 24, 10, 1)$
 334 : $P_{12125} = (28, 25, 10, 1)$
 335 : $P_{12142} = (13, 26, 10, 1)$
 336 : $P_{12147} = (18, 26, 10, 1)$
 337 : $P_{12227} = (2, 29, 10, 1)$
 338 : $P_{12252} = (27, 29, 10, 1)$
 339 : $P_{12427} = (10, 3, 11, 1)$
 340 : $P_{12446} = (29, 3, 11, 1)$
 341 : $P_{12466} = (17, 4, 11, 1)$
 342 : $P_{12468} = (19, 4, 11, 1)$
 343 : $P_{12523} = (10, 6, 11, 1)$
 344 : $P_{12528} = (15, 6, 11, 1)$
 345 : $P_{12580} = (3, 8, 11, 1)$
 346 : $P_{12607} = (30, 8, 11, 1)$
 347 : $P_{12625} = (16, 9, 11, 1)$
 348 : $P_{12640} = (31, 9, 11, 1)$
 349 : $P_{12643} = (2, 10, 11, 1)$
 350 : $P_{12657} = (16, 10, 11, 1)$
 351 : $P_{12679} = (6, 11, 11, 1)$
 352 : $P_{12702} = (29, 11, 11, 1)$
 353 : $P_{12754} = (17, 13, 11, 1)$
 354 : $P_{12758} = (21, 13, 11, 1)$
 355 : $P_{12773} = (4, 14, 11, 1)$
 356 : $P_{12778} = (9, 14, 11, 1)$
 357 : $P_{12801} = (0, 15, 11, 1)$
 358 : $P_{12807} = (6, 15, 11, 1)$
 359 : $P_{12848} = (15, 16, 11, 1)$

360 : $P_{12938} = (9, 19, 11, 1)$
 361 : $P_{12960} = (31, 19, 11, 1)$
 362 : $P_{13059} = (2, 23, 11, 1)$
 363 : $P_{13069} = (12, 23, 11, 1)$
 364 : $P_{13093} = (4, 24, 11, 1)$
 365 : $P_{13119} = (30, 24, 11, 1)$
 366 : $P_{13133} = (12, 25, 11, 1)$
 367 : $P_{13134} = (13, 25, 11, 1)$
 368 : $P_{13262} = (13, 29, 11, 1)$
 369 : $P_{13270} = (21, 29, 11, 1)$
 370 : $P_{13316} = (3, 31, 11, 1)$
 371 : $P_{13332} = (19, 31, 11, 1)$
 372 : $P_{13414} = (5, 2, 12, 1)$
 373 : $P_{13436} = (27, 2, 12, 1)$
 374 : $P_{13499} = (26, 4, 12, 1)$
 375 : $P_{13504} = (31, 4, 12, 1)$
 376 : $P_{13517} = (12, 5, 12, 1)$
 377 : $P_{13528} = (23, 5, 12, 1)$
 378 : $P_{13589} = (20, 7, 12, 1)$
 379 : $P_{13705} = (8, 11, 12, 1)$
 380 : $P_{13717} = (20, 11, 12, 1)$
 381 : $P_{13859} = (2, 16, 12, 1)$
 382 : $P_{13862} = (5, 16, 12, 1)$
 383 : $P_{13993} = (8, 20, 12, 1)$
 384 : $P_{14011} = (26, 20, 12, 1)$
 385 : $P_{14023} = (6, 21, 12, 1)$
 386 : $P_{14033} = (16, 21, 12, 1)$
 387 : $P_{14051} = (2, 22, 12, 1)$
 388 : $P_{14055} = (6, 22, 12, 1)$
 389 : $P_{14123} = (10, 24, 12, 1)$
 390 : $P_{14136} = (23, 24, 12, 1)$
 391 : $P_{14177} = (0, 26, 12, 1)$
 392 : $P_{14202} = (25, 26, 12, 1)$
 393 : $P_{14219} = (10, 27, 12, 1)$
 394 : $P_{14234} = (25, 27, 12, 1)$
 395 : $P_{14257} = (16, 28, 12, 1)$
 396 : $P_{14272} = (31, 28, 12, 1)$
 397 : $P_{14349} = (12, 31, 12, 1)$
 398 : $P_{14364} = (27, 31, 12, 1)$
 399 : $P_{14478} = (13, 3, 13, 1)$
 400 : $P_{14493} = (28, 3, 13, 1)$
 401 : $P_{14629} = (4, 8, 13, 1)$
 402 : $P_{14656} = (31, 8, 13, 1)$
 403 : $P_{14701} = (12, 10, 13, 1)$
 404 : $P_{14713} = (24, 10, 13, 1)$
 405 : $P_{14727} = (6, 11, 13, 1)$
 406 : $P_{14748} = (27, 11, 13, 1)$
 407 : $P_{14770} = (17, 12, 13, 1)$
 408 : $P_{14780} = (27, 12, 13, 1)$
 409 : $P_{14837} = (20, 14, 13, 1)$
 410 : $P_{14848} = (31, 14, 13, 1)$
 411 : $P_{14855} = (6, 15, 13, 1)$
 412 : $P_{14949} = (4, 18, 13, 1)$
 413 : $P_{14956} = (11, 18, 13, 1)$

414 : $P_{15084} = (11, 22, 13, 1)$
 415 : $P_{15087} = (14, 22, 13, 1)$
 416 : $P_{15125} = (20, 23, 13, 1)$
 417 : $P_{15133} = (28, 23, 13, 1)$
 418 : $P_{15150} = (13, 24, 13, 1)$
 419 : $P_{15154} = (17, 24, 13, 1)$
 420 : $P_{15233} = (0, 27, 13, 1)$
 421 : $P_{15251} = (18, 27, 13, 1)$
 422 : $P_{15309} = (12, 29, 13, 1)$
 423 : $P_{15315} = (18, 29, 13, 1)$
 424 : $P_{15375} = (14, 31, 13, 1)$
 425 : $P_{15385} = (24, 31, 13, 1)$
 426 : $P_{15498} = (9, 3, 14, 1)$
 427 : $P_{15516} = (27, 3, 14, 1)$
 428 : $P_{15557} = (4, 5, 14, 1)$
 429 : $P_{15582} = (29, 5, 14, 1)$
 430 : $P_{15608} = (23, 6, 14, 1)$
 431 : $P_{15626} = (9, 7, 14, 1)$
 432 : $P_{15628} = (11, 7, 14, 1)$
 433 : $P_{15698} = (17, 9, 14, 1)$
 434 : $P_{15708} = (27, 9, 14, 1)$
 435 : $P_{15858} = (17, 14, 14, 1)$
 436 : $P_{15866} = (25, 14, 14, 1)$
 437 : $P_{15907} = (2, 16, 14, 1)$
 438 : $P_{15912} = (7, 16, 14, 1)$
 439 : $P_{15943} = (6, 17, 14, 1)$
 440 : $P_{15953} = (16, 17, 14, 1)$
 441 : $P_{16040} = (7, 20, 14, 1)$
 442 : $P_{16056} = (23, 20, 14, 1)$
 443 : $P_{16099} = (2, 22, 14, 1)$
 444 : $P_{16101} = (4, 22, 14, 1)$
 445 : $P_{16209} = (16, 25, 14, 1)$
 446 : $P_{16213} = (20, 25, 14, 1)$
 447 : $P_{16231} = (6, 26, 14, 1)$
 448 : $P_{16254} = (29, 26, 14, 1)$
 449 : $P_{16268} = (11, 27, 14, 1)$
 450 : $P_{16283} = (26, 27, 14, 1)$
 451 : $P_{16309} = (20, 28, 14, 1)$
 452 : $P_{16314} = (25, 28, 14, 1)$
 453 : $P_{16353} = (0, 30, 14, 1)$
 454 : $P_{16379} = (26, 30, 14, 1)$
 455 : $P_{16591} = (14, 5, 15, 1)$
 456 : $P_{16599} = (22, 5, 15, 1)$
 457 : $P_{16635} = (26, 6, 15, 1)$
 458 : $P_{16636} = (27, 6, 15, 1)$
 459 : $P_{16657} = (16, 7, 15, 1)$
 460 : $P_{16660} = (19, 7, 15, 1)$
 461 : $P_{16684} = (11, 8, 15, 1)$
 462 : $P_{16691} = (18, 8, 15, 1)$
 463 : $P_{16742} = (5, 10, 15, 1)$
 464 : $P_{16756} = (19, 10, 15, 1)$
 465 : $P_{16782} = (13, 11, 15, 1)$
 466 : $P_{16787} = (18, 11, 15, 1)$
 467 : $P_{16864} = (31, 13, 15, 1)$

468 : $P_{16869} = (4, 14, 15, 1)$
 469 : $P_{16878} = (13, 14, 15, 1)$
 470 : $P_{16917} = (20, 15, 15, 1)$
 471 : $P_{16919} = (22, 15, 15, 1)$
 472 : $P_{16937} = (8, 16, 15, 1)$
 473 : $P_{16941} = (12, 16, 15, 1)$
 474 : $P_{16998} = (5, 18, 15, 1)$
 475 : $P_{17001} = (8, 18, 15, 1)$
 476 : $P_{17071} = (14, 20, 15, 1)$
 477 : $P_{17088} = (31, 20, 15, 1)$
 478 : $P_{17148} = (27, 22, 15, 1)$
 479 : $P_{17149} = (28, 22, 15, 1)$
 480 : $P_{17189} = (4, 24, 15, 1)$
 481 : $P_{17211} = (26, 24, 15, 1)$
 482 : $P_{17293} = (12, 27, 15, 1)$
 483 : $P_{17309} = (28, 27, 15, 1)$
 484 : $P_{17388} = (11, 30, 15, 1)$
 485 : $P_{17393} = (16, 30, 15, 1)$
 486 : $P_{17409} = (0, 31, 15, 1)$
 487 : $P_{17429} = (20, 31, 15, 1)$
 488 : $P_{17714} = (17, 8, 16, 1)$
 489 : $P_{17720} = (23, 8, 16, 1)$
 490 : $P_{17742} = (13, 9, 16, 1)$
 491 : $P_{17754} = (25, 9, 16, 1)$
 492 : $P_{17767} = (6, 10, 16, 1)$
 493 : $P_{17776} = (15, 10, 16, 1)$
 494 : $P_{17818} = (25, 11, 16, 1)$
 495 : $P_{17857} = (0, 13, 16, 1)$
 496 : $P_{17888} = (31, 13, 16, 1)$
 497 : $P_{17931} = (10, 15, 16, 1)$
 498 : $P_{17944} = (23, 15, 16, 1)$
 499 : $P_{17990} = (5, 17, 16, 1)$
 500 : $P_{17998} = (13, 17, 16, 1)$
 501 : $P_{18051} = (2, 19, 16, 1)$
 502 : $P_{18064} = (15, 19, 16, 1)$
 503 : $P_{18098} = (17, 20, 16, 1)$
 504 : $P_{18112} = (31, 20, 16, 1)$
 505 : $P_{18182} = (5, 23, 16, 1)$
 506 : $P_{18193} = (16, 23, 16, 1)$
 507 : $P_{18289} = (16, 26, 16, 1)$
 508 : $P_{18294} = (21, 26, 16, 1)$
 509 : $P_{18343} = (6, 28, 16, 1)$
 510 : $P_{18358} = (21, 28, 16, 1)$
 511 : $P_{18378} = (9, 29, 16, 1)$
 512 : $P_{18379} = (10, 29, 16, 1)$
 513 : $P_{18435} = (2, 31, 16, 1)$
 514 : $P_{18442} = (9, 31, 16, 1)$
 515 : $P_{18541} = (12, 2, 17, 1)$
 516 : $P_{18544} = (15, 2, 17, 1)$
 517 : $P_{18578} = (17, 3, 17, 1)$
 518 : $P_{18589} = (28, 3, 17, 1)$
 519 : $P_{18596} = (3, 4, 17, 1)$
 520 : $P_{18620} = (27, 4, 17, 1)$
 521 : $P_{18669} = (12, 6, 17, 1)$

522 : $P_{18676} = (19, 6, 17, 1)$
 523 : $P_{18693} = (4, 7, 17, 1)$
 524 : $P_{18714} = (25, 7, 17, 1)$
 525 : $P_{18759} = (6, 9, 17, 1)$
 526 : $P_{18772} = (19, 9, 17, 1)$
 527 : $P_{18849} = (0, 12, 17, 1)$
 528 : $P_{18871} = (22, 12, 17, 1)$
 529 : $P_{18889} = (8, 13, 17, 1)$
 530 : $P_{18903} = (22, 13, 17, 1)$
 531 : $P_{18958} = (13, 15, 17, 1)$
 532 : $P_{18962} = (17, 15, 17, 1)$
 533 : $P_{19141} = (4, 21, 17, 1)$
 534 : $P_{19152} = (15, 21, 17, 1)$
 535 : $P_{19209} = (8, 23, 17, 1)$
 536 : $P_{19229} = (28, 23, 17, 1)$
 537 : $P_{19239} = (6, 24, 17, 1)$
 538 : $P_{19332} = (3, 27, 17, 1)$
 539 : $P_{19342} = (13, 27, 17, 1)$
 540 : $P_{19418} = (25, 29, 17, 1)$
 541 : $P_{19420} = (27, 29, 17, 1)$
 542 : $P_{19562} = (9, 2, 18, 1)$
 543 : $P_{19620} = (3, 4, 18, 1)$
 544 : $P_{19641} = (24, 4, 18, 1)$
 545 : $P_{19685} = (4, 6, 18, 1)$
 546 : $P_{19705} = (24, 6, 18, 1)$
 547 : $P_{19772} = (27, 8, 18, 1)$
 548 : $P_{19776} = (31, 8, 18, 1)$
 549 : $P_{19777} = (0, 9, 18, 1)$
 550 : $P_{19799} = (22, 9, 18, 1)$
 551 : $P_{19853} = (12, 11, 18, 1)$
 552 : $P_{19855} = (14, 11, 18, 1)$
 553 : $P_{19879} = (6, 12, 18, 1)$
 554 : $P_{19892} = (19, 12, 18, 1)$
 555 : $P_{19948} = (11, 14, 18, 1)$
 556 : $P_{19968} = (31, 14, 18, 1)$
 557 : $P_{20071} = (6, 18, 18, 1)$
 558 : $P_{20087} = (22, 18, 18, 1)$
 559 : $P_{20099} = (2, 19, 18, 1)$
 560 : $P_{20110} = (13, 19, 18, 1)$
 561 : $P_{20166} = (5, 21, 18, 1)$
 562 : $P_{20174} = (13, 21, 18, 1)$
 563 : $P_{20202} = (9, 22, 18, 1)$
 564 : $P_{20212} = (19, 22, 18, 1)$
 565 : $P_{20356} = (3, 27, 18, 1)$
 566 : $P_{20367} = (14, 27, 18, 1)$
 567 : $P_{20395} = (10, 28, 18, 1)$
 568 : $P_{20412} = (27, 28, 18, 1)$
 569 : $P_{20421} = (4, 29, 18, 1)$
 570 : $P_{20422} = (5, 29, 18, 1)$
 571 : $P_{20459} = (10, 30, 18, 1)$
 572 : $P_{20461} = (12, 30, 18, 1)$
 573 : $P_{20483} = (2, 31, 18, 1)$
 574 : $P_{20492} = (11, 31, 18, 1)$
 575 : $P_{20646} = (5, 4, 19, 1)$

576 : $P_{20672} = (31, 4, 19, 1)$
 577 : $P_{20698} = (25, 5, 19, 1)$
 578 : $P_{20702} = (29, 5, 19, 1)$
 579 : $P_{20718} = (13, 6, 19, 1)$
 580 : $P_{20721} = (16, 6, 19, 1)$
 581 : $P_{20769} = (0, 8, 19, 1)$
 582 : $P_{20774} = (5, 8, 19, 1)$
 583 : $P_{20910} = (13, 12, 19, 1)$
 584 : $P_{20922} = (25, 12, 19, 1)$
 585 : $P_{20997} = (4, 15, 19, 1)$
 586 : $P_{21019} = (26, 15, 19, 1)$
 587 : $P_{21061} = (4, 17, 19, 1)$
 588 : $P_{21072} = (15, 17, 19, 1)$
 589 : $P_{21141} = (20, 19, 19, 1)$
 590 : $P_{21147} = (26, 19, 19, 1)$
 591 : $P_{21175} = (22, 20, 19, 1)$
 592 : $P_{21180} = (27, 20, 19, 1)$
 593 : $P_{21224} = (7, 22, 19, 1)$
 594 : $P_{21245} = (28, 22, 19, 1)$
 595 : $P_{21301} = (20, 24, 19, 1)$
 596 : $P_{21303} = (22, 24, 19, 1)$
 597 : $P_{21372} = (27, 26, 19, 1)$
 598 : $P_{21374} = (29, 26, 19, 1)$
 599 : $P_{21393} = (16, 27, 19, 1)$
 600 : $P_{21405} = (28, 27, 19, 1)$
 601 : $P_{21424} = (15, 28, 19, 1)$
 602 : $P_{21440} = (31, 28, 19, 1)$
 603 : $P_{21448} = (7, 29, 19, 1)$
 604 : $P_{21609} = (8, 2, 20, 1)$
 605 : $P_{21615} = (14, 2, 20, 1)$
 606 : $P_{21673} = (8, 4, 20, 1)$
 607 : $P_{21686} = (21, 4, 20, 1)$
 608 : $P_{21713} = (16, 5, 20, 1)$
 609 : $P_{21716} = (19, 5, 20, 1)$
 610 : $P_{21730} = (1, 6, 20, 1)$
 611 : $P_{21756} = (27, 6, 20, 1)$
 612 : $P_{21775} = (14, 7, 20, 1)$
 613 : $P_{21783} = (22, 7, 20, 1)$
 614 : $P_{21840} = (15, 9, 20, 1)$
 615 : $P_{21856} = (31, 9, 20, 1)$
 616 : $P_{21927} = (6, 12, 20, 1)$
 617 : $P_{21942} = (21, 12, 20, 1)$
 618 : $P_{21986} = (1, 14, 20, 1)$
 619 : $P_{22004} = (19, 14, 20, 1)$
 620 : $P_{22119} = (6, 18, 20, 1)$
 621 : $P_{22129} = (16, 18, 20, 1)$
 622 : $P_{22167} = (22, 19, 20, 1)$
 623 : $P_{22176} = (31, 19, 20, 1)$
 624 : $P_{22248} = (7, 22, 20, 1)$
 625 : $P_{22268} = (27, 22, 20, 1)$
 626 : $P_{22352} = (15, 25, 20, 1)$
 627 : $P_{22354} = (17, 25, 20, 1)$
 628 : $P_{22418} = (17, 27, 20, 1)$
 629 : $P_{22427} = (26, 27, 20, 1)$

630 : $P_{22465} = (0, 29, 20, 1)$
 631 : $P_{22472} = (7, 29, 20, 1)$
 632 : $P_{22523} = (26, 30, 20, 1)$
 633 : $P_{22644} = (19, 2, 21, 1)$
 634 : $P_{22645} = (20, 2, 21, 1)$
 635 : $P_{22675} = (18, 3, 21, 1)$
 636 : $P_{22684} = (27, 3, 21, 1)$
 637 : $P_{22730} = (9, 5, 21, 1)$
 638 : $P_{22732} = (11, 5, 21, 1)$
 639 : $P_{22754} = (1, 6, 21, 1)$
 640 : $P_{22779} = (26, 6, 21, 1)$
 641 : $P_{22789} = (4, 7, 21, 1)$
 642 : $P_{22814} = (29, 7, 21, 1)$
 643 : $P_{22846} = (29, 8, 21, 1)$
 644 : $P_{22847} = (30, 8, 21, 1)$
 645 : $P_{22859} = (10, 9, 21, 1)$
 646 : $P_{22876} = (27, 9, 21, 1)$
 647 : $P_{22901} = (20, 10, 21, 1)$
 648 : $P_{22905} = (24, 10, 21, 1)$
 649 : $P_{22929} = (16, 11, 21, 1)$
 650 : $P_{22934} = (21, 11, 21, 1)$
 651 : $P_{22987} = (10, 13, 21, 1)$
 652 : $P_{22993} = (16, 13, 21, 1)$
 653 : $P_{23010} = (1, 14, 21, 1)$
 654 : $P_{23027} = (18, 14, 21, 1)$
 655 : $P_{23110} = (5, 17, 21, 1)$
 656 : $P_{23113} = (8, 17, 21, 1)$
 657 : $P_{23237} = (4, 21, 21, 1)$
 658 : $P_{23244} = (11, 21, 21, 1)$
 659 : $P_{23302} = (5, 23, 21, 1)$
 660 : $P_{23318} = (21, 23, 21, 1)$
 661 : $P_{23355} = (26, 24, 21, 1)$
 662 : $P_{23359} = (30, 24, 21, 1)$
 663 : $P_{23418} = (25, 26, 21, 1)$
 664 : $P_{23444} = (19, 27, 21, 1)$
 665 : $P_{23450} = (25, 27, 21, 1)$
 666 : $P_{23457} = (0, 28, 21, 1)$
 667 : $P_{23479} = (22, 28, 21, 1)$
 668 : $P_{23529} = (8, 30, 21, 1)$
 669 : $P_{23530} = (9, 30, 21, 1)$
 670 : $P_{23575} = (22, 31, 21, 1)$
 671 : $P_{23577} = (24, 31, 21, 1)$
 672 : $P_{23704} = (23, 3, 22, 1)$
 673 : $P_{23710} = (29, 3, 22, 1)$
 674 : $P_{23718} = (5, 4, 22, 1)$
 675 : $P_{23739} = (26, 4, 22, 1)$
 676 : $P_{23781} = (4, 6, 22, 1)$
 677 : $P_{23805} = (28, 6, 22, 1)$
 678 : $P_{23846} = (5, 8, 22, 1)$
 679 : $P_{23911} = (6, 10, 22, 1)$
 680 : $P_{23914} = (9, 10, 22, 1)$
 681 : $P_{23964} = (27, 11, 22, 1)$
 682 : $P_{23966} = (29, 11, 22, 1)$
 683 : $P_{23979} = (10, 12, 22, 1)$

684 : $P_{23996} = (27, 12, 22, 1)$
 685 : $P_{24015} = (14, 13, 22, 1)$
 686 : $P_{24024} = (23, 13, 22, 1)$
 687 : $P_{24074} = (9, 15, 22, 1)$
 688 : $P_{24083} = (18, 15, 22, 1)$
 689 : $P_{24111} = (14, 16, 22, 1)$
 690 : $P_{24116} = (19, 16, 22, 1)$
 691 : $P_{24194} = (1, 19, 22, 1)$
 692 : $P_{24203} = (10, 19, 22, 1)$
 693 : $P_{24243} = (18, 20, 22, 1)$
 694 : $P_{24251} = (26, 20, 22, 1)$
 695 : $P_{24385} = (0, 25, 22, 1)$
 696 : $P_{24413} = (28, 25, 22, 1)$
 697 : $P_{24487} = (6, 28, 22, 1)$
 698 : $P_{24500} = (19, 28, 22, 1)$
 699 : $P_{24514} = (1, 29, 22, 1)$
 700 : $P_{24517} = (4, 29, 22, 1)$
 701 : $P_{24700} = (27, 2, 23, 1)$
 702 : $P_{24703} = (30, 2, 23, 1)$
 703 : $P_{24747} = (10, 4, 23, 1)$
 704 : $P_{24757} = (20, 4, 23, 1)$
 705 : $P_{24789} = (20, 5, 23, 1)$
 706 : $P_{24845} = (12, 7, 23, 1)$
 707 : $P_{24856} = (23, 7, 23, 1)$
 708 : $P_{24879} = (14, 8, 23, 1)$
 709 : $P_{24880} = (15, 8, 23, 1)$
 710 : $P_{24903} = (6, 9, 23, 1)$
 711 : $P_{24918} = (21, 9, 23, 1)$
 712 : $P_{25008} = (15, 12, 23, 1)$
 713 : $P_{25024} = (31, 12, 23, 1)$
 714 : $P_{25065} = (8, 14, 23, 1)$
 715 : $P_{25082} = (25, 14, 23, 1)$
 716 : $P_{25093} = (4, 15, 23, 1)$
 717 : $P_{25119} = (30, 15, 23, 1)$
 718 : $P_{25131} = (10, 16, 23, 1)$
 719 : $P_{25143} = (22, 16, 23, 1)$
 720 : $P_{25157} = (4, 17, 23, 1)$
 721 : $P_{25164} = (11, 17, 23, 1)$
 722 : $P_{25218} = (1, 19, 23, 1)$
 723 : $P_{25228} = (11, 19, 23, 1)$
 724 : $P_{25286} = (5, 21, 23, 1)$
 725 : $P_{25289} = (8, 21, 23, 1)$
 726 : $P_{25358} = (13, 23, 23, 1)$
 727 : $P_{25376} = (31, 23, 23, 1)$
 728 : $P_{25377} = (0, 24, 23, 1)$
 729 : $P_{25383} = (6, 24, 23, 1)$
 730 : $P_{25453} = (12, 26, 23, 1)$
 731 : $P_{25455} = (14, 26, 23, 1)$
 732 : $P_{25518} = (13, 28, 23, 1)$
 733 : $P_{25530} = (25, 28, 23, 1)$
 734 : $P_{25538} = (1, 29, 23, 1)$
 735 : $P_{25542} = (5, 29, 23, 1)$
 736 : $P_{25590} = (21, 30, 23, 1)$
 737 : $P_{25591} = (22, 30, 23, 1)$

738 : $P_{25624} = (23, 31, 23, 1)$
 739 : $P_{25628} = (27, 31, 23, 1)$
 740 : $P_{25755} = (26, 3, 24, 1)$
 741 : $P_{25759} = (30, 3, 24, 1)$
 742 : $P_{25763} = (2, 4, 24, 1)$
 743 : $P_{25780} = (19, 4, 24, 1)$
 744 : $P_{25857} = (0, 7, 24, 1)$
 745 : $P_{25877} = (20, 7, 24, 1)$
 746 : $P_{25890} = (1, 8, 24, 1)$
 747 : $P_{25904} = (15, 8, 24, 1)$
 748 : $P_{25983} = (30, 10, 24, 1)$
 749 : $P_{25984} = (31, 10, 24, 1)$
 750 : $P_{26005} = (20, 11, 24, 1)$
 751 : $P_{26013} = (28, 11, 24, 1)$
 752 : $P_{26032} = (15, 12, 24, 1)$
 753 : $P_{26033} = (16, 12, 24, 1)$
 754 : $P_{26063} = (14, 13, 24, 1)$
 755 : $P_{26074} = (25, 13, 24, 1)$
 756 : $P_{26159} = (14, 16, 24, 1)$
 757 : $P_{26174} = (29, 16, 24, 1)$
 758 : $P_{26206} = (29, 17, 24, 1)$
 759 : $P_{26211} = (2, 18, 24, 1)$
 760 : $P_{26233} = (24, 18, 24, 1)$
 761 : $P_{26266} = (25, 19, 24, 1)$
 762 : $P_{26269} = (28, 19, 24, 1)$
 763 : $P_{26329} = (24, 21, 24, 1)$
 764 : $P_{26331} = (26, 21, 24, 1)$
 765 : $P_{26338} = (1, 22, 24, 1)$
 766 : $P_{26354} = (17, 22, 24, 1)$
 767 : $P_{26375} = (6, 23, 24, 1)$
 768 : $P_{26396} = (27, 23, 24, 1)$
 769 : $P_{26419} = (18, 24, 24, 1)$
 770 : $P_{26428} = (27, 24, 24, 1)$
 771 : $P_{26483} = (18, 26, 24, 1)$
 772 : $P_{26496} = (31, 26, 24, 1)$
 773 : $P_{26539} = (10, 28, 24, 1)$
 774 : $P_{26546} = (17, 28, 24, 1)$
 775 : $P_{26599} = (6, 30, 24, 1)$
 776 : $P_{26603} = (10, 30, 24, 1)$
 777 : $P_{26641} = (16, 31, 24, 1)$
 778 : $P_{26644} = (19, 31, 24, 1)$
 779 : $P_{26839} = (22, 5, 25, 1)$
 780 : $P_{26841} = (24, 5, 25, 1)$
 781 : $P_{26849} = (0, 6, 25, 1)$
 782 : $P_{26872} = (23, 6, 25, 1)$
 783 : $P_{26914} = (1, 8, 25, 1)$
 784 : $P_{26927} = (14, 8, 25, 1)$
 785 : $P_{26994} = (17, 10, 25, 1)$
 786 : $P_{27081} = (8, 13, 25, 1)$
 787 : $P_{27103} = (30, 13, 25, 1)$
 788 : $P_{27116} = (11, 14, 25, 1)$
 789 : $P_{27125} = (20, 14, 25, 1)$
 790 : $P_{27139} = (2, 15, 25, 1)$
 791 : $P_{27159} = (22, 15, 25, 1)$

792 : $P_{27172} = (3, 16, 25, 1)$
 793 : $P_{27186} = (17, 16, 25, 1)$
 794 : $P_{27313} = (16, 20, 25, 1)$
 795 : $P_{27320} = (23, 20, 25, 1)$
 796 : $P_{27362} = (1, 22, 25, 1)$
 797 : $P_{27377} = (16, 22, 25, 1)$
 798 : $P_{27401} = (8, 23, 25, 1)$
 799 : $P_{27413} = (20, 23, 25, 1)$
 800 : $P_{27491} = (2, 26, 25, 1)$
 801 : $P_{27503} = (14, 26, 25, 1)$
 802 : $P_{27545} = (24, 27, 25, 1)$
 803 : $P_{27551} = (30, 27, 25, 1)$
 804 : $P_{27588} = (3, 29, 25, 1)$
 805 : $P_{27594} = (9, 29, 25, 1)$
 806 : $P_{27658} = (9, 31, 25, 1)$
 807 : $P_{27660} = (11, 31, 25, 1)$
 808 : $P_{27751} = (6, 2, 26, 1)$
 809 : $P_{27759} = (14, 2, 26, 1)$
 810 : $P_{27777} = (0, 3, 26, 1)$
 811 : $P_{27783} = (6, 3, 26, 1)$
 812 : $P_{27811} = (2, 4, 26, 1)$
 813 : $P_{27826} = (17, 4, 26, 1)$
 814 : $P_{27919} = (14, 7, 26, 1)$
 815 : $P_{27929} = (24, 7, 26, 1)$
 816 : $P_{28101} = (4, 13, 26, 1)$
 817 : $P_{28114} = (17, 13, 26, 1)$
 818 : $P_{28171} = (10, 15, 26, 1)$
 819 : $P_{28190} = (29, 15, 26, 1)$
 820 : $P_{28196} = (3, 16, 26, 1)$
 821 : $P_{28211} = (18, 16, 26, 1)$
 822 : $P_{28249} = (24, 17, 26, 1)$
 823 : $P_{28251} = (26, 17, 26, 1)$
 824 : $P_{28259} = (2, 18, 26, 1)$
 825 : $P_{28283} = (26, 18, 26, 1)$
 826 : $P_{28382} = (29, 21, 26, 1)$
 827 : $P_{28430} = (13, 23, 26, 1)$
 828 : $P_{28435} = (18, 23, 26, 1)$
 829 : $P_{28485} = (4, 25, 26, 1)$
 830 : $P_{28501} = (20, 25, 26, 1)$
 831 : $P_{28590} = (13, 28, 26, 1)$
 832 : $P_{28597} = (20, 28, 26, 1)$
 833 : $P_{28612} = (3, 29, 26, 1)$
 834 : $P_{28619} = (10, 29, 26, 1)$
 835 : $P_{28769} = (0, 2, 27, 1)$
 836 : $P_{28778} = (9, 2, 27, 1)$
 837 : $P_{28888} = (23, 5, 27, 1)$
 838 : $P_{28892} = (27, 5, 27, 1)$
 839 : $P_{28941} = (12, 7, 27, 1)$
 840 : $P_{28956} = (27, 7, 27, 1)$
 841 : $P_{29008} = (15, 9, 27, 1)$
 842 : $P_{29009} = (16, 9, 27, 1)$
 843 : $P_{29041} = (16, 10, 27, 1)$
 844 : $P_{29043} = (18, 10, 27, 1)$
 845 : $P_{29160} = (7, 14, 27, 1)$

846 : $P_{29179} = (26, 14, 27, 1)$
 847 : $P_{29187} = (2, 15, 27, 1)$
 848 : $P_{29205} = (20, 15, 27, 1)$
 849 : $P_{29288} = (7, 18, 27, 1)$
 850 : $P_{29311} = (30, 18, 27, 1)$
 851 : $P_{29418} = (9, 22, 27, 1)$
 852 : $P_{29435} = (26, 22, 27, 1)$
 853 : $P_{29496} = (23, 24, 27, 1)$
 854 : $P_{29502} = (29, 24, 27, 1)$
 855 : $P_{29520} = (15, 25, 27, 1)$
 856 : $P_{29535} = (30, 25, 27, 1)$
 857 : $P_{29539} = (2, 26, 27, 1)$
 858 : $P_{29549} = (12, 26, 27, 1)$
 859 : $P_{29683} = (18, 30, 27, 1)$
 860 : $P_{29694} = (29, 30, 27, 1)$
 861 : $P_{29717} = (20, 31, 27, 1)$
 862 : $P_{29799} = (6, 2, 28, 1)$
 863 : $P_{29801} = (8, 2, 28, 1)$
 864 : $P_{29831} = (6, 3, 28, 1)$
 865 : $P_{29865} = (8, 4, 28, 1)$
 866 : $P_{29886} = (29, 4, 28, 1)$
 867 : $P_{29891} = (2, 5, 28, 1)$
 868 : $P_{29898} = (9, 5, 28, 1)$
 869 : $P_{29956} = (3, 7, 28, 1)$
 870 : $P_{29972} = (19, 7, 28, 1)$
 871 : $P_{30068} = (19, 10, 28, 1)$
 872 : $P_{30071} = (22, 10, 28, 1)$
 873 : $P_{30083} = (2, 11, 28, 1)$
 874 : $P_{30095} = (14, 11, 28, 1)$
 875 : $P_{30123} = (10, 12, 28, 1)$
 876 : $P_{30130} = (17, 12, 28, 1)$
 877 : $P_{30184} = (7, 14, 28, 1)$
 878 : $P_{30206} = (29, 14, 28, 1)$
 879 : $P_{30222} = (13, 15, 28, 1)$
 880 : $P_{30237} = (28, 15, 28, 1)$
 881 : $P_{30284} = (11, 17, 28, 1)$
 882 : $P_{30288} = (15, 17, 28, 1)$
 883 : $P_{30312} = (7, 18, 28, 1)$
 884 : $P_{30330} = (25, 18, 28, 1)$
 885 : $P_{30347} = (10, 19, 28, 1)$
 886 : $P_{30348} = (11, 19, 28, 1)$
 887 : $P_{30370} = (1, 20, 28, 1)$
 888 : $P_{30372} = (3, 20, 28, 1)$
 889 : $P_{30417} = (16, 21, 28, 1)$
 890 : $P_{30423} = (22, 21, 28, 1)$
 891 : $P_{30465} = (0, 23, 28, 1)$
 892 : $P_{30490} = (25, 23, 28, 1)$
 893 : $P_{30514} = (17, 24, 28, 1)$
 894 : $P_{30525} = (28, 24, 28, 1)$
 895 : $P_{30606} = (13, 27, 28, 1)$
 896 : $P_{30607} = (14, 27, 28, 1)$
 897 : $P_{30640} = (15, 28, 28, 1)$
 898 : $P_{30641} = (16, 28, 28, 1)$
 899 : $P_{30690} = (1, 30, 28, 1)$

900 : $P_{30698} = (9, 30, 28, 1)$
 901 : $P_{30820} = (3, 2, 29, 1)$
 902 : $P_{30829} = (12, 2, 29, 1)$
 903 : $P_{30891} = (10, 4, 29, 1)$
 904 : $P_{30911} = (30, 4, 29, 1)$
 905 : $P_{30957} = (12, 6, 29, 1)$
 906 : $P_{30976} = (31, 6, 29, 1)$
 907 : $P_{31027} = (18, 8, 29, 1)$
 908 : $P_{31034} = (25, 8, 29, 1)$
 909 : $P_{31054} = (13, 9, 29, 1)$
 910 : $P_{31061} = (20, 9, 29, 1)$
 911 : $P_{31123} = (18, 11, 29, 1)$
 912 : $P_{31136} = (31, 11, 29, 1)$
 913 : $P_{31275} = (10, 16, 29, 1)$
 914 : $P_{31293} = (28, 16, 29, 1)$
 915 : $P_{31305} = (8, 17, 29, 1)$
 916 : $P_{31310} = (13, 17, 29, 1)$
 917 : $P_{31364} = (3, 19, 29, 1)$
 918 : $P_{31394} = (1, 20, 29, 1)$
 919 : $P_{31395} = (2, 20, 29, 1)$
 920 : $P_{31450} = (25, 21, 29, 1)$
 921 : $P_{31455} = (30, 21, 29, 1)$
 922 : $P_{31457} = (0, 22, 29, 1)$
 923 : $P_{31478} = (21, 22, 29, 1)$
 924 : $P_{31555} = (2, 25, 29, 1)$
 925 : $P_{31574} = (21, 25, 29, 1)$
 926 : $P_{31605} = (20, 26, 29, 1)$
 927 : $P_{31613} = (28, 26, 29, 1)$
 928 : $P_{31714} = (1, 30, 29, 1)$
 929 : $P_{31721} = (8, 30, 29, 1)$
 930 : $P_{31844} = (3, 2, 30, 1)$
 931 : $P_{31856} = (15, 2, 30, 1)$
 932 : $P_{31893} = (20, 3, 30, 1)$
 933 : $P_{31895} = (22, 3, 30, 1)$
 934 : $P_{31939} = (2, 5, 30, 1)$
 935 : $P_{31948} = (11, 5, 30, 1)$
 936 : $P_{31982} = (13, 6, 30, 1)$
 937 : $P_{31998} = (29, 6, 30, 1)$
 938 : $P_{32131} = (2, 11, 30, 1)$
 939 : $P_{32141} = (12, 11, 30, 1)$
 940 : $P_{32174} = (13, 12, 30, 1)$
 941 : $P_{32181} = (20, 12, 30, 1)$
 942 : $P_{32197} = (4, 13, 30, 1)$
 943 : $P_{32214} = (21, 13, 30, 1)$
 944 : $P_{32337} = (16, 17, 30, 1)$
 945 : $P_{32343} = (22, 17, 30, 1)$
 946 : $P_{32385} = (0, 19, 30, 1)$
 947 : $P_{32388} = (3, 19, 30, 1)$
 948 : $P_{32441} = (24, 20, 30, 1)$
 949 : $P_{32460} = (11, 21, 30, 1)$
 950 : $P_{32464} = (15, 21, 30, 1)$
 951 : $P_{32519} = (6, 23, 30, 1)$
 952 : $P_{32542} = (29, 23, 30, 1)$
 953 : $P_{32581} = (4, 25, 30, 1)$

954 : $P_{32593} = (16, 25, 30, 1)$
 955 : $P_{32726} = (21, 29, 30, 1)$
 956 : $P_{32729} = (24, 29, 30, 1)$
 957 : $P_{32743} = (6, 30, 30, 1)$
 958 : $P_{32749} = (12, 30, 30, 1)$
 959 : $P_{32888} = (23, 2, 31, 1)$
 960 : $P_{32891} = (26, 2, 31, 1)$
 961 : $P_{33028} = (3, 7, 31, 1)$
 962 : $P_{33041} = (16, 7, 31, 1)$
 963 : $P_{33099} = (10, 9, 31, 1)$
 964 : $P_{33106} = (17, 9, 31, 1)$
 965 : $P_{33130} = (9, 10, 31, 1)$
 966 : $P_{33136} = (15, 10, 31, 1)$
 967 : $P_{33227} = (10, 13, 31, 1)$
 968 : $P_{33243} = (26, 13, 31, 1)$
 969 : $P_{33257} = (8, 14, 31, 1)$
 970 : $P_{33266} = (17, 14, 31, 1)$
 971 : $P_{33290} = (9, 15, 31, 1)$
 972 : $P_{33308} = (27, 15, 31, 1)$
 973 : $P_{33370} = (25, 17, 31, 1)$

974 : $P_{33375} = (30, 17, 31, 1)$
 975 : $P_{33377} = (0, 18, 31, 1)$
 976 : $P_{33406} = (29, 18, 31, 1)$
 977 : $P_{33422} = (13, 19, 31, 1)$
 978 : $P_{33424} = (15, 19, 31, 1)$
 979 : $P_{33443} = (2, 20, 31, 1)$
 980 : $P_{33444} = (3, 20, 31, 1)$
 981 : $P_{33481} = (8, 21, 31, 1)$
 982 : $P_{33486} = (13, 21, 31, 1)$
 983 : $P_{33603} = (2, 25, 31, 1)$
 984 : $P_{33624} = (23, 25, 31, 1)$
 985 : $P_{33683} = (18, 27, 31, 1)$
 986 : $P_{33747} = (18, 29, 31, 1)$
 987 : $P_{33759} = (30, 29, 31, 1)$
 988 : $P_{33777} = (16, 30, 31, 1)$
 989 : $P_{33788} = (27, 30, 31, 1)$
 990 : $P_{33818} = (25, 31, 31, 1)$
 991 : $P_{33822} = (29, 31, 31, 1)$

Line Intersection Graph

	0 1
0	0 1
1	1 0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1
in point	P_2

Line 1 intersects

Line	ℓ_0
in point	P_2

The surface has 1057 points:

Too many to print.