

Rank-65859 over GF(16)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^2 X_3 + X_1^2 X_2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(16) is 303108373

General information

Number of lines	19
Number of points	289
Number of singular points	17
Number of Eckardt points	8
Number of double points	18
Number of single points	263
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17^{19}
Type of lines on points	$3^8, 2^{18}, 1^{263}$

Singular Points

The surface has 17 singular points:

$$0 : P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0)$$

$$1 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

$$2 : P_{530} = \mathbf{P}(0, 0, 1, 1) = \mathbf{P}(0, 0, 1, 1)$$

$$3 : P_{785} = \mathbf{P}(0, 0, \delta, 1) = \mathbf{P}(0, 0, 2, 1)$$

$$4 : P_{1041} = \mathbf{P}(0, 0, \delta^{12}, 1) = \mathbf{P}(0, 0, 3, 1)$$

$$5 : P_{1297} = \mathbf{P}(0, 0, \delta^2, 1) = \mathbf{P}(0, 0, 4, 1)$$

$$6 : P_{1553} = \mathbf{P}(0, 0, \delta^9, 1) = \mathbf{P}(0, 0, 5, 1)$$

$$7 : P_{1809} = \mathbf{P}(0, 0, \delta^{13}, 1) = \mathbf{P}(0, 0, 6, 1)$$

$$8 : P_{2065} = \mathbf{P}(0, 0, \delta^7, 1) = \mathbf{P}(0, 0, 7, 1)$$

$$9 : P_{2321} = \mathbf{P}(0, 0, \delta^3, 1) = \mathbf{P}(0, 0, 8, 1)$$

$$10 : P_{2577} = \mathbf{P}(0, 0, \delta^4, 1) = \mathbf{P}(0, 0, 9, 1)$$

$$11 : P_{2833} = \mathbf{P}(0, 0, \delta^{10}, 1) = \mathbf{P}(0, 0, 10, 1)$$

$$12 : P_{3089} = \mathbf{P}(0, 0, \delta^5, 1) = \mathbf{P}(0, 0, 11, 1)$$

$$13 : P_{3345} = \mathbf{P}(0, 0, \delta^{14}, 1) = \mathbf{P}(0, 0, 12, 1)$$

$$14 : P_{3601} = \mathbf{P}(0, 0, \delta^{11}, 1) = \mathbf{P}(0, 0, 13, 1)$$

$$15 : P_{3857} = \mathbf{P}(0, 0, \delta^8, 1) = \mathbf{P}(0, 0, 14, 1)$$

$$16 : P_{4113} = \mathbf{P}(0, 0, \delta^6, 1) = \mathbf{P}(0, 0, 15, 1)$$

The 19 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned}
\ell_0 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0 \\
\ell_1 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{256} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{256} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2 \\
\ell_2 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{529} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{529} = \mathbf{Pl}(0, 0, 1, 0, 0, 1)_{4656} \\
\ell_3 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69904} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{69904} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)_{33} \\
\ell_4 &= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70160} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70160} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_1 \\
\ell_5 &= \begin{bmatrix} 1 & \delta^{14} & 0 & 0 \\ 0 & 0 & 1 & \delta^{10} \end{bmatrix}_{3542} = \begin{bmatrix} 1 & 12 & 0 & 0 \\ 0 & 0 & 1 & 10 \end{bmatrix}_{3542} = \mathbf{Pl}(0, 0, 11, 10, 13, 1)_{58696} \\
\ell_6 &= \begin{bmatrix} 1 & \delta^3 & 0 & 0 \\ 0 & 0 & 1 & \delta^7 \end{bmatrix}_{2447} = \begin{bmatrix} 1 & 8 & 0 & 0 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{2447} = \mathbf{Pl}(0, 0, 14, 7, 9, 1)_{42469} \\
\ell_7 &= \begin{bmatrix} 1 & \delta^{13} & 0 & 0 \\ 0 & 0 & 1 & \delta^5 \end{bmatrix}_{1905} = \begin{bmatrix} 1 & 6 & 0 & 0 \\ 0 & 0 & 1 & 11 \end{bmatrix}_{1905} = \mathbf{Pl}(0, 0, 10, 11, 7, 1)_{34185} \\
\ell_8 &= \begin{bmatrix} 1 & \delta^6 & 0 & 0 \\ 0 & 0 & 1 & \delta^{14} \end{bmatrix}_{4363} = \begin{bmatrix} 1 & 15 & 0 & 0 \\ 0 & 0 & 1 & 12 \end{bmatrix}_{4363} = \mathbf{Pl}(0, 0, 2, 12, 14, 1)_{62497} \\
\ell_9 &= \begin{bmatrix} 1 & \delta^2 & 0 & 0 \\ 0 & 0 & 1 & \delta^{11} \end{bmatrix}_{1361} = \begin{bmatrix} 1 & 4 & 0 & 0 \\ 0 & 0 & 1 & 13 \end{bmatrix}_{1361} = \mathbf{Pl}(0, 0, 9, 13, 5, 1)_{25994} \\
\ell_{10} &= \begin{bmatrix} 1 & \delta^8 & 0 & 0 \\ 0 & 0 & 1 & \delta^{14} \end{bmatrix}_{4090} = \begin{bmatrix} 1 & 14 & 0 & 0 \\ 0 & 0 & 1 & 12 \end{bmatrix}_{4090} = \mathbf{Pl}(0, 0, 2, 12, 15, 1)_{66577} \\
\ell_{11} &= \begin{bmatrix} 1 & \delta^{12} & 0 & 0 \\ 0 & 0 & 1 & \delta^{13} \end{bmatrix}_{1081} = \begin{bmatrix} 1 & 3 & 0 & 0 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{1081} = \mathbf{Pl}(0, 0, 4, 6, 2, 1)_{13599} \\
\ell_{12} &= \begin{bmatrix} 1 & \delta^{11} & 0 & 0 \\ 0 & 0 & 1 & \delta^{10} \end{bmatrix}_{3815} = \begin{bmatrix} 1 & 13 & 0 & 0 \\ 0 & 0 & 1 & 10 \end{bmatrix}_{3815} = \mathbf{Pl}(0, 0, 11, 10, 12, 1)_{54616} \\
\ell_{13} &= \begin{bmatrix} 1 & \delta^5 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{3260} = \begin{bmatrix} 1 & 11 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{3260} = \mathbf{Pl}(0, 0, 1, 1, 10, 1)_{46146} \\
\ell_{14} &= \begin{bmatrix} 1 & \delta^{10} & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{2987} = \begin{bmatrix} 1 & 10 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{2987} = \mathbf{Pl}(0, 0, 1, 1, 11, 1)_{50226} \\
\ell_{15} &= \begin{bmatrix} 1 & \delta & 0 & 0 \\ 0 & 0 & 1 & \delta^{13} \end{bmatrix}_{808} = \begin{bmatrix} 1 & 2 & 0 & 0 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{808} = \mathbf{Pl}(0, 0, 4, 6, 3, 1)_{17679} \\
\ell_{16} &= \begin{bmatrix} 1 & \delta^4 & 0 & 0 \\ 0 & 0 & 1 & \delta^7 \end{bmatrix}_{2720} = \begin{bmatrix} 1 & 9 & 0 & 0 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{2720} = \mathbf{Pl}(0, 0, 14, 7, 8, 1)_{38389} \\
\ell_{17} &= \begin{bmatrix} 1 & \delta^7 & 0 & 0 \\ 0 & 0 & 1 & \delta^5 \end{bmatrix}_{2178} = \begin{bmatrix} 1 & 7 & 0 & 0 \\ 0 & 0 & 1 & 11 \end{bmatrix}_{2178} = \mathbf{Pl}(0, 0, 10, 11, 6, 1)_{30105} \\
\ell_{18} &= \begin{bmatrix} 1 & \delta^9 & 0 & 0 \\ 0 & 0 & 1 & \delta^{11} \end{bmatrix}_{1634} = \begin{bmatrix} 1 & 5 & 0 & 0 \\ 0 & 0 & 1 & 13 \end{bmatrix}_{1634} = \mathbf{Pl}(0, 0, 9, 13, 4, 1)_{21914}
\end{aligned}$$

Rank of lines: (0, 256, 529, 69904, 70160, 3542, 2447, 1905, 4363, 1361, 4090, 1081, 3815, 3260, 2987, 808, 2720, 2178, 1634)

Rank of points on Klein quadric: (0, 2, 4656, 33, 1, 58696, 42469, 34185, 62497, 25994, 66577, 13599, 54616, 46146, 50226, 17679, 38389, 30105, 21914)

Eckardt Points

The surface has 8 Eckardt points:

- 0 : $P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0)$,
- 1 : $P_{530} = \mathbf{P}(0, 0, 1, 1) = \mathbf{P}(0, 0, 1, 1)$,
- 2 : $P_{785} = \mathbf{P}(0, 0, \delta, 1) = \mathbf{P}(0, 0, 2, 1)$,
- 3 : $P_{1297} = \mathbf{P}(0, 0, \delta^2, 1) = \mathbf{P}(0, 0, 4, 1)$,
- 4 : $P_{2577} = \mathbf{P}(0, 0, \delta^4, 1) = \mathbf{P}(0, 0, 9, 1)$,
- 5 : $P_{2833} = \mathbf{P}(0, 0, \delta^{10}, 1) = \mathbf{P}(0, 0, 10, 1)$,
- 6 : $P_{3089} = \mathbf{P}(0, 0, \delta^5, 1) = \mathbf{P}(0, 0, 11, 1)$,
- 7 : $P_{3857} = \mathbf{P}(0, 0, \delta^8, 1) = \mathbf{P}(0, 0, 14, 1)$.

Double Points

The surface has 18 Double points:

The double points on the surface are:

- | | |
|---|--|
| $P_0 = (1, 0, 0, 0) = \ell_0 \cap \ell_1$ | $P_{13} = (9, 1, 0, 0) = \ell_0 \cap \ell_{12}$ |
| $P_5 = (1, 1, 0, 0) = \ell_0 \cap \ell_2$ | $P_{14} = (10, 1, 0, 0) = \ell_0 \cap \ell_{13}$ |
| $P_1 = (0, 1, 0, 0) = \ell_0 \cap \ell_3$ | $P_{15} = (11, 1, 0, 0) = \ell_0 \cap \ell_{14}$ |
| $P_6 = (2, 1, 0, 0) = \ell_0 \cap \ell_5$ | $P_{16} = (12, 1, 0, 0) = \ell_0 \cap \ell_{15}$ |
| $P_7 = (3, 1, 0, 0) = \ell_0 \cap \ell_6$ | $P_{17} = (13, 1, 0, 0) = \ell_0 \cap \ell_{16}$ |
| $P_8 = (4, 1, 0, 0) = \ell_0 \cap \ell_7$ | $P_{18} = (14, 1, 0, 0) = \ell_0 \cap \ell_{17}$ |
| $P_9 = (5, 1, 0, 0) = \ell_0 \cap \ell_8$ | $P_{19} = (15, 1, 0, 0) = \ell_0 \cap \ell_{18}$ |
| $P_{10} = (6, 1, 0, 0) = \ell_0 \cap \ell_9$ | $P_3 = (0, 0, 0, 1) = \ell_3 \cap \ell_4$ |
| $P_{11} = (7, 1, 0, 0) = \ell_0 \cap \ell_{10}$ | |
| $P_{12} = (8, 1, 0, 0) = \ell_0 \cap \ell_{11}$ | |

Single Points

The surface has 263 single points:

The single points on the surface are:

- | | |
|---|---|
| 0 : $P_{20} = (1, 0, 1, 0)$ lies on line ℓ_1 | 19 : $P_{104} = (5, 5, 1, 0)$ lies on line ℓ_2 |
| 1 : $P_{21} = (2, 0, 1, 0)$ lies on line ℓ_1 | 20 : $P_{121} = (6, 6, 1, 0)$ lies on line ℓ_2 |
| 2 : $P_{22} = (3, 0, 1, 0)$ lies on line ℓ_1 | 21 : $P_{138} = (7, 7, 1, 0)$ lies on line ℓ_2 |
| 3 : $P_{23} = (4, 0, 1, 0)$ lies on line ℓ_1 | 22 : $P_{155} = (8, 8, 1, 0)$ lies on line ℓ_2 |
| 4 : $P_{24} = (5, 0, 1, 0)$ lies on line ℓ_1 | 23 : $P_{172} = (9, 9, 1, 0)$ lies on line ℓ_2 |
| 5 : $P_{25} = (6, 0, 1, 0)$ lies on line ℓ_1 | 24 : $P_{189} = (10, 10, 1, 0)$ lies on line ℓ_2 |
| 6 : $P_{26} = (7, 0, 1, 0)$ lies on line ℓ_1 | 25 : $P_{206} = (11, 11, 1, 0)$ lies on line ℓ_2 |
| 7 : $P_{27} = (8, 0, 1, 0)$ lies on line ℓ_1 | 26 : $P_{223} = (12, 12, 1, 0)$ lies on line ℓ_2 |
| 8 : $P_{28} = (9, 0, 1, 0)$ lies on line ℓ_1 | 27 : $P_{240} = (13, 13, 1, 0)$ lies on line ℓ_2 |
| 9 : $P_{29} = (10, 0, 1, 0)$ lies on line ℓ_1 | 28 : $P_{257} = (14, 14, 1, 0)$ lies on line ℓ_2 |
| 10 : $P_{30} = (11, 0, 1, 0)$ lies on line ℓ_1 | 29 : $P_{274} = (15, 15, 1, 0)$ lies on line ℓ_2 |
| 11 : $P_{31} = (12, 0, 1, 0)$ lies on line ℓ_1 | 30 : $P_{290} = (0, 1, 0, 1)$ lies on line ℓ_3 |
| 12 : $P_{32} = (13, 0, 1, 0)$ lies on line ℓ_1 | 31 : $P_{306} = (0, 2, 0, 1)$ lies on line ℓ_3 |
| 13 : $P_{33} = (14, 0, 1, 0)$ lies on line ℓ_1 | 32 : $P_{322} = (0, 3, 0, 1)$ lies on line ℓ_3 |
| 14 : $P_{34} = (15, 0, 1, 0)$ lies on line ℓ_1 | 33 : $P_{338} = (0, 4, 0, 1)$ lies on line ℓ_3 |
| 15 : $P_{36} = (1, 1, 1, 0)$ lies on line ℓ_2 | 34 : $P_{354} = (0, 5, 0, 1)$ lies on line ℓ_3 |
| 16 : $P_{53} = (2, 2, 1, 0)$ lies on line ℓ_2 | 35 : $P_{370} = (0, 6, 0, 1)$ lies on line ℓ_3 |
| 17 : $P_{70} = (3, 3, 1, 0)$ lies on line ℓ_2 | 36 : $P_{386} = (0, 7, 0, 1)$ lies on line ℓ_3 |
| 18 : $P_{87} = (4, 4, 1, 0)$ lies on line ℓ_2 | 37 : $P_{402} = (0, 8, 0, 1)$ lies on line ℓ_3 |

38 : $P_{418} = (0, 9, 0, 1)$ lies on line ℓ_3
 39 : $P_{434} = (0, 10, 0, 1)$ lies on line ℓ_3
 40 : $P_{450} = (0, 11, 0, 1)$ lies on line ℓ_3
 41 : $P_{466} = (0, 12, 0, 1)$ lies on line ℓ_3
 42 : $P_{482} = (0, 13, 0, 1)$ lies on line ℓ_3
 43 : $P_{498} = (0, 14, 0, 1)$ lies on line ℓ_3
 44 : $P_{514} = (0, 15, 0, 1)$ lies on line ℓ_3
 45 : $P_{555} = (10, 1, 1, 1)$ lies on line ℓ_{13}
 46 : $P_{556} = (11, 1, 1, 1)$ lies on line ℓ_{14}
 47 : $P_{574} = (13, 2, 1, 1)$ lies on line ℓ_{13}
 48 : $P_{576} = (15, 2, 1, 1)$ lies on line ℓ_{14}
 49 : $P_{581} = (4, 3, 1, 1)$ lies on line ℓ_{14}
 50 : $P_{584} = (7, 3, 1, 1)$ lies on line ℓ_{13}
 51 : $P_{596} = (3, 4, 1, 1)$ lies on line ℓ_{13}
 52 : $P_{600} = (7, 4, 1, 1)$ lies on line ℓ_{14}
 53 : $P_{618} = (9, 5, 1, 1)$ lies on line ℓ_{13}
 54 : $P_{621} = (12, 5, 1, 1)$ lies on line ℓ_{14}
 55 : $P_{633} = (8, 6, 1, 1)$ lies on line ℓ_{14}
 56 : $P_{639} = (14, 6, 1, 1)$ lies on line ℓ_{13}
 57 : $P_{644} = (3, 7, 1, 1)$ lies on line ℓ_{14}
 58 : $P_{645} = (4, 7, 1, 1)$ lies on line ℓ_{13}
 59 : $P_{663} = (6, 8, 1, 1)$ lies on line ℓ_{13}
 60 : $P_{671} = (14, 8, 1, 1)$ lies on line ℓ_{14}
 61 : $P_{678} = (5, 9, 1, 1)$ lies on line ℓ_{14}
 62 : $P_{685} = (12, 9, 1, 1)$ lies on line ℓ_{13}
 63 : $P_{690} = (1, 10, 1, 1)$ lies on line ℓ_{14}
 64 : $P_{700} = (11, 10, 1, 1)$ lies on line ℓ_{13}
 65 : $P_{706} = (1, 11, 1, 1)$ lies on line ℓ_{13}
 66 : $P_{715} = (10, 11, 1, 1)$ lies on line ℓ_{14}
 67 : $P_{726} = (5, 12, 1, 1)$ lies on line ℓ_{13}
 68 : $P_{730} = (9, 12, 1, 1)$ lies on line ℓ_{14}
 69 : $P_{739} = (2, 13, 1, 1)$ lies on line ℓ_{14}
 70 : $P_{752} = (15, 13, 1, 1)$ lies on line ℓ_{13}
 71 : $P_{759} = (6, 14, 1, 1)$ lies on line ℓ_{14}
 72 : $P_{761} = (8, 14, 1, 1)$ lies on line ℓ_{13}
 73 : $P_{771} = (2, 15, 1, 1)$ lies on line ℓ_{13}
 74 : $P_{782} = (13, 15, 1, 1)$ lies on line ℓ_{14}
 75 : $P_{806} = (5, 1, 2, 1)$ lies on line ℓ_8
 76 : $P_{808} = (7, 1, 2, 1)$ lies on line ℓ_{10}
 77 : $P_{827} = (10, 2, 2, 1)$ lies on line ℓ_8
 78 : $P_{831} = (14, 2, 2, 1)$ lies on line ℓ_{10}
 79 : $P_{842} = (9, 3, 2, 1)$ lies on line ℓ_{10}
 80 : $P_{848} = (15, 3, 2, 1)$ lies on line ℓ_8
 81 : $P_{854} = (5, 4, 2, 1)$ lies on line ℓ_{10}
 82 : $P_{862} = (13, 4, 2, 1)$ lies on line ℓ_8
 83 : $P_{867} = (2, 5, 2, 1)$ lies on line ℓ_{10}
 84 : $P_{873} = (8, 5, 2, 1)$ lies on line ℓ_8
 85 : $P_{888} = (7, 6, 2, 1)$ lies on line ℓ_8
 86 : $P_{892} = (11, 6, 2, 1)$ lies on line ℓ_{10}
 87 : $P_{899} = (2, 7, 2, 1)$ lies on line ℓ_8
 88 : $P_{909} = (12, 7, 2, 1)$ lies on line ℓ_{10}
 89 : $P_{916} = (3, 8, 2, 1)$ lies on line ℓ_8
 90 : $P_{923} = (10, 8, 2, 1)$ lies on line ℓ_{10}
 91 : $P_{935} = (6, 9, 2, 1)$ lies on line ℓ_8

92 : $P_{942} = (13, 9, 2, 1)$ lies on line ℓ_{10}
 93 : $P_{949} = (4, 10, 2, 1)$ lies on line ℓ_{10}
 94 : $P_{954} = (9, 10, 2, 1)$ lies on line ℓ_8
 95 : $P_{964} = (3, 11, 2, 1)$ lies on line ℓ_{10}
 96 : $P_{973} = (12, 11, 2, 1)$ lies on line ℓ_8
 97 : $P_{991} = (14, 12, 2, 1)$ lies on line ℓ_8
 98 : $P_{992} = (15, 12, 2, 1)$ lies on line ℓ_{10}
 99 : $P_{1001} = (8, 13, 2, 1)$ lies on line ℓ_{10}
 100 : $P_{1004} = (11, 13, 2, 1)$ lies on line ℓ_8
 101 : $P_{1010} = (1, 14, 2, 1)$ lies on line ℓ_{10}
 102 : $P_{1013} = (4, 14, 2, 1)$ lies on line ℓ_8
 103 : $P_{1026} = (1, 15, 2, 1)$ lies on line ℓ_8
 104 : $P_{1031} = (6, 15, 2, 1)$ lies on line ℓ_{10}
 105 : $P_{1041} = (0, 0, 3, 1)$ lies on line ℓ_4
 106 : $P_{1321} = (8, 1, 4, 1)$ lies on line ℓ_{11}
 107 : $P_{1325} = (12, 1, 4, 1)$ lies on line ℓ_{15}
 108 : $P_{1330} = (1, 2, 4, 1)$ lies on line ℓ_{15}
 109 : $P_{1338} = (9, 2, 4, 1)$ lies on line ℓ_{11}
 110 : $P_{1346} = (1, 3, 4, 1)$ lies on line ℓ_{11}
 111 : $P_{1358} = (13, 3, 4, 1)$ lies on line ℓ_{15}
 112 : $P_{1363} = (2, 4, 4, 1)$ lies on line ℓ_{15}
 113 : $P_{1372} = (11, 4, 4, 1)$ lies on line ℓ_{11}
 114 : $P_{1380} = (3, 5, 4, 1)$ lies on line ℓ_{11}
 115 : $P_{1391} = (14, 5, 4, 1)$ lies on line ℓ_{15}
 116 : $P_{1395} = (2, 6, 4, 1)$ lies on line ℓ_{11}
 117 : $P_{1396} = (3, 6, 4, 1)$ lies on line ℓ_{15}
 118 : $P_{1419} = (10, 7, 4, 1)$ lies on line ℓ_{11}
 119 : $P_{1424} = (15, 7, 4, 1)$ lies on line ℓ_{15}
 120 : $P_{1429} = (4, 8, 4, 1)$ lies on line ℓ_{15}
 121 : $P_{1440} = (15, 8, 4, 1)$ lies on line ℓ_{11}
 122 : $P_{1448} = (7, 9, 4, 1)$ lies on line ℓ_{11}
 123 : $P_{1449} = (8, 9, 4, 1)$ lies on line ℓ_{15}
 124 : $P_{1462} = (5, 10, 4, 1)$ lies on line ℓ_{15}
 125 : $P_{1463} = (6, 10, 4, 1)$ lies on line ℓ_{11}
 126 : $P_{1482} = (9, 11, 4, 1)$ lies on line ℓ_{15}
 127 : $P_{1487} = (14, 11, 4, 1)$ lies on line ℓ_{11}
 128 : $P_{1493} = (4, 12, 4, 1)$ lies on line ℓ_{11}
 129 : $P_{1495} = (6, 12, 4, 1)$ lies on line ℓ_{15}
 130 : $P_{1515} = (10, 13, 4, 1)$ lies on line ℓ_{15}
 131 : $P_{1517} = (12, 13, 4, 1)$ lies on line ℓ_{11}
 132 : $P_{1528} = (7, 14, 4, 1)$ lies on line ℓ_{15}
 133 : $P_{1534} = (13, 14, 4, 1)$ lies on line ℓ_{11}
 134 : $P_{1542} = (5, 15, 4, 1)$ lies on line ℓ_{11}
 135 : $P_{1548} = (11, 15, 4, 1)$ lies on line ℓ_{15}
 136 : $P_{1553} = (0, 0, 5, 1)$ lies on line ℓ_4
 137 : $P_{1809} = (0, 0, 6, 1)$ lies on line ℓ_4
 138 : $P_{2065} = (0, 0, 7, 1)$ lies on line ℓ_4
 139 : $P_{2321} = (0, 0, 8, 1)$ lies on line ℓ_4
 140 : $P_{2599} = (6, 1, 9, 1)$ lies on line ℓ_9
 141 : $P_{2608} = (15, 1, 9, 1)$ lies on line ℓ_{18}
 142 : $P_{2616} = (7, 2, 9, 1)$ lies on line ℓ_{18}
 143 : $P_{2621} = (12, 2, 9, 1)$ lies on line ℓ_9
 144 : $P_{2633} = (8, 3, 9, 1)$ lies on line ℓ_{18}
 145 : $P_{2635} = (10, 3, 9, 1)$ lies on line ℓ_9

146 : $P_{2642} = (1, 4, 9, 1)$ lies on line ℓ_9
 147 : $P_{2655} = (14, 4, 9, 1)$ lies on line ℓ_{18}
 148 : $P_{2658} = (1, 5, 9, 1)$ lies on line ℓ_{18}
 149 : $P_{2664} = (7, 5, 9, 1)$ lies on line ℓ_9
 150 : $P_{2682} = (9, 6, 9, 1)$ lies on line ℓ_{18}
 151 : $P_{2686} = (13, 6, 9, 1)$ lies on line ℓ_9
 152 : $P_{2695} = (6, 7, 9, 1)$ lies on line ℓ_{18}
 153 : $P_{2700} = (11, 7, 9, 1)$ lies on line ℓ_9
 154 : $P_{2707} = (2, 8, 9, 1)$ lies on line ℓ_9
 155 : $P_{2710} = (5, 8, 9, 1)$ lies on line ℓ_{18}
 156 : $P_{2725} = (4, 9, 9, 1)$ lies on line ℓ_9
 157 : $P_{2731} = (10, 9, 9, 1)$ lies on line ℓ_{18}
 158 : $P_{2739} = (2, 10, 9, 1)$ lies on line ℓ_{18}
 159 : $P_{2751} = (14, 10, 9, 1)$ lies on line ℓ_9
 160 : $P_{2761} = (8, 11, 9, 1)$ lies on line ℓ_9
 161 : $P_{2766} = (13, 11, 9, 1)$ lies on line ℓ_{18}
 162 : $P_{2772} = (3, 12, 9, 1)$ lies on line ℓ_9
 163 : $P_{2780} = (11, 12, 9, 1)$ lies on line ℓ_{18}
 164 : $P_{2789} = (4, 13, 9, 1)$ lies on line ℓ_{18}
 165 : $P_{2790} = (5, 13, 9, 1)$ lies on line ℓ_9
 166 : $P_{2813} = (12, 14, 9, 1)$ lies on line ℓ_{18}
 167 : $P_{2816} = (15, 14, 9, 1)$ lies on line ℓ_9
 168 : $P_{2820} = (3, 15, 9, 1)$ lies on line ℓ_{18}
 169 : $P_{2826} = (9, 15, 9, 1)$ lies on line ℓ_9
 170 : $P_{2853} = (4, 1, 10, 1)$ lies on line ℓ_7
 171 : $P_{2863} = (14, 1, 10, 1)$ lies on line ℓ_{17}
 172 : $P_{2870} = (5, 2, 10, 1)$ lies on line ℓ_{17}
 173 : $P_{2873} = (8, 2, 10, 1)$ lies on line ℓ_7
 174 : $P_{2892} = (11, 3, 10, 1)$ lies on line ℓ_{17}
 175 : $P_{2893} = (12, 3, 10, 1)$ lies on line ℓ_7
 176 : $P_{2906} = (9, 4, 10, 1)$ lies on line ℓ_7
 177 : $P_{2907} = (10, 4, 10, 1)$ lies on line ℓ_{17}
 178 : $P_{2917} = (4, 5, 10, 1)$ lies on line ℓ_{17}
 179 : $P_{2926} = (13, 5, 10, 1)$ lies on line ℓ_7
 180 : $P_{2930} = (1, 6, 10, 1)$ lies on line ℓ_7
 181 : $P_{2944} = (15, 6, 10, 1)$ lies on line ℓ_{17}
 182 : $P_{2946} = (1, 7, 10, 1)$ lies on line ℓ_{17}
 183 : $P_{2950} = (5, 7, 10, 1)$ lies on line ℓ_7
 184 : $P_{2972} = (11, 8, 10, 1)$ lies on line ℓ_7
 185 : $P_{2974} = (13, 8, 10, 1)$ lies on line ℓ_{17}
 186 : $P_{2980} = (3, 9, 10, 1)$ lies on line ℓ_{17}
 187 : $P_{2992} = (15, 9, 10, 1)$ lies on line ℓ_7
 188 : $P_{2996} = (3, 10, 10, 1)$ lies on line ℓ_7
 189 : $P_{3001} = (8, 10, 10, 1)$ lies on line ℓ_{17}
 190 : $P_{3015} = (6, 11, 10, 1)$ lies on line ℓ_{17}
 191 : $P_{3016} = (7, 11, 10, 1)$ lies on line ℓ_7
 192 : $P_{3027} = (2, 12, 10, 1)$ lies on line ℓ_7
 193 : $P_{3032} = (7, 12, 10, 1)$ lies on line ℓ_{17}
 194 : $P_{3047} = (6, 13, 10, 1)$ lies on line ℓ_7
 195 : $P_{3050} = (9, 13, 10, 1)$ lies on line ℓ_{17}
 196 : $P_{3059} = (2, 14, 10, 1)$ lies on line ℓ_{17}
 197 : $P_{3067} = (10, 14, 10, 1)$ lies on line ℓ_7
 198 : $P_{3085} = (12, 15, 10, 1)$ lies on line ℓ_{17}
 199 : $P_{3087} = (14, 15, 10, 1)$ lies on line ℓ_7

200 : $P_{3107} = (2, 1, 11, 1)$ lies on line ℓ_5
 201 : $P_{3114} = (9, 1, 11, 1)$ lies on line ℓ_{12}
 202 : $P_{3125} = (4, 2, 11, 1)$ lies on line ℓ_5
 203 : $P_{3132} = (11, 2, 11, 1)$ lies on line ℓ_{12}
 204 : $P_{3139} = (2, 3, 11, 1)$ lies on line ℓ_{12}
 205 : $P_{3143} = (6, 3, 11, 1)$ lies on line ℓ_5
 206 : $P_{3161} = (8, 4, 11, 1)$ lies on line ℓ_5
 207 : $P_{3168} = (15, 4, 11, 1)$ lies on line ℓ_{12}
 208 : $P_{3175} = (6, 5, 11, 1)$ lies on line ℓ_{12}
 209 : $P_{3179} = (10, 5, 11, 1)$ lies on line ℓ_5
 210 : $P_{3189} = (4, 6, 11, 1)$ lies on line ℓ_{12}
 211 : $P_{3197} = (12, 6, 11, 1)$ lies on line ℓ_5
 212 : $P_{3214} = (13, 7, 11, 1)$ lies on line ℓ_{12}
 213 : $P_{3215} = (14, 7, 11, 1)$ lies on line ℓ_5
 214 : $P_{3224} = (7, 8, 11, 1)$ lies on line ℓ_{12}
 215 : $P_{3226} = (9, 8, 11, 1)$ lies on line ℓ_5
 216 : $P_{3244} = (11, 9, 11, 1)$ lies on line ℓ_5
 217 : $P_{3247} = (14, 9, 11, 1)$ lies on line ℓ_{12}
 218 : $P_{3261} = (12, 10, 11, 1)$ lies on line ℓ_{12}
 219 : $P_{3262} = (13, 10, 11, 1)$ lies on line ℓ_5
 220 : $P_{3270} = (5, 11, 11, 1)$ lies on line ℓ_{12}
 221 : $P_{3280} = (15, 11, 11, 1)$ lies on line ℓ_5
 222 : $P_{3282} = (1, 12, 11, 1)$ lies on line ℓ_5
 223 : $P_{3289} = (8, 12, 11, 1)$ lies on line ℓ_{12}
 224 : $P_{3298} = (1, 13, 11, 1)$ lies on line ℓ_{12}
 225 : $P_{3300} = (3, 13, 11, 1)$ lies on line ℓ_5
 226 : $P_{3316} = (3, 14, 11, 1)$ lies on line ℓ_{12}
 227 : $P_{3318} = (5, 14, 11, 1)$ lies on line ℓ_5
 228 : $P_{3336} = (7, 15, 11, 1)$ lies on line ℓ_5
 229 : $P_{3339} = (10, 15, 11, 1)$ lies on line ℓ_{12}
 230 : $P_{3345} = (0, 0, 12, 1)$ lies on line ℓ_4
 231 : $P_{3601} = (0, 0, 13, 1)$ lies on line ℓ_4
 232 : $P_{3876} = (3, 1, 14, 1)$ lies on line ℓ_6
 233 : $P_{3886} = (13, 1, 14, 1)$ lies on line ℓ_{16}
 234 : $P_{3892} = (3, 2, 14, 1)$ lies on line ℓ_{16}
 235 : $P_{3895} = (6, 2, 14, 1)$ lies on line ℓ_6
 236 : $P_{3910} = (5, 3, 14, 1)$ lies on line ℓ_6
 237 : $P_{3919} = (14, 3, 14, 1)$ lies on line ℓ_{16}
 238 : $P_{3927} = (6, 4, 14, 1)$ lies on line ℓ_{16}
 239 : $P_{3933} = (12, 4, 14, 1)$ lies on line ℓ_6
 240 : $P_{3948} = (11, 5, 14, 1)$ lies on line ℓ_{16}
 241 : $P_{3952} = (15, 5, 14, 1)$ lies on line ℓ_6
 242 : $P_{3958} = (5, 6, 14, 1)$ lies on line ℓ_{16}
 243 : $P_{3963} = (10, 6, 14, 1)$ lies on line ℓ_6
 244 : $P_{3977} = (8, 7, 14, 1)$ lies on line ℓ_{16}
 245 : $P_{3978} = (9, 7, 14, 1)$ lies on line ℓ_6
 246 : $P_{3986} = (1, 8, 14, 1)$ lies on line ℓ_6
 247 : $P_{3997} = (12, 8, 14, 1)$ lies on line ℓ_{16}
 248 : $P_{4002} = (1, 9, 14, 1)$ lies on line ℓ_{16}
 249 : $P_{4003} = (2, 9, 14, 1)$ lies on line ℓ_6
 250 : $P_{4024} = (7, 10, 14, 1)$ lies on line ℓ_6
 251 : $P_{4032} = (15, 10, 14, 1)$ lies on line ℓ_{16}
 252 : $P_{4035} = (2, 11, 14, 1)$ lies on line ℓ_{16}
 253 : $P_{4037} = (4, 11, 14, 1)$ lies on line ℓ_6

254 : $P_{4059} = (10, 12, 14, 1)$ lies on line ℓ_{16}
 255 : $P_{4062} = (13, 12, 14, 1)$ lies on line ℓ_6
 256 : $P_{4072} = (7, 13, 14, 1)$ lies on line ℓ_{16}
 257 : $P_{4079} = (14, 13, 14, 1)$ lies on line ℓ_6
 258 : $P_{4090} = (9, 14, 14, 1)$ lies on line ℓ_{16}

259 : $P_{4092} = (11, 14, 14, 1)$ lies on line ℓ_6
 260 : $P_{4101} = (4, 15, 14, 1)$ lies on line ℓ_{16}
 261 : $P_{4105} = (8, 15, 14, 1)$ lies on line ℓ_6
 262 : $P_{4113} = (0, 0, 15, 1)$ lies on line ℓ_4

The single points on the surface are:

Points on surface but on no line

The surface has 0 points not on any line:

The points on the surface but not on lines are:

Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
0	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	1	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
5	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0
7	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1	0	0
8	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
9	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1
10	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
11	1	0	0	0	1	0	0	0	0	0	0	0	0	0	1	0	0	0	0
12	1	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0
13	1	0	0	0	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0
14	1	0	0	0	1	0	0	0	0	0	0	0	1	0	0	0	0	0	0
15	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
16	1	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0
17	1	0	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0
18	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}
in point	P_0	P_5	P_1	P_6	P_7	P_8	P_9	P_{10}	P_{11}	P_{12}	P_{13}	P_{14}	P_{15}	P_{16}	P_{17}	P_{18}	P_{19}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_4
in point	P_0	P_2	P_2

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_4
in point	P_5	P_2	P_2

Line 3 intersects

Line	ℓ_0	ℓ_4
in point	P_1	P_3

Line 4 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}
in point	P_2	P_2	P_3	P_{3089}	P_{3857}	P_{2833}	P_{785}	P_{2577}	P_{785}	P_{1297}	P_{3089}	P_{530}	P_{530}	P_{1297}	P_{3857}	P_{2833}	P_{2833}

Line 5 intersects

Line	ℓ_0	ℓ_4	ℓ_{12}
in point	P_6	P_{3089}	P_{3089}

Line 6 intersects

Line	ℓ_0	ℓ_4	ℓ_{16}
in point	P_7	P_{3857}	P_{3857}

Line 7 intersects

Line	ℓ_0	ℓ_4	ℓ_{17}
in point	P_8	P_{2833}	P_{2833}

Line 8 intersects

Line	ℓ_0	ℓ_4	ℓ_{10}
in point	P_9	P_{785}	P_{785}

Line 9 intersects

Line	ℓ_0	ℓ_4	ℓ_{18}
in point	P_{10}	P_{2577}	P_{2577}

Line 10 intersects

Line	ℓ_0	ℓ_4	ℓ_8
in point	P_{11}	P_{785}	P_{785}

Line 11 intersects

Line	ℓ_0	ℓ_4	ℓ_{15}
in point	P_{12}	P_{1297}	P_{1297}

Line 12 intersects

Line	ℓ_0	ℓ_4	ℓ_5
in point	P_{13}	P_{3089}	P_{3089}

Line 13 intersects

Line	ℓ_0	ℓ_4	ℓ_{14}
in point	P_{14}	P_{530}	P_{530}

Line 14 intersects

Line	ℓ_0	ℓ_4	ℓ_{13}
in point	P_{15}	P_{530}	P_{530}

Line 15 intersects

Line	ℓ_0	ℓ_4	ℓ_{11}
in point	P_{16}	P_{1297}	P_{1297}

Line 16 intersects

Line	ℓ_0	ℓ_4	ℓ_6
in point	P_{17}	P_{3857}	P_{3857}

Line 17 intersects

Line	ℓ_0	ℓ_4	ℓ_7
in point	P_{18}	P_{2833}	P_{2833}

Line 18 intersects

Line	ℓ_0	ℓ_4	ℓ_9
in point	P_{19}	P_{2577}	P_{2577}

The surface has 289 points:

The points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$	54 : $P_{370} = (0, 6, 0, 1)$	108 : $P_{899} = (2, 7, 2, 1)$
1 : $P_1 = (0, 1, 0, 0)$	55 : $P_{386} = (0, 7, 0, 1)$	109 : $P_{909} = (12, 7, 2, 1)$
2 : $P_2 = (0, 0, 1, 0)$	56 : $P_{402} = (0, 8, 0, 1)$	110 : $P_{916} = (3, 8, 2, 1)$
3 : $P_3 = (0, 0, 0, 1)$	57 : $P_{418} = (0, 9, 0, 1)$	111 : $P_{923} = (10, 8, 2, 1)$
4 : $P_5 = (1, 1, 0, 0)$	58 : $P_{434} = (0, 10, 0, 1)$	112 : $P_{935} = (6, 9, 2, 1)$
5 : $P_6 = (2, 1, 0, 0)$	59 : $P_{450} = (0, 11, 0, 1)$	113 : $P_{942} = (13, 9, 2, 1)$
6 : $P_7 = (3, 1, 0, 0)$	60 : $P_{466} = (0, 12, 0, 1)$	114 : $P_{949} = (4, 10, 2, 1)$
7 : $P_8 = (4, 1, 0, 0)$	61 : $P_{482} = (0, 13, 0, 1)$	115 : $P_{954} = (9, 10, 2, 1)$
8 : $P_9 = (5, 1, 0, 0)$	62 : $P_{498} = (0, 14, 0, 1)$	116 : $P_{964} = (3, 11, 2, 1)$
9 : $P_{10} = (6, 1, 0, 0)$	63 : $P_{514} = (0, 15, 0, 1)$	117 : $P_{973} = (12, 11, 2, 1)$
10 : $P_{11} = (7, 1, 0, 0)$	64 : $P_{530} = (0, 0, 1, 1)$	118 : $P_{991} = (14, 12, 2, 1)$
11 : $P_{12} = (8, 1, 0, 0)$	65 : $P_{555} = (10, 1, 1, 1)$	119 : $P_{992} = (15, 12, 2, 1)$
12 : $P_{13} = (9, 1, 0, 0)$	66 : $P_{556} = (11, 1, 1, 1)$	120 : $P_{1001} = (8, 13, 2, 1)$
13 : $P_{14} = (10, 1, 0, 0)$	67 : $P_{574} = (13, 2, 1, 1)$	121 : $P_{1004} = (11, 13, 2, 1)$
14 : $P_{15} = (11, 1, 0, 0)$	68 : $P_{576} = (15, 2, 1, 1)$	122 : $P_{1010} = (1, 14, 2, 1)$
15 : $P_{16} = (12, 1, 0, 0)$	69 : $P_{581} = (4, 3, 1, 1)$	123 : $P_{1013} = (4, 14, 2, 1)$
16 : $P_{17} = (13, 1, 0, 0)$	70 : $P_{584} = (7, 3, 1, 1)$	124 : $P_{1026} = (1, 15, 2, 1)$
17 : $P_{18} = (14, 1, 0, 0)$	71 : $P_{596} = (3, 4, 1, 1)$	125 : $P_{1031} = (6, 15, 2, 1)$
18 : $P_{19} = (15, 1, 0, 0)$	72 : $P_{600} = (7, 4, 1, 1)$	126 : $P_{1041} = (0, 0, 3, 1)$
19 : $P_{20} = (1, 0, 1, 0)$	73 : $P_{618} = (9, 5, 1, 1)$	127 : $P_{1297} = (0, 0, 4, 1)$
20 : $P_{21} = (2, 0, 1, 0)$	74 : $P_{621} = (12, 5, 1, 1)$	128 : $P_{1321} = (8, 1, 4, 1)$
21 : $P_{22} = (3, 0, 1, 0)$	75 : $P_{633} = (8, 6, 1, 1)$	129 : $P_{1325} = (12, 1, 4, 1)$
22 : $P_{23} = (4, 0, 1, 0)$	76 : $P_{639} = (14, 6, 1, 1)$	130 : $P_{1330} = (1, 2, 4, 1)$
23 : $P_{24} = (5, 0, 1, 0)$	77 : $P_{644} = (3, 7, 1, 1)$	131 : $P_{1338} = (9, 2, 4, 1)$
24 : $P_{25} = (6, 0, 1, 0)$	78 : $P_{645} = (4, 7, 1, 1)$	132 : $P_{1346} = (1, 3, 4, 1)$
25 : $P_{26} = (7, 0, 1, 0)$	79 : $P_{663} = (6, 8, 1, 1)$	133 : $P_{1358} = (13, 3, 4, 1)$
26 : $P_{27} = (8, 0, 1, 0)$	80 : $P_{671} = (14, 8, 1, 1)$	134 : $P_{1363} = (2, 4, 4, 1)$
27 : $P_{28} = (9, 0, 1, 0)$	81 : $P_{678} = (5, 9, 1, 1)$	135 : $P_{1372} = (11, 4, 4, 1)$
28 : $P_{29} = (10, 0, 1, 0)$	82 : $P_{685} = (12, 9, 1, 1)$	136 : $P_{1380} = (3, 5, 4, 1)$
29 : $P_{30} = (11, 0, 1, 0)$	83 : $P_{690} = (1, 10, 1, 1)$	137 : $P_{1391} = (14, 5, 4, 1)$
30 : $P_{31} = (12, 0, 1, 0)$	84 : $P_{700} = (11, 10, 1, 1)$	138 : $P_{1395} = (2, 6, 4, 1)$
31 : $P_{32} = (13, 0, 1, 0)$	85 : $P_{706} = (1, 11, 1, 1)$	139 : $P_{1396} = (3, 6, 4, 1)$
32 : $P_{33} = (14, 0, 1, 0)$	86 : $P_{715} = (10, 11, 1, 1)$	140 : $P_{1419} = (10, 7, 4, 1)$
33 : $P_{34} = (15, 0, 1, 0)$	87 : $P_{726} = (5, 12, 1, 1)$	141 : $P_{1424} = (15, 7, 4, 1)$
34 : $P_{36} = (1, 1, 1, 0)$	88 : $P_{730} = (9, 12, 1, 1)$	142 : $P_{1429} = (4, 8, 4, 1)$
35 : $P_{53} = (2, 2, 1, 0)$	89 : $P_{739} = (2, 13, 1, 1)$	143 : $P_{1440} = (15, 8, 4, 1)$
36 : $P_{70} = (3, 3, 1, 0)$	90 : $P_{752} = (15, 13, 1, 1)$	144 : $P_{1448} = (7, 9, 4, 1)$
37 : $P_{87} = (4, 4, 1, 0)$	91 : $P_{759} = (6, 14, 1, 1)$	145 : $P_{1449} = (8, 9, 4, 1)$
38 : $P_{104} = (5, 5, 1, 0)$	92 : $P_{761} = (8, 14, 1, 1)$	146 : $P_{1462} = (5, 10, 4, 1)$
39 : $P_{121} = (6, 6, 1, 0)$	93 : $P_{771} = (2, 15, 1, 1)$	147 : $P_{1463} = (6, 10, 4, 1)$
40 : $P_{138} = (7, 7, 1, 0)$	94 : $P_{782} = (13, 15, 1, 1)$	148 : $P_{1482} = (9, 11, 4, 1)$
41 : $P_{155} = (8, 8, 1, 0)$	95 : $P_{785} = (0, 0, 2, 1)$	149 : $P_{1487} = (14, 11, 4, 1)$
42 : $P_{172} = (9, 9, 1, 0)$	96 : $P_{806} = (5, 1, 2, 1)$	150 : $P_{1493} = (4, 12, 4, 1)$
43 : $P_{189} = (10, 10, 1, 0)$	97 : $P_{808} = (7, 1, 2, 1)$	151 : $P_{1495} = (6, 12, 4, 1)$
44 : $P_{206} = (11, 11, 1, 0)$	98 : $P_{827} = (10, 2, 2, 1)$	152 : $P_{1515} = (10, 13, 4, 1)$
45 : $P_{223} = (12, 12, 1, 0)$	99 : $P_{831} = (14, 2, 2, 1)$	153 : $P_{1517} = (12, 13, 4, 1)$
46 : $P_{240} = (13, 13, 1, 0)$	100 : $P_{842} = (9, 3, 2, 1)$	154 : $P_{1528} = (7, 14, 4, 1)$
47 : $P_{257} = (14, 14, 1, 0)$	101 : $P_{848} = (15, 3, 2, 1)$	155 : $P_{1534} = (13, 14, 4, 1)$
48 : $P_{274} = (15, 15, 1, 0)$	102 : $P_{854} = (5, 4, 2, 1)$	156 : $P_{1542} = (5, 15, 4, 1)$
49 : $P_{290} = (0, 1, 0, 1)$	103 : $P_{862} = (13, 4, 2, 1)$	157 : $P_{1548} = (11, 15, 4, 1)$
50 : $P_{306} = (0, 2, 0, 1)$	104 : $P_{867} = (2, 5, 2, 1)$	158 : $P_{1553} = (0, 0, 5, 1)$
51 : $P_{322} = (0, 3, 0, 1)$	105 : $P_{873} = (8, 5, 2, 1)$	159 : $P_{1809} = (0, 0, 6, 1)$
52 : $P_{338} = (0, 4, 0, 1)$	106 : $P_{888} = (7, 6, 2, 1)$	160 : $P_{2065} = (0, 0, 7, 1)$
53 : $P_{354} = (0, 5, 0, 1)$	107 : $P_{892} = (11, 6, 2, 1)$	161 : $P_{2321} = (0, 0, 8, 1)$

162 : $P_{2577} = (0, 0, 9, 1)$	205 : $P_{2944} = (15, 6, 10, 1)$	248 : $P_{3289} = (8, 12, 11, 1)$
163 : $P_{2599} = (6, 1, 9, 1)$	206 : $P_{2946} = (1, 7, 10, 1)$	249 : $P_{3298} = (1, 13, 11, 1)$
164 : $P_{2608} = (15, 1, 9, 1)$	207 : $P_{2950} = (5, 7, 10, 1)$	250 : $P_{3300} = (3, 13, 11, 1)$
165 : $P_{2616} = (7, 2, 9, 1)$	208 : $P_{2972} = (11, 8, 10, 1)$	251 : $P_{3316} = (3, 14, 11, 1)$
166 : $P_{2621} = (12, 2, 9, 1)$	209 : $P_{2974} = (13, 8, 10, 1)$	252 : $P_{3318} = (5, 14, 11, 1)$
167 : $P_{2633} = (8, 3, 9, 1)$	210 : $P_{2980} = (3, 9, 10, 1)$	253 : $P_{3336} = (7, 15, 11, 1)$
168 : $P_{2635} = (10, 3, 9, 1)$	211 : $P_{2992} = (15, 9, 10, 1)$	254 : $P_{3339} = (10, 15, 11, 1)$
169 : $P_{2642} = (1, 4, 9, 1)$	212 : $P_{2996} = (3, 10, 10, 1)$	255 : $P_{3345} = (0, 0, 12, 1)$
170 : $P_{2655} = (14, 4, 9, 1)$	213 : $P_{3001} = (8, 10, 10, 1)$	256 : $P_{3601} = (0, 0, 13, 1)$
171 : $P_{2658} = (1, 5, 9, 1)$	214 : $P_{3015} = (6, 11, 10, 1)$	257 : $P_{3857} = (0, 0, 14, 1)$
172 : $P_{2664} = (7, 5, 9, 1)$	215 : $P_{3016} = (7, 11, 10, 1)$	258 : $P_{3876} = (3, 1, 14, 1)$
173 : $P_{2682} = (9, 6, 9, 1)$	216 : $P_{3027} = (2, 12, 10, 1)$	259 : $P_{3886} = (13, 1, 14, 1)$
174 : $P_{2686} = (13, 6, 9, 1)$	217 : $P_{3032} = (7, 12, 10, 1)$	260 : $P_{3892} = (3, 2, 14, 1)$
175 : $P_{2695} = (6, 7, 9, 1)$	218 : $P_{3047} = (6, 13, 10, 1)$	261 : $P_{3895} = (6, 2, 14, 1)$
176 : $P_{2700} = (11, 7, 9, 1)$	219 : $P_{3050} = (9, 13, 10, 1)$	262 : $P_{3910} = (5, 3, 14, 1)$
177 : $P_{2707} = (2, 8, 9, 1)$	220 : $P_{3059} = (2, 14, 10, 1)$	263 : $P_{3919} = (14, 3, 14, 1)$
178 : $P_{2710} = (5, 8, 9, 1)$	221 : $P_{3067} = (10, 14, 10, 1)$	264 : $P_{3927} = (6, 4, 14, 1)$
179 : $P_{2725} = (4, 9, 9, 1)$	222 : $P_{3085} = (12, 15, 10, 1)$	265 : $P_{3933} = (12, 4, 14, 1)$
180 : $P_{2731} = (10, 9, 9, 1)$	223 : $P_{3087} = (14, 15, 10, 1)$	266 : $P_{3948} = (11, 5, 14, 1)$
181 : $P_{2739} = (2, 10, 9, 1)$	224 : $P_{3089} = (0, 0, 11, 1)$	267 : $P_{3952} = (15, 5, 14, 1)$
182 : $P_{2751} = (14, 10, 9, 1)$	225 : $P_{3107} = (2, 1, 11, 1)$	268 : $P_{3958} = (5, 6, 14, 1)$
183 : $P_{2761} = (8, 11, 9, 1)$	226 : $P_{3114} = (9, 1, 11, 1)$	269 : $P_{3963} = (10, 6, 14, 1)$
184 : $P_{2766} = (13, 11, 9, 1)$	227 : $P_{3125} = (4, 2, 11, 1)$	270 : $P_{3977} = (8, 7, 14, 1)$
185 : $P_{2772} = (3, 12, 9, 1)$	228 : $P_{3132} = (11, 2, 11, 1)$	271 : $P_{3978} = (9, 7, 14, 1)$
186 : $P_{2780} = (11, 12, 9, 1)$	229 : $P_{3139} = (2, 3, 11, 1)$	272 : $P_{3986} = (1, 8, 14, 1)$
187 : $P_{2789} = (4, 13, 9, 1)$	230 : $P_{3143} = (6, 3, 11, 1)$	273 : $P_{3997} = (12, 8, 14, 1)$
188 : $P_{2790} = (5, 13, 9, 1)$	231 : $P_{3161} = (8, 4, 11, 1)$	274 : $P_{4002} = (1, 9, 14, 1)$
189 : $P_{2813} = (12, 14, 9, 1)$	232 : $P_{3168} = (15, 4, 11, 1)$	275 : $P_{4003} = (2, 9, 14, 1)$
190 : $P_{2816} = (15, 14, 9, 1)$	233 : $P_{3175} = (6, 5, 11, 1)$	276 : $P_{4024} = (7, 10, 14, 1)$
191 : $P_{2820} = (3, 15, 9, 1)$	234 : $P_{3179} = (10, 5, 11, 1)$	277 : $P_{4032} = (15, 10, 14, 1)$
192 : $P_{2826} = (9, 15, 9, 1)$	235 : $P_{3189} = (4, 6, 11, 1)$	278 : $P_{4035} = (2, 11, 14, 1)$
193 : $P_{2833} = (0, 0, 10, 1)$	236 : $P_{3197} = (12, 6, 11, 1)$	279 : $P_{4037} = (4, 11, 14, 1)$
194 : $P_{2853} = (4, 1, 10, 1)$	237 : $P_{3214} = (13, 7, 11, 1)$	280 : $P_{4059} = (10, 12, 14, 1)$
195 : $P_{2863} = (14, 1, 10, 1)$	238 : $P_{3215} = (14, 7, 11, 1)$	281 : $P_{4062} = (13, 12, 14, 1)$
196 : $P_{2870} = (5, 2, 10, 1)$	239 : $P_{3224} = (7, 8, 11, 1)$	282 : $P_{4072} = (7, 13, 14, 1)$
197 : $P_{2873} = (8, 2, 10, 1)$	240 : $P_{3226} = (9, 8, 11, 1)$	283 : $P_{4079} = (14, 13, 14, 1)$
198 : $P_{2892} = (11, 3, 10, 1)$	241 : $P_{3244} = (11, 9, 11, 1)$	284 : $P_{4090} = (9, 14, 14, 1)$
199 : $P_{2893} = (12, 3, 10, 1)$	242 : $P_{3247} = (14, 9, 11, 1)$	285 : $P_{4092} = (11, 14, 14, 1)$
200 : $P_{2906} = (9, 4, 10, 1)$	243 : $P_{3261} = (12, 10, 11, 1)$	286 : $P_{4101} = (4, 15, 14, 1)$
201 : $P_{2907} = (10, 4, 10, 1)$	244 : $P_{3262} = (13, 10, 11, 1)$	287 : $P_{4105} = (8, 15, 14, 1)$
202 : $P_{2917} = (4, 5, 10, 1)$	245 : $P_{3270} = (5, 11, 11, 1)$	288 : $P_{4113} = (0, 0, 15, 1)$
203 : $P_{2926} = (13, 5, 10, 1)$	246 : $P_{3280} = (15, 11, 11, 1)$	
204 : $P_{2930} = (1, 6, 10, 1)$	247 : $P_{3282} = (1, 12, 11, 1)$	