

Rank-35 over GF(64)

January 15, 2021

The equation

The equation of the surface is :

$$X_2^3 + X_0^2 X_1 = 0$$

(0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)

The point rank of the equation over GF(64) is 270417

General information

Number of lines	65
Number of points	4161
Number of singular points	65
Number of Eckardt points	0
Number of double points	0
Number of single points	4160
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	65^{65}
Type of lines on points	$65, 1^{4160}$

Singular Points

The surface has 65 singular points:

$$0 : P_1 = \mathbf{P}(0, 1, 0, 0) = \mathbf{P}(0, 1, 0, 0)$$

$$1 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

$$2 : P_{4226} = \mathbf{P}(0, 1, 0, 1) = \mathbf{P}(0, 1, 0, 1)$$

$$3 : P_{4290} = \mathbf{P}(0, \epsilon, 0, 1) = \mathbf{P}(0, 2, 0, 1)$$

$$4 : P_{4354} = \mathbf{P}(0, \epsilon^{58}, 0, 1) = \mathbf{P}(0, 3, 0, 1)$$

$$5 : P_{4418} = \mathbf{P}(0, \epsilon^2, 0, 1) = \mathbf{P}(0, 4, 0, 1)$$

$$6 : P_{4482} = \mathbf{P}(0, \epsilon^{53}, 0, 1) = \mathbf{P}(0, 5, 0, 1)$$

$$7 : P_{4546} = \mathbf{P}(0, \epsilon^{59}, 0, 1) = \mathbf{P}(0, 6, 0, 1)$$

$$8 : P_{4610} = \mathbf{P}(0, \epsilon^{39}, 0, 1) = \mathbf{P}(0, 7, 0, 1)$$

$$9 : P_{4674} = \mathbf{P}(0, \epsilon^3, 0, 1) = \mathbf{P}(0, 8, 0, 1)$$

$$10 : P_{4738} = \mathbf{P}(0, \epsilon^{34}, 0, 1) = \mathbf{P}(0, 9, 0, 1)$$

$$11 : P_{4802} = \mathbf{P}(0, \epsilon^{54}, 0, 1) = \mathbf{P}(0, 10, 0, 1)$$

$$12 : P_{4866} = \mathbf{P}(0, \epsilon^{18}, 0, 1) = \mathbf{P}(0, 11, 0, 1)$$

$$13 : P_{4930} = \mathbf{P}(0, \epsilon^{60}, 0, 1) = \mathbf{P}(0, 12, 0, 1)$$

$$14 : P_{4994} = \mathbf{P}(0, \epsilon^{31}, 0, 1) = \mathbf{P}(0, 13, 0, 1)$$

$$15 : P_{5058} = \mathbf{P}(0, \epsilon^{40}, 0, 1) = \mathbf{P}(0, 14, 0, 1)$$

$$16 : P_{5122} = \mathbf{P}(0, \epsilon^{48}, 0, 1) = \mathbf{P}(0, 15, 0, 1)$$

$$17 : P_{5186} = \mathbf{P}(0, \epsilon^4, 0, 1) = \mathbf{P}(0, 16, 0, 1)$$

$$\begin{aligned}
18 : P_{5250} &= \mathbf{P}(0, \epsilon^{43}, 0, 1) = \mathbf{P}(0, 17, 0, 1) \\
19 : P_{5314} &= \mathbf{P}(0, \epsilon^{35}, 0, 1) = \mathbf{P}(0, 18, 0, 1) \\
20 : P_{5378} &= \mathbf{P}(0, \epsilon^{22}, 0, 1) = \mathbf{P}(0, 19, 0, 1) \\
21 : P_{5442} &= \mathbf{P}(0, \epsilon^{55}, 0, 1) = \mathbf{P}(0, 20, 0, 1) \\
22 : P_{5506} &= \mathbf{P}(0, \epsilon^{15}, 0, 1) = \mathbf{P}(0, 21, 0, 1) \\
23 : P_{5570} &= \mathbf{P}(0, \epsilon^{19}, 0, 1) = \mathbf{P}(0, 22, 0, 1) \\
24 : P_{5634} &= \mathbf{P}(0, \epsilon^{26}, 0, 1) = \mathbf{P}(0, 23, 0, 1) \\
25 : P_{5698} &= \mathbf{P}(0, \epsilon^{61}, 0, 1) = \mathbf{P}(0, 24, 0, 1) \\
26 : P_{5762} &= \mathbf{P}(0, \epsilon^{51}, 0, 1) = \mathbf{P}(0, 25, 0, 1) \\
27 : P_{5826} &= \mathbf{P}(0, \epsilon^{32}, 0, 1) = \mathbf{P}(0, 26, 0, 1) \\
28 : P_{5890} &= \mathbf{P}(0, \epsilon^{29}, 0, 1) = \mathbf{P}(0, 27, 0, 1) \\
29 : P_{5954} &= \mathbf{P}(0, \epsilon^{41}, 0, 1) = \mathbf{P}(0, 28, 0, 1) \\
30 : P_{6018} &= \mathbf{P}(0, \epsilon^{13}, 0, 1) = \mathbf{P}(0, 29, 0, 1) \\
31 : P_{6082} &= \mathbf{P}(0, \epsilon^{49}, 0, 1) = \mathbf{P}(0, 30, 0, 1) \\
32 : P_{6146} &= \mathbf{P}(0, \epsilon^{11}, 0, 1) = \mathbf{P}(0, 31, 0, 1) \\
33 : P_{6210} &= \mathbf{P}(0, \epsilon^5, 0, 1) = \mathbf{P}(0, 32, 0, 1) \\
34 : P_{6274} &= \mathbf{P}(0, \epsilon^6, 0, 1) = \mathbf{P}(0, 33, 0, 1) \\
35 : P_{6338} &= \mathbf{P}(0, \epsilon^{44}, 0, 1) = \mathbf{P}(0, 34, 0, 1) \\
36 : P_{6402} &= \mathbf{P}(0, \epsilon^7, 0, 1) = \mathbf{P}(0, 35, 0, 1) \\
37 : P_{6466} &= \mathbf{P}(0, \epsilon^{36}, 0, 1) = \mathbf{P}(0, 36, 0, 1) \\
38 : P_{6530} &= \mathbf{P}(0, \epsilon^{45}, 0, 1) = \mathbf{P}(0, 37, 0, 1) \\
39 : P_{6594} &= \mathbf{P}(0, \epsilon^{23}, 0, 1) = \mathbf{P}(0, 38, 0, 1) \\
40 : P_{6658} &= \mathbf{P}(0, \epsilon^8, 0, 1) = \mathbf{P}(0, 39, 0, 1) \\
41 : P_{6722} &= \mathbf{P}(0, \epsilon^{56}, 0, 1) = \mathbf{P}(0, 40, 0, 1)
\end{aligned}$$

$$\begin{aligned}
42 : P_{6786} &= \mathbf{P}(0, \epsilon^{37}, 0, 1) = \mathbf{P}(0, 41, 0, 1) \\
43 : P_{6850} &= \mathbf{P}(0, \epsilon^{16}, 0, 1) = \mathbf{P}(0, 42, 0, 1) \\
44 : P_{6914} &= \mathbf{P}(0, \epsilon^{46}, 0, 1) = \mathbf{P}(0, 43, 0, 1) \\
45 : P_{6978} &= \mathbf{P}(0, \epsilon^{20}, 0, 1) = \mathbf{P}(0, 44, 0, 1) \\
46 : P_{7042} &= \mathbf{P}(0, \epsilon^{24}, 0, 1) = \mathbf{P}(0, 45, 0, 1) \\
47 : P_{7106} &= \mathbf{P}(0, \epsilon^{27}, 0, 1) = \mathbf{P}(0, 46, 0, 1) \\
48 : P_{7170} &= \mathbf{P}(0, \epsilon^9, 0, 1) = \mathbf{P}(0, 47, 0, 1) \\
49 : P_{7234} &= \mathbf{P}(0, \epsilon^{62}, 0, 1) = \mathbf{P}(0, 48, 0, 1) \\
50 : P_{7298} &= \mathbf{P}(0, \epsilon^{57}, 0, 1) = \mathbf{P}(0, 49, 0, 1) \\
51 : P_{7362} &= \mathbf{P}(0, \epsilon^{52}, 0, 1) = \mathbf{P}(0, 50, 0, 1) \\
52 : P_{7426} &= \mathbf{P}(0, \epsilon^{38}, 0, 1) = \mathbf{P}(0, 51, 0, 1) \\
53 : P_{7490} &= \mathbf{P}(0, \epsilon^{33}, 0, 1) = \mathbf{P}(0, 52, 0, 1) \\
54 : P_{7554} &= \mathbf{P}(0, \epsilon^{17}, 0, 1) = \mathbf{P}(0, 53, 0, 1) \\
55 : P_{7618} &= \mathbf{P}(0, \epsilon^{30}, 0, 1) = \mathbf{P}(0, 54, 0, 1) \\
56 : P_{7682} &= \mathbf{P}(0, \epsilon^{47}, 0, 1) = \mathbf{P}(0, 55, 0, 1) \\
57 : P_{7746} &= \mathbf{P}(0, \epsilon^{42}, 0, 1) = \mathbf{P}(0, 56, 0, 1) \\
58 : P_{7810} &= \mathbf{P}(0, \epsilon^{21}, 0, 1) = \mathbf{P}(0, 57, 0, 1) \\
59 : P_{7874} &= \mathbf{P}(0, \epsilon^{14}, 0, 1) = \mathbf{P}(0, 58, 0, 1) \\
60 : P_{7938} &= \mathbf{P}(0, \epsilon^{25}, 0, 1) = \mathbf{P}(0, 59, 0, 1) \\
61 : P_{8002} &= \mathbf{P}(0, \epsilon^{50}, 0, 1) = \mathbf{P}(0, 60, 0, 1) \\
62 : P_{8066} &= \mathbf{P}(0, \epsilon^{28}, 0, 1) = \mathbf{P}(0, 61, 0, 1) \\
63 : P_{8130} &= \mathbf{P}(0, \epsilon^{12}, 0, 1) = \mathbf{P}(0, 62, 0, 1) \\
64 : P_{8194} &= \mathbf{P}(0, \epsilon^{10}, 0, 1) = \mathbf{P}(0, 63, 0, 1)
\end{aligned}$$

The 65 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned}
\ell_0 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4160} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4160} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)_{4225} \\
\ell_1 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043520} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043520} = \mathbf{Pl}(0, 0, 0, 1, 0, 0)_{129} \\
\ell_2 &= \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{274625} = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{274625} = \mathbf{Pl}(0, 1, 0, 1, 1, 0)_{12417} \\
\ell_3 &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{32} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7144436} = \begin{bmatrix} 1 & 52 & 26 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7144436} = \mathbf{Pl}(0, 26, 0, 52, 1, 0)_{18919} \\
\ell_4 &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7381613} = \begin{bmatrix} 1 & 45 & 27 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7381613} = \mathbf{Pl}(0, 27, 0, 45, 1, 0)_{18031} \\
\ell_5 &= \begin{bmatrix} 1 & \epsilon^3 & \epsilon & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{570056} = \begin{bmatrix} 1 & 8 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{570056} = \mathbf{Pl}(0, 2, 0, 8, 1, 0)_{13307} \\
\ell_6 &= \begin{bmatrix} 1 & \epsilon^{48} & \epsilon^{58} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{865487} = \begin{bmatrix} 1 & 15 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{865487} = \mathbf{Pl}(0, 3, 0, 15, 1, 0)_{14197} \\
\ell_7 &= \begin{bmatrix} 1 & \epsilon^{57} & \epsilon^{61} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6599345} = \begin{bmatrix} 1 & 49 & 24 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6599345} = \mathbf{Pl}(0, 24, 0, 49, 1, 0)_{18536} \\
\ell_8 &= \begin{bmatrix} 1 & \epsilon^{27} & \epsilon^{51} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6853166} = \begin{bmatrix} 1 & 46 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6853166} = \mathbf{Pl}(0, 25, 0, 46, 1, 0)_{18156} \\
\ell_9 &= \begin{bmatrix} 1 & \epsilon^{36} & \epsilon^{33} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14001764} = \begin{bmatrix} 1 & 36 & 52 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14001764} = \mathbf{Pl}(0, 52, 0, 36, 1, 0)_{16913}
\end{aligned}$$

$$\begin{aligned}
\ell_{10} &= \begin{bmatrix} 1 & \epsilon^{51} & \epsilon^{17} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14222297} = \begin{bmatrix} 1 & 25 & 53 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14222297} = \mathbf{Pl}(0, 53, 0, 25, 1, 0)_{15517} \\
\ell_{11} &= \begin{bmatrix} 1 & \epsilon^{18} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12299915} = \begin{bmatrix} 1 & 11 & 46 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12299915} = \mathbf{Pl}(0, 46, 0, 11, 1, 0)_{13732} \\
\ell_{12} &= \begin{bmatrix} 1 & \epsilon^{27} & \epsilon^9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12711854} = \begin{bmatrix} 1 & 46 & 47 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12711854} = \mathbf{Pl}(0, 47, 0, 46, 1, 0)_{18178} \\
\ell_{13} &= \begin{bmatrix} 1 & \epsilon^{27} & \epsilon^{30} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14575982} = \begin{bmatrix} 1 & 46 & 54 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14575982} = \mathbf{Pl}(0, 54, 0, 46, 1, 0)_{18185} \\
\ell_{14} &= \begin{bmatrix} 1 & \epsilon^{15} & \epsilon^{47} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14738261} = \begin{bmatrix} 1 & 21 & 55 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14738261} = \mathbf{Pl}(0, 55, 0, 21, 1, 0)_{15011} \\
\ell_{15} &= \begin{bmatrix} 1 & \epsilon^{60} & \epsilon^{20} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11771468} = \begin{bmatrix} 1 & 12 & 44 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11771468} = \mathbf{Pl}(0, 44, 0, 12, 1, 0)_{13857} \\
\ell_{16} &= \begin{bmatrix} 1 & \epsilon^9 & \epsilon^{24} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12183407} = \begin{bmatrix} 1 & 47 & 45 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12183407} = \mathbf{Pl}(0, 45, 0, 47, 1, 0)_{18303} \\
\ell_{17} &= \begin{bmatrix} 1 & \epsilon^6 & \epsilon^2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1206689} = \begin{bmatrix} 1 & 33 & 4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1206689} = \mathbf{Pl}(0, 4, 0, 33, 1, 0)_{16484} \\
\ell_{18} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{53} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1552052} = \begin{bmatrix} 1 & 52 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1552052} = \mathbf{Pl}(0, 5, 0, 52, 1, 0)_{18898} \\
\ell_{19} &= \begin{bmatrix} 1 & \epsilon^{21} & \epsilon^{49} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8230457} = \begin{bmatrix} 1 & 57 & 30 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8230457} = \mathbf{Pl}(0, 30, 0, 57, 1, 0)_{19558} \\
\ell_{20} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{11} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8475956} = \begin{bmatrix} 1 & 52 & 31 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8475956} = \mathbf{Pl}(0, 31, 0, 52, 1, 0)_{18924} \\
\ell_{21} &= \begin{bmatrix} 1 & \epsilon^{51} & \epsilon^{59} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1706009} = \begin{bmatrix} 1 & 25 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1706009} = \mathbf{Pl}(0, 6, 0, 25, 1, 0)_{15470} \\
\ell_{22} &= \begin{bmatrix} 1 & \epsilon^{54} & \epsilon^{39} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1909898} = \begin{bmatrix} 1 & 10 & 7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1909898} = \mathbf{Pl}(0, 7, 0, 10, 1, 0)_{13566} \\
\ell_{23} &= \begin{bmatrix} 1 & \epsilon^{60} & \epsilon^{41} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7510604} = \begin{bmatrix} 1 & 12 & 28 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7510604} = \mathbf{Pl}(0, 28, 0, 12, 1, 0)_{13841} \\
\ell_{24} &= \begin{bmatrix} 1 & \epsilon^{39} & \epsilon^{13} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7756103} = \begin{bmatrix} 1 & 7 & 29 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7756103} = \mathbf{Pl}(0, 29, 0, 7, 1, 0)_{13207} \\
\ell_{25} &= \begin{bmatrix} 1 & \epsilon^{60} & \epsilon^{62} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12836684} = \begin{bmatrix} 1 & 12 & 48 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12836684} = \mathbf{Pl}(0, 48, 0, 12, 1, 0)_{13861} \\
\ell_{26} &= \begin{bmatrix} 1 & \epsilon^{45} & \epsilon^{57} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13207013} = \begin{bmatrix} 1 & 37 & 49 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13207013} = \mathbf{Pl}(0, 49, 0, 37, 1, 0)_{17037} \\
\ell_{27} &= \begin{bmatrix} 1 & \epsilon^{48} & \epsilon^{16} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11251343} = \begin{bmatrix} 1 & 15 & 42 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11251343} = \mathbf{Pl}(0, 42, 0, 15, 1, 0)_{14236} \\
\ell_{28} &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^{46} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11713214} = \begin{bmatrix} 1 & 62 & 43 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11713214} = \mathbf{Pl}(0, 43, 0, 62, 1, 0)_{20206} \\
\ell_{29} &= \begin{bmatrix} 1 & \epsilon^{30} & \epsilon^{52} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13544054} = \begin{bmatrix} 1 & 54 & 50 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13544054} = \mathbf{Pl}(0, 50, 0, 54, 1, 0)_{19197} \\
\ell_{30} &= \begin{bmatrix} 1 & \epsilon^{51} & \epsilon^{38} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13689689} = \begin{bmatrix} 1 & 25 & 51 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{13689689} = \mathbf{Pl}(0, 51, 0, 25, 1, 0)_{15515}
\end{aligned}$$

$$\begin{aligned}
\ell_{31} &= \begin{bmatrix} 1 & \epsilon^{42} & \epsilon^{56} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10889336} = \begin{bmatrix} 1 & 56 & 40 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10889336} = \mathbf{Pl}(0, 40, 0, 56, 1, 0)_{19441} \\
\ell_{32} &= \begin{bmatrix} 1 & \epsilon^{48} & \epsilon^{37} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10985039} = \begin{bmatrix} 1 & 15 & 41 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10985039} = \mathbf{Pl}(0, 41, 0, 15, 1, 0)_{14235} \\
\ell_{33} &= \begin{bmatrix} 1 & \epsilon^{39} & \epsilon^{34} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2430023} = \begin{bmatrix} 1 & 7 & 9 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2430023} = \mathbf{Pl}(0, 9, 0, 7, 1, 0)_{13187} \\
\ell_{34} &= \begin{bmatrix} 1 & \epsilon^9 & \epsilon^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2330159} = \begin{bmatrix} 1 & 47 & 8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2330159} = \mathbf{Pl}(0, 8, 0, 47, 1, 0)_{18266} \\
\ell_{35} &= \begin{bmatrix} 1 & \epsilon^3 & \epsilon^{22} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5097224} = \begin{bmatrix} 1 & 8 & 19 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5097224} = \mathbf{Pl}(0, 19, 0, 8, 1, 0)_{13324} \\
\ell_{36} &= \begin{bmatrix} 1 & \epsilon^{42} & \epsilon^{35} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5030648} = \begin{bmatrix} 1 & 56 & 18 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5030648} = \mathbf{Pl}(0, 18, 0, 56, 1, 0)_{19419} \\
\ell_{37} &= \begin{bmatrix} 1 & \epsilon^{54} & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2975114} = \begin{bmatrix} 1 & 10 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2975114} = \mathbf{Pl}(0, 11, 0, 10, 1, 0)_{13570} \\
\ell_{38} &= \begin{bmatrix} 1 & \epsilon^{36} & \epsilon^{54} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2816996} = \begin{bmatrix} 1 & 36 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2816996} = \mathbf{Pl}(0, 10, 0, 36, 1, 0)_{16871} \\
\ell_{39} &= \begin{bmatrix} 1 & \epsilon^3 & \epsilon^{43} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4564616} = \begin{bmatrix} 1 & 8 & 17 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4564616} = \mathbf{Pl}(0, 17, 0, 8, 1, 0)_{13322} \\
\ell_{40} &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4523006} = \begin{bmatrix} 1 & 62 & 16 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4523006} = \mathbf{Pl}(0, 16, 0, 62, 1, 0)_{20179} \\
\ell_{41} &= \begin{bmatrix} 1 & \epsilon^{21} & \epsilon^{28} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16485881} = \begin{bmatrix} 1 & 57 & 61 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16485881} = \mathbf{Pl}(0, 61, 0, 57, 1, 0)_{19589} \\
\ell_{42} &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^{50} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16169645} = \begin{bmatrix} 1 & 45 & 60 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16169645} = \mathbf{Pl}(0, 60, 0, 45, 1, 0)_{18064} \\
\ell_{43} &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^8 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10577261} = \begin{bmatrix} 1 & 45 & 39 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10577261} = \mathbf{Pl}(0, 39, 0, 45, 1, 0)_{18043} \\
\ell_{44} &= \begin{bmatrix} 1 & \epsilon^6 & \epsilon^{23} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10261025} = \begin{bmatrix} 1 & 33 & 38 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10261025} = \mathbf{Pl}(0, 38, 0, 33, 1, 0)_{16518} \\
\ell_{45} &= \begin{bmatrix} 1 & \epsilon^{30} & \epsilon^{10} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17006006} = \begin{bmatrix} 1 & 54 & 63 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17006006} = \mathbf{Pl}(0, 63, 0, 54, 1, 0)_{19210} \\
\ell_{46} &= \begin{bmatrix} 1 & \epsilon^{36} & \epsilon^{12} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16664804} = \begin{bmatrix} 1 & 36 & 62 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16664804} = \mathbf{Pl}(0, 62, 0, 36, 1, 0)_{16923} \\
\ell_{47} &= \begin{bmatrix} 1 & \epsilon^9 & \epsilon^{45} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10052975} = \begin{bmatrix} 1 & 47 & 37 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10052975} = \mathbf{Pl}(0, 37, 0, 47, 1, 0)_{18295} \\
\ell_{48} &= \begin{bmatrix} 1 & \epsilon^{45} & \epsilon^{36} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9745061} = \begin{bmatrix} 1 & 37 & 36 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9745061} = \mathbf{Pl}(0, 36, 0, 37, 1, 0)_{17024} \\
\ell_{49} &= \begin{bmatrix} 1 & \epsilon^{30} & \epsilon^{31} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3690806} = \begin{bmatrix} 1 & 54 & 13 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3690806} = \mathbf{Pl}(0, 13, 0, 54, 1, 0)_{19160} \\
\ell_{50} &= \begin{bmatrix} 1 & \epsilon^{54} & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3241418} = \begin{bmatrix} 1 & 10 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3241418} = \mathbf{Pl}(0, 12, 0, 10, 1, 0)_{13571} \\
\ell_{51} &= \begin{bmatrix} 1 & \epsilon^{15} & \epsilon^{26} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6216533} = \begin{bmatrix} 1 & 21 & 23 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6216533} = \mathbf{Pl}(0, 23, 0, 21, 1, 0)_{14979}
\end{aligned}$$

$$\begin{aligned}
\ell_{52} &= \begin{bmatrix} 1 & \epsilon^{57} & \epsilon^{19} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6066737} = \begin{bmatrix} 1 & 49 & 22 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6066737} = \mathbf{Pl}(0, 22, 0, 49, 1, 0)_{18534} \\
\ell_{53} &= \begin{bmatrix} 1 & \epsilon^{18} & \epsilon^{48} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4044491} = \begin{bmatrix} 1 & 11 & 15 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4044491} = \mathbf{Pl}(0, 15, 0, 11, 1, 0)_{13701} \\
\ell_{54} &= \begin{bmatrix} 1 & \epsilon^{57} & \epsilon^{40} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3936305} = \begin{bmatrix} 1 & 49 & 14 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3936305} = \mathbf{Pl}(0, 14, 0, 49, 1, 0)_{18526} \\
\ell_{55} &= \begin{bmatrix} 1 & \epsilon^{45} & \epsilon^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5750501} = \begin{bmatrix} 1 & 37 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5750501} = \mathbf{Pl}(0, 21, 0, 37, 1, 0)_{17009} \\
\ell_{56} &= \begin{bmatrix} 1 & \epsilon^{39} & \epsilon^{55} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5359367} = \begin{bmatrix} 1 & 7 & 20 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5359367} = \mathbf{Pl}(0, 20, 0, 7, 1, 0)_{13198} \\
\ell_{57} &= \begin{bmatrix} 1 & 1 & \epsilon^{21} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15187649} = \begin{bmatrix} 1 & 1 & 57 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15187649} = \mathbf{Pl}(0, 57, 0, 1, 1, 0)_{12473} \\
\ell_{58} &= \begin{bmatrix} 1 & 1 & \epsilon^{42} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14921345} = \begin{bmatrix} 1 & 1 & 56 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14921345} = \mathbf{Pl}(0, 56, 0, 1, 1, 0)_{12472} \\
\ell_{59} &= \begin{bmatrix} 1 & \epsilon^{21} & \epsilon^7 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9561977} = \begin{bmatrix} 1 & 57 & 35 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9561977} = \mathbf{Pl}(0, 35, 0, 57, 1, 0)_{19563} \\
\ell_{60} &= \begin{bmatrix} 1 & \epsilon^6 & \epsilon^{44} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9195809} = \begin{bmatrix} 1 & 33 & 34 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9195809} = \mathbf{Pl}(0, 34, 0, 33, 1, 0)_{16514} \\
\ell_{61} &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^{25} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15974078} = \begin{bmatrix} 1 & 62 & 59 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15974078} = \mathbf{Pl}(0, 59, 0, 62, 1, 0)_{20222} \\
\ell_{62} &= \begin{bmatrix} 1 & \epsilon^{42} & \epsilon^{14} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15682808} = \begin{bmatrix} 1 & 56 & 58 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{15682808} = \mathbf{Pl}(0, 58, 0, 56, 1, 0)_{19459} \\
\ell_{63} &= \begin{bmatrix} 1 & \epsilon^{18} & \epsilon^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8837963} = \begin{bmatrix} 1 & 11 & 33 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8837963} = \mathbf{Pl}(0, 33, 0, 11, 1, 0)_{13719} \\
\ell_{64} &= \begin{bmatrix} 1 & \epsilon^{15} & \epsilon^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8613269} = \begin{bmatrix} 1 & 21 & 32 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{8613269} = \mathbf{Pl}(0, 32, 0, 21, 1, 0)_{14988}
\end{aligned}$$

Rank of lines: (4160, 17043520, 274625, 7144436, 7381613, 570056, 865487, 6599345, 6853166, 14001764, 14222297, 12299915, 12711854, 14575982, 14738261, 11771468, 12183407, 1206689, 1552052, 8230457, 8475956, 1706009, 1909898, 7510604, 7756103, 12836684, 13207013, 11251343, 11713214, 13544054, 13689689, 10889336, 10985039, 2430023, 2330159, 5097224, 5030648, 2975114, 2816996, 4564616, 4523006, 16485881, 16169645, 10577261, 10261025, 17006006, 16664804, 10052975, 9745061, 3690806, ...15682808, 8837963, 8613269)

Rank of points on Klein quadric: (4225, 129, 12417, 18919, 18031, 13307, 14197, 18536, 18156, 16913, 15517, 13732, 18178, 18185, 15011, 13857, 18303, 16484, 18898, 19558, 18924, 15470, 13566, 13841, 13207, 13861, 17037, 14236, 20206, 19197, 15515, 19441, 14235, 13187, 18266, 13324, 19419, 13570, 16871, 13322, 20179, 19589, 18064, 18043, 16518, 19210, 16923, 18295, 17024, 19160, ...19459, 13719, 14988)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 4160 single points:
Too many to print.

Points on surface but on no line

The surface has 0 points not on any line:
The points on the surface but not on lines are:

Line Intersection Graph

[illegible]

Line 0 intersects

Line 1 intersects

Line 2 intersects

Line 3 intersects

Line 4 intersects

Line 5 intersects

Line 6 intersects

Line 7 intersects

Line 8 intersects

Line 9 intersects

Line 10 intersects

Line 11 intersects

8

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Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}	ℓ_{23}	ℓ_{24}	ℓ_{25}	ℓ_{26}	ℓ_{27}	ℓ_{28}	ℓ_{29}	ℓ_{30}	ℓ_{31}	ℓ_{32}	ℓ_{33}	ℓ_{34}	ℓ_{35}	ℓ_{36}	ℓ_{37}	ℓ_{38}	ℓ_{39}	ℓ_{40}	ℓ_{41}	ℓ_{42}	ℓ_{43}	ℓ_{44}	ℓ_{45}	ℓ_{46}	ℓ_{47}	ℓ_{48}	ℓ_{49}	ℓ_{50}	ℓ_{51}	ℓ_{52}	ℓ_{53}	ℓ_{54}	ℓ_{55}	ℓ_{56}	ℓ_{57}	ℓ_{58}	ℓ_{59}	ℓ_{60}	ℓ_{61}	ℓ_{62}	ℓ_{63}	ℓ_{64}	ℓ_{65}	ℓ_{66}	ℓ_{67}	ℓ_{68}	ℓ_{69}	ℓ_{70}	ℓ_{71}	ℓ_{72}	ℓ_{73}	ℓ_{74}	ℓ_{75}	ℓ_{76}	ℓ_{77}	ℓ_{78}	ℓ_{79}	ℓ_{80}	ℓ_{81}	ℓ_{82}	ℓ_{83}	ℓ_{84}	ℓ_{85}	ℓ_{86}	ℓ_{87}	ℓ_{88}	ℓ_{89}	ℓ_{90}	ℓ_{91}	ℓ_{92}	ℓ_{93}	ℓ_{94}	ℓ_{95}	ℓ_{96}	ℓ_{97}	ℓ_{98}	ℓ_{99}	ℓ_{100}	ℓ_{101}	ℓ_{102}	ℓ_{103}	ℓ_{104}	ℓ_{105}	ℓ_{106}	ℓ_{107}	ℓ_{108}	ℓ_{109}	ℓ_{110}	ℓ_{111}	ℓ_{112}	ℓ_{113}	ℓ_{114}	ℓ_{115}	ℓ_{116}	ℓ_{117}	ℓ_{118}	ℓ_{119}	ℓ_{120}	ℓ_{121}	ℓ_{122}	ℓ_{123}	ℓ_{124}	ℓ_{125}	ℓ_{126}	ℓ_{127}	ℓ_{128}	ℓ_{129}	ℓ_{130}	ℓ_{131}	ℓ_{132}	ℓ_{133}	ℓ_{134}	ℓ_{135}	ℓ_{136}	ℓ_{137}	ℓ_{138}	ℓ_{139}	ℓ_{140}	ℓ_{141}	ℓ_{142}	ℓ_{143}	ℓ_{144}	ℓ_{145}	ℓ_{146}	ℓ_{147}	ℓ_{148}	ℓ_{149}	ℓ_{150}	ℓ_{151}	ℓ_{152}	ℓ_{153}	ℓ_{154}	ℓ_{155}	ℓ_{156}	ℓ_{157}	ℓ_{158}	ℓ_{159}	ℓ_{160}	ℓ_{161}	ℓ_{162}	ℓ_{163}	ℓ_{164}	ℓ_{165}	ℓ_{166}	ℓ_{167}	ℓ_{168}	ℓ_{169}	ℓ_{170}	ℓ_{171}	ℓ_{172}	ℓ_{173}	ℓ_{174}	ℓ_{175}	ℓ_{176}	ℓ_{177}	ℓ_{178}	ℓ_{179}	ℓ_{180}	ℓ_{181}	ℓ_{182}	ℓ_{183}	ℓ_{184}	ℓ_{185}	ℓ_{186}	ℓ_{187}	ℓ_{188}	ℓ_{189}	ℓ_{190}	ℓ_{191}	ℓ_{192}	ℓ_{193}	ℓ_{194}	ℓ_{195}	ℓ_{196}	ℓ_{197}	ℓ_{198}	ℓ_{199}	ℓ_{200}	ℓ_{201}	ℓ_{202}	ℓ_{203}	ℓ_{204}	ℓ_{205}	ℓ_{206}	ℓ_{207}	ℓ_{208}	ℓ_{209}	ℓ_{210}	ℓ_{211}	ℓ_{212}	ℓ_{213}	ℓ_{214}	ℓ_{215}	ℓ_{216}	ℓ_{217}	ℓ_{218}	ℓ_{219}	ℓ_{220}	ℓ_{221}	ℓ_{222}	ℓ_{223}	ℓ_{224}	ℓ_{225}	ℓ_{226}	ℓ_{227}	ℓ_{228}	ℓ_{229}	ℓ_{230}	ℓ_{231}	ℓ_{232}	ℓ_{233}	ℓ_{234}	ℓ_{235}	ℓ_{236}	ℓ_{237}	ℓ_{238}	ℓ_{239}	ℓ_{240}	ℓ_{241}	ℓ_{242}	ℓ_{243}	ℓ_{244}	ℓ_{245}	ℓ_{246}	ℓ_{247}	ℓ_{248}	ℓ_{249}	ℓ_{250}	ℓ_{251}	ℓ_{252}	ℓ_{253}	ℓ_{254}	ℓ_{255}	ℓ_{256}	ℓ_{257}	ℓ_{258}	ℓ_{259}	ℓ_{260}	ℓ_{261}	ℓ_{262}	ℓ_{263}	ℓ_{264}	ℓ_{265}	ℓ_{266}	ℓ_{267}	ℓ_{268}	ℓ_{269}	ℓ_{270}	ℓ_{271}	ℓ_{272}	ℓ_{273}	ℓ_{274}	ℓ_{275}	ℓ_{276}	ℓ_{277}	ℓ_{278}	ℓ_{279}	ℓ_{280}	ℓ_{281}	ℓ_{282}	ℓ_{283}	ℓ_{284}	ℓ_{285}	ℓ_{286}	ℓ_{287}	ℓ_{288}	ℓ_{289}	ℓ_{290}	ℓ_{291}	ℓ_{292}	ℓ_{293}	ℓ_{294}	ℓ_{295}	ℓ_{296}	ℓ_{297}	ℓ_{298}	ℓ_{299}	$\$
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Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}	ℓ_{23}	ℓ_{24}	ℓ_{25}	ℓ_{26}	ℓ_{27}	ℓ_{28}	ℓ_{29}	ℓ_{30}	ℓ_{31}	ℓ_{32}	ℓ_{33}	ℓ_{34}	ℓ_{35}	ℓ_{36}	ℓ_{37}	ℓ_{38}	ℓ_{39}	ℓ_{40}	ℓ_{41}	ℓ_{42}	ℓ_{43}	ℓ_{44}	ℓ_{45}	ℓ_{46}	ℓ_{47}	ℓ_{48}	ℓ_{49}	ℓ_{50}	ℓ_{51}	ℓ_{52}	ℓ_{53}	ℓ_{54}	ℓ_{55}	ℓ_{56}	ℓ_{57}	ℓ_{58}	ℓ_{59}	ℓ_{60}	ℓ_{61}	ℓ_{62}	ℓ_{63}	ℓ_{64}	ℓ_{65}	ℓ_{66}	ℓ_{67}	ℓ_{68}	ℓ_{69}	ℓ_{70}	ℓ_{71}	ℓ_{72}	ℓ_{73}	ℓ_{74}	ℓ_{75}	ℓ_{76}	ℓ_{77}	ℓ_{78}	ℓ_{79}	ℓ_{80}	ℓ_{81}	ℓ_{82}	ℓ_{83}	ℓ_{84}	ℓ_{85}	ℓ_{86}	ℓ_{87}	ℓ_{88}	ℓ_{89}	ℓ_{90}	ℓ_{91}	ℓ_{92}	ℓ_{93}	ℓ_{94}	ℓ_{95}	ℓ_{96}	ℓ_{97}	ℓ_{98}	ℓ_{99}	ℓ_{100}	ℓ_{101}	ℓ_{102}	ℓ_{103}	ℓ_{104}	ℓ_{105}	ℓ_{106}	ℓ_{107}	ℓ_{108}	ℓ_{109}	ℓ_{110}	ℓ_{111}	ℓ_{112}	ℓ_{113}	ℓ_{114}	ℓ_{115}	ℓ_{116}	ℓ_{117}	ℓ_{118}	ℓ_{119}	ℓ_{120}	ℓ_{121}	ℓ_{122}	ℓ_{123}	ℓ_{124}	ℓ_{125}	ℓ_{126}	ℓ_{127}	ℓ_{128}	ℓ_{129}	ℓ_{130}	ℓ_{131}	ℓ_{132}	ℓ_{133}	ℓ_{134}	ℓ_{135}	ℓ_{136}	ℓ_{137}	ℓ_{138}	ℓ_{139}	ℓ_{140}	ℓ_{141}	ℓ_{142}	ℓ_{143}	ℓ_{144}	ℓ_{145}	ℓ_{146}	ℓ_{147}	ℓ_{148}	ℓ_{149}	ℓ_{150}	ℓ_{151}	ℓ_{152}	ℓ_{153}	ℓ_{154}	ℓ_{155}	ℓ_{156}	ℓ_{157}	ℓ_{158}	ℓ_{159}	ℓ_{160}	ℓ_{161}	ℓ_{162}	ℓ_{163}	ℓ_{164}	ℓ_{165}	ℓ_{166}	ℓ_{167}	ℓ_{168}	ℓ_{169}	ℓ_{170}	ℓ_{171}	ℓ_{172}	ℓ_{173}	ℓ_{174}	ℓ_{175}	ℓ_{176}	ℓ_{177}	ℓ_{178}	ℓ_{179}	ℓ_{180}	ℓ_{181}	ℓ_{182}	ℓ_{183}	ℓ_{184}	ℓ_{185}	ℓ_{186}	ℓ_{187}	ℓ_{188}	ℓ_{189}	ℓ_{190}	ℓ_{191}	ℓ_{192}	ℓ_{193}	ℓ_{194}	ℓ_{195}	ℓ_{196}	ℓ_{197}	ℓ_{198}	ℓ_{199}	ℓ_{200}	ℓ_{201}	ℓ_{202}	ℓ_{203}	ℓ_{204}	ℓ_{205}	ℓ_{206}	ℓ_{207}	ℓ_{208}	ℓ_{209}	ℓ_{210}	ℓ_{211}	ℓ_{212}	ℓ_{213}	ℓ_{214}	ℓ_{215}	ℓ_{216}	ℓ_{217}	ℓ_{218}	ℓ_{219}	ℓ_{220}	ℓ_{221}	ℓ_{222}	ℓ_{223}	ℓ_{224}	ℓ_{225}	ℓ_{226}	ℓ_{227}	ℓ_{228}	ℓ_{229}	ℓ_{230}	ℓ_{231}	ℓ_{232}	ℓ_{233}	ℓ_{234}	ℓ_{235}	ℓ_{236}	ℓ_{237}	ℓ_{238}	ℓ_{239}	ℓ_{240}	ℓ_{241}	ℓ_{242}	ℓ_{243}	ℓ_{244}	ℓ_{245}	ℓ_{246}	ℓ_{247}	ℓ_{248}	ℓ_{249}	ℓ_{250}	ℓ_{251}	ℓ_{252}	ℓ_{253}	ℓ_{254}	ℓ_{255}	ℓ_{256}	ℓ_{257}	ℓ_{258}	ℓ_{259}	ℓ_{260}	ℓ_{261}	ℓ_{262}	ℓ_{263}	ℓ_{264}	ℓ_{265}	ℓ_{266}	ℓ_{267}	ℓ_{268}	ℓ_{269}	ℓ_{270}	ℓ_{271}	ℓ_{272}	ℓ_{273}	ℓ_{274}	ℓ_{275}	ℓ_{276}	ℓ_{277}	ℓ_{278}	ℓ_{279}	ℓ_{280}	ℓ_{281}	ℓ_{282}	ℓ_{283}	ℓ_{284}	ℓ_{285}	ℓ_{286}	ℓ_{287}	ℓ_{288}	ℓ_{289}	ℓ_{290}	ℓ_{291}	ℓ_{292}	ℓ_{293}	ℓ_{294}	ℓ_{295}	ℓ_{296}	ℓ_{297}	ℓ_{298}	ℓ
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Line 64 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

The surface has 4161 points:
Too many to print.