

# Toward Intrinsic Room-Temperature Ferromagnetism in Two-Dimensional Semiconductors

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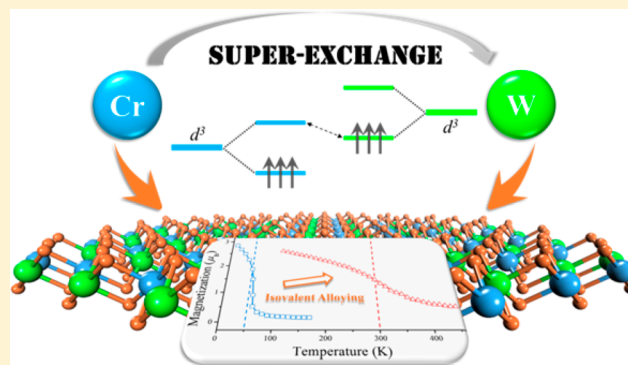
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## Supporting Information

**ABSTRACT:** Two-dimensional (2D) ferromagnetic semiconductors have been recognized as the cornerstone for next-generation electric devices, but the development is highly limited by the weak ferromagnetic coupling and low Curie temperature ( $T_C$ ). Here, we reported a general mechanism which can significantly enhance the ferromagnetic coupling in 2D semiconductors without introducing carriers. On the basis of a double-orbital model, we revealed that the superexchange-driven ferromagnetism is closely related to the virtual exchange gap, and lowering this gap by isovalent alloying can significantly enhance the ferromagnetic (FM) coupling. On the basis of the experimentally available two-dimensional  $\text{CrI}_3$  and  $\text{CrGeTe}_3$ , the FM coupling in two semiconducting alloy compounds  $\text{CrWI}_6$  and  $\text{CrWGe}_2\text{Te}_6$  monolayers are calculated to be enhanced by 3~5 times without introducing any carriers. Furthermore, a room-temperature ferromagnetic semiconductor is achieved under a small in-plane strain (4%). Thus, our findings not only deepen the understanding of FM semiconductors but also open a new door for realistic spintronics.



## 1. INTRODUCTION

The discovery of spintronic behaviors (e.g., giant magnetoresistance effect) gives new dimensions to manipulate the spin and charge of materials, leading to novel functional spintronic devices.<sup>1</sup> One of the most promising candidates of spintronic materials is ferromagnetic (FM) semiconductor. Different from the usual antiferromagnetic (AFM) insulators, FM semiconductors simultaneously possess spontaneous net magnetization and the moderate electrical resistivity at finite temperature, leading to potential spintronic applications such as data storage, sensing, capacitor, and logical devices.<sup>2,3</sup> For practical interests, a feasible FM semiconductor with strong ferromagnetism that can survive at room temperature (300 K) is highly desirable.<sup>4</sup> However, FM semiconductors are rare in nature and their Curie temperatures ( $T_C$ ) are usually much lower than room temperature, such as the recent experimentally realized two-dimensional (2D) FM semiconductors whose  $T_C$  are below 45 K.<sup>5–7</sup> Actually, experimental observation of room-temperature intrinsic FM semiconductors has never been reported despite decades of tremendous efforts

since the first FM semiconductor ( $\text{CrBr}_3$ )<sup>8</sup> was discovered more than half a century ago.

It is known that FM metals may have very high  $T_C$  (e.g., ~420 K for  $\text{Sr}_2\text{FeMoO}_6$  double perovskite<sup>9</sup> and ~780 K for 2D  $\text{Fe}_2\text{Si}$ <sup>10</sup>) because of the strong double-exchange interaction driven by charge carriers.<sup>11</sup> Similarly, in the diluted magnetic semiconductors (DMSs), the carrier-mediated exchange could lead to a relatively strong FM coupling. However, the reproducible  $T_C$  is still limited below ~200 K (e.g., 155 K for  $\text{GaMnAs}$ ).<sup>12–14</sup> Carrier injection may further enhance the ferromagnetism,<sup>15</sup> but doping a high concentration of carriers may destroy the semiconducting properties. On the other hand, FM coupling driven by superexchange in a conventional intrinsic FM semiconductor is carrier-free, but is usually rather weak, resulting in a  $T_C$  below ~100 K.<sup>16–19</sup> Although, in principle, the superexchange mechanism does not prohibit the occurrence of strong semiconducting ferromagnetism, it is still a critical and open question as to whether the  $T_C$  of an intrinsic

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FM semiconductor can be improved up to room temperature without introducing carriers?

Here, we demonstrate that superexchange indeed can lead to carrier-free room-temperature semiconducting ferromagnetism. Using a double-orbital model, we reveal a general mechanism that FM coupling in a semiconductor can be significantly enhanced by reducing the virtual exchange gap ( $G_{\text{ex}}$ ) between the occupied and empty spin-polarized orbitals of adjacent magnetic ions. The explored mechanism is then applied to two experimentally reported systems, namely,  $\text{CrI}_3$  and  $\text{CrGeTe}_3$  thin layers, which are intrinsic FM semiconductors with low  $T_{\text{C}}$ .<sup>5,6</sup> By isovalent alloying of Cr with W to construct alloy compounds  $\text{CrWI}_6$  and  $\text{CrWGe}_2\text{Te}_6$  monolayers, the  $G_{\text{ex}}$  between occupied  $\text{W-}t_{2g}\uparrow$  and empty  $\text{Cr-}e_g\uparrow$  orbitals is much reduced. First-principles calculations and classical Monte Carlo (MC) simulations demonstrated that both  $\text{CrWI}_6$  and  $\text{CrWGe}_2\text{Te}_6$  monolayers are robust intrinsic FM semiconductors with  $T_{\text{C}}$  of  $\sim 180$  K, which is indeed much higher than that of the pristine  $\text{CrI}_3$  (45 K) and  $\text{CrGeTe}_3$  thin layers (30 K). And the  $T_{\text{C}}$  of  $\text{CrWGe}_2\text{Te}_6$  monolayer can be enhanced up to room temperature (300 K) under a small tensile strain (4%) without introducing any carriers. Besides, the applicability of the proposed mechanism is also confirmed in another typical magnetic system, that is, the  $\text{HgCr}_2\text{S}_4$  spinel and  $\text{MnS}_2$  monolayer.

## 2. METHODS

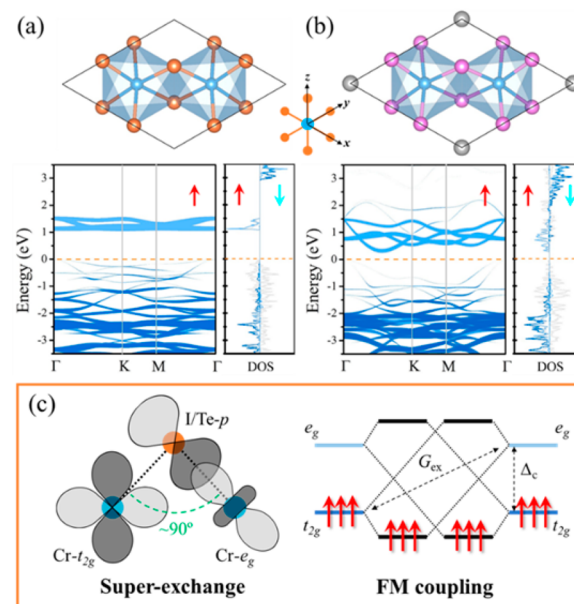
Our first-principles calculations were based on density functional theory (DFT) implemented in the Vienna Ab Initio Simulation Package (VASP).<sup>20</sup> Generalized gradient approximation (GGA) for exchange-correlation functional given by Perdew, Burke, and Ernzerhof (PBE)<sup>21</sup> was used. The effective Hubbard  $U_{\text{eff}} = 3$  and 1 eV were added according to Dudarev's<sup>22</sup> method for the Cr-d and W-d orbitals, respectively. Because the  $U_{\text{eff}}$  values of Cr in different systems are usually taken within the range of 2–4 eV and the  $U_{\text{eff}}$  difference of 2 eV between 3d and 5d elements ( $U_{\text{eff},3d} - U_{\text{eff},5d} = 2$  eV) is reasonable.<sup>23–25</sup> A test for different  $U_{\text{eff}}$  values is also performed (Table S2 in the Supporting Information). The projector augmented wave (PAW)<sup>26</sup> method was used to treat the core electrons. We also have performed calculations using HSE06 hybridized functional<sup>27</sup> on the magnetic properties. The results are very similar to those from DFT+ $U$  calculations (Table S4 in the Supporting Information). The plane wave cutoff energy was set to be 500 eV and the first Brillouin zone was sampled by using a  $\Gamma$ -centered  $12 \times 12 \times 1$  Monkhorst–Pack<sup>28</sup> grid. A vacuum space of 20 Å along the  $z$  direction was adopted to model the 2D system. The spin-orbit coupling (SOC) was included in the electronic self-consistent calculations. The phonon calculations were performed by using the PHONOPY code.<sup>29</sup> The first-principles-based cluster expansion (CE) calculations and Monte Carlo (MC) simulations for the ordered-disordered phase transition of alloy systems are performed by using the Alloy-Theoretic Automated Toolkit (ATAT) package.<sup>31</sup> To confirm the stability of the  $\text{CrWI}_6$  and  $\text{CrWGe}_2\text{Te}_6$ , we adopt our global optimization approach<sup>32</sup> for searching quasi-2D structures as implemented in the Crystal structure Analysis by Particle Swarm Optimization (CALYPSO) code.<sup>33,34</sup> In these calculations, the only given prior structure information is the chemical composition.

The spin dynamical process is studied by the classical Metropolis MC simulations.<sup>35</sup> For  $\text{CrI}_3$ ,  $\text{CrWI}_6$ , and  $\text{CrWGe}_2\text{Te}_6$  monolayer, a  $30 \times 30$  2D honeycomb spin-lattice containing 1800 spin sites with the periodic boundary condition is used. During the simulation steps, each spin is rotated randomly in all directions. The average magnetization per site is taken after the system reaches the equilibrium (with at least  $10^5$  simulation steps) state at a given temperature. The Curie temperature ( $T_{\text{C}}$ ) is taken as the critical point of the specific heat, defined as  $C_V = (\langle E^2 \rangle - \langle E \rangle^2)/k_{\text{B}}T^2$ . The estimated  $T_{\text{C}}$  of  $\text{CrI}_3$  monolayer ( $\sim 50$  K) is very close to the

experimental result ( $\sim 45$  K), suggesting the rationality of this method.

## 3. RESULTS AND DISCUSSION

**3.1. Weak Ferromagnetism in  $\text{CrI}_3$  and  $\text{CrGeTe}_3$ .** To explore how to enhance the ferromagnetism, first of all, it is necessary to understand why the ferromagnetism is usually so weak in an intrinsic FM semiconductor. The recent experimentally reported 2D intrinsic FM semiconductors, namely, the  $\text{CrI}_3$ <sup>6</sup> and  $\text{CrGeTe}_3$ ,<sup>5</sup> are two typical examples. In both systems, each Cr is coordinated by six ligands (I or Te) (Figure 1a,b). Because of the octahedral crystal field, the Cr-d



**Figure 1.** Atomic structure (top view), projected band structure, and density of states (DOS) for  $\text{Cr-}t_{2g}$  (dark blue),  $\text{Cr-}e_g$  (light blue), I-p (gray), and Te-p (gray) orbitals of (a)  $\text{CrI}_3$  and (b)  $\text{CrGeTe}_3$  monolayer. Blue, orange, pink, and gray balls represent Cr, I, Te, and Ge atoms, respectively. Red and cyan arrows represent spin-up and spin-down channels. (c) Schematic diagrams of the superexchange interaction and FM coupling in  $\text{CrI}_3$  and  $\text{CrGeTe}_3$  monolayer.  $G_{\text{ex}}$  is the virtual exchange gap.  $\Delta_c$  represents the energy gap opened by the crystal field. Red arrows represent the spin-up electrons.

orbitals split into two parts, that is, the threefold  $t_{2g}$  and twofold  $e_g$  manifolds. The lower  $t_{2g}$  orbitals are half occupied while the higher  $e_g$  orbitals are empty, which makes these systems magnetic semiconducting (Figure 1a,b). Furthermore, in both systems, the Cr–I/Te–Cr bonding angle is close to 90°, which explains the occurrence of FM coupling according to the well-known Goodenough–Kanamori–Anderson (GKA)<sup>36–38</sup> rules of the superexchange theorem (Figure 1c). However, the overall FM coupling driven by superexchange is rather weak because of the competitive AFM interactions (i.e., the Cr–Cr direct exchange). But it is still unclear as to what is the higher limit of the strength of FM coupling in such systems. Can it be strong enough to survive at room temperature? If looking a little deeper into the electronic structures of  $\text{CrI}_3$  and  $\text{CrGeTe}_3$  monolayer, one may find a similarity between them, that is, the large energy gap between occupied  $t_{2g}\uparrow$  and empty  $e_g\uparrow$  orbitals. A reasonable doubt comes out that since the FM coupling originates from the

virtual exchange between a half occupied and an empty orbital (the  $t_{2g}\uparrow$ - $p$ - $e_g\uparrow$  exchange in this case; see Figure 1c) in a superexchange system, if we can reduce the energy gap between them (i.e., the  $G_{ex}$ ), will the FM coupling be enhanced?

### 3.2. Enhancing FM Coupling via Orbital Engineering.

To explore how  $G_{ex}$  affects the magnetic coupling, here we introduce a double-orbital model from the perspective of the tight-binding theorem in which the lower orbital is half occupied and the higher one is empty. This is the simplest FM semiconducting system. On the basis of the mean field approximation, the general Hamiltonian is given as<sup>39,40</sup>

$$\hat{H} = \hat{H}_t + \hat{H}_M$$

where the first term  $H_t$  represents hopping between nearest neighboring sites and the second term  $H_M$  corresponds to the mean-field exchange field. To be more specific,

$$\hat{H}_t = \sum_{\mu\nu} \sum_{\sigma=\uparrow,\downarrow} (t_{i\mu j\nu, \sigma} c_{i\mu, \sigma}^\dagger c_{j\nu, \sigma} + h.c.)$$

$$\hat{H}_M = \sum_{l=i,j} \sum_{\sigma=\uparrow,\downarrow} \sum_{\mu=\alpha,\beta} \epsilon_{l\mu} c_{l\mu, \sigma}^\dagger c_{l\mu, \sigma} - \sum_{l=i,j} \sum_{\mu=\alpha,\beta} \frac{1}{2} u_l m_l \cdot S_{l\mu}$$

where  $i$  and  $j$  represent the two neighboring magnetic sites,  $\mu$  and  $\nu$  are the orbital indexes ( $\mu, \nu = \alpha, \beta$ ),  $\epsilon$  represents the on-site energy of each orbital,  $u_l$  represents the strength of exchange splitting,  $S$  is the spin operator, and  $m$  is the unit vector of the spin direction. The strength of crystal field is defined as  $\Delta_{cl} = |\epsilon_{l\alpha} - \epsilon_{l\beta}|$ . Generally speaking, in an intrinsic magnetic semiconducting system (e.g., transition-metal compound),  $\Delta_{cl}$  for each cation is similar and  $t_{i\mu j\nu} \ll u_l$  due to strong electronic correlation. For simplification, we assume that  $\Delta_{ci} = \Delta_{cj} = \Delta_c$  and  $t_{i\mu j\nu} = t$ . In the usual case,  $u_i = u_j = u$  and  $\epsilon_{i\mu} = \epsilon_{j\mu}$ , that is,  $G_{ex} = \Delta_c$ . When the second-order perturbation method is applied, the relative energies of FM ( $E_{FM}$ ) and AFM ( $E_{AFM}$ ) alignments are (see the Supporting Information for details)

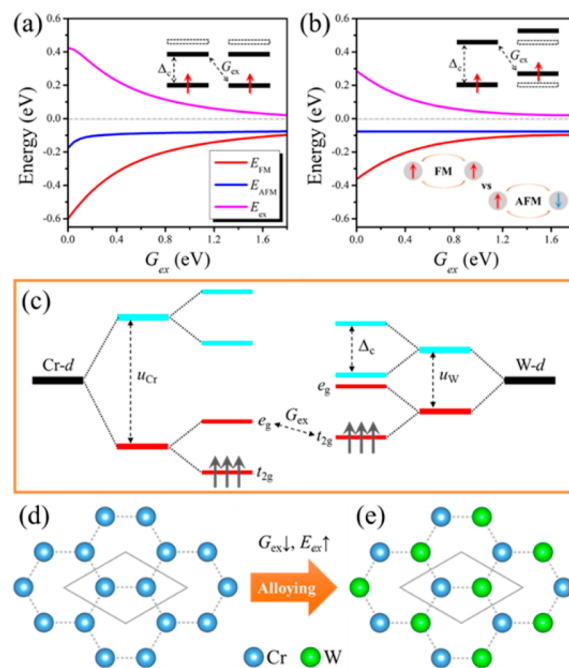
$$E_{FM} = -\frac{2t^2}{G_{ex}}$$

$$E_{AFM} = -2t^2 \left( \frac{1}{G_{ex} + u} + \frac{1}{u} \right)$$

From these equations, one finds that both  $E_{FM}$  and  $E_{AFM}$  decreases with the decreasing of  $G_{ex}$ . But as  $G_{ex}$  decreases,  $E_{FM}$  falls much more rapidly than  $E_{AFM}$  does when  $G_{ex}$  is approaching to near zero, leading to an increment of the total exchange energy ( $E_{ex} = E_{AFM} - E_{FM}$ ) (Figure 2a).

Staggering the energy level between  $i$  and  $j$  sites is another possibility to reduce the  $G_{ex}$ . In this case, the  $\alpha_i - \beta_j$  and  $\alpha_j - \beta_i$  exchange are not equivalent. Such an energy level stagger can be realized by either introducing an exchange-split difference ( $\Delta_u = u_i - u_j$ ) or average on-site energy difference ( $\Delta_o = \epsilon_{i\alpha} - \epsilon_{j\alpha}$ ) between neighboring magnetic sites. We first consider the former case (i.e.,  $\Delta_u \neq 0$ , while  $\Delta_o = 0$ ). Here, we assume that  $\Delta_u > 0$ . It is easy to get  $G_{ex} = \Delta_c - \Delta_u/2$ . The relative energies are

$$E_{FM} = -t^2 \left( \frac{1}{G_{ex}} - \frac{1}{G_{ex} - 2\Delta_c} \right)$$



**Figure 2.** Relative energies of ferromagnetic ( $E_{FM}$ ), antiferromagnetic ( $E_{AFM}$ ) alignments and exchange energy ( $E_{ex} = E_{AFM} - E_{FM}$ ) as a function of  $G_{ex}$  under the circumstance of (a) averagely lowering the higher empty orbitals and (b) staggering the energy levels between neighboring magnetic sites. (c) Schematic diagrams of orbital evolution and the origin of energy level staggering in Cr, W alloy systems. Red and cyan bars represent spin-up and spin-down orbitals, respectively.  $u_{Cr}$  and  $u_W$  are exchange splits for Cr- and W-d orbitals, respectively.  $\Delta_c$  is the energy gap opened by the crystal field. (d) The pure phase and (e) one of the typical alloy phases for  $CrI_3$ - or  $CrGeTe_3$ -based systems.

$$E_{AFM} = -2t^2 \left( \frac{1}{\Delta_c + u_0} + \frac{1}{u_0} \right)$$

where  $u_0 = (u_i + u_j)/2$ . One finds that  $E_{FM}$  increases along with  $G_{ex}$ , while  $E_{AFM}$  is independent of  $G_{ex}$  (Figure 2b). Thus, as  $G_{ex}$  decreases,  $E_{ex}$  also increases. For the case where the average on-site energies are different ( $\Delta_o \neq 0$ ), the results are very similar (see the Supporting Information).

From the above analysis based on double-orbital model, we can deduce that the large  $G_{ex}$  of  $CrI_3$  and  $CrGeTe_3$  is probably responsible for their weak FM coupling. Once we can properly reduce the  $G_{ex}$  in these systems, their semiconducting ferromagnetism is expected to be greatly enhanced. Next, we will demonstrate this idea by first-principles calculations.

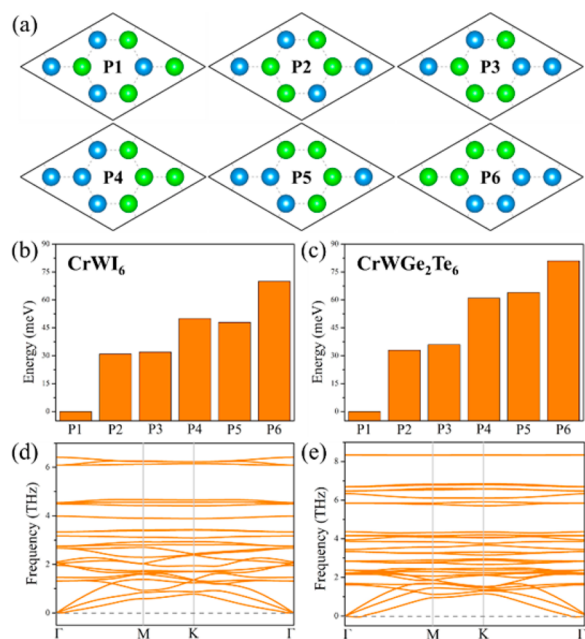
A practical way to reduce the  $G_{ex}$  and enhance semiconducting ferromagnetism is constructing alloyed transition-metal compounds. Because the exchange split and on-site energy of d orbitals for different transition metals under an octahedral field could be different. For instance, the tungsten (W) usually exhibits much smaller exchange split than Cr in an octahedral crystal field. This results in a distinct staggering between Cr-d and W-d orbitals, which may lead to reduction of  $G_{ex}$  between empty Cr- $e_g\uparrow$  and occupied W- $t_{2g}\uparrow$  orbitals (Figure 2c). The other reason that we choose W to alloying  $CrI_3$  and  $CrGeTe_3$  is that W can exhibit the same valence state (+3) and occupation state ( $d^3$ ) as Cr in these systems. Note that although the W metal bulk is nonmagnetic, W has been widely used to synthesize alloys with strong magnetism, such as



the martensite.<sup>41</sup> To demonstrate our idea, here we focus on the case where the concentration of W is 50% (Figure 2d,e). The alloy compounds are denoted as CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub>.

### 3.3. Stability and Feasibility of CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub>

There could be plenty of possible alloyed configurations for CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> depending on the distribution pattern of Cr and W at the metal sites. To find out the optimal alloyed configuration, we have considered six possible distribution patterns of Cr and W atoms in a 2 × 2 supercell containing four Cr and W sublattices (Figure 3a). We find that, for both



**Figure 3.** (a) Considered possible distribution patterns (P1–P6) of Cr and W atoms in a 2 × 2 supercell for CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> monolayer. Blue and green balls represent Cr and W atoms, respectively. The I, Ge, and Te atoms are omitted for simplicity. Relative energies per formula unit for each considered distribution pattern of (b) CrW<sub>1</sub>I<sub>6</sub> and (c) CrWGe<sub>2</sub>Te<sub>6</sub> monolayer. Phonon dispersion for P1 pattern, namely, the honeycomb checkboard (d) CrW<sub>1</sub>I<sub>6</sub> and (e) CrWGe<sub>2</sub>Te<sub>6</sub> monolayer.

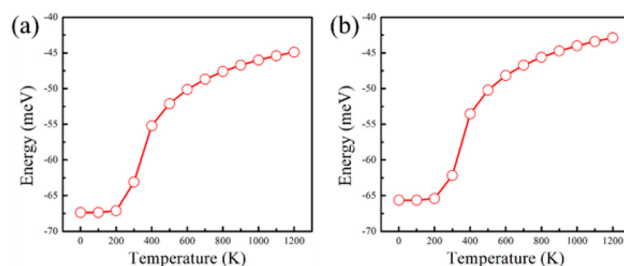
CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub>, the honeycomb-checkboard (HC) pattern (see P1 in Figure 3a) is lower by at least 30 meV/formula-unit in energy compared to that of the other patterns. Note that the relative energies (Figure 3b) of different alloyed configurations are based on electronic energies. The enthalpy, zero-point energy, and site entropy are not considered in these calculations.

We further performed first-principles-based CE calculations to determine the intermediate alloy ground states. The results show that the ordered HC pattern is indeed the ground state for both CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> (see the Supporting Information for details).

To examine the feasibility of HC CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> monolayer, first, we calculated their formation energies ( $E_f$ ). For CrW<sub>1</sub>I<sub>6</sub>,  $E_f = (E_{\text{CrW}_1\text{I}_6} - \mu_{\text{Cr}} - \mu_{\text{W}} - 6\mu_{\text{I}})/8$ , and for CrWGe<sub>2</sub>Te<sub>6</sub>,  $E_f = (E_{\text{CrWGe}_2\text{Te}_6} - \mu_{\text{Cr}} - \mu_{\text{W}} - 2\mu_{\text{Ge}} - 6\mu_{\text{Te}})/10$ , where the chemical potential  $\mu_{\text{Cr}}$ ,  $\mu_{\text{W}}$ ,  $\mu_{\text{I}}$ ,  $\mu_{\text{Ge}}$ , and  $\mu_{\text{Te}}$  are taken from bcc Cr, W metal crystal, solid iodine, Ge crystal, and hexagonal Te crystal, respectively. The calculated  $E_f$  for HC CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> monolayers are −0.474 and −0.216 eV, respectively, with negative values indicating

exothermic chemical reaction. These values are comparable to those of pristine CrI<sub>3</sub> (−0.903 eV) and CrGeTe<sub>3</sub> (−0.552 eV) monolayer. From the CE results (Figure S3 in the Supporting Information), we can also find that the relative energies of the alloy phases are lower by ~70 meV/metal compared to those of the pure phases, namely, CrI<sub>3</sub>, WI<sub>3</sub>, CrGeTe<sub>3</sub>, and WGeTe<sub>3</sub>. This indicates that the HC alloy phases can stably exist without any phase separation. To find out whether the HC configurations of CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> are the globally stable structure, we also performed a global structural optimization based on our PSO algorithm for two-dimensional layered materials as implemented in the CALYPSO code. The results show that, among all predicted quasi-2D structures, the HC CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> monolayers have the lowest energy.

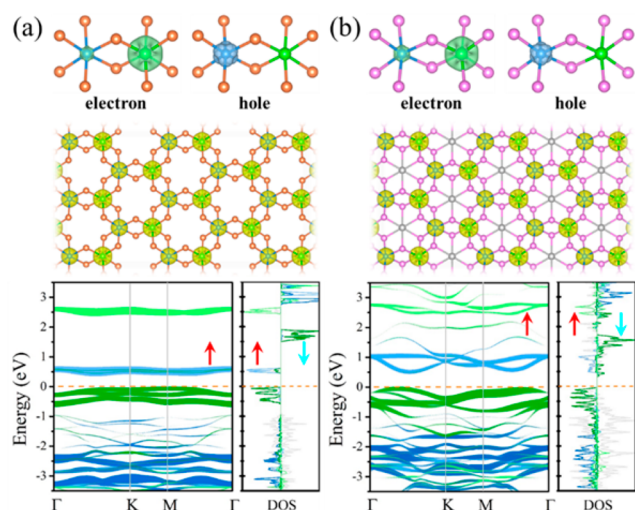
Next, we calculated their phonon dispersion (Figure 3d,e) and performed ab initio molecular dynamical simulations (Figure S6 in the Supporting Information), which partially demonstrate their dynamical and thermal stabilities. To further consider the entropy effect and explore whether the ordered HC alloy phases can survive at a finite temperature, we performed MC simulations to explore the ordered–disordered phase transitions of the alloy systems (see the Supporting Information for details), in which the CE Hamiltonian used in MC simulations is fitted from the extensive first-principles total energy calculations. As shown in Figure 4a,b, it is interesting to



**Figure 4.** Excess energy as a function of temperature from Monte Carlo simulation for ordered–disordered phase transition of (a) CrW<sub>1</sub>I<sub>6</sub> and (b) CrWGe<sub>2</sub>Te<sub>6</sub> monolayer.

find that the ordered–disordered phase transition temperature for these two alloy systems are ~400 K, which is sufficiently high for room-temperature applications.

**3.4. Electronic and Magnetic Properties of CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub>.** In both CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub>, W adopts the same oxidation (+3) and spin state ( $S = 3/2$ ) as Cr. Figure 5 (upper panel) shows the electron (−1 to 0 eV) and hole (0 to 1 eV) density around the Fermi level (set to 0 eV). One sees a distinct in-plane electron–hole separation. From the shape of the isosurfaces, we could consider that the electrons are mainly from W- $t_{2g}$  orbitals while the holes are from Cr- $e_g$  orbitals, indicating an energy level stagger between Cr-d and W-d orbitals near the Fermi level (Figure S7 in the Supporting Information). This is verified by the projected electronic structures (Figure 5, bottom panel). By extracting the maximally localized Wannier functions (MLWFs) (see the Supporting Information for details), we find that the energy level stagger is mainly caused by the exchange-split difference between Cr ( $u_{\text{Cr}} = \sim 4.6$  eV) and W ( $u_{\text{W}} = \sim 1.8$  eV). As a result, the  $G_{\text{ex}}$  between occupied W- $t_{2g}\uparrow$  and empty Cr- $e_g\uparrow$  orbitals ( $\sim 0.11$  and  $\sim 0.15$  eV for CrW<sub>1</sub>I<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub>, respectively) in the alloy systems are much reduced compared

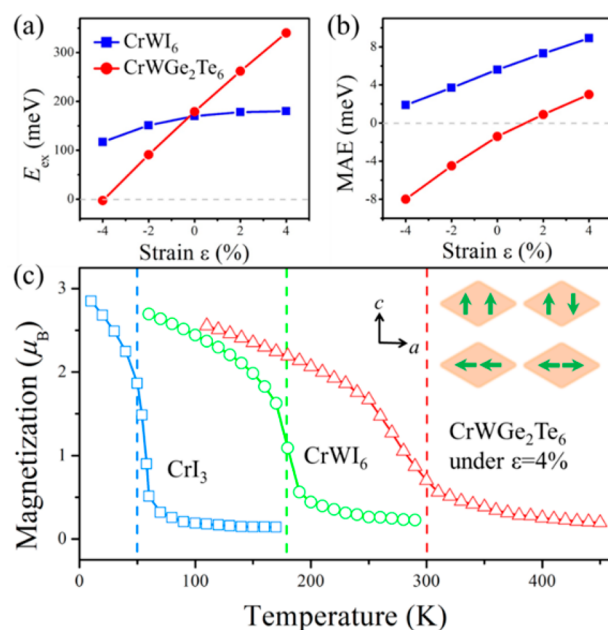


**Figure 5.** Spatial electron and hole density around the Fermi energy (upper panel), spin density (middle panel), projected band structures, and density of states (bottom panel) for (a) CrWI<sub>6</sub> and (b) CrWGe<sub>2</sub>Te<sub>6</sub> monolayer. Blue, orange, pink, and gray balls represent Cr, I, Te, and Ge atoms, respectively. Dark blue, light blue, dark green, light green, and gray represent contribution from Cr-*t*<sub>2g</sub>, Cr-*e*<sub>g</sub>, W-*t*<sub>2g</sub>, W-*e*<sub>g</sub>, and I/Te-*p* orbitals, respectively. Red and cyan arrows represent spin-up and spin-down channels.

to those between occupied Cr-*t*<sub>2g</sub>↑ and empty Cr-*e*<sub>g</sub>↑ orbitals (~2.0 and ~1.7 eV for CrI<sub>3</sub> and CrGeTe<sub>3</sub>, respectively) in the pure hosts (Table S1 in the Supporting Information). As expected, our calculations show that the ground states of CrWI<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> monolayer are FM with  $E_{\text{ex}}$  of 170 and 179 meV/unit cell, respectively, which are much larger than those of pristine CrI<sub>3</sub> (53 meV) and CrGeTe<sub>3</sub> (78 meV). Note that the enhancement of ferromagnetism in these systems is not mainly caused by the delocalization of W-d orbitals, which might strengthen the d-p-d hybridizations. In fact, our calculation shows that the hypothetical WI<sub>3</sub> monolayer is AFM instead of FM (see Table S1 and Figure S8 in the Supporting Information).

We also studied another key factor of the stability of long-range FM order in 2D systems, namely, the magnetocrystalline anisotropy.<sup>42</sup> Same as CrI<sub>3</sub>, CrWI<sub>6</sub> monolayer exhibits an out-of-plane easy axis of net magnetization. Because of the enhanced spin-orbit coupling (SOC) effect of the 5d W<sup>3+</sup> ion, the magnetocrystalline anisotropic energy (MAE =  $E_{\text{out-of-plane}} - E_{\text{in-plane}}$ ) is 5.4 meV/unit cell (with respect to the in-plane hard axis), much larger than that of CrI<sub>3</sub> (1.5 meV/unit cell). But the CrWGe<sub>2</sub>Te<sub>6</sub> monolayer exhibits an in-plane easy axis with MAE of -1.4 meV/unit cell, similar to 2D CrGeTe<sub>3</sub>.<sup>5</sup>

It was reported that external strain can alter the magnetocrystalline anisotropy as well as the magnetic coupling,<sup>43,44</sup> here we also studied the strain effect on the ferromagnetism of CrWI<sub>6</sub> and CrWGe<sub>2</sub>Te<sub>6</sub> monolayer. Figure 6a,b shows the  $E_{\text{ex}}$  and MAE as a function of the in-plane biaxial strain. We find that a tensile strain can only slightly increase the  $E_{\text{ex}}$  of CrWI<sub>6</sub>. Interestingly, for CrWGe<sub>2</sub>Te<sub>6</sub>,  $E_{\text{ex}}$  is very sensitive to the strain. With a small tensile strain of 4%, the  $E_{\text{ex}}$  is nearly doubled (from 179 to 340 meV). Its global electronic band gap (0.4 eV) barely changes compared to the equilibrium state (0.41 eV). We also calculated its  $\mu$ ,  $\Delta_c$ , and  $G_{\text{ex}}$  under different strains (Table S1 in the Supporting Information). The results



**Figure 6.** (a) Total exchange energy ( $E_{\text{ex}} = E_{\text{AFM}} - E_{\text{FM}}$ , positive values indicate ferromagnetic couplings) and (b) magnetic anisotropic energy ( $\text{MAE} = E_{\text{in-plane}} - E_{\text{out-of-plane}}$ , positive values indicate easy out-of-plane magnetization axis) per unit cell as a function of in-plane biaxial strain ( $\epsilon$ ). (c) Magnetic moment per site as a function of temperature for CrI<sub>3</sub>, CrWI<sub>6</sub> monolayer, and CrWGe<sub>2</sub>Te<sub>6</sub> monolayer under 4% tensile strain from Monte Carlo simulations. Inset: Four spin configurations considered in the DFT+SOC calculations.

show that these parameters are slightly changed, which implies that the drastic change of  $E_{\text{ex}}$  with strain is probably due to the weakening of direct *t*<sub>2g</sub>-*t*<sub>2g</sub> AFM exchange. On the other hand, a tensile strain also greatly increases the MAE. For CrWGe<sub>2</sub>Te<sub>6</sub>, a tensile strain of 4% will change the orientation of easy axis from in-plane to out-of-plane and result in a MAE of 3.0 meV, which allows the formation of long-range FM order.

Now, we explore the magnetic behavior under finite temperatures and estimate the  $T_C$ . From the spin density (Figure 5 middle panel), one sees that the spin-polarized charges are mainly localized at each metal site; thus here we use the Heisenberg model in addition to a magnetic anisotropic term to describe the magnetic behavior of these systems (the in-plane anisotropy is omitted). The spin Hamiltonian

$$\hat{H} = - \sum_{\langle ij \rangle} J \vec{S}_i \cdot \vec{S}_j - \sum_i D (S_{iz})^2$$

where the summation  $\langle ij \rangle$  runs over all nearest-neighboring Cr and W sites.  $J$  is the exchange interaction parameter,  $D$  is the single-site magnetic anisotropy parameter,  $S_{iz}$  represent components of  $\vec{S}$  along  $z$  (out-of-plane) orientations and  $|\vec{S}| = 3/2$  for both Cr and W. The calculated  $J$  and  $D$  from different spin configurations (Figure 6c) are listed in Table S3 in the Supporting Information. Then by classical Metropolis MC simulations (Figure 6c), the  $T_C$  of CrI<sub>3</sub>, CrWI<sub>6</sub>, and CrWGe<sub>2</sub>Te<sub>6</sub> monolayer under a tensile strain of 4% are estimated to be ~50 K (very close to the experimental value ~45 K<sup>6</sup>), ~180 K, and ~300 K, respectively.

**3.5. Generality.** Finally, we briefly discuss the generality of the proposed mechanism, that is, reducing the  $G_{\text{ex}}$  to enhance

the semiconducting ferromagnetism. In particular, we consider the case of energy level staggering achieved by alloying transition-metal compounds which was already adopted experimentally to tune the properties in systems such as double perovskites. Here is a guideline to realize a desired FM alloy compound semiconductor with improved  $T_C$ : (i) choose a well-established magnetic semiconductor with transition-metal A as basis material; (ii) choose the transition-metal element B which should have the same occupation state (e.g.,  $d^3$ ) as A when embedded in the material; (iii) the  $\Delta_u$  between A and B should be large enough to greatly reduce the  $G_{ex}$ . Thus, a 3d-4d or 3d-5d combination of A-B alloy compound is recommended. With this design principle, besides the two systems ( $CrI_3$  and  $CrGeTe_3$ ) presented here, we have found other systems (i.e., the  $HgCr_2S_4$  bulk<sup>45</sup> and  $MnS_2$  monolayer;<sup>46</sup> see the [Supporting Information](#) for details) whose ferromagnetism can also be enhanced by alloying engineering. Particularly, alloying Mn with Re in the  $MnS_2$  monolayer will lead to a  $T_C$  of  $\sim 340$  K, exceeding the room temperature. Overall, we suggest that the proposed mechanism in this work can be widely applied in many magnetic systems (both 2D and 3D systems) to achieve high-temperature FM semiconductors.

#### 4. CONCLUSION

In summary, based on a double-orbital model and first-principle calculations, we propose a new general idea to improve the  $T_C$  of a carrier-free FM semiconductor under the framework of superexchange theory. On the basis of recent experimentally realized FM thin layers, two feasible 2D alloy systems, namely, the  $CrWI_6$  and  $CrWGe_2Te_6$  monolayers, are used to prove our proposed mechanism. We show that reducing the  $G_{ex}$  will significantly enhance the FM coupling and improve the  $T_C$  up to room temperature. Thus, our results reveal new insights into the magnetic exchange and general mechanism of FM coupling in semiconductors, which gives great opportunity to realize room-temperature FM semiconductors. We expect future experimental realizations of room-temperature FM semiconductors in the alloy transition-metal compounds.

#### ■ ASSOCIATED CONTENT

##### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: [10.1021/jacs.8b07879](https://doi.org/10.1021/jacs.8b07879).

Double-orbital model analysis, detailed structural and electronic properties of  $CrWI_6$  and  $CrWGe_2Te_6$  monolayers, and magnetism in  $HgCr_{2-x}Mo_xS_4$  and  $Mn_xRe_{1-x}S_2$  bulk ([PDF](#))

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#### Notes

The authors declare no competing financial interest.

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