CS 11: Introduction to Computer Science

From Arrays to Lists

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Goals for this session

- Lists: one of the most important CS data structures
 - What "real world" needs do they meet?
 - Examples of lists
- The same List interface can be implemented many ways
- The Array Lists we've been building are lists implemented as arrays
- First glimpse: linked lists
- But first: detailed review of SmartArrays

Review: Building List Arrays

I'd like to write a main program like this:

```
int *new array with squares(int size);
void print array(int *array, int length);
int main ()
        int *squares array ptr;
        int len;
        cout << "How many squares do you want to store? ";</pre>
        cin >> len;
        squares array ptr = new array with squares(len);
        print array(squares array ptr, len);
        delete [] squares array ptr;
```

How many squares do you want to store? 5

int	int	int	int	int
0	1	4	9	16
arr[0]	arr[1]	arr[2]	arr[3]	arr[4]

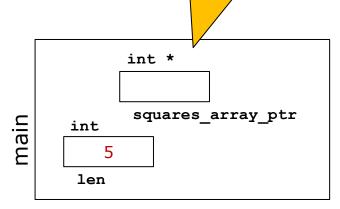
```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array_ptr = new_array_with_squares(len);
    print_array(squares_array_ptr, len);
    delete [] squares_array_ptr;
}
```

How many squares do you want to store? 5

main()'s local variables live in its activation record, of course.

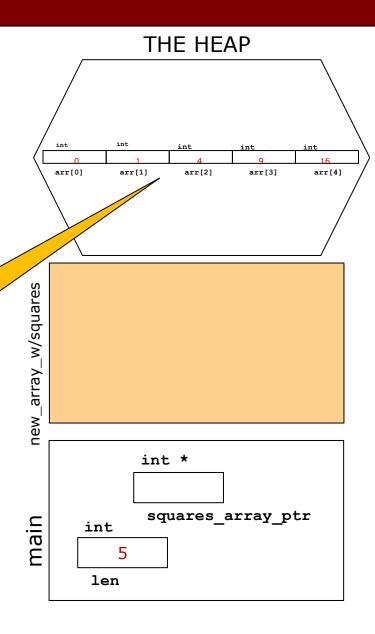


```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store?"
    cin >> len;

    squares_array_ptr = new array with squares do you want to store?"
    cin >> len;
```

new_array_with_squares will allocate it on the heap using new...

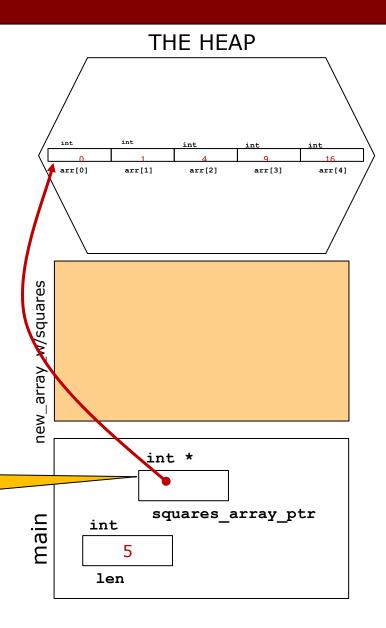


```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array_ptr = new_array_with_squares(len);
    print_array(squares_array_ptr, len);
    delete [] squares_array_ptr;
}
```

...and will return a pointer that we can keep here.

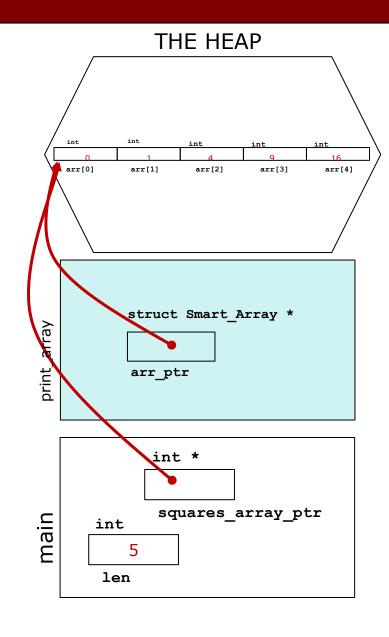


```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares array ptr = new array with squares(len);
    print_array(squares_array_ptr, len);
    delete [] squares_array_tr;
}
```

...so we can pass the pointer into the printing function which can then find the array!



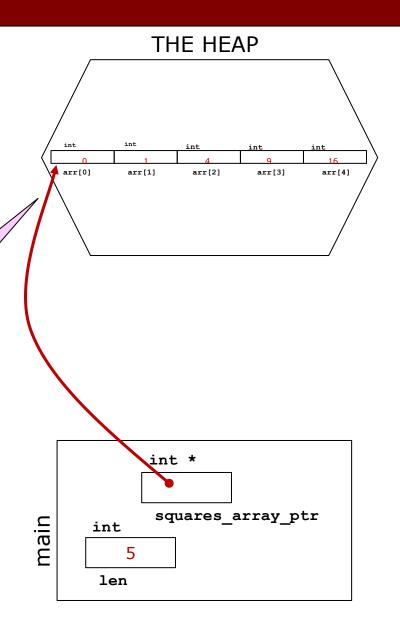
```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

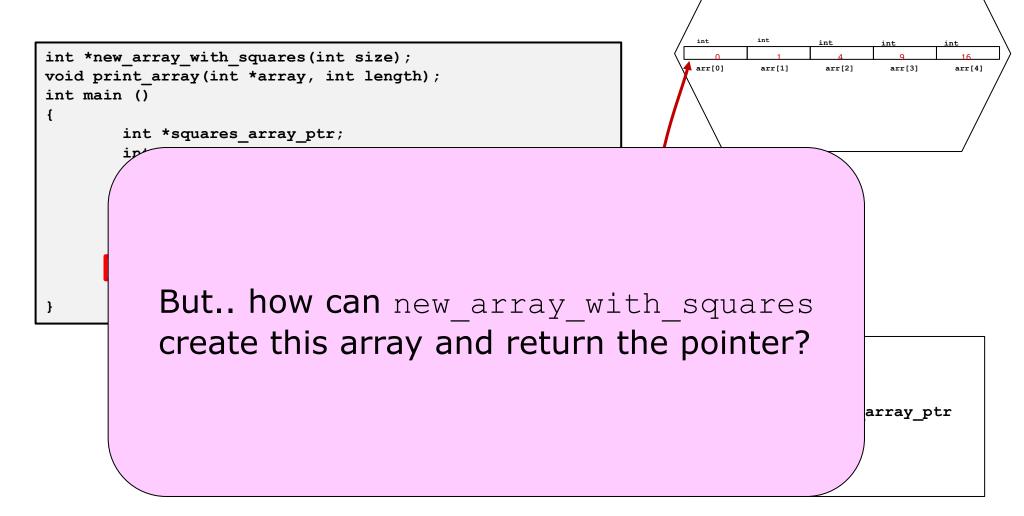
    cout << "How many squares do you want to storic cin >> len;

    squares array ptr = new array with soric print_array(squares_array_ptr, lendelete [] squares_array_ptr;
}
```

Crucially...

Both the array and at least one pointer to it live on after the function that created the array returns!





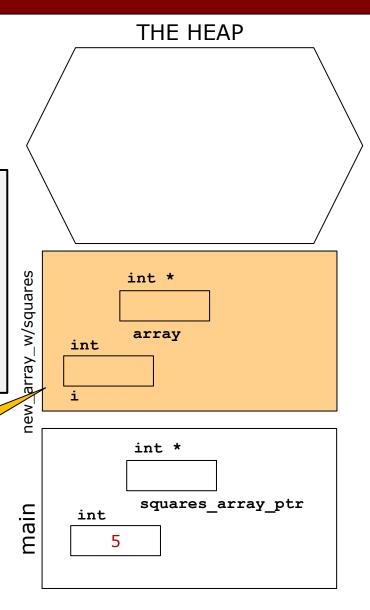
THE HEAP

Creating the array on the heap

```
int *new_array_with_squares(int size)
{
    int i;
    int *array = new int [size];

    // Fill with squares
    for (i = 0; i < size; i++) {
        array[i] = i * i; // array[i] gets i squared
    }
    return array;
}</pre>
```

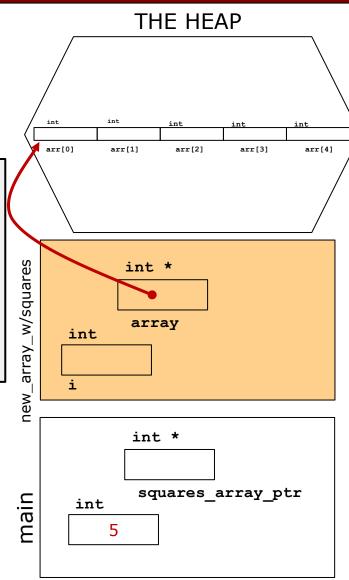
new_array_with_squares' local variables live in its activation record while it is running!



Creating the array on the heap

```
int *new_array_with_squares(int size)
{
    int i;
    int *array = new int [size];

    // Fill with squares
    for (i = 0; i < size; i++) {
        array[i] = i * i; // array[i] gets i squared
    }
    return array;
}</pre>
```

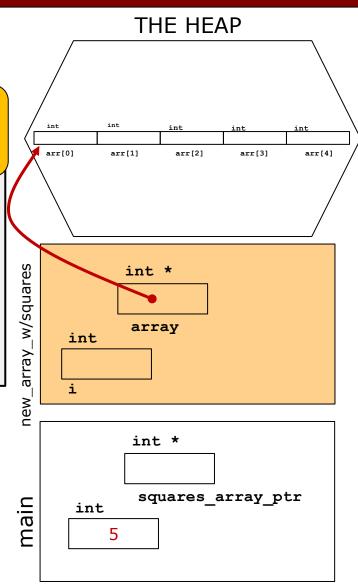


Creating the array on the heap

The C++ new operation allocates the array *on the heap!*

```
int *new_array_w
{
    int i;
    int *array = new int [size];

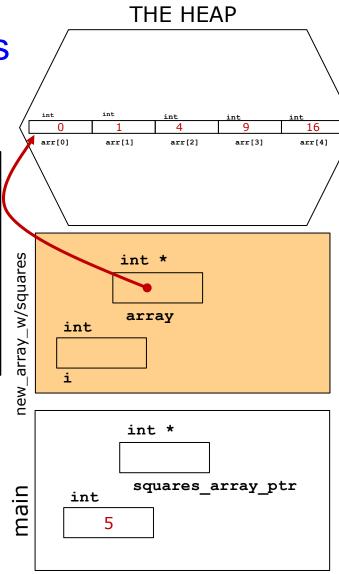
    // Fill with squares
    for (i = 0; i < size; i++) {
        array[i] = i * i; // array[i] gets i squared
    }
    return array;
}</pre>
```



Filling the array with squared numbers

```
int *new_array_with_squares(int size)
{
    int i;
    int *array = new int [size];

    // Fill with squares
    for (i = 0; i < size; i++) {
        array[i] = i * i; // array[i] gets i squared
    }
    return array;
}</pre>
```



How does main find the array?

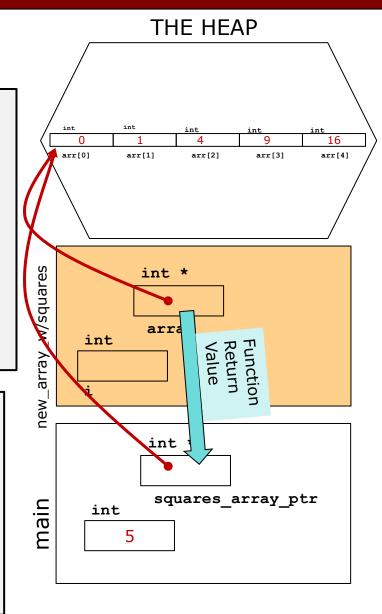
```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array_ptr = new_array_with_squares(len);
    print_array(squares_array_ptr, len);
    delete [] squares_array_ptr;
}
```

```
int *new_array_with_squares(int size)
{
    int i;
    int *array = new int [size];

    // Fill with squares
    for (i = 0; i < size; i++) {
        array[i] = i * i; // array[i] gets i squared
    }
    return array;
}</pre>
```



How does main find the array?

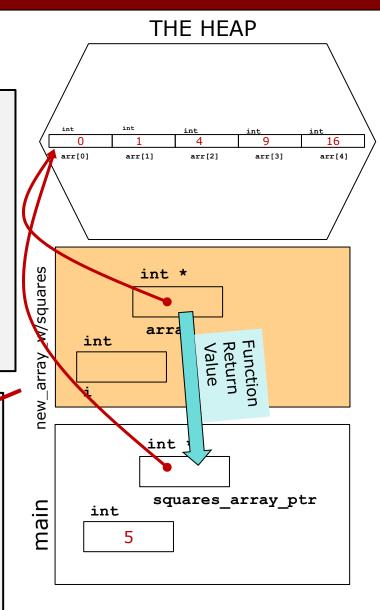
```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array_ptr = new_array_with_squares(len);
    print_array(squares_array_ptr, len);
    delete [] squares_array_ptr;
}
```

```
int *new_array_with_squares(int size)
{
    int i,
    int *array = new int [size];

    // Fill with squares
    for (i = 0; i < size; i+), {
        array[i] = i * i; // array[i] gets i squared
    }
    return array;
}</pre>
```



THE HEAP

Now we can pass the array to a function as always

```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares array ptr = new array with squares(len);
    print_array(squares_array_ptr, len);
    delete [] squares_array_ptr;
}
```

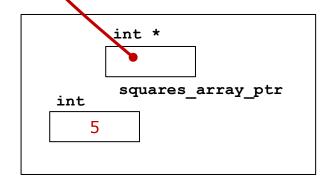
int int int int int

0 1 4 9 16

arr[0] arr[1] arr[2] arr[3] arr[4]

How many squares do you want to store? 5

```
array[0] = 0
array[1] = 1
array[2] = 4
array[3] = 9
array[4] = 16
```



...and use the array until it's deleted!

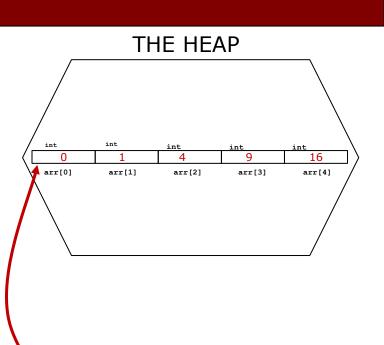
```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

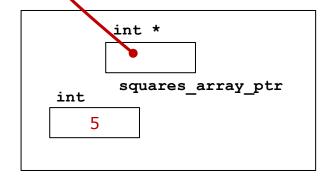
    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array_ptr = new_array_with_squares(len);
    print array(squares array ptr, len);
    delete [] squares_array_ptr;
}
```

How many squares do you want to store? 5

```
array[0] = 0
array[1] = 1
array[2] = 4
array[3] = 9
array[4] = 16
```





...and use the array until it's deleted!

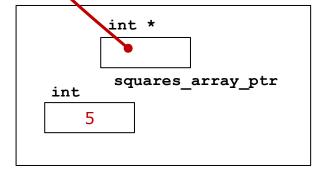
```
int *new_array_with_squares(int size);
void print_array(int *array, int length);
int main ()
{
    int *squares_array_ptr;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array_ptr = new_array_with_squares(len);
    print array(squares array ptr, len);
    delete [] squares_array_ptr;
}
```

THE HEAP

If we weren't about to leave anyway, we should set squares_array_ptr=nullptr



...and use the array until it's deleted!

```
THE HEAP
```

```
squares_array_ptr = new_array_with_squa
print array(squares array ptr, len);
delete [] squares_array_ptr;
```

IMPORTANT:

Is required for deleting arrays
Is forbidden when deleting anything else

C++ typically does not give you a nice error message: your program will behave unpredictably, maybe SEGFAULT, etc.

This is hard to debug if wrong; get it right!

What if we don't know how big the array should be?

We'll build a dynamic list array!

The idea...

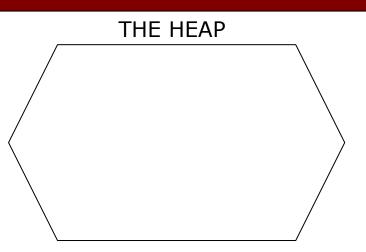
- We will build a service that can grow our arrays as necessary
- We can change our minds and ask for more each time, but...
- C++ arrays can't grow!
- The function will reallocate a bigger array if necessary. If so it will:
 - Copy all the data from the old to the new
 - Always return the pointer to the latest array...the caller uses that!

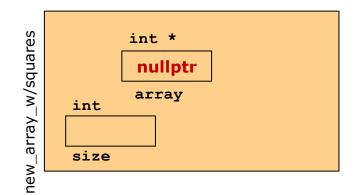
Calling a function that can grow arrays

```
/*
 * Get new array on heap and fill each
 * arr[] with i squared
 */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

    return array;
}</pre>
```



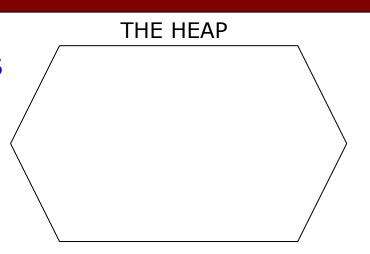


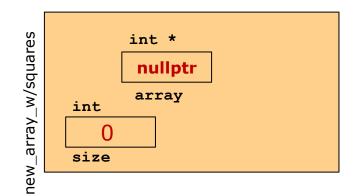
Calling a function that can grow arrays

```
/*
 * Get new array on heap and fill each
 * arr[] with i squared
 */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

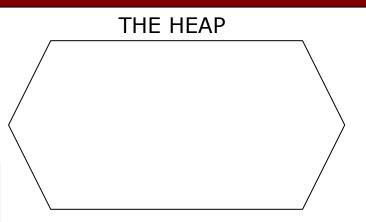
    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

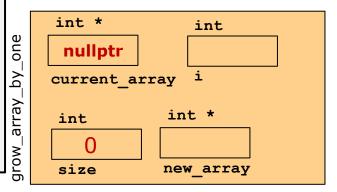
    return array;
}</pre>
```

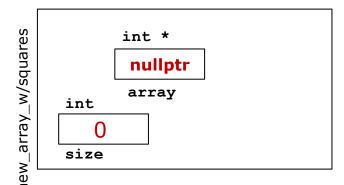


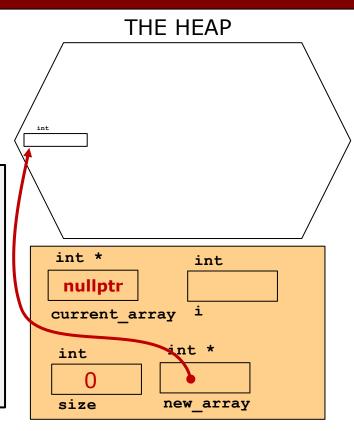


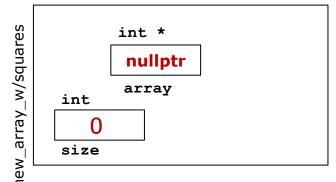
```
THE HEAP
      int *
                          int
one
       nullptr
grow_array_by.
     current array i
                      int *
      int
      size
                     new array
_array_w/squares
              int *
               nullptr
               array
      int
      size
```





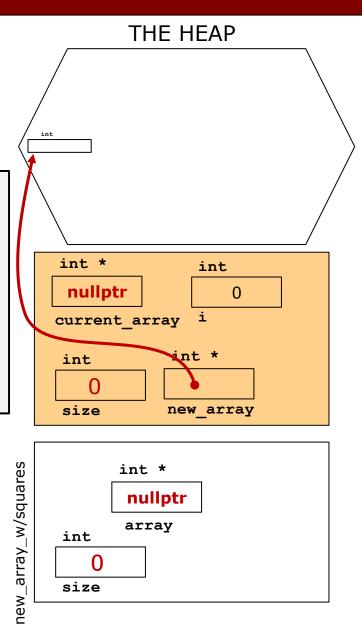






Does nothing this time

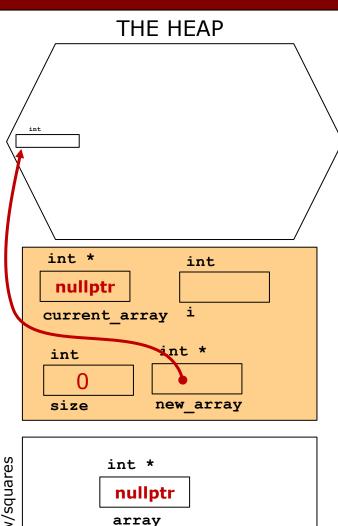
(size is 0)

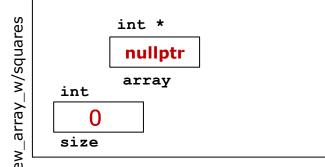


```
int *grow array by one(int *current array, int size)
    int i;
   int *new array = new int [size + 1];
   for (i = 0; i < size; i++) {
       new array[i] = current array[i];
   delete [] current array; // OK to use delete on nullptr
                                // the first time through
    return new ar
```

Does nothing this time

```
(current array is nullptr)
```

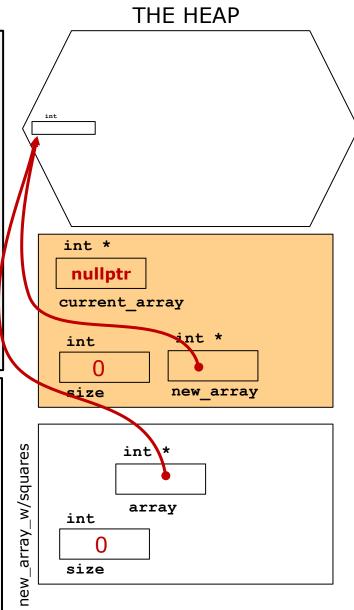




```
/*
 * Get new array on heap and fill each
 * arr[] with i squared
 */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

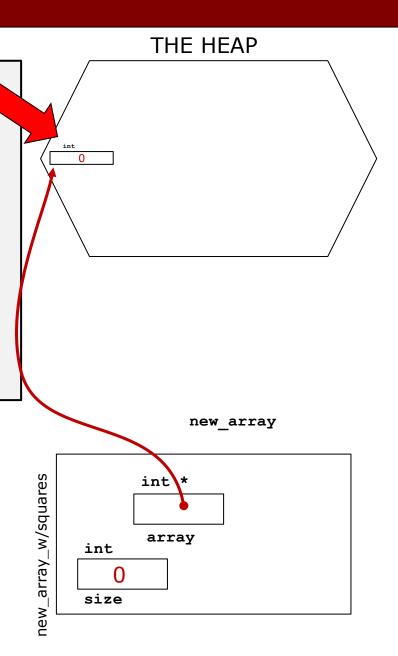
    return array;
}</pre>
```



```
/*
 * Get new array on heap and fill each
 * arr[] with i squared
 */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow array by one(array, size);
        array[size] = size * size; }

    return array;
}</pre>
```



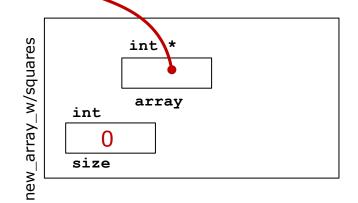
```
/*
  * Get new array on heap and fill each
  * arr[] with i squared
  */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

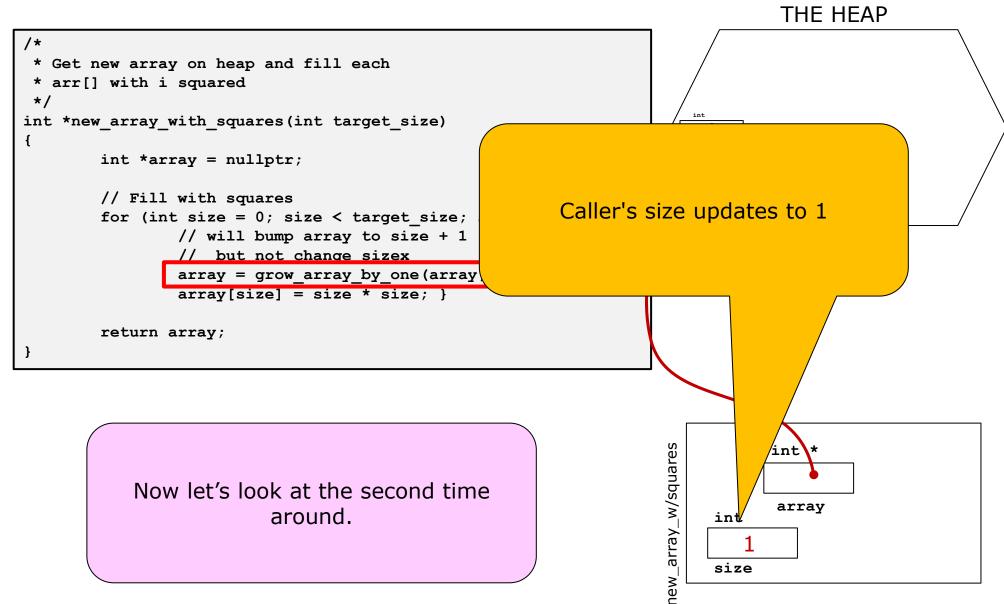
    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

    return array;
}</pre>
```

THE HEAP

Now let's look at the second time around.





array

int

size

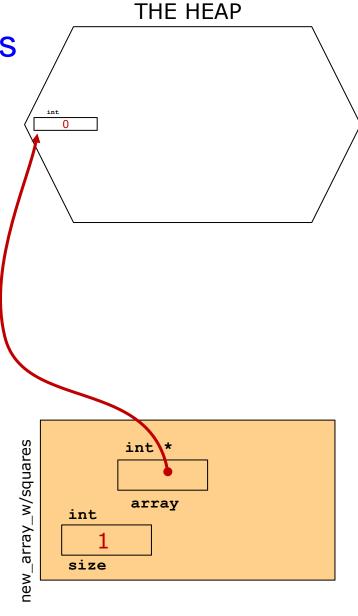
Now let's look at the second time around.

Calling a function that can grow arrays

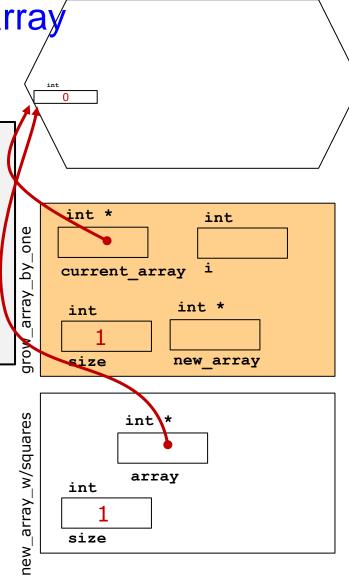
```
/*
 * Get new array on heap and fill each
 * arr[] with i squared
 */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

    return array;
}</pre>
```



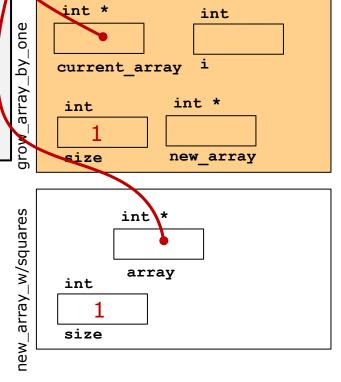
Allocating the second version of the array



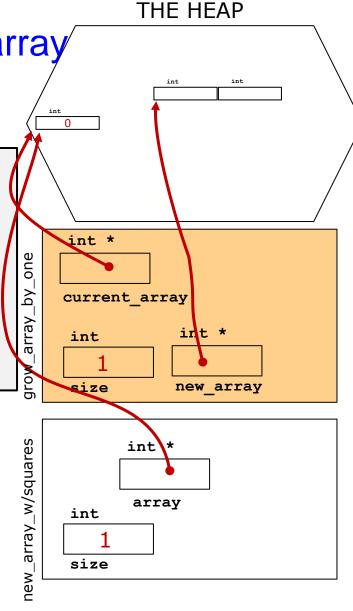
THE HEAP

THE HEAP

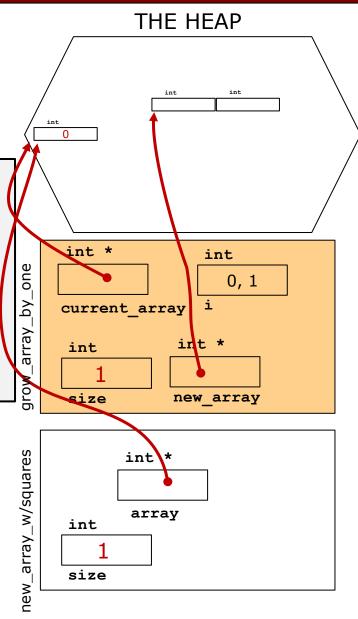
Allocating the *second* version of the array



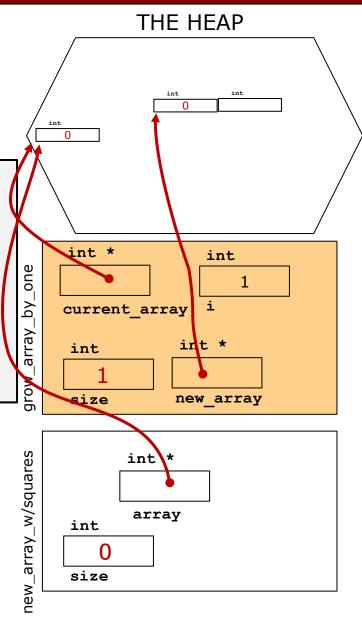
Allocating the second version of the array



Copying the old to the new



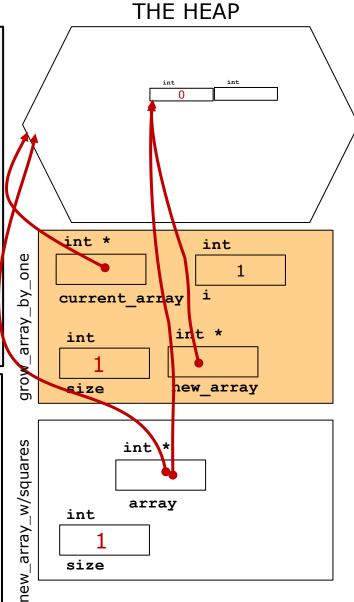
Deleting the one that's been replaced



```
/*
  * Get new array on heap and fill each
  * arr[] with i squared
  */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

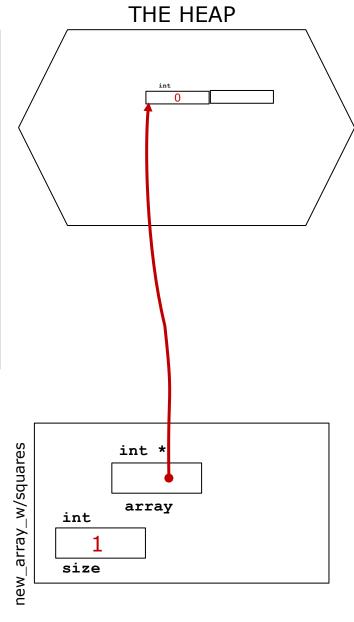
    return array;
}</pre>
```



```
/*
 * Get new array on heap and fill each
 * arr[] with i squared
 */
int *new_array_with_squares(int target_size)
{
    int *array = nullptr;

    // Fill with squares
    for (int size = 0; size < target_size; size++) {
        // will bump array to size + 1
        // but not change sizex
        array = grow_array_by_one(array, size);
        array[size] = size * size; }

    return array;
}</pre>
```



Moving Towards A Class-based Implementation Put Array Control Variables in a Struct

A first step: using structs

Data for the array implementation is in a Smart_Array struct.

```
int main ()
{
    Smart_Array squares_array;
    int len;

    cout << "How many squares do you want to store? ";
    cin >> len;

    squares_array = new_array_with_squares(len);
    print_array(squares_array);
    delete_smart_array(&squares_array);
}
```

A first step: using structs

```
Smart set_at function is like:
```

```
arr[i] = ...
```

...but automatically grows the array as needed.

The Smart_Array Struct

This struct encapsulates both the pointer to the current allocated array, and its size.

```
struct Smart_Array {
    int *current_array;
    int size; // highest set index+1
};
```

```
struct Smart_Array {
    int *current_array;
    int size; // highest set index+1
};
```

```
int get_at(Smart_Array arr, int i)
{
     // Here we assume that all requests are
     // properly within the size of the array
     return arr.current_array[i];
}
```

```
struct Smart_Array {
    int *current_array;
    int size; // highest set index+1
};
```

```
void set_at(Smart_Array *arr_ptr, int i, int new_value)
{
     while(arr_ptr->size <= i) {
          grow_array(arr_ptr);
     }
     arr_ptr->current_array[i] = new_value;
}
```

Example of two of the Smart array

In the end we'll update the array in the obvious way, but...

```
struct Smart_Array {
    int *current_array;
    int size; // highest set
};
```

```
void set_at(Smart_Array *arr_r, int i, int new_value)
{
    while(arr_ptr->size = i) {
        grow_array arr_ptr);
    }
    arr_ptr->current_array[i] = new_value;
}
```

```
struct Smart_Array {
    int *current_array;
    int size; // highest set
};
```

We automatically grow the array for the caller *if* it's not already big enough.

```
void set_at(Smart_Array *arr r, int i, int new_value)
{
    while(arr_ptr->size <= i) {
        grow_array(arr_ptr);
    }
    arr_ptr->current_array[i] = new_value;
}
```

struct Smart_Array {
 int *current_array;
 int size; // highest
};

Grow_array may update the struct by allocating a new array and changing the size, thus we must pass it into this function by reference,

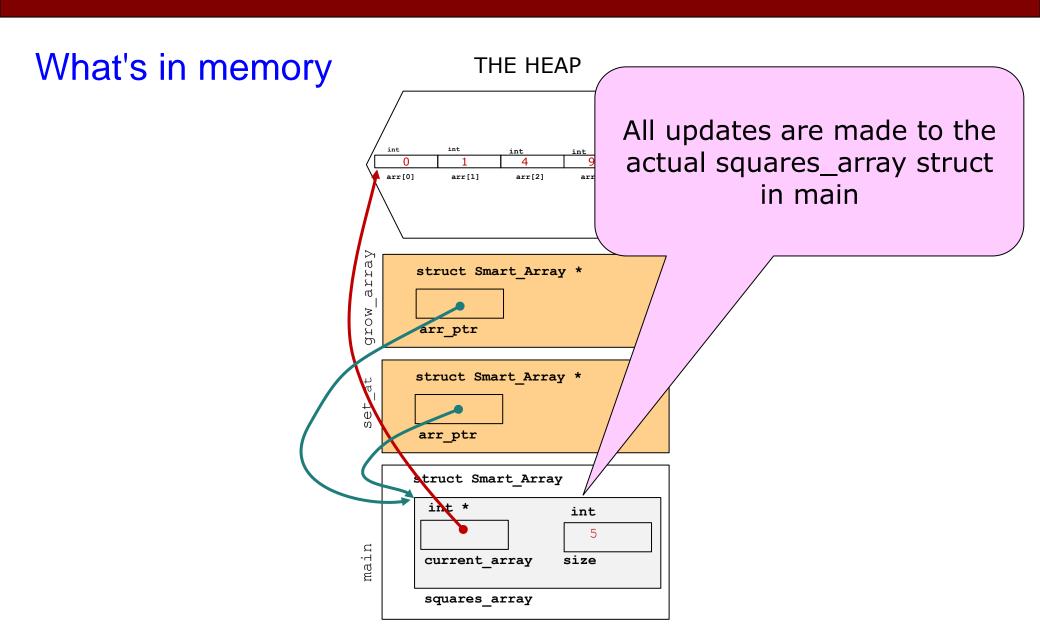
I.e. we receive here the *address* of the caller's Smart_Array struct, not a copy.

```
void set_at(Smart_Array *arr_ptr, int i, int new_value)
{
    while(arr_ptr->size <= i) {
        grow_array(arr_ptr);
    }
    arr_ptr->current_array[i] = new_value;
}
```

```
struct Smart_Array {
    int *current_array;
    int size; // highest
};
```

..and for the same reason we pass in the pointer to grow_array, which is actually manipulating the struct that lives in main's activation record.

```
void set_at(Smart_Array *arr_ptr int i, int new_value)
{
      while(arr_ptr->size <= i) {
            grow_array(arr_ptr);
      }
      arr_ptr->current_array[i] = new_value;
}
```



Grow array function

```
struct Smart_Array {
    int *current_array;
    int size; // highes
};
```

Using the arr_ptr argument, grow_array is updating the struct that's on the stack in *main's* activation record.

```
void grow array(Smart Array *arr ptr)
        int i;
                                  r ptr->size + 1];
        int *new array = new in/
        for (i = 0; i < arr p)
                               size; i++) {
                new array[i/
                             /arr ptr->current array[i];
        delete [] arr // tr->current_array;
        arr ptr->size = arr ptr->size + 1;
        arr ptr->current array = new array;
```

The next step: Wrapping it as a class

Public or private?

```
Class Smart_Array {
    int *current_array;
    int size; // highest set index+1
};
```

What else are we missing?

The Smart_Array Class

```
Class Smart Array {

private:

int *current_array;

int size; // highest set index+1

};
```

Constructor and destructor

What needs to change when we use a class?

The old set_at/get_at functions:

```
void set_at(Smart_Array *arr_ptr, int i, int new_value)
int get at(Smart Array arr, int i);
```

```
Class Smart Array {
  public:
            Smart Array();
            ~Smart Array();
            void set at(int i, int new value);
            int get at(int i);
  private:
            int *current array;
            int size; // highest set index+1
   };
The old set_at/get_at functions:
void set at(Smart Array *arr_ptr, int i, int new_value)
int get at(Smart Array arr, int i)
```

With classes, we don't have to pass the pointer explicitly...C++ knows which instance is to be referenced.

```
Class Smart Array {
public:
        Smart Array();
        ~Smart Array();
        void set at(int i, int new value);
        int get at(int i);
private:
        int *current array;
        int size; // highest set index+1
};
```

The old set_at/get_at/functions:
void set_at(Smart Array *arr_ptr, int i, int new_value)
int get at(Smart Array arr, int i)

```
automatically as needed.
  Class Smart Array {
  public:
           Smart Array();
           ~Smart Array();
           void set at(int i,
                                     new value);
           int get at(int i);
  private:
           void grow array();
           int *current array;
           int size; // highest set index+1
   };
The old grow_array function:
void grow array(Smart Array *arr ptr);
```

Private:

Users see an array that grows

From Arrays to Lists

What the user sees

```
Class Smart Array {
public:
        Smart Array();
        ~Smart Array();
        void set at(int i, int new value;
        int get at(int i);
};
        void grow array();
        int *current array;
        int size; // highest set index+1
```

What the user sees

HEY!

That's a pretty good start on an interface to *any* list, not just to an array!

List interface: what other functions might we want?

```
Class List {
public:
    List();
    ~List();

    // By index
    void set_at(int i, int new_value;
    int get_at(int i);
};
```

```
Class List {
public:
        List();
        ~List();
        // By index
        void set at(int i, int new value;
        int get at(int i);
        // At front
        int removeFirst();
        void addToFront(int n);
```

```
Class List {
public:
        List();
                          Remove the first item...
         ~List();
                          ...leaving us with a new first item!
         // By index
         void set at(in
         int get at(int i);
         // At front
         int removeFirst();
        void addToFront(int n);
```

```
Class List {
public:
        List();
                           Put a new item at the front...
         ~List();
                           ...bumping back all the others!!
        // By index
        void set at(int
         int get_at(int i);
        // At front
         int removeFirst();
        void addToFront(int n);
```

```
Class List {
public:
        List();
        ~List();
                       Append a new item to
        // By index
                       the end of the list.
        void set at(i
        int get at(ir
        // At front
        int removeFirst
        void addToFront
                            n);
        // At back
        void addToBack(int n);
```

```
Class List {
public:
        List();
        ~List();
        // By index
        void set at(int i, int new value;
        int get at(int i);
        // At front
        int removeFirst();
        void addToFront(int n);
        // At back
        void addToBack(int n);
        void addAtPostition(int n, int position);
```

```
Class List {
  public:
    List();
    ~List();
```

Many other variations on the List interface are possible.

```
// At back
void addToBack(int n);
};
```

Review: what we've just seen

- Lists are a very useful data abstraction
- Typical list interfaces let you:
 - Add items to the list at the beginning and/or end
 - Remove items from the beginning and/or end
 - Get to all the items by index in the current list
 - Sometimes:
 - Remove items from the middle of the list
 - Insert items in the middle of the list
 - Etc.
- NOW WE WILL EXPLORE AN INTERESTING IDEA: ARE THERE DIFFERENT WAYS OF PROVIDING THIS SAME LIST MANAGEMENT SERVICE?

DISCUSSION

What would happen if we tried to add these new capabilities using our array-based implementation?

Removing from the front of an array-based list

int	int	int	int	int	int
8	3	4	7	9	
arr[0]	arr[1]	arr[2]	arr[3]	arr[4]	arr[4]

Removing from the front of an array-based list

int	int	int	int	int	int
8	3	4	7	9	
arr[0]	arr[1]	arr[2]	arr[3]	arr[4]	arr[4]
int	int	int	int	int	int
8	3	4	7	9	
arr[0]	arr[1]	arr[2]	arr[3]	arr[4]	arr[4]

Adding at the end of an array-based list

int	int	int	int	int	int
8	3	4	7	9	
arr[0]	arr[1]	arr[2]	arr[3]	arr[4]	arr[4]
int	int	int	int	int	int
int 8	int 3	int 4	int 7	int 9	int
_	T		int 7 arr[3]		int arr[4]

Implementing lists with arrays

- Adding at the end is:
 - Easy?
 - Hard?
- Adding at the beginning is:
 - Easy?
 - Hard?
- Getting a value by index is:
 - Easy?
 - Hard?

- Deleting at the end is:
 - Easy?
 - Hard?
- Deleting at the beginning is:
 - Easy?
 - Hard?
- Inserting / deleting in the middle is:
 - Easy?
 - Hard?

DISCUSSION

Are there other ways we could implement the same interface?

A first look at *linked* lists

struct Node

Node* next
int element

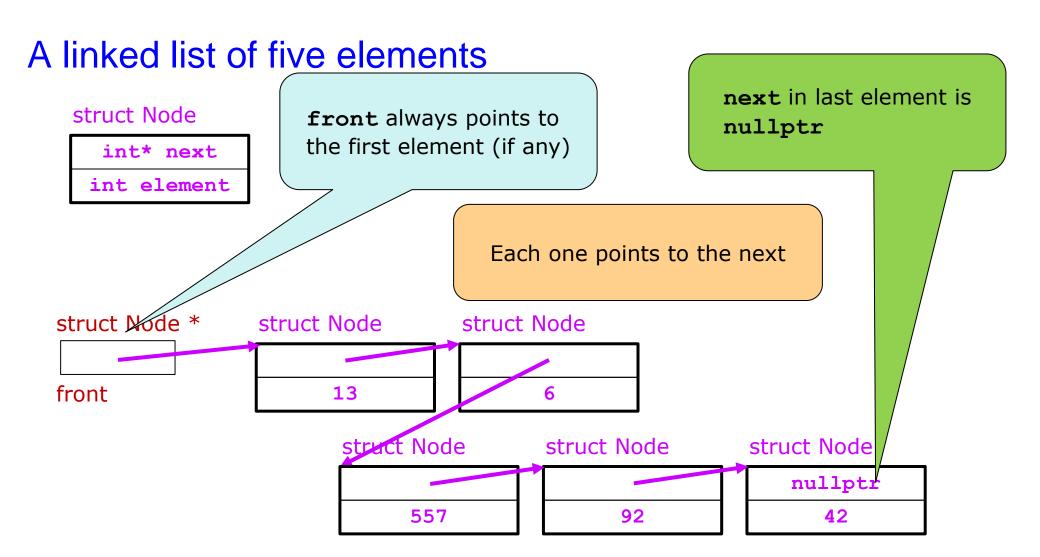
Declaration of struct Node

We will use this *Node* struct for every element in the list.

struct Node *
nullptr
front

The list as a whole is represented by a single **Node** pointer variable called "front".

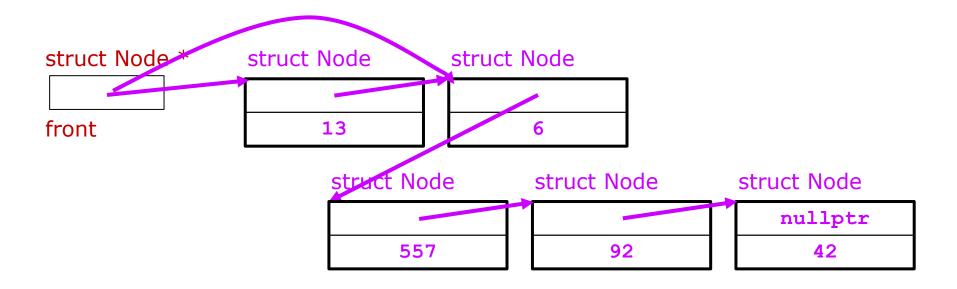
If the list is empty, then front contains nullptr.



Removing the first element

struct Node

int* next
int element



Implementing lists using linked nodes

- Adding at the end is:
 - Easy?
 - Hard?
- Adding at the beginning is:
 - Easy?
 - Hard?
- Getting a value by index is:
 - Easy?
 - Hard?

- Deleting at the end is:
 - Easy?
 - Hard?
- Deleting at the beginning is:
 - Easy?
 - Hard?
- Inserting / deleting in the middle is:
 - Easy?
 - Hard?

Summary

Summary

- We reviewed dynamic array lists arrays that grow as needed
- We evolved from a struct- to a class-based implementation, focusing on...
- ...clean interfaces that hide implementation details
- We started exploring lists as an Abstract Data Type (independent of implementation details
- We started looking at linked, lists a classic implementation of lists
- We compared the performance tradeoffs between array-based lists and linked lists using pointers