

Rank-76 over GF(2)

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The equation

The equation of the surface is :

$$X_1^3 + X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_2 = 0$$

(0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)

The point rank of the equation over GF(2) is 76

General information

Number of lines	1
Number of points	7
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	3
Number of points off lines	4
Number of Hesse planes	0
Number of axes	0
Type of points on lines	3
Type of lines on points	$1^3, 0^4$

Singular Points

The surface has 1 singular points:

$$0 : P_8 = \mathbf{P}(1, 1, 1, 0) = \mathbf{P}(1, 1, 1, 0)$$

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_1 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_1 = \mathbf{Pl}(1, 0, 1, 0, 0, 0)_3$$

Rank of lines: (1)

Rank of points on Klein quadric: (3)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 3 single points:

The single points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$ lies on line ℓ_0

1 : $P_7 = (0, 1, 1, 0)$ lies on line ℓ_0

2 : $P_8 = (1, 1, 1, 0)$ lies on line ℓ_0

The single points on the surface are:

Points on surface but on no line

The surface has 4 points not on any line:

The points on the surface but not on lines are:

0 : $P_5 = (1, 1, 0, 0)$

1 : $P_6 = (1, 0, 1, 0)$

2 : $P_{10} = (0, 1, 0, 1)$

3 : $P_{12} = (0, 0, 1, 1)$

Line Intersection Graph

$$\begin{array}{c|c} & 0 \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line
in point

The surface has 7 points:

The points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$

1 : $P_5 = (1, 1, 0, 0)$

2 : $P_6 = (1, 0, 1, 0)$

3 : $P_7 = (0, 1, 1, 0)$

4 : $P_8 = (1, 1, 1, 0)$

5 : $P_{10} = (0, 1, 0, 1)$

6 : $P_{12} = (0, 0, 1, 1)$