

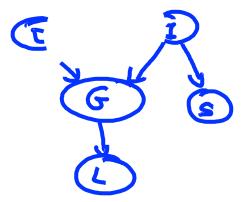
#### Representation

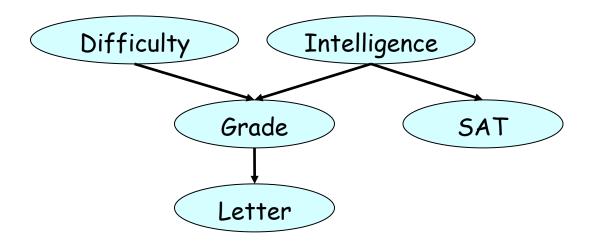
#### **Bayesian Networks**

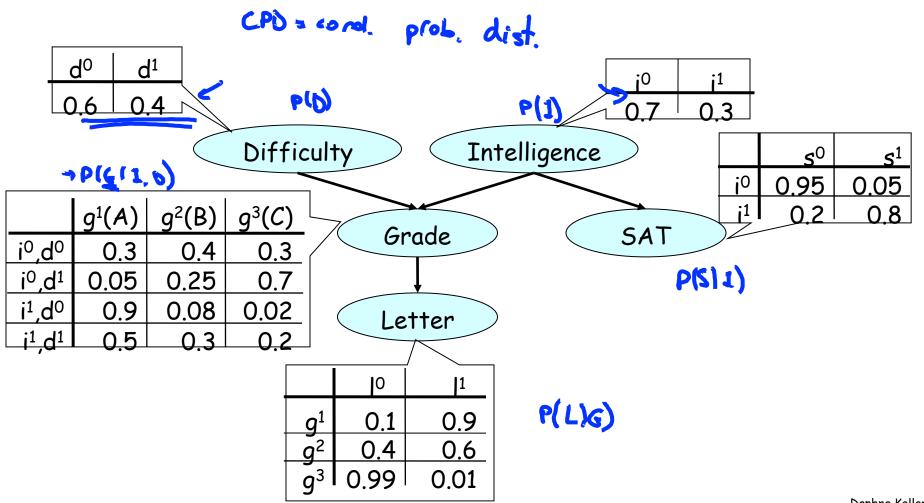
# Semantics & Factorization

- Grade
- · Course Difficulty
- Student Intelligence
- Student SAT
- Reference Letter

P(G,D,I,S,L)



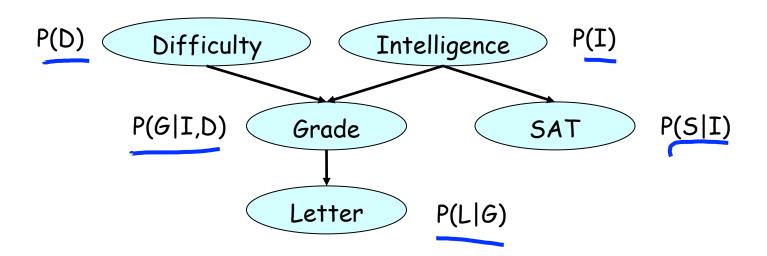




Daphne Koller

#### 链式法则

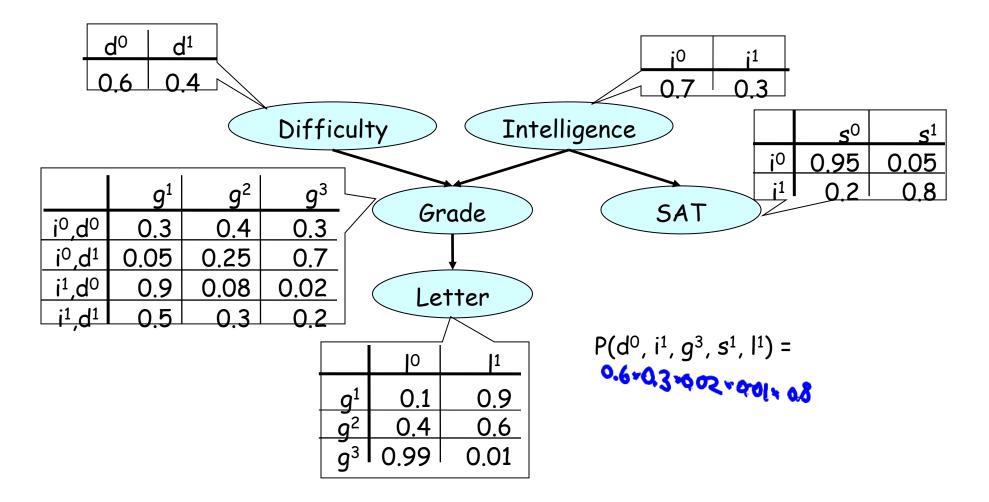
#### Chain Rule for Bayesian Networks



P(D,I,G,S,L) = P(D) P(I) P(G|I,D) P(S|I) P(L|G)

Distribution defined as a product of factors!

Daphne Koller



## Bayesian Network

- A Bayesian network is: <sub>有向无环图</sub>
  - A directed acyclic graph (DAG) G whose nodes represent the random variables  $X_1,...,X_n$
  - For each node  $X_i$  a CPD  $P(X_i \mid Par_G(X_i))$
- The BN represents a joint distribution via the chain rule for Bayesian networks

$$P(X_1,...,X_n) = \prod_{i} P(X_i \mid Par_G(X_i))$$

Daphne Koller

### BN Is a Legal Distribution: P ≥ 0

```
P is a product of cpD,

CPDs are non-regative
```

# BN Is a Legal Distribution: $\Sigma P = 1$

 $\sum_{D,I,G,S,L} P(D,I,G,S,L) = \sum_{D,I,G,S,L} P(D) P(I) P(G|I,D) P(S|I) P(L|G)$ 

=  $\sum_{D,I,G,S} P(D) P(I) P(G|I,D) P(S|I) \sum_{L} P(L|G)$ 

 $= \sum_{D,I} P(D) P(I) P(G|I,D) P(S|I)$ 

=  $\sum_{D,I,G} P(D) P(I) P(G|I,D) \sum_{S} P(S|I)$ 

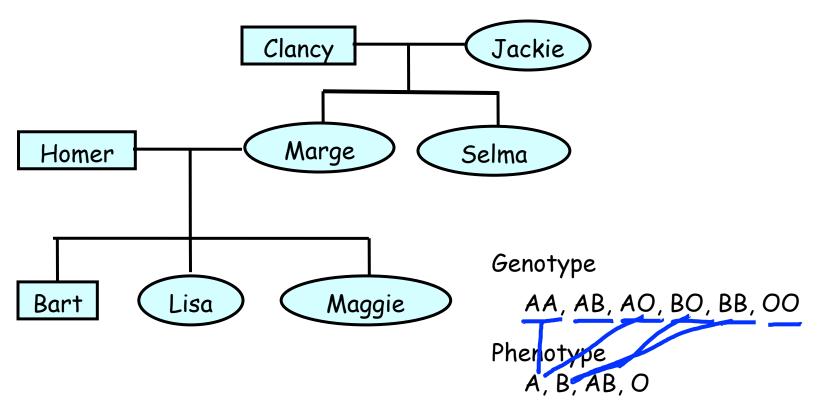
 $= \sum_{D,I} P(D) P(I) \sum_{G} P(G|I,D)$ 

#### P Factorizes over G

- Let G be a graph over  $X_1,...,X_n$ .
- P factorizes over G if

$$P(X_1,...,X_n) = \Pi_i P(X_i \mid Par_G(X_i))$$

#### Genetic Inheritance



#### BNs for Genetic Inheritance

