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Lead-free hybrid perovskite $N(CH_3)_4SnI_3$ with robust ferroelectricity induced by large and non-polar $N(CH_3)_4$ molecular cation

The ferroelectricity in the hybrid perovskite $CH_3NH_3Pbl_3$ is under debate because it results from the polar molecular cation $CH_3NH_3^+$ while the molecular orientation was reported to be random. Here we predict that a Pb-free hybrid perovskite $N(CH_3)_4Snl_3$ with non-polar molecular cation $N(CH_3)_4^+$ has strong ferroelectricity with a spontaneous polarization of 16.13 μ C cm⁻². The large polarization results from the distortion of Snl_6 octahedron induced by the large $N(CH_3)_4^+$ and is independent of the molecular orientation, so the ferroelectricity is robust. The ferroelectric R3m perovskite structure of $N(CH_3)_4Snl_3$ can be synthesized as the ground state under a hydrostatic pressure over 3 GPa and remains stable under ambient pressure. Given the strong ferroelectricity, good stability and high visible-light absorption, $N(CH_3)_4Snl_3$ may be an ideal light-absorber semiconductor for high-efficiency solar cells because its ferroelectric polarization can facilitate electron-hole separation and produce large bulk photovoltaic effect, making the design of homogeneous bulk photovoltaic devices possible.

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he organic-inorganic hybrid perovskites (OIHPs) drew intensive attention in the past decade as the light-absorber material in the all-solid-state solar cells and the power conversion efficiency (PCE) of the solar cells based on the hybrid perovskites such as CH3NH3PbI3 or NH2CHNH2PbI3 is now as high as 25.2%¹⁻⁵, which is getting closer to that of the monocrystalline silicon (band gap $E_g = 1.2 \text{ eV}$, PCE = 26%)⁶, and higher than that of the commercialized thin-film solar cells based on CdTe ($E_g = 1.5 \text{ eV}$) and CuIn_xGa_{1-x}Se₂ ($E_g = 1.0$ -1.7 eV, PCE = 20%)^{7,8}. The OIHPs have a chemical formula ABX₃, where A = organic molecule cation, B = inorganic cation (Pb₂⁺ or Sn_2^+), and X = halide anion (Cl⁻, I⁻, Br⁻, or their mixture). One unexpected advantage of the hybrid perovskites as the lightabsorber material in solar cells is that it may have ferroelectricity, and the ferroelectric polarization can enhance the electron-hole separation and therefore prevent their recombination9. Furthermore, the bulk Rashba effect in the ferroelectric material may also slow down the electron-hole recombination 10.

Although the ferroelectricity of CH3NH3PbI3 was studied both experimentally and theoretically, the evidence of its ferroelectricity is still under debate and not robust 11,12. For hybrid perovskites such as CH₃NH₃PbI₃ and [(CH₃)₃NCH₂I]PbI₃, the A site is occupied by polar organic molecular cations, which can produce spontaneous polarization if the orientation of the polar molecular cations is ordered along a certain direction. However, recent molecular dynamics simulations showed that the polar Asite molecular cations are rotating and their orientation is random at room temperature, so the ferroelectricity should be very weak, or appear in a certain area but disappear quickly. Strong ferroelectricity can exist only after a disorder-order transition occurs for the polar A-site molecule cation in the whole thin film, but it is very difficult to control the molecular orientation. Besides the polarization induced by A-site molecular cations, there are some debates on whether the ferroelectricity of OIHPs can result from the conventional structural distortion induced by B-site ion (displacive mechanism)¹³. This mechanism is independent of the polarity and orientation of A-site molecular cations, so the ferroelectricity can be robust and can be induced in OIHPs with non-polar molecular cation on A-site. Unfortunately, firstprinciples calculations showed that the polarization induced by the B-site ion displacement is very weak in CH3NH3PbI3, and OIHPs with non-polar molecular cation on A site have seldom been reported to have strong ferroelectricity so far¹⁴. Since there is no OIHPs with both robust ferroelectricity and suitable band gaps as the light-absorber materials in solar cells, it has not yet been achieved to enhance the electron-hole separation and increase PCE by introducing robust ferroelectric polarization in the hybrid perovskite solar cells.

In this work, we find unexpectedly that a Pb-free hybrid perovskite N(CH₃)₄SnI₃ with the non-polar molecular cation $N(CH_3)_4$ at A site and R3m structure can have robust and strong ferroelectricity with an intrinsic spontaneous polarization as large as $16.13 \,\mu\text{C cm}^{-2}$. The large polarization results from the displacement of Sn²⁺ cation from the center of SnI₆ octahedron, rather than the polar molecular cation, so it is robust and unrelated to the orientation of the non-polar molecular cation $N(CH_3)_4^+$. The band gap of $N(CH_3)_4SnI_3$ is 2.12 eV and can be tuned effectively from 2.12 to 1.0 eV by applying a 3 GPa hydrostatic pressure, and its optical absorption coefficients for visible light are high. So it can be a potential high-efficiency lightabsorber semiconductor in solar cells. The stability calculation showed that the R3m structure is the ground state of N(CH₃)₄SnI₃ under a 3 GPa hydrostatic pressure, and the phonon dispersion calculations showed that the R3m structure is dynamically stable and can remain stable even after the pressure is released. Therefore, the R3m N(CH₃)₄SnI₃ can be synthesized under high pressure and then used as the stable light-absorber material in solar cells under the ambient conditions. As far as we know, N(CH₃)₄SnI₃ is a hybrid perovskite with both strong ferroelectricity and suitable band gap for the visible light absorption, so it offers an ideal material candidate for fabricating stable and Pb-free hybrid perovskite solar cells with a high efficiency enhanced by ferroelectricity.

Results

Since the ferroelectricity is sensitive to the orientation of molecular cation in hybrid perovskites such as CH₃NH₃PbI₃ with a polar molecular cation at A site, its ferroelectricity may be weak and not stable. In this study, we intend to search for hybrid perovskites with stable and strong ferroelectric polarization, so we focus on the hybrid perovskites with non-polar molecular cations. In the well-studied ferroelectric ABO₃ perovskites, it had been demonstrated that a large A-site cation can induce large structural distortion and thus strong polarization. Therefore, our search is further focused on the large and non-polar A-site molecular cations, among which the N(CH₃)₄+ is obviously an ideal candidate, so we expect that N(CH₃)₄SnI₃ may be potential hybrid perovskite with strong ferroelectricity. In the following sections we will discuss the stability and ferroelectricity of N(CH₃)₄SnI₃.

Structural stability under zero and finite pressure. In order to predict the stable crystal structure of N(CH₃)₄SnI₃, seven different structures are considered in the present study, including five three-dimensional (3D) structures as shown in Fig. 1a, f, one two-dimensional (2D) structure in Fig. 1e and one one-dimensional (1D) structure in Fig. 1d.

Four 3D structures in Fig. 1a are derived by replacing the Asite cation of inorganic ABX3 perovskite by the non-polar N(CH₃)₄⁺ group and B-site cation by Sn²⁺. It is well known that the perovskite ABX3 compounds can have different lattice symmetries at different temperatures, e.g., the cubic structure with the $Pm\bar{3}m$ space group at high temperatures and the structures with the Pnma, R3c, and R3m space groups at lower temperatures, which can be considered as the distorted cubic structures with the tilting or rotating of the BX6 octahedrons and the displacement of the B cation. The four structures with $Pm\bar{3}m$, Pnma, R3c, and R3m space groups are all adopted as the initial N(CH₃)₄SnI₃ structures in the present study and denoted as 3Dcubic structures. For the ABX₃ perovskites with large A cations (e.g., BaMnO₃), the hexagonal structure with the space group $P6_3/mmc$ had also been reported, so the $P6_3/mmc$ structure is also adopted as an initial structure of N(CH₃)₄SnI₃ and denoted as 3D-hex in Fig. 1f.

In the experiments, Liu et al. synthesized N(CH₃)₄PbI₃ at room temperature and ambient pressure¹⁵. The characterization showed that it has the 1D (*P*6₃/*m*) structure, where the PbI₆ octahedrons share three I atoms with adjacent ones and form lines in the lattice. Because of the similarity of Pb and Sn, we also consider the 1D structure as the initial N(CH₃)₄SnI₃ structure (see Fig. 1d). Furthermore, we construct the 2D structure (see Fig. 1e) as the initial structure, where SnI₆ octahedrons share two I atoms with adjacent ones and then form a 2D plane. Although 1D, 2D, and 3D-hex are not perovskite structures, we still consider them as N(CH₃)₄SnI₃ initial structures in order to check the stability of the 3D-cubic structures.

In order to predict the stability of the seven structures under different pressures, the total enthalpy H_{tot} is calculated as

$$H_{\text{tot}} = U + PV \,, \tag{1}$$

where U is the internal energy of the supercell, P is the hydrostatic

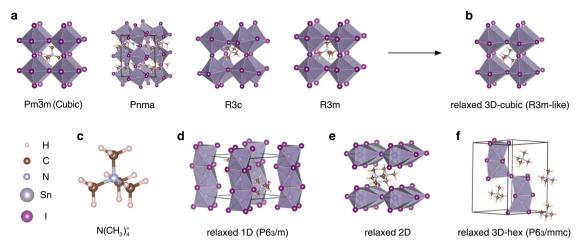


Fig. 1 The initial and relaxed structures of N(CH₃)₄Snl₃. a The initial 3D-cubic structures with symmetry $Pm\bar{3}m$, Pnma, R3c, and R3m. **b** The relaxed 3D-cubic structure from the initial ones in **a**. **c** The organic molecule N(CH₃)₄+ located at A site. **d** The relaxed 1D ($P6_3/m$) structure which represents the experimental structure at the ambient pressure. **e** The relaxed 2D structure and **f** the relaxed 3D-hex ($P6_3/mmc$) structure.

Table 1 Total enthalpy per formula unit $H_{\rm tot}/{\rm f.u.}$ (in eV) of the relaxed structures under 0 and 6 GPa.

	Pressure	3D-cubic	2D	1D	3D-hex
H _{tot} /f.u.	0 GPa	-99.402	-99.265	-99.514	-99.434
	6 GPa	-89.008	-88.348	-88.956	-88.923

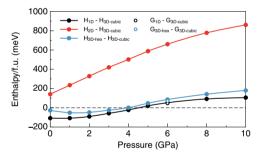


Fig. 2 Enthalpy differences as functions of hydrostatic pressure. Solid black circles: enthalpy differences between 1D and 3D-cubic structures of N (CH₃)₄Snl₃. Solid red circles: enthalpy differences between 2D and 3D-cubic structures. Solid blue circles: enthalpy differences between 3D-hex and 3D-cubic structures. The calculated Gibbs free energy differences between 3D-cubic and 1D (open black circle), 3D-hex (open blue circle) structures at 6 GPa and 300 K are also marked.

pressure, and V is the volume of the supercell. The total enthalpy per formula unit $(H_{\rm tot}/f.\rm u.)$ of the structures relaxed from $Pm\bar{3}m$, Pnma, R3c, and R3m are in the range of -99.406 to -99.394 eV. The absolute difference of $H_{\rm tot}/f.\rm u.$ is less than 12 meV, i.e., 0.57 meV/atom. All the $H_{\rm tot}/f.\rm u.$ of four initial 3D-cubic structures are listed in Supplementary Table 1. The difference is negligible and can be attributed to the numerical error and the different orientations of the $N(CH_3)_4^+$ at A site. According to the symmetry analysis 16 , we found that the symmetries of the relaxed structures are all R3m-like (see Fig. 1b), i.e., whatever the initial structure is $(Pm\bar{3}m, Pnma, R3c, \text{ or } R3m)$, the relaxed structures are the same. We use the average value of $H_{\rm tot}/f.\rm u. = -99.402$ eV for the 3D-cubic relaxed structure hereafter (see Table 1). The detailed 3D-cubic crystal structure and lattice parameters are

shown in Supplementary Fig. 1 and Supplementary Table 2. In the relaxed structure, the SnI_6 octahedrons sit in the corners of the cubic box. There is no tilt of SnI_6 octahedrons, but the Sn atom displaces from the center of the SnI_6 octahedron, producing three short $\mathrm{Sn-I}$ bonds and three longer $\mathrm{Sn-I}$ bonds.

Figure 1c shows the organic molecule $N(CH_3)_4^+$ at A site. The different directions of the N–C bonds in $N(CH_3)_4^+$ can lead to different initial structures despite the same lattice space group of ABX₃. However, we found that the difference of the total enthalpies is small, so the effect of the initial rotation of N $(CH_3)_4^+$ on the relaxed structures can be neglected. More details can be found in Supplementary Table 3.

The relaxed 1D and 2D structures are shown in Figs. 1d, e. $H_{\rm tot}/f.$ u. are -99.514 and -99.265 eV for 1D and 2D structures, respectively (see Table 1). Under 0 GPa, the energy of 1D structure is about 100 meV lower than that of 3D-cubic and 250 meV lower than that of 2D, which means the 1D structure is more stable under the ambient pressure. Our calculation is consistent with the experimental result¹⁵.

Figure 1f shows the relaxed 3D-hex structure. $H_{\rm tot}/f$.u. under 0 GPa is about $-99.434\,{\rm eV}$ (see Table 1) and it is about 30 meV lower than that of 3D-cubic structure but still about 80 meV higher than that of 1D structure, meaning that the 3D-hex structure is also more stable than 3D-cubic structure under the ambient pressure.

Although the 3D-cubic perovskite structure is not the most energetically preferred at 0 GPa, it was suggested that the 3Dcubic perovskite can be synthesized and the electronic structure can be modified under a high pressure¹⁷. So, we apply a hydrostatic pressure up to 10 GPa on the 1D, 2D, 3D-cubic, and 3D-hex structures, respectively, to investigate the behavior of the structure under different pressures. We compare $H_{\text{tot}}/\text{f.u.}$ differences between 3D-cubic and 2D $(H_{2D} - H_{3D-cubic})$, 1D $(H_{\rm 1D}-H_{\rm 3D-cubic})$, and 3D-hex $(H_{\rm 3D-hex}-H_{\rm 3D-cubic})$ structures in Fig. 2. Under pressures below 4.5 GPa, $H_{\rm 1D}-H_{\rm 3D-cubic}<0$, which means the 1D structure is more stable than 3D-cubic structure (see black line in Fig. 2). When the pressure increases above 4.5 GPa, $H_{1D} - H_{3D-cubic} > 0$, where the 3D-cubic structure becomes more energetically preferred than 1D. Similarly, when the pressure is higher than 4.5 GPa, the 3D-cubic structure is more stable than 3D-hex structure (see blue line in Fig. 2). Meanwhile, since $H_{\rm 2D} - H_{\rm 3D-cubic} > 0$ in the whole pressure range, the 3Dcubic structures are always more stable than 2D ones (see red line in Fig. 2). Our calculation indicates that the 3D-cubic

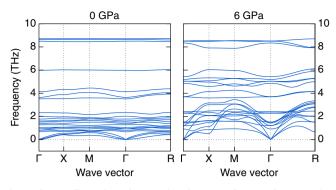


Fig. 3 Phonon dispersion of R3m N(CH₃)₄Snl₃ under 0 and 6 GPa. The high-symmetry wave vectors are Γ (0, 0, 0), X (0, 1/2, 0), M (1/2, 1/2, 0), and R (1/2, 1/2, 1/2).

 $N(CH_3)_4SnI_3$ (with the R3m space group) is more stable under high pressure, which makes the synthesis of 3D-cubic $N(CH_3)_4SnI_3$ perovskite possible.

We also considered the vibration contribution to the stability of different phases through calculating the Gibbs free energy G as following 18 :

$$G = H_{\text{tot}} + F_{\text{vib}}(T)$$

$$= H_{\text{tot}} + \frac{1}{2} \sum_{i,\mathbf{q}} \hbar \omega_{i,\mathbf{q}} + k_{\text{B}} T \sum_{i,\mathbf{q}} \ln \left[1 - \exp\left(-\frac{\hbar \omega_{i,\mathbf{q}}}{k_{\text{B}} T}\right) \right]$$
(2)

where $F_{\rm vib}(T)$ is the vibration contribution (including the internal vibrational energy and vibrational entropy) to the Gibbs free energy, $\omega_{i,q}$ is the phonon frequency of band index i and wave vector ${\bf q}$, T is the temperature, $k_{\rm B}$ is the Boltzmann constant, \hbar is the reduced Planck's constant. As shown in Fig. 2, at 6 GPa and T=300 K, the calculated G difference (per formula unit) between 3D-cubic and 1D NH₄SnI₃ is 46 meV, which is close to the enthalpy difference (52 meV); the calculated G difference between 3D-cubic and 3D-hex NH₄SnI₃ is 71 meV, which is also close to the enthalpy difference (85 meV). Obviously, the vibration contribution to the G differences is only a few meV, much smaller than the large positive value of the $H_{\rm tot}$ difference at 6 GPa. Therefore, the 3D-cubic structure is still more stable than 3D-hex and 1D structure, and our conclusion about the stability of different phases is not changed after the vibration contribution is considered.

Since the molecule $N(CH_3)_4^+$ is at A site, we also considered the van der Waals (vdW) interactions for the structural relaxation. When the vdW interaction is included in the relaxation, the lattice constant is about 6.73 Å, which is smaller than ~7.04 Å (without vdW). However, for the pressure-dependent total enthalpy ($H_{tot}/f.u.$) which is crucial to determine the stable state at high pressure, the conclusion is not changed, i.e., the 3D-cubic is the most stable structure at high pressure. The detailed results can be found in Supplementary Fig. 2.

Since $N(CH_3)_4SnI_3$ can phase-separate into $N(CH_3)_4I$ and SnI_2 and then become unstable, we also calculated the formation enthalpy (energy cost) of the chemical reaction $N(CH_3)_4I + SnI_2 \rightarrow N(CH_3)_4SnI_3$ in the pressure range of 0–6 GPa. The calculated energy costs for 3D-cubic $N(CH_3)_4SnI_3$ are all negative (see Supplementary Fig. 3), which means that 3D-cubic $N(CH_3)_4SnI_3$ is thermodynamically stable with respect to the phase-separation, and furthermore, it may be synthesized through mixing $N(CH_3)_4I$ and SnI_2 at high pressure.

Dynamic stability of ferroelectric structure. In order to investigate the dynamic stability of the *R3m* structure, we calculated its

phonon dispersion under 0 and 6 GPa via the phonopy package¹⁹. The results are shown in Fig. 3. Both the phonon dispersions at 0 and 6 GPa have no imaginary frequency, which indicates that the 3D-cubic structure is dynamically stable under both ambient and high pressures. The phonon dispersion calculated at 0 GPa is similar to that of 6 GPa, so we can conclude that even after the pressure is released, the 3D-cubic structure can still remain stable.

Spontaneous polarization. In order to predict whether 3D-cubic $N(CH_3)_4SnI_3$ (see Fig. 1b) has a large spontaneous polarization, we calculated the spontaneous polarization of $N(CH_3)_4SnI_3$ by using the Berry phase method²⁰. The overall spontaneous polarization **P** of the ferroelectric phase can be written as

$$\mathbf{P} = (P_x, P_y, P_z) = \mathbf{P}_{\text{ferro}} - \mathbf{P}_{\text{para}}$$
 (3)

where $\mathbf{P}_{\text{ferro}}$ (\mathbf{P}_{para}) is the polarization of the ferroelectric (paraelectric) phase. P_x , P_y , P_z are the three components of \mathbf{P} along [100], [010], and [001] directions, respectively.

The calculated polarization of the ferroelectric phase (R3m) of N(CH₃)₄SnI₃ is shown in Fig. 4a. In the calculation of ferroelectric polarization, the tetragonal structure with $P\overline{4}m2$ space group is used as the paraelectric phase. All the atoms are moved manually from the paraelectric phase to the ferroelectric phase to form the intermediate phases. The atomic displacements are indicated by the distortion percentage (the horizontal axis of Fig. 4a).

With respect to the paraelectric phase, the overall spontaneous polarization is found to be $\mathbf{P}=(9.94,\ 9.53,\ -8.40)\ \mu\text{C cm}^{-2}$. The polarization is nearly along the $[11\bar{1}]$ direction with a magnitude of $|\mathbf{P}|=16.13\ \mu\text{C cm}^{-2}$. In order to examine the contribution of the N(CH₃)₄+ molecule displacement to \mathbf{P} , we fix Sn and I positions and move N(CH₃)₄+ manually from the paraelectric phase to the ferroelectric phase. The contribution of the N(CH₃)₄+ off-centering displacement is $\mathbf{P}_{\rm org}=(-0.49,\ -0.53,\ -0.33)\ \mu\text{C cm}^{-2}$, which is nearly along $[\bar{1}\bar{1}\bar{1}]$ with the magnitude of 0.79 μ C cm⁻². In contrast, by fixing N(CH₃)₄+ but relaxing the positions of Sn and I atoms, the calculated contribution of Sn–I off-centering displacement is $\mathbf{P}_{\rm inorg}=(10.36,\ 10.27,\ -8.03)\ \mu\text{C cm}^{-2}$, with the magnitude of $16.65\ \mu$ C cm⁻² pointing to $11\bar{1}$, which is one order of magnitude larger than $\mathbf{P}_{\rm org}$. Therefore, we can conclude that the spontaneous polarization \mathbf{P} is mainly attributed to the Sn–I displacement.

Moreover, because of the non-polar feature of $N(CH_3)_4^+$ group, we can further ignore the effect originating from the internal polarization of $N(CH_3)_4^+$ molecule. As a comparison, the available measured polarization of $CH_3NH_3PbI_3$ is about $7~\mu C~cm^{-2}$ (ref. 11). So the polarization of $N(CH_3)_4SnI_3$ is large enough and therefore can play a positive role in suppressing the recombination of photon-generated electron-hole pairs in the PV devices.

Band structure and band gap. After making sure that the R3m N (CH₃)₄SnI₃ has strong ferroelectricity and can also be stable, now we will study its band structure and band gap (E_g) in order to ensure that it is suitable as a light-absorber semiconductor in solar cells.

The band structure and band gap are calculated using the generalized gradient approximation (GGA) with the exchange-correlation functional in the Perdew–Burke–Ernzerhof (PBE) form, and the spin-orbit coupling (SOC) effect is also considered. For 1D $\rm N(CH_3)_4SnI_3$ structure, the experimentally measured band gap is $\rm 2.6\,eV^{21}$ which is used as the reference for us to choose the appropriate functional for predicting the properties of N(CH_3)_4SnI_3. We have tried four different methods, including PBE, PBE+SOC,

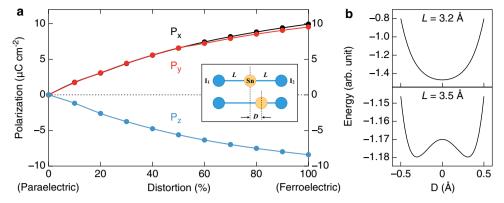


Fig. 4 Spontaneous polarization and the I-Sn-I model for explaining the ferroelectricity mechanism. a Polarization of the 3D-cubic R3m N(CH₃)₄SnI₃ as a function of the atomic distortion from the paraelectric to the ferroelectric phase. The black, red, and blue lines indicate P_x , P_y , and P_z component of polarization, respectively. Inset: illustration of the linear I-Sn-I model. **b** The total energy as a function of the Sn²⁺ displacement for L = 3.2 and 3.5 Å, respectively.

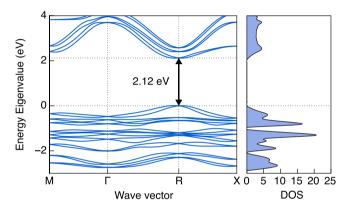


Fig. 5 Band structure and DOS of R3m **N(CH**₃)₄**Snl**₃**.** The high-symmetry wave vectors are M(1/2, 1/2, 0), Γ (0, 0, 0), R(1/2, 1/2, 1/2), and X(0, 1/2, 0). The Fermi level is shifted to 0 eV.

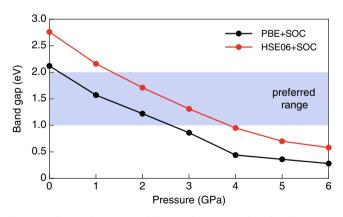


Fig. 6 Band gap of R3m 3D-cubic N(CH₃)₄Snl₃ as a function of external hydrostatic pressure. Black line: calculated using PBE+SOC, red line: calculated using HSE06+SOC. The blue color shows the band gap range suitable for the light-absorber semiconductor in solar cells.

HSE06, and HSE06+SOC, to calculate the 1D N(CH₃)₄SnI₃ band gap and the results are 2.76, 2.64, 3.47, and 3.33 eV (the corresponding band structure and density of states (DOS) are shown in Supplementary Fig. 4), respectively. Obviously, the calculated band gap of 1D N(CH₃)₄SnI₃ using PBE+SOC agrees well with the experimental data, indicating that the PBE+SOC method may be more suitable for predicting the band gap of

 $N(CH_3)_4SnI_3$ accurately. Therefore, we choose PBE+SOC to calculate the band structure and band gap for 3D-cubic $N(CH_3)_4SnI_3$.

The calculated band structure and DOS of the R3m 3D-cubic N(CH₃)₄SnI₃ performed by PBE+SOC under 0 GPa are shown in Fig. 5. We can see that the R3m 3D-cubic N(CH₃)₄SnI₃ is a direct band gap semiconductor at ambient condition, where the valence band maximum (VBM) and the conduction band minimum (CBM) are both located at the R point. The optical band gap $E_{\rm g} = 2.12$ eV.

The band gap of N(CH₃)₄SnI₃ can be tuned effectively through external pressure. In Fig. 6, we plot the calculated E_g using both PBE+SOC and HSE06+SOC under hydrostatic pressures up to 6 GPa. For the PBE+SOC case, as the pressure increases from 0 to 6 GPa, $E_{\rm g}$ decreases from 2.12 to 0.28 eV. For the HSE06+SOC case, Eg decreases from 2.76 to 0.58 eV with pressure increasing from 0 to 6 GPa. Although the band gaps calculated by the two methods have different absolute values, they have the same trend with respect to the pressure, i.e., with the increasing pressure, the band gaps both decrease with a similar slope. The monotonic decrease of the band gap with the hydrostatic pressure can be understood according to the composition of the VBM and CBM states. For R3m N(CH₃)₄SnI₃, the VBM state is mainly composed of anti-bonding hybridization between Sn s and I p orbitals, and the CBM state is mainly the non-bonding Sn p state²². When the pressure increases, the lattice constant decreases, so the Sn-I bond length is shortened, which increases the s-p hybridization between Sn and I and shifts the VBM level up. In contrast, the Sn p states is weakly affected under pressure, so the CBM level remains unchanged. As a result, the band gap decreases monotonically as the pressure increases.

Band structure engineering has been implemented to increase the PCE of the metal-halide perovskite solar cells by reducing the optical band gap to $1.3-1.4\,\mathrm{eV^{17}}$. The thin-film materials with $E_\mathrm{g}=1.0-2.0\,\mathrm{eV}$ are proven to be suitable for light-absorber semiconductors in solar cells^{7,8}, which is shown by the blue area in Fig. 6. In our calculation, when the pressure increases to $0.25\,\mathrm{GPa}$, the band gap decreases to $2.0\,\mathrm{eV}$. When the external pressure increases to $2.6\,\mathrm{GPa}$, the band gap decreases to $1.0\,\mathrm{eV}$. These results suggest that after the sample is synthesized under high pressure, the subsequent pressure release process can be controlled to tune the electronic band gap to fit the requirement of the light-absorber semiconductor in solar cells.

In order to demonstrate the potential application of the R3m N(CH₃)₄SnI₃, we also calculated the optical absorption spectrum for R3m N(CH₃)₄SnI₃. The results are shown in Supplementary

Table 2 Ionic radius of N(CH₃)₄⁺, NH₄⁺, Cs⁺, Sn²⁺, I⁻ and the tolerance factor t of ASnI₃ ($A = N(CH_3)_4$ ⁺, NH₄⁺, and Cs⁺).

A	lonic radius (Å)	Ref.	t (ASnl ₃)
N(CH ₃) ₄ + NH ₄ + Cs+ Sn ² +	3.20	15	1.13
NH ₄ +	1.61	30	0.80
Cs ⁺	1.78	30	0.83
Sn ²⁺	1.18	31	-
1-	2.20	31	-

Table 3 The total energy/f.u. (in eV) of NH₄Snl₃ and CsSnl₃ relaxed from initial structures Pm3m, Pnma, R3c, and R3m.

	Pm3m	Pnma	R3c	R3m
NH ₄ Snl ₃	-34.376	-34.631	-34.601	-34.463
CsSnl ₃	-14.041	-14.089	-14.068	-14.040

Fig. 5. The calculated absorption coefficient increases sharply as the photon energy is above the band gap, so N(CH₃)₄SnI₃ can absorb visible light effectively and act as a potential high-efficiency light-absorber semiconductor in solar cells.

Discussion

Understanding the origin of the ferroelectric feature of 3D-cubic $N(CH_3)_4SnI_3$ can help the design of the ferroelectric OIHPs. The symmetry of the ABX₃ perovskite structure can be estimated by the empirical Goldschmit tolerance factor $t = \frac{r_A + r_B}{\sqrt{2}(r_B + r_X)}$, where r_A , r_B and r_X are the radius of A, B and X, respectively. The structure tends to be *Pnma* when t < 0.8, $Pm\bar{3}m$ (cubic) when 0.8 < t < 1.0, and R3c or R3m when t > 1.0 (ref. ¹⁵). The radius of A-site group can determine the value of t and then play an important role in the structure symmetry. In $N(CH_3)_4SnI_3$, the ionic radius of $N(CH_3)_4^+$ is about 3.2 Å and the corresponding t = 1.13 (see Table 2). The relatively large $N(CH_3)_4^+$ makes the BX₆ octahedrons untilted. Meanwhile, the Sn^{2+} displaces from the center of SnI_6 octahedron in order to form a better bonding with the neighboring I^- . The overall structure is R3m-like. It appears that the large tolerance factor is crucial to the ferroelectricity in 3D-cubic $N(CH_3)_4SnI_3$.

We double check this conclusion by investigating NH₄SnI₃ and CsSnI₃, in which the A-site groups are smaller. The radii of NH₄⁺ and Cs⁺ are 1.61 and 1.78 Å (see Table 2), respectively. The tolerance factors are both relatively smaller (0.80 and 0.83, respectively, see Table 2). We construct the initial structures of NH₄SnI₃ and CsSnI₃ from Pm3m, Pnma, R3c, and R3m and relax all the structures. The calculated total energies of the relaxed structures are listed in Table 3. The most stable structures of both NH₄SnI₃ and CsSnI₃ are *Pnma*, which means the ferroelectricity is suppressed. The previous experimental and theoretical results also gave the same results²³. Furthermore, we investigate the role of A group on the ground state structure by increasing the volume of Pm3m, Pnma, R3c, R3m CsSnI₃ and fixing the volume during the relaxation. We find that R3m CsSnI₃ structure tends to be the most stable at large volume (see Supplementary Fig. 6). Since the increasing of the volume can be regarded as equivalent to the enlargement of the A-site group and the increasing of t, so the results indicated that the large t makes $N(CH_3)_4SnI_3$ form the ferroelectric structure.

The fact that a perovskite with a large tolerance factor t tends to be ferroelectric can be understood as follows. When the Sn–I

distances in the cubic paraelectric structure is large (a large t), the second-order Jahn–Teller effect (electronic hybridization) is more important, which results in the off-centering $\mathrm{Sn^{2+}}$ displacements and thus ferroelectric polarization. For small t, the $\mathrm{Sn-I}$ bond lengths are small so that the Pauli repulsion between the $\mathrm{Sn^{2+}}$ ion and $\mathrm{I^{-}}$ ion is strong, which keeps the Sn ions at the center of the octahedrons. Note that the same mechanism also explains the ferroelectricity in the classic inorganic perovskite ferroelectric: $\mathrm{BaTiO_3}$ with a large t is ferroelectric while $\mathrm{SrTiO_3}$ with a small t is not.

To see the competition between the electronic hybridization and Pauli repulsion clearly, let us consider a simple linear I-Sn-I model (see the inset of Fig. 4a). We adopt the repulsion part of the Lennard-Jones potential to approximate the total Pauli repulsion energy: $E_{\text{rep}} = \frac{a}{(L+D)^{12}} + \frac{1}{(L-D)^{12}}$ (a > 0), where L is original Sn-I₁ and Sn-I₂ bond distance and D is the displacement of the Sn²⁺. With a simple tight-binding model, the energy lowering due to the hybridization between the empty orbital of Sn²⁺ ion and occupied orbital of the I⁻ ion (for simplicity, we consider only one orbital for each ion): $E_{\text{hop}} \approx -\frac{\left(t_{\text{Sn}-I_1}\right)^2}{\Delta} - \frac{\left(t_{\text{Sn}-I_2}\right)^2}{\Delta}$, where $t_{\text{Sn}-I_1}$ $\left(t_{\text{Sn}-I_2}\right)$ is the hopping integral between Sn and I₁(I₂) ion, $\Delta(>0)$ is the energy difference between the empty orbital of Sn²⁺ and occupied orbital of the I⁻. According to Harrison's method²⁴, the dependence of the hopping integral on the bond distance can be written as: $t_{\text{Sn}-I_1} = \frac{b}{(L+D)^2}$ and $t_{\text{Sn}-I_2} = \frac{b}{(L-D)^2}$ (*b* is a constant). In Fig. 4b, we plot the total energy $E_{\text{tot}} = E_{\text{rep}} + E_{\text{hop}}$ as a function of D for two cases with different $Sn-I_1(I_2)$ bond distance (L=3.2or 3.5 Å) in the centrosymmetric linear model. As can be seen in Fig. 4b, in the case of short L (i.e., 3.2 Å), the energy minimum locates at D = 0, i.e., there is no ferroelectric instability. When the L is large (i.e., 3.5 Å, which corresponds to the 3D-cubic structure in our work), the energy curve becomes a double-well potential, indicating a ferroelectric instability (see Fig. 4b). In summary of above discussion, the Pauli repulsion dominates when the Sn-I₁(I₂) distance is small, while the second-order Jahn-Teller effect dominates in the case of long $Sn-I_1(I_2)$ distance.

To summarize, the Pb-free hybrid perovskite N(CH₃)₄SnI₃ with the non-polar molecular cation $N(CH_3)_4^+$ at A site and R3m structure is found to be a photovoltaic light-absorber semiconductor with robust and strong ferroelectricity. Its calculated spontaneous polarization is as large as $16.13 \,\mu\text{C cm}^{-2}$ along $[11\bar{1}]$ direction. In contrast to the transient ferroelectricity of CH₃NH₃PbI₃ which is sensitive to the orientation ordering of the polar molecular cation, the large intrinsic polarization of N (CH₃)₄SnI₃ results mainly from the Sn off-centering displacement induced by the large size of the N(CH₃)₄⁺ molecular cation and large structural tolerance factor, so it is permanent and robust at room temperature. The ferroelectric R3m structure is the ground state under hydrostatic pressure higher than 3 GPa, and is dynamically stable under the 0-6 GPa pressure according to the calculated phonon dispersion. Therefore, we propose that the ferroelectric R3m phase of N(CH₃)₄SnI₃ can be synthesized under high pressure (3 GPa) and can remain stable under ambient condition after the pressure is released. Its band gap can be tuned effectively from 2.12 to 1.0 eV by applying a hydrostatic pressure in the range of 0-3 GPa and its absorption coefficient of visible light is high. Therefore, this Pb-free and ferroelectric hybrid perovskite N(CH₃)₄SnI₃ is a suitable light-absorber semiconductor for solar cells. Its spontaneous polarization can suppress the recombination of the photo-generated electron-hole pairs, so it can be a high-efficiency light-absorber semiconductor in solar cells.

Unlike the traditional solar cells based on the heterogeneous p-n junction, the OIHPs semiconductor N(CH₃)₄SnI₃ with

strong ferroelectricity and suitable band gap may have large bulk photovoltaic effect and can be used for designing homogeneous bulk photovoltaic devices. Our work paves a way for designing high-efficiency and Pb-free OIHPs solar cells.

Methods

The structural relaxation and electronic structure calculations are performed using the plane-wave pseudopotential method based on the density functional theory (DFT) as implemented in the Vienna Ab initio Simulation Package (VASP)²⁵. For the exchange-correlation functional, we tested both the semi-local GGA in the PBE²⁶ form and the Heyd–Scuseria–Ernzerhof (HSE)²⁷ hybrid functional both with the SOC included. For the plane-wave basis, we use an energy cutoff $E_{\rm cut}=520\,{\rm eV}$. In the relaxation process, the ionic relaxation loop breaks when the change of energy reaches $1.0\times10^{-6}\,{\rm eV}$ and forces are below $0.005\,{\rm eV/Å}$. A $5\times5\times5$ Monkhorst–Pack k–point mesh centered at Γ point is used for structure relaxation, dynamic stability, ferroelectric calculations. We involve 5 valence electrons for N atom, 4 for C atom, 1 for H atom, 14 for Sn atom, and 7 for I atom. We adopted the DFT-D3 correction method with Becke–Jonson damping²⁸ as implemented in VASP to include the vdW effect.

To obtain the phonon dispersion, we first calculate the force constants using the finite displacement method. Then, phonon frequencies and eigenvectors are calculated with the phonopy software package¹⁹.

The optical absorption spectra and spontaneous polarization are calculated based on the converged charge density of the static electronic structure calculations. The imaginary part of the frequency-dependent dielectric function is calculated using the random phase approximation as formalized by Gajdoš et al.²⁹, and the real part is derived using the Kramers–Kronig transformation. Then, the frequency-dependent optical absorption coefficient is obtained from the dielectric function. The spontaneous ferroelectric polarization is calculated using the Berry phase method²⁰.

Reporting summary. Further information on research design is available in the Nature Research Reporting Summary linked to this article.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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Author contributions

H.J.X. and S.C. designed the study. H.W. and Y. Y. performed the DFT calculations. All authors contributed to the discussion of the results and writing of the manuscript.

Competing interests

The authors declare no competing interests.

Additional information

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