# Rank-65839 over GF(8)

January 15, 2021

# The equation

The equation of the surface is:

$$X_2^3 + X_3^3 + X_0^2 X_2 + X_1^2 X_2 + X_0 X_1 X_2 = 0$$

 $(\ 0,\ 0,\ 1,\ 1,\ 0,\ 1,\ 0,\ 0,\ 1,\ 0,\ 0,\ 0,\ 0,\ 0,\ 0,\ 1,\ 0,\ 0,\ 0)$ 

The point rank of the equation over GF(8) is 1243944077

## General information

Number of lines	1
Number of points	73
Number of singular points	0
Number of Eckardt points	0
Number of double points	0
Number of single points	9
Number of points off lines	64
Number of Hesse planes	0
Number of axes	0
Type of points on lines	9
Type of lines on points	$1^9, 0^{64}$

## Singular Points

The surface has 0 singular points:

## The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0$$

Rank of lines: (0)

Rank of points on Klein quadric: (0)

#### **Eckardt Points**

The surface has 0 Eckardt points:

#### **Double Points**

The surface has 0 Double points: The double points on the surface are:

## Single Points

The surface has 9 single points: The single points on the surface are:

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\begin{array}{lll} 0: \ P_0 = (1,0,0,0) \ \mbox{lies on line} \ \ell_0 \\ 1: \ P_1 = (0,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 2: \ P_5 = (1,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 3: \ P_6 = (2,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ 4: \ P_7 = (3,1,0,0) \ \mbox{lies on line} \ \ell_0 \\ \end{array}
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The single points on the surface are:

### Points on surface but on no line

The surface has 64 points not on any line: The points on the surface but not on lines are:

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0: P_{12} = (1, 0, 1, 0)
                                                                  22: P_{294} = (5, 3, 3, 1)
1: P_{19} = (0, 1, 1, 0)
                                                                  23: P_{295} = (6, 3, 3, 1)
2: P_{20} = (1, 1, 1, 0)
                                                                  24: P_{308} = (3, 5, 3, 1)
3: P_{40} = (5, 3, 1, 0)
                                                                  25: P_{311} = (6,5,3,1)
4: P_{41} = (6, 3, 1, 0)
                                                                  26: P_{316} = (3, 6, 3, 1)
5: P_{54} = (3, 5, 1, 0)
                                                                  27: P_{318} = (5, 6, 3, 1)
6: P_{57} = (6, 5, 1, 0)
                                                                  28: P_{331} = (2,0,4,1)
7: P_{62} = (3, 6, 1, 0)
                                                                  29: P_{343} = (6, 1, 4, 1)
8: P_{64} = (5, 6, 1, 0)
                                                                  30: P_{344} = (7, 1, 4, 1)
9: P_{138} = (0,0,1,1)
                                                                  31: P_{345} = (0, 2, 4, 1)
10: P_{208} = (7, 0, 2, 1)
                                                                  32: P_{347} = (2, 2, 4, 1)
11: P_{213} = (4, 1, 2, 1)
                                                                  33: P_{378} = (1, 6, 4, 1)
12: P_{214} = (5, 1, 2, 1)
                                                                  34: P_{384} = (7, 6, 4, 1)
13: P_{234} = (1, 4, 2, 1)
                                                                  35: P_{386} = (1,7,4,1)
14: P_{238} = (5, 4, 2, 1)
                                                                  36: P_{391} = (6,7,4,1)
15: P_{242} = (1, 5, 2, 1)
                                                                  37: P_{394} = (1,0,5,1)
16: P_{245} = (4, 5, 2, 1)
                                                                  38: P_{401} = (0, 1, 5, 1)
17: P_{257} = (0, 7, 2, 1)
                                                                  39: P_{402} = (1, 1, 5, 1)
18: P_{264} = (7,7,2,1)
                                                                  40: P_{422} = (5, 3, 5, 1)
19: P_{266} = (1, 0, 3, 1)
                                                                  41: P_{423} = (6, 3, 5, 1)
20: P_{273} = (0, 1, 3, 1)
                                                                  42: P_{436} = (3, 5, 5, 1)
21: P_{274} = (1, 1, 3, 1)
                                                                  43: P_{439} = (6,5,5,1)
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44: P_{444} = (3, 6, 5, 1)
                                                                   55: P_{525} = (4, 0, 7, 1)
45: P_{446} = (5, 6, 5, 1)
                                                                   56: P_{531} = (2, 1, 7, 1)
46: P_{458} = (1, 0, 6, 1)
                                                                   57: P_{532} = (3, 1, 7, 1)
47: P_{465} = (0, 1, 6, 1)
                                                                   58: P_{538} = (1, 2, 7, 1)
48: P_{466} = (1, 1, 6, 1)
                                                                   59: P_{540} = (3, 2, 7, 1)
49: P_{486} = (5, 3, 6, 1)
                                                                   60: P_{546} = (1, 3, 7, 1)
50: P_{487} = (6, 3, 6, 1)
                                                                   61: P_{547} = (2, 3, 7, 1)
51: P_{500} = (3, 5, 6, 1)
                                                                   62: P_{553} = (0, 4, 7, 1)
52: P_{503} = (6, 5, 6, 1)
                                                                   63: P_{557} = (4, 4, 7, 1)
53: P_{508} = (3, 6, 6, 1)
54: P_{510} = (5, 6, 6, 1)
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# Line Intersection Graph

 $\begin{array}{c|c} 0 \\ \hline 0 & 0 \end{array}$ 

Neighbor sets in the line intersection graph: Line 0 intersects

Line in point

The surface has 73 points:

The points on the surface are:

$0: P_0 = (1, 0, 0, 0)$	$25: P_{245} = (4, 5, 2, 1)$	$50: P_{423} = (6, 3, 5, 1)$
$1: P_1 = (0, 1, 0, 0)$	$26: P_{257} = (0, 7, 2, 1)$	$51: P_{436} = (3, 5, 5, 1)$
$2: P_5 = (1, 1, 0, 0)$	$27: P_{264} = (7, 7, 2, 1)$	$52: P_{439} = (6, 5, 5, 1)$
$3: P_6 = (2, 1, 0, 0)$	$28: P_{266} = (1, 0, 3, 1)$	$53: P_{444} = (3, 6, 5, 1)$
$4: P_7 = (3, 1, 0, 0)$	$29: P_{273} = (0, 1, 3, 1)$	$54: P_{446} = (5, 6, 5, 1)$
$5: P_8 = (4, 1, 0, 0)$	$30: P_{274} = (1, 1, 3, 1)$	$55: P_{458} = (1,0,6,1)$
$6: P_9 = (5, 1, 0, 0)$	$31: P_{294} = (5, 3, 3, 1)$	$56: P_{465} = (0, 1, 6, 1)$
$7: P_{10} = (6, 1, 0, 0)$	$32: P_{295} = (6, 3, 3, 1)$	$57: P_{466} = (1, 1, 6, 1)$
$8: P_{11} = (7, 1, 0, 0)$	$33: P_{308} = (3, 5, 3, 1)$	$58: P_{486} = (5, 3, 6, 1)$
$9: P_{12} = (1, 0, 1, 0)$	$34: P_{311} = (6, 5, 3, 1)$	$59: P_{487} = (6, 3, 6, 1)$
$10: P_{19} = (0, 1, 1, 0)$	$35: P_{316} = (3, 6, 3, 1)$	$60: P_{500} = (3, 5, 6, 1)$
$11: P_{20} = (1, 1, 1, 0)$	$36: P_{318} = (5, 6, 3, 1)$	$61: P_{503} = (6, 5, 6, 1)$
$12: P_{40} = (5, 3, 1, 0)$	$37: P_{331} = (2,0,4,1)$	$62: P_{508} = (3, 6, 6, 1)$
$13: P_{41} = (6, 3, 1, 0)$	$38: P_{343} = (6, 1, 4, 1)$	$63: P_{510} = (5, 6, 6, 1)$
$14: P_{54} = (3, 5, 1, 0)$	$39: P_{344} = (7, 1, 4, 1)$	$64: P_{525} = (4, 0, 7, 1)$
$15: P_{57} = (6, 5, 1, 0)$	$40: P_{345} = (0, 2, 4, 1)$	$65: P_{531} = (2, 1, 7, 1)$
$16: P_{62} = (3, 6, 1, 0)$	$41: P_{347} = (2, 2, 4, 1)$	$66: P_{532} = (3, 1, 7, 1)$
$17: P_{64} = (5, 6, 1, 0)$	$42: P_{378} = (1, 6, 4, 1)$	$67: P_{538} = (1, 2, 7, 1)$
$18: P_{138} = (0, 0, 1, 1)$	$43: P_{384} = (7, 6, 4, 1)$	$68: P_{540} = (3, 2, 7, 1)$
$19: P_{208} = (7, 0, 2, 1)$	$44: P_{386} = (1, 7, 4, 1)$	$69: P_{546} = (1, 3, 7, 1)$
$20: P_{213} = (4, 1, 2, 1)$	$45: P_{391} = (6, 7, 4, 1)$	$70: P_{547} = (2, 3, 7, 1)$
$21: P_{214} = (5, 1, 2, 1)$	$46: P_{394} = (1, 0, 5, 1)$	$71: P_{553} = (0, 4, 7, 1)$
$22: P_{234} = (1, 4, 2, 1)$	$47: P_{401} = (0, 1, 5, 1)$	$72: P_{557} = (4, 4, 7, 1)$
$23: P_{238} = (5, 4, 2, 1)$	$48: P_{402} = (1, 1, 5, 1)$	00. (,,,,,,
$24: P_{242} = (1, 5, 2, 1)$	$49: P_{422} = (5, 3, 5, 1)$	