

# Mathematica 7 Test Results

## For Integration Problems Involving Logarithms

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}\left[\frac{a}{x}\right]}{a x - x^2}, x, 1, 0 \right\}$$

$$\frac{\text{PolyLog}\left[2, 1 - \frac{a}{x}\right]}{a}$$

$$\frac{1}{2 a} \left( 2 \text{Log}\left[\frac{a}{x}\right] (\text{Log}[x] - \text{Log}[-a + x]) + \text{Log}[x] \left( \text{Log}[x] - 2 \text{Log}[-a + x] + 2 \text{Log}\left[1 - \frac{x}{a}\right] \right) + 2 \text{PolyLog}\left[2, \frac{x}{a}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}\left[\frac{a}{x^2}\right]}{a x - x^3}, x, 1, 0 \right\}$$

$$\frac{\text{PolyLog}\left[2, 1 - \frac{a}{x^2}\right]}{2 a}$$

$$\frac{1}{2 a} \left( 2 \text{Log}\left[\frac{a}{x^2}\right] \text{Log}[x] + 2 \text{Log}[x]^2 + 2 \text{Log}[x] \text{Log}\left[1 - \frac{x}{\sqrt{a}}\right] + 2 \text{Log}[x] \text{Log}\left[1 + \frac{x}{\sqrt{a}}\right] - \right.$$

$$\left. \text{Log}\left[\frac{a}{x^2}\right] \text{Log}[-a + x^2] - 2 \text{Log}[x] \text{Log}[-a + x^2] + 2 \text{PolyLog}\left[2, -\frac{x}{\sqrt{a}}\right] + 2 \text{PolyLog}\left[2, \frac{x}{\sqrt{a}}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}\left[\frac{x}{a}\right]}{a - x}, x, 1, 0 \right\}$$

$$\text{PolyLog}\left[2, 1 - \frac{x}{a}\right]$$

$$-\text{Log}\left[\frac{x}{a}\right] \text{Log}\left[1 - \frac{x}{a}\right] - \text{PolyLog}\left[2, \frac{x}{a}\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x \text{Log}\left[\frac{x^2}{a}\right]}{a - x^2}, x, 2, 0 \right\}$$

$$\frac{1}{2} \text{PolyLog}\left[2, 1 - \frac{x^2}{a}\right]$$

$$\frac{1}{2} \left( -\text{Log}\left[\frac{x^2}{a}\right] \text{Log}\left[1 - \frac{x^2}{a}\right] - \text{PolyLog}\left[2, \frac{x^2}{a}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a + b \text{Log}[c (d + e x)^n])^4, x, 5, 0 \right\}$$

$$\begin{aligned}
& -24 a b^3 n^3 x + 24 b^4 n^4 x - \frac{24 b^4 n^3 (d+ex) \operatorname{Log}[c (d+ex)^n]}{e} + \frac{12 b^2 n^2 (d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^2}{e} - \\
& \frac{4 b n (d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^3}{e} + \frac{(d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^4}{e} \\
& \frac{1}{e} \left( -b^4 d n^4 \operatorname{Log}[d+ex]^4 + 4 b^3 d n^3 \operatorname{Log}[d+ex]^3 (a-b n + b \operatorname{Log}[c (d+ex)^n]) - \right. \\
& 6 b^2 d n^2 \operatorname{Log}[d+ex]^2 (a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a-b n) \operatorname{Log}[c (d+ex)^n] + b^2 \operatorname{Log}[c (d+ex)^n]^2) + \\
& 4 b d n \operatorname{Log}[d+ex] (a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3 + \\
& 3 b (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d+ex)^n] + 3 b^2 (a-b n) \operatorname{Log}[c (d+ex)^n]^2 + b^3 \operatorname{Log}[c (d+ex)^n]^3) + \\
& ex (a^4 - 4 a^3 b n + 12 a^2 b^2 n^2 - 24 a b^3 n^3 + 24 b^4 n^4 + 4 b (a^3 - 3 a^2 b n + 6 a b^2 n^2 - 6 b^3 n^3) \operatorname{Log}[c (d+ex)^n] + \\
& \left. 6 b^2 (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d+ex)^n]^2 + 4 b^3 (a-b n) \operatorname{Log}[c (d+ex)^n]^3 + b^4 \operatorname{Log}[c (d+ex)^n]^4) \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{ (a+b \operatorname{Log}[c (d+ex)^n])^3, x, 4, 0 \} \\
& 6 a b^2 n^2 x - 6 b^3 n^3 x + \frac{6 b^3 n^2 (d+ex) \operatorname{Log}[c (d+ex)^n]}{e} - \\
& \frac{3 b n (d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^2}{e} + \frac{(d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^3}{e} \\
& \frac{1}{e} \left( b^3 d n^3 \operatorname{Log}[d+ex]^3 - 3 b^2 d n^2 \operatorname{Log}[d+ex]^2 (a-b n + b \operatorname{Log}[c (d+ex)^n]) + \right. \\
& 3 b d n \operatorname{Log}[d+ex] (a^2 - 2 a b n + 2 b^2 n^2 + 2 b (a-b n) \operatorname{Log}[c (d+ex)^n] + b^2 \operatorname{Log}[c (d+ex)^n]^2) + ex (a^3 - 3 a^2 b n + 6 a b^2 n^2 - \\
& \left. 6 b^3 n^3 + 3 b (a^2 - 2 a b n + 2 b^2 n^2) \operatorname{Log}[c (d+ex)^n] + 3 b^2 (a-b n) \operatorname{Log}[c (d+ex)^n]^2 + b^3 \operatorname{Log}[c (d+ex)^n]^3) \right)
\end{aligned}$$

Unable to integrate:

$$\begin{aligned}
& \{ (a+b \operatorname{Log}[c (d+ex)^n])^{5/2}, x, 4, 0 \} \\
& \frac{15 b^{5/2} e^{-\frac{a}{b n}} n^{5/2} \sqrt{\pi} (d+ex) (c (d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8 e} + \\
& \frac{15 b^2 n^2 (d+ex) \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{4 e} - \frac{5 b n (d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^{3/2}}{2 e} + \frac{(d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^{5/2}}{e} \\
& \int (a+b \operatorname{Log}[c (d+ex)^n])^{5/2} dx
\end{aligned}$$

Unable to integrate:

$$\begin{aligned}
& \{ (a+b \operatorname{Log}[c (d+ex)^n])^{3/2}, x, 3, 0 \} \\
& \frac{3 b^{3/2} e^{-\frac{a}{b n}} n^{3/2} \sqrt{\pi} (d+ex) (c (d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4 e} - \\
& \frac{3 b n (d+ex) \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}}{2 e} + \frac{(d+ex) (a+b \operatorname{Log}[c (d+ex)^n])^{3/2}}{e} \\
& \int (a+b \operatorname{Log}[c (d+ex)^n])^{3/2} dx
\end{aligned}$$

Unable to integrate:

$$\{ \sqrt{a+b \operatorname{Log}[c (d+ex)^n]}, x, 2, 0 \}$$

# Mathematica 7 Test Results for Integration Problems Involving Logarithms

$$-\frac{\sqrt{b} e^{-\frac{a}{bn}} \sqrt{n} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erfi}\left[\frac{\sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2 e} + \frac{(d+ex) \sqrt{a+b \operatorname{Log}[c(d+ex)^n]}}{e} \int \sqrt{a+b \operatorname{Log}[c(d+ex)^n]} dx$$

Unable to integrate:

$$\{(a-b \operatorname{Log}[c(d+ex)^n])^{5/2}, x, 4, 0\}$$

$$-\frac{15 b^{5/2} e^{\frac{a}{bn}} n^{5/2} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erf}\left[\frac{\sqrt{a-b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{8 e} + \frac{15 b^2 n^2 (d+ex) \sqrt{a-b \operatorname{Log}[c(d+ex)^n]}}{4 e} + \frac{5 b n (d+ex) (a-b \operatorname{Log}[c(d+ex)^n])^{3/2}}{2 e} + \frac{(d+ex) (a-b \operatorname{Log}[c(d+ex)^n])^{5/2}}{e} \int (a-b \operatorname{Log}[c(d+ex)^n])^{5/2} dx$$

Unable to integrate:

$$\{(a-b \operatorname{Log}[c(d+ex)^n])^{3/2}, x, 3, 0\}$$

$$-\frac{3 b^{3/2} e^{\frac{a}{bn}} n^{3/2} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erf}\left[\frac{\sqrt{a-b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{4 e} + \frac{3 b n (d+ex) \sqrt{a-b \operatorname{Log}[c(d+ex)^n]}}{2 e} + \frac{(d+ex) (a-b \operatorname{Log}[c(d+ex)^n])^{3/2}}{e} \int (a-b \operatorname{Log}[c(d+ex)^n])^{3/2} dx$$

Unable to integrate:

$$\{\sqrt{a-b \operatorname{Log}[c(d+ex)^n]}, x, 2, 0\}$$

$$-\frac{\sqrt{b} e^{\frac{a}{bn}} \sqrt{n} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-1/n} \operatorname{Erf}\left[\frac{\sqrt{a-b \operatorname{Log}[c(d+ex)^n]}}{\sqrt{b} \sqrt{n}}\right]}{2 e} + \frac{(d+ex) \sqrt{a-b \operatorname{Log}[c(d+ex)^n]}}{e} \int \sqrt{a-b \operatorname{Log}[c(d+ex)^n]} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\operatorname{Log}[1+ax^n]}{x}, x, 1, 0\right\}$$

$$-\frac{\operatorname{PolyLog}[2, -ax^n]}{n}$$

$$\frac{\operatorname{Log}[-ax^n] \operatorname{Log}[1+ax^n] + \operatorname{PolyLog}[2, 1+ax^n]}{n}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\operatorname{Log}[x^{-n}(a+x^n)]}{x}, x, 2, 0\right\}$$

$$\frac{\text{PolyLog}[2, -a x^{-n}]}{n}$$

$$\frac{1}{2} \text{Log}[x] \left( n \text{Log}[x] + 2 \text{Log}[1 + a x^{-n}] - 2 \text{Log}\left[\frac{a + x^n}{a}\right] \right) - \frac{\text{PolyLog}\left[2, -\frac{x^n}{a}\right]}{n}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}[a + b x^2]^2}{x^3}, x, 4, 0 \right\}$$

$$\frac{b \text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[a + b x^2]}{a} - \frac{(a + b x^2) \text{Log}[a + b x^2]^2}{2 a x^2} + \frac{b \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right]}{a}$$

$$- \frac{\text{Log}[a + b x^2]^2}{2 x^2} -$$

$$\begin{aligned} & \frac{1}{2 a} b \left( \text{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + \text{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 \text{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \text{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \text{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \text{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + \right. \\ & 4 \text{Log}[x] \text{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \text{Log}[x] \text{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] - 4 \text{Log}[x] \text{Log}[a + b x^2] - \\ & 2 \text{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \text{Log}[a + b x^2] - 2 \text{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \text{Log}[a + b x^2] + 2 \text{Log}[a + b x^2]^2 + \\ & \left. 4 \text{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \text{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 \text{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \text{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}[c (a + b x^2)^n]^2}{x}, x, 5, 0 \right\}$$

$$\frac{1}{2} \text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[c (a + b x^2)^n]^2 + n \text{Log}[c (a + b x^2)^n] \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - n^2 \text{PolyLog}\left[3, \frac{a + b x^2}{a}\right]$$

$$\text{Log}[x] \left( -n \text{Log}[a + b x^2] + \text{Log}[c (a + b x^2)^n] \right)^2 +$$

$$2 n \left( -n \text{Log}[a + b x^2] + \text{Log}[c (a + b x^2)^n] \right) \left( \text{Log}[x] \left( \text{Log}[a + b x^2] - \text{Log}\left[1 + \frac{b x^2}{a}\right] \right) - \frac{1}{2} \text{PolyLog}\left[2, -\frac{b x^2}{a}\right] \right) +$$

$$\frac{1}{2} n^2 \left( \text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[a + b x^2]^2 + 2 \text{Log}[a + b x^2] \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}[c (a + b x^2)^n]^2}{x^3}, x, 4, 0 \right\}$$

$$\frac{b n \text{Log}\left[-\frac{b x^2}{a}\right] \text{Log}[c (a + b x^2)^n]}{a} - \frac{(a + b x^2) \text{Log}[c (a + b x^2)^n]^2}{2 a x^2} + \frac{b n^2 \text{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right]}{a}$$

$$\frac{n \left( -2 b x^2 \operatorname{Log}[x] + (a + b x^2) \operatorname{Log}[a + b x^2] \right) \left( n \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^n] \right)}{a x^2} -$$

$$\frac{\left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right)^2}{2 x^2} + n^2 \left( -\frac{\operatorname{Log}[a + b x^2]^2}{2 x^2} - \right.$$

$$\frac{1}{2 a} b \left( \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + \right.$$

$$4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] - 4 \operatorname{Log}[x] \operatorname{Log}[a + b x^2] - 2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] -$$

$$2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] + 2 \operatorname{Log}[a + b x^2]^2 + 4 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] +$$

$$\left. \left. 4 \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Log}[c (a + b x^2)^n]^3}{x}, x, 6, 0 \right\}$$

$$\frac{1}{2} \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[c (a + b x^2)^n]^3 + \frac{3}{2} n \operatorname{Log}[c (a + b x^2)^n]^2 \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] -$$

$$3 n^2 \operatorname{Log}[c (a + b x^2)^n] \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] + 3 n^3 \operatorname{PolyLog}\left[4, \frac{a + b x^2}{a}\right]$$

$$\operatorname{Log}[x] \left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right)^3 +$$

$$3 n \left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right)^2 \left( \operatorname{Log}[x] \left( \operatorname{Log}[a + b x^2] - \operatorname{Log}\left[1 + \frac{b x^2}{a}\right] \right) - \frac{1}{2} \operatorname{PolyLog}\left[2, -\frac{b x^2}{a}\right] \right) -$$

$$\frac{3}{2} n^2 \left( n \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^n] \right)$$

$$\left( \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[a + b x^2]^2 + 2 \operatorname{Log}[a + b x^2] \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - 2 \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] \right) + \frac{1}{2} n^3 \left( \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[a + b x^2]^3 + \right.$$

$$\left. 3 \operatorname{Log}[a + b x^2]^2 \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] - 6 \operatorname{Log}[a + b x^2] \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] + 6 \operatorname{PolyLog}\left[4, 1 + \frac{b x^2}{a}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Log}[c (a + b x^2)^n]^3}{x^3}, x, 6, 0 \right\}$$

$$\frac{3 b n \operatorname{Log}\left[-\frac{b x^2}{a}\right] \operatorname{Log}[c (a + b x^2)^n]^2}{2 a} - \frac{(a + b x^2) \operatorname{Log}[c (a + b x^2)^n]^3}{2 a x^2} +$$

$$\frac{3 b n^2 \operatorname{Log}[c (a + b x^2)^n] \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right]}{a} - \frac{3 b n^3 \operatorname{PolyLog}\left[3, \frac{a + b x^2}{a}\right]}{a}$$

$$\begin{aligned}
& \frac{1}{2} \left( \frac{\left( n \operatorname{Log}[a + b x^2] - \operatorname{Log}[c (a + b x^2)^n] \right)^3}{x^2} + \right. \\
& \frac{6 b n \operatorname{Log}[x] \left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right)^2}{a} - \frac{3 b n \operatorname{Log}[a + b x^2] \left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right)^2}{a} - \\
& \frac{3 n \operatorname{Log}[a + b x^2] \left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right)^2}{x^2} + 6 n^2 \left( -n \operatorname{Log}[a + b x^2] + \operatorname{Log}[c (a + b x^2)^n] \right) \\
& \left( -\frac{\operatorname{Log}[a + b x^2]^2}{2 x^2} - \frac{1}{2 a} b \left( \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right]^2 + 2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + \right. \right. \\
& 2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}\left[\frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 4 \operatorname{Log}[x] \operatorname{Log}\left[1 - \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \operatorname{Log}[x] \operatorname{Log}\left[1 + \frac{i \sqrt{b} x}{\sqrt{a}}\right] - \\
& 4 \operatorname{Log}[x] \operatorname{Log}[a + b x^2] - 2 \operatorname{Log}\left[-\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] - 2 \operatorname{Log}\left[\frac{i \sqrt{a}}{\sqrt{b}} + x\right] \operatorname{Log}[a + b x^2] + 2 \operatorname{Log}[a + b x^2]^2 + \\
& \left. \left. 4 \operatorname{PolyLog}\left[2, -\frac{i \sqrt{b} x}{\sqrt{a}}\right] + 4 \operatorname{PolyLog}\left[2, \frac{i \sqrt{b} x}{\sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} - \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] + 2 \operatorname{PolyLog}\left[2, \frac{1}{2} + \frac{i \sqrt{b} x}{2 \sqrt{a}}\right] \right) \right) - \\
& \frac{1}{a x^2} n^3 \left( \operatorname{Log}[a + b x^2]^2 \left( -3 b x^2 \operatorname{Log}\left[-\frac{b x^2}{a}\right] + (a + b x^2) \operatorname{Log}[a + b x^2] \right) - 6 b x^2 \operatorname{Log}[a + b x^2] \operatorname{PolyLog}\left[2, 1 + \frac{b x^2}{a}\right] + \right. \\
& \left. \left. 6 b x^2 \operatorname{PolyLog}\left[3, 1 + \frac{b x^2}{a}\right] \right) \right)
\end{aligned}$$

Unable to integrate:

$$\left\{ \operatorname{Log}\left[\frac{c x}{b + a x}\right]^3, x, 6, 0 \right\}$$

$$\frac{3 b \operatorname{Log}\left[\frac{b}{b + a x}\right] \operatorname{Log}\left[\frac{c x}{b + a x}\right]^2}{a} + x \operatorname{Log}\left[\frac{c x}{b + a x}\right]^3 + \frac{6 b \operatorname{Log}\left[\frac{c x}{b + a x}\right] \operatorname{PolyLog}\left[2, \frac{a x}{b + a x}\right]}{a} - \frac{6 b \operatorname{PolyLog}\left[3, \frac{a x}{b + a x}\right]}{a}$$

$$\int \operatorname{Log}\left[\frac{c x}{b + a x}\right]^3 dx$$

Unable to integrate:

$$\left\{ \operatorname{Log}\left[\frac{c (b + a x)^2}{x^2}\right]^3, x, 7, 0 \right\}$$

$$\frac{(b + a x) \operatorname{Log}\left[c \left(a + \frac{b}{x}\right)^2\right]^3}{a} - \frac{6 b \operatorname{Log}\left[c \left(a + \frac{b}{x}\right)^2\right]^2 \operatorname{Log}\left[-\frac{b}{a x}\right]}{a} - \frac{24 b \operatorname{Log}\left[c \left(a + \frac{b}{x}\right)^2\right] \operatorname{PolyLog}\left[2, 1 + \frac{b}{a x}\right]}{a} + \frac{48 b \operatorname{PolyLog}\left[3, \frac{a + \frac{b}{x}}{a}\right]}{a}$$

$$\int \operatorname{Log}\left[\frac{c (b + a x)^2}{x^2}\right]^3 dx$$

Unable to integrate:

$$\left\{ \operatorname{Log}\left[\frac{c x^2}{(b + a x)^2}\right]^3, x, 7, 0 \right\}$$

$$\frac{(b + a x) \operatorname{Log}\left[\frac{c}{\left(a + \frac{b}{x}\right)^2}\right]^3}{a} + \frac{6 b \operatorname{Log}\left[\frac{c}{\left(a + \frac{b}{x}\right)^2}\right]^2 \operatorname{Log}\left[-\frac{b}{a x}\right]}{a} - \frac{24 b \operatorname{Log}\left[\frac{c}{\left(a + \frac{b}{x}\right)^2}\right] \operatorname{PolyLog}\left[2, 1 + \frac{b}{a x}\right]}{a} - \frac{48 b \operatorname{PolyLog}\left[3, \frac{a + \frac{b}{x}}{a}\right]}{a}$$

$$\int \text{Log}\left[\frac{c x^2}{(b + a x)^2}\right]^3 dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]^3, x, 6, 0\right\}$$

$$\frac{(b + a x) \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]^3}{a} - \frac{3 b n \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]^2 \text{Log}\left[-\frac{b}{a x}\right]}{a} - \frac{6 b n^2 \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right] \text{PolyLog}\left[2, 1 + \frac{b}{a x}\right]}{a} + \frac{6 b n^3 \text{PolyLog}\left[3, \frac{a + \frac{b}{x}}{a}\right]}{a}$$

$$3 n x \text{Log}\left[a + \frac{b}{x}\right] \left(-n \text{Log}\left[a + \frac{b}{x}\right] + \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]\right)^2 + x \left(-n \text{Log}\left[a + \frac{b}{x}\right] + \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]\right)^3 +$$

$$\frac{3 b n \left(-n \text{Log}\left[a + \frac{b}{x}\right] + \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]\right)^2 \text{Log}[b + a x]}{a} + 3 n^2 \left(-n \text{Log}\left[a + \frac{b}{x}\right] + \text{Log}\left[c\left(a + \frac{b}{x}\right)^n\right]\right) \left(x \text{Log}\left[a + \frac{b}{x}\right]^2 +$$

$$\frac{b \left(\text{Log}\left[\frac{b}{a} + x\right]^2 + 2 \left(\text{Log}\left[a + \frac{b}{x}\right] + \text{Log}[x] - \text{Log}\left[\frac{b}{a} + x\right]\right) \text{Log}[b + a x] - 2 \left(\text{Log}[x] \text{Log}\left[1 + \frac{a x}{b}\right] + \text{PolyLog}\left[2, -\frac{a x}{b}\right]\right)\right)}{a}\right) +$$

$$\frac{n^3 \left(\text{Log}\left[a + \frac{b}{x}\right]^2 \left((b + a x) \text{Log}\left[a + \frac{b}{x}\right] - 3 b \text{Log}\left[-\frac{b}{a x}\right]\right) - 6 b \text{Log}\left[a + \frac{b}{x}\right] \text{PolyLog}\left[2, 1 + \frac{b}{a x}\right] + 6 b \text{PolyLog}\left[3, 1 + \frac{b}{a x}\right]\right)}{a}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Log}[1 + b x^m]}{x}, x, 1, 0\right\}$$

$$- \frac{\text{PolyLog}[2, -b x^m]}{m}$$

$$\frac{\text{Log}[-b x^m] \text{Log}[1 + b x^m] + \text{PolyLog}[2, 1 + b x^m]}{m}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Log}\left[c\left(a + b x^m\right)^n\right]^2}{x}, x, 5, 0\right\}$$

$$\frac{\text{Log}\left[-\frac{b x^m}{a}\right] \text{Log}\left[c\left(a + b x^m\right)^n\right]^2}{m} + \frac{2 n \text{Log}\left[c\left(a + b x^m\right)^n\right] \text{PolyLog}\left[2, 1 + \frac{b x^m}{a}\right]}{m} - \frac{2 n^2 \text{PolyLog}\left[3, \frac{a + b x^m}{a}\right]}{m}$$

$$\text{Log}[x] \left(-n \text{Log}[a + b x^m] + \text{Log}\left[c\left(a + b x^m\right)^n\right]\right)^2 +$$

$$2 n \left(-n \text{Log}[a + b x^m] + \text{Log}\left[c\left(a + b x^m\right)^n\right]\right) \left(\text{Log}[x] \left(\text{Log}[a + b x^m] - \text{Log}\left[1 + \frac{b x^m}{a}\right]\right) - \frac{\text{PolyLog}\left[2, -\frac{b x^m}{a}\right]}{m}\right) +$$

$$\frac{n^2 \left(\text{Log}\left[-\frac{b x^m}{a}\right] \text{Log}[a + b x^m]^2 + 2 \text{Log}[a + b x^m] \text{PolyLog}\left[2, 1 + \frac{b x^m}{a}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{b x^m}{a}\right]\right)}{m}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\text{Log}\left[c\left(a + b x^m\right)^n\right]^3}{x}, x, 6, 0\right\}$$

$$\begin{aligned}
& \frac{\operatorname{Log}\left[-\frac{bx^m}{a}\right] \operatorname{Log}\left[c(a+bx^m)^n\right]^3}{m} + \frac{3n \operatorname{Log}\left[c(a+bx^m)^n\right]^2 \operatorname{PolyLog}\left[2, 1+\frac{bx^m}{a}\right]}{m} - \\
& \frac{6n^2 \operatorname{Log}\left[c(a+bx^m)^n\right] \operatorname{PolyLog}\left[3, 1+\frac{bx^m}{a}\right]}{m} + \frac{6n^3 \operatorname{PolyLog}\left[4, \frac{a+bx^m}{a}\right]}{m} \\
& \frac{1}{m} \left( -m n^3 \operatorname{Log}[x] \operatorname{Log}[a+bx^m]^3 + n^3 \operatorname{Log}\left[-\frac{bx^m}{a}\right] \operatorname{Log}[a+bx^m]^3 + 3 m n^2 \operatorname{Log}[x] \operatorname{Log}[a+bx^m]^2 \operatorname{Log}\left[c(a+bx^m)^n\right] - \right. \\
& \quad 3 n^2 \operatorname{Log}\left[-\frac{bx^m}{a}\right] \operatorname{Log}[a+bx^m]^2 \operatorname{Log}\left[c(a+bx^m)^n\right] - 3 m n \operatorname{Log}[x] \operatorname{Log}[a+bx^m] \operatorname{Log}\left[c(a+bx^m)^n\right]^2 + \\
& \quad 3 n \operatorname{Log}\left[-\frac{bx^m}{a}\right] \operatorname{Log}[a+bx^m] \operatorname{Log}\left[c(a+bx^m)^n\right]^2 + m \operatorname{Log}[x] \operatorname{Log}\left[c(a+bx^m)^n\right]^3 + \\
& \quad \left. 3 n \operatorname{Log}\left[c(a+bx^m)^n\right]^2 \operatorname{PolyLog}\left[2, 1+\frac{bx^m}{a}\right] - 6 n^2 \operatorname{Log}\left[c(a+bx^m)^n\right] \operatorname{PolyLog}\left[3, 1+\frac{bx^m}{a}\right] + 6 n^3 \operatorname{PolyLog}\left[4, 1+\frac{bx^m}{a}\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Log}\left[c(a+bx)^n\right]^2}{x}, x, 4, 0 \right\} \\
& \operatorname{Log}\left[-\frac{bx}{a}\right] \operatorname{Log}\left[c(a+bx)^n\right]^2 + 2n \operatorname{Log}\left[c(a+bx)^n\right] \operatorname{PolyLog}\left[2, 1+\frac{bx}{a}\right] - 2n^2 \operatorname{PolyLog}\left[3, \frac{a+bx}{a}\right] \\
& \operatorname{Log}[x] \left( -n \operatorname{Log}[a+bx] + \operatorname{Log}\left[c(a+bx)^n\right] \right)^2 + \\
& 2n \left( -n \operatorname{Log}[a+bx] + \operatorname{Log}\left[c(a+bx)^n\right] \right) \left( \operatorname{Log}[x] \left( \operatorname{Log}[a+bx] - \operatorname{Log}\left[1+\frac{bx}{a}\right] \right) - \operatorname{PolyLog}\left[2, -\frac{bx}{a}\right] \right) + \\
& n^2 \left( \operatorname{Log}\left[-\frac{bx}{a}\right] \operatorname{Log}[a+bx]^2 + 2 \operatorname{Log}[a+bx] \operatorname{PolyLog}\left[2, 1+\frac{bx}{a}\right] - 2 \operatorname{PolyLog}\left[3, 1+\frac{bx}{a}\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Log}\left[c(a+bx)^n\right]^3}{x}, x, 5, 0 \right\} \\
& \operatorname{Log}\left[-\frac{bx}{a}\right] \operatorname{Log}\left[c(a+bx)^n\right]^3 + 3n \operatorname{Log}\left[c(a+bx)^n\right]^2 \operatorname{PolyLog}\left[2, 1+\frac{bx}{a}\right] - \\
& 6n^2 \operatorname{Log}\left[c(a+bx)^n\right] \operatorname{PolyLog}\left[3, 1+\frac{bx}{a}\right] + 6n^3 \operatorname{PolyLog}\left[4, \frac{a+bx}{a}\right] \\
& \operatorname{Log}[x] \left( -n \operatorname{Log}[a+bx] + \operatorname{Log}\left[c(a+bx)^n\right] \right)^3 + \\
& 3n \left( -n \operatorname{Log}[a+bx] + \operatorname{Log}\left[c(a+bx)^n\right] \right)^2 \left( \operatorname{Log}[x] \left( \operatorname{Log}[a+bx] - \operatorname{Log}\left[1+\frac{bx}{a}\right] \right) - \operatorname{PolyLog}\left[2, -\frac{bx}{a}\right] \right) - \\
& 3n^2 \left( n \operatorname{Log}[a+bx] - \operatorname{Log}\left[c(a+bx)^n\right] \right) \left( \operatorname{Log}\left[-\frac{bx}{a}\right] \operatorname{Log}[a+bx]^2 + 2 \operatorname{Log}[a+bx] \operatorname{PolyLog}\left[2, 1+\frac{bx}{a}\right] - 2 \operatorname{PolyLog}\left[3, 1+\frac{bx}{a}\right] \right) + \\
& n^3 \left( \operatorname{Log}\left[-\frac{bx}{a}\right] \operatorname{Log}[a+bx]^3 + 3 \operatorname{Log}[a+bx]^2 \operatorname{PolyLog}\left[2, 1+\frac{bx}{a}\right] - 6 \operatorname{Log}[a+bx] \operatorname{PolyLog}\left[3, 1+\frac{bx}{a}\right] + 6 \operatorname{PolyLog}\left[4, 1+\frac{bx}{a}\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Log}\left[c(a+bx)^n\right]^3}{x^2}, x, 5, 0 \right\} \\
& \frac{3bn \operatorname{Log}\left[-\frac{bx}{a}\right] \operatorname{Log}\left[c(a+bx)^n\right]^2}{a} - \frac{(a+bx) \operatorname{Log}\left[c(a+bx)^n\right]^3}{ax} + \\
& \frac{6bn^2 \operatorname{Log}\left[c(a+bx)^n\right] \operatorname{PolyLog}\left[2, 1+\frac{bx}{a}\right]}{a} - \frac{6bn^3 \operatorname{PolyLog}\left[3, \frac{a+bx}{a}\right]}{a}
\end{aligned}$$



$$\begin{aligned}
& -\frac{1}{a x} \left( -3 b n^3 x \operatorname{Log}[x] \operatorname{Log}[a + b x]^2 + 3 b n^3 x \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[a + b x]^2 + b n^3 x \operatorname{Log}[a + b x]^3 + \right. \\
& 6 b n^2 x \operatorname{Log}[x] \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n] - 6 b n^2 x \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n] - \\
& 3 b n^2 x \operatorname{Log}[a + b x]^2 \operatorname{Log}[c (a + b x)^n] - 3 b n x \operatorname{Log}[x] \operatorname{Log}[c (a + b x)^n]^2 + 3 b n x \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n]^2 + \\
& \left. a \operatorname{Log}[c (a + b x)^n]^3 - 6 b n^2 x \operatorname{Log}[c (a + b x)^n] \operatorname{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + 6 b n^3 x \operatorname{PolyLog}\left[3, 1 + \frac{b x}{a}\right] \right)
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Log}[c (a + b x)^n]^3}{x^3}, x, 9, 0 \right\} \\
& \frac{3 b^2 n^2 \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[c (a + b x)^n]}{a^2} - \frac{3 b n (a + b x) \operatorname{Log}[c (a + b x)^n]^2}{2 a^2 x} - \frac{3 b^2 n \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[c (a + b x)^n]^2}{2 a^2} + \\
& \frac{b^2 \operatorname{Log}[c (a + b x)^n]^3}{2 a^2} - \frac{\operatorname{Log}[c (a + b x)^n]^3}{2 x^2} + \frac{3 b^2 n^2 (n - \operatorname{Log}[c (a + b x)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{b x}{a}\right]}{a^2} + \frac{3 b^2 n^3 \operatorname{PolyLog}\left[3, \frac{a + b x}{a}\right]}{a^2} \\
& \frac{1}{2 a^2 x^2} \left( 3 b^2 n^3 x^2 \operatorname{Log}[a + b x]^2 - 3 b^2 n^3 x^2 \operatorname{Log}[x] \operatorname{Log}[a + b x]^2 + 3 b^2 n^3 x^2 \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[a + b x]^2 + b^2 n^3 x^2 \operatorname{Log}[a + b x]^3 + \right. \\
& 6 b^2 n^2 x^2 \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[c (a + b x)^n] - 6 b^2 n^2 x^2 \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n] + 6 b^2 n^2 x^2 \operatorname{Log}[x] \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n] - \\
& 6 b^2 n^2 x^2 \operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n] - 3 b^2 n^2 x^2 \operatorname{Log}[a + b x]^2 \operatorname{Log}[c (a + b x)^n] - \\
& 3 a b n x \operatorname{Log}[c (a + b x)^n]^2 - 3 b^2 n x^2 \operatorname{Log}[x] \operatorname{Log}[c (a + b x)^n]^2 + 3 b^2 n x^2 \operatorname{Log}[a + b x] \operatorname{Log}[c (a + b x)^n]^2 - \\
& \left. a^2 \operatorname{Log}[c (a + b x)^n]^3 + 6 b^2 n^2 x^2 (n - \operatorname{Log}[c (a + b x)^n]) \operatorname{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + 6 b^2 n^3 x^2 \operatorname{PolyLog}\left[3, 1 + \frac{b x}{a}\right] \right)
\end{aligned}$$

Unable to integrate:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Log}[(c + d x)^2]^2}{a + b x}, x, 4, 0 \right\} \\
& \frac{\operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[(c + d x)^2]^2}{b} + \frac{4 \operatorname{Log}[(c + d x)^2] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b} - \frac{8 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b} \\
& \int \frac{\operatorname{Log}[(c + d x)^2]^2}{a + b x} dx
\end{aligned}$$

Unable to integrate:

$$\begin{aligned}
& \left\{ \frac{\operatorname{Log}[(c + d x)^2]^2}{(a + b x)^2}, x, 6, 0 \right\} \\
& \frac{4 d \operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[(c + d x)^2]}{b (b c - a d)} - \frac{d \operatorname{Log}[(c + d x)^2]^2}{b (b c - a d)} - \frac{\operatorname{Log}[(c + d x)^2]^2}{b (a + b x)} + \frac{8 d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b (b c - a d)} \\
& \int \frac{\operatorname{Log}[(c + d x)^2]^2}{(a + b x)^2} dx
\end{aligned}$$

Unable to integrate:

$$\left\{ \frac{\operatorname{Log}[(c + d x)^2]^2}{(a + b x)^3}, x, 12, 0 \right\}$$

$$\frac{4 d^2 \operatorname{Log}[a + b x]}{b (b c - a d)^2} - \frac{4 d^2 \operatorname{Log}[c + d x]}{b (b c - a d)^2} - \frac{2 d \operatorname{Log}[(c + d x)^2]}{b (b c - a d) (a + b x)} -$$

$$\frac{2 d^2 \operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[(c + d x)^2]}{b (b c - a d)^2} + \frac{d^2 \operatorname{Log}[(c + d x)^2]^2}{2 b (b c - a d)^2} - \frac{\operatorname{Log}[(c + d x)^2]^2}{2 b (a + b x)^2} - \frac{4 d^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b (b c - a d)^2}$$

$$\int \frac{\operatorname{Log}[(c + d x)^2]^2}{(a + b x)^3} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Log}[(c + d x)^3]^2}{a + b x}, x, 4, 0 \right\}$$

$$\frac{\operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[(c + d x)^3]^2}{b} + \frac{6 \operatorname{Log}[(c + d x)^3] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b} - \frac{18 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b}$$

$$\frac{1}{b} \left( 9 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}[a + b x] - 9 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] - \right.$$

$$6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] \operatorname{Log}[(c + d x)^3] + 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[(c + d x)^3] +$$

$$\left. \operatorname{Log}[a + b x] \operatorname{Log}[(c + d x)^3]^2 + 6 \operatorname{Log}[(c + d x)^3] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 18 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right)$$

Unable to integrate:

$$\left\{ \frac{\operatorname{Log}[(c + d x)^2]^3}{a + b x}, x, 5, 0 \right\}$$

$$\frac{\operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[(c + d x)^2]^3}{b} + \frac{6 \operatorname{Log}[(c + d x)^2]^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b} -$$

$$\frac{24 \operatorname{Log}[(c + d x)^2] \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b} + \frac{48 \operatorname{PolyLog}\left[4, \frac{b (c + d x)}{b c - a d}\right]}{b}$$

$$\int \frac{\operatorname{Log}[(c + d x)^2]^3}{a + b x} dx$$

Unable to integrate:

$$\left\{ \frac{\operatorname{Log}[(c + d x)^2]^3}{(a + b x)^2}, x, 9, 0 \right\}$$

$$\frac{6 d \operatorname{Log}\left[-\frac{d (a + b x)}{b c - a d}\right] \operatorname{Log}[(c + d x)^2]^2}{b (b c - a d)} - \frac{d \operatorname{Log}[(c + d x)^2]^3}{b (b c - a d)} -$$

$$\frac{\operatorname{Log}[(c + d x)^2]^3}{b (a + b x)} + \frac{24 d \operatorname{Log}[(c + d x)^2] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b (b c - a d)} - \frac{48 d \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right]}{b (b c - a d)}$$

$$\int \frac{\operatorname{Log}[(c + d x)^2]^3}{(a + b x)^2} dx$$

Unable to integrate:

$$\left\{ \frac{\text{Log}[(c+dx)^2]^3}{(a+bx)^3}, x, 15, 0 \right\}$$

$$\frac{12 d^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^2]}{b(bc-ad)^2} - \frac{3 d^2 \text{Log}[(c+dx)^2]^2}{b(bc-ad)^2} - \frac{3 d \text{Log}[(c+dx)^2]^2}{b(bc-ad)(a+bx)} - \frac{3 d^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^2]^2}{b(bc-ad)^2} +$$

$$\frac{d^2 \text{Log}[(c+dx)^2]^3}{2b(bc-ad)^2} - \frac{\text{Log}[(c+dx)^2]^3}{2b(a+bx)^2} + \frac{12 d^2 (2 - \text{Log}[(c+dx)^2]) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)^2} + \frac{24 d^2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)^2}$$

$$\int \frac{\text{Log}[(c+dx)^2]^3}{(a+bx)^3} dx$$

Unable to integrate:

$$\left\{ \frac{\text{Log}[(c+dx)^3]^3}{a+bx}, x, 5, 0 \right\}$$

$$\frac{\text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^3]^3}{b} + \frac{9 \text{Log}[(c+dx)^3]^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b} -$$

$$\frac{54 \text{Log}[(c+dx)^3] \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b} + \frac{162 \text{PolyLog}\left[4, \frac{b(c+dx)}{bc-ad}\right]}{b}$$

$$\int \frac{\text{Log}[(c+dx)^3]^3}{a+bx} dx$$

Unable to integrate:

$$\left\{ \frac{\text{Log}[(c+dx)^3]^3}{(a+bx)^2}, x, 9, 0 \right\}$$

$$\frac{9 d \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^3]^2}{b(bc-ad)} - \frac{d \text{Log}[(c+dx)^3]^3}{b(bc-ad)} -$$

$$\frac{\text{Log}[(c+dx)^3]^3}{b(a+bx)} + \frac{54 d \text{Log}[(c+dx)^3] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)} - \frac{162 d \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)}$$

$$\int \frac{\text{Log}[(c+dx)^3]^3}{(a+bx)^2} dx$$

Unable to integrate:

$$\left\{ \frac{\text{Log}[(c+dx)^3]^3}{(a+bx)^3}, x, 15, 0 \right\}$$

$$\frac{27 d^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^3]}{b(bc-ad)^2} - \frac{9 d^2 \text{Log}[(c+dx)^3]^2}{2b(bc-ad)^2} - \frac{9 d \text{Log}[(c+dx)^3]^2}{2b(bc-ad)(a+bx)} - \frac{9 d^2 \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^3]^2}{2b(bc-ad)^2} +$$

$$\frac{d^2 \text{Log}[(c+dx)^3]^3}{2b(bc-ad)^2} - \frac{\text{Log}[(c+dx)^3]^3}{2b(a+bx)^2} + \frac{27 d^2 (3 - \text{Log}[(c+dx)^3]) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)^2} + \frac{81 d^2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)^2}$$

$$\int \frac{\text{Log}[(c+dx)^3]^3}{(a+bx)^3} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}[(c+dx)^n]^3}{a+bx}, x, 5, 0 \right\}$$

$$\frac{\text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^n]^3}{b} + \frac{3n \text{Log}[(c+dx)^n]^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b} -$$

$$\frac{6n^2 \text{Log}[(c+dx)^n] \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b} + \frac{6n^3 \text{PolyLog}\left[4, \frac{b(c+dx)}{bc-ad}\right]}{b}$$

$$\frac{1}{b} \left( -n^3 \text{Log}[a+bx] \text{Log}[c+dx]^3 + n^3 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx]^3 + 3n^2 \text{Log}[a+bx] \text{Log}[c+dx]^2 \text{Log}[(c+dx)^n] - \right.$$

$$3n^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx]^2 \text{Log}[(c+dx)^n] - 3n \text{Log}[a+bx] \text{Log}[c+dx] \text{Log}[(c+dx)^n]^2 +$$

$$3n \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx] \text{Log}[(c+dx)^n]^2 + \text{Log}[a+bx] \text{Log}[(c+dx)^n]^3 +$$

$$\left. 3n \text{Log}[(c+dx)^n]^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 6n^2 \text{Log}[(c+dx)^n] \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 6n^3 \text{PolyLog}\left[4, \frac{b(c+dx)}{bc-ad}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\text{Log}[(c+dx)^n]^3}{(a+bx)^2}, x, 9, 0 \right\}$$

$$\frac{3dn \text{Log}\left[-\frac{d(a+bx)}{bc-ad}\right] \text{Log}[(c+dx)^n]^2}{b(bc-ad)} - \frac{d \text{Log}[(c+dx)^n]^3}{b(bc-ad)} -$$

$$\frac{\text{Log}[(c+dx)^n]^3}{b(a+bx)} + \frac{6dn^2 \text{Log}[(c+dx)^n] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)} - \frac{6dn^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]}{b(bc-ad)}$$

$$\frac{1}{b} \left( \frac{(n \text{Log}[c+dx] - \text{Log}[(c+dx)^n])^3}{a+bx} + \right.$$

$$\frac{3dn \text{Log}[a+bx] (-n \text{Log}[c+dx] + \text{Log}[(c+dx)^n])^2}{bc-ad} + \frac{3dn \text{Log}[c+dx] (-n \text{Log}[c+dx] + \text{Log}[(c+dx)^n])^2}{-bc+ad} -$$

$$\frac{3n \text{Log}[c+dx] (-n \text{Log}[c+dx] + \text{Log}[(c+dx)^n])^2}{a+bx} + \frac{1}{(bc-ad)(a+bx)} 3n^2 (n \text{Log}[c+dx] - \text{Log}[(c+dx)^n])$$

$$\left( \text{Log}[c+dx] \left( -2d(a+bx) \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + b(c+dx) \text{Log}[c+dx] \right) - 2d(a+bx) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) -$$

$$\frac{1}{(bc-ad)(a+bx)} n^3 \left( \text{Log}[c+dx]^2 \left( -3d(a+bx) \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + b(c+dx) \text{Log}[c+dx] \right) - \right.$$

$$\left. \left. 6d(a+bx) \text{Log}[c+dx] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 6d(a+bx) \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right)$$

Unable to integrate:

$$\left\{ \frac{x^2 \text{Log}[c+dx]}{a+bx^3}, x, 4, 0 \right\}$$

$$\frac{\text{Log}\left[\frac{d((-1)^{1/3}a^{1/3}-b^{1/3}x)}{b^{1/3}c+(-1)^{1/3}a^{1/3}d}\right] \text{Log}[c+dx]}{3b} + \frac{\text{Log}\left[-\frac{d(a^{1/3}+b^{1/3}x)}{b^{1/3}c-a^{1/3}d}\right] \text{Log}[c+dx]}{3b} + \frac{\text{Log}\left[-\frac{d((-1)^{2/3}a^{1/3}+b^{1/3}x)}{b^{1/3}c-(-1)^{2/3}a^{1/3}d}\right] \text{Log}[c+dx]}{3b} +$$

$$\frac{\text{PolyLog}\left[2, \frac{b^{1/3}(c+dx)}{b^{1/3}c-a^{1/3}d}\right]}{3b} + \frac{\text{PolyLog}\left[2, \frac{b^{1/3}(c+dx)}{b^{1/3}c+(-1)^{1/3}a^{1/3}d}\right]}{3b} + \frac{\text{PolyLog}\left[2, \frac{b^{1/3}(c+dx)}{b^{1/3}c-(-1)^{2/3}a^{1/3}d}\right]}{3b}$$

$$\int \frac{x^2 \text{Log}[c+dx]}{a+bx^3} dx$$

Unable to integrate:

$$\left\{ \frac{x^2 \operatorname{Log}[c + d x]}{a + b x^4}, x, 8, 0 \right\}$$

$$- \frac{i \operatorname{Log}\left[\frac{d(i(-a)^{1/4} - b^{1/4} x)}{b^{1/4} c + i(-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4(-a)^{1/4} b^{3/4}} + \frac{\operatorname{Log}\left[\frac{d((-a)^{1/4} - b^{1/4} x)}{b^{1/4} c + (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4(-a)^{1/4} b^{3/4}} +$$

$$\frac{i \operatorname{Log}\left[-\frac{d(i(-a)^{1/4} + b^{1/4} x)}{b^{1/4} c - i(-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4(-a)^{1/4} b^{3/4}} - \frac{\operatorname{Log}\left[-\frac{d((-a)^{1/4} + b^{1/4} x)}{b^{1/4} c - (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4(-a)^{1/4} b^{3/4}} - \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4(-a)^{1/4} b^{3/4}} +$$

$$\frac{i \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c - i(-a)^{1/4} d}\right]}{4(-a)^{1/4} b^{3/4}} - \frac{i \operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c + i(-a)^{1/4} d}\right]}{4(-a)^{1/4} b^{3/4}} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c + (-a)^{1/4} d}\right]}{4(-a)^{1/4} b^{3/4}}$$

$$\int \frac{x^2 \operatorname{Log}[c + d x]}{a + b x^4} dx$$

Unable to integrate:

$$\left\{ \frac{x^3 \operatorname{Log}[c + d x]}{a + b x^4}, x, 5, 0 \right\}$$

$$\frac{\operatorname{Log}\left[\frac{d(i(-a)^{1/4} - b^{1/4} x)}{b^{1/4} c + i(-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4b} + \frac{\operatorname{Log}\left[\frac{d((-a)^{1/4} - b^{1/4} x)}{b^{1/4} c + (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4b} +$$

$$\frac{\operatorname{Log}\left[-\frac{d(i(-a)^{1/4} + b^{1/4} x)}{b^{1/4} c - i(-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4b} + \frac{\operatorname{Log}\left[-\frac{d((-a)^{1/4} + b^{1/4} x)}{b^{1/4} c - (-a)^{1/4} d}\right] \operatorname{Log}[c + d x]}{4b} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c - (-a)^{1/4} d}\right]}{4b} +$$

$$\frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c - i(-a)^{1/4} d}\right]}{4b} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c + i(-a)^{1/4} d}\right]}{4b} + \frac{\operatorname{PolyLog}\left[2, \frac{b^{1/4}(c + d x)}{b^{1/4} c + (-a)^{1/4} d}\right]}{4b}$$

$$\int \frac{x^3 \operatorname{Log}[c + d x]}{a + b x^4} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\operatorname{Log}[c(a + b x)^n]^3}{d x + e x^2}, x, 12, 0 \right\}$$

$$\frac{\operatorname{Log}\left[-\frac{b x}{a}\right] \operatorname{Log}[c(a + b x)^n]^3}{d} - \frac{\operatorname{Log}[c(a + b x)^n]^3 \operatorname{Log}\left[\frac{b(d + e x)}{b d - a e}\right]}{d} - \frac{3 n \operatorname{Log}[c(a + b x)^n]^2 \operatorname{PolyLog}\left[2, -\frac{e(a + b x)}{b d - a e}\right]}{d} +$$

$$\frac{3 n \operatorname{Log}[c(a + b x)^n]^2 \operatorname{PolyLog}\left[2, 1 + \frac{b x}{a}\right]}{d} + \frac{6 n^2 \operatorname{Log}[c(a + b x)^n] \operatorname{PolyLog}\left[3, -\frac{e(a + b x)}{b d - a e}\right]}{d} -$$

$$\frac{6 n^2 \operatorname{Log}[c(a + b x)^n] \operatorname{PolyLog}\left[3, 1 + \frac{b x}{a}\right]}{d} + \frac{6 n^3 \operatorname{PolyLog}\left[4, \frac{a + b x}{a}\right]}{d} - \frac{6 n^3 \operatorname{PolyLog}\left[4, -\frac{e(a + b x)}{b d - a e}\right]}{d}$$

$$\begin{aligned} & \frac{1}{d} \left( \text{Log}[x] \left( -n \text{Log}[a + b x] + \text{Log}[c (a + b x)^n] \right)^3 + \right. \\ & \quad \left( n \text{Log}[a + b x] - \text{Log}[c (a + b x)^n] \right)^3 \text{Log}[d + e x] + 3 n \left( -n \text{Log}[a + b x] + \text{Log}[c (a + b x)^n] \right)^2 \\ & \quad \left( \text{Log}[x] \text{Log}[a + b x] - \text{Log}[x] \text{Log}\left[1 + \frac{b x}{a}\right] - \text{Log}[a + b x] \text{Log}\left[\frac{b (d + e x)}{b d - a e}\right] - \text{PolyLog}\left[2, -\frac{b x}{a}\right] - \text{PolyLog}\left[2, \frac{e (a + b x)}{-b d + a e}\right] \right) - \\ & \quad 3 n^2 \left( n \text{Log}[a + b x] - \text{Log}[c (a + b x)^n] \right) \left( \text{Log}\left[-\frac{b x}{a}\right] \text{Log}[a + b x]^2 - \text{Log}[a + b x]^2 \text{Log}\left[\frac{b (d + e x)}{b d - a e}\right] - 2 \text{Log}[a + b x] \right. \\ & \quad \left. \text{PolyLog}\left[2, \frac{e (a + b x)}{-b d + a e}\right] + 2 \text{Log}[a + b x] \text{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + 2 \text{PolyLog}\left[3, \frac{e (a + b x)}{-b d + a e}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{b x}{a}\right] \right) + \\ & \quad n^3 \left( \text{Log}\left[-\frac{b x}{a}\right] \text{Log}[a + b x]^3 - \text{Log}[a + b x]^3 \text{Log}\left[\frac{b (d + e x)}{b d - a e}\right] - 3 \text{Log}[a + b x]^2 \text{PolyLog}\left[2, \frac{e (a + b x)}{-b d + a e}\right] + \right. \\ & \quad \left. 3 \text{Log}[a + b x]^2 \text{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + 6 \text{Log}[a + b x] \text{PolyLog}\left[3, \frac{e (a + b x)}{-b d + a e}\right] - \right. \\ & \quad \left. 6 \text{Log}[a + b x] \text{PolyLog}\left[3, 1 + \frac{b x}{a}\right] - 6 \text{PolyLog}\left[4, \frac{e (a + b x)}{-b d + a e}\right] + 6 \text{PolyLog}\left[4, 1 + \frac{b x}{a}\right] \right) \Bigg) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned} & \left\{ \frac{\text{Log}\left[\frac{a+bx}{c+dx}\right]^2}{x}, x, 9, 0 \right\} \\ & -\text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \text{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \text{Log}\left[-\frac{(b c - a d) x}{a (c + d x)}\right] \text{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 \text{Log}\left[\frac{a + b x}{c + d x}\right] \text{PolyLog}\left[2, \frac{d \left(\frac{a}{b} + x\right)}{c + d x}\right] + \\ & \quad 2 \text{Log}\left[\frac{a + b x}{c + d x}\right] \text{PolyLog}\left[2, \frac{c (a + b x)}{a (c + d x)}\right] - 2 \text{PolyLog}\left[3, \frac{c (a + b x)}{a (c + d x)}\right] + 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right] \\ & \text{Log}\left[-\frac{b x}{a}\right] \text{Log}\left[\frac{a}{b} + x\right]^2 + \text{Log}\left[-\frac{d x}{c}\right] \text{Log}\left[\frac{c}{d} + x\right]^2 + \\ & \quad \text{Log}[x] \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 + 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \\ & \quad \left( \text{Log}[x] \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[1 + \frac{b x}{a}\right] + \text{Log}\left[1 + \frac{d x}{c}\right] \right) - \text{PolyLog}\left[2, -\frac{b x}{a}\right] + \text{PolyLog}\left[2, -\frac{d x}{c}\right] \right) + \\ & \quad 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, 1 + \frac{d x}{c}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{b x}{a}\right] - \\ & \quad 2 \left( \text{Log}\left[-\frac{b x}{a}\right] \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] + \frac{1}{2} \text{Log}\left[\frac{a (c + d x)}{c (a + b x)}\right]^2 \left( \text{Log}\left[-\frac{b x}{a}\right] + \text{Log}\left[\frac{-b c + a d}{d (a + b x)}\right] - \text{Log}\left[\frac{b c x - a d x}{a c + b c x}\right] \right) + \right. \\ & \quad \left( -\text{Log}\left[-\frac{b x}{a}\right] + \text{Log}\left[-\frac{d x}{c}\right] \right) \text{Log}\left[\frac{a (c + d x)}{c (a + b x)}\right] \text{Log}\left[1 + \frac{d x}{c}\right] + \frac{1}{2} \left( \text{Log}\left[-\frac{b x}{a}\right] - \text{Log}\left[-\frac{d x}{c}\right] \right) \text{Log}\left[1 + \frac{d x}{c}\right] \\ & \quad \left( -2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[1 + \frac{d x}{c}\right] \right) + \left( \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a (c + d x)}{c (a + b x)}\right] \right) \text{PolyLog}\left[2, 1 + \frac{b x}{a}\right] + \text{Log}\left[\frac{a (c + d x)}{c (a + b x)}\right] \\ & \quad \left( -\text{PolyLog}\left[2, \frac{a (c + d x)}{c (a + b x)}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right] \right) + \left( \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a (c + d x)}{c (a + b x)}\right] \right) \text{PolyLog}\left[2, 1 + \frac{d x}{c}\right] - \\ & \quad \text{PolyLog}\left[3, 1 + \frac{b x}{a}\right] + \text{PolyLog}\left[3, \frac{a (c + d x)}{c (a + b x)}\right] - \text{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right] - \text{PolyLog}\left[3, 1 + \frac{d x}{c}\right] - 2 \text{PolyLog}\left[3, 1 + \frac{d x}{c}\right] \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned} & \left\{ \frac{\text{Log}[x]}{\sqrt{a + b \text{Log}[x]}}, x, 4, 0 \right\} \\ & - \frac{(2 a + b) e^{-\frac{a}{b}} \sqrt{\pi} \text{Erfi}\left[\frac{\sqrt{a + b \text{Log}[x]}}{\sqrt{b}}\right]}{2 b^{3/2}} + \frac{x \sqrt{a + b \text{Log}[x]}}{b} \end{aligned}$$

$$\frac{e^{-\frac{a}{b}} \left( 2 a e^{a/b} x + 2 b e^{a/b} x \operatorname{Log}[x] - 2 a \sqrt{\pi} \sqrt{-\frac{a+b \operatorname{Log}[x]}{b}} - b \sqrt{\pi} \sqrt{-\frac{a+b \operatorname{Log}[x]}{b}} + (2 a + b) \sqrt{\pi} \operatorname{Erf} \left[ \sqrt{-\frac{a+b \operatorname{Log}[x]}{b}} \right] \sqrt{-\frac{a+b \operatorname{Log}[x]}{b}} \right)}{2 b \sqrt{a + b \operatorname{Log}[x]}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{A + B \operatorname{Log}[x]}{\sqrt{a + b \operatorname{Log}[x]}}, x, 4, 0 \right\}$$

$$\frac{(2 A b - (2 a + b) B) e^{-\frac{a}{b}} \sqrt{\pi} \operatorname{Erfi} \left[ \frac{\sqrt{a + b \operatorname{Log}[x]}}{\sqrt{b}} \right]}{2 b^{3/2}} + \frac{B x \sqrt{a + b \operatorname{Log}[x]}}{b}$$

$$\frac{1}{2 b \sqrt{a + b \operatorname{Log}[x]}}$$

$$e^{-\frac{a}{b}} \left( 2 a B e^{a/b} x + 2 b B e^{a/b} x \operatorname{Log}[x] + 2 A b \sqrt{\pi} \sqrt{-\frac{a + b \operatorname{Log}[x]}{b}} - 2 a B \sqrt{\pi} \sqrt{-\frac{a + b \operatorname{Log}[x]}{b}} - b B \sqrt{\pi} \sqrt{-\frac{a + b \operatorname{Log}[x]}{b}} + \right.$$

$$\left. (-2 A b + (2 a + b) B) \sqrt{\pi} \operatorname{Erf} \left[ \sqrt{-\frac{a + b \operatorname{Log}[x]}{b}} \right] \sqrt{-\frac{a + b \operatorname{Log}[x]}{b}} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{\operatorname{Cos}[x] \operatorname{Log}[\operatorname{Cos}[x]], x, 4, 0\}$$

$$\operatorname{ArcTanh}[\operatorname{Sin}[x]] - \operatorname{Sin}[x] + \operatorname{Log}[\operatorname{Cos}[x]] \operatorname{Sin}[x]$$

$$-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{x}{2}\right] - \operatorname{Sin}\left[\frac{x}{2}\right]\right] + \operatorname{Log}\left[\operatorname{Cos}\left[\frac{x}{2}\right] + \operatorname{Sin}\left[\frac{x}{2}\right]\right] + (-1 + \operatorname{Log}[\operatorname{Cos}[x]]) \operatorname{Sin}[x]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a x + b x \operatorname{Log}[c x^n]^4}, x, 5, 0 \right\}$$

$$-\frac{\operatorname{ArcTan}\left[\frac{b^{1/4} \operatorname{Log}[c x^n]}{(-a)^{1/4}}\right]}{2 (-a)^{3/4} b^{1/4} n} - \frac{\operatorname{ArcTanh}\left[\frac{b^{1/4} \operatorname{Log}[c x^n]}{(-a)^{1/4}}\right]}{2 (-a)^{3/4} b^{1/4} n}$$

$$\frac{1}{4 \sqrt{2} a^{3/4} b^{1/4} n} \left( -2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} b^{1/4} \operatorname{Log}[c x^n]}{a^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} b^{1/4} \operatorname{Log}[c x^n]}{a^{1/4}}\right] - \right.$$

$$\left. \operatorname{Log}\left[\sqrt{a} - \sqrt{2} a^{1/4} b^{1/4} \operatorname{Log}[c x^n] + \sqrt{b} \operatorname{Log}[c x^n]^2\right] + \operatorname{Log}\left[\sqrt{a} + \sqrt{2} a^{1/4} b^{1/4} \operatorname{Log}[c x^n] + \sqrt{b} \operatorname{Log}[c x^n]^2\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{a x + \frac{b x}{\operatorname{Log}[c x^n]^4}}, x, 7, 0 \right\}$$

$$-\frac{(-b)^{1/4} \operatorname{ArcTan}\left[\frac{a^{1/4} \operatorname{Log}[c x^n]}{(-b)^{1/4}}\right]}{2 a^{5/4} n} - \frac{(-b)^{1/4} \operatorname{ArcTanh}\left[\frac{a^{1/4} \operatorname{Log}[c x^n]}{(-b)^{1/4}}\right]}{2 a^{5/4} n} + \frac{\operatorname{Log}[c x^n]}{a n}$$

$$\frac{1}{8 a^{5/4} n} \left( 2 \sqrt{2} b^{1/4} \text{ArcTan}\left[1 - \frac{\sqrt{2} a^{1/4} \text{Log}[c x^n]}{b^{1/4}}\right] - 2 \sqrt{2} b^{1/4} \text{ArcTan}\left[1 + \frac{\sqrt{2} a^{1/4} \text{Log}[c x^n]}{b^{1/4}}\right] + 8 a^{1/4} \text{Log}[c x^n] + \sqrt{2} b^{1/4} \text{Log}\left[\sqrt{b} - \sqrt{2} a^{1/4} b^{1/4} \text{Log}[c x^n] + \sqrt{a} \text{Log}[c x^n]^2\right] - \sqrt{2} b^{1/4} \text{Log}\left[\sqrt{b} + \sqrt{2} a^{1/4} b^{1/4} \text{Log}[c x^n] + \sqrt{a} \text{Log}[c x^n]^2\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{(1 + \text{Log}[x])^5}{x}, x, 2, 0 \right\}$$

$$\frac{1}{6} (1 + \text{Log}[x])^6$$

$$\frac{1}{6} \text{Log}[x] (6 + 15 \text{Log}[x] + 20 \text{Log}[x]^2 + 15 \text{Log}[x]^3 + 6 \text{Log}[x]^4 + \text{Log}[x]^5)$$

Unable to integrate:

$$\left\{ \frac{\text{Log}[1 + \sqrt{x} - x]}{x}, x, 10, 0 \right\}$$

$$-2 \text{Log}\left[-\frac{1}{4} (1 + \sqrt{5}) (1 - \sqrt{5} - 2 \sqrt{x})\right] \text{Log}[\sqrt{x}] - 2 \text{Log}\left[-\frac{1}{4} (1 - \sqrt{5}) (1 + \sqrt{5} - 2 \sqrt{x})\right] \text{Log}[\sqrt{x}] +$$

$$2 \text{Log}[1 + \sqrt{x} - x] \text{Log}[\sqrt{x}] - 2 \text{PolyLog}\left[2, -\frac{1}{2} (1 - \sqrt{5}) \sqrt{x}\right] - 2 \text{PolyLog}\left[2, -\frac{1}{2} (1 + \sqrt{5}) \sqrt{x}\right]$$

$$\int \frac{\text{Log}[1 + \sqrt{x} - x]}{x} dx$$