

Rank-65618 over GF(16)

January 15, 2021

The equation

The equation of the surface is :

$$X_0^3 + X_1^3 + X_2^3 + X_3^3 + X_0^2 X_3 + X_0 X_1 X_2 = 0$$

(1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

The point rank of the equation over GF(16) is 303112742

General information

Number of lines	12
Number of points	321
Number of singular points	3
Number of Eckardt points	0
Number of double points	18
Number of single points	156
Number of points off lines	144
Number of Hesse planes	0
Number of axes	0
Type of points on lines	17^{12}
Type of lines on points	$4^3, 2^{18}, 1^{156}, 0^{144}$

Singular Points

The surface has 3 singular points:

$$0 : P_4 = \mathbf{P}(1, 1, 1, 1) = \mathbf{P}(1, 1, 1, 1)$$

$$1 : P_{3010} = \mathbf{P}(1, \delta^5, \delta^{10}, 1) = \mathbf{P}(1, 11, 10, 1)$$

$$2 : P_{3250} = \mathbf{P}(1, \delta^{10}, \delta^5, 1) = \mathbf{P}(1, 10, 11, 1)$$

The 12 Lines

The lines and their Pluecker coordinates are:

$$\ell_0 = \left[\begin{array}{cccc} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{array} \right]_{274} = \left[\begin{array}{cccc} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \end{array} \right]_{274} = \mathbf{Pl}(1, 0, 1, 0, 0, 1)_{4657}$$

$$\begin{aligned}
\ell_1 &= \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 1 & \delta^5 & 0 \end{bmatrix}_{2741} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{2741} = \mathbf{Pl}(11, 0, 10, 0, 0, 1)_{4946} \\
\ell_2 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 1 & \delta^{10} & 0 \end{bmatrix}_{3013} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 10 & 0 \end{bmatrix}_{3013} = \mathbf{Pl}(10, 0, 11, 0, 0, 1)_{4976} \\
\ell_3 &= \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{530} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}_{530} = \mathbf{Pl}(0, 0, 1, 1, 1, 1)_{9426} \\
\ell_4 &= \begin{bmatrix} 1 & \delta^5 & 0 & 0 \\ 0 & 0 & 1 & \delta^5 \end{bmatrix}_{3270} = \begin{bmatrix} 1 & 11 & 0 & 0 \\ 0 & 0 & 1 & 11 \end{bmatrix}_{3270} = \mathbf{Pl}(0, 0, 10, 11, 1, 1)_{9705} \\
\ell_5 &= \begin{bmatrix} 1 & \delta^{10} & 0 & 0 \\ 0 & 0 & 1 & \delta^{10} \end{bmatrix}_{2996} = \begin{bmatrix} 1 & 10 & 0 & 0 \\ 0 & 0 & 1 & 10 \end{bmatrix}_{2996} = \mathbf{Pl}(0, 0, 11, 10, 1, 1)_{9736} \\
\ell_6 &= \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{289} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}_{289} = \mathbf{Pl}(1, 1, 0, 0, 1, 1)_{8961} \\
\ell_7 &= \begin{bmatrix} 1 & 0 & \delta^5 & 0 \\ 0 & 1 & 0 & \delta^5 \end{bmatrix}_{3179} = \begin{bmatrix} 1 & 0 & 11 & 0 \\ 0 & 1 & 0 & 11 \end{bmatrix}_{3179} = \mathbf{Pl}(10, 11, 0, 0, 1, 1)_{8970} \\
\ell_8 &= \begin{bmatrix} 1 & 0 & \delta^{10} & 0 \\ 0 & 1 & 0 & \delta^{10} \end{bmatrix}_{2890} = \begin{bmatrix} 1 & 0 & 10 & 0 \\ 0 & 1 & 0 & 10 \end{bmatrix}_{2890} = \mathbf{Pl}(11, 10, 0, 0, 1, 1)_{8971} \\
\ell_9 &= \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4642} = \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}_{4642} = \mathbf{Pl}(1, 1, 1, 1, 0, 1)_{5586} \\
\ell_{10} &= \begin{bmatrix} 1 & 0 & \delta^{10} & 1 \\ 0 & 1 & \delta^5 & 0 \end{bmatrix}_{7109} = \begin{bmatrix} 1 & 0 & 10 & 1 \\ 0 & 1 & 11 & 0 \end{bmatrix}_{7109} = \mathbf{Pl}(11, 10, 10, 11, 0, 1)_{7981} \\
\ell_{11} &= \begin{bmatrix} 1 & 0 & \delta^5 & 1 \\ 0 & 1 & \delta^{10} & 0 \end{bmatrix}_{7381} = \begin{bmatrix} 1 & 0 & 11 & 1 \\ 0 & 1 & 10 & 0 \end{bmatrix}_{7381} = \mathbf{Pl}(10, 11, 11, 10, 0, 1)_{7770}
\end{aligned}$$

Rank of lines: (274, 2741, 3013, 530, 3270, 2996, 289, 3179, 2890, 4642, 7109, 7381)

Rank of points on Klein quadric: (4657, 4946, 4976, 9426, 9705, 9736, 8961, 8970, 8971, 5586, 7981, 7770)

Eckardt Points

The surface has 0 Eckardt points:

Double Points

The surface has 18 Double points:

The double points on the surface are:

$$\begin{aligned}
P_{205} &= (10, 11, 1, 0) = \ell_0 \cap \ell_1 \\
P_{190} &= (11, 10, 1, 0) = \ell_0 \cap \ell_2 \\
P_5 &= (1, 1, 0, 0) = \ell_0 \cap \ell_3 \\
P_{20} &= (1, 0, 1, 0) = \ell_0 \cap \ell_6 \\
P_{35} &= (0, 1, 1, 0) = \ell_0 \cap \ell_9 \\
P_{36} &= (1, 1, 1, 0) = \ell_1 \cap \ell_2 \\
P_{14} &= (10, 1, 0, 0) = \ell_1 \cap \ell_4 \\
P_{30} &= (11, 0, 1, 0) = \ell_1 \cap \ell_8 \\
P_{179} &= (0, 10, 1, 0) = \ell_1 \cap \ell_{10} \\
P_{15} &= (11, 1, 0, 0) = \ell_2 \cap \ell_5
\end{aligned}$$

$$\begin{aligned}
P_{29} &= (10, 0, 1, 0) = \ell_2 \cap \ell_7 \\
P_{195} &= (0, 11, 1, 0) = \ell_2 \cap \ell_{11} \\
P_{699} &= (10, 10, 1, 1) = \ell_3 \cap \ell_7 \\
P_{716} &= (11, 11, 1, 1) = \ell_3 \cap \ell_8 \\
P_{2859} &= (10, 1, 10, 1) = \ell_4 \cap \ell_6 \\
P_{3004} &= (11, 10, 10, 1) = \ell_4 \cap \ell_7 \\
P_{3116} &= (11, 1, 11, 1) = \ell_5 \cap \ell_6 \\
P_{3275} &= (10, 11, 11, 1) = \ell_5 \cap \ell_8
\end{aligned}$$

Single Points

The surface has 156 single points:
The single points on the surface are:

- | | |
|---|--|
| 0 : $P_{54} = (3, 2, 1, 0)$ lies on line ℓ_0 | 48 : $P_{631} = (6, 6, 1, 1)$ lies on line ℓ_3 |
| 1 : $P_{56} = (5, 2, 1, 0)$ lies on line ℓ_2 | 49 : $P_{648} = (7, 7, 1, 1)$ lies on line ℓ_3 |
| 2 : $P_{57} = (6, 2, 1, 0)$ lies on line ℓ_1 | 50 : $P_{665} = (8, 8, 1, 1)$ lies on line ℓ_3 |
| 3 : $P_{69} = (2, 3, 1, 0)$ lies on line ℓ_0 | 51 : $P_{682} = (9, 9, 1, 1)$ lies on line ℓ_3 |
| 4 : $P_{79} = (12, 3, 1, 0)$ lies on line ℓ_1 | 52 : $P_{733} = (12, 12, 1, 1)$ lies on line ℓ_3 |
| 5 : $P_{81} = (14, 3, 1, 0)$ lies on line ℓ_2 | 53 : $P_{750} = (13, 13, 1, 1)$ lies on line ℓ_3 |
| 6 : $P_{88} = (5, 4, 1, 0)$ lies on line ℓ_0 | 54 : $P_{767} = (14, 14, 1, 1)$ lies on line ℓ_3 |
| 7 : $P_{91} = (8, 4, 1, 0)$ lies on line ℓ_1 | 55 : $P_{784} = (15, 15, 1, 1)$ lies on line ℓ_3 |
| 8 : $P_{96} = (13, 4, 1, 0)$ lies on line ℓ_2 | 56 : $P_{803} = (2, 1, 2, 1)$ lies on line ℓ_6 |
| 9 : $P_{101} = (2, 5, 1, 0)$ lies on line ℓ_1 | 57 : $P_{834} = (1, 3, 2, 1)$ lies on line ℓ_9 |
| 10 : $P_{103} = (4, 5, 1, 0)$ lies on line ℓ_0 | 58 : $P_{866} = (1, 5, 2, 1)$ lies on line ℓ_{11} |
| 11 : $P_{105} = (6, 5, 1, 0)$ lies on line ℓ_2 | 59 : $P_{882} = (1, 6, 2, 1)$ lies on line ℓ_{10} |
| 12 : $P_{117} = (2, 6, 1, 0)$ lies on line ℓ_2 | 60 : $P_{958} = (13, 10, 2, 1)$ lies on line ℓ_7 |
| 13 : $P_{120} = (5, 6, 1, 0)$ lies on line ℓ_1 | 61 : $P_{976} = (15, 11, 2, 1)$ lies on line ℓ_8 |
| 14 : $P_{122} = (7, 6, 1, 0)$ lies on line ℓ_0 | 62 : $P_{1060} = (3, 1, 3, 1)$ lies on line ℓ_6 |
| 15 : $P_{137} = (6, 7, 1, 0)$ lies on line ℓ_0 | 63 : $P_{1074} = (1, 2, 3, 1)$ lies on line ℓ_9 |
| 16 : $P_{140} = (9, 7, 1, 0)$ lies on line ℓ_2 | 64 : $P_{1208} = (7, 10, 3, 1)$ lies on line ℓ_7 |
| 17 : $P_{146} = (15, 7, 1, 0)$ lies on line ℓ_1 | 65 : $P_{1221} = (4, 11, 3, 1)$ lies on line ℓ_8 |
| 18 : $P_{151} = (4, 8, 1, 0)$ lies on line ℓ_2 | 66 : $P_{1234} = (1, 12, 3, 1)$ lies on line ℓ_{10} |
| 19 : $P_{156} = (9, 8, 1, 0)$ lies on line ℓ_0 | 67 : $P_{1266} = (1, 14, 3, 1)$ lies on line ℓ_{11} |
| 20 : $P_{160} = (13, 8, 1, 0)$ lies on line ℓ_1 | 68 : $P_{1317} = (4, 1, 4, 1)$ lies on line ℓ_6 |
| 21 : $P_{170} = (7, 9, 1, 0)$ lies on line ℓ_1 | 69 : $P_{1378} = (1, 5, 4, 1)$ lies on line ℓ_9 |
| 22 : $P_{171} = (8, 9, 1, 0)$ lies on line ℓ_0 | 70 : $P_{1426} = (1, 8, 4, 1)$ lies on line ℓ_{10} |
| 23 : $P_{178} = (15, 9, 1, 0)$ lies on line ℓ_2 | 71 : $P_{1460} = (3, 10, 4, 1)$ lies on line ℓ_7 |
| 24 : $P_{214} = (3, 12, 1, 0)$ lies on line ℓ_2 | 72 : $P_{1480} = (7, 11, 4, 1)$ lies on line ℓ_8 |
| 25 : $P_{224} = (13, 12, 1, 0)$ lies on line ℓ_0 | 73 : $P_{1506} = (1, 13, 4, 1)$ lies on line ℓ_{11} |
| 26 : $P_{225} = (14, 12, 1, 0)$ lies on line ℓ_1 | 74 : $P_{1574} = (5, 1, 5, 1)$ lies on line ℓ_6 |
| 27 : $P_{231} = (4, 13, 1, 0)$ lies on line ℓ_1 | 75 : $P_{1586} = (1, 2, 5, 1)$ lies on line ℓ_{10} |
| 28 : $P_{235} = (8, 13, 1, 0)$ lies on line ℓ_2 | 76 : $P_{1618} = (1, 4, 5, 1)$ lies on line ℓ_9 |
| 29 : $P_{239} = (12, 13, 1, 0)$ lies on line ℓ_0 | 77 : $P_{1650} = (1, 6, 5, 1)$ lies on line ℓ_{11} |
| 30 : $P_{246} = (3, 14, 1, 0)$ lies on line ℓ_1 | 78 : $P_{1722} = (9, 10, 5, 1)$ lies on line ℓ_7 |
| 31 : $P_{255} = (12, 14, 1, 0)$ lies on line ℓ_2 | 79 : $P_{1741} = (12, 11, 5, 1)$ lies on line ℓ_8 |
| 32 : $P_{258} = (15, 14, 1, 0)$ lies on line ℓ_0 | 80 : $P_{1831} = (6, 1, 6, 1)$ lies on line ℓ_6 |
| 33 : $P_{266} = (7, 15, 1, 0)$ lies on line ℓ_2 | 81 : $P_{1842} = (1, 2, 6, 1)$ lies on line ℓ_{11} |
| 34 : $P_{268} = (9, 15, 1, 0)$ lies on line ℓ_1 | 82 : $P_{1890} = (1, 5, 6, 1)$ lies on line ℓ_{10} |
| 35 : $P_{273} = (14, 15, 1, 0)$ lies on line ℓ_0 | 83 : $P_{1922} = (1, 7, 6, 1)$ lies on line ℓ_9 |
| 36 : $P_{290} = (0, 1, 0, 1)$ lies on line ℓ_6 | 84 : $P_{1983} = (14, 10, 6, 1)$ lies on line ℓ_7 |
| 37 : $P_{291} = (1, 1, 0, 1)$ lies on line ℓ_9 | 85 : $P_{1993} = (8, 11, 6, 1)$ lies on line ℓ_8 |
| 38 : $P_{434} = (0, 10, 0, 1)$ lies on line ℓ_7 | 86 : $P_{2088} = (7, 1, 7, 1)$ lies on line ℓ_6 |
| 39 : $P_{435} = (1, 10, 0, 1)$ lies on line ℓ_{11} | 87 : $P_{2162} = (1, 6, 7, 1)$ lies on line ℓ_9 |
| 40 : $P_{450} = (0, 11, 0, 1)$ lies on line ℓ_8 | 88 : $P_{2210} = (1, 9, 7, 1)$ lies on line ℓ_{11} |
| 41 : $P_{451} = (1, 11, 0, 1)$ lies on line ℓ_{10} | 89 : $P_{2229} = (4, 10, 7, 1)$ lies on line ℓ_7 |
| 42 : $P_{530} = (0, 0, 1, 1)$ lies on line ℓ_3 | 90 : $P_{2244} = (3, 11, 7, 1)$ lies on line ℓ_8 |
| 43 : $P_{531} = (1, 0, 1, 1)$ lies on line ℓ_9 | 91 : $P_{2306} = (1, 15, 7, 1)$ lies on line ℓ_{10} |
| 44 : $P_{563} = (2, 2, 1, 1)$ lies on line ℓ_3 | 92 : $P_{2345} = (8, 1, 8, 1)$ lies on line ℓ_6 |
| 45 : $P_{580} = (3, 3, 1, 1)$ lies on line ℓ_3 | 93 : $P_{2386} = (1, 4, 8, 1)$ lies on line ℓ_{11} |
| 46 : $P_{597} = (4, 4, 1, 1)$ lies on line ℓ_3 | 94 : $P_{2466} = (1, 9, 8, 1)$ lies on line ℓ_9 |
| 47 : $P_{614} = (5, 5, 1, 1)$ lies on line ℓ_3 | 95 : $P_{2487} = (6, 10, 8, 1)$ lies on line ℓ_7 |

- 96 : $P_{2511} = (14, 11, 8, 1)$ lies on line ℓ_8
 97 : $P_{2530} = (1, 13, 8, 1)$ lies on line ℓ_{10}
 98 : $P_{2602} = (9, 1, 9, 1)$ lies on line ℓ_6
 99 : $P_{2690} = (1, 7, 9, 1)$ lies on line ℓ_{10}
 100 : $P_{2706} = (1, 8, 9, 1)$ lies on line ℓ_9
 101 : $P_{2749} = (12, 10, 9, 1)$ lies on line ℓ_7
 102 : $P_{2758} = (5, 11, 9, 1)$ lies on line ℓ_8
 103 : $P_{2818} = (1, 15, 9, 1)$ lies on line ℓ_{11}
 104 : $P_{2833} = (0, 0, 10, 1)$ lies on line ℓ_4
 105 : $P_{2834} = (1, 0, 10, 1)$ lies on line ℓ_{10}
 106 : $P_{2878} = (13, 2, 10, 1)$ lies on line ℓ_4
 107 : $P_{2888} = (7, 3, 10, 1)$ lies on line ℓ_4
 108 : $P_{2900} = (3, 4, 10, 1)$ lies on line ℓ_4
 109 : $P_{2922} = (9, 5, 10, 1)$ lies on line ℓ_4
 110 : $P_{2943} = (14, 6, 10, 1)$ lies on line ℓ_4
 111 : $P_{2949} = (4, 7, 10, 1)$ lies on line ℓ_4
 112 : $P_{2967} = (6, 8, 10, 1)$ lies on line ℓ_4
 113 : $P_{2989} = (12, 9, 10, 1)$ lies on line ℓ_4
 114 : $P_{3030} = (5, 12, 10, 1)$ lies on line ℓ_4
 115 : $P_{3056} = (15, 13, 10, 1)$ lies on line ℓ_4
 116 : $P_{3065} = (8, 14, 10, 1)$ lies on line ℓ_4
 117 : $P_{3075} = (2, 15, 10, 1)$ lies on line ℓ_4
 118 : $P_{3089} = (0, 0, 11, 1)$ lies on line ℓ_5
 119 : $P_{3090} = (1, 0, 11, 1)$ lies on line ℓ_{11}
 120 : $P_{3136} = (15, 2, 11, 1)$ lies on line ℓ_5
 121 : $P_{3141} = (4, 3, 11, 1)$ lies on line ℓ_5
 122 : $P_{3160} = (7, 4, 11, 1)$ lies on line ℓ_5
 123 : $P_{3181} = (12, 5, 11, 1)$ lies on line ℓ_5
 124 : $P_{3193} = (8, 6, 11, 1)$ lies on line ℓ_5
 125 : $P_{3204} = (3, 7, 11, 1)$ lies on line ℓ_5
 126 : $P_{3231} = (14, 8, 11, 1)$ lies on line ℓ_5
 127 : $P_{3238} = (5, 9, 11, 1)$ lies on line ℓ_5
 128 : $P_{3290} = (9, 12, 11, 1)$ lies on line ℓ_5
 129 : $P_{3299} = (2, 13, 11, 1)$ lies on line ℓ_5
 130 : $P_{3319} = (6, 14, 11, 1)$ lies on line ℓ_5
 131 : $P_{3342} = (13, 15, 11, 1)$ lies on line ℓ_5
 132 : $P_{3373} = (12, 1, 12, 1)$ lies on line ℓ_6
 133 : $P_{3394} = (1, 3, 12, 1)$ lies on line ℓ_{11}
 134 : $P_{3510} = (5, 10, 12, 1)$ lies on line ℓ_7
 135 : $P_{3530} = (9, 11, 12, 1)$ lies on line ℓ_8
 136 : $P_{3554} = (1, 13, 12, 1)$ lies on line ℓ_9
 137 : $P_{3570} = (1, 14, 12, 1)$ lies on line ℓ_{10}
 138 : $P_{3630} = (13, 1, 13, 1)$ lies on line ℓ_6
 139 : $P_{3666} = (1, 4, 13, 1)$ lies on line ℓ_{10}
 140 : $P_{3730} = (1, 8, 13, 1)$ lies on line ℓ_{11}
 141 : $P_{3776} = (15, 10, 13, 1)$ lies on line ℓ_7
 142 : $P_{3779} = (2, 11, 13, 1)$ lies on line ℓ_8
 143 : $P_{3794} = (1, 12, 13, 1)$ lies on line ℓ_9
 144 : $P_{3887} = (14, 1, 14, 1)$ lies on line ℓ_6
 145 : $P_{3906} = (1, 3, 14, 1)$ lies on line ℓ_{10}
 146 : $P_{4025} = (8, 10, 14, 1)$ lies on line ℓ_7
 147 : $P_{4039} = (6, 11, 14, 1)$ lies on line ℓ_8
 148 : $P_{4050} = (1, 12, 14, 1)$ lies on line ℓ_{11}
 149 : $P_{4098} = (1, 15, 14, 1)$ lies on line ℓ_9
 150 : $P_{4144} = (15, 1, 15, 1)$ lies on line ℓ_6
 151 : $P_{4226} = (1, 7, 15, 1)$ lies on line ℓ_{11}
 152 : $P_{4258} = (1, 9, 15, 1)$ lies on line ℓ_{10}
 153 : $P_{4275} = (2, 10, 15, 1)$ lies on line ℓ_7
 154 : $P_{4302} = (13, 11, 15, 1)$ lies on line ℓ_8
 155 : $P_{4338} = (1, 14, 15, 1)$ lies on line ℓ_9

The single points on the surface are:

Points on surface but on no line

The surface has 144 points not on any line:

The points on the surface but not on lines are:

- 0 : $P_{586} = (9, 3, 1, 1)$
 1 : $P_{588} = (11, 3, 1, 1)$
 2 : $P_{619} = (10, 5, 1, 1)$
 3 : $P_{623} = (14, 5, 1, 1)$
 4 : $P_{659} = (2, 8, 1, 1)$
 5 : $P_{668} = (11, 8, 1, 1)$
 6 : $P_{691} = (2, 10, 1, 1)$
 7 : $P_{698} = (9, 10, 1, 1)$
 8 : $P_{709} = (4, 11, 1, 1)$
 9 : $P_{719} = (14, 11, 1, 1)$
 10 : $P_{773} = (4, 15, 1, 1)$
 11 : $P_{779} = (10, 15, 1, 1)$
 12 : $P_{825} = (8, 2, 2, 1)$
 13 : $P_{845} = (12, 3, 2, 1)$
 14 : $P_{876} = (11, 5, 2, 1)$
 15 : $P_{888} = (7, 6, 2, 1)$
 16 : $P_{910} = (13, 7, 2, 1)$
 17 : $P_{919} = (6, 8, 2, 1)$
 18 : $P_{965} = (4, 11, 2, 1)$
 19 : $P_{971} = (10, 11, 2, 1)$
 20 : $P_{1006} = (13, 13, 2, 1)$
 21 : $P_{1066} = (9, 1, 3, 1)$
 22 : $P_{1068} = (11, 1, 3, 1)$
 23 : $P_{1085} = (12, 2, 3, 1)$
 24 : $P_{1096} = (7, 3, 3, 1)$
 25 : $P_{1168} = (15, 7, 3, 1)$

26 : $P_{1192} = (7, 9, 3, 1)$	80 : $P_{2763} = (10, 11, 9, 1)$
27 : $P_{1239} = (6, 12, 3, 1)$	81 : $P_{2767} = (14, 11, 9, 1)$
28 : $P_{1262} = (13, 13, 3, 1)$	82 : $P_{2781} = (12, 12, 9, 1)$
29 : $P_{1275} = (10, 14, 3, 1)$	83 : $P_{2828} = (11, 15, 9, 1)$
30 : $P_{1376} = (15, 4, 4, 1)$	84 : $P_{2851} = (2, 1, 10, 1)$
31 : $P_{1383} = (6, 5, 4, 1)$	85 : $P_{2858} = (9, 1, 10, 1)$
32 : $P_{1416} = (7, 7, 4, 1)$	86 : $P_{2906} = (9, 4, 10, 1)$
33 : $P_{1435} = (10, 8, 4, 1)$	87 : $P_{2908} = (11, 4, 10, 1)$
34 : $P_{1466} = (9, 10, 4, 1)$	88 : $P_{2997} = (4, 10, 10, 1)$
35 : $P_{1468} = (11, 10, 4, 1)$	89 : $P_{3007} = (14, 10, 10, 1)$
36 : $P_{1496} = (7, 12, 4, 1)$	90 : $P_{3035} = (10, 12, 10, 1)$
37 : $P_{1517} = (12, 13, 4, 1)$	91 : $P_{3039} = (14, 12, 10, 1)$
38 : $P_{1550} = (13, 15, 4, 1)$	92 : $P_{3045} = (4, 13, 10, 1)$
39 : $P_{1579} = (10, 1, 5, 1)$	93 : $P_{3051} = (10, 13, 10, 1)$
40 : $P_{1583} = (14, 1, 5, 1)$	94 : $P_{3059} = (2, 14, 10, 1)$
41 : $P_{1596} = (11, 2, 5, 1)$	95 : $P_{3068} = (11, 14, 10, 1)$
42 : $P_{1623} = (6, 4, 5, 1)$	96 : $P_{3109} = (4, 1, 11, 1)$
43 : $P_{1645} = (12, 5, 5, 1)$	97 : $P_{3119} = (14, 1, 11, 1)$
44 : $P_{1662} = (13, 6, 5, 1)$	98 : $P_{3125} = (4, 2, 11, 1)$
45 : $P_{1672} = (7, 7, 5, 1)$	99 : $P_{3131} = (10, 2, 11, 1)$
46 : $P_{1748} = (3, 12, 5, 1)$	100 : $P_{3187} = (2, 6, 11, 1)$
47 : $P_{1789} = (12, 14, 5, 1)$	101 : $P_{3196} = (11, 6, 11, 1)$
48 : $P_{1848} = (7, 2, 6, 1)$	102 : $P_{3210} = (9, 7, 11, 1)$
49 : $P_{1902} = (13, 5, 6, 1)$	103 : $P_{3212} = (11, 7, 11, 1)$
50 : $P_{1931} = (10, 7, 6, 1)$	104 : $P_{3243} = (10, 9, 11, 1)$
51 : $P_{1942} = (5, 8, 6, 1)$	105 : $P_{3247} = (14, 9, 11, 1)$
52 : $P_{1965} = (12, 9, 6, 1)$	106 : $P_{3267} = (2, 11, 11, 1)$
53 : $P_{1987} = (2, 11, 6, 1)$	107 : $P_{3274} = (9, 11, 11, 1)$
54 : $P_{1996} = (11, 11, 6, 1)$	108 : $P_{3399} = (6, 3, 12, 1)$
55 : $P_{2039} = (6, 14, 6, 1)$	109 : $P_{3416} = (7, 4, 12, 1)$
56 : $P_{2055} = (6, 15, 6, 1)$	110 : $P_{3428} = (3, 5, 12, 1)$
57 : $P_{2110} = (13, 2, 7, 1)$	111 : $P_{3485} = (12, 8, 12, 1)$
58 : $P_{2128} = (15, 3, 7, 1)$	112 : $P_{3501} = (12, 9, 12, 1)$
59 : $P_{2136} = (7, 4, 7, 1)$	113 : $P_{3515} = (10, 10, 12, 1)$
60 : $P_{2152} = (7, 5, 7, 1)$	114 : $P_{3519} = (14, 10, 12, 1)$
61 : $P_{2171} = (10, 6, 7, 1)$	115 : $P_{3564} = (11, 13, 12, 1)$
62 : $P_{2215} = (6, 9, 7, 1)$	116 : $P_{3582} = (13, 14, 12, 1)$
63 : $P_{2250} = (9, 11, 7, 1)$	117 : $P_{3646} = (13, 2, 13, 1)$
64 : $P_{2252} = (11, 11, 7, 1)$	118 : $P_{3662} = (13, 3, 13, 1)$
65 : $P_{2317} = (12, 15, 7, 1)$	119 : $P_{3677} = (12, 4, 13, 1)$
66 : $P_{2339} = (2, 1, 8, 1)$	120 : $P_{3736} = (7, 8, 13, 1)$
67 : $P_{2348} = (11, 1, 8, 1)$	121 : $P_{3765} = (4, 10, 13, 1)$
68 : $P_{2359} = (6, 2, 8, 1)$	122 : $P_{3771} = (10, 10, 13, 1)$
69 : $P_{2395} = (10, 4, 8, 1)$	123 : $P_{3804} = (11, 12, 13, 1)$
70 : $P_{2422} = (5, 6, 8, 1)$	124 : $P_{3831} = (6, 14, 13, 1)$
71 : $P_{2455} = (6, 8, 8, 1)$	125 : $P_{3849} = (8, 15, 13, 1)$
72 : $P_{2478} = (13, 9, 8, 1)$	126 : $P_{3915} = (10, 3, 14, 1)$
73 : $P_{2525} = (12, 12, 8, 1)$	127 : $P_{3949} = (12, 5, 14, 1)$
74 : $P_{2536} = (7, 13, 8, 1)$	128 : $P_{3959} = (6, 6, 14, 1)$
75 : $P_{2632} = (7, 3, 9, 1)$	129 : $P_{4019} = (2, 10, 14, 1)$
76 : $P_{2685} = (12, 6, 9, 1)$	130 : $P_{4028} = (11, 10, 14, 1)$
77 : $P_{2695} = (6, 7, 9, 1)$	131 : $P_{4062} = (13, 12, 14, 1)$
78 : $P_{2718} = (13, 8, 9, 1)$	132 : $P_{4071} = (6, 13, 14, 1)$
79 : $P_{2724} = (3, 9, 9, 1)$	133 : $P_{4086} = (5, 14, 14, 1)$

134 : $P_{4104} = (7, 15, 14, 1)$
 135 : $P_{4133} = (4, 1, 15, 1)$
 136 : $P_{4139} = (10, 1, 15, 1)$
 137 : $P_{4190} = (13, 4, 15, 1)$
 138 : $P_{4215} = (6, 6, 15, 1)$
 139 : $P_{4237} = (12, 7, 15, 1)$

140 : $P_{4268} = (11, 9, 15, 1)$
 141 : $P_{4329} = (8, 13, 15, 1)$
 142 : $P_{4344} = (7, 14, 15, 1)$
 143 : $P_{4366} = (13, 15, 15, 1)$

Line Intersection Graph

	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	1	1	0	0	1	0	0	1	0	0
1	1	0	1	0	1	0	0	0	1	0	1	0
2	1	1	0	0	0	1	0	1	0	0	0	1
3	1	0	0	0	0	0	1	1	1	0	1	1
4	0	1	0	0	0	0	1	1	1	1	0	1
5	0	0	1	0	0	0	1	1	1	1	1	0
6	1	0	0	1	1	1	0	0	0	0	1	1
7	0	0	1	1	1	1	0	0	0	1	1	0
8	0	1	0	1	1	1	0	0	0	1	0	1
9	1	0	0	0	1	1	0	1	1	0	1	1
10	0	1	0	1	0	1	1	1	0	1	0	1
11	0	0	1	1	1	0	1	0	1	1	1	0

Neighbor sets in the line intersection graph:

Line 0 intersects

Line	ℓ_1	ℓ_2	ℓ_3	ℓ_6	ℓ_9
in point	P_{205}	P_{190}	P_5	P_{20}	P_{35}

Line 1 intersects

Line	ℓ_0	ℓ_2	ℓ_4	ℓ_8	ℓ_{10}
in point	P_{205}	P_{36}	P_{14}	P_{30}	P_{179}

Line 2 intersects

Line	ℓ_0	ℓ_1	ℓ_5	ℓ_7	ℓ_{11}
in point	P_{190}	P_{36}	P_{15}	P_{29}	P_{195}

Line 3 intersects

Line	ℓ_0	ℓ_6	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}
in point	P_5	P_4	P_{699}	P_{716}	P_4	P_4

Line 4 intersects

Line	ℓ_1	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{11}
in point	P_{14}	P_{2859}	P_{3004}	P_{3010}	P_{3010}	P_{3010}

Line 5 intersects

Line	ℓ_2	ℓ_6	ℓ_7	ℓ_8	ℓ_9	ℓ_{10}
in point	P_{15}	P_{3116}	P_{3250}	P_{3275}	P_{3250}	P_{3250}

Line 6 intersects

Line	ℓ_0	ℓ_3	ℓ_4	ℓ_5	ℓ_{10}	ℓ_{11}
in point	P_{20}	P_4	P_{2859}	P_{3116}	P_4	P_4

Line 7 intersects

Line	ℓ_2	ℓ_3	ℓ_4	ℓ_5	ℓ_9	ℓ_{10}
in point	P_{29}	P_{699}	P_{3004}	P_{3250}	P_{3250}	P_{3250}

Line 8 intersects

Line	ℓ_1	ℓ_3	ℓ_4	ℓ_5	ℓ_9	ℓ_{11}
in point	P_{30}	P_{716}	P_{3010}	P_{3275}	P_{3010}	P_{3010}

Line 9 intersects

Line	ℓ_0	ℓ_4	ℓ_5	ℓ_7	ℓ_8	ℓ_{10}	ℓ_{11}
in point	P_{35}	P_{3010}	P_{3250}	P_{3250}	P_{3010}	P_{3250}	P_{3010}

Line 10 intersects

Line	ℓ_1	ℓ_3	ℓ_5	ℓ_6	ℓ_7	ℓ_9	ℓ_{11}
in point	P_{179}	P_4	P_{3250}	P_4	P_{3250}	P_{3250}	P_4

Line 11 intersects

Line	ℓ_2	ℓ_3	ℓ_4	ℓ_6	ℓ_8	ℓ_9	ℓ_{10}
in point	P_{195}	P_4	P_{3010}	P_4	P_{3010}	P_{3010}	P_4

The surface has 321 points:

The points on the surface are:

0 : $P_4 = (1, 1, 1, 1)$	40 : $P_{231} = (4, 13, 1, 0)$	80 : $P_{773} = (4, 15, 1, 1)$
1 : $P_5 = (1, 1, 0, 0)$	41 : $P_{235} = (8, 13, 1, 0)$	81 : $P_{779} = (10, 15, 1, 1)$
2 : $P_{14} = (10, 1, 0, 0)$	42 : $P_{239} = (12, 13, 1, 0)$	82 : $P_{784} = (15, 15, 1, 1)$
3 : $P_{15} = (11, 1, 0, 0)$	43 : $P_{246} = (3, 14, 1, 0)$	83 : $P_{803} = (2, 1, 2, 1)$
4 : $P_{20} = (1, 0, 1, 0)$	44 : $P_{255} = (12, 14, 1, 0)$	84 : $P_{825} = (8, 2, 2, 1)$
5 : $P_{29} = (10, 0, 1, 0)$	45 : $P_{258} = (15, 14, 1, 0)$	85 : $P_{834} = (1, 3, 2, 1)$
6 : $P_{30} = (11, 0, 1, 0)$	46 : $P_{266} = (7, 15, 1, 0)$	86 : $P_{845} = (12, 3, 2, 1)$
7 : $P_{35} = (0, 1, 1, 0)$	47 : $P_{268} = (9, 15, 1, 0)$	87 : $P_{866} = (1, 5, 2, 1)$
8 : $P_{36} = (1, 1, 1, 0)$	48 : $P_{273} = (14, 15, 1, 0)$	88 : $P_{876} = (11, 5, 2, 1)$
9 : $P_{54} = (3, 2, 1, 0)$	49 : $P_{290} = (0, 1, 0, 1)$	89 : $P_{882} = (1, 6, 2, 1)$
10 : $P_{56} = (5, 2, 1, 0)$	50 : $P_{291} = (1, 1, 0, 1)$	90 : $P_{888} = (7, 6, 2, 1)$
11 : $P_{57} = (6, 2, 1, 0)$	51 : $P_{434} = (0, 10, 0, 1)$	91 : $P_{910} = (13, 7, 2, 1)$
12 : $P_{69} = (2, 3, 1, 0)$	52 : $P_{435} = (1, 10, 0, 1)$	92 : $P_{919} = (6, 8, 2, 1)$
13 : $P_{79} = (12, 3, 1, 0)$	53 : $P_{450} = (0, 11, 0, 1)$	93 : $P_{958} = (13, 10, 2, 1)$
14 : $P_{81} = (14, 3, 1, 0)$	54 : $P_{451} = (1, 11, 0, 1)$	94 : $P_{965} = (4, 11, 2, 1)$
15 : $P_{88} = (5, 4, 1, 0)$	55 : $P_{530} = (0, 0, 1, 1)$	95 : $P_{971} = (10, 11, 2, 1)$
16 : $P_{91} = (8, 4, 1, 0)$	56 : $P_{531} = (1, 0, 1, 1)$	96 : $P_{976} = (15, 11, 2, 1)$
17 : $P_{96} = (13, 4, 1, 0)$	57 : $P_{563} = (2, 2, 1, 1)$	97 : $P_{1006} = (13, 13, 2, 1)$
18 : $P_{101} = (2, 5, 1, 0)$	58 : $P_{580} = (3, 3, 1, 1)$	98 : $P_{1060} = (3, 1, 3, 1)$
19 : $P_{103} = (4, 5, 1, 0)$	59 : $P_{586} = (9, 3, 1, 1)$	99 : $P_{1066} = (9, 1, 3, 1)$
20 : $P_{105} = (6, 5, 1, 0)$	60 : $P_{588} = (11, 3, 1, 1)$	100 : $P_{1068} = (11, 1, 3, 1)$
21 : $P_{117} = (2, 6, 1, 0)$	61 : $P_{597} = (4, 4, 1, 1)$	101 : $P_{1074} = (1, 2, 3, 1)$
22 : $P_{120} = (5, 6, 1, 0)$	62 : $P_{614} = (5, 5, 1, 1)$	102 : $P_{1085} = (12, 2, 3, 1)$
23 : $P_{122} = (7, 6, 1, 0)$	63 : $P_{619} = (10, 5, 1, 1)$	103 : $P_{1096} = (7, 3, 3, 1)$
24 : $P_{137} = (6, 7, 1, 0)$	64 : $P_{623} = (14, 5, 1, 1)$	104 : $P_{1168} = (15, 7, 3, 1)$
25 : $P_{140} = (9, 7, 1, 0)$	65 : $P_{631} = (6, 6, 1, 1)$	105 : $P_{1192} = (7, 9, 3, 1)$
26 : $P_{146} = (15, 7, 1, 0)$	66 : $P_{648} = (7, 7, 1, 1)$	106 : $P_{1208} = (7, 10, 3, 1)$
27 : $P_{151} = (4, 8, 1, 0)$	67 : $P_{659} = (2, 8, 1, 1)$	107 : $P_{1221} = (4, 11, 3, 1)$
28 : $P_{156} = (9, 8, 1, 0)$	68 : $P_{665} = (8, 8, 1, 1)$	108 : $P_{1234} = (1, 12, 3, 1)$
29 : $P_{160} = (13, 8, 1, 0)$	69 : $P_{668} = (11, 8, 1, 1)$	109 : $P_{1239} = (6, 12, 3, 1)$
30 : $P_{170} = (7, 9, 1, 0)$	70 : $P_{682} = (9, 9, 1, 1)$	110 : $P_{1262} = (13, 13, 3, 1)$
31 : $P_{171} = (8, 9, 1, 0)$	71 : $P_{691} = (2, 10, 1, 1)$	111 : $P_{1266} = (1, 14, 3, 1)$
32 : $P_{178} = (15, 9, 1, 0)$	72 : $P_{698} = (9, 10, 1, 1)$	112 : $P_{1275} = (10, 14, 3, 1)$
33 : $P_{179} = (0, 10, 1, 0)$	73 : $P_{699} = (10, 10, 1, 1)$	113 : $P_{1317} = (4, 1, 4, 1)$
34 : $P_{190} = (11, 10, 1, 0)$	74 : $P_{709} = (4, 11, 1, 1)$	114 : $P_{1376} = (15, 4, 4, 1)$
35 : $P_{195} = (0, 11, 1, 0)$	75 : $P_{716} = (11, 11, 1, 1)$	115 : $P_{1378} = (1, 5, 4, 1)$
36 : $P_{205} = (10, 11, 1, 0)$	76 : $P_{719} = (14, 11, 1, 1)$	116 : $P_{1383} = (6, 5, 4, 1)$
37 : $P_{214} = (3, 12, 1, 0)$	77 : $P_{733} = (12, 12, 1, 1)$	117 : $P_{1416} = (7, 7, 4, 1)$
38 : $P_{224} = (13, 12, 1, 0)$	78 : $P_{750} = (13, 13, 1, 1)$	118 : $P_{1426} = (1, 8, 4, 1)$
39 : $P_{225} = (14, 12, 1, 0)$	79 : $P_{767} = (14, 14, 1, 1)$	119 : $P_{1435} = (10, 8, 4, 1)$

120 : $P_{1460} = (3, 10, 4, 1)$	174 : $P_{2345} = (8, 1, 8, 1)$	228 : $P_{3059} = (2, 14, 10, 1)$
121 : $P_{1466} = (9, 10, 4, 1)$	175 : $P_{2348} = (11, 1, 8, 1)$	229 : $P_{3065} = (8, 14, 10, 1)$
122 : $P_{1468} = (11, 10, 4, 1)$	176 : $P_{2359} = (6, 2, 8, 1)$	230 : $P_{3068} = (11, 14, 10, 1)$
123 : $P_{1480} = (7, 11, 4, 1)$	177 : $P_{2386} = (1, 4, 8, 1)$	231 : $P_{3075} = (2, 15, 10, 1)$
124 : $P_{1496} = (7, 12, 4, 1)$	178 : $P_{2395} = (10, 4, 8, 1)$	232 : $P_{3089} = (0, 0, 11, 1)$
125 : $P_{1506} = (1, 13, 4, 1)$	179 : $P_{2422} = (5, 6, 8, 1)$	233 : $P_{3090} = (1, 0, 11, 1)$
126 : $P_{1517} = (12, 13, 4, 1)$	180 : $P_{2455} = (6, 8, 8, 1)$	234 : $P_{3109} = (4, 1, 11, 1)$
127 : $P_{1550} = (13, 15, 4, 1)$	181 : $P_{2466} = (1, 9, 8, 1)$	235 : $P_{3116} = (11, 1, 11, 1)$
128 : $P_{1574} = (5, 1, 5, 1)$	182 : $P_{2478} = (13, 9, 8, 1)$	236 : $P_{3119} = (14, 1, 11, 1)$
129 : $P_{1579} = (10, 1, 5, 1)$	183 : $P_{2487} = (6, 10, 8, 1)$	237 : $P_{3125} = (4, 2, 11, 1)$
130 : $P_{1583} = (14, 1, 5, 1)$	184 : $P_{2511} = (14, 11, 8, 1)$	238 : $P_{3131} = (10, 2, 11, 1)$
131 : $P_{1586} = (1, 2, 5, 1)$	185 : $P_{2525} = (12, 12, 8, 1)$	239 : $P_{3136} = (15, 2, 11, 1)$
132 : $P_{1596} = (11, 2, 5, 1)$	186 : $P_{2530} = (1, 13, 8, 1)$	240 : $P_{3141} = (4, 3, 11, 1)$
133 : $P_{1618} = (1, 4, 5, 1)$	187 : $P_{2536} = (7, 13, 8, 1)$	241 : $P_{3160} = (7, 4, 11, 1)$
134 : $P_{1623} = (6, 4, 5, 1)$	188 : $P_{2602} = (9, 1, 9, 1)$	242 : $P_{3181} = (12, 5, 11, 1)$
135 : $P_{1645} = (12, 5, 5, 1)$	189 : $P_{2632} = (7, 3, 9, 1)$	243 : $P_{3187} = (2, 6, 11, 1)$
136 : $P_{1650} = (1, 6, 5, 1)$	190 : $P_{2685} = (12, 6, 9, 1)$	244 : $P_{3193} = (8, 6, 11, 1)$
137 : $P_{1662} = (13, 6, 5, 1)$	191 : $P_{2690} = (1, 7, 9, 1)$	245 : $P_{3196} = (11, 6, 11, 1)$
138 : $P_{1672} = (7, 7, 5, 1)$	192 : $P_{2695} = (6, 7, 9, 1)$	246 : $P_{3204} = (3, 7, 11, 1)$
139 : $P_{1722} = (9, 10, 5, 1)$	193 : $P_{2706} = (1, 8, 9, 1)$	247 : $P_{3210} = (9, 7, 11, 1)$
140 : $P_{1741} = (12, 11, 5, 1)$	194 : $P_{2718} = (13, 8, 9, 1)$	248 : $P_{3212} = (11, 7, 11, 1)$
141 : $P_{1748} = (3, 12, 5, 1)$	195 : $P_{2724} = (3, 9, 9, 1)$	249 : $P_{3231} = (14, 8, 11, 1)$
142 : $P_{1789} = (12, 14, 5, 1)$	196 : $P_{2749} = (12, 10, 9, 1)$	250 : $P_{3238} = (5, 9, 11, 1)$
143 : $P_{1831} = (6, 1, 6, 1)$	197 : $P_{2758} = (5, 11, 9, 1)$	251 : $P_{3243} = (10, 9, 11, 1)$
144 : $P_{1842} = (1, 2, 6, 1)$	198 : $P_{2763} = (10, 11, 9, 1)$	252 : $P_{3247} = (14, 9, 11, 1)$
145 : $P_{1848} = (7, 2, 6, 1)$	199 : $P_{2767} = (14, 11, 9, 1)$	253 : $P_{3250} = (1, 10, 11, 1)$
146 : $P_{1890} = (1, 5, 6, 1)$	200 : $P_{2781} = (12, 12, 9, 1)$	254 : $P_{3267} = (2, 11, 11, 1)$
147 : $P_{1902} = (13, 5, 6, 1)$	201 : $P_{2818} = (1, 15, 9, 1)$	255 : $P_{3274} = (9, 11, 11, 1)$
148 : $P_{1922} = (1, 7, 6, 1)$	202 : $P_{2828} = (11, 15, 9, 1)$	256 : $P_{3275} = (10, 11, 11, 1)$
149 : $P_{1931} = (10, 7, 6, 1)$	203 : $P_{2833} = (0, 0, 10, 1)$	257 : $P_{3290} = (9, 12, 11, 1)$
150 : $P_{1942} = (5, 8, 6, 1)$	204 : $P_{2834} = (1, 0, 10, 1)$	258 : $P_{3299} = (2, 13, 11, 1)$
151 : $P_{1965} = (12, 9, 6, 1)$	205 : $P_{2851} = (2, 1, 10, 1)$	259 : $P_{3319} = (6, 14, 11, 1)$
152 : $P_{1983} = (14, 10, 6, 1)$	206 : $P_{2858} = (9, 1, 10, 1)$	260 : $P_{3342} = (13, 15, 11, 1)$
153 : $P_{1987} = (2, 11, 6, 1)$	207 : $P_{2859} = (10, 1, 10, 1)$	261 : $P_{3373} = (12, 1, 12, 1)$
154 : $P_{1993} = (8, 11, 6, 1)$	208 : $P_{2878} = (13, 2, 10, 1)$	262 : $P_{3394} = (1, 3, 12, 1)$
155 : $P_{1996} = (11, 11, 6, 1)$	209 : $P_{2888} = (7, 3, 10, 1)$	263 : $P_{3399} = (6, 3, 12, 1)$
156 : $P_{2039} = (6, 14, 6, 1)$	210 : $P_{2900} = (3, 4, 10, 1)$	264 : $P_{3416} = (7, 4, 12, 1)$
157 : $P_{2055} = (6, 15, 6, 1)$	211 : $P_{2906} = (9, 4, 10, 1)$	265 : $P_{3428} = (3, 5, 12, 1)$
158 : $P_{2088} = (7, 1, 7, 1)$	212 : $P_{2908} = (11, 4, 10, 1)$	266 : $P_{3485} = (12, 8, 12, 1)$
159 : $P_{2110} = (13, 2, 7, 1)$	213 : $P_{2922} = (9, 5, 10, 1)$	267 : $P_{3501} = (12, 9, 12, 1)$
160 : $P_{2128} = (15, 3, 7, 1)$	214 : $P_{2943} = (14, 6, 10, 1)$	268 : $P_{3510} = (5, 10, 12, 1)$
161 : $P_{2136} = (7, 4, 7, 1)$	215 : $P_{2949} = (4, 7, 10, 1)$	269 : $P_{3515} = (10, 10, 12, 1)$
162 : $P_{2152} = (7, 5, 7, 1)$	216 : $P_{2967} = (6, 8, 10, 1)$	270 : $P_{3519} = (14, 10, 12, 1)$
163 : $P_{2162} = (1, 6, 7, 1)$	217 : $P_{2989} = (12, 9, 10, 1)$	271 : $P_{3530} = (9, 11, 12, 1)$
164 : $P_{2171} = (10, 6, 7, 1)$	218 : $P_{2997} = (4, 10, 10, 1)$	272 : $P_{3554} = (1, 13, 12, 1)$
165 : $P_{2210} = (1, 9, 7, 1)$	219 : $P_{3004} = (11, 10, 10, 1)$	273 : $P_{3564} = (11, 13, 12, 1)$
166 : $P_{2215} = (6, 9, 7, 1)$	220 : $P_{3007} = (14, 10, 10, 1)$	274 : $P_{3570} = (1, 14, 12, 1)$
167 : $P_{2229} = (4, 10, 7, 1)$	221 : $P_{3010} = (1, 11, 10, 1)$	275 : $P_{3582} = (13, 14, 12, 1)$
168 : $P_{2244} = (3, 11, 7, 1)$	222 : $P_{3030} = (5, 12, 10, 1)$	276 : $P_{3630} = (13, 1, 13, 1)$
169 : $P_{2250} = (9, 11, 7, 1)$	223 : $P_{3035} = (10, 12, 10, 1)$	277 : $P_{3646} = (13, 2, 13, 1)$
170 : $P_{2252} = (11, 11, 7, 1)$	224 : $P_{3039} = (14, 12, 10, 1)$	278 : $P_{3662} = (13, 3, 13, 1)$
171 : $P_{2306} = (1, 15, 7, 1)$	225 : $P_{3045} = (4, 13, 10, 1)$	279 : $P_{3666} = (1, 4, 13, 1)$
172 : $P_{2317} = (12, 15, 7, 1)$	226 : $P_{3051} = (10, 13, 10, 1)$	280 : $P_{3677} = (12, 4, 13, 1)$
173 : $P_{2339} = (2, 1, 8, 1)$	227 : $P_{3056} = (15, 13, 10, 1)$	281 : $P_{3730} = (1, 8, 13, 1)$

282 : $P_{3736} = (7, 8, 13, 1)$	296 : $P_{4019} = (2, 10, 14, 1)$	310 : $P_{4215} = (6, 6, 15, 1)$
283 : $P_{3765} = (4, 10, 13, 1)$	297 : $P_{4025} = (8, 10, 14, 1)$	311 : $P_{4226} = (1, 7, 15, 1)$
284 : $P_{3771} = (10, 10, 13, 1)$	298 : $P_{4028} = (11, 10, 14, 1)$	312 : $P_{4237} = (12, 7, 15, 1)$
285 : $P_{3776} = (15, 10, 13, 1)$	299 : $P_{4039} = (6, 11, 14, 1)$	313 : $P_{4258} = (1, 9, 15, 1)$
286 : $P_{3779} = (2, 11, 13, 1)$	300 : $P_{4050} = (1, 12, 14, 1)$	314 : $P_{4268} = (11, 9, 15, 1)$
287 : $P_{3794} = (1, 12, 13, 1)$	301 : $P_{4062} = (13, 12, 14, 1)$	315 : $P_{4275} = (2, 10, 15, 1)$
288 : $P_{3804} = (11, 12, 13, 1)$	302 : $P_{4071} = (6, 13, 14, 1)$	316 : $P_{4302} = (13, 11, 15, 1)$
289 : $P_{3831} = (6, 14, 13, 1)$	303 : $P_{4086} = (5, 14, 14, 1)$	317 : $P_{4329} = (8, 13, 15, 1)$
290 : $P_{3849} = (8, 15, 13, 1)$	304 : $P_{4098} = (1, 15, 14, 1)$	318 : $P_{4338} = (1, 14, 15, 1)$
291 : $P_{3887} = (14, 1, 14, 1)$	305 : $P_{4104} = (7, 15, 14, 1)$	319 : $P_{4344} = (7, 14, 15, 1)$
292 : $P_{3906} = (1, 3, 14, 1)$	306 : $P_{4133} = (4, 1, 15, 1)$	320 : $P_{4366} = (13, 15, 15, 1)$
293 : $P_{3915} = (10, 3, 14, 1)$	307 : $P_{4139} = (10, 1, 15, 1)$	
294 : $P_{3949} = (12, 5, 14, 1)$	308 : $P_{4144} = (15, 1, 15, 1)$	
295 : $P_{3959} = (6, 6, 14, 1)$	309 : $P_{4190} = (13, 4, 15, 1)$	