Rank-65858 over GF(4)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_2 + X_1^2 X_2 + X_0 X_1 X_2 = 0$$

(1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over ${\rm GF}(4)$ is 1431722670

General information

Number of lines	0
Number of points	21
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	0
Number of points off lines	21
Number of Hesse planes	0
Number of axes	0
Type of points on lines	
Type of lines on points	0^{21}

Singular Points

The surface has 0 singular points:

The 0 Lines

The lines and their Pluecker coordinates are:

Rank of lines: ()

Rank of points on Klein quadric: ()

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 0 single points: The single points on the surface are:

The single points on the surface are:

Points on surface but on no line

The surface has 21 points not on any line: The points on the surface but not on lines are:

```
0: P_4 = (1, 1, 1, 1)
                                                                   11: P_{39} = (1, 0, 1, 1)
                                                                   12: P_{42} = (0, 1, 1, 1)
1: P_{23} = (1,0,0,1)
2: P_{24} = (2,0,0,1)
                                                                   13: P_{53} = (0, 0, 2, 1)
3: P_{25} = (3,0,0,1)
                                                                   14: P_{55} = (2,0,2,1)
4: P_{26} = (0, 1, 0, 1)
                                                                   15: P_{61} = (0, 2, 2, 1)
5: P_{27} = (1, 1, 0, 1)
                                                                   16: P_{63} = (2, 2, 2, 1)
6: P_{30} = (0, 2, 0, 1)
                                                                   17: P_{69} = (0, 0, 3, 1)
                                                                   18: P_{72} = (3, 0, 3, 1)
7: P_{32} = (2, 2, 0, 1)
8: P_{34} = (0, 3, 0, 1)
                                                                   19: P_{81} = (0, 3, 3, 1)
9: P_{37} = (3, 3, 0, 1)
                                                                   20: P_{84} = (3, 3, 3, 1)
10: P_{38} = (0, 0, 1, 1)
```

Line Intersection Graph

Neighbor sets in the line intersection graph:

The surface has 21 points:

The points on the surface are:

```
0: P_4 = (1, 1, 1, 1)
                                            8: P_{34} = (0,3,0,1)
                                                                                        16: P_{63} = (2, 2, 2, 1)
1: P_{23} = (1,0,0,1)
                                            9: P_{37} = (3,3,0,1)
                                                                                        17: P_{69} = (0, 0, 3, 1)
                                                                                        18: P_{72} = (3, 0, 3, 1)
2: P_{24} = (2,0,0,1)
                                            10: P_{38} = (0, 0, 1, 1)
                                            11: P_{39} = (1, 0, 1, 1)
3: P_{25} = (3,0,0,1)
                                                                                        19: P_{81} = (0, 3, 3, 1)
4: P_{26} = (0, 1, 0, 1)
                                            12: P_{42} = (0, 1, 1, 1)
                                                                                        20: P_{84} = (3, 3, 3, 1)
5: P_{27} = (1, 1, 0, 1)
                                            13: P_{53} = (0, 0, 2, 1)
6: P_{30} = (0, 2, 0, 1)
                                            14: P_{55} = (2, 0, 2, 1)
7: P_{32} = (2, 2, 0, 1)
                                            15: P_{61} = (0, 2, 2, 1)
```