

**Problem 1. Section 1.1 #14**

Find the domain, range, and all zeroes/intercepts, if any, of the function  $f(x) = \frac{x}{x^2-16}$ .

- Domain: We need to ensure that the denominator is never zero; to find values that make the denominator zero, we solve the equation  $x^2 - 16 = 0$  to get that the values  $x = -4, 4$  are not in the domain. This means that our domain is  $\boxed{\{x \mid x \neq -4, 4\}}$ .
- Range: To find the range, we need to know all values of  $y$  such that  $\frac{x}{x^2-16} = y$  has a solution. We can simplify this to  $x = (x^2 - 16)y$ , and we see that this equation has a solution for all  $y$ , so our range is  $\boxed{\mathbb{R}}$ .
- Zeroes: Solving the equation  $\frac{x}{x^2-16} = 0$  gives us  $\boxed{x = 0}$  as the only zero.
- Intercepts: We plug in  $x = 0$  to get  $f(0) = \frac{0}{0^2-16} = 0$ , so  $\boxed{y = 0}$  is our only  $y$ -intercept.

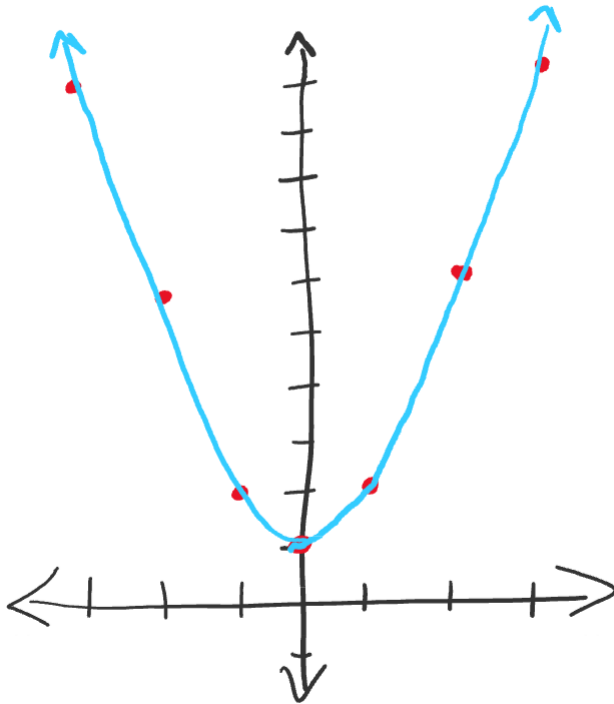
**Problem 2. Section 1.1 #18**

Find the domain, range, and all zeroes/intercepts, if any, of the function  $f(x) = \frac{1}{\sqrt{x-9}}$ .

- Domain: The square-root in the denominator is not defined when  $x < 9$ , and when  $x = 9$ , we have  $1/0$ , so our domain is  $\boxed{(9, \infty)}$ .
- Range: We want to know all values of  $y$  such that  $\frac{1}{\sqrt{x-9}} = y$  has a solution. We can simplify to get  $1 = y\sqrt{x-9}$ , which has a solution as long as  $y \neq 0$ . Therefore, our range is  $\boxed{\{y \mid y \neq 0\}}$ .
- Zeroes: Solving the equation  $\frac{1}{\sqrt{x-9}} = 0$  gives us  $1 = 0$ , which has no solutions, so the function has  $\boxed{\text{no zeroes}}$ .
- Intercepts: We plug in  $x = 0$  to get  $f(0) = \frac{1}{\sqrt{-9}}$ , which is not defined, so the function has  $\boxed{\text{no } y\text{-intercepts}}$  either.

**Problem 3. Section 1.1 #22**

Sketch the graph of the function  $f(x) = x^2 + 1$ .



#### Problem 4. Section 1.1 #28

Determine whether the graph represents a function. If it does, find ...

The graph does not represent a function.

#### Problem 5. Section 1.1 #30

Determine whether the graph represents a function. If it does, find ...

- a. The domain is  $\mathbb{R}$ , and the range is  $(-\infty, 3)$ .
- b. The  $x$ -intercepts are around 0.25 and 3.75.
- c. The  $y$ -intercept is at -1.
- d. The function is increasing on  $(-\infty, 2]$ .
- e. The function is decreasing on  $[2, \infty)$ .
- f. The function is constant on  $[2, 2]$ .
- g. The function does not have any special symmetry.
- h. The function is neither even nor odd.

**Problem 6. Section 1.1 #32**

Determine whether the graph represents a function. If it does, find ...

The graph does not represent a function.

**Problem 7. Section 1.1 #52**

A rental car company rents cars for a flat fee of \$20 and an hourly charge of \$10.25. Therefore, the total cost  $C$  to rent a car is a function of the hours  $t$  the car is rented plus the flat fee.

- a. Write the formula for the function that models this situation

$$\boxed{C(t) = 20 + 10.25t}$$

- b. Find the total cost to rent a car for 2 days and 7 hours.

2 days and 7 hours is  $2 \cdot 24 + 7 = 55$  hours, and  $C(55) = 20 + 10.25(55) = 583.75$ , so the total cost is \$583.75.

- c. Determine how long the car was rented if the bill is \$432.73.

We need to solve the equation  $C(t) = 432.73$ :

$$20 + 10.25t = 432.73$$

$$10.25t = 412.73$$

$$t = \frac{412.73}{10.25} \approx 40.27$$

So the car was rented for about 40.27 hours.