

# Rank-76355 over GF(16)

January 15, 2021

## The equation

The equation of the surface is :

$$X_0^2 X_3 + X_1^2 X_3 + X_1 X_2^2 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

( 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0 )

The point rank of the equation over GF(16) is 303108373

## General information

Number of lines	27
Number of points	369
Number of singular points	0
Number of Eckardt points	5
Number of double points	120
Number of single points	204
Number of points off lines	40
Number of Hesse planes	0
Number of axes	0
Type of points on lines	$17^{27}$
Type of lines on points	$3^5, 2^{120}, 1^{204}, 0^{40}$

## Singular Points

The surface has 0 singular points:

## The 27 Lines

The lines and their Pluecker coordinates are:

$$\begin{aligned}\ell_0 = a_1 &= \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]_{256} = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]_{256} = \mathbf{Pl}(0, 0, 1, 0, 0, 0)_2 \\ \ell_1 = a_2 &= \left[ \begin{array}{cccc} 1 & \delta^{14} & 0 & 0 \\ 0 & 0 & 1 & \delta^7 \end{array} \right]_{3539} = \left[ \begin{array}{cccc} 1 & 12 & 0 & 0 \\ 0 & 0 & 1 & 7 \end{array} \right]_{3539} = \mathbf{Pl}(0, 0, 14, 7, 14, 1)_{62869}\end{aligned}$$

$$\begin{aligned}
\ell_2 = a_3 &= \begin{bmatrix} 1 & \delta^{13} & 0 & 0 \\ 0 & 0 & 1 & \delta^{14} \end{bmatrix}_{1906} = \begin{bmatrix} 1 & 6 & 0 & 0 \\ 0 & 0 & 1 & 12 \end{bmatrix}_{1906} = \mathbf{Pl}(0, 0, 2, 12, 2, 1)_{13537} \\
\ell_3 = a_4 &= \begin{bmatrix} 1 & 0 & \delta^4 & 1 \\ 0 & 1 & \delta^{11} & \delta^7 \end{bmatrix}_{6950} = \begin{bmatrix} 1 & 0 & 9 & 1 \\ 0 & 1 & 13 & 7 \end{bmatrix}_{6950} = \mathbf{Pl}(14, 0, 9, 13, 8, 1)_{38248} \\
\ell_4 = a_5 &= \begin{bmatrix} 1 & \delta^{11} & 0 & 0 \\ 0 & 0 & 1 & \delta^{13} \end{bmatrix}_{3811} = \begin{bmatrix} 1 & 13 & 0 & 0 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{3811} = \mathbf{Pl}(0, 0, 4, 6, 4, 1)_{21759} \\
\ell_5 = a_6 &= \begin{bmatrix} 1 & \delta^7 & 0 & \delta^{11} \\ 0 & 0 & 1 & \delta^{11} \end{bmatrix}_{58964} = \begin{bmatrix} 1 & 7 & 0 & 13 \\ 0 & 0 & 1 & 13 \end{bmatrix}_{58964} = \mathbf{Pl}(0, 9, 9, 13, 9, 1)_{42338} \\
\ell_6 = b_1 &= \begin{bmatrix} 1 & 0 & \delta^3 & 1 \\ 0 & 1 & \delta^{11} & \delta^7 \end{bmatrix}_{6677} = \begin{bmatrix} 1 & 0 & 8 & 1 \\ 0 & 1 & 13 & 7 \end{bmatrix}_{6677} = \mathbf{Pl}(13, 9, 8, 3, 9, 1)_{44013} \\
\ell_7 = b_2 &= \begin{bmatrix} 1 & 0 & \delta^7 & 0 \\ 0 & 1 & \delta^{10} & \delta^5 \end{bmatrix}_{2097} = \begin{bmatrix} 1 & 0 & 7 & 0 \\ 0 & 1 & 10 & 11 \end{bmatrix}_{2097} = \mathbf{Pl}(10, 11, 11, 0, 6, 1)_{29535} \\
\ell_8 = b_3 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{3020} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{3020} = \mathbf{Pl}(1, 1, 1, 0, 10, 1)_{45696} \\
\ell_9 = b_4 &= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70160} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{70160} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_1 \\
\ell_{10} = b_5 &= \begin{bmatrix} 1 & 0 & \delta^{11} & 0 \\ 0 & 1 & \delta^5 & \delta^{10} \end{bmatrix}_{3720} = \begin{bmatrix} 1 & 0 & 13 & 0 \\ 0 & 1 & 11 & 10 \end{bmatrix}_{3720} = \mathbf{Pl}(11, 10, 10, 0, 12, 1)_{54001} \\
\ell_{11} = b_6 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0 \\
\ell_{12} = c_{12} &= \begin{bmatrix} 1 & 0 & \delta^{13} & 0 \\ 0 & 1 & \delta^{10} & \delta^5 \end{bmatrix}_{1824} = \begin{bmatrix} 1 & 0 & 6 & 0 \\ 0 & 1 & 10 & 11 \end{bmatrix}_{1824} = \mathbf{Pl}(10, 11, 11, 0, 7, 1)_{33615} \\
\ell_{13} = c_{13} &= \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{2747} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{2747} = \mathbf{Pl}(1, 1, 1, 0, 11, 1)_{49776} \\
\ell_{14} = c_{14} &= \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4624} = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{4624} = \mathbf{Pl}(0, 1, 1, 0, 0, 0)_{18} \\
\ell_{15} = c_{15} &= \begin{bmatrix} 1 & 0 & \delta^{14} & 0 \\ 0 & 1 & \delta^5 & \delta^{10} \end{bmatrix}_{3447} = \begin{bmatrix} 1 & 0 & 12 & 0 \\ 0 & 1 & 11 & 10 \end{bmatrix}_{3447} = \mathbf{Pl}(11, 10, 10, 0, 13, 1)_{58081} \\
\ell_{16} = c_{16} &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{273} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_{273} = \mathbf{Pl}(1, 0, 0, 0, 0, 1)_{4626} \\
\ell_{17} = c_{23} &= \begin{bmatrix} 1 & 0 & \delta^9 & 1 \\ 0 & 1 & \delta^{13} & \delta^{11} \end{bmatrix}_{5947} = \begin{bmatrix} 1 & 0 & 5 & 1 \\ 0 & 1 & 6 & 13 \end{bmatrix}_{5947} = \mathbf{Pl}(6, 4, 5, 15, 4, 1)_{23156} \\
\ell_{18} = c_{24} &= \begin{bmatrix} 1 & \delta^{14} & 0 & \delta^7 \\ 0 & 0 & 1 & \delta^7 \end{bmatrix}_{34115} = \begin{bmatrix} 1 & 12 & 0 & 7 \\ 0 & 0 & 1 & 7 \end{bmatrix}_{34115} = \mathbf{Pl}(0, 14, 14, 7, 14, 1)_{62898} \\
\ell_{19} = c_{25} &= \begin{bmatrix} 1 & 0 & \delta^{12} & 1 \\ 0 & 1 & \delta^{14} & \delta^{13} \end{bmatrix}_{5295} = \begin{bmatrix} 1 & 0 & 3 & 1 \\ 0 & 1 & 12 & 6 \end{bmatrix}_{5295} = \mathbf{Pl}(12, 2, 3, 8, 2, 1)_{14507} \\
\ell_{20} = c_{26} &= \begin{bmatrix} 1 & 0 & \delta^8 & 1 \\ 0 & 1 & \delta^7 & \delta^{14} \end{bmatrix}_{8389} = \begin{bmatrix} 1 & 0 & 14 & 1 \\ 0 & 1 & 7 & 12 \end{bmatrix}_{8389} = \mathbf{Pl}(2, 0, 14, 7, 15, 1)_{66951} \\
\ell_{21} = c_{34} &= \begin{bmatrix} 1 & \delta^{13} & 0 & \delta^{14} \\ 0 & 0 & 1 & \delta^{14} \end{bmatrix}_{54322} = \begin{bmatrix} 1 & 6 & 0 & 12 \\ 0 & 0 & 1 & 12 \end{bmatrix}_{54322} = \mathbf{Pl}(0, 2, 2, 12, 2, 1)_{13554} \\
\ell_{22} = c_{35} &= \begin{bmatrix} 1 & 0 & \delta^6 & 1 \\ 0 & 1 & \delta^7 & \delta^{14} \end{bmatrix}_{8662} = \begin{bmatrix} 1 & 0 & 15 & 1 \\ 0 & 1 & 7 & 12 \end{bmatrix}_{8662} = \mathbf{Pl}(7, 14, 15, 5, 14, 1)_{65907}
\end{aligned}$$

$$\begin{aligned}
\ell_{23} = c_{36} &= \begin{bmatrix} 1 & 0 & \delta & 1 \\ 0 & 1 & \delta^{14} & \delta^{13} \end{bmatrix}_{5022} = \begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 12 & 6 \end{bmatrix}_{5022} = \mathbf{PI}(4, 0, 2, 12, 3, 1)_{17621} \\
\ell_{24} = c_{45} &= \begin{bmatrix} 1 & \delta^{11} & 0 & \delta^{13} \\ 0 & 0 & 1 & \delta^{13} \end{bmatrix}_{30019} = \begin{bmatrix} 1 & 13 & 0 & 6 \\ 0 & 0 & 1 & 6 \end{bmatrix}_{30019} = \mathbf{PI}(0, 4, 4, 6, 4, 1)_{21778} \\
\ell_{25} = c_{46} &= \begin{bmatrix} 1 & \delta^7 & 0 & 0 \\ 0 & 0 & 1 & \delta^{11} \end{bmatrix}_{2180} = \begin{bmatrix} 1 & 7 & 0 & 0 \\ 0 & 0 & 1 & 13 \end{bmatrix}_{2180} = \mathbf{PI}(0, 0, 9, 13, 9, 1)_{42314} \\
\ell_{26} = c_{56} &= \begin{bmatrix} 1 & 0 & \delta^2 & 1 \\ 0 & 1 & \delta^{13} & \delta^{11} \end{bmatrix}_{5674} = \begin{bmatrix} 1 & 0 & 4 & 1 \\ 0 & 1 & 6 & 13 \end{bmatrix}_{5674} = \mathbf{PI}(9, 0, 4, 6, 5, 1)_{25848}
\end{aligned}$$

Rank of lines: ( 256, 3539, 1906, 6950, 3811, 58964, 6677, 2097, 3020, 70160, 3720, 0, 1824, 2747, 4624, 3447, 273, 5947, 34115, 5295, 8389, 54322, 8662, 5022, 30019, 2180, 5674 )

Rank of points on Klein quadric: ( 2, 62869, 13537, 38248, 21759, 42338, 44013, 29535, 45696, 1, 54001, 0, 33615, 49776, 18, 58081, 4626, 23156, 62898, 14507, 66951, 13554, 65907, 17621, 21778, 42314, 25848 )

### Eckardt Points

The surface has 5 Eckardt points:

$$\begin{aligned}
0 : E_{14} &= a_1 \cap b_4 \cap c_{14} = P_2 = \mathbf{P}(0, 0, 1, 0) = \mathbf{P}(0, 0, 1, 0), \\
1 : E_{34} &= a_3 \cap b_4 \cap c_{34} = P_{785} = \mathbf{P}(0, 0, \delta, 1) = \mathbf{P}(0, 0, 2, 1), \\
2 : E_{54} &= a_5 \cap b_4 \cap c_{45} = P_{1297} = \mathbf{P}(0, 0, \delta^2, 1) = \mathbf{P}(0, 0, 4, 1), \\
3 : E_{64} &= a_6 \cap b_4 \cap c_{46} = P_{2577} = \mathbf{P}(0, 0, \delta^4, 1) = \mathbf{P}(0, 0, 9, 1), \\
4 : E_{24} &= a_2 \cap b_4 \cap c_{24} = P_{3857} = \mathbf{P}(0, 0, \delta^8, 1) = \mathbf{P}(0, 0, 14, 1).
\end{aligned}$$

### Double Points

The surface has 120 Double points:

The double points on the surface are:

$$\begin{aligned}
P_{33} &= (14, 0, 1, 0) = \ell_0 \cap \ell_7 = a_1 \cap b_2 & P_{845} &= (12, 3, 2, 1) = \ell_2 \cap \ell_{22} = a_3 \cap c_{35} \\
P_{29} &= (10, 0, 1, 0) = \ell_0 \cap \ell_8 = a_1 \cap b_3 & P_{979} &= (2, 12, 2, 1) = \ell_2 \cap \ell_{23} = a_3 \cap c_{36} \\
P_{28} &= (9, 0, 1, 0) = \ell_0 \cap \ell_{10} = a_1 \cap b_5 & P_{2801} &= (0, 14, 9, 1) = \ell_3 \cap \ell_6 = a_4 \cap b_1 \\
P_0 &= (1, 0, 0, 0) = \ell_0 \cap \ell_{11} = a_1 \cap b_6 & P_{2742} &= (5, 10, 9, 1) = \ell_3 \cap \ell_7 = a_4 \cap b_2 \\
P_{23} &= (4, 0, 1, 0) = \ell_0 \cap \ell_{12} = a_1 \cap c_{12} & P_{2599} &= (6, 1, 9, 1) = \ell_3 \cap \ell_8 = a_4 \cap b_3 \\
P_{30} &= (11, 0, 1, 0) = \ell_0 \cap \ell_{13} = a_1 \cap c_{13} & P_{2755} &= (2, 11, 9, 1) = \ell_3 \cap \ell_{10} = a_4 \cap b_5 \\
P_{21} &= (2, 0, 1, 0) = \ell_0 \cap \ell_{15} = a_1 \cap c_{15} & P_{11} &= (7, 1, 0, 0) = \ell_3 \cap \ell_{11} = a_4 \cap b_6 \\
P_{20} &= (1, 0, 1, 0) = \ell_0 \cap \ell_{16} = a_1 \cap c_{16} & P_{2578} &= (1, 0, 9, 1) = \ell_3 \cap \ell_{14} = a_4 \cap c_{14} \\
P_{4104} &= (7, 15, 14, 1) = \ell_1 \cap \ell_6 = a_2 \cap b_1 & P_{2824} &= (7, 15, 9, 1) = \ell_3 \cap \ell_{18} = a_4 \cap c_{24} \\
P_{3875} &= (2, 1, 14, 1) = \ell_1 \cap \ell_8 = a_2 \cap b_3 & P_{2716} &= (11, 8, 9, 1) = \ell_3 \cap \ell_{21} = a_4 \cap c_{34} \\
P_{4048} &= (15, 11, 14, 1) = \ell_1 \cap \ell_{10} = a_2 \cap b_5 & P_{2702} &= (13, 7, 9, 1) = \ell_3 \cap \ell_{24} = a_4 \cap c_{45} \\
P_6 &= (2, 1, 0, 0) = \ell_1 \cap \ell_{11} = a_2 \cap b_6 & P_{2794} &= (9, 13, 9, 1) = \ell_3 \cap \ell_{25} = a_4 \cap c_{46} \\
P_{4030} &= (13, 10, 14, 1) = \ell_1 \cap \ell_{12} = a_2 \cap c_{12} & P_{1422} &= (13, 7, 4, 1) = \ell_4 \cap \ell_6 = a_5 \cap b_1 \\
P_{3947} &= (10, 5, 14, 1) = \ell_1 \cap \ell_{17} = a_2 \cap c_{23} & P_{1469} &= (12, 10, 4, 1) = \ell_4 \cap \ell_7 = a_5 \cap b_2 \\
P_{3965} &= (12, 6, 14, 1) = \ell_1 \cap \ell_{19} = a_2 \cap c_{25} & P_{1322} &= (9, 1, 4, 1) = \ell_4 \cap \ell_8 = a_5 \cap b_3 \\
P_{3983} &= (14, 7, 14, 1) = \ell_1 \cap \ell_{20} = a_2 \cap c_{26} & P_{13} &= (9, 1, 0, 0) = \ell_4 \cap \ell_{11} = a_5 \cap b_6 \\
P_{924} &= (11, 8, 2, 1) = \ell_2 \cap \ell_6 = a_3 \cap b_1 & P_{1478} &= (5, 11, 4, 1) = \ell_4 \cap \ell_{15} = a_5 \cap c_{15} \\
P_{948} &= (3, 10, 2, 1) = \ell_2 \cap \ell_7 = a_3 \cap b_2 & P_{1383} &= (6, 5, 4, 1) = \ell_4 \cap \ell_{19} = a_5 \cap c_{25} \\
P_{968} &= (7, 11, 2, 1) = \ell_2 \cap \ell_{10} = a_3 \cap b_5 & P_{1547} &= (10, 15, 4, 1) = \ell_4 \cap \ell_{22} = a_5 \cap c_{35} \\
P_8 &= (4, 1, 0, 0) = \ell_2 \cap \ell_{11} = a_3 \cap b_6 & P_{1397} &= (4, 6, 4, 1) = \ell_4 \cap \ell_{26} = a_5 \cap c_{56} \\
P_{805} &= (4, 1, 2, 1) = \ell_2 \cap \ell_{13} = a_3 \cap c_{13} & P_{491} &= (9, 13, 0, 1) = \ell_5 \cap \ell_6 = a_6 \cap b_1 \\
P_{999} &= (6, 13, 2, 1) = \ell_2 \cap \ell_{17} = a_3 \cap c_{23} & P_{697} &= (8, 10, 1, 1) = \ell_5 \cap \ell_7 = a_6 \cap b_2
\end{aligned}$$

$$\begin{aligned}
P_{2095} &= (14, 1, 7, 1) = \ell_5 \cap \ell_8 = a_6 \cap b_3 \\
P_{4295} &= (6, 11, 15, 1) = \ell_5 \cap \ell_{10} = a_6 \cap b_5 \\
P_{132} &= (1, 7, 1, 0) = \ell_5 \cap \ell_{16} = a_6 \cap c_{16} \\
P_{4056} &= (7, 12, 14, 1) = \ell_5 \cap \ell_{20} = a_6 \cap c_{26} \\
P_{844} &= (11, 3, 2, 1) = \ell_5 \cap \ell_{23} = a_6 \cap c_{36} \\
P_{1438} &= (13, 8, 4, 1) = \ell_5 \cap \ell_{26} = a_6 \cap c_{56} \\
P_{3510} &= (5, 10, 12, 1) = \ell_6 \cap \ell_{12} = b_1 \cap c_{12} \\
P_{4135} &= (6, 1, 15, 1) = \ell_6 \cap \ell_{13} = b_1 \cap c_{13} \\
P_{2322} &= (1, 0, 8, 1) = \ell_6 \cap \ell_{14} = b_1 \cap c_{14} \\
P_{3267} &= (2, 11, 11, 1) = \ell_6 \cap \ell_{15} = b_1 \cap c_{15} \\
P_{244} &= (1, 14, 1, 0) = \ell_6 \cap \ell_{16} = b_1 \cap c_{16} \\
P_{3249} &= (0, 10, 11, 1) = \ell_7 \cap \ell_{12} = b_2 \cap c_{12} \\
P_{3007} &= (14, 10, 10, 1) = \ell_7 \cap \ell_{17} = b_2 \cap c_{23} \\
P_{1214} &= (13, 10, 3, 1) = \ell_7 \cap \ell_{18} = b_2 \cap c_{24} \\
P_{3776} &= (15, 10, 13, 1) = \ell_7 \cap \ell_{19} = b_2 \cap c_{25} \\
P_{4021} &= (4, 10, 14, 1) = \ell_7 \cap \ell_{20} = b_2 \cap c_{26} \\
P_{546} &= (0, 1, 1, 1) = \ell_8 \cap \ell_{13} = b_3 \cap c_{13} \\
P_{2349} &= (12, 1, 8, 1) = \ell_8 \cap \ell_{17} = b_3 \cap c_{23} \\
P_{1829} &= (4, 1, 6, 1) = \ell_8 \cap \ell_{21} = b_3 \cap c_{34} \\
P_{1070} &= (13, 1, 3, 1) = \ell_8 \cap \ell_{22} = b_3 \cap c_{35} \\
P_{808} &= (7, 1, 2, 1) = \ell_8 \cap \ell_{23} = b_3 \cap c_{36} \\
P_{3009} &= (0, 11, 10, 1) = \ell_{10} \cap \ell_{15} = b_5 \cap c_{15} \\
P_{3274} &= (9, 11, 11, 1) = \ell_{10} \cap \ell_{19} = b_5 \cap c_{25} \\
P_{1993} &= (8, 11, 6, 1) = \ell_{10} \cap \ell_{22} = b_5 \cap c_{35} \\
P_{710} &= (5, 11, 1, 1) = \ell_{10} \cap \ell_{24} = b_5 \cap c_{45} \\
P_{1476} &= (3, 11, 4, 1) = \ell_{10} \cap \ell_{26} = b_5 \cap c_{56} \\
P_1 &= (0, 1, 0, 0) = \ell_{11} \cap \ell_{16} = b_6 \cap c_{16} \\
P_{16} &= (12, 1, 0, 0) = \ell_{11} \cap \ell_{20} = b_6 \cap c_{26} \\
P_{10} &= (6, 1, 0, 0) = \ell_{11} \cap \ell_{23} = b_6 \cap c_{36} \\
P_{18} &= (14, 1, 0, 0) = \ell_{11} \cap \ell_{25} = b_6 \cap c_{46} \\
P_{17} &= (13, 1, 0, 0) = \ell_{11} \cap \ell_{26} = b_6 \cap c_{56} \\
P_{692} &= (3, 10, 1, 1) = \ell_{12} \cap \ell_{21} = c_{12} \cap c_{34} \\
P_{2997} &= (4, 10, 10, 1) = \ell_{12} \cap \ell_{22} = c_{12} \cap c_{35} \\
P_{960} &= (15, 10, 2, 1) = \ell_{12} \cap \ell_{23} = c_{12} \cap c_{36} \\
P_{2493} &= (12, 10, 8, 1) = \ell_{12} \cap \ell_{24} = c_{12} \cap c_{45} \\
P_{2745} &= (8, 10, 9, 1) = \ell_{12} \cap \ell_{25} = c_{12} \cap c_{46} \\
P_{1471} &= (14, 10, 4, 1) = \ell_{12} \cap \ell_{26} = c_{12} \cap c_{56} \\
P_{3363} &= (2, 1, 12, 1) = \ell_{13} \cap \ell_{18} = c_{13} \cap c_{24} \\
P_{1576} &= (7, 1, 5, 1) = \ell_{13} \cap \ell_{19} = c_{13} \cap c_{25}
\end{aligned}$$

$$\begin{aligned}
P_{3886} &= (13, 1, 14, 1) = \ell_{13} \cap \ell_{20} = c_{13} \cap c_{26} \\
P_{3626} &= (9, 1, 13, 1) = \ell_{13} \cap \ell_{24} = c_{13} \cap c_{45} \\
P_{2607} &= (14, 1, 9, 1) = \ell_{13} \cap \ell_{25} = c_{13} \cap c_{46} \\
P_{1325} &= (12, 1, 4, 1) = \ell_{13} \cap \ell_{26} = c_{13} \cap c_{56} \\
P_{1554} &= (1, 0, 5, 1) = \ell_{14} \cap \ell_{17} = c_{14} \cap c_{23} \\
P_{1042} &= (1, 0, 3, 1) = \ell_{14} \cap \ell_{19} = c_{14} \cap c_{25} \\
P_{3858} &= (1, 0, 14, 1) = \ell_{14} \cap \ell_{20} = c_{14} \cap c_{26} \\
P_{4114} &= (1, 0, 15, 1) = \ell_{14} \cap \ell_{22} = c_{14} \cap c_{35} \\
P_{786} &= (1, 0, 2, 1) = \ell_{14} \cap \ell_{23} = c_{14} \cap c_{36} \\
P_{1298} &= (1, 0, 4, 1) = \ell_{14} \cap \ell_{26} = c_{14} \cap c_{56} \\
P_{2244} &= (3, 11, 7, 1) = \ell_{15} \cap \ell_{17} = c_{15} \cap c_{23} \\
P_{720} &= (15, 11, 1, 1) = \ell_{15} \cap \ell_{18} = c_{15} \cap c_{24} \\
P_{4041} &= (8, 11, 14, 1) = \ell_{15} \cap \ell_{20} = c_{15} \cap c_{26} \\
P_{1736} &= (7, 11, 5, 1) = \ell_{15} \cap \ell_{21} = c_{15} \cap c_{34} \\
P_{970} &= (9, 11, 2, 1) = \ell_{15} \cap \ell_{23} = c_{15} \cap c_{36} \\
P_{2759} &= (6, 11, 9, 1) = \ell_{15} \cap \ell_{25} = c_{15} \cap c_{46} \\
P_{164} &= (1, 9, 1, 0) = \ell_{16} \cap \ell_{17} = c_{16} \cap c_{23} \\
P_{212} &= (1, 12, 1, 0) = \ell_{16} \cap \ell_{18} = c_{16} \cap c_{24} \\
P_{84} &= (1, 4, 1, 0) = \ell_{16} \cap \ell_{19} = c_{16} \cap c_{25} \\
P_{116} &= (1, 6, 1, 0) = \ell_{16} \cap \ell_{21} = c_{16} \cap c_{34} \\
P_{52} &= (1, 2, 1, 0) = \ell_{16} \cap \ell_{22} = c_{16} \cap c_{35} \\
P_{228} &= (1, 13, 1, 0) = \ell_{16} \cap \ell_{24} = c_{16} \cap c_{45} \\
P_{374} &= (4, 6, 0, 1) = \ell_{17} \cap \ell_{24} = c_{23} \cap c_{45} \\
P_{2718} &= (13, 8, 9, 1) = \ell_{17} \cap \ell_{25} = c_{23} \cap c_{46} \\
P_{1441} &= (0, 9, 4, 1) = \ell_{17} \cap \ell_{26} = c_{23} \cap c_{56} \\
P_{400} &= (14, 7, 0, 1) = \ell_{18} \cap \ell_{22} = c_{24} \cap c_{35} \\
P_{893} &= (12, 6, 2, 1) = \ell_{18} \cap \ell_{23} = c_{24} \cap c_{36} \\
P_{1387} &= (10, 5, 4, 1) = \ell_{18} \cap \ell_{26} = c_{24} \cap c_{56} \\
P_{468} &= (2, 12, 0, 1) = \ell_{19} \cap \ell_{21} = c_{25} \cap c_{34} \\
P_{849} &= (0, 4, 2, 1) = \ell_{19} \cap \ell_{23} = c_{25} \cap c_{36} \\
P_{2636} &= (11, 3, 9, 1) = \ell_{19} \cap \ell_{25} = c_{25} \cap c_{46} \\
P_{3917} &= (12, 3, 14, 1) = \ell_{20} \cap \ell_{21} = c_{26} \cap c_{34} \\
P_{3889} &= (0, 2, 14, 1) = \ell_{20} \cap \ell_{22} = c_{26} \cap c_{35} \\
P_{4107} &= (10, 15, 14, 1) = \ell_{20} \cap \ell_{24} = c_{26} \cap c_{45} \\
P_{1511} &= (6, 13, 4, 1) = \ell_{21} \cap \ell_{26} = c_{34} \cap c_{56} \\
P_{2776} &= (7, 12, 9, 1) = \ell_{22} \cap \ell_{25} = c_{35} \cap c_{46} \\
P_{871} &= (6, 5, 2, 1) = \ell_{23} \cap \ell_{24} = c_{36} \cap c_{45}
\end{aligned}$$

## Single Points

The surface has 204 single points:  
The single points on the surface are:

$$\begin{aligned}
0 : P_3 &= (0, 0, 0, 1) \text{ lies on line } b_4 \\
1 : P_5 &= (1, 1, 0, 0) \text{ lies on line } b_6 \\
2 : P_7 &= (3, 1, 0, 0) \text{ lies on line } b_6 \\
3 : P_9 &= (5, 1, 0, 0) \text{ lies on line } b_6 \\
4 : P_{12} &= (8, 1, 0, 0) \text{ lies on line } b_6 \\
5 : P_{14} &= (10, 1, 0, 0) \text{ lies on line } b_6 \\
6 : P_{15} &= (11, 1, 0, 0) \text{ lies on line } b_6 \\
7 : P_{19} &= (15, 1, 0, 0) \text{ lies on line } b_6
\end{aligned}$$

$$\begin{aligned}
8 : P_{22} &= (3, 0, 1, 0) \text{ lies on line } a_1 \\
9 : P_{24} &= (5, 0, 1, 0) \text{ lies on line } a_1 \\
10 : P_{25} &= (6, 0, 1, 0) \text{ lies on line } a_1 \\
11 : P_{26} &= (7, 0, 1, 0) \text{ lies on line } a_1 \\
12 : P_{27} &= (8, 0, 1, 0) \text{ lies on line } a_1 \\
13 : P_{31} &= (12, 0, 1, 0) \text{ lies on line } a_1 \\
14 : P_{32} &= (13, 0, 1, 0) \text{ lies on line } a_1 \\
15 : P_{34} &= (15, 0, 1, 0) \text{ lies on line } a_1
\end{aligned}$$

16 :  $P_{36} = (1, 1, 1, 0)$  lies on line  $c_{16}$   
 17 :  $P_{68} = (1, 3, 1, 0)$  lies on line  $c_{16}$   
 18 :  $P_{100} = (1, 5, 1, 0)$  lies on line  $c_{16}$   
 19 :  $P_{148} = (1, 8, 1, 0)$  lies on line  $c_{16}$   
 20 :  $P_{180} = (1, 10, 1, 0)$  lies on line  $c_{16}$   
 21 :  $P_{196} = (1, 11, 1, 0)$  lies on line  $c_{16}$   
 22 :  $P_{260} = (1, 15, 1, 0)$  lies on line  $c_{16}$   
 23 :  $P_{275} = (1, 0, 0, 1)$  lies on line  $c_{14}$   
 24 :  $P_{300} = (10, 1, 0, 1)$  lies on line  $b_3$   
 25 :  $P_{301} = (11, 1, 0, 1)$  lies on line  $c_{13}$   
 26 :  $P_{440} = (6, 10, 0, 1)$  lies on line  $b_2$   
 27 :  $P_{441} = (7, 10, 0, 1)$  lies on line  $c_{12}$   
 28 :  $P_{462} = (12, 11, 0, 1)$  lies on line  $b_5$   
 29 :  $P_{463} = (13, 11, 0, 1)$  lies on line  $c_{15}$   
 30 :  $P_{530} = (0, 0, 1, 1)$  lies on line  $b_4$   
 31 :  $P_{531} = (1, 0, 1, 1)$  lies on line  $c_{14}$   
 32 :  $P_{585} = (8, 3, 1, 1)$  lies on line  $b_1$   
 33 :  $P_{624} = (15, 5, 1, 1)$  lies on line  $c_{35}$   
 34 :  $P_{660} = (3, 8, 1, 1)$  lies on line  $c_{25}$   
 35 :  $P_{774} = (5, 15, 1, 1)$  lies on line  $c_{23}$   
 36 :  $P_{825} = (8, 2, 2, 1)$  lies on line  $a_3$   
 37 :  $P_{830} = (13, 2, 2, 1)$  lies on line  $c_{36}$   
 38 :  $P_{858} = (9, 4, 2, 1)$  lies on line  $a_3$   
 39 :  $P_{878} = (13, 5, 2, 1)$  lies on line  $a_3$   
 40 :  $P_{882} = (1, 6, 2, 1)$  lies on line  $a_3$   
 41 :  $P_{902} = (5, 7, 2, 1)$  lies on line  $a_3$   
 42 :  $P_{907} = (10, 7, 2, 1)$  lies on line  $c_{36}$   
 43 :  $P_{916} = (3, 8, 2, 1)$  lies on line  $c_{36}$   
 44 :  $P_{934} = (5, 9, 2, 1)$  lies on line  $c_{36}$   
 45 :  $P_{944} = (15, 9, 2, 1)$  lies on line  $a_3$   
 46 :  $P_{997} = (4, 13, 2, 1)$  lies on line  $c_{36}$   
 47 :  $P_{1019} = (10, 14, 2, 1)$  lies on line  $a_3$   
 48 :  $P_{1023} = (14, 14, 2, 1)$  lies on line  $c_{36}$   
 49 :  $P_{1033} = (8, 15, 2, 1)$  lies on line  $c_{36}$   
 50 :  $P_{1039} = (14, 15, 2, 1)$  lies on line  $a_3$   
 51 :  $P_{1041} = (0, 0, 3, 1)$  lies on line  $b_4$   
 52 :  $P_{1072} = (15, 1, 3, 1)$  lies on line  $c_{13}$   
 53 :  $P_{1112} = (7, 4, 3, 1)$  lies on line  $c_{23}$   
 54 :  $P_{1115} = (10, 4, 3, 1)$  lies on line  $a_6$   
 55 :  $P_{1138} = (1, 6, 3, 1)$  lies on line  $c_{34}$   
 56 :  $P_{1147} = (10, 6, 3, 1)$  lies on line  $b_1$   
 57 :  $P_{1176} = (7, 8, 3, 1)$  lies on line  $c_{45}$   
 58 :  $P_{1212} = (11, 10, 3, 1)$  lies on line  $c_{12}$   
 59 :  $P_{1228} = (11, 11, 3, 1)$  lies on line  $c_{15}$   
 60 :  $P_{1231} = (14, 11, 3, 1)$  lies on line  $b_5$   
 61 :  $P_{1331} = (2, 2, 4, 1)$  lies on line  $c_{56}$   
 62 :  $P_{1340} = (11, 2, 4, 1)$  lies on line  $a_5$   
 63 :  $P_{1347} = (2, 3, 4, 1)$  lies on line  $a_5$   
 64 :  $P_{1360} = (15, 3, 4, 1)$  lies on line  $c_{56}$   
 65 :  $P_{1368} = (7, 4, 4, 1)$  lies on line  $c_{56}$   
 66 :  $P_{1376} = (15, 4, 4, 1)$  lies on line  $a_5$   
 67 :  $P_{1418} = (9, 7, 4, 1)$  lies on line  $c_{56}$   
 68 :  $P_{1432} = (7, 8, 4, 1)$  lies on line  $a_5$   
 69 :  $P_{1455} = (14, 9, 4, 1)$  lies on line  $a_5$

70 :  $P_{1497} = (8, 12, 4, 1)$  lies on line  $a_5$   
 71 :  $P_{1500} = (11, 12, 4, 1)$  lies on line  $c_{56}$   
 72 :  $P_{1506} = (1, 13, 4, 1)$  lies on line  $a_5$   
 73 :  $P_{1524} = (3, 14, 4, 1)$  lies on line  $a_5$   
 74 :  $P_{1529} = (8, 14, 4, 1)$  lies on line  $c_{56}$   
 75 :  $P_{1542} = (5, 15, 4, 1)$  lies on line  $c_{56}$   
 76 :  $P_{1553} = (0, 0, 5, 1)$  lies on line  $b_4$   
 77 :  $P_{1572} = (3, 1, 5, 1)$  lies on line  $b_3$   
 78 :  $P_{1708} = (11, 9, 5, 1)$  lies on line  $c_{24}$   
 79 :  $P_{1709} = (12, 9, 5, 1)$  lies on line  $b_1$   
 80 :  $P_{1715} = (2, 10, 5, 1)$  lies on line  $b_2$   
 81 :  $P_{1723} = (10, 10, 5, 1)$  lies on line  $c_{12}$   
 82 :  $P_{1739} = (10, 11, 5, 1)$  lies on line  $b_5$   
 83 :  $P_{1762} = (1, 13, 5, 1)$  lies on line  $c_{45}$   
 84 :  $P_{1772} = (11, 13, 5, 1)$  lies on line  $c_{35}$   
 85 :  $P_{1805} = (12, 15, 5, 1)$  lies on line  $a_6$   
 86 :  $P_{1809} = (0, 0, 6, 1)$  lies on line  $b_4$   
 87 :  $P_{1810} = (1, 0, 6, 1)$  lies on line  $c_{14}$   
 88 :  $P_{1828} = (3, 1, 6, 1)$  lies on line  $c_{13}$   
 89 :  $P_{1843} = (2, 2, 6, 1)$  lies on line  $c_{23}$   
 90 :  $P_{1856} = (15, 2, 6, 1)$  lies on line  $b_1$   
 91 :  $P_{1859} = (2, 3, 6, 1)$  lies on line  $c_{45}$   
 92 :  $P_{1881} = (8, 4, 6, 1)$  lies on line  $c_{24}$   
 93 :  $P_{1920} = (15, 6, 6, 1)$  lies on line  $a_6$   
 94 :  $P_{1975} = (6, 10, 6, 1)$  lies on line  $c_{12}$   
 95 :  $P_{1978} = (9, 10, 6, 1)$  lies on line  $b_2$   
 96 :  $P_{1986} = (1, 11, 6, 1)$  lies on line  $c_{15}$   
 97 :  $P_{2021} = (4, 13, 6, 1)$  lies on line  $c_{25}$   
 98 :  $P_{2065} = (0, 0, 7, 1)$  lies on line  $b_4$   
 99 :  $P_{2066} = (1, 0, 7, 1)$  lies on line  $c_{14}$   
 100 :  $P_{2089} = (8, 1, 7, 1)$  lies on line  $c_{13}$   
 101 :  $P_{2182} = (5, 7, 7, 1)$  lies on line  $c_{34}$   
 102 :  $P_{2202} = (9, 8, 7, 1)$  lies on line  $c_{24}$   
 103 :  $P_{2214} = (5, 9, 7, 1)$  lies on line  $c_{25}$   
 104 :  $P_{2218} = (9, 9, 7, 1)$  lies on line  $c_{35}$   
 105 :  $P_{2227} = (2, 10, 7, 1)$  lies on line  $c_{12}$   
 106 :  $P_{2232} = (7, 10, 7, 1)$  lies on line  $b_2$   
 107 :  $P_{2242} = (1, 11, 7, 1)$  lies on line  $b_5$   
 108 :  $P_{2271} = (14, 12, 7, 1)$  lies on line  $b_1$   
 109 :  $P_{2292} = (3, 14, 7, 1)$  lies on line  $c_{45}$   
 110 :  $P_{2321} = (0, 0, 8, 1)$  lies on line  $b_4$   
 111 :  $P_{2342} = (5, 1, 8, 1)$  lies on line  $c_{13}$   
 112 :  $P_{2375} = (6, 3, 8, 1)$  lies on line  $c_{24}$   
 113 :  $P_{2434} = (1, 7, 8, 1)$  lies on line  $a_6$   
 114 :  $P_{2443} = (10, 7, 8, 1)$  lies on line  $c_{25}$   
 115 :  $P_{2492} = (11, 10, 8, 1)$  lies on line  $b_2$   
 116 :  $P_{2501} = (4, 11, 8, 1)$  lies on line  $c_{15}$   
 117 :  $P_{2508} = (11, 11, 8, 1)$  lies on line  $b_5$   
 118 :  $P_{2551} = (6, 14, 8, 1)$  lies on line  $c_{35}$   
 119 :  $P_{2555} = (10, 14, 8, 1)$  lies on line  $c_{34}$   
 120 :  $P_{2614} = (5, 2, 9, 1)$  lies on line  $c_{46}$   
 121 :  $P_{2624} = (15, 2, 9, 1)$  lies on line  $a_4$   
 122 :  $P_{2633} = (8, 3, 9, 1)$  lies on line  $a_4$   
 123 :  $P_{2645} = (4, 4, 9, 1)$  lies on line  $a_4$

- 124 :  $P_{2651} = (10, 4, 9, 1)$  lies on line  $c_{46}$   
 125 :  $P_{2660} = (3, 5, 9, 1)$  lies on line  $a_4$   
 126 :  $P_{2661} = (4, 5, 9, 1)$  lies on line  $c_{46}$   
 127 :  $P_{2683} = (10, 6, 9, 1)$  lies on line  $a_4$   
 128 :  $P_{2688} = (15, 6, 9, 1)$  lies on line  $c_{46}$   
 129 :  $P_{2690} = (1, 7, 9, 1)$  lies on line  $c_{46}$   
 130 :  $P_{2724} = (3, 9, 9, 1)$  lies on line  $c_{46}$   
 131 :  $P_{2733} = (12, 9, 9, 1)$  lies on line  $a_4$   
 132 :  $P_{2783} = (14, 12, 9, 1)$  lies on line  $a_4$   
 133 :  $P_{2803} = (2, 14, 9, 1)$  lies on line  $c_{46}$   
 134 :  $P_{2829} = (12, 15, 9, 1)$  lies on line  $c_{46}$   
 135 :  $P_{2833} = (0, 0, 10, 1)$  lies on line  $b_4$   
 136 :  $P_{2834} = (1, 0, 10, 1)$  lies on line  $c_{14}$   
 137 :  $P_{2850} = (1, 1, 10, 1)$  lies on line  $b_3$   
 138 :  $P_{2859} = (10, 1, 10, 1)$  lies on line  $c_{13}$   
 139 :  $P_{2869} = (4, 2, 10, 1)$  lies on line  $c_{24}$   
 140 :  $P_{2873} = (8, 2, 10, 1)$  lies on line  $c_{34}$   
 141 :  $P_{2916} = (3, 5, 10, 1)$  lies on line  $b_1$   
 142 :  $P_{2980} = (3, 9, 10, 1)$  lies on line  $a_6$   
 143 :  $P_{2991} = (14, 9, 10, 1)$  lies on line  $c_{45}$   
 144 :  $P_{3081} = (8, 15, 10, 1)$  lies on line  $c_{25}$   
 145 :  $P_{3089} = (0, 0, 11, 1)$  lies on line  $b_4$   
 146 :  $P_{3090} = (1, 0, 11, 1)$  lies on line  $c_{14}$   
 147 :  $P_{3106} = (1, 1, 11, 1)$  lies on line  $c_{13}$   
 148 :  $P_{3116} = (11, 1, 11, 1)$  lies on line  $b_3$   
 149 :  $P_{3152} = (15, 3, 11, 1)$  lies on line  $c_{23}$   
 150 :  $P_{3162} = (9, 4, 11, 1)$  lies on line  $c_{34}$   
 151 :  $P_{3168} = (15, 4, 11, 1)$  lies on line  $c_{45}$   
 152 :  $P_{3222} = (5, 8, 11, 1)$  lies on line  $c_{35}$   
 153 :  $P_{3315} = (2, 14, 11, 1)$  lies on line  $a_6$   
 154 :  $P_{3318} = (5, 14, 11, 1)$  lies on line  $c_{24}$   
 155 :  $P_{3345} = (0, 0, 12, 1)$  lies on line  $b_4$   
 156 :  $P_{3346} = (1, 0, 12, 1)$  lies on line  $c_{14}$   
 157 :  $P_{3376} = (15, 1, 12, 1)$  lies on line  $b_3$   
 158 :  $P_{3382} = (5, 2, 12, 1)$  lies on line  $a_6$   
 159 :  $P_{3443} = (2, 6, 12, 1)$  lies on line  $c_{35}$   
 160 :  $P_{3506} = (1, 10, 12, 1)$  lies on line  $b_2$   
 161 :  $P_{3525} = (4, 11, 12, 1)$  lies on line  $b_5$   
 162 :  $P_{3533} = (12, 11, 12, 1)$  lies on line  $c_{15}$   
 163 :  $P_{3545} = (8, 12, 12, 1)$  lies on line  $c_{45}$   
 164 :  $P_{3577} = (8, 14, 12, 1)$  lies on line  $c_{23}$   
 165 :  $P_{3583} = (14, 14, 12, 1)$  lies on line  $c_{25}$   
 166 :  $P_{3599} = (14, 15, 12, 1)$  lies on line  $c_{34}$   
 167 :  $P_{3601} = (0, 0, 13, 1)$  lies on line  $b_4$   
 168 :  $P_{3602} = (1, 0, 13, 1)$  lies on line  $c_{14}$   
 169 :  $P_{3622} = (5, 1, 13, 1)$  lies on line  $b_3$   
 170 :  $P_{3668} = (3, 4, 13, 1)$  lies on line  $c_{35}$   
 171 :  $P_{3669} = (4, 4, 13, 1)$  lies on line  $b_1$   
 172 :  $P_{3685} = (4, 5, 13, 1)$  lies on line  $a_6$   
 173 :  $P_{3722} = (9, 7, 13, 1)$  lies on line  $c_{23}$   
 174 :  $P_{3760} = (15, 9, 13, 1)$  lies on line  $c_{34}$   
 175 :  $P_{3762} = (1, 10, 13, 1)$  lies on line  $c_{12}$   
 176 :  $P_{3790} = (13, 11, 13, 1)$  lies on line  $b_5$   
 177 :  $P_{3791} = (14, 11, 13, 1)$  lies on line  $c_{15}$   
 178 :  $P_{3812} = (3, 13, 13, 1)$  lies on line  $c_{24}$   
 179 :  $P_{3893} = (4, 2, 14, 1)$  lies on line  $a_2$   
 180 :  $P_{3911} = (6, 3, 14, 1)$  lies on line  $a_2$   
 181 :  $P_{3924} = (3, 4, 14, 1)$  lies on line  $c_{26}$   
 182 :  $P_{3929} = (8, 4, 14, 1)$  lies on line  $a_2$   
 183 :  $P_{3952} = (15, 5, 14, 1)$  lies on line  $c_{26}$   
 184 :  $P_{3955} = (2, 6, 14, 1)$  lies on line  $c_{26}$   
 185 :  $P_{3990} = (5, 8, 14, 1)$  lies on line  $c_{26}$   
 186 :  $P_{3994} = (9, 8, 14, 1)$  lies on line  $a_2$   
 187 :  $P_{4010} = (9, 9, 14, 1)$  lies on line  $c_{26}$   
 188 :  $P_{4012} = (11, 9, 14, 1)$  lies on line  $a_2$   
 189 :  $P_{4050} = (1, 12, 14, 1)$  lies on line  $a_2$   
 190 :  $P_{4068} = (3, 13, 14, 1)$  lies on line  $a_2$   
 191 :  $P_{4076} = (11, 13, 14, 1)$  lies on line  $c_{26}$   
 192 :  $P_{4086} = (5, 14, 14, 1)$  lies on line  $a_2$   
 193 :  $P_{4087} = (6, 14, 14, 1)$  lies on line  $c_{26}$   
 194 :  $P_{4113} = (0, 0, 15, 1)$  lies on line  $b_4$   
 195 :  $P_{4137} = (8, 1, 15, 1)$  lies on line  $b_3$   
 196 :  $P_{4156} = (11, 2, 15, 1)$  lies on line  $c_{45}$   
 197 :  $P_{4158} = (13, 2, 15, 1)$  lies on line  $c_{25}$   
 198 :  $P_{4206} = (13, 5, 15, 1)$  lies on line  $c_{34}$   
 199 :  $P_{4282} = (9, 10, 15, 1)$  lies on line  $c_{12}$   
 200 :  $P_{4283} = (10, 10, 15, 1)$  lies on line  $b_2$   
 201 :  $P_{4299} = (10, 11, 15, 1)$  lies on line  $c_{15}$   
 202 :  $P_{4306} = (1, 12, 15, 1)$  lies on line  $c_{24}$   
 203 :  $P_{4316} = (11, 12, 15, 1)$  lies on line  $c_{23}$

The single points on the surface are:

### Points on surface but on no line

The surface has 40 points not on any line:

The points on the surface but not on lines are:

- 0 :  $P_{375} = (5, 6, 0, 1)$   
 1 :  $P_{401} = (15, 7, 0, 1)$   
 2 :  $P_{469} = (3, 12, 0, 1)$   
 3 :  $P_{490} = (8, 13, 0, 1)$   
 4 :  $P_{587} = (10, 3, 1, 1)$   
 5 :  $P_{620} = (11, 5, 1, 1)$

6 : $P_{667} = (10, 8, 1, 1)$	24 : $P_{2561} = (0, 15, 8, 1)$
7 : $P_{780} = (11, 15, 1, 1)$	25 : $P_{2565} = (4, 15, 8, 1)$
8 : $P_{1121} = (0, 5, 3, 1)$	26 : $P_{2924} = (11, 5, 10, 1)$
9 : $P_{1135} = (14, 5, 3, 1)$	27 : $P_{3084} = (11, 15, 10, 1)$
10 : $P_{1236} = (3, 12, 3, 1)$	28 : $P_{3147} = (10, 3, 11, 1)$
11 : $P_{1248} = (15, 12, 3, 1)$	29 : $P_{3227} = (10, 8, 11, 1)$
12 : $P_{1652} = (3, 6, 5, 1)$	30 : $P_{3441} = (0, 6, 12, 1)$
13 : $P_{1654} = (5, 6, 5, 1)$	31 : $P_{3552} = (15, 12, 12, 1)$
14 : $P_{1681} = (0, 8, 5, 1)$	32 : $P_{3589} = (4, 15, 12, 1)$
15 : $P_{1683} = (2, 8, 5, 1)$	33 : $P_{3695} = (14, 5, 13, 1)$
16 : $P_{1866} = (9, 3, 6, 1)$	34 : $P_{3713} = (0, 7, 13, 1)$
17 : $P_{1908} = (3, 6, 6, 1)$	35 : $P_{3814} = (5, 13, 13, 1)$
18 : $P_{2017} = (0, 13, 6, 1)$	36 : $P_{4161} = (0, 3, 15, 1)$
19 : $P_{2185} = (8, 7, 7, 1)$	37 : $P_{4170} = (9, 3, 15, 1)$
20 : $P_{2195} = (2, 8, 7, 1)$	38 : $P_{4233} = (8, 7, 15, 1)$
21 : $P_{2257} = (0, 12, 7, 1)$	39 : $P_{4240} = (15, 7, 15, 1)$
22 : $P_{2534} = (5, 13, 8, 1)$	
23 : $P_{2537} = (8, 13, 8, 1)$	

### Line Intersection Graph

		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
		$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_6$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$	$b_6$	$c_{12}$	$c_{13}$	$c_{14}$	$c_{15}$	$c_{16}$	$c_{23}$	$c_{24}$	$c_{25}$	$c_{26}$	$c_{34}$	$c_{35}$	$c_{36}$	$c_{45}$	$c_{46}$	$c_{56}$
0	$a_1$	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0
1	$a_2$	0	0	0	0	0	0	1	0	1	1	1	1	1	0	0	0	0	1	1	1	1	0	0	0	0	0	0
2	$a_3$	0	0	0	0	0	0	1	1	0	1	1	1	0	1	0	0	0	1	0	0	0	1	1	1	0	0	0
3	$a_4$	0	0	0	0	0	0	1	1	1	0	1	1	0	0	1	0	0	0	1	0	0	1	0	0	1	1	0
4	$a_5$	0	0	0	0	0	0	1	1	1	1	0	1	0	0	0	1	0	0	0	1	0	0	1	0	1	0	1
5	$a_6$	0	0	0	0	0	0	1	1	1	1	1	0	0	0	0	0	1	0	0	0	1	0	0	1	0	1	1
6	$b_1$	0	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0
7	$b_2$	1	0	1	1	1	1	0	0	0	0	0	0	1	0	0	0	0	1	1	1	1	0	0	0	0	0	0
8	$b_3$	1	1	0	1	1	1	0	0	0	0	0	0	0	1	0	0	0	1	0	0	0	1	1	1	0	0	0
9	$b_4$	1	1	1	0	1	1	0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	1	0	0	1	1	0
10	$b_5$	1	1	1	1	0	1	0	0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	1	0	1	0	1
11	$b_6$	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	1	0	0	1	0	1	1
12	$c_{12}$	1	1	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1
13	$c_{13}$	1	0	1	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	1	1	1
14	$c_{14}$	1	0	0	1	0	0	1	0	0	1	0	0	0	0	0	0	0	1	0	1	1	0	1	1	0	0	1
15	$c_{15}$	1	0	0	0	1	0	1	0	0	0	1	0	0	0	0	0	0	1	1	0	1	1	0	1	0	1	0
16	$c_{16}$	1	0	0	0	0	1	1	0	0	0	0	1	0	0	0	0	0	1	1	1	0	1	1	0	1	0	0
17	$c_{23}$	0	1	1	0	0	0	0	1	1	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	1	1	1
18	$c_{24}$	0	1	0	1	0	0	0	1	0	1	0	0	0	1	0	1	1	0	0	0	0	0	1	1	0	0	1
19	$c_{25}$	0	1	0	0	1	0	0	1	0	0	1	0	0	1	1	0	1	0	0	0	0	1	0	1	0	1	0
20	$c_{26}$	0	1	0	0	0	1	0	1	0	0	0	1	0	1	1	1	0	0	0	0	0	1	1	0	1	0	0
21	$c_{34}$	0	0	1	1	0	0	0	0	1	1	0	0	1	0	0	1	1	0	0	1	1	0	0	0	0	0	1
22	$c_{35}$	0	0	1	0	1	0	0	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	0	0	0	1	0
23	$c_{36}$	0	0	1	0	0	1	0	0	1	0	0	1	1	0	1	1	0	0	1	1	0	0	0	0	1	0	0
24	$c_{45}$	0	0	0	1	1	0	0	0	0	1	1	0	1	1	0	0	1	1	0	0	1	0	0	1	0	0	0
25	$c_{46}$	0	0	0	1	0	1	0	0	0	1	0	1	1	1	0	1	0	1	0	1	0	0	1	0	0	0	0
26	$c_{56}$	0	0	0	0	1	1	0	0	0	0	1	1	1	1	1	0	0	1	1	0	0	1	0	0	0	0	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$
in point	$P_{33}$	$P_{29}$	$P_2$	$P_{28}$	$P_0$	$P_{23}$	$P_{30}$	$P_2$	$P_{21}$	$P_{20}$

Line 1 intersects

Line	$\ell_6$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$
in point	$P_{4104}$	$P_{3875}$	$P_{3857}$	$P_{4048}$	$P_6$	$P_{4030}$	$P_{3947}$	$P_{3857}$	$P_{3965}$	$P_{3983}$

Line 2 intersects

Line	$\ell_6$	$\ell_7$	$\ell_9$	$\ell_{10}$	$\ell_{11}$	$\ell_{13}$	$\ell_{17}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$
in point	$P_{924}$	$P_{948}$	$P_{785}$	$P_{968}$	$P_8$	$P_{805}$	$P_{999}$	$P_{785}$	$P_{845}$	$P_{979}$

Line 3 intersects

Line	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_{10}$	$\ell_{11}$	$\ell_{14}$	$\ell_{18}$	$\ell_{21}$	$\ell_{24}$	$\ell_{25}$
in point	$P_{2801}$	$P_{2742}$	$P_{2599}$	$P_{2755}$	$P_{11}$	$P_{2578}$	$P_{2824}$	$P_{2716}$	$P_{2702}$	$P_{2794}$

Line 4 intersects

Line	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{11}$	$\ell_{15}$	$\ell_{19}$	$\ell_{22}$	$\ell_{24}$	$\ell_{26}$
in point	$P_{1422}$	$P_{1469}$	$P_{1322}$	$P_{1297}$	$P_{13}$	$P_{1478}$	$P_{1383}$	$P_{1547}$	$P_{1297}$	$P_{1397}$

Line 5 intersects

Line	$\ell_6$	$\ell_7$	$\ell_8$	$\ell_9$	$\ell_{10}$	$\ell_{16}$	$\ell_{20}$	$\ell_{23}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{491}$	$P_{697}$	$P_{2095}$	$P_{2577}$	$P_{4295}$	$P_{132}$	$P_{4056}$	$P_{844}$	$P_{2577}$	$P_{1438}$

Line 6 intersects

Line	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$
in point	$P_{4104}$	$P_{924}$	$P_{2801}$	$P_{1422}$	$P_{491}$	$P_{3510}$	$P_{4135}$	$P_{2322}$	$P_{3267}$	$P_{244}$

Line 7 intersects

Line	$\ell_0$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{12}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$
in point	$P_{33}$	$P_{948}$	$P_{2742}$	$P_{1469}$	$P_{697}$	$P_{3249}$	$P_{3007}$	$P_{1214}$	$P_{3776}$	$P_{4021}$

Line 8 intersects

Line	$\ell_0$	$\ell_1$	$\ell_3$	$\ell_4$	$\ell_5$	$\ell_{13}$	$\ell_{17}$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$
in point	$P_{29}$	$P_{3875}$	$P_{2599}$	$P_{1322}$	$P_{2095}$	$P_{546}$	$P_{2349}$	$P_{1829}$	$P_{1070}$	$P_{808}$

Line 9 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_4$	$\ell_5$	$\ell_{14}$	$\ell_{18}$	$\ell_{21}$	$\ell_{24}$	$\ell_{25}$
in point	$P_2$	$P_{3857}$	$P_{785}$	$P_{1297}$	$P_{2577}$	$P_2$	$P_{3857}$	$P_{785}$	$P_{1297}$	$P_{2577}$

Line 10 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_5$	$\ell_{15}$	$\ell_{19}$	$\ell_{22}$	$\ell_{24}$	$\ell_{26}$
in point	$P_{28}$	$P_{4048}$	$P_{968}$	$P_{2755}$	$P_{4295}$	$P_{3009}$	$P_{3274}$	$P_{1993}$	$P_{710}$	$P_{1476}$

Line 11 intersects

Line	$\ell_0$	$\ell_1$	$\ell_2$	$\ell_3$	$\ell_4$	$\ell_{16}$	$\ell_{20}$	$\ell_{23}$	$\ell_{25}$	$\ell_{26}$
in point	$P_0$	$P_6$	$P_8$	$P_{11}$	$P_{13}$	$P_1$	$P_{16}$	$P_{10}$	$P_{18}$	$P_{17}$

Line 12 intersects

Line	$\ell_0$	$\ell_1$	$\ell_6$	$\ell_7$	$\ell_{21}$	$\ell_{22}$	$\ell_{23}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{23}$	$P_{4030}$	$P_{3510}$	$P_{3249}$	$P_{692}$	$P_{2997}$	$P_{960}$	$P_{2493}$	$P_{2745}$	$P_{1471}$

Line 13 intersects

Line	$\ell_0$	$\ell_2$	$\ell_6$	$\ell_8$	$\ell_{18}$	$\ell_{19}$	$\ell_{20}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{30}$	$P_{805}$	$P_{4135}$	$P_{546}$	$P_{3363}$	$P_{1576}$	$P_{3886}$	$P_{3626}$	$P_{2607}$	$P_{1325}$



Line 14 intersects

Line	$\ell_0$	$\ell_3$	$\ell_6$	$\ell_9$	$\ell_{17}$	$\ell_{19}$	$\ell_{20}$	$\ell_{22}$	$\ell_{23}$	$\ell_{26}$
in point	$P_2$	$P_{2578}$	$P_{2322}$	$P_2$	$P_{1554}$	$P_{1042}$	$P_{3858}$	$P_{4114}$	$P_{786}$	$P_{1298}$

Line 15 intersects

Line	$\ell_0$	$\ell_4$	$\ell_6$	$\ell_{10}$	$\ell_{17}$	$\ell_{18}$	$\ell_{20}$	$\ell_{21}$	$\ell_{23}$	$\ell_{25}$
in point	$P_{21}$	$P_{1478}$	$P_{3267}$	$P_{3009}$	$P_{2244}$	$P_{720}$	$P_{4041}$	$P_{1736}$	$P_{970}$	$P_{2759}$

Line 16 intersects

Line	$\ell_0$	$\ell_5$	$\ell_6$	$\ell_{11}$	$\ell_{17}$	$\ell_{18}$	$\ell_{19}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$
in point	$P_{20}$	$P_{132}$	$P_{244}$	$P_1$	$P_{164}$	$P_{212}$	$P_{84}$	$P_{116}$	$P_{52}$	$P_{228}$

Line 17 intersects

Line	$\ell_1$	$\ell_2$	$\ell_7$	$\ell_8$	$\ell_{14}$	$\ell_{15}$	$\ell_{16}$	$\ell_{24}$	$\ell_{25}$	$\ell_{26}$
in point	$P_{3947}$	$P_{999}$	$P_{3007}$	$P_{2349}$	$P_{1554}$	$P_{2244}$	$P_{164}$	$P_{374}$	$P_{2718}$	$P_{1441}$

Line 18 intersects

Line	$\ell_1$	$\ell_3$	$\ell_7$	$\ell_9$	$\ell_{13}$	$\ell_{15}$	$\ell_{16}$	$\ell_{22}$	$\ell_{23}$	$\ell_{26}$
in point	$P_{3857}$	$P_{2824}$	$P_{1214}$	$P_{3857}$	$P_{3363}$	$P_{720}$	$P_{212}$	$P_{400}$	$P_{893}$	$P_{1387}$

Line 19 intersects

Line	$\ell_1$	$\ell_4$	$\ell_7$	$\ell_{10}$	$\ell_{13}$	$\ell_{14}$	$\ell_{16}$	$\ell_{21}$	$\ell_{23}$	$\ell_{25}$
in point	$P_{3965}$	$P_{1383}$	$P_{3776}$	$P_{3274}$	$P_{1576}$	$P_{1042}$	$P_{84}$	$P_{468}$	$P_{849}$	$P_{2636}$

Line 20 intersects

Line	$\ell_1$	$\ell_5$	$\ell_7$	$\ell_{11}$	$\ell_{13}$	$\ell_{14}$	$\ell_{15}$	$\ell_{21}$	$\ell_{22}$	$\ell_{24}$
in point	$P_{3983}$	$P_{4056}$	$P_{4021}$	$P_{16}$	$P_{3886}$	$P_{3858}$	$P_{4041}$	$P_{3917}$	$P_{3889}$	$P_{4107}$

Line 21 intersects

Line	$\ell_2$	$\ell_3$	$\ell_8$	$\ell_9$	$\ell_{12}$	$\ell_{15}$	$\ell_{16}$	$\ell_{19}$	$\ell_{20}$	$\ell_{26}$
in point	$P_{785}$	$P_{2716}$	$P_{1829}$	$P_{785}$	$P_{692}$	$P_{1736}$	$P_{116}$	$P_{468}$	$P_{3917}$	$P_{1511}$

Line 22 intersects

Line	$\ell_2$	$\ell_4$	$\ell_8$	$\ell_{10}$	$\ell_{12}$	$\ell_{14}$	$\ell_{16}$	$\ell_{18}$	$\ell_{20}$	$\ell_{25}$
in point	$P_{845}$	$P_{1547}$	$P_{1070}$	$P_{1993}$	$P_{2997}$	$P_{4114}$	$P_{52}$	$P_{400}$	$P_{3889}$	$P_{2776}$

Line 23 intersects

Line	$\ell_2$	$\ell_5$	$\ell_8$	$\ell_{11}$	$\ell_{12}$	$\ell_{14}$	$\ell_{15}$	$\ell_{18}$	$\ell_{19}$	$\ell_{24}$
in point	$P_{979}$	$P_{844}$	$P_{808}$	$P_{10}$	$P_{960}$	$P_{786}$	$P_{970}$	$P_{893}$	$P_{849}$	$P_{871}$

Line 24 intersects

Line	$\ell_3$	$\ell_4$	$\ell_9$	$\ell_{10}$	$\ell_{12}$	$\ell_{13}$	$\ell_{16}$	$\ell_{17}$	$\ell_{20}$	$\ell_{23}$
in point	$P_{2702}$	$P_{1297}$	$P_{1297}$	$P_{710}$	$P_{2493}$	$P_{3626}$	$P_{228}$	$P_{374}$	$P_{4107}$	$P_{871}$

Line 25 intersects

Line	$\ell_3$	$\ell_5$	$\ell_9$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{15}$	$\ell_{17}$	$\ell_{19}$	$\ell_{22}$
in point	$P_{2794}$	$P_{2577}$	$P_{2577}$	$P_{18}$	$P_{2745}$	$P_{2607}$	$P_{2759}$	$P_{2718}$	$P_{2636}$	$P_{2776}$

Line 26 intersects

Line	$\ell_4$	$\ell_5$	$\ell_{10}$	$\ell_{11}$	$\ell_{12}$	$\ell_{13}$	$\ell_{14}$	$\ell_{17}$	$\ell_{18}$	$\ell_{21}$
in point	$P_{1397}$	$P_{1438}$	$P_{1476}$	$P_{17}$	$P_{1471}$	$P_{1325}$	$P_{1298}$	$P_{1441}$	$P_{1387}$	$P_{1511}$

The surface has 369 points:

The points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$	54 : $P_{400} = (14, 7, 0, 1)$	108 : $P_{1033} = (8, 15, 2, 1)$
1 : $P_1 = (0, 1, 0, 0)$	55 : $P_{401} = (15, 7, 0, 1)$	109 : $P_{1039} = (14, 15, 2, 1)$
2 : $P_2 = (0, 0, 1, 0)$	56 : $P_{440} = (6, 10, 0, 1)$	110 : $P_{1041} = (0, 0, 3, 1)$
3 : $P_3 = (0, 0, 0, 1)$	57 : $P_{441} = (7, 10, 0, 1)$	111 : $P_{1042} = (1, 0, 3, 1)$
4 : $P_5 = (1, 1, 0, 0)$	58 : $P_{462} = (12, 11, 0, 1)$	112 : $P_{1070} = (13, 1, 3, 1)$
5 : $P_6 = (2, 1, 0, 0)$	59 : $P_{463} = (13, 11, 0, 1)$	113 : $P_{1072} = (15, 1, 3, 1)$
6 : $P_7 = (3, 1, 0, 0)$	60 : $P_{468} = (2, 12, 0, 1)$	114 : $P_{1112} = (7, 4, 3, 1)$
7 : $P_8 = (4, 1, 0, 0)$	61 : $P_{469} = (3, 12, 0, 1)$	115 : $P_{1115} = (10, 4, 3, 1)$
8 : $P_9 = (5, 1, 0, 0)$	62 : $P_{490} = (8, 13, 0, 1)$	116 : $P_{1121} = (0, 5, 3, 1)$
9 : $P_{10} = (6, 1, 0, 0)$	63 : $P_{491} = (9, 13, 0, 1)$	117 : $P_{1135} = (14, 5, 3, 1)$
10 : $P_{11} = (7, 1, 0, 0)$	64 : $P_{530} = (0, 0, 1, 1)$	118 : $P_{1138} = (1, 6, 3, 1)$
11 : $P_{12} = (8, 1, 0, 0)$	65 : $P_{531} = (1, 0, 1, 1)$	119 : $P_{1147} = (10, 6, 3, 1)$
12 : $P_{13} = (9, 1, 0, 0)$	66 : $P_{546} = (0, 1, 1, 1)$	120 : $P_{1176} = (7, 8, 3, 1)$
13 : $P_{14} = (10, 1, 0, 0)$	67 : $P_{585} = (8, 3, 1, 1)$	121 : $P_{1212} = (11, 10, 3, 1)$
14 : $P_{15} = (11, 1, 0, 0)$	68 : $P_{587} = (10, 3, 1, 1)$	122 : $P_{1214} = (13, 10, 3, 1)$
15 : $P_{16} = (12, 1, 0, 0)$	69 : $P_{620} = (11, 5, 1, 1)$	123 : $P_{1228} = (11, 11, 3, 1)$
16 : $P_{17} = (13, 1, 0, 0)$	70 : $P_{624} = (15, 5, 1, 1)$	124 : $P_{1231} = (14, 11, 3, 1)$
17 : $P_{18} = (14, 1, 0, 0)$	71 : $P_{660} = (3, 8, 1, 1)$	125 : $P_{1236} = (3, 12, 3, 1)$
18 : $P_{19} = (15, 1, 0, 0)$	72 : $P_{667} = (10, 8, 1, 1)$	126 : $P_{1248} = (15, 12, 3, 1)$
19 : $P_{20} = (1, 0, 1, 0)$	73 : $P_{692} = (3, 10, 1, 1)$	127 : $P_{1297} = (0, 0, 4, 1)$
20 : $P_{21} = (2, 0, 1, 0)$	74 : $P_{697} = (8, 10, 1, 1)$	128 : $P_{1298} = (1, 0, 4, 1)$
21 : $P_{22} = (3, 0, 1, 0)$	75 : $P_{710} = (5, 11, 1, 1)$	129 : $P_{1322} = (9, 1, 4, 1)$
22 : $P_{23} = (4, 0, 1, 0)$	76 : $P_{720} = (15, 11, 1, 1)$	130 : $P_{1325} = (12, 1, 4, 1)$
23 : $P_{24} = (5, 0, 1, 0)$	77 : $P_{774} = (5, 15, 1, 1)$	131 : $P_{1331} = (2, 2, 4, 1)$
24 : $P_{25} = (6, 0, 1, 0)$	78 : $P_{780} = (11, 15, 1, 1)$	132 : $P_{1340} = (11, 2, 4, 1)$
25 : $P_{26} = (7, 0, 1, 0)$	79 : $P_{785} = (0, 0, 2, 1)$	133 : $P_{1347} = (2, 3, 4, 1)$
26 : $P_{27} = (8, 0, 1, 0)$	80 : $P_{786} = (1, 0, 2, 1)$	134 : $P_{1360} = (15, 3, 4, 1)$
27 : $P_{28} = (9, 0, 1, 0)$	81 : $P_{805} = (4, 1, 2, 1)$	135 : $P_{1368} = (7, 4, 4, 1)$
28 : $P_{29} = (10, 0, 1, 0)$	82 : $P_{808} = (7, 1, 2, 1)$	136 : $P_{1376} = (15, 4, 4, 1)$
29 : $P_{30} = (11, 0, 1, 0)$	83 : $P_{825} = (8, 2, 2, 1)$	137 : $P_{1383} = (6, 5, 4, 1)$
30 : $P_{31} = (12, 0, 1, 0)$	84 : $P_{830} = (13, 2, 2, 1)$	138 : $P_{1387} = (10, 5, 4, 1)$
31 : $P_{32} = (13, 0, 1, 0)$	85 : $P_{844} = (11, 3, 2, 1)$	139 : $P_{1397} = (4, 6, 4, 1)$
32 : $P_{33} = (14, 0, 1, 0)$	86 : $P_{845} = (12, 3, 2, 1)$	140 : $P_{1418} = (9, 7, 4, 1)$
33 : $P_{34} = (15, 0, 1, 0)$	87 : $P_{849} = (0, 4, 2, 1)$	141 : $P_{1422} = (13, 7, 4, 1)$
34 : $P_{36} = (1, 1, 1, 0)$	88 : $P_{858} = (9, 4, 2, 1)$	142 : $P_{1432} = (7, 8, 4, 1)$
35 : $P_{52} = (1, 2, 1, 0)$	89 : $P_{871} = (6, 5, 2, 1)$	143 : $P_{1438} = (13, 8, 4, 1)$
36 : $P_{68} = (1, 3, 1, 0)$	90 : $P_{878} = (13, 5, 2, 1)$	144 : $P_{1441} = (0, 9, 4, 1)$
37 : $P_{84} = (1, 4, 1, 0)$	91 : $P_{882} = (1, 6, 2, 1)$	145 : $P_{1455} = (14, 9, 4, 1)$
38 : $P_{100} = (1, 5, 1, 0)$	92 : $P_{893} = (12, 6, 2, 1)$	146 : $P_{1469} = (12, 10, 4, 1)$
39 : $P_{116} = (1, 6, 1, 0)$	93 : $P_{902} = (5, 7, 2, 1)$	147 : $P_{1471} = (14, 10, 4, 1)$
40 : $P_{132} = (1, 7, 1, 0)$	94 : $P_{907} = (10, 7, 2, 1)$	148 : $P_{1476} = (3, 11, 4, 1)$
41 : $P_{148} = (1, 8, 1, 0)$	95 : $P_{916} = (3, 8, 2, 1)$	149 : $P_{1478} = (5, 11, 4, 1)$
42 : $P_{164} = (1, 9, 1, 0)$	96 : $P_{924} = (11, 8, 2, 1)$	150 : $P_{1497} = (8, 12, 4, 1)$
43 : $P_{180} = (1, 10, 1, 0)$	97 : $P_{934} = (5, 9, 2, 1)$	151 : $P_{1500} = (11, 12, 4, 1)$
44 : $P_{196} = (1, 11, 1, 0)$	98 : $P_{944} = (15, 9, 2, 1)$	152 : $P_{1506} = (1, 13, 4, 1)$
45 : $P_{212} = (1, 12, 1, 0)$	99 : $P_{948} = (3, 10, 2, 1)$	153 : $P_{1511} = (6, 13, 4, 1)$
46 : $P_{228} = (1, 13, 1, 0)$	100 : $P_{960} = (15, 10, 2, 1)$	154 : $P_{1524} = (3, 14, 4, 1)$
47 : $P_{244} = (1, 14, 1, 0)$	101 : $P_{968} = (7, 11, 2, 1)$	155 : $P_{1529} = (8, 14, 4, 1)$
48 : $P_{260} = (1, 15, 1, 0)$	102 : $P_{970} = (9, 11, 2, 1)$	156 : $P_{1542} = (5, 15, 4, 1)$
49 : $P_{275} = (1, 0, 0, 1)$	103 : $P_{979} = (2, 12, 2, 1)$	157 : $P_{1547} = (10, 15, 4, 1)$
50 : $P_{300} = (10, 1, 0, 1)$	104 : $P_{997} = (4, 13, 2, 1)$	158 : $P_{1553} = (0, 0, 5, 1)$
51 : $P_{301} = (11, 1, 0, 1)$	105 : $P_{999} = (6, 13, 2, 1)$	159 : $P_{1554} = (1, 0, 5, 1)$
52 : $P_{374} = (4, 6, 0, 1)$	106 : $P_{1019} = (10, 14, 2, 1)$	160 : $P_{1572} = (3, 1, 5, 1)$
53 : $P_{375} = (5, 6, 0, 1)$	107 : $P_{1023} = (14, 14, 2, 1)$	161 : $P_{1576} = (7, 1, 5, 1)$

162 : $P_{1652} = (3, 6, 5, 1)$	216 : $P_{2492} = (11, 10, 8, 1)$	270 : $P_{3081} = (8, 15, 10, 1)$
163 : $P_{1654} = (5, 6, 5, 1)$	217 : $P_{2493} = (12, 10, 8, 1)$	271 : $P_{3084} = (11, 15, 10, 1)$
164 : $P_{1681} = (0, 8, 5, 1)$	218 : $P_{2501} = (4, 11, 8, 1)$	272 : $P_{3089} = (0, 0, 11, 1)$
165 : $P_{1683} = (2, 8, 5, 1)$	219 : $P_{2508} = (11, 11, 8, 1)$	273 : $P_{3090} = (1, 0, 11, 1)$
166 : $P_{1708} = (11, 9, 5, 1)$	220 : $P_{2534} = (5, 13, 8, 1)$	274 : $P_{3106} = (1, 1, 11, 1)$
167 : $P_{1709} = (12, 9, 5, 1)$	221 : $P_{2537} = (8, 13, 8, 1)$	275 : $P_{3116} = (11, 1, 11, 1)$
168 : $P_{1715} = (2, 10, 5, 1)$	222 : $P_{2551} = (6, 14, 8, 1)$	276 : $P_{3147} = (10, 3, 11, 1)$
169 : $P_{1723} = (10, 10, 5, 1)$	223 : $P_{2555} = (10, 14, 8, 1)$	277 : $P_{3152} = (15, 3, 11, 1)$
170 : $P_{1736} = (7, 11, 5, 1)$	224 : $P_{2561} = (0, 15, 8, 1)$	278 : $P_{3162} = (9, 4, 11, 1)$
171 : $P_{1739} = (10, 11, 5, 1)$	225 : $P_{2565} = (4, 15, 8, 1)$	279 : $P_{3168} = (15, 4, 11, 1)$
172 : $P_{1762} = (1, 13, 5, 1)$	226 : $P_{2577} = (0, 0, 9, 1)$	280 : $P_{3222} = (5, 8, 11, 1)$
173 : $P_{1772} = (11, 13, 5, 1)$	227 : $P_{2578} = (1, 0, 9, 1)$	281 : $P_{3227} = (10, 8, 11, 1)$
174 : $P_{1805} = (12, 15, 5, 1)$	228 : $P_{2599} = (6, 1, 9, 1)$	282 : $P_{3249} = (0, 10, 11, 1)$
175 : $P_{1809} = (0, 0, 6, 1)$	229 : $P_{2607} = (14, 1, 9, 1)$	283 : $P_{3267} = (2, 11, 11, 1)$
176 : $P_{1810} = (1, 0, 6, 1)$	230 : $P_{2614} = (5, 2, 9, 1)$	284 : $P_{3274} = (9, 11, 11, 1)$
177 : $P_{1828} = (3, 1, 6, 1)$	231 : $P_{2624} = (15, 2, 9, 1)$	285 : $P_{3315} = (2, 14, 11, 1)$
178 : $P_{1829} = (4, 1, 6, 1)$	232 : $P_{2633} = (8, 3, 9, 1)$	286 : $P_{3318} = (5, 14, 11, 1)$
179 : $P_{1843} = (2, 2, 6, 1)$	233 : $P_{2636} = (11, 3, 9, 1)$	287 : $P_{3345} = (0, 0, 12, 1)$
180 : $P_{1856} = (15, 2, 6, 1)$	234 : $P_{2645} = (4, 4, 9, 1)$	288 : $P_{3346} = (1, 0, 12, 1)$
181 : $P_{1859} = (2, 3, 6, 1)$	235 : $P_{2651} = (10, 4, 9, 1)$	289 : $P_{3363} = (2, 1, 12, 1)$
182 : $P_{1866} = (9, 3, 6, 1)$	236 : $P_{2660} = (3, 5, 9, 1)$	290 : $P_{3376} = (15, 1, 12, 1)$
183 : $P_{1881} = (8, 4, 6, 1)$	237 : $P_{2661} = (4, 5, 9, 1)$	291 : $P_{3382} = (5, 2, 12, 1)$
184 : $P_{1908} = (3, 6, 6, 1)$	238 : $P_{2683} = (10, 6, 9, 1)$	292 : $P_{3441} = (0, 6, 12, 1)$
185 : $P_{1920} = (15, 6, 6, 1)$	239 : $P_{2688} = (15, 6, 9, 1)$	293 : $P_{3443} = (2, 6, 12, 1)$
186 : $P_{1975} = (6, 10, 6, 1)$	240 : $P_{2690} = (1, 7, 9, 1)$	294 : $P_{3506} = (1, 10, 12, 1)$
187 : $P_{1978} = (9, 10, 6, 1)$	241 : $P_{2702} = (13, 7, 9, 1)$	295 : $P_{3510} = (5, 10, 12, 1)$
188 : $P_{1986} = (1, 11, 6, 1)$	242 : $P_{2716} = (11, 8, 9, 1)$	296 : $P_{3525} = (4, 11, 12, 1)$
189 : $P_{1993} = (8, 11, 6, 1)$	243 : $P_{2718} = (13, 8, 9, 1)$	297 : $P_{3533} = (12, 11, 12, 1)$
190 : $P_{2017} = (0, 13, 6, 1)$	244 : $P_{2724} = (3, 9, 9, 1)$	298 : $P_{3545} = (8, 12, 12, 1)$
191 : $P_{2021} = (4, 13, 6, 1)$	245 : $P_{2733} = (12, 9, 9, 1)$	299 : $P_{3552} = (15, 12, 12, 1)$
192 : $P_{2065} = (0, 0, 7, 1)$	246 : $P_{2742} = (5, 10, 9, 1)$	300 : $P_{3577} = (8, 14, 12, 1)$
193 : $P_{2066} = (1, 0, 7, 1)$	247 : $P_{2745} = (8, 10, 9, 1)$	301 : $P_{3583} = (14, 14, 12, 1)$
194 : $P_{2089} = (8, 1, 7, 1)$	248 : $P_{2755} = (2, 11, 9, 1)$	302 : $P_{3589} = (4, 15, 12, 1)$
195 : $P_{2095} = (14, 1, 7, 1)$	249 : $P_{2759} = (6, 11, 9, 1)$	303 : $P_{3599} = (14, 15, 12, 1)$
196 : $P_{2182} = (5, 7, 7, 1)$	250 : $P_{2776} = (7, 12, 9, 1)$	304 : $P_{3601} = (0, 0, 13, 1)$
197 : $P_{2185} = (8, 7, 7, 1)$	251 : $P_{2783} = (14, 12, 9, 1)$	305 : $P_{3602} = (1, 0, 13, 1)$
198 : $P_{2195} = (2, 8, 7, 1)$	252 : $P_{2794} = (9, 13, 9, 1)$	306 : $P_{3622} = (5, 1, 13, 1)$
199 : $P_{2202} = (9, 8, 7, 1)$	253 : $P_{2801} = (0, 14, 9, 1)$	307 : $P_{3626} = (9, 1, 13, 1)$
200 : $P_{2214} = (5, 9, 7, 1)$	254 : $P_{2803} = (2, 14, 9, 1)$	308 : $P_{3668} = (3, 4, 13, 1)$
201 : $P_{2218} = (9, 9, 7, 1)$	255 : $P_{2824} = (7, 15, 9, 1)$	309 : $P_{3669} = (4, 4, 13, 1)$
202 : $P_{2227} = (2, 10, 7, 1)$	256 : $P_{2829} = (12, 15, 9, 1)$	310 : $P_{3685} = (4, 5, 13, 1)$
203 : $P_{2232} = (7, 10, 7, 1)$	257 : $P_{2833} = (0, 0, 10, 1)$	311 : $P_{3695} = (14, 5, 13, 1)$
204 : $P_{2242} = (1, 11, 7, 1)$	258 : $P_{2834} = (1, 0, 10, 1)$	312 : $P_{3713} = (0, 7, 13, 1)$
205 : $P_{2244} = (3, 11, 7, 1)$	259 : $P_{2850} = (1, 1, 10, 1)$	313 : $P_{3722} = (9, 7, 13, 1)$
206 : $P_{2257} = (0, 12, 7, 1)$	260 : $P_{2859} = (10, 1, 10, 1)$	314 : $P_{3760} = (15, 9, 13, 1)$
207 : $P_{2271} = (14, 12, 7, 1)$	261 : $P_{2869} = (4, 2, 10, 1)$	315 : $P_{3762} = (1, 10, 13, 1)$
208 : $P_{2292} = (3, 14, 7, 1)$	262 : $P_{2873} = (8, 2, 10, 1)$	316 : $P_{3776} = (15, 10, 13, 1)$
209 : $P_{2321} = (0, 0, 8, 1)$	263 : $P_{2916} = (3, 5, 10, 1)$	317 : $P_{3790} = (13, 11, 13, 1)$
210 : $P_{2322} = (1, 0, 8, 1)$	264 : $P_{2924} = (11, 5, 10, 1)$	318 : $P_{3791} = (14, 11, 13, 1)$
211 : $P_{2342} = (5, 1, 8, 1)$	265 : $P_{2980} = (3, 9, 10, 1)$	319 : $P_{3812} = (3, 13, 13, 1)$
212 : $P_{2349} = (12, 1, 8, 1)$	266 : $P_{2991} = (14, 9, 10, 1)$	320 : $P_{3814} = (5, 13, 13, 1)$
213 : $P_{2375} = (6, 3, 8, 1)$	267 : $P_{2997} = (4, 10, 10, 1)$	321 : $P_{3857} = (0, 0, 14, 1)$
214 : $P_{2434} = (1, 7, 8, 1)$	268 : $P_{3007} = (14, 10, 10, 1)$	322 : $P_{3858} = (1, 0, 14, 1)$
215 : $P_{2443} = (10, 7, 8, 1)$	269 : $P_{3009} = (0, 11, 10, 1)$	323 : $P_{3875} = (2, 1, 14, 1)$

324 : $P_{3886} = (13, 1, 14, 1)$	340 : $P_{4021} = (4, 10, 14, 1)$	356 : $P_{4156} = (11, 2, 15, 1)$
325 : $P_{3889} = (0, 2, 14, 1)$	341 : $P_{4030} = (13, 10, 14, 1)$	357 : $P_{4158} = (13, 2, 15, 1)$
326 : $P_{3893} = (4, 2, 14, 1)$	342 : $P_{4041} = (8, 11, 14, 1)$	358 : $P_{4161} = (0, 3, 15, 1)$
327 : $P_{3911} = (6, 3, 14, 1)$	343 : $P_{4048} = (15, 11, 14, 1)$	359 : $P_{4170} = (9, 3, 15, 1)$
328 : $P_{3917} = (12, 3, 14, 1)$	344 : $P_{4050} = (1, 12, 14, 1)$	360 : $P_{4206} = (13, 5, 15, 1)$
329 : $P_{3924} = (3, 4, 14, 1)$	345 : $P_{4056} = (7, 12, 14, 1)$	361 : $P_{4233} = (8, 7, 15, 1)$
330 : $P_{3929} = (8, 4, 14, 1)$	346 : $P_{4068} = (3, 13, 14, 1)$	362 : $P_{4240} = (15, 7, 15, 1)$
331 : $P_{3947} = (10, 5, 14, 1)$	347 : $P_{4076} = (11, 13, 14, 1)$	363 : $P_{4282} = (9, 10, 15, 1)$
332 : $P_{3952} = (15, 5, 14, 1)$	348 : $P_{4086} = (5, 14, 14, 1)$	364 : $P_{4283} = (10, 10, 15, 1)$
333 : $P_{3955} = (2, 6, 14, 1)$	349 : $P_{4087} = (6, 14, 14, 1)$	365 : $P_{4295} = (6, 11, 15, 1)$
334 : $P_{3965} = (12, 6, 14, 1)$	350 : $P_{4104} = (7, 15, 14, 1)$	366 : $P_{4299} = (10, 11, 15, 1)$
335 : $P_{3983} = (14, 7, 14, 1)$	351 : $P_{4107} = (10, 15, 14, 1)$	367 : $P_{4306} = (1, 12, 15, 1)$
336 : $P_{3990} = (5, 8, 14, 1)$	352 : $P_{4113} = (0, 0, 15, 1)$	368 : $P_{4316} = (11, 12, 15, 1)$
337 : $P_{3994} = (9, 8, 14, 1)$	353 : $P_{4114} = (1, 0, 15, 1)$	
338 : $P_{4010} = (9, 9, 14, 1)$	354 : $P_{4135} = (6, 1, 15, 1)$	
339 : $P_{4012} = (11, 9, 14, 1)$	355 : $P_{4137} = (8, 1, 15, 1)$	