Rank-67115 over GF(64)

January 15, 2021

The equation

The equation of the surface is:

$$X_3^3 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_2^2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over $\mathrm{GF}(64)$ is -2130177979

General information

Number of lines	12
Number of points	4353
Number of singular points	3
Number of Eckardt points	0
Number of double points	18
Number of single points	732
Number of points off lines	3600
Number of Hesse planes	0
Number of axes	0
Type of points on lines	65^{12}
Type of lines on points	$4^3, 2^{18}, 1^{732}, 0^{3600}$

Singular Points

The surface has 3 singular points:

$$0: P_{4226} = \mathbf{P}(0,1,0,1) = \mathbf{P}(0,1,0,1) \\ 1: P_{4227} = \mathbf{P}(1,1,0,1) = \mathbf{P}(1,1,0,1)$$

The 12 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4162} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4162} = \mathbf{Pl}(1,0,1,0,0,1)_{270529}$$

$$\ell_2 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{17043456} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{17043456} = \mathbf{Pl}(0,0,0,0,0,1)_{270401}$$

$$\ell_3 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{64} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{64} = \mathbf{Pl}(1,0,0,0,1,0)_{4226}$$

$$\ell_4 = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{17043521} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{17043521} = \mathbf{Pl}(0,1,0,0,0,1)_{270465}$$

$$\ell_5 = \begin{bmatrix} 1 & 0 & \epsilon^{21} & \epsilon^{21} \\ 0 & 1 & 1 & 1 \end{bmatrix}_{15416570} = \begin{bmatrix} 1 & 0 & 57 & 57 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{15416570} = \mathbf{Pl}(1,0,1,1,56,1)_{14958979}$$

$$\ell_6 = \begin{bmatrix} 1 & 0 & \epsilon^{42} & \epsilon^{42} \\ 0 & 1 & 1 & 1 \end{bmatrix}_{15146105} = \begin{bmatrix} 1 & 0 & 56 & 56 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{15146105} = \mathbf{Pl}(1,0,1,1,57,1)_{15221059}$$

$$\ell_7 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{4226} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{4226} = \mathbf{Pl}(1,1,1,0,1,1)_{536640}$$

$$\ell_8 = \begin{bmatrix} 1 & 0 & \epsilon^{21} & 1 \\ 0 & 1 & \epsilon^{21} & 0 \end{bmatrix}_{503538} = \begin{bmatrix} 1 & 0 & 57 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{503538} = \mathbf{Pl}(1,1,1,56,0,1)_{504825}$$

$$\ell_9 = \begin{bmatrix} 1 & 0 & \epsilon^{42} & \epsilon^{21} \\ 0 & 1 & 0 & 1 \end{bmatrix}_{15412408} = \begin{bmatrix} 1 & 0 & 56 & 57 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{15412408} = \mathbf{Pl}(1,1,1,57,0,1)_{508794}$$

$$\ell_{10} = \begin{bmatrix} 1 & 0 & \epsilon^{42} & \epsilon^{21} \\ 0 & 1 & \epsilon^{42} & 0 \end{bmatrix}_{499376} = \begin{bmatrix} 1 & 0 & 57 & 56 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{15150265} = \mathbf{Pl}(1,1,0,57,56,1)_{14958537}$$

Rank of lines: (0, 4162, 17043456, 64, 17043521, 15416570, 15146105, 4226, 503538, 15412408, 499376, 15150265)

Rank of points on Klein quadric: (0, 270529, 270401, 4226, 270465, 14958979, 15221059, 536640, 504825, 15220554, 508794, 14958537)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 18 Double points: The double points on the surface are:

$$\begin{array}{lll} P_5 = (1,1,0,0) = \ell_0 \cap \ell_1 & P_{3651} = (0,56,1,0) = \ell_2 \cap \ell_8 \\ P_1 = (0,1,0,0) = \ell_0 \cap \ell_2 & P_{3715} = (0,57,1,0) = \ell_2 \cap \ell_{10} \\ P_0 = (1,0,0,0) = \ell_0 \cap \ell_3 & P_{11962} = (57,57,1,1) = \ell_5 \cap \ell_9 \\ P_{60} = (56,1,0,0) = \ell_0 \cap \ell_5 & P_{11842} = (1,56,1,1) = \ell_5 \cap \ell_{10} \\ P_{61} = (57,1,0,0) = \ell_0 \cap \ell_6 & P_{11906} = (1,57,1,1) = \ell_6 \cap \ell_8 \\ P_{131} = (0,1,1,0) = \ell_1 \cap \ell_2 & P_{11897} = (56,56,1,1) = \ell_6 \cap \ell_{11} \\ P_{68} = (1,0,1,0) = \ell_1 \cap \ell_7 & P_{237122} = (1,56,56,1) = \ell_8 \cap \ell_9 \\ P_{3708} = (57,56,1,0) = \ell_1 \cap \ell_9 & P_{241282} = (1,57,57,1) = \ell_{10} \cap \ell_{11} \\ P_2 = (0,0,1,0) = \ell_2 \cap \ell_4 & P_{241282} = (1,57,57,1) = \ell_{10} \cap \ell_{11} \end{array}$$

Single Points

The surface has 732 single points: The single points on the surface are:

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0: P_6 = (2, 1, 0, 0) lies on line \ell_0
                                                                      48: P_{54} = (50, 1, 0, 0) lies on line \ell_0
1: P_7 = (3, 1, 0, 0) lies on line \ell_0
                                                                       49: P_{55} = (51, 1, 0, 0) lies on line \ell_0
2: P_8 = (4, 1, 0, 0) lies on line \ell_0
                                                                      50: P_{56} = (52, 1, 0, 0) lies on line \ell_0
3: P_9 = (5, 1, 0, 0) lies on line \ell_0
                                                                      51: P_{57} = (53, 1, 0, 0) lies on line \ell_0
4: P_{10} = (6, 1, 0, 0) lies on line \ell_0
                                                                      52: P_{58} = (54, 1, 0, 0) lies on line \ell_0
5: P_{11} = (7, 1, 0, 0) lies on line \ell_0
                                                                      53: P_{59} = (55, 1, 0, 0) lies on line \ell_0
6: P_{12} = (8, 1, 0, 0) lies on line \ell_0
                                                                      54: P_{62} = (58, 1, 0, 0) lies on line \ell_0
7: P_{13} = (9, 1, 0, 0) lies on line \ell_0
                                                                      55: P_{63} = (59, 1, 0, 0) lies on line \ell_0
8: P_{14} = (10, 1, 0, 0) lies on line \ell_0
                                                                      56: P_{64} = (60, 1, 0, 0) lies on line \ell_0
9: P_{15} = (11, 1, 0, 0) lies on line \ell_0
                                                                      57: P_{65} = (61, 1, 0, 0) lies on line \ell_0
10: P_{16} = (12, 1, 0, 0) lies on line \ell_0
                                                                      58: P_{66} = (62, 1, 0, 0) lies on line \ell_0
11: P_{17} = (13, 1, 0, 0) lies on line \ell_0
                                                                      59: P_{67} = (63, 1, 0, 0) lies on line \ell_0
12: P_{18} = (14, 1, 0, 0) lies on line \ell_0
                                                                      60: P_{195} = (0, 2, 1, 0) lies on line \ell_2
13: P_{19} = (15, 1, 0, 0) lies on line \ell_0
                                                                      61: P_{198} = (3, 2, 1, 0) lies on line \ell_1
14: P_{20} = (16, 1, 0, 0) lies on line \ell_0
                                                                      62: P_{259} = (0, 3, 1, 0) lies on line \ell_2
15: P_{21} = (17, 1, 0, 0) lies on line \ell_0
                                                                      63: P_{261} = (2, 3, 1, 0) lies on line \ell_1
16: P_{22} = (18, 1, 0, 0) lies on line \ell_0
                                                                      64: P_{323} = (0, 4, 1, 0) lies on line \ell_2
17: P_{23} = (19, 1, 0, 0) lies on line \ell_0
                                                                      65: P_{328} = (5, 4, 1, 0) lies on line \ell_1
18 : P_{24} = (20, 1, 0, 0) lies on line \ell_0
                                                                      66: P_{387} = (0, 5, 1, 0) lies on line \ell_2
19: P_{25} = (21, 1, 0, 0) lies on line \ell_0
                                                                      67: P_{391} = (4, 5, 1, 0) lies on line \ell_1
20: P_{26} = (22, 1, 0, 0) lies on line \ell_0
                                                                       68: P_{451} = (0, 6, 1, 0) lies on line \ell_2
                                                                      69 : P_{458} = (7, 6, 1, 0) lies on line \ell_1
21: P_{27} = (23, 1, 0, 0) lies on line \ell_0
22: P_{28} = (24, 1, 0, 0) lies on line \ell_0
                                                                       70: P_{515} = (0, 7, 1, 0) lies on line \ell_2
23: P_{29} = (25, 1, 0, 0) lies on line \ell_0
                                                                       71 : P_{521} = (6,7,1,0) lies on line \ell_1
24: P_{30} = (26, 1, 0, 0) lies on line \ell_0
                                                                       72: P_{579} = (0, 8, 1, 0) lies on line \ell_2
25: P_{31} = (27, 1, 0, 0) lies on line \ell_0
                                                                      73: P_{588} = (9, 8, 1, 0) lies on line \ell_1
26: P_{32} = (28, 1, 0, 0) lies on line \ell_0
                                                                       74: P_{643} = (0, 9, 1, 0) lies on line \ell_2
27: P_{33} = (29, 1, 0, 0) lies on line \ell_0
                                                                       75: P_{651} = (8, 9, 1, 0) lies on line \ell_1
28: P_{34} = (30, 1, 0, 0) lies on line \ell_0
                                                                       76 : P_{707} = (0, 10, 1, 0) lies on line \ell_2
29: P_{35} = (31, 1, 0, 0) lies on line \ell_0
                                                                      77: P_{718} = (11, 10, 1, 0) lies on line \ell_1
30: P_{36} = (32, 1, 0, 0) lies on line \ell_0
                                                                       78: P_{771} = (0, 11, 1, 0) lies on line \ell_2
31: P_{37} = (33, 1, 0, 0) lies on line \ell_0
                                                                       79: P_{781} = (10, 11, 1, 0) lies on line \ell_1
32 : P_{38} = (34, 1, 0, 0) lies on line \ell_0
                                                                      80: P_{835} = (0, 12, 1, 0) lies on line \ell_2
33 : P_{39} = (35, 1, 0, 0) lies on line \ell_0
                                                                      81: P_{848} = (13, 12, 1, 0) lies on line \ell_1
34: P_{40} = (36, 1, 0, 0) lies on line \ell_0
                                                                      82: P_{899} = (0, 13, 1, 0) lies on line \ell_2
35: P_{41} = (37, 1, 0, 0) lies on line \ell_0
                                                                      83: P_{911} = (12, 13, 1, 0) lies on line \ell_1
36: P_{42} = (38, 1, 0, 0) lies on line \ell_0
                                                                      84: P_{963} = (0, 14, 1, 0) lies on line \ell_2
37: P_{43} = (39, 1, 0, 0) lies on line \ell_0
                                                                      85: P_{978} = (15, 14, 1, 0) lies on line \ell_1
38: P_{44} = (40, 1, 0, 0) lies on line \ell_0
                                                                      86: P_{1027} = (0, 15, 1, 0) lies on line \ell_2
39: P_{45} = (41, 1, 0, 0) lies on line \ell_0
                                                                      87: P_{1041} = (14, 15, 1, 0) lies on line \ell_1
40 : P_{46} = (42, 1, 0, 0) lies on line \ell_0
                                                                      88 : P_{1091} = (0, 16, 1, 0) lies on line \ell_2
41: P_{47} = (43, 1, 0, 0) lies on line \ell_0
                                                                      89: P_{1108} = (17, 16, 1, 0) lies on line \ell_1
42 : P_{48} = (44, 1, 0, 0) lies on line \ell_0
                                                                      90: P_{1155} = (0, 17, 1, 0) lies on line \ell_2
43: P_{49} = (45, 1, 0, 0) lies on line \ell_0
                                                                      91: P_{1171} = (16, 17, 1, 0) lies on line \ell_1
44: P_{50} = (46, 1, 0, 0) lies on line \ell_0
                                                                      92: P_{1219} = (0, 18, 1, 0) lies on line \ell_2
45: P_{51} = (47, 1, 0, 0) lies on line \ell_0
                                                                      93: P_{1238} = (19, 18, 1, 0) lies on line \ell_1
46: P_{52} = (48, 1, 0, 0) lies on line \ell_0
                                                                      94: P_{1283} = (0, 19, 1, 0) lies on line \ell_2
47: P_{53} = (49, 1, 0, 0) lies on line \ell_0
                                                                      95: P_{1301} = (18, 19, 1, 0) lies on line \ell_1
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96: P_{1347} = (0, 20, 1, 0) lies on line \ell_2
                                                                     150: P_{3075} = (0, 47, 1, 0) lies on line \ell_2
97: P_{1368} = (21, 20, 1, 0) lies on line \ell_1
                                                                     151: P_{3121} = (46, 47, 1, 0) lies on line \ell_1
98: P_{1411} = (0, 21, 1, 0) lies on line \ell_2
                                                                     152: P_{3139} = (0, 48, 1, 0) lies on line \ell_2
99: P_{1431} = (20, 21, 1, 0) lies on line \ell_1
                                                                     153: P_{3188} = (49, 48, 1, 0) lies on line \ell_1
100: P_{1475} = (0, 22, 1, 0) lies on line \ell_2
                                                                     154: P_{3203} = (0, 49, 1, 0) lies on line \ell_2
101: P_{1498} = (23, 22, 1, 0) lies on line \ell_1
                                                                     155: P_{3251} = (48, 49, 1, 0) lies on line \ell_1
102: P_{1539} = (0, 23, 1, 0) lies on line \ell_2
                                                                     156: P_{3267} = (0, 50, 1, 0) lies on line \ell_2
103: P_{1561} = (22, 23, 1, 0) lies on line \ell_1
                                                                     157: P_{3318} = (51, 50, 1, 0) lies on line \ell_1
104 : P_{1603} = (0, 24, 1, 0) lies on line \ell_2
                                                                     158: P_{3331} = (0, 51, 1, 0) lies on line \ell_2
105: P_{1628} = (25, 24, 1, 0) lies on line \ell_1
                                                                     159: P_{3381} = (50, 51, 1, 0) lies on line \ell_1
106: P_{1667} = (0, 25, 1, 0) lies on line \ell_2
                                                                     160: P_{3395} = (0, 52, 1, 0) lies on line \ell_2
107: P_{1691} = (24, 25, 1, 0) lies on line \ell_1
                                                                     161: P_{3448} = (53, 52, 1, 0) lies on line \ell_1
108: P_{1731} = (0, 26, 1, 0) lies on line \ell_2
                                                                     162: P_{3459} = (0, 53, 1, 0) lies on line \ell_2
109: P_{1758} = (27, 26, 1, 0) lies on line \ell_1
                                                                     163: P_{3511} = (52, 53, 1, 0) lies on line \ell_1
110: P_{1795} = (0, 27, 1, 0) lies on line \ell_2
                                                                     164: P_{3523} = (0, 54, 1, 0) lies on line \ell_2
111: P_{1821} = (26, 27, 1, 0) lies on line \ell_1
                                                                     165: P_{3578} = (55, 54, 1, 0) lies on line \ell_1
112: P_{1859} = (0, 28, 1, 0) lies on line \ell_2
                                                                     166: P_{3587} = (0, 55, 1, 0) lies on line \ell_2
113: P_{1888} = (29, 28, 1, 0) lies on line \ell_1
                                                                     167: P_{3641} = (54, 55, 1, 0) lies on line \ell_1
114: P_{1923} = (0, 29, 1, 0) lies on line \ell_2
                                                                     168: P_{3779} = (0, 58, 1, 0) lies on line \ell_2
115: P_{1951} = (28, 29, 1, 0) lies on line \ell_1
                                                                     169: P_{3838} = (59, 58, 1, 0) lies on line \ell_1
116: P_{1987} = (0, 30, 1, 0) lies on line \ell_2
                                                                     170: P_{3843} = (0, 59, 1, 0) lies on line \ell_2
117: P_{2018} = (31, 30, 1, 0) lies on line \ell_1
                                                                     171: P_{3901} = (58, 59, 1, 0) lies on line \ell_1
118: P_{2051} = (0, 31, 1, 0) lies on line \ell_2
                                                                     172: P_{3907} = (0, 60, 1, 0) lies on line \ell_2
119: P_{2081} = (30, 31, 1, 0) lies on line \ell_1
                                                                     173: P_{3968} = (61, 60, 1, 0) lies on line \ell_1
120: P_{2115} = (0, 32, 1, 0) lies on line \ell_2
                                                                     174: P_{3971} = (0, 61, 1, 0) lies on line \ell_2
121: P_{2148} = (33, 32, 1, 0) lies on line \ell_1
                                                                     175: P_{4031} = (60, 61, 1, 0) lies on line \ell_1
122: P_{2179} = (0, 33, 1, 0) lies on line \ell_2
                                                                     176: P_{4035} = (0, 62, 1, 0) lies on line \ell_2
123: P_{2211} = (32, 33, 1, 0) lies on line \ell_1
                                                                     177: P_{4098} = (63, 62, 1, 0) lies on line \ell_1
124: P_{2243} = (0, 34, 1, 0) lies on line \ell_2
                                                                     178: P_{4099} = (0, 63, 1, 0) lies on line \ell_2
125: P_{2278} = (35, 34, 1, 0) lies on line \ell_1
                                                                     179: P_{4161} = (62, 63, 1, 0) lies on line \ell_1
126: P_{2307} = (0, 35, 1, 0) lies on line \ell_2
                                                                     180: P_{4228} = (2, 1, 0, 1) lies on line \ell_3
127: P_{2341} = (34, 35, 1, 0) lies on line \ell_1
                                                                     181: P_{4229} = (3, 1, 0, 1) lies on line \ell_3
128: P_{2371} = (0, 36, 1, 0) lies on line \ell_2
                                                                     182: P_{4230} = (4, 1, 0, 1) lies on line \ell_3
129: P_{2408} = (37, 36, 1, 0) lies on line \ell_1
                                                                     183: P_{4231} = (5, 1, 0, 1) lies on line \ell_3
130: P_{2435} = (0, 37, 1, 0) lies on line \ell_2
                                                                     184: P_{4232} = (6, 1, 0, 1) lies on line \ell_3
131: P_{2471} = (36, 37, 1, 0) lies on line \ell_1
                                                                     185: P_{4233} = (7, 1, 0, 1) lies on line \ell_3
132: P_{2499} = (0, 38, 1, 0) lies on line \ell_2
                                                                     186: P_{4234} = (8, 1, 0, 1) lies on line \ell_3
133: P_{2538} = (39, 38, 1, 0) lies on line \ell_1
                                                                     187: P_{4235} = (9, 1, 0, 1) lies on line \ell_3
134 : P_{2563} = (0, 39, 1, 0) lies on line \ell_2
                                                                     188: P_{4236} = (10, 1, 0, 1) lies on line \ell_3
135: P_{2601} = (38, 39, 1, 0) lies on line \ell_1
                                                                     189: P_{4237} = (11, 1, 0, 1) lies on line \ell_3
                                                                     190: P_{4238} = (12, 1, 0, 1) lies on line \ell_3
136: P_{2627} = (0, 40, 1, 0) lies on line \ell_2
137: P_{2668} = (41, 40, 1, 0) lies on line \ell_1
                                                                     191: P_{4239} = (13, 1, 0, 1) lies on line \ell_3
138 : P_{2691} = (0, 41, 1, 0) lies on line \ell_2
                                                                     192: P_{4240} = (14, 1, 0, 1) lies on line \ell_3
139: P_{2731} = (40, 41, 1, 0) lies on line \ell_1
                                                                     193: P_{4241} = (15, 1, 0, 1) lies on line \ell_3
140: P_{2755} = (0, 42, 1, 0) lies on line \ell_2
                                                                     194: P_{4242} = (16, 1, 0, 1) lies on line \ell_3
141: P_{2798} = (43, 42, 1, 0) lies on line \ell_1
                                                                     195: P_{4243} = (17, 1, 0, 1) lies on line \ell_3
142: P_{2819} = (0, 43, 1, 0) lies on line \ell_2
                                                                     196: P_{4244} = (18, 1, 0, 1) lies on line \ell_3
143: P_{2861} = (42, 43, 1, 0) lies on line \ell_1
                                                                     197: P_{4245} = (19, 1, 0, 1) lies on line \ell_3
144: P_{2883} = (0, 44, 1, 0) lies on line \ell_2
                                                                     198: P_{4246} = (20, 1, 0, 1) lies on line \ell_3
145: P_{2928} = (45, 44, 1, 0) lies on line \ell_1
                                                                     199: P_{4247} = (21, 1, 0, 1) lies on line \ell_3
146 : P_{2947} = (0, 45, 1, 0) lies on line \ell_2
                                                                     200: P_{4248} = (22, 1, 0, 1) lies on line \ell_3
147: P_{2991} = (44, 45, 1, 0) lies on line \ell_1
                                                                     201: P_{4249} = (23, 1, 0, 1) lies on line \ell_3
                                                                     202 : P_{4250} = (24, 1, 0, 1) lies on line \ell_3
148: P_{3011} = (0, 46, 1, 0) lies on line \ell_2
149: P_{3058} = (47, 46, 1, 0) lies on line \ell_1
                                                                     203: P_{4251} = (25, 1, 0, 1) lies on line \ell_3
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204: P_{4252} = (26, 1, 0, 1) lies on line \ell_3
                                                                     258: P_{8870} = (37, 9, 1, 1) lies on line \ell_5
205 : P_{4253} = (27, 1, 0, 1) lies on line \ell_3
                                                                     259: P_{8878} = (45, 9, 1, 1) lies on line \ell_6
206: P_{4254} = (28, 1, 0, 1) lies on line \ell_3
                                                                     260: P_{8904} = (7, 10, 1, 1) lies on line \ell_6
                                                                     261: P_{8909} = (12, 10, 1, 1) lies on line \ell_5
207: P_{4255} = (29, 1, 0, 1) lies on line \ell_3
208 : P_{4256} = (30, 1, 0, 1) lies on line \ell_3
                                                                     262: P_{9013} = (52, 11, 1, 1) lies on line \ell_5
209: P_{4257} = (31, 1, 0, 1) lies on line \ell_3
                                                                     263: P_{9023} = (62, 11, 1, 1) lies on line \ell_6
                                                                     264 : P_{9075} = (50, 12, 1, 1) lies on line \ell_6
210: P_{4258} = (32, 1, 0, 1) lies on line \ell_3
211: P_{4259} = (33, 1, 0, 1) lies on line \ell_3
                                                                     265: P_{9088} = (63, 12, 1, 1) lies on line \ell_5
212 : P_{4260} = (34, 1, 0, 1) lies on line \ell_3
                                                                     266: P_{9096} = (7, 13, 1, 1) lies on line \ell_5
213: P_{4261} = (35, 1, 0, 1) lies on line \ell_3
                                                                     267: P_{9100} = (11, 13, 1, 1) lies on line \ell_6
214: P_{4262} = (36, 1, 0, 1) lies on line \ell_3
                                                                     268: P_{9186} = (33, 14, 1, 1) lies on line \ell_6
215: P_{4263} = (37, 1, 0, 1) lies on line \ell_3
                                                                     269: P_{9199} = (46, 14, 1, 1) lies on line \ell_5
216: P_{4264} = (38, 1, 0, 1) lies on line \ell_3
                                                                     270: P_{9239} = (22, 15, 1, 1) lies on line \ell_5
217: P_{4265} = (39, 1, 0, 1) lies on line \ell_3
                                                                     271: P_{9241} = (24, 15, 1, 1) lies on line \ell_6
218: P_{4266} = (40, 1, 0, 1) lies on line \ell_3
                                                                     272: P_{9283} = (2, 16, 1, 1) lies on line \ell_6
219: P_{4267} = (41, 1, 0, 1) lies on line \ell_3
                                                                     273: P_{9300} = (19, 16, 1, 1) lies on line \ell_5
220: P_{4268} = (42, 1, 0, 1) lies on line \ell_3
                                                                     274: P_{9388} = (43, 17, 1, 1) lies on line \ell_5
221: P_{4269} = (43, 1, 0, 1) lies on line \ell_3
                                                                     275: P_{9404} = (59, 17, 1, 1) lies on line \ell_6
222: P_{4270} = (44, 1, 0, 1) lies on line \ell_3
                                                                     276: P_{9411} = (2, 18, 1, 1) lies on line \ell_5
223: P_{4271} = (45, 1, 0, 1) lies on line \ell_3
                                                                     277: P_{9426} = (17, 18, 1, 1) lies on line \ell_6
224 : P_{4272} = (46, 1, 0, 1) lies on line \ell_3
                                                                     278: P_{9513} = (40, 19, 1, 1) lies on line \ell_6
225 : P_{4273} = (47, 1, 0, 1) lies on line \ell_3
                                                                     279: P_{9531} = (58, 19, 1, 1) lies on line \ell_5
226: P_{4274} = (48, 1, 0, 1) lies on line \ell_3
                                                                     280: P_{9573} = (36, 20, 1, 1) lies on line \ell_6
227: P_{4275} = (49, 1, 0, 1) lies on line \ell_3
                                                                     281: P_{9586} = (49, 20, 1, 1) lies on line \ell_5
228: P_{4276} = (50, 1, 0, 1) lies on line \ell_3
                                                                     282: P_{9610} = (9, 21, 1, 1) lies on line \ell_5
229 : P_{4277} = (51, 1, 0, 1) lies on line \ell_3
                                                                     283: P_{9630} = (29, 21, 1, 1) lies on line \ell_6
230: P_{4278} = (52, 1, 0, 1) lies on line \ell_3
                                                                     284: P_{9697} = (32, 22, 1, 1) lies on line \ell_5
231: P_{4279} = (53, 1, 0, 1) lies on line \ell_3
                                                                     285: P_{9720} = (55, 22, 1, 1) lies on line \ell_6
232: P_{4280} = (54, 1, 0, 1) lies on line \ell_3
                                                                     286: P_{9743} = (14, 23, 1, 1) lies on line \ell_6
233: P_{4281} = (55, 1, 0, 1) lies on line \ell_3
                                                                     287: P_{9753} = (24, 23, 1, 1) lies on line \ell_5
234: P_{4282} = (56, 1, 0, 1) lies on line \ell_3
                                                                     288: P_{9840} = (47, 24, 1, 1) lies on line \ell_6
235: P_{4283} = (57, 1, 0, 1) lies on line \ell_3
                                                                     289: P_{9847} = (54, 24, 1, 1) lies on line \ell_5
236: P_{4284} = (58, 1, 0, 1) lies on line \ell_3
                                                                     290: P_{9871} = (14, 25, 1, 1) lies on line \ell_5
237: P_{4285} = (59, 1, 0, 1) lies on line \ell_3
                                                                     291: P_{9879} = (22, 25, 1, 1) lies on line \ell_6
238: P_{4286} = (60, 1, 0, 1) lies on line \ell_3
                                                                     292: P_{9960} = (39, 26, 1, 1) lies on line \ell_5
239: P_{4287} = (61, 1, 0, 1) lies on line \ell_3
                                                                     293: P_{9981} = (60, 26, 1, 1) lies on line \ell_6
240: P_{4288} = (62, 1, 0, 1) lies on line \ell_3
                                                                     294: P_{9990} = (5, 27, 1, 1) lies on line \ell_6
241 : P_{4289} = (63, 1, 0, 1) lies on line \ell_3
                                                                     295: P_{10016} = (31, 27, 1, 1) lies on line \ell_5
242 : P_{8314} = (56, 0, 1, 1) lies on line \ell_5
                                                                     296: P_{10058} = (9, 28, 1, 1) lies on line \ell_6
243: P_{8315} = (57, 0, 1, 1) lies on line \ell_6
                                                                     297: P_{10069} = (20, 28, 1, 1) lies on line \ell_5
                                                                     298: P_{10157} = (44, 29, 1, 1) lies on line \ell_5
244: P_{8426} = (41, 2, 1, 1) lies on line \ell_5
245: P_{8427} = (42, 2, 1, 1) lies on line \ell_6
                                                                     299: P_{10161} = (48, 29, 1, 1) lies on line \ell_6
246: P_{8466} = (17, 3, 1, 1) lies on line \ell_5
                                                                     300: P_{10182} = (5, 30, 1, 1) lies on line \ell_5
247: P_{8468} = (19, 3, 1, 1) lies on line \ell_6
                                                                     301: P_{10203} = (26, 30, 1, 1) lies on line \ell_6
248: P_{8539} = (26, 4, 1, 1) lies on line \ell_5
                                                                     302: P_{10276} = (35, 31, 1, 1) lies on line \ell_6
                                                                     303: P_{10302} = (61, 31, 1, 1) lies on line \ell_5
249: P_{8544} = (31, 4, 1, 1) lies on line \ell_6
250: P_{8611} = (34, 5, 1, 1) lies on line \ell_5
                                                                     304: P_{10320} = (15, 32, 1, 1) lies on line \ell_5
251: P_{8615} = (38, 5, 1, 1) lies on line \ell_6
                                                                     305: P_{10351} = (46, 32, 1, 1) lies on line \ell_6
                                                                     306: P_{10392} = (23, 33, 1, 1) lies on line \ell_6
252: P_{8652} = (11, 6, 1, 1) lies on line \ell_5
253: P_{8653} = (12, 6, 1, 1) lies on line \ell_6
                                                                     307: P_{10424} = (55, 33, 1, 1) lies on line \ell_5
254: P_{8756} = (51, 7, 1, 1) lies on line \ell_5
                                                                     308: P_{10463} = (30, 34, 1, 1) lies on line \ell_5
255: P_{8758} = (53, 7, 1, 1) lies on line \ell_6
                                                                     309: P_{10494} = (61, 34, 1, 1) lies on line \ell_6
256: P_{8789} = (20, 8, 1, 1) lies on line \ell_6
                                                                     310: P_{10501} = (4, 35, 1, 1) lies on line \ell_6
257: P_{8798} = (29, 8, 1, 1) lies on line \ell_5
                                                                     311: P_{10535} = (38, 35, 1, 1) lies on line \ell_5
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366: P_{13378} = (1, 16, 2, 1) lies on line \ell_8
312: P_{10569} = (8, 36, 1, 1) lies on line \ell_6
313 : P_{10606} = (45, 36, 1, 1) lies on line \ell_5
                                                                     367: P_{13396} = (19, 16, 2, 1) lies on line \ell_9
314: P_{10646} = (21, 37, 1, 1) lies on line \ell_5
                                                                     368: P_{13506} = (1, 18, 2, 1) lies on line \ell_{10}
315: P_{10674} = (49, 37, 1, 1) lies on line \ell_6
                                                                     369: P_{13522} = (17, 18, 2, 1) lies on line \ell_{11}
316: P_{10716} = (27, 38, 1, 1) lies on line \ell_6
                                                                     370: P_{16513} = (0, 1, 3, 1) lies on line \ell_4
317: P_{10749} = (60, 38, 1, 1) lies on line \ell_5
                                                                     371: P_{16515} = (2, 1, 3, 1) lies on line \ell_7
318: P_{10757} = (4, 39, 1, 1) lies on line \ell_5
                                                                     372: P_{19010} = (1, 40, 3, 1) lies on line \ell_8
319: P_{10787} = (34, 39, 1, 1) lies on line \ell_6
                                                                     373: P_{19051} = (42, 40, 3, 1) lies on line \ell_9
320: P_{10820} = (3, 40, 1, 1) lies on line \ell_6
                                                                     374: P_{19202} = (1, 43, 3, 1) lies on line \ell_{10}
321: P_{10859} = (42, 40, 1, 1) lies on line \ell_5
                                                                     375: P_{19242} = (41, 43, 3, 1) lies on line \ell_{11}
322: P_{10899} = (18, 41, 1, 1) lies on line \ell_5
                                                                     376: P_{20609} = (0, 1, 4, 1) lies on line \ell_4
323: P_{10939} = (58, 41, 1, 1) lies on line \ell_6
                                                                     377: P_{20614} = (5, 1, 4, 1) lies on line \ell_7
324: P_{10961} = (16, 42, 1, 1) lies on line \ell_6
                                                                     378: P_{22786} = (1, 35, 4, 1) lies on line \ell_8
325: P_{11004} = (59, 42, 1, 1) lies on line \ell_5
                                                                     379: P_{22823} = (38, 35, 4, 1) lies on line \ell_9
326: P_{11012} = (3, 43, 1, 1) lies on line \ell_5
                                                                     380: P_{23042} = (1, 39, 4, 1) lies on line \ell_{10}
327: P_{11050} = (41, 43, 1, 1) lies on line \ell_6
                                                                     381: P_{23075} = (34, 39, 4, 1) lies on line \ell_{11}
328: P_{11081} = (8, 44, 1, 1) lies on line \ell_5
                                                                     382: P_{24705} = (0, 1, 5, 1) lies on line \ell_4
329: P_{11110} = (37, 44, 1, 1) lies on line \ell_6
                                                                     383: P_{24709} = (4, 1, 5, 1) lies on line \ell_7
330: P_{11165} = (28, 45, 1, 1) lies on line \ell_6
                                                                     384: P_{26370} = (1, 27, 5, 1) lies on line \ell_8
331: P_{11185} = (48, 45, 1, 1) lies on line \ell_5
                                                                     385: P_{26400} = (31, 27, 5, 1) lies on line \ell_9
332 : P_{11226} = (25, 46, 1, 1) lies on line \ell_5
                                                                     386: P_{26562} = (1, 30, 5, 1) lies on line \ell_{10}
333 : P_{11255} = (54, 46, 1, 1) lies on line \ell_6
                                                                     387: P_{26587} = (26, 30, 5, 1) lies on line \ell_{11}
                                                                     388 : P_{28801} = (0, 1, 6, 1) lies on line \ell_4
334 : P_{11280} = (15, 47, 1, 1) lies on line \ell_6
335 : P_{11298} = (33, 47, 1, 1) lies on line \ell_5
                                                                     389 : P_{28808} = (7, 1, 6, 1) lies on line \ell_7
336: P_{11350} = (21, 48, 1, 1) lies on line \ell_6
                                                                     390: P_{31938} = (1, 50, 6, 1) lies on line \ell_8
337: P_{11365} = (36, 48, 1, 1) lies on line \ell_5
                                                                     391 : P_{31990} = (53, 50, 6, 1) lies on line \ell_9
338 : P_{11421} = (28, 49, 1, 1) lies on line \ell_5
                                                                     392: P_{32066} = (1, 52, 6, 1) lies on line \ell_{10}
339 : P_{11437} = (44, 49, 1, 1) lies on line \ell_6
                                                                     393: P_{32116} = (51, 52, 6, 1) lies on line \ell_{11}
340: P_{11463} = (6, 50, 1, 1) lies on line \ell_6
                                                                     394: P_{32897} = (0, 1, 7, 1) lies on line \ell_4
341: P_{11510} = (53, 50, 1, 1) lies on line \ell_5
                                                                     395: P_{32903} = (6, 1, 7, 1) lies on line \ell_7
                                                                     396 : P_{33474} = (1, 10, 7, 1) lies on line \ell_8
342: P_{11534} = (13, 51, 1, 1) lies on line \ell_5
343 : P_{11584} = (63, 51, 1, 1) lies on line \ell_6
                                                                     397: P_{33485} = (12, 10, 7, 1) lies on line \ell_9
344: P_{11591} = (6, 52, 1, 1) lies on line \ell_5
                                                                     398: P_{33666} = (1, 13, 7, 1) lies on line \ell_{10}
345 : P_{11636} = (51, 52, 1, 1) lies on line \ell_6
                                                                     399: P_{33676} = (11, 13, 7, 1) lies on line \ell_{11}
346: P_{11659} = (10, 53, 1, 1) lies on line \ell_6
                                                                     400: P_{36993} = (0, 1, 8, 1) lies on line \ell_4
347: P_{11711} = (62, 53, 1, 1) lies on line \ell_5
                                                                     401: P_{37002} = (9, 1, 8, 1) lies on line \ell_7
348: P_{11736} = (23, 54, 1, 1) lies on line \ell_5
                                                                     402: P_{39234} = (1, 36, 8, 1) lies on line \ell_8
349 : P_{11745} = (32, 54, 1, 1) lies on line \ell_6
                                                                     403: P_{39278} = (45, 36, 8, 1) lies on line \ell_9
350: P_{11802} = (25, 55, 1, 1) lies on line \ell_6
                                                                     404: P_{39746} = (1, 44, 8, 1) lies on line \ell_{10}
351: P_{11824} = (47, 55, 1, 1) lies on line \ell_5
                                                                     405: P_{39782} = (37, 44, 8, 1) lies on line \ell_{11}
352: P_{11985} = (16, 58, 1, 1) lies on line \ell_5
                                                                     406: P_{41089} = (0, 1, 9, 1) lies on line \ell_4
353: P_{12012} = (43, 58, 1, 1) lies on line \ell_6
                                                                     407: P_{41097} = (8, 1, 9, 1) lies on line \ell_7
                                                                     408 : P_{42370} = (1, 21, 9, 1) lies on line \ell_{10}
354: P_{12051} = (18, 59, 1, 1) lies on line \ell_6
355: P_{12073} = (40, 59, 1, 1) lies on line \ell_5
                                                                     409: P_{42398} = (29, 21, 9, 1) lies on line \ell_{11}
356: P_{12127} = (30, 60, 1, 1) lies on line \ell_6
                                                                     410: P_{42818} = (1, 28, 9, 1) lies on line \ell_8
357: P_{12132} = (35, 60, 1, 1) lies on line \ell_5
                                                                     411: P_{42837} = (20, 28, 9, 1) lies on line \ell_9
358: P_{12188} = (27, 61, 1, 1) lies on line \ell_5
                                                                     412: P_{45185} = (0, 1, 10, 1) lies on line \ell_4
359: P_{12200} = (39, 61, 1, 1) lies on line \ell_6
                                                                     413: P_{45196} = (11, 1, 10, 1) lies on line \ell_7
360: P_{12238} = (13, 62, 1, 1) lies on line \ell_6
                                                                     414: P_{48514} = (1, 53, 10, 1) lies on line \ell_8
361: P_{12275} = (50, 62, 1, 1) lies on line \ell_5
                                                                     415: P_{48575} = (62, 53, 10, 1) lies on line \ell_9
362: P_{12299} = (10, 63, 1, 1) lies on line \ell_5
                                                                     416: P_{49154} = (1, 63, 10, 1) lies on line \ell_{10}
363: P_{12341} = (52, 63, 1, 1) lies on line \ell_6
                                                                     417: P_{49205} = (52, 63, 10, 1) lies on line \ell_{11}
364 : P_{12417} = (0, 1, 2, 1) lies on line \ell_4
                                                                     418 : P_{49281} = (0, 1, 11, 1) lies on line \ell_4
365: P_{12420} = (3, 1, 2, 1) lies on line \ell_7
                                                                     419: P_{49291} = (10, 1, 11, 1) lies on line \ell_7
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420 : P_{49602} = (1, 6, 11, 1) lies on line \ell_{10}
                                                                     474 : P_{86594} = (1, 8, 20, 1) lies on line \ell_8
421: P_{49613} = (12, 6, 11, 1) lies on line \ell_{11}
                                                                     475: P_{86622} = (29, 8, 20, 1) lies on line \ell_9
422: P_{50050} = (1, 13, 11, 1) lies on line \ell_8
                                                                     476: P_{87874} = (1, 28, 20, 1) lies on line \ell_{10}
423: P_{50056} = (7, 13, 11, 1) lies on line \ell_9
                                                                     477: P_{87882} = (9, 28, 20, 1) lies on line \ell_{11}
424: P_{53377} = (0, 1, 12, 1) lies on line \ell_4
                                                                     478: P_{90241} = (0, 1, 21, 1) lies on line \ell_4
425: P_{53390} = (13, 1, 12, 1) lies on line \ell_7
                                                                     479: P_{90261} = (20, 1, 21, 1) lies on line \ell_7
426: P_{53698} = (1, 6, 12, 1) lies on line \ell_8
                                                                     480: P_{92546} = (1, 37, 21, 1) lies on line \ell_{10}
                                                                     481: P_{92594} = (49, 37, 21, 1) lies on line \ell_{11}
427: P_{53708} = (11, 6, 12, 1) lies on line \ell_9
428: P_{53954} = (1, 10, 12, 1) lies on line \ell_{10}
                                                                     482: P_{93250} = (1, 48, 21, 1) lies on line \ell_8
429: P_{53960} = (7, 10, 12, 1) lies on line \ell_{11}
                                                                     483: P_{93285} = (36, 48, 21, 1) lies on line \ell_9
430: P_{57473} = (0, 1, 13, 1) lies on line \ell_4
                                                                     484: P_{94337} = (0, 1, 22, 1) lies on line \ell_4
431: P_{57485} = (12, 1, 13, 1) lies on line \ell_7
                                                                     485: P_{94360} = (23, 1, 22, 1) lies on line \ell_7
432 : P_{60674} = (1, 51, 13, 1) lies on line \ell_{10}
                                                                     486: P_{95234} = (1, 15, 22, 1) lies on line \ell_{10}
433: P_{60736} = (63, 51, 13, 1) lies on line \ell_{11}
                                                                     487: P_{95257} = (24, 15, 22, 1) lies on line \ell_{11}
434: P_{61378} = (1, 62, 13, 1) lies on line \ell_8
                                                                     488: P_{95874} = (1, 25, 22, 1) lies on line \ell_8
435: P_{61427} = (50, 62, 13, 1) lies on line \ell_9
                                                                     489: P_{95887} = (14, 25, 22, 1) lies on line \ell_9
                                                                     490 : P_{98433} = (0, 1, 23, 1) lies on line \ell_4
436: P_{61569} = (0, 1, 14, 1) lies on line \ell_4
437: P_{61584} = (15, 1, 14, 1) lies on line \ell_7
                                                                     491: P_{98455} = (22, 1, 23, 1) lies on line \ell_7
438: P_{62978} = (1, 23, 14, 1) lies on line \ell_8
                                                                     492: P_{100482} = (1, 33, 23, 1) lies on line \ell_8
439: P_{63001} = (24, 23, 14, 1) lies on line \ell_9
                                                                     493: P_{100536} = (55, 33, 23, 1) lies on line \ell_9
440: P_{63106} = (1, 25, 14, 1) lies on line \ell_{10}
                                                                     494: P_{101826} = (1, 54, 23, 1) lies on line \ell_{10}
441 : P_{63127} = (22, 25, 14, 1) lies on line \ell_{11}
                                                                     495: P_{101857} = (32, 54, 23, 1) lies on line \ell_{11}
442: P_{65665} = (0, 1, 15, 1) lies on line \ell_4
                                                                     496: P_{102529} = (0, 1, 24, 1) lies on line \ell_4
443 : P_{65679} = (14, 1, 15, 1) lies on line \ell_7
                                                                     497: P_{102554} = (25, 1, 24, 1) lies on line \ell_7
444: P_{67650} = (1, 32, 15, 1) lies on line \ell_{10}
                                                                     498: P_{103426} = (1, 15, 24, 1) lies on line \ell_8
445: P_{67695} = (46, 32, 15, 1) lies on line \ell_{11}
                                                                     499: P_{103447} = (22, 15, 24, 1) lies on line \ell_9
446: P_{68610} = (1, 47, 15, 1) lies on line \ell_8
                                                                     500: P_{103938} = (1, 23, 24, 1) lies on line \ell_{10}
447: P_{68642} = (33, 47, 15, 1) lies on line \ell_9
                                                                     501: P_{103951} = (14, 23, 24, 1) lies on line \ell_{11}
448: P_{69761} = (0, 1, 16, 1) lies on line \ell_4
                                                                     502: P_{106625} = (0, 1, 25, 1) lies on line \ell_4
449: P_{69778} = (17, 1, 16, 1) lies on line \ell_7
                                                                     503: P_{106649} = (24, 1, 25, 1) lies on line \ell_7
450: P_{72386} = (1, 42, 16, 1) lies on line \ell_8
                                                                     504: P_{109506} = (1, 46, 25, 1) lies on line \ell_{10}
451: P_{72444} = (59, 42, 16, 1) lies on line \ell_9
                                                                     505: P_{109559} = (54, 46, 25, 1) lies on line \ell_{11}
452: P_{73410} = (1, 58, 16, 1) lies on line \ell_{10}
                                                                     506: P_{110082} = (1, 55, 25, 1) lies on line \ell_8
453 : P_{73452} = (43, 58, 16, 1) lies on line \ell_{11}
                                                                     507: P_{110128} = (47, 55, 25, 1) lies on line \ell_9
454: P_{73857} = (0, 1, 17, 1) lies on line \ell_4
                                                                     508: P_{110721} = (0, 1, 26, 1) lies on line \ell_4
455: P_{73873} = (16, 1, 17, 1) lies on line \ell_7
                                                                     509: P_{110748} = (27, 1, 26, 1) lies on line \ell_7
456: P_{73986} = (1, 3, 17, 1) lies on line \ell_{10}
                                                                     510: P_{110914} = (1, 4, 26, 1) lies on line \ell_{10}
457: P_{74004} = (19, 3, 17, 1) lies on line \ell_{11}
                                                                     511: P_{110944} = (31, 4, 26, 1) lies on line \ell_{11}
458: P_{74946} = (1, 18, 17, 1) lies on line \ell_8
                                                                     512: P_{112578} = (1, 30, 26, 1) lies on line \ell_8
459 : P_{74947} = (2, 18, 17, 1) lies on line \ell_9
                                                                     513: P_{112582} = (5, 30, 26, 1) lies on line \ell_9
                                                                     514 : P_{114817} = (0, 1, 27, 1) lies on line \ell_4
460: P_{77953} = (0, 1, 18, 1) lies on line \ell_4
461: P_{77972} = (19, 1, 18, 1) lies on line \ell_7
                                                                     515: P_{114843} = (26, 1, 27, 1) lies on line \ell_7
                                                                     516: P_{117186} = (1, 38, 27, 1) lies on line \ell_8
462: P_{80514} = (1, 41, 18, 1) lies on line \ell_{10}
463: P_{80571} = (58, 41, 18, 1) lies on line \ell_{11}
                                                                     517: P_{117245} = (60, 38, 27, 1) lies on line \ell_9
464: P_{81666} = (1, 59, 18, 1) lies on line \ell_8
                                                                     518: P_{118658} = (1, 61, 27, 1) lies on line \ell_{10}
465: P_{81705} = (40, 59, 18, 1) lies on line \ell_9
                                                                     519: P_{118696} = (39, 61, 27, 1) lies on line \ell_{11}
466: P_{82049} = (0, 1, 19, 1) lies on line \ell_4
                                                                     520: P_{118913} = (0, 1, 28, 1) lies on line \ell_4
467: P_{82067} = (18, 1, 19, 1) lies on line \ell_7
                                                                     521: P_{118942} = (29, 1, 28, 1) lies on line \ell_7
468: P_{82178} = (1, 3, 19, 1) lies on line \ell_8
                                                                     522: P_{121730} = (1, 45, 28, 1) lies on line \ell_8
469: P_{82194} = (17, 3, 19, 1) lies on line \ell_9
                                                                     523: P_{121777} = (48, 45, 28, 1) lies on line \ell_9
470: P_{83010} = (1, 16, 19, 1) lies on line \ell_{10}
                                                                     524: P_{121986} = (1, 49, 28, 1) lies on line \ell_{10}
471: P_{83011} = (2, 16, 19, 1) lies on line \ell_{11}
                                                                     525: P_{122029} = (44, 49, 28, 1) lies on line \ell_{11}
472: P_{86145} = (0, 1, 20, 1) lies on line \ell_4
                                                                     526: P_{123009} = (0, 1, 29, 1) lies on line \ell_4
473: P_{86166} = (21, 1, 20, 1) lies on line \ell_7
                                                                     527: P_{123037} = (28, 1, 29, 1) lies on line \ell_7
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582 : P_{160130} = (1, 5, 38, 1) lies on line \ell_8
528: P_{123458} = (1, 8, 29, 1) lies on line \ell_{10}
529: P_{123477} = (20, 8, 29, 1) lies on line \ell_{11}
                                                                     583: P_{160163} = (34, 5, 38, 1) lies on line \ell_9
                                                                     584: P_{162050} = (1, 35, 38, 1) lies on line \ell_{10}
530: P_{124290} = (1, 21, 29, 1) lies on line \ell_8
531: P_{124298} = (9, 21, 29, 1) lies on line \ell_9
                                                                     585: P_{162053} = (4, 35, 38, 1) lies on line \ell_{11}
532: P_{127105} = (0, 1, 30, 1) lies on line \ell_4
                                                                     586: P_{163969} = (0, 1, 39, 1) lies on line \ell_4
533: P_{127136} = (31, 1, 30, 1) lies on line \ell_7
                                                                     587: P_{164007} = (38, 1, 39, 1) lies on line \ell_7
                                                                     588: P_{165570} = (1, 26, 39, 1) lies on line \ell_{10}
534: P_{129218} = (1, 34, 30, 1) lies on line \ell_{10}
535: P_{129278} = (61, 34, 30, 1) lies on line \ell_{11}
                                                                     589: P_{165629} = (60, 26, 39, 1) lies on line \ell_{11}
536: P_{130882} = (1, 60, 30, 1) lies on line \ell_8
                                                                     590: P_{167810} = (1, 61, 39, 1) lies on line \ell_8
537: P_{130916} = (35, 60, 30, 1) lies on line \ell_9
                                                                     591: P_{167836} = (27, 61, 39, 1) lies on line \ell_9
538: P_{131201} = (0, 1, 31, 1) lies on line \ell_4
                                                                     592: P_{168065} = (0, 1, 40, 1) lies on line \ell_4
539: P_{131231} = (30, 1, 31, 1) lies on line \ell_7
                                                                     593: P_{168106} = (41, 1, 40, 1) lies on line \ell_7
540: P_{131394} = (1, 4, 31, 1) lies on line \ell_8
                                                                     594: P_{169218} = (1, 19, 40, 1) lies on line \ell_8
541: P_{131419} = (26, 4, 31, 1) lies on line \ell_9
                                                                     595: P_{169275} = (58, 19, 40, 1) lies on line \ell_9
542: P_{132866} = (1, 27, 31, 1) lies on line \ell_{10}
                                                                     596: P_{171778} = (1, 59, 40, 1) lies on line \ell_{10}
543: P_{132870} = (5, 27, 31, 1) lies on line \ell_{11}
                                                                     597: P_{171795} = (18, 59, 40, 1) lies on line \ell_{11}
544: P_{135297} = (0, 1, 32, 1) lies on line \ell_4
                                                                     598: P_{172161} = (0, 1, 41, 1) lies on line \ell_4
545: P_{135330} = (33, 1, 32, 1) lies on line \ell_7
                                                                     599: P_{172201} = (40, 1, 41, 1) lies on line \ell_7
546: P_{136642} = (1, 22, 32, 1) lies on line \ell_{10}
                                                                     600: P_{172226} = (1, 2, 41, 1) lies on line \ell_{10}
547: P_{136696} = (55, 22, 32, 1) lies on line \ell_{11}
                                                                     601: P_{172267} = (42, 2, 41, 1) lies on line \ell_{11}
548: P_{138690} = (1, 54, 32, 1) lies on line \ell_8
                                                                     602: P_{174850} = (1, 43, 41, 1) lies on line \ell_8
549: P_{138712} = (23, 54, 32, 1) lies on line \ell_9
                                                                     603: P_{174852} = (3, 43, 41, 1) lies on line \ell_9
550: P_{139393} = (0, 1, 33, 1) lies on line \ell_4
                                                                     604: P_{176257} = (0, 1, 42, 1) lies on line \ell_4
551: P_{139425} = (32, 1, 33, 1) lies on line \ell_7
                                                                     605: P_{176300} = (43, 1, 42, 1) lies on line \ell_7
552: P_{140226} = (1, 14, 33, 1) lies on line \ell_8
                                                                     606: P_{176322} = (1, 2, 42, 1) lies on line \ell_8
553: P_{140271} = (46, 14, 33, 1) lies on line \ell_9
                                                                     607: P_{176362} = (41, 2, 42, 1) lies on line \ell_9
554: P_{142338} = (1, 47, 33, 1) lies on line \ell_{10}
                                                                     608: P_{178754} = (1, 40, 42, 1) lies on line \ell_{10}
555: P_{142352} = (15, 47, 33, 1) lies on line \ell_{11}
                                                                     609: P_{178756} = (3, 40, 42, 1) lies on line \ell_{11}
556: P_{143489} = (0, 1, 34, 1) lies on line \ell_4
                                                                     610: P_{180353} = (0, 1, 43, 1) lies on line \ell_4
557: P_{143524} = (35, 1, 34, 1) lies on line \ell_7
                                                                     611: P_{180395} = (42, 1, 43, 1) lies on line \ell_7
558: P_{143746} = (1, 5, 34, 1) lies on line \ell_{10}
                                                                     612: P_{181378} = (1, 17, 43, 1) lies on line \ell_{10}
559: P_{143783} = (38, 5, 34, 1) lies on line \ell_{11}
                                                                     613: P_{181436} = (59, 17, 43, 1) lies on line \ell_{11}
560: P_{145922} = (1, 39, 34, 1) lies on line \ell_8
                                                                     614: P_{184002} = (1, 58, 43, 1) lies on line \ell_8
561: P_{145925} = (4, 39, 34, 1) lies on line \ell_9
                                                                     615: P_{184017} = (16, 58, 43, 1) lies on line \ell_9
562: P_{147585} = (0, 1, 35, 1) lies on line \ell_4
                                                                     616: P_{184449} = (0, 1, 44, 1) lies on line \ell_4
563: P_{147619} = (34, 1, 35, 1) lies on line \ell_7
                                                                     617: P_{184494} = (45, 1, 44, 1) lies on line \ell_7
564: P_{149506} = (1, 31, 35, 1) lies on line \ell_8
                                                                     618: P_{186242} = (1, 29, 44, 1) lies on line \ell_{10}
565: P_{149566} = (61, 31, 35, 1) lies on line \ell_9
                                                                     619: P_{186289} = (48, 29, 44, 1) lies on line \ell_{11}
566: P_{151362} = (1, 60, 35, 1) lies on line \ell_{10}
                                                                     620: P_{187522} = (1, 49, 44, 1) lies on line \ell_8
                                                                     621: P_{187549} = (28, 49, 44, 1) lies on line \ell_9
567: P_{151391} = (30, 60, 35, 1) lies on line \ell_{11}
568: P_{151681} = (0, 1, 36, 1) lies on line \ell_4
                                                                     622: P_{188545} = (0, 1, 45, 1) lies on line \ell_4
569: P_{151718} = (37, 1, 36, 1) lies on line \ell_7
                                                                     623: P_{188589} = (44, 1, 45, 1) lies on line \ell_7
570: P_{152898} = (1, 20, 36, 1) lies on line \ell_8
                                                                     624: P_{189058} = (1, 9, 45, 1) lies on line \ell_8
571: P_{152946} = (49, 20, 36, 1) lies on line \ell_9
                                                                     625: P_{189094} = (37, 9, 45, 1) lies on line \ell_9
572: P_{154690} = (1, 48, 36, 1) lies on line \ell_{10}
                                                                     626: P_{190786} = (1, 36, 45, 1) lies on line \ell_{10}
573: P_{154710} = (21, 48, 36, 1) lies on line \ell_{11}
                                                                     627: P_{190793} = (8, 36, 45, 1) lies on line \ell_{11}
574: P_{155777} = (0, 1, 37, 1) lies on line \ell_4
                                                                     628: P_{192641} = (0, 1, 46, 1) lies on line \ell_4
575: P_{155813} = (36, 1, 37, 1) lies on line \ell_7
                                                                     629: P_{192688} = (47, 1, 46, 1) lies on line \ell_7
576: P_{156290} = (1, 9, 37, 1) lies on line \ell_{10}
                                                                     630: P_{193474} = (1, 14, 46, 1) lies on line \ell_{10}
577: P_{156334} = (45, 9, 37, 1) lies on line \ell_{11}
                                                                     631: P_{193506} = (33, 14, 46, 1) lies on line \ell_{11}
578: P_{158530} = (1, 44, 37, 1) lies on line \ell_8
                                                                     632: P_{194626} = (1, 32, 46, 1) lies on line \ell_8
579: P_{158537} = (8, 44, 37, 1) lies on line \ell_9
                                                                     633: P_{194640} = (15, 32, 46, 1) lies on line \ell_9
580 : P_{159873} = (0, 1, 38, 1) lies on line \ell_4
                                                                     634: P_{196737} = (0, 1, 47, 1) lies on line \ell_4
581: P_{159912} = (39, 1, 38, 1) lies on line \ell_7
                                                                     635: P_{196783} = (46, 1, 47, 1) lies on line \ell_7
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685 : P_{230881} = (32, 22, 55, 1) lies on line \ell_9
636: P_{198210} = (1, 24, 47, 1) lies on line \ell_8
637: P_{198263} = (54, 24, 47, 1) lies on line \ell_9
                                                                     686: P_{231554} = (1, 33, 55, 1) lies on line \ell_{10}
638: P_{200194} = (1, 55, 47, 1) lies on line \ell_{10}
                                                                     687: P_{231576} = (23, 33, 55, 1) lies on line \ell_{11}
639: P_{200218} = (25, 55, 47, 1) lies on line \ell_{11}
                                                                     688: P_{233538} = (1, 0, 56, 1) lies on line \ell_{10}
                                                                     689: P_{233594} = (57, 0, 56, 1) lies on line \ell_{11}
640: P_{200833} = (0, 1, 48, 1) lies on line \ell_4
                                                                     690 : P_{233601} = (0, 1, 56, 1) lies on line \ell_4
641: P_{200882} = (49, 1, 48, 1) lies on line \ell_7
                                                                     691: P_{233658} = (57, 1, 56, 1) lies on line \ell_7
642: P_{202626} = (1, 29, 48, 1) lies on line \ell_8
                                                                     692: P_{237634} = (1, 0, 57, 1) lies on line \ell_8
643: P_{202669} = (44, 29, 48, 1) lies on line \ell_9
644: P_{203650} = (1, 45, 48, 1) lies on line \ell_{10}
                                                                     693: P_{237689} = (56, 0, 57, 1) lies on line \ell_9
645: P_{203677} = (28, 45, 48, 1) lies on line \ell_{11}
                                                                     694: P_{237697} = (0, 1, 57, 1) lies on line \ell_4
646: P_{204929} = (0, 1, 49, 1) lies on line \ell_4
                                                                     695: P_{237753} = (56, 1, 57, 1) lies on line \ell_7
647: P_{204977} = (48, 1, 49, 1) lies on line \ell_7
                                                                     696: P_{241793} = (0, 1, 58, 1) lies on line \ell_4
648: P_{206146} = (1, 20, 49, 1) lies on line \ell_{10}
                                                                     697: P_{241852} = (59, 1, 58, 1) lies on line \ell_7
649: P_{206181} = (36, 20, 49, 1) lies on line \ell_{11}
                                                                     698: P_{242946} = (1, 19, 58, 1) lies on line \ell_{10}
650: P_{207234} = (1, 37, 49, 1) lies on line \ell_8
                                                                     699: P_{242985} = (40, 19, 58, 1) lies on line \ell_{11}
651: P_{207254} = (21, 37, 49, 1) lies on line \ell_9
                                                                     700: P_{244354} = (1, 41, 58, 1) lies on line \ell_8
652: P_{209025} = (0, 1, 50, 1) lies on line \ell_4
                                                                     701: P_{244371} = (18, 41, 58, 1) lies on line \ell_9
653: P_{209076} = (51, 1, 50, 1) lies on line \ell_7
                                                                     702: P_{245889} = (0, 1, 59, 1) lies on line \ell_4
                                                                     703 : P_{245947} = (58, 1, 59, 1) lies on line \ell_7
654: P_{209730} = (1, 12, 50, 1) lies on line \ell_8
                                                                     704: P_{246914} = (1, 17, 59, 1) lies on line \ell_8
655: P_{209792} = (63, 12, 50, 1) lies on line \ell_9
656: P_{212930} = (1, 62, 50, 1) lies on line \ell_{10}
                                                                     705 : P_{246956} = (43, 17, 59, 1) lies on line \ell_9
657: P_{212942} = (13, 62, 50, 1) lies on line \ell_{11}
                                                                     706 : P_{248514} = (1, 42, 59, 1) lies on line \ell_{10}
658: P_{213121} = (0, 1, 51, 1) lies on line \ell_4
                                                                      707: P_{248529} = (16, 42, 59, 1) lies on line \ell_{11}
659 : P_{213171} = (50, 1, 51, 1) lies on line \ell_7
                                                                     708 : P_{249985} = (0, 1, 60, 1) lies on line \ell_4
                                                                     709 : P_{250046} = (61, 1, 60, 1) lies on line \ell_7
660: P_{213506} = (1, 7, 51, 1) lies on line \ell_{10}
661: P_{213558} = (53, 7, 51, 1) lies on line \ell_{11}
                                                                     710: P_{251586} = (1, 26, 60, 1) lies on line \ell_8
662: P_{216386} = (1, 52, 51, 1) lies on line \ell_8
                                                                     711: P_{251624} = (39, 26, 60, 1) lies on line \ell_9
663: P_{216391} = (6, 52, 51, 1) lies on line \ell_9
                                                                     712: P_{252354} = (1, 38, 60, 1) lies on line \ell_{10}
664: P_{217217} = (0, 1, 52, 1) lies on line \ell_4
                                                                     713: P_{252380} = (27, 38, 60, 1) lies on line \ell_{11}
665: P_{217270} = (53, 1, 52, 1) lies on line \ell_7
                                                                     714: P_{254081} = (0, 1, 61, 1) lies on line \ell_4
666: P_{217858} = (1, 11, 52, 1) lies on line \ell_{10}
                                                                     715: P_{254141} = (60, 1, 61, 1) lies on line \ell_7
667: P_{217919} = (62, 11, 52, 1) lies on line \ell_{11}
                                                                     716: P_{256002} = (1, 31, 61, 1) lies on line \ell_{10}
668: P_{221186} = (1, 63, 52, 1) lies on line \ell_8
                                                                     717: P_{256036} = (35, 31, 61, 1) lies on line \ell_{11}
669: P_{221195} = (10, 63, 52, 1) lies on line \ell_9
                                                                     718 : P_{256194} = (1, 34, 61, 1) lies on line \ell_8
670: P_{221313} = (0, 1, 53, 1) lies on line \ell_4
                                                                     719: P_{256223} = (30, 34, 61, 1) lies on line \ell_9
                                                                     720: P_{258177} = (0, 1, 62, 1) lies on line \ell_4
671: P_{221365} = (52, 1, 53, 1) lies on line \ell_7
672: P_{221698} = (1, 7, 53, 1) lies on line \ell_8
                                                                     721: P_{258240} = (63, 1, 62, 1) lies on line \ell_7
673: P_{221748} = (51, 7, 53, 1) lies on line \ell_9
                                                                     722: P_{258818} = (1, 11, 62, 1) lies on line \ell_8
                                                                     723 : P_{258869} = (52, 11, 62, 1) lies on line \ell_9
674: P_{224450} = (1, 50, 53, 1) lies on line \ell_{10}
675: P_{224455} = (6, 50, 53, 1) lies on line \ell_{11}
                                                                     724: P_{261506} = (1, 53, 62, 1) lies on line \ell_{10}
676: P_{225409} = (0, 1, 54, 1) lies on line \ell_4
                                                                     725: P_{261515} = (10, 53, 62, 1) lies on line \ell_{11}
677: P_{225464} = (55, 1, 54, 1) lies on line \ell_7
                                                                     726: P_{262273} = (0, 1, 63, 1) lies on line \ell_4
678 : P_{226882} = (1, 24, 54, 1) lies on line \ell_{10}
                                                                     727 : P_{262335} = (62, 1, 63, 1) lies on line \ell_7
679: P_{226928} = (47, 24, 54, 1) lies on line \ell_{11}
                                                                     728: P_{262978} = (1, 12, 63, 1) lies on line \ell_{10}
680: P_{228290} = (1, 46, 54, 1) lies on line \ell_8
                                                                     729: P_{263027} = (50, 12, 63, 1) lies on line \ell_{11}
681 : P_{228314} = (25, 46, 54, 1) lies on line \ell_9
                                                                     730: P_{265474} = (1, 51, 63, 1) lies on line \ell_8
682: P_{229505} = (0, 1, 55, 1) lies on line \ell_4
                                                                     731: P_{265486} = (13, 51, 63, 1) lies on line \ell_9
683: P_{229559} = (54, 1, 55, 1) lies on line \ell_7
684: P_{230850} = (1, 22, 55, 1) lies on line \ell_8
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The single points on the surface are:

Points on surface but on no line

The surface has 3600 points not on any line: Too many to print.

Line Intersection Graph

	0123456789	10	11
0	0111011000	0	0
1	1010000101	0	1
2	1100100010	1	0
3	1000100111	1	1
4	0011011101	0	1
5	1000101101	1	0
6	1000110110	0	1
7	0101111010	1	0
8	0011001101	1	0
9	0101110010	0	1
10	0011010110	0	1
11	0101101001	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6
in point	P_5	P_1	P_0	P_{60}	P_{61}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_7	ℓ_9	ℓ_{11}
in point	P_5	P_{131}	P_{68}	P_{3708}	P_{3771}

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_4	ℓ_8	ℓ_{10}
in point	P_1	P_{131}	P_2	P_{3651}	P_{3715}

Line 3 intersects

Line	ℓ_0	ℓ_4	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}
in point	P_0	P_{4226}	P_{4227}	P_{4227}	P_{4226}	P_{4227}	P_{4226}

Line 4 intersects

Line	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_9	ℓ_{11}
in point	P_2	P_{4226}	P_{8322}	P_{8322}	P_{8322}	P_{4226}	P_{4226}

Line 5 intersects

Line	ℓ_0	ℓ_4	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}
in point	P_{60}	P_{8322}	P_{8322}	P_{8322}	P_{11962}	P_{11842}

Line 6 intersects

Line	ℓ_0	ℓ_4	ℓ_5	ℓ_7	ℓ_8	ℓ_{11}
in point	P_{61}	P_{8322}	P_{8322}	P_{8322}	P_{11906}	P_{11897}

Line 7 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_8	ℓ_{10}
in point	P_{68}	P_{4227}	P_{8322}	P_{8322}	P_{8322}	P_{4227}	P_{4227}

Line 8 intersects

Line	ℓ_2	ℓ_3	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}
in point	P_{3651}	P_{4227}	P_{11906}	P_{4227}	P_{237122}	P_{4227}

Line 9 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_8	ℓ_{11}
in point	P_{3708}	P_{4226}	P_{4226}	P_{11962}	P_{237122}	P_{4226}

Line 10 intersects

Line	ℓ_2	ℓ_3	ℓ_5	ℓ_7	ℓ_8	ℓ_{11}
in point	P_{3715}	P_{4227}	P_{11842}	P_{4227}	P_{4227}	P_{241282}

Line 11 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_6	ℓ_9	ℓ_{10}
in point	P_{3771}	P_{4226}	P_{4226}	P_{11897}	P_{4226}	P_{241282}

The surface has 4353 points:

Too many to print.