

Mathematica 7 Test Results

For Integration Problems Involving Exponentials

Unable to integrate:

$$\{e^{(a+bx)^3} x^3, x, 21, 0\}$$

$$-\frac{2 a e^{(a+bx)^3}}{3 b^4} + \frac{e^{(a+bx)^3} x}{3 b^3} + \frac{(1+3 a^3) (a+bx) \operatorname{Gamma}\left[\frac{1}{3}, -(a+bx)^3\right]}{9 b^4 \left(-(a+bx)^3\right)^{1/3}} - \frac{a^2 (a+bx)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a+bx)^3\right]}{b^4 \left(-(a+bx)^3\right)^{2/3}}$$

$$\int e^{(a+bx)^3} x^3 dx$$

Unable to integrate:

$$\{e^{(a+bx)^3} x^2, x, 9, 0\}$$

$$\frac{e^{(a+bx)^3}}{3 b^3} - \frac{a^2 (a+bx) \operatorname{Gamma}\left[\frac{1}{3}, -(a+bx)^3\right]}{3 b^3 \left(-(a+bx)^3\right)^{1/3}} + \frac{2 a (a+bx)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a+bx)^3\right]}{3 b^3 \left(-(a+bx)^3\right)^{2/3}}$$

$$\int e^{(a+bx)^3} x^2 dx$$

Unable to integrate:

$$\{e^{(a+bx)^3} x, x, 5, 0\}$$

$$\frac{a (a+bx) \operatorname{Gamma}\left[\frac{1}{3}, -(a+bx)^3\right]}{3 b^2 \left(-(a+bx)^3\right)^{1/3}} - \frac{(a+bx)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a+bx)^3\right]}{3 b^2 \left(-(a+bx)^3\right)^{2/3}}$$

$$\int e^{(a+bx)^3} x dx$$

Unable to integrate:

$$\{e^{(a+bx)^n} (a+bx)^m, x, 2, 0\}$$

$$-\frac{(a+bx)^{1+m} \left(-(a+bx)^n\right)^{-\frac{1+m}{n}} \operatorname{Gamma}\left[\frac{1+m}{n}, -(a+bx)^n\right]}{b n}$$

$$\int e^{(a+bx)^n} (a+bx)^m dx$$

Unable to integrate:

$$\{f^{(a+bx)^n} (a+bx)^m, x, 2, 0\}$$

$$-\frac{(a+bx)^{1+m} \operatorname{Gamma}\left[\frac{1+m}{n}, -(a+bx)^n \operatorname{Log}[f]\right] \left(-(a+bx)^n \operatorname{Log}[f]\right)^{-\frac{1+m}{n}}}{b n}$$

$$\int f^{(a+bx)^n} (a+bx)^m dx$$

Unable to integrate:

$$\{e^{(c+dx)^3} (a+bx)^2, x, 13, 0\}$$

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$$\frac{b^2 e^{(c+dx)^3}}{3 d^3} - \frac{(b c - a d)^2 (c + d x) \text{Gamma}\left[\frac{1}{3}, -(c + d x)^3\right]}{3 d^3 \left(-(c + d x)^3\right)^{1/3}} + \frac{2 b (b c - a d) (c + d x)^2 \text{Gamma}\left[\frac{2}{3}, -(c + d x)^3\right]}{3 d^3 \left(-(c + d x)^3\right)^{2/3}}$$

$$\int e^{(c+dx)^3} (a + b x)^2 dx$$

Unable to integrate:

$$\{e^{(c+dx)^3} (a + b x), x, 6, 0\}$$

$$\frac{(b c - a d) (c + d x) \text{Gamma}\left[\frac{1}{3}, -(c + d x)^3\right]}{3 d^2 \left(-(c + d x)^3\right)^{1/3}} - \frac{b (c + d x)^2 \text{Gamma}\left[\frac{2}{3}, -(c + d x)^3\right]}{3 d^2 \left(-(c + d x)^3\right)^{2/3}}$$

$$\int e^{(c+dx)^3} (a + b x) dx$$

Incorrect antiderivative:

$$\left\{\frac{4^x}{a + 2^x b}, x, 4, 0\right\}$$

$$\frac{2^x}{b \log[2]} - \frac{a \log[a + 2^x b]}{b^2 \log[2]}$$

$$\frac{\log[-a - 2^x b]}{b \log[4]}$$

Incorrect antiderivative:

$$\left\{\frac{2^{2x}}{a + 2^x b}, x, 4, 0\right\}$$

$$\frac{2^x}{b \log[2]} - \frac{a \log[a + 2^x b]}{b^2 \log[2]}$$

$$\frac{\log[-a - 2^x b]}{b \log[4]}$$

Incorrect antiderivative:

$$\left\{\frac{4^x}{a - 2^x b}, x, 4, 0\right\}$$

$$-\frac{2^x}{b \log[2]} - \frac{a \log[-a + 2^x b]}{b^2 \log[2]}$$

$$-\frac{\log[-a + 2^x b]}{b \log[4]}$$

Incorrect antiderivative:

$$\left\{\frac{2^{2x}}{a - 2^x b}, x, 4, 0\right\}$$

$$-\frac{2^x}{b \log[2]} - \frac{a \log[a - 2^x b]}{b^2 \log[2]}$$

$$-\frac{\log[-a + 2^x b]}{b \log[4]}$$

Incorrect antiderivative:

$$\left\{ \frac{4^x}{a + 2^{-x} b}, x, 5, 0 \right\}$$

$$- \frac{2^x b}{a^2 \operatorname{Log}[2]} + \frac{4^x}{a \operatorname{Log}[4]} + \frac{b^2 \operatorname{Log}[2^x a + b]}{a^3 \operatorname{Log}[2]}$$

$$\frac{\operatorname{Log}[-2^x a - b]}{a \operatorname{Log}[8]}$$

Incorrect antiderivative:

$$\left\{ \frac{2^{2x}}{a + 2^{-x} b}, x, 5, 0 \right\}$$

$$\frac{2^{-1+2x}}{a \operatorname{Log}[2]} - \frac{2^x b}{a^2 \operatorname{Log}[2]} + \frac{b^2 \operatorname{Log}[2^x a + b]}{a^3 \operatorname{Log}[2]}$$

$$\frac{\operatorname{Log}[-2^x a - b]}{a \operatorname{Log}[8]}$$

Incorrect antiderivative:

$$\left\{ \frac{4^x}{a - 2^{-x} b}, x, 5, 0 \right\}$$

$$\frac{2^x b}{a^2 \operatorname{Log}[2]} + \frac{4^x}{a \operatorname{Log}[4]} + \frac{b^2 \operatorname{Log}[2^x a - b]}{a^3 \operatorname{Log}[2]}$$

$$\frac{\operatorname{Log}[-2^x a + b]}{a \operatorname{Log}[8]}$$

Incorrect antiderivative:

$$\left\{ \frac{2^{2x}}{a - 2^{-x} b}, x, 5, 0 \right\}$$

$$\frac{2^{-1+2x}}{a \operatorname{Log}[2]} + \frac{2^x b}{a^2 \operatorname{Log}[2]} + \frac{b^2 \operatorname{Log}[-2^x a + b]}{a^3 \operatorname{Log}[2]}$$

$$\frac{\operatorname{Log}[-2^x a + b]}{a \operatorname{Log}[8]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{2^x}{a + 4^{-x} b}, x, 6, 0 \right\}$$

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTan}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

$$\frac{8^x \operatorname{Hypergeometric2F1}\left[1, \frac{\operatorname{Log}[8]}{\operatorname{Log}[4]}, \frac{\operatorname{Log}[32]}{\operatorname{Log}[4]}, -\frac{4^x a}{b}\right]}{b \operatorname{Log}[8]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{2^x}{a + 2^{-2x} b}, x, 4, 0 \right\}$$

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTan}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

$$\frac{8^x \operatorname{Hypergeometric2F1}\left[1, \frac{\operatorname{Log}[8]}{\operatorname{Log}[4]}, \frac{\operatorname{Log}[32]}{\operatorname{Log}[4]}, -\frac{4^x a}{b}\right]}{b \operatorname{Log}[8]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{2^x}{a - 4^{-x} b}, x, 6, 0 \right\}$$

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTanh}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

$$- \frac{8^x \operatorname{Hypergeometric2F1}\left[1, \frac{\operatorname{Log}[8]}{\operatorname{Log}[4]}, \frac{\operatorname{Log}[32]}{\operatorname{Log}[4]}, \frac{4^x a}{b}\right]}{b \operatorname{Log}[8]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{2^x}{a - 2^{-2x} b}, x, 4, 0 \right\}$$

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTanh}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

$$- \frac{8^x \operatorname{Hypergeometric2F1}\left[1, \frac{\operatorname{Log}[8]}{\operatorname{Log}[4]}, \frac{\operatorname{Log}[32]}{\operatorname{Log}[4]}, \frac{4^x a}{b}\right]}{b \operatorname{Log}[8]}$$

Incorrect antiderivative:

$$\left\{ \frac{4^x}{\sqrt{a + 2^x b}}, x, 4, 0 \right\}$$

$$- \frac{4 a \sqrt{a + 2^x b}}{3 b^2 \operatorname{Log}[2]} + \frac{2^{1+x} \sqrt{a + 2^x b}}{3 b \operatorname{Log}[2]}$$

$$\frac{2 \sqrt{a + 2^x b}}{b \operatorname{Log}[4]}$$

Incorrect antiderivative:

$$\left\{ \frac{2^{2x}}{\sqrt{a + 2^x b}}, x, 3, 0 \right\}$$

$$- \frac{4 a \sqrt{a + 2^x b}}{3 b^2 \operatorname{Log}[2]} + \frac{2^{1+x} \sqrt{a + 2^x b}}{3 b \operatorname{Log}[2]}$$

$$\frac{2 \sqrt{a + 2^x b}}{b \operatorname{Log}[4]}$$

Incorrect antiderivative:

$$\left\{ \frac{4^x}{\sqrt{a - 2^x b}}, x, 4, 0 \right\}$$

$$- \frac{4 a \sqrt{a - 2^x b}}{3 b^2 \operatorname{Log}[2]} - \frac{2^{1+x} \sqrt{a - 2^x b}}{3 b \operatorname{Log}[2]}$$

$$- \frac{2 \sqrt{a - 2^x b}}{b \operatorname{Log}[4]}$$

Incorrect antiderivative:

$$\left\{ \frac{2^{2x}}{\sqrt{a - 2^x b}}, x, 3, 0 \right\}$$

$$- \frac{4 a \sqrt{a - 2^x b}}{3 b^2 \operatorname{Log}[2]} - \frac{2^{1+x} \sqrt{a - 2^x b}}{3 b \operatorname{Log}[2]}$$

$$- \frac{2 \sqrt{a - 2^x b}}{b \operatorname{Log}[4]}$$

Unable to integrate:

$$\left\{ \frac{a^x b^x}{x^2}, x, 3, 0 \right\}$$

$$- \frac{a^x b^x}{x} + \operatorname{ExpIntegralEi}[x (\operatorname{Log}[a] + \operatorname{Log}[b])] (\operatorname{Log}[a] + \operatorname{Log}[b])$$

$$\int \frac{a^x b^x}{x^2} dx$$

Unable to integrate:

$$\left\{ \frac{a^x b^x}{x^3}, x, 4, 0 \right\}$$

$$- \frac{a^x b^x}{2 x^2} - \frac{a^x b^x (\operatorname{Log}[a] + \operatorname{Log}[b])}{2 x} + \frac{1}{2} \operatorname{ExpIntegralEi}[x (\operatorname{Log}[a] + \operatorname{Log}[b])] (\operatorname{Log}[a] + \operatorname{Log}[b])^2$$

$$\int \frac{a^x b^x}{x^3} dx$$

Unable to integrate:

$$\left\{ e^{a+c+b x^n+d x^n}, x, 2, 0 \right\}$$

$$- \frac{e^{a+c} x^{-(b+d) x^n} \operatorname{Gamma}\left[\frac{1}{n}, -(b+d) x^n\right]}{n}$$

$$\int e^{a+c+b x^n+d x^n} dx$$

Unable to integrate:

$$\left\{ f^{a+b x^n} g^{c+d x^n}, x, 2, 0 \right\}$$

$$- \frac{f^a g^c x \operatorname{Gamma}\left[\frac{1}{n}, -x^n (b \operatorname{Log}[f] + d \operatorname{Log}[g])\right] (-x^n (b \operatorname{Log}[f] + d \operatorname{Log}[g]))^{-1/n}}{n}$$

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$$\int f^{a+bx^n} g^{c+dx^n} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{e^x}{1 - e^{2x}}, x, 2, 0 \right\}$$

$$\text{ArcTanh}[e^x]$$

$$\frac{1}{2} (-\text{Log}[-1 + e^x] + \text{Log}[1 + e^x])$$

Unable to integrate:

$$\left\{ \frac{x}{a + b f^{c+dx} + c f^{2c+2dx}}, x, 7, 0 \right\}$$

$$\frac{c x^2}{\sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right)} - \frac{c x^2}{\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right)} - \frac{2 c x \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right) d \text{Log}[f]} +$$

$$\frac{2 c x \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right) d \text{Log}[f]} - \frac{2 c \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right) d^2 \text{Log}[f]^2} + \frac{2 c \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right) d^2 \text{Log}[f]^2}$$

$$\int \frac{x}{a + b f^{c+dx} + c f^{2c+2dx}} dx$$

Unable to integrate:

$$\left\{ \frac{x^2}{a + b f^{c+dx} + c f^{2c+2dx}}, x, 9, 0 \right\}$$

$$\frac{2 c x^3}{3 \sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right)} - \frac{2 c x^3}{3 \sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right)} - \frac{2 c x^2 \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right) d \text{Log}[f]} +$$

$$\frac{2 c x^2 \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right) d \text{Log}[f]} - \frac{4 c x \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right) d^2 \text{Log}[f]^2} + \frac{4 c x \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right) d^2 \text{Log}[f]^2} +$$

$$\frac{4 c \text{PolyLog}\left[3, -\frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b - \sqrt{b^2 - 4 a c} \right) d^3 \text{Log}[f]^3} - \frac{4 c \text{PolyLog}\left[3, -\frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} \left(b + \sqrt{b^2 - 4 a c} \right) d^3 \text{Log}[f]^3}$$

$$\int \frac{x^2}{a + b f^{c+dx} + c f^{2c+2dx}} dx$$

Unable to integrate:

$$\left\{ \frac{x}{a + b f^{-c-dx} + c f^{c+dx}}, x, 8, 0 \right\}$$

$$\frac{x \text{Log}\left[1 + \frac{2 c f^{c+dx}}{a - \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d \text{Log}[f]} - \frac{x \text{Log}\left[1 + \frac{2 c f^{c+dx}}{a + \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d \text{Log}[f]} + \frac{\text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{a - \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d^2 \text{Log}[f]^2} - \frac{\text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{a + \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d^2 \text{Log}[f]^2}$$

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$$\int \frac{x}{a + b f^{-c-d x} + c f^{c+d x}} dx$$

Unable to integrate:

$$\left\{ \frac{x^2}{a + b f^{-c-d x} + c f^{c+d x}}, x, 10, 0 \right\}$$

$$\frac{x^2 \operatorname{Log}\left[1 + \frac{2 c f^{c+d x}}{a - \sqrt{a^2 - 4 b c}}\right] - x^2 \operatorname{Log}\left[1 + \frac{2 c f^{c+d x}}{a + \sqrt{a^2 - 4 b c}}\right] - 2 x \operatorname{PolyLog}\left[2, -\frac{2 c f^{c+d x}}{a - \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d \operatorname{Log}[f]} - \frac{2 x \operatorname{PolyLog}\left[2, -\frac{2 c f^{c+d x}}{a + \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d \operatorname{Log}[f]} + \frac{2 x \operatorname{PolyLog}\left[2, -\frac{2 c f^{c+d x}}{a - \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d^2 \operatorname{Log}[f]^2} - \frac{2 x \operatorname{PolyLog}\left[2, -\frac{2 c f^{c+d x}}{a + \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d^2 \operatorname{Log}[f]^2} - \frac{2 \operatorname{PolyLog}\left[3, -\frac{2 c f^{c+d x}}{a - \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d^3 \operatorname{Log}[f]^3} - \frac{2 \operatorname{PolyLog}\left[3, -\frac{2 c f^{c+d x}}{a + \sqrt{a^2 - 4 b c}}\right]}{\sqrt{a^2 - 4 b c} d^3 \operatorname{Log}[f]^3}$$

$$\int \frac{x^2}{a + b f^{-c-d x} + c f^{c+d x}} dx$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Csc}[e^x] \operatorname{Sec}[e^x], x, 2, 0\}$$

$$\operatorname{Log}[\operatorname{Tan}[e^x]]$$

$$-\operatorname{Log}[2 \operatorname{Cos}[e^x]] + \operatorname{Log}[2 \operatorname{Sin}[e^x]]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sec}[e^x], x, 2, 0\}$$

$$\operatorname{ArcTanh}[\operatorname{Sin}[e^x]]$$

$$-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{e^x}{2}\right] - \operatorname{Sin}\left[\frac{e^x}{2}\right]\right] + \operatorname{Log}\left[\operatorname{Cos}\left[\frac{e^x}{2}\right] + \operatorname{Sin}\left[\frac{e^x}{2}\right]\right]$$

Incorrect antiderivative:

$$\{f^{a+b x+c x^2} \operatorname{Sinh}[c+d x+e x^2], x, 9, 0\}$$

$$\frac{e^{-c+\frac{(d-b \operatorname{Log}[f])^2}{4(e-c \operatorname{Log}[f])}} f^a \sqrt{\pi} \operatorname{Erfi}\left[\frac{d-b \operatorname{Log}[f]+2 x(e-c \operatorname{Log}[f])}{2 \sqrt{-e+c \operatorname{Log}[f]}}\right]}{4 \sqrt{-e+c \operatorname{Log}[f]}} + \frac{e^{\frac{c}{4}-\frac{(d+b \operatorname{Log}[f])^2}{4(e+c \operatorname{Log}[f])}} f^a \sqrt{\pi} \operatorname{Erfi}\left[\frac{d+b \operatorname{Log}[f]+2 x(e+c \operatorname{Log}[f])}{2 \sqrt{e+c \operatorname{Log}[f]}}\right]}{4 \sqrt{e+c \operatorname{Log}[f]}}$$

$$\frac{1}{4\left(e^2-c^2 \operatorname{Log}[f]^2\right)} f^{a-\frac{b d}{2(e+c \operatorname{Log}[f])}+\frac{c\left(d^2+b^2 \operatorname{Log}[f]^2\right)}{2\left(e^2-c^2 \operatorname{Log}[f]^2\right)}} \sqrt{\pi}$$

$$\left(\frac{d^2+b^2 \operatorname{Log}[f]^2}{4 e+4 c \operatorname{Log}[f]} f^{\frac{b c d \operatorname{Log}[f]}{-e^2+c^2 \operatorname{Log}[f]^2}} \operatorname{Erfi}\left[\frac{-d-2 e x+(b+2 c x) \operatorname{Log}[f]}{2 \sqrt{-e+c \operatorname{Log}[f]}}\right] \sqrt{-e+c \operatorname{Log}[f]}(e+c \operatorname{Log}[f])(\operatorname{Cosh}[c]-\operatorname{Sinh}[c])+\right.$$

$$\left.\frac{d^2+b^2 \operatorname{Log}[f]^2}{4 e+4 c \operatorname{Log}[f]} \operatorname{Erfi}\left[\frac{d+2 e x+(b+2 c x) \operatorname{Log}[f]}{2 \sqrt{e+c \operatorname{Log}[f]}}\right](e-c \operatorname{Log}[f]) \sqrt{e+c \operatorname{Log}[f]}(\operatorname{Cosh}[c]+\operatorname{Sinh}[c])\right)$$

Incorrect antiderivative:

$$\{f^{a+b x+c x^2} \operatorname{Cosh}[c+d x+e x^2], x, 9, 0\}$$

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$$\begin{aligned}
 & \frac{e^{-c + \frac{(d-b \operatorname{Log}[f])^2}{4(e-c \operatorname{Log}[f])}} f^a \sqrt{\pi} \operatorname{Erfi}\left[\frac{d-b \operatorname{Log}[f]+2 x(e-c \operatorname{Log}[f])}{2 \sqrt{-e+c \operatorname{Log}[f]}}\right] + e^{-c - \frac{(d-b \operatorname{Log}[f])^2}{4(e+c \operatorname{Log}[f])}} f^a \sqrt{\pi} \operatorname{Erfi}\left[\frac{d+b \operatorname{Log}[f]+2 x(e+c \operatorname{Log}[f])}{2 \sqrt{e+c \operatorname{Log}[f]}}\right]}{4 \sqrt{-e+c \operatorname{Log}[f]}} + \frac{4 \sqrt{e+c \operatorname{Log}[f]}}{4 \sqrt{e+c \operatorname{Log}[f]}} \\
 & \frac{1}{4 \left(e^2 - c^2 \operatorname{Log}[f]^2\right)} f^{a - \frac{b d}{2(e+c \operatorname{Log}[f])} + \frac{c(d^2+b^2 \operatorname{Log}[f]^2)}{2(e^2-c^2 \operatorname{Log}[f]^2)}} \sqrt{\pi} \\
 & \left(-e^{\frac{d^2+b^2 \operatorname{Log}[f]^2}{4 e+4 c \operatorname{Log}[f]}} f^{-\frac{b c d \operatorname{Log}[f]}{e^2+c^2 \operatorname{Log}[f]^2}} \operatorname{Erfi}\left[\frac{-d-2 e x+(b+2 c x) \operatorname{Log}[f]}{2 \sqrt{-e+c \operatorname{Log}[f]}}\right] \sqrt{-e+c \operatorname{Log}[f]} (e+c \operatorname{Log}[f]) (\operatorname{Cosh}[c] - \operatorname{Sinh}[c]) + \right. \\
 & \left. e^{\frac{d^2+b^2 \operatorname{Log}[f]^2}{-4 e+4 c \operatorname{Log}[f]}} \operatorname{Erfi}\left[\frac{d+2 e x+(b+2 c x) \operatorname{Log}[f]}{2 \sqrt{e+c \operatorname{Log}[f]}}\right] (e-c \operatorname{Log}[f]) \sqrt{e+c \operatorname{Log}[f]} (\operatorname{Cosh}[c] + \operatorname{Sinh}[c]) \right)
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \left\{ \frac{e^{-x}}{\sqrt{1-e^{-2x}}}, x, 2, 0 \right\} \\
 & -\operatorname{ArcSin}[e^{-x}] \\
 & \frac{e^x \sqrt{1-e^{-2x}} \operatorname{ArcTan}\left[\sqrt{-1+e^{2x}}\right]}{\sqrt{-1+e^{2x}}}
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \left\{ \frac{e^x}{1-e^{2x}}, x, 2, 0 \right\} \\
 & \operatorname{ArcTanh}[e^x] \\
 & \frac{1}{2} (-\operatorname{Log}[-1+e^x] + \operatorname{Log}[1+e^x])
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \left\{ \frac{e^x}{-1+e^{2x}}, x, 2, 0 \right\} \\
 & -\operatorname{ArcTanh}[e^x] \\
 & \frac{1}{2} (\operatorname{Log}[-1+e^x] - \operatorname{Log}[1+e^x])
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \{e^x \operatorname{Sech}[e^x], x, 2, 0\} \\
 & \operatorname{ArcTan}[\operatorname{Sinh}[e^x]] \\
 & 2 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{e^x}{2}\right]\right]
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sec}[1-e^x]^3, x, 3, 0\}$$

Mathematica 7 Test Results for Integration Problems Involving Exponentials

$$-\frac{1}{2} \operatorname{ArcTanh}[\sin[1 - e^x]] - \frac{1}{2} \sec[1 - e^x] \tan[1 - e^x]$$

$$\frac{1}{2} \left(\log\left[\cos\left[\frac{1}{2}(1 - e^x)\right] - \sin\left[\frac{1}{2}(1 - e^x)\right]\right] - \log\left[\cos\left[\frac{1}{2}(1 - e^x)\right] + \sin\left[\frac{1}{2}(1 - e^x)\right]\right] - \sec[1 - e^x] \tan[1 - e^x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{e^{3x}}{-1 + e^{2x}}, x, 4, 0 \right\}$$

$$e^x - \operatorname{ArcTanh}[e^x]$$

$$\frac{1}{2} (2 e^x + \log[-1 + e^x] - \log[1 + e^x])$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{-e^{-x} + e^x}, x, 2, 0 \right\}$$

$$-\operatorname{ArcTanh}[e^x]$$

$$\frac{1}{2} (\log[-1 + e^x] - \log[1 + e^x])$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{-e^x + e^{3x}}, x, 5, 0 \right\}$$

$$e^{-x} - \operatorname{ArcTanh}[e^x]$$

$$e^{-x} + \frac{1}{2} \log[-1 + e^{-x}] - \frac{1}{2} \log[1 + e^{-x}]$$