

#### RAJARATA UNIVERSITY OF SRI LANKA

# **FACULTY OF APPLIED SCIENCES**

# B.Sc. (General) Degree in Information and Communication Technology

# Third Year - Semester II Examination - July/August 2020

# ICT 3202 - OPERATIONAL RESEARCH

Time: Two (02) hours

- Answer any <u>FOUR (04)</u> questions.
- Calculators are allowed.
- Each question carries equal marks.
- 1. Using the graphical method solve the following Linear Programming Problems.

Minimize  $Z=40x_1+50x_2$ 

Subject to 
$$2x_1 + x_2 \le 10$$
  
 $x_1 - 2x_2 \le 0$   
 $x_1 + x_2 \ge 3$   
 $2x_1 - x_2 \ge 0$   
 $x_1, x_2 \ge 0$ 

(20 marks)

What kind of issue will be arisen if the constraint  $2x_1 + x_2 \le 10$  is changed as  $2x_1 + x_2 \ge 10$ ?

(05 marks)

2. Given below is the unit costs with suppliers S1, S2, S3 and demand D1, D2, D3 and D4.

		Cost pe	Availability		
Supplier	D1	D2	D3	D4	(supply)
S1	16	10	14	12	100
S2	24	18	8	14	90
S3	18	22	20	16	60
Demand	50	64	80	56	250

a) Find an initial solution using North West Corner method.

(10 marks)

b) Find the optimum solution for the above problem using MODI (Modified Distribution) method.

(10 marks)

c) What step would you taken if the wholesaler D4 demands 60 units?

(05 marks)

3. Machine shop has four machines (M<sub>1</sub> to M<sub>4</sub>) available for fabrication of products as per customer specifications. On one occasion, orders have been received for five jobs (J<sub>1</sub> to J<sub>5</sub>). Each job requires one machine and no machine can do more than one job. The expected profits in rupee by machine-job combinations are shown in table below.

	$J_1$	$J_2$	$J_3$	$J_4$	$J_5$
$M_1$	75	95	100	110	60
$M_2$	95	100	<b>75</b> .	90	70
$M_3$	55	75	95	90	100
M <sub>4</sub>	105	110	95	85	130

Find the optimal assignment of the jobs to machines.

Which job will not be accepted?

(25 marks)

4. The following table gives the data for the activities of a project.

Activity	A	В	С	D	Е	F	G	Н	I	J
Immediate	-	-	A	A	В	D	С	D	E,	F,
predecessor									Н	G
Time(weeks)	5	4	2	2	6	5	7	8	5	11

a) Draw the network diagram

(10 marks)

b) Find the critical path.

(05 marks)

c) If activity time of J is changed as 5 weeks what would be the project completion time?

(05 marks)

d) Which activities can be delayed more than two months without affecting the completion time of the project

(05 marks)

- 5. The arrival rate of customers to a bank counter is 15 customers per hour. The service rate of customers in system system is 20 customers per hour. Assuming that customers arrive according to a Poisson distribution and service times according to an exponential distribution. Find the followings.
  - a) The utility factor of the system.

(04 marks)

b) The average time a customer spends in the system.

(04 marks)

c) The average number of customers in the system.

(04 marks)

- d) The average time a customer spends in the queue waiting for (04 marks) service.
- e) The average number of customers in the queue.

(04 marks)

f) The probability that the system will be idle.

(05 marks)

--- End ---