Rank-74280 over GF(8)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_2^3 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(1, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 0) The point rank of the equation over GF(8) is 1361384078

General information

Number of lines	0
Number of points	49
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	0
Number of points off lines	49
Number of Hesse planes	0
Number of axes	0
Type of points on lines	
Type of lines on points	0^{49}

Singular Points

The surface has 0 singular points:

The 0 Lines

The lines and their Pluecker coordinates are:

Rank of lines: ()

Rank of points on Klein quadric: ()

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 0 single points: The single points on the surface are:

The single points on the surface are:

Points on surface but on no line

The surface has 49 points not on any line: The points on the surface but not on lines are:

$0: P_{1} = (0, 1, 0, 0)$ $1: P_{3} = (0, 0, 0, 1)$ $2: P_{4} = (1, 1, 1, 1)$ $3: P_{13} = (2, 0, 1, 0)$ $4: P_{15} = (4, 0, 1, 0)$ $5: P_{18} = (7, 0, 1, 0)$ $6: P_{20} = (1, 1, 1, 0)$	$25: P_{213} = (4, 1, 2, 1)$ $26: P_{225} = (0, 3, 2, 1)$ $27: P_{237} = (4, 4, 2, 1)$ $28: P_{272} = (7, 0, 3, 1)$ $29: P_{279} = (6, 1, 3, 1)$ $30: P_{304} = (7, 4, 3, 1)$ $31: P_{319} = (6, 6, 3, 1)$
$7: P_{30} = (3, 2, 1, 0)$	$32: P_{321} = (0,7,3,1)$
$8: P_{48} = (5, 4, 1, 0)$	$33: P_{344} = (7, 1, 4, 1)$
$9: P_{73} = (6,7,1,0)$	$34: P_{369} = (0, 5, 4, 1)$
$10: P_{75} = (1,0,0,1)$	$35: P_{392} = (7,7,4,1)$
$11: P_{85} = (3, 1, 0, 1)$	$36: P_{395} = (2, 0, 5, 1)$
$12: P_{87} = (5, 1, 0, 1)$	$37: P_{404} = (3, 1, 5, 1)$
$13: P_{88} = (6, 1, 0, 1)$	$38: P_{409} = (0, 2, 5, 1)$
$14: P_{97} = (7, 2, 0, 1)$	$39: P_{420} = (3, 3, 5, 1)$
$15: P_{108} = (2, 4, 0, 1)$	$40: P_{451} = (2, 7, 5, 1)$
$16: P_{134} = (4, 7, 0, 1)$	$41: P_{461} = (4, 0, 6, 1)$
$17: P_{139} = (1, 0, 1, 1)$	$42: P_{470} = (5, 1, 6, 1)$
$18: P_{146} = (0, 1, 1, 1)$	$43: P_{477} = (4, 2, 6, 1)$
$19: P_{160} = (7, 2, 1, 1)$	$44: P_{489} = (0, 4, 6, 1)$
$20: P_{165} = (4, 3, 1, 1)$	$45: P_{502} = (5, 5, 6, 1)$
$21: P_{171} = (2, 4, 1, 1)$	$46: P_{531} = (2, 1, 7, 1)$
$22: P_{184} = (7, 5, 1, 1)$	$47: P_{539} = (2, 2, 7, 1)$
23: $P_{187} = (2, 6, 1, 1)$	$48: P_{569} = (0, 6, 7, 1)$
$24: P_{197} = (4,7,1,1)$	

Line Intersection Graph

Neighbor sets in the line intersection graph: The surface has 49 points:

The points on the surface are:

$0: P_1 = (0, 1, 0, 0)$	17: $P_{139} = (1, 0, 1, 1)$	$34: P_{369} = (0, 5, 4, 1)$
$1: P_3 = (0,0,0,1)$	18: $P_{146} = (0, 1, 1, 1)$	$35: P_{392} = (7,7,4,1)$
$2: P_4 = (1, 1, 1, 1)$	19: $P_{160} = (7, 2, 1, 1)$	$36: P_{395} = (2, 0, 5, 1)$
$3: P_{13} = (2,0,1,0)$	$20: P_{165} = (4, 3, 1, 1)$	$37: P_{404} = (3, 1, 5, 1)$
$4: P_{15} = (4,0,1,0)$	$21: P_{171} = (2, 4, 1, 1)$	$38: P_{409} = (0, 2, 5, 1)$
$5: P_{18} = (7,0,1,0)$	$22: P_{184} = (7, 5, 1, 1)$	$39: P_{420} = (3, 3, 5, 1)$
$6: P_{20} = (1, 1, 1, 0)$	$23: P_{187} = (2, 6, 1, 1)$	$40: P_{451} = (2, 7, 5, 1)$
$7: P_{30} = (3, 2, 1, 0)$	$24: P_{197} = (4,7,1,1)$	$41: P_{461} = (4, 0, 6, 1)$
$8: P_{48} = (5, 4, 1, 0)$	$25: P_{213} = (4, 1, 2, 1)$	$42: P_{470} = (5, 1, 6, 1)$
$9: P_{73} = (6,7,1,0)$	$26: P_{225} = (0, 3, 2, 1)$	43: $P_{477} = (4, 2, 6, 1)$
$10: P_{75} = (1, 0, 0, 1)$	$27: P_{237} = (4, 4, 2, 1)$	$44: P_{489} = (0, 4, 6, 1)$
$11: P_{85} = (3, 1, 0, 1)$	$28: P_{272} = (7, 0, 3, 1)$	$45: P_{502} = (5, 5, 6, 1)$
$12: P_{87} = (5, 1, 0, 1)$	$29: P_{279} = (6, 1, 3, 1)$	$46: P_{531} = (2, 1, 7, 1)$
$13: P_{88} = (6, 1, 0, 1)$	$30: P_{304} = (7, 4, 3, 1)$	$47: P_{539} = (2, 2, 7, 1)$
$14: P_{97} = (7, 2, 0, 1)$	$31: P_{319} = (6, 6, 3, 1)$	$48: P_{569} = (0, 6, 7, 1)$
$15: P_{108} = (2, 4, 0, 1)$	$32: P_{321} = (0,7,3,1)$	
$16: P_{134} = (4, 7, 0, 1)$	$33: P_{344} = (7, 1, 4, 1)$	