

# Rubi 3 Test Suite Results

## Indefinite Integration Problems Involving Trig Functions

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{1+\operatorname{Cos}[c+d x]}, x, -6, 6 \right\}$$

$$(a+b) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{(a+b)(1+\operatorname{Cos}[c+d x])}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]$$


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$$d \sqrt{\frac{1}{1+\operatorname{Sec}[c+d x]}} \sqrt{a+b \operatorname{Sec}[c+d x]}$$

$$\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}}$$


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$$d \sqrt{\frac{a+b-(a-b) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}}$$

Unable to integrate:

$$\{x \operatorname{Cos}[2 x] \operatorname{Sec}[x], x, -1, 0\}$$

$$2 \operatorname{Cos}[x]-x \operatorname{Log}\left[1-i e^{i x}\right]+x \operatorname{Log}\left[1+i e^{i x}\right]-i \operatorname{PolyLog}\left[2,-i e^{i x}\right]+i \operatorname{PolyLog}\left[2, i e^{i x}\right]+2 x \operatorname{Sin}[x]$$

$$\operatorname{Int}\left[x \operatorname{Cos}[2 x] \operatorname{Sec}[x], x\right]$$

Unable to integrate:

$$\{x \operatorname{Cos}[2 x] \operatorname{Sec}[x]^3, x, -1, 0\}$$

$$-3 i x \operatorname{ArcTan}\left[e^{i x}\right]+\frac{3}{2} i \operatorname{PolyLog}\left[2,-i e^{i x}\right]-\frac{3}{2} i \operatorname{PolyLog}\left[2, i e^{i x}\right]+\frac{\operatorname{Sec}[x]}{2}-\frac{1}{2} x \operatorname{Sec}[x] \operatorname{Tan}[x]$$

$$\operatorname{Int}\left[x \operatorname{Cos}[2 x] \operatorname{Sec}[x]^3, x\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a+c \operatorname{Sec}[x]+b \operatorname{Tan}[x]}, x, -9, 9 \right\}$$

$$\frac{a x}{a^2+b^2}+\frac{2 a c \operatorname{ArcTanh}\left[\frac{b+(-a+c) \operatorname{Tan}\left[\frac{x}{2}\right]}{\sqrt{a^2+b^2-c^2}}\right]}{\left(a^2+b^2\right) \sqrt{a^2+b^2-c^2}}+\frac{b \operatorname{Log}[c+a \operatorname{Cos}[x]+b \operatorname{Sin}[x]]}{a^2+b^2}$$

$$\frac{2 a \operatorname{ArcTan}\left[\operatorname{Tan}\left[\frac{x}{2}\right]\right]}{a^2+b^2}+\frac{2 a c \operatorname{ArcTanh}\left[\frac{b-(a-c) \operatorname{Tan}\left[\frac{x}{2}\right]}{\sqrt{a^2+b^2-c^2}}\right]}{\left(a^2+b^2\right) \sqrt{a^2+b^2-c^2}}-\frac{b \operatorname{Log}\left[\operatorname{Sec}\left[\frac{x}{2}\right]^2\right]}{a^2+b^2}+\frac{b \operatorname{Log}\left[a+c+2 b \operatorname{Tan}\left[\frac{x}{2}\right]-(a-c) \operatorname{Tan}\left[\frac{x}{2}\right]^2\right]}{a^2+b^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a+b \operatorname{Cot}[x]+c \operatorname{Csc}[x]}, x, -9, 9 \right\}$$

$$\frac{a x}{a^2 + b^2} + \frac{2 a c \operatorname{ArcTanh}\left[\frac{a + (-b+c) \operatorname{Tan}\left[\frac{x}{2}\right]}{\sqrt{a^2+b^2-c^2}}\right]}{(a^2 + b^2) \sqrt{a^2 + b^2 - c^2}} - \frac{b \operatorname{Log}[c + b \operatorname{Cos}[x] + a \operatorname{Sin}[x]]}{a^2 + b^2}$$

$$\frac{2 a \operatorname{ArcTan}\left[\operatorname{Tan}\left[\frac{x}{2}\right]\right]}{a^2 + b^2} + \frac{2 a c \operatorname{ArcTanh}\left[\frac{a - (b-c) \operatorname{Tan}\left[\frac{x}{2}\right]}{\sqrt{a^2+b^2-c^2}}\right]}{(a^2 + b^2) \sqrt{a^2 + b^2 - c^2}} + \frac{b \operatorname{Log}\left[\operatorname{Sec}\left[\frac{x}{2}\right]^2\right]}{a^2 + b^2} - \frac{b \operatorname{Log}\left[b + c + 2 a \operatorname{Tan}\left[\frac{x}{2}\right] - (b - c) \operatorname{Tan}\left[\frac{x}{2}\right]^2\right]}{a^2 + b^2}$$

Unable to integrate:

$$\left\{ \frac{x \operatorname{Cos}[x] - \operatorname{Sin}[x]}{(x - \operatorname{Sin}[x])^2}, x, -7, 7 \right\}$$

$$\frac{x}{x - \operatorname{Sin}[x]}$$

$$-\operatorname{Int}\left[\frac{1}{x - \operatorname{Sin}[x]}, x\right] + \operatorname{Int}\left[\frac{\operatorname{Cos}[x]}{x - \operatorname{Sin}[x]}, x\right] + \operatorname{Log}[-x + \operatorname{Sin}[x]] + \frac{x}{x - \operatorname{Sin}[x]}$$

Unable to integrate:

$$\left\{ \frac{1}{\operatorname{Cos}[x]^{3/2} \sqrt{3 \operatorname{Cos}[x] + \operatorname{Sin}[x]}}, x, -6, 6 \right\}$$

$$\frac{2 \sqrt{3 \operatorname{Cos}[x] + \operatorname{Sin}[x]}}{\sqrt{\operatorname{Cos}[x]}}$$

$$\frac{4 \operatorname{Cos}\left[\frac{x}{2}\right]^2 \operatorname{Subst}\left[\operatorname{Int}\left[\frac{1}{\sqrt{3+2x-3x^2} \sqrt{1-x^2}^{3/2}}, x\right], x, \operatorname{Tan}\left[\frac{x}{2}\right]\right] \sqrt{3+2 \operatorname{Tan}\left[\frac{x}{2}\right]-3 \operatorname{Tan}\left[\frac{x}{2}\right]^2} \sqrt{1-\operatorname{Tan}\left[\frac{x}{2}\right]^2}}{\sqrt{\operatorname{Cos}\left[\frac{x}{2}\right]^2 \left(3+2 \operatorname{Tan}\left[\frac{x}{2}\right]-3 \operatorname{Tan}\left[\frac{x}{2}\right]^2\right)} \sqrt{\operatorname{Cos}\left[\frac{x}{2}\right]^2 \left(1-\operatorname{Tan}\left[\frac{x}{2}\right]^2\right)}}$$

$$\frac{2 \operatorname{Cos}\left[\frac{x}{2}\right]^2 \operatorname{Subst}\left[\operatorname{Int}\left[\frac{1}{\sqrt{3+2x-3x^2} \sqrt{1-x^2}}, x\right], x, \operatorname{Tan}\left[\frac{x}{2}\right]\right] \sqrt{3+2 \operatorname{Tan}\left[\frac{x}{2}\right]-3 \operatorname{Tan}\left[\frac{x}{2}\right]^2} \sqrt{1-\operatorname{Tan}\left[\frac{x}{2}\right]^2}}{\sqrt{\operatorname{Cos}\left[\frac{x}{2}\right]^2 \left(3+2 \operatorname{Tan}\left[\frac{x}{2}\right]-3 \operatorname{Tan}\left[\frac{x}{2}\right]^2\right)} \sqrt{\operatorname{Cos}\left[\frac{x}{2}\right]^2 \left(1-\operatorname{Tan}\left[\frac{x}{2}\right]^2\right)}}$$

Unable to integrate:

$$\left\{ \frac{\operatorname{Csc}[x] \sqrt{\operatorname{Cos}[x] + \operatorname{Sin}[x]}}{\operatorname{Cos}[x]^{3/2}}, x, -6, 6 \right\}$$

$$-\operatorname{Log}[\operatorname{Sin}[x]] + 2 \operatorname{Log}\left[-\sqrt{\operatorname{Cos}[x]} + \sqrt{\operatorname{Cos}[x] + \operatorname{Sin}[x]}\right] + \frac{2 \sqrt{\operatorname{Cos}[x] + \operatorname{Sin}[x]}}{\sqrt{\operatorname{Cos}[x]}}$$

$$\frac{\text{Subst}\left[\text{Int}\left[\frac{\sqrt{1+2x-x^2}}{x(1-x^2)^{3/2}}, x\right], x, \tan\left[\frac{x}{2}\right]\right] \sqrt{1 - \tan\left[\frac{x}{2}\right]^2} \sqrt{\cos\left[\frac{x}{2}\right]^2 \left(1 + 2 \tan\left[\frac{x}{2}\right] - \tan\left[\frac{x}{2}\right]^2\right)}}{\sqrt{\cos\left[\frac{x}{2}\right]^2 \left(1 - \tan\left[\frac{x}{2}\right]^2\right)} \sqrt{1 + 2 \tan\left[\frac{x}{2}\right] - \tan\left[\frac{x}{2}\right]^2}} +$$

$$\frac{\text{Subst}\left[\text{Int}\left[\frac{x\sqrt{1+2x-x^2}}{(1-x^2)^{3/2}}, x\right], x, \tan\left[\frac{x}{2}\right]\right] \sqrt{1 - \tan\left[\frac{x}{2}\right]^2} \sqrt{\cos\left[\frac{x}{2}\right]^2 \left(1 + 2 \tan\left[\frac{x}{2}\right] - \tan\left[\frac{x}{2}\right]^2\right)}}{\sqrt{\cos\left[\frac{x}{2}\right]^2 \left(1 - \tan\left[\frac{x}{2}\right]^2\right)} \sqrt{1 + 2 \tan\left[\frac{x}{2}\right] - \tan\left[\frac{x}{2}\right]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\{\cos[x]^{12} \sin[x]^{10} - \cos[x]^{10} \sin[x]^{12}, x, -23, 23\}$$

$$\frac{1}{11} \cos[x]^{11} \sin[x]^{11}$$

$$\frac{3 \cos[x]^{11} \sin[x]}{5632} - \frac{3 \cos[x]^{13} \sin[x]}{5632} + \frac{1}{512} \cos[x]^{11} \sin[x]^3 - \frac{7 \cos[x]^{13} \sin[x]^3}{2816} + \frac{7 \cos[x]^{11} \sin[x]^5}{1280} - \frac{7}{880} \cos[x]^{13} \sin[x]^5 +$$

$$\frac{1}{80} \cos[x]^{11} \sin[x]^7 - \frac{9}{440} \cos[x]^{13} \sin[x]^7 + \frac{1}{40} \cos[x]^{11} \sin[x]^9 - \frac{1}{22} \cos[x]^{13} \sin[x]^9 + \frac{1}{22} \cos[x]^{11} \sin[x]^{11}$$