

Mathematica 7 Test Results

For Algebraic Function Integration Problems

Algebraic function problems involving linear polynomials

Valid but unnecessarily complicated antiderivative:

$$\frac{\left\{ \frac{1}{\sqrt{3-x} \sqrt{5+x}}, x, 1, 0 \right\} - \text{ArcSin}\left[\frac{1}{4}(-1-x)\right] + 2\sqrt{-3+x}\sqrt{5+x} \text{ArcSinh}\left[\frac{\sqrt{-3+x}}{2\sqrt{2}}\right]}{\sqrt{-(-3+x)(5+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\frac{\left\{ \frac{1}{\sqrt{(3-x)(5+x)}}, x, 2, 0 \right\} - \text{ArcSin}\left[\frac{1}{4}(-1-x)\right] + 2\sqrt{-3+x}\sqrt{5+x} \text{ArcSinh}\left[\frac{\sqrt{-3+x}}{2\sqrt{2}}\right]}{\sqrt{-(-3+x)(5+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\frac{\left\{ \frac{1}{\sqrt{-3-x} \sqrt{5+x}}, x, 1, 0 \right\} + \text{ArcSin}[4+x] + 2\sqrt{3+x}\sqrt{5+x} \text{ArcSinh}\left[\frac{\sqrt{3+x}}{\sqrt{2}}\right]}{\sqrt{-(3+x)(5+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\frac{\left\{ \frac{1}{\sqrt{(-3-x)(5+x)}}, x, 2, 0 \right\} + \text{ArcSin}[4+x] + 2\sqrt{3+x}\sqrt{5+x} \text{ArcSinh}\left[\frac{\sqrt{3+x}}{\sqrt{2}}\right]}{\sqrt{-(3+x)(5+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{1-x} \sqrt{x}}, x, 1, 0 \right\}$$

$$2 \operatorname{ArcSin}[\sqrt{x}]$$

$$\frac{2 \sqrt{-1+x} \sqrt{x} \operatorname{Log}\left[2 \left(\sqrt{-1+x} + \sqrt{x}\right)\right]}{\sqrt{-(-1+x) x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{3-x} \sqrt{-2+x}}, x, 1, 0 \right\}$$

$$-\operatorname{ArcSin}[5-2x]$$

$$\frac{2 \sqrt{-3+x} \sqrt{-2+x} \operatorname{ArcSinh}[\sqrt{-3+x}]}{\sqrt{-(-3+x) (-2+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-1+x} \sqrt{1+x}}, x, 1, 0 \right\}$$

$$\operatorname{ArcCosh}[x]$$

$$2 \operatorname{ArcSinh}\left[\frac{\sqrt{-1+x}}{\sqrt{2}}\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{(c+dx)^{5/4}}{(a+bx)^{1/4}}, x, 6, 0 \right\}$$

$$\frac{5(b^2c-ad)(a+bx)^{3/4}(c+dx)^{1/4}}{8b^2} + \frac{(a+bx)^{3/4}(c+dx)^{5/4}}{2b} -$$

$$\frac{5(b^2c-ad)^2 \operatorname{ArcTan}\left[\frac{d^{1/4}(a+bx)^{1/4}}{b^{1/4}(c+dx)^{1/4}}\right]}{16b^{9/4}d^{3/4}} + \frac{5(b^2c-ad)^2 \operatorname{ArcTanh}\left[\frac{d^{1/4}(a+bx)^{1/4}}{b^{1/4}(c+dx)^{1/4}}\right]}{16b^{9/4}d^{3/4}}$$

$$\frac{(c+dx)^{1/4} \left(-d(a+bx) (-9bc+5ad-4bdx) + 5(b^2c-ad)^2 \left(\frac{d(a+bx)}{-bc+ad} \right)^{1/4} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{4}, \frac{5}{4}, \frac{b(c+dx)}{bc-ad}\right] \right)}{8b^2d(a+bx)^{1/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{(c+dx)^{1/4}}{(a+bx)^{1/4}}, x, 5, 0 \right\}$$

$$\frac{(a+bx)^{3/4}(c+dx)^{1/4}}{b} - \frac{(bc-ad) \operatorname{ArcTan}\left[\frac{d^{1/4}(a+bx)^{1/4}}{b^{1/4}(c+dx)^{1/4}}\right]}{2b^{5/4}d^{3/4}} + \frac{(bc-ad) \operatorname{ArcTanh}\left[\frac{d^{1/4}(a+bx)^{1/4}}{b^{1/4}(c+dx)^{1/4}}\right]}{2b^{5/4}d^{3/4}}$$

$$\frac{(c+dx)^{1/4} \left(d(a+bx) + (bc-ad) \left(\frac{d(a+bx)}{-bc+ad} \right)^{1/4} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{4}, \frac{5}{4}, \frac{b(c+dx)}{bc-ad}\right] \right)}{bd(a+bx)^{1/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(a+bx)^{1/4} (c+dx)^{3/4}}, x, 4, 0 \right\}$$

$$-\frac{2 \operatorname{ArcTan}\left[\frac{d^{1/4} (a+bx)^{1/4}}{b^{1/4} (c+dx)^{1/4}}\right]}{b^{1/4} d^{3/4}} + \frac{2 \operatorname{ArcTanh}\left[\frac{d^{1/4} (a+bx)^{1/4}}{b^{1/4} (c+dx)^{1/4}}\right]}{b^{1/4} d^{3/4}}$$

$$\frac{4 \left(\frac{d (a+bx)}{-b c + a d} \right)^{1/4} (c+dx)^{1/4} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{4}, \frac{5}{4}, \frac{b (c+dx)}{b c - a d}\right]}{d (a+bx)^{1/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a+b\sqrt{x})^7, x, 3, 0 \right\}$$

$$-\frac{a (a+b\sqrt{x})^8}{36 b^2} + \frac{2 (a+b\sqrt{x})^8 \sqrt{x}}{9 b}$$

$$a^7 x + \frac{14}{3} a^6 b x^{3/2} + \frac{21}{2} a^5 b^2 x^2 + 14 a^4 b^3 x^{5/2} + \frac{35}{3} a^3 b^4 x^3 + 6 a^2 b^5 x^{7/2} + \frac{7}{4} a b^6 x^4 + \frac{2}{9} b^7 x^{9/2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a+b\sqrt{x})^8, x, 3, 0 \right\}$$

$$-\frac{a (a+b\sqrt{x})^9}{45 b^2} + \frac{(a+b\sqrt{x})^9 \sqrt{x}}{5 b}$$

$$a^8 x + \frac{16}{3} a^7 b x^{3/2} + 14 a^6 b^2 x^2 + \frac{112}{5} a^5 b^3 x^{5/2} + \frac{70}{3} a^4 b^4 x^3 + 16 a^3 b^5 x^{7/2} + 7 a^2 b^6 x^4 + \frac{16}{9} a b^7 x^{9/2} + \frac{b^8 x^5}{5}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-4+bx} \sqrt{4+bx}}, x, 1, 0 \right\}$$

$$\frac{\operatorname{ArcCosh}\left[\frac{bx}{4}\right]}{b}$$

$$\frac{2 \operatorname{ArcSinh}\left[\frac{1}{2} \sqrt{-2 + \frac{bx}{2}}\right]}{b}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{4-x} \sqrt{x}}, x, 1, 0 \right\}$$

$$2 \operatorname{ArcSin}\left[\frac{\sqrt{x}}{2}\right]$$

$$\frac{2 \sqrt{-4+x} \sqrt{x} \operatorname{Log}\left[2 \left(\sqrt{-4+x} + \sqrt{x}\right)\right]}{\sqrt{-(-4+x) x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{x}}{a + b x^2}, x, 4, 0 \right\}$$

$$\frac{\operatorname{ArcTan}\left[\frac{b^{1/4}\sqrt{x}}{(-a)^{1/4}}\right]}{(-a)^{1/4}b^{3/4}} - \frac{\operatorname{ArcTanh}\left[\frac{b^{1/4}\sqrt{x}}{(-a)^{1/4}}\right]}{(-a)^{1/4}b^{3/4}} - \frac{-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} b^{1/4}\sqrt{x}}{a^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} b^{1/4}\sqrt{x}}{a^{1/4}}\right] + \operatorname{Log}\left[\sqrt{a} - \sqrt{2} a^{1/4} b^{1/4} \sqrt{x} + \sqrt{b} x\right] - \operatorname{Log}\left[\sqrt{a} + \sqrt{2} a^{1/4} b^{1/4} \sqrt{x} + \sqrt{b} x\right]}{2 \sqrt{2} a^{1/4} b^{3/4}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{x}}{1 - x^2}, x, 4, 0 \right\}$$

$$-\operatorname{ArcTan}[\sqrt{x}] + \operatorname{ArcTanh}[\sqrt{x}]$$

$$\frac{1}{2} \left(-2 \operatorname{ArcTan}[\sqrt{x}] - \operatorname{Log}[-1 + \sqrt{x}] + \operatorname{Log}[1 + \sqrt{x}] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(-2 + x) \sqrt{2 + x}}, x, 1, 0 \right\}$$

$$-\operatorname{ArcTanh}\left[\frac{\sqrt{2 + x}}{2}\right]$$

$$\frac{1}{2} \left(\operatorname{Log}[2 - \sqrt{2 + x}] - \operatorname{Log}[2 + \sqrt{2 + x}] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{1 - x} + \sqrt{1 + x}}{-\sqrt{1 - x} + \sqrt{1 + x}}, x, 8, 0 \right\}$$

$$\sqrt{1 - x} \sqrt{1 + x} - 2 \operatorname{ArcTanh}\left[\frac{\sqrt{1 - x}}{\sqrt{1 + x}}\right] + \operatorname{Log}[x]$$

$$\sqrt{1 - x^2} + \operatorname{Log}[x] - \operatorname{Log}\left[2 \left(2 + \sqrt{1 - x} - \sqrt{1 + x}\right)\right] + \operatorname{Log}[-1 + \sqrt{1 + x}] - \operatorname{Log}[1 + \sqrt{1 + x}] + \operatorname{Log}\left[-2 \left(2 + \sqrt{1 - x} + \sqrt{1 + x}\right)\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{1 + x^2}}{-1 + x^2}, x, 3, 0 \right\}$$

$$\operatorname{ArcSinh}[x] - \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{2} x}{\sqrt{1 + x^2}}\right]$$

$$\operatorname{ArcSinh}[x] + \frac{\operatorname{Log}[-1 + x] - \operatorname{Log}[1 + x] + \operatorname{Log}\left[-1 + x - \sqrt{2} \sqrt{1 + x^2}\right] - \operatorname{Log}\left[1 + x + \sqrt{2} \sqrt{1 + x^2}\right]}{\sqrt{2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{x (a + b x)^{1/3}}, x, 5, 0 \right\}$$

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$$\frac{\sqrt{3} \operatorname{ArcTan}\left[\frac{a^{1/3}+2(a+bx)^{1/3}}{\sqrt{3} a^{1/3}}\right]}{a^{1/3}} + \frac{\operatorname{Log}\left[a^{1/3} - (a+bx)^{1/3}\right]}{a^{1/3}} - \frac{\operatorname{Log}\left[a^{2/3} + a^{1/3}(a+bx)^{1/3} + (a+bx)^{2/3}\right]}{2 a^{1/3}}$$

$$- \frac{3\left(\frac{a+bx}{bx}\right)^{1/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{3}, \frac{4}{3}, -\frac{a}{bx}\right]}{(a+bx)^{1/3}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{(-1+x)^{1/3}}{(1+x)^{1/3}}, x, 6, 0\right\}$$

$$(-1+x)^{1/3}(1+x)^{2/3} - \frac{2 \operatorname{ArcTan}\left[\frac{1+\frac{2(-1+x)^{1/3}}{(1+x)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{3}} + \frac{2}{3} \operatorname{Log}\left[1 - \frac{(-1+x)^{1/3}}{(1+x)^{1/3}}\right] - \frac{1}{3} \operatorname{Log}\left[1 + \frac{(-1+x)^{2/3}}{(1+x)^{2/3}} + \frac{(-1+x)^{1/3}}{(1+x)^{1/3}}\right]$$

$$\left(\frac{-1+x}{1+x}\right)^{1/3} \left(1+x-2^{2/3}(1+x)^{1/3} \operatorname{Hypergeometric2F1}\left[\frac{1}{3}, \frac{1}{3}, \frac{4}{3}, \frac{1-x}{2}\right]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{\sqrt{2x-x^2}}{2-2x}, x, 2, 0\right\}$$

$$-\frac{1}{2}\sqrt{2x-x^2} + \frac{1}{2} \operatorname{ArcTanh}\left[\sqrt{2x-x^2}\right]$$

$$\frac{\sqrt{-(-2+x)x} \left(-\sqrt{-2+x}\sqrt{x} + \operatorname{ArcTan}\left[\frac{-2+\sqrt{x}}{\sqrt{-2+x}}\right] + \operatorname{ArcTan}\left[\frac{2+\sqrt{x}}{\sqrt{-2+x}}\right]\right)}{2\sqrt{-2+x}\sqrt{x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{(2-2x)\sqrt{2x-x^2}}, x, 1, 0\right\}$$

$$\frac{1}{2} \operatorname{ArcTanh}\left[\sqrt{2x-x^2}\right]$$

$$\frac{(-2+x)^{3/2}x^{3/2} \left(\operatorname{ArcTan}\left[\frac{-2+\sqrt{x}}{\sqrt{-2+x}}\right] + \operatorname{ArcTan}\left[\frac{2+\sqrt{x}}{\sqrt{-2+x}}\right]\right)}{2(-(-2+x)x)^{3/2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{(2-2x)(2x-x^2)^{3/2}}, x, 2, 0\right\}$$

$$-\frac{1}{2\sqrt{2x-x^2}} + \frac{1}{2} \operatorname{ArcTanh}\left[\sqrt{2x-x^2}\right]$$

$$-\frac{1+\sqrt{-2+x}\sqrt{x} \operatorname{ArcTan}\left[\frac{-2+\sqrt{x}}{\sqrt{-2+x}}\right] + \sqrt{-2+x}\sqrt{x} \operatorname{ArcTan}\left[\frac{2+\sqrt{x}}{\sqrt{-2+x}}\right]}{2\sqrt{-(-2+x)x}}$$

Algebraic function problems involving binomials

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{1-x^2} \sqrt{-1+2x^2}}, x, -2, 0 \right\}$$

$$-\text{EllipticF}[\text{ArcCos}[x], 2]$$

$$\frac{\sqrt{1-2x^2} \text{EllipticF}[\text{ArcSin}[x], 2]}{\sqrt{-1+2x^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a+bx^2) \sqrt{2+dx^2} \sqrt{3+fx^2}, x, -5, 0 \right\}$$

0

$$\frac{1}{15d^{3/2}f^2} \left(\sqrt{d} f x \sqrt{2+dx^2} \sqrt{3+fx^2} (5adf + b(2f+3d(1+fx^2))) + \right. \\ \left. i\sqrt{3} (-5adf(3d+2f) + 2b(9d^2 - 6df + 4f^2)) \text{EllipticE}\left[\frac{\sqrt{d}x}{\sqrt{2}}\right], \frac{2f}{3d} \right) + \\ \left. i\sqrt{3} (3d-2f) (-6bd + 2bf + 5adf) \text{EllipticF}\left[\frac{\sqrt{d}x}{\sqrt{2}}\right], \frac{2f}{3d} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (a+bx^2) \sqrt{c+dx^2} \sqrt{e+fx^2}, x, -7, 0 \right\}$$

0

$$\frac{1}{15d\sqrt{\frac{d}{c}}f^2\sqrt{c+dx^2}\sqrt{e+fx^2}} \left(\sqrt{\frac{d}{c}} f x (c+dx^2) (e+fx^2) (5adf + b(cf+d(e+3fx^2))) + \right. \\ \left. ie(-5adf(de+cf) + 2b(d^2e^2 - cdef + c^2f^2)) \sqrt{1+\frac{dx^2}{c}} \sqrt{1+\frac{fx^2}{e}} \text{EllipticE}\left[\frac{\sqrt{\frac{d}{c}}x}{\sqrt{\frac{d}{c}}}, \frac{cf}{de} \right] - \right. \\ \left. ie(-de+cf) (-2bde + bcf + 5adf) \sqrt{1+\frac{dx^2}{c}} \sqrt{1+\frac{fx^2}{e}} \text{EllipticF}\left[\frac{\sqrt{\frac{d}{c}}x}{\sqrt{\frac{d}{c}}}, \frac{cf}{de} \right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x^4 \sqrt{-1+3x^2}}{\sqrt{2-3x^2}}, x, -1, 0 \right\}$$

0

$$\frac{-3x\sqrt{2-3x^2} (-7+12x^2+27x^4) - 24\sqrt{3-9x^2} \text{EllipticE}\left[\text{ArcSin}\left[\sqrt{\frac{3}{2}}x\right], 2\right] + 10\sqrt{3-9x^2} \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{3}{2}}x\right], 2\right]}{405\sqrt{-1+3x^2}}$$

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Incorrect antiderivative:

$$\left\{ \frac{1}{\sqrt{-1+x} \sqrt{1+x} \sqrt{-1+2x^2}}, x, -7, 0 \right\}$$

$$-i \operatorname{EllipticF}[i \operatorname{ArcCosh}[x], 2]$$

$$\frac{2(-1+x)^{3/2} \sqrt{\frac{1+x}{1-x}} \sqrt{\frac{1-2x^2}{(-1+x)^2}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{2+\sqrt{2}+\frac{1}{-1+x}}}{2^{3/4}}\right], 4\left(-4+3\sqrt{2}\right)\right]}{\sqrt{3+2\sqrt{2}} \sqrt{1+x} \sqrt{-1+2x^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{1-x^2}}{1+x}, x, 4, 0 \right\}$$

$$\sqrt{1-x^2} + \operatorname{ArcSin}[x]$$

$$\sqrt{1-x^2} \left(1 - \frac{2 \operatorname{Log}\left[2\left(\sqrt{-1+x} + \sqrt{1+x}\right)\right]}{\sqrt{-1+x} \sqrt{1+x}} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{1-x^2}}{-1+x}, x, 4, 0 \right\}$$

$$\sqrt{1-x^2} - \operatorname{ArcSin}[x]$$

$$\sqrt{1-x^2} \left(1 + \frac{2 \operatorname{ArcSinh}\left[\frac{\sqrt{-1+x}}{\sqrt{2}}\right]}{\sqrt{-1+x} \sqrt{1+x}} \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x}{x - \sqrt{1-x^2}}, x, 7, 0 \right\}$$

$$\frac{x}{2} + \frac{\sqrt{1-x^2}}{2} - \frac{\operatorname{ArcTanh}[\sqrt{2} x]}{2\sqrt{2}} - \frac{\operatorname{ArcTanh}[\sqrt{2} \sqrt{1-x^2}]}{2\sqrt{2}}$$

$$\frac{1}{8} \left(4x + 4\sqrt{1-x^2} + \sqrt{2} \operatorname{Log}[\sqrt{2} - 2x] - \sqrt{2} \operatorname{Log}[\sqrt{2} + 2x] + \sqrt{2} \operatorname{Log}[2 - 2\sqrt{2} x] + \right.$$

$$\left. \sqrt{2} \operatorname{Log}[2 + 2\sqrt{2} x] - \sqrt{2} \operatorname{Log}\left[8\left(2 - \sqrt{2} x + \sqrt{2 - 2x^2}\right)\right] - \sqrt{2} \operatorname{Log}\left[8\left(2 + \sqrt{2} x + \sqrt{2 - 2x^2}\right)\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x}{x - \sqrt{1+2x^2}}, x, 7, 0 \right\}$$

$$-x - \sqrt{1+2x^2} + \operatorname{ArcTan}[x] + \operatorname{ArcTan}[\sqrt{1+2x^2}]$$

Mathematica 7 Test Results for Algebraic Function Integration Problems

$$\frac{1}{4} \left(-4 x - 4 \sqrt{1 + 2 x^2} + 4 \operatorname{ArcTan}[x] - 4 \operatorname{ArcTan}\left[\frac{1}{\sqrt{1 + 2 x^2}}\right] + \right. \\ \left. 2 i \operatorname{Log}[1 + x^2] - i \operatorname{Log}[32 + 96 x^2 - 64 x \sqrt{1 + 2 x^2}] - i \operatorname{Log}\left[32 \left(1 + 3 x^2 + 2 x \sqrt{1 + 2 x^2}\right)\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{-1 + 4 x^2}}{x + \sqrt{-1 + 4 x^2}}, x, 7, 0 \right\}$$

$$\frac{4 x}{3} - \frac{1}{3} \sqrt{-1 + 4 x^2} - \frac{\operatorname{ArcTanh}[\sqrt{3} x]}{3 \sqrt{3}} + \frac{\operatorname{ArcTanh}[\sqrt{3} \sqrt{-1 + 4 x^2}]}{3 \sqrt{3}}$$

$$\frac{1}{18} \left(24 x - 6 \sqrt{-1 + 4 x^2} + \sqrt{3} \operatorname{Log}[\sqrt{3} - 3 x] - \sqrt{3} \operatorname{Log}[\sqrt{3} + 3 x] - \sqrt{3} \operatorname{Log}[3 - 3 \sqrt{3} x] - \right. \\ \left. \sqrt{3} \operatorname{Log}[3 + 3 \sqrt{3} x] + \sqrt{3} \operatorname{Log}[54 + 72 \sqrt{3} x - 18 \sqrt{-3 + 12 x^2}] + \sqrt{3} \operatorname{Log}\left[18 \left(-3 + 4 \sqrt{3} x + \sqrt{-3 + 12 x^2}\right)\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{x \sqrt{-1 + x^3}}, x, 1, 0 \right\}$$

$$\frac{2}{3} \operatorname{ArcTan}[\sqrt{-1 + x^3}]$$

$$\frac{2 \sqrt{-1 + x^3} \operatorname{ArcTanh}[\sqrt{1 - x^3}]}{3 \sqrt{1 - x^3}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x}{(1 - x^3)^{2/3}}, x, 5, 0 \right\}$$

$$-\frac{\operatorname{ArcTan}\left[\frac{1 - \frac{2 x}{(1 - x^3)^{1/3}}}{\sqrt{3}}\right]}{\sqrt{3}} + \frac{1}{6} \operatorname{Log}\left[1 + \frac{x^2}{(1 - x^3)^{2/3}} - \frac{x}{(1 - x^3)^{1/3}}\right] - \frac{1}{3} \operatorname{Log}\left[1 + \frac{x}{(1 - x^3)^{1/3}}\right]$$

$$\frac{1}{2} x^2 \operatorname{Hypergeometric2F1}\left[\frac{2}{3}, \frac{2}{3}, \frac{5}{3}, x^3\right]$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ x (1 - x^3)^{1/3}, x, 6, 0 \right\}$$

$$\frac{1}{3} x^2 (1 - x^3)^{1/3} - \frac{\operatorname{ArcTan}\left[\frac{1 - \frac{2 x}{(1 - x^3)^{1/3}}}{\sqrt{3}}\right]}{3 \sqrt{3}} + \frac{1}{18} \operatorname{Log}\left[1 + \frac{x^2}{(1 - x^3)^{2/3}} - \frac{x}{(1 - x^3)^{1/3}}\right] - \frac{1}{9} \operatorname{Log}\left[1 + \frac{x}{(1 - x^3)^{1/3}}\right]$$

$$\frac{1}{6} x^2 \left(2 (1 - x^3)^{1/3} + \operatorname{Hypergeometric2F1}\left[\frac{2}{3}, \frac{2}{3}, \frac{5}{3}, x^3\right] \right)$$

Unable to integrate:

$$\left\{ \frac{\sqrt{b x^2 + \sqrt{a + b^2 x^4}}}{\sqrt{a + b^2 x^4}}, x, 1, 0 \right\}$$

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{2} \sqrt{b} x}{\sqrt{b x^2 + \sqrt{a + b^2 x^4}}}\right]}{\sqrt{2} \sqrt{b}}$$

$$\int \frac{\sqrt{b x^2 + \sqrt{a + b^2 x^4}}}{\sqrt{a + b^2 x^4}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{-b x^2 + \sqrt{a + b^2 x^4}}}{\sqrt{a + b^2 x^4}}, x, 1, 0 \right\}$$

$$\frac{\text{ArcTan}\left[\frac{\sqrt{2} \sqrt{b} x}{\sqrt{-b x^2 + \sqrt{a + b^2 x^4}}}\right]}{\sqrt{2} \sqrt{b}}$$

$$\int \frac{\sqrt{-b x^2 + \sqrt{a + b^2 x^4}}}{\sqrt{a + b^2 x^4}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{2 x^2 + \sqrt{3 + 4 x^4}}}{(c + d x) \sqrt{3 + 4 x^4}}, x, 3, 0 \right\}$$

$$\frac{\left(\frac{1}{2} - \frac{i}{2}\right) \text{ArcTan}\left[\frac{\sqrt{3} d + 2 i c x}{\sqrt{2 i c^2 - \sqrt{3} d^2} \sqrt{\sqrt{3} - 2 i x^2}}\right] - \left(\frac{1}{2} + \frac{i}{2}\right) \text{ArcTanh}\left[\frac{\sqrt{3} d - 2 i c x}{\sqrt{2 i c^2 + \sqrt{3} d^2} \sqrt{\sqrt{3} + 2 i x^2}}\right]}{\sqrt{2 i c^2 - \sqrt{3} d^2}}$$

$$\int \frac{\sqrt{2 x^2 + \sqrt{3 + 4 x^4}}}{(c + d x) \sqrt{3 + 4 x^4}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{2 x^2 + \sqrt{3 + 4 x^4}}}{(c + d x)^2 \sqrt{3 + 4 x^4}}, x, 5, 0 \right\}$$

$$\frac{\left(\frac{1}{2} - \frac{i}{2}\right) d \sqrt{\sqrt{3} - 2 i x^2}}{\left(2 i c^2 - \sqrt{3} d^2\right) (c + d x)} - \frac{\left(\frac{1}{2} + \frac{i}{2}\right) d \sqrt{\sqrt{3} + 2 i x^2}}{\left(2 i c^2 + \sqrt{3} d^2\right) (c + d x)} +$$

$$\frac{(1 + i) c \operatorname{ArcTan}\left[\frac{\sqrt{3} d + 2 i c x}{\sqrt{2 i c^2 - \sqrt{3} d^2} \sqrt{\sqrt{3} - 2 i x^2}}\right] - (1 - i) c \operatorname{ArcTanh}\left[\frac{\sqrt{3} d - 2 i c x}{\sqrt{2 i c^2 + \sqrt{3} d^2} \sqrt{\sqrt{3} + 2 i x^2}}\right]}{\left(2 i c^2 - \sqrt{3} d^2\right)^{3/2}} + \frac{\left(2 i c^2 + \sqrt{3} d^2\right)^{3/2}}$$

$$\int \frac{\sqrt{2 x^2 + \sqrt{3 + 4 x^4}}}{(c + d x)^2 \sqrt{3 + 4 x^4}} dx$$

Unable to integrate:

$$\left\{\frac{x^{23/2}}{\sqrt{1+x^5}}, x, 5, 0\right\}$$

$$-\frac{3}{20} x^{5/2} \sqrt{1+x^5} + \frac{1}{10} x^{15/2} \sqrt{1+x^5} + \frac{3}{20} \operatorname{ArcSinh}\left[x^{5/2}\right]$$

$$\int \frac{x^{23/2}}{\sqrt{1+x^5}} dx$$

Unable to integrate:

$$\left\{\frac{x^{13/2}}{\sqrt{1+x^5}}, x, 4, 0\right\}$$

$$\frac{1}{5} x^{5/2} \sqrt{1+x^5} - \frac{1}{5} \operatorname{ArcSinh}\left[x^{5/2}\right]$$

$$\int \frac{x^{13/2}}{\sqrt{1+x^5}} dx$$

Unable to integrate:

$$\left\{\frac{x^{3/2}}{\sqrt{1+x^5}}, x, 2, 0\right\}$$

$$\frac{2}{5} \operatorname{ArcSinh}\left[x^{5/2}\right]$$

$$\int \frac{x^{3/2}}{\sqrt{1+x^5}} dx$$

Unable to integrate:

$$\left\{\frac{x^{23/2}}{\sqrt{a+b x^5}}, x, 5, 0\right\}$$

$$-\frac{3 a x^{5/2} \sqrt{a+b x^5}}{20 b^2} + \frac{x^{15/2} \sqrt{a+b x^5}}{10 b} + \frac{3 a^2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x^{5/2}}{\sqrt{a+b x^5}}\right]}{20 b^{5/2}}$$

$$\int \frac{x^{23/2}}{\sqrt{a + b x^5}} dx$$

Unable to integrate:

$$\left\{ \frac{x^{13/2}}{\sqrt{a + b x^5}}, x, 4, 0 \right\}$$

$$\frac{x^{5/2} \sqrt{a + b x^5}}{5 b} - \frac{a \operatorname{ArcTanh}\left[\frac{\sqrt{b} x^{5/2}}{\sqrt{a + b x^5}}\right]}{5 b^{3/2}}$$

$$\int \frac{x^{13/2}}{\sqrt{a + b x^5}} dx$$

Unable to integrate:

$$\left\{ \frac{x^{3/2}}{\sqrt{a + b x^5}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x^{5/2}}{\sqrt{a + b x^5}}\right]}{5 \sqrt{b}}$$

$$\int \frac{x^{3/2}}{\sqrt{a + b x^5}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{x^{23}}}{\sqrt{1 + x^5}}, x, 6, 0 \right\}$$

$$-\frac{\sqrt{x^{23}} \left(3 x^{5/2} \sqrt{1 + x^5} - 2 x^{15/2} \sqrt{1 + x^5} - 3 \operatorname{ArcSinh}\left[x^{5/2}\right] \right)}{20 x^{23/2}}$$

$$\int \frac{\sqrt{x^{23}}}{\sqrt{1 + x^5}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{x^{13}}}{\sqrt{1 + x^5}}, x, 5, 0 \right\}$$

$$\frac{\sqrt{x^{13}} \left(x^{5/2} \sqrt{1 + x^5} - \operatorname{ArcSinh}\left[x^{5/2}\right] \right)}{5 x^{13/2}}$$

$$\int \frac{\sqrt{x^{13}}}{\sqrt{1 + x^5}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{x^3}}{\sqrt{1+x^5}}, x, 3, 0 \right\}$$

$$\frac{2 \sqrt{x^3} \operatorname{ArcSinh}[x^{5/2}]}{5 x^{3/2}}$$

$$\int \frac{\sqrt{x^3}}{\sqrt{1+x^5}} dx$$

Incorrect antiderivative:

$$\left\{ \frac{x^{1/3}}{1-x^6}, x, 13, 0 \right\}$$

$$\begin{aligned} & -\frac{\operatorname{ArcTan}\left[\frac{1+2x^{2/3}}{\sqrt{3}}\right]}{2\sqrt{3}} - \frac{1}{3} \operatorname{ArcTan}\left[\left(x^{2/3} + \cos\left[\frac{\pi}{9}\right]\right) \csc\left[\frac{\pi}{9}\right]\right] \left(1 - \cos\left[\frac{2\pi}{9}\right]\right) \cot\left[\frac{\pi}{9}\right] - \\ & \frac{1}{6} \log\left[1 - x^{2/3}\right] + \frac{1}{12} \log\left[1 + x^{2/3} + x^{4/3}\right] - \frac{1}{6} \cos\left[\frac{2\pi}{9}\right] \log\left[1 + x^{4/3} + 2x^{2/3} \cos\left[\frac{\pi}{9}\right]\right] + \\ & \frac{1}{6} \cos\left[\frac{\pi}{9}\right] \log\left[1 + x^{4/3} - 2x^{2/3} \sin\left[\frac{\pi}{18}\right]\right] + \frac{1}{3} \operatorname{ArcTan}\left[\left(x^{2/3} - \cos\left[\frac{2\pi}{9}\right]\right) \csc\left[\frac{2\pi}{9}\right]\right] \cot\left[\frac{2\pi}{9}\right] \left(1 - \sin\left[\frac{\pi}{18}\right]\right) - \\ & \frac{1}{6} \log\left[1 + x^{4/3} - 2x^{2/3} \cos\left[\frac{2\pi}{9}\right]\right] \sin\left[\frac{\pi}{18}\right] + \frac{1}{3} \operatorname{ArcTan}\left[\sec\left[\frac{\pi}{18}\right] \left(x^{2/3} - \sin\left[\frac{\pi}{18}\right]\right)\right] \left(1 + \cos\left[\frac{\pi}{9}\right]\right) \tan\left[\frac{\pi}{18}\right] \\ & \frac{1}{12} \left(-2\sqrt{3} \operatorname{ArcTan}\left[\frac{-1+2x^{1/3}}{\sqrt{3}}\right] + 2\sqrt{3} \operatorname{ArcTan}\left[\frac{1+2x^{1/3}}{\sqrt{3}}\right] - 4 \operatorname{ArcTan}\left[\cot\left[\frac{\pi}{9}\right] - x^{1/3} \csc\left[\frac{\pi}{9}\right]\right] \cos\left[\frac{\pi}{18}\right] - \right. \\ & \quad 4 \operatorname{ArcTan}\left[\cot\left[\frac{\pi}{9}\right] + x^{1/3} \csc\left[\frac{\pi}{9}\right]\right] \cos\left[\frac{\pi}{18}\right] - 2 \log\left[-1 + x^{1/3}\right] - 2 \log\left[1 + x^{1/3}\right] + \log\left[1 - x^{1/3} + x^{2/3}\right] + \log\left[1 + x^{1/3} + x^{2/3}\right] + \\ & \quad 2 \cos\left[\frac{\pi}{9}\right] \log\left[1 + x^{2/3} - 2x^{1/3} \cos\left[\frac{2\pi}{9}\right]\right] + 2 \cos\left[\frac{\pi}{9}\right] \log\left[1 + x^{2/3} + 2x^{1/3} \cos\left[\frac{2\pi}{9}\right]\right] - 2 \cos\left[\frac{2\pi}{9}\right] \log\left[1 + x^{2/3} - 2x^{1/3} \sin\left[\frac{\pi}{18}\right]\right] - \\ & \quad 2 \cos\left[\frac{2\pi}{9}\right] \log\left[1 + x^{2/3} + 2x^{1/3} \sin\left[\frac{\pi}{18}\right]\right] - 2 \log\left[1 + x^{2/3} - 2x^{1/3} \cos\left[\frac{\pi}{9}\right]\right] \sin\left[\frac{\pi}{18}\right] - 2 \log\left[1 + x^{2/3} + 2x^{1/3} \cos\left[\frac{\pi}{9}\right]\right] \sin\left[\frac{\pi}{18}\right] + \\ & \quad 4 \operatorname{ArcTan}\left[\left(x^{1/3} - \cos\left[\frac{2\pi}{9}\right]\right) \csc\left[\frac{2\pi}{9}\right]\right] \sin\left[\frac{\pi}{9}\right] - 4 \operatorname{ArcTan}\left[\left(x^{1/3} + \cos\left[\frac{2\pi}{9}\right]\right) \csc\left[\frac{2\pi}{9}\right]\right] \sin\left[\frac{\pi}{9}\right] - \\ & \quad \left. 4 \operatorname{ArcTan}\left[x^{1/3} \sec\left[\frac{\pi}{18}\right] - \tan\left[\frac{\pi}{18}\right]\right] \sin\left[\frac{2\pi}{9}\right] + 4 \operatorname{ArcTan}\left[x^{1/3} \sec\left[\frac{\pi}{18}\right] + \tan\left[\frac{\pi}{18}\right]\right] \sin\left[\frac{2\pi}{9}\right] \right) \end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + \frac{b}{x^2}}}, x, 1, 0 \right\}$$

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a + \frac{b}{x^2}}}{\sqrt{a}}\right]}{\sqrt{a}}$$

$$\frac{\sqrt{a + \frac{b}{x^2}} x \log\left[2 \left(a x + \sqrt{a} \sqrt{b + a x^2}\right)\right]}{\sqrt{a} \sqrt{b + a x^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-a + \frac{b}{x^2}} x}, x, 1, 0 \right\}$$

$$- \frac{\text{ArcTan}\left[\frac{\sqrt{-a + \frac{b}{x^2}}}{\sqrt{a}}\right]}{\sqrt{a}}$$

$$\frac{\sqrt{-b + a x^2} \text{Log}\left[2 \left(a x + \sqrt{a} \sqrt{-b + a x^2}\right)\right]}{\sqrt{a} \sqrt{-a + \frac{b}{x^2}} x}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{2 + \frac{b}{x^2}} x^2}, x, 2, 0 \right\}$$

$$- \frac{\text{ArcSinh}\left[\frac{\sqrt{b}}{\sqrt{2} x}\right]}{\sqrt{b}}$$

$$\frac{\sqrt{b + 2 x^2} \left(\text{Log}[\sqrt{b} x] - \text{Log}\left[2 \left(b + \sqrt{b} \sqrt{b + 2 x^2}\right)\right] \right)}{\sqrt{b} \sqrt{2 + \frac{b}{x^2}} x}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{2 - \frac{b}{x^2}} x^2}, x, 2, 0 \right\}$$

$$- \frac{\text{ArcSin}\left[\frac{\sqrt{b}}{\sqrt{2} x}\right]}{\sqrt{b}}$$

$$\frac{\sqrt{b - 2 x^2} \left(\text{Log}[\sqrt{b} x] - \text{Log}\left[2 \left(b + \sqrt{b} \sqrt{b - 2 x^2}\right)\right] \right)}{\sqrt{b} \sqrt{2 - \frac{b}{x^2}} x}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a + \frac{b}{x^2}} x^2}, x, 2, 0 \right\}$$

$$- \frac{\text{ArcTanh}\left[\frac{\sqrt{b}}{\sqrt{a + \frac{b}{x^2}} x}\right]}{\sqrt{b}}$$

$$\frac{\sqrt{b + a x^2} \left(\text{Log}[\sqrt{b} x] - \text{Log}\left[2 \left(b + \sqrt{b} \sqrt{b + a x^2}\right)\right] \right)}{\sqrt{b} \sqrt{a + \frac{b}{x^2}} x}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{2 + \frac{b}{x^2}}}{b + 2 x^2}, x, 3, 0 \right\}$$

$$- \frac{\text{ArcSinh}\left[\frac{\sqrt{b}}{\sqrt{2} x}\right]}{\sqrt{b}}$$

$$\frac{\sqrt{2 + \frac{b}{x^2}} x \left(\text{Log}[\sqrt{b} x] - \text{Log}\left[2 \left(b + \sqrt{b} \sqrt{b + 2 x^2}\right)\right] \right)}{\sqrt{b} \sqrt{b + 2 x^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{2 - \frac{b}{x^2}}}{-b + 2 x^2}, x, 3, 0 \right\}$$

$$- \frac{\text{ArcSin}\left[\frac{\sqrt{b}}{\sqrt{2} x}\right]}{\sqrt{b}}$$

$$- \frac{\sqrt{2 - \frac{b}{x^2}} x \left(\text{Log}[\sqrt{b} x] - \text{Log}\left[2 \left(b + \sqrt{b} \sqrt{b - 2 x^2}\right)\right] \right)}{\sqrt{b} \sqrt{b - 2 x^2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{-1 + x^2}{\sqrt{a + b \left(-1 + \frac{1}{x^2}\right)} x^3}, x, 5, 0 \right\}$$

$$\frac{\sqrt{a - b + \frac{b}{x^2}}}{b} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a - b + \frac{b}{x^2}}}{\sqrt{a - b}}\right]}{\sqrt{a - b}}$$

$$\frac{\sqrt{a - b} \left(b + a x^2 - b x^2\right) + b x \sqrt{b + a x^2 - b x^2} \text{Log}\left[2 \left(a x - b x + \sqrt{a - b} \sqrt{b + a x^2 - b x^2}\right)\right]}{\sqrt{a - b} b \sqrt{a + b \left(-1 + \frac{1}{x^2}\right)} x^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{-1 + x^2}{\sqrt{a - b + \frac{b}{x^2}} x^3}, x, 5, 0 \right\}$$

$$\frac{\sqrt{a-b+\frac{b}{x^2}}}{b} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a-b+\frac{b}{x^2}}}{\sqrt{a-b}}\right]}{\sqrt{a-b}}$$

$$\frac{\sqrt{a-b} \left(b+a x^2-b x^2\right)+b x \sqrt{b+a x^2-b x^2} \operatorname{Log}\left[2\left(a x-b x+\sqrt{a-b} \sqrt{b+a x^2-b x^2}\right)\right]}{\sqrt{a-b} b \sqrt{a+b\left(-1+\frac{1}{x^2}\right)} x^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{\sqrt{a+\frac{b}{x^3}} x}, x, 1, 0\right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{a+\frac{b}{x^3}}}{\sqrt{a}}\right]}{3 \sqrt{a}}$$

$$\frac{2 \sqrt{a+\frac{b}{x^3}} x^{3/2} \operatorname{Log}\left[2\left(a x^{3/2}+\sqrt{a} \sqrt{b+a x^3}\right)\right]}{3 \sqrt{a} \sqrt{b+a x^3}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{\sqrt{-a+\frac{b}{x^3}} x}, x, 1, 0\right\}$$

$$-\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{-a+\frac{b}{x^3}}}{\sqrt{a}}\right]}{3 \sqrt{a}}$$

$$\frac{2 \sqrt{-b+a x^3} \operatorname{Log}\left[2\left(a x^{3/2}+\sqrt{a} \sqrt{-b+a x^3}\right)\right]}{3 \sqrt{a} \sqrt{-a+\frac{b}{x^3}} x^{3/2}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{\frac{1}{\sqrt{a+\frac{b}{x^4}} x^3}, x, 2, 0\right\}$$

$$-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{b}}{\sqrt{a+\frac{b}{x^4}} x^2}\right]}{2 \sqrt{b}}$$

$$\frac{\sqrt{b+a x^4}\left(\operatorname{Log}\left[\sqrt{b} x^2\right]-\operatorname{Log}\left[2\left(b+\sqrt{b} \sqrt{b+a x^4}\right)\right]\right)}{2 \sqrt{b} \sqrt{a+\frac{b}{x^4}} x^2}$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{a + \frac{b}{x^5}}}, x, 1, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{a + \frac{b}{x^5}}}{\sqrt{a}}\right]}{5 \sqrt{a}}$$

$$\int \frac{1}{\sqrt{a + \frac{b}{x^5}}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{-a + \frac{b}{x^5}}}, x, 1, 0 \right\}$$

$$-\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{-a + \frac{b}{x^5}}}{\sqrt{a}}\right]}{5 \sqrt{a}}$$

$$\int \frac{1}{\sqrt{-a + \frac{b}{x^5}}} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{a x + b x^2}}, x, 1, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b x}}{\sqrt{a x + b x^2}}\right]}{\sqrt{b}}$$

$$\frac{2 \sqrt{x} \sqrt{a + b x} \operatorname{Log}\left[2 \left(b \sqrt{x} + \sqrt{b} \sqrt{a + b x}\right)\right]}{\sqrt{b} \sqrt{x} (a + b x)}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{6 x - x^2}}, x, 1, 0 \right\}$$

$$-\operatorname{ArcSin}\left[\frac{3 - x}{3}\right]$$

$$\frac{2 \sqrt{-6 + x} \sqrt{x} \operatorname{Log}\left[2 \left(\sqrt{-6 + x} + \sqrt{x}\right)\right]}{\sqrt{-(-6 + x) x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{(1-x)x}}, x, 3, 0 \right\}$$

$$-\text{ArcSin}[1-2x]$$

$$\frac{2\sqrt{-1+x}\sqrt{x}\text{Log}\left[2\left(\sqrt{-1+x}+\sqrt{x}\right)\right]}{\sqrt{-(-1+x)x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{4x+x^2}}, x, 1, 0 \right\}$$

$$2\text{ArcTanh}\left[\frac{x}{\sqrt{4x+x^2}}\right]$$

$$\frac{2\sqrt{x}\sqrt{4+x}\text{ArcSinh}\left[\frac{\sqrt{x}}{2}\right]}{\sqrt{x(4+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-2x+x^2}}, x, 1, 0 \right\}$$

$$2\text{ArcTanh}\left[\frac{x}{\sqrt{-2x+x^2}}\right]$$

$$\frac{2\sqrt{-2+x}\sqrt{x}\text{Log}\left[2\left(\sqrt{-2+x}+\sqrt{x}\right)\right]}{\sqrt{(-2+x)x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \sqrt{5x-9x^2}, x, 2, 0 \right\}$$

$$-\frac{1}{36}(5-18x)\sqrt{5x-9x^2}-\frac{25}{216}\text{ArcSin}\left[\frac{1}{5}(5-18x)\right]$$

$$\frac{\sqrt{-x(-5+9x)}\left(3\sqrt{x}\sqrt{-5+9x}(-5+18x)-25\text{Log}\left[2\left(3\sqrt{x}+\sqrt{-5+9x}\right)\right]\right)}{108\sqrt{x}\sqrt{-5+9x}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{ax+bx^2}}, x, 1, 0 \right\}$$

$$\frac{2\text{ArcTanh}\left[\frac{\sqrt{b}x}{\sqrt{ax+bx^2}}\right]}{\sqrt{b}}$$

$$\frac{2\sqrt{x}\sqrt{a+bx}\text{Log}\left[2\left(b\sqrt{x}+\sqrt{b}\sqrt{a+bx}\right)\right]}{\sqrt{b}\sqrt{x(a+bx)}}$$

Mathematica 7 Test Results for Algebraic Function Integration Problems

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x(a+bx)}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{bx}}{\sqrt{x(a+bx)}}\right]}{\sqrt{b}}$$

$$\frac{2 \sqrt{x} \sqrt{a+bx} \operatorname{Log}\left[2\left(b \sqrt{x} + \sqrt{b} \sqrt{a+bx}\right)\right]}{\sqrt{b} \sqrt{x(a+bx)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{\left(b + \frac{a}{x}\right) x^2}}, x, 1, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{bx}}{\sqrt{x(a+bx)}}\right]}{\sqrt{b}}$$

$$\frac{2 \sqrt{x} \sqrt{a+bx} \operatorname{Log}\left[2\left(b \sqrt{x} + \sqrt{b} \sqrt{a+bx}\right)\right]}{\sqrt{b} \sqrt{x(a+bx)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{\frac{a+bx^3}{x}}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{bx}}{\sqrt{\frac{a+bx^3}{x}}}\right]}{3 \sqrt{b}}$$

$$\frac{2 \sqrt{x} \sqrt{\frac{a+bx^3}{x}} \operatorname{Log}\left[2\left(b x^{3/2} + \sqrt{b} \sqrt{a+bx^3}\right)\right]}{3 \sqrt{b} \sqrt{a+bx^3}}$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{\frac{a+bx^5}{x^3}}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{bx}}{\sqrt{\frac{a+bx^5}{x^3}}}\right]}{5 \sqrt{b}}$$

$$\int \frac{1}{\sqrt{\frac{a+bx^5}{x^3}}} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x^{2-n} (a + b x^n)}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x}{\sqrt{x^2 (b + a x^n)}}\right]}{\sqrt{b} n}$$

$$\frac{2 x^{1-\frac{n}{2}} \sqrt{a + b x^n} \operatorname{Log}\left[2 \left(b x^{n/2} + \sqrt{b} \sqrt{a + b x^n}\right)\right]}{\sqrt{b} n \sqrt{x^{2-n} (a + b x^n)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{\frac{a-bx^3}{x}}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{\frac{a-bx^3}{x}}}\right]}{3 \sqrt{b}}$$

$$\frac{2 \sqrt{x} \sqrt{\frac{a-bx^3}{x}} \operatorname{ArcTan}\left[\frac{\sqrt{b} x^{3/2}}{\sqrt{a-bx^3}}\right]}{3 \sqrt{b} \sqrt{a-bx^3}}$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{\frac{a-bx^5}{x^3}}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{\frac{a-bx^5}{x^3}}}\right]}{5 \sqrt{b}}$$

$$\int \frac{1}{\sqrt{\frac{a-bx^5}{x^3}}} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x^{2-n} (a - b x^n)}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{b} x}{\sqrt{-x^2 (b - a x^n)}}\right]}{\sqrt{b} n}$$

$$\frac{2 x^{1-\frac{n}{2}} \sqrt{a - b x^n} \operatorname{ArcTan}\left[\frac{\sqrt{b} x^{n/2}}{\sqrt{a - b x^n}}\right]}{\sqrt{b} n \sqrt{x^2 (-b + a x^n)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x^n (a + b x^{2-n})}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x}{\sqrt{x^2 (b + a x^{-2+n})}}\right]}{\sqrt{b} (2 - n)}$$

$$- \frac{2 \sqrt{a} x^{n/2} \sqrt{1 + \frac{b x^{2-n}}{a}} \operatorname{ArcSinh}\left[\frac{\sqrt{b} x^{\frac{1-n}{2}}}{\sqrt{a}}\right]}{\sqrt{b} (-2 + n) \sqrt{b x^2 + a x^n}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x^2 (b + a x^{-2+n})}}, x, 1, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x}{\sqrt{x^2 (b + a x^{-2+n})}}\right]}{\sqrt{b} (2 - n)}$$

$$- \frac{2 \sqrt{a} x^{n/2} \sqrt{1 + \frac{b x^{2-n}}{a}} \operatorname{ArcSinh}\left[\frac{\sqrt{b} x^{\frac{1-n}{2}}}{\sqrt{a}}\right]}{\sqrt{b} (-2 + n) \sqrt{b x^2 + a x^n}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x (b x + a x^{-1+n})}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x}{\sqrt{x^2 (b + a x^{-2+n})}}\right]}{\sqrt{b} (2 - n)}$$

$$- \frac{2 \sqrt{a} x^{n/2} \sqrt{1 + \frac{b x^{2-n}}{a}} \operatorname{ArcSinh}\left[\frac{\sqrt{b} x^{\frac{1-n}{2}}}{\sqrt{a}}\right]}{\sqrt{b} (-2 + n) \sqrt{b x^2 + a x^n}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{b x^2 + a x^n}}, x, 2, 0 \right\}$$

$$\frac{2 \operatorname{ArcTanh}\left[\frac{\sqrt{b} x}{\sqrt{x^2 (b + a x^{-2+n})}}\right]}{\sqrt{b} (2 - n)}$$

$$- \frac{2 \sqrt{a} x^{n/2} \sqrt{1 + \frac{b x^{2-n}}{a}} \operatorname{ArcSinh}\left[\frac{\sqrt{b} x^{\frac{1-n}{2}}}{\sqrt{a}}\right]}{\sqrt{b} (-2 + n) \sqrt{b x^2 + a x^n}}$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{\frac{6}{x^3} - x^2}}, x, 2, 0 \right\}$$

$$\frac{2}{5} \text{ArcTan} \left[\frac{x}{\sqrt{\frac{6-x^5}{x^3}}} \right]$$

$$\int \frac{1}{\sqrt{\frac{6}{x^3} - x^2}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{1 + (x^3)^{2/3}}, x, 2, 0 \right\}$$

$$\frac{x \text{ArcTan}[(x^3)^{1/3}]}{(x^3)^{1/3}}$$

$$\int \frac{1}{1 + (x^3)^{2/3}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{1 + (x^2)^{3/2}}, x, 5, 0 \right\}$$

$$-\frac{x \text{ArcTan} \left[\frac{1-2\sqrt{x^2}}{\sqrt{3}} \right]}{\sqrt{3} \sqrt{x^2}} - \frac{x \text{Log} [1 + x^2 - \sqrt{x^2}]}{6 \sqrt{x^2}} + \frac{x \text{Log} [1 + \sqrt{x^2}]}{3 \sqrt{x^2}}$$

$$\int \frac{1}{1 + (x^2)^{3/2}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{1 + 4 \sqrt{x^4}}, x, 2, 0 \right\}$$

$$\frac{x \text{ArcTan} [2 (x^4)^{1/4}]}{2 (x^4)^{1/4}}$$

$$\int \frac{1}{1 + 4 \sqrt{x^4}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{1 - 4 \sqrt{x^4}}, x, 2, 0 \right\}$$

$$\frac{x \text{ArcTanh} [2 (x^4)^{1/4}]}{2 (x^4)^{1/4}}$$

$$\int \frac{1}{1 - 4 \sqrt{x^4}} dx$$

Incorrect antiderivative:

$$\left\{ \frac{1}{1 + 4 \left(x^6\right)^{1/3}}, x, 2, 0 \right\}$$

$$\frac{x \operatorname{ArcTan}\left[2 \left(x^6\right)^{1/6}\right]}{2 \left(x^6\right)^{1/6}}$$

$$\frac{1}{24 \left(-x^6\right)^{5/6}} \left(-2 x \left(-x^{12}\right)^{1/3} \operatorname{Beta}\left[-64 x^6, \frac{1}{2}, 0\right] + 2 x \left(x^6\right)^{2/3} \operatorname{Beta}\left[-64 x^6, \frac{5}{6}, 0\right] + \left(-x^6\right)^{5/6} \right. \\ \left. \left(-2 \operatorname{ArcTan}\left[\sqrt{3} - 4 x\right] + 4 \operatorname{ArcTan}\left[2 x\right] + 2 \operatorname{ArcTan}\left[\sqrt{3} + 4 x\right] - \sqrt{3} \operatorname{Log}\left[1 - 2 \sqrt{3} x + 4 x^2\right] + \sqrt{3} \operatorname{Log}\left[1 + 2 \sqrt{3} x + 4 x^2\right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{1 - 4 \left(x^6\right)^{1/3}}, x, 2, 0 \right\}$$

$$\frac{x \operatorname{ArcTanh}\left[2 \left(x^6\right)^{1/6}\right]}{2 \left(x^6\right)^{1/6}}$$

$$\frac{1}{24 \left(x^6\right)^{1/6}} \left(2 x \operatorname{Beta}\left[64 x^6, \frac{1}{2}, 0\right] + 2 x \operatorname{Beta}\left[64 x^6, \frac{5}{6}, 0\right] + \left(x^6\right)^{1/6} \right. \\ \left. \left(2 \sqrt{3} \operatorname{ArcTan}\left[\frac{-1 + 4 x}{\sqrt{3}}\right] + 2 \sqrt{3} \operatorname{ArcTan}\left[\frac{1 + 4 x}{\sqrt{3}}\right] - 2 \operatorname{Log}\left[-1 + 2 x\right] + 2 \operatorname{Log}\left[1 + 2 x\right] - \operatorname{Log}\left[1 - 2 x + 4 x^2\right] + \operatorname{Log}\left[1 + 2 x + 4 x^2\right] \right) \right)$$

Unable to integrate:

$$\left\{ \frac{1}{1 + 4 \left(x^{2n}\right)^{\frac{1}{n}}}, x, 2, 0 \right\}$$

$$\frac{1}{2} x \left(x^{2n}\right)^{-\frac{1}{2n}} \operatorname{ArcTan}\left[2 \left(x^{2n}\right)^{\frac{1}{2n}}\right]$$

$$\int \frac{1}{1 + 4 \left(x^{2n}\right)^{\frac{1}{n}}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{1 - 4 \left(x^{2n}\right)^{\frac{1}{n}}}, x, 2, 0 \right\}$$

$$\frac{1}{2} x \left(x^{2n}\right)^{-\frac{1}{2n}} \operatorname{ArcTanh}\left[2 \left(x^{2n}\right)^{\frac{1}{2n}}\right]$$

$$\int \frac{1}{1 - 4 \left(x^{2n}\right)^{\frac{1}{n}}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{a + b (c x^m)^{\frac{1}{m}}}, x, 2, 0 \right\}$$

$$\frac{x (c x^m)^{-1/m} \operatorname{Log}\left[a + b (c x^m)^{\frac{1}{m}}\right]}{b}$$

$$\int \frac{1}{a + b (c x^m)^{\frac{1}{m}}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{a + b (c x^m)^{2/m}}, x, 2, 0 \right\}$$

$$\frac{x (c x^m)^{-1/m} \operatorname{ArcTan}\left[\frac{\sqrt{b} (c x^m)^{\frac{1}{m}}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}}$$

$$\int \frac{1}{a + b (c x^m)^{2/m}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{(a + b (c x^m)^{2/m})^2}, x, 3, 0 \right\}$$

$$\frac{x}{2 a (a + b (c x^m)^{2/m})} + \frac{x (c x^m)^{-1/m} \operatorname{ArcTan}\left[\frac{\sqrt{b} (c x^m)^{\frac{1}{m}}}{\sqrt{a}}\right]}{2 a^{3/2} \sqrt{b}}$$

$$\int \frac{1}{(a + b (c x^m)^{2/m})^2} dx$$

Unable to integrate:

$$\left\{ \frac{1}{(a + b (c x^m)^{2/m})^3}, x, 4, 0 \right\}$$

$$\frac{x}{4 a (a + b (c x^m)^{2/m})^2} + \frac{3 x}{8 a^2 (a + b (c x^m)^{2/m})} + \frac{3 x (c x^m)^{-1/m} \operatorname{ArcTan}\left[\frac{\sqrt{b} (c x^m)^{\frac{1}{m}}}{\sqrt{a}}\right]}{8 a^{5/2} \sqrt{b}}$$

$$\int \frac{1}{(a + b (c x^m)^{2/m})^3} dx$$

Unable to integrate:

$$\left\{ \frac{1}{a + b (c x^m)^{3/m}}, x, 5, 0 \right\}$$

$$- \frac{x (c x^m)^{-1/m} \operatorname{ArcTan}\left[\frac{a^{1/3} - 2 b^{1/3} (c x^m)^{\frac{1}{m}}}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} a^{2/3} b^{1/3}} + \frac{x (c x^m)^{-1/m} \operatorname{Log}\left[a^{1/3} + b^{1/3} (c x^m)^{\frac{1}{m}}\right]}{3 a^{2/3} b^{1/3}} - \frac{x (c x^m)^{-1/m} \operatorname{Log}\left[a^{2/3} - a^{1/3} b^{1/3} (c x^m)^{\frac{1}{m}} + b^{2/3} (c x^m)^{2/m}\right]}{6 a^{2/3} b^{1/3}}$$

Mathematica 7 Test Results for Algebraic Function Integration Problems

$$\int \frac{1}{a + b (c x^m)^{3/m}} dx$$

Unable to integrate:

$$\left\{ \frac{1}{(a + b (c x^m)^{3/m})^2}, x, 6, 0 \right\}$$

$$\frac{x}{3 a (a + b (c x^m)^{3/m})} - \frac{2 x (c x^m)^{-1/m} \text{ArcTan}\left[\frac{a^{1/3} - 2 b^{1/3} (c x^m)^{\frac{1}{m}}}{\sqrt{3} a^{1/3}}\right]}{3 \sqrt{3} a^{5/3} b^{1/3}} +$$

$$\frac{2 x (c x^m)^{-1/m} \text{Log}\left[a^{1/3} + b^{1/3} (c x^m)^{\frac{1}{m}}\right]}{9 a^{5/3} b^{1/3}} - \frac{x (c x^m)^{-1/m} \text{Log}\left[a^{2/3} - a^{1/3} b^{1/3} (c x^m)^{\frac{1}{m}} + b^{2/3} (c x^m)^{2/m}\right]}{9 a^{5/3} b^{1/3}}$$

$$\int \frac{1}{(a + b (c x^m)^{3/m})^2} dx$$

Unable to integrate:

$$\left\{ \frac{1}{(a + b (c x^m)^{3/m})^3}, x, 7, 0 \right\}$$

$$\frac{x}{6 a (a + b (c x^m)^{3/m})^2} + \frac{5 x}{18 a^2 (a + b (c x^m)^{3/m})} - \frac{5 x (c x^m)^{-1/m} \text{ArcTan}\left[\frac{a^{1/3} - 2 b^{1/3} (c x^m)^{\frac{1}{m}}}{\sqrt{3} a^{1/3}}\right]}{9 \sqrt{3} a^{8/3} b^{1/3}} +$$

$$\frac{5 x (c x^m)^{-1/m} \text{Log}\left[a^{1/3} + b^{1/3} (c x^m)^{\frac{1}{m}}\right]}{27 a^{8/3} b^{1/3}} - \frac{5 x (c x^m)^{-1/m} \text{Log}\left[a^{2/3} - a^{1/3} b^{1/3} (c x^m)^{\frac{1}{m}} + b^{2/3} (c x^m)^{2/m}\right]}{54 a^{8/3} b^{1/3}}$$

$$\int \frac{1}{(a + b (c x^m)^{3/m})^3} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ x^{-1+n-p(1+q)} (a x^n + b x^p)^q, x, 2, 0 \right\}$$

$$\frac{x^{-p(1+q)} (x^n (a + b x^{-n+p}))^{1+q}}{a (n-p) (1+q)}$$

$$\frac{x^{-p(1+q)} \left(1 + \frac{a x^{n-p}}{b}\right)^{-q} (a x^n + b x^p)^q \left(a x^n \left(1 + \frac{a x^{n-p}}{b}\right)^q + b x^p \left(-1 + \left(1 + \frac{a x^{n-p}}{b}\right)^q\right)\right)}{a (n-p) (1+q)}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x^{1+m} (a (2+m) + b (3+m) x^2)}{\sqrt{a + b x^2}}, x, 1, 0 \right\}$$

$$x^{2+m} \sqrt{a + b x^2}$$

$$\frac{x^{2+m} \sqrt{a + b x^2} \left((3+m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, 1 + \frac{m}{2}, 2 + \frac{m}{2}, -\frac{b x^2}{a}\right] - \text{Hypergeometric2F1}\left[\frac{1}{2}, 1 + \frac{m}{2}, 2 + \frac{m}{2}, -\frac{b x^2}{a}\right] \right)}{(2+m) \sqrt{1 + \frac{b x^2}{a}}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{a(2+m)x^{1+m}}{\sqrt{a+bx^2}} + \frac{b(3+m)x^{3+m}}{\sqrt{a+bx^2}}, x, 2, 0 \right\}$$

$$\frac{x^{2+m}\sqrt{a+bx^2}}{(2+m)\sqrt{1+\frac{bx^2}{a}}} \left((3+m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, 1+\frac{m}{2}, 2+\frac{m}{2}, -\frac{bx^2}{a}\right] - \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+\frac{m}{2}, 2+\frac{m}{2}, -\frac{bx^2}{a}\right] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x^{-1+m}(2am+b(-1+2m)x)}{2(a+bx)^{3/2}}, x, 2, 0 \right\}$$

$$\frac{x^m}{\sqrt{a+bx}}$$

$$\frac{1}{2a^2(1+m)\sqrt{1+\frac{bx}{a}}} x^m \sqrt{a+bx} \left(2a(1+m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, m, 1+m, -\frac{bx}{a}\right] - \right.$$

$$\left. bx \left(2m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, 2+m, -\frac{bx}{a}\right] + \text{Hypergeometric2F1}\left[\frac{3}{2}, 1+m, 2+m, -\frac{bx}{a}\right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{x^{-1+m}(am+b(-1+m)x^2)}{(a+bx^2)^{3/2}}, x, 1, 0 \right\}$$

$$\frac{x^m}{\sqrt{a+bx^2}}$$

$$\frac{1}{a^2(2+m)\sqrt{1+\frac{bx^2}{a}}} x^m \sqrt{a+bx^2} \left(a(2+m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{m}{2}, 1+\frac{m}{2}, -\frac{bx^2}{a}\right] - \right.$$

$$\left. bx^2 \left(m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+\frac{m}{2}, 2+\frac{m}{2}, -\frac{bx^2}{a}\right] + \text{Hypergeometric2F1}\left[\frac{3}{2}, 1+\frac{m}{2}, 2+\frac{m}{2}, -\frac{bx^2}{a}\right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ -\frac{bx^m}{2(a+bx)^{3/2}} + \frac{mx^{-1+m}}{\sqrt{a+bx}}, x, 5, 0 \right\}$$

$$\frac{x^m}{\sqrt{a+bx}}$$

$$\frac{1}{2a^2(1+m)\sqrt{1+\frac{bx}{a}}} x^m \sqrt{a+bx} \left(2a(1+m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, m, 1+m, -\frac{bx}{a}\right] - \right.$$

$$\left. bx \left(2m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+m, 2+m, -\frac{bx}{a}\right] + \text{Hypergeometric2F1}\left[\frac{3}{2}, 1+m, 2+m, -\frac{bx}{a}\right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ -\frac{b x^{1+m}}{(a+b x^2)^{3/2}} + \frac{m x^{-1+m}}{\sqrt{a+b x^2}}, x, 3, 0 \right\}$$

$$\frac{x^m}{\sqrt{a+b x^2}}$$

$$\frac{1}{a^2 (2+m) \sqrt{1+\frac{b x^2}{a}}} x^m \sqrt{a+b x^2} \left(a (2+m) \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{m}{2}, 1+\frac{m}{2}, -\frac{b x^2}{a}\right] - \right.$$

$$\left. b x^2 \left(m \text{Hypergeometric2F1}\left[\frac{1}{2}, 1+\frac{m}{2}, 2+\frac{m}{2}, -\frac{b x^2}{a}\right] + \text{Hypergeometric2F1}\left[\frac{3}{2}, 1+\frac{m}{2}, 2+\frac{m}{2}, -\frac{b x^2}{a}\right] \right) \right)$$

Valid but unnecessarily complicated antiderivative:

$$\{x^n \sqrt{a^2 + x^{1+n}}, x, 2, 0\}$$

$$\frac{2 (a^2 + x^{1+n})^{3/2}}{3 (1+n)}$$

$$\frac{2 \left(2 a^2 x^{1+n} + x^{2+2n} + a^4 \left(1 - \sqrt{1 + \frac{x^{1+n}}{a^2}} \right) \right)}{3 (1+n) \sqrt{a^2 + x^{1+n}}}$$

Algebraic function problems involving trinomials

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{b x - b^2 x^2}}, x, 1, 0 \right\}$$

$$-\frac{\text{ArcSin}[1 - 2 b x]}{b}$$

$$\frac{2 \sqrt{x} \sqrt{-1 + b x} \text{Log}\left[2 \left(b \sqrt{x} + \sqrt{b} \sqrt{-1 + b x}\right)\right]}{\sqrt{b} \sqrt{-b x (-1 + b x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{x + \sqrt{-3 - 4 x - x^2}}, x, 9, 0 \right\}$$

$$-\text{ArcTan}\left[\frac{\sqrt{-1 - x}}{\sqrt{3 + x}}\right] - \sqrt{2} \text{ArcTan}\left[\frac{1 - \frac{3\sqrt{-1-x}}{\sqrt{3+x}}}{\sqrt{2}}\right] - \frac{1}{2} \text{Log}\left[\frac{2}{3 + x}\right] + \frac{1}{2} \text{Log}\left[-\frac{2 x}{3 + x} - \frac{2 \sqrt{-1 - x}}{\sqrt{3 + x}}\right]$$

$$\begin{aligned}
& \frac{1}{8} \left(4 \operatorname{ArcSin}[2 + x] - 4 \sqrt{2} \operatorname{ArcTan}[\sqrt{2} (1 + x)] + \right. \\
& 2 \sqrt{1 - 2 i \sqrt{2}} \operatorname{ArcTan} \left[\left(60 + 51 i \sqrt{2} + (-16 + 6 i \sqrt{2}) x^4 + 54 i \sqrt{1 - 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} + \right. \right. \\
& \quad \left. x \left(68 + 176 i \sqrt{2} + 99 i \sqrt{1 - 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) + 2 i x^3 \left(34 (i + \sqrt{2}) + 9 \sqrt{1 - 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) + \right. \\
& \quad \left. \left. i x^2 \left(44 i + 185 \sqrt{2} + 72 \sqrt{1 - 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) \right] \right) / \\
& \left(93 i + 150 \sqrt{2} + 20 (17 i + 22 \sqrt{2}) x + (493 i + 466 \sqrt{2}) x^2 + 16 (19 i + 13 \sqrt{2}) x^3 + (66 i + 32 \sqrt{2}) x^4 \right) - \\
& \frac{1}{\sqrt{1 + 2 i \sqrt{2}}} 2 i (-i + 2 \sqrt{2}) \operatorname{ArcTan} \left[\left(-60 + 51 i \sqrt{2} + 2 (8 + 3 i \sqrt{2}) x^4 + 54 i \sqrt{1 + 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} + \right. \right. \\
& \quad \left. 2 x^3 \left(34 + 34 i \sqrt{2} + 9 i \sqrt{1 + 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) + x^2 \left(44 + 185 i \sqrt{2} + 72 i \sqrt{1 + 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) + \right. \\
& \quad \left. \left. i x \left(68 i + 176 \sqrt{2} + 99 \sqrt{1 + 2 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) \right] \right) / \\
& \left(-93 i + 150 \sqrt{2} + 20 (-17 i + 22 \sqrt{2}) x + (-493 i + 466 \sqrt{2}) x^2 + 16 (-19 i + 13 \sqrt{2}) x^3 + (-66 i + 32 \sqrt{2}) x^4 \right) + \\
& 2 \operatorname{Log}[3 + 4 x + 2 x^2] + \frac{(-i + 2 \sqrt{2}) \operatorname{Log}[4 (3 + 4 x + 2 x^2)^2]}{\sqrt{1 + 2 i \sqrt{2}}} + \frac{(i + 2 \sqrt{2}) \operatorname{Log}[4 (3 + 4 x + 2 x^2)^2]}{\sqrt{1 - 2 i \sqrt{2}}} - \\
& \frac{1}{\sqrt{1 - 2 i \sqrt{2}}} \\
& (i + 2 \sqrt{2}) \operatorname{Log}[(3 + 4 x + 2 x^2) \\
& \left(-3 - 6 i \sqrt{2} + (-2 - 2 i \sqrt{2}) x^2 + 2 \sqrt{2 - 4 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} + 2 x \left(-2 - 4 i \sqrt{2} + \sqrt{2 - 4 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) \right)] - \\
& \frac{1}{\sqrt{1 + 2 i \sqrt{2}}} (-i + 2 \sqrt{2}) \operatorname{Log}[(3 + 4 x + 2 x^2) \left(-3 + 6 i \sqrt{2} + 2 i (i + \sqrt{2}) x^2 + \right. \\
& \quad \left. 2 \sqrt{2 + 4 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} + 2 x \left(-2 + 4 i \sqrt{2} + \sqrt{2 + 4 i \sqrt{2}} \sqrt{-3 - 4 x - x^2} \right) \right)] \Big)
\end{aligned}$$

Incorrect antiderivative:

$$\begin{aligned}
& \left\{ \frac{1}{\sqrt{8 x - 8 x^2 + 4 x^3 - x^4}}, x, 3, 0 \right\} \\
& - \frac{\sqrt{3 + (1 - x)^2} \sqrt{(2 - x) x} \operatorname{EllipticF}[\operatorname{ArcSin}[1 - x], -\frac{1}{3}]}{\sqrt{3} \sqrt{3 - 2 (1 - x)^2 - (1 - x)^4}}
\end{aligned}$$

$$\frac{\sqrt{-i + \sqrt{3} + \frac{4i}{x}} \sqrt{-\frac{i(-2+x)}{(-i+\sqrt{3})x}} x (-4+x-i\sqrt{3}x) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{i+\sqrt{3}-\frac{4i}{x}}}{\sqrt{2} 3^{1/4}}\right], \frac{2\sqrt{3}}{-i+\sqrt{3}}\right]}{\sqrt{2} \sqrt{i + \sqrt{3} - \frac{4i}{x}} \sqrt{-x(-8+8x-4x^2+x^3)}}$$

Valid but unnecessarily complicated antiderivative:

$$\frac{\{\sqrt{3-2x^2-x^4}, x, 5, 0\} - \frac{1}{3}x\sqrt{3-2x^2-x^4} - \frac{2\operatorname{EllipticE}[\operatorname{ArcSin}[x], -\frac{1}{3}]}{\sqrt{3}} + \frac{4\operatorname{EllipticF}[\operatorname{ArcSin}[x], -\frac{1}{3}]}{\sqrt{3}} - x(-3+2x^2+x^4) - 2i\sqrt{3-2x^2-x^4}\operatorname{EllipticE}\left[i\operatorname{ArcSinh}\left[\frac{x}{\sqrt{3}}\right], -3\right] - 4i\sqrt{3-2x^2-x^4}\operatorname{EllipticF}\left[i\operatorname{ArcSinh}\left[\frac{x}{\sqrt{3}}\right], -3\right]}{3\sqrt{3-2x^2-x^4}}$$

Valid but unnecessarily complicated antiderivative:

$$\frac{\{\sqrt{(1-x^2)(3+x^2)}, x, 6, 0\} - \frac{1}{3}x\sqrt{3-2x^2-x^4} - \frac{2\operatorname{EllipticE}[\operatorname{ArcSin}[x], -\frac{1}{3}]}{\sqrt{3}} + \frac{4\operatorname{EllipticF}[\operatorname{ArcSin}[x], -\frac{1}{3}]}{\sqrt{3}} - x(-3+2x^2+x^4) - 2i\sqrt{3-2x^2-x^4}\operatorname{EllipticE}\left[i\operatorname{ArcSinh}\left[\frac{x}{\sqrt{3}}\right], -3\right] - 4i\sqrt{3-2x^2-x^4}\operatorname{EllipticF}\left[i\operatorname{ArcSinh}\left[\frac{x}{\sqrt{3}}\right], -3\right]}{3\sqrt{3-2x^2-x^4}}$$

Incorrect antiderivative:

$$\frac{\{\sqrt{8x-8x^2+4x^3-x^4}, x, 6, 0\} - \frac{1}{3}\sqrt{3-2(1-x)^2-(1-x)^4}(1-x) + \frac{2\operatorname{EllipticE}[\operatorname{ArcSin}[1-x], -\frac{1}{3}]}{\sqrt{3}} - \frac{4\operatorname{EllipticF}[\operatorname{ArcSin}[1-x], -\frac{1}{3}]}{\sqrt{3}} - \frac{1}{3\sqrt{-x(-8+8x-4x^2+x^3)}}}{\left(-16+24x-24x^2+14x^3-5x^4+x^5 - \frac{2i\sqrt{2}(-2+x)x\sqrt{\frac{4-2x+x^2}{x^2}}\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{i+\sqrt{3}-\frac{4i}{x}}}{\sqrt{2} 3^{1/4}}\right], \frac{2\sqrt{3}}{-i+\sqrt{3}}\right]}{\sqrt{-\frac{i(-2+x)}{(-i+\sqrt{3})x}}} + 8i\sqrt{2}\sqrt{-\frac{i(-2+x)}{(-i+\sqrt{3})x}}x^2\sqrt{\frac{4-2x+x^2}{x^2}}\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{i+\sqrt{3}-\frac{4i}{x}}}{\sqrt{2} 3^{1/4}}\right], \frac{2\sqrt{3}}{-i+\sqrt{3}}\right] \right)}$$

Incorrect antiderivative:

$$\left\{ \sqrt{(2-x)(4-2x+x^2)}, x, 7, 0 \right\}$$

$$-\frac{1}{3} \sqrt{3-2(1-x)^2-(1-x)^4} (1-x) + \frac{2 \operatorname{EllipticE}[\operatorname{ArcSin}[1-x], -\frac{1}{3}]}{\sqrt{3}} - \frac{4 \operatorname{EllipticF}[\operatorname{ArcSin}[1-x], -\frac{1}{3}]}{\sqrt{3}}$$

$$\frac{1}{3(-2+x)x} \sqrt{-x(-8+8x-4x^2+x^3)} \sqrt{\frac{4-2x+x^2}{x^2}}$$

$$\left(\sqrt{\frac{4-2x+x^2}{x^2}} (-4+4x-3x^2+x^3) + 2\sqrt{2} (-i+\sqrt{3}) \sqrt{-\frac{i(-2+x)}{(-i+\sqrt{3})x}} \operatorname{EllipticE}[\operatorname{ArcSin}[\frac{\sqrt{i+\sqrt{3}-\frac{4i}{x}}}{\sqrt{2} 3^{1/4}}], \frac{2\sqrt{3}}{-i+\sqrt{3}}] + 8i\sqrt{2} \sqrt{-\frac{i(-2+x)}{(-i+\sqrt{3})x}} \operatorname{EllipticF}[\operatorname{ArcSin}[\frac{\sqrt{i+\sqrt{3}-\frac{4i}{x}}}{\sqrt{2} 3^{1/4}}], \frac{2\sqrt{3}}{-i+\sqrt{3}}] \right)$$

Incorrect antiderivative:

$$\left\{ \frac{1}{\sqrt{9-6x-44x^2+15x^3+3x^4}}, x, 6, 0 \right\}$$

$$\sqrt{\frac{1}{613} (91-6\sqrt{213})} \sqrt{15-\sqrt{213}+\frac{2(-3+x)}{x^2}} \sqrt{15+\sqrt{213}+\frac{2(-3+x)}{x^2}} x^2 \operatorname{EllipticF}[\operatorname{ArcSin}[\frac{6(-\frac{1}{6}+\frac{1}{x})}{\sqrt{91-6\sqrt{213}}}], \frac{-6552+432\sqrt{213}}{-6552-432\sqrt{213}}]$$

$$\sqrt{9-6x-44x^2+15x^3+3x^4}$$

$$- \left(2 \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{((x-\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 1]) (\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2] - \right.$$

$$\left. \frac{\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 4]}{((\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 1] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 4]))} \right) / ((x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2]) ((\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 3]) (\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 1] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 4]))) / ((\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 1] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 3]) (\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 4])))]$$

$$\sqrt{\frac{x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 1]}{x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2]}} (x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2])^2$$

$$\sqrt{\frac{x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 3]}{x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2]}}$$

$$\sqrt{\frac{x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 4]}{x - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2]}} \Big/$$

$$(\sqrt{((9-6x-44x^2+15x^3+3x^4) (\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 1] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 3]) (\operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 2] - \operatorname{Root}[9-6\#1-44\#1^2+15\#1^3+3\#1^4\&, 4]))})$$

Incorrect antiderivative:

$$\left\{ \sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4}, x, -3, 0 \right\}$$
$$\frac{\sqrt{\frac{1}{613} \left(91 - 6\sqrt{213} \right)} \sqrt{15 - \sqrt{213} + \frac{2(-3+x)}{x^2}} \sqrt{15 + \sqrt{213} + \frac{2(-3+x)}{x^2}} x^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{6\left(-\frac{1}{6}+\frac{1}{x}\right)}{\sqrt{91-6\sqrt{213}}}\right], \frac{-6552+432\sqrt{213}}{-6552-432\sqrt{213}}\right]}{\sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4}}$$
$$\left(\frac{5}{12} + \frac{x}{3}\right) \sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4} + \frac{1}{24} \left(\left(736 \left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)^2 \right.$$
$$\left. - \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right]\right)\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)/\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)]\right],$$
$$- \left(\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]\right)$$
$$\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)/$$
$$\left(\left(-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]\right)$$
$$\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right) \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] +$$
$$\text{EllipticPi}\left[\frac{-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]}{-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]},$$
$$\text{ArcSin}\left[\sqrt{\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right]\right)\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)/\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)\right],$$
$$- \left(\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]\right)$$
$$\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)/$$
$$\left(\left(-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]\right)$$
$$\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)$$
$$\left.\left(-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)\right]$$
$$\sqrt{\frac{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]}{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]}}$$
$$\sqrt{\frac{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]}{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]}}$$
$$\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)$$
$$\sqrt{\left(\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right]\right)\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right)/\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)\right)}$$

$$\left(\sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4} \left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right] \right) \right) /$$
$$\left(\sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4} \left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right] \right) \right.$$
$$\sqrt{\left((-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]) \right.$$
$$\left. \left. (-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]) \right) \right) +$$
$$348 \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right]\right) \left(-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] + \right.\right.}\right.\right.$$
$$\left.\left.\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right)\right) / \left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right) \right.$$
$$\left. \left. (-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]) \right) \right],$$
$$\left(\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right] \right) \right.$$
$$\left. \left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right] \right) \right) /$$
$$\left(\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right] \right) \right.$$
$$\left. \left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right] \right) \right)]$$
$$\sqrt{\frac{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right]}{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]}} \left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)^2$$
$$\sqrt{\frac{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]}{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]}}$$
$$\sqrt{\frac{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]}{x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]}}$$
$$\left(\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right] \right) \Bigg/$$
$$\left(\sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4} \left(-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right] \right) \right.$$
$$\sqrt{\left((-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]) \right.$$
$$\left. \left. (-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]) \right) \right) -$$
$$\frac{1}{\sqrt{9 - 6x - 44x^2 + 15x^3 + 3x^4}} 577 \left(\left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right]\right) \right.$$
$$\left. \left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 3\right]\right) \left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 4\right]\right) + \right.$$
$$\left. \left(x - \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)^2 \right.$$
$$\left. \left(-\text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 1\right] + \text{Root}\left[9 - 6\#1 - 44\#1^2 + 15\#1^3 + 3\#1^4 \&, 2\right]\right)$$

[illegible]

$$\left(-\text{Root}\left[9 - 6 \#1 - 44 \#1^2 + 15 \#1^3 + 3 \#1^4 \&, 1\right] - \text{Root}\left[9 - 6 \#1 - 44 \#1^2 + 15 \#1^3 + 3 \#1^4 \&, 2\right] - \right. \\ \left. \text{Root}\left[9 - 6 \#1 - 44 \#1^2 + 15 \#1^3 + 3 \#1^4 \&, 3\right] - \text{Root}\left[9 - 6 \#1 - 44 \#1^2 + 15 \#1^3 + 3 \#1^4 \&, 4\right] \right) \Bigg/ \\ \left(-\text{Root}\left[9 - 6 \#1 - 44 \#1^2 + 15 \#1^3 + 3 \#1^4 \&, 2\right] + \text{Root}\left[9 - 6 \#1 - 44 \#1^2 + 15 \#1^3 + 3 \#1^4 \&, 4\right] \right) \Bigg) \Bigg)$$

Incorrect antiderivative:

$$\left\{ \frac{x}{\sqrt{-71 - 96x + 10x^2 + x^4}}, x, -1, 0 \right\} \\ - \frac{1}{8} \text{Log}\left[-10001 - 3124x^2 + 1408x^3 - 54x^4 + 128x^5 - 20x^6 - x^8 + \sqrt{-71 - 96x + 10x^2 + x^4} (781 - 528x + 27x^2 - 80x^3 + 15x^4 + x^6)\right] \\ - \left(2 \left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] \right) \left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] \right) \right. \\ \left(\text{EllipticPi}\left[\frac{\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]}{\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]}, \right. \\ \text{ArcSin}\left[\sqrt{\left(\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right]\right) \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \right. \right.} \\ \left. \left. \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)\right) / \left(\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right]\right) \right. \\ \left. \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)\right)\right], \\ - \left(\left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 3\right]\right) \right. \\ \left. \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right) \right) \Bigg/ \\ \left(\left(-\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] + \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 3\right]\right) \right. \\ \left. \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right) \right) \\ \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] \right) + \\ \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\left(\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right]\right) \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \right. \right.} \right. \right. \\ \left. \left. \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)\right) / \left(\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right]\right) \right. \right. \\ \left. \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)\right)\right], \\ - \left(\left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 3\right]\right) \right. \\ \left. \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right) \right) \Bigg/ \\ \left(\left(-\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] + \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 3\right]\right) \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \right. \right. \\ \left. \left. \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)\right) \Bigg] \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] \Bigg) \\ \sqrt{\frac{x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 3\right]}{\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right]\right) \left(-\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] + \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 3\right]\right)}} \\ \sqrt{\frac{x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]}{\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right]\right) \left(-\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] + \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)}} \Bigg/ \\ \left(\sqrt{-71 - 96x + 10x^2 + x^4} \right. \\ \left. \sqrt{\frac{\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right]\right) \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)}{\left(x - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 2\right]\right) \left(\text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 1\right] - \text{Root}\left[-71 - 96\#1 + 10\#1^2 + \#1^4 \&, 4\right]\right)}} \right)$$

Mathematica 7 Test Results for Algebraic Function Integration Problems

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x+x^2}}, x, 1, 0 \right\}$$

$$2 \operatorname{ArcTanh}\left[\frac{x}{\sqrt{x+x^2}}\right]$$

$$\frac{2 \sqrt{x} \sqrt{1+x} \operatorname{ArcSinh}[\sqrt{x}]}{\sqrt{x(1+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{(b-x)(-a+x)}}, x, 2, 0 \right\}$$

$$-\operatorname{ArcTan}\left[\frac{a+b-2x}{2\sqrt{-ab+(a+b)x-x^2}}\right]$$

$$-\frac{\sqrt{b-x}\sqrt{-a+x}\operatorname{ArcTan}\left[\frac{a+b-2x}{2\sqrt{b-x}\sqrt{-a+x}}\right]}{\sqrt{(b-x)(-a+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{-7+2x+5x^2}(8+12x+5x^2)}, x, 3, 0 \right\}$$

$$\left(-\frac{1}{20}+\frac{i}{10}\right)\operatorname{ArcTan}\left[\frac{\left(\frac{1}{50}+\frac{i}{100}\right)((-164-8i)-(100+40i)x)}{\sqrt{-7+2x+5x^2}}\right]-\left(\frac{1}{10}-\frac{i}{20}\right)\operatorname{ArcTanh}\left[\frac{\left(\frac{1}{100}+\frac{i}{50}\right)((-164+8i)-(100-40i)x)}{\sqrt{-7+2x+5x^2}}\right]$$

$$\frac{1}{40}\left((2+4i)\operatorname{ArcTan}\left[\frac{5(2+x)}{2\sqrt{-7+2x+5x^2}}\right]+i\left((4+2i)\operatorname{ArcTan}\left[\frac{2\sqrt{-7+2x+5x^2}}{5(2+x)}\right]+\operatorname{Log}\left[\frac{1327104}{625}\right]-\right.\right.$$

$$\left.\left.2\operatorname{Log}[8+12x+5x^2]+(1+2i)\operatorname{Log}[9+26x+15x^2-5\sqrt{-7+2x+5x^2}-5x\sqrt{-7+2x+5x^2}]+(1-2i)\operatorname{Log}[9+26x+15x^2+5\sqrt{-7+2x+5x^2}+5x\sqrt{-7+2x+5x^2}]\right)\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{(1+\sqrt{x})^{1/3}}{x}, x, 7, 0 \right\}$$

$$6(1+\sqrt{x})^{1/3}-2\sqrt{3}\operatorname{ArcTan}\left[\frac{1+2(1+\sqrt{x})^{1/3}}{\sqrt{3}}\right]+2\operatorname{Log}[1-(1+\sqrt{x})^{1/3}]-\operatorname{Log}[1+(1+\sqrt{x})^{1/3}+(1+\sqrt{x})^{2/3}]$$

$$\frac{6+6\sqrt{x}-3\left(1+\frac{1}{\sqrt{x}}\right)^{2/3}\operatorname{Hypergeometric2F1}\left[\frac{2}{3},\frac{2}{3},\frac{5}{3},-\frac{1}{\sqrt{x}}\right]}{(1+\sqrt{x})^{2/3}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(1+x) \sqrt{2x+x^2}}, x, 1, 0 \right\}$$

$$\text{ArcTan}\left[\sqrt{2x+x^2}\right]$$

$$\frac{2\sqrt{x} \sqrt{2+x} \text{ArcTan}\left[\sqrt{\frac{x}{2+x}}\right]}{\sqrt{x(2+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(1+2x) \sqrt{x+x^2}}, x, 1, 0 \right\}$$

$$\text{ArcTan}\left[2\sqrt{x+x^2}\right]$$

$$\frac{2\sqrt{x} \sqrt{1+x} \text{ArcTan}\left[\sqrt{\frac{x}{1+x}}\right]}{\sqrt{x(1+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{x-x^2}}{1+x}, x, 3, 0 \right\}$$

$$\sqrt{x-x^2} - \frac{3}{2} \text{ArcSin}[1-2x] + \sqrt{2} \text{ArcTan}\left[\frac{1-3x}{2\sqrt{2}\sqrt{x-x^2}}\right]$$

$$\frac{1}{2\sqrt{-1+x}\sqrt{x}} \sqrt{-(-1+x)x}$$

$$\left(2\sqrt{-1+x}\sqrt{x} - 6\text{Log}\left[2\left(\sqrt{-1+x} + \sqrt{x}\right)\right] - \sqrt{2}\text{Log}\left[-1-2\sqrt{2}\sqrt{-1+x}\sqrt{x}+3x\right] + \sqrt{2}\text{Log}\left[-1+2\sqrt{2}\sqrt{-1+x}\sqrt{x}+3x\right]\right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ (ax^m + bx^{1+6m})^5, x, 3, 0 \right\}$$

$$\frac{(a + bx^{1+5m})^6}{6b(1+5m)}$$

$$\frac{x^{1+5m} (6a^5 + 15a^4bx^{1+5m} + 20a^3b^2x^{2+10m} + 15a^2b^3x^{3+15m} + 6ab^4x^{4+20m} + b^5x^{5+25m})}{6+30m}$$

Incorrect antiderivative:

$$\left\{ \frac{\sqrt{-\frac{x}{1+x}}}{x}, x, 2, 0 \right\}$$

$$2\text{ArcTan}\left[\sqrt{-\frac{x}{1+x}}\right]$$

$$\frac{2 \sqrt{-\frac{x}{1+x}} \operatorname{ArcSinh}[\sqrt{x}]}{\sqrt{\frac{x}{1+x}}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{\frac{1-x}{1+x}}}{-1+x}, x, 2, 0 \right\}$$

$$2 \operatorname{ArcTan}\left[\sqrt{\frac{1-x}{1+x}}\right]$$

$$\frac{2 \sqrt{\frac{1-x}{1+x}} \sqrt{1-x^2} \operatorname{ArcSin}\left[\frac{\sqrt{1+x}}{\sqrt{2}}\right]}{-1+x}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{4-(2+x)^2}}, x, 2, 0 \right\}$$

$$-\operatorname{ArcSin}\left[\frac{1}{2}(-2-x)\right]$$

$$\frac{2 \sqrt{x} \sqrt{4+x} \operatorname{ArcSinh}\left[\frac{\sqrt{x}}{2}\right]}{\sqrt{-x(4+x)}}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x}-x^{5/2}}, x, 4, 0 \right\}$$

$$\operatorname{ArcTan}[\sqrt{x}] + \operatorname{ArcTanh}[\sqrt{x}]$$

$$\frac{1}{2} \left(2 \operatorname{ArcTan}[\sqrt{x}] - \operatorname{Log}[-1+\sqrt{x}] + \operatorname{Log}[1+\sqrt{x}] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{x}(1-x^2)}, x, 4, 0 \right\}$$

$$\operatorname{ArcTan}[\sqrt{x}] + \operatorname{ArcTanh}[\sqrt{x}]$$

$$\frac{1}{2} \left(2 \operatorname{ArcTan}[\sqrt{x}] - \operatorname{Log}[-1+\sqrt{x}] + \operatorname{Log}[1+\sqrt{x}] \right)$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{x}}{x-x^3}, x, 4, 0 \right\}$$

$$\operatorname{ArcTan}[\sqrt{x}] + \operatorname{ArcTanh}[\sqrt{x}]$$

$$\frac{1}{2} \left(2 \operatorname{ArcTan}[\sqrt{x}] - \operatorname{Log}[-1 + \sqrt{x}] + \operatorname{Log}[1 + \sqrt{x}] \right)$$

Unable to integrate:

$$\left\{ \frac{1}{1-x^4} - \frac{\sqrt{x^6}}{x-x^5}, x, 9, 0 \right\}$$

$$\frac{\operatorname{ArcTan}[x]}{2} + \frac{\sqrt{x^6} (\operatorname{ArcTan}[x] - \operatorname{ArcTanh}[x])}{2 x^3} + \frac{\operatorname{ArcTanh}[x]}{2}$$

$$\int \left(\frac{1}{1-x^4} - \frac{\sqrt{x^6}}{x-x^5} \right) dx$$

Unable to integrate:

$$\left\{ \frac{1}{1-x^4} - \frac{\sqrt{x^6}}{x(1-x^4)}, x, 8, 0 \right\}$$

$$\frac{\operatorname{ArcTan}[x]}{2} + \frac{\sqrt{x^6} (\operatorname{ArcTan}[x] - \operatorname{ArcTanh}[x])}{2 x^3} + \frac{\operatorname{ArcTanh}[x]}{2}$$

$$\int \left(\frac{1}{1-x^4} - \frac{\sqrt{x^6}}{x(1-x^4)} \right) dx$$

Unable to integrate:

$$\left\{ \frac{x - \sqrt{x^6}}{x-x^5}, x, 9, 0 \right\}$$

$$\frac{\operatorname{ArcTan}[x]}{2} + \frac{\sqrt{x^6} (\operatorname{ArcTan}[x] - \operatorname{ArcTanh}[x])}{2 x^3} + \frac{\operatorname{ArcTanh}[x]}{2}$$

$$\int \frac{x - \sqrt{x^6}}{x-x^5} dx$$

Unable to integrate:

$$\left\{ \frac{x - \sqrt{x^6}}{x(1-x^4)}, x, 9, 0 \right\}$$

$$\frac{\operatorname{ArcTan}[x]}{2} + \frac{\sqrt{x^6} (\operatorname{ArcTan}[x] - \operatorname{ArcTanh}[x])}{2 x^3} + \frac{\operatorname{ArcTanh}[x]}{2}$$

$$\int \frac{x - \sqrt{x^6}}{x(1-x^4)} dx$$

Unable to integrate:

$$\left\{ \frac{1 - \frac{\sqrt{x^6}}{x}}{1-x^4}, x, 9, 0 \right\}$$

$$\frac{\text{ArcTan}[x]}{2} + \frac{\sqrt{x^6} (\text{ArcTan}[x] - \text{ArcTanh}[x])}{2 x^3} + \frac{\text{ArcTanh}[x]}{2}$$

$$\int \frac{1 - \frac{\sqrt{x^6}}{x}}{1 - x^4} dx$$

Unable to integrate:

$$\left\{ \frac{x}{x + \sqrt{x^6}}, x, 10, 0 \right\}$$

$$\frac{\text{ArcTan}[x]}{2} + \frac{\sqrt{x^6} (\text{ArcTan}[x] - \text{ArcTanh}[x])}{2 x^3} + \frac{\text{ArcTanh}[x]}{2}$$

$$\int \frac{x}{x + \sqrt{x^6}} dx$$

Unable to integrate:

$$\left\{ \frac{\sqrt{x} - \sqrt{x^3}}{x - x^3}, x, 11, 0 \right\}$$

$$\text{ArcTan}[\sqrt{x}] + \frac{\sqrt{x^3} (\text{ArcTan}[\sqrt{x}] - \text{ArcTanh}[\sqrt{x}])}{x^{3/2}} + \text{ArcTanh}[\sqrt{x}]$$

$$\int \frac{\sqrt{x} - \sqrt{x^3}}{x - x^3} dx$$

Unable to integrate:

$$\left\{ \frac{1}{\sqrt{x} + \sqrt{x^3}}, x, 12, 0 \right\}$$

$$\text{ArcTan}[\sqrt{x}] + \frac{\sqrt{x^3} (\text{ArcTan}[\sqrt{x}] - \text{ArcTanh}[\sqrt{x}])}{x^{3/2}} + \text{ArcTanh}[\sqrt{x}]$$

$$\int \frac{1}{\sqrt{x} + \sqrt{x^3}} dx$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{\sqrt{1 + \frac{1}{x^2}} x}{(1 + x^2)^2}, x, 3, 0 \right\}$$

$$\frac{1}{\sqrt{1 + \frac{1}{x^2}}}$$

$$\frac{\sqrt{1 + \frac{1}{x^2}} x^2}{1 + x^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{\sqrt{1 + \frac{1}{x^2}} x (1 + x^2)}, x, 3, 0 \right\}$$

$$\frac{1}{\sqrt{1 + \frac{1}{x^2}}}$$

$$\frac{\sqrt{1 + \frac{1}{x^2}} x^2}{1 + x^2}$$

Valid but unnecessarily complicated antiderivative:

$$\left\{ \frac{1}{(1 + x) \sqrt{2x + x^2}}, x, 1, 0 \right\}$$

$$\text{ArcTan}\left[\sqrt{2x + x^2}\right]$$

$$\frac{2\sqrt{x}\sqrt{2+x}\text{ArcTan}\left[\sqrt{\frac{x}{2+x}}\right]}{\sqrt{x(2+x)}}$$