

Mathematica 7 Test Results

For Integration Problems Involving Hyperbolic Functions

Problems involving hyperbolic sines

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a \sinh[x]^2}}, x, 2, 0 \right\}$$

$$- \frac{\operatorname{ArcCoth}[\cosh[x]] \sinh[x]}{\sqrt{a \sinh[x]^2}}$$

$$\frac{\left(-\log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right] \right) \sinh[x]}{\sqrt{a \sinh[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{3 + 5 i \sinh[c + d x]}, x, 1, 0 \right\}$$

$$\frac{\operatorname{ArcTan}\left[\frac{1}{4} \left(5 i - 3 \tanh\left[\frac{1}{2} (c + d x)\right] \right)\right]}{2 d}$$

$$\frac{1}{8 d} \left(2 \operatorname{ArcTan}\left[3 \coth\left[\frac{1}{2} (c + d x)\right]\right] + 2 \operatorname{ArcTan}\left[3 \tanh\left[\frac{1}{2} (c + d x)\right]\right] - i \left(\log[-4 + 5 \cosh[c + d x]] - \log[4 + 5 \cosh[c + d x]] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(3 + 5 i \sinh[c + d x])^2}, x, 2, 0 \right\}$$

$$- \frac{3 \operatorname{ArcTan}\left[\frac{1}{4} \left(5 i - 3 \tanh\left[\frac{1}{2} (c + d x)\right] \right)\right]}{32 d} + \frac{5 i \cosh[c + d x]}{16 d (3 + 5 i \sinh[c + d x])}$$

$$\frac{1}{384 d}$$

$$\left(-9 \left(2 \operatorname{ArcTan}\left[3 \coth\left[\frac{1}{2} (c + d x)\right]\right] + 2 \operatorname{ArcTan}\left[3 \tanh\left[\frac{1}{2} (c + d x)\right]\right] - i \log[-4 + 5 \cosh[c + d x]] + i \log[4 + 5 \cosh[c + d x]] \right) + \right.$$

$$\left. 40 \left(\frac{1}{3 \cosh\left[\frac{1}{2} (c + d x)\right] + i \sinh\left[\frac{1}{2} (c + d x)\right]} + \frac{3}{\cosh\left[\frac{1}{2} (c + d x)\right] + 3 i \sinh\left[\frac{1}{2} (c + d x)\right]} \right) \sinh\left[\frac{1}{2} (c + d x)\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(3 + 5 i \sinh[c + d x])^3}, x, 3, 0 \right\}$$

$$\frac{43 \operatorname{ArcTan}\left[\frac{1}{4} \left(5 i - 3 \tanh\left[\frac{1}{2} (c + d x)\right] \right)\right]}{1024 d} + \frac{5 i \cosh[c + d x]}{32 d (3 + 5 i \sinh[c + d x])^2} - \frac{45 i \cosh[c + d x]}{512 d (3 + 5 i \sinh[c + d x])}$$

$$\frac{1}{4096 d} \left(86 \operatorname{ArcTan} \left[3 \coth \left[\frac{1}{2} (c + d x) \right] \right] + 86 \operatorname{ArcTan} \left[3 \tanh \left[\frac{1}{2} (c + d x) \right] \right] - 43 i \operatorname{Log} [-4 + 5 \cosh [c + d x]] + \right. \\ \left. 43 i \operatorname{Log} [4 + 5 \cosh [c + d x]] - \frac{80 i}{\left(3 \cosh \left[\frac{1}{2} (c + d x) \right] + i \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} + \frac{80 i}{\left(\cosh \left[\frac{1}{2} (c + d x) \right] + 3 i \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} + \right. \\ \left. \left(-\frac{120}{3 \cosh \left[\frac{1}{2} (c + d x) \right] + i \sinh \left[\frac{1}{2} (c + d x) \right]} - \frac{360}{\cosh \left[\frac{1}{2} (c + d x) \right] + 3 i \sinh \left[\frac{1}{2} (c + d x) \right]} \right) \sinh \left[\frac{1}{2} (c + d x) \right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(3 + 5 i \sinh [c + d x])^4}, x, 4, 0 \right\} \\ - \frac{279 \operatorname{ArcTan} \left[\frac{1}{4} \left(5 i - 3 \tanh \left[\frac{1}{2} (c + d x) \right] \right) \right]}{16384 d} + \\ \frac{5 i \cosh [c + d x]}{48 d (3 + 5 i \sinh [c + d x])^3} - \frac{25 i \cosh [c + d x]}{512 d (3 + 5 i \sinh [c + d x])^2} + \frac{995 i \cosh [c + d x]}{24576 d (3 + 5 i \sinh [c + d x])} \\ \frac{1}{589824 d} \left(-5022 \operatorname{ArcTan} \left[3 \coth \left[\frac{1}{2} (c + d x) \right] \right] - 5022 \operatorname{ArcTan} \left[3 \tanh \left[\frac{1}{2} (c + d x) \right] \right] + 2511 i \operatorname{Log} [-4 + 5 \cosh [c + d x]] - \right. \\ \left. 2511 i \operatorname{Log} [4 + 5 \cosh [c + d x]] + \frac{4640 i}{\left(3 \cosh \left[\frac{1}{2} (c + d x) \right] + i \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} - \frac{1440 i}{\left(\cosh \left[\frac{1}{2} (c + d x) \right] + 3 i \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} + \right. \\ \left. 40 \left(\frac{80}{\left(3 \cosh \left[\frac{1}{2} (c + d x) \right] + i \sinh \left[\frac{1}{2} (c + d x) \right] \right)^3} + \frac{199}{3 \cosh \left[\frac{1}{2} (c + d x) \right] + i \sinh \left[\frac{1}{2} (c + d x) \right]} + \right. \\ \left. \frac{240}{\left(\cosh \left[\frac{1}{2} (c + d x) \right] + 3 i \sinh \left[\frac{1}{2} (c + d x) \right] \right)^3} + \frac{597}{\cosh \left[\frac{1}{2} (c + d x) \right] + 3 i \sinh \left[\frac{1}{2} (c + d x) \right]} \right) \sinh \left[\frac{1}{2} (c + d x) \right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{5 + 3 i \sinh [c + d x]}, x, 1, 0 \right\} \\ - \frac{\operatorname{ArcTanh} \left[\frac{1}{4} \left(3 i - 5 \tanh \left[\frac{1}{2} (c + d x) \right] \right) \right]}{2 d} \\ \frac{1}{8 d} \left(-2 i \operatorname{ArcTan} \left[\frac{2 \cosh \left[\frac{1}{2} (c + d x) \right] - \sinh \left[\frac{1}{2} (c + d x) \right]}{\cosh \left[\frac{1}{2} (c + d x) \right] - 2 \sinh \left[\frac{1}{2} (c + d x) \right]} \right] + 2 i \operatorname{ArcTan} \left[\frac{\cosh \left[\frac{1}{2} (c + d x) \right] + 2 \sinh \left[\frac{1}{2} (c + d x) \right]}{2 \cosh \left[\frac{1}{2} (c + d x) \right] + \sinh \left[\frac{1}{2} (c + d x) \right]} \right] - \right. \\ \left. \operatorname{Log} [5 \cosh [c + d x] - 4 \sinh [c + d x]] + \operatorname{Log} [5 \cosh [c + d x] + 4 \sinh [c + d x]] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(5 + 3 i \sinh [c + d x])^2}, x, 2, 0 \right\} \\ - \frac{5 \operatorname{ArcTanh} \left[\frac{1}{4} \left(3 i - 5 \tanh \left[\frac{1}{2} (c + d x) \right] \right) \right]}{32 d} - \frac{3 i \cosh [c + d x]}{16 d (5 + 3 i \sinh [c + d x])}$$

$$\frac{1}{640 d (-5 i + 3 \sinh[c + d x])} \left(-120 \cosh[c + d x] + \left(24 i - 50 i \operatorname{ArcTan} \left[\frac{2 \cosh \left[\frac{1}{2} (c + d x) \right] - \sinh \left[\frac{1}{2} (c + d x) \right]}{\cosh \left[\frac{1}{2} (c + d x) \right] - 2 \sinh \left[\frac{1}{2} (c + d x) \right]} \right] + 50 i \operatorname{ArcTan} \left[\frac{\cosh \left[\frac{1}{2} (c + d x) \right] + 2 \sinh \left[\frac{1}{2} (c + d x) \right]}{2 \cosh \left[\frac{1}{2} (c + d x) \right] + \sinh \left[\frac{1}{2} (c + d x) \right]} \right] - 25 \log[5 \cosh[c + d x] - 4 \sinh[c + d x]] + 25 \log[5 \cosh[c + d x] + 4 \sinh[c + d x]] \right) (-5 i + 3 \sinh[c + d x]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(5 + 3 i \sinh[c + d x])^3}, x, 3, 0 \right\} - \frac{59 \operatorname{ArcTanh} \left[\frac{1}{4} \left(3 i - 5 \tanh \left[\frac{1}{2} (c + d x) \right] \right) \right]}{1024 d} - \frac{3 i \cosh[c + d x]}{32 d (5 + 3 i \sinh[c + d x])^2} - \frac{45 i \cosh[c + d x]}{512 d (5 + 3 i \sinh[c + d x])} - \frac{1}{4096 d} \left(-118 i \operatorname{ArcTan} \left[\frac{2 \cosh \left[\frac{1}{2} (c + d x) \right] - \sinh \left[\frac{1}{2} (c + d x) \right]}{\cosh \left[\frac{1}{2} (c + d x) \right] - 2 \sinh \left[\frac{1}{2} (c + d x) \right]} \right] + 118 i \operatorname{ArcTan} \left[\frac{\cosh \left[\frac{1}{2} (c + d x) \right] + 2 \sinh \left[\frac{1}{2} (c + d x) \right]}{2 \cosh \left[\frac{1}{2} (c + d x) \right] + \sinh \left[\frac{1}{2} (c + d x) \right]} \right] - 59 \log[5 \cosh[c + d x] - 4 \sinh[c + d x]] + 59 \log[5 \cosh[c + d x] + 4 \sinh[c + d x]] + \frac{48}{\left((1 + 2 i) \cosh \left[\frac{1}{2} (c + d x) \right] - (2 + i) \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} + \frac{48}{\left((2 + i) \cosh \left[\frac{1}{2} (c + d x) \right] + (1 + 2 i) \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} - \frac{144 \sinh \left[\frac{1}{2} (c + d x) \right] \left(-3 i \cosh \left[\frac{1}{2} (c + d x) \right] + 5 \sinh \left[\frac{1}{2} (c + d x) \right] \right)}{-5 i + 3 \sinh[c + d x]} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(5 + 3 i \sinh[c + d x])^4}, x, 4, 0 \right\} - \frac{385 \operatorname{ArcTanh} \left[\frac{1}{4} \left(3 i - 5 \tanh \left[\frac{1}{2} (c + d x) \right] \right) \right]}{16384 d} - \frac{i \cosh[c + d x]}{16 d (5 + 3 i \sinh[c + d x])^3} - \frac{25 i \cosh[c + d x]}{512 d (5 + 3 i \sinh[c + d x])^2} - \frac{311 i \cosh[c + d x]}{8192 d (5 + 3 i \sinh[c + d x])} - \frac{1}{327680 d} \left(-3850 i \operatorname{ArcTan} \left[\frac{2 \cosh \left[\frac{1}{2} (c + d x) \right] - \sinh \left[\frac{1}{2} (c + d x) \right]}{\cosh \left[\frac{1}{2} (c + d x) \right] - 2 \sinh \left[\frac{1}{2} (c + d x) \right]} \right] + 3850 i \operatorname{ArcTan} \left[\frac{\cosh \left[\frac{1}{2} (c + d x) \right] + 2 \sinh \left[\frac{1}{2} (c + d x) \right]}{2 \cosh \left[\frac{1}{2} (c + d x) \right] + \sinh \left[\frac{1}{2} (c + d x) \right]} \right] - 1925 \log[5 \cosh[c + d x] - 4 \sinh[c + d x]] + 1925 \log[5 \cosh[c + d x] + 4 \sinh[c + d x]] + \frac{2656 - 192 i}{\left((1 + 2 i) \cosh \left[\frac{1}{2} (c + d x) \right] - (2 + i) \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} + \frac{2656 + 192 i}{\left((2 + i) \cosh \left[\frac{1}{2} (c + d x) \right] + (1 + 2 i) \sinh \left[\frac{1}{2} (c + d x) \right] \right)^2} + \frac{1}{(-5 i + 3 \sinh[c + d x])^3} 2 (-235150 + 166615 \cosh[c + d x] + 82530 \cosh[2 (c + d x)] - 13995 \cosh[3 (c + d x)] - 298563 i \sinh[c + d x] + 89364 i \sinh[2 (c + d x)] + 8397 i \sinh[3 (c + d x)]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{a + i a \sinh[c + d x]}, x, 1, 0 \right\}$$

$$\frac{2 \, i \, a \, \text{Cosh}[c + d \, x]}{d \sqrt{a + i \, a \, \text{Sinh}[c + d \, x]}}$$

$$\frac{2 \left(i \, \text{Cosh}\left[\frac{1}{2} (c + d \, x)\right] + \text{Sinh}\left[\frac{1}{2} (c + d \, x)\right] \right) \sqrt{a + i \, a \, \text{Sinh}[c + d \, x]}}{d \left(\text{Cosh}\left[\frac{1}{2} (c + d \, x)\right] + i \, \text{Sinh}\left[\frac{1}{2} (c + d \, x)\right] \right)}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x}{a + b \, \text{Sinh}[x]}, x, 8, 0 \right\}$$

$$\frac{x \, \text{Log}\left[1 + \frac{b e^x}{a - \sqrt{a^2 + b^2}}\right]}{\sqrt{a^2 + b^2}} - \frac{x \, \text{Log}\left[1 + \frac{b e^x}{a + \sqrt{a^2 + b^2}}\right]}{\sqrt{a^2 + b^2}} + \frac{\text{PolyLog}\left[2, -\frac{b e^x}{a - \sqrt{a^2 + b^2}}\right]}{\sqrt{a^2 + b^2}} - \frac{\text{PolyLog}\left[2, -\frac{b e^x}{a + \sqrt{a^2 + b^2}}\right]}{\sqrt{a^2 + b^2}}$$

$$- \frac{i \, \pi \, \text{ArcTanh}\left[\frac{-b + a \, \text{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^2 + b^2}}\right]}{\sqrt{a^2 + b^2}} -$$

$$\frac{1}{\sqrt{-a^2 - b^2}} \left(2 \, \text{ArcCos}\left[-\frac{i \, a}{b}\right] \, \text{ArcTanh}\left[\frac{(a + i \, b) \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] + (\pi - 2 \, i \, x) \, \text{ArcTanh}\left[\frac{(a - i \, b) \, \text{Tan}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] - \right.$$

$$\left. \left(\text{ArcCos}\left[-\frac{i \, a}{b}\right] + 2 \, i \, \text{ArcTanh}\left[\frac{(a + i \, b) \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] \right) \text{Log}\left[\frac{(i \, a + b) \left(a + i \left(b + \sqrt{-a^2 - b^2}\right)\right) \left(-i + \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)}{b \left(i \, a + b + i \sqrt{-a^2 - b^2} \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)} \right] -$$

$$\left(\text{ArcCos}\left[-\frac{i \, a}{b}\right] - 2 \, i \, \text{ArcTanh}\left[\frac{(a + i \, b) \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] \right) \text{Log}\left[\frac{(i \, a + b) \left(i \, a - b + \sqrt{-a^2 - b^2}\right) \left(i + \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)}{b \left(a - i \, b + \sqrt{-a^2 - b^2} \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)} \right] +$$

$$\left(\text{ArcCos}\left[-\frac{i \, a}{b}\right] - 2 \, i \, \text{ArcTanh}\left[\frac{(a + i \, b) \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] - 2 \, i \, \text{ArcTanh}\left[\frac{(a - i \, b) \, \text{Tan}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] \right)$$

$$\text{Log}\left[\frac{\left(\frac{1}{2} - \frac{i}{2}\right) \sqrt{-a^2 - b^2} \, e^{-x/2}}{\sqrt{-i \, b} \sqrt{a + b \, \text{Sinh}[x]}}\right] +$$

$$\left(\text{ArcCos}\left[-\frac{i \, a}{b}\right] + 2 \, i \left(\text{ArcTanh}\left[\frac{(a + i \, b) \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] + \text{ArcTanh}\left[\frac{(a - i \, b) \, \text{Tan}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]}{\sqrt{-a^2 - b^2}}\right] \right) \right)$$

$$\text{Log}\left[\frac{\left(\frac{1}{2} + \frac{i}{2}\right) \sqrt{-a^2 - b^2} \, e^{x/2}}{\sqrt{-i \, b} \sqrt{a + b \, \text{Sinh}[x]}}\right] + i \left(\text{PolyLog}\left[2, \frac{\left(i \, a + \sqrt{-a^2 - b^2}\right) \left(i \, a + b - i \sqrt{-a^2 - b^2} \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)}{b \left(i \, a + b + i \sqrt{-a^2 - b^2} \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)} \right] - \right.$$

$$\left. \left. \text{PolyLog}\left[2, \frac{\left(a + i \sqrt{-a^2 - b^2}\right) \left(-a + i \, b + \sqrt{-a^2 - b^2} \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)}{b \left(i \, a + b + i \sqrt{-a^2 - b^2} \, \text{Cot}\left[\frac{1}{4} (\pi + 2 \, i \, x)\right]\right)} \right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x^2}{1 + i \, \text{Sinh}[x]}, x, 6, 0 \right\}$$

$$\begin{aligned}
& x^2 - 4 x \operatorname{Log}\left[1 + e^{\frac{i\pi}{2}x}\right] - 4 \operatorname{PolyLog}\left[2, -e^{\frac{i\pi}{2}x}\right] + i x^2 \operatorname{Tan}\left[\frac{\pi}{4} - \frac{i x}{2}\right] \\
& \frac{1}{1 + i \operatorname{Sinh}[x]} 2 \left(\operatorname{Cosh}\left[\frac{x}{2}\right] + i \operatorname{Sinh}\left[\frac{x}{2}\right] \right) \\
& \left(\frac{1}{2\sqrt{2}} \left(-i\sqrt{2} \pi x + 2(-1)^{3/4} x^2 + 2i\sqrt{2} (\pi + 2ix) \operatorname{Log}[1 - i e^{-x}] + 4i\sqrt{2} \pi \operatorname{Log}[1 + e^x] - 4i\sqrt{2} \pi \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] - \right. \right. \\
& \quad \left. \left. 2i\sqrt{2} \pi \operatorname{Log}\left[\operatorname{Sin}\left[\frac{1}{4}(\pi + 2ix)\right]\right] + 4\sqrt{2} \operatorname{PolyLog}[2, i e^{-x}] \right) \left(\operatorname{Cosh}\left[\frac{x}{2}\right] + i \operatorname{Sinh}\left[\frac{x}{2}\right] \right) + x^2 \operatorname{Sinh}\left[\frac{x}{2}\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{x^2}{1 - i \operatorname{Sinh}[x]}, x, 6, 0 \right\} \\
& -x^2 - 4 x \operatorname{Log}\left[1 + e^{\frac{i\pi}{2}x}\right] + 4 \operatorname{PolyLog}\left[2, -e^{\frac{i\pi}{2}x}\right] - i x^2 \operatorname{Tan}\left[\frac{\pi}{4} + \frac{i x}{2}\right] \\
& i \left(-3 \pi x - (1 - i) x^2 - 2 \pi \operatorname{Log}[1 + i e^{-x}] + 4 i x \operatorname{Log}[1 + i e^{-x}] + 4 \pi \operatorname{Log}[1 + e^x] + \right. \\
& \quad \left. 2 \pi \operatorname{Log}\left[-\operatorname{Cos}\left[\frac{1}{4}(\pi + 2ix)\right]\right] - 4 \pi \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] - 4 i \operatorname{PolyLog}[2, -i e^{-x}] - \frac{2 i x^2 \operatorname{Sinh}\left[\frac{x}{2}\right]}{\operatorname{Cosh}\left[\frac{x}{2}\right] - i \operatorname{Sinh}\left[\frac{x}{2}\right]} \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{x}{(a + b \operatorname{Sinh}[c + d x])^2}, x, 12, 0 \right\} \\
& \frac{a x \operatorname{Log}\left[1 + \frac{b e^{c+dx}}{a - \sqrt{a^2 + b^2}}\right]}{(a^2 + b^2)^{3/2} d} - \frac{a x \operatorname{Log}\left[1 + \frac{b e^{c+dx}}{a + \sqrt{a^2 + b^2}}\right]}{(a^2 + b^2)^{3/2} d} + \frac{\operatorname{Log}[a + b \operatorname{Sinh}[c + d x]]}{(a^2 + b^2) d^2} + \\
& \frac{a \operatorname{PolyLog}\left[2, -\frac{b e^{c+dx}}{a - \sqrt{a^2 + b^2}}\right]}{(a^2 + b^2)^{3/2} d^2} - \frac{a \operatorname{PolyLog}\left[2, -\frac{b e^{c+dx}}{a + \sqrt{a^2 + b^2}}\right]}{(a^2 + b^2)^{3/2} d^2} - \frac{b x \operatorname{Cosh}[c + d x]}{(a^2 + b^2) d (a + b \operatorname{Sinh}[c + d x])} \\
& \frac{1}{d^2} \left(\frac{1}{((a^2 + b^2) e^{2c})^{3/2} (-1 + e^{2c})} e^{2c} \left(-2 d e^{2c} \sqrt{(a^2 + b^2) e^{2c}} x - \sqrt{(a^2 + b^2) e^{2c}} \operatorname{Log}[2 a e^{c+dx} + b (-1 + e^{2(c+dx)})] \right) + \right. \\
& \quad e^{2c} \sqrt{(a^2 + b^2) e^{2c}} \operatorname{Log}[2 a e^{c+dx} + b (-1 + e^{2(c+dx)})] - a d e^c x \operatorname{Log}\left[1 + \frac{b e^{2c+dx}}{a e^c - \sqrt{(a^2 + b^2) e^{2c}}}\right] + \\
& \quad a d e^{3c} x \operatorname{Log}\left[1 + \frac{b e^{2c+dx}}{a e^c - \sqrt{(a^2 + b^2) e^{2c}}}\right] + a d e^c x \operatorname{Log}\left[1 + \frac{b e^{2c+dx}}{a e^c + \sqrt{(a^2 + b^2) e^{2c}}}\right] - \\
& \quad a d e^{3c} x \operatorname{Log}\left[1 + \frac{b e^{2c+dx}}{a e^c + \sqrt{(a^2 + b^2) e^{2c}}}\right] + a e^c (-1 + e^{2c}) \operatorname{PolyLog}\left[2, -\frac{b e^{2c+dx}}{a e^c - \sqrt{(a^2 + b^2) e^{2c}}}\right] - \\
& \quad \left. a e^c (-1 + e^{2c}) \operatorname{PolyLog}\left[2, -\frac{b e^{2c+dx}}{a e^c + \sqrt{(a^2 + b^2) e^{2c}}}\right] \right) + \frac{d x \operatorname{Csch}[c] (a \operatorname{Cosh}[c] + b \operatorname{Sinh}[d x])}{(a^2 + b^2) (a + b \operatorname{Sinh}[c + d x])}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{e + f x}{(a + b \operatorname{Sinh}[c + d x])^2}, x, 16, 0 \right\}$$

$$\begin{aligned}
& -\frac{2 a e \operatorname{ArcTanh}\left[\frac{b-a \operatorname{Tanh}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2+b^2}}\right]}{\left(a^2+b^2\right)^{3 / 2} d}+\frac{a f x \operatorname{Log}\left[1+\frac{b e^{c+d x}}{a-\sqrt{a^2+b^2}}\right]}{\left(a^2+b^2\right)^{3 / 2} d}-\frac{a f x \operatorname{Log}\left[1+\frac{b e^{c+d x}}{a+\sqrt{a^2+b^2}}\right]}{\left(a^2+b^2\right)^{3 / 2} d}+\frac{f \operatorname{Log}[a+b \operatorname{Sinh}[c+d x]]}{\left(a^2+b^2\right) d^2}+ \\
& \frac{a f \operatorname{PolyLog}\left[2,-\frac{b e^{c+d x}}{a-\sqrt{a^2+b^2}}\right]}{\left(a^2+b^2\right)^{3 / 2} d^2}-\frac{a f \operatorname{PolyLog}\left[2,-\frac{b e^{c+d x}}{a+\sqrt{a^2+b^2}}\right]}{\left(a^2+b^2\right)^{3 / 2} d^2}-\frac{b e \operatorname{Cosh}[c+d x]}{\left(a^2+b^2\right) d(a+b \operatorname{Sinh}[c+d x])}-\frac{b f x \operatorname{Cosh}[c+d x]}{\left(a^2+b^2\right) d(a+b \operatorname{Sinh}[c+d x])} \\
& \frac{1}{d^2} \\
& \left(-\frac{1}{\left(-a^2-b^2\right)^{3 / 2} \sqrt{\left(a^2+b^2\right) e^{2 c}}(-1+e^{2 c})}\left(-2 \sqrt{-a^2-b^2} d e^{2 c} \sqrt{\left(a^2+b^2\right) e^{2 c}} f x-2 a d e \sqrt{\left(a^2+b^2\right) e^{2 c}} \operatorname{ArcTan}\left[\frac{a+b e^{c+d x}}{\sqrt{-a^2-b^2}}\right]+2\right.\right. \\
& \left.\left.a d e e^{2 c} \sqrt{\left(a^2+b^2\right) e^{2 c}} \operatorname{ArcTan}\left[\frac{a+b e^{c+d x}}{\sqrt{-a^2-b^2}}\right]-\sqrt{-a^2-b^2} \sqrt{\left(a^2+b^2\right) e^{2 c}} f \operatorname{Log}\left[2 a e^{c+d x}+b(-1+e^{2(c+d x)})\right]\right)+ \\
& \left.\sqrt{-a^2-b^2} e^{2 c} \sqrt{\left(a^2+b^2\right) e^{2 c}} f \operatorname{Log}\left[2 a e^{c+d x}+b(-1+e^{2(c+d x)})\right]-a \sqrt{-a^2-b^2} d e^c f x \operatorname{Log}\left[1+\frac{b e^{2 c+d x}}{a e^c-\sqrt{\left(a^2+b^2\right) e^{2 c}}}\right]+ \right. \\
& \left. a \sqrt{-a^2-b^2} d e^{3 c} f x \operatorname{Log}\left[1+\frac{b e^{2 c+d x}}{a e^c-\sqrt{\left(a^2+b^2\right) e^{2 c}}}\right]+a \sqrt{-a^2-b^2} d e^c f x \operatorname{Log}\left[1+\frac{b e^{2 c+d x}}{a e^c+\sqrt{\left(a^2+b^2\right) e^{2 c}}}\right]- \right. \\
& \left. a \sqrt{-a^2-b^2} d e^{3 c} f x \operatorname{Log}\left[1+\frac{b e^{2 c+d x}}{a e^c+\sqrt{\left(a^2+b^2\right) e^{2 c}}}\right]+a \sqrt{-a^2-b^2} e^c(-1+e^{2 c}) f \operatorname{PolyLog}\left[2,-\frac{b e^{2 c+d x}}{a e^c-\sqrt{\left(a^2+b^2\right) e^{2 c}}}\right]- \right. \\
& \left. a \sqrt{-a^2-b^2} e^c(-1+e^{2 c}) f \operatorname{PolyLog}\left[2,-\frac{b e^{2 c+d x}}{a e^c+\sqrt{\left(a^2+b^2\right) e^{2 c}}}\right]\right)+\frac{d(e+f x) \operatorname{Csch}[c](a \operatorname{Cosh}[c]+b \operatorname{Sinh}[d x])}{\left(a^2+b^2\right)(a+b \operatorname{Sinh}[c+d x])} \Bigg)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{\sqrt{a+i a \operatorname{Sinh}[x]}, x, 1, 0\right\} \\
& \frac{2 i a \operatorname{Cosh}[x]}{\sqrt{a+i a \operatorname{Sinh}[x]}} \\
& \frac{2\left(i \operatorname{Cosh}\left[\frac{x}{2}\right]+\operatorname{Sinh}\left[\frac{x}{2}\right]\right) \sqrt{a+i a \operatorname{Sinh}[x]}}{\operatorname{Cosh}\left[\frac{x}{2}\right]+i \operatorname{Sinh}\left[\frac{x}{2}\right]}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{\sqrt{a-i a \operatorname{Sinh}[x]}, x, 1, 0\right\} \\
& -\frac{2 i a \operatorname{Cosh}[x]}{\sqrt{a-i a \operatorname{Sinh}[x]}} \\
& -\frac{2 i\left(\operatorname{Cosh}\left[\frac{x}{2}\right]+i \operatorname{Sinh}\left[\frac{x}{2}\right]\right) \sqrt{a-i a \operatorname{Sinh}[x]}}{\operatorname{Cosh}\left[\frac{x}{2}\right]-i \operatorname{Sinh}\left[\frac{x}{2}\right]}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\sqrt{a+i a \operatorname{Sinh}[c+d x]}, x, 1, 0\right\}$$

$$\frac{2 i a \operatorname{Cosh}[c+d x]}{d \sqrt{a+i a \operatorname{Sinh}[c+d x]}}$$

$$\frac{2 \left(i \operatorname{Cosh}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sinh}\left[\frac{1}{2}(c+d x)\right] \right) \sqrt{a+i a \operatorname{Sinh}[c+d x]}}{d \left(\operatorname{Cosh}\left[\frac{1}{2}(c+d x)\right] + i \operatorname{Sinh}\left[\frac{1}{2}(c+d x)\right] \right)}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x}{a+b \operatorname{Sinh}[x]^2}, x, 9, 0 \right\}$$

$$\frac{x \operatorname{Log}\left[1+\frac{b e^{2 x}}{2 a-2 \sqrt{a} \sqrt{a-b}-b}\right]}{2 \sqrt{a} \sqrt{a-b}} - \frac{x \operatorname{Log}\left[1+\frac{b e^{2 x}}{2 a+2 \sqrt{a} \sqrt{a-b}-b}\right]}{2 \sqrt{a} \sqrt{a-b}} + \frac{\operatorname{PolyLog}\left[2,-\frac{b e^{2 x}}{2 a-2 \sqrt{a} \sqrt{a-b}-b}\right]}{4 \sqrt{a} \sqrt{a-b}} - \frac{\operatorname{PolyLog}\left[2,-\frac{b e^{2 x}}{2 a+2 \sqrt{a} \sqrt{a-b}-b}\right]}{4 \sqrt{a} \sqrt{a-b}}$$

$$-\frac{1}{4 \sqrt{a}(-a+b)} \left(4 x \operatorname{ArcTan}\left[\frac{a \operatorname{Coth}[x]}{\sqrt{-a}(a-b)}\right] - 2 i \operatorname{ArcCos}\left[1-\frac{2 a}{b}\right] \operatorname{ArcTan}\left[\frac{\sqrt{-a^2+a b} \operatorname{Tanh}[x]}{a}\right] + \right.$$

$$\left. \left(\operatorname{ArcCos}\left[1-\frac{2 a}{b}\right] + 2 \left(\operatorname{ArcTan}\left[\frac{a \operatorname{Coth}[x]}{\sqrt{-a}(a-b)}\right] + \operatorname{ArcTan}\left[\frac{\sqrt{-a^2+a b} \operatorname{Tanh}[x]}{a}\right] \right) \right) \operatorname{Log}\left[\frac{\sqrt{2} \sqrt{a}(-a+b) e^{-x}}{\sqrt{b} \sqrt{2 a-b+b \operatorname{Cosh}[2 x]}}\right] +$$

$$\left(\operatorname{ArcCos}\left[1-\frac{2 a}{b}\right] - 2 \left(\operatorname{ArcTan}\left[\frac{a \operatorname{Coth}[x]}{\sqrt{-a}(a-b)}\right] + \operatorname{ArcTan}\left[\frac{\sqrt{-a^2+a b} \operatorname{Tanh}[x]}{a}\right] \right) \right) \operatorname{Log}\left[\frac{\sqrt{2} \sqrt{a}(-a+b) e^x}{\sqrt{b} \sqrt{2 a-b+b \operatorname{Cosh}[2 x]}}\right] -$$

$$\left(\operatorname{ArcCos}\left[1-\frac{2 a}{b}\right] + 2 \operatorname{ArcTan}\left[\frac{\sqrt{-a^2+a b} \operatorname{Tanh}[x]}{a}\right] \right) \left(\operatorname{Log}[2] + \operatorname{Log}\left[\frac{a(a+i(\sqrt{b}+\sqrt{a}(-a+b)))}{b(a+i \sqrt{a}(-a+b) \operatorname{Tanh}[x])}\right] \right) (-1+\operatorname{Tanh}[x]) \right) -$$

$$\left(\operatorname{ArcCos}\left[1-\frac{2 a}{b}\right] - 2 \operatorname{ArcTan}\left[\frac{\sqrt{-a^2+a b} \operatorname{Tanh}[x]}{a}\right] \right) \operatorname{Log}\left[\frac{2 a(i a-i b+\sqrt{a}(-a+b)) \operatorname{Sech}[x](\operatorname{Cosh}[x]+\operatorname{Sinh}[x])}{-i a b+b \sqrt{a}(-a+b) \operatorname{Tanh}[x]}\right] +$$

$$i \left(-\operatorname{PolyLog}\left[2,\frac{(-2 a+b-2 i \sqrt{a}(-a+b))(i a+\sqrt{a}(-a+b) \operatorname{Tanh}[x])}{-i a b+b \sqrt{a}(-a+b) \operatorname{Tanh}[x]}\right] + \right.$$

$$\left. \operatorname{PolyLog}\left[2,\frac{(-2 a+b+2 i \sqrt{a}(-a+b))(i a+\sqrt{a}(-a+b) \operatorname{Tanh}[x])}{-i a b+b \sqrt{a}(-a+b) \operatorname{Tanh}[x]}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a+b \operatorname{Sinh}[x]^3}, x, 7, 0 \right\}$$

$$-\frac{2 \operatorname{ArcTanh}\left[\frac{b^{1/3}-a^{1/3} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}+b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}+b^{2/3}}} - \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{2/3} b^{1/3}-a^{1/3} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}-(-1)^{1/3} b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}-(-1)^{1/3} b^{2/3}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{1/3} b^{1/3}+a^{1/3} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}+(-1)^{2/3} b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}+(-1)^{2/3} b^{2/3}}}$$

$$\frac{2}{3} \operatorname{RootSum}\left[-b+3 b \#1^2+8 a \#1^3-3 b \#1^4+b \#1^6 \&, \frac{x \#1+2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right] \#1-\operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1}{b+4 a \#1-2 b \#1^2+b \#1^4} \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a+b \operatorname{Sinh}[x]^5}, x, 11, 0 \right\}$$

$$\begin{aligned}
& -\frac{2 \operatorname{ArcTanh}\left[\frac{b^{1/5}-a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}+b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}+b^{2/5}}} - \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{2/5} b^{1/5}-a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}+(-1)^{4/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}+(-1)^{4/5} b^{2/5}}} - \\
& \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{4/5} b^{1/5}-a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}-(-1)^{3/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}-(-1)^{3/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{1/5} b^{1/5}+a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}+(-1)^{2/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}+(-1)^{2/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{3/5} b^{1/5}+a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}-(-1)^{1/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}-(-1)^{1/5} b^{2/5}}} \\
& -\frac{8}{5} \operatorname{RootSum}\left[-b+5 b \#1^2-10 b \#1^4+32 a \#1^5+10 b \#1^6-5 b \#1^8+b \#1^{10} \&, \right. \\
& \left. \frac{x \#1^3+2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right] \#1-\operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^3}{b-4 b \#1^2+16 a \#1^3+6 b \#1^4-4 b \#1^6+b \#1^8} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{a+b \operatorname{Sinh}[x]^6}, x, 10, 0 \right\} \\
& \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Coth}[x]}{\sqrt{a^{1/3}-b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3}-b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Coth}[x]}{\sqrt{a^{1/3}+(-1)^{1/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3}+(-1)^{1/3} b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Coth}[x]}{\sqrt{a^{1/3}-(-1)^{2/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3}-(-1)^{2/3} b^{1/3}}} \\
& -\frac{16}{3} \operatorname{RootSum}\left[b-6 b \#1+15 b \#1^2+64 a \#1^3-20 b \#1^3+15 b \#1^4-6 b \#1^5+b \#1^6 \&, \right. \\
& \left. \frac{x \#1^2+\operatorname{Log}\left[-\operatorname{Cosh}[x]-\operatorname{Sinh}[x]+\operatorname{Cosh}[x] \#1-\operatorname{Sinh}[x] \#1\right] \#1^2}{-b+5 b \#1+32 a \#1^2-10 b \#1^2+10 b \#1^3-5 b \#1^4+b \#1^5} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{a+b \operatorname{Sinh}[x]^8}, x, 13, 0 \right\} \\
& -\frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Coth}[x]}{\sqrt{(-a)^{1/4}-b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}-b^{1/4}}} - \frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Coth}[x]}{\sqrt{(-a)^{1/4}-i b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}-i b^{1/4}}} - \frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Coth}[x]}{\sqrt{(-a)^{1/4}+i b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}+i b^{1/4}}} - \frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Coth}[x]}{\sqrt{(-a)^{1/4}+b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}+b^{1/4}}} \\
& 16 \operatorname{RootSum}\left[b-8 b \#1+28 b \#1^2-56 b \#1^3+256 a \#1^4+70 b \#1^4-56 b \#1^5+28 b \#1^6-8 b \#1^7+b \#1^8 \&, \right. \\
& \left. \frac{x \#1^3+\operatorname{Log}\left[-\operatorname{Cosh}[x]-\operatorname{Sinh}[x]+\operatorname{Cosh}[x] \#1-\operatorname{Sinh}[x] \#1\right] \#1^3}{-b+7 b \#1-21 b \#1^2+128 a \#1^3+35 b \#1^3-35 b \#1^4+21 b \#1^5-7 b \#1^6+b \#1^7} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{a-b \operatorname{Sinh}[x]^3}, x, 7, 0 \right\} \\
& -\frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{1/3} b^{1/3}-a^{1/3} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}+(-1)^{2/3} b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}+(-1)^{2/3} b^{2/3}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{b^{1/3}+a^{1/3} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}+b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}+b^{2/3}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{2/3} b^{1/3}+a^{1/3} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}-(-1)^{1/3} b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}-(-1)^{1/3} b^{2/3}}} \\
& -\frac{2}{3} \operatorname{RootSum}\left[-b+3 b \#1^2-8 a \#1^3-3 b \#1^4+b \#1^6 \&, \frac{x \#1+2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right] \#1-\operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1}{b-4 a \#1-2 b \#1^2+b \#1^4} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a - b \sinh[x]^5}, x, 11, 0 \right\}$$

$$- \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{1/5} b^{1/5} - a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} + (-1)^{2/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} + (-1)^{2/5} b^{2/5}}} - \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{3/5} b^{1/5} - a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} - (-1)^{1/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} - (-1)^{1/5} b^{2/5}}} +$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{b^{1/5} + a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} + b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} + b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{2/5} b^{1/5} + a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} + (-1)^{4/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} + (-1)^{4/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{4/5} b^{1/5} + a^{1/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} - (-1)^{3/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} - (-1)^{3/5} b^{2/5}}}$$

$$- \frac{8}{5} \operatorname{RootSum}\left[-b + 5 b \#1^2 - 10 b \#1^4 - 32 a \#1^5 + 10 b \#1^6 - 5 b \#1^8 + b \#1^{10} \&, \right.$$

$$\left. \frac{x \#1^3 + 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^3}{b - 4 b \#1^2 - 16 a \#1^3 + 6 b \#1^4 - 4 b \#1^6 + b \#1^8} \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a - b \sinh[x]^6}, x, 10, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Coth}[x]}{\sqrt{a^{1/3} + b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3} + b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Coth}[x]}{\sqrt{a^{1/3} - (-1)^{1/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3} - (-1)^{1/3} b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Coth}[x]}{\sqrt{a^{1/3} + (-1)^{2/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3} + (-1)^{2/3} b^{1/3}}}$$

$$- \frac{16}{3} \operatorname{RootSum}\left[b - 6 b \#1 + 15 b \#1^2 - 64 a \#1^3 - 20 b \#1^3 + 15 b \#1^4 - 6 b \#1^5 + b \#1^6 \&, \right.$$

$$\left. \frac{x \#1^2 + \operatorname{Log}\left[-\operatorname{Cosh}[x] - \sinh[x] + \operatorname{Cosh}[x] \#1 - \sinh[x] \#1\right] \#1^2}{-b + 5 b \#1 - 32 a \#1^2 - 10 b \#1^2 + 10 b \#1^3 - 5 b \#1^4 + b \#1^5} \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a - b \sinh[x]^8}, x, 13, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Coth}[x]}{\sqrt{a^{1/4} - b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} - b^{1/4}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Coth}[x]}{\sqrt{a^{1/4} - i b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} - i b^{1/4}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Coth}[x]}{\sqrt{a^{1/4} + i b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} + i b^{1/4}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Coth}[x]}{\sqrt{a^{1/4} + b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} + b^{1/4}}}$$

$$- 16 \operatorname{RootSum}\left[b - 8 b \#1 + 28 b \#1^2 - 56 b \#1^3 - 256 a \#1^4 + 70 b \#1^4 - 56 b \#1^5 + 28 b \#1^6 - 8 b \#1^7 + b \#1^8 \&, \right.$$

$$\left. \frac{x \#1^3 + \operatorname{Log}\left[-\operatorname{Cosh}[x] - \sinh[x] + \operatorname{Cosh}[x] \#1 - \sinh[x] \#1\right] \#1^3}{-b + 7 b \#1 - 21 b \#1^2 - 128 a \#1^3 + 35 b \#1^3 - 35 b \#1^4 + 21 b \#1^5 - 7 b \#1^6 + b \#1^7} \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{1 + \sinh[x]^5}, x, 8, 0 \right\}$$

$$- \frac{1}{5} \sqrt{2} \operatorname{ArcTanh}\left[\frac{1 - \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{2}}\right] - \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{2/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 + (-1)^{4/5}}}\right]}{5 \sqrt{1 + (-1)^{4/5}}} -$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{4/5} \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 - (-1)^{3/5}}}\right]}{5 \sqrt{1 - (-1)^{3/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{1/5} + \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 + (-1)^{2/5}}}\right]}{5 \sqrt{1 + (-1)^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(-1)^{3/5} + \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 - (-1)^{1/5}}}\right]}{5 \sqrt{1 - (-1)^{1/5}}}$$

$$\frac{1}{10} \left(2 \sqrt{2} \operatorname{ArcTanh} \left[\frac{-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{2}} \right] - \operatorname{RootSum} \left[1 + 2 \#1 + 2 \#1^3 + 14 \#1^4 - 2 \#1^5 - 2 \#1^7 + \#1^8 \&, \right. \right. \\ \left. \frac{1}{1 + 3 \#1^2 + 28 \#1^3 - 5 \#1^4 - 7 \#1^6 + 4 \#1^7} \left(-x - 2 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] - \right. \right. \\ \left. 4 x \#1 - 8 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1 - 9 x \#1^2 - \right. \\ \left. 18 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^2 - 24 x \#1^3 - \right. \\ \left. 48 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^3 + 9 x \#1^4 + \right. \\ \left. 18 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^4 - 4 x \#1^5 - \right. \\ \left. 8 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^5 + x \#1^6 + \right. \\ \left. \left. 2 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^6 \right) \& \right) \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{1 + \operatorname{Sinh}[x]^8}, x, 13, 0 \right\} \\ \frac{\operatorname{ArcTanh} \left[\frac{\operatorname{Coth}[x]}{\sqrt{1 - (-1)^{1/4}}} \right]}{4 \sqrt{1 - (-1)^{1/4}}} + \frac{\operatorname{ArcTanh} \left[\frac{\operatorname{Coth}[x]}{\sqrt{1 + (-1)^{1/4}}} \right]}{4 \sqrt{1 + (-1)^{1/4}}} + \frac{\operatorname{ArcTanh} \left[\frac{\operatorname{Coth}[x]}{\sqrt{1 - (-1)^{3/4}}} \right]}{4 \sqrt{1 - (-1)^{3/4}}} + \frac{\operatorname{ArcTanh} \left[\frac{\operatorname{Coth}[x]}{\sqrt{1 + (-1)^{3/4}}} \right]}{4 \sqrt{1 + (-1)^{3/4}}} \\ 16 \operatorname{RootSum} \left[1 - 8 \#1 + 28 \#1^2 - 56 \#1^3 + 326 \#1^4 - 56 \#1^5 + 28 \#1^6 - 8 \#1^7 + \#1^8 \&, \right. \\ \left. \frac{x \#1^3 + \operatorname{Log} \left[-\operatorname{Cosh}[x] - \operatorname{Sinh}[x] + \operatorname{Cosh}[x] \#1 - \operatorname{Sinh}[x] \#1 \right] \#1^3}{-1 + 7 \#1 - 21 \#1^2 + 163 \#1^3 - 35 \#1^4 + 21 \#1^5 - 7 \#1^6 + \#1^7} \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{1 - \operatorname{Sinh}[x]^5}, x, 8, 0 \right\} \\ - \frac{2 \operatorname{ArcTanh} \left[\frac{(-1)^{1/5} - \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{1 + (-1)^{2/5}}} \right]}{5 \sqrt{1 + (-1)^{2/5}}} - \frac{2 \operatorname{ArcTanh} \left[\frac{(-1)^{3/5} - \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{1 - (-1)^{1/5}}} \right]}{5 \sqrt{1 - (-1)^{1/5}}} + \\ \frac{1}{5} \sqrt{2} \operatorname{ArcTanh} \left[\frac{1 + \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{2}} \right] + \frac{2 \operatorname{ArcTanh} \left[\frac{(-1)^{2/5} + \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{1 + (-1)^{4/5}}} \right]}{5 \sqrt{1 + (-1)^{4/5}}} + \frac{2 \operatorname{ArcTanh} \left[\frac{(-1)^{4/5} + \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{1 - (-1)^{3/5}}} \right]}{5 \sqrt{1 - (-1)^{3/5}}}$$

$$\frac{1}{10} \left(2 \sqrt{2} \operatorname{ArcTanh} \left[\frac{1 + \operatorname{Tanh} \left[\frac{x}{2} \right]}{\sqrt{2}} \right] + \operatorname{RootSum} \left[1 - 2 \#1 - 2 \#1^3 + 14 \#1^4 + 2 \#1^5 + 2 \#1^7 + \#1^8 \&, \right. \right. \\ \left. \frac{1}{-1 - 3 \#1^2 + 28 \#1^3 + 5 \#1^4 + 7 \#1^6 + 4 \#1^7} \left(-x - 2 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] + \right. \right. \\ \left. 4 x \#1 + 8 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1 - 9 x \#1^2 - \right. \\ \left. 18 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^2 + 24 x \#1^3 + \right. \\ \left. 48 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^3 + 9 x \#1^4 + \right. \\ \left. 18 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^4 + 4 x \#1^5 + \right. \\ \left. 8 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^5 + x \#1^6 + \right. \\ \left. \left. 2 \operatorname{Log} \left[-\operatorname{Cosh} \left[\frac{x}{2} \right] - \operatorname{Sinh} \left[\frac{x}{2} \right] + \operatorname{Cosh} \left[\frac{x}{2} \right] \#1 - \operatorname{Sinh} \left[\frac{x}{2} \right] \#1 \right] \#1^6 \right) \& \right) \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \operatorname{Sinh} \left[\frac{a + b x}{c + d x} \right], x, 5, 0 \right\}$$

$$\frac{(b c - a d) \operatorname{Cosh} \left[\frac{b}{d} \right] \operatorname{CoshIntegral} \left[-\frac{b c - a d}{d (c + d x)} \right]}{d^2} + \frac{(c + d x) \operatorname{Sinh} \left[\frac{a + b x}{c + d x} \right]}{d} + \frac{(b c - a d) \operatorname{Sinh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{a}{c + d x} - \frac{b c}{d (c + d x)} \right]}{d^2}$$

$$\frac{1}{2 d^2} \left((b c - a d) \operatorname{CoshIntegral} \left[\frac{b c - a d}{c d + d^2 x} \right] \left(\operatorname{Cosh} \left[\frac{b}{d} \right] - \operatorname{Sinh} \left[\frac{b}{d} \right] \right) + (b c - a d) \operatorname{CoshIntegral} \left[\frac{-b c + a d}{d (c + d x)} \right] \left(\operatorname{Cosh} \left[\frac{b}{d} \right] + \operatorname{Sinh} \left[\frac{b}{d} \right] \right) + \right. \\ \left. 2 c d \operatorname{Sinh} \left[\frac{a + b x}{c + d x} \right] + 2 d^2 x \operatorname{Sinh} \left[\frac{a + b x}{c + d x} \right] + b c \operatorname{Cosh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{-b c + a d}{d (c + d x)} \right] - a d \operatorname{Cosh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{-b c + a d}{d (c + d x)} \right] + \right. \\ \left. b c \operatorname{Sinh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{-b c + a d}{d (c + d x)} \right] - a d \operatorname{Sinh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{-b c + a d}{d (c + d x)} \right] + b c \operatorname{Cosh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{b c - a d}{c d + d^2 x} \right] - \right. \\ \left. a d \operatorname{Cosh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{b c - a d}{c d + d^2 x} \right] - b c \operatorname{Sinh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{b c - a d}{c d + d^2 x} \right] + a d \operatorname{Sinh} \left[\frac{b}{d} \right] \operatorname{SinhIntegral} \left[\frac{b c - a d}{c d + d^2 x} \right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x^2}{\operatorname{Sinh}[x]^{3/2}} - x^2 \sqrt{\operatorname{Sinh}[x]}, x, 4, 0 \right\}$$

$$-\frac{2 x^2 \operatorname{Cosh}[x]}{\sqrt{\operatorname{Sinh}[x]}} + 8 x \sqrt{\operatorname{Sinh}[x]} - \frac{16 i \operatorname{EllipticE} \left[\frac{\pi}{4} - \frac{i x}{2}, 2 \right] \sqrt{\operatorname{Sinh}[x]}}{\sqrt{i \operatorname{Sinh}[x]}}$$

$$-\frac{1}{\sqrt{\operatorname{Sinh}[x]}} 2 \left(x^2 \operatorname{Cosh}[x] - 4 (-2 + x) \operatorname{Sinh}[x] - \right. \\ \left. 8 \sqrt{2} \operatorname{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \operatorname{Cosh}[2 x] + \operatorname{Sinh}[2 x] \right] (-\operatorname{Cosh}[x] + \operatorname{Sinh}[x]) \sqrt{-\operatorname{Sinh}[x] (\operatorname{Cosh}[x] + \operatorname{Sinh}[x])} \right)$$

Problems involving hyperbolic cosines

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{5 + 3 \cosh[c + d x]}, x, 1, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{1}{2} \tanh\left[\frac{1}{2} (c + d x)\right]\right]}{2 d}$$

$$\frac{-\log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] - \sinh\left[\frac{1}{2} (c + d x)\right]\right] + \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] + \sinh\left[\frac{1}{2} (c + d x)\right]\right]}{4 d}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(5 + 3 \cosh[c + d x])^2}, x, 2, 0 \right\}$$

$$\frac{5 \operatorname{ArcTanh}\left[\frac{1}{2} \tanh\left[\frac{1}{2} (c + d x)\right]\right]}{32 d} - \frac{3 \sinh[c + d x]}{16 d (5 + 3 \cosh[c + d x])}$$

$$\frac{1}{64 d (5 + 3 \cosh[c + d x])}$$

$$\left(-15 \cosh[c + d x] \left(\log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] - \sinh\left[\frac{1}{2} (c + d x)\right]\right] - \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] + \sinh\left[\frac{1}{2} (c + d x)\right]\right] \right) + \right.$$

$$\left. 25 \left(-\log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] - \sinh\left[\frac{1}{2} (c + d x)\right]\right] + \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] + \sinh\left[\frac{1}{2} (c + d x)\right]\right] \right) - 12 \sinh[c + d x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(5 + 3 \cosh[c + d x])^3}, x, 3, 0 \right\}$$

$$\frac{59 \operatorname{ArcTanh}\left[\frac{1}{2} \tanh\left[\frac{1}{2} (c + d x)\right]\right]}{1024 d} - \frac{3 \sinh[c + d x]}{32 d (5 + 3 \cosh[c + d x])^2} - \frac{45 \sinh[c + d x]}{512 d (5 + 3 \cosh[c + d x])}$$

$$- \frac{1}{4096 d (5 + 3 \cosh[c + d x])^2} \left(3481 \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] - \sinh\left[\frac{1}{2} (c + d x)\right]\right] + \right.$$

$$3540 \cosh[c + d x] \left(\log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] - \sinh\left[\frac{1}{2} (c + d x)\right]\right] - \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] + \sinh\left[\frac{1}{2} (c + d x)\right]\right] \right) +$$

$$531 \cosh[2 (c + d x)] \left(\log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] - \sinh\left[\frac{1}{2} (c + d x)\right]\right] - \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] + \sinh\left[\frac{1}{2} (c + d x)\right]\right] \right) -$$

$$3481 \log\left[2 \cosh\left[\frac{1}{2} (c + d x)\right] + \sinh\left[\frac{1}{2} (c + d x)\right]\right] + 2184 \sinh[c + d x] + 540 \sinh[2 (c + d x)] \Big)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(5 + 3 \cosh[c + d x])^4}, x, 4, 0 \right\}$$

$$\frac{385 \operatorname{ArcTanh}\left[\frac{1}{2} \tanh\left[\frac{1}{2} (c + d x)\right]\right]}{16384 d} - \frac{\sinh[c + d x]}{16 d (5 + 3 \cosh[c + d x])^3} - \frac{25 \sinh[c + d x]}{512 d (5 + 3 \cosh[c + d x])^2} - \frac{311 \sinh[c + d x]}{8192 d (5 + 3 \cosh[c + d x])}$$

$$\begin{aligned}
& - \frac{1}{131\,072\,d\,(5+3\,\text{Cosh}[c+dx])^3} \\
& \left(296\,450\,\text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] - \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] + 10\,395\,\text{Cosh}[3(c+dx)]\,\text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] - \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\
& \quad 377\,685\,\text{Cosh}[c+dx] \left(\text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] - \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] - \text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] + \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\
& \quad 103\,950\,\text{Cosh}[2(c+dx)] \left(\text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] - \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] - \text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] + \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] \right) - \\
& \quad 296\,450\,\text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] + \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] - 10\,395\,\text{Cosh}[3(c+dx)]\,\text{Log}\left[2\,\text{Cosh}\left[\frac{1}{2}(c+dx)\right] + \text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] + \\
& \quad \left. 175\,788\,\text{Sinh}[c+dx] + 84\,240\,\text{Sinh}[2(c+dx)] + 11\,196\,\text{Sinh}[3(c+dx)] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{x}{a+b\,\text{Cosh}[c+dx]}, x, 8, 0 \right\} \\
& \frac{x\,\text{Log}\left[1+\frac{b\,e^{c+dx}}{a-\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}\,d} - \frac{x\,\text{Log}\left[1+\frac{b\,e^{c+dx}}{a+\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}\,d} + \frac{\text{PolyLog}\left[2, -\frac{b\,e^{c+dx}}{a-\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}\,d^2} - \frac{\text{PolyLog}\left[2, -\frac{b\,e^{c+dx}}{a+\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}\,d^2} \\
& - \frac{1}{\sqrt{-a^2+b^2}\,d^2} \\
& \left(2(c+dx)\,\text{ArcTan}\left[\frac{(a+b)\,\text{Coth}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] - 2\left(c-i\,\text{ArcCos}\left[-\frac{a}{b}\right]\right)\,\text{ArcTan}\left[\frac{(a-b)\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] + \left(\text{ArcCos}\left[-\frac{a}{b}\right] + \right. \right. \\
& \quad \left. 2\,\text{ArcTan}\left[\frac{(a+b)\,\text{Coth}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] - 2\,\text{ArcTan}\left[\frac{(a-b)\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] \right) \text{Log}\left[\frac{\sqrt{-a^2+b^2}\,e^{-\frac{c}{2}-\frac{dx}{2}}}{\sqrt{2}\,\sqrt{b}\,\sqrt{a+b\,\text{Cosh}[c+dx]}}\right] + \\
& \quad \left(\text{ArcCos}\left[-\frac{a}{b}\right] - 2\,\text{ArcTan}\left[\frac{(a+b)\,\text{Coth}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] + 2\,\text{ArcTan}\left[\frac{(a-b)\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] \right) \\
& \quad \text{Log}\left[\frac{\sqrt{-a^2+b^2}\,e^{\frac{1}{2}(c+dx)}}{\sqrt{2}\,\sqrt{b}\,\sqrt{a+b\,\text{Cosh}[c+dx]}}\right] - \\
& \quad \left(\text{ArcCos}\left[-\frac{a}{b}\right] - 2\,\text{ArcTan}\left[\frac{(a-b)\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] \right) \text{Log}\left[\frac{(a+b)\left(a-b+i\sqrt{-a^2+b^2}\right)\left(-1+\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}{b\left(a+b+i\sqrt{-a^2+b^2}\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}\right] - \\
& \quad \left(\text{ArcCos}\left[-\frac{a}{b}\right] + 2\,\text{ArcTan}\left[\frac{(a-b)\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{-a^2+b^2}}\right] \right) \text{Log}\left[\frac{(a+b)\left(-a+b+i\sqrt{-a^2+b^2}\right)\left(1+\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}{b\left(a+b+i\sqrt{-a^2+b^2}\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}\right] + \\
& \quad i \left(\text{PolyLog}\left[2, \frac{(a-i\sqrt{-a^2+b^2})\left(a+b-i\sqrt{-a^2+b^2}\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}{b\left(a+b+i\sqrt{-a^2+b^2}\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}\right] - \right. \\
& \quad \left. \text{PolyLog}\left[2, \frac{(a+i\sqrt{-a^2+b^2})\left(a+b-i\sqrt{-a^2+b^2}\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}{b\left(a+b+i\sqrt{-a^2+b^2}\,\text{Tanh}\left[\frac{1}{2}(c+dx)\right]\right)}\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{e + f x}{(a + b \cosh[c + d x])^2}, x, 16, 0 \right\} \\
& \frac{2 a e \operatorname{ArcTanh}\left[\frac{(a-b) \operatorname{Tanh}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2} d} + \frac{a f x \log\left[1 + \frac{b e^{c+d x}}{a-\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2} d} - \frac{a f x \log\left[1 + \frac{b e^{c+d x}}{a+\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2} d} + \frac{f \log[a + b \cosh[c + d x]]}{(a^2-b^2) d^2} + \\
& \frac{a f \operatorname{PolyLog}\left[2, -\frac{b e^{c+d x}}{a-\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2} d^2} - \frac{a f \operatorname{PolyLog}\left[2, -\frac{b e^{c+d x}}{a+\sqrt{a^2-b^2}}\right]}{(a^2-b^2)^{3/2} d^2} - \frac{b e \sinh[c + d x]}{(a^2-b^2) d (a + b \cosh[c + d x])} - \frac{b f x \sinh[c + d x]}{(a^2-b^2) d (a + b \cosh[c + d x])} \\
& \frac{1}{d^2} \left(-\frac{1}{(-a^2+b^2)^{3/2} \sqrt{(a^2-b^2) e^{2c}} (1+e^{2c})} \left(-2 \sqrt{-a^2+b^2} d e^{2c} \sqrt{(a^2-b^2) e^{2c}} f x + 2 a d e \sqrt{(a^2-b^2) e^{2c}} \operatorname{ArcTan}\left[\frac{a + b e^{c+d x}}{\sqrt{-a^2+b^2}}\right] + 2 a \right. \right. \\
& \quad d e e^{2c} \sqrt{(a^2-b^2) e^{2c}} \operatorname{ArcTan}\left[\frac{a + b e^{c+d x}}{\sqrt{-a^2+b^2}}\right] + \sqrt{-a^2+b^2} \sqrt{(a^2-b^2) e^{2c}} f \log[b + 2 a e^{c+d x} + b e^{2(c+d x)}] + \\
& \quad \sqrt{-a^2+b^2} e^{2c} \sqrt{(a^2-b^2) e^{2c}} f \log[b + 2 a e^{c+d x} + b e^{2(c+d x)}] + a \sqrt{-a^2+b^2} d e^c f x \log\left[1 + \frac{b e^{2c+d x}}{a e^c - \sqrt{(a^2-b^2) e^{2c}}}\right] + \\
& \quad a \sqrt{-a^2+b^2} d e^{3c} f x \log\left[1 + \frac{b e^{2c+d x}}{a e^c - \sqrt{(a^2-b^2) e^{2c}}}\right] - a \sqrt{-a^2+b^2} d e^c f x \log\left[1 + \frac{b e^{2c+d x}}{a e^c + \sqrt{(a^2-b^2) e^{2c}}}\right] - \\
& \quad a \sqrt{-a^2+b^2} d e^{3c} f x \log\left[1 + \frac{b e^{2c+d x}}{a e^c + \sqrt{(a^2-b^2) e^{2c}}}\right] + a \sqrt{-a^2+b^2} e^c (1+e^{2c}) f \operatorname{PolyLog}\left[2, -\frac{b e^{2c+d x}}{a e^c - \sqrt{(a^2-b^2) e^{2c}}}\right] - \\
& \quad \left. a \sqrt{-a^2+b^2} e^c (1+e^{2c}) f \operatorname{PolyLog}\left[2, -\frac{b e^{2c+d x}}{a e^c + \sqrt{(a^2-b^2) e^{2c}}}\right] \right) + \frac{d (e + f x) \operatorname{Sech}[c] (a \sinh[c] - b \sinh[d x])}{(a^2-b^2) (a + b \cosh[c + d x])} \Bigg)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{\sqrt{1 - \cosh[x]^2}}, x, 3, 0 \right\} \\
& - \frac{\operatorname{ArcCoth}[\cosh[x]] \sinh[x]}{\sqrt{-\sinh[x]^2}} \\
& \frac{(-\log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right]) \sinh[x]}{\sqrt{-\sinh[x]^2}}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{\sqrt{-1 + \cosh[x]^2}}, x, 3, 0 \right\} \\
& - \frac{\operatorname{ArcCoth}[\cosh[x]] \sinh[x]}{\sqrt{\sinh[x]^2}}
\end{aligned}$$

$$\frac{\left(-\operatorname{Log}\left[2 \operatorname{Cosh}\left[\frac{x}{2}\right]\right]+\operatorname{Log}\left[2 \operatorname{Sinh}\left[\frac{x}{2}\right]\right]\right) \operatorname{Sinh}[x]}{\sqrt{\operatorname{Sinh}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{x}{a+b \operatorname{Cosh}[x]^2}, x, 9, 0\right\}$$

$$\frac{x \operatorname{Log}\left[1+\frac{b e^{2 x}}{2 a+b-2 \sqrt{a} \sqrt{a+b}}\right]}{2 \sqrt{a} \sqrt{a+b}}-\frac{x \operatorname{Log}\left[1+\frac{b e^{2 x}}{2 a+b+2 \sqrt{a} \sqrt{a+b}}\right]}{2 \sqrt{a} \sqrt{a+b}}+\frac{\operatorname{PolyLog}\left[2,-\frac{b e^{2 x}}{2 a+b-2 \sqrt{a} \sqrt{a+b}}\right]}{4 \sqrt{a} \sqrt{a+b}}-\frac{\operatorname{PolyLog}\left[2,-\frac{b e^{2 x}}{2 a+b+2 \sqrt{a} \sqrt{a+b}}\right]}{4 \sqrt{a} \sqrt{a+b}}$$

$$-\frac{1}{4 \sqrt{-a(a+b)}}\left(4 x \operatorname{ArcTan}\left[\frac{(a+b) \operatorname{Coth}[x]}{\sqrt{-a(a+b)}}\right]+2 i \operatorname{ArcCos}\left[-1-\frac{2 a}{b}\right] \operatorname{ArcTan}\left[\frac{a \operatorname{Tanh}[x]}{\sqrt{-a(a+b)}}\right]+ \right.$$

$$\left.\left(\operatorname{ArcCos}\left[-1-\frac{2 a}{b}\right]+2 \operatorname{ArcTan}\left[\frac{(a+b) \operatorname{Coth}[x]}{\sqrt{-a(a+b)}}\right]-2 \operatorname{ArcTan}\left[\frac{a \operatorname{Tanh}[x]}{\sqrt{-a(a+b)}}\right]\right) \operatorname{Log}\left[\frac{\sqrt{2} \sqrt{-a(a+b)} e^{-x}}{\sqrt{b} \sqrt{2 a+b+b \operatorname{Cosh}[2 x]}}\right]+$$

$$\left(\operatorname{ArcCos}\left[-1-\frac{2 a}{b}\right]-2 \operatorname{ArcTan}\left[\frac{(a+b) \operatorname{Coth}[x]}{\sqrt{-a(a+b)}}\right]+2 \operatorname{ArcTan}\left[\frac{a \operatorname{Tanh}[x]}{\sqrt{-a(a+b)}}\right]\right) \operatorname{Log}\left[\frac{\sqrt{2} \sqrt{-a(a+b)} e^x}{\sqrt{b} \sqrt{2 a+b+b \operatorname{Cosh}[2 x]}}\right]-$$

$$\left(\operatorname{ArcCos}\left[-1-\frac{2 a}{b}\right]-2 \operatorname{ArcTan}\left[\frac{a \operatorname{Tanh}[x]}{\sqrt{-a(a+b)}}\right]\right)\left(\operatorname{Log}[2]+\operatorname{Log}\left[\frac{(a+b)\left(a+i \sqrt{-a(a+b)}\right)(-1+\operatorname{Tanh}[x])}{b(a+b+i \sqrt{-a(a+b)}) \operatorname{Tanh}[x]}\right]\right)-$$

$$\left(\operatorname{ArcCos}\left[-1-\frac{2 a}{b}\right]+2 \operatorname{ArcTan}\left[\frac{a \operatorname{Tanh}[x]}{\sqrt{-a(a+b)}}\right]\right)\left(\operatorname{Log}[2]+\operatorname{Log}\left[-\frac{(a+b)\left(a-i \sqrt{-a(a+b)}\right)(1+\operatorname{Tanh}[x])}{b(a+b+i \sqrt{-a(a+b)}) \operatorname{Tanh}[x]}\right]\right)+$$

$$i\left(\operatorname{PolyLog}\left[2,\frac{\left(2 a+b-2 i \sqrt{-a(a+b)}\right)(a+b-i \sqrt{-a(a+b)}) \operatorname{Tanh}[x]}{b(a+b+i \sqrt{-a(a+b)}) \operatorname{Tanh}[x]}\right]-\right.$$

$$\left.\operatorname{PolyLog}\left[2,\frac{\left(2 a+b+2 i \sqrt{-a(a+b)}\right)(a+b-i \sqrt{-a(a+b)}) \operatorname{Tanh}[x]}{b(a+b+i \sqrt{-a(a+b)}) \operatorname{Tanh}[x]}\right]\right)\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{a+b \operatorname{Cosh}[x]^3}, x, 7, 0\right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1 / 3}-b^{1 / 3}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2 / 3}-b^{2 / 3}}}\right]}{3 a^{2 / 3} \sqrt{a^{2 / 3}-b^{2 / 3}}}+\frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1 / 3}-(-1)^{2 / 3} b^{1 / 3}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2 / 3}+(-1)^{1 / 3} b^{2 / 3}}}\right]}{3 a^{2 / 3} \sqrt{a^{2 / 3}+(-1)^{1 / 3} b^{2 / 3}}}+\frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1 / 3}+(-1)^{1 / 3} b^{1 / 3}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2 / 3}-(-1)^{2 / 3} b^{2 / 3}}}\right]}{3 a^{2 / 3} \sqrt{a^{2 / 3}-(-1)^{2 / 3} b^{2 / 3}}}$$

$$\frac{2}{3} \operatorname{RootSum}\left[b+3 b \# 1^2+8 a \# 1^3+3 b \# 1^4+b \# 1^6 \&, \frac{x \# 1+2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right] \# 1-\operatorname{Sinh}\left[\frac{x}{2}\right] \# 1\right] \# 1}{b+4 a \# 1+2 b \# 1^2+b \# 1^4} \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{a+b \operatorname{Cosh}[x]^5}, x, 11, 0\right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/5}-b^{1/5}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}-b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}-b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/5}+(-1)^{3/5} b^{1/5}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}+(-1)^{1/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}+(-1)^{1/5} b^{2/5}}} +$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/5}+(-1)^{1/5} b^{1/5}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}-(-1)^{2/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}-(-1)^{2/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/5}-(-1)^{4/5} b^{1/5}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}+(-1)^{3/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}+(-1)^{3/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/5}-(-1)^{2/5} b^{1/5}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5}-(-1)^{4/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5}-(-1)^{4/5} b^{2/5}}}$$

$$\frac{8}{5} \operatorname{RootSum}\left[b+5 b \#1^2+10 b \#1^4+32 a \#1^5+10 b \#1^6+5 b \#1^8+b \#1^{10} \&, \right.$$

$$\left. \frac{x \#1^3+2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right] \#1-\operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^3}{b+4 b \#1^2+16 a \#1^3+6 b \#1^4+4 b \#1^6+b \#1^8} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{a+b \operatorname{Cosh}[x]^6}, x, 10, 0\right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Tanh}[x]}{\sqrt{a^{1/3}+b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3}+b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Tanh}[x]}{\sqrt{a^{1/3}-(-1)^{1/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3}-(-1)^{1/3} b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Tanh}[x]}{\sqrt{a^{1/3}+(-1)^{2/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3}+(-1)^{2/3} b^{1/3}}}$$

$$\frac{16}{3} \operatorname{RootSum}\left[b+6 b \#1+15 b \#1^2+64 a \#1^3+20 b \#1^3+15 b \#1^4+6 b \#1^5+b \#1^6 \&, \right.$$

$$\left. \frac{x \#1^2+\operatorname{Log}\left[-\operatorname{Cosh}[x]-\operatorname{Sinh}[x]+\operatorname{Cosh}[x] \#1-\operatorname{Sinh}[x] \#1\right] \#1^2}{b+5 b \#1+32 a \#1^2+10 b \#1^2+10 b \#1^3+5 b \#1^4+b \#1^5} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{a+b \operatorname{Cosh}[x]^8}, x, 13, 0\right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Tanh}[x]}{\sqrt{(-a)^{1/4}-b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}-b^{1/4}}} - \frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Tanh}[x]}{\sqrt{(-a)^{1/4}-i b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}-i b^{1/4}}} - \frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Tanh}[x]}{\sqrt{(-a)^{1/4}+i b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}+i b^{1/4}}} - \frac{\operatorname{ArcTanh}\left[\frac{(-a)^{1/8} \operatorname{Tanh}[x]}{\sqrt{(-a)^{1/4}+b^{1/4}}}\right]}{4 (-a)^{7/8} \sqrt{(-a)^{1/4}+b^{1/4}}}$$

$$16 \operatorname{RootSum}\left[b+8 b \#1+28 b \#1^2+56 b \#1^3+256 a \#1^4+70 b \#1^4+56 b \#1^5+28 b \#1^6+8 b \#1^7+b \#1^8 \&, \right.$$

$$\left. \frac{x \#1^3+\operatorname{Log}\left[-\operatorname{Cosh}[x]-\operatorname{Sinh}[x]+\operatorname{Cosh}[x] \#1-\operatorname{Sinh}[x] \#1\right] \#1^3}{b+7 b \#1+21 b \#1^2+128 a \#1^3+35 b \#1^3+35 b \#1^4+21 b \#1^5+7 b \#1^6+b \#1^7} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{a-b \operatorname{Cosh}[x]^3}, x, 7, 0\right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/3}+b^{1/3}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}-b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}-b^{2/3}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/3}+(-1)^{2/3} b^{1/3}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}+(-1)^{1/3} b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}+(-1)^{1/3} b^{2/3}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{\left(a^{1/3}-(-1)^{1/3} b^{1/3}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/3}-(-1)^{2/3} b^{2/3}}}\right]}{3 a^{2/3} \sqrt{a^{2/3}-(-1)^{2/3} b^{2/3}}}$$

$$-\frac{2}{3} \operatorname{RootSum}\left[b+3 b \#1^2-8 a \#1^3+3 b \#1^4+b \#1^6 \&, \frac{x \#1+2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right] \#1-\operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1}{b-4 a \#1+2 b \#1^2+b \#1^4} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a - b \cosh[x]^5}, x, 11, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{(a^{1/5} + b^{1/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} - b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} - b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(a^{1/5} - (-1)^{2/5} b^{1/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} + (-1)^{1/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} + (-1)^{1/5} b^{2/5}}} +$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{(a^{1/5} - (-1)^{1/5} b^{1/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} - (-1)^{2/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} - (-1)^{2/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(a^{1/5} + (-1)^{4/5} b^{1/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} + (-1)^{3/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} + (-1)^{3/5} b^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(a^{1/5} + (-1)^{2/5} b^{1/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^{2/5} - (-1)^{4/5} b^{2/5}}}\right]}{5 a^{4/5} \sqrt{a^{2/5} - (-1)^{4/5} b^{2/5}}}$$

$$- \frac{8}{5} \operatorname{RootSum}\left[b + 5 b \#1^2 + 10 b \#1^4 - 32 a \#1^5 + 10 b \#1^6 + 5 b \#1^8 + b \#1^{10} \&, \right.$$

$$\left. \frac{x \#1^3 + 2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^3}{b + 4 b \#1^2 - 16 a \#1^3 + 6 b \#1^4 + 4 b \#1^6 + b \#1^8} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a - b \cosh[x]^6}, x, 10, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Tanh}[x]}{\sqrt{a^{1/3} - b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3} - b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Tanh}[x]}{\sqrt{a^{1/3} + (-1)^{1/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3} + (-1)^{1/3} b^{1/3}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/6} \operatorname{Tanh}[x]}{\sqrt{a^{1/3} - (-1)^{2/3} b^{1/3}}}\right]}{3 a^{5/6} \sqrt{a^{1/3} - (-1)^{2/3} b^{1/3}}}$$

$$- \frac{16}{3} \operatorname{RootSum}\left[b + 6 b \#1 + 15 b \#1^2 - 64 a \#1^3 + 20 b \#1^3 + 15 b \#1^4 + 6 b \#1^5 + b \#1^6 \&, \right.$$

$$\left. \frac{x \#1^2 + \operatorname{Log}\left[-\cosh[x] - \sinh[x] + \cosh[x] \#1 - \sinh[x] \#1\right] \#1^2}{b + 5 b \#1 - 32 a \#1^2 + 10 b \#1^2 + 10 b \#1^3 + 5 b \#1^4 + b \#1^5} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a - b \cosh[x]^8}, x, 13, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Tanh}[x]}{\sqrt{a^{1/4} - b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} - b^{1/4}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Tanh}[x]}{\sqrt{a^{1/4} - i b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} - i b^{1/4}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Tanh}[x]}{\sqrt{a^{1/4} + i b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} + i b^{1/4}}} + \frac{\operatorname{ArcTanh}\left[\frac{a^{1/8} \operatorname{Tanh}[x]}{\sqrt{a^{1/4} + b^{1/4}}}\right]}{4 a^{7/8} \sqrt{a^{1/4} + b^{1/4}}}$$

$$- 16 \operatorname{RootSum}\left[b + 8 b \#1 + 28 b \#1^2 + 56 b \#1^3 - 256 a \#1^4 + 70 b \#1^4 + 56 b \#1^5 + 28 b \#1^6 + 8 b \#1^7 + b \#1^8 \&, \right.$$

$$\left. \frac{x \#1^3 + \operatorname{Log}\left[-\cosh[x] - \sinh[x] + \cosh[x] \#1 - \sinh[x] \#1\right] \#1^3}{b + 7 b \#1 + 21 b \#1^2 - 128 a \#1^3 + 35 b \#1^3 + 35 b \#1^4 + 21 b \#1^5 + 7 b \#1^6 + b \#1^7} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{1 + \cosh[x]^5}, x, 8, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{(1 + (-1)^{1/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 - (-1)^{2/5}}}\right]}{5 \sqrt{1 - (-1)^{2/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(1 + (-1)^{3/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 + (-1)^{1/5}}}\right]}{5 \sqrt{1 + (-1)^{1/5}}} +$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{(1 - (-1)^{2/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 - (-1)^{4/5}}}\right]}{5 \sqrt{1 - (-1)^{4/5}}} + \frac{2 \operatorname{ArcTanh}\left[\frac{(1 - (-1)^{4/5}) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{1 + (-1)^{3/5}}}\right]}{5 \sqrt{1 + (-1)^{3/5}}} + \frac{\sinh[x]}{5 (1 + \cosh[x])}$$

$$\begin{aligned}
& -\frac{1}{10} \text{RootSum}\left[1 - 2 \#1 + 8 \#1^2 - 14 \#1^3 + 30 \#1^4 - 14 \#1^5 + 8 \#1^6 - 2 \#1^7 + \#1^8 \&, \right. \\
& \quad \frac{1}{-1 + 8 \#1 - 21 \#1^2 + 60 \#1^3 - 35 \#1^4 + 24 \#1^5 - 7 \#1^6 + 4 \#1^7} \left(x + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] - \right. \\
& \quad 4 x \#1 - 8 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1 + \\
& \quad 15 x \#1^2 + 30 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^2 - \\
& \quad 40 x \#1^3 - 80 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^3 + \\
& \quad 15 x \#1^4 + 30 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^4 - \\
& \quad 4 x \#1^5 - 8 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^5 + x \#1^6 + \\
& \quad \left. 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^6 \right) \& \left. + \frac{1}{5} \tanh\left[\frac{x}{2}\right] \right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{1 + \cosh[x]^8}, x, 11, 0 \right\} \\
& \frac{\text{ArcTanh}\left[\frac{\tanh[x]}{\sqrt{1 - (-1)^{1/4}}}\right]}{4 \sqrt{1 - (-1)^{1/4}}} + \frac{\text{ArcTanh}\left[\frac{\tanh[x]}{\sqrt{1 + (-1)^{1/4}}}\right]}{4 \sqrt{1 + (-1)^{1/4}}} + \frac{\text{ArcTanh}\left[\frac{\tanh[x]}{\sqrt{1 - (-1)^{3/4}}}\right]}{4 \sqrt{1 - (-1)^{3/4}}} + \frac{\text{ArcTanh}\left[\frac{\tanh[x]}{\sqrt{1 + (-1)^{3/4}}}\right]}{4 \sqrt{1 + (-1)^{3/4}}} \\
& 16 \text{RootSum}\left[1 + 8 \#1 + 28 \#1^2 + 56 \#1^3 + 326 \#1^4 + 56 \#1^5 + 28 \#1^6 + 8 \#1^7 + \#1^8 \&, \right. \\
& \quad \left. \frac{x \#1^3 + \log\left[-\cosh[x] - \sinh[x] + \cosh[x] \#1 - \sinh[x] \#1\right] \#1^3}{1 + 7 \#1 + 21 \#1^2 + 163 \#1^3 + 35 \#1^4 + 21 \#1^5 + 7 \#1^6 + \#1^7} \& \right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{1 - \cosh[x]^5}, x, 8, 0 \right\} \\
& \frac{2 \text{ArcTanh}\left[\frac{(1 - (-1)^{1/5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{1 - (-1)^{2/5}}}\right]}{5 \sqrt{1 - (-1)^{2/5}}} + \frac{2 \text{ArcTanh}\left[\frac{(1 - (-1)^{3/5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{1 + (-1)^{1/5}}}\right]}{5 \sqrt{1 + (-1)^{1/5}}} + \\
& \frac{2 \text{ArcTanh}\left[\frac{(1 + (-1)^{2/5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{1 - (-1)^{4/5}}}\right]}{5 \sqrt{1 - (-1)^{4/5}}} + \frac{2 \text{ArcTanh}\left[\frac{(1 + (-1)^{4/5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{1 + (-1)^{3/5}}}\right]}{5 \sqrt{1 + (-1)^{3/5}}} - \frac{\sinh[x]}{5 (1 - \cosh[x])}
\end{aligned}$$

$$\frac{1}{5} \operatorname{Coth}\left[\frac{x}{2}\right] + \frac{1}{10} \operatorname{RootSum}\left[1 + 2 \#1 + 8 \#1^2 + 14 \#1^3 + 30 \#1^4 + 14 \#1^5 + 8 \#1^6 + 2 \#1^7 + \#1^8 \&, \frac{1}{1 + 8 \#1 + 21 \#1^2 + 60 \#1^3 + 35 \#1^4 + 24 \#1^5 + 7 \#1^6 + 4 \#1^7}\right. \\ \left. \left(x + 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] + 4 x \#1 + 8 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1 + 15 x \#1^2 + 30 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^2 + 40 x \#1^3 + 80 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^3 + 15 x \#1^4 + 30 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^4 + 4 x \#1^5 + 8 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^5 + x \#1^6 + 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^6\right) \& \right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\operatorname{Cosh}\left[\frac{a+b x}{c+d x}\right], x, 5, 0\right\} \\ \frac{(c+d x) \operatorname{Cosh}\left[\frac{a+b x}{c+d x}\right]}{d} + \frac{(b c-a d) \operatorname{CoshIntegral}\left[-\frac{b c-a d}{d(c+d x)}\right] \operatorname{Sinh}\left[\frac{b}{d}\right]}{d^2} + \frac{(b c-a d) \operatorname{Cosh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{a}{c+d x}-\frac{b c}{d(c+d x)}\right]}{d^2} \\ \frac{1}{2 d^2} \left(2 c d \operatorname{Cosh}\left[\frac{a+b x}{c+d x}\right] + 2 d^2 x \operatorname{Cosh}\left[\frac{a+b x}{c+d x}\right] + (b c-a d) \operatorname{CoshIntegral}\left[\frac{b c-a d}{c d+d^2 x}\right] \left(-\operatorname{Cosh}\left[\frac{b}{d}\right] + \operatorname{Sinh}\left[\frac{b}{d}\right]\right) + \right. \\ (b c-a d) \operatorname{CoshIntegral}\left[\frac{-b c+a d}{d(c+d x)}\right] \left(\operatorname{Cosh}\left[\frac{b}{d}\right] + \operatorname{Sinh}\left[\frac{b}{d}\right]\right) + b c \operatorname{Cosh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{-b c+a d}{d(c+d x)}\right] - \\ a d \operatorname{Cosh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{-b c+a d}{d(c+d x)}\right] + b c \operatorname{Sinh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{-b c+a d}{d(c+d x)}\right] - \\ a d \operatorname{Sinh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{-b c+a d}{d(c+d x)}\right] - b c \operatorname{Cosh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{b c-a d}{c d+d^2 x}\right] + \\ \left. a d \operatorname{Cosh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{b c-a d}{c d+d^2 x}\right] + b c \operatorname{Sinh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{b c-a d}{c d+d^2 x}\right] - a d \operatorname{Sinh}\left[\frac{b}{d}\right] \operatorname{SinhIntegral}\left[\frac{b c-a d}{c d+d^2 x}\right]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{x^2}{\operatorname{Cosh}[x]^{3/2}} + x^2 \sqrt{\operatorname{Cosh}[x]}, x, 3, 0\right\} \\ -8 x \sqrt{\operatorname{Cosh}[x]} - 16 i \operatorname{EllipticE}\left[\frac{i x}{2}, 2\right] + \frac{2 x^2 \operatorname{Sinh}[x]}{\sqrt{\operatorname{Cosh}[x]}} \\ \frac{1}{\sqrt{\operatorname{Cosh}[x]}} \\ 2 \left(x^2 \operatorname{Sinh}[x] - 2 (\operatorname{Cosh}[x] - \operatorname{Sinh}[x]) \left(4 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -\operatorname{Cosh}[2 x] - \operatorname{Sinh}[2 x]\right] \sqrt{1 + \operatorname{Cosh}[2 x] + \operatorname{Sinh}[2 x]} + \right. \right. \\ \left. \left. (-2 + x) (1 + \operatorname{Cosh}[2 x] + \operatorname{Sinh}[2 x])\right)\right)$$

Problems involving hyperbolic tangents

Valid but unnecessarily complicated antiderivative:

 $\{x \tanh[a + b x], x, 4, 0\}$

$$-\frac{x^2}{2} + \frac{x \log[1 + e^{2a+2bx}]}{b} + \frac{\text{PolyLog}[2, -e^{2a+2bx}]}{2b^2}$$

$$\frac{1}{2} \left(x^2 \tanh[a] - \frac{1}{b^2} \left(-i b \pi x + i \pi \log[1 + e^{2bx}] - 2bx \log[1 - e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}] - i \pi \log[\cosh[bx]] - \right. \right.$$

$$2 \text{ArcTanh}[\text{Coth}[a]] (bx + \log[1 - e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]) - \log[i \sinh[bx + \text{ArcTanh}[\text{Coth}[a]]]] \Big) +$$

$$\left. \left. \text{PolyLog}[2, e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}] + b^2 e^{-\text{ArcTanh}[\text{Coth}[a]]} x^2 \sqrt{-\text{Csch}[a]^2 \tanh[a]} \right) \right)$$

Valid but unnecessarily complicated antiderivative:

 $\{x \tanh[a + b x]^3, x, 6, 0\}$

$$-\frac{x^2}{2} + \frac{x \log[1 + e^{2a+2bx}]}{b} + \frac{\text{PolyLog}[2, -e^{2a+2bx}]}{2b^2} + \frac{x \text{Sech}[a + b x]^2}{2b} - \frac{\tanh[a + b x]}{2b^2}$$

$$\frac{1}{2} \left(\frac{i \pi x}{b} - \frac{i \pi \log[1 + e^{2bx}]}{b^2} + \frac{2x \log[1 - e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]}{b} + \frac{i \pi \log[\cosh[bx]]}{b^2} + \right.$$

$$\frac{2 \text{ArcTanh}[\text{Coth}[a]] (bx + \log[1 - e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]) - \log[i \sinh[bx + \text{ArcTanh}[\text{Coth}[a]]]]}{b^2} -$$

$$\frac{\text{PolyLog}[2, e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]}{b^2} + \frac{x \text{Sech}[a + b x]^2}{b} -$$

$$\left. \frac{\text{Sech}[a] \text{Sech}[a + b x] \sinh[bx]}{b^2} + x^2 \tanh[a] - e^{-\text{ArcTanh}[\text{Coth}[a]]} x^2 \sqrt{-\text{Csch}[a]^2 \tanh[a]} \right)$$

Valid but unnecessarily complicated antiderivative:

 $\{x^2 \tanh[a + b x]^2, x, 6, 0\}$

$$-\frac{x^2}{b} + \frac{x^3}{3} + \frac{2x \log[1 + e^{2a+2bx}]}{b^2} + \frac{\text{PolyLog}[2, -e^{2a+2bx}]}{b^3} - \frac{x^2 \tanh[a + b x]}{b}$$

$$\frac{i \pi x}{b^2} + \frac{x^3}{3} - \frac{i \pi \log[1 + e^{2bx}]}{b^3} + \frac{2x \log[1 - e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]}{b^2} + \frac{i \pi \log[\cosh[bx]]}{b^3} +$$

$$\frac{2 \text{ArcTanh}[\text{Coth}[a]] (bx + \log[1 - e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]) - \log[i \sinh[bx + \text{ArcTanh}[\text{Coth}[a]]]]}{b^3} -$$

$$\frac{\text{PolyLog}[2, e^{-2(bx + \text{ArcTanh}[\text{Coth}[a]])}]}{b^3} - \frac{x^2 \text{Sech}[a] \text{Sech}[a + b x] \sinh[bx]}{b} - \frac{e^{-\text{ArcTanh}[\text{Coth}[a]]} x^2 \sqrt{-\text{Csch}[a]^2 \tanh[a]}}{b}$$

Valid but unnecessarily complicated antiderivative:

 $\{\sqrt{1 - \tanh[x]^2}, x, 2, 0\}$ $\text{ArcSin}[\tanh[x]]$

$$2 \text{ArcTan}\left[\tanh\left[\frac{x}{2}\right]\right] \cosh[x] \sqrt{\text{Sech}[x]^2}$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{a+b \tanh[x]^2}, x, 4, 0\}$$

$$-\sqrt{b} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \tanh[x]}{\sqrt{a+b \tanh[x]^2}}\right] + \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \tanh[x]}{\sqrt{a+b \tanh[x]^2}}\right]$$

$$\begin{aligned} & \frac{1}{2} \left(-\sqrt{a+b} \operatorname{Log}\left[(a+b)^{3/2} (-1+\tanh[x])\right] + \right. \\ & \quad \left. \sqrt{a+b} \operatorname{Log}\left[(a+b)^{3/2} (1+\tanh[x])\right] - 2\sqrt{b} \operatorname{Log}\left[2\left(b \tanh[x] + \sqrt{b} \sqrt{a+b \tanh[x]^2}\right)\right] - \right. \\ & \quad \left. \sqrt{a+b} \operatorname{Log}\left[4\left(a-b \tanh[x] + \sqrt{a+b} \sqrt{a+b \tanh[x]^2}\right)\right] + \sqrt{a+b} \operatorname{Log}\left[-4\left(a+b \tanh[x] + \sqrt{a+b} \sqrt{a+b \tanh[x]^2}\right)\right] \right) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{\sqrt{a+b \tanh[x]^2}}, x, 2, 0\right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \tanh[x]}{\sqrt{a+b \tanh[x]^2}}\right]}{\sqrt{a+b}}$$

$$\begin{aligned} & \frac{1}{2\sqrt{a+b}} \left(-\operatorname{Log}\left[\sqrt{a+b} (-1+\tanh[x])\right] + \operatorname{Log}\left[\sqrt{a+b} (1+\tanh[x])\right] - \right. \\ & \quad \left. \operatorname{Log}\left[4\left(a-b \tanh[x] + \sqrt{a+b} \sqrt{a+b \tanh[x]^2}\right)\right] + \operatorname{Log}\left[-4\left(a+b \tanh[x] + \sqrt{a+b} \sqrt{a+b \tanh[x]^2}\right)\right] \right) \end{aligned}$$

Problems involving hyperbolic cotangents

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Coth}[a + b x], x, 4, 0\}$$

$$-\frac{x^2}{2} + \frac{x \operatorname{Log}\left[1 - e^{2a+2bx}\right]}{b} + \frac{\operatorname{PolyLog}\left[2, e^{2a+2bx}\right]}{2b^2}$$

$$\frac{1}{2} \left(\frac{i \pi x}{b} + x^2 \operatorname{Coth}[a] - \frac{i \pi \operatorname{Log}\left[1 + e^{2bx}\right]}{b^2} + \frac{2 x \operatorname{Log}\left[1 - e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right]}{b} + \frac{i \pi \operatorname{Log}[\operatorname{Cosh}[bx]]}{b^2} + \right.$$

$$\left. \frac{2 \operatorname{ArcTanh}[\operatorname{Tanh}[a]] \left(bx + \operatorname{Log}\left[1 - e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] - \operatorname{Log}[i \operatorname{Sinh}[bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]]]\right]}{b^2} - \right.$$

$$\left. \frac{\operatorname{PolyLog}\left[2, e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right]}{b^2} - e^{-\operatorname{ArcTanh}[\operatorname{Tanh}[a]]} x^2 \operatorname{Coth}[a] \sqrt{\operatorname{Sech}[a]^2} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Coth}[a + b x]^3, x, 6, 0\}$$

$$-\frac{x^2}{2} - \frac{\operatorname{Coth}[a + b x]}{2b^2} - \frac{x \operatorname{Csch}[a + b x]^2}{2b} + \frac{x \operatorname{Log}\left[1 - e^{2a+2bx}\right]}{b} + \frac{\operatorname{PolyLog}\left[2, e^{2a+2bx}\right]}{2b^2}$$

$$\frac{1}{2} \left(\frac{i \pi x}{b} + x^2 \operatorname{Coth}[a] - \frac{x \operatorname{Csch}[a + b x]^2}{b} - \frac{i \pi \operatorname{Log}\left[1 + e^{2bx}\right]}{b^2} + \frac{2 x \operatorname{Log}\left[1 - e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right]}{b} + \frac{i \pi \operatorname{Log}[\operatorname{Cosh}[bx]]}{b^2} + \right.$$

$$\left. \frac{2 \operatorname{ArcTanh}[\operatorname{Tanh}[a]] \left(bx + \operatorname{Log}\left[1 - e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] - \operatorname{Log}[i \operatorname{Sinh}[bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]]]\right]}{b^2} - \right.$$

$$\left. \frac{\operatorname{PolyLog}\left[2, e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right]}{b^2} - e^{-\operatorname{ArcTanh}[\operatorname{Tanh}[a]]} x^2 \operatorname{Coth}[a] \sqrt{\operatorname{Sech}[a]^2} + \frac{\operatorname{Csch}[a] \operatorname{Csch}[a + b x] \operatorname{Sinh}[bx]}{b^2} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x^2 \operatorname{Coth}[a + b x]^2, x, 6, 0\}$$

$$-\frac{x^2}{b} + \frac{x^3}{3} - \frac{x^2 \operatorname{Coth}[a + b x]}{b} + \frac{2 x \operatorname{Log}\left[1 - e^{2a+2bx}\right]}{b^2} + \frac{\operatorname{PolyLog}\left[2, e^{2a+2bx}\right]}{b^3}$$

$$\frac{x^3}{3} + \frac{1}{b^3} \left(i b \pi x - i \pi \operatorname{Log}\left[1 + e^{2bx}\right] + 2 b x \operatorname{Log}\left[1 - e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] + i \pi \operatorname{Log}[\operatorname{Cosh}[bx]] + \right.$$

$$\left. 2 \operatorname{ArcTanh}[\operatorname{Tanh}[a]] \left(bx + \operatorname{Log}\left[1 - e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] - \operatorname{Log}[i \operatorname{Sinh}[bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]]]\right] - \right.$$

$$\left. \operatorname{PolyLog}\left[2, e^{-2(bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] - b^2 e^{-\operatorname{ArcTanh}[\operatorname{Tanh}[a]]} x^2 \operatorname{Coth}[a] \sqrt{\operatorname{Sech}[a]^2} \right) + \frac{x^2 \operatorname{Csch}[a] \operatorname{Csch}[a + b x] \operatorname{Sinh}[bx]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{1 + \operatorname{Coth}[x]}, x, 1, 0\}$$

$$\sqrt{2} \operatorname{ArcCoth}\left[\frac{\sqrt{1 + \operatorname{Coth}[x]}}{\sqrt{2}}\right]$$

$$\frac{(1 + i) \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \sqrt{i(1 + \operatorname{Coth}[x])}\right] (1 + \operatorname{Coth}[x])^{3/2}}{(i(1 + \operatorname{Coth}[x]))^{3/2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{1 + \text{Coth}[x]}}, x, 2, 0 \right\}$$

$$\frac{\text{ArcCoth}\left[\frac{\sqrt{1+\text{Coth}[x]}}{\sqrt{2}}\right]}{\sqrt{2}} - \frac{1}{\sqrt{1 + \text{Coth}[x]}}$$

$$\frac{(1 - i) \text{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \sqrt{i(1 + \text{Coth}[x])}\right] + (1 - i) \text{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \sqrt{i(1 + \text{Coth}[x])}\right] \text{Coth}[x] - 2 \sqrt{i(1 + \text{Coth}[x])}}{2 \sqrt{i(1 + \text{Coth}[x])} \sqrt{1 + \text{Coth}[x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{1 - \text{Coth}[x]^2}, x, 2, 0 \right\}$$

$$\text{ArcCsc}[\text{Tanh}[x]]$$

$$\sqrt{-\text{Csch}[x]^2} \left(-\text{Log}\left[2 \cosh\left[\frac{x}{2}\right]\right] + \text{Log}\left[2 \sinh\left[\frac{x}{2}\right]\right] \right) \sinh[x]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{-1 + \text{Coth}[x]^2}, x, 3, 0 \right\}$$

$$-\text{ArcTanh}\left[\frac{\text{Coth}[x]}{\sqrt{\text{Csch}[x]^2}}\right]$$

$$\sqrt{\text{Csch}[x]^2} \left(-\text{Log}\left[2 \cosh\left[\frac{x}{2}\right]\right] + \text{Log}\left[2 \sinh\left[\frac{x}{2}\right]\right] \right) \sinh[x]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{a + b \text{Coth}[x]^2}, x, 4, 0 \right\}$$

$$-\sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Coth}[x]}{\sqrt{a + b \text{Coth}[x]^2}}\right] + \sqrt{a + b} \text{ArcTanh}\left[\frac{\sqrt{a + b} \text{Coth}[x]}{\sqrt{a + b \text{Coth}[x]^2}}\right]$$

$$\frac{1}{2} \left(-\sqrt{a + b} \text{Log}\left[(a + b)^{3/2} (-1 + \text{Coth}[x])\right] + \right.$$

$$\left. \sqrt{a + b} \text{Log}\left[(a + b)^{3/2} (1 + \text{Coth}[x])\right] - 2 \sqrt{b} \text{Log}\left[2 \left(b \text{Coth}[x] + \sqrt{b} \sqrt{a + b \text{Coth}[x]^2}\right)\right] - \right.$$

$$\left. \sqrt{a + b} \text{Log}\left[-4 \left(a - b \text{Coth}[x] + \sqrt{a + b} \sqrt{a + b \text{Coth}[x]^2}\right)\right] + \sqrt{a + b} \text{Log}\left[4 \left(a + b \text{Coth}[x] + \sqrt{a + b} \sqrt{a + b \text{Coth}[x]^2}\right)\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + b \text{Coth}[x]^2}}, x, 2, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Coth}[x]}{\sqrt{a+b \text{Coth}[x]^2}}\right]}{\sqrt{a + b}}$$

$$\frac{1}{2 \sqrt{a + b}} \left(-\text{Log}\left[\sqrt{a + b} (-1 + \text{Coth}[x])\right] + \text{Log}\left[\sqrt{a + b} (1 + \text{Coth}[x])\right] - \right.$$

$$\left. \text{Log}\left[-4 \left(a - b \text{Coth}[x] + \sqrt{a + b} \sqrt{a + b \text{Coth}[x]^2}\right)\right] + \text{Log}\left[4 \left(a + b \text{Coth}[x] + \sqrt{a + b} \sqrt{a + b \text{Coth}[x]^2}\right)\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{ (1 + \text{Coth}[x]^2)^{3/2}, x, 8, 0 \}$$

$$-\frac{5}{2} \text{ArcCsch}[\text{Tanh}[x]] + 2\sqrt{2} \text{ArcTanh}\left[\frac{\sqrt{2} \text{Coth}[x]}{\sqrt{1 + \text{Coth}[x]^2}}\right] - \frac{1}{2} \text{Coth}[x] \sqrt{1 + \text{Coth}[x]^2}$$

$$\frac{1}{2} (1 + \text{Coth}[x]^2)^{3/2} \text{Sinh}[x] \left(-\text{Cosh}[x] \text{Sech}[2x] - \frac{\text{ArcTan}\left[\frac{\text{Cosh}[x]}{\sqrt{-\text{Cosh}[2x]}}\right] \text{Sinh}[x]^2}{(-\text{Cosh}[2x])^{3/2}} - \right.$$

$$\left. \frac{4 \text{ArcTanh}\left[\frac{\text{Cosh}[x]}{\sqrt{\text{Cosh}[2x]}}\right] \text{Sinh}[x]^2}{\text{Cosh}[2x]^{3/2}} + \frac{4\sqrt{2} \text{Log}\left[\sqrt{2} \text{Cosh}[x] + \sqrt{\text{Cosh}[2x]}\right] \text{Sinh}[x]^2}{\text{Cosh}[2x]^{3/2}} \right)$$

Problems involving hyperbolic secants

Valid but unnecessarily complicated antiderivative:

 $\{x \operatorname{Sech}[a + b x], x, 4, 0\}$

$$\frac{2 x \operatorname{ArcTan}\left[e^{a+b x}\right]}{b}-\frac{i \operatorname{PolyLog}\left[2,-i e^{a+b x}\right]}{b^2}+\frac{i \operatorname{PolyLog}\left[2, i e^{a+b x}\right]}{b^2}$$

$$-\frac{1}{2 b^2}\left(\left(-2 i a+\pi-2 i b x\right)\left(\operatorname{Log}\left[1-i e^{a+b x}\right]-\operatorname{Log}\left[1+i e^{a+b x}\right]\right)-\right.$$

$$\left.\left(-2 i a+\pi\right) \operatorname{Log}\left[\operatorname{Cot}\left[\frac{1}{4}\left(2 i a+\pi+2 i b x\right)\right]\right]+2 i\left(\operatorname{PolyLog}\left[2,-i e^{a+b x}\right]-\operatorname{PolyLog}\left[2, i e^{a+b x}\right]\right)\right)$$

Valid but unnecessarily complicated antiderivative:

 $\{x^2 \operatorname{Sech}[a + b x]^2, x, 5, 0\}$

$$\frac{x^2}{b}-\frac{2 x \operatorname{Log}\left[1+e^{2 a+2 b x}\right]}{b^2}-\frac{\operatorname{PolyLog}\left[2,-e^{2 a+2 b x}\right]}{b^3}+\frac{x^2 \operatorname{Tanh}[a+b x]}{b}$$

$$\frac{1}{b^3}\left(-i b \pi x+i \pi \operatorname{Log}\left[1+e^{2 b x}\right]-2 b x \operatorname{Log}\left[1-e^{-2(b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right]-i \pi \operatorname{Log}[\operatorname{Cosh}[b x]]-\right.$$

$$2 \operatorname{ArcTanh}[\operatorname{Coth}[a]](b x+\operatorname{Log}\left[1-e^{-2(b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right]-\operatorname{Log}[i \operatorname{Sinh}[b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]]]])+\\ \left.\operatorname{PolyLog}\left[2, e^{-2(b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right]+b^2 x^2 \operatorname{Sech}[a] \operatorname{Sech}[a+b x] \operatorname{Sinh}[b x]+b^2 e^{-\operatorname{ArcTanh}[\operatorname{Coth}[a]]} x^2 \sqrt{-\operatorname{Csch}[a]^2 \operatorname{Tanh}[a]}\right)$$

Valid but unnecessarily complicated antiderivative:

 $\{(c+d x) \operatorname{Sech}[a + b x], x, 5, 0\}$

$$\frac{2(c+d x) \operatorname{ArcTan}\left[e^{a+b x}\right]}{b}-\frac{i d \operatorname{PolyLog}\left[2,-i e^{a+b x}\right]}{b^2}+\frac{i d \operatorname{PolyLog}\left[2, i e^{a+b x}\right]}{b^2}$$

$$\frac{1}{b^2}\left(2 b c \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}(a+b x)\right]\right]-\frac{1}{2} d\left(\left(-2 i a+\pi-2 i b x\right)\left(\operatorname{Log}\left[1-i e^{a+b x}\right]-\operatorname{Log}\left[1+i e^{a+b x}\right]\right)-\right.$$

$$\left.\left(-2 i a+\pi\right) \operatorname{Log}\left[\operatorname{Cot}\left[\frac{1}{4}\left(2 i a+\pi+2 i b x\right)\right]\right]+2 i\left(\operatorname{PolyLog}\left[2,-i e^{a+b x}\right]-\operatorname{PolyLog}\left[2, i e^{a+b x}\right]\right)\right)\right)$$

Valid but unnecessarily complicated antiderivative:

 $\{(c+d x)^2 \operatorname{Sech}[a + b x]^2, x, 6, 0\}$

$$\frac{(c+d x)^2}{b}-\frac{2 d(c+d x) \operatorname{Log}\left[1+e^{2 a+2 b x}\right]}{b^2}-\frac{d^2 \operatorname{PolyLog}\left[2,-e^{2 a+2 b x}\right]}{b^3}+\frac{(c+d x)^2 \operatorname{Tanh}[a+b x]}{b}$$

$$\frac{1}{b^3} \operatorname{Sech}[a]\left(d^2 e^{-\operatorname{ArcTanh}[\operatorname{Coth}[a]]}\left(-i b e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \pi x \operatorname{Coth}[a]+b^2 x^2 \sqrt{-\operatorname{Csch}[a]^2}+i e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \pi \operatorname{Coth}[a] \operatorname{Log}\left[1+e^{2 b x}\right]-\right.\right.$$

$$2 b e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} x \operatorname{Coth}[a] \operatorname{Log}\left[1-e^{-2(b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right]-i e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \pi \operatorname{Coth}[a] \operatorname{Log}[\operatorname{Cosh}[b x]]-\\ 2 e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \operatorname{ArcTanh}[\operatorname{Coth}[a]] \operatorname{Coth}[a](b x+\operatorname{Log}\left[1-e^{-2(b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right]-\operatorname{Log}[i \operatorname{Sinh}[b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]]]])+\\ \left.\left.e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \operatorname{Coth}[a] \operatorname{PolyLog}\left[2, e^{-2(b x+\operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right]\right) \operatorname{Sinh}[a]+\\ \left.2 b c d(-\operatorname{Cosh}[a] \operatorname{Log}[\operatorname{Cosh}[a+b x]]+b x \operatorname{Sinh}[a])+b^2(c+d x)^2 \operatorname{Sech}[a+b x] \operatorname{Sinh}[b x]\right)$$

Valid but unnecessarily complicated antiderivative:

 $\{\sqrt{\operatorname{Sech}[x]^2}, x, 2, 0\}$

$\text{ArcSin}[\text{Tanh}[x]]$

$$2 \text{ArcTan}\left[\text{Tanh}\left[\frac{x}{2}\right]\right] \text{Cosh}[x] \sqrt{\text{Sech}[x]^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{3+5 \text{Sech}[x]}, x, 3, 0\right\}$$

$$\frac{x}{3} - \frac{5}{6} \text{ArcTanh}\left[\frac{1}{2} \text{Tanh}\left[\frac{x}{2}\right]\right]$$

$$\frac{1}{12} \left(4x + 5 \log\left[2 \cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right]\right] - 5 \log\left[2 \cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]\right]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\sqrt{1+\text{Sech}[x]^2}, x, 4, 0\right\}$$

$$\text{ArcSin}\left[\frac{\text{Tanh}[x]}{\sqrt{2}}\right] + \text{ArcTanh}\left[\frac{\text{Tanh}[x]}{\sqrt{2-\text{Tanh}[x]^2}}\right]$$

$$\frac{\sqrt{2} \left(\text{ArcSinh}\left[\frac{\sinh[x]}{\sqrt{2}}\right] + \text{ArcTan}\left[\frac{\sqrt{2} \sinh[x]}{\sqrt{3+\cosh[2x]}}\right]\right) \cosh[x] \sqrt{1+\text{Sech}[x]^2}}{\sqrt{3+\cosh[2x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\sqrt{a+b \text{Sech}[x]^2}, x, 4, 0\right\}$$

$$\sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \text{Tanh}[x]}{\sqrt{a+b \text{Sech}[x]^2}}\right] + \sqrt{a} \text{ArcTanh}\left[\frac{\sqrt{a} \text{Tanh}[x]}{\sqrt{a+b \text{Sech}[x]^2}}\right]$$

$$\frac{1}{a+2b+a \cosh[2x]} \sqrt{2} \cosh[x]$$

$$\frac{\left(\sqrt{b} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{b} \sinh[x]}{\sqrt{a+2b+a \cosh[2x]}}\right] \sqrt{a+2b+a \cosh[2x]} + \sqrt{a} \sqrt{a+b} \text{ArcSinh}\left[\frac{\sqrt{a} \sinh[x]}{\sqrt{a+b}}\right] \sqrt{\frac{a+2b+a \cosh[2x]}{a+b}}\right)}{\sqrt{a+b \text{Sech}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{\sqrt{1+\text{Sech}[x]^2}}, x, 2, 0\right\}$$

$$\text{ArcTanh}\left[\frac{\text{Tanh}[x]}{\sqrt{2-\text{Tanh}[x]^2}}\right]$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{2} \sinh[x]}{\sqrt{3+\cosh[2x]}}\right] \sqrt{3+\cosh[2x]} \text{Sech}[x]}{\sqrt{2} \sqrt{1+\text{Sech}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-1 - \text{Sech}[x]^2}}, x, 2, 0 \right\}$$

$$\text{ArcTan}\left[\frac{\text{Tanh}[x]}{\sqrt{-2 + \text{Tanh}[x]^2}}\right]$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{2} \text{Sinh}[x]}{\sqrt{3 + \text{Cosh}[2x]}}\right] \sqrt{3 + \text{Cosh}[2x]} \text{Sech}[x]}{\sqrt{2} \sqrt{-1 - \text{Sech}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + b \text{Sech}[x]^2}}, x, 2, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a} \text{Tanh}[x]}{\sqrt{a + b \text{Sech}[x]^2}}\right]}{\sqrt{a}}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a} \text{Sinh}[x]}{\sqrt{a + 2b + a \text{Cosh}[2x]}}\right] \sqrt{a + 2b + a \text{Cosh}[2x]} \text{Sech}[x]}{\sqrt{2} \sqrt{a} \sqrt{a + b \text{Sech}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (1 + \text{Sech}[x]^2)^{3/2}, x, 7, 0 \right\}$$

$$2 \text{ArcSin}\left[\frac{\text{Tanh}[x]}{\sqrt{2}}\right] + \text{ArcTanh}\left[\frac{\text{Tanh}[x]}{\sqrt{2 - \text{Tanh}[x]^2}}\right] + \frac{1}{2} \text{Tanh}[x] \sqrt{2 - \text{Tanh}[x]^2}$$

$$\frac{1}{4 (1 + \text{Cosh}[x]) \sqrt{\frac{3 + \text{Cosh}[2x]}{(1 + \text{Cosh}[x])^2}}} \text{Sech}[x] \sqrt{1 + \text{Sech}[x]^2} \left(24 (-1)^{1/4} \text{Cosh}[x]^2 \text{EllipticF}\left[i \text{ArcSinh}\left[(-1)^{1/4} \text{Tanh}\left[\frac{x}{2}\right]\right], -1\right] - \right.$$

$$32 (-1)^{1/4} \text{Cosh}[x]^2 \text{EllipticPi}\left[-i, i \text{ArcSinh}\left[(-1)^{1/4} \text{Tanh}\left[\frac{x}{2}\right]\right], -1\right] -$$

$$8 (-1)^{1/4} \text{EllipticPi}\left[i, \text{ArcSin}\left[(-1)^{3/4} \text{Tanh}\left[\frac{x}{2}\right]\right], -1\right] - 8 (-1)^{1/4} \text{Cosh}[2x] \text{EllipticPi}\left[i, \text{ArcSin}\left[(-1)^{3/4} \text{Tanh}\left[\frac{x}{2}\right]\right], -1\right] +$$

$$\left. \sqrt{(3 + \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} \text{Sinh}[x] + \text{Cosh}[x] \sqrt{(3 + \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} \text{Sinh}[x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (-1 - \text{Sech}[x]^2)^{3/2}, x, 8, 0 \right\}$$

$$\text{ArcTan}\left[\frac{\text{Tanh}[x]}{\sqrt{-2 + \text{Tanh}[x]^2}}\right] + 2 \text{ArcTanh}\left[\frac{\text{Tanh}[x]}{\sqrt{-2 + \text{Tanh}[x]^2}}\right] - \frac{1}{2} \text{Tanh}[x] \sqrt{-2 + \text{Tanh}[x]^2}$$

$$\begin{aligned}
& - \frac{1}{4 (1 + \cosh[x]) \sqrt{\frac{3 + \cosh[2x]}{(1 + \cosh[x])^2}}} \\
& \operatorname{Sech}[x] \sqrt{-1 - \operatorname{Sech}[x]^2} \left(24 (-1)^{1/4} \cosh[x]^2 \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[(-1)^{1/4} \tanh\left[\frac{x}{2}\right]\right], -1\right] - 32 (-1)^{1/4} \cosh[x]^2 \right. \\
& \quad \operatorname{EllipticPi}\left[-i, i \operatorname{ArcSinh}\left[(-1)^{1/4} \tanh\left[\frac{x}{2}\right]\right], -1\right] - 8 (-1)^{1/4} \operatorname{EllipticPi}\left[i, \operatorname{ArcSin}\left[(-1)^{3/4} \tanh\left[\frac{x}{2}\right]\right], -1\right] - \\
& \quad 8 (-1)^{1/4} \cosh[2x] \operatorname{EllipticPi}\left[i, \operatorname{ArcSin}\left[(-1)^{3/4} \tanh\left[\frac{x}{2}\right]\right], -1\right] + \\
& \quad \left. \sqrt{(3 + \cosh[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4 \sinh[x] + \cosh[x]} \sqrt{(3 + \cosh[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4 \sinh[x]} \right)
\end{aligned}$$

Incorrect antiderivative:

$$\begin{aligned}
& \left\{ \operatorname{Sech}\left[a + \frac{\log[c x^n]}{n(-2+p)}\right]^p, x, 1, 0 \right\} \\
& \frac{(2-p)x \operatorname{Sech}\left[a - \frac{\log[c x^n]}{n(2-p)}\right]^{-2+p}}{1-p} + \frac{(2-p)x \operatorname{Sech}\left[a - \frac{\log[c x^n]}{n(2-p)}\right]^{-1+p} \sinh\left[a - \frac{\log[c x^n]}{n(2-p)}\right]}{1-p} \\
& \frac{2^{-1+p} e^a (-2+p)x (c x^n)^{\frac{1}{n(-2+p)}} \left(\frac{e^{\frac{a(2+p)}{-2+p}} (c x^n)^{\frac{1}{n(-2+p)}}}{\frac{4a}{e^{-2+p}} + \frac{2ap}{e^{-2+p}}} \right)^{-1+p}}{-1+p}
\end{aligned}$$

Incorrect antiderivative:

$$\begin{aligned}
& \left\{ \operatorname{Sech}\left[a - \frac{\log[c x^n]}{n(-2+p)}\right]^p, x, 1, 0 \right\} \\
& \frac{(2-p)x \operatorname{Sech}\left[a + \frac{\log[c x^n]}{n(2-p)}\right]^{-2+p}}{1-p} - \frac{(2-p)x \operatorname{Sech}\left[a + \frac{\log[c x^n]}{n(2-p)}\right]^{-1+p} \sinh\left[a + \frac{\log[c x^n]}{n(2-p)}\right]}{1-p} \\
& \frac{2^{-1+p} e^{-a} (-2+p)x (c x^n)^{\frac{1}{n(-2+p)}} \left(\frac{e^{\frac{a(2+p)}{-2+p}} (c x^n)^{\frac{1}{n(-2+p)}}}{\frac{2ap}{e^{-2+p}} + \frac{4a}{e^{-2+p}}} \right)^{-1+p}}{-1+p}
\end{aligned}$$

Problems involving hyperbolic cosecants

Valid but unnecessarily complicated antiderivative:

$$\{ \text{Csch}[a + b x], x, 1, 0 \}$$

$$-\frac{\text{ArcCoth}[\text{Cosh}[a + b x]]}{b}$$

$$\frac{-\text{Log}\left[2 \text{Cosh}\left[\frac{1}{2}(a + b x)\right]\right] + \text{Log}\left[2 \text{Sinh}\left[\frac{1}{2}(a + b x)\right]\right]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\{ x \text{Csch}[a + b x], x, 4, 0 \}$$

$$-\frac{2 x \text{ArcTanh}\left[e^{a+b x}\right]}{b} - \frac{\text{PolyLog}\left[2, -e^{a+b x}\right]}{b^2} + \frac{\text{PolyLog}\left[2, e^{a+b x}\right]}{b^2}$$

$$\frac{1}{b^2} \left(a \text{Log}\left[1 - e^{-a-b x}\right] + b x \text{Log}\left[1 - e^{-a-b x}\right] - a \text{Log}\left[1 + e^{-a-b x}\right] - \right.$$

$$\left. b x \text{Log}\left[1 + e^{-a-b x}\right] - a \text{Log}\left[\text{Tanh}\left[\frac{1}{2}(a + b x)\right]\right] + \text{PolyLog}\left[2, -e^{-a-b x}\right] - \text{PolyLog}\left[2, e^{-a-b x}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{ x^2 \text{Csch}[a + b x]^2, x, 5, 0 \}$$

$$-\frac{x^2}{b} - \frac{x^2 \text{Coth}[a + b x]}{b} + \frac{2 x \text{Log}\left[1 - e^{2 a+2 b x}\right]}{b^2} + \frac{\text{PolyLog}\left[2, e^{2 a+2 b x}\right]}{b^3}$$

$$\frac{1}{b^3} \text{Csch}[a] \left(-b^2 e^{-\text{ArcTanh}[\text{Tanh}[a]]} x^2 \text{Cosh}[a] \sqrt{\text{Sech}[a]^2} + i b \pi x \text{Sinh}[a] - \right.$$

$$i \pi \text{Log}\left[1 + e^{2 b x}\right] \text{Sinh}[a] + 2 b x \text{Log}\left[1 - e^{-2(b x + \text{ArcTanh}[\text{Tanh}[a]])}\right] \text{Sinh}[a] + i \pi \text{Log}[\text{Cosh}[b x]] \text{Sinh}[a] +$$

$$2 \text{ArcTanh}[\text{Tanh}[a]] \left(b x + \text{Log}\left[1 - e^{-2(b x + \text{ArcTanh}[\text{Tanh}[a]])}\right] - \text{Log}[i \text{Sinh}[b x + \text{ArcTanh}[\text{Tanh}[a]]]\right] \text{Sinh}[a] -$$

$$\left. \text{PolyLog}\left[2, e^{-2(b x + \text{ArcTanh}[\text{Tanh}[a]])}\right] \text{Sinh}[a] + b^2 x^2 \text{Csch}[a + b x] \text{Sinh}[b x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{ x \text{Csch}[a + b x]^3, x, 5, 0 \}$$

$$\frac{x \text{ArcTanh}\left[e^{a+b x}\right]}{b} - \frac{\text{Csch}[a + b x]}{2 b^2} - \frac{x \text{Coth}[a + b x] \text{Csch}[a + b x]}{2 b} + \frac{\text{PolyLog}\left[2, -e^{a+b x}\right]}{2 b^2} - \frac{\text{PolyLog}\left[2, e^{a+b x}\right]}{2 b^2}$$

$$\frac{1}{8 b^2} \left(-b x \text{Csch}\left[\frac{1}{2}(a + b x)\right]^2 - 4 a \text{Log}\left[1 - e^{-a-b x}\right] - 4 b x \text{Log}\left[1 - e^{-a-b x}\right] + 4 a \text{Log}\left[1 + e^{-a-b x}\right] + \right.$$

$$4 b x \text{Log}\left[1 + e^{-a-b x}\right] + 4 a \text{Log}\left[\text{Tanh}\left[\frac{1}{2}(a + b x)\right]\right] - 4 \text{PolyLog}\left[2, -e^{-a-b x}\right] + 4 \text{PolyLog}\left[2, e^{-a-b x}\right] -$$

$$\left. b x \text{Sech}\left[\frac{1}{2}(a + b x)\right]^2 + 2 \text{Csch}\left[\frac{a}{2}\right] \text{Csch}\left[\frac{1}{2}(a + b x)\right] \text{Sinh}\left[\frac{b x}{2}\right] + 2 \text{Sech}\left[\frac{a}{2}\right] \text{Sech}\left[\frac{1}{2}(a + b x)\right] \text{Sinh}\left[\frac{b x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{ (c + d x) \text{Csch}[a + b x], x, 5, 0 \}$$

$$-\frac{2(c + d x) \text{ArcTanh}\left[e^{a+b x}\right]}{b} - \frac{d \text{PolyLog}\left[2, -e^{a+b x}\right]}{b^2} + \frac{d \text{PolyLog}\left[2, e^{a+b x}\right]}{b^2}$$

$$\frac{1}{b^2} \left(a \, d \, \text{Log}[1 - e^{-a-bx}] + b \, d \, x \, \text{Log}[1 - e^{-a-bx}] - a \, d \, \text{Log}[1 + e^{-a-bx}] - b \, d \, x \, \text{Log}[1 + e^{-a-bx}] - b \, c \, \text{Log}\left[2 \, \text{Cosh}\left[\frac{1}{2} (a + bx)\right]\right] + \right. \\ \left. b \, c \, \text{Log}\left[2 \, \text{Sinh}\left[\frac{1}{2} (a + bx)\right]\right] - a \, d \, \text{Log}\left[\text{Tanh}\left[\frac{1}{2} (a + bx)\right]\right] + d \, \text{PolyLog}[2, -e^{-a-bx}] - d \, \text{PolyLog}[2, e^{-a-bx}]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\{(c+dx)^2 \text{Csch}[a+bx]^2, x, 6, 0\} \\ -\frac{(c+dx)^2}{b} - \frac{(c+dx)^2 \text{Coth}[a+bx]}{b} + \frac{2d(c+dx) \text{Log}[1 - e^{2a+2bx}]}{b^2} + \frac{d^2 \text{PolyLog}[2, e^{2a+2bx}]}{b^3} \\ \frac{1}{b^3} \text{Csch}[a] \left(-2bcd(bx \text{Cosh}[a] - \text{Log}[\text{Sinh}[a+bx]] \text{Sinh}[a]) + b^2(c+dx)^2 \text{Csch}[a+bx] \text{Sinh}[bx] + \right. \\ d^2 e^{-\text{ArcTanh}[\text{Tanh}[a]]} \text{Cosh}[a] \left(-b^2 x^2 \sqrt{\text{Sech}[a]^2} + i b e^{\text{ArcTanh}[\text{Tanh}[a]]} \pi x \text{Tanh}[a] - i e^{\text{ArcTanh}[\text{Tanh}[a]]} \pi \text{Log}[1 + e^{2bx}] \text{Tanh}[a] + \right. \\ 2 b e^{\text{ArcTanh}[\text{Tanh}[a]]} x \text{Log}[1 - e^{-2(bx+\text{ArcTanh}[\text{Tanh}[a]])}] \text{Tanh}[a] + i e^{\text{ArcTanh}[\text{Tanh}[a]]} \pi \text{Log}[\text{Cosh}[bx]] \text{Tanh}[a] + \\ \left. 2 e^{\text{ArcTanh}[\text{Tanh}[a]]} \text{ArcTanh}[\text{Tanh}[a]] (bx + \text{Log}[1 - e^{-2(bx+\text{ArcTanh}[\text{Tanh}[a]])}] - \text{Log}[i \text{Sinh}[bx + \text{ArcTanh}[\text{Tanh}[a]]]) \right) \text{Tanh}[a] - \\ \left. e^{\text{ArcTanh}[\text{Tanh}[a]]} \text{PolyLog}[2, e^{-2(bx+\text{ArcTanh}[\text{Tanh}[a]])}] \text{Tanh}[a] \right) \left. \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{(c+dx) \text{Csch}[a+bx]^3, x, 6, 0\} \\ \frac{(c+dx) \text{ArcTanh}[e^{a+bx}]}{b} - \frac{d \text{Csch}[a+bx]}{2b^2} - \frac{(c+dx) \text{Coth}[a+bx] \text{Csch}[a+bx]}{2b} + \frac{d \text{PolyLog}[2, -e^{a+bx}]}{2b^2} - \frac{d \text{PolyLog}[2, e^{a+bx}]}{2b^2} \\ -\frac{1}{8b^2} \left(bcd \text{Csch}\left[\frac{1}{2} (a+bx)\right]^2 + bdx \text{Csch}\left[\frac{1}{2} (a+bx)\right]^2 + 4ad \text{Log}[1 - e^{-a-bx}] + 4bdx \text{Log}[1 - e^{-a-bx}] - \right. \\ 4ad \text{Log}[1 + e^{-a-bx}] - 4bdx \text{Log}[1 + e^{-a-bx}] - 4bc \text{Log}[\text{Cosh}\left[\frac{1}{2} (a+bx)\right]] + 4bc \text{Log}[\text{Sinh}\left[\frac{1}{2} (a+bx)\right]] - \\ 4ad \text{Log}[\text{Tanh}\left[\frac{1}{2} (a+bx)\right]] + 4d \text{PolyLog}[2, -e^{-a-bx}] - 4d \text{PolyLog}[2, e^{-a-bx}] + bc \text{Sech}\left[\frac{1}{2} (a+bx)\right]^2 + \\ \left. bdx \text{Sech}\left[\frac{1}{2} (a+bx)\right]^2 - 2d \text{Csch}\left[\frac{a}{2}\right] \text{Csch}\left[\frac{1}{2} (a+bx)\right] \text{Sinh}\left[\frac{bx}{2}\right] - 2d \text{Sech}\left[\frac{a}{2}\right] \text{Sech}\left[\frac{1}{2} (a+bx)\right] \text{Sinh}\left[\frac{bx}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{(c+dx)^2 \text{Csch}[a+bx]^3, x, 9, 0\} \\ -\frac{d^2 \text{ArcCoth}[\text{Cosh}[a+bx]]}{b^3} + \frac{(c+dx)^2 \text{ArcTanh}[e^{a+bx}]}{b} - \frac{d(c+dx) \text{Csch}[a+bx]}{b^2} - \frac{(c+dx)^2 \text{Coth}[a+bx] \text{Csch}[a+bx]}{2b} + \\ \frac{d(c+dx) \text{PolyLog}[2, -e^{a+bx}]}{b^2} - \frac{d(c+dx) \text{PolyLog}[2, e^{a+bx}]}{b^2} - \frac{d^2 \text{PolyLog}[3, -e^{a+bx}]}{b^3} + \frac{d^2 \text{PolyLog}[3, e^{a+bx}]}{b^3} \\ -\frac{1}{8b^3} \left(8bd(c+dx) \text{Csch}[a] + b^2(c+dx)^2 \text{Csch}\left[\frac{1}{2} (a+bx)\right]^2 - \right. \\ 4(-2b^2cdx \text{Log}[1 - e^{a+bx}] - b^2d^2x^2 \text{Log}[1 - e^{a+bx}] - b^2c^2 \text{Log}[-1 + e^{a+bx}] + 2d^2 \text{Log}[-1 + e^{a+bx}] + b^2c^2 \text{Log}[1 + e^{a+bx}] - \\ 2d^2 \text{Log}[1 + e^{a+bx}] + 2b^2cdx \text{Log}[1 + e^{a+bx}] + b^2d^2x^2 \text{Log}[1 + e^{a+bx}] + 2bd(c+dx) \text{PolyLog}[2, -e^{a+bx}] - \\ 2bd(c+dx) \text{PolyLog}[2, e^{a+bx}] - 2d^2 \text{PolyLog}[3, -e^{a+bx}] + 2d^2 \text{PolyLog}[3, e^{a+bx}]) + b^2(c+dx)^2 \text{Sech}\left[\frac{1}{2} (a+bx)\right]^2 - \\ \left. 4bd(c+dx) \text{Csch}\left[\frac{a}{2}\right] \text{Csch}\left[\frac{1}{2} (a+bx)\right] \text{Sinh}\left[\frac{bx}{2}\right] - 4bd(c+dx) \text{Sech}\left[\frac{a}{2}\right] \text{Sech}\left[\frac{1}{2} (a+bx)\right] \text{Sinh}\left[\frac{bx}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{-\text{Csch}[x]^2}, x, 2, 0\}$$

$$\text{ArcCsc}[\text{Tanh}[x]]$$

$$\sqrt{-\text{Csch}[x]^2} \left(-\text{Log}\left[2 \cosh\left[\frac{x}{2}\right]\right] + \text{Log}\left[2 \sinh\left[\frac{x}{2}\right]\right] \right) \sinh[x]$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{a \text{Csch}[x]^2}, x, 2, 0\}$$

$$-\text{ArcCoth}[\cosh[x]] \sqrt{a \text{Csch}[x]^2} \sinh[x]$$

$$\sqrt{a \text{Csch}[x]^2} \left(-\text{Log}\left[2 \cosh\left[\frac{x}{2}\right]\right] + \text{Log}\left[2 \sinh\left[\frac{x}{2}\right]\right] \right) \sinh[x]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + i a \text{Csch}[x]}}, x, 1, 0 \right\}$$

$$\frac{\left(\sqrt{2} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{a}}{\sqrt{-a + i a \text{Csch}[x]}}\right] + 2 \text{ArcTan}\left[\frac{\sqrt{-a + i a \text{Csch}[x]}}{\sqrt{a}}\right] \right) \sqrt{-a + i a \text{Csch}[x]} \sqrt{a + i a \text{Csch}[x]} \tanh[x] - \left(\sqrt{a} \coth[x] \left(\sqrt{2} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{a}}{\sqrt{i a (i + \text{Csch}[x])}}\right] - i \left(\text{Log}\left[\frac{2 i a (2 \sqrt{a} + i \sqrt{i a (i + \text{Csch}[x])} + \sqrt{a + i a \text{Csch}[x]})}{\sqrt{a} + \sqrt{a + i a \text{Csch}[x]}}\right] + \text{Log}\left[\frac{4 i a^{3/2} - 2 a (\sqrt{i a (i + \text{Csch}[x])} + i \sqrt{a + i a \text{Csch}[x]})}{-\sqrt{a} + \sqrt{a + i a \text{Csch}[x]}}\right] \right) \right) \right) / \left(\sqrt{i a (i + \text{Csch}[x])} \sqrt{a + i a \text{Csch}[x]} \right)}{a^{3/2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a - i a \text{Csch}[x]}}, x, 1, 0 \right\}$$

$$\frac{\left(\sqrt{2} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{a}}{\sqrt{-a - i a \text{Csch}[x]}}\right] + 2 \text{ArcTan}\left[\frac{\sqrt{-a - i a \text{Csch}[x]}}{\sqrt{a}}\right] \right) \sqrt{-a - i a \text{Csch}[x]} \sqrt{a - i a \text{Csch}[x]} \tanh[x] - \left(\sqrt{a} \coth[x] \left(\sqrt{2} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{a}}{\sqrt{-i a (-i + \text{Csch}[x])}}\right] - i \left(\text{Log}\left[\frac{2 i a (2 \sqrt{a} + i \sqrt{-i a (-i + \text{Csch}[x])} + \sqrt{a - i a \text{Csch}[x]})}{\sqrt{a} + \sqrt{a - i a \text{Csch}[x]}}\right] + \text{Log}\left[\frac{4 i a^{3/2} - 2 a (\sqrt{-i a (-i + \text{Csch}[x])} + i \sqrt{a - i a \text{Csch}[x]})}{-\sqrt{a} + \sqrt{a - i a \text{Csch}[x]}}\right] \right) \right) \right) / \left(\sqrt{a (-1 - i \text{Csch}[x])} \sqrt{a - i a \text{Csch}[x]} \right)}{a^{3/2}}$$

Valid but unnecessarily complicated antiderivative:

$$\{a + b \text{Csch}[x], x, 2, 0\}$$

$$a x - b \text{ArcCoth}[\cosh[x]]$$

$$a x - b \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] + b \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a + b \operatorname{Csch}[x])^2, x, 4, 0 \right\}$$

$$a^2 x - 2 a b \operatorname{ArcCoth}[\cosh[x]] - b^2 \operatorname{Coth}[x]$$

$$\frac{1}{2} \left(-b^2 \operatorname{Coth}\left[\frac{x}{2}\right] + 2 a \left(a x - 2 b \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] + 2 b \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right] \right) - b^2 \operatorname{Tanh}\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a + b \operatorname{Csch}[x])^3, x, 6, 0 \right\}$$

$$a^3 x - 3 a^2 b \operatorname{ArcCoth}[\cosh[x]] + \frac{1}{2} b^3 \operatorname{ArcCoth}[\cosh[x]] - 3 a b^2 \operatorname{Coth}[x] - \frac{1}{2} b^3 \operatorname{Coth}[x] \operatorname{Csch}[x]$$

$$\frac{1}{8} \left(8 a^3 x - 12 a b^2 \operatorname{Coth}\left[\frac{x}{2}\right] - b^3 \operatorname{Csch}\left[\frac{x}{2}\right]^2 - 24 a^2 b \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] + \right. \\ \left. 4 b^3 \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] + 24 a^2 b \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right] - 4 b^3 \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right] - b^3 \operatorname{Sech}\left[\frac{x}{2}\right]^2 - 12 a b^2 \operatorname{Tanh}\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{3 + 5 i \operatorname{Csch}[x]}, x, 3, 0 \right\}$$

$$\frac{x}{3} - \frac{5}{6} i \operatorname{ArcTan}\left[\frac{1}{4} \left(3 - 5 i \operatorname{Tanh}\left[\frac{x}{2}\right] \right)\right]$$

$$\frac{1}{24} \left(8 x + 10 i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] - 2 \sinh\left[\frac{x}{2}\right]}{2 \cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right]}\right] - \right. \\ \left. 10 i \operatorname{ArcTan}\left[\frac{2 \cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{\cosh\left[\frac{x}{2}\right] + 2 \sinh\left[\frac{x}{2}\right]}\right] + 5 \operatorname{Log}[5 \cosh[x] - 4 \sinh[x]] - 5 \operatorname{Log}[5 \cosh[x] + 4 \sinh[x]] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{1 - \operatorname{Csch}[x]^2}, x, 4, 0 \right\}$$

$$\operatorname{ArcSin}\left[\frac{\operatorname{Coth}[x]}{\sqrt{2}}\right] + \operatorname{ArcTanh}\left[\frac{\operatorname{Coth}[x]}{\sqrt{2 - \operatorname{Coth}[x]^2}}\right]$$

$$\frac{\sqrt{2 - 2 \operatorname{Csch}[x]^2} \left(\operatorname{ArcTan}\left[\frac{\sqrt{2} \operatorname{Cosh}[x]}{\sqrt{-3 + \operatorname{Cosh}[2 x]}}\right] + \operatorname{Log}\left[\sqrt{2} \operatorname{Cosh}[x] + \sqrt{-3 + \operatorname{Cosh}[2 x]}\right] \right) \operatorname{Sinh}[x]}{\sqrt{-3 + \operatorname{Cosh}[2 x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{-1 + \operatorname{Csch}[x]^2}, x, 4, 0 \right\}$$

$$-\operatorname{ArcTan}\left[\frac{\operatorname{Coth}[x]}{\sqrt{-2 + \operatorname{Coth}[x]^2}}\right] - \operatorname{ArcTanh}\left[\frac{\operatorname{Coth}[x]}{\sqrt{-2 + \operatorname{Coth}[x]^2}}\right]$$

$$\frac{\sqrt{2} \sqrt{-1 + \text{Csch}[x]^2} \left(\text{ArcTan}\left[\frac{\sqrt{2} \text{Cosh}[x]}{\sqrt{-3 + \text{Cosh}[2x]}}\right] + \text{Log}\left[\sqrt{2} \text{Cosh}[x] + \sqrt{-3 + \text{Cosh}[2x]}\right] \right) \text{Sinh}[x]}{\sqrt{-3 + \text{Cosh}[2x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{a + b \text{Csch}[x]^2}, x, 4, 0 \right\}$$

$$\sqrt{a} \text{ArcTanh}\left[\frac{\sqrt{a} \text{Coth}[x]}{\sqrt{a + b \text{Csch}[x]^2}}\right] - \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Coth}[x]}{\sqrt{a + b \text{Csch}[x]^2}}\right]$$

$$\frac{\sqrt{a + b \text{Csch}[x]^2} \left(-\sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{b} \text{Cosh}[x]}{\sqrt{-a + 2 b + a \text{Cosh}[2x]}}\right] + \sqrt{a} \text{Log}\left[\sqrt{2} \sqrt{a} \text{Cosh}[x] + \sqrt{-a + 2 b + a \text{Cosh}[2x]}\right] \right) \text{Sinh}[x]}{\sqrt{-\frac{a}{2} + b + \frac{1}{2} a \text{Cosh}[2x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{1 - \text{Csch}[x]^2}}, x, 2, 0 \right\}$$

$$\text{ArcTanh}\left[\frac{\text{Coth}[x]}{\sqrt{2 - \text{Coth}[x]^2}}\right]$$

$$\frac{\sqrt{-3 + \text{Cosh}[2x]} \text{Csch}[x] \text{Log}\left[\sqrt{2} \text{Cosh}[x] + \sqrt{-3 + \text{Cosh}[2x]}\right]}{\sqrt{2 - 2 \text{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-1 + \text{Csch}[x]^2}}, x, 2, 0 \right\}$$

$$\text{ArcTan}\left[\frac{\text{Coth}[x]}{\sqrt{-2 + \text{Coth}[x]^2}}\right]$$

$$\frac{\sqrt{-3 + \text{Cosh}[2x]} \text{Csch}[x] \text{Log}\left[\sqrt{2} \text{Cosh}[x] + \sqrt{-3 + \text{Cosh}[2x]}\right]}{\sqrt{2} \sqrt{-1 + \text{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + b \text{Csch}[x]^2}}, x, 2, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a} \text{Coth}[x]}{\sqrt{a + b \text{Csch}[x]^2}}\right]}{\sqrt{a}}$$

$$\frac{\sqrt{-a + 2 b + a \text{Cosh}[2x]} \text{Csch}[x] \text{Log}\left[\sqrt{2} \sqrt{a} \text{Cosh}[x] + \sqrt{-a + 2 b + a \text{Cosh}[2x]}\right]}{\sqrt{2} \sqrt{a} \sqrt{a + b \text{Csch}[x]^2}}$$

Incorrect antiderivative:

$$\left\{ \text{Csch}\left[a + \frac{\text{Log}[c x^n]}{n(-2+p)}\right]^p, x, 1, 0\right\}$$

$$-\frac{(2-p)x \text{Csch}\left[a - \frac{\text{Log}[c x^n]}{n(2-p)}\right]^{-2+p}}{1-p} - \frac{(2-p)x \text{Cosh}\left[a - \frac{\text{Log}[c x^n]}{n(2-p)}\right] \text{Csch}\left[a - \frac{\text{Log}[c x^n]}{n(2-p)}\right]^{-1+p}}{1-p}$$

$$\frac{2^{-1+p} e^{-\frac{4a}{-2+p}} (-2+p)x \left(e^{\frac{4a}{-2+p}} - e^{\frac{2ap}{-2+p}} (c x^n)^{\frac{2}{n(-2+p)}} \right) \left(\frac{e^{\frac{a(2+p)}{-2+p}} (c x^n)^{\frac{1}{n(-2+p)}}}{-\frac{4a}{-2+p} + \frac{2ap}{-2+p} (c x^n)^{\frac{2}{n(-2+p)}}} \right)^p}{-1+p}$$

Incorrect antiderivative:

$$\left\{ \text{Csch}\left[a - \frac{\text{Log}[c x^n]}{n(-2+p)}\right]^p, x, 1, 0\right\}$$

$$-\frac{(2-p)x \text{Csch}\left[a + \frac{\text{Log}[c x^n]}{n(2-p)}\right]^{-2+p}}{1-p} + \frac{(2-p)x \text{Cosh}\left[a + \frac{\text{Log}[c x^n]}{n(2-p)}\right] \text{Csch}\left[a + \frac{\text{Log}[c x^n]}{n(2-p)}\right]^{-1+p}}{1-p}$$

$$\frac{2^{-1+p} e^{-\frac{2ap}{-2+p}} (-2+p)x \left(e^{\frac{2ap}{-2+p}} - e^{\frac{4a}{-2+p}} (c x^n)^{\frac{2}{n(-2+p)}} \right) \left(-\frac{e^{\frac{a(2+p)}{-2+p}} (c x^n)^{\frac{1}{n(-2+p)}}}{-\frac{2ap}{-2+p} - \frac{4a}{-2+p} (c x^n)^{\frac{2}{n(-2+p)}}} \right)^p}{-1+p}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Csch}[a + b \text{Log}[c x^n]]}{x}, x, 2, 0\right\}$$

$$-\frac{\text{ArcCoth}[\text{Cosh}[a + b \text{Log}[c x^n]]]}{bn}$$

$$\frac{-\text{Log}\left[2 \text{Cosh}\left[\frac{1}{2} (a + b \text{Log}[c x^n])\right]\right] + \text{Log}\left[2 \text{Sinh}\left[\frac{1}{2} (a + b \text{Log}[c x^n])\right]\right]}{bn}$$

Problems involving two hyperbolic functions

Valid but unnecessarily complicated antiderivative:

$$\{\text{Csch}[a + b x] \text{Sech}[a + b x], x, 1, 0\}$$

$$\frac{\text{Log}[\text{Tanh}[a + b x]]}{b} - \frac{\text{Log}[2 \text{Cosh}[a + b x]] + \text{Log}[2 \text{Sinh}[a + b x]]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{\text{Sinh}[a + b x]}}{\sqrt{\text{Cosh}[a + b x]}}, x, 4, 0 \right\}$$

$$-\frac{\text{ArcTan}\left[\frac{\sqrt{\text{Sinh}[a + b x]}}{\sqrt{\text{Cosh}[a + b x]}}\right]}{b} + \frac{\text{ArcTanh}\left[\frac{\sqrt{\text{Sinh}[a + b x]}}{\sqrt{\text{Cosh}[a + b x]}}\right]}{b} - \frac{2 \sqrt{\text{Cosh}[a + b x]} \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{4}, \frac{5}{4}, \text{Cosh}[a + b x]^2\right] \text{Sinh}[a + b x]^{3/2}}{b \left(-\text{Sinh}[a + b x]^2\right)^{3/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{\text{Cosh}[a + b x]}}{\sqrt{\text{Sinh}[a + b x]}}, x, 4, 0 \right\}$$

$$-\frac{\text{ArcTan}\left[\frac{\sqrt{\text{Cosh}[a + b x]}}{\sqrt{\text{Sinh}[a + b x]}}\right]}{b} + \frac{\text{ArcTanh}\left[\frac{\sqrt{\text{Cosh}[a + b x]}}{\sqrt{\text{Sinh}[a + b x]}}\right]}{b} - \frac{2 \text{Cosh}[a + b x]^{3/2} \text{Hypergeometric2F1}\left[\frac{3}{4}, \frac{3}{4}, \frac{7}{4}, \text{Cosh}[a + b x]^2\right] \sqrt{\text{Sinh}[a + b x]}}{3 b \left(-\text{Sinh}[a + b x]^2\right)^{1/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Sinh}[a + b x]^{1/3}}{\text{Cosh}[a + b x]^{1/3}}, x, 6, 0 \right\}$$

$$-\frac{\sqrt{3} \text{ArcTan}\left[\frac{1 + \frac{2 \text{Sinh}[a + b x]^{2/3}}{\text{Cosh}[a + b x]^{2/3}}}{\sqrt{3}}\right]}{2 b} - \frac{\text{Log}\left[1 - \frac{\text{Sinh}[a + b x]^{2/3}}{\text{Cosh}[a + b x]^{2/3}}\right]}{2 b} + \frac{\text{Log}\left[1 + \frac{\text{Sinh}[a + b x]^{2/3}}{\text{Cosh}[a + b x]^{2/3}} + \frac{\text{Sinh}[a + b x]^{4/3}}{\text{Cosh}[a + b x]^{4/3}}\right]}{4 b} - \frac{3 \text{Cosh}[a + b x]^{2/3} \text{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{3}, \frac{4}{3}, \text{Cosh}[a + b x]^2\right] \text{Sinh}[a + b x]^{4/3}}{2 b \left(-\text{Sinh}[a + b x]^2\right)^{2/3}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Cosh}[a + b x]^{1/3}}{\text{Sinh}[a + b x]^{1/3}}, x, 6, 0 \right\}$$

$$\begin{aligned}
& -\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{1+\frac{2 \operatorname{Cosh}[a+b x]^{2/3}}{\operatorname{Sinh}[a+b x]^{2/3}}}{\sqrt{3}}\right]}{2 b}-\frac{\operatorname{Log}\left[1-\frac{\operatorname{Cosh}[a+b x]^{2/3}}{\operatorname{Sinh}[a+b x]^{2/3}}\right]}{2 b}+\frac{\operatorname{Log}\left[1+\frac{\operatorname{Cosh}[a+b x]^{4/3}}{\operatorname{Sinh}[a+b x]^{4/3}}+\frac{\operatorname{Cosh}[a+b x]^{2/3}}{\operatorname{Sinh}[a+b x]^{2/3}}\right]}{4 b} \\
& -\frac{3 \operatorname{Cosh}[a+b x]^{4/3} \operatorname{Hypergeometric2F1}\left[\frac{2}{3}, \frac{2}{3}, \frac{5}{3}, \operatorname{Cosh}[a+b x]^2\right] \operatorname{Sinh}[a+b x]^{2/3}}{4 b\left(-\operatorname{Sinh}[a+b x]^2\right)^{1/3}}
\end{aligned}$$

Unable to integrate:

$$\{\operatorname{Sech}[a+b x]^4 \operatorname{Tanh}[a+b x]^n, x, 3, 0\}$$

$$\frac{\operatorname{Tanh}[a+b x]^{1+n}}{b(1+n)}-\frac{\operatorname{Tanh}[a+b x]^{3+n}}{b(3+n)}$$

$$\int \operatorname{Sech}[a+b x]^4 \operatorname{Tanh}[a+b x]^n dx$$

Unable to integrate:

$$\{\operatorname{Coth}[x]^n \operatorname{Csch}[x]^4, x, 3, 0\}$$

$$\frac{\operatorname{Coth}[x]^{1+n}}{1+n}-\frac{\operatorname{Coth}[x]^{3+n}}{3+n}$$

$$\int \operatorname{Coth}[x]^n \operatorname{Csch}[x]^4 dx$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Coth}[x]^4 \operatorname{Csch}[x]^3, x, 4, 0\}$$

$$\frac{1}{16} \operatorname{ArcCoth}[\operatorname{Cosh}[x]]+\frac{1}{16} \operatorname{Coth}[x] \operatorname{Csch}[x]+\frac{1}{24} \operatorname{Coth}[x]^3 \operatorname{Csch}[x]-\frac{1}{6} \operatorname{Coth}[x]^5 \operatorname{Csch}[x]$$

$$\frac{1}{384}\left(-6 \operatorname{Csch}\left[\frac{x}{2}\right]^2-6 \operatorname{Csch}\left[\frac{x}{2}\right]^4-\operatorname{Csch}\left[\frac{x}{2}\right]^6+24 \operatorname{Log}[\operatorname{Cosh}\left[\frac{x}{2}\right]]-24 \operatorname{Log}[\operatorname{Sinh}\left[\frac{x}{2}\right]]-6 \operatorname{Sech}\left[\frac{x}{2}\right]^2+6 \operatorname{Sech}\left[\frac{x}{2}\right]^4-\operatorname{Sech}\left[\frac{x}{2}\right]^6\right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Cosh}[a+b x]^{3/2} \operatorname{Sinh}[a+b x], x, 3, 0\}$$

$$\frac{2 x \operatorname{Cosh}[a+b x]^{5/2}}{5 b}+\frac{12 i \operatorname{EllipticE}\left[\frac{1}{2} i(a+b x), 2\right]}{25 b^2}-\frac{4 \operatorname{Cosh}[a+b x]^{3/2} \operatorname{Sinh}[a+b x]}{25 b^2}$$

$$\begin{aligned}
& \frac{1}{25 b^2 \sqrt{\operatorname{Cosh}[a+b x]}}\left(\operatorname{Cosh}[a+b x]\right. \\
& \quad \left.(5 b x-12 \operatorname{Coth}[a]-2 \operatorname{Cosh}[2 b x] \operatorname{Sinh}[2 a]+\operatorname{Cosh}[2 a](5 b x \operatorname{Cosh}[2 b x]-2 \operatorname{Sinh}[2 b x])+5 b x \operatorname{Sinh}[2 a] \operatorname{Sinh}[2 b x])+\right. \\
& \quad \left.\frac{1}{\sqrt{1+\operatorname{Cosh}[2(a+b x)]+\operatorname{Sinh}[2(a+b x)]}} \operatorname{Csch}\left[\frac{a}{2}\right] \operatorname{Sech}\left[\frac{a}{2}\right]\right. \\
& \quad \left.\left(6 \operatorname{Cosh}[a+b x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-\operatorname{Cosh}[2(a+b x)]-\operatorname{Sinh}[2(a+b x)]\right](\operatorname{Cosh}[a]+\operatorname{Sinh}[a])+\right.\right. \\
& \quad \left.\left.\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-\operatorname{Cosh}[2(a+b x)]-\operatorname{Sinh}[2(a+b x)]\right]\right.\right. \\
& \quad \left.\left.\left(\operatorname{Cosh}[b x]+\operatorname{Sinh}[b x]\right)(1+\operatorname{Cosh}[2(a+b x)]+\operatorname{Sinh}[2(a+b x)])\right)\right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \sinh[a + b x]}{\sqrt{\cosh[a + b x]}}, x, 2, 0 \right\}$$

$$\frac{2 x \sqrt{\cosh[a + b x]}}{b} + \frac{4 i \operatorname{EllipticE}\left[\frac{1}{2} i (a + b x), 2\right]}{b^2}$$

$$\frac{1}{3 b^2 \sqrt{\cosh[a + b x]}}$$

$$\left(6 \cosh[a + b x] \operatorname{Csch}[a] (-2 \cosh[a] + b x \sinh[a]) + \frac{1}{\sqrt{1 + \cosh[2 (a + b x)] + \sinh[2 (a + b x)]}} \operatorname{Csch}\left[\frac{a}{2}\right] \operatorname{Sech}\left[\frac{a}{2}\right] \right.$$

$$\left(6 \cosh[a + b x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -\cosh[2 (a + b x)] - \sinh[2 (a + b x)]\right] (\cosh[a] + \sinh[a]) + \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -\cosh[2 (a + b x)] - \sinh[2 (a + b x)]\right] \right.$$

$$\left. \left. (\cosh[b x] + \sinh[b x]) (1 + \cosh[2 (a + b x)] + \sinh[2 (a + b x)]) \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \sinh[a + b x]}{\cosh[a + b x]^{5/2}}, x, 3, 0 \right\}$$

$$-\frac{2 x}{3 b \cosh[a + b x]^{3/2}} + \frac{4 i \operatorname{EllipticE}\left[\frac{1}{2} i (a + b x), 2\right]}{3 b^2} + \frac{4 \sinh[a + b x]}{3 b^2 \sqrt{\cosh[a + b x]}}$$

$$\frac{1}{9 b^2 \cosh[a + b x]^{3/2}}$$

$$\left(-6 \operatorname{Csch}[a] (\cosh[a] + \cosh[a + 2 b x] + b x \sinh[a]) + \frac{1}{\sqrt{1 + \cosh[2 (a + b x)] + \sinh[2 (a + b x)]}} \cosh[a + b x] \operatorname{Csch}\left[\frac{a}{2}\right] \right.$$

$$\operatorname{Sech}\left[\frac{a}{2}\right] \left(6 \cosh[a + b x] \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -\cosh[2 (a + b x)] - \sinh[2 (a + b x)]\right] (\cosh[a] + \sinh[a]) + \right.$$

$$\left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -\cosh[2 (a + b x)] - \sinh[2 (a + b x)]\right] \right.$$

$$\left. \left. (\cosh[b x] + \sinh[b x]) (1 + \cosh[2 (a + b x)] + \sinh[2 (a + b x)]) \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \cosh[a + b x] \sinh[a + b x]^{3/2}, x, 4, 0\}$$

$$\frac{12 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right] \sqrt{\sinh[a + b x]}}{25 b^2 \sqrt{i \sinh[a + b x]}} - \frac{4 \cosh[a + b x] \sinh[a + b x]^{3/2}}{25 b^2} + \frac{2 x \sinh[a + b x]^{5/2}}{5 b}$$

$$\frac{1}{100 b^2 \sqrt{\sinh[a + b x]}} \operatorname{Sech}[a] \left(24 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \cosh[2(a + b x)] + \sinh[2(a + b x)]\right] (\cosh[b x] - \sinh[b x]) \right. \\ \left. \sqrt{1 - \cosh[2 a + 2 b x] - \sinh[2 a + 2 b x]} + 8 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, \cosh[2(a + b x)] + \sinh[2(a + b x)]\right] \right. \\ \left. (\cosh[b x] + \sinh[b x]) \sqrt{1 - \cosh[2 a + 2 b x] - \sinh[2 a + 2 b x]} + 2 \sinh[a + b x] \right. \\ \left. (-10 b x \cosh[a] + 5 b x \cosh[a + 2 b x] + 5 b x \cosh[3 a + 2 b x] + 24 \sinh[a] - 2 \sinh[a + 2 b x] - 2 \sinh[3 a + 2 b x]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \cosh[a + b x]}{\sqrt{\sinh[a + b x]}}, x, 3, 0 \right\} \\ \frac{2 x \sqrt{\sinh[a + b x]}}{b} - \frac{4 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right] \sqrt{\sinh[a + b x]}}{b^2 \sqrt{i \sinh[a + b x]}} \\ \frac{1}{3 b^2 \sqrt{\sinh[a + b x]}} 2 \left(3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \cosh[2(a + b x)] + \sinh[2(a + b x)]\right] \operatorname{Sech}[a] (-\cosh[b x] + \sinh[b x]) \right. \\ \left. \sqrt{1 - \cosh[2 a + 2 b x] - \sinh[2 a + 2 b x]} - \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, \cosh[2(a + b x)] + \sinh[2(a + b x)]\right] \right. \\ \left. \operatorname{Sech}[a] (\cosh[b x] + \sinh[b x]) \sqrt{1 - \cosh[2 a + 2 b x] - \sinh[2 a + 2 b x]} + 3 \sinh[a + b x] (b x - 2 \tanh[a]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \cosh[a + b x]}{\sinh[a + b x]^{5/2}}, x, 4, 0 \right\} \\ - \frac{2 x}{3 b \sinh[a + b x]^{3/2}} - \frac{4 \cosh[a + b x]}{3 b^2 \sqrt{\sinh[a + b x]}} + \frac{4 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right] \sqrt{\sinh[a + b x]}}{3 b^2 \sqrt{i \sinh[a + b x]}} \\ - \frac{1}{9 b^2 \sqrt{\sinh[a + b x]}} 2 \operatorname{Sech}[a] \left(3 \operatorname{Csch}[a + b x] (b x \cosh[a] + \sinh[a] + \sinh[a + 2 b x]) + \right. \\ \left. 3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \cosh[2(a + b x)] + \sinh[2(a + b x)]\right] (-\cosh[b x] + \sinh[b x]) \right. \\ \left. \sqrt{1 - \cosh[2 a + 2 b x] - \sinh[2 a + 2 b x]} - \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, \cosh[2(a + b x)] + \sinh[2(a + b x)]\right] \right. \\ \left. (\cosh[b x] + \sinh[b x]) \sqrt{1 - \cosh[2 a + 2 b x] - \sinh[2 a + 2 b x]} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Sech}[a + b x]^{9/2} \sinh[a + b x], x, 5, 0\} \\ \frac{12 i \sqrt{\cosh[a + b x]} \operatorname{EllipticE}\left[\frac{1}{2} i (a + b x), 2\right] \sqrt{\operatorname{Sech}[a + b x]}}{35 b^2} - \\ \frac{2 x \operatorname{Sech}[a + b x]^{7/2}}{7 b} + \frac{12 \sqrt{\operatorname{Sech}[a + b x]} \sinh[a + b x]}{35 b^2} + \frac{4 \operatorname{Sech}[a + b x]^{5/2} \sinh[a + b x]}{35 b^2}$$

$$\frac{1}{70 b^2} \left(\frac{24 \sqrt{2} e^{-a-bx} \sqrt{\frac{e^{a+bx}}{1+e^{2(a+bx)}}} \left(1 + e^{2(a+bx)} + (-1 + e^{2a}) \sqrt{1 + e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2(a+bx)}\right] \right)}{-1 + e^{2a}} - \right. \\ \left. \operatorname{Csch}[a] \operatorname{Sech}[a+bx]^{7/2} (9 \operatorname{Cosh}[a] + 11 \operatorname{Cosh}[a+2bx] + \operatorname{Cosh}[3a+2bx] + 3 \operatorname{Cosh}[3a+4bx] + 20 bx \operatorname{Sinh}[a]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Sech}[a+bx]^{5/2} \operatorname{Sinh}[a+bx], x, 4, 0\} \\ \frac{4 i \sqrt{\operatorname{Cosh}[a+bx]} \operatorname{EllipticE}\left[\frac{1}{2} i (a+bx), 2\right] \sqrt{\operatorname{Sech}[a+bx]}}{3 b^2} - \frac{2 x \operatorname{Sech}[a+bx]^{3/2}}{3 b} + \frac{4 \sqrt{\operatorname{Sech}[a+bx]} \operatorname{Sinh}[a+bx]}{3 b^2} \\ \frac{1}{3 b^2} \left(\frac{2 \sqrt{2} e^{-a-bx} \sqrt{\frac{e^{a+bx}}{1+e^{2(a+bx)}}} \left(1 + e^{2(a+bx)} + (-1 + e^{2a}) \sqrt{1 + e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2(a+bx)}\right] \right)}{-1 + e^{2a}} - \right. \\ \left. \operatorname{Csch}[a] \operatorname{Sech}[a+bx]^{3/2} (\operatorname{Cosh}[a] + \operatorname{Cosh}[a+2bx] + bx \operatorname{Sinh}[a]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \sqrt{\operatorname{Sech}[a+bx]} \operatorname{Sinh}[a+bx], x, 3, 0\} \\ \frac{2 x}{b \sqrt{\operatorname{Sech}[a+bx]}} + \frac{4 i \sqrt{\operatorname{Cosh}[a+bx]} \operatorname{EllipticE}\left[\frac{1}{2} i (a+bx), 2\right] \sqrt{\operatorname{Sech}[a+bx]}}{b^2} \\ \frac{e^{-a-bx} \left((1 + e^{2(a+bx)}) (-2 + bx) + 4 \sqrt{1 + e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2(a+bx)}\right] \right) \sqrt{\operatorname{Sech}[a+bx]}}{b^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \operatorname{Sinh}[a+bx]}{\operatorname{Sech}[a+bx]^{3/2}}, x, 4, 0 \right\} \\ \frac{2 x}{5 b \operatorname{Sech}[a+bx]^{5/2}} + \frac{12 i \sqrt{\operatorname{Cosh}[a+bx]} \operatorname{EllipticE}\left[\frac{1}{2} i (a+bx), 2\right] \sqrt{\operatorname{Sech}[a+bx]}}{25 b^2} - \frac{4 \operatorname{Sinh}[a+bx]}{25 b^2 \operatorname{Sech}[a+bx]^{3/2}} \\ \frac{1}{100 b^2} e^{-3(a+bx)} \left((1 + e^{2(a+bx)}) (2 + 5 bx + 2 e^{2(a+bx)} (-12 + 5 bx) + e^{4(a+bx)} (-2 + 5 bx)) + \right. \\ \left. 48 e^{2(a+bx)} \sqrt{1 + e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2(a+bx)}\right] \right) \sqrt{\operatorname{Sech}[a+bx]}$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Cosh}[a+bx] \operatorname{Csch}[a+bx]^{9/2}, x, 6, 0\}$$

$$\frac{12 \cosh[a + b x] \sqrt{\operatorname{Csch}[a + b x]}}{35 b^2} - \frac{4 \cosh[a + b x] \operatorname{Csch}[a + b x]^{5/2}}{35 b^2} - \frac{2 x \operatorname{Csch}[a + b x]^{7/2}}{7 b} - \frac{12 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right]}{35 b^2 \sqrt{\operatorname{Csch}[a + b x]} \sqrt{i \sinh[a + b x]}}$$

$$\frac{1}{70 b^2} \left(- \frac{24 \sqrt{2} e^{-a-bx} \sqrt{\frac{e^{a+bx}}{-1+e^{2(a+bx)}}} \left(-1 + e^{2(a+bx)} + (1 + e^{2a}) \sqrt{1 - e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2(a+bx)}\right] \right)}{1 + e^{2a}} + \right.$$

$$\left. \operatorname{Csch}[a + b x]^{7/2} \operatorname{Sech}[a] (-20 b x \cosh[a] - 9 \sinh[a] - 11 \sinh[a + 2 b x] + \sinh[3 a + 2 b x] + 3 \sinh[3 a + 4 b x]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \cosh[a + b x] \operatorname{Csch}[a + b x]^{5/2}, x, 5, 0\}$$

$$- \frac{4 \cosh[a + b x] \sqrt{\operatorname{Csch}[a + b x]}}{3 b^2} - \frac{2 x \operatorname{Csch}[a + b x]^{3/2}}{3 b} + \frac{4 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right]}{3 b^2 \sqrt{\operatorname{Csch}[a + b x]} \sqrt{i \sinh[a + b x]}}$$

$$\frac{1}{3 b^2} \left(2 \sqrt{2} e^{-a-bx} \sqrt{\frac{e^{a+bx}}{-1+e^{2(a+bx)}}} \left(-1 + e^{2(a+bx)} + (1 + e^{2a}) \sqrt{1 - e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2(a+bx)}\right] \right) \right.$$

$$\left. \operatorname{Csch}[a + b x]^{3/2} \operatorname{Sech}[a] (b x \cosh[a] + \sinh[a] + \sinh[a + 2 b x]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x \cosh[a + b x] \sqrt{\operatorname{Csch}[a + b x]}, x, 4, 0\}$$

$$\frac{2 x}{b \sqrt{\operatorname{Csch}[a + b x]}} - \frac{4 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right]}{b^2 \sqrt{\operatorname{Csch}[a + b x]} \sqrt{i \sinh[a + b x]}}$$

$$\frac{e^{-a-bx} \sqrt{\operatorname{Csch}[a + b x]} \left((-1 + e^{2(a+bx)}) (-2 + b x) - 4 \sqrt{1 - e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2(a+bx)}\right] \right)}{b^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \cosh[a + b x]}{\operatorname{Csch}[a + b x]^{3/2}}, x, 5, 0 \right\}$$

$$\frac{2 x}{5 b \operatorname{Csch}[a + b x]^{5/2}} - \frac{4 \cosh[a + b x]}{25 b^2 \operatorname{Csch}[a + b x]^{3/2}} + \frac{12 i \operatorname{EllipticE}\left[\frac{\pi}{4} - \frac{1}{2} i (a + b x), 2\right]}{25 b^2 \sqrt{\operatorname{Csch}[a + b x]} \sqrt{i \sinh[a + b x]}}$$

$$\frac{1}{100 b^2} e^{-3(a+bx)} \sqrt{\operatorname{Csch}[a + b x]} \left((-1 + e^{2(a+bx)}) (2 + 5 b x + e^{2(a+bx)} (24 - 10 b x) + e^{4(a+bx)} (-2 + 5 b x)) + \right.$$

$$\left. 48 e^{2(a+bx)} \sqrt{1 - e^{2(a+bx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, e^{2(a+bx)}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x^3 \operatorname{Sech}[a + b x]^2 \operatorname{Tanh}[a + b x], x, 6, 0\}$$

$$\frac{3 x^2}{2 b^2} - \frac{3 x \operatorname{Log}\left[1 + e^{2 a + 2 b x}\right]}{b^3} - \frac{3 \operatorname{PolyLog}\left[2, -e^{2 a + 2 b x}\right]}{2 b^4} - \frac{x^3 \operatorname{Sech}[a + b x]^2}{2 b} + \frac{3 x^2 \operatorname{Tanh}[a + b x]}{2 b^2}$$

$$- \frac{1}{2 b^4} e^{-\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \left(3 i b e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \pi x - 3 i e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \pi \operatorname{Log}\left[1 + e^{2 b x}\right] + \right.$$

$$6 b e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} x \operatorname{Log}\left[1 - e^{-2 (b x + \operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right] + 3 i e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \pi \operatorname{Log}[\operatorname{Cosh}[b x]] +$$

$$6 e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \operatorname{ArcTanh}[\operatorname{Coth}[a]] (b x + \operatorname{Log}\left[1 - e^{-2 (b x + \operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right] - \operatorname{Log}[i \operatorname{Sinh}[b x + \operatorname{ArcTanh}[\operatorname{Coth}[a]]]]) -$$

$$3 e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} \operatorname{PolyLog}\left[2, e^{-2 (b x + \operatorname{ArcTanh}[\operatorname{Coth}[a]])}\right] + b^3 e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} x^3 \operatorname{Sech}[a + b x]^2 -$$

$$\left. 3 b^2 e^{\operatorname{ArcTanh}[\operatorname{Coth}[a]]} x^2 \operatorname{Sech}[a] \operatorname{Sech}[a + b x] \operatorname{Sinh}[b x] - 3 b^2 x^2 \sqrt{-\operatorname{Csch}[a]^2} \operatorname{Tanh}[a] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x^2 \operatorname{Coth}[a + b x] \operatorname{Csch}[a + b x], x, 5, 0\}$$

$$- \frac{4 x \operatorname{ArcTanh}\left[e^{a + b x}\right]}{b^2} - \frac{x^2 \operatorname{Csch}[a + b x]}{b} - \frac{2 \operatorname{PolyLog}\left[2, -e^{a + b x}\right]}{b^3} + \frac{2 \operatorname{PolyLog}\left[2, e^{a + b x}\right]}{b^3}$$

$$- \frac{1}{b^3} \left(b^2 x^2 \operatorname{Csch}[a + b x] - 2 a \operatorname{Log}\left[1 - e^{-a - b x}\right] - 2 b x \operatorname{Log}\left[1 - e^{-a - b x}\right] + 2 a \operatorname{Log}\left[1 + e^{-a - b x}\right] + \right.$$

$$\left. 2 b x \operatorname{Log}\left[1 + e^{-a - b x}\right] + 2 a \operatorname{Log}\left[\operatorname{Tanh}\left[\frac{1}{2} (a + b x)\right]\right] - 2 \operatorname{PolyLog}\left[2, -e^{-a - b x}\right] + 2 \operatorname{PolyLog}\left[2, e^{-a - b x}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x^3 \operatorname{Coth}[a + b x] \operatorname{Csch}[a + b x]^2, x, 6, 0\}$$

$$- \frac{3 x^2}{2 b^2} - \frac{3 x^2 \operatorname{Coth}[a + b x]}{2 b^2} - \frac{x^3 \operatorname{Csch}[a + b x]^2}{2 b} + \frac{3 x \operatorname{Log}\left[1 - e^{2 a + 2 b x}\right]}{b^3} + \frac{3 \operatorname{PolyLog}\left[2, e^{2 a + 2 b x}\right]}{2 b^4}$$

$$- \frac{x^3 \operatorname{Csch}[a + b x]^2}{2 b} + \frac{3 x^2 \operatorname{Csch}[a] \operatorname{Csch}[a + b x] \operatorname{Sinh}[b x]}{2 b^2} + \frac{1}{2 b^4 \sqrt{\operatorname{Sech}[a]^2 (\operatorname{Cosh}[a]^2 - \operatorname{Sinh}[a]^2)}}$$

$$3 \operatorname{Csch}[a] \operatorname{Sech}[a] \left(-b^2 e^{-\operatorname{ArcTanh}[\operatorname{Tanh}[a]]} x^2 + \frac{1}{\sqrt{1 - \operatorname{Tanh}[a]^2}} i (-b x (-\pi + 2 i \operatorname{ArcTanh}[\operatorname{Tanh}[a]]) - \right.$$

$$\pi \operatorname{Log}\left[1 + e^{2 b x}\right] - 2 (i b x + i \operatorname{ArcTanh}[\operatorname{Tanh}[a]]) \operatorname{Log}\left[1 - e^{2 i (i b x + i \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] + \pi \operatorname{Log}[\operatorname{Cosh}[b x]] +$$

$$\left. 2 i \operatorname{ArcTanh}[\operatorname{Tanh}[a]] \operatorname{Log}[i \operatorname{Sinh}[b x + \operatorname{ArcTanh}[\operatorname{Tanh}[a]]]] + i \operatorname{PolyLog}\left[2, e^{2 i (i b x + i \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}\right] \right) \operatorname{Tanh}[a]$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Csch}[a + b x] \operatorname{Sech}[a + b x], x, 1, 0\}$$

$$\frac{\operatorname{Log}[\operatorname{Tanh}[a + b x]]}{b}$$

$$\frac{-\operatorname{Log}[2 \operatorname{Cosh}[a + b x]] + \operatorname{Log}[2 \operatorname{Sinh}[a + b x]]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Csch}[a + b x] \operatorname{Sech}[a + b x]^2, x, 9, 0\}$$

$$\begin{aligned}
& -\frac{\text{ArcTan}[\text{Sinh}[a + b x]]}{b^2} - \frac{2 x \text{ArcTanh}[e^{a+bx}]}{b} - \frac{\text{PolyLog}[2, -e^{a+bx}]}{b^2} + \frac{\text{PolyLog}[2, e^{a+bx}]}{b^2} + \frac{x \text{Sech}[a + b x]}{b} \\
& \frac{1}{b^2} \left(-2 \text{ArcTan}[\text{Tanh}\left[\frac{1}{2}(a + b x)\right]] + a \text{Log}[1 - e^{-a-bx}] + b x \text{Log}[1 - e^{-a-bx}] - a \text{Log}[1 + e^{-a-bx}] - \right. \\
& \quad \left. b x \text{Log}[1 + e^{-a-bx}] - a \text{Log}[\text{Tanh}\left[\frac{1}{2}(a + b x)\right]] + \text{PolyLog}[2, -e^{-a-bx}] - \text{PolyLog}[2, e^{-a-bx}] + b x \text{Sech}[a + b x] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{x^2 \text{Csch}[a + b x] \text{Sech}[a + b x]^3, x, 14, 0\} \\
& -\frac{2 x^2 \text{ArcTanh}[e^{2a+2bx}]}{b} + \frac{\text{Log}[\text{Cosh}[a + b x]]}{b^3} - \frac{x \text{PolyLog}[2, -e^{2a+2bx}]}{b^2} + \\
& \frac{x \text{PolyLog}[2, e^{2a+2bx}]}{b^2} + \frac{\text{PolyLog}[3, -e^{2a+2bx}]}{2 b^3} - \frac{\text{PolyLog}[3, e^{2a+2bx}]}{2 b^3} + \frac{x^2 \text{Sech}[a + b x]^2}{2 b} - \frac{x \text{Tanh}[a + b x]}{b^2} \\
& \frac{1}{6} \left(4 x^3 \text{Csch}[2 a] + \frac{1}{b^3 (1 + e^{2a})} \left(-12 b e^{2a} x + 4 b^3 e^{2a} x^3 + 6 \text{Log}[1 + e^{2(a+bx)}] + 6 e^{2a} \text{Log}[1 + e^{2(a+bx)}] - 6 b^2 x^2 \text{Log}[1 + e^{2(a+bx)}] - \right. \right. \\
& \quad \left. 6 b^2 e^{2a} x^2 \text{Log}[1 + e^{2(a+bx)}] - 6 b (1 + e^{2a}) x \text{PolyLog}[2, -e^{2(a+bx)}] + 3 (1 + e^{2a}) \text{PolyLog}[3, -e^{2(a+bx)}] \right) + \\
& \quad \left. -2 b^2 x^2 (2 b e^{2a} x - 3 (-1 + e^{2a}) \text{Log}[1 - e^{2(a+bx)}]) + 6 b (-1 + e^{2a}) x \text{PolyLog}[2, e^{2(a+bx)}] - 3 (-1 + e^{2a}) \text{PolyLog}[3, e^{2(a+bx)}] \right) \\
& \quad \left. \frac{3 x^2 \text{Sech}[a + b x]^2}{b} - \frac{6 x \text{Sech}[a] \text{Sech}[a + b x] \text{Sinh}[b x]}{b^2} \right) + \\
& \quad \frac{b^3 (-1 + e^{2a})}{b^3 (-1 + e^{2a})}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{x \text{Csch}[a + b x] \text{Sech}[a + b x]^3, x, 9, 0\} \\
& -\frac{2 x \text{ArcTanh}[e^{2a+2bx}]}{b} - \frac{\text{PolyLog}[2, -e^{2a+2bx}]}{2 b^2} + \frac{\text{PolyLog}[2, e^{2a+2bx}]}{2 b^2} + \frac{x \text{Sech}[a + b x]^2}{2 b} - \frac{\text{Tanh}[a + b x]}{2 b^2} \\
& x^2 \text{Csch}[2 a] + \frac{x \text{Sech}[a + b x]^2}{2 b} + \frac{1}{2 b^2 \sqrt{\text{Csch}[a]^2 (-\text{Cosh}[a]^2 + \text{Sinh}[a]^2)}} \\
& \text{Csch}[a] \left(-b^2 e^{-\text{ArcTanh}[\text{Coth}[a]]} x^2 + \frac{1}{\sqrt{1 - \text{Coth}[a]^2}} i \text{Coth}[a] (-b x (-\pi + 2 i \text{ArcTanh}[\text{Coth}[a]])) - \right. \\
& \quad \pi \text{Log}[1 + e^{2bx}] - 2 (i b x + i \text{ArcTanh}[\text{Coth}[a]]) \text{Log}[1 - e^{2 i (i b x + i \text{ArcTanh}[\text{Coth}[a]])}] + \pi \text{Log}[\text{Cosh}[b x]] + \\
& \quad \left. 2 i \text{ArcTanh}[\text{Coth}[a]] \text{Log}[i \text{Sinh}[b x + \text{ArcTanh}[\text{Coth}[a]]]] + i \text{PolyLog}[2, e^{2 i (i b x + i \text{ArcTanh}[\text{Coth}[a]])}] \right) \text{Sech}[a] - \\
& \frac{\text{Sech}[a] \text{Sech}[a + b x] \text{Sinh}[b x]}{2 b^2} + \frac{1}{2 b^2 \sqrt{\text{Sech}[a]^2 (\text{Cosh}[a]^2 - \text{Sinh}[a]^2)}} \text{Csch}[a] \text{Sech}[a] \\
& \left(-b^2 e^{-\text{ArcTanh}[\text{Tanh}[a]]} x^2 + \frac{1}{\sqrt{1 - \text{Tanh}[a]^2}} i (-b x (-\pi + 2 i \text{ArcTanh}[\text{Tanh}[a]])) - \pi \text{Log}[1 + e^{2bx}] - \right. \\
& \quad 2 (i b x + i \text{ArcTanh}[\text{Tanh}[a]]) \text{Log}[1 - e^{2 i (i b x + i \text{ArcTanh}[\text{Tanh}[a]])}] + \pi \text{Log}[\text{Cosh}[b x]] + \\
& \quad \left. 2 i \text{ArcTanh}[\text{Tanh}[a]] \text{Log}[i \text{Sinh}[b x + \text{ArcTanh}[\text{Tanh}[a]]]] + i \text{PolyLog}[2, e^{2 i (i b x + i \text{ArcTanh}[\text{Tanh}[a]])}] \right) \text{Tanh}[a]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Csch}[a + b x]^2 \operatorname{Sech}[a + b x], x, 9, 0\}$$

$$-\frac{\operatorname{ArcCoth}[\operatorname{Cosh}[a + b x]]}{b^2} - \frac{2 x \operatorname{ArcTan}[e^{a+bx}]}{b} - \frac{x \operatorname{Csch}[a + b x]}{b} + \frac{i \operatorname{PolyLog}[2, -i e^{a+bx}]}{b^2} - \frac{i \operatorname{PolyLog}[2, i e^{a+bx}]}{b^2}$$

$$\frac{1}{2 b^2} \left(-2 b x \operatorname{Csch}[a] - 2 i a \operatorname{Log}[1 - i e^{a+bx}] + \pi \operatorname{Log}[1 - i e^{a+bx}] - 2 i b x \operatorname{Log}[1 - i e^{a+bx}] + 2 i a \operatorname{Log}[1 + i e^{a+bx}] - \right.$$

$$\pi \operatorname{Log}[1 + i e^{a+bx}] + 2 i b x \operatorname{Log}[1 + i e^{a+bx}] - 2 \operatorname{Log}\left[2 \operatorname{Cosh}\left[\frac{1}{2}(a + b x)\right]\right] + 2 i a \operatorname{Log}\left[\operatorname{Cot}\left[\frac{1}{4}(2 i a + \pi + 2 i b x)\right]\right] -$$

$$\pi \operatorname{Log}\left[\operatorname{Cot}\left[\frac{1}{4}(2 i a + \pi + 2 i b x)\right]\right] + 2 \operatorname{Log}\left[2 \operatorname{Sinh}\left[\frac{1}{2}(a + b x)\right]\right] + 2 i \operatorname{PolyLog}[2, -i e^{a+bx}] -$$

$$2 i \operatorname{PolyLog}[2, i e^{a+bx}] + b x \operatorname{Csch}\left[\frac{a}{2}\right] \operatorname{Csch}\left[\frac{1}{2}(a + b x)\right] \operatorname{Sinh}\left[\frac{b x}{2}\right] + b x \operatorname{Sech}\left[\frac{a}{2}\right] \operatorname{Sech}\left[\frac{1}{2}(a + b x)\right] \operatorname{Sinh}\left[\frac{b x}{2}\right] \Big)$$

Valid but unnecessarily complicated antiderivative:

$$\{x^2 \operatorname{Csch}[a + b x]^2 \operatorname{Sech}[a + b x]^3, x, 24, 0\}$$

$$-\frac{3 x^2 \operatorname{ArcTan}[e^{a+bx}]}{b} + \frac{\operatorname{ArcTan}[\operatorname{Sinh}[a + b x]]}{b^3} - \frac{4 x \operatorname{ArcTanh}[e^{a+bx}]}{b^2} -$$

$$\frac{2 \operatorname{PolyLog}[2, -e^{a+bx}]}{b^3} + \frac{3 i x \operatorname{PolyLog}[2, -i e^{a+bx}]}{b^2} - \frac{3 i x \operatorname{PolyLog}[2, i e^{a+bx}]}{b^2} + \frac{2 \operatorname{PolyLog}[2, e^{a+bx}]}{b^3} -$$

$$\frac{3 i \operatorname{PolyLog}[3, -i e^{a+bx}]}{b^3} + \frac{3 i \operatorname{PolyLog}[3, i e^{a+bx}]}{b^3} - \frac{x \operatorname{Sech}[a + b x]}{b^2} - \frac{x^2 \operatorname{Csch}[a + b x] (3 - \operatorname{Sech}[a + b x]^2)}{2 b}$$

$$-\frac{x^2 \operatorname{Csch}[a]}{b} + \frac{1}{b^3} 2 \left(-a \operatorname{Log}\left[\operatorname{Tanh}\left[\frac{1}{2}(a + b x)\right]\right] - \right.$$

$$i \left((i a + i b x) (\operatorname{Log}[1 - e^{i(i a + i b x)}] - \operatorname{Log}[1 + e^{i(i a + i b x)}]) + i (\operatorname{PolyLog}[2, -e^{i(i a + i b x)}] - \operatorname{PolyLog}[2, e^{i(i a + i b x)}]) \right) \Big) -$$

$$\frac{1}{2 b^3} i \left(4 i \operatorname{ArcTan}[e^{a+bx}] + 3 b^2 x^2 \operatorname{Log}[1 - i e^{a+bx}] - 3 b^2 x^2 \operatorname{Log}[1 + i e^{a+bx}] - 6 b x \operatorname{PolyLog}[2, -i e^{a+bx}] + \right.$$

$$6 b x \operatorname{PolyLog}[2, i e^{a+bx}] + 6 \operatorname{PolyLog}[3, -i e^{a+bx}] - 6 \operatorname{PolyLog}[3, i e^{a+bx}] \Big) -$$

$$\frac{x \operatorname{Sech}[a] \operatorname{Sech}[a + b x] (2 \operatorname{Cosh}[a] + b x \operatorname{Sinh}[a])}{2 b^2} + \frac{x^2 \operatorname{Csch}\left[\frac{a}{2}\right] \operatorname{Csch}\left[\frac{a}{2} + \frac{b x}{2}\right] \operatorname{Sinh}\left[\frac{b x}{2}\right]}{2 b} +$$

$$\frac{x^2 \operatorname{Sech}\left[\frac{a}{2}\right] \operatorname{Sech}\left[\frac{a}{2} + \frac{b x}{2}\right] \operatorname{Sinh}\left[\frac{b x}{2}\right]}{2 b} - \frac{x^2 \operatorname{Sech}[a] \operatorname{Sech}[a + b x]^2 \operatorname{Sinh}[b x]}{2 b}$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Csch}[a + b x]^2 \operatorname{Sech}[a + b x]^3, x, 11, 0\}$$

$$-\frac{\operatorname{ArcCoth}[\operatorname{Cosh}[a + b x]]}{b^2} - \frac{3 x \operatorname{ArcTan}[e^{a+bx}]}{b} + \frac{3 i \operatorname{PolyLog}[2, -i e^{a+bx}]}{2 b^2} -$$

$$\frac{3 i \operatorname{PolyLog}[2, i e^{a+bx}]}{2 b^2} - \frac{\operatorname{Sech}[a + b x]}{2 b^2} - \frac{x \operatorname{Csch}[a + b x] (3 - \operatorname{Sech}[a + b x]^2)}{2 b}$$

$$\begin{aligned}
& -\frac{x \operatorname{Csch}[a]}{b} - \frac{\operatorname{Log}\left[2 \operatorname{Cosh}\left[\frac{a}{2} + \frac{bx}{2}\right]\right]}{b^2} + \frac{\operatorname{Log}\left[2 \operatorname{Sinh}\left[\frac{a}{2} + \frac{bx}{2}\right]\right]}{b^2} + \\
& \frac{1}{2b^2} 3 \left(\left(-i a + \frac{\pi}{2} - i b x \right) \left(\operatorname{Log}\left[1 - e^{i \left(-i a + \frac{\pi}{2} - i b x \right)}\right] - \operatorname{Log}\left[1 + e^{i \left(-i a + \frac{\pi}{2} - i b x \right)}\right] \right) - \right. \\
& \quad \left. \left(-i a + \frac{\pi}{2} \right) \operatorname{Log}\left[\operatorname{Tan}\left[\frac{1}{2} \left(-i a + \frac{\pi}{2} - i b x \right)\right]\right] + i \left(\operatorname{PolyLog}\left[2, -e^{i \left(-i a + \frac{\pi}{2} - i b x \right)}\right] - \operatorname{PolyLog}\left[2, e^{i \left(-i a + \frac{\pi}{2} - i b x \right)}\right] \right) \right) + \\
& \frac{\operatorname{Sech}[a] \operatorname{Sech}[a + b x] \left(-\operatorname{Cosh}[a] - b x \operatorname{Sinh}[a] \right)}{2 b^2} + \frac{x \operatorname{Csch}\left[\frac{a}{2}\right] \operatorname{Csch}\left[\frac{a}{2} + \frac{bx}{2}\right] \operatorname{Sinh}\left[\frac{bx}{2}\right]}{2 b} + \\
& \frac{x \operatorname{Sech}\left[\frac{a}{2}\right] \operatorname{Sech}\left[\frac{a}{2} + \frac{bx}{2}\right] \operatorname{Sinh}\left[\frac{bx}{2}\right]}{2 b} - \frac{x \operatorname{Sech}[a] \operatorname{Sech}[a + b x]^2 \operatorname{Sinh}[b x]}{2 b}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{x^2 \operatorname{Csch}[a + b x]^3 \operatorname{Sech}[a + b x], x, 14, 0\} \\
& \frac{2 x^2 \operatorname{ArcTanh}\left[e^{2 a + 2 b x}\right]}{b} - \frac{x \operatorname{Coth}[a + b x]}{b^2} - \frac{x^2 \operatorname{Csch}[a + b x]^2}{2 b} + \frac{\operatorname{Log}[\operatorname{Sinh}[a + b x]]}{b^3} + \\
& \frac{x \operatorname{PolyLog}\left[2, -e^{2 a + 2 b x}\right]}{b^2} - \frac{x \operatorname{PolyLog}\left[2, e^{2 a + 2 b x}\right]}{b^2} - \frac{\operatorname{PolyLog}\left[3, -e^{2 a + 2 b x}\right]}{2 b^3} + \frac{\operatorname{PolyLog}\left[3, e^{2 a + 2 b x}\right]}{2 b^3} \\
& \frac{1}{6} \left(-4 x^3 \operatorname{Csch}[2 a] - \frac{3 x^2 \operatorname{Csch}[a + b x]^2}{b} + \right. \\
& \quad \left. \frac{-2 b^2 x^2 \left(2 b e^{2 a} x - 3 \left(1 + e^{2 a} \right) \operatorname{Log}\left[1 + e^{2 (a + b x)}\right] \right) + 6 b \left(1 + e^{2 a} \right) x \operatorname{PolyLog}\left[2, -e^{2 (a + b x)}\right] - 3 \left(1 + e^{2 a} \right) \operatorname{PolyLog}\left[3, -e^{2 (a + b x)}\right]}{b^3 \left(1 + e^{2 a} \right)} + \right. \\
& \quad \left. \frac{1}{b^3 \left(-1 + e^{2 a} \right)} \right. \\
& \quad \left. \left(-12 b e^{2 a} x + 4 b^3 e^{2 a} x^3 - 6 \operatorname{Log}\left[1 - e^{2 (a + b x)}\right] + 6 e^{2 a} \operatorname{Log}\left[1 - e^{2 (a + b x)}\right] + 6 b^2 x^2 \operatorname{Log}\left[1 - e^{2 (a + b x)}\right] - 6 b^2 e^{2 a} x^2 \operatorname{Log}\left[1 - e^{2 (a + b x)}\right] - \right. \right. \\
& \quad \left. \left. 6 b \left(-1 + e^{2 a} \right) x \operatorname{PolyLog}\left[2, e^{2 (a + b x)}\right] + 3 \left(-1 + e^{2 a} \right) \operatorname{PolyLog}\left[3, e^{2 (a + b x)}\right] \right) + \frac{6 x \operatorname{Csch}[a] \operatorname{Csch}[a + b x] \operatorname{Sinh}[b x]}{b^2} \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{x \operatorname{Csch}[a + b x]^3 \operatorname{Sech}[a + b x], x, 9, 0\} \\
& \frac{2 x \operatorname{ArcTanh}\left[e^{2 a + 2 b x}\right]}{b} - \frac{\operatorname{Coth}[a + b x]}{2 b^2} - \frac{x \operatorname{Csch}[a + b x]^2}{2 b} + \frac{\operatorname{PolyLog}\left[2, -e^{2 a + 2 b x}\right]}{2 b^2} - \frac{\operatorname{PolyLog}\left[2, e^{2 a + 2 b x}\right]}{2 b^2}
\end{aligned}$$

$$\begin{aligned}
& -x^2 \operatorname{Csch}[2a] - \frac{x \operatorname{Csch}[a+bx]^2}{2b} - \frac{1}{2b^2 \sqrt{\operatorname{Csch}[a]^2 (-\operatorname{Cosh}[a]^2 + \operatorname{Sinh}[a]^2)}} \\
& \operatorname{Csch}[a] \left(-b^2 e^{-\operatorname{ArcTanh}[\operatorname{Coth}[a]]} x^2 + \frac{1}{\sqrt{1 - \operatorname{Coth}[a]^2}} i \operatorname{Coth}[a] (-bx (-\pi + 2i \operatorname{ArcTanh}[\operatorname{Coth}[a]])) - \right. \\
& \quad \pi \operatorname{Log}[1 + e^{2bx}] - 2(i bx + i \operatorname{ArcTanh}[\operatorname{Coth}[a]]) \operatorname{Log}[1 - e^{2i(i bx + i \operatorname{ArcTanh}[\operatorname{Coth}[a]])}] + \pi \operatorname{Log}[\operatorname{Cosh}[bx]] + \\
& \quad \left. 2i \operatorname{ArcTanh}[\operatorname{Coth}[a]] \operatorname{Log}[i \operatorname{Sinh}[bx + \operatorname{ArcTanh}[\operatorname{Coth}[a]]]] + i \operatorname{PolyLog}[2, e^{2i(i bx + i \operatorname{ArcTanh}[\operatorname{Coth}[a]])}] \right) \operatorname{Sech}[a] + \\
& \frac{\operatorname{Csch}[a] \operatorname{Csch}[a+bx] \operatorname{Sinh}[bx]}{2b^2} - \frac{1}{2b^2 \sqrt{\operatorname{Sech}[a]^2 (\operatorname{Cosh}[a]^2 - \operatorname{Sinh}[a]^2)}} \operatorname{Csch}[a] \operatorname{Sech}[a] \\
& \left(-b^2 e^{-\operatorname{ArcTanh}[\operatorname{Tanh}[a]]} x^2 + \frac{1}{\sqrt{1 - \operatorname{Tanh}[a]^2}} i (-bx (-\pi + 2i \operatorname{ArcTanh}[\operatorname{Tanh}[a]])) - \pi \operatorname{Log}[1 + e^{2bx}] - \right. \\
& \quad 2(i bx + i \operatorname{ArcTanh}[\operatorname{Tanh}[a]]) \operatorname{Log}[1 - e^{2i(i bx + i \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}] + \pi \operatorname{Log}[\operatorname{Cosh}[bx]] + \\
& \quad \left. 2i \operatorname{ArcTanh}[\operatorname{Tanh}[a]] \operatorname{Log}[i \operatorname{Sinh}[bx + \operatorname{ArcTanh}[\operatorname{Tanh}[a]]]] + i \operatorname{PolyLog}[2, e^{2i(i bx + i \operatorname{ArcTanh}[\operatorname{Tanh}[a]])}] \right) \operatorname{Tanh}[a]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{x^2 \operatorname{Csch}[a+bx]^3 \operatorname{Sech}[a+bx]^2, x, 24, 0\} \\
& -\frac{\operatorname{ArcCoth}[\operatorname{Cosh}[a+bx]]}{b^3} + \frac{4x \operatorname{ArcTan}[e^{a+bx}]}{b^2} + \frac{3x^2 \operatorname{ArcTanh}[e^{a+bx}]}{b} - \frac{x \operatorname{Csch}[a+bx]}{b^2} + \\
& \frac{3x \operatorname{PolyLog}[2, -e^{a+bx}]}{b^2} - \frac{2i \operatorname{PolyLog}[2, -i e^{a+bx}]}{b^3} + \frac{2i \operatorname{PolyLog}[2, i e^{a+bx}]}{b^3} - \frac{3x \operatorname{PolyLog}[2, e^{a+bx}]}{b^2} - \\
& \frac{3 \operatorname{PolyLog}[3, -e^{a+bx}]}{b^3} + \frac{3 \operatorname{PolyLog}[3, e^{a+bx}]}{b^3} - \frac{x^2 (3 + \operatorname{Csch}[a+bx]^2) \operatorname{Sech}[a+bx]}{2b} \\
& -\frac{x \operatorname{Csch}[a]}{b^2} - \frac{x^2 \operatorname{Csch}\left[\frac{a}{2} + \frac{bx}{2}\right]^2}{8b} - \\
& \frac{1}{b^3} 2 \left(\left(-i a + \frac{\pi}{2} - i bx \right) \left(\operatorname{Log}[1 - e^{i(-i a + \frac{\pi}{2} - i bx)}] - \operatorname{Log}[1 + e^{i(-i a + \frac{\pi}{2} - i bx)}] \right) - \left(-i a + \frac{\pi}{2} \right) \operatorname{Log}\left[\operatorname{Tan}\left[\frac{1}{2} \left(-i a + \frac{\pi}{2} - i bx \right)\right]\right] + \right. \\
& \quad \left. i \left(\operatorname{PolyLog}[2, -e^{i(-i a + \frac{\pi}{2} - i bx)}] - \operatorname{PolyLog}[2, e^{i(-i a + \frac{\pi}{2} - i bx)}] \right) \right) - \frac{1}{2b^3} \\
& (4 \operatorname{ArcTanh}[e^{a+bx}] + 3b^2 x^2 \operatorname{Log}[1 - e^{a+bx}] - 3b^2 x^2 \operatorname{Log}[1 + e^{a+bx}] - 6bx \operatorname{PolyLog}[2, -e^{a+bx}] + \\
& \quad 6bx \operatorname{PolyLog}[2, e^{a+bx}] + 6 \operatorname{PolyLog}[3, -e^{a+bx}] - 6 \operatorname{PolyLog}[3, e^{a+bx}]) - \frac{x^2 \operatorname{Sech}\left[\frac{a}{2} + \frac{bx}{2}\right]^2}{8b} - \\
& \frac{x^2 \operatorname{Sech}[a+bx]}{b} + \frac{x \operatorname{Csch}\left[\frac{a}{2}\right] \operatorname{Csch}\left[\frac{a}{2} + \frac{bx}{2}\right] \operatorname{Sinh}\left[\frac{bx}{2}\right]}{2b^2} + \frac{x \operatorname{Sech}\left[\frac{a}{2}\right] \operatorname{Sech}\left[\frac{a}{2} + \frac{bx}{2}\right] \operatorname{Sinh}\left[\frac{bx}{2}\right]}{2b^2}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{x \operatorname{Csch}[a+bx]^3 \operatorname{Sech}[a+bx]^2, x, 11, 0\}$$

$$\frac{\text{ArcTan}[\text{Sinh}[a + b x]]}{b^2} + \frac{3 x \text{ArcTanh}[e^{a+bx}]}{b} - \frac{\text{Csch}[a + b x]}{2 b^2} +$$

$$\frac{3 \text{PolyLog}[2, -e^{a+bx}]}{2 b^2} - \frac{3 \text{PolyLog}[2, e^{a+bx}]}{2 b^2} - \frac{x (3 + \text{Csch}[a + b x]^2) \text{Sech}[a + b x]}{2 b}$$

$$\frac{1}{8 b^2} \left(16 \text{ArcTan}[\text{Tanh}[\frac{1}{2} (a + b x)]] - b x \text{Csch}[\frac{1}{2} (a + b x)]^2 - 12 a \text{Log}[1 - e^{-a-bx}] - 12 b x \text{Log}[1 - e^{-a-bx}] + 12 a \text{Log}[1 + e^{-a-bx}] + \right.$$

$$12 b x \text{Log}[1 + e^{-a-bx}] + 12 a \text{Log}[\text{Tanh}[\frac{1}{2} (a + b x)]] - 12 \text{PolyLog}[2, -e^{-a-bx}] + 12 \text{PolyLog}[2, e^{-a-bx}] - b x \text{Sech}[\frac{1}{2} (a + b x)]^2 -$$

$$8 b x \text{Sech}[a + b x] + 2 \text{Csch}[\frac{a}{2}] \text{Csch}[\frac{1}{2} (a + b x)] \text{Sinh}[\frac{b x}{2}] + 2 \text{Sech}[\frac{a}{2}] \text{Sech}[\frac{1}{2} (a + b x)] \text{Sinh}[\frac{b x}{2}] \Bigg)$$

Valid but unnecessarily complicated antiderivative:

{Sinh[x] Tanh[2 x], x, 5, 0}

$$-\frac{\text{ArcTan}[\sqrt{2} \text{Sinh}[x]]}{\sqrt{2}} + \text{Sinh}[x]$$

$$\frac{1}{8} \left(-\sqrt{2} \left(2 \text{ArcTan}\left[\frac{\text{Cosh}[\frac{x}{2}] + \text{Sinh}[\frac{x}{2}]}{(1 + \sqrt{2}) \text{Cosh}[\frac{x}{2}] - (-1 + \sqrt{2}) \text{Sinh}[\frac{x}{2}]}\right] + 2 \text{ArcTan}\left[\frac{\text{Cosh}[\frac{x}{2}] + \text{Sinh}[\frac{x}{2}]}{(-1 + \sqrt{2}) \text{Cosh}[\frac{x}{2}] - (1 + \sqrt{2}) \text{Sinh}[\frac{x}{2}]}\right] + \right.$$

$$2 \text{ArcTan}[\sqrt{2} \text{Sinh}[x]] - i \text{Log}[2 (\sqrt{2} + 2 \text{Cosh}[x])] - i \text{Log}[-2 \sqrt{2} + 4 \text{Cosh}[x]] + i \text{Log}[2 \text{Cosh}[2 x]] \Bigg) + 8 \text{Sinh}[x] \Bigg)$$

Valid but unnecessarily complicated antiderivative:

{Sinh[x] Tanh[4 x], x, 6, 0}

$$-\frac{1}{4} \sqrt{2 - \sqrt{2}} \text{ArcTan}\left[\frac{2 \text{Sinh}[x]}{\sqrt{2 - \sqrt{2}}}\right] - \frac{1}{4} \sqrt{2 + \sqrt{2}} \text{ArcTan}\left[\frac{2 \text{Sinh}[x]}{\sqrt{2 + \sqrt{2}}}\right] + \text{Sinh}[x]$$

$$-\frac{1}{16} \text{RootSum}[1 + \#1^8 \&,$$

$$\frac{x + 2 \text{Log}[-\text{Cosh}[\frac{x}{2}] - \text{Sinh}[\frac{x}{2}] + \text{Cosh}[\frac{x}{2}] \#1 - \text{Sinh}[\frac{x}{2}] \#1] + x \#1^6 + 2 \text{Log}[-\text{Cosh}[\frac{x}{2}] - \text{Sinh}[\frac{x}{2}] + \text{Cosh}[\frac{x}{2}] \#1 - \text{Sinh}[\frac{x}{2}] \#1] \#1^6}{\#1^7} \&$$

$$] +$$

$$\text{Sinh}[$$

$$x]$$

Valid but unnecessarily complicated antiderivative:

{Sinh[x] Tanh[5 x], x, 7, 0}

$$-\frac{1}{5} \text{ArcTan}[\text{Sinh}[x]] + \frac{1}{10} (1 + \sqrt{5}) \text{ArcTan}[(1 - \sqrt{5}) \text{Sinh}[x]] + \frac{1}{10} (1 - \sqrt{5}) \text{ArcTan}[(1 + \sqrt{5}) \text{Sinh}[x]] + \text{Sinh}[x]$$

$$\begin{aligned}
& -\frac{2}{5} \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]\right] - \\
& \frac{1}{20} \operatorname{RootSum}\left[1 - \#1^2 + \#1^4 - \#1^6 + \#1^8 \&, \frac{1}{-\#1 + 2 \#1^3 - 3 \#1^5 + 4 \#1^7} \left(3 x + 6 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] - \right. \right. \\
& \quad x \#1^2 - 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^2 - x \#1^4 - \\
& \quad 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^4 + 3 x \#1^6 + \\
& \quad \left. 6 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^6\right) \&] + \operatorname{Sinh}[x]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Sinh}[x] \operatorname{Tanh}[6 x], x, 7, 0\}$$

$$\begin{aligned}
& -\frac{\operatorname{ArcTan}\left[\sqrt{2} \operatorname{Sinh}[x]\right]}{3 \sqrt{2}} + \frac{1}{12} \left(\sqrt{2} + \sqrt{6}\right) \operatorname{ArcTan}\left[\left(\sqrt{2} - \sqrt{6}\right) \operatorname{Sinh}[x]\right] + \\
& \frac{1}{12} \left(\sqrt{2} - \sqrt{6}\right) \operatorname{ArcTan}\left[\left(\sqrt{2} + \sqrt{6}\right) \operatorname{Sinh}[x]\right] + \operatorname{Sinh}[x] \\
& \frac{1}{24} \left(-\sqrt{2} \left(2 \operatorname{ArcTan}\left[\frac{\operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]}{\left(1 + \sqrt{2}\right) \operatorname{Cosh}\left[\frac{x}{2}\right] - \left(-1 + \sqrt{2}\right) \operatorname{Sinh}\left[\frac{x}{2}\right]}\right] + 2 \operatorname{ArcTan}\left[\frac{\operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]}{\left(-1 + \sqrt{2}\right) \operatorname{Cosh}\left[\frac{x}{2}\right] - \left(1 + \sqrt{2}\right) \operatorname{Sinh}\left[\frac{x}{2}\right]}\right] + \right. \right. \\
& \quad \left. 2 \operatorname{ArcTan}\left[\sqrt{2} \operatorname{Sinh}[x]\right] - \mathfrak{i} \operatorname{Log}\left[2 \left(\sqrt{2} + 2 \operatorname{Cosh}[x]\right)\right] - \mathfrak{i} \operatorname{Log}\left[-2 \sqrt{2} + 4 \operatorname{Cosh}[x]\right] + \mathfrak{i} \operatorname{Log}\left[2 \operatorname{Cosh}[2 x]\right]\right) - \\
& \operatorname{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{1}{-\#1^3 + 2 \#1^7} \left(2 x + 4 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] - x \#1^2 - \right. \right. \\
& \quad 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^2 - x \#1^4 - 2 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \right. \\
& \quad \left. \left. \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^4 + 2 x \#1^6 + 4 \operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right] - \operatorname{Sinh}\left[\frac{x}{2}\right] + \operatorname{Cosh}\left[\frac{x}{2}\right] \#1 - \operatorname{Sinh}\left[\frac{x}{2}\right] \#1\right] \#1^6\right) \&] + 24 \operatorname{Sinh}[x] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Coth}[4 x] \operatorname{Sinh}[x], x, 5, 0\}$$

$$\begin{aligned}
& -\frac{1}{4} \operatorname{ArcTan}[\operatorname{Sinh}[x]] - \frac{\operatorname{ArcTan}\left[\sqrt{2} \operatorname{Sinh}[x]\right]}{2 \sqrt{2}} + \operatorname{Sinh}[x] \\
& \frac{1}{16} \left(-2 \sqrt{2} \operatorname{ArcTan}\left[\frac{\operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]}{\left(1 + \sqrt{2}\right) \operatorname{Cosh}\left[\frac{x}{2}\right] - \left(-1 + \sqrt{2}\right) \operatorname{Sinh}\left[\frac{x}{2}\right]}\right] - \right. \\
& \quad 2 \sqrt{2} \operatorname{ArcTan}\left[\frac{\operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]}{\left(-1 + \sqrt{2}\right) \operatorname{Cosh}\left[\frac{x}{2}\right] - \left(1 + \sqrt{2}\right) \operatorname{Sinh}\left[\frac{x}{2}\right]}\right] - 2 \sqrt{2} \operatorname{ArcTan}\left[\sqrt{2} \operatorname{Sinh}[x]\right] - 8 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]\right] + \\
& \quad \left. \mathfrak{i} \sqrt{2} \operatorname{Log}\left[2 \left(\sqrt{2} + 2 \operatorname{Cosh}[x]\right)\right] + \mathfrak{i} \sqrt{2} \operatorname{Log}\left[-2 \sqrt{2} + 4 \operatorname{Cosh}[x]\right] - \mathfrak{i} \sqrt{2} \operatorname{Log}\left[2 \operatorname{Cosh}[2 x]\right] + 16 \operatorname{Sinh}[x]\right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Coth}[5 x] \operatorname{Sinh}[x], x, 6, 0\}$$

$$\begin{aligned}
 & -\frac{1}{10} \sqrt{10-2\sqrt{5}} \operatorname{ArcTan}\left[\frac{4\sinh[x]}{\sqrt{10-2\sqrt{5}}}\right] - \frac{1}{10} \sqrt{10+2\sqrt{5}} \operatorname{ArcTan}\left[\frac{4\sinh[x]}{\sqrt{10+2\sqrt{5}}}\right] + \sinh[x] \\
 & \frac{1}{20\sqrt{5}} \left(\sqrt{2} \left(-(-5+\sqrt{5}) \sqrt{5+\sqrt{5}} \operatorname{ArcTan}\left[\frac{(-3+\sqrt{5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{10-2\sqrt{5}}}\right] + (-5+\sqrt{5}) \sqrt{5+\sqrt{5}} \operatorname{ArcTan}\left[\frac{(5+\sqrt{5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{10-2\sqrt{5}}}\right] + \right. \right. \\
 & \left. \left. \sqrt{5-\sqrt{5}} (5+\sqrt{5}) \left(\operatorname{ArcTan}\left[\frac{(-5+\sqrt{5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{2(5+\sqrt{5})}}\right] - \operatorname{ArcTan}\left[\frac{(3+\sqrt{5}) \tanh\left[\frac{x}{2}\right]}{\sqrt{2(5+\sqrt{5})}}\right] \right) \right) + 20\sqrt{5} \sinh[x] \right)
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \{\operatorname{Sech}[2x] \sinh[x], x, 2, 0\} \\
 & -\frac{\operatorname{ArcTanh}[\sqrt{2} \cosh[x]]}{\sqrt{2}} \\
 & \frac{1}{4\sqrt{2}} \left(-2i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2}) \cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2}) \sinh\left[\frac{x}{2}\right]}\right] + 2i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2}) \cosh\left[\frac{x}{2}\right] - (1+\sqrt{2}) \sinh\left[\frac{x}{2}\right]}\right] - \right. \\
 & \left. 4 \operatorname{ArcTanh}\left[\sqrt{2} - i \tanh\left[\frac{x}{2}\right]\right] - \operatorname{Log}\left[2\left(\sqrt{2} + 2 \cosh[x]\right)\right] + \operatorname{Log}\left[-2\sqrt{2} + 4 \cosh[x]\right] \right)
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \{\operatorname{Sech}[4x] \sinh[x], x, 4, 0\} \\
 & \frac{1}{4} \sqrt{2+\sqrt{2}} \operatorname{ArcTanh}\left[\frac{2 \cosh[x]}{\sqrt{2-\sqrt{2}}}\right] - \frac{1}{4} \sqrt{2-\sqrt{2}} \operatorname{ArcTanh}\left[\frac{2 \cosh[x]}{\sqrt{2+\sqrt{2}}}\right] \\
 & \frac{1}{16} \operatorname{RootSum}\left[1+\#1^8 \&, \right. \\
 & \left. \frac{-x-2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right]-\sinh\left[\frac{x}{2}\right]+\cosh\left[\frac{x}{2}\right] \#1-\sinh\left[\frac{x}{2}\right] \#1\right]+x \#1^2+2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right]-\sinh\left[\frac{x}{2}\right]+\cosh\left[\frac{x}{2}\right] \#1-\sinh\left[\frac{x}{2}\right] \#1\right] \#1^2}{\#1^5} \& \right. \\
 & \left. \right]
 \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
 & \{\operatorname{Sech}[6x] \sinh[x], x, 7, 0\} \\
 & \frac{\operatorname{ArcTanh}[\sqrt{2} \cosh[x]]}{3\sqrt{2}} - \frac{1}{12} \left(\sqrt{2}-\sqrt{6} \right) \operatorname{ArcTanh}\left[\left(\sqrt{2}-\sqrt{6}\right) \cosh[x]\right] - \frac{1}{12} \left(\sqrt{2}+\sqrt{6} \right) \operatorname{ArcTanh}\left[\left(\sqrt{2}+\sqrt{6}\right) \cosh[x]\right]
 \end{aligned}$$

$$\frac{1}{24\sqrt{2}} \left(4i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] - 4i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + \right. \\ \left. 8 \operatorname{ArcTanh}\left[\sqrt{2} - i \operatorname{Tanh}\left[\frac{x}{2}\right]\right] + 2 \operatorname{Log}\left[2\left(\sqrt{2} + 2 \cosh[x]\right)\right] - 2 \operatorname{Log}\left[-2\sqrt{2} + 4 \cosh[x]\right] + \right. \\ \left. \sqrt{2} \operatorname{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{1}{-\#1^3 + 2\#1^7} \left(-x - 2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right) + x\#1^2 + \right. \right. \right. \\ \left. \left. 2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right]\#1^2 - x\#1^4 - 2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \right. \right. \right. \\ \left. \left. \left. \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right]\#1^4 + x\#1^6 + 2 \operatorname{Log}\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right]\#1^6\right)\&\right] \Bigg)$$

Valid but unnecessarily complicated antiderivative:

{Csch[4 x] Sinh[x], x, 4, 0}

$$-\frac{1}{4} \operatorname{ArcTan}[\sinh[x]] + \frac{\operatorname{ArcTan}[\sqrt{2} \sinh[x]]}{2\sqrt{2}} \\ \frac{1}{16} \left(2\sqrt{2} \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + \right. \\ \left. 2\sqrt{2} \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + 2\sqrt{2} \operatorname{ArcTan}[\sqrt{2} \sinh[x]] - 8 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]\right] - \right. \\ \left. i\sqrt{2} \operatorname{Log}\left[2\left(\sqrt{2} + 2 \cosh[x]\right)\right] - i\sqrt{2} \operatorname{Log}\left[-2\sqrt{2} + 4 \cosh[x]\right] + i\sqrt{2} \operatorname{Log}[2 \cosh[2x]] \right)$$

FullSimplify::ztest1:

$$\text{Unable to decide whether numeric quantity } -\frac{16}{5(3+\sqrt{5})^2} - \frac{8}{\sqrt{5}(3+\sqrt{5})^2} + \frac{2\sqrt{\frac{1}{5}(6+2\sqrt{5})}}{(3+\sqrt{5})^2} + \frac{6\sqrt{\frac{1}{5}(30+10\sqrt{5})}}{5(3+\sqrt{5})^2}$$

is equal to zero. Assuming it is. >>

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Tanh[2 x], x, 5, 0}

$$-\frac{\operatorname{ArcTanh}[\sqrt{2} \cosh[x]]}{\sqrt{2}} + \cosh[x] \\ \frac{1}{4\sqrt{2}} \left(-2i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + 2i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] - \right. \\ \left. 4 \operatorname{ArcTanh}\left[\sqrt{2} - i \operatorname{Tanh}\left[\frac{x}{2}\right]\right] + 4\sqrt{2} \cosh[x] - \operatorname{Log}\left[2\left(\sqrt{2} + 2 \cosh[x]\right)\right] + \operatorname{Log}\left[-2\sqrt{2} + 4 \cosh[x]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Tanh[3 x], x, 4, 0}

$$-\frac{\operatorname{ArcTanh}\left[\frac{2\operatorname{Cosh}[x]}{\sqrt{3}}\right]}{\sqrt{3}} + \operatorname{Cosh}[x]$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{2-i\operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{3}}\right]}{\sqrt{3}} - \frac{\operatorname{ArcTanh}\left[\frac{2+i\operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{3}}\right]}{\sqrt{3}} + \operatorname{Cosh}[x]$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Tanh[4 x], x, 6, 0}

$$-\frac{1}{4}\sqrt{2-\sqrt{2}}\operatorname{ArcTanh}\left[\frac{2\operatorname{Cosh}[x]}{\sqrt{2-\sqrt{2}}}\right] - \frac{1}{4}\sqrt{2+\sqrt{2}}\operatorname{ArcTanh}\left[\frac{2\operatorname{Cosh}[x]}{\sqrt{2+\sqrt{2}}}\right] + \operatorname{Cosh}[x]$$

$$\operatorname{Cosh}[x] + \frac{1}{16}\operatorname{RootSum}\left[1+\#1^8\&, \frac{-x-2\operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right]\#1-\operatorname{Sinh}\left[\frac{x}{2}\right]\#1\right]+x\#1^6+2\operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right]\#1-\operatorname{Sinh}\left[\frac{x}{2}\right]\#1\right]\#1^6}{\#1^7}\&\right]$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Tanh[5 x], x, 6, 0}

$$-\frac{1}{10}\sqrt{10-2\sqrt{5}}\operatorname{ArcTanh}\left[\frac{4\operatorname{Cosh}[x]}{\sqrt{10-2\sqrt{5}}}\right] - \frac{1}{10}\sqrt{10+2\sqrt{5}}\operatorname{ArcTanh}\left[\frac{4\operatorname{Cosh}[x]}{\sqrt{10+2\sqrt{5}}}\right] + \operatorname{Cosh}[x]$$

$$\operatorname{Cosh}[x] + \frac{1}{4}\operatorname{RootSum}\left[1-\#1^2+\#1^4-\#1^6+\#1^8\&, \frac{1}{-\#1+2\#1^3-3\#1^5+4\#1^7}\left(-x-2\operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right]\#1-\operatorname{Sinh}\left[\frac{x}{2}\right]\#1\right]+x\#1^2+2\operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right]\#1-\operatorname{Sinh}\left[\frac{x}{2}\right]\#1\right]\#1^2-x\#1^4-2\operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right]\#1-\operatorname{Sinh}\left[\frac{x}{2}\right]\#1\right]\#1^4+x\#1^6+2\operatorname{Log}\left[-\operatorname{Cosh}\left[\frac{x}{2}\right]-\operatorname{Sinh}\left[\frac{x}{2}\right]+\operatorname{Cosh}\left[\frac{x}{2}\right]\#1-\operatorname{Sinh}\left[\frac{x}{2}\right]\#1\right]\#1^6\right)\&\right]$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Tanh[6 x], x, 8, 0}

$$-\frac{\operatorname{ArcTanh}\left[\sqrt{2}\operatorname{Cosh}[x]\right]}{3\sqrt{2}} + \frac{1}{12}\left(\sqrt{2}+\sqrt{6}\right)\operatorname{ArcTanh}\left[\left(\sqrt{2}-\sqrt{6}\right)\operatorname{Cosh}[x]\right] + \frac{1}{12}\left(\sqrt{2}-\sqrt{6}\right)\operatorname{ArcTanh}\left[\left(\sqrt{2}+\sqrt{6}\right)\operatorname{Cosh}[x]\right] + \operatorname{Cosh}[x]$$

$$\frac{1}{24\sqrt{2}} \left(-4i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + 4i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] - \right. \\ \left. 8 \operatorname{ArcTanh}\left[\sqrt{2} - i \tanh\left[\frac{x}{2}\right]\right] + 24\sqrt{2} \cosh[x] - 2 \log\left[2\left(\sqrt{2} + 2\cosh[x]\right)\right] + 2 \log\left[-2\sqrt{2} + 4\cosh[x]\right] + \right. \\ \left. \sqrt{2} \operatorname{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{1}{-\#1^3 + 2\#1^7} \left(-2x - 4 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right] - \right. \right. \right. \\ \left. \left. x\#1^2 - 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right]\#1^2 + x\#1^4 + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \right. \right. \right. \\ \left. \left. \left. \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right]\#1^4 + 2x\#1^6 + 4 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right]\#1 - \sinh\left[\frac{x}{2}\right]\#1\right]\#1^6\right) \&\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\cosh[x] \coth[2x], x, 4, 0\}$$

$$-\frac{1}{2} \operatorname{ArcTanh}[\cosh[x]] + \cosh[x]$$

$$\frac{1}{2} \left(2 \cosh[x] - \log\left[\cosh\left[\frac{x}{2}\right]\right] + \log\left[\sinh\left[\frac{x}{2}\right]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\cosh[x] \coth[4x], x, 5, 0\}$$

$$-\frac{1}{4} \operatorname{ArcTanh}[\cosh[x]] - \frac{\operatorname{ArcTanh}[\sqrt{2} \cosh[x]]}{2\sqrt{2}} + \cosh[x]$$

$$\frac{1}{8\sqrt{2}} \left(-2i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + \right. \\ \left. 2i \operatorname{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] - 4 \operatorname{ArcTanh}\left[\sqrt{2} - i \tanh\left[\frac{x}{2}\right]\right] + 8\sqrt{2} \cosh[x] - \right. \\ \left. 2\sqrt{2} \log\left[\cosh\left[\frac{x}{2}\right]\right] - \log\left[2\left(\sqrt{2} + 2\cosh[x]\right)\right] + \log\left[-2\sqrt{2} + 4\cosh[x]\right] + 2\sqrt{2} \log\left[\sinh\left[\frac{x}{2}\right]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\cosh[x] \coth[6x], x, 6, 0\}$$

$$-\frac{1}{6} \operatorname{ArcTanh}[\cosh[x]] - \frac{1}{6} \operatorname{ArcTanh}[2 \cosh[x]] - \frac{\operatorname{ArcTanh}\left[\frac{2 \cosh[x]}{\sqrt{3}}\right]}{2\sqrt{3}} + \cosh[x]$$

$$\frac{1}{12} \left(-2\sqrt{3} \operatorname{ArcTanh}\left[\frac{2 - i \tanh\left[\frac{x}{2}\right]}{\sqrt{3}}\right] - 2\sqrt{3} \operatorname{ArcTanh}\left[\frac{2 + i \tanh\left[\frac{x}{2}\right]}{\sqrt{3}}\right] + \right. \\ \left. 12 \cosh[x] - 2 \log\left[\cosh\left[\frac{x}{2}\right]\right] + \log[-1 + 2 \cosh[x]] - \log[1 + 2 \cosh[x]] + 2 \log\left[\sinh\left[\frac{x}{2}\right]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\cosh[x] \operatorname{Sech}[2x], x, 2, 0\}$$

$$\frac{\text{ArcTan}\left[\sqrt{2} \sinh[x]\right]}{\sqrt{2}}$$

$$\frac{1}{4\sqrt{2}} \left(2 \text{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + 2 \text{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + \right.$$

$$\left. 2 \text{ArcTan}\left[\sqrt{2} \sinh[x]\right] - i \log\left[2\left(\sqrt{2} + 2 \cosh[x]\right)\right] - i \log\left[-2\sqrt{2} + 4 \cosh[x]\right] + i \log\left[2 \cosh[2x]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Sech[4 x], x, 4, 0}

$$\frac{1}{4} \sqrt{2+\sqrt{2}} \text{ArcTan}\left[\frac{2 \sinh[x]}{\sqrt{2-\sqrt{2}}}\right] - \frac{1}{4} \sqrt{2-\sqrt{2}} \text{ArcTan}\left[\frac{2 \sinh[x]}{\sqrt{2+\sqrt{2}}}\right]$$

$$\frac{1}{16} \text{RootSum}\left[1 + \#1^8 \&, \right.$$

$$\left. \frac{x + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] + x \#1^2 + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^2}{\#1^5} \&\right]$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Sech[6 x], x, 7, 0}

$$-\frac{\text{ArcTan}\left[\sqrt{2} \sinh[x]\right]}{3\sqrt{2}} + \frac{1}{12} \left(\sqrt{2} - \sqrt{6} \right) \text{ArcTan}\left[\left(\sqrt{2} - \sqrt{6}\right) \sinh[x]\right] + \frac{1}{12} \left(\sqrt{2} + \sqrt{6} \right) \text{ArcTan}\left[\left(\sqrt{2} + \sqrt{6}\right) \sinh[x]\right]$$

$$\frac{1}{24} \left(-\sqrt{2} \left(2 \text{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (-1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + 2 \text{ArcTan}\left[\frac{\cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\cosh\left[\frac{x}{2}\right] - (1+\sqrt{2})\sinh\left[\frac{x}{2}\right]}\right] + \right.$$

$$\left. 2 \text{ArcTan}\left[\sqrt{2} \sinh[x]\right] - i \log\left[2\left(\sqrt{2} + 2 \cosh[x]\right)\right] - i \log\left[-2\sqrt{2} + 4 \cosh[x]\right] + i \log\left[2 \cosh[2x]\right] \right) +$$

$$\text{RootSum}\left[1 - \#1^4 + \#1^8 \&, \frac{1}{-\#1^3 + 2 \#1^7} \left(x + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] + x \#1^2 + \right.$$

$$2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^2 + x \#1^4 + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \right.$$

$$\left. \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^4 + x \#1^6 + 2 \log\left[-\cosh\left[\frac{x}{2}\right] - \sinh\left[\frac{x}{2}\right] + \cosh\left[\frac{x}{2}\right] \#1 - \sinh\left[\frac{x}{2}\right] \#1\right] \#1^6 \&\right)$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Csch[2 x], x, 3, 0}

$$-\frac{1}{2} \text{ArcTanh}\left[\cosh[x]\right]$$

$$\frac{1}{2} \left(-\log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Csch[4 x], x, 4, 0}

$$\begin{aligned}
& -\frac{1}{4} \operatorname{ArcTanh}[\operatorname{Cosh}[x]] + \frac{\operatorname{ArcTanh}[\sqrt{2} \operatorname{Cosh}[x]]}{2\sqrt{2}} \\
& \frac{1}{8\sqrt{2}} \left(2i \operatorname{ArcTan}\left[\frac{\operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]}{(1+\sqrt{2})\operatorname{Cosh}\left[\frac{x}{2}\right] - (-1+\sqrt{2})\operatorname{Sinh}\left[\frac{x}{2}\right]}\right] - \right. \\
& \quad \left. 2i \operatorname{ArcTan}\left[\frac{\operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]}{(-1+\sqrt{2})\operatorname{Cosh}\left[\frac{x}{2}\right] - (1+\sqrt{2})\operatorname{Sinh}\left[\frac{x}{2}\right]}\right] + 4 \operatorname{ArcTanh}[\sqrt{2} - i \operatorname{Tanh}\left[\frac{x}{2}\right]] \right) - \\
& \quad \left. 2\sqrt{2} \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] + \operatorname{Log}\left[2\left(\sqrt{2} + 2\operatorname{Cosh}[x]\right)\right] - \operatorname{Log}\left[-2\sqrt{2} + 4\operatorname{Cosh}[x]\right] + 2\sqrt{2} \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{x}{2}\right]\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

{Cosh[x] Csch[6 x], x, 6, 0}

$$\begin{aligned}
& -\frac{1}{6} \operatorname{ArcTanh}[\operatorname{Cosh}[x]] - \frac{1}{6} \operatorname{ArcTanh}[2 \operatorname{Cosh}[x]] + \frac{\operatorname{ArcTanh}\left[\frac{2 \operatorname{Cosh}[x]}{\sqrt{3}}\right]}{2\sqrt{3}} \\
& \frac{1}{12} \left(2\sqrt{3} \operatorname{ArcTanh}\left[\frac{2 - i \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{3}}\right] + 2\sqrt{3} \operatorname{ArcTanh}\left[\frac{2 + i \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{3}}\right] - \right. \\
& \quad \left. 2 \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] + \operatorname{Log}[-1 + 2 \operatorname{Cosh}[x]] - \operatorname{Log}[1 + 2 \operatorname{Cosh}[x]] + 2 \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{x}{2}\right]\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

{\sqrt{\operatorname{Cosh}[x] \operatorname{Coth}[x]}, x, 2, 0}

$$\begin{aligned}
& 2\sqrt{\operatorname{Cosh}[x] \operatorname{Coth}[x]} \operatorname{Tanh}[x] \\
& \frac{2\sqrt{\operatorname{Cosh}[x] \operatorname{Coth}[x]} \left(-1 + (-\operatorname{Sinh}[x]^2)^{1/4}\right) \operatorname{Tanh}[x]}{(-\operatorname{Sinh}[x]^2)^{1/4}}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]^2}{a + b \operatorname{Sinh}[x]}, x, 5, 0 \right\} \\
& \frac{b \operatorname{ArcCoth}[\operatorname{Cosh}[x]]}{a^2} - \frac{2\sqrt{a^2 + b^2} \operatorname{ArcTanh}\left[\frac{b - a \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^2 + b^2}}\right]}{a^2} - \frac{\operatorname{Coth}[x]}{a} \\
& \frac{2(a^2 + b^2) \operatorname{ArcTan}\left[\frac{b - a \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{-a^2 - b^2}}\right] - a\sqrt{-a^2 - b^2} \operatorname{Coth}[x] + b\sqrt{-a^2 - b^2} \left(\operatorname{Log}\left[2 \operatorname{Cosh}\left[\frac{x}{2}\right]\right] - \operatorname{Log}\left[2 \operatorname{Sinh}\left[\frac{x}{2}\right]\right]\right)}{a^2 \sqrt{-a^2 - b^2}}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]^2}{i + \operatorname{Sinh}[x]}, x, 4, 0 \right\} \\
& -\operatorname{ArcCoth}[\operatorname{Cosh}[x]] + i \operatorname{Coth}[x]
\end{aligned}$$

$$\frac{1}{2} i \left(\coth\left[\frac{x}{2}\right] + 2 i \left(\log\left[\cosh\left[\frac{x}{2}\right]\right] - \log\left[\sinh\left[\frac{x}{2}\right]\right] \right) + \tanh\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Csch}[x]^4}{a + b \sinh[x]}, x, 9, 0 \right\}$$

$$-\frac{b \operatorname{ArcCoth}[\cosh[x]]}{2 a^2} + \frac{b^3 \operatorname{ArcCoth}[\cosh[x]]}{a^4} - \frac{2 b^4 \operatorname{ArcTanh}\left[\frac{b-a \tanh\left[\frac{x}{2}\right]}{\sqrt{a^2+b^2}}\right]}{a^4 \sqrt{a^2+b^2}} + \frac{\coth[x]}{a} - \frac{b^2 \coth[x]}{a^3} - \frac{\coth[x]^3}{3 a} + \frac{b \coth[x] \operatorname{Csch}[x]}{2 a^2}$$

$$\frac{1}{24 a^4} \left(\frac{48 b^4 \operatorname{ArcTan}\left[\frac{b-a \tanh\left[\frac{x}{2}\right]}{\sqrt{-a^2-b^2}}\right]}{\sqrt{-a^2-b^2}} + 4 a \left(2 a^2 - 3 b^2 \right) \coth\left[\frac{x}{2}\right] + 3 a^2 b \operatorname{Csch}\left[\frac{x}{2}\right]^2 - \right.$$

$$12 a^2 b \log\left[\cosh\left[\frac{x}{2}\right]\right] + 24 b^3 \log\left[\cosh\left[\frac{x}{2}\right]\right] + 12 a^2 b \log\left[\sinh\left[\frac{x}{2}\right]\right] - 24 b^3 \log\left[\sinh\left[\frac{x}{2}\right]\right] +$$

$$\left. 3 a^2 b \operatorname{Sech}\left[\frac{x}{2}\right]^2 + 8 a^3 \operatorname{Csch}[x]^3 \sinh\left[\frac{x}{2}\right]^4 - \frac{1}{2} a^3 \operatorname{Csch}\left[\frac{x}{2}\right]^4 \sinh[x] + 8 a^3 \tanh\left[\frac{x}{2}\right] - 12 a b^2 \tanh\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]}{i + \sinh[x]}, x, 4, 0 \right\}$$

$$i \operatorname{ArcCoth}[\cosh[x]] - \frac{i \cosh[x]}{1 - i \sinh[x]}$$

$$i \left(\log\left[\cosh\left[\frac{x}{2}\right]\right] - \log\left[\sinh\left[\frac{x}{2}\right]\right] \right) + \frac{2 \sinh\left[\frac{x}{2}\right]}{\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^2}{i + \sinh[x]}, x, 5, 0 \right\}$$

$$-\operatorname{ArcCoth}[\cosh[x]] + i \coth[x] + \frac{\cosh[x]}{1 - i \sinh[x]}$$

$$\frac{1}{2} i \coth\left[\frac{x}{2}\right] - \log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right] + \frac{2 i \sinh\left[\frac{x}{2}\right]}{\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right]} + \frac{1}{2} i \tanh\left[\frac{x}{2}\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^3}{i + \sinh[x]}, x, 7, 0 \right\}$$

$$-\frac{3}{2} i \operatorname{ArcCoth}[\cosh[x]] - \coth[x] + \frac{1}{2} i \coth[x] \operatorname{Csch}[x] + \frac{i \cosh[x]}{1 - i \sinh[x]}$$

$$\frac{1}{8} \left(-4 \coth\left[\frac{x}{2}\right] + i \operatorname{Csch}\left[\frac{x}{2}\right]^2 - 12 i \log\left[\cosh\left[\frac{x}{2}\right]\right] + 12 i \log\left[\sinh\left[\frac{x}{2}\right]\right] + i \operatorname{Sech}\left[\frac{x}{2}\right]^2 - \frac{16 \sinh\left[\frac{x}{2}\right]}{\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right]} - 4 \tanh\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Csch}[x]^4}{i + \text{Sinh}[x]}, x, 9, 0 \right\}$$

$$\frac{3}{2} \text{ArcCoth}[\text{Cosh}[x]] - 2 i \text{Coth}[x] + \frac{1}{3} i \text{Coth}[x]^3 - \frac{1}{2} \text{Coth}[x] \text{Csch}[x] - \frac{\text{Cosh}[x]}{1 - i \text{Sinh}[x]}$$

$$\frac{1}{24} \left(-20 i \text{Coth}\left[\frac{x}{2}\right] - 3 \text{Csch}\left[\frac{x}{2}\right]^2 + 36 \text{Log}\left[\text{Cosh}\left[\frac{x}{2}\right]\right] - 36 \text{Log}\left[\text{Sinh}\left[\frac{x}{2}\right]\right] - \right.$$

$$\left. 3 \text{Sech}\left[\frac{x}{2}\right]^2 - \frac{48 i \text{Sinh}\left[\frac{x}{2}\right]}{\text{Cosh}\left[\frac{x}{2}\right] - i \text{Sinh}\left[\frac{x}{2}\right]} - 8 i \text{Csch}[x]^3 \text{Sinh}\left[\frac{x}{2}\right]^4 + \frac{1}{2} i \text{Csch}\left[\frac{x}{2}\right]^4 \text{Sinh}[x] - 20 i \text{Tanh}\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Cosh}[x]^3}{a + b \text{Tanh}[x]}, x, 10, 0 \right\}$$

$$\frac{2 b^4 \text{ArcTan}\left[\frac{b + a \text{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a^2 - b^2}}\right]}{(a^2 - b^2)^{5/2}} + \frac{b^3 \text{Cosh}[x]}{(a^2 - b^2)^2} - \frac{b \text{Cosh}[x]^3}{3 (a^2 - b^2)} - \frac{a b^2 \text{Sinh}[x]}{(a^2 - b^2)^2} + \frac{a \text{Sinh}[x]}{a^2 - b^2} + \frac{a \text{Sinh}[x]^3}{3 (a^2 - b^2)}$$

$$\frac{1}{12 (a - b)^{5/2} (a + b)^3 (a + b \text{Tanh}[x])}$$

$$\text{Sech}[x] (a \text{Cosh}[x] + b \text{Sinh}[x]) \left(24 b^4 \sqrt{a + b} \text{ArcTan}\left[\frac{b + a \text{Tanh}\left[\frac{x}{2}\right]}{\sqrt{a - b} \sqrt{a + b}}\right] - 3 \sqrt{a - b} b (a^3 + a^2 b - 5 a b^2 - 5 b^3) \text{Cosh}[x] - \right.$$

$$(a - b)^{3/2} b (a + b)^2 \text{Cosh}[3 x] + 9 a^4 \sqrt{a - b} \text{Sinh}[x] + 9 a^3 \sqrt{a - b} b \text{Sinh}[x] - 21 a^2 \sqrt{a - b} b^2 \text{Sinh}[x] -$$

$$\left. 21 a \sqrt{a - b} b^3 \text{Sinh}[x] + a^4 \sqrt{a - b} \text{Sinh}[3 x] + a^3 \sqrt{a - b} b \text{Sinh}[3 x] - a^2 \sqrt{a - b} b^2 \text{Sinh}[3 x] - a \sqrt{a - b} b^3 \text{Sinh}[3 x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]^2}{1 + \text{Tanh}[x]}, x, 5, 0 \right\}$$

$$\frac{3 x}{2} - \text{Coth}[x] - \text{Log}[\text{Sinh}[x]] - \frac{1}{2 (1 + \text{Tanh}[x])}$$

$$- \frac{1}{4 (1 + \text{Tanh}[x])} (4 - 6 x + \text{Cosh}[x]^2 + 4 \text{Coth}[x] + 4 \text{Log}[\text{Sinh}[x]] -$$

$$\text{Cosh}[x] \text{Sinh}[x] - \text{Sinh}[x]^2 - 6 x \text{Tanh}[x] + 4 \text{Log}[\text{Sinh}[x]] \text{Tanh}[x] + \text{Sinh}[x]^2 \text{Tanh}[x])$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]^3}{1 + \text{Tanh}[x]}, x, 7, 0 \right\}$$

$$- \frac{3 x}{2} + \text{Coth}[x] - \frac{\text{Coth}[x]^2}{2} + 2 \text{Log}[\text{Sinh}[x]] + \frac{1}{2 (1 + \text{Tanh}[x])}$$

$$\frac{1}{4 (1 + \text{Tanh}[x])}$$

$$(\text{Cosh}[2 x] (1 + \text{Tanh}[x]) - 2 (-2 + 3 x - 2 \text{Coth}[x] + \text{Csch}[x]^2 - 4 \text{Log}[\text{Sinh}[x]]) + \text{Csch}[x] \text{Sech}[x] + \text{Cosh}[x] \text{Sinh}[x] +$$

$$\text{Sinh}[x]^2 + 3 x \text{Tanh}[x] - 4 \text{Log}[\text{Sinh}[x]] \text{Tanh}[x])$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Sech}[x]^2}{a + b \tanh[x]}, x, 2, 0 \right\}$$

$$\frac{\text{Log}[a + b \tanh[x]]}{b}$$

$$\frac{-\text{Log}[\cosh[x]] + \text{Log}[-a \cosh[x] - b \sinh[x]]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Sech}[x]^3}{1 + \tanh[x]}, x, 4, 0 \right\}$$

$$\text{ArcTan}[\sinh[x]] + \text{Sech}[x]$$

$$2 \text{ArcTan}\left[\tanh\left[\frac{x}{2}\right]\right] + \text{Sech}[x]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Csch}[x]^4}{a + b \tanh[x]}, x, 5, 0 \right\}$$

$$\frac{(a^2 - b^2) \coth[x]}{a^3} + \frac{b \coth[x]^2}{2 a^2} - \frac{\coth[x]^3}{3 a} - \frac{b (a^2 - b^2) \text{Log}[b + a \coth[x]]}{a^4}$$

$$\frac{1}{6 a^4 (a + b \tanh[x])} \left(-2 \coth[x] \left(-2 a^4 + 3 a^2 b^2 + a^4 \text{Csch}[x]^2 \right) + \right.$$

$$\left. b \left(a^3 \text{Csch}[x]^2 + 2 a \left(2 a^2 - 3 b^2 + 3 (a^2 - b^2) \text{Log}[\sinh[x]] - 3 (a^2 - b^2) \text{Log}[a \cosh[x] + b \sinh[x]] \right) + \right. \right.$$

$$\left. \left. 3 a^2 b \text{Csch}[x] \text{Sech}[x] + 6 b (a^2 - b^2) (\text{Log}[\sinh[x]] - \text{Log}[a \cosh[x] + b \sinh[x]]) \tanh[x] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Csch}[x]}{1 + \tanh[x]}, x, 4, 0 \right\}$$

$$-\text{ArcCoth}[\cosh[x]] + \cosh[x] - \sinh[x]$$

$$\frac{\cosh[x] - \text{Log}\left[2 \cosh\left[\frac{x}{2}\right]\right] + \text{Log}\left[2 \sinh\left[\frac{x}{2}\right]\right] - \left(\text{Log}\left[\cosh\left[\frac{x}{2}\right]\right] - \text{Log}\left[\sinh\left[\frac{x}{2}\right]\right] + \sinh[x]\right) \tanh[x]}{1 + \tanh[x]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Csch}[x]^3}{1 + \tanh[x]}, x, 5, 0 \right\}$$

$$-\frac{1}{2} \text{ArcCoth}[\cosh[x]] + \cosh[x] - \frac{1}{2} \coth[x] \text{Csch}[x]$$

$$\frac{1}{8} \left(4 \coth\left[\frac{x}{2}\right] - \text{Csch}\left[\frac{x}{2}\right]^2 - 4 \text{Log}\left[\cosh\left[\frac{x}{2}\right]\right] + 4 \text{Log}\left[\sinh\left[\frac{x}{2}\right]\right] - \text{Sech}\left[\frac{x}{2}\right]^2 - 4 \tanh\left[\frac{x}{2}\right] \right)$$

PossibleZeroQ::ztest1:

Unable to decide whether numeric quantity $-\sqrt{1-i} + \sqrt{1+i} - \sqrt{-1+i} \sqrt{1+i} \sqrt{-1+\sqrt{1-i} \sqrt{1+i}}$ is equal to zero. Assuming it is. >>

PossibleZeroQ::ztest1: Unable to decide whether numeric quantity

$$\frac{-1 + \text{Abs}\left[\sqrt{1-i} + \sqrt{1+i}\right]}{\left((2 \text{Im}[\ll 1 \gg] + 2 \text{Im}[\ll 1 \gg] \text{Re}[\ll 1 \gg] - 2 \text{Im}[\ll 1 \gg] \text{Re}[\ll 1 \gg])^2 + (-\text{Power}[\ll 2 \gg] + \text{Im}[\ll 1 \gg]^2 + 2 \text{Plus}[\ll 2 \gg] + \text{Re}[\ll 1 \gg]^2 - \text{Power}[\ll 2 \gg])^2\right)^{1/4}}$$

is equal to zero. Assuming it is. >>

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Tanh}[x]^2}{1 + \text{Coth}[x]}, x, 5, 0\right\}$$

$$\frac{3x}{2} - \text{Log}[\text{Cosh}[x]] - \text{Tanh}[x] + \frac{1}{2(1 + \text{Tanh}[x])}$$

$$-\frac{4 - 6x + 2 \text{Cosh}[x]^2 - 6x \text{Coth}[x] - \text{Cosh}[2x](1 + \text{Coth}[x]) + 4 \text{Log}[\text{Cosh}[x]] + 4 \text{Coth}[x] \text{Log}[\text{Cosh}[x]] + \text{Sinh}[2x] + 4 \text{Tanh}[x]}{4(1 + \text{Coth}[x])}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Tanh}[x]^3}{1 + \text{Coth}[x]}, x, 7, 0\right\}$$

$$-\frac{3x}{2} + 2 \text{Log}[\text{Cosh}[x]] + \text{Tanh}[x] - \frac{\text{Tanh}[x]^2}{2} - \frac{1}{2(1 + \text{Tanh}[x])}$$

$$\frac{1}{4(1 + \text{Coth}[x])} \left(4 - 6x - \text{Cosh}[x]^2(-1 + \text{Coth}[x]) + 8 \text{Log}[\text{Cosh}[x]] + \text{Coth}[x](-6x + 8 \text{Log}[\text{Cosh}[x]]) + 2 \text{Csch}[x] \text{Sech}[x] + 2 \text{Sech}[x]^2 + \text{Cosh}[x] \text{Sinh}[x] - \text{Sinh}[x]^2 + 4 \text{Tanh}[x]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Sech}[x]^4}{a + b \text{Coth}[x]}, x, 5, 0\right\}$$

$$-\frac{b(a^2 - b^2) \text{Log}[b + a \text{Tanh}[x]]}{a^4} + \frac{(a^2 - b^2) \text{Tanh}[x]}{a^3} + \frac{b \text{Tanh}[x]^2}{2a^2} - \frac{\text{Tanh}[x]^3}{3a}$$

$$\frac{1}{6a^4(a + b \text{Coth}[x])} \left(6b^2(a^2 - b^2) \text{Coth}[x](\text{Log}[\text{Cosh}[x]] - \text{Log}[b \text{Cosh}[x] + a \text{Sinh}[x]]) + a(4a^2b - 6b^3 + 6a^2b \text{Log}[\text{Cosh}[x]] - 6b^3 \text{Log}[\text{Cosh}[x]] - 6a^2b \text{Log}[b \text{Cosh}[x] + a \text{Sinh}[x]] + 6b^3 \text{Log}[b \text{Cosh}[x] + a \text{Sinh}[x]] - 3ab^2 \text{Csch}[x] \text{Sech}[x] + a^2 \text{Sech}[x]^3(-b \text{Cosh}[x] + 2a \text{Sinh}[x]) + 4a^3 \text{Tanh}[x] - 6ab^2 \text{Tanh}[x])\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Sech}[x]}{1 + \text{Coth}[x]}, x, 4, 0\right\}$$

$$\text{ArcTan}[\text{Sinh}[x]] + \text{Cosh}[x] - \text{Sinh}[x]$$

$$\frac{2 \text{ArcTan}\left[\text{Tanh}\left[\frac{x}{2}\right]\right] + (2 \text{ArcTan}\left[\text{Tanh}\left[\frac{x}{2}\right]\right] + \text{Cosh}[x]) \text{Coth}[x] - \text{Sinh}[x]}{1 + \text{Coth}[x]}$$

Incorrect antiderivative:

$$\left\{\frac{\text{Sech}[x]}{1 + 2 \text{Coth}[x]}, x, 4, 0\right\}$$

$$\begin{aligned}
& -i \operatorname{ArcTan}[\operatorname{Sinh}[x]] + \frac{4 i \operatorname{ArcTan}\left[\frac{i+2 \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{5}}\right]}{\sqrt{5}} \\
& - \frac{1}{\left(\sqrt{2-i}-\sqrt{2+i}\right) \sqrt{10\left(2+\sqrt{5}\right)}} \\
& i \left(\frac{-5-(2+i) \sqrt{5}-(2+i)\left(2+\sqrt{5}\right)\left((9-2 i)-(4-i) \sqrt{5}+\sqrt{(-4+2 i)\left(-2+\sqrt{5}\right)}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{(-20-10 i)\left(-2+\sqrt{5}\right)}} \right) + \\
& 2 \sqrt{9+4 \sqrt{5}} \operatorname{ArcTanh}\left[\frac{-\sqrt{2-i}-\sqrt{2+i}+\left(\sqrt{2-i}-\sqrt{2+i}+i \sqrt{2\left(2+\sqrt{5}\right)}\right) \operatorname{Tanh}\left[\frac{x}{2}\right]}{\sqrt{2\left(-2+\sqrt{5}\right)}}\right] + \\
& \left(2-5 \sqrt{9+4 \sqrt{5}}+2 \sqrt{5\left(9+4 \sqrt{5}\right)}\right) \\
& \left(\operatorname{Log}\left[(2+i)\left(\sqrt{(-4+2 i)\left(2+\sqrt{5}\right)}-\left((-2+i)+\sqrt{5}\right) \operatorname{Cosh}[x]-\left((2-i)+\sqrt{5}\right) \operatorname{Sinh}[x]\right)\right]-\right. \\
& \left.\operatorname{Log}\left[i \sqrt{10\left(2+\sqrt{5}\right)}+\left(-\sqrt{10-5 i}+\sqrt{10+5 i}\right) \operatorname{Cosh}[x]+\left(\sqrt{10-5 i}+\sqrt{10+5 i}\right) \operatorname{Sinh}[x]\right]\right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{\frac{\operatorname{Csch}[x]^3}{1+\operatorname{Coth}[x]}, x, 4, 0\right\} \\
& \operatorname{ArcCoth}[\operatorname{Cosh}[x]]-\operatorname{Csch}[x] \\
& -\operatorname{Csch}[x]+\operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right]-\operatorname{Log}\left[\operatorname{Sinh}\left[\frac{x}{2}\right]\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{\frac{\operatorname{Coth}[x]^2}{i+\operatorname{Csch}[x]}, x, 3, 0\right\} \\
& -i x-\operatorname{ArcCoth}[\operatorname{Cosh}[x]] \\
& -i x-\operatorname{Log}\left[2 \operatorname{Cosh}\left[\frac{x}{2}\right]\right]+\operatorname{Log}\left[2 \operatorname{Sinh}\left[\frac{x}{2}\right]\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{\frac{\operatorname{Coth}[x]^4}{i+\operatorname{Csch}[x]}, x, 6, 0\right\} \\
& -i x-\frac{1}{2} \operatorname{ArcCoth}[\operatorname{Cosh}[x]]+i \operatorname{Coth}[x]-\frac{1}{2} \operatorname{Coth}[x] \operatorname{Csch}[x]
\end{aligned}$$

$$-\frac{1}{8} i \left(8 x - 4 \operatorname{Coth}\left[\frac{x}{2}\right] - i \operatorname{Csch}\left[\frac{x}{2}\right]^2 - 4 i \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] + 4 i \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{x}{2}\right]\right] - i \operatorname{Sech}\left[\frac{x}{2}\right]^2 - 4 \operatorname{Tanh}\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^2}{i + \operatorname{Csch}[x]}, x, 6, 0 \right\}$$

$$-\operatorname{ArcCoth}[\operatorname{Cosh}[x]] + \frac{i \operatorname{Cosh}[x]}{i - \operatorname{Sinh}[x]}$$

$$-\operatorname{Log}\left[2 \operatorname{Cosh}\left[\frac{x}{2}\right]\right] + \operatorname{Log}\left[2 \operatorname{Sinh}\left[\frac{x}{2}\right]\right] - \frac{2 i \operatorname{Sinh}\left[\frac{x}{2}\right]}{\operatorname{Cosh}\left[\frac{x}{2}\right] + i \operatorname{Sinh}\left[\frac{x}{2}\right]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^3}{i + \operatorname{Csch}[x]}, x, 7, 0 \right\}$$

$$i \operatorname{ArcCoth}[\operatorname{Cosh}[x]] - \operatorname{Coth}[x] + \frac{\operatorname{Cosh}[x]}{i - \operatorname{Sinh}[x]}$$

$$-\frac{1}{2} \operatorname{Coth}\left[\frac{x}{2}\right] + i \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] - i \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{x}{2}\right]\right] - \frac{2 \operatorname{Sinh}\left[\frac{x}{2}\right]}{\operatorname{Cosh}\left[\frac{x}{2}\right] + i \operatorname{Sinh}\left[\frac{x}{2}\right]} - \frac{1}{2} \operatorname{Tanh}\left[\frac{x}{2}\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^4}{i + \operatorname{Csch}[x]}, x, 9, 0 \right\}$$

$$\frac{3}{2} \operatorname{ArcCoth}[\operatorname{Cosh}[x]] + i \operatorname{Coth}[x] - \frac{1}{2} \operatorname{Coth}[x] \operatorname{Csch}[x] - \frac{i \operatorname{Cosh}[x]}{i - \operatorname{Sinh}[x]}$$

$$\frac{1}{8} \left(4 i \operatorname{Coth}\left[\frac{x}{2}\right] - \operatorname{Csch}\left[\frac{x}{2}\right]^2 + 12 \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{x}{2}\right]\right] - 12 \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{x}{2}\right]\right] - \operatorname{Sech}\left[\frac{x}{2}\right]^2 + \frac{16 \operatorname{Sinh}\left[\frac{x}{2}\right]}{-i \operatorname{Cosh}\left[\frac{x}{2}\right] + \operatorname{Sinh}\left[\frac{x}{2}\right]} + 4 i \operatorname{Tanh}\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Sinh}[x]^2}{(i + \operatorname{Sinh}[x])^2}, x, 5, 0 \right\}$$

$$x + \frac{5 i \operatorname{Cosh}[x]}{3 (1 - i \operatorname{Sinh}[x])} + \frac{i \operatorname{Cosh}[x]}{3 (i + \operatorname{Sinh}[x])^2}$$

$$\frac{3 (-4 i + 3 x) \operatorname{Cosh}\left[\frac{x}{2}\right] + (10 i - 3 x) \operatorname{Cosh}\left[\frac{3x}{2}\right] - 6 i (-3 i + 2 x + x \operatorname{Cosh}[x]) \operatorname{Sinh}\left[\frac{x}{2}\right]}{6 \left(\operatorname{Cosh}\left[\frac{x}{2}\right] - i \operatorname{Sinh}\left[\frac{x}{2}\right]\right)^3}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Coth}[x]^2}{(i + \operatorname{Sinh}[x])^2}, x, 5, 0 \right\}$$

$$2 i \operatorname{ArcCoth}[\operatorname{Cosh}[x]] + \operatorname{Coth}[x] - \frac{2 i \operatorname{Cosh}[x]}{1 - i \operatorname{Sinh}[x]}$$

$$\frac{1}{2} \left(\coth\left[\frac{x}{2}\right] + 4i \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] - 4i \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right] + \frac{8 \sinh\left[\frac{x}{2}\right]}{\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right]} + \tanh\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\coth[x]^3}{(i + \sinh[x])^2}, x, 5, 0 \right\}$$

$$2i \operatorname{Csch}[x] + \frac{\operatorname{Csch}[x]^2}{2} + 2 \operatorname{Log}[\sinh[x]] - 2 \operatorname{Log}[i + \sinh[x]]$$

$$-4i \operatorname{ArcTan}\left[\coth\left[\frac{x}{2}\right]\right] + i \coth\left[\frac{x}{2}\right] + \frac{1}{8} \operatorname{Csch}\left[\frac{x}{2}\right]^2 - 2 \operatorname{Log}[4 \cosh[x]] + 2 \operatorname{Log}[\sinh[x]] - \frac{1}{8} \operatorname{Sech}\left[\frac{x}{2}\right]^2 - i \tanh\left[\frac{x}{2}\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]}{(i + \sinh[x])^2}, x, 6, 0 \right\}$$

$$\operatorname{ArcCoth}[\cosh[x]] - \frac{4 \cosh[x]}{3(1 - i \sinh[x])} + \frac{\cosh[x]}{3(i + \sinh[x])^2}$$

$$\operatorname{Log}\left[2 \cosh\left[\frac{x}{2}\right]\right] - \operatorname{Log}\left[2 \sinh\left[\frac{x}{2}\right]\right] - \frac{i}{3i + 3 \sinh[x]} - \frac{2 \sinh\left[\frac{x}{2}\right](5i + 4 \sinh[x])}{3 \left(\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right]\right)^3}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^2}{(i + \sinh[x])^2}, x, 7, 0 \right\}$$

$$2i \operatorname{ArcCoth}[\cosh[x]] + \coth[x] - \frac{7i \cosh[x]}{3(1 - i \sinh[x])} + \frac{i \cosh[x]}{3(i + \sinh[x])^2}$$

$$\frac{1}{6} \left(3 \coth\left[\frac{x}{2}\right] + 12i \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] - 12i \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right] + \frac{2}{i + \sinh[x]} - \frac{4 \sinh\left[\frac{x}{2}\right](8i + 7 \sinh[x])}{(i \cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right])^3} + 3 \tanh\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Csch}[x]^3}{(i + \sinh[x])^2}, x, 9, 0 \right\}$$

$$-\frac{7}{2} \operatorname{ArcCoth}[\cosh[x]] + 2i \coth[x] + \frac{1}{2} \coth[x] \operatorname{Csch}[x] + \frac{10 \cosh[x]}{3(1 - i \sinh[x])} - \frac{\cosh[x]}{3(i + \sinh[x])^2}$$

$$\frac{1}{24} \left(24i \coth\left[\frac{x}{2}\right] + 3 \operatorname{Csch}\left[\frac{x}{2}\right]^2 - 84 \operatorname{Log}\left[\cosh\left[\frac{x}{2}\right]\right] + 84 \operatorname{Log}\left[\sinh\left[\frac{x}{2}\right]\right] + \right.$$

$$\left. 3 \operatorname{Sech}\left[\frac{x}{2}\right]^2 + \frac{8}{(\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right])^2} + \frac{160i \sinh\left[\frac{x}{2}\right]}{\cosh\left[\frac{x}{2}\right] - i \sinh\left[\frac{x}{2}\right]} + \frac{16 \sinh\left[\frac{x}{2}\right]}{(i \cosh\left[\frac{x}{2}\right] + \sinh\left[\frac{x}{2}\right])^3} + 24i \tanh\left[\frac{x}{2}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\cosh[x]^3}{(1 - i \sinh[x])^3}, x, 6, 0 \right\}$$

$$\frac{-i \operatorname{Log}[i + \operatorname{Sinh}[x]] + \frac{2}{i + \operatorname{Sinh}[x]}}{2 - 2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]\right] + \operatorname{Log}[\operatorname{Cosh}[x]] - 2 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]\right] \operatorname{Sinh}[x] - i \operatorname{Log}[\operatorname{Cosh}[x]] \operatorname{Sinh}[x]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Cosh}[x]^3}{1 - \operatorname{Sinh}[x]^2}, x, 4, 0 \right\}$$

$$2 \operatorname{ArcTanh}[\operatorname{Sinh}[x]] - \operatorname{Sinh}[x]$$

$$-\operatorname{Log}[2(-1 + \operatorname{Sinh}[x])] + \operatorname{Log}[2(1 + \operatorname{Sinh}[x])] - \operatorname{Sinh}[x]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \operatorname{Sech}[c + d x]^2}{a + b \operatorname{Tanh}[c + d x]^2}, x, 10, 0 \right\}$$

$$\frac{x \operatorname{Log}\left[1 + \frac{(a+b) e^{2c+2dx}}{a-2\sqrt{-a}\sqrt{b-b}}\right]}{2\sqrt{-a}\sqrt{b}d} - \frac{x \operatorname{Log}\left[1 + \frac{(a+b) e^{2c+2dx}}{a+2\sqrt{-a}\sqrt{b-b}}\right]}{2\sqrt{-a}\sqrt{b}d} + \frac{\operatorname{PolyLog}\left[2, -\frac{(a+b) e^{2c+2dx}}{a-2\sqrt{-a}\sqrt{b-b}}\right]}{4\sqrt{-a}\sqrt{b}d^2} - \frac{\operatorname{PolyLog}\left[2, -\frac{(a+b) e^{2c+2dx}}{a+2\sqrt{-a}\sqrt{b-b}}\right]}{4\sqrt{-a}\sqrt{b}d^2}$$

$$- \frac{1}{4\sqrt{ab}d^2} \left(4(c+dx) \operatorname{ArcTan}\left[\frac{a \operatorname{Coth}[c+dx]}{\sqrt{ab}}\right] + 2 \left(2c - i \operatorname{ArcCos}\left[\frac{-a+b}{a+b}\right] \right) \operatorname{ArcTan}\left[\frac{b \operatorname{Tanh}[c+dx]}{\sqrt{ab}}\right] + \right.$$

$$\left. \left(\operatorname{ArcCos}\left[\frac{-a+b}{a+b}\right] + 2 \left(\operatorname{ArcTan}\left[\frac{a \operatorname{Coth}[c+dx]}{\sqrt{ab}}\right] + \operatorname{ArcTan}\left[\frac{b \operatorname{Tanh}[c+dx]}{\sqrt{ab}}\right] \right) \right) \operatorname{Log}\left[\frac{\sqrt{2}\sqrt{ab}e^{-c-dx}}{\sqrt{a+b}\sqrt{a-b+(a+b)\operatorname{Cosh}[2(c+dx)]}}\right] +$$

$$\left(\operatorname{ArcCos}\left[\frac{-a+b}{a+b}\right] - 2 \left(\operatorname{ArcTan}\left[\frac{a \operatorname{Coth}[c+dx]}{\sqrt{ab}}\right] + \operatorname{ArcTan}\left[\frac{b \operatorname{Tanh}[c+dx]}{\sqrt{ab}}\right] \right) \right) \operatorname{Log}\left[\frac{\sqrt{2}\sqrt{ab}e^{c+dx}}{\sqrt{a+b}\sqrt{a-b+(a+b)\operatorname{Cosh}[2(c+dx)]}}\right] -$$

$$\left(\operatorname{ArcCos}\left[\frac{-a+b}{a+b}\right] + 2 \operatorname{ArcTan}\left[\frac{b \operatorname{Tanh}[c+dx]}{\sqrt{ab}}\right] \right) \operatorname{Log}\left[\frac{2a(b-i\sqrt{ab}) \operatorname{Sech}[c+dx] (\operatorname{Cosh}[c+dx] - \operatorname{Sinh}[c+dx])}{(a+b)(a+i\sqrt{ab}\operatorname{Tanh}[c+dx])}\right] -$$

$$\left(\operatorname{ArcCos}\left[\frac{-a+b}{a+b}\right] - 2 \operatorname{ArcTan}\left[\frac{b \operatorname{Tanh}[c+dx]}{\sqrt{ab}}\right] \right) \operatorname{Log}\left[\frac{2a(b+i\sqrt{ab}) \operatorname{Sech}[c+dx] (\operatorname{Cosh}[c+dx] + \operatorname{Sinh}[c+dx])}{(a+b)(a+i\sqrt{ab}\operatorname{Tanh}[c+dx])}\right] +$$

$$i \left(-\operatorname{PolyLog}\left[2, \frac{(-a+b-2i\sqrt{ab})(-a+i\sqrt{ab}\operatorname{Tanh}[c+dx])}{(a+b)(a+i\sqrt{ab}\operatorname{Tanh}[c+dx])}\right] + \right.$$

$$\left. \operatorname{PolyLog}\left[2, \frac{(-a+b+2i\sqrt{ab})(i a + \sqrt{ab}\operatorname{Tanh}[c+dx])}{(a+b)(-i a + \sqrt{ab}\operatorname{Tanh}[c+dx])}\right] \right)$$

Unable to integrate:

$$\left\{ \frac{x^2 \operatorname{Sech}[c + d x]^2}{a + b \operatorname{Tanh}[c + d x]^2}, x, 12, 0 \right\}$$

$$\frac{x^2 \operatorname{Log}\left[1 + \frac{(a+b) e^{2c+2dx}}{a-2\sqrt{-a}\sqrt{b}-b}\right]}{2\sqrt{-a}\sqrt{b}d} - \frac{x^2 \operatorname{Log}\left[1 + \frac{(a+b) e^{2c+2dx}}{a+2\sqrt{-a}\sqrt{b}-b}\right]}{2\sqrt{-a}\sqrt{b}d} + \frac{x \operatorname{PolyLog}\left[2, -\frac{(a+b) e^{2c+2dx}}{a-2\sqrt{-a}\sqrt{b}-b}\right]}{2\sqrt{-a}\sqrt{b}d^2} -$$

$$\frac{x \operatorname{PolyLog}\left[2, -\frac{(a+b) e^{2c+2dx}}{a+2\sqrt{-a}\sqrt{b}-b}\right]}{2\sqrt{-a}\sqrt{b}d^2} - \frac{\operatorname{PolyLog}\left[3, -\frac{(a+b) e^{2c+2dx}}{a-2\sqrt{-a}\sqrt{b}-b}\right]}{4\sqrt{-a}\sqrt{b}d^3} + \frac{\operatorname{PolyLog}\left[3, -\frac{(a+b) e^{2c+2dx}}{a+2\sqrt{-a}\sqrt{b}-b}\right]}{4\sqrt{-a}\sqrt{b}d^3}$$

$$\int \frac{x^2 \operatorname{Sech}[c+dx]^2}{a+b \operatorname{Tanh}[c+dx]^2} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Coth}[x]^3}{a+b \operatorname{Sinh}[x]^3}, x, 10, 0 \right\}$$

$$\frac{b^{2/3} \operatorname{ArcTan}\left[\frac{a^{1/3}-2b^{1/3} \operatorname{Sinh}[x]}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} a^{5/3}} - \frac{\operatorname{Csch}[x]^2}{2a} + \frac{\operatorname{Log}[\operatorname{Sinh}[x]]}{a} -$$

$$\frac{b^{2/3} \operatorname{Log}[a^{1/3}+b^{1/3} \operatorname{Sinh}[x]]}{3a^{5/3}} + \frac{b^{2/3} \operatorname{Log}[a^{2/3}-a^{1/3}b^{1/3} \operatorname{Sinh}[x]+b^{2/3} \operatorname{Sinh}[x]^2]}{6a^{5/3}} - \frac{\operatorname{Log}[a+b \operatorname{Sinh}[x]^3]}{3a}$$

$$- \frac{1}{24a} \left(8 \operatorname{RootSum}\left[-b+3b \#1^2+8a \#1^3-3b \#1^4+b \#1^6 \&, \right. \right.$$

$$\left. \frac{-bx+b \operatorname{Log}[-e^x+\#1]+4ax \#1^3-4a \operatorname{Log}[-e^x+\#1] \#1^3-3bx \#1^4+3b \operatorname{Log}[-e^x+\#1] \#1^4}{b-2b \#1^2-4a \#1^3+b \#1^4} \& \right] +$$

$$3 \left(8x + \operatorname{Csch}\left[\frac{x}{2}\right]^2 - 8 \operatorname{Log}[\operatorname{Sinh}[x]] - \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Tanh}[x]^3}{a+b \operatorname{Cosh}[x]^3}, x, 10, 0 \right\}$$

$$- \frac{b^{2/3} \operatorname{ArcTan}\left[\frac{a^{1/3}-2b^{1/3} \operatorname{Cosh}[x]}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} a^{5/3}} + \frac{\operatorname{Log}[\operatorname{Cosh}[x]]}{a} + \frac{b^{2/3} \operatorname{Log}[a^{1/3}+b^{1/3} \operatorname{Cosh}[x]]}{3a^{5/3}} -$$

$$\frac{b^{2/3} \operatorname{Log}[a^{2/3}-a^{1/3}b^{1/3} \operatorname{Cosh}[x]+b^{2/3} \operatorname{Cosh}[x]^2]}{6a^{5/3}} - \frac{\operatorname{Log}[a+b \operatorname{Cosh}[x]^3]}{3a} + \frac{\operatorname{Sech}[x]^2}{2a}$$

$$\frac{1}{6a} \left(-6x + 6 \operatorname{Log}[\operatorname{Cosh}[x]] - 2 \operatorname{RootSum}\left[b+3b \#1^2+8a \#1^3+3b \#1^4+b \#1^6 \&, \right. \right.$$

$$\left. \frac{-bx+b \operatorname{Log}[-e^x+\#1]-4ax \#1^3+4a \operatorname{Log}[-e^x+\#1] \#1^3-3bx \#1^4+3b \operatorname{Log}[-e^x+\#1] \#1^4}{b+2b \#1^2+4a \#1^3+b \#1^4} \& \right] + 3 \operatorname{Sech}[x]^2 \Big)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Coth}[x]}{\sqrt{1+\operatorname{Coth}[x]}}, x, 6, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{1+\operatorname{Coth}[x]}}{\sqrt{2}}\right]}{\sqrt{2}} + \frac{1}{\sqrt{1+\operatorname{Coth}[x]}}$$

$$\frac{1}{(\mathrm{i} (1 + \operatorname{Coth}[\mathbf{x}]))^{3/2} \left(\frac{1}{2} + \frac{\mathrm{i}}{2} \right) \sqrt{1 + \operatorname{Coth}[\mathbf{x}]}} \left(\operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{\mathrm{i}}{2} \right) \sqrt{\mathrm{i} (1 + \operatorname{Coth}[\mathbf{x}])} \right] + \operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{\mathrm{i}}{2} \right) \sqrt{\mathrm{i} (1 + \operatorname{Coth}[\mathbf{x}])} \right] \operatorname{Coth}[\mathbf{x}] + (1 + \mathrm{i}) \sqrt{\mathrm{i} (1 + \operatorname{Coth}[\mathbf{x}])} \right)$$

Incorrect antiderivative:

$$\{\sqrt{1 + \operatorname{Coth}[\mathbf{x}]} \operatorname{Sech}[\mathbf{x}]^2, \mathbf{x}, 4, 0\}$$

$$\operatorname{ArcTanh}[\sqrt{1 + \operatorname{Coth}[\mathbf{x}]}] + \sqrt{1 + \operatorname{Coth}[\mathbf{x}]} \operatorname{Tanh}[\mathbf{x}]$$

$$\frac{1}{2 \sqrt{\operatorname{Csch}[\mathbf{x}]} \sqrt{\operatorname{Cosh}[\mathbf{x}] + \operatorname{Sinh}[\mathbf{x}]}}$$

$$\sqrt{1 + \operatorname{Coth}[\mathbf{x}]} \left(\frac{(1 - \mathrm{i}) \operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{\mathrm{i}}{2} \right) \sqrt{\mathrm{i} + \mathrm{i} \operatorname{Coth}[\mathbf{x}]} \right] \sqrt{\operatorname{Csch}[\mathbf{x}]} \sqrt{\operatorname{Cosh}[\mathbf{x}] + \operatorname{Sinh}[\mathbf{x}]}}{\sqrt{\mathrm{i} + \mathrm{i} \operatorname{Coth}[\mathbf{x}]}} + \left(\frac{1}{2} + \frac{\mathrm{i}}{2} \right) \right)$$

$$\left(2 (-1)^{1/4} \operatorname{ArcTan} \left[\frac{(2 + \mathrm{i}) + 2 \sqrt{-1 - \mathrm{i}} \left(1 + (-1)^{1/4} \sqrt{\operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right) \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} + 2 (-1)^{1/4} \sqrt{\operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} - \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]}{(-2 - \mathrm{i}) - 2 \sqrt{-1 - \mathrm{i}} \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} + (1 + 2 \mathrm{i}) \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right] + \right.$$

$$\left. 2 (-1)^{1/4} \operatorname{ArcTan} \left[\frac{(2 + \mathrm{i}) + (-1 - \mathrm{i})^{3/2} \left((1 - \mathrm{i}) + \sqrt{2} \sqrt{\operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right) \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} + 2 (-1)^{1/4} \sqrt{\operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} - \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]}{(-2 - \mathrm{i}) + 2 \sqrt{-1 - \mathrm{i}} \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} + (1 + 2 \mathrm{i}) \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right] + \right.$$

$$(-1)^{3/4} \operatorname{Log} \left[\left(\sqrt{-1 - \mathrm{i}} - \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right)^2 \right] + (-1)^{3/4} \operatorname{Log} \left[\left(\sqrt{-1 + \mathrm{i}} - \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right)^2 \right] +$$

$$(-1)^{3/4} \operatorname{Log} \left[\left(\sqrt{-1 - \mathrm{i}} + \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right)^2 \right] + (-1)^{3/4} \operatorname{Log} \left[\left(\sqrt{-1 + \mathrm{i}} + \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right)^2 \right] - (-1)^{3/4}$$

$$\operatorname{Log} \left[32 (1 - \mathrm{i}) \left(1 + \sqrt{2} \sqrt{\operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right) - \frac{2 \left((1 + \mathrm{i}) + \mathrm{i} \sqrt{2} \sqrt{\operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]} \right) \sqrt{-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right]}}{\sqrt{-1 + \mathrm{i}}} + (2 + \mathrm{i}) \left(-1 + \operatorname{Tanh} \left[\frac{\mathbf{x}}{2} \right] \right) \right] -$$

$$\begin{aligned}
& (4 - 4i) \operatorname{Log} \left[4 \left(1 + \sqrt{\operatorname{Tanh} \left[\frac{x}{2} \right]} \right) \right] - (-1)^{3/4} \operatorname{Log} \left[-32 \left((1 + 2i) + 2i \sqrt{-1 + i} \sqrt{-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]} - \right. \right. \\
& \quad \left. \left. (1 - i) \left(\sqrt{2} + \sqrt{-2 + 2i} \sqrt{-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]} \right) \sqrt{\operatorname{Tanh} \left[\frac{x}{2} \right]} - (2 + i) \operatorname{Tanh} \left[\frac{x}{2} \right] \right) \right] - \\
& \quad (-1)^{3/4} \operatorname{Log} \left[-32i \left((2 + i) + 2 \sqrt{-1 - i} \sqrt{-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]} - \operatorname{Tanh} \left[\frac{x}{2} \right] \right) \right] + (2 - 2i) \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{x}{2} \right] \right] - \\
& \quad (-1)^{3/4} \operatorname{Log} \left[32i \left((-2 - i) + 2 \sqrt{-1 - i} \sqrt{-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]} + \operatorname{Tanh} \left[\frac{x}{2} \right] \right) \right] \Bigg) \\
& \quad \sqrt{\operatorname{Cosh}[x] + \operatorname{Sinh}[x]} \sqrt{-\left(-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]\right) \left(1 + \operatorname{Tanh} \left[\frac{x}{2} \right]\right)^3} \Bigg) / \\
& \quad \left(\sqrt{2} (1 + \operatorname{Cosh}[x]) \sqrt{\frac{\operatorname{Cosh}[x] + \operatorname{Sinh}[x]}{(1 + \operatorname{Cosh}[x])^2}} \sqrt{\operatorname{Coth} \left[\frac{x}{2} \right] - \operatorname{Tanh} \left[\frac{x}{2} \right]} \sqrt{\operatorname{Tanh} \left[\frac{x}{2} \right]} \left(1 + \operatorname{Tanh} \left[\frac{x}{2} \right]\right) \right) \Bigg) + \sqrt{1 + \operatorname{Coth}[x] \operatorname{Tanh}[x]}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]}{\sqrt{1 + \operatorname{Sinh}[x]^2}}, x, 2, 0 \right\} \\
& -\operatorname{ArcTanh} \left[\sqrt{\operatorname{Cosh}[x]^2} \right] \\
& \frac{\operatorname{Cosh}[x] \left(-\operatorname{Log} \left[2 \operatorname{Cosh} \left[\frac{x}{2} \right] \right] + \operatorname{Log} \left[2 \operatorname{Sinh} \left[\frac{x}{2} \right] \right] \right)}{\sqrt{\operatorname{Cosh}[x]^2}}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Tanh}[x]^3}{\sqrt{a + b \operatorname{Tanh}[x]^2}}, x, 6, 0 \right\} \\
& \frac{\operatorname{ArcTanh} \left[\frac{\sqrt{a + b \operatorname{Tanh}[x]^2}}{\sqrt{a + b}} \right]}{\sqrt{a + b}} - \frac{\sqrt{a + b \operatorname{Tanh}[x]^2}}{b} \\
& \frac{1}{2} \left(-\frac{\sqrt{2}}{b} + \frac{2 \operatorname{Cosh}[x] \operatorname{Log} \left[\sqrt{2} \sqrt{a + b} \operatorname{Cosh}[x] + \sqrt{a - b + (a + b) \operatorname{Cosh}[2x]} \right]}{\sqrt{a + b} \sqrt{a - b + (a + b) \operatorname{Cosh}[2x]}} \right) \sqrt{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Tanh}[x]^2}{\sqrt{a + b \operatorname{Tanh}[x]^2}}, x, 5, 0 \right\}$$

$$\begin{aligned}
& -\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Tanh}[x]}{\sqrt{a+b} \operatorname{Tanh}[x]^2}\right]}{\sqrt{b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]}{\sqrt{a+b} \operatorname{Tanh}[x]^2}\right]}{\sqrt{a+b}} \\
& \frac{\left(-\sqrt{a+b} \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{-b} \operatorname{Sinh}[x]}{\sqrt{a-b+(a+b)} \operatorname{Cosh}[2x]}\right] + \sqrt{-b} \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \operatorname{Sinh}[x]}{\sqrt{a-b+(a+b)} \operatorname{Cosh}[2x]}\right]\right) \sqrt{a-b+(a+b)} \operatorname{Cosh}[2x] \operatorname{Sech}[x]}{\sqrt{-b} \sqrt{a+b} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2}}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Tanh}[x]}{\sqrt{a+b} \operatorname{Tanh}[x]^2}, x, 3, 0 \right\} \\
& \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]^2}{\sqrt{a+b}}\right]}{\sqrt{a+b}} \\
& \frac{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \operatorname{Log}\left[\sqrt{2} \sqrt{a+b} \operatorname{Cosh}[x] + \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}\right] \operatorname{Sech}[x]}{\sqrt{a+b} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2}}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]}{\sqrt{a+b} \operatorname{Tanh}[x]^2}, x, 7, 0 \right\} \\
& -\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]^2}{\sqrt{a}}\right]}{\sqrt{a}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]^2}{\sqrt{a+b}}\right]}{\sqrt{a+b}} \\
& \left(\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \right. \\
& \quad \left. \left(-\sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a} \operatorname{Cosh}[x]}{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}}\right] + \sqrt{a} \operatorname{Log}\left[\sqrt{2} \sqrt{a+b} \operatorname{Cosh}[x] + \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}\right] \right) \operatorname{Sech}[x] \right) / \\
& \left(\sqrt{a} \sqrt{a+b} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]^2}{\sqrt{a+b} \operatorname{Tanh}[x]^2}, x, 5, 0 \right\} \\
& \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]}{\sqrt{a+b} \operatorname{Tanh}[x]^2}\right]}{\sqrt{a+b}} - \frac{\operatorname{Coth}[x] \sqrt{a+b} \operatorname{Tanh}[x]^2}{a} \\
& \frac{-\sqrt{2} \sqrt{a+b} (a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[2x] + a \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \operatorname{Sinh}[x]}{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}}\right] \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \operatorname{Sech}[x]}{a \sqrt{a+b} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2}}
\end{aligned}$$

Incorrect antiderivative:

$$\left\{ \operatorname{Tanh}[x]^3 \sqrt{a+b} \operatorname{Tanh}[x]^2, x, 7, 0 \right\}$$

$$\sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tanh[x]^2}}{\sqrt{a+b}}\right] - \sqrt{a+b \tanh[x]^2} - \frac{(a+b \tanh[x]^2)^{3/2}}{3b}$$

$$\frac{1}{3\sqrt{2}} \sqrt{(a-b+(a+b) \cosh[2x]) \operatorname{Sech}[x]^2} \left(-4 - \frac{a}{b} - \left(3\sqrt{2} \sqrt{a+b} \cosh[x] \right. \right.$$

$$\left. \left. \left(\operatorname{Log}\left[-\sqrt{a+b} \operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}\left[2 \left(a+b + \frac{\sqrt{a+b} \sqrt{(a-b+(a+b) \cosh[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b) \tanh\left[\frac{x}{2}\right]^2 \right) \right] \right) \right. \right.$$

$$\left. \left. \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right) / \left(\sqrt{(a-b+(a+b) \cosh[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4} + \operatorname{Sech}[x]^2 \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\tanh[x] \sqrt{a+b \tanh[x]^2}, x, 4, 0\}$$

$$\sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tanh[x]^2}}{\sqrt{a+b}}\right] - \sqrt{a+b \tanh[x]^2}$$

$$- \frac{1}{\sqrt{(a-b+(a+b) \cosh[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}$$

$$\left(\sqrt{\frac{a-b+a \cosh[2x]+b \cosh[2x]}{3+4 \cosh[x]+\cosh[2x]}} + \cosh[x] \left(\sqrt{\frac{a-b+a \cosh[2x]+b \cosh[2x]}{3+4 \cosh[x]+\cosh[2x]}} + \sqrt{a+b} \operatorname{Log}\left[-\sqrt{a+b} \operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \right. \right.$$

$$\left. \left. \sqrt{a+b} \operatorname{Log}\left[2 \left(a+b + \frac{\sqrt{a+b} \sqrt{(a-b+(a+b) \cosh[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b) \tanh\left[\frac{x}{2}\right]^2 \right) \right] \right) \right)$$

$$\operatorname{Sech}\left[\frac{x}{2}\right]^2 \sqrt{(a-b+(a+b) \cosh[2x]) \operatorname{Sech}[x]^2}$$

Valid but unnecessarily complicated antiderivative:

$$\{\coth[x] \sqrt{a+b \tanh[x]^2}, x, 7, 0\}$$

$$-\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tanh[x]^2}}{\sqrt{a}}\right] + \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tanh[x]^2}}{\sqrt{a+b}}\right]$$

$$-\frac{1}{\sqrt{a-b+(a+b)\cosh[2x]}} \\ \cosh[x] \left(\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{2}\sqrt{a}\cosh[x]}{\sqrt{a-b+(a+b)\cosh[2x]}}\right] - \sqrt{a+b} \operatorname{Log}\left[\sqrt{2}\sqrt{a+b}\cosh[x] + \sqrt{a-b+(a+b)\cosh[2x]}\right] \right) \\ \sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}[x]^2}$$

Incorrect antiderivative:

$$\{\operatorname{Tanh}[x]^3 (a+b\operatorname{Tanh}[x]^2)^{3/2}, x, 8, 0\}$$

$$(a+b)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right] - (a+b) \sqrt{a+b\operatorname{Tanh}[x]^2} - \frac{1}{3} (a+b\operatorname{Tanh}[x]^2)^{3/2} - \frac{(a+b\operatorname{Tanh}[x]^2)^{5/2}}{5b}$$

$$\frac{1}{15\sqrt{2}} \sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}[x]^2} \left(-26a - \frac{3a^2}{b} - 23b - \left(15\sqrt{2}(a+b)^{3/2}\cosh[x] \right. \right. \\ \left. \left. \left(\operatorname{Log}\left[-\sqrt{a+b}\operatorname{sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}\left[2\left(a+b + \frac{\sqrt{a+b}\sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b)\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right]\right) \right. \right. \\ \left. \left. \operatorname{sech}\left[\frac{x}{2}\right]^2 \right) / \left(\sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}\left[\frac{x}{2}\right]^4} + (6a+11b)\operatorname{sech}[x]^2 - 3b\operatorname{sech}[x]^4 \right) \right)$$

Incorrect antiderivative:

$$\{\operatorname{Tanh}[x] (a+b\operatorname{Tanh}[x]^2)^{3/2}, x, 6, 0\}$$

$$(a+b)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right] - (a+b) \sqrt{a+b\operatorname{Tanh}[x]^2} - \frac{1}{3} (a+b\operatorname{Tanh}[x]^2)^{3/2}$$

$$\frac{1}{\sqrt{2}} \sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}[x]^2} \left(-\frac{4}{3}(a+b) - \left(\sqrt{2}(a+b)^{3/2}\cosh[x] \right. \right. \\ \left. \left. \left(\operatorname{Log}\left[-\sqrt{a+b}\operatorname{sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}\left[2\left(a+b + \frac{\sqrt{a+b}\sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b)\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right]\right) \right. \right. \\ \left. \left. \operatorname{sech}\left[\frac{x}{2}\right]^2 \right) / \left(\sqrt{(a-b+(a+b)\cosh[2x])\operatorname{sech}\left[\frac{x}{2}\right]^4} + \frac{1}{3}b\operatorname{sech}[x]^2 \right) \right)$$

Incorrect antiderivative:

$$\left\{ \text{Coth}[x] \left(a + b \tanh[x]^2 \right)^{3/2}, x, 8, 0 \right\}$$

$$-a^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a + b \tanh[x]^2}}{\sqrt{a}}\right] + (a + b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a + b \tanh[x]^2}}{\sqrt{a + b}}\right] - b \sqrt{a + b \tanh[x]^2}$$

$$-b \sqrt{\frac{a - b + a \cosh[2x] + b \cosh[2x]}{1 + \cosh[2x]}} +$$

$$\frac{1}{2} \left(\left(3a^2 - 2ab - b^2 \right) (1 + \cosh[x]) \sqrt{\frac{1 + \cosh[2x]}{(1 + \cosh[x])^2}} \sqrt{\frac{a - b + (a + b) \cosh[2x]}{1 + \cosh[2x]}} \left(-\text{Log}\left[\sqrt{a} \tanh\left[\frac{x}{2}\right]\right] + \right. \right.$$

$$\left. \text{Log}\left[2 \left(a + 2b + a \tanh\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \right) \right] + \text{Log}\left[\right.$$

$$\left. -2 \left(a + a \tanh\left[\frac{x}{2}\right]^2 + 2b \tanh\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \right) \right] \right)$$

$$\left(-1 + \tanh\left[\frac{x}{2}\right]^2 \right) \left(1 + \tanh\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \tanh\left[\frac{x}{2}\right]^2\right)^2}} \right) /$$

$$\left(4 \sqrt{a} \sqrt{a - b + (a + b) \cosh[2x]} \sqrt{\left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \right) +$$

$$\frac{1}{\sqrt{a - b + (a + b) \cosh[2x]}} 3 \left(a^2 + 2ab + b^2 \right) \sqrt{1 + \cosh[2x]} \sqrt{\frac{a - b + (a + b) \cosh[2x]}{1 + \cosh[2x]}}$$

$$\left(\left(4 \cosh[x]^2 \sqrt{-2b + a(1 + \cosh[2x])} + b(1 + \cosh[2x]) \right) \text{Coth}[x] \left(-\frac{\text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{1 + \cosh[2x]}}{\sqrt{b(-1 + \cosh[2x])} + a(1 + \cosh[2x])}}\right]}{\sqrt{a}} + \right. \right.$$

$$\left. \left. \frac{\text{Log}\left[2 \left(a \sqrt{1 + \cosh[2x]} + b \sqrt{1 + \cosh[2x]} + \sqrt{a + b} \sqrt{b(-1 + \cosh[2x])} + a(1 + \cosh[2x]) \right) \right]}{\sqrt{a + b}} \right) \sinh[2x] \right) /$$

$$\begin{aligned}
& \left(3 \left(1 + \cosh[2x] \right)^2 \sqrt{a-b+(a+b)\cosh[2x]} \right) - \left((1 + \cosh[x]) \sqrt{\frac{1 + \cosh[2x]}{(1 + \cosh[x])^2}} \right. \\
& \left. \left(-\log\left[\sqrt{a} \tanh\left[\frac{x}{2}\right]\right] + \log\left[2 \left(a + 2b + a \tanh\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \right) \right] + \right. \right. \\
& \left. \left. \log\left[-2 \left(a + a \tanh\left[\frac{x}{2}\right]^2 + 2b \tanh\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \right) \right] \right) \right. \\
& \left. \left(-1 + \tanh\left[\frac{x}{2}\right] \right) \left(1 + \tanh\left[\frac{x}{2}\right] \right) \sqrt{\frac{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \tanh\left[\frac{x}{2}\right]\right)^2}} \right) / \right. \\
& \left. \left(4 \sqrt{a} \sqrt{1 + \cosh[2x]} \sqrt{\left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2 + a \left(1 + \tanh\left[\frac{x}{2}\right]^2\right)^2} \right) \right) \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \coth[x]^2 (a+b \tanh[x]^2)^{3/2}, x, 13, 0 \right\} \\
& -b^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \tanh[x]}{\sqrt{a+b \tanh[x]^2}}\right] + (a+b)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \tanh[x]}{\sqrt{a+b \tanh[x]^2}}\right] + \\
& \frac{b \tanh[x] \sqrt{a+b \tanh[x]^2} - \coth[x] (a+b \tanh[x]^2)^{3/2}}{1} \\
& \frac{1}{\sqrt{2} \sqrt{(a-b+(a+b)\cosh[2x]) \operatorname{Sech}[x]^2}} \\
& \operatorname{Sech}[x]^2 \left(\frac{a(a+2b) \sqrt{\frac{(a-b+(a+b)\cosh[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(a-b+(a+b)\cosh[2x]) \operatorname{Csch}[x]^2}}{b}\right], 1\right] \sinh[2x]}{\sqrt{2}} - \right. \\
& \left. a \left((a-b+(a+b)\cosh[2x]) \coth[x] + \right. \right. \\
& \left. \left. \frac{(a+b) \sqrt{\frac{(a-b+(a+b)\cosh[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{(a-b+(a+b)\cosh[2x]) \operatorname{Csch}[x]^2}}{b}\right], 1\right] \sinh[2x]}{\sqrt{2}} \right) \right) \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Tanh}[x]}{(a+b \text{Tanh}[x]^2)^{3/2}}, x, 4, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} - \frac{1}{(a+b) \sqrt{a+b \text{Tanh}[x]^2}}$$

$$\frac{-\sqrt{2} \sqrt{a+b} + \sqrt{a-b+(a+b) \text{Cosh}[2x]} \text{Log}\left[\sqrt{2} \sqrt{a+b} \text{Cosh}[x] + \sqrt{a-b+(a+b) \text{Cosh}[2x]}\right] \text{Sech}[x]}{(a+b)^{3/2} \sqrt{(a-b+(a+b) \text{Cosh}[2x]) \text{Sech}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]}{(a+b \text{Tanh}[x]^2)^{3/2}}, x, 8, 0 \right\}$$

$$-\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a}}\right]}{a^{3/2}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} + \frac{b}{a(a+b) \sqrt{a+b \text{Tanh}[x]^2}}$$

$$\left(\left(- (a+b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a} \text{Cosh}[x]}{\sqrt{a-b+(a+b) \text{Cosh}[2x]}}\right] \sqrt{a-b+(a+b) \text{Cosh}[2x]} + \right. \right.$$

$$\left. \left. \sqrt{a} \left(\sqrt{2} b \sqrt{a+b} \text{Cosh}[x] + a \sqrt{a-b+(a+b) \text{Cosh}[2x]} \text{Log}\left[\sqrt{2} \sqrt{a+b} \text{Cosh}[x] + \sqrt{a-b+(a+b) \text{Cosh}[2x]}\right] \right) \right) \right)$$

$$\text{Sech}[x] \Bigg/ \left(a^{3/2} (a+b)^{3/2} \sqrt{(a-b+(a+b) \text{Cosh}[2x]) \text{Sech}[x]^2} \right)$$

Incorrect antiderivative:

$$\left\{ \frac{\text{Coth}[x]}{(a+b \text{Tanh}[x]^2)^{5/2}}, x, 8, 0 \right\}$$

$$-\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a}}\right]}{a^{5/2}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{5/2}} + \frac{b}{3a(a+b) (a+b \text{Tanh}[x]^2)^{3/2}} + \frac{b(2a+b)}{a^2(a+b)^2 \sqrt{a+b \text{Tanh}[x]^2}}$$

$$\left(\text{Sech}[x]^2 \left(\frac{\sqrt{2} \sqrt{a} b (7a^2 - 2ab - 3b^2 + (7a^2 + 10ab + 3b^2) \text{Cosh}[2x])}{(a+b)^2} - \frac{1}{(a+b)^{5/2}} 3(a-b+(a+b) \text{Cosh}[2x])^{3/2} \right. \right.$$

$$\left. \left((a+b)^{5/2} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a} \text{Cosh}[x]}{\sqrt{a-b+(a+b) \text{Cosh}[2x]}}\right] - a^{5/2} \text{Log}\left[\sqrt{2} \sqrt{a+b} \text{Cosh}[x] + \sqrt{a-b+(a+b) \text{Cosh}[2x]}\right] \right) \text{Sech}[x] \right) \Bigg/$$

$$\left(3a^{5/2} (a-b+(a+b) \text{Cosh}[2x]) \text{Sech}[x]^2 \right)^{3/2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]^3}{\sqrt{a+b \text{Coth}[x]^2}}, x, 6, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}} - \frac{\sqrt{a+b \text{Coth}[x]^2}}{b}$$

$$\frac{1}{2} \sqrt{(-a+b+(a+b) \cosh[2x]) \operatorname{Csch}[x]^2} \left(-\frac{\sqrt{2}}{b} + \frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \sinh[x]}{\sqrt{-a+b+(a+b) \cosh[2x]}}\right] \sinh[x]}{\sqrt{a+b} \sqrt{-a+b+(a+b) \cosh[2x]}} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Coth}[x]^2}{\sqrt{a+b \operatorname{Coth}[x]^2}}, x, 5, 0 \right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Coth}[x]}{\sqrt{a+b \operatorname{Coth}[x]^2}}\right]}{\sqrt{b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Coth}[x]}{\sqrt{a+b \operatorname{Coth}[x]^2}}\right]}{\sqrt{a+b}}$$

$$\left(\sqrt{-a+b+(a+b) \cosh[2x]} \operatorname{Csch}[x] \right.$$

$$\left. \left(-\sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{b} \cosh[x]}{\sqrt{-a+b+(a+b) \cosh[2x]}}\right] + \sqrt{b} \operatorname{Log}\left[\sqrt{2} \sqrt{a+b} \cosh[x] + \sqrt{-a+b+(a+b) \cosh[2x]}\right] \right) \right) /$$

$$\left(\sqrt{b} \sqrt{a+b} \sqrt{(-a+b+(a+b) \cosh[2x]) \operatorname{Csch}[x]^2} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Coth}[x]}{\sqrt{a+b \operatorname{Coth}[x]^2}}, x, 3, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Coth}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \sinh[x]}{\sqrt{-a+b+(a+b) \cosh[2x]}}\right] \sqrt{-a+b+(a+b) \cosh[2x]} \operatorname{Csch}[x]}{\sqrt{a+b} \sqrt{(-a+b+(a+b) \cosh[2x]) \operatorname{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\tanh[x]}{\sqrt{a+b \operatorname{Coth}[x]^2}}, x, 7, 0 \right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Coth}[x]^2}}{\sqrt{a}}\right]}{\sqrt{a}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Coth}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}}$$

$$\frac{\left(-\sqrt{a+b} \operatorname{ArcTan}\left[\frac{\sqrt{2} \sqrt{-a} \sinh[x]}{\sqrt{-a+b+(a+b) \cosh[2x]}}\right] + \sqrt{-a} \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \sinh[x]}{\sqrt{-a+b+(a+b) \cosh[2x]}}\right] \right) \sqrt{-a+b+(a+b) \cosh[2x]} \operatorname{Csch}[x]}{\sqrt{-a} \sqrt{a+b} \sqrt{(-a+b+(a+b) \cosh[2x]) \operatorname{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\tanh[x]^2}{\sqrt{a+b \operatorname{Coth}[x]^2}}, x, 5, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Coth}[x]}{\sqrt{a+b \text{Coth}[x]^2}}\right]}{\sqrt{a+b}} - \frac{\sqrt{a+b \text{Coth}[x]^2} \text{Tanh}[x]}{a}$$

$$\left(\left(\sqrt{2} a \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \text{Cosh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] \text{Cosh}[x] - \sqrt{a+b} \sqrt{-a+b+(a+b) \text{Cosh}[2x]} \right) \right.$$

$$\left. \sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2 \text{Tanh}[x]} \right) / \left(\sqrt{2} a \sqrt{a+b} \sqrt{-a+b+(a+b) \text{Cosh}[2x]} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\text{Coth}[x] \sqrt{a+b \text{Coth}[x]^2}, x, 4, 0\}$$

$$\sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right] - \sqrt{a+b \text{Coth}[x]^2}$$

$$-\frac{\text{Csch}[x]^2 \left(\sqrt{2} (-a+b+(a+b) \text{Cosh}[2x]) - 2 \sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \text{Sinh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] \sqrt{-a+b+(a+b) \text{Cosh}[2x]} \text{Sinh}[x] \right)}{2 \sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{a+b \text{Coth}[x]^2} \text{Tanh}[x], x, 7, 0\}$$

$$-\sqrt{a} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a}}\right] + \sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right]$$

$$\frac{\left(\sqrt{-a} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{-a} \text{Sinh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] \sqrt{-a+b+(a+b) \text{Cosh}[2x]} + \sqrt{b} \sqrt{a+b} \text{ArcSinh}\left[\frac{\sqrt{a+b} \text{Sinh}[x]}{\sqrt{b}}\right] \sqrt{\frac{-a+b+(a+b) \text{Cosh}[2x]}{b}} \right) \text{Csch}[x]}{\sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\{\text{Coth}[x] (a+b \text{Coth}[x]^2)^{3/2}, x, 6, 0\}$$

$$(a+b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right] - (a+b) \sqrt{a+b \text{Coth}[x]^2} - \frac{1}{3} (a+b \text{Coth}[x]^2)^{3/2}$$

$$\frac{(a+b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \text{Sinh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] \sqrt{-a+b+(a+b) \text{Cosh}[2x]} \text{Csch}[x]}{\sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}} -$$

$$\frac{\sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2} (4(a+b) + b \text{Csch}[x]^2)}{3 \sqrt{2}}$$

Incorrect antiderivative:

$$\{(a+b \text{Coth}[x]^2)^{3/2} \text{Tanh}[x], x, 8, 0\}$$

$$-a^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a}}\right] + (a+b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right] - b \sqrt{a+b \text{Coth}[x]^2}$$

$$\begin{aligned}
& -b \sqrt{\frac{-a+b+a \cosh[2x]+b \cosh[2x]}{-1+\cosh[2x]}} + \frac{1}{2} \left(-i \left(-3a^2+2ab+b^2 \right) (1+\cosh[x]) \sqrt{\frac{-1+\cosh[2x]}{(1+\cosh[x])^2}} \right. \\
& \sqrt{\frac{-a+b+(a+b) \cosh[2x]}{-1+\cosh[2x]}} \left(\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{b}{2a+b+2\sqrt{a(a+b)}}} \tanh\left[\frac{x}{2}\right]\right], \frac{2a+b+2\sqrt{a(a+b)}}{2a+b-2\sqrt{a(a+b)}}\right] - \right. \\
& \left. \left. 2 \operatorname{EllipticPi}\left[\frac{2a+b+2\sqrt{a(a+b)}}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{b}{2a+b+2\sqrt{a(a+b)}}} \tanh\left[\frac{x}{2}\right]\right], \frac{2a+b+2\sqrt{a(a+b)}}{2a+b-2\sqrt{a(a+b)}}\right] \right) \right. \\
& \left. \tanh\left[\frac{x}{2}\right] \sqrt{\frac{2a+b+2\sqrt{a(a+b)}+b \tanh\left[\frac{x}{2}\right]^2}{2a+b+2\sqrt{a(a+b)}}} \sqrt{1+\frac{b \tanh\left[\frac{x}{2}\right]^2}{2a+b-2\sqrt{a(a+b)}}} \right) / \\
& \left(\sqrt{\frac{b}{2a+b+2\sqrt{a(a+b)}}} \sqrt{-a+b+(a+b) \cosh[2x]} \sqrt{\tanh\left[\frac{x}{2}\right]^2 \left(-1+\tanh\left[\frac{x}{2}\right]^2\right)} \sqrt{\frac{4a \tanh\left[\frac{x}{2}\right]^2+b \left(1+\tanh\left[\frac{x}{2}\right]^2\right)^2}{\left(-1+\tanh\left[\frac{x}{2}\right]^2\right)^2}} \right) + \\
& \frac{1}{\sqrt{-a+b+(a+b) \cosh[2x]}} 3 \left(a^2+2ab+b^2\right) \sqrt{-1+\cosh[2x]} \sqrt{\frac{-a+b+(a+b) \cosh[2x]}{-1+\cosh[2x]}} \\
& \left(-i \left(1+\cosh[x] \right) \sqrt{\frac{-1+\cosh[2x]}{(1+\cosh[x])^2}} \left(\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{b}{2a+b+2\sqrt{a(a+b)}}} \tanh\left[\frac{x}{2}\right]\right], \frac{2a+b+2\sqrt{a(a+b)}}{2a+b-2\sqrt{a(a+b)}}\right] - \right. \right. \\
& \left. \left. 2 \operatorname{EllipticPi}\left[\frac{2a+b+2\sqrt{a(a+b)}}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{b}{2a+b+2\sqrt{a(a+b)}}} \tanh\left[\frac{x}{2}\right]\right], \frac{2a+b+2\sqrt{a(a+b)}}{2a+b-2\sqrt{a(a+b)}}\right] \right) \right. \\
& \left. \tanh\left[\frac{x}{2}\right] \sqrt{\frac{2a+b+2\sqrt{a(a+b)}+b \tanh\left[\frac{x}{2}\right]^2}{2a+b+2\sqrt{a(a+b)}}} \sqrt{1+\frac{b \tanh\left[\frac{x}{2}\right]^2}{2a+b-2\sqrt{a(a+b)}}} \right) / \\
& \left(\sqrt{\frac{b}{2a+b+2\sqrt{a(a+b)}}} \sqrt{-1+\cosh[2x]} \sqrt{\tanh\left[\frac{x}{2}\right]^2 \left(-1+\tanh\left[\frac{x}{2}\right]^2\right)} \sqrt{\frac{4a \tanh\left[\frac{x}{2}\right]^2+b \left(1+\tanh\left[\frac{x}{2}\right]^2\right)^2}{\left(-1+\tanh\left[\frac{x}{2}\right]^2\right)^2}} \right) + \\
& \left(4 \sqrt{2b+a(-1+\cosh[2x])+b(-1+\cosh[2x])} \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{-1+\cosh[2x]}}{\sqrt{a(-1+\cosh[2x])+b(1+\cosh[2x])}}\right]}{\sqrt{a}} + \right. \right. \\
& \left. \left. \frac{\log\left[2 \left(a \sqrt{-1+\cosh[2x]}+b \sqrt{-1+\cosh[2x]}+\sqrt{a+b} \sqrt{a(-1+\cosh[2x])+b(1+\cosh[2x])}\right)\right]}{\sqrt{a+b}} \right) \right) \\
& \left. \left. \operatorname{Sinh}[x]^2 \operatorname{Sinh}[2x] \tanh[x] \right) / \left(3 \left(-1+\cosh[2x]\right)^2 \sqrt{-a+b+(a+b) \cosh[2x]} \right) \right) \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]^2}{(a + b \text{Coth}[x]^2)^{3/2}}, x, 7, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Coth}[x]}{\sqrt{a+b \text{Coth}[x]^2}}\right]}{(a+b)^{3/2}} - \frac{\text{Coth}[x]}{(a+b) \sqrt{a+b \text{Coth}[x]^2}}$$

$$\left(\left(-2 \sqrt{a+b} \text{Cosh}[x] \sqrt{-a+b+(a+b) \text{Cosh}[2x]} + \sqrt{2} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \text{Cosh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] (-a+b+(a+b) \text{Cosh}[2x]) \right) \right. \\ \left. \sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2} \text{Sinh}[x] \right) / \left(\sqrt{2} (a+b)^{3/2} (-a+b+(a+b) \text{Cosh}[2x])^{3/2} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]}{(a + b \text{Coth}[x]^2)^{3/2}}, x, 4, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} - \frac{1}{(a+b) \sqrt{a+b \text{Coth}[x]^2}}$$

$$\frac{-\sqrt{2} \sqrt{a+b} + \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \text{Sinh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] \sqrt{-a+b+(a+b) \text{Cosh}[2x]} \text{Csch}[x]}{(a+b)^{3/2} \sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Tanh}[x]}{(a + b \text{Coth}[x]^2)^{3/2}}, x, 8, 0 \right\}$$

$$-\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a}}\right]}{a^{3/2}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Coth}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} + \frac{b}{a(a+b) \sqrt{a+b \text{Coth}[x]^2}}$$

$$\frac{\frac{\sqrt{2} b}{a(a+b)} + \frac{\left((a+b)^{3/2} \text{ArcTan}\left[\frac{\sqrt{2} \sqrt{-a} \text{Sinh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] + (-a)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a+b} \text{Sinh}[x]}{\sqrt{-a+b+(a+b) \text{Cosh}[2x]}}\right] \right) \sqrt{-a+b+(a+b) \text{Cosh}[2x]} \text{Csch}[x]}{(-a)^{3/2} (a+b)^{3/2}}}{\sqrt{(-a+b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Coth}[x]}{\sqrt{a+b \text{Sinh}[x]}}, x, 2, 0 \right\}$$

$$-\frac{2 \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Sinh}[x]}}{\sqrt{a}}\right]}{\sqrt{a}}$$

$$-\frac{2\sqrt{b}\operatorname{ArcSinh}\left[\frac{\sqrt{a}\sqrt{\operatorname{Csch}[x]}}{\sqrt{b}}\right]\sqrt{1+\frac{a\operatorname{Csch}[x]}{b}}}{\sqrt{a}\sqrt{\operatorname{Csch}[x]}\sqrt{a+b\operatorname{Sinh}[x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\operatorname{Coth}[x]}{\sqrt{a+b\operatorname{Sinh}[x]^3}},x,2,0\right\}$$

$$-\frac{2\operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Sinh}[x]^3}}{\sqrt{a}}\right]}{3\sqrt{a}}$$

$$-\frac{2\sqrt{b}\operatorname{ArcSinh}\left[\frac{\sqrt{a}\operatorname{Csch}[x]^{3/2}}{\sqrt{b}}\right]\sqrt{1+\frac{a\operatorname{Csch}[x]^3}{b}}}{3\sqrt{a}\operatorname{Csch}[x]^{3/2}\sqrt{a+b\operatorname{Sinh}[x]^3}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\operatorname{Coth}[x]}{\sqrt{a+b\operatorname{Sinh}[x]^4}},x,2,0\right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Sinh}[x]^4}}{\sqrt{a}}\right]}{2\sqrt{a}}$$

$$-\frac{\sqrt{b}\operatorname{ArcSinh}\left[\frac{\sqrt{a}\operatorname{Csch}[x]^2}{\sqrt{b}}\right]\sqrt{1+\frac{a\operatorname{Csch}[x]^4}{b}}\operatorname{Sinh}[x]^2}{2\sqrt{a}\sqrt{a+b\operatorname{Sinh}[x]^4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\operatorname{Coth}[x]\sqrt{a+b\operatorname{Sinh}[x]},x,3,0\right\}$$

$$-2\sqrt{a}\operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Sinh}[x]}}{\sqrt{a}}\right]+2\sqrt{a+b\operatorname{Sinh}[x]}$$

$$\frac{2\left(b+a\operatorname{Csch}[x]-\sqrt{a}\sqrt{b}\operatorname{ArcSinh}\left[\frac{\sqrt{a}\sqrt{\operatorname{Csch}[x]}}{\sqrt{b}}\right]\sqrt{\operatorname{Csch}[x]}\sqrt{1+\frac{a\operatorname{Csch}[x]}{b}}\right)\sqrt{a+b\operatorname{Sinh}[x]}}{b+a\operatorname{Csch}[x]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\operatorname{Tanh}[x]}{\sqrt{a+b\operatorname{Cosh}[x]}},x,2,0\right\}$$

$$-\frac{2\operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Cosh}[x]}}{\sqrt{a}}\right]}{\sqrt{a}}$$

$$-\frac{2\sqrt{b}\operatorname{ArcSinh}\left[\frac{\sqrt{a}\sqrt{\operatorname{Sech}[x]}}{\sqrt{b}}\right]\sqrt{1+\frac{a\operatorname{Sech}[x]}{b}}}{\sqrt{a}\sqrt{a+b\operatorname{Cosh}[x]}\sqrt{\operatorname{Sech}[x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Tanh}[x]}{\sqrt{a + b \text{Cosh}[x]^3}}, x, 2, 0 \right\}$$

$$- \frac{2 \text{ArcTanh}\left[\frac{\sqrt{a + b \text{Cosh}[x]^3}}{\sqrt{a}}\right]}{3 \sqrt{a}}$$

$$- \frac{2 \sqrt{b} \text{ArcSinh}\left[\frac{\sqrt{a} \text{Sech}[x]^{3/2}}{\sqrt{b}}\right] \sqrt{1 + \frac{a \text{Sech}[x]^3}{b}}}{3 \sqrt{a} \sqrt{a + b \text{Cosh}[x]^3} \text{Sech}[x]^{3/2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Tanh}[x]}{\sqrt{a + b \text{Cosh}[x]^4}}, x, 2, 0 \right\}$$

$$- \frac{\text{ArcTanh}\left[\frac{\sqrt{a + b \text{Cosh}[x]^4}}{\sqrt{a}}\right]}{2 \sqrt{a}}$$

$$- \frac{\sqrt{b} \text{ArcSinh}\left[\frac{\sqrt{a} \text{Sech}[x]^2}{\sqrt{b}}\right] \text{Cosh}[x]^2 \sqrt{1 + \frac{a \text{Sech}[x]^4}{b}}}{2 \sqrt{a} \sqrt{a + b \text{Cosh}[x]^4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{a + b \text{Cosh}[x]} \text{Tanh}[x], x, 3, 0 \right\}$$

$$- 2 \sqrt{a} \text{ArcTanh}\left[\frac{\sqrt{a + b \text{Cosh}[x]}}{\sqrt{a}}\right] + 2 \sqrt{a + b \text{Cosh}[x]}$$

$$\frac{2 \sqrt{a + b \text{Cosh}[x]} \left(b + a \text{Sech}[x] - \sqrt{a} \sqrt{b} \text{ArcSinh}\left[\frac{\sqrt{a} \sqrt{\text{Sech}[x]}}{\sqrt{b}}\right] \sqrt{\text{Sech}[x]} \sqrt{1 + \frac{a \text{Sech}[x]}{b}} \right)}{b + a \text{Sech}[x]}$$

Unable to integrate:

$$\left\{ \text{Tanh}[x] \sqrt{a + b \text{Tanh}[x]^4}, x, 8, 0 \right\}$$

$$- \sqrt{a + b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[x]^2 - \sqrt{a + b \text{Tanh}[x]^4}}{\sqrt{a + b}}\right] - \frac{1}{2} \sqrt{b} \text{Log}\left[\sqrt{b} \text{Tanh}[x]^2 + \sqrt{a + b \text{Tanh}[x]^4}\right] +$$

$$\frac{1}{4} \left(-\sqrt{b} \text{Tanh}[x]^2 - \sqrt{a + b \text{Tanh}[x]^4} \right) - \frac{a}{4 \left(\sqrt{b} \text{Tanh}[x]^2 + \sqrt{a + b \text{Tanh}[x]^4} \right)}$$

$$\int \text{Tanh}[x] \sqrt{a + b \text{Tanh}[x]^4} \, dx$$

Unable to integrate:

$$\left\{ \frac{\text{Tanh}[x]}{\sqrt{a + b \text{Tanh}[x]^4}}, x, 3, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{a+b \operatorname{Tanh}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^4}}\right]}{2 \sqrt{a+b}} \\ \int \frac{\operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^4}} \, dx$$

Timed out after 60 seconds:

$$\left\{\frac{\operatorname{Tanh}[x]}{\left(a+b \operatorname{Tanh}[x]^4\right)^{3/2}}, x, 11, 0\right\} \\ -\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Sech}[x]^2-\sqrt{a+b \operatorname{Tanh}[x]^4}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}}- \\ \frac{\sqrt{b}}{(a+b)\left(a+\left(\sqrt{b} \operatorname{Tanh}[x]^2+\sqrt{a+b \operatorname{Tanh}[x]^4}\right)^2\right)}-\frac{\sqrt{b} \operatorname{Tanh}[x]^2+\sqrt{a+b \operatorname{Tanh}[x]^4}}{(a+b)\left(a+\left(\sqrt{b} \operatorname{Tanh}[x]^2+\sqrt{a+b \operatorname{Tanh}[x]^4}\right)^2\right)}$$

???

Unable to integrate:

$$\left\{\operatorname{Coth}[x] \sqrt{a+b \operatorname{Coth}[x]^4}, x, 8, 0\right\} \\ \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Coth}[x]^4}+\sqrt{b} \operatorname{Csch}[x]^2}{\sqrt{a+b}}\right]+\frac{1}{4}\left(-\sqrt{b} \operatorname{Coth}[x]^2-\sqrt{a+b \operatorname{Coth}[x]^4}\right)- \\ \frac{a}{4\left(\sqrt{b} \operatorname{Coth}[x]^2+\sqrt{a+b \operatorname{Coth}[x]^4}\right)}-\frac{1}{2} \sqrt{b} \operatorname{Log}\left[\sqrt{b} \operatorname{Coth}[x]^2+\sqrt{a+b \operatorname{Coth}[x]^4}\right] \\ \int \operatorname{Coth}[x] \sqrt{a+b \operatorname{Coth}[x]^4} \, dx$$

Timed out after 60 seconds:

$$\left\{\frac{\operatorname{Coth}[x]}{\sqrt{a+b \operatorname{Coth}[x]^4}}, x, 3, 0\right\} \\ \frac{\operatorname{ArcTanh}\left[\frac{a+b \operatorname{Coth}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Coth}[x]^4}}\right]}{2 \sqrt{a+b}}$$

???

Timed out after 60 seconds:

$$\left\{\frac{\operatorname{Coth}[x]}{\left(a+b \operatorname{Coth}[x]^4\right)^{3/2}}, x, 11, 0\right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b\text{Coth}[x]^4}+\sqrt{b}\text{Csch}[x]^2}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} - \frac{\sqrt{b}}{(a+b)\left(a+\left(\sqrt{b}\text{Coth}[x]^2+\sqrt{a+b\text{Coth}[x]^4}\right)^2\right)} - \frac{\sqrt{b}\text{Coth}[x]^2+\sqrt{a+b\text{Coth}[x]^4}}{(a+b)\left(a+\left(\sqrt{b}\text{Coth}[x]^2+\sqrt{a+b\text{Coth}[x]^4}\right)^2\right)}$$

???

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{A+B\text{Sinh}[x]}{i-\text{Sinh}[x]}, x, 2, 0\right\}$$

$$-Bx + \frac{(A+iB)\text{Cosh}[x]}{1+i\text{Sinh}[x]}$$

$$\frac{(i\text{Cosh}\left[\frac{x}{2}\right]-\text{Sinh}\left[\frac{x}{2}\right])\left(Bx\text{Cosh}\left[\frac{x}{2}\right]+i(2A+B(2i+x))\text{Sinh}\left[\frac{x}{2}\right]\right)}{-i+\text{Sinh}[x]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{A+B\text{Cosh}[x]}{i-\text{Sinh}[x]}, x, 5, 0\right\}$$

$$-B\text{Log}[i-\text{Sinh}[x]] + \frac{A\text{Cosh}[x]}{1+i\text{Sinh}[x]}$$

$$-\frac{1}{-i+\text{Sinh}[x]}\left(\text{Cosh}\left[\frac{x}{2}\right]+i\text{Sinh}\left[\frac{x}{2}\right]\right)$$

$$\left(B\text{Cosh}\left[\frac{x}{2}\right]\left(2\text{ArcTan}\left[\text{Tanh}\left[\frac{x}{2}\right]\right]-i\text{Log}[\text{Cosh}[x]]\right)+\left(2A+2iB\text{ArcTan}\left[\text{Tanh}\left[\frac{x}{2}\right]\right]+B\text{Log}[\text{Cosh}[x]]\right)\text{Sinh}\left[\frac{x}{2}\right]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\{(a\text{Cosh}[x]+b\text{Sinh}[x])^5, x, 3, 0\}$$

$$(a^2-b^2)^2(b\text{Cosh}[x]+a\text{Sinh}[x])+\frac{2}{3}(a^2-b^2)(b\text{Cosh}[x]+a\text{Sinh}[x])^3+\frac{1}{5}(b\text{Cosh}[x]+a\text{Sinh}[x])^5$$

$$\frac{1}{240}\left(150b(a^2-b^2)^2\text{Cosh}[x]-25b(-3a^4+2a^2b^2+b^4)\text{Cosh}[3x]+3b(5a^4+10a^2b^2+b^4)\text{Cosh}[5x]+150a(a^2-b^2)^2\text{Sinh}[x]+25a(a^4+2a^2b^2-3b^4)\text{Sinh}[3x]+3a(a^4+10a^2b^2+5b^4)\text{Sinh}[5x]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{a\text{Cosh}[x]+b\text{Sinh}[x]}, x, 1, 0\}$$

$$\frac{2i\text{EllipticE}\left[\frac{1}{4}(\pi-2i(x+i\text{ArcTan}[ib,a])), 2\right]\sqrt{a\text{Cosh}[x]+b\text{Sinh}[x]}}{\sqrt{-\frac{a\text{Cosh}[x]+b\text{Sinh}[x]}{a^2-b^2}}}$$

$$\left(b \left(-a^2 + b^2 \right) \text{HypergeometricPFQ} \left[\left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cosh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right]^2 \right] \sinh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right] + \right. \\ \left. \sqrt{-\sinh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right]^2} \left(2 a^3 \sqrt{1 - \frac{b^2}{a^2}} \cosh[x] - 2 a \left(a^2 - b^2 \right) \cosh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right] + \right. \right. \\ \left. \left. 2 a^2 b \sqrt{1 - \frac{b^2}{a^2}} \sinh[x] + a^2 b \sinh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right] - b^3 \sinh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right] \right) \right) \right) / \\ \left(a b \sqrt{1 - \frac{b^2}{a^2}} \sqrt{a \cosh[x] + b \sinh[x]} \sqrt{-\sinh \left[x + \text{ArcTanh} \left[\frac{b}{a} \right] \right]^2} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \left(a \cosh[x] + b \sinh[x] \right)^{3/2}, x, 2, 0 \right\} \\ \frac{2}{3} \left(b \cosh[x] + a \sinh[x] \right) \sqrt{a \cosh[x] + b \sinh[x]} + \\ \frac{2 i \left(a^2 - b^2 \right) \text{EllipticF} \left[\frac{1}{4} \left(\pi - 2 i \left(x + i \text{ArcTan}[i b, a] \right) \right), 2 \right] \sqrt{-\frac{a \cosh[x] + b \sinh[x]}{\sqrt{a^2 - b^2}}}}{3 \sqrt{a \cosh[x] + b \sinh[x]}} \\ \frac{1}{3 \sqrt{1 - \frac{a^2}{b^2}} b} - 2 \sqrt{a \cosh[x] + b \sinh[x]} \\ \left(\left(a^2 - b^2 \right) \sqrt{\cosh \left[x + \text{ArcTanh} \left[\frac{a}{b} \right] \right]^2} \text{HypergeometricPFQ} \left[\left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, -\sinh \left[x + \text{ArcTanh} \left[\frac{a}{b} \right] \right]^2 \right] \text{sech} \left[x + \text{ArcTanh} \left[\frac{a}{b} \right] \right] + \right. \\ \left. \sqrt{1 - \frac{a^2}{b^2}} b \left(b \cosh[x] + a \sinh[x] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \left(a \cosh[x] + b \sinh[x] \right)^{5/2}, x, 2, 0 \right\} \\ \frac{2}{5} \left(b \cosh[x] + a \sinh[x] \right) \left(a \cosh[x] + b \sinh[x] \right)^{3/2} + \\ \frac{6 i \left(a^2 - b^2 \right) \text{EllipticE} \left[\frac{1}{4} \left(\pi - 2 i \left(x + i \text{ArcTan}[i b, a] \right) \right), 2 \right] \sqrt{a \cosh[x] + b \sinh[x]}}{5 \sqrt{-\frac{a \cosh[x] + b \sinh[x]}{\sqrt{a^2 - b^2}}}}$$

$$\frac{1}{5 b \sqrt{a \cosh[x] + b \sinh[x]}}$$

$$\left((a \cosh[x] + b \sinh[x]) \left(6 a (a^2 - b^2) + 2 a b^2 \cosh[2 x] + b (a^2 + b^2) \sinh[2 x] \right) - \frac{1}{a \sqrt{1 - \frac{b^2}{a^2}} \sqrt{-\sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right]^2}} \right. \\ \left. 3 (a - b)^2 (a + b)^2 \left(b \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cosh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right]^2\right] \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right] + \right. \right. \\ \left. \left. \sqrt{-\sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right]^2} \left(2 a \cosh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right] - b \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right] \right) \right) \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a \cosh[x] + b \sinh[x]}}, x, 1, 0 \right\}$$

$$\frac{2 i \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i b, a])), 2\right] \sqrt{-\frac{a \cosh[x] + b \sinh[x]}{\sqrt{a^2 - b^2}}}}{\sqrt{a \cosh[x] + b \sinh[x]}}$$

$$\frac{1}{\sqrt{1 - \frac{a^2}{b^2}} b} 2 \sqrt{\cosh\left[x + \operatorname{ArcTanh}\left[\frac{a}{b}\right]\right]^2}$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, -\sinh\left[x + \operatorname{ArcTanh}\left[\frac{a}{b}\right]\right]^2\right] \operatorname{Sech}\left[x + \operatorname{ArcTanh}\left[\frac{a}{b}\right]\right] \sqrt{a \cosh[x] + b \sinh[x]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a \cosh[x] + b \sinh[x])^{3/2}}, x, 2, 0 \right\}$$

$$\frac{2 (b \cosh[x] + a \sinh[x])}{(a^2 - b^2) \sqrt{a \cosh[x] + b \sinh[x]}} - \frac{2 i \operatorname{EllipticE}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i b, a])), 2\right] \sqrt{a \cosh[x] + b \sinh[x]}}{(a^2 - b^2) \sqrt{-\frac{a \cosh[x] + b \sinh[x]}{\sqrt{a^2 - b^2}}}}$$

$$\left(b \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cosh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right]^2\right] \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right] - \right. \\ \left. \sqrt{-\sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right]^2} \left(2 a \sqrt{1 - \frac{b^2}{a^2}} \cosh[x] - 2 a \cosh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right] + b \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right] \right) \right) \Bigg/$$

$$\left(a b \sqrt{1 - \frac{b^2}{a^2}} \sqrt{a \cosh[x] + b \sinh[x]} \sqrt{-\sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{a}\right]\right]^2} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a \cosh[x] + b \sinh[x])^{5/2}}, x, 2, 0 \right\}$$

$$\frac{2 (b \cosh[x] + a \sinh[x])}{3 (a^2 - b^2) (a \cosh[x] + b \sinh[x])^{3/2}} + \frac{2 i \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i b, a])) , 2\right] \sqrt{-\frac{a \cosh[x] + b \sinh[x]}{\sqrt{a^2 - b^2}}}}{3 (a^2 - b^2) \sqrt{a \cosh[x] + b \sinh[x]}}$$

$$\frac{1}{3 (a^2 - b^2)^2 (a \cosh[x] + b \sinh[x])^{3/2}} \left(2 (a^2 - b^2) (b \cosh[x] + a \sinh[x]) - 2 \sqrt{1 - \frac{a^2}{b^2}} b \sqrt{\cosh\left[x + \operatorname{ArcTanh}\left[\frac{a}{b}\right]\right]^2} \right. \\ \left. \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, -\sinh\left[x + \operatorname{ArcTanh}\left[\frac{a}{b}\right]\right]^2 \operatorname{Sech}\left[x + \operatorname{ArcTanh}\left[\frac{a}{b}\right]\right] (a \cosh[x] + b \sinh[x])^2 \right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{a \operatorname{Coth}[x] + b \operatorname{Csch}[x], x, 3, 0\}$$

$$-b \operatorname{ArcCoth}[\cosh[x]] + a \log[\sinh[x]]$$

$$-b \log\left[\cosh\left[\frac{x}{2}\right]\right] + b \log\left[\sinh\left[\frac{x}{2}\right]\right] + a \log[\sinh[x]]$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Coth}[x] + \operatorname{Csch}[x], x, 3, 0\}$$

$$2 \log\left[\sinh\left[\frac{x}{2}\right]\right]$$

$$-\log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right] + \log[\sinh[x]]$$

Valid but unnecessarily complicated antiderivative:

$$\{-\operatorname{Coth}[x] + \operatorname{Csch}[x], x, 3, 0\}$$

$$-2 \log\left[\cosh\left[\frac{x}{2}\right]\right]$$

$$-\log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right] - \log[\sinh[x]]$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Csch}[x] + \sinh[x], x, 3, 0\}$$

$$-\operatorname{ArcCoth}[\cosh[x]] + \cosh[x]$$

$$\cosh[x] - \log\left[2 \cosh\left[\frac{x}{2}\right]\right] + \log\left[2 \sinh\left[\frac{x}{2}\right]\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{\sqrt{\operatorname{Csch}[x] + \sinh[x]}, x, 3, 0\}$$

$$2 \sqrt{\cosh[x] \operatorname{Coth}[x]} \tanh[x]$$

$$\frac{2 \sqrt{\cosh[x] \operatorname{Coth}[x]} \left(-1 + (-\sinh[x]^2)^{1/4}\right) \tanh[x]}{(-\sinh[x]^2)^{1/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sinh[x] - \tanh[x]}, x, 3, 0 \right\}$$

$$-\frac{1}{4} \coth\left[\frac{x}{2}\right]^2 + \frac{1}{2} \log\left[\tanh\left[\frac{x}{2}\right]\right]$$

$$-\frac{1}{4} \operatorname{csch}\left[\frac{x}{2}\right]^2 \left(1 - \log\left[\cosh\left[\frac{x}{2}\right]\right] + \cosh[x] \left(\log\left[\cosh\left[\frac{x}{2}\right]\right] - \log\left[\sinh\left[\frac{x}{2}\right]\right] \right) + \log\left[\sinh\left[\frac{x}{2}\right]\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(\coth[x]^2 + \operatorname{csch}[x]^2)^2}, x, 8, 0 \right\}$$

$$x - \frac{\operatorname{ArcTanh}\left[\sqrt{2} \coth[x]\right]}{\sqrt{2}} + \frac{\coth[x]}{1 - 2 \coth[x]^2}$$

$$\frac{(3 + \cosh[2x]) \operatorname{csch}[x]^4 \left(6x + 2x \cosh[2x] - \sqrt{2} \operatorname{ArcTanh}\left[\frac{\tanh[x]}{\sqrt{2}}\right] (3 + \cosh[2x]) - 2 \sinh[2x] \right)}{8 (\coth[x]^2 + \operatorname{csch}[x]^2)^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a + b \cosh[x] + c \sinh[x])^4}, x, 4, 0 \right\}$$

$$-\frac{c \cosh[x] + b \sinh[x]}{3 (a^2 - b^2 + c^2) (a + b \cosh[x] + c \sinh[x])^3} -$$

$$\frac{6a (2a^2 + 3b^2 - 3c^2) \operatorname{ArcTanh}\left[\frac{c - (a-b) \tanh\left[\frac{x}{2}\right]}{\sqrt{a^2 - b^2 + c^2}}\right] + \frac{\sqrt{a^2 - b^2 + c^2} (c \cosh[x] + b \sinh[x]) (5a (a^2 - b^2 + c^2) + (11a^2 + 4(b^2 - c^2)) (a + b \cosh[x] + c \sinh[x]))}{(a + b \cosh[x] + c \sinh[x])^2}}{6 (a^2 - b^2 + c^2)^{7/2}}$$

$$-\frac{a (2a^2 + 3b^2 - 3c^2) \operatorname{ArcTan}\left[\frac{c + (-a+b) \tanh\left[\frac{x}{2}\right]}{\sqrt{-a^2 + b^2 - c^2}}\right]}{(-a^2 + b^2 - c^2)^{7/2}} -$$

$$\frac{1}{24b (a^2 - b^2 + c^2)^3 (a + b \cosh[x] + c \sinh[x])^3} (-44a^5c - 82a^3b^2c - 24ab^4c + 82a^3c^3 + 48ab^2c^3 - 24ac^5 -$$

$$30a^2bc (2a^2 + 3b^2 - 3c^2) \cosh[x] - 6ac (a^2 (-7b^2 + 11c^2) + 2(b^4 + b^2c^2 - 2c^4)) \cosh[2x] + 22a^2b^3c \cosh[3x] +$$

$$8b^5c \cosh[3x] - 22a^2b^3c^3 \cosh[3x] - 16b^3c^3 \cosh[3x] + 8b^5c^5 \cosh[3x] + 72a^4b^2 \sinh[x] - 9a^2b^4 \sinh[x] +$$

$$12b^6 \sinh[x] - 132a^4c^2 \sinh[x] - 72a^2b^2c^2 \sinh[x] - 36b^4c^2 \sinh[x] + 81a^2c^4 \sinh[x] + 36b^2c^4 \sinh[x] -$$

$$12c^6 \sinh[x] + 54a^3b^3 \sinh[2x] + 6ab^5 \sinh[2x] - 78a^3b^3c^2 \sinh[2x] - 48ab^3c^2 \sinh[2x] + 42abc^4 \sinh[2x] +$$

$$11a^2b^4 \sinh[3x] + 4b^6 \sinh[3x] - 4b^4c^2 \sinh[3x] - 11a^2c^4 \sinh[3x] - 4b^2c^4 \sinh[3x] + 4c^6 \sinh[3x])$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a + a \cosh[x] + c \sinh[x]}, x, 1, 0 \right\}$$

$$\frac{\log\left[a + c \tanh\left[\frac{x}{2}\right]\right]}{c}$$

$$\frac{-\log\left[\cosh\left[\frac{x}{2}\right]\right] + \log\left[-a \cosh\left[\frac{x}{2}\right] - c \sinh\left[\frac{x}{2}\right]\right]}{c}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a + a \cosh[x] + c \sinh[x])^2}, x, 2, 0 \right\}$$

$$\frac{a \log[a + c \tanh[\frac{x}{2}]]}{c^3} - \frac{c \cosh[x] + a \sinh[x]}{c^2 (a + a \cosh[x] + c \sinh[x])}$$

$$\frac{2 a \left(-\log[\cosh[\frac{x}{2}]] + \log[-a \cosh[\frac{x}{2}] - c \sinh[\frac{x}{2}]] \right) + \frac{c (-a^2 + c^2) \sinh[\frac{x}{2}]}{a (a \cosh[\frac{x}{2}] + c \sinh[\frac{x}{2}])} - c \tanh[\frac{x}{2}]}{2 c^3}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a + a \cosh[x] + c \sinh[x])^4}, x, 4, 0 \right\}$$

$$-\frac{c \cosh[x] + a \sinh[x]}{3 c^2 (a + a \cosh[x] + c \sinh[x])^3} + \frac{3 a (5 a^2 - 3 c^2) \log[a + c \tanh[\frac{x}{2}]] - \frac{c (c \cosh[x] + a \sinh[x]) (5 a c^2 + (15 a^2 - 4 c^2) (a + a \cosh[x] + c \sinh[x]))}{(a + a \cosh[x] + c \sinh[x])^2}}{6 c^7}$$

$$\frac{1}{384 c^7} \left(192 (-5 a^3 + 3 a c^2) \log[\cosh[\frac{x}{2}]] + 192 a (5 a^2 - 3 c^2) \log[a \cosh[\frac{x}{2}] + c \sinh[\frac{x}{2}]] - \right.$$

$$\frac{1}{a (a \cosh[\frac{x}{2}] + c \sinh[\frac{x}{2}])^3} c \operatorname{sech}[\frac{x}{2}]^3 (-150 a^5 c + 130 a^3 c^3 - 24 a c^5 + (-75 a^5 c + 75 a^3 c^3 + 12 a c^5) \cosh[x] +$$

$$6 a c (25 a^4 - 15 a^2 c^2 + 4 c^4) \cosh[2 x] + 75 a^5 c \cosh[3 x] - 35 a^3 c^3 \cosh[3 x] + 4 a c^5 \cosh[3 x] +$$

$$150 a^6 \sinh[x] - 255 a^4 c^2 \sinh[x] + 129 a^2 c^4 \sinh[x] - 12 c^6 \sinh[x] + 120 a^6 \sinh[2 x] - 72 a^4 c^2 \sinh[2 x] +$$

$$\left. 36 a^2 c^4 \sinh[2 x] + 30 a^6 \sinh[3 x] + 37 a^4 c^2 \sinh[3 x] - 27 a^2 c^4 \sinh[3 x] + 4 c^6 \sinh[3 x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^4}, x, 4, 0 \right\}$$

$$\frac{c \cosh[x] + b \sinh[x]}{7 \sqrt{b^2 - c^2} \left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^4} + \frac{3 (c \cosh[x] + b \sinh[x])}{35 (b^2 - c^2) \left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^3} +$$

$$\frac{2 (c \cosh[x] + b \sinh[x])}{35 (b^2 - c^2)^{3/2} \left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^2} - \frac{2 \left(c + \sqrt{b^2 - c^2} \sinh[x] \right)}{35 c (b^2 - c^2)^{3/2} (c \cosh[x] + b \sinh[x])}$$

$$\frac{1}{1120 (-b^2 c + c^3) (c \cosh[x] + b \sinh[x])^7}$$

$$\left(-832 b^4 c \sqrt{b^2 - c^2} + 1664 b^2 c^3 \sqrt{b^2 - c^2} - 832 c^5 \sqrt{b^2 - c^2} + 1190 b c (b^2 - c^2)^2 \cosh[x] + \right.$$

$$448 c \sqrt{b^2 - c^2} (-b^4 + c^4) \cosh[2 x] + 112 b^5 c \cosh[3 x] + 56 b^3 c^3 \cosh[3 x] - 168 b c^5 \cosh[3 x] - 28 b^5 c \cosh[5 x] +$$

$$28 b c^5 \cosh[5 x] + 6 b^5 c \cosh[7 x] + 20 b^3 c^3 \cosh[7 x] + 6 b c^5 \cosh[7 x] - 35 b^6 \sinh[x] + 1295 b^4 c^2 \sinh[x] -$$

$$2485 b^2 c^4 \sinh[x] + 1225 c^6 \sinh[x] - 896 b^3 c^2 \sqrt{b^2 - c^2} \sinh[2 x] + 896 b c^4 \sqrt{b^2 - c^2} \sinh[2 x] +$$

$$21 b^6 \sinh[3 x] + 189 b^4 c^2 \sinh[3 x] - 161 b^2 c^4 \sinh[3 x] - 49 c^6 \sinh[3 x] - 7 b^6 \sinh[5 x] - 35 b^4 c^2 \sinh[5 x] +$$

$$\left. 35 b^2 c^4 \sinh[5 x] + 7 c^6 \sinh[5 x] + b^6 \sinh[7 x] + 15 b^4 c^2 \sinh[7 x] + 15 b^2 c^4 \sinh[7 x] + c^6 \sinh[7 x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{(a + b \cosh[x] + c \sinh[x])^{5/2}, x, 5, 0\}$$

$$\frac{16}{15} a (c \cosh[x] + b \sinh[x]) \sqrt{a + b \cosh[x] + c \sinh[x]} + \frac{2}{5} (c \cosh[x] + b \sinh[x]) (a + b \cosh[x] + c \sinh[x])^{3/2} +$$

$$2 i (23 a^2 + 9 (b^2 - c^2)) \operatorname{EllipticE}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{a + b \cosh[x] + c \sinh[x]}$$

$$15 \sqrt{\frac{a + b \cosh[x] + c \sinh[x]}{a - \sqrt{b^2 - c^2}}}$$

$$16 i a (a^2 - b^2 + c^2) \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{\frac{a + b \cosh[x] + c \sinh[x]}{a - \sqrt{b^2 - c^2}}}$$

$$15 \sqrt{a + b \cosh[x] + c \sinh[x]}$$

$$\sqrt{a + b \cosh[x] + c \sinh[x]} \left(\frac{2 b (23 a^2 + 9 b^2 - 9 c^2)}{15 c} + \frac{22}{15} a c \cosh[x] + \frac{2}{5} b c \cosh[2 x] + \frac{22}{15} a b \sinh[x] + \frac{1}{5} (b^2 + c^2) \sinh[2 x] \right) +$$

$$\left(2 a^3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}\right] \operatorname{Sech}\left[\right.$$

$$x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \sqrt{-1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]}$$

$$\sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \right) /$$

$$\left(\sqrt{1 - \frac{b^2}{c^2}} c \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right)$$

$$\begin{aligned}
& \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} + \\
& \left(34 a b^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right] \operatorname{Sech} \left[\right. \right. \\
& \quad \left. \left. x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \sqrt{-1 + i \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \sqrt{1 + i \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \right. \\
& \quad \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \right) / \\
& \left(15 \sqrt{1 - \frac{b^2}{c^2}} c \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \\
& \quad \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} -
\end{aligned}$$

$$\begin{aligned}
& \left(34 a c \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}\right] \operatorname{Sech}\left[\right. \\
& \quad \left. x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \sqrt{-1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \\
& \quad \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \right) / \\
& \left(15 \sqrt{1 - \frac{b^2}{c^2}} \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right. \\
& \quad \left. \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) - \\
& \frac{1}{15 c} 23 a^2 b^2 \left(\left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \\
& \left. \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) \bigg/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right) \\
& \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \\
& \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \bigg/ \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} - \\
& \frac{1}{5c} 3b^4 \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)} \right] \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right. \\
& \left. \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \right. \\
& \left. \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right. \\
& \left. - \frac{c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}\right]}{15} a^2 c \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right. \\
& \left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \\
& \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \left(- \frac{2b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right)}{b^2 - c^2} + \frac{c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right) + \\
& \frac{6}{5} b^2 c \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)} \right] \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right. \\
& \left. \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) / \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right) \\
& \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}}
\end{aligned}$$

$$\begin{aligned}
& \left(\sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}}} - \frac{2b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right) - \\
& \frac{3}{5} c^3 \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}\right] \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right. \\
& \left. \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) / \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right) \\
& \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \\
& \left(\sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}}} - \frac{2b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right) - \\
& \frac{3}{5} c^3 \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}\right] \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right. \\
& \left. \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) / \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a + b \cosh[x] + c \sinh[x])^{3/2}, x, 4, 0 \right\}$$

$$\begin{aligned}
& -\frac{2}{3} (c \cosh[x] + b \sinh[x]) \sqrt{a + b \cosh[x] + c \sinh[x]} + \\
& \frac{8 i a \operatorname{EllipticE}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{a + b \cosh[x] + c \sinh[x]}}{3 \sqrt{\frac{a + b \cosh[x] + c \sinh[x]}{a - \sqrt{b^2 - c^2}}}} - \\
& \frac{2 i (a^2 - b^2 + c^2) \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{\frac{a + b \cosh[x] + c \sinh[x]}{a - \sqrt{b^2 - c^2}}}}{3 \sqrt{a + b \cosh[x] + c \sinh[x]}} \\
& \left(\frac{8 a b}{3 c} + \frac{2}{3} c \cosh[x] + \frac{2}{3} b \sinh[x] \right) \sqrt{a + b \cosh[x] + c \sinh[x]} + \\
& \left(2 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right] \operatorname{Sech}\left[\right. \right. \\
& \left. \left. x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \sqrt{-1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \right. \\
& \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \right) \right. \\
& \left. \left(\sqrt{1 - \frac{b^2}{c^2}} c \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} + \\
& \left(2 b^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right] \operatorname{Sech} \left[\right. \right. \\
& \left. \left. x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \sqrt{-1 + i \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \sqrt{1 + i \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \right. \\
& \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \right) / \\
& \left(3 \sqrt{1 - \frac{b^2}{c^2}} c \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right. \\
& \left. \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left(2 c \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right) \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right) \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right] \operatorname{Sech} \left[\right. \right. \\
& \quad \left. \left. x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \sqrt{-1 + i \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \sqrt{1 + i \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right]} \right. \\
& \quad \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right) \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right) \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \right) / \\
& \quad \left(3 \sqrt{1 - \frac{b^2}{c^2}} \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right) \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \\
& \quad \left. \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right) \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) - \\
& \quad \frac{1}{3 c} 4 a b^2 \left(c \operatorname{AppellF1} \left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right)}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right)}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)} \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \\
& \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \Bigg/ \left(b\sqrt{1-\frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right. \\
& \sqrt{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}} \\
& \sqrt{1 - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}} - \frac{2b \left(a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}}{b^2 - c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}} \\
& \frac{4}{3} a c \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}, \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}\right] \right. \\
& \sqrt{-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}}
\end{aligned}$$

$$\left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right. \\ \left. \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \right. \\ \left. \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2 b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right. \\ \left. - \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{\sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}, x, 1, 0 \right\}$$

$$2 i \operatorname{EllipticE}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}$$

$$\sqrt{\frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a - \sqrt{b^2 - c^2}}}$$

$$\frac{2 b \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}}{c} +$$

$$\left(2 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}\right] \operatorname{Sech}\left[\right.$$

$$\begin{aligned}
 & \left(x + \operatorname{ArcTanh}\left[\frac{b}{c}\right] \right) \sqrt{-1 + i \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \\
 & \sqrt{\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \sqrt{\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right) / \\
 & \left(\sqrt{1 - \frac{b^2}{c^2}} c \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \\
 & \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) - \\
 & \frac{1}{c} b^2 \left(\left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)} \right) \right. \\
 & \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) \bigg/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right. \\
& \left. \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \right. \\
& \left. \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2 b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right. \\
& \left. - \frac{c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}\right]}{\sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right)
\end{aligned}$$

$$\left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right)$$

$$\sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}}$$

$$\sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}}, x, 1, 0 \right\}$$

$$\frac{2 \operatorname{I} \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 \operatorname{I} (x + \operatorname{I} \operatorname{ArcTan}[\operatorname{I} c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{\frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a - \sqrt{b^2 - c^2}}}}{\sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}}$$

$$\frac{1}{\sqrt{1 - \frac{b^2}{c^2}} c} {}_2\operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, \frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a + \operatorname{I} \sqrt{1 - \frac{b^2}{c^2}} c}, \frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a - \operatorname{I} \sqrt{1 - \frac{b^2}{c^2}} c}\right] \operatorname{Sech}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]$$

$$\sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]} \sqrt{\frac{(b^2 - c^2) \left(1 - \operatorname{I} \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{b^2 - \operatorname{I} a \sqrt{1 - \frac{b^2}{c^2}} c - c^2}} \sqrt{\frac{(b^2 - c^2) \left(1 + \operatorname{I} \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]\right)}{b^2 + \operatorname{I} a \sqrt{1 - \frac{b^2}{c^2}} c - c^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x])^{3/2}}, x, 2, 0 \right\}$$

$$-\frac{2 (c \operatorname{Cosh}[x] + b \operatorname{Sinh}[x])}{(a^2 - b^2 + c^2) \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}} +$$

$$\frac{2 \operatorname{I} \operatorname{EllipticE}\left[\frac{1}{4} (\pi - 2 \operatorname{I} (x + \operatorname{I} \operatorname{ArcTan}[\operatorname{I} c, b])), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}}{(a^2 - b^2 + c^2) \sqrt{\frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a - \sqrt{b^2 - c^2}}}}$$

$$\begin{aligned}
& \sqrt{a + b \cosh[x] + c \sinh[x]} \left(-\frac{2(b^2 - c^2)}{b c (-a^2 + b^2 - c^2)} + \frac{2(a c - b^2 \sinh[x] + c^2 \sinh[x])}{b(a^2 - b^2 + c^2)(a + b \cosh[x] + c \sinh[x])} \right) + \\
& \left(2 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}\right] \operatorname{Sech}\left[\right. \right. \\
& \left. \left. x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \sqrt{-1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \right. \\
& \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \right) / \\
& \left(\sqrt{1 - \frac{b^2}{c^2}} c (a^2 - b^2 + c^2) \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \\
& \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) - \\
& \frac{1}{c(a^2 - b^2 + c^2)} b^2 \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)} \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \\
& \left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) \bigg/ \left(b\sqrt{1-\frac{c^2}{b^2}} \sqrt{-1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right. \\
& \sqrt{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}} \\
& \left. \sqrt{1 - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}} - \frac{2b\left(a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2-c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}} \right. \\
& \left. - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{\sqrt{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right}}} \right) + \\
& \frac{1}{a^2-b^2+c^2} c \left(\left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)}, \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}} \left(-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}}\right)} \right] \right. \right. \\
& \left. \sqrt{-1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \right. \\
& \left. \left. \sqrt{1 + \frac{a}{b\sqrt{1-\frac{c^2}{b^2}}} - \frac{a+b\sqrt{1-\frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b\sqrt{1-\frac{c^2}{b^2}}}} \sqrt{1 - \frac{c^2}{b^2}} \right) \right)
\end{aligned}$$

$$\left. \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right/ \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right. \\ \left. \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \right. \\ \left. \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2 b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \operatorname{Cosh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x])^{5/2}}, x, 5, 0 \right\} \\ - \frac{2 (c \operatorname{Cosh}[x] + b \operatorname{Sinh}[x])}{3 (a^2 - b^2 + c^2) (a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x])^{3/2}} - \frac{1}{3 (a^2 - b^2 + c^2)} 2 \left(\frac{2 (-2 a c \operatorname{Cosh}[x] - 2 a b \operatorname{Sinh}[x])}{(-a^2 + b^2 - c^2) \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}} + \right. \\ \left. \frac{4 i a \operatorname{EllipticE}\left[\frac{1}{2} \left(\frac{\pi}{2} - i (x + i \operatorname{ArcTan}[i c, b])\right), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}}{(-a^2 + b^2 - c^2) \sqrt{\frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a - \sqrt{b^2 - c^2}}}} + \right. \\ \left. \frac{4 i \left(-a^2 b + \frac{1}{2} b \left(\frac{3 a^2}{2} + \frac{b^2}{2} - \frac{c^2}{2}\right)\right) \operatorname{EllipticF}\left[\frac{1}{2} \left(\frac{\pi}{2} - i (x + i \operatorname{ArcTan}[i c, b])\right), \frac{2}{1 - \frac{a}{\sqrt{b^2 - c^2}}}\right] \sqrt{\frac{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}{a - \sqrt{b^2 - c^2}}}}{b (-a^2 + b^2 - c^2) \sqrt{a + b \operatorname{Cosh}[x] + c \operatorname{Sinh}[x]}} \right)$$

$$\begin{aligned}
& \sqrt{a + b \cosh[x] + c \sinh[x]} \\
& \left(\frac{8 a (b^2 - c^2)}{3 b c (a^2 - b^2 + c^2)^2} - \frac{2 (-a c + b^2 \sinh[x] - c^2 \sinh[x])}{3 b (a^2 - b^2 + c^2) (a + b \cosh[x] + c \sinh[x])^2} - \frac{2 (-3 a^2 c - b^2 c + c^3 + 4 a b^2 \sinh[x] - 4 a c^2 \sinh[x])}{3 b (-a^2 + b^2 - c^2)^2 (a + b \cosh[x] + c \sinh[x])} \right) + \\
& \left(2 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}\right] \operatorname{Sech}\left[\right. \right. \\
& \left. \left. x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \sqrt{-1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \right. \\
& \left. \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \sqrt{1 + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}} \right) / \\
& \left(\sqrt{1 - \frac{b^2}{c^2}} c (a^2 - b^2 + c^2)^2 \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \\
& \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) + \\
& \left(2 b^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right)\right)}{\sqrt{1 - \frac{b^2}{c^2}} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c}\right) c}\right] \operatorname{Sech}\left[\right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left(x + \operatorname{ArcTanh}\left[\frac{b}{c}\right] \right) \sqrt{-1 + i \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \\
& \sqrt{\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{1 + \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{1 + \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \Bigg/ \\
& \left(3 \sqrt{1 - \frac{b^2}{c^2}} c \left(a^2 - b^2 + c^2 \right)^2 \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right. \right. \\
& \left. \left. \sqrt{1 - \frac{b^2}{c^2}} c \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) \right) - \right. \\
& \left. \left(2 c \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{3}{2}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}, -\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right] \operatorname{Sech}\left[\right. \right. \\
& \left. \left. x + \operatorname{ArcTanh}\left[\frac{b}{c}\right] \right] \sqrt{-1 + i \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{1 + i \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \sqrt{a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right]} \right. \\
& \left. \sqrt{\frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{1 + \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \left(-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c}} \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \operatorname{Sinh}\left[x + \operatorname{ArcTanh}\left[\frac{b}{c}\right]\right] \right)}{1 + \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \left(1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} \right) c} \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left(3 \sqrt{1 - \frac{b^2}{c^2}} \left(a^2 - b^2 + c^2 \right)^2 \sqrt{-1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) \right. \\
& \left. \sqrt{1 - \frac{i a}{\sqrt{1 - \frac{b^2}{c^2}} c} + \frac{i \left(a + \sqrt{1 - \frac{b^2}{c^2}} c \sinh \left[x + \operatorname{ArcTanh} \left[\frac{b}{c} \right] \right] \right)}{\sqrt{1 - \frac{b^2}{c^2}} c}} \right) - \frac{1}{3 c \left(a^2 - b^2 + c^2 \right)^2} \right. \\
& 4 a b^2 \left(c \operatorname{AppellF1} \left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)} \right] \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right. \\
& \left. \sinh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right] \right) / \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]} \sqrt{1 - \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]} \right. \\
& \left. \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh \left[x + \operatorname{ArcTanh} \left[\frac{c}{b} \right] \right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)}} \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}}} - \frac{2 b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right) + \frac{1}{3 \left(a^2 - b^2 + c^2\right)^2} \\
& 4 a c \left(c \operatorname{AppellF1}\left[-\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}, \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}\right] \right. \\
& \left. \sqrt{-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \sqrt{1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}} - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}}} \right. \\
& \left. \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right] \right) / \left(b \sqrt{1 - \frac{c^2}{b^2}} \sqrt{-1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \right) \\
& \sqrt{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]} \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(-1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} \\
& \sqrt{1 - \frac{a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}} \left(1 + \frac{a}{b \sqrt{1 - \frac{c^2}{b^2}}}\right)}} - \frac{2 b \left(a + b \sqrt{1 - \frac{c^2}{b^2}} \cosh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]\right)}{b^2 - c^2} + \frac{c \sinh\left[x + \operatorname{ArcTanh}\left[\frac{c}{b}\right]\right]}{b \sqrt{1 - \frac{c^2}{b^2}}} \right)
\end{aligned}$$

Timed out after 60 seconds:

$$\begin{aligned}
& \left\{ \left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^{5/2}, x, 3, 0 \right\} \\
& \frac{64 \left(b^2 - c^2\right) \left(c \cosh[x] + b \sinh[x]\right)}{15} + \frac{16}{15} \sqrt{b^2 - c^2} \left(c \cosh[x] + b \sinh[x]\right) \sqrt{\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]} + \\
& 15 \sqrt{\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]} \\
& \frac{2}{5} \left(c \cosh[x] + b \sinh[x]\right) \left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]\right)^{3/2}
\end{aligned}$$

???

Timed out after 60 seconds:

$$\left\{ \left(\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^{3/2}, x, 2, 0 \right\}$$

$$\frac{8 \sqrt{b^2 - c^2} (c \cosh[x] + b \sinh[x])}{3 \sqrt{\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}} + \frac{2}{3} (c \cosh[x] + b \sinh[x]) \sqrt{\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}$$

???

Timed out after 60 seconds:

$$\left\{ \sqrt{\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}, x, 1, 0 \right\}$$

$$\frac{2 (c \cosh[x] + b \sinh[x])}{\sqrt{\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}}$$

???

Timed out after 60 seconds:

$$\left\{ \left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^{5/2}, x, 3, 0 \right\}$$

$$\frac{64 (b^2 - c^2) (c \cosh[x] + b \sinh[x])}{15 \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}} - \frac{16}{15} \sqrt{b^2 - c^2} (c \cosh[x] + b \sinh[x]) \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]} +$$

$$\frac{2}{5} (c \cosh[x] + b \sinh[x]) \left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^{3/2}$$

???

Timed out after 60 seconds:

$$\left\{ \left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x] \right)^{3/2}, x, 2, 0 \right\}$$

$$- \frac{8 \sqrt{b^2 - c^2} (c \cosh[x] + b \sinh[x])}{3 \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}} + \frac{2}{3} (c \cosh[x] + b \sinh[x]) \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}$$

???

Timed out after 60 seconds:

$$\left\{ \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}, x, 1, 0 \right\}$$

$$\frac{2 (c \cosh[x] + b \sinh[x])}{\sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}}$$

???

Simplify::infd: Expression

$$2 \sqrt{b^2 - c^2} \left(\frac{\sqrt{-\sqrt{\text{Plus}[\ll 2 \gg]} + b \cosh[x] + c \sinh[x]} \left(c + \sqrt{\text{Power}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]} \sinh[x] \right)}{4 c \sqrt{b^2 - c^2} (c \cosh[x] + b \sinh[x])} + \right. \\ \left. \frac{1}{8 c \sqrt{b^2 - c^2}} \left(- \left(2 i c \sqrt{\text{Power}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]} \text{EllipticF}[\text{ArcSin}[\text{Times}[\ll 2 \gg]], 2 \text{Power}[\ll 2 \gg] \text{Power}[\ll 2 \gg]] \right. \right. \right. \\ \left. \left. \left. \sqrt{\text{Power}[\ll 2 \gg] \text{Plus}[\ll 3 \gg]} \sqrt{\text{Power}[\ll 2 \gg] \text{Plus}[\ll 3 \gg]} \sqrt{\text{Power}[\ll 2 \gg] \text{Plus}[\ll 3 \gg]} \right) / \left((\text{Times}[\ll 3 \gg] + \right. \right. \right. \\ \left. \left. \left. \text{Times}[\ll 3 \gg]) \sqrt{\text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]} \right) - \frac{2 b \text{Power}[\ll 2 \gg] + i c \text{Plus}[\ll 2 \gg]}{\sqrt{\text{Power}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]}} \right) \right) \right)$$

simplified to Indeterminate. >>

$$\text{Simplify::infd: Expression } 2 \left(\left((c \cosh[x] + b \sinh[x]) \left(-c \sqrt{\text{Power}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]} - b^2 \sinh[x] + c^2 \sinh[x] \right) \left(\frac{b \cosh[x] \sqrt{\text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]}}{(\text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg])^2} + \right. \right. \right. \\ \left. \left. \frac{c \sinh[x] \sqrt{\text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]}}{(\text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg])^2} \right) \right) / \left(4 c \sqrt{b^2 - c^2} (b \cosh[x] + c \sinh[x]) \right) - \left((c \cosh[x] \right. \\ \left. + b \sinh[x])^2 \left(\frac{b \cosh[x] \sqrt{\ll 1 \gg}}{(\ll 1 \gg)^2} + \frac{c \sinh[x] \sqrt{\ll 1 \gg}}{(\ll 1 \gg)^2} \right) \left(\left(6 i c (b^2 - \text{Power}[\ll 2 \gg]) \text{EllipticF}[\text{ArcSin}[\text{Times} \right. \right. \right. \\ \left. \left. \left. [\ll 2 \gg]], 2 \text{Power}[\ll 2 \gg] \text{Power}[\ll 2 \gg]] \sqrt{\text{Power}[\ll 2 \gg] \text{Plus}[\ll 3 \gg]} \sqrt{\text{Power}[\ll 2 \gg] \text{Plus}[\ll 3 \gg]} \right. \right. \right. \\ \left. \left. \left. \sqrt{\text{Power}[\ll 2 \gg] \text{Plus}[\ll 3 \gg]} \right) / \left((\text{Times}[\ll 3 \gg] + \text{Times}[\ll 3 \gg]) \right. \right. \right. \\ \left. \left. \left. \sqrt{\text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]} \right) + \right. \right. \\ \left. \left. \frac{(-\text{Power}[\ll 2 \gg] + c^2) (2 b \text{Power}[\ll 2 \gg] + i c \text{Plus}[\ll 2 \gg])}{\text{Power}[\ll 2 \gg] + \text{Times}[\ll 2 \gg]} \right) \right) / \left(8 c \sqrt{b^2 - c^2} (b \cosh[x] + c \sinh[x]) \right) \right) \left. \right) \left. \right) \sqrt{-\sqrt{\text{Plus}[\ll 2 \gg]} + b \cosh[x] + c \sinh[x]} \right) \text{ simplified to Indeterminate. >>}$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}}, x, 1, 0 \right\}$$

$$\frac{i \sqrt{2} \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), 1\right] \sqrt{\frac{\sqrt{b^2 - c^2} - b \cosh[x] - c \sinh[x]}{\sqrt{b^2 - c^2}}}}{\sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}}$$

$$\int \frac{1}{\sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}} dx$$

Timed out after 60 seconds:

$$\left\{ \frac{1}{\left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]\right)^{3/2}}, x, 2, 0 \right\}$$

$$-\frac{c \cosh[x] + b \sinh[x]}{2 \sqrt{b^2 - c^2} \left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]\right)^{3/2}} - \frac{i \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), 1\right] \sqrt{\frac{\sqrt{b^2 - c^2} - b \cosh[x] - c \sinh[x]}{\sqrt{b^2 - c^2}}}}{2 \sqrt{2} \sqrt{b^2 - c^2} \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}}$$

???

Timed out after 60 seconds:

$$\left\{ \frac{1}{\left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]\right)^{5/2}}, x, 3, 0 \right\}$$

$$-\frac{c \cosh[x] + b \sinh[x]}{4 \sqrt{b^2 - c^2} \left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]\right)^{5/2}} + \frac{3 (c \cosh[x] + b \sinh[x])}{16 (b^2 - c^2) \left(-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]\right)^{3/2}} +$$

$$\frac{3 i \operatorname{EllipticF}\left[\frac{1}{4} (\pi - 2 i (x + i \operatorname{ArcTan}[i c, b])), 1\right] \sqrt{\frac{\sqrt{b^2 - c^2} - b \cosh[x] - c \sinh[x]}{\sqrt{b^2 - c^2}}}}{16 \sqrt{2} (b^2 - c^2) \sqrt{-\sqrt{b^2 - c^2} + b \cosh[x] + c \sinh[x]}}$$

???

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x}{a + b \cosh[x] \sinh[x]}, x, 9, 0 \right\}$$

$$\frac{x \operatorname{Log}\left[1 + \frac{b e^{2x}}{2 a - \sqrt{4 a^2 + b^2}}\right]}{\sqrt{4 a^2 + b^2}} - \frac{x \operatorname{Log}\left[1 + \frac{b e^{2x}}{2 a + \sqrt{4 a^2 + b^2}}\right]}{\sqrt{4 a^2 + b^2}} + \frac{\operatorname{PolyLog}\left[2, -\frac{b e^{2x}}{2 a - \sqrt{4 a^2 + b^2}}\right]}{2 \sqrt{4 a^2 + b^2}} - \frac{\operatorname{PolyLog}\left[2, -\frac{b e^{2x}}{2 a + \sqrt{4 a^2 + b^2}}\right]}{2 \sqrt{4 a^2 + b^2}}$$

$$\begin{aligned}
& \frac{1}{2} \left(-\frac{\mathrm{i} \pi \operatorname{ArcTanh}\left[\frac{-b+2a \operatorname{Tanh}[x]}{\sqrt{4a^2+b^2}}\right]}{\sqrt{4a^2+b^2}} - \frac{1}{\sqrt{-4a^2-b^2}} \left(2 \operatorname{ArcCos}\left[-\frac{2\mathrm{i}a}{b}\right] \operatorname{ArcTanh}\left[\frac{(2a+\mathrm{i}b) \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] + \right. \right. \\
& \quad \left. \left. (\pi-4\mathrm{i}x) \operatorname{ArcTanh}\left[\frac{(2a-\mathrm{i}b) \operatorname{Tan}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] - \left(\operatorname{ArcCos}\left[-\frac{2\mathrm{i}a}{b}\right] + 2\mathrm{i} \operatorname{ArcTanh}\left[\frac{(2a+\mathrm{i}b) \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] \right) \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[\frac{(2\mathrm{i}a+b) \left(-2\mathrm{i}a+b+\sqrt{-4a^2-b^2}\right) \left(1+\mathrm{i} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)}{b \left(2\mathrm{i}a+b+\mathrm{i}\sqrt{-4a^2-b^2} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)} \right] - \right. \right. \\
& \quad \left. \left. \left(\operatorname{ArcCos}\left[-\frac{2\mathrm{i}a}{b}\right] - 2\mathrm{i} \operatorname{ArcTanh}\left[\frac{(2a+\mathrm{i}b) \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] \right) \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[\frac{(2\mathrm{i}a+b) \left(2\mathrm{i}a-b+\sqrt{-4a^2-b^2}\right) \left(\mathrm{i}+\operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)}{b \left(2a-\mathrm{i}b+\sqrt{-4a^2-b^2} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)} \right] + \right. \right. \\
& \quad \left. \left. \left(\operatorname{ArcCos}\left[-\frac{2\mathrm{i}a}{b}\right] - 2\mathrm{i} \operatorname{ArcTanh}\left[\frac{(2a+\mathrm{i}b) \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] - 2\mathrm{i} \operatorname{ArcTanh}\left[\frac{(2a-\mathrm{i}b) \operatorname{Tan}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] \right) \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[-\frac{(-1)^{3/4} \sqrt{-4a^2-b^2} e^{-x}}{2 \sqrt{-\mathrm{i}b} \sqrt{a+b \operatorname{Cosh}[x] \operatorname{Sinh}[x]}} \right] + \right. \right. \\
& \quad \left. \left. \left(\operatorname{ArcCos}\left[-\frac{2\mathrm{i}a}{b}\right] + 2\mathrm{i} \left(\operatorname{ArcTanh}\left[\frac{(2a+\mathrm{i}b) \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] + \operatorname{ArcTanh}\left[\frac{(2a-\mathrm{i}b) \operatorname{Tan}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]}{\sqrt{-4a^2-b^2}}\right] \right) \right. \right. \\
& \quad \left. \left. \operatorname{Log}\left[\frac{(-1)^{1/4} \sqrt{-4a^2-b^2} e^x}{2 \sqrt{-\mathrm{i}b} \sqrt{a+b \operatorname{Cosh}[x] \operatorname{Sinh}[x]}} \right] + \right. \right. \\
& \quad \left. \left. \mathrm{i} \left(\operatorname{PolyLog}\left[2, \frac{\left(2\mathrm{i}a+\sqrt{-4a^2-b^2}\right) \left(2\mathrm{i}a+b-\mathrm{i}\sqrt{-4a^2-b^2} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)}{b \left(2\mathrm{i}a+b+\mathrm{i}\sqrt{-4a^2-b^2} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)} \right] - \right. \right. \\
& \quad \left. \left. \operatorname{PolyLog}\left[2, \frac{\left(2a+\mathrm{i}\sqrt{-4a^2-b^2}\right) \left(-2a+\mathrm{i}b+\sqrt{-4a^2-b^2} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)}{b \left(2\mathrm{i}a+b+\mathrm{i}\sqrt{-4a^2-b^2} \operatorname{Cot}\left[\frac{1}{4}(\pi+4\mathrm{i}x)\right]\right)} \right] \right) \right) \right) \right)
\end{aligned}$$

Miscellaneous problems involving hyperbolic functions

Incorrect antiderivative:

$$\begin{aligned}
& \left\{ \frac{\text{Tanh}[x]^5}{\sqrt{a+b \text{Tanh}[x]^2+c \text{Tanh}[x]^4}}, x, 9, 0 \right\} \\
& \frac{b \text{ArcTanh}\left[\frac{b+2 c \text{Tanh}[x]^2}{2 \sqrt{c} \sqrt{a+b \text{Tanh}[x]^2+c \text{Tanh}[x]^4}}\right]}{4 c^{3/2}} - \frac{\text{ArcTanh}\left[\frac{b+2 c \text{Tanh}[x]^2}{2 \sqrt{c} \sqrt{a+b \text{Tanh}[x]^2+c \text{Tanh}[x]^4}}\right]}{2 \sqrt{c}} + \\
& \frac{\text{ArcTanh}\left[\frac{2 a+b+(b+2 c) \text{Tanh}[x]^2}{2 \sqrt{a+b+c} \sqrt{a+b \text{Tanh}[x]^2+c \text{Tanh}[x]^4}}\right]}{2 \sqrt{a+b+c}} - \frac{\sqrt{a+b \text{Tanh}[x]^2+c \text{Tanh}[x]^4}}{2 c} \\
& - \frac{\sqrt{\frac{3 a-b+3 c+4 a \text{Cosh}[2 x]-4 c \text{Cosh}[2 x]+a \text{Cosh}[4 x]+b \text{Cosh}[4 x]+c \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]}}}{2 c} + \\
& \left(- \left(2 \sqrt{\left(\frac{3 a}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} - \frac{b}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{3 c}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \right. \right. \right. \\
& \quad \frac{4 a \text{Cosh}[2 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} - \frac{4 c \text{Cosh}[2 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{a \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \\
& \quad \left. \frac{b \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{c \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} \right) \text{Sinh}[2 x] \Bigg) / \\
& (3 a-b+3 c+4 a \text{Cosh}[2 x]-4 c \text{Cosh}[2 x]+a \text{Cosh}[4 x]+b \text{Cosh}[4 x]+c \text{Cosh}[4 x]) + \\
& \left(2 b \sqrt{\left(\frac{3 a}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} - \frac{b}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{3 c}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \right. \right. \\
& \quad \frac{4 a \text{Cosh}[2 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} - \frac{4 c \text{Cosh}[2 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{a \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \\
& \quad \left. \frac{b \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{c \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} \right) \text{Sinh}[2 x] \Bigg) / \\
& (c(3 a-b+3 c+4 a \text{Cosh}[2 x]-4 c \text{Cosh}[2 x]+a \text{Cosh}[4 x]+b \text{Cosh}[4 x]+c \text{Cosh}[4 x])) + \\
& \left(\sqrt{\left(\frac{3 a}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} - \frac{b}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{3 c}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \right. \right. \\
& \quad \frac{4 a \text{Cosh}[2 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} - \frac{4 c \text{Cosh}[2 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{a \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \\
& \quad \left. \frac{b \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} + \frac{c \text{Cosh}[4 x]}{3+4 \text{Cosh}[2 x]+\text{Cosh}[4 x]} \right) \text{Sinh}[4 x] \Bigg) / \\
& (3 a-b+3 c+4 a \text{Cosh}[2 x]-4 c \text{Cosh}[2 x]+a \text{Cosh}[4 x]+b \text{Cosh}[4 x]+c \text{Cosh}[4 x]) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left((b-c) (1 + \cosh[2x]) \sqrt{\frac{3a-b+3c+(4a-4c)\cosh[2x] + (a+b+c)\cosh[4x]}{(1+\cosh[2x])^2}} \right. \\
& (3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \operatorname{Csch}[x] \operatorname{Log}[b+2c\tanh[x]^2 + \\
& 2\sqrt{c} \sqrt{a+b\tanh[x]^2 + c\tanh[x]^4}] \operatorname{Sech}[x] \left(\frac{b\operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \right. \\
& \frac{c\operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \\
& \left. \frac{c\cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \Bigg) \Bigg/ \\
& \left(8\sqrt{2}\sqrt{c} (b-c+c\cosh[2x]) \sqrt{3a-b+3c+(4a-4c)\cosh[2x] + (a+b+c)\cosh[4x]} \right. \\
& \left. \sqrt{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \operatorname{Sech}[x]^4} \right) + \\
& \left(c\cosh[2x] (3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \left(2a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \\
& \left. 2c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b+4c+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+ \right. \right.} \right. \\
& \left. \left. c\cosh[4x]) + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\right. \right. \\
& \left. \left((b+2c)\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \Bigg/ \right. \\
& \left. \left(2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \left. \left. b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg] +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]}+\right.\right. \\
& \quad b \sqrt{3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]}+ \\
& \quad c \sqrt{3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]}+\sqrt{a+b+c} \\
& \quad \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.} \\
& \quad \left. b\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right. \\
& \quad \left. c\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)\right)\right] \Bigg) \\
& \operatorname{Sech}[x]^2 \left(\frac{b \operatorname{Sech}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c+4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} - \right. \\
& \quad \frac{c \operatorname{Sech}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c+4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} + \\
& \quad \left. \frac{c \operatorname{Cosh}[2 x] \operatorname{Sech}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c+4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} \right) \\
& \left. (4 a \operatorname{Sinh}[2 x]-4 c \operatorname{Sinh}[2 x]+2 a \operatorname{Sinh}[4 x]+2 b \operatorname{Sinh}[4 x]+2 c \operatorname{Sinh}[4 x]) \right) / \\
& \left(32(b-c+c \operatorname{Cosh}[2 x]) \sqrt{3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]} \right. \\
& \quad \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.} \\
& \quad \left. b\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right. \\
& \quad \left. c\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)\right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c}\left(-4 a-2 b+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.}\right.\right.} \\
& \quad \left. \left. c \operatorname{Cosh}[4 x]\right)+b\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.} \\
& \quad \left. c\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)\right)\right) \Bigg) \\
& \quad \left(-2 a+2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.}\right.} \\
& \quad \left. \left. c \operatorname{Cosh}[4 x]\right)+b\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.} \\
& \quad \left. \left. c\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)\right)\right) \Bigg) \sqrt{\left(-1+\frac{1}{2(a+b+c)}\right.} \\
& \quad \left(-2 a+2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.}\right.} \\
& \quad \left. \left. c \operatorname{Cosh}[4 x]\right)+b\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)+\right.} \\
& \quad \left. \left. c\left(3 a-b+3 c+4 a \operatorname{Cosh}[2 x]-4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]\right)\right)\right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \left(c \left(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b+2c)\sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]}}{2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])})}\right]}{\sqrt{a+b+c}} \right. \\
& \left. + \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + b \sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + c \sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \sqrt{a+b+c} \sqrt{(2b^2-8ac+a(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])})}\right] \right] \operatorname{Sech}[x]^2 \right) \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \\
& \left(32(b-c+c \cosh[2x]) \sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} \right. \\
& \left. + \sqrt{(2b^2-8ac+a(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])} \right. \\
& \left. + \frac{1}{a+b+c} \left(-4a-2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])} \right) \right) \\
& \left(-2a+2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])} \right)
\end{aligned}$$

$$\begin{aligned}
& b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \Big) \\
& \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(-2 a + 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right.} \right. \\
& \quad b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \\
& \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Big) \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(-2 a + 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right.} \right. \\
& \quad b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \\
& \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Big) \Big) \\
& \sqrt{(3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Sech}[x]^4} \Big) - \left((b - c) (1 + \cosh[2 x]) \right. \\
& \sqrt{\frac{3 a - b + 3 c + (4 a - 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x]}{(1 + \cosh[2 x])^2}} \\
& (3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \\
& \operatorname{Log}\left[b + 2 c \tanh[x]^2 + 2 \sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}\right] \\
& \operatorname{Sech}[x]^2 \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} - \right. \\
& \frac{c \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \\
& \left.\frac{c \cosh[2 x] \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) \Big) \Big) \\
& \left(8 \sqrt{2} \sqrt{c} (b - c + c \cosh[2 x]) \sqrt{3 a - b + 3 c + (4 a - 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x]} \right. \\
& \left. \sqrt{(3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Sech}[x]^4} \right) - \\
& \left((b - c) \sqrt{c} (1 + \cosh[2 x]) \sqrt{\frac{3 a - b + 3 c + (4 a - 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x]}{(1 + \cosh[2 x])^2}} \right. \\
& (3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \\
& \operatorname{Csch}[x] \\
& \operatorname{Log}\left[b + 2 c \tanh[x]^2 + 2 \sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}\right] \\
& \operatorname{Sech}[x] \sinh[2 x]
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{b \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \right. \\
& \quad \left. \frac{c \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \quad \left. \frac{c \operatorname{Cosh}[2x] \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \Bigg/ \\
& \left(4 \sqrt{2} (b-c+c \operatorname{Cosh}[2x])^2 \sqrt{3a-b+3c+(4a-4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \right. \\
& \quad \left. \sqrt{(3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Sech}[x]^4} \right) + \\
& \left((b-c) \sqrt{\frac{3a-b+3c+(4a-4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}{(1+\operatorname{Cosh}[2x])^2}} \right. \\
& \quad (3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x] \\
& \quad \operatorname{Log}[b+2c \operatorname{Tanh}[x]^2 + 2\sqrt{c} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}] \\
& \quad \operatorname{Sech}[x] \operatorname{Sinh}[2x] \\
& \quad \left(\frac{b \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \frac{c \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \quad \left. \frac{c \operatorname{Cosh}[2x] \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \Bigg/ \\
& \left(4 \sqrt{2} \sqrt{c} (b-c+c \operatorname{Cosh}[2x]) \sqrt{3a-b+3c+(4a-4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \right. \\
& \quad \left. \sqrt{(3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Sech}[x]^4} \right) - \\
& \left(c^2 \operatorname{Cosh}[2x] (3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \right. \\
& \quad \left(2a \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \right. \\
& \quad 2b \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \\
& \quad \left. 2c \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(2b+4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a \operatorname{Cosh}[2x]-4c \operatorname{Cosh}[2x]+a \operatorname{Cosh}[4x]+b \operatorname{Cosh}[4x]+ \right. \right.} \right. \\
& \quad \left. \left. c \operatorname{Cosh}[4x]) + b(3a-b+3c+4a \operatorname{Cosh}[2x]-4c \operatorname{Cosh}[2x]+a \operatorname{Cosh}[4x]+b \operatorname{Cosh}[4x]+c \operatorname{Cosh}[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c+4a \operatorname{Cosh}[2x]-4c \operatorname{Cosh}[2x]+a \operatorname{Cosh}[4x]+b \operatorname{Cosh}[4x]+c \operatorname{Cosh}[4x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b+2c)\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{(2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])+c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))})\right]}{\right. \\
& \left. \frac{1}{\sqrt{a+b+c}} 2\operatorname{Log}\left[2\left(a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}+b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}+c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}+\sqrt{a+b+c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])+c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))})\right]\right]} \right) \\
& \operatorname{Sech}[x]^2 \sinh[2x] \left(\frac{b\operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} - \frac{c\operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \frac{c\cosh[2x]\operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right) \\
& \left(4a\sinh[2x]-4c\sinh[2x]+2a\sinh[4x]+2b\sinh[4x]+2c\sinh[4x] \right) \Bigg/ \\
& \left(16(b-c+c\cosh[2x])^2 \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])+c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \\
& \left. \sqrt{\left(\frac{1}{a+b+c}\left(-4a-2b+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))}\right.\right.} \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left(\left(\left(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \right) \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \\
& \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \\
& \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \\
& \sqrt{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) + \\
& \left(c(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \left(2a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad 2b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. 2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \\
& \quad c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a \cosh[2x]-4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\right. \right. \\
& \left((b+2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \Bigg/ \\
& \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log} \left[2 \left(a \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \right. \right. \\
& \quad b \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + c \\
& \quad \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \sqrt{a+b+c} \\
& \quad \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad b(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad \left. \left. c(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \Bigg] \\
& \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x] \left(\frac{b \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \right. \\
& \quad \frac{c \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \\
& \quad \left. \frac{c \operatorname{Cosh}[2x] \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \\
& \left. (4a \operatorname{Sinh}[2x] - 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \right) \Bigg/ \\
& \left(16(b-c+c \operatorname{Cosh}[2x]) \sqrt{3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right. \\
& \quad \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad b(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad \left. c(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(-4a - 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \right. \right.} \\
& \quad \quad c \operatorname{Cosh}[4x]) + b(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad \left. \left. c(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \Bigg) \\
& \quad \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \right. \\
& \quad \quad b(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad \left. \left. c(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \\
& \quad \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \right. \\
& \quad \quad \left. \left. b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c+4a \operatorname{Cosh}[2x] - 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left(\left(\left(c \cosh[4x] \right) + c \left(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \right) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \\
& \quad \left. \left. \left. b \cosh[4x] + c \cosh[4x] \right) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \quad \left. \left. \left. c \cosh[4x] \right) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \\
& \sqrt{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{sech}[x]^4} \Bigg) - \left(c \cosh[2x] \right. \\
& \left. \frac{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])}{\left(2a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad \left. \left. 2b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad \left. \left. 2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \\
& \quad \left. \left. \left. c \cosh[4x] \right) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \Bigg) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}} \right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\right. \right. \\
& \quad \left((b + 2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \Bigg] \Bigg/ \\
& \quad \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad \left. \left. b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \right. \right. \\
& \quad \left. \left. \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \quad \left. \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right] \Bigg) \operatorname{sech}[x]^2
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& (4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& (8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) \Bigg) / \\
& \left(64(b-c+c \cosh[2x]) (3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])^{3/2} \right. \\
& \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-4a-2b+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right.} \\
& \quad \left. \left. c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \right. \\
& \quad \left. \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \left(-2a+2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad \left. b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad \left. \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a+2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a+2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \sqrt{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) - \left((b-c)(1+\cosh[2x]) \right. \\
& \left. \sqrt{\frac{3a-b+3c+(4a-4c)\cosh[2x] + (a+b+c)\cosh[4x]}{(1+\cosh[2x])^2}} \right. \\
& \left. (3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right)
\end{aligned}$$

Csch[x]

$$\text{Log}\left[b + 2 c \tanh[x]^2 + 2 \sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}\right]$$

Sech[x]

$$\left(\frac{b \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \frac{c \cosh[2 x] \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) \left((2 (4 a - 4 c) \sinh[2 x] + 4 (a + b + c) \sinh[4 x]) \right) /$$

$$\left(16 \sqrt{2} \sqrt{c} (b - c + c \cosh[2 x]) (3 a - b + 3 c + (4 a - 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x])^{3/2} \right. \\ \left. \sqrt{(3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Sech}[x]^4} \right) +$$

$$\left((b - c) (1 + \cosh[2 x]) \sqrt{\frac{3 a - b + 3 c + (4 a - 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x]}{(1 + \cosh[2 x])^2}} \right)$$

Csch[x]

$$\text{Log}\left[b + 2 c \tanh[x]^2 + 2 \sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}\right]$$

Sech[x]

$$\left(\frac{b \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \frac{c \cosh[2 x] \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) (8 (a - c) \sinh[2 x] + 4 (a + b + c) \sinh[4 x]) /$$

$$\left(8 \sqrt{2} \sqrt{c} (b - c + c \cosh[2 x]) \sqrt{3 a - b + 3 c + (4 a - 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x]} \right. \\ \left. \sqrt{(3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Sech}[x]^4} \right) +$$

$$\left(c \cosh[2 x] \left(2 a \sqrt{3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right. \\ \left. \left. 2 b \sqrt{3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right.$$

$$\begin{aligned} & \left(2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \\ & \sqrt{\left(\frac{1}{a+b+c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\ & \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b + 2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}}\right]} \right) + \\ & \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right] \operatorname{Sech}[x]^2 \right) \\ & \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\ & (4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\ & (8(a - c) \sinh[2x] + 4(a + b + c) \sinh[4x]) \left(\right) \end{aligned}$$

$$\begin{aligned}
& \left(\begin{aligned} & b (3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\ & c (3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \end{aligned} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-4a - 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \sqrt{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) - \left(c \cosh[2x] \right. \\
& \left. \frac{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])}{\left(2a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b + 2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{\sqrt{c}}\right] \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} \right) + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} \right) \right] \operatorname{Sech}[x]^2 \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \left(4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x] \right) + \\
& \left(a(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + b(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + c(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) \right) \Bigg/ \left(128\sqrt{2} (a+b+c) \right) \\
& \left((b - c + c \cosh[2x]) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \left. (2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-4a - 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} \right) \right)} \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} \right) \right)}
\end{aligned}$$

$$\begin{aligned}
& \left(b \cosh[4x] + c \cosh[4x] \right) + b \left(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \\
& \left. c \cosh[4x] \right) + c \left(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \Big) \Big) \\
& \left(1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] \right. \right. \right. \\
& \left. \left. \left. 4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right. \right. \right. \\
& \left. \left. \left. 4x] + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)^{3/2} \\
& \sqrt{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{sech}[x]^4} \Big) - \left(c \cosh[2x] \right. \\
& (3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \left(2a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& 2b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \left. \left. 2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \right. \\
& \left. \left. \left. c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \right. \\
& \left. \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \Big) \Big) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\right. \right. \\
& \left((b + 2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \Big) \Big) \\
& \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) \Big) + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \\
& \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) \Big) +
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{sech}[x]^4} \Bigg) + \left(c\cosh[2x] \right. \\
& \frac{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])}{\left(2a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right.} \\
& \quad 2b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \\
& \quad \left. \left. 2c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} \right. \\
& \quad \left. \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}\right) \right] \right) / \\
& \quad \left(2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right.} \\
& \quad \quad b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \\
& \quad \quad \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} 2\operatorname{Log}\left[2\left(a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \right. \\
& \quad b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + c \\
& \quad \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c} \\
& \quad \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + } \\
& \quad \quad b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \\
& \quad \quad \left. \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \right] \Bigg] \operatorname{sech}[x]^2 \\
& \left(\frac{b\operatorname{sech}[x]^2\sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{c\operatorname{sech}[x]^2\sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \quad \left. \frac{c\cosh[2x]\operatorname{sech}[x]^2\sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& (4a\sinh[2x]-4c\sinh[2x]+2a\sinh[4x]+2b\sinh[4x]+2c\sinh[4x]) \\
& (a(8a\sinh[2x]-8c\sinh[2x]+4a\sinh[4x]+4b\sinh[4x]+4c\sinh[4x]) + \\
& \quad b(8a\sinh[2x]-8c\sinh[2x]+4a\sinh[4x]+4b\sinh[4x]+4c\sinh[4x]) +
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(\frac{1}{a+b+c} \left(2b+4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{1}{\sqrt{c}}\right] \right. \\
& \quad \left. \left((b+2c) \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right) / \\
& \quad \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \\
& \quad \left. + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \Bigg) + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \right. \\
& \quad \left. \left. + b \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + c \right. \right. \\
& \quad \left. \left. \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \quad \left. \left. \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg] \operatorname{Sech}[x]^2 \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \right. \\
& \quad \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right) \\
& \quad (4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& \quad (a(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad b(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad c(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])) \Bigg) / \\
& \left(32\sqrt{2} (b-c+c\cosh[2x]) \sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \quad \left. (2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])) + \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\begin{aligned} & b (3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\ & c (3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \end{aligned} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-4a - 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right)^2 \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \sqrt{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) - \left(c \cosh[2x] \right. \\
& \left. \frac{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])}{\left(2a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}} \right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\right. \right. \\
& \left. \left. \left((b + 2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] \right) /
\end{aligned}$$

$$\begin{aligned}
& \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \quad \left. \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right] \operatorname{Sech}[x]^2 \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \quad \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& (4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& (a(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad b(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad c(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])) \Bigg/ \left(64\sqrt{2} (a+b+c) \right) \\
& (b - c + c \cosh[2x]) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \\
& (2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \\
& \left(\frac{1}{a+b+c} \left(-4a - 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \quad c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right)^{3/2} \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a+2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])\right)\right)} \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a+2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])\right)\right)} \\
& \sqrt{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) - \left(c\cosh[2x]\right. \\
& \left.(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \left.(2a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& \left.2b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& \left.2c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}\right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b+4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])\right)\right)} \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b+2c)\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])}\right]}{\sqrt{a+b+c}} \right. \\
& \left. 2\operatorname{Log}\left[2\left(a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right.\right.\right. \\
& \left.\left.\left.b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c}\right.\right.\right. \\
& \left.\left.\left.\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])\right)\right] + \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{sech}[x]^4} \Bigg) + \left(c\cosh[2x] \right. \\
& (3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b^2+4c+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])} \right. \right. \right. \\
& \quad \left. \left. \left. c\cosh[4x]) + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \right) \Bigg) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}}\operatorname{ArcTanh}\left[\frac{(b+2c)\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])} \right. \right. \right. \\
& \quad \left. \left. \left. b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \right] + \frac{1}{\sqrt{a+b+c}} 2\operatorname{Log}\left[2\left(a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \right. \right. \\
& \quad \left. \left. \left. b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])} \right. \right. \right. \\
& \quad \left. \left. \left. b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \right] \operatorname{sech}[x]^2 \\
& \left(\frac{b\operatorname{sech}[x]^2\sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{c\operatorname{sech}[x]^2\sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \frac{c\cosh[2x]\operatorname{sech}[x]^2\sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& (4a\sinh[2x]-4c\sinh[2x]+2a\sinh[4x]+2b\sinh[4x]+2c\sinh[4x]) \\
& \left(\frac{a(8a\sinh[2x]-8c\sinh[2x]+4a\sinh[4x]+4b\sinh[4x]+4c\sinh[4x])}{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{b (8 a \sinh[2 x] - 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])}{\sqrt{3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}} + \\
& \left. \frac{c (8 a \sinh[2 x] - 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])}{\sqrt{3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}} \right) \Bigg/ \\
& \left(32 (b - c + c \cosh[2 x]) \sqrt{3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right. \\
& \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& \quad c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-4 a - 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right.} \right. \right. \\
& \quad c \cosh[4 x]) + b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& \quad \left. \left. c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right)} \\
& \left(-2 a + 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& \quad \left. \left. c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(-2 a + 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + \right.} \right. \right. \\
& \quad b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \\
& \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right)} \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(-2 a + 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + \right.} \right. \right. \\
& \quad b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \\
& \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c + 4 a \cosh[2 x] - 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right)} \\
& \sqrt{(3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Sech}[x]^4} \Bigg) + \left((b - c) (1 + \cosh[2 x]) \right. \\
& \quad (3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \\
& \quad \operatorname{Csch}[x] \\
& \quad \left. \operatorname{Log}\left[b + 2 c \tanh[x]^2 + 2 \sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4} \right] \right. \\
& \quad \left. \operatorname{Sech}[x] \right. \\
& \quad \left. \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c + 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& \left(- \frac{4(3a-b+3c+(4a-4c)\cosh[2x] + (a+b+c)\cosh[4x])\sinh[2x]}{(1+\cosh[2x])^3} + \right. \\
& \left. \frac{2(4a-4c)\sinh[2x] + 4(a+b+c)\sinh[4x]}{(1+\cosh[2x])^2} \right) \Bigg/ \\
& \left(16\sqrt{2}\sqrt{c}(b-c+c\cosh[2x])\sqrt{3a-b+3c+(4a-4c)\cosh[2x] + (a+b+c)\cosh[4x]} \right. \\
& \sqrt{\frac{3a-b+3c+(4a-4c)\cosh[2x] + (a+b+c)\cosh[4x]}{(1+\cosh[2x])^2}} \\
& \left. \sqrt{(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Sech}[x]^4} \right) + \\
& \left(c \cosh[2x](3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \left(2a\sqrt{3a-b+3c+4a\cosh[2x] - 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c+4a\cosh[2x] - 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \\
& \left. 2c\sqrt{3a-b+3c+4a\cosh[2x] - 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2b+4c+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \left. \left. c\cosh[4x] + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \operatorname{Sech}[x]^2} \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& (4a\sinh[2x] - 4c\sinh[2x] + 2a\sinh[4x] + 2b\sinh[4x] + 2c\sinh[4x]) \\
& \left((8a\sinh[2x] - 8c\sinh[2x] + 4a\sinh[4x] + 4b\sinh[4x] + 4c\sinh[4x]) \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left(4 \sqrt{2} \sqrt{c} \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \left. \left(1 - \frac{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}{8c} \right) \right) - \\
& \left((b+2c) (8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) \right) / \\
& \quad \left(4 \sqrt{c} \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) - \\
& \left((b+2c) \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad (a(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) +} \\
& \quad b(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) +} \\
& \quad \left. c(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) \right) / \\
& \quad \left(4 \sqrt{c} (2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right)^{3/2} \Big) / \\
& \left(\sqrt{c} (1 - ((b+2c)^2 (3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right. \right. \\
& \quad (4c(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \left. \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) + \\
& \left(2 \left(\frac{a(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{2 \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} + \right. \right. \\
& \quad \frac{b(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{2 \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} + \\
& \quad \frac{c(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{2 \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} + \\
& \quad \left. \frac{\sqrt{a+b+c} (a(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) +} \right. \\
& \quad b(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) +} \\
& \quad \left. c(8a \sinh[2x] - 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) \right) \Big) / \\
& \quad \left(2 \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \left. c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Big) \Big) / \\
& \left(\sqrt{a+b+c} \left(a \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad \left. b \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{c \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c}}{\sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}} \right) \Bigg/ \\
& \left(32(b-c+c \cosh[2x]) \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(-4a-2b+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \\
& \quad \left(-2a+2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \\
& \quad \left(-1 + \frac{1}{2(a+b+c)} \left(-2a+2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right) \Bigg) \\
& \quad \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a+2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right) \Bigg) \\
& \quad \sqrt{(3a-b+3c+4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) - \left(c \cosh[2x] \right. \\
& \quad \left. (3a-b+3c+4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \right. \\
& \quad \left(2a \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad \left. 2b \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad \left. 2c \sqrt{3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \\
& \quad \left. \sqrt{\left(\frac{1}{a+b+c} \left(2b+4c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c+4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \right)
\end{aligned}$$

$$\begin{aligned}
& \left(c \cosh[4x] + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg) \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b + 2c)\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{c}\sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}\right]} \right. \\
& \left. + \frac{1}{\sqrt{a + b + c}} 2 \operatorname{Log}\left[2\left(a\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + b\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c}\sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}\right)\right] \operatorname{Sech}[x]^2 \right) \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \left(4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x] \right) \operatorname{Tanh}[x] \Bigg) \\
& \left(16(b - c + c \cosh[2x]) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \left. + \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right. \\
& \left. + \sqrt{\left(\frac{1}{a + b + c} \left(-4a - 2b + \sqrt{2}\sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}\right)\right)} \right)
\end{aligned}$$

$$\begin{aligned}
& \left(c \cosh[4x] + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg) \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \left. b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + \right.} \right. \right. \\
& \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \left. \left. c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + \right.} \right. \right. \\
& \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \left. \left. c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \Bigg) \\
& \sqrt{(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Sech}[x]^4} \Bigg) - \left((b - c)(1 + \cosh[2x]) \right. \\
& \sqrt{\frac{3a - b + 3c + (4a - 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& (3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \operatorname{Csch}[x] \\
& \log[b + 2c \tanh[x]^2 + 2\sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}] \\
& \operatorname{Sech}[x] \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right. \\
& \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& (\operatorname{Sech}[x]^4 (8(a - c) \sinh[2x] + 4(a + b + c) \sinh[4x]) - \\
& 4(3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Sech}[x]^4 \tanh[x]) \Bigg) \Bigg) / \\
& \left(16\sqrt{2} \sqrt{c} (b - c + c \cosh[2x]) \sqrt{3a - b + 3c + (4a - 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \left. ((3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Sech}[x]^4)^{3/2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left(c \cosh[2x] (3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \left(2a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& 2b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \left. \left. 2c \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(2b + 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \operatorname{ArcTanh}\left[\frac{(b + 2c) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}}\right]}{\sqrt{a + b + c}} \right. \\
& \left. 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \right. \\
& \left. \left. b \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \right. \right. \\
& \left. \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right] \right) \operatorname{Sech}[x]^2 \\
& \left(\frac{b \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{c \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Sech}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& (4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x])
\end{aligned}$$

$$\begin{aligned}
& \left(\text{Sech}[x]^4 (8 (a - c) \sinh[2x] + 4 (a + b + c) \sinh[4x]) - \right. \\
& \left. 4 (3a - b + 3c + 4 (a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \text{Sech}[x]^4 \tanh[x] \right) / \\
& \left(64 (b - c + c \cosh[2x]) \sqrt{3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-4a - 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right.} \\
& c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \Bigg) \\
& \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a + b + c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \\
& b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \\
& c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a + b + c)} \left(-2a + 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \\
& b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \\
& c \cosh[4x]) + c(3a - b + 3c + 4a \cosh[2x] - 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \Bigg) \Bigg) \\
& \left((3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \text{Sech}[x]^4 \right)^{3/2} \Bigg) + \left((b - c) (1 + \cosh[2x]) \right. \\
& \sqrt{\frac{3a - b + 3c + (4a - 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& (3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \text{Csch}[x] \\
& \log[b + 2c \tanh[x]^2 + 2\sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}] \\
& \text{Sech}[x] \\
& \left(\frac{2b \cosh[2x] \text{Sech}[x]^2}{\sqrt{3a - b + 3c + 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{2 c \cosh[2 x] \operatorname{sech}[x]^2}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} + \\
& \frac{2 c \cosh[2 x]^2 \operatorname{sech}[x]^2}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} + \\
& \frac{2 c \operatorname{sech}[x]^2 \sinh[2 x]^2}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} - \\
& \frac{b \operatorname{sech}[x]^2 \sinh[2 x] (8(a-c) \sinh[2 x]+4(a+b+c) \sinh[4 x])}{2(3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x])^{3/2}} + \\
& \frac{c \operatorname{sech}[x]^2 \sinh[2 x] (8(a-c) \sinh[2 x]+4(a+b+c) \sinh[4 x])}{2(3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x])^{3/2}} - \\
& \frac{c \cosh[2 x] \operatorname{sech}[x]^2 \sinh[2 x] (8(a-c) \sinh[2 x]+4(a+b+c) \sinh[4 x])}{2(3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x])^{3/2}} - \\
& \frac{2 b \operatorname{sech}[x]^2 \sinh[2 x] \tanh[x]}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} + \\
& \frac{2 c \operatorname{sech}[x]^2 \sinh[2 x] \tanh[x]}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} - \\
& \left. \frac{2 c \cosh[2 x] \operatorname{sech}[x]^2 \sinh[2 x] \tanh[x]}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} \right) \Bigg/ \\
& \left(8 \sqrt{2} \sqrt{c} (b-c+c \cosh[2 x]) \sqrt{3 a-b+3 c+(4 a-4 c) \cosh[2 x]+(a+b+c) \cosh[4 x]} \right. \\
& \left. \sqrt{(3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]) \operatorname{sech}[x]^4} \right) + \\
& \left(c \cosh[2 x] (3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]) \right. \\
& \left(2 a \sqrt{3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]} + \right. \\
& 2 b \sqrt{3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]} + \\
& \left. 2 c \sqrt{3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(2 b+4 c+\sqrt{2} \sqrt{(2 b^2-8 a c+a(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+ \right. \right.} \right. \\
& \left. \left. c \cosh[4 x]) + b(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) + \right. \right. \\
& \left. \left. c(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{\text{ArcTanh}\left[\frac{\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{\sqrt{c}} - \frac{1}{\sqrt{c}} \text{ArcTanh}\left[\frac{(b+2c)\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])})}\right]} \right) \\
& + \frac{1}{\sqrt{a+b+c}} 2 \text{Log}\left[2\left(a\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + b\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + c\sqrt{3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c}\sqrt{(2b^2-8ac+a(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + b(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c(3a-b+3c+4a\cosh[2x]-4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])})}\right]\right]
\end{aligned}$$

$$\text{Sech}[x]^2 (4a \sinh[2x] - 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x])$$

$$\begin{aligned}
& \left(\frac{2b \cosh[2x] \text{Sech}[x]^2}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{2c \cosh[2x] \text{Sech}[x]^2}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \frac{2c \cosh[2x]^2 \text{Sech}[x]^2}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \frac{2c \text{Sech}[x]^2 \sinh[2x]^2}{\sqrt{3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{b \text{Sech}[x]^2 \sinh[2x] (8(a-c)\sinh[2x] + 4(a+b+c)\sinh[4x])}{2(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])^{3/2}} + \frac{c \text{Sech}[x]^2 \sinh[2x] (8(a-c)\sinh[2x] + 4(a+b+c)\sinh[4x])}{2(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])^{3/2}} - \frac{c \cosh[2x] \text{Sech}[x]^2 \sinh[2x] (8(a-c)\sinh[2x] + 4(a+b+c)\sinh[4x])}{2(3a-b+3c+4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])^{3/2}} \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{2 b \operatorname{Sech}[x]^2 \sinh[2 x] \tanh[x]}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} + \\
& \frac{2 c \operatorname{Sech}[x]^2 \sinh[2 x] \tanh[x]}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} - \\
& \left. \frac{2 c \cosh[2 x] \operatorname{Sech}[x]^2 \sinh[2 x] \tanh[x]}{\sqrt{3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]}} \right) \Bigg/ \\
& \left(32(b-c+c \cosh[2 x]) \sqrt{3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]} \right. \\
& \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right.} \\
& \quad b(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) + \\
& \quad \left. c(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right) } \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-4 a-2 b+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+ \right.} \right. \right. \\
& \quad \left. \left. c \cosh[4 x]\right)+b(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right.} \\
& \quad \left. \left. \left. +c(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right) \right) \right) } \\
& \left(-2 a+2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right.} \right. \\
& \quad \left. b(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) + \right. \\
& \quad \left. \left. c(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right) \right) } \\
& \sqrt{\left(-1+\frac{1}{2(a+b+c)} \left(-2 a+2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+ \right.} \right. \right. \\
& \quad \left. \left. b \cosh[4 x]+c \cosh[4 x]\right)+b(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+ \right. \\
& \quad \left. \left. \left. c \cosh[4 x]\right)+c(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right) \right) \right) } \\
& \sqrt{\left(1+\frac{1}{2(a+b+c)} \left(-2 a+2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+ \right.} \right. \right. \\
& \quad \left. \left. b \cosh[4 x]+c \cosh[4 x]\right)+b(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+ \right. \\
& \quad \left. \left. \left. c \cosh[4 x]\right)+c(3 a-b+3 c+4 a \cosh[2 x]-4 c \cosh[2 x]+a \cosh[4 x]+b \cosh[4 x]+c \cosh[4 x]) \right) \right) \right) } \\
& \sqrt{\left(3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x] \right) \operatorname{Sech}[x]^4} \Bigg) + \left((b-c)(1+\cosh[2 x]) \right. \\
& \sqrt{\frac{3 a-b+3 c+(4 a-4 c) \cosh[2 x]+(a+b+c) \cosh[4 x]}{(1+\cosh[2 x])^2}} \\
& (3 a-b+3 c+4(a-c) \cosh[2 x]+(a+b+c) \cosh[4 x]) \\
& \operatorname{Csch}[x] \\
& \operatorname{Sech}[x]
\end{aligned}$$

$$\left(\frac{b \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \frac{c \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \frac{c \operatorname{Cosh}[2x] \operatorname{Sech}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \left(4c \operatorname{Sech}[x]^2 \operatorname{Tanh}[x] + \frac{\sqrt{c} (2b \operatorname{Sech}[x]^2 \operatorname{Tanh}[x] + 4c \operatorname{Sech}[x]^2 \operatorname{Tanh}[x]^3)}{\sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}} \right) \Bigg/ \left(8 \sqrt{2} \sqrt{c} (b-c+c \operatorname{Cosh}[2x]) \sqrt{3a-b+3c+(4a-4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \sqrt{(3a-b+3c+4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Sech}[x]^4} (b+2c \operatorname{Tanh}[x]^2 + 2\sqrt{c} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}) \right)$$

Timed out after 60 seconds:

$$\left\{ \frac{\operatorname{Tanh}[x]^3}{\sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}, x, 7, 0 \right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{b+2c \operatorname{Tanh}[x]^2}{2\sqrt{c} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}\right]}{2\sqrt{c}} + \frac{\operatorname{ArcTanh}\left[\frac{2a+b+(b+2c) \operatorname{Tanh}[x]^2}{2\sqrt{a+b+c} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}\right]}{2\sqrt{a+b+c}}$$

???

Timed out after 60 seconds:

$$\left\{ \frac{\operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}, x, 4, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{2a+b+(b+2c) \operatorname{Tanh}[x]^2}{2\sqrt{a+b+c} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}\right]}{2\sqrt{a+b+c}}$$

???

Unable to integrate:

$$\left\{ \frac{\operatorname{Coth}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}, x, 6, 0 \right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{2a+b \operatorname{Tanh}[x]^2}{2\sqrt{a} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}\right]}{2\sqrt{a}} + \frac{\operatorname{ArcTanh}\left[\frac{2a+b+(b+2c) \operatorname{Tanh}[x]^2}{2\sqrt{a+b+c} \sqrt{a+b \operatorname{Tanh}[x]^2 + c \operatorname{Tanh}[x]^4}}\right]}{2\sqrt{a+b+c}}$$

$$\int \frac{\text{Coth}[x]}{\sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}} dx$$

Timed out after 60 seconds:

$$\left\{ \frac{\text{Coth}[x]^3}{\sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}, x, 9, 0 \right\}$$

$$- \frac{\text{ArcTanh}\left[\frac{2 a + b \tanh[x]^2}{2 \sqrt{a} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}\right]}{2 \sqrt{a}} + \frac{b \text{ArcTanh}\left[\frac{2 a + b \tanh[x]^2}{2 \sqrt{a} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}\right]}{4 a^{3/2}} +$$

$$\frac{\text{ArcTanh}\left[\frac{2 a + b + (b + 2 c) \tanh[x]^2}{2 \sqrt{a + b + c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}\right]}{2 \sqrt{a + b + c}} - \frac{\text{Coth}[x]^2 \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}{2 a}$$

???

Incorrect antiderivative:

$$\left\{ \frac{\text{Coth}[x]^5}{\sqrt{a + b \coth[x]^2 + c \coth[x]^4}}, x, 9, 0 \right\}$$

$$\frac{b \text{ArcTanh}\left[\frac{b + 2 c \coth[x]^2}{2 \sqrt{c} \sqrt{a + b \coth[x]^2 + c \coth[x]^4}}\right]}{4 c^{3/2}} - \frac{\text{ArcTanh}\left[\frac{b + 2 c \coth[x]^2}{2 \sqrt{c} \sqrt{a + b \coth[x]^2 + c \coth[x]^4}}\right]}{2 \sqrt{c}} +$$

$$\frac{\text{ArcTanh}\left[\frac{2 a + b + (b + 2 c) \coth[x]^2}{2 \sqrt{a + b + c} \sqrt{a + b \coth[x]^2 + c \coth[x]^4}}\right]}{2 \sqrt{a + b + c}} - \frac{\sqrt{a + b \coth[x]^2 + c \coth[x]^4}}{2 c}$$

$$- \frac{\sqrt{\frac{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}{3 - 4 \cosh[2 x] + \cosh[4 x]}}}{2 c} +$$

$$\left(\left(2 \sqrt{\left(\frac{3 a}{3 - 4 \cosh[2 x] + \cosh[4 x]} - \frac{b}{3 - 4 \cosh[2 x] + \cosh[4 x]} + \frac{3 c}{3 - 4 \cosh[2 x] + \cosh[4 x]} - \right.} \right. \right.$$

$$\frac{4 a \cosh[2 x]}{3 - 4 \cosh[2 x] + \cosh[4 x]} + \frac{4 c \cosh[2 x]}{3 - 4 \cosh[2 x] + \cosh[4 x]} + \frac{a \cosh[4 x]}{3 - 4 \cosh[2 x] + \cosh[4 x]} +$$

$$\left. \frac{b \cosh[4 x]}{3 - 4 \cosh[2 x] + \cosh[4 x]} + \frac{c \cosh[4 x]}{3 - 4 \cosh[2 x] + \cosh[4 x]} \right) \text{Sinh}[2 x] \Bigg) /$$

$$(3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) -$$

$$\begin{aligned}
& \left(2b \sqrt{\left(\frac{3a}{3-4\cosh[2x]+\cosh[4x]} - \frac{b}{3-4\cosh[2x]+\cosh[4x]} + \frac{3c}{3-4\cosh[2x]+\cosh[4x]} - \right.} \right. \\
& \quad \frac{4a\cosh[2x]}{3-4\cosh[2x]+\cosh[4x]} + \frac{4c\cosh[2x]}{3-4\cosh[2x]+\cosh[4x]} + \frac{a\cosh[4x]}{3-4\cosh[2x]+\cosh[4x]} + \\
& \quad \left. \frac{b\cosh[4x]}{3-4\cosh[2x]+\cosh[4x]} + \frac{c\cosh[4x]}{3-4\cosh[2x]+\cosh[4x]} \right) \sinh[2x] \Bigg/ \\
& \quad (c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])) + \\
& \left(\sqrt{\left(\frac{3a}{3-4\cosh[2x]+\cosh[4x]} - \frac{b}{3-4\cosh[2x]+\cosh[4x]} + \frac{3c}{3-4\cosh[2x]+\cosh[4x]} - \right.} \right. \\
& \quad \frac{4a\cosh[2x]}{3-4\cosh[2x]+\cosh[4x]} + \frac{4c\cosh[2x]}{3-4\cosh[2x]+\cosh[4x]} + \frac{a\cosh[4x]}{3-4\cosh[2x]+\cosh[4x]} + \\
& \quad \left. \frac{b\cosh[4x]}{3-4\cosh[2x]+\cosh[4x]} + \frac{c\cosh[4x]}{3-4\cosh[2x]+\cosh[4x]} \right) \sinh[4x] \Bigg/ \\
& \quad \left. (3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \\
& \left((b-c)(1+\cosh[2x])(3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]) \right. \\
& \quad \sqrt{\frac{3a-b+3c+(-4a+4c)\cosh[2x]+(a+b+c)\cosh[4x]}{(1+\cosh[2x])^2}} \operatorname{Csch}[x] \\
& \quad \left. \left(\log[\sqrt{c}\tanh[x]^2] - \log[2c+b\tanh[x]^2+2\sqrt{c}\sqrt{c+\tanh[x]^2(b+a\tanh[x]^2)}] \right) \right) \\
& \operatorname{Sech}[x] \left(-\frac{b\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \right. \\
& \quad \frac{c\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \\
& \quad \left. \frac{c\cosh[2x]\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right) \Bigg/ \\
& \left(8\sqrt{2}\sqrt{c}(b-c-c\cosh[2x])\sqrt{3a-b+3c+(-4a+4c)\cosh[2x]+(a+b+c)\cosh[4x]} \right. \\
& \quad \left. \sqrt{(3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \right) - \\
& \left(c\cosh[2x](3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]) \right.
\end{aligned}$$

$$\begin{aligned}
& \left(2a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \\
& \left. 2c\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])} \right. \right. \\
& \quad c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}\right)\right] \Big/ \\
& \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])} \right. \\
& \quad b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Big] + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2\left(a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \right. \\
& \quad b\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \\
& \quad c\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c} \\
& \quad \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])} \right. \\
& \quad \left. \left. b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \right] \Big] \\
& \left(-\frac{b\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \right. \\
& \frac{c\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \\
& \left. \frac{c\cosh[2x]\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right)
\end{aligned}$$

$$\begin{aligned}
& \left. (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \right) / \\
& \left(16 (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right. \\
& \quad \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \\
& \quad \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right.} \\
& \quad \quad \quad \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \right. \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \quad \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \\
& \quad \quad \quad \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \quad \left. \left. (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \right.} \\
& \quad \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \\
& \quad \quad \quad \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \right) \\
& \quad \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] +} \right. \right.} \\
& \quad \quad \quad \left. \left. a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \right. \\
& \quad \quad \left. \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \right. \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \right) \\
& \quad \left. \sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Csch}[x]^4} \right) \right) / \\
& \left(- \left(c \cosh[2 x] (-8 a \cosh[2 x] + 8 c \cosh[2 x] + 8 a \cosh[4 x] + 8 b \cosh[4 x] + 8 c \cosh[4 x]) \right. \right. \\
& \quad \left. \left. (3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \right. \right. \\
& \quad \left. \left(2 a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right. \\
& \quad \left. \left. 2 b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \Big) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \quad \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}\right) \right] / \\
& \quad \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Big) + \\
& \quad \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad \left. \left. b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \right. \right. \\
& \quad \left. \left. \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \quad \left. \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right.} \\
& \quad \left. \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) \Big) \\
& \left(- \frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \right. \\
& \quad \frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \\
& \quad \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \Big) \\
& \left(16(b-c-c \cosh[2x]) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) +
\end{aligned}$$

$$\begin{aligned}
& c \left(3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x] \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + \right. \right.} \\
& \quad c \operatorname{Cosh}[4 x]) + b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \right) \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \right. \\
& \quad b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + \right. \right.} \\
& \quad b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \\
& \quad \left. \left. \operatorname{Cosh}[4 x]) + c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \right) \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + \right. \right.} \\
& \quad b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \\
& \quad \left. \left. \operatorname{Cosh}[4 x]) + c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \right) \\
& \sqrt{(3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]) \operatorname{Csch}[x]^4} \Bigg) - \left((b - c) (1 + \operatorname{Cosh}[2 x]) \right. \\
& (3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]) \\
& \sqrt{\frac{3 a - b + 3 c + (-4 a + 4 c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}{(1 + \operatorname{Cosh}[2 x])^2}} \\
& \operatorname{Csch}[x]^2 \\
& \left(\operatorname{Log}[\sqrt{c} \operatorname{Tanh}[x]^2] - \operatorname{Log}[2 c + b \operatorname{Tanh}[x]^2 + 2 \sqrt{c} \sqrt{c + \operatorname{Tanh}[x]^2 (b + a \operatorname{Tanh}[x]^2)}] \right) \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} + \right. \\
& \quad \frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} + \\
& \quad \left. \frac{c \operatorname{Cosh}[2 x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} \right) \Bigg) / \\
& \left(8 \sqrt{2} \sqrt{c} (b - c - c \operatorname{Cosh}[2 x]) \sqrt{3 a - b + 3 c + (-4 a + 4 c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]} \right. \\
& \left. \sqrt{(3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]) \operatorname{Csch}[x]^4} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left((b-c) (1 + \cosh[2x]) (3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \right. \\
& \sqrt{\frac{3a-b+3c+(-4a+4c) \cosh[2x] + (a+b+c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \left. \left(\log[\sqrt{c} \tanh[x]^2] - \log[2c+b \tanh[x]^2 + 2\sqrt{c} \sqrt{c + \tanh[x]^2 (b+a \tanh[x]^2)}] \right) \right. \\
& \operatorname{sech}[x]^2 \\
& \left(-\frac{b \operatorname{csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \right. \\
& \frac{c \operatorname{csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \\
& \left. \frac{c \cosh[2x] \operatorname{csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \Bigg/ \\
& \left(8\sqrt{2} \sqrt{c} (b-c-c \cosh[2x]) \sqrt{3a-b+3c+(-4a+4c) \cosh[2x] + (a+b+c) \cosh[4x]} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \operatorname{csch}[x]^4} \right) + \\
& \left((b-c) \sqrt{c} (1 + \cosh[2x]) (3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \right. \\
& \sqrt{\frac{3a-b+3c+(-4a+4c) \cosh[2x] + (a+b+c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \operatorname{csch}[x] \\
& \left. \left(\log[\sqrt{c} \tanh[x]^2] - \log[2c+b \tanh[x]^2 + 2\sqrt{c} \sqrt{c + \tanh[x]^2 (b+a \tanh[x]^2)}] \right) \right. \\
& \operatorname{sech}[x] \\
& \sinh[2x] \\
& \left(-\frac{b \operatorname{csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \right. \\
& \frac{c \operatorname{csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \\
& \left. \frac{c \cosh[2x] \operatorname{csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \Bigg/ \\
& \left(4\sqrt{2} (b-c-c \cosh[2x])^2 \sqrt{3a-b+3c+(-4a+4c) \cosh[2x] + (a+b+c) \cosh[4x]} \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \Bigg) + \\
& \left((b-c)(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \sqrt{\frac{3a-b+3c+(-4a+4c)\cosh[2x] + (a+b+c)\cosh[4x]}{(1+\cosh[2x])^2}} \\
& \operatorname{Csch}[x] \\
& \left. \left(\operatorname{Log}[\sqrt{c}\tanh[x]^2] - \operatorname{Log}[2c+b\tanh[x]^2+2\sqrt{c}\sqrt{c+\tanh[x]^2(b+a\tanh[x]^2)}] \right) \right) \\
& \operatorname{Sech}[x]\operatorname{Sinh}[2x] \\
& \left(-\frac{b\operatorname{Csch}[x]^2\operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \frac{c\operatorname{Csch}[x]^2\operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \\
& \left. \frac{c\cosh[2x]\operatorname{Csch}[x]^2\operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \Bigg) / \\
& \left(4\sqrt{2}\sqrt{c}(b-c-c\cosh[2x])\sqrt{3a-b+3c+(-4a+4c)\cosh[2x] + (a+b+c)\cosh[4x]} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \right) + \\
& \left(c\cosh[2x](3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \left(2a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \\
& \left. \left. 2c\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])\right.} \right. \right. \\
& \left. \left. c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{Coth}[x]\operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2\sqrt{c}} \operatorname{ArcTanh} \left[\left((b+2c) \sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] / \\
& \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log} \left[2 \left(a \sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad b \sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad c \sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \\
& \quad \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg] \Bigg) \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \right. \\
& \quad \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \\
& (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \Bigg) / \\
& \left(8(b-c-c \cosh[2x]) \sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right)\right)} \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right)\right)} \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left(c^2 \cosh[2x] \right. \\
& \left. \frac{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])}{\left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right)\right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right)\right)} \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \left. \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b + 2c) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}\right)\right] \right) / \\
& \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right) + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \left. \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]))} + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right)\right]
\end{aligned}$$

$$\begin{aligned}
& \left(c (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}} \right]}{2\sqrt{c}} - \right. \\
& \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b + 2c) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] \Bigg/ \\
& \left(2\sqrt{c} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg] + \\
& \frac{1}{\sqrt{a + b + c}} \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \\
& \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg] \sinh[2x] \right) \\
& \left(- \frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right)
\end{aligned}$$

$$\begin{aligned}
& \left. (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \right) / \\
& \left(8 (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right. \\
& \quad \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \\
& \quad \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right.} \\
& \quad \quad \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \right. \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \\
& \quad \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] +} \right. \right.} \right. \\
& \quad \quad \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right. \\
& \quad \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \quad \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] +} \right. \right.} \right. \\
& \quad \quad \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right. \\
& \quad \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \quad \sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Csch}[x]^4} \Bigg) + \left(c \cosh[2 x] \right. \\
& \quad \left. \frac{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x])}{\left(2 a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right.} \right. \\
& \quad \quad \left. \frac{2 b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}{2 c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}} \right) \\
& \quad \sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right.} \right. \\
& \quad \quad \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \right. \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& c \left(3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x] \right) \Big) \Big) \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}}{2 \sqrt{2} \sqrt{c}}\right]}{2 \sqrt{c}} \right. \\
& \frac{1}{2 \sqrt{c}} \operatorname{ArcTanh}\left[\left((b + 2 c) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}\right) \right] \Big) \Big) / \\
& \left(2 \sqrt{c} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} + \right. \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \Big) \Big) + \\
& \frac{1}{\sqrt{a + b + c}} \operatorname{Log}\left[2 \left(a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right. \\
& b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \\
& c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \sqrt{a + b + c} \\
& \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right] \Big) \Big) \\
& \left(- \frac{b \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \frac{c \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \right. \\
& \left. \frac{c \cosh[2 x] \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) \\
& (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\
& (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) \Big) / \\
& \left(32 (b - c - c \cosh[2 x]) (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])^{3/2} \right. \\
& \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \Big) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right. \right.}
\end{aligned}$$

$$\begin{aligned}
& \left(\left(\left(c \cosh[4x] \right) + b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) + \right. \right. \\
& \left. \left. c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \Bigg) \\
& \left(2a - 2c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right. \right. \\
& \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right. \right. \\
& \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \Bigg) \\
& \sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]} \operatorname{Csch}[x]^4 \Bigg) + \left((b - c) (1 + \cosh[2x]) \right. \\
& \left. \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \right. \\
& \operatorname{Csch}[x] \\
& \left(\operatorname{Log}[\sqrt{c} \tanh[x]^2] - \operatorname{Log}[2c + b \tanh[x]^2 + 2\sqrt{c} \sqrt{c + \tanh[x]^2 (b + a \tanh[x]^2)}] \right) \\
& \operatorname{Sech}[x] \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \left(-8(a - c) \sinh[2x] + 4(a + b + c) \sinh[4x] \right) \Bigg) / \\
& \left(8\sqrt{2} \sqrt{c} (b - c - c \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \left. \sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]} \operatorname{Csch}[x]^4 \right) -
\end{aligned}$$

$$\begin{aligned}
& \left(c \cosh[2x] \left(2a \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \right. \right. \\
& \quad 2b \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \\
& \quad \left. \left. 2c \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]))} \right. \right. \\
& \quad c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \quad \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c) \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} \right) \right] / \\
& \quad \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]))} + \right. \\
& \quad b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) \right) \right] + \\
& \quad \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \right. \right. \\
& \quad b \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \\
& \quad c \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \sqrt{a+b+c} \\
& \quad \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]))} + \\
& \quad b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& \quad \left. \left. \left. c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) \right) \right) \right] \right) \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} + \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} + \right. \\
& \quad \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} \right) \\
& (-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x])
\end{aligned}$$

$$\begin{aligned}
& \left. (-8 (a - c) \sinh[2 x] + 4 (a + b + c) \sinh[4 x]) \right) / \\
& \left(16 (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right. \\
& \quad \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \\
& \quad \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right.} \\
& \quad \quad \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \right. \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \quad \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \quad b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \\
& \quad \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \\
& \quad \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] +} \right. \right.} \\
& \quad \quad \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right. \\
& \quad \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \quad \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] +} \right. \right.} \\
& \quad \quad \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right. \\
& \quad \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right) \\
& \quad \sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Csch}[x]^4} \Bigg) - \left((b - c) (1 + \cosh[2 x]) \right. \\
& \quad (3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \\
& \quad \left. \sqrt{\frac{3 a - b + 3 c + (-4 a + 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x]}{(1 + \cosh[2 x])^2}} \right. \\
& \quad \operatorname{Csch}[x] \\
& \quad \left(\log[\sqrt{c} \tanh[x]^2] - \log[2 c + b \tanh[x]^2 + 2 \sqrt{c} \sqrt{c + \tanh[x]^2 (b + a \tanh[x]^2)}] \right) \\
& \quad \operatorname{Sech}[x] \\
& \quad \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& \left(2(-4a+4c)\operatorname{Sinh}[2x] + 4(a+b+c)\operatorname{Sinh}[4x] \right) \Bigg/ \\
& \left(16\sqrt{2}\sqrt{c}(b-c-c\cosh[2x])(3a-b+3c+(-4a+4c)\cosh[2x] + (a+b+c)\cosh[4x])^{3/2} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \right) + \\
& \left(c \cosh[2x] (3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \left(2a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \\
& \left. \left. 2c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \right. \\
& \left. \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x])} \right. \right. \right.} \\
& \quad \left. \left. \left. c\cosh[4x] + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right. \right. \\
& \quad \left. \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \right) \Bigg) \\
& \operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}\right)\right] \Bigg/ \\
& \left(2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x])} + \right. \\
& \quad \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \quad \left. \left. b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \quad \left. \left. c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \quad \left. \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x])} \right) \right] +
\end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \Big) \Bigg] \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \frac{c \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \right. \\
& \left. \frac{c \cosh[2 x] \operatorname{Csch}[x]^2 \sinh[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) \\
& (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\
& (a (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& b (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])) \Bigg) \Bigg/ \left(64 \sqrt{2} (a + b + c) \right. \\
& (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \\
& (2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \Bigg) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right.} \right. \\
& \left. \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right.} \right. \\
& \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \\
& \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \Bigg) \\
& \left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right.} \right. \\
& \left. \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg)^{3/2}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \Bigg) + \left(c\cosh[2x] \right. \\
& \left. \frac{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])}{\left(2a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \left. \left. 2b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \left. \left. 2c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + \right. \right.} \right. \\
& \left. \left. c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \left. \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}\right)\right] \right) / \\
& \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right.} \\
& \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \Bigg) + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \left. \left. b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \left. \left. c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \left. \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right.} \\
& \left. \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \Bigg] \\
& \left(-\frac{b\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \frac{c\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{c\cosh[2x]\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right)
\end{aligned}$$

$$\begin{aligned}
& (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\
& (a (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& b (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])) \Bigg) / \left(64 \sqrt{2} (a + b + c) \right. \\
& (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \\
& (2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right.} \right. \\
& c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \Bigg) \Bigg)} \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right.} \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \Bigg) \\
& \left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x] \right. \right.} \right. \\
& 4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x] + c \cosh[4 x] + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \Bigg) \Bigg)^{3/2} \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right.} \right. \\
& b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \\
& c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \Bigg) \Bigg)} \\
& \sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Csch}[x]^4} \Bigg) + \left(c \cosh[2 x] \right. \\
& (3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \\
& \left(2 a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \\
& 2 b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \\
& 2 c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \Bigg) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right.} \right.}
\end{aligned}$$

$$\begin{aligned}
& c \cosh[4x] + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \Big) \Big) \\
& \operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} \right) \right] \Big/ \\
& \left(2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \right. \\
& b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) \Big)} \Big) + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2\left(a\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \right. \right. \\
& b\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \\
& c\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \sqrt{a+b+c} \\
& \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) \Big)} \Big) \Big] \Big) \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} + \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} \right) \\
& (-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& (a(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& b(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& c(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])) \Big/ \\
& \left(16\sqrt{2}(b-c-c \cosh[2x])\sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} \right. \\
& (2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) \Big)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \\
& \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \\
& \quad \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + c \right. \\
& \quad \left. (3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \Bigg)^2 \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+ \right. \right. \\
& \quad \left. \left. b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+ \right. \right. \\
& \quad \left. \left. c\cosh[4x]) + c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+ \right. \right. \\
& \quad \left. \left. b\cosh[4x]+c\cosh[4x]))} + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+ \right. \right. \\
& \quad \left. \left. c\cosh[4x]) + c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \sqrt{(3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \Bigg) - \left(c\cosh[2x] \right. \\
& \quad \left. (3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]) \right. \\
& \quad \left(2a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& \quad \left. 2b\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \\
& \quad \left. \left. 2c\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right) \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}} \right]}{2\sqrt{c}} - \right. \\
& \quad \left. \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right] \right) / \\
& \quad \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} + \right. \\
& \quad \left. b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \Bigg) + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& b \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \\
& c \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} + \sqrt{a+b+c} \\
& \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) +} \\
& \quad b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) +} \\
& \quad c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) \Bigg] \Bigg) \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} + \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} + \right. \\
& \quad \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x]+(a+b+c) \cosh[4x]}} \right) \\
& (-4a \sinh[2x]+4c \sinh[2x]+2a \sinh[4x]+2b \sinh[4x]+2c \sinh[4x]) \\
& (a(-8a \sinh[2x]+8c \sinh[2x]+4a \sinh[4x]+4b \sinh[4x]+4c \sinh[4x]) + \\
& \quad b(-8a \sinh[2x]+8c \sinh[2x]+4a \sinh[4x]+4b \sinh[4x]+4c \sinh[4x]) + \\
& \quad c(-8a \sinh[2x]+8c \sinh[2x]+4a \sinh[4x]+4b \sinh[4x]+4c \sinh[4x])) \Bigg) \Bigg/ \left(32 \sqrt{2} (a+b+c) \right) \\
& (b-c-c \cosh[2x]) \sqrt{3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]} \\
& (2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) + \\
& \quad b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \\
& \quad c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) \Bigg) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) +} \right. \right.} \\
& \quad \left. \left. c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) \right) \right) \Bigg) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) +} \right. \right.} \\
& \quad \left. \left. c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) \right) \right) \Bigg) \\
& \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) +} \right. \\
& \quad \left. b(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) \right) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x]+4c \cosh[2x]+a \cosh[4x]+b \cosh[4x]+c \cosh[4x])) +} \right. \right.} \right.}
\end{aligned}$$

$$\begin{aligned}
& \left(b \cosh[4x] + c \cosh[4x] \right) + b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \\
& \left. c \cosh[4x] \right) + c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \Big) \Big) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{\left(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \right. \\
& \left. \left. \left. b \cosh[4x] + c \cosh[4x] \right) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \\
& \left. \left. \left. c \cosh[4x] \right) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) \Big) \\
& \sqrt{\left(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x] \right) \operatorname{Csch}[x]^4} \Big) + \left(c \cosh[2x] \right. \\
& \left. \frac{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])}{\left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b - 4c + \sqrt{2} \sqrt{\left(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \right. \\
& \left. \left. \left. c \cosh[4x] \right) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \right. \\
& \left. \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \Big) \Big) \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{c}} \right]}{2\sqrt{c}} - \right. \\
& \left. \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b + 2c) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] \right) / \\
& \left(2\sqrt{c} \sqrt{\left(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Big) + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \left. \left. \sqrt{\left(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \right. \\
& \left. \left. \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \Bigg) + \left(c\cosh[2x] \right. \\
& (3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \\
& \left(2a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \\
& \left. \left. 2c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + \right. \right.} \right. \\
& \left. \left. c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{Csch}[x]^2 \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \frac{1}{2\sqrt{c}} \operatorname{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}\right)\right] \Bigg) \\
& \left(2\sqrt{c} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right.} \\
& \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \Bigg) + \\
& \frac{1}{\sqrt{a+b+c}} \operatorname{Log}\left[2\left(a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \\
& c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \sqrt{a+b+c} \\
& \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right.} \\
& \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \Bigg] \\
& \left(-\frac{b\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \frac{c\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{c\cosh[2x]\operatorname{Csch}[x]^2\sinh[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right)
\end{aligned}$$

$$\begin{aligned}
& (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\
& (a (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& b (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) +
\end{aligned}$$

$$c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) \Bigg) /$$

$$\left(32 (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right.$$

$$\begin{aligned}
& (2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \Big)^{3/2}
\end{aligned}$$

$$\sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right) \right) \Bigg)}$$

$$\begin{aligned}
& (2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \Bigg)
\end{aligned}$$

$$\sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right) \right) \Bigg)}$$

$$\sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right) \right) \Bigg)}$$

$$\sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Csch}[x]^4} \Bigg) - \left(c \cosh[2 x] \right.$$

$$(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x])$$

$$\sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right) \right) \Bigg)}$$

$$\begin{aligned}
& \text{Csch}[x]^2 \left(-\frac{\text{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{c}}\right]}{2\sqrt{c}} - \right. \\
& \frac{1}{2\sqrt{c}} \text{ArcTanh}\left[\left((b+2c)\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}\right)\right] \Big/ \\
& \left(2\sqrt{c}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+}\right. \\
& \quad b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])+ \\
& \quad \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))\right) \Big) + \\
& \frac{1}{\sqrt{a+b+c}} \text{Log}\left[2\left(a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \right.\right. \\
& \quad b\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \\
& \quad c\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c} \\
& \quad \left.\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+}\right. \\
& \quad \left. b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])+}\right. \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))\right)\right] \Big) \\
& \left(-\frac{b\text{Csch}[x]^2\text{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \frac{c\text{Csch}[x]^2\text{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \right. \\
& \quad \left. \frac{c\cosh[2x]\text{Csch}[x]^2\text{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right) \\
& (-4a\text{Sinh}[2x]+4c\text{Sinh}[2x]+2a\text{Sinh}[4x]+2b\text{Sinh}[4x]+2c\text{Sinh}[4x]) \\
& \left(\frac{a(-8a\text{Sinh}[2x]+8c\text{Sinh}[2x]+4a\text{Sinh}[4x]+4b\text{Sinh}[4x]+4c\text{Sinh}[4x])}{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}} + \right. \\
& \quad \frac{b(-8a\text{Sinh}[2x]+8c\text{Sinh}[2x]+4a\text{Sinh}[4x]+4b\text{Sinh}[4x]+4c\text{Sinh}[4x])}{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}} + \\
& \quad \left. \frac{c(-8a\text{Sinh}[2x]+8c\text{Sinh}[2x]+4a\text{Sinh}[4x]+4b\text{Sinh}[4x]+4c\text{Sinh}[4x])}{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}} \right) \Big/ \\
& \left(16(b-c-c\cosh[2x])\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \quad \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))+}\right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])}{\sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)}} \right. \\
& \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \\
& \left. \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \right) \\
& \left. \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])} \right) \right)} \right) \right) \\
& \sqrt{(3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left((b-c)(1+\cosh[2x]) \right. \\
& \left. \frac{(3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x])}{\sqrt{\frac{3a-b+3c+(-4a+4c) \cosh[2x] + (a+b+c) \cosh[4x]}{(1+\cosh[2x])^2}}} \right. \\
& \operatorname{Csch}[x] \\
& \left. \left(\operatorname{Log}[\sqrt{c} \tanh[x]^2] - \operatorname{Log}[2c+b \tanh[x]^2 + 2\sqrt{c} \sqrt{c+\tanh[x]^2(b+a \tanh[x]^2)}] \right) \right) \\
& \operatorname{Sech}[x] \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \right. \\
& \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \\
& (-4(3a-b+3c-4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]) \coth[x] \operatorname{Csch}[x]^4 +
\end{aligned}$$

$$\begin{aligned}
& \left(-\frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \quad \left. \frac{c \operatorname{Cosh}[2x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2x]}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \\
& (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \\
& (-4(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Coth}[x] \operatorname{Csch}[x]^4 + \\
& \quad \operatorname{Csch}[x]^4 (-8(a-c) \operatorname{Sinh}[2x] + 4(a+b+c) \operatorname{Sinh}[4x])) \Bigg) / \\
& \left(32(b-c-c \operatorname{Cosh}[2x]) \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right. \\
& \quad \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \\
& \quad b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \\
& \quad c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]))} \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \right) \right)} \\
& \left(2a-2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right.} \\
& \quad \left. b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \right) \\
& \quad \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + \right. \right.} \right. \\
& \quad \left. \left. b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + \right. \right. \\
& \quad \left. \left. c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \right) \right)} \\
& \quad \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + \right. \right.} \right. \\
& \quad \left. \left. b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + \right. \right. \\
& \quad \left. \left. c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \right) \right)} \\
& \left((3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4 \right)^{3/2} \Bigg) + \left((b-c) (1 + \operatorname{Cosh}[2x]) \right. \\
& \quad \left. (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \right)
\end{aligned}$$

$$\sqrt{\frac{3 a-b+3 c+(-4 a+4 c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}{(1+\operatorname{Cosh}[2 x])^2}}$$

Csch[x]

$$\left(\operatorname{Log}\left[\sqrt{c} \operatorname{Tanh}[x]^2\right]-\operatorname{Log}\left[2 c+b \operatorname{Tanh}[x]^2+2 \sqrt{c} \sqrt{c+\operatorname{Tanh}[x]^2(b+a \operatorname{Tanh}[x]^2)}\right]\right)$$

Sech[x]

$$\left(-\frac{2 b \operatorname{Cosh}[2 x] \operatorname{Csch}[x]^2}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}+\frac{2 c \operatorname{Cosh}[2 x] \operatorname{Csch}[x]^2}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}+\frac{2 c \operatorname{Cosh}[2 x]^2 \operatorname{Csch}[x]^2}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}+\frac{2 b \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}-\frac{2 c \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}+\frac{2 c \operatorname{Cosh}[2 x] \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}+\frac{2 c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]^2}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}}+\frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x](-8(a-c) \operatorname{Sinh}[2 x]+4(a+b+c) \operatorname{Sinh}[4 x])}{2(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])^{3/2}}-\frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x](-8(a-c) \operatorname{Sinh}[2 x]+4(a+b+c) \operatorname{Sinh}[4 x])}{2(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])^{3/2}}-\frac{c \operatorname{Cosh}[2 x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x](-8(a-c) \operatorname{Sinh}[2 x]+4(a+b+c) \operatorname{Sinh}[4 x])}{2(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])^{3/2}}\right) /$$

$$\left(8 \sqrt{2} \sqrt{c}(b-c-c \operatorname{Cosh}[2 x]) \sqrt{3 a-b+3 c+(-4 a+4 c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}-\sqrt{(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]) \operatorname{Csch}[x]^4}\right)-$$

$$\left(c \operatorname{Cosh}[2 x](3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])\right)$$

$$\begin{aligned}
& \left(2 a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \\
& 2 b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \\
& \left. 2 c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right.} \\
& \quad \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(- \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}}{2 \sqrt{2} \sqrt{c}}\right]}{2 \sqrt{c}} - \right. \\
& \frac{1}{2 \sqrt{c}} \operatorname{ArcTanh}\left[\left((b + 2 c) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}\right)\right] \Big/ \\
& \left(2 \sqrt{c} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right.} \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \\
& \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \Big] + \\
& \frac{1}{\sqrt{a + b + c}} \operatorname{Log}\left[2 \left(a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right. \\
& \quad \left. b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \\
& \quad \left. c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \sqrt{a + b + c} \right. \\
& \quad \left. \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right.} \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Big] \right) \\
& (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\
& \left(- \frac{2 b \cosh[2 x] \operatorname{Csch}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \right. \\
& \frac{2 c \cosh[2 x] \operatorname{Csch}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \\
& \frac{2 c \cosh[2 x]^2 \operatorname{Csch}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} +
\end{aligned}$$

$$\begin{aligned}
& \frac{2 b \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} - \\
& \frac{2 c \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} - \\
& \frac{2 c \operatorname{Cosh}[2 x] \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} + \\
& \frac{2 c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]^2}{\sqrt{3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x]}} + \\
& \frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x](-8(a-c) \operatorname{Sinh}[2 x]+4(a+b+c) \operatorname{Sinh}[4 x])}{2(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])^{3/2}} - \\
& \frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x](-8(a-c) \operatorname{Sinh}[2 x]+4(a+b+c) \operatorname{Sinh}[4 x])}{2(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])^{3/2}} - \\
& \left. \frac{c \operatorname{Cosh}[2 x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x](-8(a-c) \operatorname{Sinh}[2 x]+4(a+b+c) \operatorname{Sinh}[4 x])}{2(3 a-b+3 c-4(a-c) \operatorname{Cosh}[2 x]+(a+b+c) \operatorname{Cosh}[4 x])^{3/2}} \right) \Bigg/ \\
& \left(16(b-c-c \operatorname{Cosh}[2 x]) \sqrt{3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]} \right. \\
& \quad \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right.} \\
& \quad \quad b(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) + \\
& \quad \quad \left. c(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right) \Bigg) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(4 a+2 b+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+ \right.} \right. \right.} \\
& \quad \quad \quad c \operatorname{Cosh}[4 x]) + b(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) + \\
& \quad \quad \quad \left. \left. c(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right) \right) \Bigg) \Bigg) \\
& \quad \left(2 a-2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right.} \right. \\
& \quad \quad b(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) + \\
& \quad \quad \left. \left. c(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right) \right) \Bigg) \\
& \quad \sqrt{\left(-1+\frac{1}{2(a+b+c)} \left(2 a-2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+ \right.} \right. \right.} \\
& \quad \quad \quad b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) + b(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+ \\
& \quad \quad \quad \left. \left. c \operatorname{Cosh}[4 x]) + c(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right) \right) \Bigg) \Bigg) \\
& \quad \sqrt{\left(1+\frac{1}{2(a+b+c)} \left(2 a-2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+ \right.} \right. \right.} \\
& \quad \quad \quad b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) + b(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+ \\
& \quad \quad \quad \left. \left. c \operatorname{Cosh}[4 x]) + c(3 a-b+3 c-4 a \operatorname{Cosh}[2 x]+4 c \operatorname{Cosh}[2 x]+a \operatorname{Cosh}[4 x]+b \operatorname{Cosh}[4 x]+c \operatorname{Cosh}[4 x]) \right) \right) \Bigg) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. c \cosh[4x] + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \\
& \sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]} \operatorname{Csch}[x]^4 + \left((b - c)(1 + \cosh[2x]) \right. \\
& \left. \operatorname{Csch}[x] \right. \\
& \left. \left(\log[\sqrt{c} \tanh[x]^2] - \log[2c + b \tanh[x]^2 + 2\sqrt{c} \sqrt{c + \tanh[x]^2 (b + a \tanh[x]^2)}] \right) \right. \\
& \left. \operatorname{Sech}[x] \right. \\
& \left. \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \right. \\
& \left. \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \left(-\frac{4(3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]) \sinh[2x]}{(1 + \cosh[2x])^3} + \right. \\
& \left. \frac{2(-4a + 4c) \sinh[2x] + 4(a + b + c) \sinh[4x]}{(1 + \cosh[2x])^2} \right) \Bigg) / \\
& \left(16\sqrt{2}\sqrt{c}(b - c - c \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \left. \sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]} \operatorname{Csch}[x]^4 \right) - \\
& \left(c \cosh[2x] (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2b - 4c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right.}
\end{aligned}$$

$$\begin{aligned}
& c \left(3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x] \right) \Big) \Big) \operatorname{Csch}[x]^2 \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} + \frac{c \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} + \right. \\
& \quad \left. \frac{c \operatorname{Cosh}[2 x] \operatorname{Csch}[x]^2 \operatorname{Sinh}[2 x]}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} \right) \\
& (-4 a \operatorname{Sinh}[2 x] + 4 c \operatorname{Sinh}[2 x] + 2 a \operatorname{Sinh}[4 x] + 2 b \operatorname{Sinh}[4 x] + 2 c \operatorname{Sinh}[4 x]) \\
& \left(-(-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) \right) / \\
& \left(8 \sqrt{2} c \sqrt{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]} \right. \\
& \quad \left. \left(1 - \frac{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]}{8 c} \right) \right) - \\
& \left((b + 2 c) (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) \right) / \\
& \left(4 \sqrt{c} \sqrt{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]} \right. \\
& \quad \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) +} \\
& \quad b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) +} \\
& \quad \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \Big) - \\
& \left((b + 2 c) \sqrt{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]} \right. \\
& \quad (a (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) +} \\
& \quad b (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) +} \\
& \quad \left. c (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) \right) \Big) / \\
& \left(4 \sqrt{c} \left(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \right. \right. \\
& \quad b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) +} \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right)^{3/2} \right) \Big) / \\
& \left(2 \sqrt{c} \left(1 - ((b + 2 c)^2 (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) / \right. \\
& \quad (4 c (2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) +} \\
& \quad b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) +} \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \Big) \right) + \\
& \left(\frac{a (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x])}{2 \sqrt{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]}} + \right. \\
& \quad \left. \frac{b (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x])}{2 \sqrt{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]}} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])}{2 \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}} + \\
& \left(\sqrt{a + b + c} \left(a (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \right. \right. \\
& \quad b (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& \quad \left. \left. c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) \right) \right) / \\
& \left(2 \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \\
& \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \Bigg) / \\
& \left(\sqrt{a + b + c} \left(a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \right. \\
& \quad b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \\
& \quad c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \sqrt{a + b + c} \\
& \quad \left. \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \\
& \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \Bigg) \Bigg) / \\
& \left(16 (b - c - c \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right. \\
& \quad \left. \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \\
& \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] +} \right. \right. \\
& \quad \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) +} \right. \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \\
& \quad \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \\
& \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] +} \right. \right. \\
& \quad \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \\
& \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] +} \right. \right. \\
& \quad \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \\
& \quad \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left(\left(c \cosh[4x] + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} + \left((b - c)(1 + \cosh[2x]) \right. \\
& \left. \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \right. \\
& \left. \operatorname{Csch}[x] \right. \\
& \left. \operatorname{Sech}[x] \right. \\
& \left(-\frac{b \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \frac{c \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \left. \frac{c \cosh[2x] \operatorname{Csch}[x]^2 \sinh[2x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \left(\frac{2b \operatorname{Sech}[x]^2 \tanh[x] + \frac{\sqrt{c}(2a \operatorname{Sech}[x]^2 \tanh[x]^3 + 2 \operatorname{Sech}[x]^2 \tanh[x](b + a \tanh[x]^2))}{\sqrt{c + \tanh[x]^2(b + a \tanh[x]^2)}}}{2 \operatorname{Csch}[x] \operatorname{Sech}[x] - \frac{2c + b \tanh[x]^2 + 2\sqrt{c} \sqrt{c + \tanh[x]^2(b + a \tanh[x]^2)}}}{2c + b \tanh[x]^2 + 2\sqrt{c} \sqrt{c + \tanh[x]^2(b + a \tanh[x]^2)}}} \right) \\
& \left(8\sqrt{2} \sqrt{c} (b - c - c \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \left. \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \right)
\end{aligned}$$

Timed out after 60 seconds:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]^3}{\sqrt{a + b \operatorname{Coth}[x]^2 + c \operatorname{Coth}[x]^4}}, x, 7, 0 \right\} \\
& - \frac{\operatorname{ArcTanh}\left[\frac{b + 2c \operatorname{Coth}[x]^2}{2\sqrt{c} \sqrt{a + b \operatorname{Coth}[x]^2 + c \operatorname{Coth}[x]^4}}\right]}{2\sqrt{c}} + \frac{\operatorname{ArcTanh}\left[\frac{2a + b + (b + 2c) \operatorname{Coth}[x]^2}{2\sqrt{a + b + c} \sqrt{a + b \operatorname{Coth}[x]^2 + c \operatorname{Coth}[x]^4}}\right]}{2\sqrt{a + b + c}}
\end{aligned}$$

???

Timed out after 60 seconds:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Coth}[x]}{\sqrt{a + b \operatorname{Coth}[x]^2 + c \operatorname{Coth}[x]^4}}, x, 4, 0 \right\} \\
& \frac{\operatorname{ArcTanh}\left[\frac{2a + b + (b + 2c) \operatorname{Coth}[x]^2}{2\sqrt{a + b + c} \sqrt{a + b \operatorname{Coth}[x]^2 + c \operatorname{Coth}[x]^4}}\right]}{2\sqrt{a + b + c}}
\end{aligned}$$

???

Unable to integrate:

$$\left\{ \frac{\text{Tanh}[x]}{\sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}, x, 6, 0 \right\}$$

$$- \frac{\text{ArcTanh}\left[\frac{2 a + b \text{Coth}[x]^2}{2 \sqrt{a} \sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}\right]}{2 \sqrt{a}} + \frac{\text{ArcTanh}\left[\frac{2 a + b + (b + 2 c) \text{Coth}[x]^2}{2 \sqrt{a + b + c} \sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}\right]}{2 \sqrt{a + b + c}}$$

$$\int \frac{\text{Tanh}[x]}{\sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}} dx$$

Incorrect antiderivative:

$$\left\{ \frac{\text{Tanh}[x]^3}{\sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}, x, 9, 0 \right\}$$

$$- \frac{\text{ArcTanh}\left[\frac{2 a + b \text{Coth}[x]^2}{2 \sqrt{a} \sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}\right]}{2 \sqrt{a}} + \frac{b \text{ArcTanh}\left[\frac{2 a + b \text{Coth}[x]^2}{2 \sqrt{a} \sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}\right]}{4 a^{3/2}} +$$

$$\frac{\text{ArcTanh}\left[\frac{2 a + b + (b + 2 c) \text{Coth}[x]^2}{2 \sqrt{a + b + c} \sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4}}\right]}{2 \sqrt{a + b + c}} - \frac{\sqrt{a + b \text{Coth}[x]^2 + c \text{Coth}[x]^4} \text{Tanh}[x]^2}{2 a}$$

$$\sqrt{\frac{3 a - b + 3 c - 4 a \text{Cosh}[2 x] + 4 c \text{Cosh}[2 x] + a \text{Cosh}[4 x] + b \text{Cosh}[4 x] + c \text{Cosh}[4 x]}{3 - 4 \text{Cosh}[2 x] + \text{Cosh}[4 x]}} \left(-\frac{1}{2 a} + \frac{\text{Sech}[x]^2}{2 a} \right) +$$

$$\left(\left((-a + b) (1 + \text{Cosh}[2 x]) (3 a - b + 3 c - 4 (a - c) \text{Cosh}[2 x] + (a + b + c) \text{Cosh}[4 x]) \right. \right.$$

$$\sqrt{\frac{3 a - b + 3 c + (-4 a + 4 c) \text{Cosh}[2 x] + (a + b + c) \text{Cosh}[4 x]}{(1 + \text{Cosh}[2 x])^2}} \text{Coth}[x] \text{Csch}[x]^2 \text{Log}\left[\right.$$

$$b + 2 a \text{Tanh}[x]^2 + 2 \sqrt{a} \sqrt{c + b \text{Tanh}[x]^2 + a \text{Tanh}[x]^4} \left. \left(\frac{a \text{Coth}[2 x] \text{Sinh}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \text{Cosh}[2 x] + (a + b + c) \text{Cosh}[4 x]}} - \right. \right.$$

$$\frac{a \text{Csch}[2 x] \text{Sinh}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \text{Cosh}[2 x] + (a + b + c) \text{Cosh}[4 x]}} +$$

$$\left. \left. \frac{b \text{Csch}[2 x] \text{Sinh}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \text{Cosh}[2 x] + (a + b + c) \text{Cosh}[4 x]}} \right) \right) \sqrt{\quad}$$

$$\begin{aligned}
& \left(8 \sqrt{2} \sqrt{a} (-a + b + a \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \quad \left. \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \right) + \\
& \left(a \cosh[2x] (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \quad \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4a + 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2} \sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}\right) \right] / \\
& \left(2\sqrt{a} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) + \\
& \frac{1}{\sqrt{a + b + c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad \left. b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad \left. c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \right. \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right] \left(\frac{a \coth[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{a \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{b \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& \left(-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x] \right) \Bigg/ \\
& \left(32(-a+b+a\cosh[2x]) \sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right. \\
& \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \Bigg) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \right. \right.} \\
& \quad c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \\
& \left(2a-2c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \right. \\
& \quad b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \right.} \\
& \quad \left(2a-2c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \right. \\
& \quad c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] +} \right. \right.} \\
& \quad a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) +} \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \right) \Bigg) \\
& \left(\sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \operatorname{Csch}[x]^4} \right) \Bigg) \\
& \left(- \left(5 \sqrt{\left(\frac{3a}{3-4\cosh[2x] + \cosh[4x]} - \frac{b}{3-4\cosh[2x] + \cosh[4x]} + \frac{3c}{3-4\cosh[2x] + \cosh[4x]} - \right.} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{4 a \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{4 c \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{a \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \\
& \left. \frac{b \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{c \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} \right) \operatorname{Sech}[x] \sinh[3 x] \Bigg) / \\
& \left(2 (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) + \\
& \left(b \sqrt{\left(\frac{3 a}{3-4 \cosh[2 x]+\cosh[4 x]} - \frac{b}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{3 c}{3-4 \cosh[2 x]+\cosh[4 x]} - \right.} \right. \\
& \frac{4 a \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{4 c \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{a \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \\
& \left. \frac{b \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{c \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} \right) \operatorname{Sech}[x] \sinh[3 x] \Bigg) / \\
& \left(a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) + \\
& \left(\sqrt{\left(\frac{3 a}{3-4 \cosh[2 x]+\cosh[4 x]} - \frac{b}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{3 c}{3-4 \cosh[2 x]+\cosh[4 x]} - \right.} \right. \\
& \frac{4 a \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{4 c \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{a \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \\
& \left. \frac{b \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{c \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} \right) \operatorname{Sech}[x] \sinh[5 x] \Bigg) / \\
& \left(2 (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) + \\
& \left(5 \sqrt{\left(\frac{3 a}{3-4 \cosh[2 x]+\cosh[4 x]} - \frac{b}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{3 c}{3-4 \cosh[2 x]+\cosh[4 x]} - \right.} \right. \\
& \frac{4 a \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{4 c \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{a \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \\
& \left. \frac{b \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{c \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} \right) \tanh[x] \Bigg) / \\
& \left(3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x] \right) - \\
& \left(3 b \sqrt{\left(\frac{3 a}{3-4 \cosh[2 x]+\cosh[4 x]} - \frac{b}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{3 c}{3-4 \cosh[2 x]+\cosh[4 x]} - \right.} \right. \\
& \frac{4 a \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{4 c \cosh[2 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{a \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \\
& \left. \frac{b \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} + \frac{c \cosh[4 x]}{3-4 \cosh[2 x]+\cosh[4 x]} \right) \tanh[x] \Bigg) / \\
& \left. \left(a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left(\left(a \cosh[2x] (-8a \cosh[2x] + 8c \cosh[2x] + 8a \cosh[4x] + 8b \cosh[4x] + 8c \cosh[4x]) \right. \right. \\
& \quad (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \quad \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4a + 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}\right)\right] / \\
& \left(2\sqrt{a} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right] + \\
& \frac{1}{\sqrt{a + b + c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \quad \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right] \Bigg) \\
& \left(\frac{a \coth[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{a \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \Bigg/ \\
& \left(32(-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right. \\
& \quad \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) +} \\
& \quad b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) +} \right. \right.} \\
& \quad \quad c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \quad c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \Bigg) \\
& \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) +} \right. \\
& \quad b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& \quad \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \right) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \\
& \quad b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \\
& \quad \quad c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \\
& \quad b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \\
& \quad \quad c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \Bigg) \Bigg) \\
& \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left((-a+b)(1+\operatorname{Cosh}[2x]) \right. \\
& \quad (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \\
& \quad \sqrt{\frac{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}{(1+\operatorname{Cosh}[2x])^2}} \\
& \quad \operatorname{Coth}[x]^2 \\
& \quad \operatorname{Csch}[x]^2 \\
& \quad \left. \operatorname{Log}[b+2a \operatorname{Tanh}[x]^2+2\sqrt{a} \sqrt{c+b \operatorname{Tanh}[x]^2+a \operatorname{Tanh}[x]^4}] \right. \\
& \quad \left. \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \\
& \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \Bigg) \Bigg/ \\
& \left(4 \sqrt{2} \sqrt{a} (-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \right) - \\
& \left((-a+b) (1+\operatorname{Cosh}[2x]) (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \right. \\
& \left. \sqrt{\frac{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}{(1+\operatorname{Cosh}[2x])^2}} \right. \\
& \left. \operatorname{Csch}[x]^4 \right. \\
& \left. \operatorname{Log}\left[b+2a \operatorname{Tanh}[x]^2+2\sqrt{a} \sqrt{c+b \operatorname{Tanh}[x]^2+a \operatorname{Tanh}[x]^4}\right] \right. \\
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \right. \\
& \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \\
& \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \Bigg) \Bigg/ \\
& \left(8 \sqrt{2} \sqrt{a} (-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \right) - \\
& \left(\sqrt{a} (-a+b) (1+\operatorname{Cosh}[2x]) (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \right. \\
& \left. \sqrt{\frac{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}{(1+\operatorname{Cosh}[2x])^2}} \right. \\
& \left. \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \right. \\
& \left. \operatorname{Log}\left[b+2a \operatorname{Tanh}[x]^2+2\sqrt{a} \sqrt{c+b \operatorname{Tanh}[x]^2+a \operatorname{Tanh}[x]^4}\right] \right. \\
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \\
& \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \operatorname{Sinh}[2x] \Bigg) / \\
& \left(4 \sqrt{2} (-a+b+a \operatorname{Cosh}[2x])^2 \sqrt{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \right) + \\
& \left((-a+b) (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \right. \\
& \left. \sqrt{\frac{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}{(1+\operatorname{Cosh}[2x])^2}} \right. \\
& \left. \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \right. \\
& \left. \operatorname{Log}\left[b+2a \operatorname{Tanh}[x]^2+2\sqrt{a} \sqrt{c+b \operatorname{Tanh}[x]^2+a \operatorname{Tanh}[x]^4}\right] \right. \\
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \operatorname{Sinh}[2x] \right) / \\
& \left(4 \sqrt{2} \sqrt{a} (-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c+(-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]} \right. \\
& \left. \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \right) - \\
& \left(a \operatorname{Cosh}[2x] (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \right. \\
& \left(2a \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \right. \\
& 2b \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \\
& \left. 2c \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + \right. \right.} \right. \\
& \left. \left. c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \text{Coth}[x] \text{Csch}[x]^2 \left(\frac{\text{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]}}{2\sqrt{2}\sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \text{ArcTanh}\left[\left((2a+b)\sqrt{3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]}\right)\right] / \\
& \left(2\sqrt{a}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right.} + \\
& \quad b(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]) + \\
& \quad \left. c(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right)} + \\
& \frac{1}{\sqrt{a+b+c}} 2 \text{Log}\left[2\left(a\sqrt{3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]} + \right. \right. \\
& \quad b\sqrt{3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]} + c \\
& \quad \left. \sqrt{3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]} + \sqrt{a+b+c} \right. \\
& \quad \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right.} + \\
& \quad \left. b(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right) + \\
& \quad \left. \left. c(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right)\right)} \Bigg] \\
& \left(\frac{a\text{Coth}[2x]\text{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\text{Cosh}[2x]+(a+b+c)\text{Cosh}[4x]}} - \frac{a\text{Csch}[2x]\text{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\text{Cosh}[2x]+(a+b+c)\text{Cosh}[4x]}} + \right. \\
& \quad \left. \frac{b\text{Csch}[2x]\text{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\text{Cosh}[2x]+(a+b+c)\text{Cosh}[4x]}} \right) \\
& \left(-4a\text{Sinh}[2x] + 4c\text{Sinh}[2x] + 2a\text{Sinh}[4x] + 2b\text{Sinh}[4x] + 2c\text{Sinh}[4x] \right) / \\
& \left(16(-a+b+a\text{Cosh}[2x])\sqrt{3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]} \right. \\
& \quad \sqrt{(2b^2-8ac+a(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right.} + \\
& \quad b(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]) + \\
& \quad \left. c(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c}\left(-2b-4c+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right.} \right.} \right. \\
& \quad \left. \left. c\text{Cosh}[4x]) + b(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a\text{Cosh}[2x]+4c\text{Cosh}[2x]+a\text{Cosh}[4x]+b\text{Cosh}[4x]+c\text{Cosh}[4x])\right)\right)} \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left(2a - 2c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right. \\
& \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right. \\
& \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left(a^2 \cosh[2x] \right. \\
& \quad (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \quad \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a + 2b + \sqrt{2} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right. \\
& \quad c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{a}} \right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] / \\
& \quad \left(2\sqrt{a} \sqrt{2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right] + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \\
& \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg] \\
& \left(\frac{a \coth[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{a \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \quad \left. \frac{b \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \left. \sinh[2x] (-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \right) / \\
& \left(16(-a + b + a \cosh[2x])^2 \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \\
& \quad \left. \sqrt{\left(\frac{1}{a + b + c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \right. \right.} \\
& \quad \quad \quad c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad \quad c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg) \right) \\
& \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a + b + c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right. \right.} \\
& \quad \quad \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \\
& \quad \quad \quad c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg) \right) \\
& \sqrt{\left(1 + \frac{1}{2(a + b + c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right. \right.} \\
& \quad \quad \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \\
& \quad \quad \quad c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg) \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \\
& \operatorname{Sinh}[2x] (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \Bigg/ \\
& \left(16(-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right. \\
& \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])} \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \right. \right.} \\
& c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])} \Bigg) \Bigg) \\
& \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \right. \\
& b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])} \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \\
& b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \\
& c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])} \Bigg) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \\
& b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \\
& c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])} \Bigg) \Bigg) \Bigg) \\
& \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left(a \operatorname{Cosh}[2x] \right. \\
& (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \\
& \left. (2a \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \right.
\end{aligned}$$

$$\begin{aligned}
& 2 b \sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}+ \\
& 2 c \sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}\left.\right) \\
& \sqrt{\left(\frac{1}{a+b+c}\left(4 a+2 b+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)+\right.\right.\right.} \right. \\
& \quad \left.\left.\left.c \cosh [4 x]\right)+b\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)+\right.\right. \\
& \quad \left.\left.\left.c\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)\right)\right)\right)} \\
& \operatorname{Csch}[x]^2\left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}}{2 \sqrt{2} \sqrt{a}}\right]}{\sqrt{a}}-\right. \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2 a+b) \sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}\right)\right] / \\
& \left(2 \sqrt{a} \sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)+\right.\right.} \\
& \quad \left.\left.\left.b\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)+\right.\right.\right. \\
& \quad \left.\left.\left.c\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)\right)\right)\right]+ \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2\left(a \sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}+\right.\right. \\
& \quad \left.\left.b \sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}+c\right.\right. \\
& \quad \left.\left.\sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]}+\sqrt{a+b+c}\right.\right. \\
& \quad \left.\left.\sqrt{\left(2 b^2-8 a c+a\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)+\right.\right.\right. \\
& \quad \left.\left.\left.\left.b\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)+\right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.c\left(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]\right)\right)\right)\right)\right)\right] \\
& \left(\frac{a \operatorname{Coth}[2 x] \operatorname{Sinh}[x]^2}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}-\frac{a \operatorname{Csch}[2 x] \operatorname{Sinh}[x]^2}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}+\right. \\
& \quad \left.\frac{b \operatorname{Csch}[2 x] \operatorname{Sinh}[x]^2}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}\right) \\
& (-4 a \operatorname{Sinh}[2 x]+4 c \operatorname{Sinh}[2 x]+2 a \operatorname{Sinh}[4 x]+2 b \operatorname{Sinh}[4 x]+2 c \operatorname{Sinh}[4 x]) \\
& (-8 a \operatorname{Sinh}[2 x]+8 c \operatorname{Sinh}[2 x]+4 a \operatorname{Sinh}[4 x]+4 b \operatorname{Sinh}[4 x]+4 c \operatorname{Sinh}[4 x])\left.\right) /
\end{aligned}$$

$$\begin{aligned}
& \left(64 (-a + b + a \cosh[2x]) (3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])^{3/2} \right. \\
& \quad \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right.} \\
& \quad \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \right. \\
& \quad \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \quad \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \quad \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \\
& \quad \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \\
& \quad \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \quad \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \\
& \quad \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \\
& \quad \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \quad \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) + \left((-a + b) (1 + \cosh[2x]) \right. \\
& \quad \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \quad \operatorname{Coth}[x] \\
& \quad \operatorname{Csch}[x]^2 \\
& \quad \left. \log[b + 2a \tanh[x]^2 + 2\sqrt{a} \sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}] \right. \\
& \quad \left(\frac{a \operatorname{Coth}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right. \\
& \quad \frac{a \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \quad \left. \frac{b \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left. (-8 (a - c) \sinh[2x] + 4 (a + b + c) \sinh[4x]) \right) / \\
& \left(8 \sqrt{2} \sqrt{a} (-a + b + a \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \quad \left. \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{csch}[x]^4} \right) + \\
& \left(a \cosh[2x] \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4a + 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right) \\
& \operatorname{csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2} \sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] / \\
& \left(2\sqrt{a} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) + \\
& \frac{1}{\sqrt{a + b + c}} 2 \log\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \quad \left. \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \right. \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \\
& (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \\
& (-8(a-c) \operatorname{Sinh}[2x] + 4(a+b+c) \operatorname{Sinh}[4x]) \Bigg/ \\
& \left(32(-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right. \\
& \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \right. \right.} \\
& c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \Bigg) \\
& \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \right. \\
& b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) +} \\
& c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \\
& b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \\
& c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] +} \right. \right.} \\
& b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] +} \\
& c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) \Bigg) \Bigg) \\
& \sqrt{(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left((-a+b)(1 + \operatorname{Cosh}[2x]) \right. \\
& (3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \\
& \sqrt{\frac{3a-b+3c + (-4a+4c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}{(1 + \operatorname{Cosh}[2x])^2}}
\end{aligned}$$

$$\begin{aligned}
& \text{Coth}[x] \\
& \text{Csch}[x]^2 \\
& \text{Log}\left[b + 2 a \tanh[x]^2 + 2 \sqrt{a} \sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}\right] \\
& \left(\frac{a \coth[2 x] \sinh[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} - \right. \\
& \quad \frac{a \text{Csch}[2 x] \sinh[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \\
& \quad \left. \frac{b \text{Csch}[2 x] \sinh[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) \\
& \left(2 (-4 a + 4 c) \sinh[2 x] + 4 (a + b + c) \sinh[4 x] \right) \Bigg/ \\
& \left(16 \sqrt{2} \sqrt{a} (-a + b + a \cosh[2 x]) (3 a - b + 3 c + (-4 a + 4 c) \cosh[2 x] + (a + b + c) \cosh[4 x])^{3/2} \right. \\
& \quad \left. \sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \text{Csch}[x]^4} \right) - \\
& \left(a \cosh[2 x] (3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \right. \\
& \quad \left(2 a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \\
& \quad 2 b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \\
& \quad \left. 2 c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right) \\
& \quad \left. \sqrt{\left(\frac{1}{a + b + c} \left(4 a + 2 b + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right. \right. \right. \right. \\
& \quad \left. \left. \left. c \cosh[4 x] \right) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \quad \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \\
& \text{Csch}[x]^2 \left(\frac{\text{ArcTanh}\left[\frac{\sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]}}{2 \sqrt{2} \sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \text{ArcTanh}\left[\left((2 a + b) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right) \right] \Bigg/ \\
& \left(2 \sqrt{a} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])} \right. \\
& \quad \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right.
\end{aligned}$$

$$\begin{aligned}
& c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log} \left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \right. \\
& \left. \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \\
& \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right] \Bigg] + \\
& \left(\frac{a \coth[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} - \frac{a \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} + \right. \\
& \left. \frac{b \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x]}} \right) \\
& (-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& (a(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& b(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& c(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])) \Bigg] \Bigg/ \left(128 \sqrt{2} (a+b+c) \right. \\
& (-a+b+a \cosh[2x]) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \\
& (2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg] \\
& \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \Bigg] \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right.} \right. \\
& \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.}
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. c \left(3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x] \right) \right) \right] \right) \\
& \left(\frac{a \coth[2 x] \sinh[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} - \frac{a \operatorname{csch}[2 x] \sinh[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} + \right. \\
& \left. \frac{b \operatorname{csch}[2 x] \sinh[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]}} \right) \\
& (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\
& (a (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& b (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\
& c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])) \Bigg) / \left(128 \sqrt{2} (a + b + c) \right. \\
& (-a + b + a \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \\
& (2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\
& c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg) \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right.} \right. \\
& \left. \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \\
& \left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right.} \right. \\
& \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\
& \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg)^{3/2} \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right.} \right. \\
& \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \\
& \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \Bigg) - \left(a\cosh[2x] \right. \\
& (3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \\
& \left(2a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \\
& \left. \left. 2c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + \right. \right.} \right. \\
& \left. \left. c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg)} \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}}{2\sqrt{2}\sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a+b)\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}\right)\right] / \\
& \left(2\sqrt{a}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right.} \\
& \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \Bigg) + \\
& \frac{1}{\sqrt{a+b+c}} 2\operatorname{Log}\left[2\left(a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \right. \\
& \left. b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + c \right. \\
& \left. \sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \sqrt{a+b+c} \right. \\
& \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right.} \\
& \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg] \Bigg) \\
& \left(\frac{a\coth[2x]\sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{a\operatorname{Csch}[2x]\sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \left. \frac{b\operatorname{Csch}[2x]\sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right)
\end{aligned}$$

$$\left. \begin{aligned} & (-4 a \sinh[2 x] + 4 c \sinh[2 x] + 2 a \sinh[4 x] + 2 b \sinh[4 x] + 2 c \sinh[4 x]) \\ & (a (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\ & \quad b (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x]) + \\ & \quad c (-8 a \sinh[2 x] + 8 c \sinh[2 x] + 4 a \sinh[4 x] + 4 b \sinh[4 x] + 4 c \sinh[4 x])) \end{aligned} \right) /$$

$$\begin{aligned} & \left(32 \sqrt{2} (-a + b + a \cosh[2 x]) \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right. \\ & \quad (2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\ & \quad \quad b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \\ & \quad \quad c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x])) \\ & \quad \left. \sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \right.} \right. \right. \\ & \quad \quad \quad \left. \left. \left. c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \right. \\ & \quad \quad \quad \left. \left. \left. c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right)} \right) \\ & \quad \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + \right. \right. \\ & \quad \quad \left. \left. b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) + c \right. \right. \\ & \quad \quad \left. \left. (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right)^2 \\ & \quad \left. \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right. \right.} \right. \right. \\ & \quad \quad \quad \left. \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \right. \\ & \quad \quad \quad \left. \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right)} \right) \\ & \quad \left. \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + \right. \right. \right.} \right. \right. \\ & \quad \quad \quad \left. \left. \left. b \cosh[4 x] + c \cosh[4 x]) + b (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + \right. \right. \right. \\ & \quad \quad \quad \left. \left. \left. c \cosh[4 x]) + c (3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]) \right) \right) \right)} \right) \\ & \quad \left. \sqrt{(3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \operatorname{Csch}[x]^4} \right) - \left(a \cosh[2 x] \right. \\ & \quad (3 a - b + 3 c - 4 (a - c) \cosh[2 x] + (a + b + c) \cosh[4 x]) \\ & \quad \left(2 a \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \right. \\ & \quad \quad 2 b \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} + \\ & \quad \quad \left. \left. 2 c \sqrt{3 a - b + 3 c - 4 a \cosh[2 x] + 4 c \cosh[2 x] + a \cosh[4 x] + b \cosh[4 x] + c \cosh[4 x]} \right) \right) \end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{a}} \right]}{\sqrt{a}} \right. \\
& \quad \left. - \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a+b) \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right] \right. \\
& \quad \left. \left(2\sqrt{a} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \right. \\
& \quad \left. \left. + b \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + c \right. \right. \\
& \quad \left. \left. \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \quad \left. \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg] \\
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} - \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \right. \\
& \quad \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right) \\
& (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \\
& (a(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x]) + \\
& \quad b(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x]) + \\
& \quad c(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x])) \Bigg) \Bigg/ \left(64 \sqrt{2} (a+b+c) \right. \\
& \quad \left. (-a+b+a\cosh[2x]) \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \quad \left. (2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])) + \right. \\
& \quad \left. b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right.
\end{aligned}$$

$$\begin{aligned}
& c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \\
& \left(\frac{1}{a+b+c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) + \right. \right. \\
& \quad c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right)^{3/2} \\
& \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) + \right. \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \\
& \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \\
& \quad b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) + \left(a \cosh[2x] \right. \\
& (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{a}} \right]}{\sqrt{a}} - \right. \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] / \\
& \quad \left(2\sqrt{a} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) + \right. \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right] + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \\
& \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg] \\
& \left(\frac{a \coth[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \frac{a \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \right. \\
& \quad \left. \frac{b \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& (-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& (a(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad b(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad c(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])) \Bigg) / \left(64 \sqrt{2} (a + b + c) \right) \\
& (-a + b + a \cosh[2x]) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \\
& (2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \Bigg) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4a + 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right)} \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right)} \\
& \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a + b + c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left(\left(\left(b \cosh[4x] + c \cosh[4x] \right) + b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \right. \\
& \left. \left. \left. c \cosh[4x] \right) + c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \right) \\
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{\left(2b^2 - 8ac + a \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \right. \right. \\
& \left. \left. \left. b \cosh[4x] + c \cosh[4x] \right) + b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \right. \\
& \left. \left. \left. c \cosh[4x] \right) + c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \right) \\
& \sqrt{\left(3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x] \right) \operatorname{Csch}[x]^4} \Bigg) - \left(a \cosh[2x] \right. \\
& \left. \frac{\left(3a - b + 3c - 4(a-c) \cosh[2x] + (a+b+c) \cosh[4x] \right)}{\left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a + 2b + \sqrt{2} \sqrt{\left(2b^2 - 8ac + a \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \right. \right. \right. \\
& \left. \left. \left. c \cosh[4x] \right) + b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) + \right. \right. \right. \\
& \left. \left. \left. c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \right) \right) \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2} \sqrt{a}} \right]}{\sqrt{a}} - \right. \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right] \Bigg/ \\
& \left(2\sqrt{a} \sqrt{\left(2b^2 - 8ac + a \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) + \right. \right. \\
& \left. \left. b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) + \right. \right. \\
& \left. \left. c \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) \right) \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \left. \left. b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \right. \right. \\
& \left. \left. \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \right. \right. \\
& \left. \left. \sqrt{\left(2b^2 - 8ac + a \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) + \right. \right. \right. \\
& \left. \left. \left. b \left(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x] \right) + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. c \left(3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x] \right) \right) \right) \right] \\
& \left(\frac{a \operatorname{Coth}[2 x] \operatorname{Sinh}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} - \frac{a \operatorname{Csch}[2 x] \operatorname{Sinh}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} + \right. \\
& \left. \frac{b \operatorname{Csch}[2 x] \operatorname{Sinh}[x]^2}{\sqrt{3 a - b + 3 c - 4 (a - c) \operatorname{Cosh}[2 x] + (a + b + c) \operatorname{Cosh}[4 x]}} \right) \\
& (-4 a \operatorname{Sinh}[2 x] + 4 c \operatorname{Sinh}[2 x] + 2 a \operatorname{Sinh}[4 x] + 2 b \operatorname{Sinh}[4 x] + 2 c \operatorname{Sinh}[4 x]) \\
& (a (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) + \\
& b (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x]) + \\
& c (-8 a \operatorname{Sinh}[2 x] + 8 c \operatorname{Sinh}[2 x] + 4 a \operatorname{Sinh}[4 x] + 4 b \operatorname{Sinh}[4 x] + 4 c \operatorname{Sinh}[4 x])) \Bigg/ \\
& \left(64 (-a + b + a \operatorname{Cosh}[2 x]) \sqrt{3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]} \right. \\
& \left(2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \right. \\
& b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \\
& \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right)^{3/2} \right. \\
& \left. \sqrt{\left(\frac{1}{a + b + c} \left(-2 b - 4 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + \right. \right. \right.} \right. \\
& \left. \left. \left. c \operatorname{Cosh}[4 x]) + b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \right. \right. \right. \\
& \left. \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \right) \Bigg) \\
& \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \right. \\
& b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + \\
& \left. \left. c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + \right. \right. \right.} \\
& \left. \left. \left. b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + \right. \right. \right. \\
& \left. \left. \left. c \operatorname{Cosh}[4 x]) + c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \right) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2 (a + b + c)} \left(2 a - 2 c + \sqrt{2} \sqrt{2 b^2 - 8 a c + a (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + \right. \right. \right.} \\
& \left. \left. \left. b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) + b (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + \right. \right. \right. \\
& \left. \left. \left. c \operatorname{Cosh}[4 x]) + c (3 a - b + 3 c - 4 a \operatorname{Cosh}[2 x] + 4 c \operatorname{Cosh}[2 x] + a \operatorname{Cosh}[4 x] + b \operatorname{Cosh}[4 x] + c \operatorname{Cosh}[4 x]) \right) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{Csch}[x]^4} \Bigg) + \left(a\cosh[2x] \right. \\
& (3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right. \right. \\
& \quad \left. \left. + c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}}{2\sqrt{2}\sqrt{a}} \right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a+b)\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right) \right] / \\
& \left(2\sqrt{a}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \\
& \quad \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right. \\
& \quad \left. + c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \Bigg] + \\
& \frac{1}{\sqrt{a+b+c}} 2\operatorname{Log}\left[2\left(a\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \right. \\
& \quad \left. \left. + b\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \right. \\
& \quad \left. \left. + \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \right. \\
& \quad \left. \left. + \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right. \right. \\
& \quad \left. \left. + c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \Bigg] \Bigg) \\
& \left(\frac{a\coth[2x]\sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \frac{a\operatorname{Csch}[2x]\sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \right. \\
& \quad \left. \frac{b\operatorname{Csch}[2x]\sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& (-4a\sinh[2x] + 4c\sinh[2x] + 2a\sinh[4x] + 2b\sinh[4x] + 2c\sinh[4x]) \\
& \left(\frac{a(-8a\sinh[2x] + 8c\sinh[2x] + 4a\sinh[4x] + 4b\sinh[4x] + 4c\sinh[4x])}{\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{b(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} + \\
& \frac{c(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} \Bigg) \Bigg/ \\
& \left(32(-a + b + a \cosh[2x]) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \\
& \quad \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(-2b - 4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right.} \\
& \quad \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \\
& \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) +} \right. \\
& \quad \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \\
& \sqrt{\left(-1 + \frac{1}{2(a + b + c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \right. \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \sqrt{\left(1 + \frac{1}{2(a + b + c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] +} \right. \right.} \right. \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] +} \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \Bigg) \Bigg) \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) - \left((-a + b)(1 + \cosh[2x]) \right. \\
& (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \operatorname{Coth}[x] \\
& \operatorname{Csch}[x]^2 \\
& \log[b + 2a \tanh[x]^2 + 2\sqrt{a} \sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}]
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{a \coth[2x] \sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} - \right. \\
& \frac{a \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} + \\
& \left. \frac{b \operatorname{csch}[2x] \sinh[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]}} \right) \\
& (-4(3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \coth[x] \operatorname{csch}[x]^4 + \\
& \operatorname{csch}[x]^4 (-8(a-c)\sinh[2x] + 4(a+b+c)\sinh[4x])) \Bigg) / \\
& \left(16\sqrt{2}\sqrt{a}(-a+b+a\cosh[2x])\sqrt{3a-b+3c+(-4a+4c)\cosh[2x] + (a+b+c)\cosh[4x]} \right. \\
& \left. ((3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x])\operatorname{csch}[x]^4)^{3/2} \right) - \\
& \left(a \cosh[2x] (3a-b+3c-4(a-c)\cosh[2x] + (a+b+c)\cosh[4x]) \right. \\
& \left(2a\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \right. \\
& 2b\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} + \\
& \left. 2c\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + \right. \right.} \right. \\
& \left. \left. c\cosh[4x]) + b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \right. \\
& \left. \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \right) \Bigg) \\
& \operatorname{csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]}}{2\sqrt{2}\sqrt{a}}\right]}{\sqrt{a}} \right) - \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a+b)\sqrt{3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]} \right) \right] / \\
& \left(2\sqrt{a}\sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right.} \\
& \left. b(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) + \right. \\
& \left. c(3a-b+3c-4a\cosh[2x] + 4c\cosh[2x] + a\cosh[4x] + b\cosh[4x] + c\cosh[4x]) \right) \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{\sqrt{a+b+c}} \left(2 \operatorname{Log} \left[2 \left(a \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \right. \right. \right. \\
& \quad b \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + c \\
& \quad \left. \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} + \sqrt{a+b+c} \right. \\
& \quad \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x])) + \right. \\
& \quad \left. b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right. \\
& \quad \left. \left. \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \right] \right) \\
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} - \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} + \right. \\
& \quad \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]}} \right) \\
& (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \\
& (-4(3a-b+3c-4(a-c) \operatorname{Cosh}[2x] + (a+b+c) \operatorname{Cosh}[4x]) \operatorname{Coth}[x] \operatorname{Csch}[x]^4 + \\
& \quad \operatorname{Csch}[x]^4 (-8(a-c) \operatorname{Sinh}[2x] + 4(a+b+c) \operatorname{Sinh}[4x])) \Bigg/ \\
& \left(64(-a+b+a \operatorname{Cosh}[2x]) \sqrt{3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]} \right. \\
& \quad \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \\
& \quad b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \\
& \quad c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]))} \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \Bigg) \\
& \left(2a-2c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right.} \\
& \quad \left. b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \Bigg) \\
& \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + \right. \right.} \right. \\
& \quad \left. \left. b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) + b(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + \right. \right. \\
& \quad \left. \left. c \operatorname{Cosh}[4x]) + c(3a-b+3c-4a \operatorname{Cosh}[2x] + 4c \operatorname{Cosh}[2x] + a \operatorname{Cosh}[4x] + b \operatorname{Cosh}[4x] + c \operatorname{Cosh}[4x]) \right) \right) \Bigg) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right. \right. \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right)\right)} \\
& \left((3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4\right)^{3/2} + \left((-a + b)(1 + \cosh[2x])\right. \\
& \quad \left.(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])\right. \\
& \quad \left.\sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}}\right. \\
& \quad \left.\operatorname{Coth}[x] \operatorname{Csch}[x]^2\right. \\
& \quad \left.\operatorname{Log}[b + 2a \tanh[x]^2 + 2\sqrt{a} \sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}]\right. \\
& \quad \left(\frac{2a \cosh[x] \operatorname{Coth}[2x] \sinh[x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right. \\
& \quad \frac{2a \cosh[x] \operatorname{Csch}[2x] \sinh[x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \quad \frac{2b \cosh[x] \operatorname{Csch}[2x] \sinh[x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \quad \frac{2a \operatorname{Coth}[2x] \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \\
& \quad \frac{2b \operatorname{Coth}[2x] \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \\
& \quad \frac{2a \operatorname{Csch}[2x]^2 \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \\
& \quad \frac{a \operatorname{Coth}[2x] \sinh[x]^2 (-8(a - c) \sinh[2x] + 4(a + b + c) \sinh[4x])}{2(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])^{3/2}} + \\
& \quad \frac{a \operatorname{Csch}[2x] \sinh[x]^2 (-8(a - c) \sinh[2x] + 4(a + b + c) \sinh[4x])}{2(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])^{3/2}} - \\
& \quad \left.\frac{b \operatorname{Csch}[2x] \sinh[x]^2 (-8(a - c) \sinh[2x] + 4(a + b + c) \sinh[4x])}{2(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x])^{3/2}}\right) \Bigg) / \\
& \left(8\sqrt{2} \sqrt{a} (-a + b + a \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}\right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} + \\
& \left(a \cosh[2x] (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right) \\
& \sqrt{\left(\frac{1}{a + b + c} \left(4a + 2b + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \\
& \left. \left. c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right)} \\
& \operatorname{Csch}[x]^2 \left(\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}}{2\sqrt{2}\sqrt{a}}\right]}{\sqrt{a}} - \right. \\
& \frac{1}{\sqrt{a}} \operatorname{ArcTanh}\left[\left((2a + b) \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}\right) \right] / \\
& \left(2\sqrt{a} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) + \\
& \frac{1}{\sqrt{a + b + c}} 2 \operatorname{Log}\left[2 \left(a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + c \\
& \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a + b + c} \\
& \left. \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \\
& \left. b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \left. \left. c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) \right) \right) \right] \Bigg) \\
& (-4a \sinh[2x] + 4c \sinh[2x] + 2a \sinh[4x] + 2b \sinh[4x] + 2c \sinh[4x]) \\
& \left(\frac{2a \cosh[x] \coth[2x] \sinh[x]}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{2 a \cosh [x] \operatorname{csch}[2 x] \sinh [x]}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}+ \\
& \frac{2 b \cosh [x] \operatorname{csch}[2 x] \sinh [x]}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}+ \\
& \frac{2 a \coth [2 x] \operatorname{csch}[2 x] \sinh [x]^2}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}- \\
& \frac{2 b \coth [2 x] \operatorname{csch}[2 x] \sinh [x]^2}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}- \\
& \frac{2 a \operatorname{csch}[2 x]^2 \sinh [x]^2}{\sqrt{3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x]}}- \\
& \frac{a \coth [2 x] \sinh [x]^2(-8(a-c) \sinh [2 x]+4(a+b+c) \sinh [4 x])}{2(3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x])^{3 / 2}}+ \\
& \frac{a \operatorname{csch}[2 x] \sinh [x]^2(-8(a-c) \sinh [2 x]+4(a+b+c) \sinh [4 x])}{2(3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x])^{3 / 2}}- \\
& \left. \frac{b \operatorname{csch}[2 x] \sinh [x]^2(-8(a-c) \sinh [2 x]+4(a+b+c) \sinh [4 x])}{2(3 a-b+3 c-4(a-c) \cosh [2 x]+(a+b+c) \cosh [4 x])^{3 / 2}} \right) \Bigg/ \\
& \left(32(-a+b+a \cosh [2 x]) \sqrt{3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]} \right. \\
& \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) \right.} \\
& \quad b(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) + \\
& \quad \left. \left. c(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) \right) \right) \\
& \sqrt{\left(\frac{1}{a+b+c} \left(-2 b-4 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+ \right.} \right. \right. \\
& \quad \left. \left. c \cosh [4 x]) \right)+b(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) + \right. \\
& \quad \left. \left. c(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) \right) \right) \right) \\
& \left(2 a-2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) \right.} \right. \\
& \quad \left. b(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) + \right. \\
& \quad \left. \left. c(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) \right) \right) \\
& \sqrt{\left(-1+\frac{1}{2(a+b+c)} \left(2 a-2 c+\sqrt{2} \sqrt{\left(2 b^2-8 a c+a(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+ \right.} \right. \right. \\
& \quad \left. \left. b \cosh [4 x]+c \cosh [4 x]) \right)+b(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+ \right. \\
& \quad \left. \left. c \cosh [4 x]) \right)+c(3 a-b+3 c-4 a \cosh [2 x]+4 c \cosh [2 x]+a \cosh [4 x]+b \cosh [4 x]+c \cosh [4 x]) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right)\right)} \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \Bigg) + \left((-a + b) (1 + \cosh[2x]) \right. \\
& \quad \left. \cosh[x] \right. \\
& \quad \left. \operatorname{Csch}[x]^2 \right. \\
& \quad \left. \log[b + 2a \tanh[x]^2 + 2\sqrt{a} \sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}] \right. \\
& \quad \left(\frac{a \cosh[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right. \\
& \quad \frac{a \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \quad \left. \frac{b \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} \right) \\
& \quad \left(-\frac{4(3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]) \sinh[2x]}{(1 + \cosh[2x])^3} + \right. \\
& \quad \left. \frac{2(-4a + 4c) \sinh[2x] + 4(a + b + c) \sinh[4x]}{(1 + \cosh[2x])^2} \right) \Bigg) / \\
& \left(16\sqrt{2} \sqrt{a} (-a + b + a \cosh[2x]) \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \right. \\
& \quad \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \quad \left. \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \right) + \\
& \left(a \cosh[2x] (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \right. \\
& \quad \left(2a \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \\
& \quad 2b \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad \left. \left. 2c \sqrt{3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(\frac{1}{a+b+c} \left(4a+2b+\sqrt{2} \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \right. \\
& \quad \left. \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \right) \operatorname{Csch}[x]^2} \\
& \left(\frac{a \operatorname{Coth}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} - \frac{a \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} + \right. \\
& \quad \left. \frac{b \operatorname{Csch}[2x] \operatorname{Sinh}[x]^2}{\sqrt{3a-b+3c-4(a-c)\cosh[2x]+(a+b+c)\cosh[4x]}} \right) \\
& (-4a \operatorname{Sinh}[2x] + 4c \operatorname{Sinh}[2x] + 2a \operatorname{Sinh}[4x] + 2b \operatorname{Sinh}[4x] + 2c \operatorname{Sinh}[4x]) \\
& \left((-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x]) \right) / \\
& \left(4\sqrt{2} a \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \quad \left(1 - \frac{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}{8a} \right) \Big) - \\
& \left(((2a+b)(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x])) \right) / \\
& \quad \left(4\sqrt{a} \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \quad \left. \sqrt{(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]))} \right. \\
& \quad \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \Big) - \\
& \left((2a+b) \sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]} \right. \\
& \quad (a(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x]) + \\
& \quad b(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x]) + \\
& \quad c(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x])) \Big) / \\
& \quad \left(4\sqrt{a} (2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])) \right. \\
& \quad \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right)^{3/2} \Big) / \\
& \left(\sqrt{a} \left(1 - ((2a+b)^2(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])) \right) / \right. \\
& \quad \left(4a(2b^2-8ac+a(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x])) \right. \\
& \quad \left. + b(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]) \right) \Big) \Big) + \\
& \left(2 \frac{a(-8a \operatorname{Sinh}[2x] + 8c \operatorname{Sinh}[2x] + 4a \operatorname{Sinh}[4x] + 4b \operatorname{Sinh}[4x] + 4c \operatorname{Sinh}[4x])}{2\sqrt{3a-b+3c-4a\cosh[2x]+4c\cosh[2x]+a\cosh[4x]+b\cosh[4x]+c\cosh[4x]}} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{b(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{2\sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} + \\
& \frac{c(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])}{2\sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]}} + \\
& \left(\sqrt{a+b+c} (a(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \right. \\
& \quad b(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x]) + \\
& \quad \left. c(-8a \sinh[2x] + 8c \sinh[2x] + 4a \sinh[4x] + 4b \sinh[4x] + 4c \sinh[4x])) \right) / \\
& \left(2\sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \\
& \quad \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \Bigg) / \\
& \left(\sqrt{a+b+c} \left(a\sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \right. \right. \\
& \quad b\sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \\
& \quad c\sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} + \sqrt{a+b+c} \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right) \Bigg) / \\
& \left(32(-a+b+a \cosh[2x]) \sqrt{3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]} \right. \\
& \quad \left. \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \\
& \quad \sqrt{\left(\frac{1}{a+b+c} \left(-2b-4c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \right. \\
& \quad \left. \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right) \Bigg) \\
& \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right.} \right. \\
& \quad \left. b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x]) + \right. \\
& \quad \left. c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \\
& \quad \sqrt{\left(-1 + \frac{1}{2(a+b+c)} \left(2a-2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a-b+3c-4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])) \right) \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(1 + \frac{1}{2(a+b+c)} \left(2a - 2c + \sqrt{2} \sqrt{(2b^2 - 8ac + a(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + \right. \right.} \right. \\
& \quad \left. \left. b \cosh[4x] + c \cosh[4x]) + b(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + \right. \right. \\
& \quad \left. \left. c \cosh[4x]) + c(3a - b + 3c - 4a \cosh[2x] + 4c \cosh[2x] + a \cosh[4x] + b \cosh[4x] + c \cosh[4x])\right)\right)} \\
& \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} + \left((-a + b)(1 + \cosh[2x])\right. \\
& \quad (3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \\
& \quad \sqrt{\frac{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]}{(1 + \cosh[2x])^2}} \\
& \quad \operatorname{Coth}[x] \\
& \quad \operatorname{Csch}[x]^2 \\
& \quad \left(\frac{a \operatorname{Coth}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} - \right. \\
& \quad \frac{a \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}} + \\
& \quad \left. \frac{b \operatorname{Csch}[2x] \sinh[x]^2}{\sqrt{3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]}}\right) \\
& \quad \left(4a \operatorname{Sech}[x]^2 \tanh[x] + \frac{\sqrt{a} (2b \operatorname{Sech}[x]^2 \tanh[x] + 4a \operatorname{Sech}[x]^2 \tanh[x]^3)}{\sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}}\right) \Bigg) \Bigg/ (8 \\
& \quad \sqrt{2} \\
& \quad \sqrt{a} \\
& \quad (-a + b + a \cosh[2x]) \\
& \quad \sqrt{3a - b + 3c + (-4a + 4c) \cosh[2x] + (a + b + c) \cosh[4x]} \\
& \quad \sqrt{(3a - b + 3c - 4(a - c) \cosh[2x] + (a + b + c) \cosh[4x]) \operatorname{Csch}[x]^4} \\
& \quad \left(b + 2a \tanh[x]^2 + 2\sqrt{a} \sqrt{c + b \tanh[x]^2 + a \tanh[x]^4}\right) \Bigg)
\end{aligned}$$

Timed out after 60 seconds:

$$\begin{aligned}
& \{\tanh[x] \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}, x, 6, 0\} \\
& \frac{(b + 2c) \operatorname{ArcTanh}\left[\frac{b + 2c \tanh[x]^2}{2\sqrt{c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}\right]}{4\sqrt{c}} + \\
& \frac{1}{2} \sqrt{a + b + c} \operatorname{ArcTanh}\left[\frac{2a + b + (b + 2c) \tanh[x]^2}{2\sqrt{a + b + c} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4}}\right] - \frac{1}{2} \sqrt{a + b \tanh[x]^2 + c \tanh[x]^4} \\
& ???
\end{aligned}$$

Timed out after 60 seconds:

$$\{\operatorname{Coth}[x] \sqrt{a + b \operatorname{Coth}[x]^2 + c \operatorname{Coth}[x]^4}, x, 6, 0\}$$

$$\begin{aligned}
& - \frac{(b+2c) \operatorname{ArcTanh}\left[\frac{b+2c \coth[x]^2}{2\sqrt{c} \sqrt{a+b \coth[x]^2+c \coth[x]^4}}\right]}{4\sqrt{c}} + \\
& \frac{1}{2} \sqrt{a+b+c} \operatorname{ArcTanh}\left[\frac{2a+b+(b+2c) \coth[x]^2}{2\sqrt{a+b+c} \sqrt{a+b \coth[x]^2+c \coth[x]^4}}\right] - \frac{1}{2} \sqrt{a+b \coth[x]^2+c \coth[x]^4} \\
& ???
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{A+B \cosh[x]+C \sinh[x]}{(a+b \cosh[x]+c \sinh[x])^3}, x, 3, 0 \right\} \\
& - \frac{(2a^2A+b(Ab-3aB)-c(Ac-3aC)) \operatorname{ArcTanh}\left[\frac{c-(a-b) \tanh\left[\frac{x}{2}\right]}{\sqrt{a^2-b^2+c^2}}\right]}{(a^2-b^2+c^2)^{5/2}} - \frac{Bc-bC+(Ac-aC) \cosh[x]+(Ab-aB) \sinh[x]}{2(a^2-b^2+c^2)(a+b \cosh[x]+c \sinh[x])^2} - \\
& \frac{aBc-abC+(a(3Ac-aC)-2c(bB-cC)) \cosh[x]+(a(3Ab-aB)-2b(bB-cC)) \sinh[x]}{2(a^2-b^2+c^2)^2(a+b \cosh[x]+c \sinh[x])} \\
& \frac{(2a^2A+Ab^2-3abB-Ac^2+3acC) \operatorname{ArcTan}\left[\frac{c+(-a+b) \tanh\left[\frac{x}{2}\right]}{\sqrt{-a^2+b^2-c^2}}\right]}{(a^2+b^2-c^2)^{5/2}} + \frac{1}{4b(a^2-b^2+c^2)^2(a+b \cosh[x]+c \sinh[x])^2} \\
& (6a^3Ac+3aAb^2c-9a^2bBc-3aAc^3-2a^4C+4a^2b^2C-2b^4C+5a^2c^2C+4b^2c^2C-2c^4C+ \\
& 2bc(2a^2A+Ab^2-3abB-Ac^2+3acC) \cosh[x]+c(3aA(-b^2+c^2)+a^2(bB-cC)+2(b^2-c^2)(bB-cC)) \cosh[2x]- \\
& 8a^2Ab^2 \sinh[x]+2Ab^4 \sinh[x]+4a^3bB \sinh[x]+2ab^3B \sinh[x]+12a^2Ac^2 \sinh[x]-2Ab^2c^2 \sinh[x]- \\
& 8abBc^2 \sinh[x]-4a^3cC \sinh[x]-2ab^2cC \sinh[x]+8a^3cC \sinh[x]-3aAb^3 \sinh[2x]+a^2b^2B \sinh[2x]+ \\
& 2b^4B \sinh[2x]+3aAbc^2 \sinh[2x]-2b^2Bc^2 \sinh[2x]-a^2b cC \sinh[2x]-2b^3cC \sinh[2x]+2b c^3C \sinh[2x])
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{e^x \tanh[2x], x, 8, 0\} \\
& e^x + \frac{\operatorname{ArcTan}[1-\sqrt{2} e^x]}{\sqrt{2}} - \frac{\operatorname{ArcTan}[1+\sqrt{2} e^x]}{\sqrt{2}} + \frac{\operatorname{Log}[1-\sqrt{2} e^x+e^{2x}]}{2\sqrt{2}} - \frac{\operatorname{Log}[1+\sqrt{2} e^x+e^{2x}]}{2\sqrt{2}} \\
& e^x + \frac{1}{2} \operatorname{RootSum}\left[1+\#1^4 \&, \frac{x-\operatorname{Log}[e^x-\#1]}{\#1^3} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{e^x \tanh[3x], x, 7, 0\} \\
& e^x - \frac{2 \operatorname{ArcTan}[e^x]}{3} - \frac{1}{3} \operatorname{ArcTan}\left[\frac{e^x}{1-e^{2x}}\right] - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3} e^x}{1+e^{2x}}\right]}{\sqrt{3}} \\
& e^x - \frac{2 \operatorname{ArcTan}[e^x]}{3} - \frac{1}{3} \operatorname{RootSum}\left[1-\#1^2+\#1^4 \&, \frac{-2x+2 \operatorname{Log}[-e^x+\#1]+x \#1^2-\operatorname{Log}[-e^x+\#1] \#1^2}{-\#1+2 \#1^3} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \tanh[4x], x, 10, 0\}$$

$$e^x - \frac{1}{4} \sqrt{2 - \sqrt{2}} \operatorname{ArcTan}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 - e^{2x}}\right] - \frac{1}{4} \sqrt{2 + \sqrt{2}} \operatorname{ArcTan}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 - e^{2x}}\right] -$$

$$\frac{1}{4} \sqrt{2 - \sqrt{2}} \operatorname{ArcTanh}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 + e^{2x}}\right] - \frac{1}{4} \sqrt{2 + \sqrt{2}} \operatorname{ArcTanh}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 + e^{2x}}\right]$$

$$e^x + \frac{1}{4} \operatorname{RootSum}\left[1 + \#1^8 \&, \frac{x - \operatorname{Log}[e^x - \#1]}{\#1^7} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Tanh}[2x]^2, x, 17, 0\}$$

$$e^x + \frac{e^x}{1 + e^{4x}} + \frac{\operatorname{ArcTan}[1 - \sqrt{2} e^x]}{2\sqrt{2}} - \frac{\operatorname{ArcTan}[1 + \sqrt{2} e^x]}{2\sqrt{2}} + \frac{\operatorname{Log}[1 - \sqrt{2} e^x + e^{2x}]}{4\sqrt{2}} - \frac{\operatorname{Log}[1 + \sqrt{2} e^x + e^{2x}]}{4\sqrt{2}}$$

$$e^x + \frac{e^x}{1 + e^{4x}} + \frac{1}{4} \operatorname{RootSum}\left[1 + \#1^4 \&, \frac{x - \operatorname{Log}[e^x - \#1]}{\#1^3} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Tanh}[3x]^2, x, 17, 0\}$$

$$e^x + \frac{2e^x}{3(1 + e^{6x})} - \frac{2\operatorname{ArcTan}[e^x]}{9} - \frac{1}{9} \operatorname{ArcTan}\left[\frac{e^x}{1 - e^{2x}}\right] - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3} e^x}{1 + e^{2x}}\right]}{3\sqrt{3}}$$

$$e^x + \frac{2e^x}{3(1 + e^{6x})} - \frac{2\operatorname{ArcTan}[e^x]}{9} - \frac{1}{9} \operatorname{RootSum}\left[1 - \#1^2 + \#1^4 \&, \frac{-2x + 2\operatorname{Log}[-e^x + \#1] + x\#1^2 - \operatorname{Log}[-e^x + \#1]\#1^2}{-\#1 + 2\#1^3} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Tanh}[4x]^2, x, 21, 0\}$$

$$e^x + \frac{e^x}{2(1 + e^{8x})} - \frac{1}{16} \sqrt{2 - \sqrt{2}} \operatorname{ArcTan}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 - e^{2x}}\right] - \frac{1}{16} \sqrt{2 + \sqrt{2}} \operatorname{ArcTan}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 - e^{2x}}\right] -$$

$$\frac{1}{16} \sqrt{2 - \sqrt{2}} \operatorname{ArcTanh}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 + e^{2x}}\right] - \frac{1}{16} \sqrt{2 + \sqrt{2}} \operatorname{ArcTanh}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 + e^{2x}}\right]$$

$$e^x + \frac{e^x}{2(1 + e^{8x})} + \frac{1}{16} \operatorname{RootSum}\left[1 + \#1^8 \&, \frac{x - \operatorname{Log}[e^x - \#1]}{\#1^7} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Coth}[4x], x, 10, 0\}$$

$$e^x - \frac{\operatorname{ArcTan}[e^x]}{2} + \frac{\operatorname{ArcTan}[1 - \sqrt{2} e^x]}{2\sqrt{2}} - \frac{\operatorname{ArcTan}[1 + \sqrt{2} e^x]}{2\sqrt{2}} - \frac{\operatorname{ArcTanh}[e^x]}{2} + \frac{\operatorname{Log}[1 - \sqrt{2} e^x + e^{2x}]}{4\sqrt{2}} - \frac{\operatorname{Log}[1 + \sqrt{2} e^x + e^{2x}]}{4\sqrt{2}}$$

$$\frac{1}{4} \left(4e^x - 2\operatorname{ArcTan}[e^x] + \operatorname{Log}[1 - e^x] - \operatorname{Log}[1 + e^x] + \operatorname{RootSum}\left[1 + \#1^4 \&, \frac{x - \operatorname{Log}[e^x - \#1]}{\#1^3} \&\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Coth}[4x]^2, x, 25, 0\}$$

$$\begin{aligned}
& e^x + \frac{e^x}{2(1 - e^{8x})} - \frac{\text{ArcTan}[e^x]}{8} + \frac{\text{ArcTan}[1 - \sqrt{2} e^x]}{8\sqrt{2}} - \\
& \frac{\text{ArcTan}[1 + \sqrt{2} e^x]}{8\sqrt{2}} - \frac{\text{ArcTanh}[e^x]}{8} + \frac{\text{Log}[1 - \sqrt{2} e^x + e^{2x}]}{16\sqrt{2}} - \frac{\text{Log}[1 + \sqrt{2} e^x + e^{2x}]}{16\sqrt{2}} \\
& \frac{1}{16} \left(16 e^x - \frac{8 e^x}{-1 + e^{8x}} - 2 \text{ArcTan}[e^x] + \text{Log}[1 - e^x] - \text{Log}[1 + e^x] + \text{RootSum}\left[1 + \#1^4 \&, \frac{x - \text{Log}[e^x - \#1]}{\#1^3} \&\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

 $\{e^x \text{Sech}[2x], x, 7, 0\}$

$$\begin{aligned}
& -\frac{\text{ArcTan}[1 - \sqrt{2} e^x]}{\sqrt{2}} + \frac{\text{ArcTan}[1 + \sqrt{2} e^x]}{\sqrt{2}} + \frac{\text{Log}[1 - \sqrt{2} e^x + e^{2x}]}{2\sqrt{2}} - \frac{\text{Log}[1 + \sqrt{2} e^x + e^{2x}]}{2\sqrt{2}} \\
& -\frac{1}{2} \text{RootSum}\left[1 + \#1^4 \&, \frac{x - \text{Log}[-e^x + \#1]}{\#1} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

 $\{e^x \text{Sech}[3x], x, 7, 0\}$

$$\begin{aligned}
& -\frac{\text{ArcTan}\left[\frac{1-2e^{2x}}{\sqrt{3}}\right]}{\sqrt{3}} - \frac{1}{3} \text{Log}[1 + e^{2x}] + \frac{1}{6} \text{Log}[1 - e^{2x} + e^{4x}] \\
& \frac{2x}{3} - \frac{1}{3} \text{Log}[2(1 + e^{2x})] - \frac{1}{3} \text{RootSum}\left[1 - \#1^2 + \#1^4 \&, \frac{x - \text{Log}[-e^x + \#1]}{\#1^2} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

 $\{e^x \text{Sech}[4x], x, 9, 0\}$

$$\begin{aligned}
& \frac{1}{4} \sqrt{2 + \sqrt{2}} \text{ArcTan}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 - e^{2x}}\right] - \frac{1}{4} \sqrt{2 - \sqrt{2}} \text{ArcTan}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 - e^{2x}}\right] + \\
& \frac{1}{4} \sqrt{2 + \sqrt{2}} \text{ArcTanh}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 + e^{2x}}\right] - \frac{1}{4} \sqrt{2 - \sqrt{2}} \text{ArcTanh}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 + e^{2x}}\right] \\
& -\frac{1}{4} \text{RootSum}\left[1 + \#1^8 \&, \frac{x - \text{Log}[-e^x + \#1]}{\#1^3} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

 $\{e^x \text{Sech}[2x]^2, x, 8, 0\}$

$$\begin{aligned}
& -\frac{e^x}{1 + e^{4x}} - \frac{\text{ArcTan}[1 - \sqrt{2} e^x]}{2\sqrt{2}} + \frac{\text{ArcTan}[1 + \sqrt{2} e^x]}{2\sqrt{2}} - \frac{\text{Log}[1 - \sqrt{2} e^x + e^{2x}]}{4\sqrt{2}} + \frac{\text{Log}[1 + \sqrt{2} e^x + e^{2x}]}{4\sqrt{2}} \\
& -\frac{e^x}{1 + e^{4x}} - \frac{1}{4} \text{RootSum}\left[1 + \#1^4 \&, \frac{x - \text{Log}[-e^x + \#1]}{\#1^3} \&\right]
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

 $\{e^x \text{Sech}[3x]^2, x, 8, 0\}$

$$-\frac{2 e^x}{3 \left(1 + e^{6x}\right)} + \frac{2 \operatorname{ArcTan}\left[e^x\right]}{9} + \frac{1}{9} \operatorname{ArcTan}\left[\frac{e^x}{1 - e^{2x}}\right] + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{3} e^x}{1 + e^{2x}}\right]}{3 \sqrt{3}}$$

$$\frac{1}{9} \left(-\frac{6 e^x}{1 + e^{6x}} + 2 \operatorname{ArcTan}\left[e^x\right] + \operatorname{RootSum}\left[1 - \#1^2 + \#1^4 \&, \frac{-2x + 2 \operatorname{Log}\left[-e^x + \#1\right] + x \#1^2 - \operatorname{Log}\left[-e^x + \#1\right] \#1^2}{-\#1 + 2 \#1^3} \&\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sech}[4x]^2, x, 10, 0\}$$

$$-\frac{e^x}{2 \left(1 + e^{8x}\right)} + \frac{1}{16} \sqrt{2 - \sqrt{2}} \operatorname{ArcTan}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 - e^{2x}}\right] + \frac{1}{16} \sqrt{2 + \sqrt{2}} \operatorname{ArcTan}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 - e^{2x}}\right] +$$

$$\frac{1}{16} \sqrt{2 - \sqrt{2}} \operatorname{ArcTanh}\left[\frac{\sqrt{2 - \sqrt{2}} e^x}{1 + e^{2x}}\right] + \frac{1}{16} \sqrt{2 + \sqrt{2}} \operatorname{ArcTanh}\left[\frac{\sqrt{2 + \sqrt{2}} e^x}{1 + e^{2x}}\right]$$

$$-\frac{e^x}{2 \left(1 + e^{8x}\right)} - \frac{1}{16} \operatorname{RootSum}\left[1 + \#1^8 \&, \frac{x - \operatorname{Log}\left[-e^x + \#1\right]}{\#1^7} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Csch}[2x], x, 5, 0\}$$

$$\operatorname{ArcTan}\left[e^x\right] - \operatorname{ArcTanh}\left[e^x\right]$$

$$\frac{1}{2} \left(2 \operatorname{ArcTan}\left[e^x\right] + \operatorname{Log}\left[-1 + e^x\right] - \operatorname{Log}\left[1 + e^x\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Csch}[4x], x, 11, 0\}$$

$$-\frac{1}{2} \operatorname{ArcTan}\left[e^x\right] - \frac{\operatorname{ArcTan}\left[1 - \sqrt{2} e^x\right]}{2 \sqrt{2}} + \frac{\operatorname{ArcTan}\left[1 + \sqrt{2} e^x\right]}{2 \sqrt{2}} - \frac{\operatorname{ArcTanh}\left[e^x\right]}{2} - \frac{\operatorname{Log}\left[1 - \sqrt{2} e^x + e^{2x}\right]}{4 \sqrt{2}} + \frac{\operatorname{Log}\left[1 + \sqrt{2} e^x + e^{2x}\right]}{4 \sqrt{2}}$$

$$\frac{1}{4} \left(-2 \operatorname{ArcTan}\left[e^x\right] + \operatorname{Log}\left[1 - e^x\right] - \operatorname{Log}\left[1 + e^x\right] - \operatorname{RootSum}\left[1 + \#1^4 \&, \frac{x - \operatorname{Log}\left[-e^x + \#1\right]}{\#1^3} \&\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Csch}[4x]^2, x, 12, 0\}$$

$$\frac{e^x}{2 \left(1 - e^{8x}\right)} - \frac{\operatorname{ArcTan}\left[e^x\right]}{8} + \frac{\operatorname{ArcTan}\left[1 - \sqrt{2} e^x\right]}{8 \sqrt{2}} - \frac{\operatorname{ArcTan}\left[1 + \sqrt{2} e^x\right]}{8 \sqrt{2}} - \frac{\operatorname{ArcTanh}\left[e^x\right]}{8} + \frac{\operatorname{Log}\left[1 - \sqrt{2} e^x + e^{2x}\right]}{16 \sqrt{2}} - \frac{\operatorname{Log}\left[1 + \sqrt{2} e^x + e^{2x}\right]}{16 \sqrt{2}}$$

$$\frac{1}{16} \left(-\frac{8 e^x}{-1 + e^{8x}} - 2 \operatorname{ArcTan}\left[e^x\right] + \operatorname{Log}\left[1 - e^x\right] - \operatorname{Log}\left[1 + e^x\right] + \operatorname{RootSum}\left[1 + \#1^4 \&, \frac{x - \operatorname{Log}\left[e^x - \#1\right]}{\#1^3} \&\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sech}[2x] \operatorname{Tanh}[2x], x, 10, 0\}$$

$$-\frac{e^{3x}}{1 + e^{4x}} - \frac{\operatorname{ArcTan}\left[1 - \sqrt{2} e^x\right]}{2 \sqrt{2}} + \frac{\operatorname{ArcTan}\left[1 + \sqrt{2} e^x\right]}{2 \sqrt{2}} + \frac{\operatorname{Log}\left[1 - \sqrt{2} e^x + e^{2x}\right]}{4 \sqrt{2}} - \frac{\operatorname{Log}\left[1 + \sqrt{2} e^x + e^{2x}\right]}{4 \sqrt{2}}$$

$$-\frac{e^{3x}}{1 + e^{4x}} - \frac{1}{4} \operatorname{RootSum}\left[1 + \#1^4 \&, \frac{x - \operatorname{Log}\left[-e^x + \#1\right]}{\#1} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sech}[2x]^2 \operatorname{Tanh}[2x], x, 11, 0\}$$

$$-\frac{e^x}{3(1+e^{4x})^2} - \frac{4e^{5x}}{3(1+e^{4x})^2} + \frac{e^x}{12(1+e^{4x})} - \frac{\operatorname{ArcTan}[1-\sqrt{2}e^x]}{8\sqrt{2}} +$$

$$\frac{\operatorname{ArcTan}[1+\sqrt{2}e^x]}{8\sqrt{2}} - \frac{\operatorname{Log}[1-\sqrt{2}e^x+e^{2x}]}{16\sqrt{2}} + \frac{\operatorname{Log}[1+\sqrt{2}e^x+e^{2x}]}{16\sqrt{2}}$$

$$-\frac{e^x(1+5e^{4x})}{4(1+e^{4x})^2} - \frac{1}{16} \operatorname{RootSum}\left[1+\#1^4 \&, \frac{x-\operatorname{Log}[-e^x+\#1]}{\#1^3} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sech}[2x] \operatorname{Tanh}[2x]^2, x, 12, 0\}$$

$$-\frac{e^{3x}}{(1+e^{4x})^2} - \frac{2e^{7x}}{(1+e^{4x})^2} + \frac{5e^{3x}}{4(1+e^{4x})} - \frac{5\operatorname{ArcTan}[1-\sqrt{2}e^x]}{8\sqrt{2}} +$$

$$\frac{5\operatorname{ArcTan}[1+\sqrt{2}e^x]}{8\sqrt{2}} + \frac{5\operatorname{Log}[1-\sqrt{2}e^x+e^{2x}]}{16\sqrt{2}} - \frac{5\operatorname{Log}[1+\sqrt{2}e^x+e^{2x}]}{16\sqrt{2}}$$

$$\frac{e^{3x}-3e^{7x}}{4(1+e^{4x})^2} - \frac{5}{16} \operatorname{RootSum}\left[1+\#1^4 \&, \frac{x-\operatorname{Log}[-5e^x+5\#1]}{\#1} \&\right]$$

Valid but unnecessarily complicated antiderivative:

$$\{e^x \operatorname{Sech}[2x]^2 \operatorname{Tanh}[2x]^2, x, 13, 0\}$$

$$-\frac{4e^x}{7(1+e^{4x})^3} - \frac{4e^{5x}}{7(1+e^{4x})^3} - \frac{4e^{9x}}{3(1+e^{4x})^3} + \frac{e^x}{14(1+e^{4x})^2} + \frac{e^x}{8(1+e^{4x})} -$$

$$\frac{3\operatorname{ArcTan}[1-\sqrt{2}e^x]}{16\sqrt{2}} + \frac{3\operatorname{ArcTan}[1+\sqrt{2}e^x]}{16\sqrt{2}} - \frac{3\operatorname{Log}[1-\sqrt{2}e^x+e^{2x}]}{32\sqrt{2}} + \frac{3\operatorname{Log}[1+\sqrt{2}e^x+e^{2x}]}{32\sqrt{2}}$$

$$\frac{1}{96} \left(-\frac{4e^x(9+6e^{4x}+29e^{8x})}{(1+e^{4x})^3} - 9 \operatorname{RootSum}\left[1+\#1^4 \&, \frac{x-\operatorname{Log}[-3e^x+3\#1]}{\#1^3} \&\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{e^x}{a - \operatorname{Tanh}[2x]}, x, 6, 0 \right\}$$

$$-\frac{e^x}{1-a} + \frac{\operatorname{ArcTan}\left[\frac{(1-a)^{1/4}e^x}{(1+a)^{1/4}}\right]}{(1-a)^{5/4}(1+a)^{3/4}} + \frac{\operatorname{ArcTanh}\left[\frac{(1-a)^{1/4}e^x}{(1+a)^{1/4}}\right]}{(1-a)^{5/4}(1+a)^{3/4}}$$

$$\frac{2(-1+a)e^x + \operatorname{RootSum}\left[1+a-\#1^4 \&, \frac{x-\operatorname{Log}[-e^x+\#1]}{\#1^3} \&\right]}{2(-1+a)^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{e^x}{(a - \operatorname{Tanh}[2x])^2}, x, 13, 0 \right\}$$

$$\frac{e^x}{(1-a)^2} + \frac{e^x}{(1-a)^2(1+a)(1+a-(1-a)e^{4x})} + \frac{(1-2a)\text{ArcTan}\left[\frac{(1-a)^{1/4}e^x}{(1+a)^{1/4}}\right]}{2(1-a)^{9/4}(1+a)^{7/4}} - \frac{\text{ArcTan}\left[\frac{(1-a)^{1/4}e^x}{(1+a)^{1/4}}\right]}{(1-a)^{9/4}(1+a)^{3/4}} + \frac{(1-2a)\text{ArcTanh}\left[\frac{(1-a)^{1/4}e^x}{(1+a)^{1/4}}\right]}{2(1-a)^{9/4}(1+a)^{7/4}} - \frac{\text{ArcTanh}\left[\frac{(1-a)^{1/4}e^x}{(1+a)^{1/4}}\right]}{(1-a)^{9/4}(1+a)^{3/4}} - \frac{4(-1+a)e^x + \frac{4(-1+a)e^x}{(1+a)(1+e^{4x}+ae^{4x})} + \frac{(1+4a)\text{RootSum}\left[1+a-11^4+a11^4\&, \frac{x-\text{Log}[-e^x+1]}{11^3}\&]\right]}{1+a}}{4(-1+a)^3}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Sech}[x]^2}{a+b\text{Tanh}[x]}, x, 2, 0\right\}$$

$$\frac{\text{Log}[a+b\text{Tanh}[x]]}{b}$$

$$\frac{-\text{Log}[\text{Cosh}[x]] + \text{Log}[-a\text{Cosh}[x] - b\text{Sinh}[x]]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Sech}[x]^2}{\sqrt{4-\text{Sech}[x]^2}}, x, 2, 0\right\}$$

$$\frac{\text{ArcSinh}\left[\frac{\text{Tanh}[x]}{\sqrt{3}}\right]}{1}$$

$$3\sqrt{2+\text{Sech}[x]^2+2\text{Tanh}[x]^2}$$

$$2i\text{Cosh}\left[\frac{x}{2}\right]^2\left(\text{EllipticF}\left[i\text{ArcSinh}\left[\sqrt{3}\text{Tanh}\left[\frac{x}{2}\right]\right], \frac{1}{9}\right)-2\text{EllipticPi}\left[\frac{1}{3}, i\text{ArcSinh}\left[\sqrt{3}\text{Tanh}\left[\frac{x}{2}\right]\right], \frac{1}{9}\right]\right)$$

$$\text{Sech}[x]\sqrt{3+\text{Tanh}\left[\frac{x}{2}\right]^2}\sqrt{1+3\text{Tanh}\left[\frac{x}{2}\right]^2}$$

FullSimplify::infd:

$$\text{Expression} - \left((-7+4\sqrt{3})(5-3\text{Cosh}[2x])^2 \text{Sech}\left[\frac{x}{2}\right]^4 \text{Sech}[x]^4 \right) / \left(16\sqrt{\frac{4+2\sqrt{3}-3\text{Cosh}[x]-2\sqrt{3}\text{Cosh}[x]}{1+\text{Cosh}[x]}} \right.$$

$$\sqrt{\frac{4-2\sqrt{3}+(3-2\text{Power}[\<<2\>>])\text{Cosh}[x]}{1+\text{Cosh}[x]}} \sqrt{\frac{4-2\sqrt{3}+(-3+2\text{Power}[\<<2\>>])\text{Cosh}[x]}{1+\text{Cosh}[x]}}$$

$$\left. \sqrt{\frac{52-30\sqrt{3}+(-45+26\text{Power}[\<<2\>>])\text{Cosh}[x]}{1+\text{Cosh}[x]}} (1-4\text{Tanh}[x]^2)^{3/2} \right) \text{simplified to Indeterminate. } \gg$$

FullSimplify::infd:

$$\text{Expression} - \left((-7 + 4\sqrt{3}) (5 - 3 \cosh[2x])^2 \operatorname{sech}\left[\frac{x}{2}\right]^4 \operatorname{sech}[x]^4 \right) / \left(16 \sqrt{\frac{4 + 2\sqrt{3} - 3 \cosh[x] - 2\sqrt{3} \cosh[x]}{1 + \cosh[x]}} \right. \\ \left. \sqrt{\frac{4 - 2\sqrt{3} + (3 + \operatorname{Times}[\llcorner 2 \ggcorner]) \cosh[x]}{1 + \cosh[x]}} \sqrt{\frac{4 - 2\sqrt{3} + (-3 + \operatorname{Times}[\llcorner 2 \ggcorner]) \cosh[x]}{1 + \cosh[x]}} \right. \\ \left. \sqrt{\frac{52 - 30\sqrt{3} + (-45 + \operatorname{Times}[\llcorner 2 \ggcorner]) \cosh[x]}{1 + \cosh[x]}} (1 - 4 \tanh[x]^2)^{3/2} \right) - \frac{\operatorname{sech}[x]^2}{\sqrt{1 - 4 \tanh[x]^2}}$$

simplified to Indeterminate. >>

Incorrect antiderivative:

$$\left\{ \frac{\operatorname{sech}[x]^2}{\sqrt{1 - 4 \tanh[x]^2}}, x, 2, 0 \right\} \\ - \frac{1}{\sqrt{1 - 4 \tanh[x]^2}} \\ 2 \cosh\left[\frac{x}{2}\right]^2 \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tanh\left[\frac{x}{2}\right]}{\sqrt{7 - 4\sqrt{3}}}\right], 97 - 56\sqrt{3}\right] + 2 \operatorname{EllipticPi}\left[-7 + 4\sqrt{3}, -\operatorname{ArcSin}\left[\frac{\tanh\left[\frac{x}{2}\right]}{\sqrt{7 - 4\sqrt{3}}}\right], 97 - 56\sqrt{3}\right] \right) \\ \operatorname{sech}[x] \sqrt{7 - 4\sqrt{3} - \tanh\left[\frac{x}{2}\right]^2} \sqrt{1 + (-7 + 4\sqrt{3}) \tanh\left[\frac{x}{2}\right]^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{sech}[x]^2}{\sqrt{-4 + \tanh[x]^2}}, x, 2, 0 \right\} \\ \operatorname{ArcTanh}\left[\frac{\tanh[x]}{\sqrt{-4 + \tanh[x]^2}}\right] \\ - \frac{1}{\sqrt{-4 + \tanh[x]^2}} 2 (-1)^{2/3} \cosh\left[\frac{x}{2}\right]^2 \\ \left(\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[(-1)^{5/6} \tanh\left[\frac{x}{2}\right]\right], (-1)^{2/3}\right] + 2 \operatorname{EllipticPi}\left[(-1)^{1/3}, -i \operatorname{ArcSinh}\left[(-1)^{5/6} \tanh\left[\frac{x}{2}\right]\right], (-1)^{2/3}\right] \right) \\ \operatorname{sech}[x] \sqrt{1 + (-1)^{1/3} \tanh\left[\frac{x}{2}\right]^2} \sqrt{1 - (-1)^{2/3} \tanh\left[\frac{x}{2}\right]^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{1 + \coth[x]^2} \operatorname{sech}[x]^2, x, 4, 0 \right\} \\ - \operatorname{ArcCsch}[\tanh[x]] + \sqrt{1 + \coth[x]^2} \tanh[x]$$

$$\sqrt{1 + \coth[x]^2} \left(\frac{\operatorname{ArcTan}\left[\frac{\cosh[x]}{\sqrt{-\cosh[2x]}}\right] \sinh[x]}{\sqrt{-\cosh[2x]}} + \tanh[x] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned} & \left\{ \operatorname{Sech}[x]^2 \sqrt{1 + \tanh[x]^2}, x, 3, 0 \right\} \\ & \frac{1}{2} \operatorname{ArcSinh}[\tanh[x]] + \frac{1}{2} \tanh[x] \sqrt{1 + \tanh[x]^2} \\ & \frac{1}{2} \left(2 i \cosh\left[\frac{x}{2}\right]^2 \cosh[x] \right. \\ & \quad \left. \left(\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\tanh\left[\frac{x}{2}\right]}{\sqrt{3 + 2\sqrt{2}}}\right], 17 + 12\sqrt{2}\right] - 2 \operatorname{EllipticPi}\left[3 + 2\sqrt{2}, i \operatorname{ArcSinh}\left[\frac{\tanh\left[\frac{x}{2}\right]}{\sqrt{3 + 2\sqrt{2}}}\right], 17 + 12\sqrt{2}\right] \right) \right. \\ & \quad \left. \operatorname{Sech}[2x] \sqrt{3 + 2\sqrt{2} + \tanh\left[\frac{x}{2}\right]^2} \sqrt{1 + \left(3 + 2\sqrt{2}\right) \tanh\left[\frac{x}{2}\right]^2 + \tanh[x]} \sqrt{1 + \tanh[x]^2} \right) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned} & \left\{ \frac{\operatorname{Sech}[x]^2}{2 + 2 \tanh[x] + \tanh[x]^2}, x, 2, 0 \right\} \\ & \operatorname{ArcTan}[1 + \tanh[x]] \\ & \frac{1}{2} (-\operatorname{ArcTan}[\cosh[x] (\cosh[x] - \sinh[x])] + \operatorname{ArcTan}[1 + \tanh[x]]) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned} & \left\{ \frac{\operatorname{Sech}[x]^2 (a + b \tanh[x])}{c + d \tanh[x]}, x, 4, 0 \right\} \\ & - \frac{(b c - a d) \operatorname{Log}[c + d \tanh[x]]}{d^2} + \frac{b \tanh[x]}{d} \\ & \frac{1}{d^2 (c + d \tanh[x])} \\ & \operatorname{Sech}[x]^2 (c \cosh[x] + d \sinh[x]) ((b c - a d) \cosh[x] (\operatorname{Log}[\cosh[x]] - \operatorname{Log}[c \cosh[x] + d \sinh[x]]) + b d \sinh[x]) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned} & \left\{ \frac{(a + b \coth[x]) \operatorname{Csch}[x]^2}{c + d \coth[x]}, x, 4, 0 \right\} \\ & - \frac{b \coth[x]}{d} + \frac{(b c - a d) \operatorname{Log}[c + d \coth[x]]}{d^2} \\ & - \frac{1}{d^2 (c + d \coth[x])} \\ & \operatorname{Csch}[x]^2 (d \cosh[x] + c \sinh[x]) (b d \cosh[x] + (b c - a d) (\operatorname{Log}[\sinh[x]] - \operatorname{Log}[d \cosh[x] + c \sinh[x]]) \sinh[x]) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\{\text{Cosh}[x]^3 (a + b \text{Cosh}[x]^2)^3 \text{Sinh}[x], x, 4, 0\}$$

$$-\frac{a (a + b \text{Cosh}[x]^2)^4}{40 b^2} + \frac{\text{Cosh}[x]^2 (a + b \text{Cosh}[x]^2)^4}{10 b}$$

$$\frac{1}{32} \left(12 a^2 b \text{Cosh}[x]^4 + 8 a b^2 \text{Cosh}[x]^6 + 2 b^3 \text{Cosh}[x]^8 + 4 a^3 \text{Cosh}[2 x] + \right. \\ \left. 4 a^2 b \text{Cosh}[x]^3 \text{Cosh}[3 x] + a^3 \text{Cosh}[4 x] + \frac{1}{32} a b^2 (48 \text{Cosh}[2 x] + 36 \text{Cosh}[4 x] + 16 \text{Cosh}[6 x] + 3 \text{Cosh}[8 x]) + \right. \\ \left. \frac{1}{320} b^3 (140 \text{Cosh}[2 x] + 100 \text{Cosh}[4 x] + 50 \text{Cosh}[6 x] + 15 \text{Cosh}[8 x] + 2 \text{Cosh}[10 x]) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\text{Cosh}[x] \text{Sinh}[x]^3 (a + b \text{Sinh}[x]^2)^3, x, 4, 0\}$$

$$-\frac{a (a + b \text{Sinh}[x]^2)^4}{40 b^2} + \frac{\text{Sinh}[x]^2 (a + b \text{Sinh}[x]^2)^4}{10 b}$$

$$\frac{1}{10240} \left(-20 (64 a^3 + 24 a b^2 - 7 b^3) \text{Cosh}[2 x] + 20 (16 a^3 + 18 a b^2 - 5 b^3) \text{Cosh}[4 x] + \right. \\ \left. b (-10 (16 a - 5 b) b \text{Cosh}[6 x] + 15 (2 a - b) b \text{Cosh}[8 x] + 2 (b^2 \text{Cosh}[10 x] + 160 ((-4 a + b)^2 - b^2 \text{Cosh}[2 x]) \text{Sinh}[x]^6)) \right)$$