

Rank-69 over GF(8)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^3 + X_1^3 + X_2^3 + X_0^2 X_1 + X_0^2 X_2 = 0$$

(1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0)
The point rank of the equation over GF(8) is 8865

General information

| | |
|----------------------------|---------------|
| Number of lines | 13 |
| Number of points | 105 |
| Number of singular points | 1 |
| Number of Eckardt points | 0 |
| Number of double points | 0 |
| Number of single points | 104 |
| Number of points off lines | 0 |
| Number of Hesse planes | 0 |
| Number of axes | 0 |
| Type of points on lines | 9^{13} |
| Type of lines on points | $13, 1^{104}$ |

Singular Points

The surface has 1 singular points:

$$0 : P_3 = \mathbf{P}(0, 0, 0, 1) = \mathbf{P}(0, 0, 0, 1)$$

The 13 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & \gamma^6 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{510} = \begin{bmatrix} 1 & 6 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{510} = \mathbf{Pl}(0, 0, 0, 6, 1, 0)_{276}$$

$$\begin{aligned}
\ell_1 &= \begin{bmatrix} 1 & \gamma^5 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{291} = \begin{bmatrix} 1 & 3 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{291} = \mathbf{Pl}(0, 0, 0, 3, 1, 0)_{231} \\
\ell_2 &= \begin{bmatrix} 1 & \gamma^3 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{437} = \begin{bmatrix} 1 & 5 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{437} = \mathbf{Pl}(0, 0, 0, 5, 1, 0)_{261} \\
\ell_3 &= \begin{bmatrix} 1 & 0 & \gamma^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3576} = \begin{bmatrix} 1 & 0 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3576} = \mathbf{Pl}(0, 6, 0, 0, 1, 0)_{94} \\
\ell_4 &= \begin{bmatrix} 1 & 0 & \gamma^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1824} = \begin{bmatrix} 1 & 0 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1824} = \mathbf{Pl}(0, 3, 0, 0, 1, 0)_{91} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & \gamma^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2992} = \begin{bmatrix} 1 & 0 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{2992} = \mathbf{Pl}(0, 5, 0, 0, 1, 0)_{93} \\
\ell_6 &= \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4689} = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4689} = \mathbf{Pl}(0, 1, 0, 1, 0, 0)_{25} \\
\ell_7 &= \begin{bmatrix} 1 & 1 & \gamma^6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3649} = \begin{bmatrix} 1 & 1 & 6 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3649} = \mathbf{Pl}(0, 6, 0, 1, 1, 0)_{214} \\
\ell_8 &= \begin{bmatrix} 1 & \gamma^5 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{875} = \begin{bmatrix} 1 & 3 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{875} = \mathbf{Pl}(0, 1, 0, 3, 1, 0)_{239} \\
\ell_9 &= \begin{bmatrix} 1 & 1 & \gamma^5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1897} = \begin{bmatrix} 1 & 1 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1897} = \mathbf{Pl}(0, 3, 0, 1, 1, 0)_{211} \\
\ell_{10} &= \begin{bmatrix} 1 & \gamma^3 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1021} = \begin{bmatrix} 1 & 5 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1021} = \mathbf{Pl}(0, 1, 0, 5, 1, 0)_{269} \\
\ell_{11} &= \begin{bmatrix} 1 & \gamma^6 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1094} = \begin{bmatrix} 1 & 6 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{1094} = \mathbf{Pl}(0, 1, 0, 6, 1, 0)_{284} \\
\ell_{12} &= \begin{bmatrix} 1 & 1 & \gamma^3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3065} = \begin{bmatrix} 1 & 1 & 5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{3065} = \mathbf{Pl}(0, 5, 0, 1, 1, 0)_{213}
\end{aligned}$$

Rank of lines: (510, 291, 437, 3576, 1824, 2992, 4689, 3649, 875, 1897, 1021, 1094, 3065)

Rank of points on Klein quadric: (276, 231, 261, 94, 91, 93, 25, 214, 239, 211, 269, 284, 213)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 0 Double points:

The double points on the surface are:

Single Points

The surface has 104 single points:

The single points on the surface are:

0 : $P_6 = (2, 1, 0, 0)$ lies on line ℓ_0
 1 : $P_8 = (4, 1, 0, 0)$ lies on line ℓ_1
 2 : $P_{11} = (7, 1, 0, 0)$ lies on line ℓ_2
 3 : $P_{13} = (2, 0, 1, 0)$ lies on line ℓ_3
 4 : $P_{15} = (4, 0, 1, 0)$ lies on line ℓ_4
 5 : $P_{18} = (7, 0, 1, 0)$ lies on line ℓ_5
 6 : $P_{19} = (0, 1, 1, 0)$ lies on line ℓ_6
 7 : $P_{29} = (2, 2, 1, 0)$ lies on line ℓ_7
 8 : $P_{36} = (1, 3, 1, 0)$ lies on line ℓ_8
 9 : $P_{47} = (4, 4, 1, 0)$ lies on line ℓ_9
 10 : $P_{52} = (1, 5, 1, 0)$ lies on line ℓ_{10}
 11 : $P_{60} = (1, 6, 1, 0)$ lies on line ℓ_{11}
 12 : $P_{74} = (7, 7, 1, 0)$ lies on line ℓ_{12}
 13 : $P_{84} = (2, 1, 0, 1)$ lies on line ℓ_0
 14 : $P_{86} = (4, 1, 0, 1)$ lies on line ℓ_1
 15 : $P_{89} = (7, 1, 0, 1)$ lies on line ℓ_2
 16 : $P_{93} = (3, 2, 0, 1)$ lies on line ℓ_2
 17 : $P_{94} = (4, 2, 0, 1)$ lies on line ℓ_0
 18 : $P_{95} = (5, 2, 0, 1)$ lies on line ℓ_1
 19 : $P_{99} = (1, 3, 0, 1)$ lies on line ℓ_1
 20 : $P_{102} = (4, 3, 0, 1)$ lies on line ℓ_2
 21 : $P_{104} = (6, 3, 0, 1)$ lies on line ℓ_0
 22 : $P_{111} = (5, 4, 0, 1)$ lies on line ℓ_0
 23 : $P_{112} = (6, 4, 0, 1)$ lies on line ℓ_2
 24 : $P_{113} = (7, 4, 0, 1)$ lies on line ℓ_1
 25 : $P_{115} = (1, 5, 0, 1)$ lies on line ℓ_2
 26 : $P_{117} = (3, 5, 0, 1)$ lies on line ℓ_1
 27 : $P_{121} = (7, 5, 0, 1)$ lies on line ℓ_0
 28 : $P_{123} = (1, 6, 0, 1)$ lies on line ℓ_0
 29 : $P_{124} = (2, 6, 0, 1)$ lies on line ℓ_1
 30 : $P_{127} = (5, 6, 0, 1)$ lies on line ℓ_2
 31 : $P_{132} = (2, 7, 0, 1)$ lies on line ℓ_2
 32 : $P_{133} = (3, 7, 0, 1)$ lies on line ℓ_0
 33 : $P_{136} = (6, 7, 0, 1)$ lies on line ℓ_1
 34 : $P_{140} = (2, 0, 1, 1)$ lies on line ℓ_3
 35 : $P_{142} = (4, 0, 1, 1)$ lies on line ℓ_4
 36 : $P_{145} = (7, 0, 1, 1)$ lies on line ℓ_5
 37 : $P_{146} = (0, 1, 1, 1)$ lies on line ℓ_6
 38 : $P_{155} = (2, 2, 1, 1)$ lies on line ℓ_7
 39 : $P_{162} = (1, 3, 1, 1)$ lies on line ℓ_8
 40 : $P_{173} = (4, 4, 1, 1)$ lies on line ℓ_9
 41 : $P_{178} = (1, 5, 1, 1)$ lies on line ℓ_{10}
 42 : $P_{186} = (1, 6, 1, 1)$ lies on line ℓ_{11}
 43 : $P_{200} = (7, 7, 1, 1)$ lies on line ℓ_{12}
 44 : $P_{204} = (3, 0, 2, 1)$ lies on line ℓ_5
 45 : $P_{205} = (4, 0, 2, 1)$ lies on line ℓ_3
 46 : $P_{206} = (5, 0, 2, 1)$ lies on line ℓ_4
 47 : $P_{211} = (2, 1, 2, 1)$ lies on line ℓ_{11}
 48 : $P_{217} = (0, 2, 2, 1)$ lies on line ℓ_6
 49 : $P_{228} = (3, 3, 2, 1)$ lies on line ℓ_{12}
 50 : $P_{237} = (4, 4, 2, 1)$ lies on line ℓ_7
 51 : $P_{246} = (5, 5, 2, 1)$ lies on line ℓ_9
 52 : $P_{251} = (2, 6, 2, 1)$ lies on line ℓ_8

53 : $P_{259} = (2, 7, 2, 1)$ lies on line ℓ_{10}
 54 : $P_{266} = (1, 0, 3, 1)$ lies on line ℓ_4
 55 : $P_{269} = (4, 0, 3, 1)$ lies on line ℓ_5
 56 : $P_{271} = (6, 0, 3, 1)$ lies on line ℓ_3
 57 : $P_{274} = (1, 1, 3, 1)$ lies on line ℓ_9
 58 : $P_{284} = (3, 2, 3, 1)$ lies on line ℓ_{10}
 59 : $P_{289} = (0, 3, 3, 1)$ lies on line ℓ_6
 60 : $P_{301} = (4, 4, 3, 1)$ lies on line ℓ_{12}
 61 : $P_{308} = (3, 5, 3, 1)$ lies on line ℓ_8
 62 : $P_{319} = (6, 6, 3, 1)$ lies on line ℓ_7
 63 : $P_{324} = (3, 7, 3, 1)$ lies on line ℓ_{11}
 64 : $P_{334} = (5, 0, 4, 1)$ lies on line ℓ_3
 65 : $P_{335} = (6, 0, 4, 1)$ lies on line ℓ_5
 66 : $P_{336} = (7, 0, 4, 1)$ lies on line ℓ_4
 67 : $P_{341} = (4, 1, 4, 1)$ lies on line ℓ_8
 68 : $P_{349} = (4, 2, 4, 1)$ lies on line ℓ_{11}
 69 : $P_{357} = (4, 3, 4, 1)$ lies on line ℓ_{10}
 70 : $P_{361} = (0, 4, 4, 1)$ lies on line ℓ_6
 71 : $P_{374} = (5, 5, 4, 1)$ lies on line ℓ_7
 72 : $P_{383} = (6, 6, 4, 1)$ lies on line ℓ_{12}
 73 : $P_{392} = (7, 7, 4, 1)$ lies on line ℓ_9
 74 : $P_{394} = (1, 0, 5, 1)$ lies on line ℓ_5
 75 : $P_{396} = (3, 0, 5, 1)$ lies on line ℓ_4
 76 : $P_{400} = (7, 0, 5, 1)$ lies on line ℓ_3
 77 : $P_{402} = (1, 1, 5, 1)$ lies on line ℓ_{12}
 78 : $P_{414} = (5, 2, 5, 1)$ lies on line ℓ_8
 79 : $P_{420} = (3, 3, 5, 1)$ lies on line ℓ_9
 80 : $P_{430} = (5, 4, 5, 1)$ lies on line ℓ_{11}
 81 : $P_{433} = (0, 5, 5, 1)$ lies on line ℓ_6
 82 : $P_{446} = (5, 6, 5, 1)$ lies on line ℓ_{10}
 83 : $P_{456} = (7, 7, 5, 1)$ lies on line ℓ_7
 84 : $P_{458} = (1, 0, 6, 1)$ lies on line ℓ_3
 85 : $P_{459} = (2, 0, 6, 1)$ lies on line ℓ_4
 86 : $P_{462} = (5, 0, 6, 1)$ lies on line ℓ_5
 87 : $P_{466} = (1, 1, 6, 1)$ lies on line ℓ_7
 88 : $P_{475} = (2, 2, 6, 1)$ lies on line ℓ_9
 89 : $P_{487} = (6, 3, 6, 1)$ lies on line ℓ_{11}
 90 : $P_{495} = (6, 4, 6, 1)$ lies on line ℓ_{10}
 91 : $P_{502} = (5, 5, 6, 1)$ lies on line ℓ_{12}
 92 : $P_{505} = (0, 6, 6, 1)$ lies on line ℓ_6
 93 : $P_{519} = (6, 7, 6, 1)$ lies on line ℓ_8
 94 : $P_{523} = (2, 0, 7, 1)$ lies on line ℓ_5
 95 : $P_{524} = (3, 0, 7, 1)$ lies on line ℓ_3
 96 : $P_{527} = (6, 0, 7, 1)$ lies on line ℓ_4
 97 : $P_{536} = (7, 1, 7, 1)$ lies on line ℓ_{10}
 98 : $P_{539} = (2, 2, 7, 1)$ lies on line ℓ_{12}
 99 : $P_{548} = (3, 3, 7, 1)$ lies on line ℓ_7
 100 : $P_{560} = (7, 4, 7, 1)$ lies on line ℓ_8
 101 : $P_{568} = (7, 5, 7, 1)$ lies on line ℓ_{11}
 102 : $P_{575} = (6, 6, 7, 1)$ lies on line ℓ_9
 103 : $P_{577} = (0, 7, 7, 1)$ lies on line ℓ_6

The single points on the surface are:

Points on surface but on no line

The surface has 0 points not on any line:

The points on the surface but not on lines are:

Line Intersection Graph

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|----|---|---|---|---|---|---|---|---|---|---|----|----|----|
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 2 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 3 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 4 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 5 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 6 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 7 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 8 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 |
| 9 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 |
| 10 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 |
| 11 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 |
| 12 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |

Neighbor sets in the line intersection graph:

Line 0 intersects

| Line | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 1 intersects

| Line | ℓ_0 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 2 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 3 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 4 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 5 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 6 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 7 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 8 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 9 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 10 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{11} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 11 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{12} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

Line 12 intersects

| Line | ℓ_0 | ℓ_1 | ℓ_2 | ℓ_3 | ℓ_4 | ℓ_5 | ℓ_6 | ℓ_7 | ℓ_8 | ℓ_9 | ℓ_{10} | ℓ_{11} |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------------|-------------|
| in point | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 | P_3 |

The surface has 105 points:

The points on the surface are:

| | | |
|------------------------------|-------------------------------|-------------------------------|
| 0 : $P_3 = (0, 0, 0, 1)$ | 18 : $P_{94} = (4, 2, 0, 1)$ | 36 : $P_{142} = (4, 0, 1, 1)$ |
| 1 : $P_6 = (2, 1, 0, 0)$ | 19 : $P_{95} = (5, 2, 0, 1)$ | 37 : $P_{145} = (7, 0, 1, 1)$ |
| 2 : $P_8 = (4, 1, 0, 0)$ | 20 : $P_{99} = (1, 3, 0, 1)$ | 38 : $P_{146} = (0, 1, 1, 1)$ |
| 3 : $P_{11} = (7, 1, 0, 0)$ | 21 : $P_{102} = (4, 3, 0, 1)$ | 39 : $P_{155} = (2, 2, 1, 1)$ |
| 4 : $P_{13} = (2, 0, 1, 0)$ | 22 : $P_{104} = (6, 3, 0, 1)$ | 40 : $P_{162} = (1, 3, 1, 1)$ |
| 5 : $P_{15} = (4, 0, 1, 0)$ | 23 : $P_{111} = (5, 4, 0, 1)$ | 41 : $P_{173} = (4, 4, 1, 1)$ |
| 6 : $P_{18} = (7, 0, 1, 0)$ | 24 : $P_{112} = (6, 4, 0, 1)$ | 42 : $P_{178} = (1, 5, 1, 1)$ |
| 7 : $P_{19} = (0, 1, 1, 0)$ | 25 : $P_{113} = (7, 4, 0, 1)$ | 43 : $P_{186} = (1, 6, 1, 1)$ |
| 8 : $P_{29} = (2, 2, 1, 0)$ | 26 : $P_{115} = (1, 5, 0, 1)$ | 44 : $P_{200} = (7, 7, 1, 1)$ |
| 9 : $P_{36} = (1, 3, 1, 0)$ | 27 : $P_{117} = (3, 5, 0, 1)$ | 45 : $P_{204} = (3, 0, 2, 1)$ |
| 10 : $P_{47} = (4, 4, 1, 0)$ | 28 : $P_{121} = (7, 5, 0, 1)$ | 46 : $P_{205} = (4, 0, 2, 1)$ |
| 11 : $P_{52} = (1, 5, 1, 0)$ | 29 : $P_{123} = (1, 6, 0, 1)$ | 47 : $P_{206} = (5, 0, 2, 1)$ |
| 12 : $P_{60} = (1, 6, 1, 0)$ | 30 : $P_{124} = (2, 6, 0, 1)$ | 48 : $P_{211} = (2, 1, 2, 1)$ |
| 13 : $P_{74} = (7, 7, 1, 0)$ | 31 : $P_{127} = (5, 6, 0, 1)$ | 49 : $P_{217} = (0, 2, 2, 1)$ |
| 14 : $P_{84} = (2, 1, 0, 1)$ | 32 : $P_{132} = (2, 7, 0, 1)$ | 50 : $P_{228} = (3, 3, 2, 1)$ |
| 15 : $P_{86} = (4, 1, 0, 1)$ | 33 : $P_{133} = (3, 7, 0, 1)$ | 51 : $P_{237} = (4, 4, 2, 1)$ |
| 16 : $P_{89} = (7, 1, 0, 1)$ | 34 : $P_{136} = (6, 7, 0, 1)$ | 52 : $P_{246} = (5, 5, 2, 1)$ |
| 17 : $P_{93} = (3, 2, 0, 1)$ | 35 : $P_{140} = (2, 0, 1, 1)$ | 53 : $P_{251} = (2, 6, 2, 1)$ |

54 : $P_{259} = (2, 7, 2, 1)$
 55 : $P_{266} = (1, 0, 3, 1)$
 56 : $P_{269} = (4, 0, 3, 1)$
 57 : $P_{271} = (6, 0, 3, 1)$
 58 : $P_{274} = (1, 1, 3, 1)$
 59 : $P_{284} = (3, 2, 3, 1)$
 60 : $P_{289} = (0, 3, 3, 1)$
 61 : $P_{301} = (4, 4, 3, 1)$
 62 : $P_{308} = (3, 5, 3, 1)$
 63 : $P_{319} = (6, 6, 3, 1)$
 64 : $P_{324} = (3, 7, 3, 1)$
 65 : $P_{334} = (5, 0, 4, 1)$
 66 : $P_{335} = (6, 0, 4, 1)$
 67 : $P_{336} = (7, 0, 4, 1)$
 68 : $P_{341} = (4, 1, 4, 1)$
 69 : $P_{349} = (4, 2, 4, 1)$
 70 : $P_{357} = (4, 3, 4, 1)$
 71 : $P_{361} = (0, 4, 4, 1)$

72 : $P_{374} = (5, 5, 4, 1)$
 73 : $P_{383} = (6, 6, 4, 1)$
 74 : $P_{392} = (7, 7, 4, 1)$
 75 : $P_{394} = (1, 0, 5, 1)$
 76 : $P_{396} = (3, 0, 5, 1)$
 77 : $P_{400} = (7, 0, 5, 1)$
 78 : $P_{402} = (1, 1, 5, 1)$
 79 : $P_{414} = (5, 2, 5, 1)$
 80 : $P_{420} = (3, 3, 5, 1)$
 81 : $P_{430} = (5, 4, 5, 1)$
 82 : $P_{433} = (0, 5, 5, 1)$
 83 : $P_{446} = (5, 6, 5, 1)$
 84 : $P_{456} = (7, 7, 5, 1)$
 85 : $P_{458} = (1, 0, 6, 1)$
 86 : $P_{459} = (2, 0, 6, 1)$
 87 : $P_{462} = (5, 0, 6, 1)$
 88 : $P_{466} = (1, 1, 6, 1)$
 89 : $P_{475} = (2, 2, 6, 1)$

90 : $P_{487} = (6, 3, 6, 1)$
 91 : $P_{495} = (6, 4, 6, 1)$
 92 : $P_{502} = (5, 5, 6, 1)$
 93 : $P_{505} = (0, 6, 6, 1)$
 94 : $P_{519} = (6, 7, 6, 1)$
 95 : $P_{523} = (2, 0, 7, 1)$
 96 : $P_{524} = (3, 0, 7, 1)$
 97 : $P_{527} = (6, 0, 7, 1)$
 98 : $P_{536} = (7, 1, 7, 1)$
 99 : $P_{539} = (2, 2, 7, 1)$
 100 : $P_{548} = (3, 3, 7, 1)$
 101 : $P_{560} = (7, 4, 7, 1)$
 102 : $P_{568} = (7, 5, 7, 1)$
 103 : $P_{575} = (6, 6, 7, 1)$
 104 : $P_{577} = (0, 7, 7, 1)$