

Rubi 3 Test Suite Results

Indefinite Integration Problems Involving Inverse Trig Functions

Unable to integrate:

$$\left\{ \frac{\text{ArcSin}[a + b x]}{x}, x, -3, 3 \right\}$$

$$\begin{aligned} & \frac{1}{8} i (\pi - 2 \text{ArcSin}[a + b x])^2 - 2 i \text{ArcTanh} \left[\frac{(1+a) \left(-1 + a + b x - i \sqrt{1 - (a + b x)^2} \right)}{\sqrt{-1 + a^2} \left(1 + a + b x - i \sqrt{1 - (a + b x)^2} \right)} \right] \left(\text{Log}[2] - 2 \text{Log} \left[i \sqrt{1-a} + \sqrt{1+a} \right] \right) + \\ & \frac{1}{2} \pi \text{Log}[b x] - \left(\text{ArcCos}[a + b x] - i \left(\text{Log}[2] - 2 \text{Log} \left[i \sqrt{1-a} + \sqrt{1+a} \right] \right) \right) \text{Log} \left[1 + \left(-a + \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] - \\ & \left(\text{ArcCos}[a + b x] + i \left(\text{Log}[2] - 2 \text{Log} \left[i \sqrt{1-a} + \sqrt{1+a} \right] \right) \right) \text{Log} \left[1 - \left(a + \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] + \\ & i \text{PolyLog} \left[2, \left(a - \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] + i \text{PolyLog} \left[2, \left(a + \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] \end{aligned}$$

$$\text{Subst} \left[\text{Int} \left[\frac{x \cos[x]}{-a + \sin[x]}, x \right], x, \text{ArcSin}[a + b x] \right]$$

Unable to integrate:

$$\left\{ \frac{\text{ArcCos}[a + b x]}{x}, x, -2, 2 \right\}$$

$$\begin{aligned} & -\frac{1}{8} i (\pi - 2 \text{ArcSin}[a + b x])^2 + 2 i \text{ArcTanh} \left[\frac{(1+a) \left(-1 + a + b x - i \sqrt{1 - (a + b x)^2} \right)}{\sqrt{-1 + a^2} \left(1 + a + b x - i \sqrt{1 - (a + b x)^2} \right)} \right] \left(\text{Log}[2] - 2 \text{Log} \left[i \sqrt{1-a} + \sqrt{1+a} \right] \right) + \\ & \left(\text{ArcCos}[a + b x] - i \left(\text{Log}[2] - 2 \text{Log} \left[i \sqrt{1-a} + \sqrt{1+a} \right] \right) \right) \text{Log} \left[1 + \left(-a + \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] + \\ & \left(\text{ArcCos}[a + b x] + i \left(\text{Log}[2] - 2 \text{Log} \left[i \sqrt{1-a} + \sqrt{1+a} \right] \right) \right) \text{Log} \left[1 - \left(a + \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] - \\ & i \text{PolyLog} \left[2, \left(a - \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] - i \text{PolyLog} \left[2, \left(a + \sqrt{-1 + a^2} \right) \left(a + b x + i \sqrt{1 - (a + b x)^2} \right) \right] \end{aligned}$$

$$-\text{Subst} \left[\text{Int} \left[\frac{x \sin[x]}{-a + \cos[x]}, x \right], x, \text{ArcCos}[a + b x] \right]$$

Unable to integrate:

$$\left\{ \frac{\text{ArcTan} \left[\frac{\sqrt{1-ax}}{\sqrt{1+ax}} \right]}{1 - a^2 x^2}, x, -5, 5 \right\}$$

$$-\frac{i \text{PolyLog} \left[2, -\frac{i \sqrt{1-ax}}{\sqrt{1+ax}} \right]}{2a} + \frac{i \text{PolyLog} \left[2, \frac{i \sqrt{1-ax}}{\sqrt{1+ax}} \right]}{2a}$$

$$\begin{aligned}
& - \frac{\text{Subst}\left[\text{Int}\left[\frac{\text{ArcTan}\left[\frac{x}{\sqrt{2-x^2}}\right]}{x}, x\right], x, \sqrt{1-ax}\right]}{a} \\
& \frac{\text{Subst}\left[\text{Int}\left[\frac{\text{ArcTan}\left[\frac{x}{\sqrt{2-x^2}}\right]}{2\sqrt{2}x}, x\right], x, \sqrt{1-ax}\right]}{\sqrt{2}a} + \frac{\text{Subst}\left[\text{Int}\left[\frac{\text{ArcTan}\left[\frac{x}{\sqrt{2-x^2}}\right]}{2+\sqrt{2}x}, x\right], x, \sqrt{1-ax}\right]}{\sqrt{2}a}
\end{aligned}$$

Valid but unnecessarily complicated antiderivative:

$$\begin{aligned}
& \{\text{ArcCot}[a + b f^{c+dx}], x, -15, 15\} \\
& x \text{ArcCot}[a + b f^{c+dx}] - \frac{1}{2} i x \text{Log}\left[1 - \frac{b f^{c+dx}}{i-a}\right] + \frac{1}{2} i x \text{Log}\left[1 + \frac{b f^{c+dx}}{i+a}\right] - \frac{i \text{PolyLog}\left[2, \frac{b f^{c+dx}}{i-a}\right]}{2 d \text{Log}[f]} + \frac{i \text{PolyLog}\left[2, -\frac{b f^{c+dx}}{i+a}\right]}{2 d \text{Log}[f]} \\
& - \frac{i \text{Log}[f^{c+dx}] \text{Log}\left[\frac{i-a-b f^{c+dx}}{i-a}\right]}{2 d \text{Log}[f]} + \frac{i \text{Log}[f^{c+dx}] \text{Log}\left[\frac{i+a+b f^{c+dx}}{i+a}\right]}{2 d \text{Log}[f]} + \frac{i \text{Log}[f^{c+dx}] \text{Log}\left[1 - \frac{i}{a+b f^{c+dx}}\right]}{2 d \text{Log}[f]} - \\
& \frac{i \text{Log}[f^{c+dx}] \text{Log}\left[1 + \frac{i}{a+b f^{c+dx}}\right]}{2 d \text{Log}[f]} - \frac{i \text{PolyLog}\left[2, \frac{b f^{c+dx}}{i-a}\right]}{2 d \text{Log}[f]} + \frac{i \text{PolyLog}\left[2, -\frac{b f^{c+dx}}{i+a}\right]}{2 d \text{Log}[f]}
\end{aligned}$$