

Rank-67115 over GF(16)

January 15, 2021

The equation

The equation of the surface is :

$$X_3^3 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_2^2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(16) is 287383829

General information

Number of lines	12
Number of points	321
Number of singular points	3
Number of Eckardt points	0
Number of double points	18
Number of single points	156
Number of points off lines	144
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17^{12}
Type of lines on points	$4^3, 2^{18}, 1^{156}, 0^{144}$

Singular Points

The surface has 3 singular points:

$$\begin{aligned} 0 : P_{290} &= \mathbf{P}(0, 1, 0, 1) = \mathbf{P}(0, 1, 0, 1) \\ 1 : P_{291} &= \mathbf{P}(1, 1, 0, 1) = \mathbf{P}(1, 1, 0, 1) \end{aligned}$$

$$2 : P_{546} = \mathbf{P}(0, 1, 1, 1) = \mathbf{P}(0, 1, 1, 1)$$

The 12 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0$$

$$\begin{aligned}
\ell_1 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{274} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{274} = \mathbf{Pl}(1, 0, 1, 0, 0, 1)_{4657} \\
\ell_2 &= \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69888} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69888} = \mathbf{Pl}(0, 0, 0, 0, 0, 1)_{4625} \\
\ell_3 &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{16} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{16} = \mathbf{Pl}(1, 0, 0, 0, 1, 0)_{290} \\
\ell_4 &= \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69905} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{69905} = \mathbf{Pl}(0, 1, 0, 0, 0, 1)_{4641} \\
\ell_5 &= \begin{bmatrix} 1 & 0 & \delta^5 & \delta^5 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{51068} = \begin{bmatrix} 1 & 0 & 11 & 11 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{51068} = \mathbf{Pl}(1, 0, 1, 1, 10, 1)_{46147} \\
\ell_6 &= \begin{bmatrix} 1 & 0 & \delta^{10} & \delta^{10} \\ 0 & 1 & 1 & 1 \end{bmatrix}_{46427} = \begin{bmatrix} 1 & 0 & 10 & 10 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{46427} = \mathbf{Pl}(1, 0, 1, 1, 11, 1)_{50227} \\
\ell_7 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{290} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{290} = \mathbf{Pl}(1, 1, 1, 0, 1, 1)_{8976} \\
\ell_8 &= \begin{bmatrix} 1 & 0 & \delta^5 & 1 \\ 0 & 1 & \delta^5 & 0 \end{bmatrix}_{7382} = \begin{bmatrix} 1 & 0 & 11 & 1 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{7382} = \mathbf{Pl}(1, 1, 1, 10, 0, 1)_{7611} \\
\ell_9 &= \begin{bmatrix} 1 & 0 & \delta^{10} & \delta^5 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{50794} = \begin{bmatrix} 1 & 0 & 10 & 11 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{50794} = \mathbf{Pl}(1, 1, 0, 10, 11, 1)_{50136} \\
\ell_{10} &= \begin{bmatrix} 1 & 0 & \delta^{10} & 1 \\ 0 & 1 & \delta^{10} & 0 \end{bmatrix}_{7108} = \begin{bmatrix} 1 & 0 & 10 & 1 \\ 0 & 1 & 10 & 0 \end{bmatrix}_{7108} = \mathbf{Pl}(1, 1, 1, 11, 0, 1)_{7836} \\
\ell_{11} &= \begin{bmatrix} 1 & 0 & \delta^5 & \delta^{10} \\ 0 & 1 & 0 & 1 \end{bmatrix}_{46699} = \begin{bmatrix} 1 & 0 & 11 & 10 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{46699} = \mathbf{Pl}(1, 1, 0, 11, 10, 1)_{46071}
\end{aligned}$$

Rank of lines: (0, 274, 69888, 16, 69905, 51068, 46427, 290, 7382, 50794, 7108, 46699)

Rank of points on Klein quadric: (0, 4657, 4625, 290, 4641, 46147, 50227, 8976, 7611, 50136, 7836, 46071)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 18 Double points:

The double points on the surface are:

$$\begin{aligned}
P_5 &= (1, 1, 0, 0) = \ell_0 \cap \ell_1 & P_{179} &= (0, 10, 1, 0) = \ell_2 \cap \ell_8 \\
P_1 &= (0, 1, 0, 0) = \ell_0 \cap \ell_2 & P_{195} &= (0, 11, 1, 0) = \ell_2 \cap \ell_{10} \\
P_0 &= (1, 0, 0, 0) = \ell_0 \cap \ell_3 & P_{716} &= (11, 11, 1, 1) = \ell_5 \cap \ell_9 \\
P_{14} &= (10, 1, 0, 0) = \ell_0 \cap \ell_5 & P_{690} &= (1, 10, 1, 1) = \ell_5 \cap \ell_{10} \\
P_{15} &= (11, 1, 0, 0) = \ell_0 \cap \ell_6 & P_{706} &= (1, 11, 1, 1) = \ell_6 \cap \ell_8 \\
P_{35} &= (0, 1, 1, 0) = \ell_1 \cap \ell_2 & P_{699} &= (10, 10, 1, 1) = \ell_6 \cap \ell_{11} \\
P_{20} &= (1, 0, 1, 0) = \ell_1 \cap \ell_7 & P_{2994} &= (1, 10, 10, 1) = \ell_8 \cap \ell_9 \\
P_{190} &= (11, 10, 1, 0) = \ell_1 \cap \ell_9 & P_{3266} &= (1, 11, 11, 1) = \ell_{10} \cap \ell_{11} \\
P_{205} &= (10, 11, 1, 0) = \ell_1 \cap \ell_{11} \\
P_2 &= (0, 0, 1, 0) = \ell_2 \cap \ell_4
\end{aligned}$$

Single Points

The surface has 156 single points:
The single points on the surface are:

- | | |
|---|---|
| 0 : $P_6 = (2, 1, 0, 0)$ lies on line ℓ_0 | 48 : $P_{304} = (14, 1, 0, 1)$ lies on line ℓ_3 |
| 1 : $P_7 = (3, 1, 0, 0)$ lies on line ℓ_0 | 49 : $P_{305} = (15, 1, 0, 1)$ lies on line ℓ_3 |
| 2 : $P_8 = (4, 1, 0, 0)$ lies on line ℓ_0 | 50 : $P_{540} = (10, 0, 1, 1)$ lies on line ℓ_5 |
| 3 : $P_9 = (5, 1, 0, 0)$ lies on line ℓ_0 | 51 : $P_{541} = (11, 0, 1, 1)$ lies on line ℓ_6 |
| 4 : $P_{10} = (6, 1, 0, 0)$ lies on line ℓ_0 | 52 : $P_{565} = (4, 2, 1, 1)$ lies on line ℓ_6 |
| 5 : $P_{11} = (7, 1, 0, 0)$ lies on line ℓ_0 | 53 : $P_{568} = (7, 2, 1, 1)$ lies on line ℓ_5 |
| 6 : $P_{12} = (8, 1, 0, 0)$ lies on line ℓ_0 | 54 : $P_{590} = (13, 3, 1, 1)$ lies on line ℓ_5 |
| 7 : $P_{13} = (9, 1, 0, 0)$ lies on line ℓ_0 | 55 : $P_{592} = (15, 3, 1, 1)$ lies on line ℓ_6 |
| 8 : $P_{16} = (12, 1, 0, 0)$ lies on line ℓ_0 | 56 : $P_{602} = (9, 4, 1, 1)$ lies on line ℓ_5 |
| 9 : $P_{17} = (13, 1, 0, 0)$ lies on line ℓ_0 | 57 : $P_{605} = (12, 4, 1, 1)$ lies on line ℓ_6 |
| 10 : $P_{18} = (14, 1, 0, 0)$ lies on line ℓ_0 | 58 : $P_{612} = (3, 5, 1, 1)$ lies on line ℓ_5 |
| 11 : $P_{19} = (15, 1, 0, 0)$ lies on line ℓ_0 | 59 : $P_{616} = (7, 5, 1, 1)$ lies on line ℓ_6 |
| 12 : $P_{51} = (0, 2, 1, 0)$ lies on line ℓ_2 | 60 : $P_{628} = (3, 6, 1, 1)$ lies on line ℓ_6 |
| 13 : $P_{54} = (3, 2, 1, 0)$ lies on line ℓ_1 | 61 : $P_{629} = (4, 6, 1, 1)$ lies on line ℓ_5 |
| 14 : $P_{67} = (0, 3, 1, 0)$ lies on line ℓ_2 | 62 : $P_{649} = (8, 7, 1, 1)$ lies on line ℓ_6 |
| 15 : $P_{69} = (2, 3, 1, 0)$ lies on line ℓ_1 | 63 : $P_{655} = (14, 7, 1, 1)$ lies on line ℓ_5 |
| 16 : $P_{83} = (0, 4, 1, 0)$ lies on line ℓ_2 | 64 : $P_{662} = (5, 8, 1, 1)$ lies on line ℓ_6 |
| 17 : $P_{88} = (5, 4, 1, 0)$ lies on line ℓ_1 | 65 : $P_{669} = (12, 8, 1, 1)$ lies on line ℓ_5 |
| 18 : $P_{99} = (0, 5, 1, 0)$ lies on line ℓ_2 | 66 : $P_{679} = (6, 9, 1, 1)$ lies on line ℓ_5 |
| 19 : $P_{103} = (4, 5, 1, 0)$ lies on line ℓ_1 | 67 : $P_{687} = (14, 9, 1, 1)$ lies on line ℓ_6 |
| 20 : $P_{115} = (0, 6, 1, 0)$ lies on line ℓ_2 | 68 : $P_{723} = (2, 12, 1, 1)$ lies on line ℓ_6 |
| 21 : $P_{122} = (7, 6, 1, 0)$ lies on line ℓ_1 | 69 : $P_{736} = (15, 12, 1, 1)$ lies on line ℓ_5 |
| 22 : $P_{131} = (0, 7, 1, 0)$ lies on line ℓ_2 | 70 : $P_{742} = (5, 13, 1, 1)$ lies on line ℓ_5 |
| 23 : $P_{137} = (6, 7, 1, 0)$ lies on line ℓ_1 | 71 : $P_{746} = (9, 13, 1, 1)$ lies on line ℓ_6 |
| 24 : $P_{147} = (0, 8, 1, 0)$ lies on line ℓ_2 | 72 : $P_{755} = (2, 14, 1, 1)$ lies on line ℓ_5 |
| 25 : $P_{156} = (9, 8, 1, 0)$ lies on line ℓ_1 | 73 : $P_{766} = (13, 14, 1, 1)$ lies on line ℓ_6 |
| 26 : $P_{163} = (0, 9, 1, 0)$ lies on line ℓ_2 | 74 : $P_{775} = (6, 15, 1, 1)$ lies on line ℓ_6 |
| 27 : $P_{171} = (8, 9, 1, 0)$ lies on line ℓ_1 | 75 : $P_{777} = (8, 15, 1, 1)$ lies on line ℓ_5 |
| 28 : $P_{211} = (0, 12, 1, 0)$ lies on line ℓ_2 | 76 : $P_{801} = (0, 1, 2, 1)$ lies on line ℓ_4 |
| 29 : $P_{224} = (13, 12, 1, 0)$ lies on line ℓ_1 | 77 : $P_{804} = (3, 1, 2, 1)$ lies on line ℓ_7 |
| 30 : $P_{227} = (0, 13, 1, 0)$ lies on line ℓ_2 | 78 : $P_{978} = (1, 12, 2, 1)$ lies on line ℓ_8 |
| 31 : $P_{239} = (12, 13, 1, 0)$ lies on line ℓ_1 | 79 : $P_{992} = (15, 12, 2, 1)$ lies on line ℓ_9 |
| 32 : $P_{243} = (0, 14, 1, 0)$ lies on line ℓ_2 | 80 : $P_{1010} = (1, 14, 2, 1)$ lies on line ℓ_{10} |
| 33 : $P_{258} = (15, 14, 1, 0)$ lies on line ℓ_1 | 81 : $P_{1022} = (13, 14, 2, 1)$ lies on line ℓ_{11} |
| 34 : $P_{259} = (0, 15, 1, 0)$ lies on line ℓ_2 | 82 : $P_{1057} = (0, 1, 3, 1)$ lies on line ℓ_4 |
| 35 : $P_{273} = (14, 15, 1, 0)$ lies on line ℓ_1 | 83 : $P_{1059} = (2, 1, 3, 1)$ lies on line ℓ_7 |
| 36 : $P_{292} = (2, 1, 0, 1)$ lies on line ℓ_3 | 84 : $P_{1122} = (1, 5, 3, 1)$ lies on line ℓ_{10} |
| 37 : $P_{293} = (3, 1, 0, 1)$ lies on line ℓ_3 | 85 : $P_{1128} = (7, 5, 3, 1)$ lies on line ℓ_{11} |
| 38 : $P_{294} = (4, 1, 0, 1)$ lies on line ℓ_3 | 86 : $P_{1138} = (1, 6, 3, 1)$ lies on line ℓ_8 |
| 39 : $P_{295} = (5, 1, 0, 1)$ lies on line ℓ_3 | 87 : $P_{1141} = (4, 6, 3, 1)$ lies on line ℓ_9 |
| 40 : $P_{296} = (6, 1, 0, 1)$ lies on line ℓ_3 | 88 : $P_{1313} = (0, 1, 4, 1)$ lies on line ℓ_4 |
| 41 : $P_{297} = (7, 1, 0, 1)$ lies on line ℓ_3 | 89 : $P_{1318} = (5, 1, 4, 1)$ lies on line ℓ_7 |
| 42 : $P_{298} = (8, 1, 0, 1)$ lies on line ℓ_3 | 90 : $P_{1330} = (1, 2, 4, 1)$ lies on line ℓ_8 |
| 43 : $P_{299} = (9, 1, 0, 1)$ lies on line ℓ_3 | 91 : $P_{1336} = (7, 2, 4, 1)$ lies on line ℓ_9 |
| 44 : $P_{300} = (10, 1, 0, 1)$ lies on line ℓ_3 | 92 : $P_{1394} = (1, 6, 4, 1)$ lies on line ℓ_{10} |
| 45 : $P_{301} = (11, 1, 0, 1)$ lies on line ℓ_3 | 93 : $P_{1396} = (3, 6, 4, 1)$ lies on line ℓ_{11} |
| 46 : $P_{302} = (12, 1, 0, 1)$ lies on line ℓ_3 | 94 : $P_{1569} = (0, 1, 5, 1)$ lies on line ℓ_4 |
| 47 : $P_{303} = (13, 1, 0, 1)$ lies on line ℓ_3 | 95 : $P_{1573} = (4, 1, 5, 1)$ lies on line ℓ_7 |

96 : $P_{1682} = (1, 8, 5, 1)$ lies on line ℓ_8
 97 : $P_{1693} = (12, 8, 5, 1)$ lies on line ℓ_9
 98 : $P_{1762} = (1, 13, 5, 1)$ lies on line ℓ_{10}
 99 : $P_{1770} = (9, 13, 5, 1)$ lies on line ℓ_{11}
 100 : $P_{1825} = (0, 1, 6, 1)$ lies on line ℓ_4
 101 : $P_{1832} = (7, 1, 6, 1)$ lies on line ℓ_7
 102 : $P_{1954} = (1, 9, 6, 1)$ lies on line ℓ_{10}
 103 : $P_{1967} = (14, 9, 6, 1)$ lies on line ℓ_{11}
 104 : $P_{2050} = (1, 15, 6, 1)$ lies on line ℓ_8
 105 : $P_{2057} = (8, 15, 6, 1)$ lies on line ℓ_9
 106 : $P_{2081} = (0, 1, 7, 1)$ lies on line ℓ_4
 107 : $P_{2087} = (6, 1, 7, 1)$ lies on line ℓ_7
 108 : $P_{2098} = (1, 2, 7, 1)$ lies on line ℓ_{10}
 109 : $P_{2101} = (4, 2, 7, 1)$ lies on line ℓ_{11}
 110 : $P_{2146} = (1, 5, 7, 1)$ lies on line ℓ_8
 111 : $P_{2148} = (3, 5, 7, 1)$ lies on line ℓ_9
 112 : $P_{2337} = (0, 1, 8, 1)$ lies on line ℓ_4
 113 : $P_{2346} = (9, 1, 8, 1)$ lies on line ℓ_7
 114 : $P_{2434} = (1, 7, 8, 1)$ lies on line ℓ_8
 115 : $P_{2447} = (14, 7, 8, 1)$ lies on line ℓ_9
 116 : $P_{2562} = (1, 15, 8, 1)$ lies on line ℓ_{10}
 117 : $P_{2567} = (6, 15, 8, 1)$ lies on line ℓ_{11}
 118 : $P_{2593} = (0, 1, 9, 1)$ lies on line ℓ_4
 119 : $P_{2601} = (8, 1, 9, 1)$ lies on line ℓ_7
 120 : $P_{2642} = (1, 4, 9, 1)$ lies on line ℓ_{10}
 121 : $P_{2653} = (12, 4, 9, 1)$ lies on line ℓ_{11}
 122 : $P_{2786} = (1, 13, 9, 1)$ lies on line ℓ_8
 123 : $P_{2790} = (5, 13, 9, 1)$ lies on line ℓ_9
 124 : $P_{2834} = (1, 0, 10, 1)$ lies on line ℓ_{10}
 125 : $P_{2844} = (11, 0, 10, 1)$ lies on line ℓ_{11}
 126 : $P_{2849} = (0, 1, 10, 1)$ lies on line ℓ_4

127 : $P_{2860} = (11, 1, 10, 1)$ lies on line ℓ_7
 128 : $P_{3090} = (1, 0, 11, 1)$ lies on line ℓ_8
 129 : $P_{3099} = (10, 0, 11, 1)$ lies on line ℓ_9
 130 : $P_{3105} = (0, 1, 11, 1)$ lies on line ℓ_4
 131 : $P_{3115} = (10, 1, 11, 1)$ lies on line ℓ_7
 132 : $P_{3361} = (0, 1, 12, 1)$ lies on line ℓ_4
 133 : $P_{3374} = (13, 1, 12, 1)$ lies on line ℓ_7
 134 : $P_{3410} = (1, 4, 12, 1)$ lies on line ℓ_8
 135 : $P_{3418} = (9, 4, 12, 1)$ lies on line ℓ_9
 136 : $P_{3474} = (1, 8, 12, 1)$ lies on line ℓ_{10}
 137 : $P_{3478} = (5, 8, 12, 1)$ lies on line ℓ_{11}
 138 : $P_{3617} = (0, 1, 13, 1)$ lies on line ℓ_4
 139 : $P_{3629} = (12, 1, 13, 1)$ lies on line ℓ_7
 140 : $P_{3650} = (1, 3, 13, 1)$ lies on line ℓ_{10}
 141 : $P_{3664} = (15, 3, 13, 1)$ lies on line ℓ_{11}
 142 : $P_{3826} = (1, 14, 13, 1)$ lies on line ℓ_8
 143 : $P_{3827} = (2, 14, 13, 1)$ lies on line ℓ_9
 144 : $P_{3873} = (0, 1, 14, 1)$ lies on line ℓ_4
 145 : $P_{3888} = (15, 1, 14, 1)$ lies on line ℓ_7
 146 : $P_{3970} = (1, 7, 14, 1)$ lies on line ℓ_{10}
 147 : $P_{3977} = (8, 7, 14, 1)$ lies on line ℓ_{11}
 148 : $P_{4002} = (1, 9, 14, 1)$ lies on line ℓ_8
 149 : $P_{4007} = (6, 9, 14, 1)$ lies on line ℓ_9
 150 : $P_{4129} = (0, 1, 15, 1)$ lies on line ℓ_4
 151 : $P_{4143} = (14, 1, 15, 1)$ lies on line ℓ_7
 152 : $P_{4162} = (1, 3, 15, 1)$ lies on line ℓ_8
 153 : $P_{4174} = (13, 3, 15, 1)$ lies on line ℓ_9
 154 : $P_{4306} = (1, 12, 15, 1)$ lies on line ℓ_{10}
 155 : $P_{4307} = (2, 12, 15, 1)$ lies on line ℓ_{11}

The single points on the surface are:

Points on surface but on no line

The surface has 144 points not on any line:

The points on the surface but not on lines are:

0 : $P_{826} = (9, 2, 2, 1)$
 1 : $P_{900} = (3, 7, 2, 1)$
 2 : $P_{903} = (6, 7, 2, 1)$
 3 : $P_{931} = (2, 9, 2, 1)$
 4 : $P_{938} = (9, 9, 2, 1)$
 5 : $P_{967} = (6, 11, 2, 1)$
 6 : $P_{976} = (15, 11, 2, 1)$
 7 : $P_{995} = (2, 13, 2, 1)$
 8 : $P_{1006} = (13, 13, 2, 1)$
 9 : $P_{1099} = (10, 3, 3, 1)$
 10 : $P_{1115} = (10, 4, 3, 1)$
 11 : $P_{1118} = (13, 4, 3, 1)$
 12 : $P_{1155} = (2, 7, 3, 1)$

13 : $P_{1159} = (6, 7, 3, 1)$
 14 : $P_{1205} = (4, 10, 3, 1)$
 15 : $P_{1214} = (13, 10, 3, 1)$
 16 : $P_{1240} = (7, 12, 3, 1)$
 17 : $P_{1241} = (8, 12, 3, 1)$
 18 : $P_{1255} = (6, 13, 3, 1)$
 19 : $P_{1257} = (8, 13, 3, 1)$
 20 : $P_{1375} = (14, 4, 4, 1)$
 21 : $P_{1413} = (4, 7, 4, 1)$
 22 : $P_{1416} = (7, 7, 4, 1)$
 23 : $P_{1460} = (3, 10, 4, 1)$
 24 : $P_{1470} = (13, 10, 4, 1)$
 25 : $P_{1494} = (5, 12, 4, 1)$

26 : $P_{1502} = (13, 12, 4, 1)$	80 : $P_{2778} = (9, 12, 9, 1)$
27 : $P_{1525} = (4, 14, 4, 1)$	81 : $P_{2781} = (12, 12, 9, 1)$
28 : $P_{1535} = (14, 14, 4, 1)$	82 : $P_{2884} = (3, 3, 10, 1)$
29 : $P_{1644} = (11, 5, 5, 1)$	83 : $P_{2891} = (10, 3, 10, 1)$
30 : $P_{1661} = (12, 6, 5, 1)$	84 : $P_{2900} = (3, 4, 10, 1)$
31 : $P_{1664} = (15, 6, 5, 1)$	85 : $P_{2910} = (13, 4, 10, 1)$
32 : $P_{1678} = (13, 7, 5, 1)$	86 : $P_{2969} = (8, 8, 10, 1)$
33 : $P_{1680} = (15, 7, 5, 1)$	87 : $P_{2971} = (10, 8, 10, 1)$
34 : $P_{1704} = (7, 9, 5, 1)$	88 : $P_{3021} = (12, 11, 10, 1)$
35 : $P_{1708} = (11, 9, 5, 1)$	89 : $P_{3022} = (13, 11, 10, 1)$
36 : $P_{1736} = (7, 11, 5, 1)$	90 : $P_{3065} = (8, 14, 10, 1)$
37 : $P_{1738} = (9, 11, 5, 1)$	91 : $P_{3069} = (12, 14, 10, 1)$
38 : $P_{1749} = (4, 12, 5, 1)$	92 : $P_{3127} = (6, 2, 11, 1)$
39 : $P_{1758} = (13, 12, 5, 1)$	93 : $P_{3136} = (15, 2, 11, 1)$
40 : $P_{1852} = (11, 2, 6, 1)$	94 : $P_{3174} = (5, 5, 11, 1)$
41 : $P_{1856} = (15, 2, 6, 1)$	95 : $P_{3180} = (11, 5, 11, 1)$
42 : $P_{1919} = (14, 6, 6, 1)$	96 : $P_{3238} = (5, 9, 11, 1)$
43 : $P_{1923} = (2, 7, 6, 1)$	97 : $P_{3240} = (7, 9, 11, 1)$
44 : $P_{1924} = (3, 7, 6, 1)$	98 : $P_{3255} = (6, 10, 11, 1)$
45 : $P_{1976} = (7, 10, 6, 1)$	99 : $P_{3256} = (7, 10, 11, 1)$
46 : $P_{1980} = (11, 10, 6, 1)$	100 : $P_{3340} = (11, 15, 11, 1)$
47 : $P_{1987} = (2, 11, 6, 1)$	101 : $P_{3344} = (15, 15, 11, 1)$
48 : $P_{2000} = (15, 11, 6, 1)$	102 : $P_{3446} = (5, 6, 12, 1)$
49 : $P_{2020} = (3, 13, 6, 1)$	103 : $P_{3456} = (15, 6, 12, 1)$
50 : $P_{2025} = (8, 13, 6, 1)$	104 : $P_{3513} = (8, 10, 12, 1)$
51 : $P_{2169} = (8, 6, 7, 1)$	105 : $P_{3519} = (14, 10, 12, 1)$
52 : $P_{2170} = (9, 6, 7, 1)$	106 : $P_{3531} = (10, 11, 12, 1)$
53 : $P_{2181} = (4, 7, 7, 1)$	107 : $P_{3534} = (13, 11, 12, 1)$
54 : $P_{2214} = (5, 9, 7, 1)$	108 : $P_{3546} = (9, 12, 12, 1)$
55 : $P_{2220} = (11, 9, 7, 1)$	109 : $P_{3567} = (14, 13, 12, 1)$
56 : $P_{2231} = (6, 10, 7, 1)$	110 : $P_{3568} = (15, 13, 12, 1)$
57 : $P_{2236} = (11, 10, 7, 1)$	111 : $P_{3577} = (8, 14, 12, 1)$
58 : $P_{2246} = (5, 11, 7, 1)$	112 : $P_{3579} = (10, 14, 12, 1)$
59 : $P_{2250} = (9, 11, 7, 1)$	113 : $P_{3668} = (3, 4, 13, 1)$
60 : $P_{2260} = (3, 12, 7, 1)$	114 : $P_{3675} = (10, 4, 13, 1)$
61 : $P_{2265} = (8, 12, 7, 1)$	115 : $P_{3718} = (5, 7, 13, 1)$
62 : $P_{2424} = (7, 6, 8, 1)$	116 : $P_{3728} = (15, 7, 13, 1)$
63 : $P_{2426} = (9, 6, 8, 1)$	117 : $P_{3764} = (3, 10, 13, 1)$
64 : $P_{2459} = (10, 8, 8, 1)$	118 : $P_{3765} = (4, 10, 13, 1)$
65 : $P_{2493} = (12, 10, 8, 1)$	119 : $P_{3787} = (10, 11, 13, 1)$
66 : $P_{2495} = (14, 10, 8, 1)$	120 : $P_{3789} = (12, 11, 13, 1)$
67 : $P_{2516} = (3, 12, 8, 1)$	121 : $P_{3797} = (4, 12, 13, 1)$
68 : $P_{2520} = (7, 12, 8, 1)$	122 : $P_{3798} = (5, 12, 13, 1)$
69 : $P_{2532} = (3, 13, 8, 1)$	123 : $P_{3811} = (2, 13, 13, 1)$
70 : $P_{2535} = (6, 13, 8, 1)$	124 : $P_{3925} = (4, 4, 14, 1)$
71 : $P_{2555} = (10, 14, 8, 1)$	125 : $P_{3935} = (14, 4, 14, 1)$
72 : $P_{2557} = (12, 14, 8, 1)$	126 : $P_{3959} = (6, 6, 14, 1)$
73 : $P_{2611} = (2, 2, 9, 1)$	127 : $P_{3967} = (14, 6, 14, 1)$
74 : $P_{2618} = (9, 2, 9, 1)$	128 : $P_{4025} = (8, 10, 14, 1)$
75 : $P_{2680} = (7, 6, 9, 1)$	129 : $P_{4029} = (12, 10, 14, 1)$
76 : $P_{2681} = (8, 6, 9, 1)$	130 : $P_{4077} = (12, 13, 14, 1)$
77 : $P_{2723} = (2, 9, 9, 1)$	131 : $P_{4080} = (15, 13, 14, 1)$
78 : $P_{2758} = (5, 11, 9, 1)$	132 : $P_{4085} = (4, 14, 14, 1)$
79 : $P_{2760} = (7, 11, 9, 1)$	133 : $P_{4151} = (6, 2, 15, 1)$

134 : $P_{4156} = (11, 2, 15, 1)$
 135 : $P_{4214} = (5, 6, 15, 1)$
 136 : $P_{4221} = (12, 6, 15, 1)$
 137 : $P_{4230} = (5, 7, 15, 1)$
 138 : $P_{4238} = (13, 7, 15, 1)$
 139 : $P_{4291} = (2, 11, 15, 1)$

140 : $P_{4295} = (6, 11, 15, 1)$
 141 : $P_{4333} = (12, 13, 15, 1)$
 142 : $P_{4335} = (14, 13, 15, 1)$
 143 : $P_{4364} = (11, 15, 15, 1)$

Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	1	1	0	1	1	0	0	0	0	0
1	1	0	1	0	0	0	0	1	0	1	0	1
2	1	1	0	0	1	0	0	0	1	0	1	0
3	1	0	0	0	1	0	0	1	1	1	1	1
4	0	0	1	1	0	1	1	1	0	1	0	1
5	1	0	0	0	1	0	1	1	0	1	1	0
6	1	0	0	0	1	1	0	1	1	0	0	1
7	0	1	0	1	1	1	1	0	1	0	1	0
8	0	0	1	1	0	0	1	1	0	1	1	0
9	0	1	0	1	1	1	0	0	1	0	0	1
10	0	0	1	1	0	1	0	1	1	0	0	1
11	0	1	0	1	1	0	1	0	0	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_5	ℓ_6
in point	P_5	P_1	P_0	P_{14}	P_{15}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_7	ℓ_9	ℓ_{11}
in point	P_5	P_{35}	P_{20}	P_{190}	P_{205}

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_4	ℓ_8	ℓ_{10}
in point	P_1	P_{35}	P_2	P_{179}	P_{195}

Line 3 intersects

Line	ℓ_0	ℓ_4	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}	ℓ_{11}
in point	P_0	P_{290}	P_{291}	P_{291}	P_{290}	P_{291}	P_{290}

Line 4 intersects

Line	ℓ_2	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_9	ℓ_{11}
in point	P_2	P_{290}	P_{546}	P_{546}	P_{546}	P_{290}	P_{290}

Line 5 intersects

Line	ℓ_0	ℓ_4	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}
in point	P_{14}	P_{546}	P_{546}	P_{546}	P_{716}	P_{690}

Line 6 intersects

Line	ℓ_0	ℓ_4	ℓ_5	ℓ_7	ℓ_8	ℓ_{11}
in point	P_{15}	P_{546}	P_{546}	P_{546}	P_{706}	P_{699}

Line 7 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_6	ℓ_8	ℓ_{10}
in point	P_{20}	P_{291}	P_{546}	P_{546}	P_{546}	P_{291}	P_{291}

Line 8 intersects

Line	ℓ_2	ℓ_3	ℓ_6	ℓ_7	ℓ_9	ℓ_{10}
in point	P_{179}	P_{291}	P_{706}	P_{291}	P_{2994}	P_{291}

Line 9 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_8	ℓ_{11}
in point	P_{190}	P_{290}	P_{290}	P_{716}	P_{2994}	P_{290}

Line 10 intersects

Line	ℓ_2	ℓ_3	ℓ_5	ℓ_7	ℓ_8	ℓ_{11}
in point	P_{195}	P_{291}	P_{690}	P_{291}	P_{291}	P_{3266}

Line 11 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_6	ℓ_9	ℓ_{10}
in point	P_{205}	P_{290}	P_{290}	P_{699}	P_{290}	P_{3266}

The surface has 321 points:

The points on the surface are:

0 : $P_0 = (1, 0, 0, 0)$	40 : $P_{211} = (0, 12, 1, 0)$	80 : $P_{669} = (12, 8, 1, 1)$
1 : $P_1 = (0, 1, 0, 0)$	41 : $P_{224} = (13, 12, 1, 0)$	81 : $P_{679} = (6, 9, 1, 1)$
2 : $P_2 = (0, 0, 1, 0)$	42 : $P_{227} = (0, 13, 1, 0)$	82 : $P_{687} = (14, 9, 1, 1)$
3 : $P_5 = (1, 1, 0, 0)$	43 : $P_{239} = (12, 13, 1, 0)$	83 : $P_{690} = (1, 10, 1, 1)$
4 : $P_6 = (2, 1, 0, 0)$	44 : $P_{243} = (0, 14, 1, 0)$	84 : $P_{699} = (10, 10, 1, 1)$
5 : $P_7 = (3, 1, 0, 0)$	45 : $P_{258} = (15, 14, 1, 0)$	85 : $P_{706} = (1, 11, 1, 1)$
6 : $P_8 = (4, 1, 0, 0)$	46 : $P_{259} = (0, 15, 1, 0)$	86 : $P_{716} = (11, 11, 1, 1)$
7 : $P_9 = (5, 1, 0, 0)$	47 : $P_{273} = (14, 15, 1, 0)$	87 : $P_{723} = (2, 12, 1, 1)$
8 : $P_{10} = (6, 1, 0, 0)$	48 : $P_{290} = (0, 1, 0, 1)$	88 : $P_{736} = (15, 12, 1, 1)$
9 : $P_{11} = (7, 1, 0, 0)$	49 : $P_{291} = (1, 1, 0, 1)$	89 : $P_{742} = (5, 13, 1, 1)$
10 : $P_{12} = (8, 1, 0, 0)$	50 : $P_{292} = (2, 1, 0, 1)$	90 : $P_{746} = (9, 13, 1, 1)$
11 : $P_{13} = (9, 1, 0, 0)$	51 : $P_{293} = (3, 1, 0, 1)$	91 : $P_{755} = (2, 14, 1, 1)$
12 : $P_{14} = (10, 1, 0, 0)$	52 : $P_{294} = (4, 1, 0, 1)$	92 : $P_{766} = (13, 14, 1, 1)$
13 : $P_{15} = (11, 1, 0, 0)$	53 : $P_{295} = (5, 1, 0, 1)$	93 : $P_{775} = (6, 15, 1, 1)$
14 : $P_{16} = (12, 1, 0, 0)$	54 : $P_{296} = (6, 1, 0, 1)$	94 : $P_{777} = (8, 15, 1, 1)$
15 : $P_{17} = (13, 1, 0, 0)$	55 : $P_{297} = (7, 1, 0, 1)$	95 : $P_{801} = (0, 1, 2, 1)$
16 : $P_{18} = (14, 1, 0, 0)$	56 : $P_{298} = (8, 1, 0, 1)$	96 : $P_{804} = (3, 1, 2, 1)$
17 : $P_{19} = (15, 1, 0, 0)$	57 : $P_{299} = (9, 1, 0, 1)$	97 : $P_{826} = (9, 2, 2, 1)$
18 : $P_{20} = (1, 0, 1, 0)$	58 : $P_{300} = (10, 1, 0, 1)$	98 : $P_{900} = (3, 7, 2, 1)$
19 : $P_{35} = (0, 1, 1, 0)$	59 : $P_{301} = (11, 1, 0, 1)$	99 : $P_{903} = (6, 7, 2, 1)$
20 : $P_{51} = (0, 2, 1, 0)$	60 : $P_{302} = (12, 1, 0, 1)$	100 : $P_{931} = (2, 9, 2, 1)$
21 : $P_{54} = (3, 2, 1, 0)$	61 : $P_{303} = (13, 1, 0, 1)$	101 : $P_{938} = (9, 9, 2, 1)$
22 : $P_{67} = (0, 3, 1, 0)$	62 : $P_{304} = (14, 1, 0, 1)$	102 : $P_{967} = (6, 11, 2, 1)$
23 : $P_{69} = (2, 3, 1, 0)$	63 : $P_{305} = (15, 1, 0, 1)$	103 : $P_{976} = (15, 11, 2, 1)$
24 : $P_{83} = (0, 4, 1, 0)$	64 : $P_{540} = (10, 0, 1, 1)$	104 : $P_{978} = (1, 12, 2, 1)$
25 : $P_{88} = (5, 4, 1, 0)$	65 : $P_{541} = (11, 0, 1, 1)$	105 : $P_{992} = (15, 12, 2, 1)$
26 : $P_{99} = (0, 5, 1, 0)$	66 : $P_{546} = (0, 1, 1, 1)$	106 : $P_{995} = (2, 13, 2, 1)$
27 : $P_{103} = (4, 5, 1, 0)$	67 : $P_{565} = (4, 2, 1, 1)$	107 : $P_{1006} = (13, 13, 2, 1)$
28 : $P_{115} = (0, 6, 1, 0)$	68 : $P_{568} = (7, 2, 1, 1)$	108 : $P_{1010} = (1, 14, 2, 1)$
29 : $P_{122} = (7, 6, 1, 0)$	69 : $P_{590} = (13, 3, 1, 1)$	109 : $P_{1022} = (13, 14, 2, 1)$
30 : $P_{131} = (0, 7, 1, 0)$	70 : $P_{592} = (15, 3, 1, 1)$	110 : $P_{1057} = (0, 1, 3, 1)$
31 : $P_{137} = (6, 7, 1, 0)$	71 : $P_{602} = (9, 4, 1, 1)$	111 : $P_{1059} = (2, 1, 3, 1)$
32 : $P_{147} = (0, 8, 1, 0)$	72 : $P_{605} = (12, 4, 1, 1)$	112 : $P_{1099} = (10, 3, 3, 1)$
33 : $P_{156} = (9, 8, 1, 0)$	73 : $P_{612} = (3, 5, 1, 1)$	113 : $P_{1115} = (10, 4, 3, 1)$
34 : $P_{163} = (0, 9, 1, 0)$	74 : $P_{616} = (7, 5, 1, 1)$	114 : $P_{1118} = (13, 4, 3, 1)$
35 : $P_{171} = (8, 9, 1, 0)$	75 : $P_{628} = (3, 6, 1, 1)$	115 : $P_{1122} = (1, 5, 3, 1)$
36 : $P_{179} = (0, 10, 1, 0)$	76 : $P_{629} = (4, 6, 1, 1)$	116 : $P_{1128} = (7, 5, 3, 1)$
37 : $P_{190} = (11, 10, 1, 0)$	77 : $P_{649} = (8, 7, 1, 1)$	117 : $P_{1138} = (1, 6, 3, 1)$
38 : $P_{195} = (0, 11, 1, 0)$	78 : $P_{655} = (14, 7, 1, 1)$	118 : $P_{1141} = (4, 6, 3, 1)$
39 : $P_{205} = (10, 11, 1, 0)$	79 : $P_{662} = (5, 8, 1, 1)$	119 : $P_{1155} = (2, 7, 3, 1)$

120 : $P_{1159} = (6, 7, 3, 1)$	174 : $P_{2050} = (1, 15, 6, 1)$	228 : $P_{2860} = (11, 1, 10, 1)$
121 : $P_{1205} = (4, 10, 3, 1)$	175 : $P_{2057} = (8, 15, 6, 1)$	229 : $P_{2884} = (3, 3, 10, 1)$
122 : $P_{1214} = (13, 10, 3, 1)$	176 : $P_{2081} = (0, 1, 7, 1)$	230 : $P_{2891} = (10, 3, 10, 1)$
123 : $P_{1240} = (7, 12, 3, 1)$	177 : $P_{2087} = (6, 1, 7, 1)$	231 : $P_{2900} = (3, 4, 10, 1)$
124 : $P_{1241} = (8, 12, 3, 1)$	178 : $P_{2098} = (1, 2, 7, 1)$	232 : $P_{2910} = (13, 4, 10, 1)$
125 : $P_{1255} = (6, 13, 3, 1)$	179 : $P_{2101} = (4, 2, 7, 1)$	233 : $P_{2969} = (8, 8, 10, 1)$
126 : $P_{1257} = (8, 13, 3, 1)$	180 : $P_{2146} = (1, 5, 7, 1)$	234 : $P_{2971} = (10, 8, 10, 1)$
127 : $P_{1313} = (0, 1, 4, 1)$	181 : $P_{2148} = (3, 5, 7, 1)$	235 : $P_{2994} = (1, 10, 10, 1)$
128 : $P_{1318} = (5, 1, 4, 1)$	182 : $P_{2169} = (8, 6, 7, 1)$	236 : $P_{3021} = (12, 11, 10, 1)$
129 : $P_{1330} = (1, 2, 4, 1)$	183 : $P_{2170} = (9, 6, 7, 1)$	237 : $P_{3022} = (13, 11, 10, 1)$
130 : $P_{1336} = (7, 2, 4, 1)$	184 : $P_{2181} = (4, 7, 7, 1)$	238 : $P_{3065} = (8, 14, 10, 1)$
131 : $P_{1375} = (14, 4, 4, 1)$	185 : $P_{2214} = (5, 9, 7, 1)$	239 : $P_{3069} = (12, 14, 10, 1)$
132 : $P_{1394} = (1, 6, 4, 1)$	186 : $P_{2220} = (11, 9, 7, 1)$	240 : $P_{3090} = (1, 0, 11, 1)$
133 : $P_{1396} = (3, 6, 4, 1)$	187 : $P_{2231} = (6, 10, 7, 1)$	241 : $P_{3099} = (10, 0, 11, 1)$
134 : $P_{1413} = (4, 7, 4, 1)$	188 : $P_{2236} = (11, 10, 7, 1)$	242 : $P_{3105} = (0, 1, 11, 1)$
135 : $P_{1416} = (7, 7, 4, 1)$	189 : $P_{2246} = (5, 11, 7, 1)$	243 : $P_{3115} = (10, 1, 11, 1)$
136 : $P_{1460} = (3, 10, 4, 1)$	190 : $P_{2250} = (9, 11, 7, 1)$	244 : $P_{3127} = (6, 2, 11, 1)$
137 : $P_{1470} = (13, 10, 4, 1)$	191 : $P_{2260} = (3, 12, 7, 1)$	245 : $P_{3136} = (15, 2, 11, 1)$
138 : $P_{1494} = (5, 12, 4, 1)$	192 : $P_{2265} = (8, 12, 7, 1)$	246 : $P_{3174} = (5, 5, 11, 1)$
139 : $P_{1502} = (13, 12, 4, 1)$	193 : $P_{2337} = (0, 1, 8, 1)$	247 : $P_{3180} = (11, 5, 11, 1)$
140 : $P_{1525} = (4, 14, 4, 1)$	194 : $P_{2346} = (9, 1, 8, 1)$	248 : $P_{3238} = (5, 9, 11, 1)$
141 : $P_{1535} = (14, 14, 4, 1)$	195 : $P_{2424} = (7, 6, 8, 1)$	249 : $P_{3240} = (7, 9, 11, 1)$
142 : $P_{1569} = (0, 1, 5, 1)$	196 : $P_{2426} = (9, 6, 8, 1)$	250 : $P_{3255} = (6, 10, 11, 1)$
143 : $P_{1573} = (4, 1, 5, 1)$	197 : $P_{2434} = (1, 7, 8, 1)$	251 : $P_{3256} = (7, 10, 11, 1)$
144 : $P_{1644} = (11, 5, 5, 1)$	198 : $P_{2447} = (14, 7, 8, 1)$	252 : $P_{3266} = (1, 11, 11, 1)$
145 : $P_{1661} = (12, 6, 5, 1)$	199 : $P_{2459} = (10, 8, 8, 1)$	253 : $P_{3340} = (11, 15, 11, 1)$
146 : $P_{1664} = (15, 6, 5, 1)$	200 : $P_{2493} = (12, 10, 8, 1)$	254 : $P_{3344} = (15, 15, 11, 1)$
147 : $P_{1678} = (13, 7, 5, 1)$	201 : $P_{2495} = (14, 10, 8, 1)$	255 : $P_{3361} = (0, 1, 12, 1)$
148 : $P_{1680} = (15, 7, 5, 1)$	202 : $P_{2516} = (3, 12, 8, 1)$	256 : $P_{3374} = (13, 1, 12, 1)$
149 : $P_{1682} = (1, 8, 5, 1)$	203 : $P_{2520} = (7, 12, 8, 1)$	257 : $P_{3410} = (1, 4, 12, 1)$
150 : $P_{1693} = (12, 8, 5, 1)$	204 : $P_{2532} = (3, 13, 8, 1)$	258 : $P_{3418} = (9, 4, 12, 1)$
151 : $P_{1704} = (7, 9, 5, 1)$	205 : $P_{2535} = (6, 13, 8, 1)$	259 : $P_{3446} = (5, 6, 12, 1)$
152 : $P_{1708} = (11, 9, 5, 1)$	206 : $P_{2555} = (10, 14, 8, 1)$	260 : $P_{3456} = (15, 6, 12, 1)$
153 : $P_{1736} = (7, 11, 5, 1)$	207 : $P_{2557} = (12, 14, 8, 1)$	261 : $P_{3474} = (1, 8, 12, 1)$
154 : $P_{1738} = (9, 11, 5, 1)$	208 : $P_{2562} = (1, 15, 8, 1)$	262 : $P_{3478} = (5, 8, 12, 1)$
155 : $P_{1749} = (4, 12, 5, 1)$	209 : $P_{2567} = (6, 15, 8, 1)$	263 : $P_{3513} = (8, 10, 12, 1)$
156 : $P_{1758} = (13, 12, 5, 1)$	210 : $P_{2593} = (0, 1, 9, 1)$	264 : $P_{3519} = (14, 10, 12, 1)$
157 : $P_{1762} = (1, 13, 5, 1)$	211 : $P_{2601} = (8, 1, 9, 1)$	265 : $P_{3531} = (10, 11, 12, 1)$
158 : $P_{1770} = (9, 13, 5, 1)$	212 : $P_{2611} = (2, 2, 9, 1)$	266 : $P_{3534} = (13, 11, 12, 1)$
159 : $P_{1825} = (0, 1, 6, 1)$	213 : $P_{2618} = (9, 2, 9, 1)$	267 : $P_{3546} = (9, 12, 12, 1)$
160 : $P_{1832} = (7, 1, 6, 1)$	214 : $P_{2642} = (1, 4, 9, 1)$	268 : $P_{3567} = (14, 13, 12, 1)$
161 : $P_{1852} = (11, 2, 6, 1)$	215 : $P_{2653} = (12, 4, 9, 1)$	269 : $P_{3568} = (15, 13, 12, 1)$
162 : $P_{1856} = (15, 2, 6, 1)$	216 : $P_{2680} = (7, 6, 9, 1)$	270 : $P_{3577} = (8, 14, 12, 1)$
163 : $P_{1919} = (14, 6, 6, 1)$	217 : $P_{2681} = (8, 6, 9, 1)$	271 : $P_{3579} = (10, 14, 12, 1)$
164 : $P_{1923} = (2, 7, 6, 1)$	218 : $P_{2723} = (2, 9, 9, 1)$	272 : $P_{3617} = (0, 1, 13, 1)$
165 : $P_{1924} = (3, 7, 6, 1)$	219 : $P_{2758} = (5, 11, 9, 1)$	273 : $P_{3629} = (12, 1, 13, 1)$
166 : $P_{1954} = (1, 9, 6, 1)$	220 : $P_{2760} = (7, 11, 9, 1)$	274 : $P_{3650} = (1, 3, 13, 1)$
167 : $P_{1967} = (14, 9, 6, 1)$	221 : $P_{2778} = (9, 12, 9, 1)$	275 : $P_{3664} = (15, 3, 13, 1)$
168 : $P_{1976} = (7, 10, 6, 1)$	222 : $P_{2781} = (12, 12, 9, 1)$	276 : $P_{3668} = (3, 4, 13, 1)$
169 : $P_{1980} = (11, 10, 6, 1)$	223 : $P_{2786} = (1, 13, 9, 1)$	277 : $P_{3675} = (10, 4, 13, 1)$
170 : $P_{1987} = (2, 11, 6, 1)$	224 : $P_{2790} = (5, 13, 9, 1)$	278 : $P_{3718} = (5, 7, 13, 1)$
171 : $P_{2000} = (15, 11, 6, 1)$	225 : $P_{2834} = (1, 0, 10, 1)$	279 : $P_{3728} = (15, 7, 13, 1)$
172 : $P_{2020} = (3, 13, 6, 1)$	226 : $P_{2844} = (11, 0, 10, 1)$	280 : $P_{3764} = (3, 10, 13, 1)$
173 : $P_{2025} = (8, 13, 6, 1)$	227 : $P_{2849} = (0, 1, 10, 1)$	281 : $P_{3765} = (4, 10, 13, 1)$

282 : $P_{3787} = (10, 11, 13, 1)$	296 : $P_{3977} = (8, 7, 14, 1)$	310 : $P_{4214} = (5, 6, 15, 1)$
283 : $P_{3789} = (12, 11, 13, 1)$	297 : $P_{4002} = (1, 9, 14, 1)$	311 : $P_{4221} = (12, 6, 15, 1)$
284 : $P_{3797} = (4, 12, 13, 1)$	298 : $P_{4007} = (6, 9, 14, 1)$	312 : $P_{4230} = (5, 7, 15, 1)$
285 : $P_{3798} = (5, 12, 13, 1)$	299 : $P_{4025} = (8, 10, 14, 1)$	313 : $P_{4238} = (13, 7, 15, 1)$
286 : $P_{3811} = (2, 13, 13, 1)$	300 : $P_{4029} = (12, 10, 14, 1)$	314 : $P_{4291} = (2, 11, 15, 1)$
287 : $P_{3826} = (1, 14, 13, 1)$	301 : $P_{4077} = (12, 13, 14, 1)$	315 : $P_{4295} = (6, 11, 15, 1)$
288 : $P_{3827} = (2, 14, 13, 1)$	302 : $P_{4080} = (15, 13, 14, 1)$	316 : $P_{4306} = (1, 12, 15, 1)$
289 : $P_{3873} = (0, 1, 14, 1)$	303 : $P_{4085} = (4, 14, 14, 1)$	317 : $P_{4307} = (2, 12, 15, 1)$
290 : $P_{3888} = (15, 1, 14, 1)$	304 : $P_{4129} = (0, 1, 15, 1)$	318 : $P_{4333} = (12, 13, 15, 1)$
291 : $P_{3925} = (4, 4, 14, 1)$	305 : $P_{4143} = (14, 1, 15, 1)$	319 : $P_{4335} = (14, 13, 15, 1)$
292 : $P_{3935} = (14, 4, 14, 1)$	306 : $P_{4151} = (6, 2, 15, 1)$	320 : $P_{4364} = (11, 15, 15, 1)$
293 : $P_{3959} = (6, 6, 14, 1)$	307 : $P_{4156} = (11, 2, 15, 1)$	
294 : $P_{3967} = (14, 6, 14, 1)$	308 : $P_{4162} = (1, 3, 15, 1)$	
295 : $P_{3970} = (1, 7, 14, 1)$	309 : $P_{4174} = (13, 3, 15, 1)$	