# Rank-73798 over GF(8)

January 15, 2021

# The equation

The equation of the surface is:

$$X_0^3 + X_1^3 + X_0^2 X_3 + X_0 X_3^2 + X_0 X_1 X_2 = 0$$

( 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0 ) The point rank of the equation over GF(8) is 1227395670

## General information

Number of lines	1
Number of points	65
Number of singular points	1
Number of Eckardt points	0
Number of double points	0
Number of single points	9
Number of points off lines	56
Number of Hesse planes	0
Number of axes	0
Type of points on lines	9
Type of lines on points	$1^9, 0^{56}$

## Singular Points

The surface has 1 singular points:

$$0: P_2 = \mathbf{P}(0,0,1,0) = \mathbf{P}(0,0,1,0)$$

## The 1 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4744} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}_{4744} = \mathbf{Pl}(0, 1, 0, 0, 0, 0)_1$$

Rank of lines: (4744)

Rank of points on Klein quadric: (1)

## **Eckardt Points**

The surface has 0 Eckardt points:

#### **Double Points**

The surface has 0 Double points: The double points on the surface are:

#### Single Points

The surface has 9 single points: The single points on the surface are:

 $\begin{array}{lll} 0: \ P_2 = (0,0,1,0) \ \mbox{lies on line} \ \ell_0 \\ 1: \ P_3 = (0,0,0,1) \ \mbox{lies on line} \ \ell_0 \\ 2: \ P_{138} = (0,0,1,1) \ \mbox{lies on line} \ \ell_0 \\ 3: \ P_{201} = (0,0,2,1) \ \mbox{lies on line} \ \ell_0 \\ 4: \ P_{265} = (0,0,3,1) \ \mbox{lies on line} \ \ell_0 \end{array}$ 

The single points on the surface are:

#### Points on surface but on no line

The surface has 56 points not on any line: The points on the surface but not on lines are:

 $0: P_5 = (1, 1, 0, 0)$ 18:  $P_{162} = (1, 3, 1, 1)$  $1: P_{22} = (3, 1, 1, 0)$ 19:  $P_{168} = (7, 3, 1, 1)$  $2: P_{24} = (5, 1, 1, 0)$  $20: P_{171} = (2, 4, 1, 1)$  $3: P_{25} = (6, 1, 1, 0)$  $21: P_{178} = (1, 5, 1, 1)$  $4: P_{36} = (1,3,1,0)$  $22: P_{179} = (2, 5, 1, 1)$  $5: P_{52} = (1, 5, 1, 0)$ 23:  $P_{186} = (1, 6, 1, 1)$  $6: P_{60} = (1, 6, 1, 0)$  $24: P_{189} = (4, 6, 1, 1)$ 7:  $P_{83} = (1, 1, 0, 1)$  $25: P_{197} = (4,7,1,1)$  $8: P_{94} = (4, 2, 0, 1)$  $26: P_{218} = (1, 2, 2, 1)$  $27: P_{220} = (3, 2, 2, 1)$ 9:  $P_{104} = (6, 3, 0, 1)$ 10:  $P_{113} = (7, 4, 0, 1)$ 28:  $P_{227} = (2, 3, 2, 1)$ 11:  $P_{117} = (3, 5, 0, 1)$ 29:  $P_{236} = (3, 4, 2, 1)$  $12: P_{127} = (5, 6, 0, 1)$  $30: P_{237} = (4, 4, 2, 1)$  $31: P_{239} = (6,4,2,1)$ 13:  $P_{132} = (2,7,0,1)$ 14:  $P_{147} = (2, 1, 1, 1)$  $32: P_{248} = (7, 5, 2, 1)$ 15:  $P_{149} = (4, 1, 1, 1)$  $33: P_{252} = (3, 6, 2, 1)$ 16:  $P_{152} = (7, 1, 1, 1)$  $34: P_{276} = (3, 1, 3, 1)$ 17:  $P_{160} = (7, 2, 1, 1)$  $35: P_{319} = (6,6,3,1)$ 

```
36: P_{358} = (5, 3, 4, 1)
                                                                  47: P_{502} = (5, 5, 6, 1)
37: P_{362} = (1, 4, 4, 1)
                                                                  48: P_{539} = (2, 2, 7, 1)
38: P_{366} = (5, 4, 4, 1)
                                                                  49: P_{542} = (5, 2, 7, 1)
39: P_{373} = (4, 5, 4, 1)
                                                                  50: P_{543} = (6, 2, 7, 1)
40: P_{379} = (2, 6, 4, 1)
                                                                  51: P_{549} = (4, 3, 7, 1)
41: P_{388} = (3,7,4,1)
                                                                  52: P_{567} = (6, 5, 7, 1)
42: P_{390} = (5, 7, 4, 1)
                                                                  53: P_{576} = (7, 6, 7, 1)
43: P_{392} = (7, 7, 4, 1)
                                                                  54: P_{578} = (1, 7, 7, 1)
44: P_{406} = (5, 1, 5, 1)
                                                                  55: P_{583} = (6,7,7,1)
45: P_{420} = (3, 3, 5, 1)
46: P_{471} = (6, 1, 6, 1)
```

# Line Intersection Graph

 $\begin{array}{c|c} 0 \\ \hline 0 & 0 \end{array}$ 

Neighbor sets in the line intersection graph: Line 0 intersects

Line in point

The surface has 65 points:

The points on the surface are:

$0: P_2 = (0,0,1,0)$	$22: P_{168} = (7, 3, 1, 1)$	$44: P_{366} = (5, 4, 4, 1)$
$1: P_3 = (0,0,0,1)$	$23: P_{171} = (2, 4, 1, 1)$	$45: P_{373} = (4, 5, 4, 1)$
$2: P_5 = (1, 1, 0, 0)$	$24: P_{178} = (1, 5, 1, 1)$	$46: P_{379} = (2, 6, 4, 1)$
$3: P_{22} = (3, 1, 1, 0)$	$25: P_{179} = (2, 5, 1, 1)$	$47: P_{388} = (3, 7, 4, 1)$
$4: P_{24} = (5, 1, 1, 0)$	$26: P_{186} = (1, 6, 1, 1)$	$48: P_{390} = (5, 7, 4, 1)$
$5: P_{25} = (6, 1, 1, 0)$	$27: P_{189} = (4, 6, 1, 1)$	$49: P_{392} = (7,7,4,1)$
$6: P_{36} = (1, 3, 1, 0)$	$28: P_{197} = (4,7,1,1)$	$50: P_{393} = (0, 0, 5, 1)$
$7: P_{52} = (1, 5, 1, 0)$	$29: P_{201} = (0, 0, 2, 1)$	$51: P_{406} = (5, 1, 5, 1)$
$8: P_{60} = (1, 6, 1, 0)$	$30: P_{218} = (1, 2, 2, 1)$	$52: P_{420} = (3, 3, 5, 1)$
$9: P_{83} = (1, 1, 0, 1)$	$31: P_{220} = (3, 2, 2, 1)$	$53: P_{457} = (0,0,6,1)$
$10: P_{94} = (4, 2, 0, 1)$	$32: P_{227} = (2, 3, 2, 1)$	$54: P_{471} = (6, 1, 6, 1)$
11: $P_{104} = (6, 3, 0, 1)$	$33: P_{236} = (3,4,2,1)$	$55: P_{502} = (5, 5, 6, 1)$
$12: P_{113} = (7, 4, 0, 1)$	$34: P_{237} = (4, 4, 2, 1)$	$56: P_{521} = (0, 0, 7, 1)$
13: $P_{117} = (3, 5, 0, 1)$	$35: P_{239} = (6, 4, 2, 1)$	$57: P_{539} = (2, 2, 7, 1)$
$14: P_{127} = (5, 6, 0, 1)$	$36: P_{248} = (7, 5, 2, 1)$	$58: P_{542} = (5, 2, 7, 1)$
15: $P_{132} = (2,7,0,1)$	$37: P_{252} = (3, 6, 2, 1)$	$59: P_{543} = (6, 2, 7, 1)$
16: $P_{138} = (0, 0, 1, 1)$	$38: P_{265} = (0,0,3,1)$	$60: P_{549} = (4, 3, 7, 1)$
17: $P_{147} = (2, 1, 1, 1)$	$39: P_{276} = (3, 1, 3, 1)$	$61: P_{567} = (6, 5, 7, 1)$
$18: P_{149} = (4, 1, 1, 1)$	$40: P_{319} = (6, 6, 3, 1)$	$62: P_{576} = (7, 6, 7, 1)$
$19: P_{152} = (7, 1, 1, 1)$	$41: P_{329} = (0, 0, 4, 1)$	$63: P_{578} = (1,7,7,1)$
$20: P_{160} = (7, 2, 1, 1)$	$42: P_{358} = (5, 3, 4, 1)$	$64: P_{583} = (6, 7, 7, 1)$
$21: P_{162} = (1, 3, 1, 1)$	$43: P_{362} = (1, 4, 4, 1)$	000 (*)*)*)