# Rank-31 over GF(16)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 = 0$$

# General information

Number of lines	27
Number of points	369
Number of singular points	0
Number of Eckardt points	45
Number of double points	0
Number of single points	324
Number of points off lines	0
Number of Hesse planes	40
Number of axes	240
Type of points on lines	$17^{27}$
Type of lines on points	$3^{45}, 1^{324}$

## Singular Points

The surface has 0 singular points:

# The 27 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = a_1 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & \delta^5 \end{bmatrix}_{540} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 11 \end{bmatrix}_{540} = \mathbf{Pl}(0, 0, 10, 11, 11, 1)_{50505}$$

$$\ell_1 = a_2 = \begin{bmatrix} 1 & \delta^5 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{3260} = \begin{bmatrix} 1 & 11 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{3260} = \mathbf{Pl}(0, 0, 1, 1, 10, 1)_{46146}$$

$$\begin{split} \ell_2 &= a_3 = \begin{bmatrix} 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{289} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{289} = \mathbf{PI}(1,1,0,0,1,1)_{8961} \\ \ell_3 &= a_4 = \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 1 & \delta^{10} & 0 \end{bmatrix}_{3179} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 0 & 11 \end{bmatrix}_{3179} = \mathbf{PI}(10,11,0,0,1,1)_{8970} \\ \ell_4 &= a_5 &= \begin{bmatrix} 1 & 0 & 0 & \delta^{10} \\ 0 & 1 & \delta^{10} & 0 \end{bmatrix}_{43690} = \begin{bmatrix} 1 & 0 & 0 & 10 \\ 0 & 1 & 10 & 0 \end{bmatrix}_{43690} = \mathbf{PI}(11,10,1,1,0,0)_{74} \\ \ell_5 &= a_6 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \delta^5 & 0 \end{bmatrix}_{4379} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{4379} = \mathbf{PI}(10,11,11,1,0,0)_{223} \\ \ell_6 &= b_1 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{3019} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{3019} = \mathbf{PI}(11,1,0,0,10,1)_{45681} \\ \ell_7 &= b_2 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & \delta^5 \end{bmatrix}_{449} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{499} = \mathbf{PI}(10,11,0,0,11,1)_{29770} \\ \ell_8 &= b_3 &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & \delta^5 & 0 \end{bmatrix}_{4378} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 10 & 0 \end{bmatrix}_{4378} = \mathbf{PI}(10,11,0,0,10,1)_{000} \\ \ell_9 &= b_4 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 1 & \delta^5 & 0 \end{bmatrix}_{369} = \begin{bmatrix} 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{369} = \mathbf{PI}(10,11,10,1,0,0)_{209} \\ \ell_{10} &= b_5 &= \begin{bmatrix} 1 & \delta^5 & 0 & 0 \\ 0 & 0 & 1 & \delta^5 \end{bmatrix}_{3270} = \begin{bmatrix} 1 & 11 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{3270} = \mathbf{PI}(0,0,10,11,1,1)_{9705} \\ \ell_{11} &= b_6 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{48049} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{38049} = \mathbf{PI}(11,1,0,0,11,1)_{49761} \\ \ell_{14} &= c_{14} &= \begin{bmatrix} 1 & 0 & \delta^{50} & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{2746} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{3163} = \mathbf{PI}(11,10,0,0,11,1)_{49761} \\ \ell_{15} &= c_{15} &= \begin{bmatrix} 1 & \delta^{50} & 0 & 0 \\ 0 & 1 & \delta^{50} \end{bmatrix}_{3363} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{3163} = \mathbf{PI}(11,10,0,0,11,1)_{46456} \\ \ell_{17} &= c_{23} &= \begin{bmatrix} 1 & 0 & \delta^{50} & 0 \\ 0 & 1 & \delta^{50} \end{bmatrix}_{3363} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{3299} = \mathbf{PI}(0,0,11,10,1)_{46456} \\ \ell_{17} &= c_{23} &= \begin{bmatrix} 1 & \delta^{50} & 0 & 0 \\ 0 & 1 & \delta^{50} \end{bmatrix}_{3363} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{3299} = \mathbf{PI}(0,0,11,10,11,1)_{50536} \\ \ell_{19} &= c_{25} &= \begin{bmatrix} 1 & \delta^{10} & 0 & 0 \\ 0 & 0 & 1 & \delta^{50} \end{bmatrix}_{32996} = \begin{bmatrix} 1 & 10 & 0 & 0 \\ 0 & 0 & 1 & 10 \end{bmatrix}_{3299$$

$$\ell_{23} = c_{36} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4369} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4369} = \mathbf{Pl}(1, 1, 1, 1, 0, 0)_{64}$$

$$\ell_{24} = c_{45} = \begin{bmatrix} 1 & 0 & 0 & \delta^{10} \\ 0 & 1 & 1 & 0 \end{bmatrix}_{43681} = \begin{bmatrix} 1 & 0 & 0 & 10 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{43681} = \mathbf{Pl}(1, 1, 11, 1, 0, 0)_{214}$$

$$\ell_{25} = c_{46} = \begin{bmatrix} 1 & 0 & 0 & \delta^{5} \\ 0 & 1 & \delta^{5} & 0 \end{bmatrix}_{48059} = \begin{bmatrix} 1 & 0 & 0 & 11 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{48059} = \mathbf{Pl}(10, 11, 1, 1, 0, 0)_{73}$$

$$\ell_{26} = c_{56} = \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 1 & 0 & \delta^{10} \end{bmatrix}_{2890} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 0 & 10 \end{bmatrix}_{2890} = \mathbf{Pl}(11, 10, 0, 0, 1, 1)_{8971}$$

Rank of lines: (540, 3260, 289, 3179, 43690, 4379, 3019, 449, 4378, 43691, 3270, 530, 48049, 2746, 3163, 2997, 539, 433, 2906, 3269, 2987, 2996, 48058, 4369, 43681, 48059, 2890)Rank of points on Klein quadric: (50505, 46146, 8961, 8970, 74, 223, 45681, 49770, 209, 208, 9705, 9426, 199, 49761, 49771, 46425, 46456, 45691, 45690, 50536, 50226, 9736, 224, 64, 214, 73, 8971)

#### **Eckardt Points**

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The surface has 45 Eckardt points:
0: E_{36} = a_3 \cap b_6 \cap c_{36} = P_4 = \mathbf{P}(1, 1, 1, 1) = \mathbf{P}(1, 1, 1, 1),
1: E_{16} = a_1 \cap b_6 \cap c_{16} = P_5 = \mathbf{P}(1, 1, 0, 0) = \mathbf{P}(1, 1, 0, 0),
2: E_{25} = a_2 \cap b_5 \cap c_{25} = P_{14} = \mathbf{P}(\delta^{10}, 1, 0, 0) = \mathbf{P}(10, 1, 0, 0),
3: E_{15,26,34} = c_{15} \cap c_{26} \cap c_{34} = P_{15} = \mathbf{P}(\delta^5, 1, 0, 0) = \mathbf{P}(11, 1, 0, 0),
4: E_{32} = a_3 \cap b_2 \cap c_{23} = P_{20} = \mathbf{P}(1, 0, 1, 0) = \mathbf{P}(1, 0, 1, 0), 
5: E_{41} = a_4 \cap b_1 \cap c_{14} = P_{29} = \mathbf{P}(\delta^{10}, 0, 1, 0) = \mathbf{P}(10, 0, 1, 0),
6: E_{13,24,56} = c_{13} \cap c_{24} \cap c_{56} = P_{30} = \mathbf{P}(\delta^5, 0, 1, 0) = \mathbf{P}(11, 0, 1, 0),
7: E_{12,36,45} = c_{12} \cap c_{36} \cap c_{45} = P_{35} = \mathbf{P}(0,1,1,0) = \mathbf{P}(0,1,1,0),
8: E_{64} = a_6 \cap b_4 \cap c_{46} = P_{179} = \mathbf{P}(0, \delta^{10}, 1, 0) = \mathbf{P}(0, 10, 1, 0),
9: E_{53} = a_5 \cap b_3 \cap c_{35} = P_{195} = \mathbf{P}(0, \delta^5, 1, 0) = \mathbf{P}(0, 11, 1, 0),
10: E_{63} = a_6 \cap b_3 \cap c_{36} = P_{275} = \mathbf{P}(1, 0, 0, 1) = \mathbf{P}(1, 0, 0, 1),
11: E_{12,35,46} = c_{12} \cap c_{35} \cap c_{46} = P_{284} = \mathbf{P}(\delta^{10}, 0, 0, 1) = \mathbf{P}(10, 0, 0, 1),
12: E_{54} = a_5 \cap b_4 \cap c_{45} = P_{285} = \mathbf{P}(\delta^5, 0, 0, 1) = \mathbf{P}(11, 0, 0, 1),
13: E_{31} = a_3 \cap b_1 \cap c_{13} = P_{290} = \mathbf{P}(0, 1, 0, 1) = \mathbf{P}(0, 1, 0, 1),
14: E_{42} = a_4 \cap b_2 \cap c_{24} = P_{434} = \mathbf{P}(0, \delta^{10}, 0, 1) = \mathbf{P}(0, 10, 0, 1),
15: E_{14,23,56} = c_{14} \cap c_{23} \cap c_{56} = P_{450} = \mathbf{P}(0, \delta^5, 0, 1) = \mathbf{P}(0, 11, 0, 1),
16: E_{26} = a_2 \cap b_6 \cap c_{26} = P_{530} = \mathbf{P}(0, 0, 1, 1) = \mathbf{P}(0, 0, 1, 1),
17: E_{21} = a_2 \cap b_1 \cap c_{12} = P_{555} = \mathbf{P}(\delta^{10}, 1, 1, 1) = \mathbf{P}(10, 1, 1, 1),
18: E_{13,26,45} = c_{13} \cap c_{26} \cap c_{45} = P_{556} = \mathbf{P}(\delta^5, 1, 1, 1) = \mathbf{P}(11, 1, 1, 1),
19: E_{62} = a_6 \cap b_2 \cap c_{26} = P_{690} = \mathbf{P}(1, \delta^{10}, 1, 1) = \mathbf{P}(1, 10, 1, 1),
20: E_{46} = a_4 \cap b_6 \cap c_{46} = P_{699} = \mathbf{P}(\delta^{10}, \delta^{10}, 1, 1) = \mathbf{P}(10, 10, 1, 1),
21: E_{24} = a_2 \cap b_4 \cap c_{24} = P_{700} = \mathbf{P}(\delta^5, \delta^{10}, 1, 1) = \mathbf{P}(11, 10, 1, 1),
22: E_{23} = a_2 \cap b_3 \cap c_{23} = P_{706} = \mathbf{P}(1, \delta^5, 1, 1) = \mathbf{P}(1, 11, 1, 1),
23: E_{14,26,35} = c_{14} \cap c_{26} \cap c_{35} = P_{715} = \mathbf{P}(\delta^{10}, \delta^5, 1, 1) = \mathbf{P}(10, 11, 1, 1),
24: E_{56} = a_5 \cap b_6 \cap c_{56} = P_{716} = \mathbf{P}(\delta^5, \delta^5, 1, 1) = \mathbf{P}(11, 11, 1, 1),
25: E_{15} = a_1 \cap b_5 \cap c_{15} = P_{2833} = \mathbf{P}(0, 0, \delta^{10}, 1) = \mathbf{P}(0, 0, 10, 1),
26: E_{13} = a_1 \cap b_3 \cap c_{13} = P_{2850} = \mathbf{P}(1, 1, \delta^{10}, 1) = \mathbf{P}(1, 1, 10, 1),
27: E_{35} = a_3 \cap b_5 \cap c_{35} = P_{2859} = \mathbf{P}(\delta^{10}, 1, \delta^{10}, 1) = \mathbf{P}(10, 1, 10, 1),
28: E_{51} = a_5 \cap b_1 \cap c_{15} = P_{2860} = \mathbf{P}(\delta^5, 1, \delta^{10}, 1) = \mathbf{P}(11, 1, 10, 1),
29: E_{15,24,36} = c_{15} \cap c_{24} \cap c_{36} = P_{2994} = \mathbf{P}(1, \delta^{10}, \delta^{10}, 1) = \mathbf{P}(1, 10, 10, 1),
30: E_{12} = a_1 \cap b_2 \cap c_{12} = P_{3003} = \mathbf{P}(\delta^{10}, \delta^{10}, \delta^{10}, 1) = \mathbf{P}(10, 10, 10, 1),
31: E_{45} = a_4 \cap b_5 \cap c_{45} = P_{3004} = \mathbf{P}(\delta^5, \delta^{10}, \delta^{10}, 1) = \mathbf{P}(11, 10, 10, 1),
32: E_{65} = a_6 \cap b_5 \cap c_{56} = P_{3010} = \mathbf{P}(1, \delta^5, \delta^{10}, 1) = \mathbf{P}(1, 11, 10, 1),
33: E_{15,23,46} = c_{15} \cap c_{23} \cap c_{46} = P_{3019} = \mathbf{P}(\delta^{10}, \delta^5, \delta^{10}, 1) = \mathbf{P}(10, 11, 10, 1),
34: E_{14} = a_1 \cap b_4 \cap c_{14} = P_{3020} = \mathbf{P}(\delta^5, \delta^5, \delta^{10}, 1) = \mathbf{P}(11, 11, 10, 1),
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35: E_{16,25,34} = c_{16} \cap c_{25} \cap c_{34} = P_{3089} = \mathbf{P}(0,0,\delta^5,1) = \mathbf{P}(0,0,11,1),

36: E_{61} = a_6 \cap b_1 \cap c_{16} = P_{3106} = \mathbf{P}(1,1,\delta^5,1) = \mathbf{P}(1,1,11,1),

37: E_{13,25,46} = c_{13} \cap c_{25} \cap c_{46} = P_{3115} = \mathbf{P}(\delta^{10},1,\delta^5,1) = \mathbf{P}(10,1,11,1),

38: E_{34} = a_3 \cap b_4 \cap c_{34} = P_{3116} = \mathbf{P}(\delta^5,1,\delta^5,1) = \mathbf{P}(11,1,11,1),

39: E_{43} = a_4 \cap b_3 \cap c_{34} = P_{3250} = \mathbf{P}(1,\delta^{10},\delta^5,1) = \mathbf{P}(1,10,11,1),

40: E_{16,24,35} = c_{16} \cap c_{24} \cap c_{35} = P_{3259} = \mathbf{P}(\delta^{10},\delta^{10},\delta^5,1) = \mathbf{P}(10,10,11,1),

41: E_{52} = a_5 \cap b_2 \cap c_{25} = P_{3260} = \mathbf{P}(\delta^5,\delta^{10},\delta^5,1) = \mathbf{P}(11,10,11,1),

42: E_{14,25,36} = c_{14} \cap c_{25} \cap c_{36} = P_{3266} = \mathbf{P}(1,\delta^5,\delta^5,1) = \mathbf{P}(1,11,11,1),

43: E_{12,34,56} = c_{12} \cap c_{34} \cap c_{56} = P_{3275} = \mathbf{P}(\delta^{10},\delta^5,\delta^5,1) = \mathbf{P}(10,11,11,1),

44: E_{16,23,45} = c_{16} \cap c_{23} \cap c_{45} = P_{3276} = \mathbf{P}(\delta^5,\delta^5,\delta^5,1) = \mathbf{P}(11,11,11,1).
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#### **Double Points**

The surface has 0 Double points: The double points on the surface are:

#### Single Points

The surface has 324 single points: The single points on the surface are:

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0: P_{563} = (2, 2, 1, 1) lies on line b_6
                                                                   29: P_{752} = (15, 13, 1, 1) lies on line a_2
1: P_{574} = (13, 2, 1, 1) lies on line a_2
                                                                   30: P_{759} = (6, 14, 1, 1) lies on line c_{26}
2: P_{576} = (15, 2, 1, 1) lies on line c_{26}
                                                                   31: P_{761} = (8, 14, 1, 1) lies on line a_2
3: P_{580} = (3,3,1,1) lies on line b_6
                                                                   32: P_{767} = (14, 14, 1, 1) lies on line b_6
4: P_{581} = (4, 3, 1, 1) lies on line c_{26}
                                                                   33: P_{771} = (2, 15, 1, 1) lies on line a_2
                                                                   34: P_{782} = (13, 15, 1, 1) lies on line c_{26}
5: P_{584} = (7, 3, 1, 1) lies on line a_2
6: P_{596} = (3, 4, 1, 1) lies on line a_2
                                                                   35: P_{784} = (15, 15, 1, 1) lies on line b_6
7: P_{597} = (4, 4, 1, 1) lies on line b_6
                                                                   36: P_{803} = (2, 1, 2, 1) lies on line a_3
                                                                   37: P_{814} = (13, 1, 2, 1) lies on line b_1
8: P_{600} = (7, 4, 1, 1) lies on line c_{26}
9: P_{614} = (5, 5, 1, 1) lies on line b_6
                                                                   38: P_{816} = (15, 1, 2, 1) lies on line c_{13}
10: P_{618} = (9, 5, 1, 1) lies on line a_2
                                                                   39: P_{818} = (1, 2, 2, 1) lies on line c_{36}
11: P_{621} = (12, 5, 1, 1) lies on line c_{26}
                                                                   40: P_{827} = (10, 2, 2, 1) lies on line c_{12}
12: P_{631} = (6, 6, 1, 1) lies on line b_6
                                                                   41: P_{828} = (11, 2, 2, 1) lies on line c_{45}
13: P_{633} = (8, 6, 1, 1) lies on line c_{26}
                                                                   42: P_{947} = (2, 10, 2, 1) lies on line b_2
14: P_{639} = (14, 6, 1, 1) lies on line a_2
                                                                   43: P_{958} = (13, 10, 2, 1) lies on line a_4
15: P_{644} = (3, 7, 1, 1) lies on line c_{26}
                                                                   44: P_{960} = (15, 10, 2, 1) lies on line c_{24}
16: P_{645} = (4,7,1,1) lies on line a_2
                                                                   45: P_{963} = (2, 11, 2, 1) lies on line c_{23}
17: P_{648} = (7, 7, 1, 1) lies on line b_6
                                                                   46: P_{974} = (13, 11, 2, 1) lies on line c_{14}
18: P_{663} = (6, 8, 1, 1) lies on line a_2
                                                                   47: P_{976} = (15, 11, 2, 1) lies on line c_{56}
19: P_{665} = (8, 8, 1, 1) lies on line b_6
                                                                   48: P_{994} = (1, 13, 2, 1) lies on line a_6
20: P_{671} = (14, 8, 1, 1) lies on line c_{26}
                                                                   49: P_{1003} = (10, 13, 2, 1) lies on line c_{46}
21: P_{678} = (5, 9, 1, 1) lies on line c_{26}
                                                                   50: P_{1004} = (11, 13, 2, 1) lies on line b_4
22: P_{682} = (9, 9, 1, 1) lies on line b_6
                                                                   51: P_{1026} = (1, 15, 2, 1) lies on line b_3
23: P_{685} = (12, 9, 1, 1) lies on line a_2
                                                                   52: P_{1035} = (10, 15, 2, 1) lies on line c_{35}
24: P_{726} = (5, 12, 1, 1) lies on line a_2
                                                                   53: P_{1036} = (11, 15, 2, 1) lies on line a_5
25: P_{730} = (9, 12, 1, 1) lies on line c_{26}
                                                                   54: P_{1060} = (3, 1, 3, 1) lies on line a_3
26: P_{733} = (12, 12, 1, 1) lies on line b_6
                                                                   55: P_{1061} = (4, 1, 3, 1) lies on line c_{13}
27: P_{739} = (2, 13, 1, 1) lies on line c_{26}
                                                                   56: P_{1064} = (7, 1, 3, 1) lies on line b_1
28: P_{750} = (13, 13, 1, 1) lies on line b_6
                                                                   57: P_{1090} = (1, 3, 3, 1) lies on line c_{36}
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58: P_{1099} = (10, 3, 3, 1) lies on line c_{12}
                                                                  112: P_{1915} = (10, 6, 6, 1) lies on line c_{12}
59: P_{1100} = (11, 3, 3, 1) lies on line c_{45}
                                                                  113: P_{1916} = (11, 6, 6, 1) lies on line c_{45}
60: P_{1106} = (1, 4, 3, 1) lies on line b_3
                                                                  114: P_{1938} = (1, 8, 6, 1) lies on line b_3
                                                                  115: P_{1947} = (10, 8, 6, 1) lies on line c_{35}
61: P_{1115} = (10, 4, 3, 1) lies on line c_{35}
62: P_{1116} = (11, 4, 3, 1) lies on line a_5
                                                                  116: P_{1948} = (11, 8, 6, 1) lies on line a_5
63: P_{1154} = (1,7,3,1) lies on line a_6
                                                                  117: P_{1975} = (6, 10, 6, 1) lies on line b_2
64: P_{1163} = (10, 7, 3, 1) lies on line c_{46}
                                                                  118: P_{1977} = (8, 10, 6, 1) lies on line c_{24}
65: P_{1164} = (11, 7, 3, 1) lies on line b_4
                                                                  119: P_{1983} = (14, 10, 6, 1) lies on line a_4
66: P_{1204} = (3, 10, 3, 1) lies on line b_2
                                                                  120: P_{1991} = (6, 11, 6, 1) lies on line c_{23}
67: P_{1205} = (4, 10, 3, 1) lies on line c_{24}
                                                                  121: P_{1993} = (8, 11, 6, 1) lies on line c_{56}
68: P_{1208} = (7, 10, 3, 1) lies on line a_4
                                                                  122: P_{1999} = (14, 11, 6, 1) lies on line c_{14}
69: P_{1220} = (3, 11, 3, 1) lies on line c_{23}
                                                                  123: P_{2034} = (1, 14, 6, 1) lies on line a_6
70: P_{1221} = (4, 11, 3, 1) lies on line c_{56}
                                                                  124: P_{2043} = (10, 14, 6, 1) lies on line c_{46}
71: P_{1224} = (7, 11, 3, 1) lies on line c_{14}
                                                                  125: P_{2044} = (11, 14, 6, 1) lies on line b_4
72: P_{1316} = (3, 1, 4, 1) lies on line b_1
                                                                  126: P_{2084} = (3, 1, 7, 1) lies on line c_{13}
73: P_{1317} = (4, 1, 4, 1) lies on line a_3
                                                                  127: P_{2085} = (4, 1, 7, 1) lies on line b_1
74: P_{1320} = (7, 1, 4, 1) lies on line c_{13}
                                                                  128: P_{2088} = (7, 1, 7, 1) lies on line a_3
75: P_{1346} = (1, 3, 4, 1) lies on line a_6
                                                                  129: P_{2114} = (1, 3, 7, 1) lies on line b_3
76: P_{1355} = (10, 3, 4, 1) lies on line c_{46}
                                                                  130: P_{2123} = (10, 3, 7, 1) lies on line c_{35}
77: P_{1356} = (11, 3, 4, 1) lies on line b_4
                                                                  131: P_{2124} = (11, 3, 7, 1) lies on line a_5
78: P_{1362} = (1, 4, 4, 1) lies on line c_{36}
                                                                  132: P_{2130} = (1, 4, 7, 1) lies on line a_6
79: P_{1371} = (10, 4, 4, 1) lies on line c_{12}
                                                                  133: P_{2139} = (10, 4, 7, 1) lies on line c_{46}
                                                                  134: P_{2140} = (11, 4, 7, 1) lies on line b_4
80: P_{1372} = (11, 4, 4, 1) lies on line c_{45}
                                                                  135 : P_{2178} = (1, 7, 7, 1) lies on line c_{36}
81: P_{1410} = (1,7,4,1) lies on line b_3
82: P_{1419} = (10, 7, 4, 1) lies on line c_{35}
                                                                  136: P_{2187} = (10, 7, 7, 1) lies on line c_{12}
83: P_{1420} = (11, 7, 4, 1) lies on line a_5
                                                                  137: P_{2188} = (11, 7, 7, 1) lies on line c_{45}
84: P_{1460} = (3, 10, 4, 1) lies on line a_4
                                                                  138: P_{2228} = (3, 10, 7, 1) lies on line c_{24}
85: P_{1461} = (4, 10, 4, 1) lies on line b_2
                                                                  139: P_{2229} = (4, 10, 7, 1) lies on line a_4
86: P_{1464} = (7, 10, 4, 1) lies on line c_{24}
                                                                  140: P_{2232} = (7, 10, 7, 1) lies on line b_2
87: P_{1476} = (3, 11, 4, 1) lies on line c_{14}
                                                                  141: P_{2244} = (3, 11, 7, 1) lies on line c_{56}
88: P_{1477} = (4, 11, 4, 1) lies on line c_{23}
                                                                  142: P_{2245} = (4, 11, 7, 1) lies on line c_{14}
89: P_{1480} = (7, 11, 4, 1) lies on line c_{56}
                                                                  143: P_{2248} = (7, 11, 7, 1) lies on line c_{23}
90: P_{1574} = (5, 1, 5, 1) lies on line a_3
                                                                  144: P_{2343} = (6, 1, 8, 1) lies on line b_1
91: P_{1578} = (9, 1, 5, 1) lies on line b_1
                                                                  145: P_{2345} = (8, 1, 8, 1) lies on line a_3
92: P_{1581} = (12, 1, 5, 1) lies on line c_{13}
                                                                  146: P_{2351} = (14, 1, 8, 1) lies on line c_{13}
93: P_{1634} = (1, 5, 5, 1) lies on line c_{36}
                                                                  147: P_{2418} = (1, 6, 8, 1) lies on line a_6
94: P_{1643} = (10, 5, 5, 1) lies on line c_{12}
                                                                  148: P_{2427} = (10, 6, 8, 1) lies on line c_{46}
                                                                  149: P_{2428} = (11, 6, 8, 1) lies on line b_4
95: P_{1644} = (11, 5, 5, 1) lies on line c_{45}
96: P_{1698} = (1, 9, 5, 1) lies on line a_6
                                                                  150: P_{2450} = (1, 8, 8, 1) lies on line c_{36}
97: P_{1707} = (10, 9, 5, 1) lies on line c_{46}
                                                                  151: P_{2459} = (10, 8, 8, 1) lies on line c_{12}
98: P_{1708} = (11, 9, 5, 1) lies on line b_4
                                                                  152: P_{2460} = (11, 8, 8, 1) lies on line c_{45}
99: P_{1718} = (5, 10, 5, 1) lies on line b_2
                                                                  153: P_{2487} = (6, 10, 8, 1) lies on line a_4
100: P_{1722} = (9, 10, 5, 1) lies on line a_4
                                                                  154: P_{2489} = (8, 10, 8, 1) lies on line b_2
101: P_{1725} = (12, 10, 5, 1) lies on line c_{24}
                                                                  155: P_{2495} = (14, 10, 8, 1) lies on line c_{24}
102: P_{1734} = (5, 11, 5, 1) lies on line c_{23}
                                                                  156: P_{2503} = (6, 11, 8, 1) lies on line c_{14}
                                                                  157: P_{2505} = (8, 11, 8, 1) lies on line c_{23}
103: P_{1738} = (9, 11, 5, 1) lies on line c_{14}
104: P_{1741} = (12, 11, 5, 1) lies on line c_{56}
                                                                  158: P_{2511} = (14, 11, 8, 1) lies on line c_{56}
105: P_{1746} = (1, 12, 5, 1) lies on line b_3
                                                                  159: P_{2546} = (1, 14, 8, 1) lies on line b_3
106: P_{1755} = (10, 12, 5, 1) lies on line c_{35}
                                                                  160: P_{2555} = (10, 14, 8, 1) lies on line c_{35}
107: P_{1756} = (11, 12, 5, 1) lies on line a_5
                                                                  161: P_{2556} = (11, 14, 8, 1) lies on line a_5
108: P_{1831} = (6, 1, 6, 1) lies on line a_3
                                                                  162: P_{2598} = (5, 1, 9, 1) lies on line c_{13}
109: P_{1833} = (8, 1, 6, 1) lies on line c_{13}
                                                                  163: P_{2602} = (9, 1, 9, 1) lies on line a_3
                                                                  164: P_{2605} = (12, 1, 9, 1) lies on line b_1
110: P_{1839} = (14, 1, 6, 1) lies on line b_1
111: P_{1906} = (1, 6, 6, 1) lies on line c_{36}
                                                                  165: P_{2658} = (1, 5, 9, 1) lies on line b_3
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166: P_{2667} = (10, 5, 9, 1) lies on line c_{35}
                                                                  220: P_{3141} = (4, 3, 11, 1) lies on line c_{34}
167: P_{2668} = (11, 5, 9, 1) lies on line a_5
                                                                  221: P_{3144} = (7, 3, 11, 1) lies on line c_{25}
168: P_{2722} = (1, 9, 9, 1) lies on line c_{36}
                                                                  222: P_{3156} = (3, 4, 11, 1) lies on line c_{25}
169: P_{2731} = (10, 9, 9, 1) lies on line c_{12}
                                                                  223: P_{3157} = (4, 4, 11, 1) lies on line c_{16}
170: P_{2732} = (11, 9, 9, 1) lies on line c_{45}
                                                                  224: P_{3160} = (7, 4, 11, 1) lies on line c_{34}
171: P_{2742} = (5, 10, 9, 1) lies on line c_{24}
                                                                  225: P_{3174} = (5, 5, 11, 1) lies on line c_{16}
172: P_{2746} = (9, 10, 9, 1) lies on line b_2
                                                                  226: P_{3178} = (9, 5, 11, 1) lies on line c_{25}
173: P_{2749} = (12, 10, 9, 1) lies on line a_4
                                                                  227: P_{3181} = (12, 5, 11, 1) lies on line c_{34}
174: P_{2758} = (5, 11, 9, 1) lies on line c_{56}
                                                                  228: P_{3191} = (6, 6, 11, 1) lies on line c_{16}
175: P_{2762} = (9, 11, 9, 1) lies on line c_{23}
                                                                  229: P_{3193} = (8, 6, 11, 1) lies on line c_{34}
176: P_{2765} = (12, 11, 9, 1) lies on line c_{14}
                                                                  230: P_{3199} = (14, 6, 11, 1) lies on line c_{25}
                                                                  231: P_{3204} = (3, 7, 11, 1) lies on line c_{34}
177: P_{2770} = (1, 12, 9, 1) lies on line a_6
178: P_{2779} = (10, 12, 9, 1) lies on line c_{46}
                                                                  232: P_{3205} = (4, 7, 11, 1) lies on line c_{25}
179: P_{2780} = (11, 12, 9, 1) lies on line b_4
                                                                  233: P_{3208} = (7, 7, 11, 1) lies on line c_{16}
180 : P_{2867} = (2, 2, 10, 1) lies on line a_1
                                                                  234: P_{3223} = (6, 8, 11, 1) lies on line c_{25}
181: P_{2878} = (13, 2, 10, 1) lies on line b_5
                                                                  235: P_{3225} = (8, 8, 11, 1) lies on line c_{16}
182: P_{2880} = (15, 2, 10, 1) lies on line c_{15}
                                                                  236: P_{3231} = (14, 8, 11, 1) lies on line c_{34}
183 : P_{2884} = (3, 3, 10, 1) lies on line a_1
                                                                  237: P_{3238} = (5, 9, 11, 1) lies on line c_{34}
184: P_{2885} = (4, 3, 10, 1) lies on line c_{15}
                                                                  238: P_{3242} = (9, 9, 11, 1) lies on line c_{16}
185: P_{2888} = (7, 3, 10, 1) lies on line b_5
                                                                  239: P_{3245} = (12, 9, 11, 1) lies on line c_{25}
186: P_{2900} = (3, 4, 10, 1) lies on line b_5
                                                                  240: P_{3286} = (5, 12, 11, 1) lies on line c_{25}
187: P_{2901} = (4, 4, 10, 1) lies on line a_1
                                                                  241: P_{3290} = (9, 12, 11, 1) lies on line c_{34}
188: P_{2904} = (7, 4, 10, 1) lies on line c_{15}
                                                                  242: P_{3293} = (12, 12, 11, 1) lies on line c_{16}
189: P_{2918} = (5, 5, 10, 1) lies on line a_1
                                                                  243: P_{3299} = (2, 13, 11, 1) lies on line c_{34}
190: P_{2922} = (9, 5, 10, 1) lies on line b_5
                                                                  244: P_{3310} = (13, 13, 11, 1) lies on line c_{16}
191: P_{2925} = (12, 5, 10, 1) lies on line c_{15}
                                                                  245: P_{3312} = (15, 13, 11, 1) lies on line c_{25}
192: P_{2935} = (6, 6, 10, 1) lies on line a_1
                                                                  246: P_{3319} = (6, 14, 11, 1) lies on line c_{34}
193: P_{2937} = (8, 6, 10, 1) lies on line c_{15}
                                                                  247: P_{3321} = (8, 14, 11, 1) lies on line c_{25}
194: P_{2943} = (14, 6, 10, 1) lies on line b_5
                                                                  248: P_{3327} = (14, 14, 11, 1) lies on line c_{16}
195: P_{2948} = (3, 7, 10, 1) lies on line c_{15}
                                                                  249: P_{3331} = (2, 15, 11, 1) lies on line c_{25}
196: P_{2949} = (4, 7, 10, 1) lies on line b_5
                                                                  250: P_{3342} = (13, 15, 11, 1) lies on line c_{34}
197: P_{2952} = (7, 7, 10, 1) lies on line a_1
                                                                  251: P_{3344} = (15, 15, 11, 1) lies on line c_{16}
198: P_{2967} = (6, 8, 10, 1) lies on line b_5
                                                                  252: P_{3366} = (5, 1, 12, 1) lies on line b_1
199: P_{2969} = (8, 8, 10, 1) lies on line a_1
                                                                  253: P_{3370} = (9, 1, 12, 1) lies on line c_{13}
200: P_{2975} = (14, 8, 10, 1) lies on line c_{15}
                                                                  254: P_{3373} = (12, 1, 12, 1) lies on line a_3
201: P_{2982} = (5, 9, 10, 1) lies on line c_{15}
                                                                  255: P_{3426} = (1, 5, 12, 1) lies on line a_6
202: P_{2986} = (9, 9, 10, 1) lies on line a_1
                                                                  256: P_{3435} = (10, 5, 12, 1) lies on line c_{46}
203: P_{2989} = (12, 9, 10, 1) lies on line b_5
                                                                  257: P_{3436} = (11, 5, 12, 1) lies on line b_4
204: P_{3030} = (5, 12, 10, 1) lies on line b_5
                                                                  258: P_{3490} = (1, 9, 12, 1) lies on line b_3
205: P_{3034} = (9, 12, 10, 1) lies on line c_{15}
                                                                  259: P_{3499} = (10, 9, 12, 1) lies on line c_{35}
206: P_{3037} = (12, 12, 10, 1) lies on line a_1
                                                                  260: P_{3500} = (11, 9, 12, 1) lies on line a_5
207: P_{3043} = (2, 13, 10, 1) lies on line c_{15}
                                                                  261: P_{3510} = (5, 10, 12, 1) lies on line a_4
208: P_{3054} = (13, 13, 10, 1) lies on line a_1
                                                                  262: P_{3514} = (9, 10, 12, 1) lies on line c_{24}
209: P_{3056} = (15, 13, 10, 1) lies on line b_5
                                                                  263: P_{3517} = (12, 10, 12, 1) lies on line b_2
210: P_{3063} = (6, 14, 10, 1) lies on line c_{15}
                                                                  264: P_{3526} = (5, 11, 12, 1) lies on line c_{14}
211: P_{3065} = (8, 14, 10, 1) lies on line b_5
                                                                  265: P_{3530} = (9, 11, 12, 1) lies on line c_{56}
212: P_{3071} = (14, 14, 10, 1) lies on line a_1
                                                                  266: P_{3533} = (12, 11, 12, 1) lies on line c_{23}
213: P_{3075} = (2, 15, 10, 1) lies on line b_5
                                                                  267: P_{3538} = (1, 12, 12, 1) lies on line c_{36}
214: P_{3086} = (13, 15, 10, 1) lies on line c_{15}
                                                                  268: P_{3547} = (10, 12, 12, 1) lies on line c_{12}
215: P_{3088} = (15, 15, 10, 1) lies on line a_1
                                                                  269: P_{3548} = (11, 12, 12, 1) lies on line c_{45}
216: P_{3123} = (2, 2, 11, 1) lies on line c_{16}
                                                                  270: P_{3619} = (2, 1, 13, 1) lies on line c_{13}
217: P_{3134} = (13, 2, 11, 1) lies on line c_{25}
                                                                  271: P_{3630} = (13, 1, 13, 1) lies on line a_3
218: P_{3136} = (15, 2, 11, 1) lies on line c_{34}
                                                                  272: P_{3632} = (15, 1, 13, 1) lies on line b_1
219: P_{3140} = (3, 3, 11, 1) lies on line c_{16}
                                                                  273: P_{3634} = (1, 2, 13, 1) lies on line b_3
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300: P_{4039} = (6, 11, 14, 1) lies on line c_{56}
274: P_{3643} = (10, 2, 13, 1) lies on line c_{35}
275: P_{3644} = (11, 2, 13, 1) lies on line a_5
                                                                  301: P_{4041} = (8, 11, 14, 1) lies on line c_{14}
276: P_{3763} = (2, 10, 13, 1) lies on line c_{24}
                                                                  302: P_{4047} = (14, 11, 14, 1) lies on line c_{23}
277: P_{3774} = (13, 10, 13, 1) lies on line b_2
                                                                  303: P_{4082} = (1, 14, 14, 1) lies on line c_{36}
278: P_{3776} = (15, 10, 13, 1) lies on line a_4
                                                                  304: P_{4091} = (10, 14, 14, 1) lies on line c_{12}
279: P_{3779} = (2, 11, 13, 1) lies on line c_{56}
                                                                  305: P_{4092} = (11, 14, 14, 1) lies on line c_{45}
280: P_{3790} = (13, 11, 13, 1) lies on line c_{23}
                                                                  306: P_{4131} = (2, 1, 15, 1) lies on line b_1
281: P_{3792} = (15, 11, 13, 1) lies on line c_{14}
                                                                  307: P_{4142} = (13, 1, 15, 1) lies on line c_{13}
282 : P_{3810} = (1, 13, 13, 1) lies on line c_{36}
                                                                  308: P_{4144} = (15, 1, 15, 1) lies on line a_3
283: P_{3819} = (10, 13, 13, 1) lies on line c_{12}
                                                                  309: P_{4146} = (1, 2, 15, 1) lies on line a_6
284: P_{3820} = (11, 13, 13, 1) lies on line c_{45}
                                                                  310: P_{4155} = (10, 2, 15, 1) lies on line c_{46}
285: P_{3842} = (1, 15, 13, 1) lies on line a_6
                                                                  311: P_{4156} = (11, 2, 15, 1) lies on line b_4
286: P_{3851} = (10, 15, 13, 1) lies on line c_{46}
                                                                  312: P_{4275} = (2, 10, 15, 1) lies on line a_4
                                                                  313: P_{4286} = (13, 10, 15, 1) lies on line c_{24}
287: P_{3852} = (11, 15, 13, 1) lies on line b_4
288: P_{3879} = (6, 1, 14, 1) lies on line c_{13}
                                                                  314: P_{4288} = (15, 10, 15, 1) lies on line b_2
289: P_{3881} = (8, 1, 14, 1) lies on line b_1
                                                                  315: P_{4291} = (2, 11, 15, 1) lies on line c_{14}
290: P_{3887} = (14, 1, 14, 1) lies on line a_3
                                                                  316: P_{4302} = (13, 11, 15, 1) lies on line c_{56}
291 : P_{3954} = (1, 6, 14, 1) lies on line b_3
                                                                  317: P_{4304} = (15, 11, 15, 1) lies on line c_{23}
292: P_{3963} = (10, 6, 14, 1) lies on line c_{35}
                                                                  318: P_{4322} = (1, 13, 15, 1) lies on line b_3
293: P_{3964} = (11, 6, 14, 1) lies on line a_5
                                                                  319: P_{4331} = (10, 13, 15, 1) lies on line c_{35}
294: P_{3986} = (1, 8, 14, 1) lies on line a_6
                                                                  320: P_{4332} = (11, 13, 15, 1) lies on line a_5
295 : P_{3995} = (10, 8, 14, 1) lies on line c_{46}
                                                                  321: P_{4354} = (1, 15, 15, 1) lies on line c_{36}
296: P_{3996} = (11, 8, 14, 1) lies on line b_4
                                                                  322: P_{4363} = (10, 15, 15, 1) lies on line c_{12}
297: P_{4023} = (6, 10, 14, 1) lies on line c_{24}
                                                                  323: P_{4364} = (11, 15, 15, 1) lies on line c_{45}
298: P_{4025} = (8, 10, 14, 1) lies on line a_4
299: P_{4031} = (14, 10, 14, 1) lies on line b_2
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The single points on the surface are:

#### Points on surface but on no line

The surface has 0 points not on any line: The points on the surface but not on lines are:

# Line Intersection Graph

 $0\ \ 1\ \ 2\ \ 3\ \ 4\ \ 5\ \ 6\ \ 7\ \ 8\ \ 9\ 10\ 11\ \ 12\ \ 13\ \ 14\ \ 15\ \ 16\ \ 17\ \ 18\ \ 19\ \ 20\ \ 21\ \ 22\ \ 23\ \ 24\ \ 25\ \ 26$  $a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_6 \ b_1 \ b_2 \ b_3 \ b_4 \ b_5 \ b_6 \ c_{12} \ c_{13} \ c_{14} \ c_{15} \ c_{16} \ c_{23} \ c_{24} \ c_{25} \ c_{26} \ c_{34} \ c_{35} \ c_{36} \ c_{45} \ c_{46} \ c_{56}$  $1 \quad 1 \quad 0 \quad 0$  $2 a_3 \mid 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 0 \ 1 \ 1$  $0 \ 0 \ 1$  $0 \quad 1$  $0 \ 0 \ 0$  $0 \quad 0$  $4 a_{5} \mid 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$ 1 0  $5 \ a_6 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0$  $1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0$  $7 |b_2|$  $0 \ 0 \ 1$  $1 \ 0 \ 1$  $1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0$  $8 \ b_3$  $0 \quad 1$  $0 \quad 0$  $b_6$  1 1 1 1 1 0 0 0 0 0 0 0  $12 c_{12} | 1 1 0 0 0 0 1 1 0 0 0 0 0 0$ 0 0 0 1 1  $13 c_{13} | 1 0 1 0 0 0 1 0 1 0 0 0$  $0 \quad 0$  $0 \quad 0$  $15 c_{15} | 1 0 0 0 1 0 1 0 0 0 1 0 0$  $0 \ 0 \ 1$ 1 0  $18 c_{24} | 0 1 0 1 0 0 0 1 0 1 0 0 0 1 0$  $1 \ 1 \ 0 \ 0 \ 0$ 0 1 0 0 0 1 0 0 0 0 0 1 0 0 1 0 0  $22 c_{35} \mid 0 \quad 0 \quad 1 \quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 0 \quad 1 \quad 0$ 0 1  $0 \ 1 \ 0 \ 1$  $23 c_{36} | 0 0 1 0 0 1 0 0 1 0 0 1 1 0 1$ 1 0 0 1 1 0  $26\,c_{56} | \ 0\ 0\ 0\ 0\ 1\ 1\ 0\ 0\ 0\ 1\ 1\ 1\ 1\ 1\ 1\ 0\ 0\ 1\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 0$ 

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$
in point	$P_{3003}$	$P_{2850}$	$P_{3020}$	$P_{2833}$	$P_5$	$P_{3003}$	$P_{2850}$	$P_{3020}$	$P_{2833}$	$P_5$

#### Line 1 intersects

Line	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$
in point	$P_{555}$	$P_{706}$	$P_{700}$	$P_{14}$	$P_{530}$	$P_{555}$	$P_{706}$	$P_{700}$	$P_{14}$	$P_{530}$

#### Line 2 intersects

Line	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$	$\ell_{17}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$
in point	$P_{290}$	$P_{20}$	$P_{3116}$	$P_{2859}$	$P_4$	$P_{290}$	$P_{20}$	$P_{3116}$	$P_{2859}$	$P_4$

#### Line 3 intersects

Line	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{14}$	$\ell_{18}$	$\ell_{21}$	$\ell_{24}$	$\ell_{25}$
in point	$P_{29}$	$P_{434}$	$P_{3250}$	$P_{3004}$	$P_{699}$	$P_{29}$	$P_{434}$	$P_{3250}$	$P_{3004}$	$P_{699}$

## Line 4 intersects

Line	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{15}$	$\ell_{19}$	$\ell_{22}$	$\ell_{24}$	$\ell_{26}$
in point	$P_{2860}$	$P_{3260}$	$P_{195}$	$P_{285}$	$P_{716}$	$P_{2860}$	$P_{3260}$	$P_{195}$	$P_{285}$	$P_{716}$

## Line 5 intersects

Line	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{16}$	$\ell_{20}$	$\ell_{23}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{3106}$	$P_{690}$	$P_{275}$	$P_{179}$	$P_{3010}$	$P_{3106}$	$P_{690}$	$P_{275}$	$P_{179}$	$P_{3010}$

#### Line 6 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$
in point	$P_{555}$	$P_{290}$	$P_{29}$	$P_{2860}$	$P_{3106}$	$P_{555}$	$P_{290}$	$P_{29}$	$P_{2860}$	$P_{3106}$

## Line 7 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{12}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$
in point	$P_{3003}$	$P_{20}$	$P_{434}$	$P_{3260}$	$P_{690}$	$P_{3003}$	$P_{20}$	$P_{434}$	$P_{3260}$	$P_{690}$

# Line 8 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{13}$	$\ell_{17}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$
in point	$P_{2850}$	$P_{706}$	$P_{3250}$	$P_{195}$	$P_{275}$	$P_{2850}$	$P_{706}$	$P_{3250}$	$P_{195}$	$P_{275}$

## Line 9 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_{14}$	$\ell_{18}$	$\ell_{21}$	$\ell_{24}$	$\ell_{25}$
in point	$P_{3020}$	$P_{700}$	$P_{3116}$	$P_{285}$	$P_{179}$	$P_{3020}$	$P_{700}$	$P_{3116}$	$P_{285}$	$P_{179}$

# ${\rm Line}\ 10\ {\rm intersects}$

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_{15}$	$\ell_{19}$	$\ell_{22}$	$\ell_{24}$	$\ell_{26}$
in point	$P_{2833}$	$P_{14}$	$P_{2859}$	$P_{3004}$	$P_{3010}$	$P_{2833}$	$P_{14}$	$P_{2859}$	$P_{3004}$	$P_{3010}$

#### Line 11 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_{16}$	$\ell_{20}$	$\ell_{23}$	$\ell_{25}$	$\ell_{26}$
in point	$P_5$	$P_{530}$	$P_4$	$P_{699}$	$P_{716}$	$P_5$	$P_{530}$	$P_4$	$P_{699}$	$P_{716}$

## Line 12 intersects

I	Line	$\ell_0$	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in p	oint	$P_{3003}$	$P_{555}$	$P_{555}$	$P_{3003}$	$P_{3275}$	$P_{284}$	$P_{35}$	$P_{35}$	$P_{284}$	$P_{3275}$

# Line 13 intersects

Line	$\ell_0$	$\ell_2$	$\ell_6$	$\ell_8$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{2850}$	$P_{290}$	$P_{290}$	$P_{2850}$	$P_{30}$	$P_{3115}$	$P_{556}$	$P_{556}$	$P_{3115}$	$P_{30}$

#### Line 14 intersects

Line	$\ell_0$	$\ell_3$	$\ell_6$	$\ell_9$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{22}$	$\ell_{23}$	$\ell_{26}$
in point	$P_{3020}$	$P_{29}$	$P_{29}$	$P_{3020}$	$P_{450}$	$P_{3266}$	$P_{715}$	$P_{715}$	$P_{3266}$	$P_{450}$

#### Line 15 intersects

Line	$\ell_0$	$\ell_4$	$\ell_6$	$\ell_{10}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{21}$	$\ell_{23}$	$\ell_{25}$
in point	$P_{2833}$	$P_{2860}$	$P_{2860}$	$P_{2833}$	$P_{3019}$	$P_{2994}$	$P_{15}$	$P_{15}$	$P_{2994}$	$P_{3019}$

## Line 16 intersects

Line	$\ell_0$	$\ell_5$	$\ell_6$	$\ell_{11}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$
in point	$P_5$	$P_{3106}$	$P_{3106}$	$P_5$	$P_{3276}$	$P_{3259}$	$P_{3089}$	$P_{3089}$	$P_{3259}$	$P_{3276}$

# ${\rm Line}\ 17\ {\rm intersects}$

Line	$\ell_1$	$\ell_2$	$\ell_7$	$\ell_8$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{706}$	$P_{20}$	$P_{20}$	$P_{706}$	$P_{450}$	$P_{3019}$	$P_{3276}$	$P_{3276}$	$P_{3019}$	$P_{450}$

# Line 18 intersects

Line	$\ell_1$	$\ell_3$	$\ell_7$	$\ell_9$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{22}$	$\ell_{23}$	$\ell_{26}$
in point	$P_{700}$	$P_{434}$	$P_{434}$	$P_{700}$	$P_{30}$	$P_{2994}$	$P_{3259}$	$P_{3259}$	$P_{2994}$	$P_{30}$

# Line 19 intersects

Line	$\ell_1$	$\ell_4$	$\ell_7$	$\ell_{10}$	$\ell_{13}$	$\ell_{14}$	$\ell_{16}$	$\ell_{21}$	$\ell_{23}$	$\ell_{25}$
in point	$P_{14}$	$P_{3260}$	$P_{3260}$	$P_{14}$	$P_{3115}$	$P_{3266}$	$P_{3089}$	$P_{3089}$	$P_{3266}$	$P_{3115}$

## Line 20 intersects

Line	$\ell_1$	$\ell_5$	$\ell_7$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$
in point	$P_{530}$	$P_{690}$	$P_{690}$	$P_{530}$	$P_{556}$	$P_{715}$	$P_{15}$	$P_{15}$	$P_{715}$	$P_{556}$

# ${\bf Line~21~intersects}$

Line	$\ell_2$	$\ell_3$	$\ell_8$	$\ell_9$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$	$\ell_{19}$	$\ell_{20}$	$\ell_{26}$
in point	$P_{3116}$	$P_{3250}$	$P_{3250}$	$P_{3116}$	$P_{3275}$	$P_{15}$	$P_{3089}$	$P_{3089}$	$P_{15}$	$P_{3275}$

# ${\bf Line~22~intersects}$

Line	$\ell_2$	$\ell_4$	$\ell_8$	$\ell_{10}$	$\ell_{12}$	$\ell_{14}$	$\ell_{16}$	$\ell_{18}$	$\ell_{20}$	$\ell_{25}$
in point	$P_{2859}$	$P_{195}$	$P_{195}$	$P_{2859}$	$P_{284}$	$P_{715}$	$P_{3259}$	$P_{3259}$	$P_{715}$	$P_{284}$

# Line 23 intersects

Line	$\ell_2$	$\ell_5$	$\ell_8$	$\ell_{11}$	$\ell_{12}$	$\ell_{14}$	$\ell_{15}$	$\ell_{18}$	$\ell_{19}$	$\ell_{24}$
in point	$P_4$	$P_{275}$	$P_{275}$	$P_4$	$P_{35}$	$P_{3266}$	$P_{2994}$	$P_{2994}$	$P_{3266}$	$P_{35}$

# ${\bf Line~24~intersects}$

Line	$\ell_3$	$\ell_4$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{13}$	$\ell_{16}$	$\ell_{17}$	$\ell_{20}$	$\ell_{23}$
in point	$P_{3004}$	$P_{285}$	$P_{285}$	$P_{3004}$	$P_{35}$	$P_{556}$	$P_{3276}$	$P_{3276}$	$P_{556}$	$P_{35}$

## Line 25 intersects

Line	$\ell_3$	$\ell_5$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{15}$	$\ell_{17}$	$\ell_{19}$	$\ell_{22}$
in point	$P_{699}$	$P_{179}$	$P_{179}$	$P_{699}$	$P_{284}$	$P_{3115}$	$P_{3019}$	$P_{3019}$	$P_{3115}$	$P_{284}$

## Line 26 intersects

Line	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{18}$	$\ell_{21}$
in point	$P_{716}$	$P_{3010}$	$P_{3010}$	$P_{716}$	$P_{3275}$	$P_{30}$	$P_{450}$	$P_{450}$	$P_{30}$	$P_{3275}$

The surface has 369 points:

The points on the surface are:

$0: P_4 = (1, 1, 1, 1)$	9: $P_{195} = (0, 11, 1, 0)$	18: $P_{556} = (11, 1, 1, 1)$
$1: P_5 = (1, 1, 0, 0)$	$10: P_{275} = (1, 0, 0, 1)$	$19: P_{563} = (2, 2, 1, 1)$
$2: P_{14} = (10, 1, 0, 0)$	11: $P_{284} = (10, 0, 0, 1)$	$20: P_{574} = (13, 2, 1, 1)$
$3: P_{15} = (11, 1, 0, 0)$	$12: P_{285} = (11, 0, 0, 1)$	$21: P_{576} = (15, 2, 1, 1)$
$4: P_{20} = (1, 0, 1, 0)$	13: $P_{290} = (0, 1, 0, 1)$	$22: P_{580} = (3, 3, 1, 1)$
$5: P_{29} = (10, 0, 1, 0)$	$14: P_{434} = (0, 10, 0, 1)$	$23: P_{581} = (4,3,1,1)$
$6: P_{30} = (11, 0, 1, 0)$	$15: P_{450} = (0, 11, 0, 1)$	$24: P_{584} = (7, 3, 1, 1)$
$7: P_{35} = (0, 1, 1, 0)$	$16: P_{530} = (0, 0, 1, 1)$	$25: P_{596} = (3, 4, 1, 1)$
$8: P_{179} = (0, 10, 1, 0)$	17: $P_{555} = (10, 1, 1, 1)$	$26: P_{597} = (4, 4, 1, 1)$

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27: P_{600} = (7, 4, 1, 1)
                                            81: P_{1064} = (7, 1, 3, 1)
                                                                                        135: P_{1839} = (14, 1, 6, 1)
28: P_{614} = (5, 5, 1, 1)
                                            82: P_{1090} = (1, 3, 3, 1)
                                                                                        136: P_{1906} = (1, 6, 6, 1)
                                                                                        137: P_{1915} = (10, 6, 6, 1)
29: P_{618} = (9, 5, 1, 1)
                                            83: P_{1099} = (10, 3, 3, 1)
30: P_{621} = (12, 5, 1, 1)
                                            84: P_{1100} = (11, 3, 3, 1)
                                                                                        138: P_{1916} = (11, 6, 6, 1)
31: P_{631} = (6, 6, 1, 1)
                                            85: P_{1106} = (1, 4, 3, 1)
                                                                                        139: P_{1938} = (1, 8, 6, 1)
                                            86: P_{1115} = (10, 4, 3, 1)
32: P_{633} = (8, 6, 1, 1)
                                                                                        140: P_{1947} = (10, 8, 6, 1)
33: P_{639} = (14, 6, 1, 1)
                                            87: P_{1116} = (11, 4, 3, 1)
                                                                                        141: P_{1948} = (11, 8, 6, 1)
34: P_{644} = (3,7,1,1)
                                            88: P_{1154} = (1, 7, 3, 1)
                                                                                        142: P_{1975} = (6, 10, 6, 1)
35: P_{645} = (4,7,1,1)
                                            89: P_{1163} = (10, 7, 3, 1)
                                                                                        143: P_{1977} = (8, 10, 6, 1)
36: P_{648} = (7,7,1,1)
                                            90: P_{1164} = (11, 7, 3, 1)
                                                                                        144: P_{1983} = (14, 10, 6, 1)
37: P_{663} = (6, 8, 1, 1)
                                            91: P_{1204} = (3, 10, 3, 1)
                                                                                        145: P_{1991} = (6, 11, 6, 1)
38: P_{665} = (8, 8, 1, 1)
                                            92: P_{1205} = (4, 10, 3, 1)
                                                                                        146: P_{1993} = (8, 11, 6, 1)
39: P_{671} = (14, 8, 1, 1)
                                            93: P_{1208} = (7, 10, 3, 1)
                                                                                        147: P_{1999} = (14, 11, 6, 1)
40: P_{678} = (5, 9, 1, 1)
                                                                                        148: P_{2034} = (1, 14, 6, 1)
                                            94: P_{1220} = (3, 11, 3, 1)
41: P_{682} = (9, 9, 1, 1)
                                            95: P_{1221} = (4, 11, 3, 1)
                                                                                        149: P_{2043} = (10, 14, 6, 1)
42: P_{685} = (12, 9, 1, 1)
                                            96: P_{1224} = (7, 11, 3, 1)
                                                                                        150: P_{2044} = (11, 14, 6, 1)
43: P_{690} = (1, 10, 1, 1)
                                            97: P_{1316} = (3, 1, 4, 1)
                                                                                        151: P_{2084} = (3, 1, 7, 1)
44: P_{699} = (10, 10, 1, 1)
                                            98: P_{1317} = (4, 1, 4, 1)
                                                                                        152: P_{2085} = (4, 1, 7, 1)
45: P_{700} = (11, 10, 1, 1)
                                            99: P_{1320} = (7, 1, 4, 1)
                                                                                        153: P_{2088} = (7, 1, 7, 1)
46: P_{706} = (1, 11, 1, 1)
                                            100: P_{1346} = (1, 3, 4, 1)
                                                                                        154: P_{2114} = (1, 3, 7, 1)
47: P_{715} = (10, 11, 1, 1)
                                            101: P_{1355} = (10, 3, 4, 1)
                                                                                        155: P_{2123} = (10, 3, 7, 1)
48: P_{716} = (11, 11, 1, 1)
                                                                                        156: P_{2124} = (11, 3, 7, 1)
                                            102: P_{1356} = (11, 3, 4, 1)
                                                                                        157: P_{2130} = (1, 4, 7, 1)
49: P_{726} = (5, 12, 1, 1)
                                            103: P_{1362} = (1, 4, 4, 1)
50: P_{730} = (9, 12, 1, 1)
                                            104: P_{1371} = (10, 4, 4, 1)
                                                                                        158: P_{2139} = (10, 4, 7, 1)
51: P_{733} = (12, 12, 1, 1)
                                            105: P_{1372} = (11, 4, 4, 1)
                                                                                        159: P_{2140} = (11, 4, 7, 1)
52: P_{739} = (2, 13, 1, 1)
                                            106: P_{1410} = (1,7,4,1)
                                                                                        160: P_{2178} = (1, 7, 7, 1)
53: P_{750} = (13, 13, 1, 1)
                                                                                        161: P_{2187} = (10, 7, 7, 1)
                                            107: P_{1419} = (10, 7, 4, 1)
54: P_{752} = (15, 13, 1, 1)
                                            108: P_{1420} = (11, 7, 4, 1)
                                                                                        162: P_{2188} = (11, 7, 7, 1)
                                                                                        163: P_{2228} = (3, 10, 7, 1)
55: P_{759} = (6, 14, 1, 1)
                                            109: P_{1460} = (3, 10, 4, 1)
56: P_{761} = (8, 14, 1, 1)
                                            110: P_{1461} = (4, 10, 4, 1)
                                                                                        164: P_{2229} = (4, 10, 7, 1)
57: P_{767} = (14, 14, 1, 1)
                                            111: P_{1464} = (7, 10, 4, 1)
                                                                                        165: P_{2232} = (7, 10, 7, 1)
58: P_{771} = (2, 15, 1, 1)
                                            112: P_{1476} = (3, 11, 4, 1)
                                                                                        166: P_{2244} = (3, 11, 7, 1)
59: P_{782} = (13, 15, 1, 1)
                                            113: P_{1477} = (4, 11, 4, 1)
                                                                                        167: P_{2245} = (4, 11, 7, 1)
                                                                                        168: P_{2248} = (7, 11, 7, 1)
60: P_{784} = (15, 15, 1, 1)
                                            114: P_{1480} = (7, 11, 4, 1)
61: P_{803} = (2, 1, 2, 1)
                                            115: P_{1574} = (5, 1, 5, 1)
                                                                                        169: P_{2343} = (6, 1, 8, 1)
62: P_{814} = (13, 1, 2, 1)
                                            116: P_{1578} = (9, 1, 5, 1)
                                                                                        170: P_{2345} = (8, 1, 8, 1)
63: P_{816} = (15, 1, 2, 1)
                                            117: P_{1581} = (12, 1, 5, 1)
                                                                                        171: P_{2351} = (14, 1, 8, 1)
64: P_{818} = (1, 2, 2, 1)
                                                                                        172: P_{2418} = (1, 6, 8, 1)
                                            118: P_{1634} = (1, 5, 5, 1)
65: P_{827} = (10, 2, 2, 1)
                                            119: P_{1643} = (10, 5, 5, 1)
                                                                                        173: P_{2427} = (10, 6, 8, 1)
66: P_{828} = (11, 2, 2, 1)
                                            120: P_{1644} = (11, 5, 5, 1)
                                                                                        174: P_{2428} = (11, 6, 8, 1)
67: P_{947} = (2, 10, 2, 1)
                                            121: P_{1698} = (1, 9, 5, 1)
                                                                                        175: P_{2450} = (1, 8, 8, 1)
68: P_{958} = (13, 10, 2, 1)
                                            122: P_{1707} = (10, 9, 5, 1)
                                                                                        176: P_{2459} = (10, 8, 8, 1)
69: P_{960} = (15, 10, 2, 1)
                                            123: P_{1708} = (11, 9, 5, 1)
                                                                                        177: P_{2460} = (11, 8, 8, 1)
70: P_{963} = (2, 11, 2, 1)
                                            124: P_{1718} = (5, 10, 5, 1)
                                                                                        178: P_{2487} = (6, 10, 8, 1)
71: P_{974} = (13, 11, 2, 1)
                                            125: P_{1722} = (9, 10, 5, 1)
                                                                                        179: P_{2489} = (8, 10, 8, 1)
72: P_{976} = (15, 11, 2, 1)
                                                                                        180: P_{2495} = (14, 10, 8, 1)
                                            126: P_{1725} = (12, 10, 5, 1)
73: P_{994} = (1, 13, 2, 1)
                                            127: P_{1734} = (5, 11, 5, 1)
                                                                                        181: P_{2503} = (6, 11, 8, 1)
74: P_{1003} = (10, 13, 2, 1)
                                            128: P_{1738} = (9, 11, 5, 1)
                                                                                        182: P_{2505} = (8, 11, 8, 1)
75: P_{1004} = (11, 13, 2, 1)
                                            129: P_{1741} = (12, 11, 5, 1)
                                                                                        183: P_{2511} = (14, 11, 8, 1)
                                            130 : P_{1746} = (1, 12, 5, 1)
76: P_{1026} = (1, 15, 2, 1)
                                                                                        184: P_{2546} = (1, 14, 8, 1)
77: P_{1035} = (10, 15, 2, 1)
                                            131: P_{1755} = (10, 12, 5, 1)
                                                                                        185: P_{2555} = (10, 14, 8, 1)
78: P_{1036} = (11, 15, 2, 1)
                                            132: P_{1756} = (11, 12, 5, 1)
                                                                                        186: P_{2556} = (11, 14, 8, 1)
79: P_{1060} = (3, 1, 3, 1)
                                            133: P_{1831} = (6, 1, 6, 1)
                                                                                        187: P_{2598} = (5, 1, 9, 1)
80: P_{1061} = (4, 1, 3, 1)
                                            134: P_{1833} = (8, 1, 6, 1)
                                                                                        188: P_{2602} = (9, 1, 9, 1)
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189 : P_{2605} = (12, 1, 9, 1)
                                           243: P_{3054} = (13, 13, 10, 1)
                                                                                      297: P_{3366} = (5, 1, 12, 1)
190: P_{2658} = (1, 5, 9, 1)
                                           244: P_{3056} = (15, 13, 10, 1)
                                                                                      298: P_{3370} = (9, 1, 12, 1)
191: P_{2667} = (10, 5, 9, 1)
                                                                                      299: P_{3373} = (12, 1, 12, 1)
                                           245: P_{3063} = (6, 14, 10, 1)
                                                                                      300: P_{3426} = (1, 5, 12, 1)
192: P_{2668} = (11, 5, 9, 1)
                                           246: P_{3065} = (8, 14, 10, 1)
193: P_{2722} = (1, 9, 9, 1)
                                           247: P_{3071} = (14, 14, 10, 1)
                                                                                      301: P_{3435} = (10, 5, 12, 1)
                                                                                      302: P_{3436} = (11, 5, 12, 1)
194: P_{2731} = (10, 9, 9, 1)
                                           248: P_{3075} = (2, 15, 10, 1)
195: P_{2732} = (11, 9, 9, 1)
                                           249: P_{3086} = (13, 15, 10, 1)
                                                                                      303: P_{3490} = (1, 9, 12, 1)
196: P_{2742} = (5, 10, 9, 1)
                                           250: P_{3088} = (15, 15, 10, 1)
                                                                                      304: P_{3499} = (10, 9, 12, 1)
197: P_{2746} = (9, 10, 9, 1)
                                           251: P_{3089} = (0, 0, 11, 1)
                                                                                      305: P_{3500} = (11, 9, 12, 1)
198: P_{2749} = (12, 10, 9, 1)
                                           252: P_{3106} = (1, 1, 11, 1)
                                                                                      306: P_{3510} = (5, 10, 12, 1)
199: P_{2758} = (5, 11, 9, 1)
                                           253: P_{3115} = (10, 1, 11, 1)
                                                                                      307: P_{3514} = (9, 10, 12, 1)
200: P_{2762} = (9, 11, 9, 1)
                                           254: P_{3116} = (11, 1, 11, 1)
                                                                                      308: P_{3517} = (12, 10, 12, 1)
201: P_{2765} = (12, 11, 9, 1)
                                           255: P_{3123} = (2, 2, 11, 1)
                                                                                      309: P_{3526} = (5, 11, 12, 1)
202: P_{2770} = (1, 12, 9, 1)
                                           256: P_{3134} = (13, 2, 11, 1)
                                                                                      310: P_{3530} = (9, 11, 12, 1)
                                                                                      311: P_{3533} = (12, 11, 12, 1)
203: P_{2779} = (10, 12, 9, 1)
                                           257: P_{3136} = (15, 2, 11, 1)
204: P_{2780} = (11, 12, 9, 1)
                                           258: P_{3140} = (3, 3, 11, 1)
                                                                                      312: P_{3538} = (1, 12, 12, 1)
                                           259: P_{3141} = (4, 3, 11, 1)
                                                                                      313: P_{3547} = (10, 12, 12, 1)
205: P_{2833} = (0, 0, 10, 1)
                                           260: P_{3144} = (7, 3, 11, 1)
206: P_{2850} = (1, 1, 10, 1)
                                                                                      314: P_{3548} = (11, 12, 12, 1)
207: P_{2859} = (10, 1, 10, 1)
                                                                                      315: P_{3619} = (2, 1, 13, 1)
                                           261: P_{3156} = (3, 4, 11, 1)
208: P_{2860} = (11, 1, 10, 1)
                                           262: P_{3157} = (4, 4, 11, 1)
                                                                                      316: P_{3630} = (13, 1, 13, 1)
209: P_{2867} = (2, 2, 10, 1)
                                           263: P_{3160} = (7, 4, 11, 1)
                                                                                      317: P_{3632} = (15, 1, 13, 1)
                                                                                      318: P_{3634} = (1, 2, 13, 1)
210: P_{2878} = (13, 2, 10, 1)
                                           264: P_{3174} = (5, 5, 11, 1)
                                           265: P_{3178} = (9, 5, 11, 1)
                                                                                      319: P_{3643} = (10, 2, 13, 1)
211: P_{2880} = (15, 2, 10, 1)
212: P_{2884} = (3, 3, 10, 1)
                                           266: P_{3181} = (12, 5, 11, 1)
                                                                                      320: P_{3644} = (11, 2, 13, 1)
213: P_{2885} = (4, 3, 10, 1)
                                           267: P_{3191} = (6, 6, 11, 1)
                                                                                      321: P_{3763} = (2, 10, 13, 1)
214: P_{2888} = (7, 3, 10, 1)
                                           268: P_{3193} = (8, 6, 11, 1)
                                                                                      322: P_{3774} = (13, 10, 13, 1)
215: P_{2900} = (3, 4, 10, 1)
                                           269: P_{3199} = (14, 6, 11, 1)
                                                                                      323: P_{3776} = (15, 10, 13, 1)
216: P_{2901} = (4, 4, 10, 1)
                                           270: P_{3204} = (3, 7, 11, 1)
                                                                                      324: P_{3779} = (2, 11, 13, 1)
                                           271: P_{3205} = (4, 7, 11, 1)
                                                                                      325: P_{3790} = (13, 11, 13, 1)
217: P_{2904} = (7, 4, 10, 1)
218: P_{2918} = (5, 5, 10, 1)
                                           272: P_{3208} = (7,7,11,1)
                                                                                      326: P_{3792} = (15, 11, 13, 1)
219: P_{2922} = (9, 5, 10, 1)
                                           273: P_{3223} = (6, 8, 11, 1)
                                                                                      327: P_{3810} = (1, 13, 13, 1)
220: P_{2925} = (12, 5, 10, 1)
                                           274: P_{3225} = (8, 8, 11, 1)
                                                                                      328: P_{3819} = (10, 13, 13, 1)
221: P_{2935} = (6, 6, 10, 1)
                                           275: P_{3231} = (14, 8, 11, 1)
                                                                                      329: P_{3820} = (11, 13, 13, 1)
222: P_{2937} = (8, 6, 10, 1)
                                           276: P_{3238} = (5, 9, 11, 1)
                                                                                      330: P_{3842} = (1, 15, 13, 1)
223: P_{2943} = (14, 6, 10, 1)
                                           277: P_{3242} = (9, 9, 11, 1)
                                                                                      331: P_{3851} = (10, 15, 13, 1)
                                           278: P_{3245} = (12, 9, 11, 1)
224: P_{2948} = (3, 7, 10, 1)
                                                                                      332: P_{3852} = (11, 15, 13, 1)
225: P_{2949} = (4, 7, 10, 1)
                                           279: P_{3250} = (1, 10, 11, 1)
                                                                                      333: P_{3879} = (6, 1, 14, 1)
226: P_{2952} = (7, 7, 10, 1)
                                           280: P_{3259} = (10, 10, 11, 1)
                                                                                      334: P_{3881} = (8, 1, 14, 1)
227: P_{2967} = (6, 8, 10, 1)
                                           281: P_{3260} = (11, 10, 11, 1)
                                                                                      335: P_{3887} = (14, 1, 14, 1)
228: P_{2969} = (8, 8, 10, 1)
                                           282: P_{3266} = (1, 11, 11, 1)
                                                                                      336: P_{3954} = (1, 6, 14, 1)
229: P_{2975} = (14, 8, 10, 1)
                                           283: P_{3275} = (10, 11, 11, 1)
                                                                                      337: P_{3963} = (10, 6, 14, 1)
230: P_{2982} = (5, 9, 10, 1)
                                           284: P_{3276} = (11, 11, 11, 1)
                                                                                      338: P_{3964} = (11, 6, 14, 1)
231: P_{2986} = (9, 9, 10, 1)
                                           285: P_{3286} = (5, 12, 11, 1)
                                                                                      339: P_{3986} = (1, 8, 14, 1)
                                           286: P_{3290} = (9, 12, 11, 1)
                                                                                      340: P_{3995} = (10, 8, 14, 1)
232: P_{2989} = (12, 9, 10, 1)
233: P_{2994} = (1, 10, 10, 1)
                                           287: P_{3293} = (12, 12, 11, 1)
                                                                                      341: P_{3996} = (11, 8, 14, 1)
                                                                                      342: P_{4023} = (6, 10, 14, 1)
                                           288: P_{3299} = (2, 13, 11, 1)
234: P_{3003} = (10, 10, 10, 1)
235: P_{3004} = (11, 10, 10, 1)
                                           289: P_{3310} = (13, 13, 11, 1)
                                                                                      343: P_{4025} = (8, 10, 14, 1)
236: P_{3010} = (1, 11, 10, 1)
                                           290: P_{3312} = (15, 13, 11, 1)
                                                                                      344: P_{4031} = (14, 10, 14, 1)
237: P_{3019} = (10, 11, 10, 1)
                                           291: P_{3319} = (6, 14, 11, 1)
                                                                                      345: P_{4039} = (6, 11, 14, 1)
238: P_{3020} = (11, 11, 10, 1)
                                           292: P_{3321} = (8, 14, 11, 1)
                                                                                      346: P_{4041} = (8, 11, 14, 1)
239: P_{3030} = (5, 12, 10, 1)
                                           293: P_{3327} = (14, 14, 11, 1)
                                                                                      347: P_{4047} = (14, 11, 14, 1)
240: P_{3034} = (9, 12, 10, 1)
                                           294: P_{3331} = (2, 15, 11, 1)
                                                                                      348: P_{4082} = (1, 14, 14, 1)
241: P_{3037} = (12, 12, 10, 1)
                                           295: P_{3342} = (13, 15, 11, 1)
                                                                                      349: P_{4091} = (10, 14, 14, 1)
242: P_{3043} = (2, 13, 10, 1)
                                           296: P_{3344} = (15, 15, 11, 1)
                                                                                      350: P_{4092} = (11, 14, 14, 1)
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351: P_{4131} = (2, 1, 15, 1)
                                          358: P_{4286} = (13, 10, 15, 1)
                                                                                     365: P_{4332} = (11, 13, 15, 1)
352: P_{4142} = (13, 1, 15, 1)
                                                                                     366: P_{4354} = (1, 15, 15, 1)
                                          359: P_{4288} = (15, 10, 15, 1)
353: P_{4144} = (15, 1, 15, 1)
                                          360: P_{4291} = (2, 11, 15, 1)
                                                                                     367: P_{4363} = (10, 15, 15, 1)
354: P_{4146} = (1, 2, 15, 1)
                                          361: P_{4302} = (13, 11, 15, 1)
                                                                                     368: P_{4364} = (11, 15, 15, 1)
355: P_{4155} = (10, 2, 15, 1)
                                          362: P_{4304} = (15, 11, 15, 1)
356: P_{4156} = (11, 2, 15, 1)
                                          363: P_{4322} = (1, 13, 15, 1)
                                          364: P_{4331} = (10, 13, 15, 1)
357: P_{4275} = (2, 10, 15, 1)
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