

Problem 1. Section 3.5 #176

For the following exercises, find $\frac{dy}{dx}$ for the given functions.

Here $y = 3 \csc(x) + \frac{5}{x}$.

We have $\boxed{\frac{dy}{dx} = -3 \csc(x) \cot(x) - \frac{5}{x^2}}.$

Problem 2. Section 3.5 #180

For the following exercises, find $\frac{dy}{dx}$ for the given functions.

Here $y = \sin(x) \tan(x)$.

We have $\boxed{\frac{dy}{dx} = \cos(x) \tan(x) + \sin(x) \sec^2(x) = \sin(x)(1 + \sec^2(x))}.$

Problem 3. Section 3.5 #182

For the following exercises, find $\frac{dy}{dx}$ for the given functions.

Here $y = \frac{\tan(x)}{1 - \sec(x)} = \frac{\sin(x)}{\cos(x) - 1}$.

We have $\boxed{\frac{dy}{dx} = \frac{\cos(x)(\cos(x)-1) + \sin^2(x)}{(1-\cos(x))^2} = \frac{1}{1-\cos(x)}}.$

Problem 4. Section 3.5 #196

For the following exercises, find $\frac{d^2y}{dx^2}$ for the given functions.

Here $y = \sec^2(x)$. Therefore, $\boxed{\frac{dy}{dx} = 2 \sec^2(x) \tan(x)}.$

Further we have $\boxed{\frac{d^2y}{dx^2} = 2(2 \sec^2(x) \tan^2(x) + \sec^4(x)) = 2 \sec^2(x)(2 \tan^2(x) + \sec^2(x))}.$

Problem 5. Section 3.5 #198

Find all x values on the graph of $f(x) = x - 2 \cos(x)$ for $0 < x < 2\pi$ where the tangent line has slope 2.

Given that $f(x) = x - 2 \cos(x)$, we immediately have $\boxed{f'(x) = 1 + 2 \sin(x)}.$

Solve the equation $f'(x) = 2$ for x , where $0 < x < 2\pi$. We get $\boxed{x = \frac{\pi}{6} \text{ or } x = \frac{5\pi}{6}}.$

Problem 6. Section 3.5 #204

The amount of rainfall per month in Phoenix, Arizona, can be approximated by $y(t) = 0.5 + 0.3 \cos(t)$, where t is months since January. Find y' and determine the intervals where the amount of rain falling is decreasing.

As $y(t) = 0.5 + 0.3 \cos(t)$, we get $y' = -0.3 \sin(t)$. We need to find when $y' < 0$. That is to say, we need to find when $\sin(t) > 0$ as t varies from 1 to 12.

After some calculating, we obtain the intervals, which are $[1, 3]$ and $[7, 9]$, that is, from January to March and from July to September.

Problem 7. Section 3.5 #206

For the following exercises, use the quotient rule to derive the given equations.

We need to show that $\frac{d}{dx}(\sec(x)) = \sec(x) \tan(x)$.

Rewrite $\sec(x) = \frac{1}{\cos(x)}$. Then we have $\frac{d}{dx}(\sec(x)) = \frac{d}{dx} \frac{1}{\cos(x)}$.

Using the quotient rule, we get $\frac{d}{dx} \frac{1}{\cos(x)} = \frac{\sin(x)}{\cos^2(x)} = \sec(x) \tan(x)$.

Problem 8. Section 3.5 #210

For the following exercises, find the requested higher-order derivative for the given functions.

Here we have $y = 3 \sin(x) + x^2 \cos(x)$.

Therefore, we get $\frac{dy}{dx} = 3 \cos(x) + 2x \cos(x) - x^2 \sin(x)$.

Further we obtain $\frac{d^2y}{dx^2} = -3 \sin(x) + 2 \cos(x) - 2x \sin(x) - 2x \sin(x) - x^2 \cos(x)$. That is to say, $\frac{d^2y}{dx^2} = -(4x + 3) \sin(x) - (x^2 - 2) \cos(x)$.