Rank-192 over GF(64)

January 15, 2021

The equation

The equation of the surface is:

$$X_2^3 + X_0^2 X_1 + X_0^2 X_2 + X_0 X_1^2 = 0$$

(0, 0, 1, 0, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)The point rank of the equation over GF(64) is -2113658802

General information

Number of lines	65
Number of points	4161
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	4160
Number of points off lines	0
Number of Hesse planes	0
Number of axes	0
Type of points on lines	65^{65}
Type of lines on points	$65, 1^{4160}$

Singular Points

The surface has 1 singular points:

$$0: P_3 = \mathbf{P}(0,0,0,1) = \mathbf{P}(0,0,0,1)$$

The 65 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4160} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4160} = \mathbf{Pl}(0, 0, 0, 0, 1, 0)_{4225}$$

$$\ell_1 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043520} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{17043520} = \mathbf{PI}(0,0,0,1,0,0)_{129}$$

$$\ell_2 = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{370461} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3214} = \mathbf{PI}(0,0,0,1,1,0)_{12353}$$

$$\ell_3 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{270464} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{270464} = \mathbf{PI}(0,1,0,0,1,0)_{4289}$$

$$\ell_4 = \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{270462} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{270462} = \mathbf{PI}(0,1,0,1,1,0)_{12417}$$

$$\ell_5 = \begin{bmatrix} 1 & \epsilon^{10} & \epsilon^{15} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5771306} = \begin{bmatrix} 1 & 42 & 21 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5771306} = \mathbf{PI}(0,1,0,1,1,0)_{12417}$$

$$\ell_6 = \begin{bmatrix} 1 & \epsilon^{44} & \epsilon^{43} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4672802} = \begin{bmatrix} 1 & 34 & 17 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4672802} = \mathbf{PI}(0,17,0,34,1,0)_{16624}$$

$$\ell_7 = \begin{bmatrix} 1 & \epsilon^{25} & \epsilon^{23} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10389211} = \begin{bmatrix} 1 & 59 & 38 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10389211} = \mathbf{PI}(0,38,0,59,1,0)_{19820}$$

$$\ell_8 = \begin{bmatrix} 1 & \epsilon^{41} & \epsilon^{45} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{10389211} = \begin{bmatrix} 1 & 26 & 54 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14492762} = \mathbf{PI}(0,54,0,26,1,0)_{15645}$$

$$\ell_0 = \begin{bmatrix} 1 & \epsilon^{41} & \epsilon^{45} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3973916} = \begin{bmatrix} 1 & 28 & 37 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3973916} = \mathbf{PI}(0,37,0,28,1,0)_{15820}$$

$$\ell_{10} = \begin{bmatrix} 1 & \epsilon^{21} & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3370881} = \begin{bmatrix} 1 & 57 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3073861} = \mathbf{PI}(0,49,0,5,1,0)_{19539}$$

$$\ell_{11} = \begin{bmatrix} 1 & \epsilon^{21} & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3120681} = \begin{bmatrix} 1 & 22 & 42 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3170681} = \mathbf{PI}(0,48,0,52,1,0)_{18520}$$

$$\ell_{12} = \begin{bmatrix} 1 & \epsilon^{19} & \epsilon^{16} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3303124} = \begin{bmatrix} 1 & 58 & 38 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{31033124} = \mathbf{PI}(0,48,0,52,1,0)_{18021}$$

$$\ell_{14} = \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{62} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3303124} = \begin{bmatrix} 1 & 58 & 38 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30303124} = \mathbf{PI}(0,48,0,52,1,0)_{18020}$$

$$\ell_{14} = \begin{bmatrix} 1 & \epsilon^{43} & \epsilon^{43} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30305250} = \begin{bmatrix} 1 & 58 & 38 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{30305250} = \mathbf{PI}(0,38,0,58,1,0)_{19030}$$

$$\ell_{16} = \begin{bmatrix} 1 & \epsilon^{17} & \epsilon^{62} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3007286} = \begin{bmatrix} 1 & 53 & 48 & 0$$

$$\begin{split} \ell_{22} &= \begin{bmatrix} 1 & \epsilon^{41} & \epsilon & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{653276} = \begin{bmatrix} 1 & 28 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{653276} = \mathbf{Pl}(0, 2, 0, 28, 1, 0)_{18654} \\ \ell_{23} &= \begin{bmatrix} 1 & \epsilon^{52} & \epsilon^{4} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4473074} = \begin{bmatrix} 1 & 50 & 16 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4473074} = \mathbf{Pl}(0, 16, 0, 50, 1, 0)_{18655} \\ \ell_{24} &= \begin{bmatrix} 1 & \epsilon^{21} & \epsilon^{36} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9828281} = \begin{bmatrix} 1 & 57 & 36 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{9828281} = \mathbf{Pl}(0, 36, 0, 57, 1, 0)_{19564} \\ \ell_{25} &= \begin{bmatrix} 1 & \epsilon & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3208130} = \begin{bmatrix} 1 & 21 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3208130} = \mathbf{Pl}(0, 12, 0, 2, 1, 0)_{12555} \\ \ell_{26} &= \begin{bmatrix} 1 & \epsilon^{50} & \epsilon^{46} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{11704892} &= \begin{bmatrix} 1 & 60 & 43 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1704892} = \mathbf{Pl}(0, 43, 0, 60, 1, 0)_{19952} \\ \ell_{27} &= \begin{bmatrix} 1 & \epsilon^{19} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12345686} &= \begin{bmatrix} 1 & 22 & 46 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12345686} &= \mathbf{Pl}(0, 46, 0, 22, 1, 0)_{15129} \\ \ell_{28} &= \begin{bmatrix} 1 & \epsilon^{55} & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3732497} &= \begin{bmatrix} 1 & 17 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3732497} &= \mathbf{Pl}(0, 25, 0, 17, 1, 0)_{14473} \\ \ell_{29} &= \begin{bmatrix} 1 & \epsilon^{55} & \epsilon^{60} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2875250} &= \begin{bmatrix} 1 & 3 & 12 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2875250} &= \mathbf{Pl}(0, 10, 50, 1, 0)_{18649} \\ \ell_{31} &= \begin{bmatrix} 1 & \epsilon^{55} & \epsilon^{50} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2875250} &= \begin{bmatrix} 1 & 19 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2875250} &= \mathbf{Pl}(0, 7, 0, 39, 1, 0)_{14707} \\ \ell_{32} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{51} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1414739} &= \mathbf{Pl}(0, 24, 0, 8, 1, 0)_{13329} \\ \ell_{34} &= \begin{bmatrix} 1 & \epsilon^{13} & \epsilon^{50} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{16128744} &= \begin{bmatrix} 1 & 19 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1414739} &= \mathbf{Pl}(0, 24, 0, 8, 1, 0)_{13329} \\ \ell_{34} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{50} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1629744} &= \begin{bmatrix} 1 & 50 & 36 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14470275} &= \mathbf{Pl}(0, 26, 0, 51, 1, 0)_{18792} \\ \ell_{35} &= \begin{bmatrix} 1 & \epsilon^{33} & \epsilon^{50} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14833964} &= \begin{bmatrix} 1 & 51 & 26 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14833964} &= \mathbf{Pl}(0, 24, 0, 9, 1, 0)_{13456} \\ \ell_{49} &= \begin{bmatrix} 1 & \epsilon^{24} & \epsilon^{56} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14833964} &= \begin{bmatrix} 1 & 61 & 43 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{14833964} &= \mathbf{Pl}(0, 43, 0, 61, 1, 0)_$$

$$\begin{split} \ell_{43} &= \begin{bmatrix} 1 & \epsilon^{41} & \epsilon^{58} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{332063} = \begin{bmatrix} 1 & 31 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{332063} = PI(0,3,0,31,1,0)_{16229} \\ \ell_{44} &= \begin{bmatrix} 1 & \epsilon^4 & \epsilon^{51} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6728336} = \begin{bmatrix} 1 & 16 & 25 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{6728336} = PI(0,25,0,16,1,0)_{14346} \\ \ell_{45} &= \begin{bmatrix} 1 & \epsilon^{52} & \epsilon^{52} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7136114} = \begin{bmatrix} 1 & 50 & 26 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7136114} = PI(0,26,0,50,1,0)_{18665} \\ \ell_{46} &= \begin{bmatrix} 1 & \epsilon^{12} & \epsilon^{55} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{5588222} = \begin{bmatrix} 1 & 62 & 20 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7136114} = PI(0,26,0,50,1,0)_{18665} \\ \ell_{47} &= \begin{bmatrix} 1 & \epsilon^{22} & \epsilon^{55} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{165079} = \begin{bmatrix} 1 & 62 & 20 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{165079} = PI(0,4,0,23,1,0)_{15214} \\ \ell_{48} &= \begin{bmatrix} 1 & \epsilon^{22} & \epsilon^{18} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3166520} = \begin{bmatrix} 1 & 56 & 11 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3165520} = PI(0,4,0,23,1,0)_{15214} \\ \ell_{49} &= \begin{bmatrix} 1 & \epsilon^{56} & \epsilon^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7360808} = \begin{bmatrix} 1 & 40 & 27 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{7360808} = PI(0,27,0,40,1,0)_{17396} \\ \ell_{50} &= \begin{bmatrix} 1 & \epsilon^{5} & \epsilon^{59} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1735136} = \begin{bmatrix} 1 & 32 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1735136} = PI(0,77,0,35,1,0)_{16751} \\ \ell_{51} &= \begin{bmatrix} 1 & \epsilon^{56} & \epsilon^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1735136} = \begin{bmatrix} 1 & 14 & 13 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1735136} = PI(0,46,0,32,1,0)_{16359} \\ \ell_{52} &= \begin{bmatrix} 1 & \epsilon^{26} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12349847} = PI(0,46,0,23,1,0)_{16256} \\ \ell_{54} &= \begin{bmatrix} 1 & \epsilon^{26} & \epsilon^{27} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12349847} = \begin{bmatrix} 1 & 23 & 46 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12496923} = PI(0,47,0,56,1,0)_{19428} \\ \ell_{55} &= \begin{bmatrix} 1 & \epsilon^{26} & \epsilon^{29} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12753464} = \begin{bmatrix} 1 & 27 & 54 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12753464} = PI(0,47,0,56,1,0)_{19428} \\ \ell_{56} &= \begin{bmatrix} 1 & \epsilon^{41} & \epsilon^{8} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{12753464} = \begin{bmatrix} 1 & 22 & 4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{136998} = PI(0,47,0,56,1,0)_{19428} \\ \ell_{59} &= \begin{bmatrix} 1 & \epsilon^{49} & \epsilon^{2} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2026406} = \begin{bmatrix} 1 & 51 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2879411} = PI(0,47,0,57,1,0)_{15772} \\ \ell_{69} &= \begin{bmatrix} 1 & \epsilon^{23} & \epsilon^{39} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2879411} = \begin{bmatrix} 1 & 51 & 10 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2879411} =$$

$$\ell_{64} = \left[\begin{array}{cccc} 1 & \epsilon^{26} & \epsilon^{16} & 0 \\ 0 & 0 & 0 & 1 \end{array}\right]_{11284631} = \left[\begin{array}{cccc} 1 & 23 & 42 & 0 \\ 0 & 0 & 0 & 1 \end{array}\right]_{11284631} = \mathbf{Pl}(0, 42, 0, 23, 1, 0)_{15252}$$

Rank of lines: (4160, 17043520, 8321, 270464, 274625, 5771306, 4672802, 10369211, 14492762, 9973916, 13073861, 3170681, 11280470, 13003124, 4477235, 10365050, 927902, 13007285, 5592383, 9978077, 5775467, 14838125, 653276, 4473074, 9828281, 3208130, 11704892, 12345686, 6732497, 3212291, 2875250, 2030567, 1414739, 6428744, 10510685, 7140275, 9824120, 6432905, 14833964, 11709053, 1410578, 7364969, 13069700, 932063, 6728336, 7136114, 5588222, 1165079, 3166520, 7360808, ...657437, 1739297, 11284631)
Rank of points on Klein quadric: <math>(4225, 129, 12353, 4289, 12417, 17644, 16624, 19820, 15645, 15882, 12973, 19539, 15125, 18941, 18782, 19693, 16102, 19068, 20310, 16009, 17771, 18059, 15847, 18655, 19564, 12555, 19952, 15129, 14473, 12682, 18649, 17249, 14707, 13329, 16011, 18792, 19437, 13456, 17932, 20079, 14580, 17523, 12846, 16229, 14346, 18665, 20183, 15214, 19412, 17396, ...15974, 16486, 15252)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points: The double points on the surface are:

Single Points

The surface has 4160 single points: Too many to print.

Points on surface but on no line

The surface has 0 points not on any line: The points on the surface but not on lines are:

Line Intersection Graph

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(0 0	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	$\overline{1}$	1	1	1	1	1	1	1	1	1
-	1 1	0.1	1 1	1 1	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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4	_ _	10				_	_	_	1	1	_	1	_	_	_	_		_	_	_	_	_	_	_	1	_	_	_	_	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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4	4 1	11	10	1 1	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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9	2 1	11	1 1	1 1	1.0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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10	1	11	11	11	11	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1 1	11	11	1 1	1 1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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14	4 1	11	11	11	11	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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18	3 1	11	11	1 1	1 1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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20	$1 \mid \Gamma$	11	11	11	1 1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	_	_	1	1	1	1	1	1	1
2	1 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
25	$2 \mid 1$	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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24	$4 \mid 1$	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
25	5 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
26	3 1	11	1 1	1 1	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
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28	$^{3} 1$	11	11	11	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
29	9 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
30	1	11	1 1	1 1	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	Ω	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
	-																										-															1		
3.		11																										-						1	1	1	1	1	1	1	1	1	1	1
32	2 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
33	3 1	11	11	1 1	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
34	-	11																												-				1	1	1	1	1	1	1	1	1	1	1
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	_ _	11				_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_
36	$3 \mid 1$	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
3	7 1	11	11	1 1	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
	- 1	11																																										
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40	1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
4	1 1	11	11	1 1	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1
	- 1	11																																										
	- 1																																											
4:	$^{3 1}$	11	11	11	1 1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
4	4 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
		11																																										
	- 1	11																																										
4^{\prime}	7 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
48	$ _{1}$	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
		11																																										
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51	1 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
55	$2 \mid 1$	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
	- 1	11																																										
		11																																										
55	5 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
56	3 1	11	11	11	11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

Neighbor s Line 0 inte			line	inter	secti	on gr	aph:															
Line	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 1 inte	ersect	s																				
Line	ℓ_0	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 2 inte	ersect	S																				
Line	ℓ_0	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 3 inte	ersect	S																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 4 inte	ersect	S																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 5 inte	ersect	s																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 6 inte	ersect																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 7 inte	ersect	S																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 8 inte	ersect	īS.																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 9 inte	ersect	S																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 10 in	erse	cts																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22}
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

 ℓ_8

 P_3

 ℓ_9

 P_3

 ℓ_{10}

 P_3

 ℓ_6

 P_3

 P_3

 ℓ_7

 P_3

 $\overline{\ell}_{12}$

 P_3

 ℓ_{13}

 P_3

 $\overline{\ell_{14}}$

 P_3

 ℓ_{15}

 P_3

 ℓ_{16}

 P_3

 ℓ_{17}

 P_3

 ℓ_{18}

 P_3

 ℓ_{19}

 P_3

 ℓ_{20}

 P_3

 ℓ_{21}

 P_3

 P_3

Line 11 intersects

 ℓ_3

 P_3 P_3

 P_3

 P_3

Line

in point

Line 12 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 13 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 14 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 15 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .										
Line 16 in	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .										
Line 17 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 18 int		ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{19}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 19 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{20}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 20 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{21}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 21 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{22} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 22 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 23 int		ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										
Line 24 int	ersec	ets																				
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3										

Line 25 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	<u>l</u>
Line 26 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	
in point $ P_3 $	⊥-
Line 27 intersects	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1
in point $ P_3 $	┸
Line 28 intersects	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
in point $ P_3 $	⊥-
Line 29 intersects	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1
in point P ₃ P ₃	⊥-
Line 30 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	
Line 31 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	+
Line 32 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	\top_{I}
in point P ₃ P ₃	1
Line 33 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	I
in point P_3 P	⊥-
Line 34 intersects	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
in point P ₃ P ₃	<u>_</u>
Line 35 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	
Line 36 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	\top_{I}
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
Line 37 intersects	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	T.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	

Line 38 int	terse	${ m cts}$																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	1
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Ц
Line 39 int	terse	cts																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	l
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Ц
Line 40 int		cts																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	l
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	щ
Line 41 int	terse	ets																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	l
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	ئے
Line 42 int	terse	ets																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	_{
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Ц
Line 43 int																							
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	L
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Ц
Line 44 int		ets		<u>. </u>			<u>. </u>											,		,	<u>. </u>		
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	l
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	႕
Line 45 int		cts																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	l
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	
Line 46 int																							_
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	L
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	_
Line 47 int																							
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	L
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	
Line 48 int																							
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	1
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	
Line 49 int	terse	cts																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	1
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	L
Line 50 int	terse	cts																					
Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	·

 P_3 P_3

in point

 P_3

Line 51 inte	ersects																				
	ℓ_0 ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	$P_3 \mid P_3$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 52 inte	ersects																				
	ℓ_0 ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	$P_3 \mid P_3$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 53 inte	ersects																				
	ℓ_0 ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	$P_3 \mid P_3$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .
Line 54 inte	ersects																				
	ℓ_0 ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	$P_3 \mid P_3$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .
Line 55 inte				T .			1							1 .	1 ,				1 .		
	$\frac{\ell_0}{R}$ $\frac{\ell_1}{R}$	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	$P_3 \mid P_3$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .
Line 56 inte		T 0	T 4		T 4	T 4	T 0		T 0	T a			T a	T 0	1 0	I	I			T	
	$\begin{array}{c c} \ell_0 & \ell_1 \\ \hline P_1 & P_2 \end{array}$	$\begin{array}{ c c }\hline \ell_2 \\\hline P_3 \end{array}$	ℓ_3 P_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8 P_3	ℓ_9	ℓ_{10}	ℓ_{11} P_3	ℓ_{12}	ℓ_{13} P_3	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
_	$P_3 \mid P_3$	<i>F</i> 3	F ₃	P_3	P_3	P_3	P_3	<i>F</i> 3	P_3	P_3	<i>F</i> 3	P_3	<i>F</i> 3	P_3							
Line 57 inte		1 0	T 0	T 0	T 0	T 0	1 0		1 0	T 0	1 0	1 0	T 0	T 0	Ι η	Ι η	T 0	Γη.	T 0	T 0	Ι ο
	$ \begin{array}{c cc} \ell_0 & \ell_1 \\ P_3 & P_3 \end{array} $	$\begin{array}{ c c c }\hline \ell_2 \\\hline P_3 \end{array}$	$\begin{array}{ c c c }\hline \ell_3 \\\hline P_3 \end{array}$	$\begin{array}{ c c c }\hline \ell_4 \\\hline P_3 \end{array}$	ℓ_5 P_3	ℓ_6 P_3	$\begin{array}{ c c c }\hline \ell_7 \\ P_3 \end{array}$	ℓ_8 P_3	l_9 P_3	$\begin{array}{ c c }\hline \ell_{10} \\\hline P_3 \end{array}$	ℓ_{11} P_3	ℓ_{12} P_3	ℓ_{13} P_3	ℓ_{14} P_3	ℓ_{15} P_3	ℓ_{16} P_3	ℓ_{17} P_3	ℓ_{18} P_3	ℓ_{19} P_3	ℓ_{20} P_3	$\begin{array}{ c c c c }\hline \ell_{21} & \ell_{21} \\\hline P_{3} & . \end{array}$
Line 58 int ϵ		13	13	13	13	13	13	13	13	13	13	13	13	13	13	13	13	13	13	13	13 1
	$\ell_0 \mid \ell_1$	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	Γ _{ℓ11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
	$\begin{array}{c c} \epsilon_0 & \epsilon_1 \\ \hline P_3 & P_3 \end{array}$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	ℓ_{11} P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
${\rm Line}\; 59\; {\rm int} \epsilon$	ersects																				
	$\ell_0 \mid \ell_1$	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	P_3 P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3 .
Line 60 inte	ersects																				
	ℓ_0 ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
in point	$P_3 \mid P_3$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 61 inte	ersects																				
	$ \begin{array}{c cc} \ell_0 & \ell_1 \\ P_3 & P_3 \end{array} $	$\begin{array}{ c c c }\hline \ell_2 \\ P_3 \end{array}$	ℓ_3 P_3	$\begin{array}{ c c c }\hline \ell_4 \\ P_3 \end{array}$	ℓ_5 P_3	ℓ_6 P_3	$\begin{array}{ c c c }\hline \ell_7 \\ P_3 \end{array}$	ℓ_8 P_3	l_9 P_3	ℓ_{10} P_3	ℓ_{11} P_3	ℓ_{12} P_3	ℓ_{13} P_3	ℓ_{14} P_3	ℓ_{15} P_3	ℓ_{16} P_3	ℓ_{17} P_3	ℓ_{18} P_3	ℓ_{19} P_3	ℓ_{20} P_3	$egin{array}{ c c c c c } \ell_{21} & \ell_{21} & \ell_{22} \\ P_3 & L_{22} & L_{23} & L_{23} \\ \hline \end{array}$
Line 62 int ϵ					Ū		Ü	·													
Line	$\ell_0 \mid \ell_1$	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}
	$\begin{array}{c cc} c_0 & c_1 \\ \hline P_3 & P_3 \end{array}$	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3
Line 63 inte		_ ~			· ·		_			_ ~	_ ~	_		_					_		
Line	$\ell_0 \mid \ell_1$	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21} ℓ
	P_3 P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3

Line 64 intersects

Line	ℓ_0	ℓ_1	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}	ℓ_{12}	ℓ_{13}	ℓ_{14}	ℓ_{15}	ℓ_{16}	ℓ_{17}	ℓ_{18}	ℓ_{19}	ℓ_{20}	ℓ_{21}	Γ.
in point	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	P_3	Π										

The surface has 4161 points:

Too many to print.