Rank-67115 over GF(32)

January 15, 2021

The equation

The equation of the surface is:

$$X_3^3 + X_0^2 X_2 + X_1^2 X_3 + X_0 X_2^2 + X_0 X_1 X_2 = 0$$

(0, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0) The point rank of the equation over $\mathrm{GF}(32)$ is 1141965861

General information

Number of lines	6
Number of points	1089
Number of singular points	3
Number of Eckardt points	0
Number of double points	9
Number of single points	180
Number of points off lines	900
Number of Hesse planes	0
Number of axes	0
Type of points on lines	33^{6}
Type of lines on points	$2^9, 1^{180}, 0^{900}$

Singular Points

The surface has 3 singular points:

0:
$$P_{1090} = \mathbf{P}(0, 1, 0, 1) = \mathbf{P}(0, 1, 0, 1)$$

1: $P_{1091} = \mathbf{P}(1, 1, 0, 1) = \mathbf{P}(1, 1, 0, 1)$
2: $P_{2114} = \mathbf{P}(0, 1, 1, 1) = \mathbf{P}(0, 1, 1, 1)$

The 6 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}_0 = \mathbf{Pl}(1, 0, 0, 0, 0, 0)_0$$

$$\ell_1 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{1058} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{1058} = \mathbf{Pl}(1, 0, 1, 0, 0, 1)_{34913}$$

$$\ell_2 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1082368} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1082368} = \mathbf{Pl}(0, 0, 0, 0, 0, 1)_{34849}$$

$$\ell_3 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{32} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{32} = \mathbf{Pl}(1, 0, 0, 0, 1, 0)_{1090}$$

$$\ell_4 = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1082401} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}_{1082401} = \mathbf{Pl}(0, 1, 0, 0, 0, 1)_{34881}$$

$$\ell_5 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{1090} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \end{bmatrix}_{1090} = \mathbf{Pl}(1, 1, 1, 0, 1, 1)_{68640}$$

Rank of lines: (0, 1058, 1082368, 32, 1082401, 1090)

Rank of points on Klein quadric: (0, 34913, 34849, 1090, 34881, 68640)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 9 Double points: The double points on the surface are:

$P_5 = (1, 1, 0, 0) = \ell_0 \cap \ell_1$
$P_1 = (0, 1, 0, 0) = \ell_0 \cap \ell_2$
$P_0 = (1, 0, 0, 0) = \ell_0 \cap \ell_3$
$P_{67} = (0, 1, 1, 0) = \ell_1 \cap \ell_2$
$P_{36} = (1,0,1,0) = \ell_1 \cap \ell_5$

$$P_2 = (0,0,1,0) = \ell_2 \cap \ell_4$$

$$P_{1090} = (0,1,0,1) = \ell_3 \cap \ell_4$$

$$P_{1091} = (1,1,0,1) = \ell_3 \cap \ell_5$$

$$P_{2114} = (0,1,1,1) = \ell_4 \cap \ell_5$$

Single Points

The surface has 180 single points: The single points on the surface are:

 $\begin{array}{l} 0: \ P_6 = (2,1,0,0) \ \text{lies on line ℓ_0} \\ 1: \ P_7 = (3,1,0,0) \ \text{lies on line ℓ_0} \\ 2: \ P_8 = (4,1,0,0) \ \text{lies on line ℓ_0} \\ 3: \ P_9 = (5,1,0,0) \ \text{lies on line ℓ_0} \\ 4: \ P_{10} = (6,1,0,0) \ \text{lies on line ℓ_0} \\ 5: \ P_{11} = (7,1,0,0) \ \text{lies on line ℓ_0} \\ 6: \ P_{12} = (8,1,0,0) \ \text{lies on line ℓ_0} \\ 7: \ P_{13} = (9,1,0,0) \ \text{lies on line ℓ_0} \\ 8: \ P_{14} = (10,1,0,0) \ \text{lies on line ℓ_0} \\ 9: \ P_{15} = (11,1,0,0) \ \text{lies on line ℓ_0} \\ 10: \ P_{16} = (12,1,0,0) \ \text{lies on line ℓ_0} \\ 11: \ P_{17} = (13,1,0,0) \ \text{lies on line ℓ_0} \\ 12: \ P_{18} = (14,1,0,0) \ \text{lies on line ℓ_0} \\ 13: \ P_{19} = (15,1,0,0) \ \text{lies on line ℓ_0} \\ 14: \ P_{20} = (16,1,0,0) \ \text{lies on line ℓ_0} \\ \end{array}$

15: $P_{21} = (17, 1, 0, 0)$ lies on line ℓ_0 16: $P_{22} = (18, 1, 0, 0)$ lies on line ℓ_0 17: $P_{23} = (19, 1, 0, 0)$ lies on line ℓ_0 18: $P_{24} = (20, 1, 0, 0)$ lies on line ℓ_0 19: $P_{25} = (21, 1, 0, 0)$ lies on line ℓ_0 20: $P_{26} = (22, 1, 0, 0)$ lies on line ℓ_0 21: $P_{27} = (23, 1, 0, 0)$ lies on line ℓ_0 22: $P_{28} = (24, 1, 0, 0)$ lies on line ℓ_0 23: $P_{29} = (25, 1, 0, 0)$ lies on line ℓ_0 24: $P_{30} = (26, 1, 0, 0)$ lies on line ℓ_0 25: $P_{31} = (27, 1, 0, 0)$ lies on line ℓ_0 26: $P_{32} = (28, 1, 0, 0)$ lies on line ℓ_0 27: $P_{33} = (29, 1, 0, 0)$ lies on line ℓ_0 28: $P_{34} = (30, 1, 0, 0)$ lies on line ℓ_0 29: $P_{35} = (31, 1, 0, 0)$ lies on line ℓ_0

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30: P_{99} = (0, 2, 1, 0) lies on line \ell_2
                                                                      84: P_{963} = (0, 29, 1, 0) lies on line \ell_2
31: P_{102} = (3, 2, 1, 0) lies on line \ell_1
                                                                      85: P_{991} = (28, 29, 1, 0) lies on line \ell_1
32: P_{131} = (0,3,1,0) lies on line \ell_2
                                                                      86: P_{995} = (0, 30, 1, 0) lies on line \ell_2
33: P_{133} = (2, 3, 1, 0) lies on line \ell_1
                                                                      87: P_{1026} = (31, 30, 1, 0) lies on line \ell_1
34: P_{163} = (0, 4, 1, 0) lies on line \ell_2
                                                                      88: P_{1027} = (0, 31, 1, 0) lies on line \ell_2
35: P_{168} = (5, 4, 1, 0) lies on line \ell_1
                                                                      89: P_{1057} = (30, 31, 1, 0) lies on line \ell_1
                                                                      90: P_{1092} = (2, 1, 0, 1) lies on line \ell_3
36: P_{195} = (0, 5, 1, 0) lies on line \ell_2
37: P_{199} = (4,5,1,0) lies on line \ell_1
                                                                      91: P_{1093} = (3, 1, 0, 1) lies on line \ell_3
38: P_{227} = (0, 6, 1, 0) lies on line \ell_2
                                                                      92: P_{1094} = (4, 1, 0, 1) lies on line \ell_3
39: P_{234} = (7,6,1,0) lies on line \ell_1
                                                                      93: P_{1095} = (5, 1, 0, 1) lies on line \ell_3
40: P_{259} = (0,7,1,0) lies on line \ell_2
                                                                      94: P_{1096} = (6, 1, 0, 1) lies on line \ell_3
                                                                      95: P_{1097} = (7, 1, 0, 1) lies on line \ell_3
41: P_{265} = (6, 7, 1, 0) lies on line \ell_1
42: P_{291} = (0, 8, 1, 0) lies on line \ell_2
                                                                      96: P_{1098} = (8, 1, 0, 1) lies on line \ell_3
43: P_{300} = (9, 8, 1, 0) lies on line \ell_1
                                                                      97: P_{1099} = (9, 1, 0, 1) lies on line \ell_3
                                                                      98 : P_{1100} = (10, 1, 0, 1) lies on line \ell_3
44: P_{323} = (0, 9, 1, 0) lies on line \ell_2
45: P_{331} = (8, 9, 1, 0) lies on line \ell_1
                                                                      99: P_{1101} = (11, 1, 0, 1) lies on line \ell_3
46: P_{355} = (0, 10, 1, 0) lies on line \ell_2
                                                                      100: P_{1102} = (12, 1, 0, 1) lies on line \ell_3
47: P_{366} = (11, 10, 1, 0) lies on line \ell_1
                                                                      101: P_{1103} = (13, 1, 0, 1) lies on line \ell_3
48: P_{387} = (0, 11, 1, 0) lies on line \ell_2
                                                                      102: P_{1104} = (14, 1, 0, 1) lies on line \ell_3
49: P_{397} = (10, 11, 1, 0) lies on line \ell_1
                                                                      103: P_{1105} = (15, 1, 0, 1) lies on line \ell_3
50: P_{419} = (0, 12, 1, 0) lies on line \ell_2
                                                                      104: P_{1106} = (16, 1, 0, 1) lies on line \ell_3
51: P_{432} = (13, 12, 1, 0) lies on line \ell_1
                                                                      105: P_{1107} = (17, 1, 0, 1) lies on line \ell_3
52: P_{451} = (0, 13, 1, 0) lies on line \ell_2
                                                                      106: P_{1108} = (18, 1, 0, 1) lies on line \ell_3
53: P_{463} = (12, 13, 1, 0) lies on line \ell_1
                                                                      107: P_{1109} = (19, 1, 0, 1) lies on line \ell_3
54: P_{483} = (0, 14, 1, 0) lies on line \ell_2
                                                                      108: P_{1110} = (20, 1, 0, 1) lies on line \ell_3
55: P_{498} = (15, 14, 1, 0) lies on line \ell_1
                                                                      109: P_{1111} = (21, 1, 0, 1) lies on line \ell_3
56: P_{515} = (0, 15, 1, 0) lies on line \ell_2
                                                                      110: P_{1112} = (22, 1, 0, 1) lies on line \ell_3
57: P_{529} = (14, 15, 1, 0) lies on line \ell_1
                                                                      111: P_{1113} = (23, 1, 0, 1) lies on line \ell_3
58: P_{547} = (0, 16, 1, 0) lies on line \ell_2
                                                                      112: P_{1114} = (24, 1, 0, 1) lies on line \ell_3
59: P_{564} = (17, 16, 1, 0) lies on line \ell_1
                                                                      113: P_{1115} = (25, 1, 0, 1) lies on line \ell_3
60: P_{579} = (0, 17, 1, 0) lies on line \ell_2
                                                                      114: P_{1116} = (26, 1, 0, 1) lies on line \ell_3
61: P_{595} = (16, 17, 1, 0) lies on line \ell_1
                                                                      115: P_{1117} = (27, 1, 0, 1) lies on line \ell_3
62: P_{611} = (0, 18, 1, 0) lies on line \ell_2
                                                                      116: P_{1118} = (28, 1, 0, 1) lies on line \ell_3
63: P_{630} = (19, 18, 1, 0) lies on line \ell_1
                                                                      117: P_{1119} = (29, 1, 0, 1) lies on line \ell_3
64: P_{643} = (0, 19, 1, 0) lies on line \ell_2
                                                                      118: P_{1120} = (30, 1, 0, 1) lies on line \ell_3
65: P_{661} = (18, 19, 1, 0) lies on line \ell_1
                                                                      119: P_{1121} = (31, 1, 0, 1) lies on line \ell_3
66: P_{675} = (0, 20, 1, 0) lies on line \ell_2
                                                                      120: P_{3137} = (0, 1, 2, 1) lies on line \ell_4
67: P_{696} = (21, 20, 1, 0) lies on line \ell_1
                                                                      121: P_{3140} = (3, 1, 2, 1) lies on line \ell_5
68: P_{707} = (0, 21, 1, 0) lies on line \ell_2
                                                                      122: P_{4161} = (0, 1, 3, 1) lies on line \ell_4
69: P_{727} = (20, 21, 1, 0) lies on line \ell_1
                                                                      123: P_{4163} = (2, 1, 3, 1) lies on line \ell_5
70: P_{739} = (0, 22, 1, 0) lies on line \ell_2
                                                                      124: P_{5185} = (0, 1, 4, 1) lies on line \ell_4
71: P_{762} = (23, 22, 1, 0) lies on line \ell_1
                                                                      125: P_{5190} = (5, 1, 4, 1) lies on line \ell_5
72: P_{771} = (0, 23, 1, 0) lies on line \ell_2
                                                                      126: P_{6209} = (0, 1, 5, 1) lies on line \ell_4
73: P_{793} = (22, 23, 1, 0) lies on line \ell_1
                                                                      127: P_{6213} = (4, 1, 5, 1) lies on line \ell_5
74: P_{803} = (0, 24, 1, 0) lies on line \ell_2
                                                                      128: P_{7233} = (0, 1, 6, 1) lies on line \ell_4
75: P_{828} = (25, 24, 1, 0) lies on line \ell_1
                                                                      129: P_{7240} = (7, 1, 6, 1) lies on line \ell_5
76: P_{835} = (0, 25, 1, 0) lies on line \ell_2
                                                                      130: P_{8257} = (0, 1, 7, 1) lies on line \ell_4
77: P_{859} = (24, 25, 1, 0) lies on line \ell_1
                                                                      131: P_{8263} = (6, 1, 7, 1) lies on line \ell_5
78: P_{867} = (0, 26, 1, 0) lies on line \ell_2
                                                                      132: P_{9281} = (0, 1, 8, 1) lies on line \ell_4
79: P_{894} = (27, 26, 1, 0) lies on line \ell_1
                                                                      133: P_{9290} = (9, 1, 8, 1) lies on line \ell_5
80: P_{899} = (0, 27, 1, 0) lies on line \ell_2
                                                                      134: P_{10305} = (0, 1, 9, 1) lies on line \ell_4
81: P_{925} = (26, 27, 1, 0) lies on line \ell_1
                                                                      135: P_{10313} = (8, 1, 9, 1) lies on line \ell_5
                                                                      136 : P_{11329} = (0, 1, 10, 1) lies on line \ell_4
82: P_{931} = (0, 28, 1, 0) lies on line \ell_2
83: P_{960} = (29, 28, 1, 0) lies on line \ell_1
                                                                      137: P_{11340} = (11, 1, 10, 1) lies on line \ell_5
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138: P_{12353} = (0, 1, 11, 1) lies on line \ell_4
                                                                     160: P_{23617} = (0, 1, 22, 1) lies on line \ell_4
139 : P_{12363} = (10, 1, 11, 1) lies on line \ell_5
                                                                     161: P_{23640} = (23, 1, 22, 1) lies on line \ell_5
140: P_{13377} = (0, 1, 12, 1) lies on line \ell_4
                                                                     162: P_{24641} = (0, 1, 23, 1) lies on line \ell_4
141 : P_{13390} = (13, 1, 12, 1) lies on line \ell_5
                                                                     163: P_{24663} = (22, 1, 23, 1) lies on line \ell_5
142: P_{14401} = (0, 1, 13, 1) lies on line \ell_4
                                                                     164: P_{25665} = (0, 1, 24, 1) lies on line \ell_4
143: P_{14413} = (12, 1, 13, 1) lies on line \ell_5
                                                                     165: P_{25690} = (25, 1, 24, 1) lies on line \ell_5
144: P_{15425} = (0, 1, 14, 1) lies on line \ell_4
                                                                     166: P_{26689} = (0, 1, 25, 1) lies on line \ell_4
145: P_{15440} = (15, 1, 14, 1) lies on line \ell_5
                                                                     167: P_{26713} = (24, 1, 25, 1) lies on line \ell_5
146: P_{16449} = (0, 1, 15, 1) lies on line \ell_4
                                                                     168: P_{27713} = (0, 1, 26, 1) lies on line \ell_4
147: P_{16463} = (14, 1, 15, 1) lies on line \ell_5
                                                                     169: P_{27740} = (27, 1, 26, 1) lies on line \ell_5
148: P_{17473} = (0, 1, 16, 1) lies on line \ell_4
                                                                     170: P_{28737} = (0, 1, 27, 1) lies on line \ell_4
                                                                     171 : P_{28763} = (26, 1, 27, 1) lies on line \ell_5
149: P_{17490} = (17, 1, 16, 1) lies on line \ell_5
150: P_{18497} = (0, 1, 17, 1) lies on line \ell_4
                                                                     172: P_{29761} = (0, 1, 28, 1) lies on line \ell_4
151: P_{18513} = (16, 1, 17, 1) lies on line \ell_5
                                                                     173: P_{29790} = (29, 1, 28, 1) lies on line \ell_5
152: P_{19521} = (0, 1, 18, 1) lies on line \ell_4
                                                                     174: P_{30785} = (0, 1, 29, 1) lies on line \ell_4
153: P_{19540} = (19, 1, 18, 1) lies on line \ell_5
                                                                     175: P_{30813} = (28, 1, 29, 1) lies on line \ell_5
                                                                     176 : P_{31809} = (0, 1, 30, 1) lies on line \ell_4
154: P_{20545} = (0, 1, 19, 1) lies on line \ell_4
155: P_{20563} = (18, 1, 19, 1) lies on line \ell_5
                                                                     177: P_{31840} = (31, 1, 30, 1) lies on line \ell_5
156: P_{21569} = (0, 1, 20, 1) lies on line \ell_4
                                                                     178: P_{32833} = (0, 1, 31, 1) lies on line \ell_4
157: P_{21590} = (21, 1, 20, 1) lies on line \ell_5
                                                                     179: P_{32863} = (30, 1, 31, 1) lies on line \ell_5
158: P_{22593} = (0, 1, 21, 1) lies on line \ell_4
159: P_{22613} = (20, 1, 21, 1) lies on line \ell_5
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The single points on the surface are:

Points on surface but on no line

The surface has 900 points not on any line: The points on the surface but not on lines are:

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0: P_{3129} = (24, 0, 2, 1)
                                                                  22: P_{3738} = (25, 19, 2, 1)
1: P_{3131} = (26, 0, 2, 1)
                                                                 23: P_{3792} = (15, 21, 2, 1)
2: P_{3173} = (4, 2, 2, 1)
                                                                 24: P_{3801} = (24, 21, 2, 1)
3: P_{3209} = (8, 3, 2, 1)
                                                                 25: P_{3971} = (2, 27, 2, 1)
4: P_{3210} = (9, 3, 2, 1)
                                                                 26: P_{3996} = (27, 27, 2, 1)
5: P_{3258} = (25, 4, 2, 1)
                                                                 27: P_{4099} = (2, 31, 2, 1)
6: P_{3264} = (31, 4, 2, 1)
                                                                 28: P_{4128} = (31, 31, 2, 1)
7: P_{3332} = (3,7,2,1)
                                                                 29: P_{4133} = (4, 0, 3, 1)
8: P_{3335} = (6,7,2,1)
                                                                 30: P_{4136} = (7,0,3,1)
9: P_{3378} = (17, 8, 2, 1)
                                                                 31: P_{4240} = (15, 3, 3, 1)
                                                                 32: P_{4283} = (26, 4, 3, 1)
10: P_{3388} = (27, 8, 2, 1)
                                                                 33: P_{4286} = (29, 4, 3, 1)
11: P_{3429} = (4, 10, 2, 1)
12: P_{3437} = (12, 10, 2, 1)
                                                                 34: P_{4345} = (24, 6, 3, 1)
                                                                 35: P_{4350} = (29, 6, 3, 1)
13: P_{3463} = (6, 11, 2, 1)
14: P_{3472} = (15, 11, 2, 1)
                                                                 36: P_{4355} = (2,7,3,1)
15: P_{3602} = (17, 15, 2, 1)
                                                                 37: P_{4359} = (6,7,3,1)
16: P_{3613} = (28, 15, 2, 1)
                                                                 38: P_{4424} = (7, 9, 3, 1)
                                                                 39: P_{4430} = (13, 9, 3, 1)
17: P_{3658} = (9, 17, 2, 1)
18: P_{3675} = (26, 17, 2, 1)
                                                                 40: P_{4497} = (16, 11, 3, 1)
19: P_{3693} = (12, 18, 2, 1)
                                                                 41: P_{4505} = (24, 11, 3, 1)
20: P_{3709} = (28, 18, 2, 1)
                                                                 42: P_{4517} = (4, 12, 3, 1)
                                                                 43: P_{4524} = (11, 12, 3, 1)
21: P_{3721} = (8, 19, 2, 1)
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44: P_{4551} = (6, 13, 3, 1)
                                                                 98: P_{6610} = (17, 13, 5, 1)
                                                                 99: P_{6618} = (25, 13, 5, 1)
45: P_{4553} = (8, 13, 3, 1)
46: P_{4631} = (22, 15, 3, 1)
                                                                 100: P_{6664} = (7, 15, 5, 1)
47: P_{4635} = (26, 15, 3, 1)
                                                                 101: P_{6670} = (13, 15, 5, 1)
48: P_{4646} = (5, 16, 3, 1)
                                                                 102: P_{6692} = (3, 16, 5, 1)
49: P_{4663} = (22, 16, 3, 1)
                                                                 103: P_{6711} = (22, 16, 5, 1)
50: P_{4684} = (11, 17, 3, 1)
                                                                 104: P_{6759} = (6, 18, 5, 1)
51: P_{4698} = (25, 17, 3, 1)
                                                                 105: P_{6770} = (17, 18, 5, 1)
52: P_{4720} = (15, 18, 3, 1)
                                                                 106: P_{6798} = (13, 19, 5, 1)
53: P_{4735} = (30, 18, 3, 1)
                                                                 107: P_{6812} = (27, 19, 5, 1)
54: P_{4809} = (8, 21, 3, 1)
                                                                 108: P_{6824} = (7, 20, 5, 1)
55: P_{4831} = (30, 21, 3, 1)
                                                                 109: P_{6839} = (22, 20, 5, 1)
                                                                 110: P_{6853} = (4, 21, 5, 1)
56: P_{5102} = (13, 30, 3, 1)
57: P_{5105} = (16, 30, 3, 1)
                                                                 111: P_{6869} = (20, 21, 5, 1)
58: P_{5126} = (5, 31, 3, 1)
                                                                 112: P_{7024} = (15, 26, 5, 1)
59: P_{5146} = (25, 31, 3, 1)
                                                                 113: P_{7025} = (16, 26, 5, 1)
60: P_{5156} = (3, 0, 4, 1)
                                                                 114: P_{7051} = (10, 27, 5, 1)
61: P_{5160} = (7, 0, 4, 1)
                                                                 115: P_{7061} = (20, 27, 5, 1)
                                                                 116: P_{7083} = (10, 28, 5, 1)
62: P_{5219} = (2, 2, 4, 1)
63: P_{5221} = (4, 2, 4, 1)
                                                                 117: P_{7092} = (19, 28, 5, 1)
64: P_{5297} = (16, 4, 4, 1)
                                                                 118: P_{7172} = (3, 31, 5, 1)
65: P_{5323} = (10, 5, 4, 1)
                                                                 119: P_{7194} = (25, 31, 5, 1)
                                                                 120: P_{7316} = (19, 3, 6, 1)
66: P_{5324} = (11, 5, 4, 1)
67: P_{5415} = (6, 8, 4, 1)
                                                                 121: P_{7319} = (22, 3, 6, 1)
68: P_{5419} = (10, 8, 4, 1)
                                                                 122: P_{7412} = (19, 6, 6, 1)
69: P_{5464} = (23, 9, 4, 1)
                                                                 123: P_{7427} = (2, 7, 6, 1)
                                                                 124: P_{7428} = (3, 7, 6, 1)
70: P_{5467} = (26, 9, 4, 1)
71: P_{5475} = (2, 10, 4, 1)
                                                                 125: P_{7461} = (4, 8, 6, 1)
72: P_{5485} = (12, 10, 4, 1)
                                                                 126: P_{7467} = (10, 8, 6, 1)
73: P_{5540} = (3, 12, 4, 1)
                                                                 127: P_{7555} = (2, 11, 6, 1)
74: P_{5548} = (11, 12, 4, 1)
                                                                 128: P_{7568} = (15, 11, 6, 1)
75: P_{5617} = (16, 14, 4, 1)
                                                                 129: P_{7590} = (5, 12, 6, 1)
76: P_{5627} = (26, 14, 4, 1)
                                                                 130: P_{7600} = (15, 12, 6, 1)
77: P_{5653} = (20, 15, 4, 1)
                                                                 131: P_{7620} = (3, 13, 6, 1)
78: P_{5664} = (31, 15, 4, 1)
                                                                 132: P_{7625} = (8, 13, 6, 1)
79: P_{5671} = (6, 16, 4, 1)
                                                                 133: P_{7717} = (4, 16, 6, 1)
80: P_{5683} = (18, 16, 4, 1)
                                                                 134: P_{7731} = (18, 16, 6, 1)
                                                                 135: P_{7755} = (10, 17, 6, 1)
81: P_{5733} = (4, 18, 4, 1)
82: P_{5747} = (18, 18, 4, 1)
                                                                 136: P_{7774} = (29, 17, 6, 1)
83: P_{5830} = (5, 21, 4, 1)
                                                                 137: P_{7782} = (5, 18, 6, 1)
84: P_{5845} = (20, 21, 4, 1)
                                                                 138: P_{7794} = (17, 18, 6, 1)
                                                                 139: P_{7816} = (7, 19, 6, 1)
85: P_{6056} = (7, 28, 4, 1)
86: P_{6080} = (31, 28, 4, 1)
                                                                 140: P_{7827} = (18, 19, 6, 1)
87: P_{6157} = (12, 31, 4, 1)
                                                                 141: P_{7855} = (14, 20, 6, 1)
88: P_{6168} = (23, 31, 4, 1)
                                                                 142: P_{7869} = (28, 20, 6, 1)
89: P_{6193} = (16, 0, 5, 1)
                                                                 143: P_{7887} = (14, 21, 6, 1)
90: P_{6198} = (21, 0, 5, 1)
                                                                 144: P_{7902} = (29, 21, 6, 1)
91: P_{6368} = (31, 5, 5, 1)
                                                                 145: P_{7917} = (12, 22, 6, 1)
92: P_{6484} = (19, 9, 5, 1)
                                                                 146: P_{7933} = (28, 22, 6, 1)
93: P_{6496} = (31, 9, 5, 1)
                                                                 147: P_{7977} = (8, 24, 6, 1)
                                                                 148: P_{7991} = (22, 24, 6, 1)
94: P_{6550} = (21, 11, 5, 1)
95: P_{6556} = (27, 11, 5, 1)
                                                                 149: P_{8077} = (12, 27, 6, 1)
96: P_{6567} = (6, 12, 5, 1)
                                                                 150: P_{8082} = (17, 27, 6, 1)
97: P_{6576} = (15, 12, 5, 1)
                                                                 151: P_{8228} = (3, 0, 7, 1)
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206: P_{10039} = (22, 24, 8, 1)
152: P_{8229} = (4, 0, 7, 1)
153: P_{8307} = (18, 2, 7, 1)
                                                                 207: P_{10056} = (7, 25, 8, 1)
154: P_{8312} = (23, 2, 7, 1)
                                                                 208: P_{10071} = (22, 25, 8, 1)
155: P_{8361} = (8, 4, 7, 1)
                                                                 209: P_{10217} = (8, 30, 8, 1)
156: P_{8364} = (11, 4, 7, 1)
                                                                 210: P_{10239} = (30, 30, 8, 1)
157: P_{8458} = (9, 7, 7, 1)
                                                                 211: P_{10356} = (19, 2, 9, 1)
158: P_{8504} = (23, 8, 7, 1)
                                                                 212: P_{10361} = (24, 2, 9, 1)
159: P_{8505} = (24, 8, 7, 1)
                                                                 213: P_{10371} = (2, 3, 9, 1)
160: P_{8516} = (3, 9, 7, 1)
                                                                 214: P_{10377} = (8, 3, 9, 1)
161: P_{8526} = (13, 9, 7, 1)
                                                                 215: P_{10422} = (21, 4, 9, 1)
162: P_{8566} = (21, 10, 7, 1)
                                                                 216: P_{10425} = (24, 4, 9, 1)
163: P_{8569} = (24, 10, 7, 1)
                                                                 217: P_{10455} = (22, 5, 9, 1)
164: P_{8596} = (19, 11, 7, 1)
                                                                 218: P_{10459} = (26, 5, 9, 1)
165: P_{8608} = (31, 11, 7, 1)
                                                                 219: P_{10504} = (7, 7, 9, 1)
166: P_{8694} = (21, 14, 7, 1)
                                                                 220: P_{10506} = (9, 7, 9, 1)
167: P_{8701} = (28, 14, 7, 1)
                                                                 221: P_{10549} = (20, 8, 9, 1)
168: P_{8710} = (5, 15, 7, 1)
                                                                 222: P_{10550} = (21, 8, 9, 1)
169: P_{8718} = (13, 15, 7, 1)
                                                                 223: P_{10577} = (16, 9, 9, 1)
170: P_{8748} = (11, 16, 7, 1)
                                                                 224: P_{10666} = (9, 12, 9, 1)
171: P_{8765} = (28, 16, 7, 1)
                                                                 225: P_{10669} = (12, 12, 9, 1)
172: P_{8839} = (6, 19, 7, 1)
                                                                 226: P_{10705} = (16, 13, 9, 1)
173: P_{8851} = (18, 19, 7, 1)
                                                                 227: P_{10709} = (20, 13, 9, 1)
174: P_{8870} = (5, 20, 7, 1)
                                                                 228: P_{10763} = (10, 15, 9, 1)
175: P_{8887} = (22, 20, 7, 1)
                                                                 229: P_{10765} = (12, 15, 9, 1)
176: P_{9033} = (8, 25, 7, 1)
                                                                 230: P_{10819} = (2, 17, 9, 1)
177: P_{9047} = (22, 25, 7, 1)
                                                                 231: P_{10843} = (26, 17, 9, 1)
178: P_{9125} = (4, 28, 7, 1)
                                                                 232: P_{10862} = (13, 18, 9, 1)
179: P_{9152} = (31, 28, 7, 1)
                                                                 233: P_{10871} = (22, 18, 9, 1)
180: P_{9162} = (9, 29, 7, 1)
                                                                 234: P_{11054} = (13, 24, 9, 1)
                                                                 235: P_{11069} = (28, 24, 9, 1)
181: P_{9172} = (19, 29, 7, 1)
182: P_{9347} = (2, 3, 8, 1)
                                                                 236: P_{11208} = (7, 29, 9, 1)
183: P_{9354} = (9, 3, 8, 1)
                                                                 237: P_{11220} = (19, 29, 9, 1)
184 : P_{9384} = (7, 4, 8, 1)
                                                                 238: P_{11275} = (10, 31, 9, 1)
185: P_{9388} = (11, 4, 8, 1)
                                                                 239: P_{11293} = (28, 31, 9, 1)
186: P_{9429} = (20, 5, 8, 1)
                                                                 240: P_{11461} = (4, 5, 10, 1)
187: P_{9434} = (25, 5, 8, 1)
                                                                 241: P_{11468} = (11, 5, 10, 1)
188: P_{9519} = (14, 8, 8, 1)
                                                                 242: P_{11510} = (21, 6, 10, 1)
                                                                 243: P_{11514} = (25, 6, 10, 1)
189: P_{9618} = (17, 11, 8, 1)
190: P_{9619} = (18, 11, 8, 1)
                                                                 244: P_{11541} = (20, 7, 10, 1)
191: P_{9668} = (3, 13, 8, 1)
                                                                 245: P_{11546} = (25, 7, 10, 1)
192: P_{9671} = (6, 13, 8, 1)
                                                                 246: P_{11557} = (4, 8, 10, 1)
193: P_{9747} = (18, 15, 8, 1)
                                                                 247: P_{11559} = (6, 8, 10, 1)
194: P_{9750} = (21, 15, 8, 1)
                                                                 248: P_{11647} = (30, 10, 10, 1)
195: P_{9859} = (2, 19, 8, 1)
                                                                 249: P_{11786} = (9, 15, 10, 1)
196: P_{9882} = (25, 19, 8, 1)
                                                                 250: P_{11789} = (12, 15, 10, 1)
197: P_{9897} = (8, 20, 8, 1)
                                                                 251: P_{11824} = (15, 16, 10, 1)
198: P_{9909} = (20, 20, 8, 1)
                                                                 252: P_{11830} = (21, 16, 10, 1)
199: P_{9924} = (3, 21, 8, 1)
                                                                 253: P_{11847} = (6, 17, 10, 1)
200: P_{9951} = (30, 21, 8, 1)
                                                                 254: P_{11870} = (29, 17, 10, 1)
201: P_{9964} = (11, 22, 8, 1)
                                                                 255: P_{11915} = (10, 19, 10, 1)
202: P_{9974} = (21, 22, 8, 1)
                                                                 256: P_{11924} = (19, 19, 10, 1)
203: P_{9999} = (14, 23, 8, 1)
                                                                 257: P_{12077} = (12, 24, 10, 1)
204: P_{10002} = (17, 23, 8, 1)
                                                                 258: P_{12095} = (30, 24, 10, 1)
205: P_{10023} = (6, 24, 8, 1)
                                                                 259: P_{12112} = (15, 25, 10, 1)
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260: P_{12125} = (28, 25, 10, 1)
                                                                314: P_{13738} = (9, 12, 12, 1)
261: P_{12166} = (5, 27, 10, 1)
                                                                315: P_{13834} = (9, 15, 12, 1)
262: P_{12181} = (20, 27, 10, 1)
                                                                316: P_{13835} = (10, 15, 12, 1)
263: P_{12198} = (5, 28, 10, 1)
                                                                317: P_{13923} = (2, 18, 12, 1)
264: P_{12212} = (19, 28, 10, 1)
                                                                318: P_{13949} = (28, 18, 12, 1)
265: P_{12235} = (10, 29, 10, 1)
                                                                319: P_{14055} = (6, 22, 12, 1)
266: P_{12254} = (29, 29, 10, 1)
                                                                320: P_{14077} = (28, 22, 12, 1)
267: P_{12298} = (9, 31, 10, 1)
                                                                321: P_{14094} = (13, 23, 12, 1)
268: P_{12317} = (28, 31, 10, 1)
                                                                322: P_{14103} = (22, 23, 12, 1)
269: P_{12456} = (7, 4, 11, 1)
                                                                323: P_{14123} = (10, 24, 12, 1)
270: P_{12457} = (8, 4, 11, 1)
                                                                324: P_{14143} = (30, 24, 12, 1)
271: P_{12485} = (4, 5, 11, 1)
                                                                325: P_{14215} = (6, 27, 12, 1)
272: P_{12491} = (10, 5, 11, 1)
                                                                326: P_{14226} = (17, 27, 12, 1)
273: P_{12568} = (23, 7, 11, 1)
                                                                327: P_{14341} = (4, 31, 12, 1)
274: P_{12572} = (27, 7, 11, 1)
                                                                328: P_{14360} = (23, 31, 12, 1)
275: P_{12634} = (25, 9, 11, 1)
                                                                329: P_{14386} = (17, 0, 13, 1)
276: P_{12636} = (27, 9, 11, 1)
                                                                330: P_{14397} = (28, 0, 13, 1)
                                                                331: P_{14482} = (17, 3, 13, 1)
277: P_{12669} = (28, 10, 11, 1)
278: P_{12670} = (29, 10, 11, 1)
                                                                332: P_{14496} = (31, 3, 13, 1)
279: P_{12686} = (13, 11, 11, 1)
                                                                333: P_{14660} = (3, 9, 13, 1)
280: P_{12708} = (3, 12, 11, 1)
                                                                334: P_{14664} = (7, 9, 13, 1)
281: P_{12709} = (4, 12, 11, 1)
                                                                335: P_{14732} = (11, 11, 13, 1)
282: P_{12840} = (7, 16, 11, 1)
                                                                336: P_{14734} = (13, 11, 13, 1)
283: P_{12861} = (28, 16, 11, 1)
                                                                337: P_{14783} = (30, 12, 13, 1)
284: P_{12868} = (3, 17, 11, 1)
                                                                338: P_{14784} = (31, 12, 13, 1)
285: P_{12890} = (25, 17, 11, 1)
                                                                339: P_{14812} = (27, 13, 13, 1)
286: P_{12911} = (14, 18, 11, 1)
                                                                340: P_{14846} = (29, 14, 13, 1)
287: P_{12920} = (23, 18, 11, 1)
                                                                341: P_{14847} = (30, 14, 13, 1)
288: P_{13004} = (11, 21, 11, 1)
                                                                342: P_{14854} = (5, 15, 13, 1)
289: P_{13014} = (21, 21, 11, 1)
                                                                343: P_{14856} = (7, 15, 13, 1)
290: P_{13033} = (8, 22, 11, 1)
                                                                344: P_{14894} = (13, 16, 13, 1)
291: P_{13046} = (21, 22, 11, 1)
                                                                345: P_{14897} = (16, 16, 13, 1)
292: P_{13164} = (11, 26, 11, 1)
                                                                346: P_{14954} = (9, 18, 13, 1)
293: P_{13179} = (26, 26, 11, 1)
                                                                347: P_{14967} = (22, 18, 13, 1)
294: P_{13198} = (13, 27, 11, 1)
                                                                348: P_{14982} = (5, 19, 13, 1)
295: P_{13214} = (29, 27, 11, 1)
                                                                349: P_{15004} = (27, 19, 13, 1)
296: P_{13327} = (14, 31, 11, 1)
                                                                350: P_{15117} = (12, 23, 13, 1)
297: P_{13339} = (26, 31, 11, 1)
                                                                351: P_{15127} = (22, 23, 13, 1)
298: P_{13368} = (23, 0, 12, 1)
                                                                352: P_{15146} = (9, 24, 13, 1)
299: P_{13372} = (27, 0, 12, 1)
                                                                353: P_{15165} = (28, 24, 13, 1)
300: P_{13429} = (20, 2, 12, 1)
                                                                354: P_{15244} = (11, 27, 13, 1)
301: P_{13435} = (26, 2, 12, 1)
                                                                355: P_{15262} = (29, 27, 13, 1)
302: P_{13459} = (18, 3, 12, 1)
                                                                356: P_{15332} = (3, 30, 13, 1)
303: P_{13470} = (29, 3, 12, 1)
                                                                357: P_{15345} = (16, 30, 13, 1)
304: P_{13495} = (22, 4, 12, 1)
                                                                358: P_{15474} = (17, 2, 14, 1)
305: P_{13503} = (30, 4, 12, 1)
                                                                359: P_{15486} = (29, 2, 14, 1)
306: P_{13523} = (18, 5, 12, 1)
                                                                360: P_{15608} = (23, 6, 14, 1)
307: P_{13532} = (27, 5, 12, 1)
                                                                361: P_{15616} = (31, 6, 14, 1)
308: P_{13650} = (17, 9, 12, 1)
                                                                362: P_{15636} = (19, 7, 14, 1)
309: P_{13653} = (20, 9, 12, 1)
                                                                363: P_{15643} = (26, 7, 14, 1)
310: P_{13667} = (2, 10, 12, 1)
                                                                364: P_{15657} = (8, 8, 14, 1)
                                                                365: P_{15663} = (14, 8, 14, 1)
311: P_{13669} = (4, 10, 12, 1)
312: P_{13723} = (26, 11, 12, 1)
                                                                366: P_{15729} = (16, 10, 14, 1)
313: P_{13726} = (29, 11, 12, 1)
                                                                367: P_{15733} = (20, 10, 14, 1)
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368: P_{15797} = (20, 12, 14, 1)
                                                                422: P_{17775} = (14, 10, 16, 1)
369: P_{15799} = (22, 12, 14, 1)
                                                                423: P_{17781} = (20, 10, 16, 1)
370: P_{15837} = (28, 13, 14, 1)
                                                                424: P_{17796} = (3, 11, 16, 1)
371: P_{15840} = (31, 13, 14, 1)
                                                                425: P_{17817} = (24, 11, 16, 1)
372: P_{15860} = (19, 14, 14, 1)
                                                                426: P_{17866} = (9, 13, 16, 1)
373: P_{15952} = (15, 17, 14, 1)
                                                                427: P_{17877} = (20, 13, 16, 1)
374: P_{15953} = (16, 17, 14, 1)
                                                                428: P_{17893} = (4, 14, 16, 1)
375: P_{15980} = (11, 18, 14, 1)
                                                                429: P_{17915} = (26, 14, 16, 1)
376: P_{15992} = (23, 18, 14, 1)
                                                                430: P_{17966} = (13, 16, 16, 1)
377: P_{16039} = (6, 20, 14, 1)
                                                                431: P_{17999} = (14, 17, 16, 1)
378: P_{16061} = (28, 20, 14, 1)
                                                                432: P_{18000} = (15, 17, 16, 1)
379: P_{16071} = (6, 21, 14, 1)
                                                                433: P_{18041} = (24, 18, 16, 1)
380: P_{16094} = (29, 21, 14, 1)
                                                                434: P_{18043} = (26, 18, 16, 1)
381: P_{16111} = (14, 22, 14, 1)
                                                                435: P_{18195} = (18, 23, 16, 1)
382: P_{16119} = (22, 22, 14, 1)
                                                                436: P_{18198} = (21, 23, 16, 1)
383: P_{16137} = (8, 23, 14, 1)
                                                                437: P_{18278} = (5, 26, 16, 1)
384: P_{16146} = (17, 23, 14, 1)
                                                                438: P_{18288} = (15, 26, 16, 1)
                                                                439: P_{18354} = (17, 28, 16, 1)
385: P_{16396} = (11, 31, 14, 1)
386: P_{16411} = (26, 31, 14, 1)
                                                                440: P_{18366} = (29, 28, 16, 1)
387: P_{16503} = (22, 2, 15, 1)
                                                                441: P_{18404} = (3, 30, 16, 1)
388: P_{16508} = (27, 2, 15, 1)
                                                                442: P_{18414} = (13, 30, 16, 1)
389: P_{16516} = (3, 3, 15, 1)
                                                                443: P_{18451} = (18, 31, 16, 1)
390: P_{16528} = (15, 3, 15, 1)
                                                                444: P_{18462} = (29, 31, 16, 1)
391: P_{16729} = (24, 9, 15, 1)
                                                                445: P_{18478} = (13, 0, 17, 1)
392: P_{16735} = (30, 9, 15, 1)
                                                                446: P_{18493} = (28, 0, 17, 1)
393: P_{16771} = (2, 11, 15, 1)
                                                                447: P_{18543} = (14, 2, 17, 1)
394: P_{16775} = (6, 11, 15, 1)
                                                                448: P_{18558} = (29, 2, 17, 1)
395: P_{16806} = (5, 12, 15, 1)
                                                                449: P_{18574} = (13, 3, 17, 1)
396: P_{16807} = (6, 12, 15, 1)
                                                                450: P_{18592} = (31, 3, 17, 1)
397: P_{16854} = (21, 13, 15, 1)
                                                                451: P_{18723} = (2, 8, 17, 1)
398: P_{16856} = (23, 13, 15, 1)
                                                                452: P_{18748} = (27, 8, 17, 1)
399: P_{16887} = (22, 14, 15, 1)
                                                                453: P_{18765} = (12, 9, 17, 1)
400: P_{16888} = (23, 14, 15, 1)
                                                                454: P_{18773} = (20, 9, 17, 1)
401: P_{16924} = (27, 15, 15, 1)
                                                                455: P_{18825} = (8, 11, 17, 1)
402: P_{16939} = (10, 16, 15, 1)
                                                                456: P_{18835} = (18, 11, 17, 1)
403: P_{16950} = (21, 16, 15, 1)
                                                                457: P_{18886} = (5, 13, 17, 1)
404: P_{16975} = (14, 17, 15, 1)
                                                                458: P_{18906} = (25, 13, 17, 1)
                                                                459: P_{18947} = (2, 15, 17, 1)
405: P_{16977} = (16, 17, 15, 1)
406: P_{16996} = (3, 18, 15, 1)
                                                                460: P_{18973} = (28, 15, 17, 1)
407: P_{17023} = (30, 18, 15, 1)
                                                                461: P_{19027} = (18, 17, 17, 1)
408: P_{17091} = (2, 21, 15, 1)
                                                                462: P_{19046} = (5, 18, 17, 1)
409: P_{17113} = (24, 21, 15, 1)
                                                                463: P_{19047} = (6, 18, 17, 1)
410: P_{17227} = (10, 25, 15, 1)
                                                                464: P_{19209} = (8, 23, 17, 1)
411: P_{17245} = (28, 25, 15, 1)
                                                                465: P_{19215} = (14, 23, 17, 1)
412: P_{17254} = (5, 26, 15, 1)
                                                                466: P_{19317} = (20, 26, 17, 1)
413: P_{17265} = (16, 26, 15, 1)
                                                                467: P_{19328} = (31, 26, 17, 1)
414: P_{17328} = (15, 28, 15, 1)
                                                                468: P_{19335} = (6, 27, 17, 1)
415: P_{17341} = (28, 28, 15, 1)
                                                                469: P_{19341} = (12, 27, 17, 1)
416: P_{17446} = (5, 0, 16, 1)
                                                                470: P_{19377} = (16, 28, 17, 1)
417: P_{17462} = (21, 0, 16, 1)
                                                                471: P_{19390} = (29, 28, 17, 1)
418: P_{17573} = (4, 4, 16, 1)
                                                                472: P_{19414} = (21, 29, 17, 1)
419: P_{17585} = (16, 4, 16, 1)
                                                                473: P_{19418} = (25, 29, 17, 1)
420: P_{17738} = (9, 9, 16, 1)
                                                                474: P_{19478} = (21, 31, 17, 1)
421: P_{17745} = (16, 9, 16, 1)
                                                                475: P_{19484} = (27, 31, 17, 1)
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476: P_{19560} = (7, 2, 18, 1)
                                                                530: P_{21448} = (7, 29, 19, 1)
477: P_{19576} = (23, 2, 18, 1)
                                                                531: P_{21450} = (9, 29, 19, 1)
478: P_{19597} = (12, 3, 18, 1)
                                                                532: P_{21495} = (22, 30, 19, 1)
479: P_{19614} = (29, 3, 18, 1)
                                                                533: P_{21500} = (27, 30, 19, 1)
480: P_{19661} = (12, 5, 18, 1)
                                                                534: P_{21613} = (12, 2, 20, 1)
481: P_{19676} = (27, 5, 18, 1)
                                                                535: P_{21627} = (26, 2, 20, 1)
482: P_{19849} = (8, 11, 18, 1)
                                                                536: P_{21705} = (8, 5, 20, 1)
483: P_{19858} = (17, 11, 18, 1)
                                                                537: P_{21722} = (25, 5, 20, 1)
484: P_{19977} = (8, 15, 18, 1)
                                                                538: P_{21771} = (10, 7, 20, 1)
485: P_{19990} = (21, 15, 18, 1)
                                                                539: P_{21786} = (25, 7, 20, 1)
486: P_{20005} = (4, 16, 18, 1)
                                                                540: P_{21802} = (9, 8, 20, 1)
487: P_{20007} = (6, 16, 18, 1)
                                                                541: P_{21814} = (21, 8, 20, 1)
488: P_{20050} = (17, 17, 18, 1)
                                                                542: P_{21837} = (12, 9, 20, 1)
                                                                543: P_{21842} = (17, 9, 20, 1)
489: P_{20051} = (18, 17, 18, 1)
490: P_{20069} = (4, 18, 18, 1)
                                                                544: P_{21871} = (14, 10, 20, 1)
491: P_{20103} = (6, 19, 18, 1)
                                                                545: P_{21873} = (16, 10, 20, 1)
                                                                546: P_{21935} = (14, 12, 20, 1)
492: P_{20104} = (7, 19, 18, 1)
493: P_{20153} = (24, 20, 18, 1)
                                                                547: P_{21943} = (22, 12, 20, 1)
494: P_{20159} = (30, 20, 18, 1)
                                                                548: P_{21962} = (9, 13, 20, 1)
495: P_{20241} = (16, 23, 18, 1)
                                                                549: P_{21969} = (16, 13, 20, 1)
496: P_{20246} = (21, 23, 18, 1)
                                                                550: P_{22021} = (4, 15, 20, 1)
497: P_{20275} = (18, 24, 18, 1)
                                                                551: P_{22048} = (31, 15, 20, 1)
498: P_{20281} = (24, 24, 18, 1)
                                                                552: P_{22185} = (8, 20, 20, 1)
499: P_{20340} = (19, 26, 18, 1)
                                                                553: P_{22213} = (4, 21, 20, 1)
500: P_{20348} = (27, 26, 18, 1)
                                                                554: P_{22214} = (5, 21, 20, 1)
501: P_{20376} = (23, 27, 18, 1)
                                                                555: P_{22360} = (23, 25, 20, 1)
502: P_{20383} = (30, 27, 18, 1)
                                                                556: P_{22363} = (26, 25, 20, 1)
503: P_{20497} = (16, 31, 18, 1)
                                                                557: P_{22386} = (17, 26, 20, 1)
504: P_{20510} = (29, 31, 18, 1)
                                                                558: P_{22400} = (31, 26, 20, 1)
                                                                559: P_{22406} = (5, 27, 20, 1)
505: P_{20586} = (9, 2, 19, 1)
506: P_{20601} = (24, 2, 19, 1)
                                                                560: P_{22411} = (10, 27, 20, 1)
507: P_{20615} = (6, 3, 19, 1)
                                                                561: P_{22455} = (22, 28, 20, 1)
508: P_{20631} = (22, 3, 19, 1)
                                                                562: P_{22463} = (30, 28, 20, 1)
509: P_{20711} = (6, 6, 19, 1)
                                                                563: P_{22488} = (23, 29, 20, 1)
510: P_{20724} = (19, 6, 19, 1)
                                                                564: P_{22495} = (30, 29, 20, 1)
511: P_{20751} = (14, 7, 19, 1)
                                                                565: P_{22566} = (5, 0, 21, 1)
512: P_{20763} = (26, 7, 19, 1)
                                                                566: P_{22577} = (16, 0, 21, 1)
513: P_{20806} = (5, 9, 19, 1)
                                                                567: P_{22698} = (9, 4, 21, 1)
514: P_{20832} = (31, 9, 19, 1)
                                                                568: P_{22713} = (24, 4, 21, 1)
515: P_{20872} = (7, 11, 19, 1)
                                                                569: P_{22763} = (10, 6, 21, 1)
516: P_{20896} = (31, 11, 19, 1)
                                                                570: P_{22778} = (25, 6, 21, 1)
                                                                571: P_{22826} = (9, 8, 21, 1)
517: P_{20975} = (14, 14, 19, 1)
518: P_{20980} = (19, 14, 19, 1)
                                                                572: P_{22837} = (20, 8, 21, 1)
519: P_{21050} = (25, 16, 19, 1)
                                                                573: P_{22888} = (7, 10, 21, 1)
520: P_{21051} = (26, 16, 19, 1)
                                                                574: P_{22905} = (24, 10, 21, 1)
521: P_{21131} = (10, 19, 19, 1)
                                                                575: P_{22918} = (5, 11, 21, 1)
522: P_{21241} = (24, 22, 19, 1)
                                                                576: P_{22940} = (27, 11, 21, 1)
523: P_{21246} = (29, 22, 19, 1)
                                                                577: P_{22992} = (15, 13, 21, 1)
524: P_{21274} = (25, 23, 19, 1)
                                                                578: P_{23000} = (23, 13, 21, 1)
525: P_{21278} = (29, 23, 19, 1)
                                                                579: P_{23016} = (7, 14, 21, 1)
526: P_{21363} = (18, 26, 19, 1)
                                                                580: P_{23037} = (28, 14, 21, 1)
527: P_{21372} = (27, 26, 19, 1)
                                                                581: P_{23049} = (8, 15, 21, 1)
528: P_{21414} = (5, 28, 19, 1)
                                                                582: P_{23059} = (18, 15, 21, 1)
529: P_{21419} = (10, 28, 19, 1)
                                                                583: P_{23083} = (10, 16, 21, 1)
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584: P_{23088} = (15, 16, 21, 1)
                                                                638: P_{24923} = (26, 9, 23, 1)
585: P_{23244} = (11, 21, 21, 1)
                                                                639: P_{25040} = (15, 13, 23, 1)
                                                                640: P_{25046} = (21, 13, 23, 1)
586: P_{23273} = (8, 22, 21, 1)
587: P_{23276} = (11, 22, 21, 1)
                                                                641: P_{25072} = (15, 14, 23, 1)
588: P_{23313} = (16, 23, 21, 1)
                                                                642: P_{25079} = (22, 14, 23, 1)
589: P_{23315} = (18, 23, 21, 1)
                                                                643: P_{25196} = (11, 18, 23, 1)
590: P_{23506} = (17, 29, 21, 1)
                                                                644: P_{25199} = (14, 18, 23, 1)
591: P_{23514} = (25, 29, 21, 1)
                                                                645: P_{25241} = (24, 19, 23, 1)
592: P_{23544} = (23, 30, 21, 1)
                                                                646: P_{25245} = (28, 19, 23, 1)
593: P_{23549} = (28, 30, 21, 1)
                                                                647: P_{25376} = (31, 23, 23, 1)
594: P_{23570} = (17, 31, 21, 1)
                                                                648: P_{25429} = (20, 25, 23, 1)
595: P_{23580} = (27, 31, 21, 1)
                                                                649: P_{25435} = (26, 25, 23, 1)
596: P_{23664} = (15, 2, 22, 1)
                                                                650: P_{25491} = (18, 27, 23, 1)
597: P_{23676} = (27, 2, 22, 1)
                                                                651: P_{25503} = (30, 27, 23, 1)
598: P_{23687} = (6, 3, 22, 1)
                                                                652: P_{25557} = (20, 29, 23, 1)
599: P_{23700} = (19, 3, 22, 1)
                                                                653: P_{25567} = (30, 29, 23, 1)
600: P_{23725} = (12, 4, 22, 1)
                                                                654: P_{25590} = (21, 30, 23, 1)
                                                                655: P_{25597} = (28, 30, 23, 1)
601: P_{23743} = (30, 4, 22, 1)
602: P_{23754} = (9, 5, 22, 1)
                                                                656: P_{25605} = (4, 31, 23, 1)
603: P_{23771} = (26, 5, 22, 1)
                                                                657: P_{25613} = (12, 31, 23, 1)
604: P_{23983} = (14, 12, 22, 1)
                                                                658: P_{25635} = (2, 0, 24, 1)
605: P_{23989} = (20, 12, 22, 1)
                                                                659: P_{25659} = (26, 0, 24, 1)
606: P_{24048} = (15, 14, 22, 1)
                                                                660: P_{25706} = (9, 2, 24, 1)
607: P_{24056} = (23, 14, 22, 1)
                                                                661: P_{25716} = (19, 2, 24, 1)
608: P_{24068} = (3, 15, 22, 1)
                                                                662: P_{25770} = (9, 4, 24, 1)
609: P_{24091} = (26, 15, 22, 1)
                                                                663: P_{25782} = (21, 4, 24, 1)
610: P_{24100} = (3, 16, 22, 1)
                                                                664: P_{25828} = (3, 6, 24, 1)
611: P_{24102} = (5, 16, 22, 1)
                                                                665: P_{25854} = (29, 6, 24, 1)
612: P_{24170} = (9, 18, 22, 1)
                                                                666: P_{25896} = (7, 8, 24, 1)
                                                                667: P_{25912} = (23, 8, 24, 1)
613: P_{24174} = (13, 18, 22, 1)
614: P_{24230} = (5, 20, 22, 1)
                                                                668: P_{25936} = (15, 9, 24, 1)
615: P_{24232} = (7, 20, 22, 1)
                                                                669: P_{25951} = (30, 9, 24, 1)
616: P_{24303} = (14, 22, 22, 1)
                                                                670: P_{25960} = (7, 10, 24, 1)
617: P_{24333} = (12, 23, 22, 1)
                                                                671: P_{25974} = (21, 10, 24, 1)
618: P_{24334} = (13, 23, 22, 1)
                                                                672: P_{25988} = (3, 11, 24, 1)
619: P_{24359} = (6, 24, 22, 1)
                                                                673: P_{26001} = (16, 11, 24, 1)
620: P_{24361} = (8, 24, 22, 1)
                                                                674: P_{26225} = (16, 18, 24, 1)
621: P_{24392} = (7, 25, 22, 1)
                                                                675: P_{26235} = (26, 18, 24, 1)
622: P_{24393} = (8, 25, 22, 1)
                                                                676: P_{26264} = (23, 19, 24, 1)
623: P_{24501} = (20, 28, 22, 1)
                                                                677: P_{26269} = (28, 19, 24, 1)
624: P_{24511} = (30, 28, 22, 1)
                                                                678: P_{26291} = (18, 20, 24, 1)
625: P_{24564} = (19, 30, 22, 1)
                                                                679: P_{26303} = (30, 20, 24, 1)
626: P_{24572} = (27, 30, 22, 1)
                                                                680: P_{26307} = (2, 21, 24, 1)
627: P_{24621} = (12, 0, 23, 1)
                                                                681: P_{26320} = (15, 21, 24, 1)
628: P_{24636} = (27, 0, 23, 1)
                                                                682: P_{26356} = (19, 22, 24, 1)
629: P_{24680} = (7, 2, 23, 1)
                                                                683: P_{26366} = (29, 22, 24, 1)
630: P_{24691} = (18, 2, 23, 1)
                                                                684: P_{26419} = (18, 24, 24, 1)
631: P_{24815} = (14, 6, 23, 1)
                                                                685: P_{26525} = (28, 27, 24, 1)
632: P_{24832} = (31, 6, 23, 1)
                                                                686: P_{26528} = (31, 27, 24, 1)
633: P_{24844} = (11, 7, 23, 1)
                                                                687: P_{26618} = (25, 30, 24, 1)
634: P_{24860} = (27, 7, 23, 1)
                                                                688: P_{26624} = (31, 30, 24, 1)
635: P_{24872} = (7, 8, 23, 1)
                                                                689: P_{26787} = (2, 4, 25, 1)
636: P_{24889} = (24, 8, 23, 1)
                                                                690: P_{26816} = (31, 4, 25, 1)
637: P_{24901} = (4, 9, 23, 1)
                                                                691: P_{26825} = (8, 5, 25, 1)
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692: P_{26837} = (20, 5, 25, 1)
                                                                746: P_{28501} = (20, 25, 26, 1)
693: P_{26859} = (10, 6, 25, 1)
                                                                747: P_{28504} = (23, 25, 26, 1)
694: P_{26870} = (21, 6, 25, 1)
                                                                748: P_{28524} = (11, 26, 26, 1)
695: P_{26891} = (10, 7, 25, 1)
                                                                749: P_{28684} = (11, 31, 26, 1)
696: P_{26901} = (20, 7, 25, 1)
                                                                750: P_{28687} = (14, 31, 26, 1)
697: P_{26956} = (11, 9, 25, 1)
                                                                751: P_{28717} = (12, 0, 27, 1)
698: P_{26972} = (27, 9, 25, 1)
                                                                752: P_{28728} = (23, 0, 27, 1)
699: P_{27078} = (5, 13, 25, 1)
                                                                753: P_{28784} = (15, 2, 27, 1)
700: P_{27090} = (17, 13, 25, 1)
                                                                754: P_{28791} = (22, 2, 27, 1)
701: P_{27188} = (19, 16, 25, 1)
                                                                755: P_{28877} = (12, 5, 27, 1)
702: P_{27195} = (26, 16, 25, 1)
                                                                756: P_{28883} = (18, 5, 27, 1)
703: P_{27204} = (3, 17, 25, 1)
                                                                757: P_{28940} = (11, 7, 27, 1)
704: P_{27212} = (11, 17, 25, 1)
                                                                758: P_{28952} = (23, 7, 27, 1)
705: P_{27267} = (2, 19, 25, 1)
                                                                759: P_{28963} = (2, 8, 27, 1)
706: P_{27273} = (8, 19, 25, 1)
                                                                760: P_{28978} = (17, 8, 27, 1)
707: P_{27412} = (19, 23, 25, 1)
                                                                761: P_{29004} = (11, 9, 27, 1)
708: P_{27422} = (29, 23, 25, 1)
                                                                762: P_{29018} = (25, 9, 27, 1)
709: P_{27451} = (26, 24, 25, 1)
                                                                763: P_{29062} = (5, 11, 27, 1)
710: P_{27452} = (27, 24, 25, 1)
                                                                764: P_{29078} = (21, 11, 27, 1)
711: P_{27487} = (30, 25, 25, 1)
                                                                765: P_{29134} = (13, 13, 27, 1)
712: P_{27518} = (29, 26, 25, 1)
                                                                766: P_{29148} = (27, 13, 27, 1)
713: P_{27519} = (30, 26, 25, 1)
                                                                767: P_{29200} = (15, 15, 27, 1)
714: P_{27602} = (17, 29, 25, 1)
                                                                768: P_{29212} = (27, 15, 27, 1)
715: P_{27606} = (21, 29, 25, 1)
                                                                769: P_{29318} = (5, 19, 27, 1)
716: P_{27641} = (24, 30, 25, 1)
                                                                770: P_{29326} = (13, 19, 27, 1)
717: P_{27648} = (31, 30, 25, 1)
                                                                771: P_{29498} = (25, 24, 27, 1)
718: P_{27652} = (3, 31, 25, 1)
                                                                772: P_{29499} = (26, 24, 27, 1)
719: P_{27654} = (5, 31, 25, 1)
                                                                773: P_{29555} = (18, 26, 27, 1)
720: P_{27683} = (2, 0, 26, 1)
                                                                774: P_{29556} = (19, 26, 27, 1)
721: P_{27705} = (24, 0, 26, 1)
                                                                775: P_{29571} = (2, 27, 27, 1)
722: P_{27757} = (12, 2, 26, 1)
                                                                776: P_{29684} = (19, 30, 27, 1)
723: P_{27765} = (20, 2, 26, 1)
                                                                777: P_{29687} = (22, 30, 27, 1)
724: P_{27812} = (3, 4, 26, 1)
                                                                778: P_{29714} = (17, 31, 27, 1)
725: P_{27838} = (29, 4, 26, 1)
                                                                779: P_{29718} = (21, 31, 27, 1)
                                                                780: P_{29742} = (13, 0, 28, 1)
726: P_{27850} = (9, 5, 26, 1)
727: P_{27863} = (22, 5, 26, 1)
                                                                781: P_{29746} = (17, 0, 28, 1)
728: P_{27919} = (14, 7, 26, 1)
                                                                782: P_{30060} = (11, 10, 28, 1)
                                                                783: P_{30078} = (29, 10, 28, 1)
729: P_{27924} = (19, 7, 26, 1)
730: P_{27973} = (4, 9, 26, 1)
                                                                784: P_{30159} = (14, 13, 28, 1)
731: P_{27992} = (23, 9, 26, 1)
                                                                785: P_{30176} = (31, 13, 28, 1)
732: P_{28045} = (12, 11, 26, 1)
                                                                786: P_{30184} = (7, 14, 28, 1)
733: P_{28062} = (29, 11, 26, 1)
                                                                787: P_{30198} = (21, 14, 28, 1)
734: P_{28133} = (4, 14, 26, 1)
                                                                788: P_{30211} = (2, 15, 28, 1)
735: P_{28145} = (16, 14, 26, 1)
                                                                789: P_{30226} = (17, 15, 28, 1)
736: P_{28164} = (3, 15, 26, 1)
                                                                790: P_{30248} = (7, 16, 28, 1)
737: P_{28183} = (22, 15, 26, 1)
                                                                791: P_{30252} = (11, 16, 28, 1)
738: P_{28212} = (19, 16, 26, 1)
                                                                792: P_{30307} = (2, 18, 28, 1)
739: P_{28218} = (25, 16, 26, 1)
                                                                793: P_{30317} = (12, 18, 28, 1)
740: P_{28227} = (2, 17, 26, 1)
                                                                794: P_{30360} = (23, 19, 28, 1)
741: P_{28234} = (9, 17, 26, 1)
                                                                795: P_{30361} = (24, 19, 28, 1)
742: P_{28273} = (16, 18, 26, 1)
                                                                796: P_{30375} = (6, 20, 28, 1)
                                                                797: P_{30383} = (14, 20, 28, 1)
743: P_{28281} = (24, 18, 26, 1)
744: P_{28474} = (25, 24, 26, 1)
                                                                798: P_{30439} = (6, 22, 28, 1)
745: P_{28476} = (27, 24, 26, 1)
                                                                799: P_{30445} = (12, 22, 28, 1)
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800: P_{30506} = (9, 24, 28, 1)
                                                                851: P_{32254} = (29, 14, 30, 1)
801: P_{30510} = (13, 24, 28, 1)
                                                                852: P_{32356} = (3, 18, 30, 1)
802: P_{30539} = (10, 25, 28, 1)
                                                                853: P_{32368} = (15, 18, 30, 1)
                                                                854: P_{32435} = (18, 20, 30, 1)
803: P_{30544} = (15, 25, 28, 1)
804: P_{30617} = (24, 27, 28, 1)
                                                                855: P_{32441} = (24, 20, 30, 1)
805: P_{30624} = (31, 27, 28, 1)
                                                                856: P_{32452} = (3, 21, 30, 1)
806: P_{30640} = (15, 28, 28, 1)
                                                                857: P_{32457} = (8, 21, 30, 1)
807: P_{30710} = (21, 30, 28, 1)
                                                                858: P_{32555} = (10, 24, 30, 1)
808: P_{30712} = (23, 30, 28, 1)
                                                                859: P_{32557} = (12, 24, 30, 1)
809: P_{30730} = (9, 31, 28, 1)
                                                                860: P_{32602} = (25, 25, 30, 1)
810: P_{30731} = (10, 31, 28, 1)
                                                                861: P_{32607} = (30, 25, 30, 1)
811: P_{30831} = (14, 2, 29, 1)
                                                                862: P_{32634} = (25, 26, 30, 1)
812: P_{30834} = (17, 2, 29, 1)
                                                                863: P_{32638} = (29, 26, 30, 1)
813: P_{30861} = (12, 3, 29, 1)
                                                                864: P_{32659} = (18, 27, 30, 1)
814: P_{30867} = (18, 3, 29, 1)
                                                                865: P_{32664} = (23, 27, 30, 1)
815: P_{30884} = (3, 4, 29, 1)
                                                                866: P_{32693} = (20, 28, 30, 1)
816: P_{30907} = (26, 4, 29, 1)
                                                                867: P_{32695} = (22, 28, 30, 1)
                                                                868: P_{32725} = (20, 29, 30, 1)
817: P_{30948} = (3, 6, 29, 1)
                                                                869: P_{32728} = (23, 29, 30, 1)
818: P_{30969} = (24, 6, 29, 1)
819: P_{31084} = (11, 10, 29, 1)
                                                                870: P_{32745} = (8, 30, 30, 1)
820: P_{31101} = (28, 10, 29, 1)
                                                                871: P_{32910} = (13, 3, 31, 1)
821: P_{31117} = (12, 11, 29, 1)
                                                                872: P_{32914} = (17, 3, 31, 1)
822: P_{31131} = (26, 11, 29, 1)
                                                                873: P_{32931} = (2,4,31,1)
823: P_{31214} = (13, 14, 29, 1)
                                                                874: P_{32954} = (25, 4, 31, 1)
824: P_{31231} = (30, 14, 29, 1)
                                                                875: P_{32966} = (5, 5, 31, 1)
825: P_{31303} = (6, 17, 29, 1)
                                                                876: P_{32992} = (31, 5, 31, 1)
826: P_{31307} = (10, 17, 29, 1)
                                                                877: P_{33007} = (14, 6, 31, 1)
827: P_{31431} = (6, 21, 29, 1)
                                                                878: P_{33016} = (23, 6, 31, 1)
828: P_{31439} = (14, 21, 29, 1)
                                                                879: P_{33094} = (5, 9, 31, 1)
829: P_{31476} = (19, 22, 29, 1)
                                                                880: P_{33108} = (19, 9, 31, 1)
830: P_{31481} = (24, 22, 29, 1)
                                                                881: P_{33160} = (7, 11, 31, 1)
831: P_{31508} = (19, 23, 29, 1)
                                                                882: P_{33172} = (19, 11, 31, 1)
832: P_{31514} = (25, 23, 29, 1)
                                                                883: P_{33198} = (13, 12, 31, 1)
833: P_{31610} = (25, 26, 29, 1)
                                                                884: P_{33215} = (30, 12, 31, 1)
834: P_{31615} = (30, 26, 29, 1)
                                                                885: P_{33231} = (14, 13, 31, 1)
835: P_{31628} = (11, 27, 29, 1)
                                                                886: P_{33245} = (28, 13, 31, 1)
836: P_{31630} = (13, 27, 29, 1)
                                                                887: P_{33285} = (4, 15, 31, 1)
                                                                888: P_{33301} = (20, 15, 31, 1)
837: P_{31665} = (16, 28, 29, 1)
                                                                889: P_{33560} = (23, 23, 31, 1)
838: P_{31666} = (17, 28, 29, 1)
839: P_{31691} = (10, 29, 29, 1)
                                                                890: P_{33568} = (31, 23, 31, 1)
840: P_{31761} = (16, 31, 29, 1)
                                                                891: P_{33650} = (17, 26, 31, 1)
841: P_{31763} = (18, 31, 29, 1)
                                                                892: P_{33653} = (20, 26, 31, 1)
842: P_{31917} = (12, 4, 30, 1)
                                                                893: P_{33689} = (24, 27, 31, 1)
843: P_{31927} = (22, 4, 30, 1)
                                                                894: P_{33693} = (28, 27, 31, 1)
844: P_{32080} = (15, 9, 30, 1)
                                                                895: P_{33701} = (4, 28, 31, 1)
                                                                896: P_{33704} = (7, 28, 31, 1)
845: P_{32089} = (24, 9, 30, 1)
846: P_{32107} = (10, 10, 30, 1)
                                                                897: P_{33785} = (24, 30, 31, 1)
847: P_{32127} = (30, 10, 30, 1)
                                                                898: P_{33786} = (25, 30, 31, 1)
848: P_{32174} = (13, 12, 30, 1)
                                                                899: P_{33795} = (2, 31, 31, 1)
849: P_{32192} = (31, 12, 30, 1)
850: P_{32238} = (13, 14, 30, 1)
```

Line Intersection Graph

$$\begin{array}{c} 012345 \\ \hline 00111100 \\ 1101001 \\ 2110010 \\ 3100011 \\ 4001101 \\ 5010110 \end{array}$$

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3
in point	P_5	P_1	P_0

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_5
in point	P_5	P_{67}	P_{36}

 ${\bf Line~2~intersects}$

Line	ℓ_0	ℓ_1	ℓ_4
in point	P_1	P_{67}	P_2

Line 3 intersects

Line	ℓ_0	ℓ_4	ℓ_5
in point	P_0	P_{1090}	P_{1091}

Line 4 intersects

Line	ℓ_2	ℓ_3	ℓ_5
in point	P_2	P_{1090}	P_{2114}

Line 5 intersects

Line	ℓ_1	ℓ_3	ℓ_4
in point	P_{36}	P_{1091}	P_{2114}

The surface has 1089 points:

Too many to print.