

Rank-74264 over GF(32)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^3 + X_2^3 + X_0^2 X_1 + X_1^2 X_3 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

(1, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(32) is 1109428262

General information

Number of lines	1
Number of points	1089
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	33
Number of points off lines	1056
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33
Type of lines on points	$1^{33}, 0^{1056}$

Singular Points

The surface has 0 singular points:

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{1057} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{1057} = \mathbf{Pl}(1, 0, 0, 0, 0, 1)_{34850}$$

Rank of lines: (1057)

Rank of points on Klein quadric: (34850)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 33 single points:

The single points on the surface are:

- | | |
|--|---|
| 0 : $P_1 = (0, 1, 0, 0)$ lies on line ℓ_0 | 17 : $P_{548} = (1, 16, 1, 0)$ lies on line ℓ_0 |
| 1 : $P_{36} = (1, 0, 1, 0)$ lies on line ℓ_0 | 18 : $P_{580} = (1, 17, 1, 0)$ lies on line ℓ_0 |
| 2 : $P_{68} = (1, 1, 1, 0)$ lies on line ℓ_0 | 19 : $P_{612} = (1, 18, 1, 0)$ lies on line ℓ_0 |
| 3 : $P_{100} = (1, 2, 1, 0)$ lies on line ℓ_0 | 20 : $P_{644} = (1, 19, 1, 0)$ lies on line ℓ_0 |
| 4 : $P_{132} = (1, 3, 1, 0)$ lies on line ℓ_0 | 21 : $P_{676} = (1, 20, 1, 0)$ lies on line ℓ_0 |
| 5 : $P_{164} = (1, 4, 1, 0)$ lies on line ℓ_0 | 22 : $P_{708} = (1, 21, 1, 0)$ lies on line ℓ_0 |
| 6 : $P_{196} = (1, 5, 1, 0)$ lies on line ℓ_0 | 23 : $P_{740} = (1, 22, 1, 0)$ lies on line ℓ_0 |
| 7 : $P_{228} = (1, 6, 1, 0)$ lies on line ℓ_0 | 24 : $P_{772} = (1, 23, 1, 0)$ lies on line ℓ_0 |
| 8 : $P_{260} = (1, 7, 1, 0)$ lies on line ℓ_0 | 25 : $P_{804} = (1, 24, 1, 0)$ lies on line ℓ_0 |
| 9 : $P_{292} = (1, 8, 1, 0)$ lies on line ℓ_0 | 26 : $P_{836} = (1, 25, 1, 0)$ lies on line ℓ_0 |
| 10 : $P_{324} = (1, 9, 1, 0)$ lies on line ℓ_0 | 27 : $P_{868} = (1, 26, 1, 0)$ lies on line ℓ_0 |
| 11 : $P_{356} = (1, 10, 1, 0)$ lies on line ℓ_0 | 28 : $P_{900} = (1, 27, 1, 0)$ lies on line ℓ_0 |
| 12 : $P_{388} = (1, 11, 1, 0)$ lies on line ℓ_0 | 29 : $P_{932} = (1, 28, 1, 0)$ lies on line ℓ_0 |
| 13 : $P_{420} = (1, 12, 1, 0)$ lies on line ℓ_0 | 30 : $P_{964} = (1, 29, 1, 0)$ lies on line ℓ_0 |
| 14 : $P_{452} = (1, 13, 1, 0)$ lies on line ℓ_0 | 31 : $P_{996} = (1, 30, 1, 0)$ lies on line ℓ_0 |
| 15 : $P_{484} = (1, 14, 1, 0)$ lies on line ℓ_0 | 32 : $P_{1028} = (1, 31, 1, 0)$ lies on line ℓ_0 |
| 16 : $P_{516} = (1, 15, 1, 0)$ lies on line ℓ_0 | |

The single points on the surface are:

Points on surface but on no line

The surface has 1056 points not on any line:

Too many to print.

Line Intersection Graph

$$\begin{array}{c|c} 0 & \\ \hline 0 & 0 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line
in point

The surface has 1089 points:

Too many to print.