Rank-265 over GF(8)

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The equation

The equation of the surface is :

$$X_0^3 + X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_2 + X_0^2 X_3 + X_0 X_1^2 = 0$$

(1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)The point rank of the equation over GF(8) is 599191

General information

Number of lines	1
Number of points	57
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	9
Number of points off lines	48
Number of Hesse planes	0
Number of axes	0
Type of points on lines	9
Type of lines on points	$1^9, 0^{48}$

Singular Points

The surface has 0 singular points:

The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4673} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{4673} = \mathbf{Pl}(0, 0, 0, 1, 0, 1)_{769}$$

Rank of lines: (4673)

Rank of points on Klein quadric: (769)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 9 single points: The single points on the surface are:

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\begin{array}{lll} 0: \ P_1 = (0,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 1: \ P_{138} = (0,0,1,1) \ \mbox{lies on line} \ \ell_0 \\ 2: \ P_{146} = (0,1,1,1) \ \mbox{lies on line} \ \ell_0 \\ 3: \ P_{153} = (0,2,1,1) \ \mbox{lies on line} \ \ell_0 \\ 4: \ P_{161} = (0,3,1,1) \ \mbox{lies on line} \ \ell_0 \end{array}
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The single points on the surface are:

Points on surface but on no line

The surface has 48 points not on any line: The points on the surface but not on lines are:

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0: P_{13} = (2,0,1,0)
                                                                  22: P_{136} = (6,7,0,1)
1: P_{15} = (4, 0, 1, 0)
                                                                  23: P_{137} = (7,7,0,1)
2: P_{18} = (7, 0, 1, 0)
                                                                  24: P_{203} = (2,0,2,1)
3: P_{22} = (3, 1, 1, 0)
                                                                  25: P_{218} = (1, 2, 2, 1)
4: P_{24} = (5, 1, 1, 0)
                                                                  26: P_{219} = (2, 2, 2, 1)
5: P_{25} = (6, 1, 1, 0)
                                                                  27: P_{226} = (1, 3, 2, 1)
6: P_{29} = (2, 2, 1, 0)
                                                                  28: P_{266} = (1,0,3,1)
7: P_{30} = (3, 2, 1, 0)
                                                                  29: P_{274} = (1, 1, 3, 1)
                                                                  30: P_{276} = (3, 1, 3, 1)
8: P_{47} = (4, 4, 1, 0)
9: P_{48} = (5, 4, 1, 0)
                                                                  31: P_{284} = (3, 2, 3, 1)
10: P_{73} = (6, 7, 1, 0)
                                                                  32: P_{333} = (4,0,4,1)
11: P_{74} = (7, 7, 1, 0)
                                                                  33: P_{362} = (1, 4, 4, 1)
                                                                  34: P_{365} = (4, 4, 4, 1)
12: P_{76} = (2, 0, 0, 1)
13: P_{78} = (4, 0, 0, 1)
                                                                  35: P_{370} = (1, 5, 4, 1)
14: P_{81} = (7, 0, 0, 1)
                                                                  36: P_{394} = (1,0,5,1)
15: P_{85} = (3, 1, 0, 1)
                                                                  37: P_{402} = (1, 1, 5, 1)
16: P_{87} = (5, 1, 0, 1)
                                                                  38: P_{406} = (5, 1, 5, 1)
17: P_{88} = (6, 1, 0, 1)
                                                                  39: P_{430} = (5, 4, 5, 1)
18: P_{92} = (2, 2, 0, 1)
                                                                  40: P_{458} = (1,0,6,1)
19: P_{93} = (3, 2, 0, 1)
                                                                  41: P_{466} = (1, 1, 6, 1)
20: P_{110} = (4, 4, 0, 1)
                                                                  42: P_{471} = (6, 1, 6, 1)
21: P_{111} = (5, 4, 0, 1)
                                                                  43: P_{519} = (6,7,6,1)
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\begin{array}{l} 44:\ P_{528}=(7,0,7,1)\\ 45:\ P_{570}=(1,6,7,1)\\ 46:\ P_{578}=(1,7,7,1) \end{array}
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Line Intersection Graph

 $\frac{0}{0 \mid 0}$

Neighbor sets in the line intersection graph: Line 0 intersects

Line in point

The surface has 57 points: The points on the surface are:

$\begin{array}{l} 0: \ P_1 = (0,1,0,0) \\ 1: \ P_{13} = (2,0,1,0) \\ 2: \ P_{15} = (4,0,1,0) \\ 3: \ P_{18} = (7,0,1,0) \\ 4: \ P_{22} = (3,1,1,0) \\ 5: \ P_{24} = (5,1,1,0) \\ 6: \ P_{25} = (6,1,1,0) \\ 7: \ P_{29} = (2,2,1,0) \\ 8: \ P_{30} = (3,2,1,0) \\ 9: \ P_{47} = (4,4,1,0) \\ 10: \ P_{48} = (5,4,1,0) \\ 11: \ P_{73} = (6,7,1,0) \\ 12: \ P_{74} = (7,7,1,0) \\ 13: \ P_{76} = (2,0,0,1) \end{array}$	$20: P_{93} = (3, 2, 0, 1)$ $21: P_{110} = (4, 4, 0, 1)$ $22: P_{111} = (5, 4, 0, 1)$ $23: P_{136} = (6, 7, 0, 1)$ $24: P_{137} = (7, 7, 0, 1)$ $25: P_{138} = (0, 0, 1, 1)$ $26: P_{146} = (0, 1, 1, 1)$ $27: P_{153} = (0, 2, 1, 1)$ $28: P_{161} = (0, 3, 1, 1)$ $29: P_{169} = (0, 4, 1, 1)$ $30: P_{177} = (0, 5, 1, 1)$ $31: P_{185} = (0, 6, 1, 1)$ $32: P_{193} = (0, 7, 1, 1)$ $33: P_{203} = (2, 0, 2, 1)$	$40: P_{284} = (3, 2, 3, 1)$ $41: P_{333} = (4, 0, 4, 1)$ $42: P_{362} = (1, 4, 4, 1)$ $43: P_{365} = (4, 4, 4, 1)$ $44: P_{370} = (1, 5, 4, 1)$ $45: P_{394} = (1, 0, 5, 1)$ $46: P_{402} = (1, 1, 5, 1)$ $47: P_{406} = (5, 1, 5, 1)$ $48: P_{430} = (5, 4, 5, 1)$ $49: P_{458} = (1, 0, 6, 1)$ $50: P_{466} = (1, 1, 6, 1)$ $51: P_{471} = (6, 1, 6, 1)$ $52: P_{519} = (6, 7, 6, 1)$ $53: P_{528} = (7, 0, 7, 1)$
$12: P_{74} = (7, 7, 1, 0)$	$32: P_{193} = (0, 7, 1, 1)$	$52: P_{519} = (6, 7, 6, 1)$