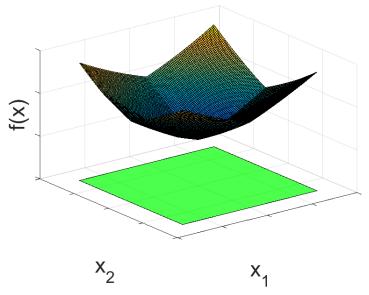
#### Animation: Proximal bundle method

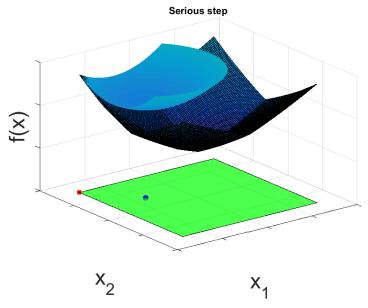
Welington de Oliveira MINES ParisTech, PSL-Research University CMA - Centre de Mathématiques Appliquées

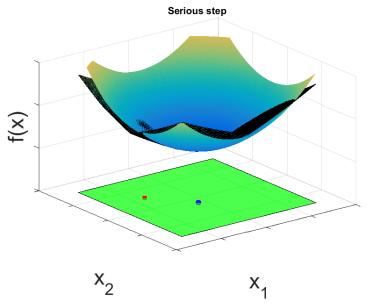
6 de outubro de 2018

#### PROXIMAL BUNDLE METHOD: PBM

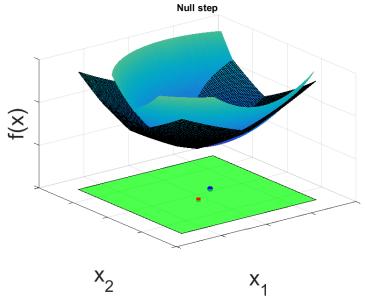
- ▶ The problem:  $\min_{x \in X} f(x)$
- ightharpoonup Both function f and feasible set X are convex
- ▶ Oracle: given  $x^k$ , an oracle provides us with  $f(x^k)$  and  $g^k \in \partial f(x^k)$
- $\blacktriangleright$  Cutting-plane model  $\check{f}^k(x) := \max_{j \in J_k} \{f(x^j) + \langle g^j, x x^j \rangle \}$
- ▶ Trial point:  $x^{k+1} := \arg\min_{x \in X} \check{f}^k(x) + \frac{1}{2t} \|x \hat{x}^k\|^2$
- ▶ Serious step: if  $f(x^{k+1}) \le f(\hat{x}^k) \kappa(f(\hat{x}^k) \check{f}^k(x^{k+1}))$  then  $\hat{x}^{k+1} \leftarrow x^{k+1}$
- ▶ Null step: if  $f(x^{k+1}) > f(\hat{x}^k) \kappa(f(\hat{x}^k) \check{f}^k(x^{k+1}))$  then  $\hat{x}^{k+1} \leftarrow \hat{x}^k$

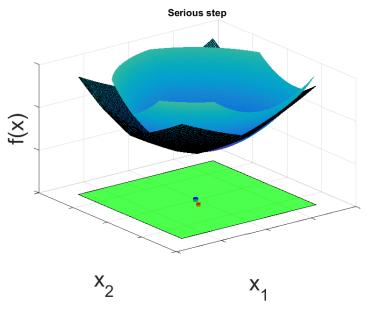


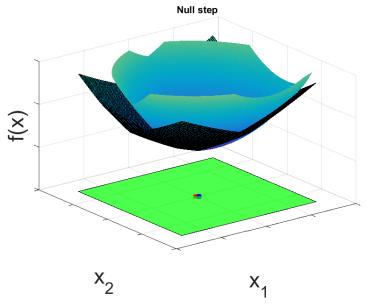


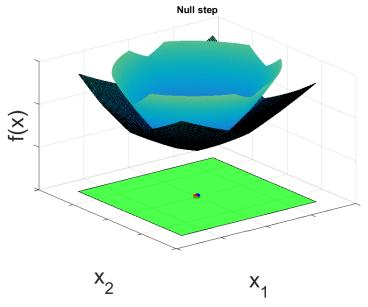


# $\operatorname{PBM}$

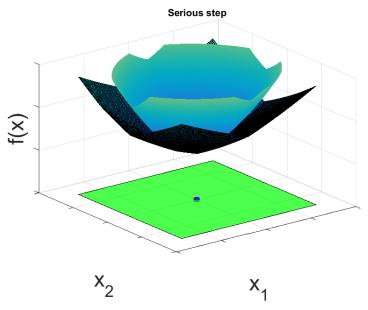


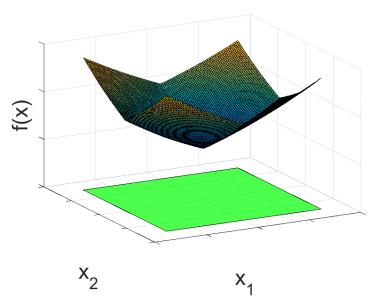


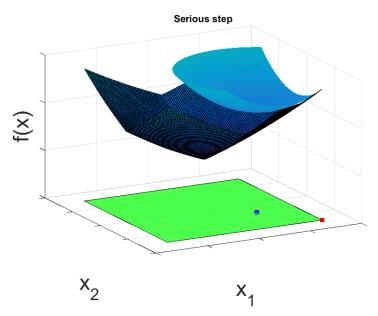


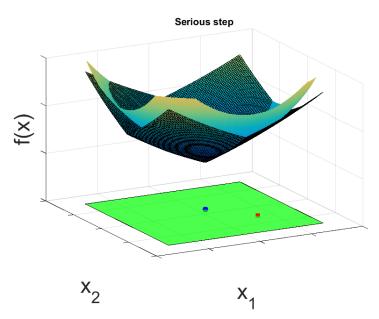


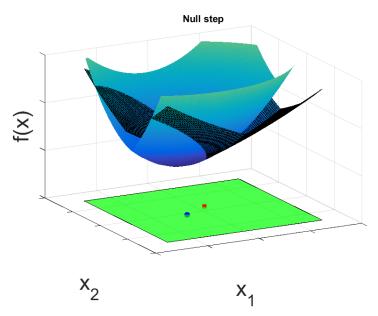
### PBM: OPTIMAL SOLUTION

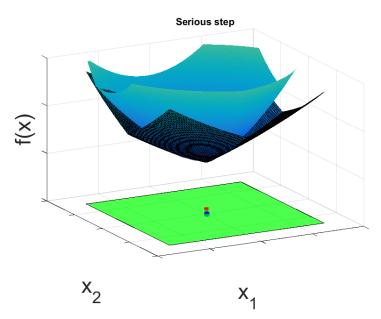


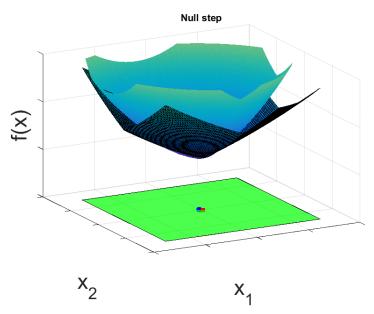


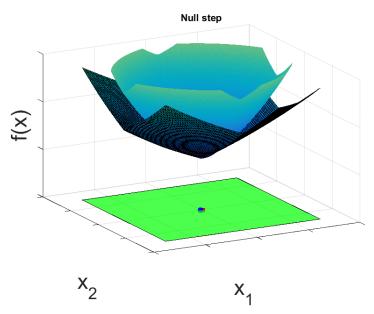












#### ANOTHER PERSPECTIVE: OPTIMAL SOLUTION

