Rank-65868 over GF(4)

January 15, 2021

The equation

The equation of the surface is:

$$X_0^3 + X_3^3 + X_0^2 X_3 + X_1^2 X_2 + X_0 X_1 X_2 = 0$$

(1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over ${\rm GF}(4)$ is 1431725466

General information

Number of lines	0
Number of points	13
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	0
Number of points off lines	13
Number of Hesse planes	0
Number of axes	0
Type of points on lines	
Type of lines on points	0^{13}

Singular Points

The surface has 1 singular points:

$$0: P_2 = \mathbf{P}(0,0,1,0) = \mathbf{P}(0,0,1,0)$$

The 0 Lines

The lines and their Pluecker coordinates are:

Rank of lines: ()

Rank of points on Klein quadric: ()

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 0 single points: The single points on the surface are:

The single points on the surface are:

Points on surface but on no line

The surface has 13 points not on any line: The points on the surface but not on lines are:

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\begin{array}{lll} 0: \ P_1 = (0,1,0,0) & 7: \ P_{46} = (1,2,1,1) \\ 1: \ P_2 = (0,0,1,0) & 8: \ P_{48} = (3,2,1,1) \\ 2: \ P_{16} = (1,2,1,0) & 9: \ P_{50} = (1,3,1,1) \\ 3: \ P_{20} = (1,3,1,0) & 10: \ P_{51} = (2,3,1,1) \\ 4: \ P_{42} = (0,1,1,1) & 11: \ P_{61} = (0,2,2,1) \\ 5: \ P_{43} = (2,1,1,1) & 12: \ P_{81} = (0,3,3,1) \\ 6: \ P_{44} = (3,1,1,1) & & & \end{array}
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Line Intersection Graph

Neighbor sets in the line intersection graph:

The surface has 13 points:

The points on the surface are:

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\begin{array}{lll} 0: \ P_1 = (0,1,0,0) & 5: \ P_{43} = (2,1,1,1) & 10: \ P_{51} = (2,3,1,1) \\ 1: \ P_2 = (0,0,1,0) & 6: \ P_{44} = (3,1,1,1) & 11: \ P_{61} = (0,2,2,1) \\ 2: \ P_{16} = (1,2,1,0) & 7: \ P_{46} = (1,2,1,1) & 12: \ P_{81} = (0,3,3,1) \\ 3: \ P_{20} = (1,3,1,0) & 8: \ P_{48} = (3,2,1,1) \\ 4: \ P_{42} = (0,1,1,1) & 9: \ P_{50} = (1,3,1,1) \end{array}
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