# Rank-65922 over GF(64)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0^2 X_1 + X_0^2 X_2 + X_0^2 X_3 + X_1^2 X_2 + X_0 X_1 X_2 = 0$$

(1, 1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(64) is -2113396602

### General information

Number of lines	12
Number of points	4353
Number of singular points	3
Number of Eckardt points	0
Number of double points	18
Number of single points	732
Number of points off lines	3600
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$65^{12}$
Type of lines on points	$4^3, 2^{18}, 1^{732}, 0^{3600}$

# Singular Points

The surface has 3 singular points:

$$\begin{array}{ll} 0: \ P_{48130} = \mathbf{P}(1, \epsilon^9, \epsilon^{54}, 1) = \mathbf{P}(1, 47, 10, 1) \\ 1: \ P_{156418} = \mathbf{P}(1, \epsilon^{18}, \epsilon^{45}, 1) = \mathbf{P}(1, 11, 37, 1) \end{array} \\ \end{array} \\ 2: \ P_{194882} = \mathbf{P}(1, \epsilon^{36}, \epsilon^{27}, 1) = \mathbf{P}(1, 36, 46, 1)$$

# The 12 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & \epsilon^{18} & 0 \\ 0 & 1 & \epsilon^{9} & 0 \end{bmatrix}_{45818} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 47 & 0 \end{bmatrix}_{45818} = \mathbf{Pl}(37, 0, 10, 0, 0, 1)_{271708}$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & \epsilon^{36} & 0 \\ 0 & 1 & \epsilon^{18} & 0 \end{bmatrix}_{149807} = \begin{bmatrix} 1 & 0 & 36 & 0 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{149807} = \mathbf{Pl}(46,0,37,0,0,1)_{275146}$$

$$\ell_2 = \begin{bmatrix} 1 & 0 & \epsilon^9 & 0 \\ 0 & 1 & \epsilon^{36} & 0 \end{bmatrix}_{195603} = \begin{bmatrix} 1 & 0 & 47 & 0 \\ 0 & 1 & 36 & 0 \end{bmatrix}_{195603} = \mathbf{Pl}(10,0,46,0,0,1)_{276253}$$

$$\ell_3 = \begin{bmatrix} 1 & 0 & \epsilon^{44} & \epsilon^{14} \\ 0 & 1 & \epsilon^{21} & \epsilon^7 \end{bmatrix}_{15589403} = \begin{bmatrix} 1 & 0 & 34 & 58 \\ 0 & 1 & 57 & 35 \end{bmatrix}_{15589403} = \mathbf{Pl}(23,41,54,52,23,1)_{6528718}$$

$$\ell_4 = \begin{bmatrix} 1 & 0 & \epsilon^{18} & 1 \\ 0 & 1 & \epsilon^9 & 0 \end{bmatrix}_{312122} = \begin{bmatrix} 1 & 0 & 11 & 1 \\ 0 & 1 & 47 & 0 \end{bmatrix}_{312122} = \mathbf{Pl}(47,10,10,37,0,1)_{430027}$$

$$\ell_5 = \begin{bmatrix} 1 & 0 & \epsilon^{37} & \epsilon^{49} \\ 0 & 1 & \epsilon^{42} & \epsilon^{56} \end{bmatrix}_{8162337} = \begin{bmatrix} 1 & 0 & 41 & 30 \\ 0 & 1 & 56 & 40 \end{bmatrix}_{8162337} = \mathbf{Pl}(22,34,25,62,22,1)_{6151410}$$

$$\ell_6 = \begin{bmatrix} 1 & 0 & \epsilon^{25} & \epsilon^{28} \\ 0 & 1 & \epsilon^{42} & \epsilon^{14} \end{bmatrix}_{16493811} = \begin{bmatrix} 1 & 0 & 59 & 61 \\ 0 & 1 & 56 & 58 \end{bmatrix}_{16493811} = \mathbf{Pl}(50,31,12,8,50,1)_{13438207}$$

$$\ell_7 = \begin{bmatrix} 1 & 0 & \epsilon^{22} & \epsilon^7 \\ 0 & 1 & \epsilon^{42} & \epsilon^{35} \end{bmatrix}_{9400907} = \begin{bmatrix} 1 & 0 & 19 & 35 \\ 0 & 1 & 56 & 18 \end{bmatrix}_{9400907} = \mathbf{Pl}(29,60,21,15,29,1)_{7970101}$$

$$\ell_8 = \begin{bmatrix} 1 & 0 & \epsilon^{36} & 1 \\ 0 & 1 & \epsilon^{18} & 0 \end{bmatrix}_{416111} = \begin{bmatrix} 1 & 0 & 36 & 1 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{416111} = \mathbf{Pl}(11,37,37,46,0,1)_{467413}$$

$$\ell_9 = \begin{bmatrix} 1 & 0 & \epsilon^{9} & 1 \\ 0 & 1 & \epsilon^{36} & 0 \end{bmatrix}_{461907} = \begin{bmatrix} 1 & 0 & 47 & 1 \\ 0 & 1 & 36 & 0 \end{bmatrix}_{461907} = \mathbf{Pl}(36,46,46,10,0,1)_{325121}$$

$$\ell_{10} = \begin{bmatrix} 1 & 0 & \epsilon^{11} & \epsilon^{35} \\ 0 & 1 & \epsilon^{21} & \epsilon^{49} \end{bmatrix}_{4924440} = \begin{bmatrix} 1 & 0 & 31 & 18 \\ 0 & 1 & 57 & 30 \end{bmatrix}_{4924440} = \mathbf{Pl}(51,59,7,45,51,1)_{13680317}$$

$$\ell_{11} = \begin{bmatrix} 1 & 0 & \epsilon^{50} & \epsilon^{56} \\ 0 & 1 & \epsilon^{21} & \epsilon^{28} \end{bmatrix}_{10905781} = \begin{bmatrix} 1 & 0 & 60 & 40 \\ 0 & 1 & 57 & 61 \end{bmatrix}_{10905781} = \mathbf{Pl}(28,19,49,33,28,1)_{7819152}$$

Rank of lines: ( 45818, 149807, 195603, 15589403, 312122, 8162337, 16493811, 9400907, 416111, 461907, 4924440, 10905781)

Rank of points on Klein quadric: ( 271708, 275146, 276253, 6528718, 430027, 6151410, 13438207, 7970101, 467413, 325121, 13680317, 7819152 )

#### **Eckardt Points**

The surface has 0 Eckardt points:

#### **Double Points**

The surface has 18 Double points: The double points on the surface are:

$$\begin{split} P_{3111} &= (36,47,1,0) = \ell_0 \cap \ell_1 \\ P_{2382} &= (11,36,1,0) = \ell_0 \cap \ell_2 \\ P_{707} &= (0,10,1,0) = \ell_0 \cap \ell_4 \\ P_{1626} &= (23,24,1,0) = \ell_0 \cap \ell_7 \\ P_{3609} &= (22,55,1,0) = \ell_0 \cap \ell_{11} \\ P_{818} &= (47,11,1,0) = \ell_1 \cap \ell_2 \\ P_{501} &= (50,6,1,0) = \ell_1 \cap \ell_3 \\ P_{950} &= (51,13,1,0) = \ell_1 \cap \ell_5 \\ P_{2435} &= (0,37,1,0) = \ell_1 \cap \ell_8 \\ P_{1375} &= (28,20,1,0) = \ell_2 \cap \ell_6 \end{split}$$

$$\begin{split} P_{3011} &= (0,46,1,0) = \ell_2 \cap \ell_9 \\ P_{3168} &= (29,48,1,0) = \ell_2 \cap \ell_{10} \\ P_{265721} &= (56,54,63,1) = \ell_3 \cap \ell_6 \\ P_{136634} &= (57,21,32,1) = \ell_3 \cap \ell_7 \\ P_{222906} &= (57,25,53,1) = \ell_5 \cap \ell_{10} \\ P_{64697} &= (56,49,14,1) = \ell_5 \cap \ell_{11} \\ P_{185210} &= (57,12,44,1) = \ell_6 \cap \ell_{11} \\ P_{41529} &= (56,7,9,1) = \ell_7 \cap \ell_{10} \end{split}$$

#### Single Points

The surface has 732 single points: The single points on the surface are:

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0: P_{14} = (10, 1, 0, 0) lies on line \ell_0
                                                                      48: P_{1139} = (48, 16, 1, 0) lies on line \ell_1
1: P_{41} = (37, 1, 0, 0) lies on line \ell_1
                                                                      49: P_{1176} = (21, 17, 1, 0) lies on line \ell_1
2: P_{50} = (46, 1, 0, 0) lies on line \ell_2
                                                                      50: P_{1196} = (41, 17, 1, 0) lies on line \ell_2
3: P_{77} = (10, 0, 1, 0) lies on line \ell_2
                                                                      51: P_{1199} = (44, 17, 1, 0) lies on line \ell_0
4: P_{104} = (37, 0, 1, 0) lies on line \ell_0
                                                                      52: P_{1246} = (27, 18, 1, 0) lies on line \ell_1
5: P_{113} = (46, 0, 1, 0) lies on line \ell_1
                                                                      53: P_{1269} = (50, 18, 1, 0) lies on line \ell_0
6: P_{142} = (11, 1, 1, 0) lies on line \ell_1
                                                                      54: P_{1277} = (58, 18, 1, 0) lies on line \ell_2
7: P_{167} = (36, 1, 1, 0) lies on line \ell_2
                                                                      55: P_{1303} = (20, 19, 1, 0) lies on line \ell_2
8: P_{178} = (47, 1, 1, 0) lies on line \ell_0
                                                                      56: P_{1339} = (56, 19, 1, 0) lies on line \ell_0
                                                                      57: P_{1345} = (62, 19, 1, 0) lies on line \ell_1
9: P_{200} = (5, 2, 1, 0) lies on line \ell_1
10: P_{244} = (49, 2, 1, 0) lies on line \ell_0
                                                                      58: P_{1354} = (7, 20, 1, 0) lies on line \ell_1
11: P_{250} = (55, 2, 1, 0) lies on line \ell_2
                                                                      59: P_{1361} = (14, 20, 1, 0) lies on line \ell_0
12 : P_{284} = (25, 3, 1, 0) lies on line \ell_2
                                                                      60: P_{1415} = (4, 21, 1, 0) lies on line \ell_0
13: P_{291} = (32, 3, 1, 0) lies on line \ell_1
                                                                      61: P_{1445} = (34, 21, 1, 0) lies on line \ell_1
                                                                      62: P_{1461} = (50, 21, 1, 0) lies on line \ell_2
14: P_{318} = (59, 3, 1, 0) lies on line \ell_0
15: P_{336} = (13, 4, 1, 0) lies on line \ell_0
                                                                      63: P_{1501} = (26, 22, 1, 0) lies on line \ell_0
                                                                      64: P_{1508} = (33, 22, 1, 0) lies on line \ell_2
16: P_{340} = (17, 4, 1, 0) lies on line \ell_2
17: P_{348} = (25, 4, 1, 0) lies on line \ell_1
                                                                      65: P_{1519} = (44, 22, 1, 0) lies on line \ell_1
18: P_{394} = (7, 5, 1, 0) lies on line \ell_0
                                                                      66: P_{1548} = (9, 23, 1, 0) lies on line \ell_1
19: P_{447} = (60, 5, 1, 0) lies on line \ell_1
                                                                      67: P_{1554} = (15, 23, 1, 0) lies on line \ell_2
                                                                      68: P_{1555} = (16, 23, 1, 0) lies on line \ell_0
20: P_{450} = (63, 5, 1, 0) lies on line \ell_2
21: P_{476} = (25, 6, 1, 0) lies on line \ell_0
                                                                      69: P_{1652} = (49, 24, 1, 0) lies on line \ell_2
22: P_{495} = (44, 6, 1, 0) lies on line \ell_2
                                                                      70: P_{1666} = (63, 24, 1, 0) lies on line \ell_1
23: P_{517} = (2,7,1,0) lies on line \ell_2
                                                                      71: P_{1693} = (26, 25, 1, 0) lies on line \ell_1
24: P_{534} = (19, 7, 1, 0) lies on line \ell_0
                                                                      72: P_{1696} = (29, 25, 1, 0) lies on line \ell_0
25: P_{538} = (23, 7, 1, 0) lies on line \ell_1
                                                                      73: P_{1698} = (31, 25, 1, 0) lies on line \ell_2
26: P_{599} = (20, 8, 1, 0) lies on line \ell_0
                                                                      74: P_{1734} = (3, 26, 1, 0) lies on line \ell_0
27: P_{612} = (33, 8, 1, 0) lies on line \ell_1
                                                                      75: P_{1743} = (12, 26, 1, 0) lies on line \ell_2
28: P_{639} = (60, 8, 1, 0) lies on line \ell_2
                                                                      76 : P_{1751} = (20, 26, 1, 0) lies on line \ell_1
29: P_{647} = (4, 9, 1, 0) lies on line \ell_1
                                                                      77: P_{1804} = (9, 27, 1, 0) lies on line \ell_0
30: P_{661} = (18, 9, 1, 0) lies on line \ell_2
                                                                      78: P_{1829} = (34, 27, 1, 0) lies on line \ell_2
                                                                      79: P_{1844} = (49, 27, 1, 0) lies on line \ell_1
31: P_{673} = (30, 9, 1, 0) lies on line \ell_0
32: P_{708} = (1, 10, 1, 0) lies on line \ell_2
                                                                      80: P_{1867} = (8, 28, 1, 0) lies on line \ell_1
33: P_{717} = (10, 10, 1, 0) lies on line \ell_1
                                                                      81: P_{1901} = (42, 28, 1, 0) lies on line \ell_2
34: P_{781} = (10, 11, 1, 0) lies on line \ell_0
                                                                      82: P_{1922} = (63, 28, 1, 0) lies on line \ell_0
35: P_{857} = (22, 12, 1, 0) lies on line \ell_1
                                                                      83: P_{1927} = (4, 29, 1, 0) lies on line \ell_2
36: P_{874} = (39, 12, 1, 0) lies on line \ell_2
                                                                      84: P_{1968} = (45, 29, 1, 0) lies on line \ell_1
37: P_{895} = (60, 12, 1, 0) lies on line \ell_0
                                                                      85: P_{1976} = (53, 29, 1, 0) lies on line \ell_0
38: P_{908} = (9, 13, 1, 0) lies on line \ell_2
                                                                      86: P_{2010} = (23, 30, 1, 0) lies on line \ell_2
                                                                      87: P_{2022} = (35, 30, 1, 0) lies on line \ell_1
39: P_{953} = (54, 13, 1, 0) lies on line \ell_0
                                                                      88 : P_{2030} = (43, 30, 1, 0) lies on line \ell_0
40: P_{989} = (26, 14, 1, 0) lies on line \ell_2
41: P_{1003} = (40, 14, 1, 0) lies on line \ell_0
                                                                      89: P_{2057} = (6, 31, 1, 0) lies on line \ell_1
42: P_{1024} = (61, 14, 1, 0) lies on line \ell_1
                                                                      90: P_{2084} = (33, 31, 1, 0) lies on line \ell_0
43: P_{1051} = (24, 15, 1, 0) lies on line \ell_1
                                                                      91: P_{2108} = (57, 31, 1, 0) lies on line \ell_2
44: P_{1061} = (34, 15, 1, 0) lies on line \ell_0
                                                                      92: P_{2131} = (16, 32, 1, 0) lies on line \ell_2
45: P_{1079} = (52, 15, 1, 0) lies on line \ell_2
                                                                      93: P_{2133} = (18, 32, 1, 0) lies on line \ell_1
46: P_{1098} = (7, 16, 1, 0) lies on line \ell_2
                                                                      94: P_{2150} = (35, 32, 1, 0) lies on line \ell_0
47: P_{1129} = (38, 16, 1, 0) lies on line \ell_0
                                                                      95: P_{2220} = (41, 33, 1, 0) lies on line \ell_0
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96: P_{2234} = (55, 33, 1, 0) lies on line \ell_1
                                                                     150: P_{3499} = (40, 53, 1, 0) lies on line \ell_2
97: P_{2241} = (62, 33, 1, 0) lies on line \ell_2
                                                                     151: P_{3539} = (16, 54, 1, 0) lies on line \ell_1
98: P_{2288} = (45, 34, 1, 0) lies on line \ell_2
                                                                     152: P_{3551} = (28, 54, 1, 0) lies on line \ell_0
                                                                     153: P_{3582} = (59, 54, 1, 0) lies on line \ell_2
99: P_{2298} = (55, 34, 1, 0) lies on line \ell_0
100: P_{2300} = (57, 34, 1, 0) lies on line \ell_1
                                                                     154: P_{3608} = (21, 55, 1, 0) lies on line \ell_2
101: P_{2310} = (3, 35, 1, 0) lies on line \ell_2
                                                                     155: P_{3640} = (53, 55, 1, 0) lies on line \ell_1
102: P_{2335} = (28, 35, 1, 0) lies on line \ell_1
                                                                     156: P_{3654} = (3, 56, 1, 0) lies on line \ell_1
103: P_{2368} = (61, 35, 1, 0) lies on line \ell_0
                                                                     157: P_{3668} = (17, 56, 1, 0) lies on line \ell_0
104: P_{2408} = (37, 36, 1, 0) lies on line \ell_1
                                                                     158: P_{3694} = (43, 56, 1, 0) lies on line \ell_2
105: P_{2436} = (1, 37, 1, 0) lies on line \ell_0
                                                                     159: P_{3720} = (5, 57, 1, 0) lies on line \ell_2
106: P_{2472} = (37, 37, 1, 0) lies on line \ell_2
                                                                     160: P_{3742} = (27, 57, 1, 0) lies on line \ell_0
107: P_{2513} = (14, 38, 1, 0) lies on line \ell_1
                                                                     161: P_{3753} = (38, 57, 1, 0) lies on line \ell_1
108: P_{2530} = (31, 38, 1, 0) lies on line \ell_0
                                                                     162: P_{3784} = (5, 58, 1, 0) lies on line \ell_0
109: P_{2553} = (54, 38, 1, 0) lies on line \ell_2
                                                                     163: P_{3801} = (22, 58, 1, 0) lies on line \ell_2
110: P_{2584} = (21, 39, 1, 0) lies on line \ell_0
                                                                     164: P_{3819} = (40, 58, 1, 0) lies on line \ell_1
111: P_{2587} = (24, 39, 1, 0) lies on line \ell_2
                                                                     165: P_{3856} = (13, 59, 1, 0) lies on line \ell_1
112: P_{2606} = (43, 39, 1, 0) lies on line \ell_1
                                                                     166: P_{3858} = (15, 59, 1, 0) lies on line \ell_0
113: P_{2645} = (18, 40, 1, 0) lies on line \ell_0
                                                                     167: P_{3899} = (56, 59, 1, 0) lies on line \ell_2
114: P_{2656} = (29, 40, 1, 0) lies on line \ell_1
                                                                     168: P_{3955} = (48, 60, 1, 0) lies on line \ell_2
115: P_{2665} = (38, 40, 1, 0) lies on line \ell_2
                                                                     169: P_{3959} = (52, 60, 1, 0) lies on line \ell_1
116: P_{2699} = (8, 41, 1, 0) lies on line \ell_2
                                                                     170: P_{3964} = (57, 60, 1, 0) lies on line \ell_0
                                                                     171: P_{3988} = (17, 61, 1, 0) lies on line \ell_1
117: P_{2715} = (24, 41, 1, 0) lies on line \ell_0
118: P_{2747} = (56, 41, 1, 0) lies on line \ell_1
                                                                     172: P_{4001} = (30, 61, 1, 0) lies on line \ell_2
119: P_{2761} = (6, 42, 1, 0) lies on line \ell_0
                                                                     173: P_{4022} = (51, 61, 1, 0) lies on line \ell_0
120: P_{2782} = (27, 42, 1, 0) lies on line \ell_2
                                                                     174: P_{4048} = (13, 62, 1, 0) lies on line \ell_2
121: P_{2809} = (54, 42, 1, 0) lies on line \ell_1
                                                                     175: P_{4066} = (31, 62, 1, 0) lies on line \ell_1
122: P_{2831} = (12, 43, 1, 0) lies on line \ell_0
                                                                     176: P_{4080} = (45, 62, 1, 0) lies on line \ell_0
123: P_{2838} = (19, 43, 1, 0) lies on line \ell_1
                                                                     177: P_{4134} = (35, 63, 1, 0) lies on line \ell_2
124: P_{2872} = (53, 43, 1, 0) lies on line \ell_2
                                                                     178: P_{4138} = (39, 63, 1, 0) lies on line \ell_0
125: P_{2925} = (42, 44, 1, 0) lies on line \ell_1
                                                                     179: P_{4157} = (58, 63, 1, 0) lies on line \ell_1
126: P_{2941} = (58, 44, 1, 0) lies on line \ell_0
                                                                     180: P_{4867} = (1, 11, 0, 1) lies on line \ell_8
127: P_{2944} = (61, 44, 1, 0) lies on line \ell_2
                                                                     181: P_{5615} = (45, 22, 0, 1) lies on line \ell_5
128: P_{2962} = (15, 45, 1, 0) lies on line \ell_1
                                                                     182: P_{5642} = (8, 23, 0, 1) lies on line \ell_3
129: P_{2966} = (19, 45, 1, 0) lies on line \ell_2
                                                                     183: P_{6016} = (62, 28, 0, 1) lies on line \ell_{11}
130: P_{2995} = (48, 45, 1, 0) lies on line \ell_0
                                                                     184: P_{6070} = (52, 29, 0, 1) lies on line \ell_7
131: P_{3012} = (1, 46, 1, 0) lies on line \ell_1
                                                                     185: P_{6467} = (1, 36, 0, 1) lies on line \ell_9
132: P_{3057} = (46, 46, 1, 0) lies on line \ell_0
                                                                     186: P_{7171} = (1, 47, 0, 1) lies on line \ell_4
133 : P_{3121} = (46, 47, 1, 0) lies on line \ell_2
                                                                     187: P_{7395} = (33, 50, 0, 1) lies on line \ell_6
134 : P_{3151} = (12, 48, 1, 0) lies on line \ell_1
                                                                     188: P_{7441} = (15, 51, 0, 1) lies on line \ell_{10}
135: P_{3171} = (32, 48, 1, 0) lies on line \ell_0
                                                                     189: P_{8467} = (18, 3, 1, 1) lies on line \ell_{10}
136: P_{3244} = (41, 49, 1, 0) lies on line \ell_1
                                                                     190: P_{8612} = (35, 5, 1, 1) lies on line \ell_7
137: P_{3245} = (42, 49, 1, 0) lies on line \ell_0
                                                                     191: P_{8898} = (1, 10, 1, 1) lies on line \ell_9
138: P_{3254} = (51, 49, 1, 0) lies on line \ell_2
                                                                     192: P_{9403} = (58, 17, 1, 1) lies on line \ell_3
139: P_{3299} = (32, 50, 1, 0) lies on line \ell_2
                                                                     193: P_{10015} = (30, 27, 1, 1) lies on line \ell_5
140: P_{3306} = (39, 50, 1, 0) lies on line \ell_1
                                                                     194: P_{10626} = (1, 37, 1, 1) lies on line \ell_4
                                                                     195 : P_{10750} = (61, 38, 1, 1) lies on line \ell_6
141: P_{3319} = (52, 50, 1, 0) lies on line \ell_0
142: P_{3333} = (2, 51, 1, 0) lies on line \ell_1
                                                                     196: P_{11049} = (40, 43, 1, 1) lies on line \ell_{11}
143: P_{3345} = (14, 51, 1, 0) lies on line \ell_2
                                                                     197: P_{11202} = (1, 46, 1, 1) lies on line \ell_8
                                                                     198 : P_{13163} = (42, 12, 2, 1) lies on line \ell_5
144: P_{3393} = (62, 51, 1, 0) lies on line \ell_0
145: P_{3401} = (6, 52, 1, 0) lies on line \ell_2
                                                                     199: P_{13587} = (18, 19, 2, 1) lies on line \ell_{11}
146: P_{3403} = (8, 52, 1, 0) lies on line \ell_0
                                                                     200: P_{13954} = (1, 25, 2, 1) lies on line \ell_9
147: P_{3454} = (59, 52, 1, 0) lies on line \ell_1
                                                                     201: P_{14042} = (25, 26, 2, 1) lies on line \ell_6
                                                                     202 : P_{14094} = (13, 27, 2, 1) lies on line \ell_3
148: P_{3461} = (2, 53, 1, 0) lies on line \ell_0
149: P_{3489} = (30, 53, 1, 0) lies on line \ell_1
                                                                     203: P_{14402} = (1, 32, 2, 1) lies on line \ell_8
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204: P_{15259} = (26, 45, 2, 1) lies on line \ell_7
                                                                     258: P_{39453} = (28, 39, 8, 1) lies on line \ell_3
205: P_{15606} = (53, 50, 2, 1) lies on line \ell_{10}
                                                                     259 : P_{40068} = (3, 49, 8, 1) lies on line \ell_6
                                                                     260: P_{40486} = (37, 55, 8, 1) lies on line \ell_{10}
206: P_{16130} = (1, 59, 2, 1) lies on line \ell_4
207: P_{16538} = (25, 1, 3, 1) lies on line \ell_5
                                                                     261: P_{42179} = (2, 18, 9, 1) lies on line \ell_5
208: P_{16617} = (40, 2, 3, 1) lies on line \ell_{10}
                                                                     262: P_{42306} = (1, 20, 9, 1) lies on line \ell_4
209: P_{16770} = (1, 5, 3, 1) lies on line \ell_8
                                                                     263: P_{42556} = (59, 23, 9, 1) lies on line \ell_{11}
                                                                     264: P_{43138} = (1, 33, 9, 1) lies on line \ell_8
210: P_{17350} = (5, 14, 3, 1) lies on line \ell_6
211: P_{18368} = (63, 29, 3, 1) lies on line \ell_3
                                                                     265: P_{43183} = (46, 33, 9, 1) lies on line \ell_3
212: P_{18757} = (4, 36, 3, 1) lies on line \ell_{11}
                                                                     266: P_{43424} = (31, 37, 9, 1) lies on line \ell_6
213: P_{19586} = (1, 49, 3, 1) lies on line \ell_4
                                                                     267: P_{44866} = (1, 60, 9, 1) lies on line \ell_9
214: P_{19854} = (13, 53, 3, 1) lies on line \ell_7
                                                                     268: P_{45495} = (54, 5, 10, 1) lies on line \ell_5
215: P_{19970} = (1, 55, 3, 1) lies on line \ell_9
                                                                     269: P_{45762} = (1, 10, 10, 1) lies on line \ell_4
216: P_{20680} = (7, 2, 4, 1) lies on line \ell_{11}
                                                                     270: P_{46780} = (59, 25, 10, 1) lies on line \ell_6
217: P_{20785} = (48, 3, 4, 1) lies on line \ell_6
                                                                     271: P_{47898} = (25, 43, 10, 1) lies on line \ell_3
218 : P_{20994} = (1, 7, 4, 1) lies on line \ell_4
                                                                     272: P_{48608} = (31, 54, 10, 1) lies on line \ell_{10}
219: P_{21507} = (2, 15, 4, 1) lies on line \ell_3
                                                                     273: P_{49218} = (1, 0, 11, 1) lies on line \ell_4
220: P_{22346} = (9, 28, 4, 1) lies on line \ell_7
                                                                     274: P_{49282} = (1, 1, 11, 1) lies on line \ell_9
221: P_{22756} = (35, 34, 4, 1) lies on line \ell_5
                                                                     275: P_{49603} = (2, 6, 11, 1) lies on line \ell_{10}
222: P_{23707} = (26, 49, 4, 1) lies on line \ell_{10}
                                                                     276: P_{49734} = (5, 8, 11, 1) lies on line \ell_5
223: P_{24386} = (1, 60, 4, 1) lies on line \ell_8
                                                                     277: P_{49858} = (1, 10, 11, 1) lies on line \ell_8
224: P_{24578} = (1, 63, 4, 1) lies on line \ell_9
                                                                     278: P_{50088} = (39, 13, 11, 1) lies on line \ell_6
225: P_{24712} = (7, 1, 5, 1) lies on line \ell_{10}
                                                                     279: P_{50776} = (23, 24, 11, 1) lies on line \ell_{11}
226: P_{24927} = (30, 4, 5, 1) lies on line \ell_7
                                                                     280: P_{52140} = (43, 45, 11, 1) lies on line \ell_3
227 : P_{25265} = (48, 9, 5, 1) lies on line \ell_3
                                                                     281: P_{52759} = (22, 55, 11, 1) lies on line \ell_7
228: P_{25474} = (1, 13, 5, 1) lies on line \ell_4
                                                                     282: P_{53331} = (18, 0, 12, 1) lies on line \ell_6
229: P_{25730} = (1, 17, 5, 1) lies on line \ell_9
                                                                     283: P_{53890} = (1, 9, 12, 1) lies on line \ell_9
230: P_{26157} = (44, 23, 5, 1) lies on line \ell_6
                                                                     284: P_{55251} = (18, 30, 12, 1) lies on line \ell_7
231: P_{26242} = (1, 25, 5, 1) lies on line \ell_8
                                                                     285: P_{56128} = (63, 43, 12, 1) lies on line \ell_5
232: P_{27665} = (16, 47, 5, 1) lies on line \ell_5
                                                                     286: P_{56578} = (1, 51, 12, 1) lies on line \ell_8
233: P_{28050} = (17, 53, 5, 1) lies on line \ell_{11}
                                                                     287: P_{56753} = (48, 53, 12, 1) lies on line \ell_{10}
234: P_{28866} = (1, 2, 6, 1) lies on line \ell_9
                                                                     288: P_{56770} = (1, 54, 12, 1) lies on line \ell_4
235 : P_{28936} = (7, 3, 6, 1) lies on line \ell_3
                                                                     289: P_{57301} = (20, 62, 12, 1) lies on line \ell_{11}
236: P_{29612} = (43, 13, 6, 1) lies on line \ell_{11}
                                                                     290: P_{57367} = (22, 63, 12, 1) lies on line \ell_3
237: P_{29954} = (1, 19, 6, 1) lies on line \ell_4
                                                                     291: P_{57774} = (45, 5, 13, 1) lies on line \ell_{10}
238: P_{30210} = (1, 23, 6, 1) lies on line \ell_8
                                                                     292: P_{57798} = (5, 6, 13, 1) lies on line \ell_7
239 : P_{31497} = (8, 43, 6, 1) lies on line \ell_6
                                                                     293: P_{57987} = (2, 9, 13, 1) lies on line \ell_{11}
240: P_{31592} = (39, 44, 6, 1) lies on line \ell_7
                                                                     294: P_{58703} = (14, 20, 13, 1) lies on line \ell_6
241: P_{31841} = (32, 48, 6, 1) lies on line \ell_{10}
                                                                     295 : P_{58818} = (1, 22, 13, 1) lies on line \ell_8
242 : P_{32357} = (36, 56, 6, 1) lies on line \ell_5
                                                                     296: P_{59853} = (12, 38, 13, 1) lies on line \ell_5
243 : P_{32894} = (61, 0, 7, 1) lies on line \ell_{10}
                                                                     297: P_{59906} = (1, 39, 13, 1) lies on line \ell_9
                                                                     298: P_{61093} = (36, 57, 13, 1) lies on line \ell_3
244: P_{33206} = (53, 5, 7, 1) lies on line \ell_3
245: P_{34434} = (1, 25, 7, 1) lies on line \ell_4
                                                                     299: P_{61250} = (1, 60, 13, 1) lies on line \ell_4
246: P_{35650} = (1, 44, 7, 1) lies on line \ell_9
                                                                     300: P_{63042} = (1, 24, 14, 1) lies on line \ell_8
247: P_{36034} = (1, 50, 7, 1) lies on line \ell_8
                                                                     301: P_{63682} = (1, 34, 14, 1) lies on line \ell_4
248: P_{36209} = (48, 52, 7, 1) lies on line \ell_7
                                                                     302: P_{64107} = (42, 40, 14, 1) lies on line \ell_6
249: P_{36248} = (23, 53, 7, 1) lies on line \ell_5
                                                                     303: P_{64509} = (60, 46, 14, 1) lies on line \ell_7
250: P_{36606} = (61, 58, 7, 1) lies on line \ell_{11}
                                                                     304: P_{64788} = (19, 51, 14, 1) lies on line \ell_3
251: P_{36885} = (20, 63, 7, 1) lies on line \ell_6
                                                                     305: P_{64834} = (1, 52, 14, 1) lies on line \ell_9
252: P_{37186} = (1, 4, 8, 1) lies on line \ell_8
                                                                     306: P_{64843} = (10, 52, 14, 1) lies on line \ell_{10}
253: P_{38082} = (1, 18, 8, 1) lies on line \ell_9
                                                                     307: P_{65880} = (23, 4, 15, 1) lies on line \ell_{10}
254: P_{38850} = (1, 30, 8, 1) lies on line \ell_4
                                                                     308: P_{66031} = (46, 6, 15, 1) lies on line \ell_{11}
255: P_{38960} = (47, 31, 8, 1) lies on line \ell_7
                                                                     309: P_{67266} = (1, 26, 15, 1) lies on line \ell_9
256: P_{38962} = (49, 31, 8, 1) lies on line \ell_5
                                                                     310: P_{68162} = (1, 40, 15, 1) lies on line \ell_4
257: P_{39022} = (45, 32, 8, 1) lies on line \ell_{11}
                                                                     311: P_{69026} = (33, 53, 15, 1) lies on line \ell_3
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312 : P_{69100} = (43, 54, 15, 1) lies on line \ell_7
                                                                     366 : P_{91274} = (9, 17, 21, 1) lies on line \ell_6
313 : P_{69452} = (11, 60, 15, 1) lies on line \ell_5
                                                                     367: P_{91970} = (1, 28, 21, 1) lies on line \ell_9
314 : P_{69495} = (54, 60, 15, 1) lies on line \ell_6
                                                                     368: P_{93048} = (55, 44, 21, 1) lies on line \ell_{11}
315: P_{69506} = (1, 61, 15, 1) lies on line \ell_8
                                                                     369: P_{94121} = (40, 61, 21, 1) lies on line \ell_5
316: P_{69974} = (21, 4, 16, 1) lies on line \ell_5
                                                                     370: P_{94448} = (47, 2, 22, 1) lies on line \ell_3
317: P_{70041} = (24, 5, 16, 1) lies on line \ell_{11}
                                                                     371: P_{94850} = (1, 9, 22, 1) lies on line \ell_8
                                                                     372 : P_{95234} = (1, 15, 22, 1) lies on line \ell_9
318: P_{71042} = (1, 21, 16, 1) lies on line \ell_8
319: P_{71137} = (32, 22, 16, 1) lies on line \ell_3
                                                                     373: P_{95298} = (1, 16, 22, 1) lies on line \ell_4
320 : P_{71299} = (2, 25, 16, 1) lies on line \ell_7
                                                                     374: P_{95566} = (13, 20, 22, 1) lies on line \ell_{11}
321: P_{72322} = (1, 41, 16, 1) lies on line \ell_9
                                                                     375: P_{96850} = (17, 40, 22, 1) lies on line \ell_7
322: P_{72514} = (1, 44, 16, 1) lies on line \ell_4
                                                                     376: P_{96989} = (28, 42, 22, 1) lies on line \ell_5
                                                                     377: P_{97198} = (45, 45, 22, 1) lies on line \ell_6
323: P_{73029} = (4, 52, 16, 1) lies on line \ell_6
324: P_{73531} = (58, 59, 16, 1) lies on line \ell_{10}
                                                                     378: P_{97878} = (21, 56, 22, 1) lies on line \ell_{10}
325: P_{73878} = (21, 1, 17, 1) lies on line \ell_7
                                                                     379: P_{98654} = (29, 4, 23, 1) lies on line \ell_3
326: P_{74242} = (1, 7, 17, 1) lies on line \ell_9
                                                                     380: P_{98889} = (8, 8, 23, 1) lies on line \ell_{10}
327: P_{74407} = (38, 9, 17, 1) lies on line \ell_5
                                                                     381: P_{100034} = (1, 26, 23, 1) lies on line \ell_4
328: P_{74536} = (39, 11, 17, 1) lies on line \ell_{10}
                                                                     382: P_{100482} = (1, 33, 23, 1) lies on line \ell_9
329: P_{74835} = (18, 16, 17, 1) lies on line \ell_3
                                                                     383: P_{100636} = (27, 35, 23, 1) lies on line \ell_{11}
                                                                     384 : P_{100912} = (47, 39, 23, 1) lies on line \ell_5
330: P_{75865} = (24, 32, 17, 1) lies on line \ell_6
                                                                     385: P_{101186} = (1, 44, 23, 1) lies on line \ell_8
331: P_{76226} = (1, 38, 17, 1) lies on line \ell_4
332 : P_{76866} = (1, 48, 17, 1) lies on line \ell_8
                                                                     386: P_{101447} = (6, 48, 23, 1) lies on line \ell_7
333 : P_{77007} = (14, 50, 17, 1) lies on line \ell_{11}
                                                                     387: P_{102066} = (49, 57, 23, 1) lies on line \ell_6
334 : P_{78581} = (52, 10, 18, 1) lies on line \ell_{11}
                                                                     388: P_{103306} = (9, 13, 24, 1) lies on line \ell_5
335 : P_{79170} = (1, 20, 18, 1) lies on line \ell_9
                                                                     389: P_{104130} = (1, 26, 24, 1) lies on line \ell_8
336: P_{79590} = (37, 26, 18, 1) lies on line \ell_3
                                                                     390: P_{104218} = (25, 27, 24, 1) lies on line \ell_7
337: P_{79741} = (60, 28, 18, 1) lies on line \ell_6
                                                                     391: P_{104322} = (1, 29, 24, 1) lies on line \ell_4
338: P_{79827} = (18, 30, 18, 1) lies on line \ell_5
                                                                     392: P_{104450} = (1, 31, 24, 1) lies on line \ell_9
339: P_{80557} = (44, 41, 18, 1) lies on line \ell_7
                                                                     393: P_{104949} = (52, 38, 24, 1) lies on line \ell_3
340: P_{81474} = (1, 56, 18, 1) lies on line \ell_4
                                                                     394: P_{106023} = (38, 55, 24, 1) lies on line \ell_6
341: P_{81601} = (0, 58, 18, 1) lies on line \ell_{10}
                                                                     395: P_{106124} = (11, 57, 24, 1) lies on line \ell_{11}
342: P_{81858} = (1, 62, 18, 1) lies on line \ell_8
                                                                     396: P_{106513} = (16, 63, 24, 1) lies on line \ell_{10}
343: P_{82529} = (32, 8, 19, 1) lies on line \ell_6
                                                                     397: P_{106619} = (58, 0, 25, 1) lies on line \ell_5
344: P_{82654} = (29, 10, 19, 1) lies on line \ell_{10}
                                                                     398: P_{106767} = (14, 3, 25, 1) lies on line \ell_7
345: P_{83234} = (33, 19, 19, 1) lies on line \ell_5
                                                                     399 : P_{107486} = (29, 14, 25, 1) lies on line \ell_{11}
346: P_{83714} = (1, 27, 19, 1) lies on line \ell_8
                                                                     400: P_{107534} = (13, 15, 25, 1) lies on line \ell_{10}
347: P_{83800} = (23, 28, 19, 1) lies on line \ell_3
                                                                     401: P_{108034} = (1, 23, 25, 1) lies on line \ell_4
348: P_{85180} = (59, 49, 19, 1) lies on line \ell_7
                                                                     402: P_{108615} = (6, 32, 25, 1) lies on line \ell_3
349 : P_{85186} = (1, 50, 19, 1) lies on line \ell_4
                                                                     403: P_{108859} = (58, 35, 25, 1) lies on line \ell_6
350: P_{85698} = (1, 58, 19, 1) lies on line \ell_9
                                                                     404: P_{109698} = (1, 49, 25, 1) lies on line \ell_9
351 : P_{85923} = (34, 61, 19, 1) lies on line \ell_{11}
                                                                     405: P_{110594} = (1, 63, 25, 1) lies on line \ell_8
                                                                     406: P_{111234} = (1, 9, 26, 1) lies on line \ell_4
352: P_{86338} = (1, 4, 20, 1) lies on line \ell_4
353: P_{86422} = (21, 5, 20, 1) lies on line \ell_6
                                                                     407: P_{112143} = (14, 23, 26, 1) lies on line \ell_5
354: P_{87019} = (42, 14, 20, 1) lies on line \ell_3
                                                                     408: P_{112671} = (30, 31, 26, 1) lies on line \ell_6
355: P_{87680} = (63, 24, 20, 1) lies on line \ell_7
                                                                     409: P_{112834} = (1, 34, 26, 1) lies on line \ell_9
356: P_{87842} = (33, 27, 20, 1) lies on line \ell_{11}
                                                                     410: P_{113394} = (49, 42, 26, 1) lies on line \ell_3
                                                                     411 : P_{113464} = (55, 43, 26, 1) lies on line \ell_7
357: P_{88258} = (1, 34, 20, 1) lies on line \ell_8
358: P_{89180} = (27, 48, 20, 1) lies on line \ell_5
                                                                     412: P_{113794} = (1, 49, 26, 1) lies on line \ell_8
359: P_{89282} = (1, 50, 20, 1) lies on line \ell_9
                                                                     413: P_{114152} = (39, 54, 26, 1) lies on line \ell_{11}
360: P_{89776} = (47, 57, 20, 1) lies on line \ell_{10}
                                                                     414: P_{114667} = (42, 62, 26, 1) lies on line \ell_{10}
361: P_{90217} = (40, 0, 21, 1) lies on line \ell_7
                                                                     415: P_{114866} = (49, 1, 27, 1) lies on line \ell_{11}
362: P_{90626} = (1, 7, 21, 1) lies on line \ell_8
                                                                     416: P_{114946} = (1, 3, 27, 1) lies on line \ell_4
363: P_{90713} = (24, 8, 21, 1) lies on line \ell_3
                                                                     417: P_{115459} = (2, 11, 27, 1) lies on line \ell_6
364 : P_{90803} = (50, 9, 21, 1) lies on line \ell_{10}
                                                                     418 : P_{115522} = (1, 12, 27, 1) lies on line \ell_9
365: P_{91074} = (1, 14, 21, 1) lies on line \ell_4
                                                                     419: P_{115704} = (55, 14, 27, 1) lies on line \ell_{10}
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474: P_{142039} = (22, 42, 33, 1) lies on line \ell_6
420: P_{116034} = (1, 20, 27, 1) lies on line \ell_8
                                                                     475: P_{143376} = (15, 63, 33, 1) lies on line \ell_5
421: P_{116478} = (61, 26, 27, 1) lies on line \ell_5
422: P_{117572} = (3, 44, 27, 1) lies on line \ell_3
                                                                     476: P_{143618} = (1, 3, 34, 1) lies on line \ell_9
423: P_{118049} = (32, 51, 27, 1) lies on line \ell_7
                                                                     477: P_{144883} = (50, 22, 34, 1) lies on line \ell_6
424: P_{119106} = (1, 4, 28, 1) lies on line \ell_9
                                                                     478: P_{145085} = (60, 25, 34, 1) lies on line \ell_3
425: P_{119288} = (55, 6, 28, 1) lies on line \ell_6
                                                                     479: P_{145218} = (1, 28, 34, 1) lies on line \ell_8
                                                                     480: P_{145600} = (63, 33, 34, 1) lies on line \ell_{11}
426: P_{120549} = (36, 26, 28, 1) lies on line \ell_7
427: P_{121395} = (50, 39, 28, 1) lies on line \ell_{11}
                                                                     481: P_{145663} = (62, 34, 34, 1) lies on line \ell_{10}
428: P_{121730} = (1, 45, 28, 1) lies on line \ell_8
                                                                     482 : P_{145816} = (23, 37, 34, 1) lies on line \ell_7
429: P_{122242} = (1, 53, 28, 1) lies on line \ell_4
                                                                     483: P_{146044} = (59, 40, 34, 1) lies on line \ell_5
430: P_{122504} = (7, 57, 28, 1) lies on line \ell_5
                                                                     484: P_{147330} = (1, 61, 34, 1) lies on line \ell_4
431 : P_{122758} = (5, 61, 28, 1) lies on line \ell_{10}
                                                                     485: P_{147695} = (46, 2, 35, 1) lies on line \ell_6
432 : P_{122879} = (62, 62, 28, 1) lies on line \ell_3
                                                                     486: P_{148708} = (35, 18, 35, 1) lies on line \ell_{10}
433: P_{123124} = (51, 2, 29, 1) lies on line \ell_7
                                                                     487: P_{148970} = (41, 22, 35, 1) lies on line \ell_{11}
434: P_{123458} = (1, 8, 29, 1) lies on line \ell_8
                                                                     488: P_{149519} = (14, 31, 35, 1) lies on line \ell_3
435: P_{123801} = (24, 13, 29, 1) lies on line \ell_{10}
                                                                     489: P_{149897} = (8, 37, 35, 1) lies on line \ell_5
436: P_{124005} = (36, 16, 29, 1) lies on line \ell_{11}
                                                                     490: P_{150402} = (1, 45, 35, 1) lies on line \ell_9
437: P_{124140} = (43, 18, 29, 1) lies on line \ell_6
                                                                     491: P_{151042} = (1, 55, 35, 1) lies on line \ell_4
438: P_{125634} = (1, 42, 29, 1) lies on line \ell_9
                                                                     492: P_{151170} = (1, 57, 35, 1) lies on line \ell_8
                                                                     493 : P_{151425} = (0, 61, 35, 1) lies on line \ell_7
439: P_{126325} = (52, 52, 29, 1) lies on line \ell_5
440: P_{126541} = (12, 56, 29, 1) lies on line \ell_3
                                                                     494: P_{151618} = (1, 0, 36, 1) lies on line \ell_8
441: P_{126978} = (1, 63, 29, 1) lies on line \ell_4
                                                                     495: P_{151682} = (1, 1, 36, 1) lies on line \ell_4
                                                                     496: P_{152051} = (50, 6, 36, 1) lies on line \ell_5
442: P_{127426} = (1, 6, 30, 1) lies on line \ell_8
443 : P_{129154} = (1, 33, 30, 1) lies on line \ell_4
                                                                     497 : P_{152500} = (51, 13, 36, 1) lies on line \ell_3
444: P_{129281} = (0, 35, 30, 1) lies on line \ell_5
                                                                     498: P_{152604} = (27, 15, 36, 1) lies on line \ell_6
445: P_{129631} = (30, 40, 30, 1) lies on line \ell_{11}
                                                                     499: P_{152901} = (4, 20, 36, 1) lies on line \ell_7
446: P_{129739} = (10, 42, 30, 1) lies on line \ell_7
                                                                     500: P_{153746} = (17, 33, 36, 1) lies on line \ell_{10}
447: P_{130000} = (15, 46, 30, 1) lies on line \ell_6
                                                                     501: P_{153986} = (1, 37, 36, 1) lies on line \ell_9
448: P_{130300} = (59, 50, 30, 1) lies on line \ell_3
                                                                     502: P_{154731} = (42, 48, 36, 1) lies on line \ell_{11}
449: P_{130690} = (1, 57, 30, 1) lies on line \ell_9
                                                                     503: P_{156221} = (60, 7, 37, 1) lies on line \ell_{11}
                                                                     504: P_{156500} = (19, 12, 37, 1) lies on line \ell_7
450: P_{130944} = (63, 60, 30, 1) lies on line \ell_{10}
451: P_{131939} = (34, 12, 31, 1) lies on line \ell_{10}
                                                                     505: P_{156813} = (12, 17, 37, 1) lies on line \ell_{10}
452: P_{132610} = (1, 23, 31, 1) lies on line \ell_9
                                                                     506: P_{157448} = (7, 27, 37, 1) lies on line \ell_6
453 : P_{133129} = (8, 31, 31, 1) lies on line \ell_{11}
                                                                     507: P_{158082} = (1, 37, 37, 1) lies on line \ell_8
454: P_{133378} = (1, 35, 31, 1) lies on line \ell_8
                                                                     508: P_{159927} = (54, 1, 38, 1) lies on line \ell_3
455 : P_{133890} = (1, 43, 31, 1) lies on line \ell_4
                                                                     509 : P_{161154} = (1, 21, 38, 1) lies on line \ell_4
456: P_{134132} = (51, 46, 31, 1) lies on line \ell_5
                                                                     510: P_{161346} = (1, 24, 38, 1) lies on line \ell_9
457: P_{134366} = (29, 50, 31, 1) lies on line \ell_7
                                                                     511: P_{161654} = (53, 28, 38, 1) lies on line \ell_5
458: P_{134474} = (9, 52, 31, 1) lies on line \ell_3
                                                                     512: P_{161900} = (43, 32, 38, 1) lies on line \ell_{10}
                                                                     513 : P_{162155} = (42, 36, 38, 1) lies on line \ell_7
459: P_{134868} = (19, 58, 31, 1) lies on line \ell_6
                                                                     514: P_{162340} = (35, 39, 38, 1) lies on line \ell_6
460: P_{137477} = (4, 35, 32, 1) lies on line \ell_{10}
461: P_{137858} = (1, 41, 32, 1) lies on line \ell_4
                                                                     515: P_{162562} = (1, 43, 38, 1) lies on line \ell_8
462 : P_{138196} = (19, 46, 32, 1) lies on line \ell_{11}
                                                                     516: P_{163847} = (6, 63, 38, 1) lies on line \ell_{11}
463: P_{138493} = (60, 50, 32, 1) lies on line \ell_5
                                                                     517: P_{164357} = (4, 7, 39, 1) lies on line \ell_3
464: P_{138754} = (1, 55, 32, 1) lies on line \ell_8
                                                                     518: P_{164433} = (16, 8, 39, 1) lies on line \ell_{11}
465: P_{139202} = (1, 62, 32, 1) lies on line \ell_9
                                                                     519: P_{164802} = (1, 14, 39, 1) lies on line \ell_8
466: P_{139211} = (10, 62, 32, 1) lies on line \ell_6
                                                                     520: P_{164983} = (54, 16, 39, 1) lies on line \ell_{10}
467: P_{140207} = (46, 13, 33, 1) lies on line \ell_7
                                                                     521: P_{164999} = (6, 17, 39, 1) lies on line \ell_5
468: P_{140354} = (1, 16, 33, 1) lies on line \ell_9
                                                                     522: P_{165890} = (1, 31, 39, 1) lies on line \ell_4
469: P_{140482} = (1, 18, 33, 1) lies on line \ell_8
                                                                     523: P_{167232} = (63, 51, 39, 1) lies on line \ell_6
                                                                     524: P_{167362} = (1, 54, 39, 1) lies on line \ell_9
470: P_{140556} = (11, 19, 33, 1) lies on line \ell_3
471: P_{140570} = (25, 19, 33, 1) lies on line \ell_{10}
                                                                     525: P_{167806} = (61, 60, 39, 1) lies on line \ell_7
472: P_{140934} = (5, 25, 33, 1) lies on line \ell_{11}
                                                                     526: P_{168514} = (1, 8, 40, 1) lies on line \ell_9
473: P_{141570} = (1, 35, 33, 1) lies on line \ell_4
                                                                     527: P_{169153} = (0, 18, 40, 1) lies on line \ell_{11}
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528 : P_{169507} = (34, 23, 40, 1) lies on line \ell_7
                                                                    582: P_{195747} = (34, 49, 46, 1) lies on line \ell_3
529: P_{169538} = (1, 24, 40, 1) lies on line \ell_4
                                                                    583: P_{196674} = (1, 0, 47, 1) lies on line \ell_9
                                                                     584 : P_{196738} = (1, 1, 47, 1) lies on line \ell_8
530: P_{170414} = (45, 37, 40, 1) lies on line \ell_3
531: P_{170543} = (46, 39, 40, 1) lies on line \ell_{10}
                                                                    585: P_{197981} = (28, 20, 47, 1) lies on line \ell_{10}
                                                                    586: P_{198235} = (26, 24, 47, 1) lies on line \ell_5
532: P_{171586} = (1, 56, 40, 1) lies on line \ell_8
                                                                    587: P_{199618} = (1, 46, 47, 1) lies on line \ell_4
533: P_{171809} = (32, 59, 40, 1) lies on line \ell_5
534: P_{171945} = (40, 61, 40, 1) lies on line \ell_6
                                                                    588: P_{199774} = (29, 48, 47, 1) lies on line \ell_6
535: P_{173110} = (53, 15, 41, 1) lies on line \ell_7
                                                                    589: P_{200004} = (3, 52, 47, 1) lies on line \ell_{11}
536: P_{173250} = (1, 18, 41, 1) lies on line \ell_4
                                                                    590: P_{200209} = (16, 55, 47, 1) lies on line \ell_3
537: P_{173620} = (51, 23, 41, 1) lies on line \ell_{10}
                                                                    591: P_{200679} = (38, 62, 47, 1) lies on line \ell_7
538: P_{173954} = (1, 29, 41, 1) lies on line \ell_8
                                                                    592: P_{201872} = (15, 17, 48, 1) lies on line \ell_7
539 : P_{174368} = (31, 35, 41, 1) lies on line \ell_3
                                                                    593: P_{202066} = (17, 20, 48, 1) lies on line \ell_3
540: P_{174487} = (22, 37, 41, 1) lies on line \ell_{11}
                                                                    594: P_{202821} = (4, 32, 48, 1) lies on line \ell_5
541: P_{174530} = (1, 38, 41, 1) lies on line \ell_9
                                                                    595: P_{203394} = (1, 41, 48, 1) lies on line \ell_8
542: P_{174773} = (52, 41, 41, 1) lies on line \ell_6
                                                                    596: P_{203458} = (1, 42, 48, 1) lies on line \ell_4
543: P_{175572} = (19, 54, 41, 1) lies on line \ell_5
                                                                    597: P_{203570} = (49, 43, 48, 1) lies on line \ell_{10}
544: P_{176962} = (1, 12, 42, 1) lies on line \ell_4
                                                                    598: P_{204034} = (1, 51, 48, 1) lies on line \ell_9
545: P_{177410} = (1, 19, 42, 1) lies on line \ell_8
                                                                    599: P_{204342} = (53, 55, 48, 1) lies on line \ell_{11}
546: P_{177553} = (16, 21, 42, 1) lies on line \ell_6
                                                                    600: P_{204400} = (47, 56, 48, 1) lies on line \ell_6
                                                                    601: P_{204900} = (35, 0, 49, 1) lies on line \ell_{11}
547: P_{178093} = (44, 29, 42, 1) lies on line \ell_{11}
548: P_{178344} = (39, 33, 42, 1) lies on line \ell_5
                                                                    602: P_{205465} = (24, 9, 49, 1) lies on line \ell_7
549: P_{178645} = (20, 38, 42, 1) lies on line \ell_{10}
                                                                     603: P_{205634} = (1, 12, 49, 1) lies on line \ell_8
550: P_{178701} = (12, 39, 42, 1) lies on line \ell_7
                                                                     604: P_{206052} = (35, 18, 49, 1) lies on line \ell_3
551 : P_{178857} = (40, 41, 42, 1) lies on line \ell_3
                                                                    605 : P_{206637} = (44, 27, 49, 1) lies on line \ell_{10}
552: P_{179586} = (1, 53, 42, 1) lies on line \ell_9
                                                                    606: P_{206722} = (1, 29, 49, 1) lies on line \ell_9
553: P_{180365} = (12, 1, 43, 1) lies on line \ell_6
                                                                    607: P_{206914} = (1, 32, 49, 1) lies on line \ell_4
554: P_{180674} = (1, 6, 43, 1) lies on line \ell_4
                                                                    608: P_{207732} = (51, 44, 49, 1) lies on line \ell_6
555: P_{181706} = (9, 22, 43, 1) lies on line \ell_{10}
                                                                    609: P_{207800} = (55, 45, 49, 1) lies on line \ell_5
556: P_{182018} = (1, 27, 43, 1) lies on line \ell_9
                                                                    610: P_{209090} = (1, 2, 50, 1) lies on line \ell_8
557: P_{183035} = (58, 42, 43, 1) lies on line \ell_{11}
                                                                    611: P_{209858} = (1, 14, 50, 1) lies on line \ell_9
558: P_{183125} = (20, 44, 43, 1) lies on line \ell_5
                                                                    612: P_{210008} = (23, 16, 50, 1) lies on line \ell_6
559: P_{183323} = (26, 47, 43, 1) lies on line \ell_3
                                                                    613: P_{210517} = (20, 24, 50, 1) lies on line \ell_3
560: P_{183746} = (1, 54, 43, 1) lies on line \ell_8
                                                                     614: P_{211106} = (33, 33, 50, 1) lies on line \ell_7
                                                                    615: P_{211660} = (11, 42, 50, 1) lies on line \ell_{10}
561: P_{184348} = (27, 63, 43, 1) lies on line \ell_7
562: P_{185346} = (1, 15, 44, 1) lies on line \ell_8
                                                                    616: P_{212570} = (25, 56, 50, 1) lies on line \ell_{11}
                                                                    617 : P_{212676} = (3, 58, 50, 1) lies on line \ell_5
563: P_{185391} = (46, 15, 44, 1) lies on line \ell_5
564: P_{185602} = (1, 19, 44, 1) lies on line \ell_9
                                                                     618: P_{212930} = (1, 62, 50, 1) lies on line \ell_4
565: P_{185824} = (31, 22, 44, 1) lies on line \ell_7
                                                                     619: P_{213324} = (11, 4, 51, 1) lies on line \ell_6
566: P_{186812} = (59, 37, 44, 1) lies on line \ell_{10}
                                                                     620: P_{214032} = (15, 15, 51, 1) lies on line \ell_{11}
567: P_{187458} = (1, 48, 44, 1) lies on line \ell_4
                                                                     621: P_{214743} = (22, 26, 51, 1) lies on line \ell_{10}
568 : P_{188328} = (39, 61, 44, 1) lies on line \ell_3
                                                                    622: P_{215015} = (38, 30, 51, 1) lies on line \ell_3
569: P_{188638} = (29, 2, 45, 1) lies on line \ell_5
                                                                    623: P_{215106} = (1, 32, 51, 1) lies on line \ell_9
570 : P_{189385} = (8, 14, 45, 1) lies on line \ell_7
                                                                    624: P_{215554} = (1, 39, 51, 1) lies on line \ell_8
571: P_{189863} = (38, 21, 45, 1) lies on line \ell_{10}
                                                                    625: P_{216386} = (1, 52, 51, 1) lies on line \ell_4
572: P_{190054} = (37, 24, 45, 1) lies on line \ell_6
                                                                     626: P_{216625} = (48, 55, 51, 1) lies on line \ell_5
573: P_{191170} = (1, 42, 45, 1) lies on line \ell_8
                                                                    627: P_{216759} = (54, 57, 51, 1) lies on line \ell_7
574: P_{192194} = (1, 58, 45, 1) lies on line \ell_4
                                                                    628: P_{217282} = (1, 2, 52, 1) lies on line \ell_4
575: P_{192278} = (21, 59, 45, 1) lies on line \ell_3
                                                                     629: P_{217791} = (62, 9, 52, 1) lies on line \ell_6
576: P_{192304} = (47, 59, 45, 1) lies on line \ell_{11}
                                                                    630: P_{217948} = (27, 12, 52, 1) lies on line \ell_3
577: P_{192386} = (1, 61, 45, 1) lies on line \ell_9
                                                                    631: P_{218227} = (50, 16, 52, 1) lies on line \ell_7
578: P_{192790} = (21, 3, 46, 1) lies on line \ell_{11}
                                                                    632 : P_{218443} = (10, 20, 52, 1) lies on line \ell_5
579: P_{193962} = (41, 21, 46, 1) lies on line \ell_5
                                                                    633: P_{219074} = (1, 30, 52, 1) lies on line \ell_8
580: P_{195058} = (49, 38, 46, 1) lies on line \ell_7
                                                                    634: P_{219714} = (1, 40, 52, 1) lies on line \ell_9
581: P_{195522} = (1, 46, 46, 1) lies on line \ell_9
                                                                     635: P_{219789} = (12, 41, 52, 1) lies on line \ell_{11}
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685: P_{244289} = (0, 40, 58, 1) lies on line \ell_3
636: P_{219813} = (36, 41, 52, 1) lies on line \ell_{10}
637: P_{221634} = (1, 6, 53, 1) lies on line \ell_9
                                                                     686: P_{244706} = (33, 46, 58, 1) lies on line \ell_{10}
                                                                     687: P_{245024} = (31, 51, 58, 1) lies on line \ell_5
638: P_{221762} = (1, 8, 53, 1) lies on line \ell_4
639: P_{221798} = (37, 8, 53, 1) lies on line \ell_7
                                                                     688: P_{245314} = (1, 56, 58, 1) lies on line \ell_9
640: P_{221930} = (41, 10, 53, 1) lies on line \ell_3
                                                                     689: P_{246146} = (1, 5, 59, 1) lies on line \ell_4
641: P_{223139} = (34, 29, 53, 1) lies on line \ell_6
                                                                     690 : P_{246314} = (41, 7, 59, 1) lies on line \ell_6
                                                                     691: P_{247234} = (1, 22, 59, 1) lies on line \ell_9
642: P_{223195} = (26, 30, 53, 1) lies on line \ell_{11}
643: P_{225026} = (1, 59, 53, 1) lies on line \ell_8
                                                                     692: P_{247805} = (60, 30, 59, 1) lies on line \ell_{10}
644: P_{225375} = (30, 0, 54, 1) lies on line \ell_3
                                                                     693: P_{248386} = (1, 40, 59, 1) lies on line \ell_8
645: P_{226254} = (13, 14, 54, 1) lies on line \ell_5
                                                                     694: P_{248819} = (50, 46, 59, 1) lies on line \ell_3
646: P_{226690} = (1, 21, 54, 1) lies on line \ell_9
                                                                     695: P_{249117} = (28, 51, 59, 1) lies on line \ell_{11}
647: P_{226754} = (1, 22, 54, 1) lies on line \ell_4
                                                                     696: P_{249646} = (45, 59, 59, 1) lies on line \ell_7
648: P_{227421} = (28, 32, 54, 1) lies on line \ell_7
                                                                     697: P_{249837} = (44, 62, 59, 1) lies on line \ell_5
649: P_{227463} = (6, 33, 54, 1) lies on line \ell_6
                                                                     698: P_{250589} = (28, 10, 60, 1) lies on line \ell_6
650: P_{227809} = (32, 38, 54, 1) lies on line \ell_{11}
                                                                     699: P_{251010} = (1, 17, 60, 1) lies on line \ell_8
651: P_{227935} = (30, 40, 54, 1) lies on line \ell_{10}
                                                                     700: P_{251114} = (41, 18, 60, 1) lies on line \ell_7
                                                                     701 : P_{251296} = (31, 21, 60, 1) lies on line \ell_{11}
652: P_{228738} = (1, 53, 54, 1) lies on line \ell_8
653: P_{229695} = (62, 3, 55, 1) lies on line \ell_5
                                                                     702: P_{251799} = (22, 29, 60, 1) lies on line \ell_5
654: P_{229869} = (44, 6, 55, 1) lies on line \ell_3
                                                                     703: P_{251842} = (1, 30, 60, 1) lies on line \ell_9
655: P_{230466} = (1, 16, 55, 1) lies on line \ell_8
                                                                     704: P_{252815} = (14, 45, 60, 1) lies on line \ell_{10}
656: P_{230583} = (54, 17, 55, 1) lies on line \ell_{11}
                                                                     705: P_{253186} = (1, 51, 60, 1) lies on line \ell_4
657: P_{230980} = (3, 24, 55, 1) lies on line \ell_{10}
                                                                     706 : P_{253776} = (15, 60, 60, 1) lies on line \ell_3
658: P_{231234} = (1, 28, 55, 1) lies on line \ell_4
                                                                     707: P_{254719} = (62, 10, 61, 1) lies on line \ell_7
                                                                     708 : P_{255078} = (37, 16, 61, 1) lies on line \ell_5
659: P_{232859} = (26, 53, 55, 1) lies on line \ell_6
660: P_{233036} = (11, 56, 55, 1) lies on line \ell_7
                                                                     709: P_{255892} = (19, 29, 61, 1) lies on line \ell_{10}
661: P_{233218} = (1, 59, 55, 1) lies on line \ell_9
                                                                     710: P_{255937} = (0, 30, 61, 1) lies on line \ell_6
662: P_{233858} = (1, 5, 56, 1) lies on line \ell_9
                                                                     711: P_{256202} = (9, 34, 61, 1) lies on line \ell_{11}
663: P_{234279} = (38, 11, 56, 1) lies on line \ell_{11}
                                                                     712: P_{257090} = (1, 48, 61, 1) lies on line \ell_9
664: P_{234773} = (20, 19, 56, 1) lies on line \ell_7
                                                                     713: P_{257346} = (1, 52, 61, 1) lies on line \ell_8
665: P_{235266} = (1, 27, 56, 1) lies on line \ell_4
                                                                     714: P_{257666} = (1, 57, 61, 1) lies on line \ell_4
666: P_{235846} = (5, 36, 56, 1) lies on line \ell_3
                                                                     715: P_{257790} = (61, 58, 61, 1) lies on line \ell_3
667: P_{235970} = (1, 38, 56, 1) lies on line \ell_8
                                                                     716: P_{258578} = (17, 7, 62, 1) lies on line \ell_5
668: P_{236185} = (24, 41, 56, 1) lies on line \ell_5
                                                                     717: P_{259828} = (51, 26, 62, 1) lies on line \ell_{11}
669 : P_{236572} = (27, 47, 56, 1) lies on line \ell_{10}
                                                                     718: P_{260296} = (7, 34, 62, 1) lies on line \ell_7
670: P_{237326} = (13, 59, 56, 1) lies on line \ell_6
                                                                     719: P_{260325} = (36, 34, 62, 1) lies on line \ell_6
671 : P_{237826} = (1, 3, 57, 1) lies on line \ell_8
                                                                     720: P_{260354} = (1, 35, 62, 1) lies on line \ell_9
672: P_{238340} = (3, 11, 57, 1) lies on line \ell_7
                                                                     721: P_{260610} = (1, 39, 62, 1) lies on line \ell_4
673: P_{238722} = (1, 17, 57, 1) lies on line \ell_4
                                                                     722: P_{260981} = (52, 44, 62, 1) lies on line \ell_{10}
                                                                     723 : P_{261195} = (10, 48, 62, 1) lies on line \ell_3
674: P_{239623} = (6, 31, 57, 1) lies on line \ell_{10}
                                                                     724: P_{261826} = (1, 58, 62, 1) lies on line \ell_8
675: P_{239864} = (55, 34, 57, 1) lies on line \ell_3
676: P_{239980} = (43, 36, 57, 1) lies on line \ell_5
                                                                     725: P_{262883} = (34, 10, 63, 1) lies on line \ell_5
677: P_{240386} = (1, 43, 57, 1) lies on line \ell_9
                                                                     726: P_{263042} = (1, 13, 63, 1) lies on line \ell_9
678: P_{240658} = (17, 47, 57, 1) lies on line \ell_6
                                                                     727: P_{264042} = (41, 28, 63, 1) lies on line \ell_{10}
679: P_{241521} = (48, 60, 57, 1) lies on line \ell_{11}
                                                                     728: P_{264194} = (1, 31, 63, 1) lies on line \ell_8
680: P_{241995} = (10, 4, 58, 1) lies on line \ell_{11}
                                                                     729: P_{265090} = (1, 45, 63, 1) lies on line \ell_4
681 : P_{242562} = (1, 13, 58, 1) lies on line \ell_8
                                                                     730: P_{265126} = (37, 45, 63, 1) lies on line \ell_{11}
682: P_{242690} = (1, 15, 58, 1) lies on line \ell_4
                                                                     731: P_{265937} = (16, 58, 63, 1) lies on line \ell_7
683: P_{242998} = (53, 19, 58, 1) lies on line \ell_6
684: P_{244027} = (58, 35, 58, 1) lies on line \ell_7
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The single points on the surface are:

### Points on surface but on no line

The surface has 3600 points not on any line: Too many to print.

# Line Intersection Graph

	0123456789	10	11
0	0110100100	0	1
1	1011010010	0	0
2	1100001001	1	0
3	0100111101	0	0
4	1001011011	1	0
5	0101100001	1	1
6	0011100010	1	1
7	1001000011	1	1
8	0100101101	1	1
9	0011110110	0	1
10	0010111110	0	0
11	1000011111	0	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_7$	$\ell_{11}$
in point	$P_{3111}$	$P_{2382}$	$P_{707}$	$P_{1626}$	$P_{3609}$

Line 1 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_8$
in point	$P_{3111}$	$P_{818}$	$P_{501}$	$P_{950}$	$P_{2435}$

Line 2 intersects

Line	$\ell_0$	$\ell_1$	$\ell_6$	$\ell_9$	$\ell_{10}$
in point	$P_{2382}$	$P_{818}$	$P_{1375}$	$P_{3011}$	$P_{3168}$

Line 3 intersects

Line	$\ell_1$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_9$
in point	$P_{501}$	$P_{156418}$	$P_{156418}$	$P_{265721}$	$P_{136634}$	$P_{156418}$

Line 4 intersects

Line	$\ell_0$	$\ell_3$	$\ell_5$	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$
in point	$P_{707}$	$P_{156418}$	$P_{156418}$	$P_{194882}$	$P_{194882}$	$P_{156418}$	$P_{194882}$

Line 5 intersects

Line	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_9$	$\ell_{10}$	$\ell_{11}$
in point	$P_{950}$	$P_{156418}$	$P_{156418}$	$P_{156418}$	$P_{222906}$	$P_{64697}$

Line 6 intersects

Line	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_8$	$\ell_{10}$	$\ell_{11}$
in point	$P_{1375}$	$P_{265721}$	$P_{194882}$	$P_{194882}$	$P_{194882}$	$P_{185210}$

Line 7 intersects

Line	$\ell_0$	$\ell_3$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$
in point	$P_{1626}$	$P_{136634}$	$P_{48130}$	$P_{48130}$	$P_{41529}$	$P_{48130}$

Line 8 intersects

Line	$\ell_1$	$\ell_4$	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{11}$
in point	$P_{2435}$	$P_{194882}$	$P_{194882}$	$P_{48130}$	$P_{48130}$	$P_{194882}$	$P_{48130}$

# Line 9 intersects

Line	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_7$	$\ell_8$	$\ell_{11}$
in point	$P_{3011}$	$P_{156418}$	$P_{156418}$	$P_{156418}$	$P_{48130}$	$P_{48130}$	$P_{48130}$

# Line 10 intersects

Line	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$
in point	$P_{3168}$	$P_{194882}$	$P_{222906}$	$P_{194882}$	$P_{41529}$	$P_{194882}$

# ${\bf Line~11~intersects}$

Line	$\ell_0$	$\ell_5$	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$
in point	$P_{3609}$	$P_{64697}$	$P_{185210}$	$P_{48130}$	$P_{48130}$	$P_{48130}$

The surface has 4353 points: Too many to print.