

# Rank-65561 over GF(32)

January 15, 2021

## The equation

The equation of the surface is :

$$X_1^3 + X_2^3 + X_0^2 X_1 + X_0 X_1 X_2 = 0$$

( 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0 )

The point rank of the equation over GF(32) is 1109428293

## General information

|                            |                |
|----------------------------|----------------|
| Number of lines            | 44             |
| Number of points           | 1409           |
| Number of singular points  | 1              |
| Number of Eckardt points   | 0              |
| Number of double points    | 0              |
| Number of single points    | 1408           |
| Number of points off lines | 0              |
| Number of Hesse planes     | 0              |
| Number of axes             | 0              |
| Type of points on lines    | $33^{44}$      |
| Type of lines on points    | $44, 1^{1408}$ |

## Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

## The 44 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned} \ell_0 &= \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{1056} = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{1056} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)_{1089} \\ \ell_1 &= \left[ \begin{array}{cccc} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{2113} = \left[ \begin{array}{cccc} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]_{2113} = \mathbf{Pl}(0, 0, 0, 0, 1, 1, 0)_{3105} \end{aligned}$$

$$\begin{aligned}
\ell_2 &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082433} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1082433} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{97} \\
\ell_3 &= \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{35937} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{35937} = \mathbf{Pl}(0, 1, 0, 1, 1, 0)_{3137} \\
\ell_4 &= \begin{bmatrix} 1 & \eta^{12} & \eta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{252622} = \begin{bmatrix} 1 & 14 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{252622} = \mathbf{Pl}(0, 7, 0, 14, 1, 0)_{3962} \\
\ell_5 &= \begin{bmatrix} 1 & \eta^{24} & \eta^{23} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{540126} = \begin{bmatrix} 1 & 30 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{540126} = \mathbf{Pl}(0, 15, 0, 30, 1, 0)_{4978} \\
\ell_6 &= \begin{bmatrix} 1 & \eta^9 & \eta^{22} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{738842} = \begin{bmatrix} 1 & 26 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{738842} = \mathbf{Pl}(0, 21, 0, 26, 1, 0)_{4732} \\
\ell_7 &= \begin{bmatrix} 1 & \eta^2 & \eta^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1053828} = \begin{bmatrix} 1 & 4 & 31 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1053828} = \mathbf{Pl}(0, 31, 0, 4, 1, 0)_{3356} \\
\ell_8 &= \begin{bmatrix} 1 & \eta^{24} & \eta^{22} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{743070} = \begin{bmatrix} 1 & 30 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{743070} = \mathbf{Pl}(0, 21, 0, 30, 1, 0)_{4984} \\
\ell_9 &= \begin{bmatrix} 1 & \eta^{17} & \eta^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1069683} = \begin{bmatrix} 1 & 19 & 31 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1069683} = \mathbf{Pl}(0, 31, 0, 19, 1, 0)_{4301} \\
\ell_{10} &= \begin{bmatrix} 1 & \eta^4 & \eta^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{626800} = \begin{bmatrix} 1 & 16 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{626800} = \mathbf{Pl}(0, 18, 0, 16, 1, 0)_{4099} \\
\ell_{11} &= \begin{bmatrix} 1 & \eta^{18} & \eta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{951299} = \begin{bmatrix} 1 & 3 & 28 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{951299} = \mathbf{Pl}(0, 28, 0, 3, 1, 0)_{3290} \\
\ell_{12} &= \begin{bmatrix} 1 & \eta^2 & \eta^{22} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{715588} = \begin{bmatrix} 1 & 4 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{715588} = \mathbf{Pl}(0, 21, 0, 4, 1, 0)_{3346} \\
\ell_{13} &= \begin{bmatrix} 1 & \eta^{26} & \eta^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1073911} = \begin{bmatrix} 1 & 23 & 31 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1073911} = \mathbf{Pl}(0, 31, 0, 23, 1, 0)_{4553} \\
\ell_{14} &= \begin{bmatrix} 1 & \eta & \eta^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{273762} = \begin{bmatrix} 1 & 2 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{273762} = \mathbf{Pl}(0, 8, 0, 2, 1, 0)_{3207} \\
\ell_{15} &= \begin{bmatrix} 1 & \eta^3 & \eta^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{178632} = \begin{bmatrix} 1 & 8 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{178632} = \mathbf{Pl}(0, 5, 0, 8, 1, 0)_{3582} \\
\ell_{16} &= \begin{bmatrix} 1 & \eta^6 & \eta^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{586634} = \begin{bmatrix} 1 & 10 & 17 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{586634} = \mathbf{Pl}(0, 17, 0, 10, 1, 0)_{3720} \\
\ell_{17} &= \begin{bmatrix} 1 & \eta^2 & \eta^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{343524} = \begin{bmatrix} 1 & 4 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{343524} = \mathbf{Pl}(0, 10, 0, 4, 1, 0)_{3335} \\
\ell_{18} &= \begin{bmatrix} 1 & \eta^{16} & \eta^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{401659} = \begin{bmatrix} 1 & 27 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{401659} = \mathbf{Pl}(0, 11, 0, 27, 1, 0)_{4785} \\
\ell_{19} &= \begin{bmatrix} 1 & \eta^{10} & \eta^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{830801} = \begin{bmatrix} 1 & 17 & 24 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{830801} = \mathbf{Pl}(0, 24, 0, 17, 1, 0)_{4168} \\
\ell_{20} &= \begin{bmatrix} 1 & \eta^6 & \eta^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{316042} = \begin{bmatrix} 1 & 10 & 9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{316042} = \mathbf{Pl}(0, 9, 0, 10, 1, 0)_{3712} \\
\ell_{21} &= \begin{bmatrix} 1 & \eta^3 & \eta^{26} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{787464} = \begin{bmatrix} 1 & 8 & 23 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{787464} = \mathbf{Pl}(0, 23, 0, 8, 1, 0)_{3600} \\
\ell_{22} &= \begin{bmatrix} 1 & \eta^4 & \eta^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{491504} = \begin{bmatrix} 1 & 16 & 14 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{491504} = \mathbf{Pl}(0, 14, 0, 16, 1, 0)_{4095}
\end{aligned}$$

$$\begin{aligned}
\ell_{23} &= \begin{bmatrix} 1 & \eta^{12} & \eta^{20} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{421742} = \begin{bmatrix} 1 & 14 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{421742} = \mathbf{Pl}(0, 12, 0, 14, 1, 0)_{3967} \\
\ell_{24} &= \begin{bmatrix} 1 & \eta^3 & \eta^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{618344} = \begin{bmatrix} 1 & 8 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{618344} = \mathbf{Pl}(0, 18, 0, 8, 1, 0)_{3595} \\
\ell_{25} &= \begin{bmatrix} 1 & \eta^{17} & \eta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{968211} = \begin{bmatrix} 1 & 19 & 28 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{968211} = \mathbf{Pl}(0, 28, 0, 19, 1, 0)_{4298} \\
\ell_{26} &= \begin{bmatrix} 1 & \eta^8 & \eta^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{319213} = \begin{bmatrix} 1 & 13 & 9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{319213} = \mathbf{Pl}(0, 9, 0, 13, 1, 0)_{3901} \\
\ell_{27} &= \begin{bmatrix} 1 & \eta^5 & \eta^{26} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{784293} = \begin{bmatrix} 1 & 5 & 23 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{784293} = \mathbf{Pl}(0, 23, 0, 5, 1, 0)_{3411} \\
\ell_{28} &= \begin{bmatrix} 1 & \eta^{17} & \eta^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{122611} = \begin{bmatrix} 1 & 19 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{122611} = \mathbf{Pl}(0, 3, 0, 19, 1, 0)_{4273} \\
\ell_{29} &= \begin{bmatrix} 1 & \eta^{16} & \eta^{17} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{672251} = \begin{bmatrix} 1 & 27 & 19 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{672251} = \mathbf{Pl}(0, 19, 0, 27, 1, 0)_{4793} \\
\ell_{30} &= \begin{bmatrix} 1 & \eta^{21} & \eta^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{635256} = \begin{bmatrix} 1 & 24 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{635256} = \mathbf{Pl}(0, 18, 0, 24, 1, 0)_{4603} \\
\ell_{31} &= \begin{bmatrix} 1 & \eta^4 & \eta^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{965040} = \begin{bmatrix} 1 & 16 & 28 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{965040} = \mathbf{Pl}(0, 28, 0, 16, 1, 0)_{4109} \\
\ell_{32} &= \begin{bmatrix} 1 & \eta^{22} & \eta^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{395317} = \begin{bmatrix} 1 & 21 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{395317} = \mathbf{Pl}(0, 11, 0, 21, 1, 0)_{4407} \\
\ell_{33} &= \begin{bmatrix} 1 & \eta^{16} & \eta^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{841371} = \begin{bmatrix} 1 & 27 & 24 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{841371} = \mathbf{Pl}(0, 24, 0, 27, 1, 0)_{4798} \\
\ell_{34} &= \begin{bmatrix} 1 & \eta & \eta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{239938} = \begin{bmatrix} 1 & 2 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{239938} = \mathbf{Pl}(0, 7, 0, 2, 1, 0)_{3206} \\
\ell_{35} &= \begin{bmatrix} 1 & \eta^{13} & \eta^{23} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{538012} = \begin{bmatrix} 1 & 28 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{538012} = \mathbf{Pl}(0, 15, 0, 28, 1, 0)_{4852} \\
\ell_{36} &= \begin{bmatrix} 1 & \eta^{20} & \eta^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{250508} = \begin{bmatrix} 1 & 12 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{250508} = \mathbf{Pl}(0, 7, 0, 12, 1, 0)_{3836} \\
\ell_{37} &= \begin{bmatrix} 1 & \eta & \eta^{23} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{510530} = \begin{bmatrix} 1 & 2 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{510530} = \mathbf{Pl}(0, 15, 0, 2, 1, 0)_{3214} \\
\ell_{38} &= \begin{bmatrix} 1 & \eta^{12} & \eta^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{387918} = \begin{bmatrix} 1 & 14 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{387918} = \mathbf{Pl}(0, 11, 0, 14, 1, 0)_{3966} \\
\ell_{39} &= \begin{bmatrix} 1 & \eta^6 & \eta^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{823402} = \begin{bmatrix} 1 & 10 & 24 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{823402} = \mathbf{Pl}(0, 24, 0, 10, 1, 0)_{3727} \\
\ell_{40} &= \begin{bmatrix} 1 & \eta^{11} & \eta^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{312871} = \begin{bmatrix} 1 & 7 & 9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{312871} = \mathbf{Pl}(0, 9, 0, 7, 1, 0)_{3523} \\
\ell_{41} &= \begin{bmatrix} 1 & \eta^8 & \eta^{26} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{792749} = \begin{bmatrix} 1 & 13 & 23 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{792749} = \mathbf{Pl}(0, 23, 0, 13, 1, 0)_{3915} \\
\ell_{42} &= \begin{bmatrix} 1 & \eta^8 & \eta^{24} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1029517} = \begin{bmatrix} 1 & 13 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1029517} = \mathbf{Pl}(0, 30, 0, 13, 1, 0)_{3922} \\
\ell_{43} &= \begin{bmatrix} 1 & \eta^{24} & \eta^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{912190} = \begin{bmatrix} 1 & 30 & 26 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{912190} = \mathbf{Pl}(0, 26, 0, 30, 1, 0)_{4989}
\end{aligned}$$

Rank of lines: ( 1056, 2113, 1082433, 35937, 252622, 540126, 738842, 1053828, 743070, 1069683, 626800, 951299, 715588, 1073911, 273762, 178632, 586634, 343524, 401659, 830801, 316042, 787464, 491504, 421742, 618344, 968211, 319213, 784293, 122611, 672251, 635256, 965040, 395317, 841371, 239938, 538012, 250508, 510530, 387918, 823402, 312871, 792749, 1029517, 912190 )

Rank of points on Klein quadric: ( 1089, 3105, 97, 3137, 3962, 4978, 4732, 3356, 4984, 4301, 4099, 3290, 3346, 4553, 3207, 3582, 3720, 3335, 4785, 4168, 3712, 3600, 4095, 3967, 3595, 4298, 3901, 3411, 4273, 4793, 4603, 4109, 4407, 4798, 3206, 4852, 3836, 3214, 3966, 3727, 3523, 3915, 3922, 4989 )

### **Eckardt Points**

The surface has 0 Eckardt points:

### **Double Points**

The surface has 0 Double points:

The double points on the surface are:

### **Single Points**

The surface has 1408 single points:

Too many to print.

### **Points on surface but on no line**

The surface has 0 points not on any line:

The points on the surface but not on lines are:

## Line Intersection Graph

[illegible]

Neighbor sets in the line intersection graph:

Line 0 intersects

[illegible]

[illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible]

|      |          |          |          |          |          |          |          |          |          |          |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |             |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |              |     |
|------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----|
| Line | $\ell_0$ | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_4$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_8$ | $\ell_9$ | $\ell_{10}$ | $\ell_{11}$ | $\ell_{12}$ | $\ell_{13}$ | $\ell_{15}$ | $\ell_{16}$ | $\ell_{17}$ | $\ell_{18}$ | $\ell_{19}$ | $\ell_{20}$ | $\ell_{21}$ | $\ell_{22}$ | $\ell_{23}$ | $\ell_{24}$ | $\ell_{25}$ | $\ell_{26}$ | $\ell_{27}$ | $\ell_{28}$ | $\ell_{29}$ | $\ell_{30}$ | $\ell_{31}$ | $\ell_{32}$ | $\ell_{33}$ | $\ell_{34}$ | $\ell_{35}$ | $\ell_{36}$ | $\ell_{37}$ | $\ell_{38}$ | $\ell_{39}$ | $\ell_{40}$ | $\ell_{41}$ | $\ell_{42}$ | $\ell_{43}$ | $\ell_{44}$ | $\ell_{45}$ | $\ell_{46}$ | $\ell_{47}$ | $\ell_{48}$ | $\ell_{49}$ | $\ell_{50}$ | $\ell_{51}$ | $\ell_{52}$ | $\ell_{53}$ | $\ell_{54}$ | $\ell_{55}$ | $\ell_{56}$ | $\ell_{57}$ | $\ell_{58}$ | $\ell_{59}$ | $\ell_{60}$ | $\ell_{61}$ | $\ell_{62}$ | $\ell_{63}$ | $\ell_{64}$ | $\ell_{65}$ | $\ell_{66}$ | $\ell_{67}$ | $\ell_{68}$ | $\ell_{69}$ | $\ell_{70}$ | $\ell_{71}$ | $\ell_{72}$ | $\ell_{73}$ | $\ell_{74}$ | $\ell_{75}$ | $\ell_{76}$ | $\ell_{77}$ | $\ell_{78}$ | $\ell_{79}$ | $\ell_{80}$ | $\ell_{81}$ | $\ell_{82}$ | $\ell_{83}$ | $\ell_{84}$ | $\ell_{85}$ | $\ell_{86}$ | $\ell_{87}$ | $\ell_{88}$ | $\ell_{89}$ | $\ell_{90}$ | $\ell_{91}$ | $\ell_{92}$ | $\ell_{93}$ | $\ell_{94}$ | $\ell_{95}$ | $\ell_{96}$ | $\ell_{97}$ | $\ell_{98}$ | $\ell_{99}$ | $\ell_{100}$ | $\ell_{101}$ | $\ell_{102}$ | $\ell_{103}$ | $\ell_{104}$ | $\ell_{105}$ | $\ell_{106}$ | $\ell_{107}$ | $\ell_{108}$ | $\ell_{109}$ | $\ell_{110}$ | $\ell_{111}$ | $\ell_{112}$ | $\ell_{113}$ | $\ell_{114}$ | $\ell_{115}$ | $\ell_{116}$ | $\ell_{117}$ | $\ell_{118}$ | $\ell_{119}$ | $\ell_{120}$ | $\ell_{121}$ | $\ell_{122}$ | $\ell_{123}$ | $\ell_{124}$ | $\ell_{125}$ | $\ell_{126}$ | $\ell_{127}$ | $\ell_{128}$ | $\ell_{129}$ | $\ell_{130}$ | $\ell_{131}$ | $\ell_{132}$ | $\ell_{133}$ | $\ell_{134}$ | $\ell_{135}$ | $\ell_{136}$ | $\ell_{137}$ | $\ell_{138}$ | $\ell_{139}$ | $\ell_{140}$ | $\ell_{141}$ | $\ell_{142}$ | $\ell_{143}$ | $\ell_{144}$ | $\ell_{145}$ | $\ell_{146}$ | $\ell_{147}$ | $\ell_{148}$ | $\ell_{149}$ | $\ell_{150}$ | $\ell_{151}$ | $\ell_{152}$ | $\ell_{153}$ | $\ell_{154}$ | $\ell_{155}$ | $\ell_{156}$ | $\ell_{157}$ | $\ell_{158}$ | $\ell_{159}$ | $\ell_{160}$ | $\ell_{161}$ | $\ell_{162}$ | $\ell_{163}$ | $\ell_{164}$ | $\ell_{165}$ | $\ell_{166}$ | $\ell_{167}$ | $\ell_{168}$ | $\ell_{169}$ | $\ell_{170}$ | $\ell_{171}$ | $\ell_{172}$ | $\ell_{173}$ | $\ell_{174}$ | $\ell_{175}$ | $\ell_{176}$ | $\ell_{177}$ | $\ell_{178}$ | $\ell_{179}$ | $\ell_{180}$ | $\ell_{181}$ | $\ell_{182}$ | $\ell_{183}$ | $\ell_{184}$ | $\ell_{185}$ | $\ell_{186}$ | $\ell_{187}$ | $\ell_{188}$ | $\ell_{189}$ | $\ell_{190}$ | $\ell_{191}$ | $\ell_{192}$ | $\ell_{193}$ | $\ell_{194}$ | $\ell_{195}$ | $\ell_{196}$ | $\ell_{197}$ | $\ell_{198}$ | $\ell_{199}$ | $\ell_{200}$ | $\ell_{201}$ | $\ell_{202}$ | $\ell_{203}$ | $\ell_{204}$ | $\ell_{205}$ | $\ell_{206}$ | $\ell_{207}$ | $\ell_{208}$ | $\ell_{209}$ | $\ell_{210}$ | $\ell_{211}$ | $\ell_{212}$ | $\ell_{213}$ | $\ell_{214}$ | $\ell_{215}$ | $\ell_{216}$ | $\ell_{217}$ | $\ell_{218}$ | $\ell_{219}$ | $\ell_{220}$ | $\ell_{221}$ | $\ell_{222}$ | $\ell_{223}$ | $\ell_{224}$ | $\ell_{225}$ | $\ell_{226}$ | $\ell_{227}$ | $\ell_{228}$ | $\ell_{229}$ | $\ell_{230}$ | $\ell_{231}$ | $\ell_{232}$ | $\ell_{233}$ | $\ell_{234}$ | $\ell_{235}$ | $\ell_{236}$ | $\ell_{237}$ | $\ell_{238}$ | $\ell_{239}$ | $\ell_{240}$ | $\ell_{241}$ | $\ell_{242}$ | $\ell_{243}$ | $\ell_{244}$ | $\ell_{245}$ | $\ell_{246}$ | $\ell_{247}$ | $\ell_{248}$ | $\ell_{249}$ | $\ell_{250}$ | $\ell_{251}$ | $\ell_{252}$ | $\ell_{253}$ | $\ell_{254}$ | $\ell_{255}$ | $\ell_{256}$ | $\ell_{257}$ | $\ell_{258}$ | $\ell_{259}$ | $\ell_{260}$ | $\ell_{261}$ | $\ell_{262}$ | $\ell_{263}$ | $\ell_{264}$ | $\ell_{265}$ | $\ell_{266}$ | $\ell_{267}$ | $\ell_{268}$ | $\ell_{269}$ | $\ell_{270}$ | $\ell_{271}$ | $\ell_{272}$ | $\ell_{273}$ | $\ell_{274}$ | $\ell_{275}$ | $\ell_{276}$ | $\ell_{277}$ | $\ell_{278}$ | $\ell_{279}$ | $\ell_{280}$ | $\ell_{281}$ | $\ell_{282}$ | $\ell_{283}$ | $\ell_{284}$ | $\ell_{285}$ | $\ell_{286}$ | $\ell_{287}$ | $\ell_{288}$ | $\ell_{289}$ | $\ell_{290}$ | $\ell_{291}$ | $\ell_{292}$ | $\ell_{293}$ | $\ell_{294}$ | $\ell_{295}$ | $\ell_{296}$ | $\ell_{297}$ | $\ell_{298}$ | $\ell_{299}$ | $\$ |
|------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----|

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Line 40 intersects

|          |          |          |          |          |          |          |          |          |          |          |             |             |             |             |             |             |             |             |             |             |             |             |             |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Line     | $\ell_0$ | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_4$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_8$ | $\ell_9$ | $\ell_{10}$ | $\ell_{11}$ | $\ell_{12}$ | $\ell_{13}$ | $\ell_{14}$ | $\ell_{15}$ | $\ell_{16}$ | $\ell_{17}$ | $\ell_{18}$ | $\ell_{19}$ | $\ell_{20}$ | $\ell_{21}$ | $\ell_{22}$ |
| in point | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       |

Line 41 intersects

|          |          |          |          |          |          |          |          |          |          |          |             |             |             |             |             |             |             |             |             |             |             |             |             |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Line     | $\ell_0$ | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_4$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_8$ | $\ell_9$ | $\ell_{10}$ | $\ell_{11}$ | $\ell_{12}$ | $\ell_{13}$ | $\ell_{14}$ | $\ell_{15}$ | $\ell_{16}$ | $\ell_{17}$ | $\ell_{18}$ | $\ell_{19}$ | $\ell_{20}$ | $\ell_{21}$ | $\ell_{22}$ |
| in point | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       |

Line 42 intersects

|          |          |          |          |          |          |          |          |          |          |          |             |             |             |             |             |             |             |             |             |             |             |             |             |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Line     | $\ell_0$ | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_4$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_8$ | $\ell_9$ | $\ell_{10}$ | $\ell_{11}$ | $\ell_{12}$ | $\ell_{13}$ | $\ell_{14}$ | $\ell_{15}$ | $\ell_{16}$ | $\ell_{17}$ | $\ell_{18}$ | $\ell_{19}$ | $\ell_{20}$ | $\ell_{21}$ | $\ell_{22}$ |
| in point | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       |

Line 43 intersects

|          |          |          |          |          |          |          |          |          |          |          |             |             |             |             |             |             |             |             |             |             |             |             |             |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Line     | $\ell_0$ | $\ell_1$ | $\ell_2$ | $\ell_3$ | $\ell_4$ | $\ell_5$ | $\ell_6$ | $\ell_7$ | $\ell_8$ | $\ell_9$ | $\ell_{10}$ | $\ell_{11}$ | $\ell_{12}$ | $\ell_{13}$ | $\ell_{14}$ | $\ell_{15}$ | $\ell_{16}$ | $\ell_{17}$ | $\ell_{18}$ | $\ell_{19}$ | $\ell_{20}$ | $\ell_{21}$ | $\ell_{22}$ |
| in point | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$    | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       | $P_3$       |

The surface has 1409 points:

Too many to print.