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Joint Research of Optics and Fluid Interface

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Subject Index xxxx, xxx

1 Setup

Let Δ be the total width the light travels with path not being straight, hence:

$$\forall x \notin \left[-\frac{\Delta}{2}, \frac{\Delta}{2} \right] : \frac{d^2}{dx^2} y = 0 \tag{1}$$

Now define the light ray incoming from left-hand side towards right-hand side and (suppose transition layers' width approaches zero) refracs at origin. And let h be the thickness of the transition layers.

Now let's assume the incoming transition layer has the same thickness as outbounding transition layer, hence we get:

$$\Delta = \frac{h}{2} (\tan \theta_{in} + \tan \theta_{out}) \tag{2}$$

Now we can first confirm our path function is a function of θ_{in} , θ_{out} , h

$$P(\theta_{in}, \theta_{out}, h) = \tag{3}$$

2 Playing with Bezier Curve

First setup the environment

```
h, t=var("h t")
hh=h/2
theta=var("theta")
tprime=var("tprime", latex_name=r"\theta^\prime")
assume(h, "constant")
assume(h>0)
assume(0<theta, theta<pi/2)
assume(0<tprime, tprime<pi/2)</pre>
```

And now we could try to solve functions like y(x) from parametric bezier curve:

```
# x(t)=(t-1)^2*tan(theta)*hh*-1+t^2*tan(tprime)*hh y=(t-1)^2*hh-t^2*hh
```

First we try to find t(x)

```
result=[]
```

[((abs(res.rhs()(x=tan(theta)*hh*-1)(h=2, theta=0.2, tprime=0.4))<1e-12 and abs(res.rhs()(x=tan(tprime)*hh)(h=2, theta=0.2, tprime=0.4)-1)<1e-12) and

result.append(res))
for res in solve((t-1)^2*tan(theta)*hh*-1+t^2*tan(tprime)*hh==x, t)]
t=result[0].rhs() if len(result)==1 else None

Where we get two solutions and only one will satisfied our assumptions (the first print is 0 and the second yields 1^1), which is:

$$t(x) = \frac{h \tan(\theta) - \sqrt{h^2 \tan(\theta) \tan(\theta') - 2(h \tan(\theta) - h \tan(\theta'))x}}{h \tan(\theta) - h \tan(\theta')}$$

And substituting back to y(t) we could get

3 Analyzing

Given a full path from v_1 to v_n , whose path will be $y(v_1, v_n, h)(x)$, we could separate it into different sections.

$$\Delta_{i \to i+1} = \frac{h}{n-1} \frac{1}{2} \left[-\tan \theta_i, \tan \theta_{i+1} \right] \tag{4}$$

$$\sum_{i=1}^{n-1} \Delta_{i \to i+1} = \frac{h}{2} (\tan \theta_1 + \tan \theta_n)$$

$$\forall x \in \underset{i \to i+1}{\Delta} : \tag{5}$$

$$(x, y(v_1, v_2, h_{12})(x)) + (\sum_{2 \to n} h_{2 \to n})$$

Here we use EPS = 1e - 12 as we're testing it with arbitarily chosen values which makes them no longer symbolic.

4 Finding path

4.1 Constructing Layers

Let function $v(\theta_{in}, \theta_{out}, \Delta, \delta)$ be the velocity of layer δ (from the entry interface), whose entry velocity is θ_{in} , exit velocity is be θ_{out} , and the whole layer thickness is Δ .²

$$a = v(x, y, \beta - \alpha, \alpha) \tag{6a}$$

$$b = v(x, y, \beta - \alpha, \beta) \tag{6b}$$

$$\alpha \le \beta$$
 (6c)

Let $a=v(x,y,\alpha)$ and $b=v(x,y,\beta)$ $(\alpha \leq \beta), \forall p \in [\alpha,\beta]: v(a,b,p-\alpha)=v(x,y,p)$

4.2 Fractal Structure

Let
$$P(\theta_{in}, \theta_{out}, h)$$
 be the path taken (7)

$$P(\theta_{in\to\alpha}, \alpha) = P(\theta_{in}, \theta_{\alpha}) \tag{8}$$

² Here we suppose every layer paraelles

5 Regarding Special Relativity

So first let the real velocity v, whom maintains the linear properties of traditional non-relativistic velocity.

Linear to non-linear (relativistic) velocity:

$$v_S = \frac{v_{ij} \pm_S ij}{\pm_S S} = v_{ij} \pm_S ij \tag{9}$$

5.1 Constant force/acceleration

Let a point located at origin, with initial velocity v(0) = 0.

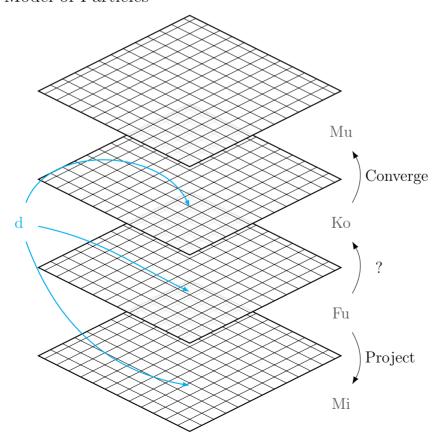
$$a_{\mathcal{L}}(v, F, m_{rest}) = \frac{F}{m_{rest}} \sqrt{1 - \frac{v^2}{c^2}}^3$$
 (10a)

$$a_{11}(t) = k \tag{10b}$$

$$v_{\mathsf{E}}(t) = v_{\mathsf{I}} \, \mathcal{I}_S \, \mathsf{I} = kt \, \mathcal{I}_S \, \mathsf{I} \tag{10c}$$

$$v_{E}(t) = \int \frac{F}{m_{rest}} \sqrt{1 - \frac{v_{E}(t)^{2}}{c^{2}}}^{3}$$
 (10d)

6 Model of Particles



7 Conclusion

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Acknowledgment

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References

[1] https://www.mail-archive.com/dou-geometry@googlegroups.com/msg00004/______.docx

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