Measure of Impurity: Classification Error

Classification error at a node t:

$$Error(t) = 1 - \max_{i} P(i \mid t)$$

- Maximum (1 1/n_c) when records are equally distributed among all classes, implying least interesting information
- Minimum (0) when all records belong to one class, implying most interesting information

Computing Error of a Single Node

$$Error(t) = 1 - \max_{i} P(i \mid t)$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Error =
$$1 - \max(0, 1) = 1 - 1 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$

Error =
$$1 - \max(1/6, 5/6) = 1 - 5/6 = 1/6$$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$

Error =
$$1 - \max(2/6, 4/6) = 1 - 4/6 = 1/3$$