# Rank-362 over GF(32)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_3 + X_1^2 X_2 = 0$$

(1, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)The point rank of the equation over GF(32) is -2111764402

# General information

Number of lines	15
Number of points	1185
Number of singular points	0
Number of Eckardt points	15
Number of double points	0
Number of single points	450
Number of points off lines	720
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$33^{15}$
Type of lines on points	$3^{15}, 1^{450}, 0^{720}$

# Singular Points

The surface has 0 singular points:

## The 15 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & \eta^{26} & \eta^{14} \\ 0 & 1 & \eta^9 & \eta^{22} \end{bmatrix}_{1005905} = \begin{bmatrix} 1 & 0 & 23 & 29 \\ 0 & 1 & 26 & 21 \end{bmatrix}_{1005905} = \mathbf{Pl}(28, 3, 14, 6, 11, 1)_{412240}$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & \eta^8 & \eta^{17} \\ 0 & 1 & \eta^{16} & \eta^{20} \end{bmatrix}_{656808} = \begin{bmatrix} 1 & 0 & 13 & 19 \\ 0 & 1 & 27 & 12 \end{bmatrix}_{656808} = \mathbf{Pl}(26, 21, 21, 26, 14, 1)_{516801}$$

$$\begin{split} \ell_2 &= \begin{bmatrix} 1 & 0 & \eta^{21} & \eta^{28} \\ 0 & 1 & \eta^{18} & \eta^{13} \end{bmatrix}_{770395} = \begin{bmatrix} 1 & 0 & 24 & 22 \\ 0 & 1 & 3 & 28 \end{bmatrix}_{770395} = \mathbf{Pl}(23,5,30,20,15,1)_{558183} \\ \ell_3 &= \begin{bmatrix} 1 & 0 & \eta^{16} & \eta^3 \\ 0 & 1 & \eta & \eta^9 \end{bmatrix}_{299965} = \begin{bmatrix} 1 & 0 & 27 & 8 \\ 0 & 1 & 2 & 26 \end{bmatrix}_{299965} = \mathbf{Pl}(3,28,28,3,30,1)_{1047436} \\ \ell_4 &= \begin{bmatrix} 1 & 0 & \eta^{10} & \eta^8 \\ 0 & 1 & \eta^{21} & \eta^{26} \end{bmatrix}_{458441} = \begin{bmatrix} 1 & 0 & 17 & 13 \\ 0 & 1 & 24 & 23 \end{bmatrix}_{458441} = \mathbf{Pl}(24,17,4,9,27,1)_{927332} \\ \ell_5 &= \begin{bmatrix} 1 & 0 & \eta^2 & \eta^{12} \\ 0 & 1 & \eta^4 & \eta^5 \end{bmatrix}_{477940} = \begin{bmatrix} 1 & 0 & 4 & 14 \\ 0 & 1 & 16 & 5 \end{bmatrix}_{477940} = \mathbf{Pl}(17,24,24,17,8,1)_{323817} \\ \ell_6 &= \begin{bmatrix} 1 & 0 & \eta^{22} & \eta^{19} \\ 0 & 1 & \eta^{10} & \eta^{21} \end{bmatrix}_{225926} = \begin{bmatrix} 1 & 0 & 21 & 6 \\ 0 & 1 & 17 & 24 \end{bmatrix}_{225926} = \mathbf{Pl}(7,12,8,22,18,1)_{636070} \\ \ell_7 &= \begin{bmatrix} 1 & 0 & \eta^{11} & \eta^{25} \\ 0 & 1 & \eta^5 & \eta^{26} \end{bmatrix}_{853740} = \begin{bmatrix} 1 & 0 & 21 & 6 \\ 0 & 1 & 5 & 23 \end{bmatrix}_{853740} = \mathbf{Pl}(24,17,19,29,31,1)_{1072226} \\ \ell_8 &= \begin{bmatrix} 1 & 0 & \eta^{6} \\ 0 & 1 & \eta^2 & \eta^{18} \end{bmatrix}_{340454} = \begin{bmatrix} 1 & 0 & 12 & 27 \\ 0 & 1 & 5 & 23 \end{bmatrix}_{340454} = \mathbf{Pl}(5,23,23,5,19,1)_{682537} \\ \ell_9 &= \begin{bmatrix} 1 & 0 & \eta^{20} & \eta^{16} \\ 0 & 1 & \eta^{11} & \eta^{21} \end{bmatrix}_{926707} = \begin{bmatrix} 1 & 0 & 12 & 27 \\ 0 & 1 & 7 & 24 \end{bmatrix}_{926707} = \mathbf{Pl}(7,12,16,11,2,1)_{119734} \\ \ell_{10} &= \begin{bmatrix} 1 & 0 & \eta^{5} & \eta^{4} \\ 0 & 1 & \eta^{26} & \eta^{13} \end{bmatrix}_{547388} = \begin{bmatrix} 1 & 0 & 5 & 16 \\ 0 & 1 & 23 & 28 \end{bmatrix}_{547388} = \mathbf{Pl}(28,3,27,31,16,1)_{588010} \\ \ell_{11} &= \begin{bmatrix} 1 & 0 & \eta^5 & \eta^4 \\ 0 & 1 & \eta^8 & \eta^{10} \end{bmatrix}_{1032189} = \begin{bmatrix} 1 & 0 & 16 & 30 \\ 0 & 1 & 13 & 17 \end{bmatrix}_{1032189} = \mathbf{Pl}(21,26,10,25,9,1)_{342979} \\ \ell_{14} &= \begin{bmatrix} 1 & 0 & \eta^3 & \eta^7 \\ 0 & 1 & \eta^{20} & \eta^{11} \end{bmatrix}_{706312} = \begin{bmatrix} 1 & 0 & 28 & 20 \\ 0 & 1 & 21 & 27 \end{bmatrix}_{706312} = \mathbf{Pl}(21,26,13,15,4,1)_{182089} \end{aligned}$$

Rank of lines: (1005905, 656808, 770395, 299965, 458441, 477940, 225926, 853740, 340454, 926707, 139167, 547388, 1032189, 706312, 95375)

Rank of points on Klein quadric: (412240, 516801, 558183, 1047436, 927332, 323817, 636070, 1072226, 682537, 119734, 588010, 466671, 372761, 342979, 182089)

#### **Eckardt Points**

The surface has 15 Eckardt points:

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The surface has 15 Eckardt points:

0: P_{4054} = \mathbf{P}(\eta^{22}, \eta^{14}, \eta, 1) = \mathbf{P}(21, 29, 2, 1),

1: P_{5885} = \mathbf{P}(\eta^{13}, \eta^{28}, \eta^2, 1) = \mathbf{P}(28, 22, 4, 1),

2: P_{7612} = \mathbf{P}(\eta^{16}, \eta^{20}, \eta^{19}, 1) = \mathbf{P}(27, 12, 6, 1),

3: P_{10643} = \mathbf{P}(\eta^{30}, \eta^{27}, \eta^{29}, 1) = \mathbf{P}(18, 11, 9, 1),

4: P_{12810} = \mathbf{P}(\eta^{29}, \eta^{23}, \eta^{27}, 1) = \mathbf{P}(9, 15, 11, 1),

5: P_{14585} = \mathbf{P}(\eta^{21}, \eta^{19}, \eta^8, 1) = \mathbf{P}(24, 6, 13, 1),

6: P_{17420} = \mathbf{P}(\eta^{27}, \eta^{15}, \eta^{23}, 1) = \mathbf{P}(11, 31, 15, 1),

7: P_{18264} = \mathbf{P}(\eta^{26}, \eta^{25}, \eta^4, 1) = \mathbf{P}(23, 25, 16, 1),

8: P_{12020} = \mathbf{P}(\eta^{15}, \eta^{29}, \eta^{30}, 1) = \mathbf{P}(31, 9, 18, 1)
  8: P_{19808} = \mathbf{P}(\eta^{15}, \eta^{29}, \eta^{30}, 1) = \mathbf{P}(31, 9, 18, 1),
  9: P_{22371} = \mathbf{P}(\eta, \eta^9, \eta^7, 1) = \mathbf{P}(2, 26, 20, 1),

10: P_{23761} = \mathbf{P}(\eta^4, \eta^5, \eta^{28}, 1) = \mathbf{P}(16, 5, 22, 1),

11: P_{27214} = \mathbf{P}(\eta^8, \eta^{10}, \eta^{25}, 1) = \mathbf{P}(13, 17, 25, 1),
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12: P_{29352} = \mathbf{P}(\eta^{11}, \eta^{7}, \eta^{16}, 1) = \mathbf{P}(7, 20, 27, 1),

13: P_{30853} = \mathbf{P}(\eta^{2}, \eta^{18}, \eta^{14}, 1) = \mathbf{P}(4, 3, 29, 1),

14: P_{33392} = \mathbf{P}(\eta^{23}, \eta^{30}, \eta^{15}, 1) = \mathbf{P}(15, 18, 31, 1).
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#### **Double Points**

The surface has 0 Double points: The double points on the surface are:

#### Single Points

The surface has 450 single points: The single points on the surface are:

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0: P_{125} = (26, 2, 1, 0) lies on line \ell_0
                                                                      36: P_{2548} = (19, 14, 1, 1) lies on line \ell_{11}
1: P_{155} = (24, 3, 1, 0) lies on line \ell_1
                                                                      37: P_{2699} = (10, 19, 1, 1) lies on line \ell_9
2: P_{166} = (3, 4, 1, 0) lies on line \ell_2
                                                                       38: P_{2701} = (12, 19, 1, 1) lies on line \ell_2
3: P_{202} = (7, 5, 1, 0) lies on line \ell_3
                                                                      39: P_{2752} = (31, 20, 1, 1) lies on line \ell_8
4: P_{237} = (10, 6, 1, 0) lies on line \ell_4
                                                                       40: P_{2794} = (9, 22, 1, 1) lies on line \ell_{12}
5 : P_{447} = (28, 12, 1, 0) lies on line \ell_5
                                                                      41: P_{2892} = (11, 25, 1, 1) lies on line \ell_1
6: P_{468} = (17, 13, 1, 0) lies on line \ell_6
                                                                       42: P_{3027} = (18, 29, 1, 1) lies on line \ell_5
7: P_{552} = (5, 16, 1, 0) lies on line \ell_7
                                                                       43: P_{3049} = (8, 30, 1, 1) lies on line \ell_4
                                                                       44: P_{3058} = (17, 30, 1, 1) lies on line \ell_0
8: P_{600} = (21, 17, 1, 0) lies on line \ell_8
9: P_{689} = (14, 20, 1, 0) lies on line \ell_9
                                                                      45: P_{3116} = (11, 0, 2, 1) lies on line \ell_{11}
10: P_{758} = (19, 22, 1, 0) lies on line \ell_{10}
                                                                       46: P_{3174} = (5, 2, 2, 1) lies on line \ell_8
11: P_{843} = (8, 25, 1, 0) lies on line \ell_{11}
                                                                       47: P_{3314} = (17, 6, 2, 1) lies on line \ell_{13}
12: P_{890} = (23, 26, 1, 0) lies on line \ell_{12}
                                                                      48: P_{3399} = (6, 9, 2, 1) lies on line \ell_3
13: P_{911} = (12, 27, 1, 0) lies on line \ell_{13}
                                                                      49: P_{3412} = (19, 9, 2, 1) lies on line \ell_5
14: P_{993} = (30, 29, 1, 0) lies on line \ell_{14}
                                                                      50: P_{3434} = (9, 10, 2, 1) lies on line \ell_{14}
15: P_{1162} = (8, 3, 0, 1) lies on line \ell_3
                                                                      51: P_{3449} = (24, 10, 2, 1) lies on line \ell_9
16: P_{1228} = (10, 5, 0, 1) lies on line \ell_8
                                                                      52: P_{3767} = (22, 20, 2, 1) lies on line \ell_4
                                                                      53: P_{3791} = (14, 21, 2, 1) lies on line \ell_{10}
17: P_{1286} = (4,7,0,1) lies on line \ell_9
18: P_{1300} = (18, 7, 0, 1) lies on line \ell_6
                                                                      54: P_{3899} = (26, 24, 2, 1) lies on line \ell_0
                                                                      55: P_{4007} = (6, 28, 2, 1) lies on line \ell_1
19: P_{1472} = (30, 12, 0, 1) lies on line \ell_{12}
20: P_{1616} = (14, 17, 0, 1) lies on line \ell_5
                                                                      56: P_{4106} = (9, 31, 2, 1) lies on line \ell_2
21: P_{1739} = (9, 21, 0, 1) lies on line \ell_{13}
                                                                      57: P_{4254} = (29, 3, 3, 1) lies on line \ell_{10}
22: P_{1746} = (16, 21, 0, 1) lies on line \ell_{14}
                                                                      58: P_{4304} = (15, 5, 3, 1) lies on line \ell_5
23: P_{1809} = (15, 23, 0, 1) lies on line \ell_2
                                                                      59: P_{4355} = (2,7,3,1) lies on line \ell_{12}
24: P_{1821} = (27, 23, 0, 1) lies on line \ell_{11}
                                                                      60: P_{4514} = (1, 12, 3, 1) lies on line \ell_3
25: P_{1828} = (2, 24, 0, 1) lies on line \ell_4
                                                                      61: P_{4561} = (16, 13, 3, 1) lies on line \ell_7
26: P_{1857} = (31, 24, 0, 1) lies on line \ell_7
                                                                      62: P_{4645} = (4, 16, 3, 1) lies on line \ell_6
27: P_{1909} = (19, 26, 0, 1) lies on line \ell_1
                                                                      63: P_{4733} = (28, 18, 3, 1) lies on line \ell_4
28: P_{1965} = (11, 28, 0, 1) lies on line \ell_0
                                                                      64: P_{4753} = (16, 19, 3, 1) lies on line \ell_8
29: P_{1967} = (13, 28, 0, 1) lies on line \ell_{10}
                                                                      65: P_{4888} = (23, 23, 3, 1) lies on line \ell_{14}
30: P_{2288} = (15, 6, 1, 1) lies on line \ell_3
                                                                      66: P_{4932} = (3, 25, 3, 1) lies on line \ell_{11}
31: P_{2351} = (14, 8, 1, 1) lies on line \ell_{14}
                                                                      67: P_{4961} = (0, 26, 3, 1) lies on line \ell_0
32: P_{2363} = (26, 8, 1, 1) lies on line \ell_7
                                                                      68: P_{5003} = (10, 27, 3, 1) lies on line \ell_2
33: P_{2404} = (3, 10, 1, 1) lies on line \ell_6
                                                                      69: P_{5086} = (29, 29, 3, 1) lies on line \ell_{13}
34: P_{2431} = (30, 10, 1, 1) lies on line \ell_{10}
                                                                      70: P_{5111} = (22, 30, 3, 1) lies on line \ell_9
35: P_{2534} = (5, 14, 1, 1) lies on line \ell_{13}
                                                                      71: P_{5151} = (30, 31, 3, 1) lies on line \ell_1
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72: P_{5168} = (15, 0, 4, 1) lies on line \ell_4
                                                                      126: P_{9263} = (14, 0, 8, 1) lies on line \ell_6
73: P_{5298} = (17, 4, 4, 1) lies on line \ell_5
                                                                      127: P_{9298} = (17, 1, 8, 1) lies on line \ell_{11}
74: P_{5380} = (3,7,4,1) lies on line \ell_2
                                                                      128: P_{9326} = (13, 2, 8, 1) lies on line \ell_1
75: P_{5513} = (8, 11, 4, 1) lies on line \ell_{12}
                                                                      129: P_{9336} = (23, 2, 8, 1) lies on line \ell_{12}
76: P_{5525} = (20, 11, 4, 1) lies on line \ell_8
                                                                      130: P_{9468} = (27, 6, 8, 1) lies on line \ell_{14}
77: P_{5608} = (7, 14, 4, 1) lies on line \ell_{14}
                                                                      131: P_{9638} = (5, 12, 8, 1) lies on line \ell_0
78: P_{5612} = (11, 14, 4, 1) lies on line \ell_{10}
                                                                      132: P_{9651} = (18, 12, 8, 1) lies on line \ell_7
79: P_{5740} = (11, 18, 4, 1) lies on line \ell_7
                                                                      133: P_{9689} = (24, 13, 8, 1) lies on line \ell_4
80: P_{5805} = (12, 20, 4, 1) lies on line \ell_0
                                                                      134 : P_{9718} = (21, 14, 8, 1) lies on line \ell_3
81: P_{5909} = (20, 23, 4, 1) lies on line \ell_3
                                                                      135: P_{9848} = (23, 18, 8, 1) lies on line \ell_2
82: P_{6079} = (30, 28, 4, 1) lies on line \ell_{11}
                                                                      136: P_{9863} = (6, 19, 8, 1) lies on line \ell_{13}
                                                                      137: P_{9980} = (27, 22, 8, 1) lies on line \ell_9
83: P_{6106} = (25, 29, 4, 1) lies on line \ell_9
84: P_{6255} = (14, 2, 5, 1) lies on line \ell_7
                                                                      138: P_{10068} = (19, 25, 8, 1) lies on line \ell_8
85: P_{6273} = (0, 3, 5, 1) lies on line \ell_2
                                                                      139: P_{10178} = (1, 29, 8, 1) lies on line \ell_{10}
                                                                      140: P_{10230} = (21, 30, 8, 1) lies on line \ell_5
86: P_{6359} = (22, 5, 5, 1) lies on line \ell_{11}
87: P_{6374} = (5, 6, 5, 1) lies on line \ell_4
                                                                      141: P_{10326} = (21, 1, 9, 1) lies on line \ell_1
88: P_{6446} = (13, 8, 5, 1) lies on line \ell_5
                                                                      142: P_{10358} = (21, 2, 9, 1) lies on line \ell_9
89: P_{6488} = (23, 9, 5, 1) lies on line \ell_9
                                                                      143: P_{10535} = (6, 8, 9, 1) lies on line \ell_8
90: P_{6609} = (16, 13, 5, 1) lies on line \ell_{13}
                                                                      144: P_{10539} = (10, 8, 9, 1) lies on line \ell_{13}
91: P_{6752} = (31, 17, 5, 1) lies on line \ell_{12}
                                                                      145: P_{10720} = (31, 13, 9, 1) lies on line \ell_6
92: P_{6772} = (19, 18, 5, 1) lies on line \ell_3
                                                                      146: P_{10752} = (31, 14, 9, 1) lies on line \ell_0
93: P_{6810} = (25, 19, 5, 1) lies on line \ell_{14}
                                                                      147: P_{10858} = (9, 18, 9, 1) lies on line \ell_5
                                                                      148: P_{10997} = (20, 22, 9, 1) lies on line \ell_2
94: P_{6853} = (4, 21, 5, 1) lies on line \ell_1
95 : P_{6903} = (22, 22, 5, 1) lies on line \ell_0
                                                                      149 : P_{11041} = (0, 24, 9, 1) lies on line \ell_{12}
96: P_{6969} = (24, 24, 5, 1) lies on line \ell_{10}
                                                                      150: P_{11066} = (25, 24, 9, 1) lies on line \ell_{11}
97: P_{7010} = (1, 26, 5, 1) lies on line \ell_8
                                                                      151: P_{11142} = (5, 27, 9, 1) lies on line \ell_{14}
98: P_{7054} = (13, 27, 5, 1) lies on line \ell_6
                                                                      152: P_{11192} = (23, 28, 9, 1) lies on line \ell_7
99: P_{7365} = (4, 5, 6, 1) lies on line \ell_{13}
                                                                      153: P_{11327} = (30, 0, 10, 1) lies on line \ell_{13}
100: P_{7433} = (8, 7, 6, 1) lies on line \ell_{10}
                                                                      154: P_{11341} = (12, 1, 10, 1) lies on line \ell_4
101: P_{7567} = (14, 11, 6, 1) lies on line \ell_{11}
                                                                      155: P_{11449} = (24, 4, 10, 1) lies on line \ell_1
102: P_{7686} = (5, 15, 6, 1) lies on line \ell_2
                                                                      156: P_{11452} = (27, 4, 10, 1) lies on line \ell_3
103: P_{7718} = (5, 16, 6, 1) lies on line \ell_9
                                                                      157: P_{11497} = (8, 6, 10, 1) lies on line \ell_5
104: P_{7722} = (9, 16, 6, 1) lies on line \ell_1
                                                                      158: P_{11573} = (20, 8, 10, 1) lies on line \ell_0
105: P_{7742} = (29, 16, 6, 1) lies on line \ell_0
                                                                      159: P_{11609} = (24, 9, 10, 1) lies on line \ell_7
106: P_{7775} = (30, 17, 6, 1) lies on line \ell_{14}
                                                                      160: P_{11933} = (28, 19, 10, 1) lies on line \ell_{12}
                                                                      161: P_{11939} = (2, 20, 10, 1) lies on line \ell_{10}
107: P_{7938} = (1, 23, 6, 1) lies on line \ell_7
108: P_{8036} = (3, 26, 6, 1) lies on line \ell_{12}
                                                                      162: P_{12002} = (1, 22, 10, 1) lies on line \ell_{11}
109: P_{8109} = (12, 28, 6, 1) lies on line \ell_5
                                                                      163: P_{12099} = (2, 25, 10, 1) lies on line \ell_{14}
110: P_{8155} = (26, 29, 6, 1) lies on line \ell_3
                                                                      164: P_{12138} = (9, 26, 10, 1) lies on line \ell_6
111: P_{8245} = (20, 0, 7, 1) lies on line \ell_{12}
                                                                      165: P_{12146} = (17, 26, 10, 1) lies on line \ell_2
                                                                      166 : P_{12168} = (7, 27, 10, 1) lies on line \ell_9
112: P_{8267} = (10, 1, 7, 1) lies on line \ell_6
113: P_{8364} = (11, 4, 7, 1) lies on line \ell_9
                                                                      167: P_{12285} = (28, 30, 10, 1) lies on line \ell_8
114: P_{8453} = (4,7,7,1) lies on line \ell_7
                                                                      168: P_{12381} = (28, 1, 11, 1) lies on line \ell_3
115: P_{8562} = (17, 10, 7, 1) lies on line \ell_4
                                                                      169: P_{12402} = (17, 2, 11, 1) lies on line \ell_{10}
116: P_{8583} = (6, 11, 7, 1) lies on line \ell_2
                                                                      170: P_{12477} = (28, 4, 11, 1) lies on line \ell_{14}
                                                                      171 : P_{12545} = (0, 7, 11, 1) lies on line \ell_1
117: P_{8609} = (0, 12, 7, 1) lies on line \ell_{14}
118: P_{8753} = (16, 16, 7, 1) lies on line \ell_5
                                                                      172: P_{12551} = (6, 7, 11, 1) lies on line \ell_4
119: P_{8796} = (27, 17, 7, 1) lies on line \ell_{10}
                                                                      173: P_{12620} = (11, 9, 11, 1) lies on line \ell_{12}
120: P_{8807} = (6, 18, 7, 1) lies on line \ell_{11}
                                                                      174: P_{12655} = (14, 10, 11, 1) lies on line \ell_0
121: P_{8808} = (7, 18, 7, 1) lies on line \ell_0
                                                                      175: P_{12661} = (20, 10, 11, 1) lies on line \ell_5
                                                                      176: P_{13081} = (24, 23, 11, 1) lies on line \ell_6
122: P_{8850} = (17, 19, 7, 1) lies on line \ell_1
123: P_{9022} = (29, 24, 7, 1) lies on line \ell_3
                                                                      177: P_{13150} = (29, 25, 11, 1) lies on line \ell_7
                                                                      178 : P_{13203} = (18, 27, 11, 1) lies on line \ell_{13}
124: P_{9167} = (14, 29, 7, 1) lies on line \ell_8
125: P_{9193} = (8, 30, 7, 1) lies on line \ell_{13}
                                                                      179: P_{13299} = (18, 30, 11, 1) lies on line \ell_2
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180: P_{13436} = (27, 2, 12, 1) lies on line \ell_2
                                                                     234 : P_{17472} = (31, 0, 16, 1) lies on line \ell_9
181 : P_{13475} = (2, 4, 12, 1) lies on line \ell_0
                                                                     235: P_{17744} = (15, 9, 16, 1) lies on line \ell_6
182: P_{13506} = (1, 5, 12, 1) lies on line \ell_{12}
                                                                     236: P_{17931} = (10, 15, 16, 1) lies on line \ell_1
183: P_{13543} = (6, 6, 12, 1) lies on line \ell_7
                                                                     237: P_{17950} = (29, 15, 16, 1) lies on line \ell_5
184 : P_{13685} = (20, 10, 12, 1) lies on line \ell_{11}
                                                                     238: P_{17965} = (12, 16, 16, 1) lies on line \ell_{12}
185 : P_{13707} = (10, 11, 12, 1) lies on line \ell_5
                                                                     239: P_{18118} = (5, 21, 16, 1) lies on line \ell_7
186 : P_{13735} = (6, 12, 12, 1) lies on line \ell_9
                                                                     240: P_{18151} = (6, 22, 16, 1) lies on line \ell_{14}
187: P_{13795} = (2, 14, 12, 1) lies on line \ell_1
                                                                     241: P_{18196} = (19, 23, 16, 1) lies on line \ell_4
188: P_{13832} = (7, 15, 12, 1) lies on line \ell_{10}
                                                                     242: P_{18238} = (29, 24, 16, 1) lies on line \ell_8
189: P_{13876} = (19, 16, 12, 1) lies on line \ell_{13}
                                                                     243: P_{18395} = (26, 29, 16, 1) lies on line \ell_2
190: P_{13889} = (0, 17, 12, 1) lies on line \ell_6
                                                                     244: P_{18416} = (15, 30, 16, 1) lies on line \ell_{11}
191: P_{14038} = (21, 21, 12, 1) lies on line \ell_4
                                                                     245: P_{18422} = (21, 30, 16, 1) lies on line \ell_{10}
192: P_{14094} = (13, 23, 12, 1) lies on line \ell_8
                                                                     246: P_{18556} = (27, 2, 17, 1) lies on line \ell_{13}
193: P_{14186} = (9, 26, 12, 1) lies on line \ell_3
                                                                     247: P_{18562} = (1, 3, 17, 1) lies on line \ell_5
194 : P_{14285} = (12, 29, 12, 1) lies on line \ell_{14}
                                                                     248: P_{18623} = (30, 4, 17, 1) lies on line \ell_6
195: P_{14387} = (18, 0, 13, 1) lies on line \ell_{14}
                                                                     249: P_{18625} = (0, 5, 17, 1) lies on line \ell_7
                                                                     250: P_{18696} = (7, 7, 17, 1) lies on line \ell_{11}
196: P_{14615} = (22, 7, 13, 1) lies on line \ell_5
197: P_{14752} = (31, 11, 13, 1) lies on line \ell_{13}
                                                                     251: P_{18727} = (6, 8, 17, 1) lies on line \ell_{10}
198: P_{14811} = (26, 13, 13, 1) lies on line \ell_1
                                                                     252: P_{18761} = (8, 9, 17, 1) lies on line \ell_8
199: P_{15005} = (28, 19, 13, 1) lies on line \ell_{11}
                                                                     253: P_{18812} = (27, 10, 17, 1) lies on line \ell_{12}
200: P_{15008} = (31, 19, 13, 1) lies on line \ell_4
                                                                     254: P_{18841} = (24, 11, 17, 1) lies on line \ell_{14}
201 : P_{15076} = (3, 22, 13, 1) lies on line \ell_7
                                                                     255: P_{18867} = (18, 12, 17, 1) lies on line \ell_1
202: P_{15145} = (8, 24, 13, 1) lies on line \ell_9
                                                                     256: P_{19034} = (25, 17, 17, 1) lies on line \ell_4
203 : P_{15189} = (20, 25, 13, 1) lies on line \ell_{10}
                                                                     257: P_{19122} = (17, 20, 17, 1) lies on line \ell_9
204: P_{15282} = (17, 28, 13, 1) lies on line \ell_6
                                                                     258: P_{19290} = (25, 25, 17, 1) lies on line \ell_2
205 : P_{15375} = (14, 31, 13, 1) lies on line \ell_3
                                                                     259: P_{19342} = (13, 27, 17, 1) lies on line \ell_0
206: P_{15383} = (22, 31, 13, 1) lies on line \ell_{12}
                                                                     260: P_{19377} = (16, 28, 17, 1) lies on line \ell_3
207: P_{15412} = (19, 0, 14, 1) lies on line \ell_0
                                                                     261: P_{19528} = (7, 1, 18, 1) lies on line \ell_{12}
208: P_{15451} = (26, 1, 14, 1) lies on line \ell_9
                                                                     262: P_{19824} = (15, 10, 18, 1) lies on line \ell_{13}
209: P_{15478} = (21, 2, 14, 1) lies on line \ell_{14}
                                                                     263: P_{19908} = (3, 13, 18, 1) lies on line \ell_9
210: P_{15500} = (11, 3, 14, 1) lies on line \ell_{13}
                                                                     264: P_{20016} = (15, 16, 18, 1) lies on line \ell_7
211: P_{15501} = (12, 3, 14, 1) lies on line \ell_7
                                                                     265: P_{20105} = (8, 19, 18, 1) lies on line \ell_6
212: P_{15589} = (4, 6, 14, 1) lies on line \ell_{10}
                                                                     266: P_{20122} = (25, 19, 18, 1) lies on line \ell_3
213: P_{15672} = (23, 8, 14, 1) lies on line \ell_1
                                                                     267: P_{20189} = (28, 21, 18, 1) lies on line \ell_2
214: P_{15742} = (29, 10, 14, 1) lies on line \ell_2
                                                                     268: P_{20225} = (0, 23, 18, 1) lies on line \ell_5
215: P_{15752} = (7, 11, 14, 1) lies on line \ell_6
                                                                     269: P_{20247} = (22, 23, 18, 1) lies on line \ell_{10}
216: P_{15907} = (2, 16, 14, 1) lies on line \ell_8
                                                                     270: P_{20360} = (7, 27, 18, 1) lies on line \ell_4
217: P_{15912} = (7, 16, 14, 1) lies on line \ell_3
                                                                     271 : P_{20423} = (6, 29, 18, 1) lies on line \ell_0
218: P_{16024} = (23, 19, 14, 1) lies on line \ell_5
                                                                     272: P_{20499} = (18, 31, 18, 1) lies on line \ell_8
219: P_{16043} = (10, 20, 14, 1) lies on line \ell_{12}
                                                                     273: P_{20523} = (10, 0, 19, 1) lies on line \ell_7
220: P_{16194} = (1, 25, 14, 1) lies on line \ell_4
                                                                     274: P_{20550} = (5, 1, 19, 1) lies on line \ell_{10}
221: P_{16325} = (4, 29, 14, 1) lies on line \ell_{11}
                                                                     275: P_{20840} = (7, 10, 19, 1) lies on line \ell_1
222: P_{16472} = (23, 1, 15, 1) lies on line \ell_8
                                                                     276: P_{20968} = (7, 14, 19, 1) lies on line \ell_8
223: P_{16490} = (9, 2, 15, 1) lies on line \ell_0
                                                                     277: P_{21048} = (23, 16, 19, 1) lies on line \ell_{11}
224: P_{16557} = (12, 4, 15, 1) lies on line \ell_{11}
                                                                     278: P_{21060} = (3, 17, 19, 1) lies on line \ell_{13}
225: P_{16631} = (22, 6, 15, 1) lies on line \ell_6
                                                                     279: P_{21088} = (31, 17, 19, 1) lies on line \ell_2
226: P_{16784} = (15, 11, 15, 1) lies on line \ell_1
                                                                     280: P_{21154} = (1, 20, 19, 1) lies on line \ell_{14}
227: P_{16894} = (29, 14, 15, 1) lies on line \ell_{12}
                                                                     281: P_{21247} = (30, 22, 19, 1) lies on line \ell_3
228: P_{16895} = (30, 14, 15, 1) lies on line \ell_2
                                                                     282: P_{21326} = (13, 25, 19, 1) lies on line \ell_9
229: P_{16952} = (23, 16, 15, 1) lies on line \ell_{10}
                                                                     283: P_{21393} = (16, 27, 19, 1) lies on line \ell_{12}
230 : P_{17034} = (9, 19, 15, 1) lies on line \ell_7
                                                                     284: P_{21405} = (28, 27, 19, 1) lies on line \ell_5
231: P_{17089} = (0, 21, 15, 1) lies on line \ell_3
                                                                     285: P_{21454} = (13, 29, 19, 1) lies on line \ell_4
                                                                     286 : P_{21498} = (25, 30, 19, 1) lies on line \ell_6
232 : P_{17109} = (20, 21, 15, 1) lies on line \ell_9
233: P_{17192} = (7, 24, 15, 1) lies on line \ell_{13}
                                                                     287: P_{21533} = (28, 31, 19, 1) lies on line \ell_0
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342: P_{25639} = (6, 0, 24, 1) lies on line \ell_5
288: P_{21638} = (5, 3, 20, 1) lies on line \ell_1
289 : P_{21940} = (19, 12, 20, 1) lies on line \ell_{10}
                                                                     343: P_{25673} = (8, 1, 24, 1) lies on line \ell_7
290: P_{21964} = (11, 13, 20, 1) lies on line \ell_3
                                                                     344: P_{25706} = (9, 2, 24, 1) lies on line \ell_4
291 : P_{21970} = (17, 13, 20, 1) lies on line \ell_{14}
                                                                     345: P_{25765} = (4, 4, 24, 1) lies on line \ell_8
292: P_{21975} = (22, 13, 20, 1) lies on line \ell_2
                                                                     346: P_{25806} = (13, 5, 24, 1) lies on line \ell_{14}
293: P_{22047} = (30, 15, 20, 1) lies on line \ell_4
                                                                     347: P_{25894} = (5, 8, 24, 1) lies on line \ell_{11}
294 : P_{22097} = (16, 17, 20, 1) lies on line \ell_0
                                                                     348: P_{25946} = (25, 9, 24, 1) lies on line \ell_0
295: P_{22219} = (10, 21, 20, 1) lies on line \ell_{11}
                                                                     349: P_{26100} = (19, 14, 24, 1) lies on line \ell_6
296: P_{22244} = (3, 22, 20, 1) lies on line \ell_8
                                                                     350: P_{26177} = (0, 17, 24, 1) lies on line \ell_9
297: P_{22299} = (26, 23, 20, 1) lies on line \ell_{12}
                                                                     351: P_{26283} = (10, 20, 24, 1) lies on line \ell_3
298: P_{22306} = (1, 24, 20, 1) lies on line \ell_6
                                                                     352: P_{26389} = (20, 23, 24, 1) lies on line \ell_1
299: P_{22546} = (17, 31, 20, 1) lies on line \ell_7
                                                                     353: P_{26403} = (2, 24, 24, 1) lies on line \ell_2
300: P_{22590} = (29, 0, 21, 1) lies on line \ell_1
                                                                     354: P_{26598} = (5, 30, 24, 1) lies on line \ell_{12}
301: P_{22607} = (14, 1, 21, 1) lies on line \ell_{13}
                                                                     355: P_{26649} = (24, 31, 24, 1) lies on line \ell_{13}
302: P_{22807} = (22, 7, 21, 1) lies on line \ell_8
                                                                     356: P_{26650} = (25, 31, 24, 1) lies on line \ell_{10}
303: P_{22829} = (12, 8, 21, 1) lies on line \ell_3
                                                                     357: P_{26755} = (2, 3, 25, 1) lies on line \ell_6
304: P_{22869} = (20, 9, 21, 1) lies on line \ell_4
                                                                     358: P_{26788} = (3, 4, 25, 1) lies on line \ell_4
305: P_{22870} = (21, 9, 21, 1) lies on line \ell_2
                                                                     359: P_{26803} = (18, 4, 25, 1) lies on line \ell_{12}
306: P_{22947} = (2, 12, 21, 1) lies on line \ell_{11}
                                                                     360: P_{26805} = (20, 4, 25, 1) lies on line \ell_{13}
307: P_{22990} = (13, 13, 21, 1) lies on line \ell_{12}
                                                                     361: P_{26831} = (14, 5, 25, 1) lies on line \ell_9
308: P_{23021} = (12, 14, 21, 1) lies on line \ell_9
                                                                     362: P_{26955} = (10, 9, 25, 1) lies on line \ell_{10}
309: P_{23061} = (20, 15, 21, 1) lies on line \ell_7
                                                                     363: P_{27012} = (3, 11, 25, 1) lies on line \ell_0
310: P_{23088} = (15, 16, 21, 1) lies on line \ell_{14}
                                                                     364: P_{27067} = (26, 12, 25, 1) lies on line \ell_5
311: P_{23179} = (10, 19, 21, 1) lies on line \ell_0
                                                                     365: P_{27309} = (12, 20, 25, 1) lies on line \ell_1
312: P_{23249} = (16, 21, 21, 1) lies on line \ell_6
                                                                     366: P_{27346} = (17, 21, 25, 1) lies on line \ell_8
313: P_{23295} = (30, 22, 21, 1) lies on line \ell_5
                                                                     367: P_{27444} = (19, 24, 25, 1) lies on line \ell_{14}
314: P_{23393} = (0, 26, 21, 1) lies on line \ell_{10}
                                                                     368: P_{27554} = (1, 28, 25, 1) lies on line \ell_2
315: P_{23655} = (6, 2, 22, 1) lies on line \ell_6
                                                                     369: P_{27788} = (11, 3, 26, 1) lies on line \ell_8
316: P_{23675} = (26, 2, 22, 1) lies on line \ell_{11}
                                                                     370: P_{27811} = (2, 4, 26, 1) lies on line \ell_7
317: P_{23680} = (31, 2, 22, 1) lies on line \ell_5
                                                                     371: P_{28065} = (0, 12, 26, 1) lies on line \ell_{13}
318: P_{23691} = (10, 3, 22, 1) lies on line \ell_4
                                                                     372: P_{28105} = (8, 13, 26, 1) lies on line \ell_0
319: P_{23794} = (17, 6, 22, 1) lies on line \ell_{12}
                                                                     373: P_{28158} = (29, 14, 26, 1) lies on line \ell_4
320: P_{23814} = (5, 7, 22, 1) lies on line \ell_3
                                                                     374: P_{28175} = (14, 15, 26, 1) lies on line \ell_{12}
321 : P_{23899} = (26, 9, 22, 1) lies on line \ell_{13}
                                                                     375 : P_{28197} = (4, 16, 26, 1) lies on line \ell_2
322: P_{24141} = (12, 17, 22, 1) lies on line \ell_8
                                                                     376: P_{28226} = (1, 17, 26, 1) lies on line \ell_1
323: P_{24169} = (8, 18, 22, 1) lies on line \ell_{14}
                                                                     377: P_{28341} = (20, 20, 26, 1) lies on line \ell_6
324: P_{24258} = (1, 21, 22, 1) lies on line \ell_0
                                                                     378: P_{28411} = (26, 22, 26, 1) lies on line \ell_{10}
325: P_{24351} = (30, 23, 22, 1) lies on line \ell_9
                                                                     379: P_{28476} = (27, 24, 26, 1) lies on line \ell_5
326: P_{24444} = (27, 26, 22, 1) lies on line \ell_7
                                                                     380: P_{28533} = (20, 26, 26, 1) lies on line \ell_{14}
327 : P_{24634} = (25, 0, 23, 1) lies on line \ell_8
                                                                     381: P_{28605} = (28, 28, 26, 1) lies on line \ell_9
328: P_{24660} = (19, 1, 23, 1) lies on line \ell_2
                                                                     382: P_{28645} = (4, 30, 26, 1) lies on line \ell_3
329: P_{24675} = (2, 2, 23, 1) lies on line \ell_3
                                                                     383: P_{28694} = (21, 31, 26, 1) lies on line \ell_{11}
330: P_{24721} = (16, 3, 23, 1) lies on line \ell_9
                                                                     384: P_{28714} = (9, 0, 27, 1) lies on line \ell_{10}
331: P_{24769} = (0, 5, 23, 1) lies on line \ell_4
                                                                     385: P_{28926} = (29, 6, 27, 1) lies on line \ell_{11}
                                                                     386: P_{28939} = (10, 7, 27, 1) lies on line \ell_{14}
332 : P_{24809} = (8, 6, 23, 1) lies on line \ell_1
333: P_{24959} = (30, 10, 23, 1) lies on line \ell_7
                                                                     387: P_{28979} = (18, 8, 27, 1) lies on line \ell_9
334 : P_{25060} = (3, 14, 23, 1) lies on line \ell_5
                                                                     388: P_{28984} = (23, 8, 27, 1) lies on line \ell_4
335: P_{25111} = (22, 15, 23, 1) lies on line \ell_{14}
                                                                     389: P_{29203} = (18, 15, 27, 1) lies on line \ell_0
336: P_{25112} = (23, 15, 23, 1) lies on line \ell_6
                                                                     390: P_{29306} = (25, 18, 27, 1) lies on line \ell_1
337: P_{25207} = (22, 18, 23, 1) lies on line \ell_{13}
                                                                     391: P_{29311} = (30, 18, 27, 1) lies on line \ell_8
338: P_{25220} = (3, 19, 23, 1) lies on line \ell_{10}
                                                                     392: P_{29402} = (25, 21, 27, 1) lies on line \ell_{12}
339: P_{25372} = (27, 23, 23, 1) lies on line \ell_0
                                                                     393: P_{29453} = (12, 23, 27, 1) lies on line \ell_{13}
340 : P_{25491} = (18, 27, 23, 1) lies on line \ell_{11}
                                                                     394 : P_{29510} = (5, 25, 27, 1) lies on line \ell_6
341: P_{25511} = (6, 28, 23, 1) lies on line \ell_{12}
                                                                     395: P_{29572} = (3, 27, 27, 1) lies on line \ell_3
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396: P_{29751} = (22, 0, 28, 1) lies on line \ell_3
                                                                     424: P_{31812} = (3, 1, 30, 1) lies on line \ell_{14}
397: P_{29791} = (30, 1, 28, 1) lies on line \ell_0
                                                                     425: P_{31933} = (28, 4, 30, 1) lies on line \ell_{10}
                                                                     426: P_{31952} = (15, 5, 30, 1) lies on line \ell_0
398: P_{29825} = (0, 3, 28, 1) lies on line \ell_{11}
399: P_{29999} = (14, 8, 28, 1) lies on line \ell_2
                                                                     427: P_{31963} = (26, 5, 30, 1) lies on line \ell_6
400: P_{30075} = (26, 10, 28, 1) lies on line \ell_8
                                                                     428: P_{31970} = (1, 6, 30, 1) lies on line \ell_9
401: P_{30109} = (28, 11, 28, 1) lies on line \ell_7
                                                                     429: P_{32057} = (24, 8, 30, 1) lies on line \ell_{12}
                                                                     430: P_{32121} = (24, 10, 30, 1) lies on line \ell_3
402: P_{30110} = (29, 11, 28, 1) lies on line \ell_9
403: P_{30176} = (31, 13, 28, 1) lies on line \ell_{10}
                                                                     431: P_{32197} = (4, 13, 30, 1) lies on line \ell_5
404: P_{30426} = (25, 21, 28, 1) lies on line \ell_5
                                                                     432: P_{32214} = (21, 13, 30, 1) lies on line \ell_8
405: P_{30548} = (19, 25, 28, 1) lies on line \ell_{12}
                                                                     433: P_{32247} = (22, 14, 30, 1) lies on line \ell_7
406: P_{30565} = (4, 26, 28, 1) lies on line \ell_4
                                                                     434: P_{32278} = (21, 15, 30, 1) lies on line \ell_{13}
407: P_{30620} = (27, 27, 28, 1) lies on line \ell_1
                                                                     435: P_{32433} = (16, 20, 30, 1) lies on line \ell_{11}
408: P_{30638} = (13, 28, 28, 1) lies on line \ell_{13}
                                                                     436: P_{32497} = (16, 22, 30, 1) lies on line \ell_4
                                                                     437: P_{32719} = (14, 29, 30, 1) lies on line \ell_1
409: P_{30715} = (26, 30, 28, 1) lies on line \ell_{14}
410: P_{30750} = (29, 31, 28, 1) lies on line \ell_6
                                                                     438 : P_{32857} = (24, 1, 31, 1) lies on line \ell_5
411: P_{30930} = (17, 5, 29, 1) lies on line \ell_3
                                                                     439: P_{32940} = (11, 4, 31, 1) lies on line \ell_2
412: P_{30978} = (1, 7, 29, 1) lies on line \ell_{13}
                                                                     440: P_{33046} = (21, 7, 31, 1) lies on line \ell_0
413 : P_{31150} = (13, 12, 29, 1) lies on line \ell_2
                                                                     441: P_{33068} = (11, 8, 31, 1) lies on line \ell_6
414: P_{31341} = (12, 18, 29, 1) lies on line \ell_6
                                                                     442: P_{33241} = (24, 13, 31, 1) lies on line \ell_{11}
                                                                     443 : P_{33312} = (31, 15, 31, 1) lies on line \ell_3
415: P_{31524} = (3, 24, 29, 1) lies on line \ell_1
416: P_{31558} = (5, 25, 29, 1) lies on line \ell_5
                                                                     444: P_{33339} = (26, 16, 31, 1) lies on line \ell_4
417: P_{31593} = (8, 26, 29, 1) lies on line \ell_{11}
                                                                     445: P_{33466} = (25, 20, 31, 1) lies on line \ell_{13}
418: P_{31629} = (12, 27, 29, 1) lies on line \ell_{10}
                                                                     446: P_{33697} = (0, 28, 31, 1) lies on line \ell_8
419: P_{31632} = (15, 27, 29, 1) lies on line \ell_8
                                                                     447: P_{33726} = (29, 28, 31, 1) lies on line \ell_{14}
420: P_{31642} = (25, 27, 29, 1) lies on line \ell_7
                                                                     448: P_{33780} = (19, 30, 31, 1) lies on line \ell_7
421: P_{31663} = (14, 28, 29, 1) lies on line \ell_4
                                                                     449: P_{33783} = (22, 30, 31, 1) lies on line \ell_1
422: P_{31764} = (19, 31, 29, 1) lies on line \ell_9
423: P_{31785} = (8, 0, 30, 1) lies on line \ell_2
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The single points on the surface are:

## Points on surface but on no line

The surface has 720 points not on any line: The points on the surface but not on lines are:

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16: P_{632} = (21, 18, 1, 0)
0: P_{36} = (1,0,1,0)
1: P_{112} = (13, 2, 1, 0)
                                                                  17: P_{652} = (9, 19, 1, 0)
2: P_{120} = (21, 2, 1, 0)
                                                                  18: P_{732} = (25, 21, 1, 0)
3: P_{190} = (27, 4, 1, 0)
                                                                  19: P_{791} = (20, 23, 1, 0)
                                                                  20: P_{832} = (29, 24, 1, 0)
4: P_{191} = (28, 4, 1, 0)
5: P_{281} = (22, 7, 1, 0)
                                                                  21: P_{906} = (7, 27, 1, 0)
6: P_{302} = (11, 8, 1, 0)
                                                                  22: P_{915} = (16, 27, 1, 0)
7: P_{351} = (28, 9, 1, 0)
                                                                  23: P_{937} = (6, 28, 1, 0)
8: P_{370} = (15, 10, 1, 0)
                                                                  24: P_{1013} = (18, 30, 1, 0)
9: P_{410} = (23, 11, 1, 0)
                                                                  25: P_{1034} = (7, 31, 1, 0)
10: P_{455} = (4, 13, 1, 0)
                                                                  26: P_{1090} = (0, 1, 0, 1)
11: P_{475} = (24, 13, 1, 0)
                                                                  27: P_{1127} = (5, 2, 0, 1)
12: P_{514} = (31, 14, 1, 0)
                                                                  28: P_{1177} = (23, 3, 0, 1)
13: P_{539} = (24, 15, 1, 0)
                                                                  29: P_{1183} = (29, 3, 0, 1)
14: P_{549} = (2, 16, 1, 0)
                                                                  30: P_{1203} = (17, 4, 0, 1)
15: P_{570} = (23, 16, 1, 0)
                                                                  31: P_{1240} = (22, 5, 0, 1)
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86: P_{3866} = (25, 23, 2, 1)
32: P_{1242} = (24, 5, 0, 1)
33: P_{1298} = (16, 7, 0, 1)
                                                                 87: P_{3906} = (1, 25, 2, 1)
                                                                 88: P_{3959} = (22, 26, 2, 1)
34: P_{1359} = (13, 9, 0, 1)
35: P_{1437} = (27, 11, 0, 1)
                                                                 89: P_{4067} = (2, 30, 2, 1)
36: P_{1448} = (6, 12, 0, 1)
                                                                 90: P_{4134} = (5, 0, 3, 1)
                                                                 91: P_{4180} = (19, 1, 3, 1)
37: P_{1463} = (21, 12, 0, 1)
38: P_{1500} = (26, 13, 0, 1)
                                                                 92: P_{4233} = (8, 3, 3, 1)
39: P_{1540} = (2, 15, 0, 1)
                                                                 93: P_{4248} = (23, 3, 3, 1)
40: P_{1582} = (12, 16, 0, 1)
                                                                 94: P_{4306} = (17, 5, 3, 1)
41: P_{1609} = (7, 17, 0, 1)
                                                                 95: P_{4315} = (26, 5, 3, 1)
42: P_{1627} = (25, 17, 0, 1)
                                                                 96: P_{4321} = (0, 6, 3, 1)
43: P_{1650} = (16, 18, 0, 1)
                                                                 97: P_{4328} = (7, 6, 3, 1)
44: P_{1743} = (13, 21, 0, 1)
                                                                 98: P_{4377} = (24, 7, 3, 1)
45: P_{1796} = (2, 23, 0, 1)
                                                                 99: P_{4381} = (28, 7, 3, 1)
                                                                 100: P_{4393} = (8, 8, 3, 1)
46: P_{1830} = (4, 24, 0, 1)
47: P_{1910} = (20, 26, 0, 1)
                                                                 101: P_{4455} = (6, 10, 3, 1)
48: P_{1918} = (28, 26, 0, 1)
                                                                 102: P_{4770} = (1, 20, 3, 1)
49: P_{1925} = (3, 27, 0, 1)
                                                                 103: P_{4861} = (28, 22, 3, 1)
                                                                 104: P_{4923} = (26, 24, 3, 1)
50: P_{1981} = (27, 28, 0, 1)
51: P_{2054} = (4, 31, 0, 1)
                                                                 105: P_{4943} = (14, 25, 3, 1)
52: P_{2082} = (0,0,1,1)
                                                                 106: P_{4950} = (21, 25, 3, 1)
53: P_{2083} = (1, 0, 1, 1)
                                                                 107: P_{4988} = (27, 26, 3, 1)
54: P_{2114} = (0, 1, 1, 1)
                                                                 108: P_{4994} = (1, 27, 3, 1)
55: P_{2194} = (17, 3, 1, 1)
                                                                 109: P_{5010} = (17, 27, 3, 1)
56: P_{2253} = (12, 5, 1, 1)
                                                                 110: P_{5044} = (19, 28, 3, 1)
57: P_{2308} = (3,7,1,1)
                                                                 111: P_{5073} = (16, 29, 3, 1)
                                                                 112: P_{5074} = (17, 29, 3, 1)
58: P_{2366} = (29, 8, 1, 1)
59: P_{2423} = (22, 10, 1, 1)
                                                                 113: P_{5108} = (19, 30, 3, 1)
60: P_{2468} = (3, 12, 1, 1)
                                                                 114: P_{5115} = (26, 30, 3, 1)
61: P_{2554} = (25, 14, 1, 1)
                                                                 115: P_{5121} = (0, 31, 3, 1)
62: P_{2651} = (26, 17, 1, 1)
                                                                 116: P_{5201} = (16, 1, 4, 1)
63: P_{2709} = (20, 19, 1, 1)
                                                                 117: P_{5274} = (25, 3, 4, 1)
64: P_{2758} = (5, 21, 1, 1)
                                                                 118: P_{5320} = (7, 5, 4, 1)
65: P_{2829} = (12, 23, 1, 1)
                                                                 119: P_{5346} = (1, 6, 4, 1)
66: P_{2875} = (26, 24, 1, 1)
                                                                 120: P_{5478} = (5, 10, 4, 1)
                                                                 121: P_{5527} = (22, 11, 4, 1)
67: P_{2918} = (5, 26, 1, 1)
68: P_{2994} = (17, 28, 1, 1)
                                                                 122: P_{5565} = (28, 12, 4, 1)
                                                                 123: P_{5572} = (3, 13, 4, 1)
69: P_{3047} = (6, 30, 1, 1)
                                                                 124: P_{5604} = (3, 14, 4, 1)
70: P_{3141} = (4, 1, 2, 1)
71: P_{3225} = (24, 3, 2, 1)
                                                                 125: P_{5640} = (7, 15, 4, 1)
72: P_{3246} = (13, 4, 2, 1)
                                                                 126: P_{5692} = (27, 16, 4, 1)
                                                                 127: P_{5714} = (17, 17, 4, 1)
73: P_{3270} = (5, 5, 2, 1)
74: P_{3339} = (10, 7, 2, 1)
                                                                 128: P_{5765} = (4, 19, 4, 1)
75: P_{3364} = (3, 8, 2, 1)
                                                                 129: P_{5839} = (14, 21, 4, 1)
76: P_{3422} = (29, 9, 2, 1)
                                                                 130: P_{5927} = (6, 24, 4, 1)
                                                                 131: P_{5932} = (11, 24, 4, 1)
77: P_{3451} = (26, 10, 2, 1)
78: P_{3481} = (24, 11, 2, 1)
                                                                 132: P_{5941} = (20, 24, 4, 1)
79: P_{3511} = (22, 12, 2, 1)
                                                                 133: P_{6010} = (25, 26, 4, 1)
80: P_{3536} = (15, 13, 2, 1)
                                                                 134: P_{6048} = (31, 27, 4, 1)
81: P_{3574} = (21, 14, 2, 1)
                                                                 135: P_{6141} = (28, 30, 4, 1)
82: P_{3643} = (26, 16, 2, 1)
                                                                 136: P_{6194} = (17, 0, 5, 1)
83: P_{3670} = (21, 17, 2, 1)
                                                                 137: P_{6217} = (8, 1, 5, 1)
84: P_{3847} = (6, 23, 2, 1)
                                                                 138: P_{6242} = (1, 2, 5, 1)
                                                                 139: P_{6253} = (12, 2, 5, 1)
85: P_{3850} = (9, 23, 2, 1)
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140: P_{6275} = (2, 3, 5, 1)
                                                                 194: P_{8578} = (1, 11, 7, 1)
141: P_{6347} = (10, 5, 5, 1)
                                                                 195: P_{8590} = (13, 11, 7, 1)
142: P_{6361} = (24, 5, 5, 1)
                                                                 196: P_{8622} = (13, 12, 7, 1)
143: P_{6397} = (28, 6, 5, 1)
                                                                 197: P_{8661} = (20, 13, 7, 1)
144: P_{6399} = (30, 6, 5, 1)
                                                                 198: P_{8751} = (14, 16, 7, 1)
145: P_{6404} = (3, 7, 5, 1)
                                                                 199: P_{8752} = (15, 16, 7, 1)
146: P_{6507} = (10, 10, 5, 1)
                                                                 200: P_{8819} = (18, 18, 7, 1)
147: P_{6645} = (20, 14, 5, 1)
                                                                 201: P_{8861} = (28, 19, 7, 1)
148: P_{6724} = (3, 17, 5, 1)
                                                                 202: P_{8864} = (31, 19, 7, 1)
149: P_{6733} = (12, 17, 5, 1)
                                                                 203: P_{8868} = (3, 20, 7, 1)
150: P_{6753} = (0, 18, 5, 1)
                                                                 204: P_{8922} = (25, 21, 7, 1)
151: P_{6788} = (3, 19, 5, 1)
                                                                 205: P_{8957} = (28, 22, 7, 1)
                                                                 206: P_{9191} = (6, 30, 7, 1)
152: P_{6793} = (8, 19, 5, 1)
153: P_{6817} = (0, 20, 5, 1)
                                                                 207: P_{9202} = (17, 30, 7, 1)
154: P_{6838} = (21, 20, 5, 1)
                                                                 208: P_{9338} = (25, 2, 8, 1)
155: P_{6856} = (7, 21, 5, 1)
                                                                 209: P_{9411} = (2, 5, 8, 1)
                                                                 210: P_{9482} = (9,7,8,1)
156: P_{6872} = (23, 21, 5, 1)
                                                                 211: P_{9576} = (7, 10, 8, 1)
157: P_{6893} = (12, 22, 5, 1)
                                                                 212: P_{9659} = (26, 12, 8, 1)
158: P_{6894} = (13, 22, 5, 1)
159: P_{6921} = (8, 23, 5, 1)
                                                                 213: P_{9672} = (7, 13, 8, 1)
160: P_{7000} = (23, 25, 5, 1)
                                                                 214: P_{9684} = (19, 13, 8, 1)
161: P_{7106} = (1, 29, 5, 1)
                                                                 215: P_{9736} = (7, 15, 8, 1)
162: P_{7263} = (30, 1, 6, 1)
                                                                 216: P_{9957} = (4, 22, 8, 1)
163: P_{7282} = (17, 2, 6, 1)
                                                                 217: P_{9961} = (8, 22, 8, 1)
164: P_{7317} = (20, 3, 6, 1)
                                                                 218: P_{10014} = (29, 23, 8, 1)
165: P_{7350} = (21, 4, 6, 1)
                                                                 219: P_{10038} = (21, 24, 8, 1)
166: P_{7361} = (0, 5, 6, 1)
                                                                 220: P_{10040} = (23, 24, 8, 1)
167: P_{7594} = (9, 12, 6, 1)
                                                                 221: P_{10044} = (27, 24, 8, 1)
168: P_{7616} = (31, 12, 6, 1)
                                                                 222: P_{10086} = (5, 26, 8, 1)
                                                                 223: P_{10164} = (19, 28, 8, 1)
169: P_{7633} = (16, 13, 6, 1)
170: P_{7854} = (13, 20, 6, 1)
                                                                 224: P_{10214} = (5, 30, 8, 1)
171: P_{7887} = (14, 21, 6, 1)
                                                                 225: P_{10224} = (15, 30, 8, 1)
172: P_{7935} = (30, 22, 6, 1)
                                                                 226: P_{10347} = (10, 2, 9, 1)
173: P_{7983} = (14, 24, 6, 1)
                                                                 227: P_{10365} = (28, 2, 9, 1)
174: P_{8006} = (5, 25, 6, 1)
                                                                 228: P_{10379} = (10, 3, 9, 1)
175: P_{8042} = (9, 26, 6, 1)
                                                                 229: P_{10494} = (29, 6, 9, 1)
176: P_{8050} = (17, 26, 6, 1)
                                                                 230: P_{10499} = (2, 7, 9, 1)
177: P_{8088} = (23, 27, 6, 1)
                                                                 231: P_{10521} = (24, 7, 9, 1)
178: P_{8167} = (6, 30, 6, 1)
                                                                 232: P_{10525} = (28, 7, 9, 1)
179: P_{8169} = (8, 30, 6, 1)
                                                                 233: P_{10534} = (5, 8, 9, 1)
180: P_{8178} = (17, 30, 6, 1)
                                                                 234: P_{10574} = (13, 9, 9, 1)
                                                                 235: P_{10594} = (1, 10, 9, 1)
181: P_{8201} = (8, 31, 6, 1)
182: P_{8238} = (13, 0, 7, 1)
                                                                 236: P_{10614} = (21, 10, 9, 1)
183: P_{8249} = (24, 0, 7, 1)
                                                                 237: P_{10624} = (31, 10, 9, 1)
184: P_{8299} = (10, 2, 7, 1)
                                                                 238: P_{10685} = (28, 12, 9, 1)
185: P_{8310} = (21, 2, 7, 1)
                                                                 239: P_{10702} = (13, 13, 9, 1)
186: P_{8317} = (28, 2, 7, 1)
                                                                 240: P_{10719} = (30, 13, 9, 1)
187: P_{8357} = (4, 4, 7, 1)
                                                                 241: P_{10770} = (17, 15, 9, 1)
188: P_{8363} = (10, 4, 7, 1)
                                                                 242: P_{10847} = (30, 17, 9, 1)
189: P_{8436} = (19, 6, 7, 1)
                                                                 243: P_{10935} = (22, 20, 9, 1)
190: P_{8465} = (16, 7, 7, 1)
                                                                 244: P_{10975} = (30, 21, 9, 1)
191: P_{8467} = (18, 7, 7, 1)
                                                                 245: P_{11110} = (5, 26, 9, 1)
192: P_{8559} = (14, 10, 7, 1)
                                                                 246: P_{11410} = (17, 3, 10, 1)
193: P_{8565} = (20, 10, 7, 1)
                                                                 247: P_{11431} = (6, 4, 10, 1)
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248: P_{11523} = (2, 7, 10, 1)
                                                                302: P_{14109} = (28, 23, 12, 1)
249: P_{11545} = (24, 7, 10, 1)
                                                                303: P_{14146} = (1, 25, 12, 1)
250: P_{11549} = (28, 7, 10, 1)
                                                                304: P_{14180} = (3, 26, 12, 1)
251: P_{11766} = (21, 14, 10, 1)
                                                                305: P_{14194} = (17, 26, 12, 1)
252: P_{11845} = (4, 17, 10, 1)
                                                                306: P_{14258} = (17, 28, 12, 1)
253: P_{11922} = (17, 19, 10, 1)
                                                                307: P_{14281} = (8, 29, 12, 1)
254: P_{11936} = (31, 19, 10, 1)
                                                                308: P_{14297} = (24, 29, 12, 1)
255: P_{11980} = (11, 21, 10, 1)
                                                                309: P_{14335} = (30, 30, 12, 1)
256: P_{12041} = (8, 23, 10, 1)
                                                                310: P_{14428} = (27, 1, 13, 1)
257: P_{12087} = (22, 24, 10, 1)
                                                                311: P_{14450} = (17, 2, 13, 1)
258: P_{12107} = (10, 25, 10, 1)
                                                                312: P_{14489} = (24, 3, 13, 1)
259: P_{12113} = (16, 25, 10, 1)
                                                                313: P_{14506} = (9, 4, 13, 1)
260: P_{12132} = (3, 26, 10, 1)
                                                                314: P_{14549} = (20, 5, 13, 1)
                                                                315: P_{14649} = (24, 8, 13, 1)
261: P_{12169} = (8, 27, 10, 1)
262: P_{12182} = (21, 27, 10, 1)
                                                                316: P_{14702} = (13, 10, 13, 1)
263: P_{12310} = (21, 31, 10, 1)
                                                                317: P_{14781} = (28, 12, 13, 1)
                                                                318: P_{14933} = (20, 17, 13, 1)
264: P_{12434} = (17, 3, 11, 1)
265: P_{12463} = (14, 4, 11, 1)
                                                                319: P_{14973} = (28, 18, 13, 1)
266: P_{12472} = (23, 4, 11, 1)
                                                                320: P_{14994} = (17, 19, 13, 1)
267: P_{12495} = (14, 5, 11, 1)
                                                                321: P_{15063} = (22, 21, 13, 1)
268: P_{12658} = (17, 10, 11, 1)
                                                                322: P_{15070} = (29, 21, 13, 1)
269: P_{12700} = (27, 11, 11, 1)
                                                                323: P_{15072} = (31, 21, 13, 1)
270: P_{12724} = (19, 12, 11, 1)
                                                                324: P_{15124} = (19, 23, 13, 1)
271: P_{12770} = (1, 14, 11, 1)
                                                                325: P_{15227} = (26, 26, 13, 1)
272: P_{12787} = (18, 14, 11, 1)
                                                                326: P_{15237} = (4, 27, 13, 1)
273: P_{12797} = (28, 14, 11, 1)
                                                                327: P_{15298} = (1, 29, 13, 1)
274: P_{12983} = (22, 20, 11, 1)
                                                                328: P_{15341} = (12, 30, 13, 1)
275: P_{12997} = (4, 21, 11, 1)
                                                                329: P_{15367} = (6, 31, 13, 1)
276: P_{13000} = (7, 21, 11, 1)
                                                                330: P_{15467} = (10, 2, 14, 1)
277: P_{13016} = (23, 21, 11, 1)
                                                                331: P_{15485} = (28, 2, 14, 1)
278: P_{13176} = (23, 26, 11, 1)
                                                                332: P_{15494} = (5, 3, 14, 1)
279: P_{13204} = (19, 27, 11, 1)
                                                                333: P_{15565} = (12, 5, 14, 1)
280: P_{13212} = (27, 27, 11, 1)
                                                                334: P_{15598} = (13, 6, 14, 1)
281: P_{13236} = (19, 28, 11, 1)
                                                                335: P_{15599} = (14, 6, 14, 1)
282: P_{13274} = (25, 29, 11, 1)
                                                                336: P_{15642} = (25, 7, 14, 1)
283: P_{13325} = (12, 31, 11, 1)
                                                                337: P_{15661} = (12, 8, 14, 1)
284: P_{13371} = (26, 0, 12, 1)
                                                                338: P_{15667} = (18, 8, 14, 1)
285: P_{13391} = (14, 1, 12, 1)
                                                                339: P_{15793} = (16, 12, 14, 1)
286: P_{13539} = (2, 6, 12, 1)
                                                                340: P_{15925} = (20, 16, 14, 1)
287: P_{13540} = (3, 6, 12, 1)
                                                                341: P_{15997} = (28, 18, 14, 1)
288: P_{13583} = (14, 7, 12, 1)
                                                                342: P_{16069} = (4, 21, 14, 1)
289: P_{13679} = (14, 10, 12, 1)
                                                                343: P_{16072} = (7, 21, 14, 1)
290: P_{13682} = (17, 10, 12, 1)
                                                                344: P_{16088} = (23, 21, 14, 1)
291: P_{13697} = (0, 11, 12, 1)
                                                                345: P_{16171} = (10, 24, 14, 1)
292: P_{13750} = (21, 12, 12, 1)
                                                                346: P_{16304} = (15, 28, 14, 1)
293: P_{13759} = (30, 12, 12, 1)
                                                                347: P_{16381} = (28, 30, 14, 1)
294: P_{13858} = (1, 16, 12, 1)
                                                                348: P_{16483} = (2, 2, 15, 1)
295: P_{13860} = (3, 16, 12, 1)
                                                                349: P_{16489} = (8, 2, 15, 1)
296: P_{13905} = (16, 17, 12, 1)
                                                                350: P_{16537} = (24, 3, 15, 1)
297: P_{13975} = (22, 19, 12, 1)
                                                                351: P_{16589} = (12, 5, 15, 1)
298: P_{13992} = (7, 20, 12, 1)
                                                                352: P_{16877} = (12, 14, 15, 1)
299: P_{14049} = (0, 22, 12, 1)
                                                                353: P_{16899} = (2, 15, 15, 1)
300: P_{14072} = (23, 22, 12, 1)
                                                                354: P_{16953} = (24, 16, 15, 1)
301: P_{14088} = (7, 23, 12, 1)
                                                                355: P_{16959} = (30, 16, 15, 1)
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356: P_{16991} = (30, 17, 15, 1)
                                                                410: P_{19385} = (24, 28, 17, 1)
357: P_{17019} = (26, 18, 15, 1)
                                                                411: P_{19393} = (0, 29, 17, 1)
358: P_{17127} = (6, 22, 15, 1)
                                                                412: P_{19421} = (28, 29, 17, 1)
359: P_{17161} = (8, 23, 15, 1)
                                                                413: P_{19454} = (29, 30, 17, 1)
360: P_{17257} = (8, 26, 15, 1)
                                                                414: P_{19663} = (14, 5, 18, 1)
361: P_{17329} = (16, 28, 15, 1)
                                                                415: P_{19710} = (29, 6, 18, 1)
362: P_{17334} = (21, 28, 15, 1)
                                                                416: P_{19727} = (14, 7, 18, 1)
363: P_{17337} = (24, 28, 15, 1)
                                                                417: P_{19746} = (1, 8, 18, 1)
364: P_{17370} = (25, 29, 15, 1)
                                                                418: P_{19752} = (7, 8, 18, 1)
365: P_{17378} = (1, 30, 15, 1)
                                                                419: P_{19760} = (15, 8, 18, 1)
366: P_{17386} = (9, 30, 15, 1)
                                                                420: P_{19846} = (5, 11, 18, 1)
367: P_{17400} = (23, 30, 15, 1)
                                                                421: P_{19876} = (3, 12, 18, 1)
368: P_{17486} = (13, 1, 16, 1)
                                                                422: P_{20015} = (14, 16, 18, 1)
369: P_{17523} = (18, 2, 16, 1)
                                                                423: P_{20017} = (16, 16, 18, 1)
370: P_{17543} = (6, 3, 16, 1)
                                                                424: P_{20054} = (21, 17, 18, 1)
371: P_{17607} = (6, 5, 16, 1)
                                                                425: P_{20081} = (16, 18, 18, 1)
372: P_{17680} = (15, 7, 16, 1)
                                                                426: P_{20100} = (3, 19, 18, 1)
                                                                427: P_{20278} = (21, 24, 18, 1)
373: P_{17685} = (20, 7, 16, 1)
374: P_{17694} = (29, 7, 16, 1)
                                                                428: P_{20280} = (23, 24, 18, 1)
375: P_{17713} = (16, 8, 16, 1)
                                                                429: P_{20284} = (27, 24, 18, 1)
376: P_{17837} = (12, 12, 16, 1)
                                                                430: P_{20309} = (20, 25, 18, 1)
377: P_{17859} = (2, 13, 16, 1)
                                                                431: P_{20329} = (8, 26, 18, 1)
378: P_{17906} = (17, 14, 16, 1)
                                                                432: P_{20361} = (8, 27, 18, 1)
379: P_{17946} = (25, 15, 16, 1)
                                                                433: P_{20374} = (21, 27, 18, 1)
380: P_{18006} = (21, 17, 16, 1)
                                                                434: P_{20636} = (27, 3, 19, 1)
381: P_{18072} = (23, 19, 16, 1)
                                                                435: P_{20793} = (24, 8, 19, 1)
382: P_{18082} = (1, 20, 16, 1)
                                                                436: P_{20889} = (24, 11, 19, 1)
383: P_{18296} = (23, 26, 16, 1)
                                                                437: P_{20900} = (3, 12, 19, 1)
384: P_{18310} = (5, 27, 16, 1)
                                                                438: P_{20964} = (3, 14, 19, 1)
385: P_{18367} = (30, 28, 16, 1)
                                                                439: P_{20972} = (11, 14, 19, 1)
386: P_{18406} = (5, 30, 16, 1)
                                                                440: P_{21049} = (24, 16, 19, 1)
387: P_{18454} = (21, 31, 16, 1)
                                                                441: P_{21055} = (30, 16, 19, 1)
388: P_{18477} = (12, 0, 17, 1)
                                                                442: P_{21069} = (12, 17, 19, 1)
389: P_{18507} = (10, 1, 17, 1)
                                                                443: P_{21215} = (30, 21, 19, 1)
                                                                444: P_{21256} = (7, 23, 19, 1)
390: P_{18594} = (1, 4, 17, 1)
391: P_{18619} = (26, 4, 17, 1)
                                                                445: P_{21262} = (13, 23, 19, 1)
392: P_{18629} = (4, 5, 17, 1)
                                                                446: P_{21277} = (28, 23, 19, 1)
393: P_{18681} = (24, 6, 17, 1)
                                                                447: P_{21299} = (18, 24, 19, 1)
                                                                448: P_{21399} = (22, 27, 19, 1)
394: P_{18726} = (5, 8, 17, 1)
395: P_{18731} = (10, 8, 17, 1)
                                                                449: P_{21429} = (20, 28, 19, 1)
396: P_{18753} = (0, 9, 17, 1)
                                                                450: P_{21443} = (2, 29, 19, 1)
                                                                451: P_{21460} = (19, 29, 19, 1)
397: P_{18854} = (5, 12, 17, 1)
398: P_{18875} = (26, 12, 17, 1)
                                                                452: P_{21588} = (19, 1, 20, 1)
399: P_{18927} = (14, 14, 17, 1)
                                                                453: P_{21625} = (24, 2, 20, 1)
400: P_{19016} = (7, 17, 17, 1)
                                                                454: P_{21644} = (11, 3, 20, 1)
401: P_{19023} = (14, 17, 17, 1)
                                                                455: P_{21645} = (12, 3, 20, 1)
402: P_{19124} = (19, 20, 17, 1)
                                                                456: P_{21677} = (12, 4, 20, 1)
403: P_{19128} = (23, 20, 17, 1)
                                                                457: P_{21726} = (29, 5, 20, 1)
404: P_{19142} = (5, 21, 17, 1)
                                                                458: P_{21746} = (17, 6, 20, 1)
405: P_{19170} = (1, 22, 17, 1)
                                                                459: P_{21791} = (30, 7, 20, 1)
406: P_{19243} = (10, 24, 17, 1)
                                                                460: P_{22077} = (28, 16, 20, 1)
407: P_{19291} = (26, 25, 17, 1)
                                                                461: P_{22081} = (0, 17, 20, 1)
408: P_{19292} = (27, 25, 17, 1)
                                                                462: P_{22123} = (10, 18, 20, 1)
409: P_{19382} = (21, 28, 17, 1)
                                                                463: P_{22155} = (10, 19, 20, 1)
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464: P_{22157} = (12, 19, 20, 1)
                                                                518: P_{24613} = (4, 0, 23, 1)
465: P_{22165} = (20, 19, 20, 1)
                                                                519: P_{24637} = (28, 0, 23, 1)
466: P_{22356} = (19, 25, 20, 1)
                                                                520: P_{24681} = (8, 2, 23, 1)
                                                                521: P_{24682} = (9, 2, 23, 1)
467: P_{22380} = (11, 26, 20, 1)
468: P_{22387} = (18, 26, 20, 1)
                                                                522: P_{24762} = (25, 4, 23, 1)
469: P_{22414} = (13, 27, 20, 1)
                                                                523: P_{24773} = (4, 5, 23, 1)
470: P_{22463} = (30, 28, 20, 1)
                                                                524: P_{24932} = (3, 10, 23, 1)
471: P_{22492} = (27, 29, 20, 1)
                                                                525: P_{24951} = (22, 10, 23, 1)
472: P_{22568} = (7, 0, 21, 1)
                                                                526: P_{25032} = (7, 13, 23, 1)
473: P_{22588} = (27, 0, 21, 1)
                                                                527: P_{25044} = (19, 13, 23, 1)
474: P_{22703} = (14, 4, 21, 1)
                                                                528: P_{25049} = (24, 13, 23, 1)
475: P_{22712} = (23, 4, 21, 1)
                                                                529: P_{25064} = (7, 14, 23, 1)
476: P_{22717} = (28, 4, 21, 1)
                                                                530: P_{25068} = (11, 14, 23, 1)
                                                                531: P_{25104} = (15, 15, 23, 1)
477: P_{22835} = (18, 8, 21, 1)
478: P_{22840} = (23, 8, 21, 1)
                                                                532: P_{25186} = (1, 18, 23, 1)
479: P_{22858} = (9, 9, 21, 1)
                                                                533: P_{25189} = (4, 18, 23, 1)
480: P_{23007} = (30, 13, 21, 1)
                                                                534: P_{25225} = (8, 19, 23, 1)
481: P_{23008} = (31, 13, 21, 1)
                                                                535: P_{25242} = (25, 19, 23, 1)
482: P_{23038} = (29, 14, 21, 1)
                                                                536: P_{25256} = (7, 20, 23, 1)
483: P_{23039} = (30, 14, 21, 1)
                                                                537: P_{25327} = (14, 22, 23, 1)
484: P_{23042} = (1, 15, 21, 1)
                                                                538: P_{25347} = (2, 23, 23, 1)
485: P_{23068} = (27, 15, 21, 1)
                                                                539: P_{25360} = (15, 23, 23, 1)
486: P_{23087} = (14, 16, 21, 1)
                                                                540: P_{25406} = (29, 24, 23, 1)
487: P_{23089} = (16, 16, 21, 1)
                                                                541: P_{25421} = (12, 25, 23, 1)
488: P_{23181} = (12, 19, 21, 1)
                                                                542: P_{25492} = (19, 27, 23, 1)
489: P_{23189} = (20, 19, 21, 1)
                                                                543: P_{25500} = (27, 27, 23, 1)
490: P_{23209} = (8, 20, 21, 1)
                                                                544: P_{25649} = (16, 0, 24, 1)
491: P_{23242} = (9, 21, 21, 1)
                                                                545: P_{25656} = (23, 0, 24, 1)
492: P_{23246} = (13, 21, 21, 1)
                                                                546: P_{25699} = (2, 2, 24, 1)
493: P_{23384} = (23, 25, 21, 1)
                                                                547: P_{25705} = (8, 2, 24, 1)
494: P_{23420} = (27, 26, 21, 1)
                                                                548: P_{25771} = (10, 4, 24, 1)
495: P_{23454} = (29, 27, 21, 1)
                                                                549: P_{25772} = (11, 4, 24, 1)
496: P_{23463} = (6, 28, 21, 1)
                                                                550: P_{25851} = (26, 6, 24, 1)
497: P_{23494} = (5, 29, 21, 1)
                                                                551: P_{25879} = (22, 7, 24, 1)
498: P_{23627} = (10, 1, 22, 1)
                                                                552: P_{25895} = (6, 8, 24, 1)
499: P_{23715} = (2, 4, 22, 1)
                                                                553: P_{25899} = (10, 8, 24, 1)
500: P_{23756} = (11, 5, 22, 1)
                                                                554: P_{25922} = (1, 9, 24, 1)
501: P_{23776} = (31, 5, 22, 1)
                                                                555: P_{25937} = (16, 9, 24, 1)
502: P_{23908} = (3, 10, 22, 1)
                                                                556: P_{26086} = (5, 14, 24, 1)
503: P_{23927} = (22, 10, 22, 1)
                                                                557: P_{26106} = (25, 14, 24, 1)
504: P_{23935} = (30, 10, 22, 1)
                                                                558: P_{26151} = (6, 16, 24, 1)
                                                                559: P_{26193} = (16, 17, 24, 1)
505: P_{23967} = (30, 11, 22, 1)
506: P_{23994} = (25, 12, 22, 1)
                                                                560: P_{26405} = (4, 24, 24, 1)
507: P_{24004} = (3, 13, 22, 1)
                                                                561: P_{26432} = (31, 24, 24, 1)
508: P_{24118} = (21, 16, 22, 1)
                                                                562: P_{26463} = (30, 25, 24, 1)
509: P_{24132} = (3, 17, 22, 1)
                                                                563: P_{26504} = (7, 27, 24, 1)
510: P_{24160} = (31, 17, 22, 1)
                                                                564: P_{26505} = (8, 27, 24, 1)
511: P_{24235} = (10, 20, 22, 1)
                                                                565: P_{26518} = (21, 27, 24, 1)
512: P_{24361} = (8, 24, 22, 1)
                                                                566: P_{26582} = (21, 29, 24, 1)
513: P_{24389} = (4, 25, 22, 1)
                                                                567: P_{26608} = (15, 30, 24, 1)
514: P_{24417} = (0, 26, 22, 1)
                                                                568: P_{26614} = (21, 30, 24, 1)
515: P_{24473} = (24, 27, 22, 1)
                                                                569: P_{26656} = (31, 31, 24, 1)
516: P_{24489} = (8, 28, 22, 1)
                                                                570: P_{26703} = (14, 1, 25, 1)
517: P_{24539} = (26, 29, 22, 1)
                                                                571: P_{26728} = (7, 2, 25, 1)
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572: P_{26753} = (0, 3, 25, 1)
                                                                626: P_{29228} = (11, 16, 27, 1)
573: P_{26865} = (16, 6, 25, 1)
                                                                627: P_{29278} = (29, 17, 27, 1)
574: P_{26891} = (10, 7, 25, 1)
                                                                628: P_{29301} = (20, 18, 27, 1)
575: P_{27046} = (5, 12, 25, 1)
                                                                629: P_{29339} = (26, 19, 27, 1)
576: P_{27059} = (18, 12, 25, 1)
                                                                630: P_{29410} = (1, 22, 27, 1)
577: P_{27101} = (28, 13, 25, 1)
                                                                631: P_{29481} = (8, 24, 27, 1)
578: P_{27110} = (5, 14, 25, 1)
                                                                632: P_{29560} = (23, 26, 27, 1)
579: P_{27124} = (19, 14, 25, 1)
                                                                633: P_{29619} = (18, 28, 27, 1)
580: P_{27130} = (25, 14, 25, 1)
                                                                634: P_{29623} = (22, 28, 27, 1)
581: P_{27156} = (19, 15, 25, 1)
                                                                635: P_{29626} = (25, 28, 27, 1)
582: P_{27173} = (4, 16, 25, 1)
                                                                636: P_{29731} = (2, 0, 28, 1)
583: P_{27216} = (15, 17, 25, 1)
                                                                637: P_{29750} = (21, 0, 28, 1)
584: P_{27219} = (18, 17, 25, 1)
                                                                638: P_{29815} = (22, 2, 28, 1)
585: P_{27364} = (3, 22, 25, 1)
                                                                639: P_{29827} = (2, 3, 28, 1)
586: P_{27403} = (10, 23, 25, 1)
                                                                640: P_{29945} = (24, 6, 28, 1)
587: P_{27495} = (6, 26, 25, 1)
                                                                641: P_{30011} = (26, 8, 28, 1)
                                                                642: P_{30014} = (29, 8, 28, 1)
588: P_{27526} = (5, 27, 25, 1)
589: P_{27599} = (14, 29, 25, 1)
                                                                643: P_{30058} = (9, 10, 28, 1)
590: P_{27684} = (3, 0, 26, 1)
                                                                644: P_{30073} = (24, 10, 28, 1)
591: P_{27743} = (30, 1, 26, 1)
                                                                645: P_{30092} = (11, 11, 28, 1)
592: P_{27782} = (5, 3, 26, 1)
                                                                646: P_{30158} = (13, 13, 28, 1)
593: P_{27789} = (12, 3, 26, 1)
                                                                647: P_{30175} = (30, 13, 28, 1)
594: P_{27874} = (1, 6, 26, 1)
                                                                648: P_{30264} = (23, 16, 28, 1)
595: P_{27962} = (25, 8, 26, 1)
                                                                649: P_{30265} = (24, 16, 28, 1)
596: P_{28078} = (13, 12, 26, 1)
                                                                650: P_{30271} = (30, 16, 28, 1)
597: P_{28098} = (1, 13, 26, 1)
                                                                651: P_{30450} = (17, 22, 28, 1)
598: P_{28102} = (5, 13, 26, 1)
                                                                652: P_{30485} = (20, 23, 28, 1)
599: P_{28141} = (12, 14, 26, 1)
                                                                653: P_{30611} = (18, 27, 28, 1)
600: P_{28159} = (30, 14, 26, 1)
                                                                654: P_{30612} = (19, 27, 28, 1)
601: P_{28161} = (0, 15, 26, 1)
                                                                655: P_{30636} = (11, 28, 28, 1)
602: P_{28308} = (19, 19, 26, 1)
                                                                656: P_{30652} = (27, 28, 28, 1)
603: P_{28325} = (4, 20, 26, 1)
                                                                657: P_{30667} = (10, 29, 28, 1)
604: P_{28326} = (5, 20, 26, 1)
                                                                658: P_{30708} = (19, 30, 28, 1)
605: P_{28383} = (30, 21, 26, 1)
                                                                659: P_{30711} = (22, 30, 28, 1)
606: P_{28392} = (7, 22, 26, 1)
                                                                660: P_{30722} = (1, 31, 28, 1)
607: P_{28395} = (10, 22, 26, 1)
                                                                661: P_{30723} = (2, 31, 28, 1)
608: P_{28429} = (12, 23, 26, 1)
                                                                662: P_{30793} = (8, 1, 29, 1)
609: P_{28470} = (21, 24, 26, 1)
                                                                663: P_{30844} = (27, 2, 29, 1)
610: P_{28472} = (23, 24, 26, 1)
                                                                664: P_{30858} = (9, 3, 29, 1)
611: P_{28481} = (0, 25, 26, 1)
                                                                665: P_{30864} = (15, 3, 29, 1)
612: P_{28505} = (24, 25, 26, 1)
                                                                666: P_{30888} = (7, 4, 29, 1)
613: P_{28532} = (19, 26, 26, 1)
                                                                667: P_{30928} = (15, 5, 29, 1)
614: P_{28541} = (28, 26, 26, 1)
                                                                668: P_{30939} = (26, 5, 29, 1)
615: P_{28630} = (21, 29, 26, 1)
                                                                669: P_{30953} = (8, 6, 29, 1)
616: P_{28739} = (2, 1, 27, 1)
                                                                670: P_{31023} = (14, 8, 29, 1)
617: P_{28785} = (16, 2, 27, 1)
                                                                671: P_{31035} = (26, 8, 29, 1)
618: P_{28804} = (3, 3, 27, 1)
                                                                672: P_{31038} = (29, 8, 29, 1)
619: P_{28845} = (12, 4, 27, 1)
                                                                673: P_{31055} = (14, 9, 29, 1)
620: P_{28872} = (7, 5, 27, 1)
                                                                674: P_{31137} = (0, 12, 29, 1)
621: P_{28973} = (12, 8, 27, 1)
                                                                675: P_{31192} = (23, 13, 29, 1)
622: P_{29016} = (23, 9, 27, 1)
                                                                676: P_{31291} = (26, 16, 29, 1)
623: P_{29032} = (7, 10, 27, 1)
                                                                677: P_{31319} = (22, 17, 29, 1)
624: P_{29118} = (29, 12, 27, 1)
                                                                678: P_{31405} = (12, 20, 29, 1)
625: P_{29180} = (27, 14, 27, 1)
                                                                679: P_{31444} = (19, 21, 29, 1)
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680: P_{31459} = (2, 22, 29, 1)
                                                                701: P_{32933} = (4, 4, 31, 1)
681: P_{31508} = (19, 23, 29, 1)
                                                                702: P_{32939} = (10, 4, 31, 1)
682: P_{31919} = (14, 4, 30, 1)
                                                                703: P_{32968} = (7, 5, 31, 1)
683: P_{31928} = (23, 4, 30, 1)
                                                                704: P_{33092} = (3, 9, 31, 1)
684: P_{31954} = (17, 5, 30, 1)
                                                                705: P_{33204} = (19, 12, 31, 1)
685: P_{32015} = (14, 7, 30, 1)
                                                                706: P_{33224} = (7, 13, 31, 1)
686: P_{32088} = (23, 9, 30, 1)
                                                                707: P_{33236} = (19, 13, 31, 1)
                                                                708: P_{33371} = (26, 17, 31, 1)
687: P_{32106} = (9, 10, 30, 1)
688: P_{32123} = (26, 10, 30, 1)
                                                                709: P_{33410} = (1, 19, 31, 1)
689: P_{32222} = (29, 13, 30, 1)
                                                                710: P_{33420} = (11, 19, 31, 1)
690: P_{32347} = (26, 17, 30, 1)
                                                                711: P_{33433} = (24, 19, 31, 1)
                                                                712: P_{33511} = (6, 22, 31, 1)
691: P_{32408} = (23, 19, 30, 1)
692: P_{32444} = (27, 20, 30, 1)
                                                                713: P_{33544} = (7, 23, 31, 1)
693: P_{32447} = (30, 20, 30, 1)
                                                                714: P_{33550} = (13, 23, 31, 1)
694: P_{32455} = (6, 21, 30, 1)
                                                                715: P_{33565} = (28, 23, 31, 1)
695: P_{32544} = (31, 23, 30, 1)
                                                                716: P_{33579} = (10, 24, 31, 1)
696: P_{32622} = (13, 26, 30, 1)
                                                                717: P_{33621} = (20, 25, 31, 1)
697: P_{32689} = (16, 28, 30, 1)
                                                                718: P_{33787} = (26, 30, 31, 1)
698: P_{32694} = (21, 28, 30, 1)
                                                                719: P_{33797} = (4, 31, 31, 1)
699: P_{32697} = (24, 28, 30, 1)
700: P_{32907} = (10, 3, 31, 1)
```

# Line Intersection Graph

	0  1	2	3 4	5	6	7	8	9	10	11	12	13	14
0	00	1	10	0	0	0	1	0	0	0	1	1	1
1	0 0	1	0.0	0	1	0	0	0	1	1	0	1	1
2	11	0	0.0	1	0	1	1	0	1	0	0	0	0
3	10	0	0 1	0	0	1	0	0	1	1	0	1	0
4	0 0	0	10	1	1	0	1	0	1	0	0	0	1
5	0 0	1	0 1	0	0	1	0	1	0	0	0	1	1
6	0 1	0	0 1	0	0	1	1	0	0	0	1	1	0
7	0 0	1	10	1	1	0	0	0	0	1	1	0	0
8	10	1	0 1	0	1	0	0	1	0	1	0	0	0
9	0 0	0	0.0	1	0	0	1	0	1	1	1	1	0
10	0 1	1	11	0	0	0	0	1	0	0	1	0	0
11	0 1	0	10	0	0	1	1	1	0	0	0	0	1
12	10	0	0.0	0	1	1	0	1	1	0	0	0	1
13	11	0	10	1	1	0	0	1	0	0	0	0	0
14	11	0	0 1	1	0	0	0	0	0	1	1	0	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_2$	$\ell_3$	$\ell_8$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$
in point	$P_{14585}$	$P_{18264}$	$P_{14585}$	$P_{30853}$	$P_{18264}$	$P_{30853}$

Line 1 intersects

Line	$\ell_2$	$\ell_6$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$
in point	$P_{23761}$	$P_{5885}$	$P_{23761}$	$P_{19808}$	$P_{5885}$	$P_{19808}$

Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_{10}$
in point	$P_{14585}$	$P_{23761}$	$P_{29352}$	$P_{29352}$	$P_{14585}$	$P_{23761}$

Line 3 intersects

Line	$\ell_0$	$\ell_4$	$\ell_7$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$
in point	$P_{18264}$	$P_{10643}$	$P_{27214}$	$P_{10643}$	$P_{27214}$	$P_{18264}$

Line 4 intersects							
	Line	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_{10}$	$\ell_{14}$
	in point	$P_{10643}$	$P_{17420}$	$P_{7612}$	$P_{7612}$	$P_{10643}$	$P_{17420}$
Line 5 intersects							
Line 5 intersects	Line	$\ell_2$	$\ell_4$	$\ell_7$	$\ell_9$	$\ell_{13}$	$\ell_{14}$
	in point	$P_{29352}$	$P_{17420}$	$P_{29352}$	$P_{22371}$	$P_{22371}$	$P_{17420}$
	P	- 29302	- 17420	- 29302	- 22311	- 22311	- 17420
Line 6 intersects	Т:	- 0	0	1 0	0 1	0	0
	Lin	_	$\ell_4$	$\ell_7$	$\ell_8$	$\ell_{12}$	$\ell_{13}$
	in poir	it $P_{5885}$	$P_{7612}$	$P_{4054}$	$P_{7612}$	$P_{4054}$	$P_{5885}$
Line 7 intersects							
	Line	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_{11}$	$\ell_{12}$
	in point	$P_{29352}$	$P_{27214}$	$P_{29352}$	$P_{4054}$	$P_{27214}$	$P_{4054}$
Line 8 intersects							
Line o intersects	Line	$\ell_0$	$\ell_2$	$\ell_4$	$\ell_6$	$\ell_9$	$\ell_{11}$
	in point	$P_{14585}$	$P_{14585}$	$P_{7612}$	$P_{7612}$	$P_{12810}$	$P_{12810}$
T	P	- 14363	- 14000	- 7012	- 7012	- 12010	- 12010
Line 9 intersects	T:	0	0	0	0	0	0
	Line	$\ell_5$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$
	in point	$P_{22371}$	$P_{12810}$	$P_{33392}$	$P_{12810}$	$P_{33392}$	$P_{22371}$
Line 10 intersects							
	Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_9$	$\ell_{12}$
	in point	$P_{23761}$	$P_{23761}$	$P_{10643}$	$P_{10643}$	$P_{33392}$	$P_{33392}$
Line 11 intersects							
Line 11 intersects	Line	$\ell_1$	$\ell_3$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{14}$
	in point	$P_{19808}$	$P_{27214}$	$P_{27214}$	$P_{12810}$	$P_{12810}$	$P_{19808}$
	P	- 19000	- 21214	- 2/214	- 12010	- 12010	- 13000
Line 12 intersects	T:	1 0	1 0	0	0	0	0
	Line	$\ell_0$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{14}$
	in point	$P_{30853}$	$P_{4054}$	$P_{4054}$	$P_{33392}$	$P_{33392}$	$P_{30853}$
Line 13 intersects			_				
	Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_9$
	in point	$P_{18264}$	$P_{5885}$	$P_{18264}$	$P_{22371}$	$P_{5885}$	$P_{22371}$
Line 14 intersects							
Line 14 interaction	Line	$\ell_0$	$\ell_1$	$\ell_4$	$\ell_5$	$\ell_{11}$	$\ell_{12}$
	in point	$P_{30853}$	$P_{19808}$	$P_{17420}$	$P_{17420}$	$P_{19808}$	$P_{30853}$
		55556	10000	11720	11740	10000	50000

The surface has 1185 points:

Too many to print.