

## REVIEW FOR TEST 2 145 01

### 1. LOGISTICS

The test in Friday, Nov. 17 during the normal class time. The location is Jackson 006 via the following email:

“Your Math 145 recitation 01-RA will be relocated on 11/17 to Jackson 006”

The test will cover Chapter 8 (Cayley’s theorem) through chapter 16 homomorphisms. Monday I will finish homomorphisms and Wednesday will be review.

### 2. DEFINITIONS

General linear group ( $GL(n, \mathbb{R})$ ,  $GL(n, \mathbb{C})$ ,  $O(n)$ ,  $SO(n)$ , the direct product of groups. Group generated by a set, partition, equivalence relation, equivalence class, conjugate elements, conjugacy classes, Quaternion group, normal subgroup, quotient group, left cosets, right cosets, index of a subgroup, commutator subgroup, simple group, center of a subgroup, homomorphism, kernel, First isomorphism theorem

### 3. THEOREMS AND FACTS YOU SHOULD KNOW AND FEEL COMFORTABLE WITH

- Every group of order  $n$  is isomorphic to a subgroup of  $S_n$  (and roughly how does this work?)
- When is  $Z_m \times Z_n$  cyclic?
- How can you tell if a group is a direct product? (10.2)
- If  $H$  is a subgroup of a finite group  $G$ , the order of  $H$  divides the order of  $G$ . (what about the order of elements of  $G$ )?
- Consequences of LaGrange’s theorem
- Cauchy’s theorem: If  $p$  is a prime divisor of the order of a finite group  $G$ , then  $G$  contains an element of order  $p$ .
- Computing conjugacy classes.
- How can you tell when a subgroup is normal? (15.2, 15.4)
- First, second and third isomorphism theorems. (Particularly the first!)