

Advanced OWL

Chin Zi Hau

Logics (*what a logic gives you*)

- Logic = a formal way to describe a domain using:
 - **Axioms:** assumptions or rules we accept as true

Logic:

What *entities/relations/time* you can represent?
What kinds of *queries or reasoning* are possible?

- Facts, objects, relations, time, ...
- Epistemological commitments: (*what can we know about it*)
 - True/false, possibility/necessity, belief/disbelief, certainty/uncertainty, ...

Types of Logic

Logic language	Logical element	Examples
Propositional	e/unknown	"It is raining AND the streets are wet"
First order logic	e/unknown	"All cats are mammals"
Modal logic	e/unknown	
Deontic logic	e/unknown	
Temporal logic	e/unknown	"I am always hungry"
Probability theory	[0,1]	"There is a 70% chance of rain tomorrow"
Fuzzy logic	Truth value, [0,1]	"Is it cold"? <i>Very Much</i> / 0.9 <i>Little</i> / 0.25 <i>Very Less</i> / 0.1

Simple declarative statements (proposition).

Introducing objects, properties and relationships

Uses operators like " \square " (necessity) and " \diamond " (possibility).

What must be true? What could be true?

How things change over time.

Likelihood of events occurring.

No clear-cut boundaries, allowing partial truth.

Question: Is $P(\text{plagiarise})$ equivalent to $\neg F(\text{plagiarise})$?

F(plagiarise)

Components of a logic

Syntax

- *Rules* that specify what a well-formed sentence (or formula) looks like
- Tells us how to build a knowledge base
- All legal expressions are sentences (otherwise known as well-formed formulas)

Semantics

- *Rules* that specify what a sentence (or formula) really means in the world
- Tells us what the knowledge base means

Propositional Logic

- The simplest type of logic
- A **proposition** is a statement that is either **true** or **false**
- There is no objects, relations, and functions.

- The symbols denote atomic statements that says something about the world
- $\neg P$ negation (means the opposite of P)
- $P \wedge Q$ conjunction (means both P and Q)
- $P \vee Q$ disjunction (means P or Q , or possibly both)
- $P \Rightarrow Q$ implication (means "if P then Q ")
- $P \Leftrightarrow Q$ biconditional (means " P if and only if Q ")

Propositional Logic vs. First Order Logic

”If Jane is younger than Lisa, then Lisa is older than Jane.”

- Using Propositional logic:

p: Jane is younger than Lisa

q: Lisa is older than Jane

p \Rightarrow q

- Using First order logic:

Younger: to be younger than (predicate with two variables)

Older: to be older than

Younger(Jane, Lisa) \Rightarrow **Older**(Lisa, Jane)

First Order Logic features

- **Atomic negation:** $\text{not } C(x)$
- **Role negation:** $\text{not } R(x,y)$
- **Intersection of concepts:** $A \cap B$ (set of individuals of A and individuals of B)
- **Union of concepts:** $A \cup B$ (set of individuals of A and individuals of B)
- **Existential restrictions:** exists at least one individual that participates in a property (owl:some)
- **Universal restriction:** only (all) individuals that participate in a property (owl:only)

not Bird(Tom)

Not isMarried(Alice, Bob)

Bird \cap Flies

Bird \cup Mammal

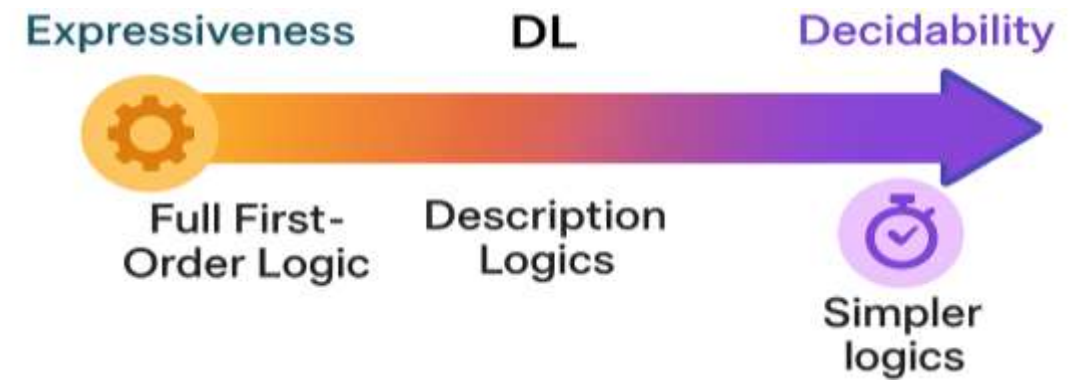
A person must have at least one pet that is a dog.

Only eats plant-based food.

First Order Logic syntax

- Constants: John, Richard, 2 ...
- Predicates: Brother, $>$, Father ...
- Functions: Sqrt, isKing, ...
- Variables: x, y, a, b, \dots
- Connectives: $\neg, \Rightarrow, \Leftrightarrow, \wedge, \vee$
- Equality: $=$
- Quantifiers: \forall, \exists

Description Logics



- A family of formal knowledge representation languages used in AI to describe and reason about concepts.
- Description Logics strike a balance between:
 - **Expressiveness** – ability to *represent complex structures and constraints*.
 - **Decidability** – ability to *perform reasoning tasks* (e.g., inference) *efficiently*.
- Why not full First-Order Logic?
 - Full FOL offers **high expressiveness but sacrifices decidability**, making reasoning computationally prohibitive.
 - DL uses selected fragments of FOL to maintain practical reasoning.

Description Logics

- In DL, three basic elements:
 - **Individuals:**
 - Specific objects (e.g., Alice, F20BD).
 - **Concepts (Classes):**
 - Groups of individuals (e.g., Person, Course).
 - **Roles (Properties):**
 - Relationships between individuals (e.g., teaches, enrolledIn).

Terms

FOL (first order logic)	DL (description logic)	OWL
constant	individual	individual
unary predicate	concept	class
binary predicate	role	property

Different Description Languages

Basic DL languages

language	name	allows
AL	Attributive language	<ul style="list-style-type: none"> Atomic negation intersection restrictions limited existential quantification
FL	Frame based	<ul style="list-style-type: none"> Concept intersection restrictions limited existential quantification role restriction
EL	Existential language	<ul style="list-style-type: none"> concept intersection existential restrictions

Extensions

	name	
F	Functional prop	uniqueness
E	Existential qualification	There exists at least one individual
U	Concept union	
		Rdfs:subPropertyOf
		Not p(x,y)
		Reflexivity, disjointness
		P(x,y) => Q(y,x)
		owl:cardinality, counting (in owl2)
(D)	Use of datatype prop	Data values or data types

$\exists \text{hasPart.Wheel}$

Specifying constraints on the type objects that can fill a role

$\exists \text{hasPart.}(\text{Wheel} \sqcap \text{HasColor.Red})$

a person can have at most 2 parents

S is used as abbreviation for ALC, some use it for ALCH

Other DL languages and their use

- **EL**

- Fragment of OWL intended for **Conceptual modelling (domain knowledge)**.
- Example: SNOMED CT ontology (2x10⁵ classes)
 - Large-scale health
 - *Appendicitis* \equiv *Inf*

Person(?x) ^ EmployedBy(?x, ?company) ^ LocatedIn(?company, London) -> LondonBasedEmployee(?x)

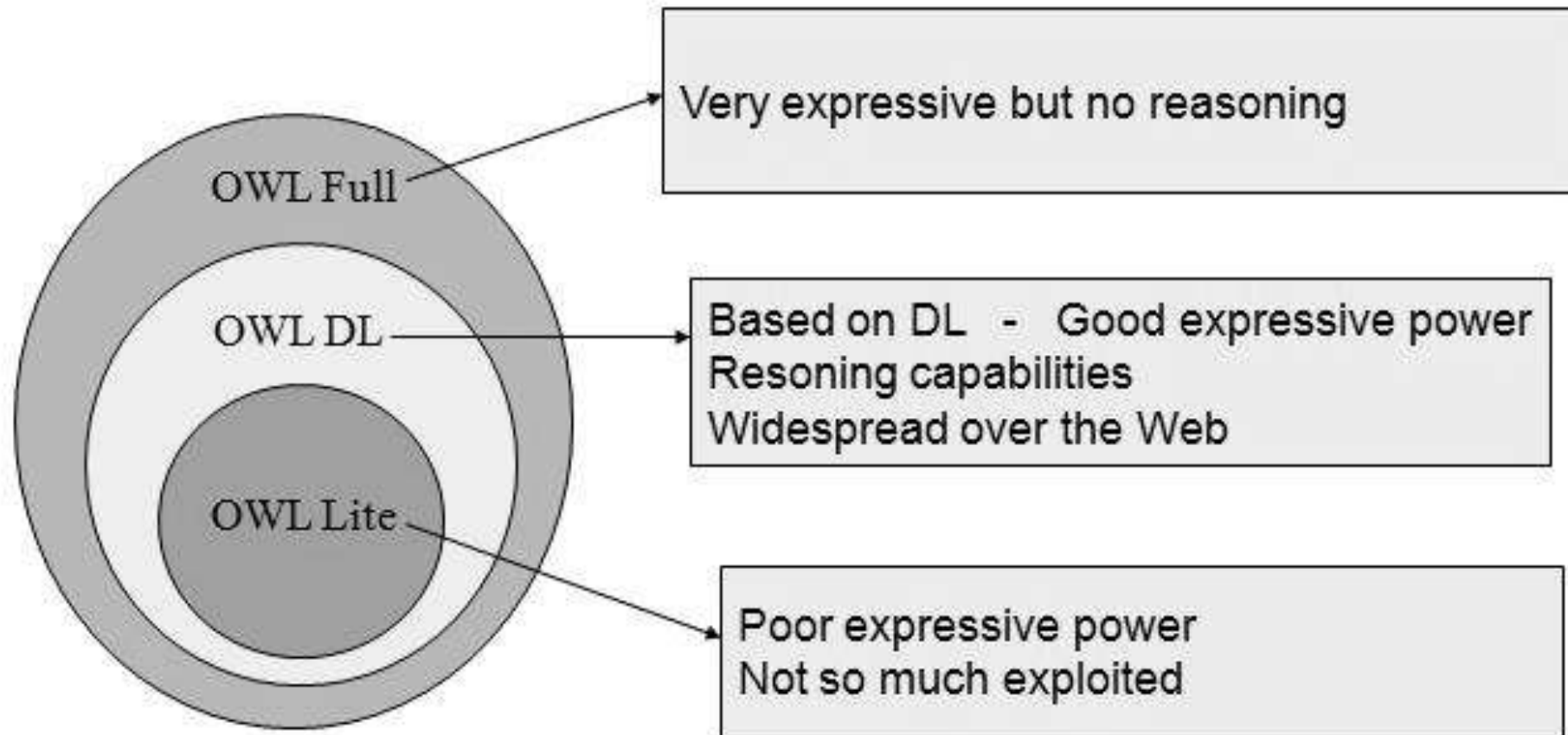
- **RL**

- Rule-based OWL, intended for **inferencing**
- In practice **SWRL (semantic web rule language)** is used (not part of OWL)

- **QL**

- Query-language, intended for **ontology based data access (OBDA)**
- Queries roles and individuals (Abox)
- **SPARQL** more general, queries also Tbox (concepts and their individuals)
 - Example: Retrieve all employees working in London offices who manage projects over \$1M.

OWL flavours/versions



OWL flavours/versions

- OWL Full -> SROIQ(*D*)
 - Very high expressiveness, prohibitive reasoning
- OWL-DL -> SHOIN
 - Lower expressiveness, decidable
- OWL 2 -> SHOIQ
 - High expressiveness, very complex reasoning
- OWL-lite -> SHIF
 - Low expressiveness, high reasoning
- **Protégé supports SHOIN**

- *S* stands for *ALC* plus **role transitivity**,
- *H* stands for **role hierarchies**, i.e., **role inclusion** axioms,
- *O* stands for **nominals**, i.e., for closed classes with one element,
- *I* stands for **inverse roles**,
- *N* stands for **cardinality restrictions**,
- *D* stands for **datatypes**,
- *F* stands for **role functionality**,
- *Q* stands for **qualified cardinality restrictions**,
- *R* stands for **generalized role inclusion axioms**, and
- *E* stands for **existential role restrictions**.

Example of First Order Logic

Sentences

- Ander is Chinese
- Alona is Ander's daughter
- Panda likes Bamboo
- Children of football fans are football fans
- Football fans like summer

First order logic representation

- $\forall x, \text{Chinese}(x) \Rightarrow \text{Person}(x)$
- $\text{Chinese}(\text{Ander})$
- $\text{hasDaughter}(\text{Ander}, \text{Alona})$
- $\forall x, y \text{ hasDaughter}(x, y) \Rightarrow \text{childOf}(y, x)$
- $\forall x, \text{Panda}(x) \Rightarrow \text{likes}(x, \text{Bamboo})$
- $\forall x, y, \text{childOf}(y, x) \text{ AND } \text{likes}(x, \text{Football}) \Rightarrow \text{likes}(y, \text{Football})$
- $\forall x, \text{likes}(x, \text{Football}) \Rightarrow \text{likes}(x, \text{Summer})$

Example in OWL

```
@prefix : <http://hw.ac.uk/basques#> .  
@prefix owl: <http://www.w3.org/2002/07/owl#> .  
@prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#> .  
@prefix xml: <http://www.w3.org/XML/1998/namespace> .  
@prefix xsd: <http://www.w3.org/2001/XMLSchema#> .  
@prefix rdfs: <http://www.w3.org/2000/01/rdf-schema#> .  
@base <http://hw.ac.uk/basques#> .
```

```
<http://hw.ac.uk/basques#> rdf:type owl:Ontology .  
:Person rdf:type owl:Class.  
:Sport rdf:type owl:Class.  
:Seanon rdf:type owl:Class.  
:Basque rdfs:subClassOf :Person.  
:Woman rdfs:subClassOf :Person.  
:Pelota rdfs:subClassOf :Sport.
```

Class definitions

```
:daughterOf rdf:type owl:ObjectProperty ;  
              rdfs:domain :Woman .  
:like rdf:type owl:ObjectProperty ;  
       rdfs:domain :Person ;  
       rdfs:range owl:Thing .
```

Object
properties

```
:Ander rdf:type owl:NamedIndividual ,  
         :Basque .  
:Alona rdf:type owl:NamedIndividual ,  
         :Person ;  
        :daughterOf :Ander .  
:summer rdf:type owl:NamedIndividual ,  
           :Season ;
```

Individuals

```
Basque(?x) ^ Sport(?y) -> likeSport(?x, ?y)      Use SWRL  
childOf(?x, ?y) ^ likeSport(?y, ?s) -> likeSport(?x, ?s)
```

The Second Rule (S2) in RDF Format

:x rdf:type <http://www.w3.org/2003/11/swrl#Variable> .

:y rdf:type <http://www.w3.org/2003/11/swrl#Variable> .

:s rdf:type <http://www.w3.org/2003/11/swrl#Variable> .

Variables

[<http://swrl.stanford.edu/ontologies/3.3/swrla.owl#isRuleEnabled>
"true"^^xsd:boolean ;

rdfs:comment "Inherited hobby"^^xsd:string ;

rdfs:label "S2"^^xsd:string ;

rdf:type <http://www.w3.org/2003/11/swrl#Imp> ;

<http://www.w3.org/2003/11/swrl#body>

[rdf:type <http://www.w3.org/2003/11/swrl#AtomList> ;

rdf:first [rdf:type
<http://www.w3.org/2003/11/swrl#IndividualPropertyAtom> ;

<http://www.w3.org/2003/11/swrl#propertyPredicate> :childOf ;

<http://www.w3.org/2003/11/swrl#argument1> :x ;

<http://www.w3.org/2003/11/swrl#argument2> :y

];

Rule body

If ?x is a childOf ?y

rdf:rest [rdf:type <http://www.w3.org/2003/11/swrl#AtomList> ;

first [rdf:type
<http://www.w3.org/2003/11/swrl#IndividualPropertyAtom> ;

<http://www.w3.org/2003/11/swrl#propertyPredicate> :likeSport ;

<http://www.w3.org/2003/11/swrl#argument1> :y ;

<http://www.w3.org/2003/11/swrl#argument2> :s

]; rdf:rest rdf:nil

];

<http://www.w3.org/2003/11/swrl#head>

[rdf:type <http://www.w3.org/2003/11/swrl#AtomList> ;

rdf:first [rdf:type
<http://www.w3.org/2003/11/swrl#IndividualPropertyAtom> ;

<http://www.w3.org/2003/11/swrl#propertyPredicate> :likeSport ;

<http://www.w3.org/2003/11/swrl#argument1> :x ;

<http://www.w3.org/2003/11/swrl#argument2> :s

]; rdf:rest rdf:nil

];

Rule body

SWRL Example (human-readable)

Rule Name: S2 – Inherited Hobby

If:

- ?x is a child of ?y
- ?y likes sport ?s

Then:

- ?x also likes sport ?s

SWRL Syntax:

- $\text{childOf}(\text{?x}, \text{?y}) \wedge \text{likeSport}(\text{?y}, \text{?s}) \rightarrow \text{likeSport}(\text{?x}, \text{?s})$

OWL Advanced Features (Restrictions & Characteristics)

- Class restrictions
 - Class intersection (`owl:and`)
 - Class union (`owl:or`)
 - Class complement (`owl:not`)
 - Subclass of complex class
 - Enumerated class (list of individuals)
- Individual restrictions
 - Same individuals (`owl:sameAs`)
 - Different individuals (`owl:differeFrom`)
- Object Property restrictions
 - Existential restriction (`owl:some`)
 - Universal restriction (`owl:only`)
 - Equivalence (`owl:some` and `owl:only`)
 - Range value restriction (`owl:value`)
- Cardinality restrictions
 - Minimum range (`owl:min`)
 - Maximum range (`owl:max`)
 - Exact range (`owl:exactly`)

- Property characteristics
 - Inverse property (`owl:inverseOf`)
 - Symmetric (`owl:SymmetricProperty`, `owl:AssymetricProperty`)

• Disjoint (`owl:propertyDisjointWith`)

`:hasGrandparent owl:propertyChainAxiom
(:hasParent :hasParent) .`

• Transitive (`owl:TransitiveProperty`)
`inAxiom)`

Margherita Pizzas have toppings of Tomato and Mozzarella - moreover, they only have toppings of Tomato and Mozzarella

ns
comparison

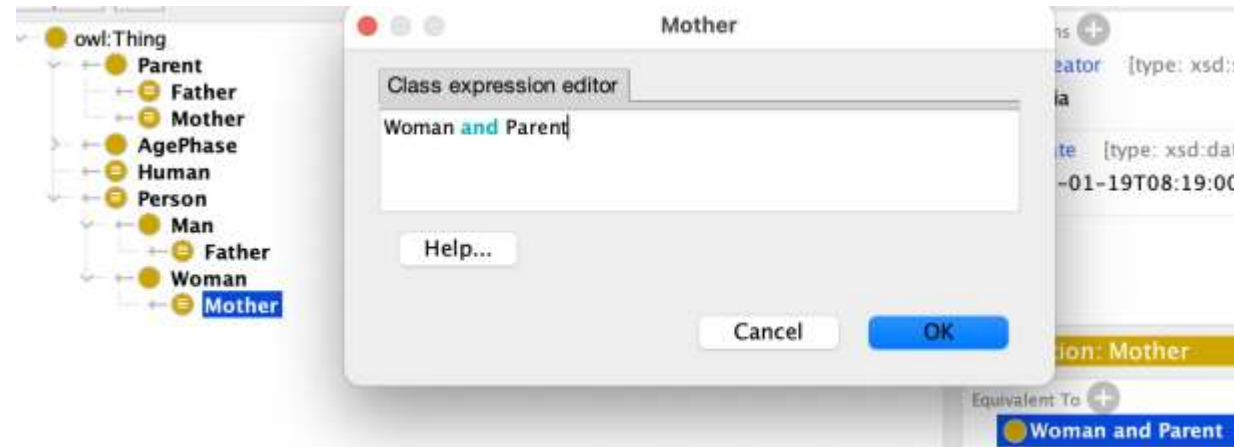
OWL: Intersection of classes

Woman(x) and Parent(x) \Leftrightarrow Mother(x)


- We can define a class as the intersection of two classes.
- Individuals of such class will be those belonging to both intersected classes
- Example Mother is Woman and Parent

```
:Mother rdf:type owl:Class ;  
    owl:equivalentClass [ owl:intersectionOf ( :Parent  
                                                :Woman  
                                                ) ;  
                           rdf:type owl:Class  
                           ] ;
```

- Inference
 - Any individual mother will also be Parent



One-way vs Two-way statements (\sqsubseteq vs \equiv)

- \rightarrow \square One-way (implication / constraint)
 - $A \sqsubseteq B$ means: If x is $A \rightarrow x$ must be B
 - \checkmark From $x:A$ infer $x:B$
 - \times From $x:B$ cannot infer $x:A$
- \rightleftarrows Two-way (equivalence / definition)
 - $A \equiv B$ means: $A \sqsubseteq B$ AND $B \sqsubseteq A$ (x is $A \leftrightarrow x$ is B)
 - \checkmark From $x:A$ infer $x:B$
 - \checkmark From $x:B$ infer $x:A$ (enables auto-classification)
-  Protégé (Manchester syntax)
 - $A \sqsubseteq B \rightarrow \text{Class: } A \text{ SubClassOf: } B$
 - $A \equiv B \rightarrow \text{Class: } A \text{ EquivalentTo: } B$

OWL: Union of classes

$$Father(x) \text{ or } Mother(x) \Leftrightarrow Parent(x)$$

- A **union** class is the class of individuals that belong to at least one of union classes
- Example Parent is Mother or Father

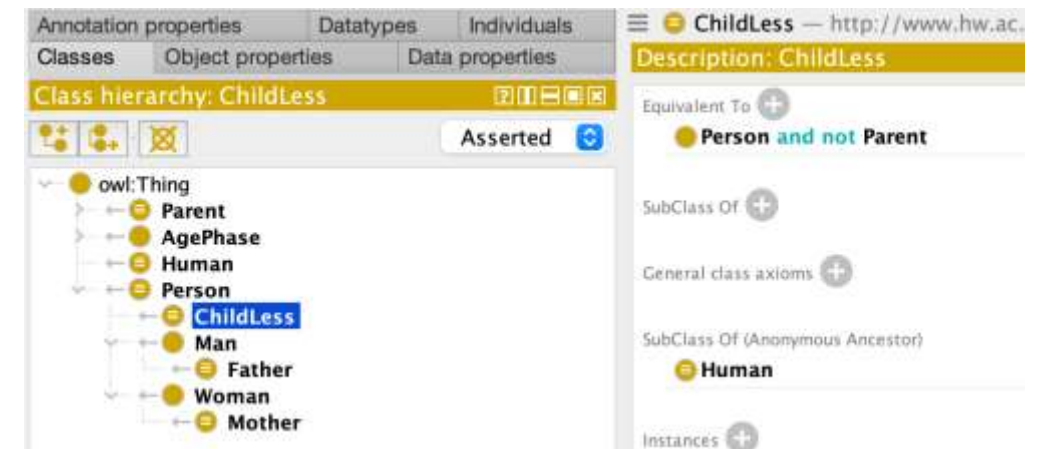
```
:Parent rdf:type owl:Class ;  
    owl:equivalentClass [ rdf:type owl:Class ;  
        owl:unionOf ( :Father  
            :Mother  
        )  
    ] ;
```



OWL: Complement classes (\neg)

*Person(x) and **not** Parent(x) \Leftrightarrow ChildlessPerson(x)*

- A complement class is the class of individuals that belong to one class and not to another
- Example, person who have no children are defined as the complement of
 - Person **and not** Parent



```
:ChildlessPerson rdf:type owl:Class ;  
    owl:equivalentClass [ owl:intersectionOf ( :Person  
        [ rdf:type owl:Class ;  
          owl:complementOf :Parent  
        ]  
    ) ;  
    rdf:type owl:Class  
] ;
```


OWL: Subclass of complex class

$$Parent(x) \text{ and } Man(x) \Rightarrow GrandFather(x)$$

- A class can be
- Individuals of also individual
- Example
 - A Grandfather

$$GrandFather(x) \Rightarrow Parent(x) \text{ and } Man(x)$$

- This expression is sufficient

$$GrandFather(x) \equiv Man(x) \wedge \exists y (hasChild(x, y) \wedge Parent(y))$$

- ✓ If
- ✗ If x is a Man AND a Parent \rightarrow x is NOT necessarily a GrandFather

:GrandFather

:Parent

Childless

Man

SubClass Of

Parent and Man

General class axioms

SubClass Of (Anonymous Ancestor)

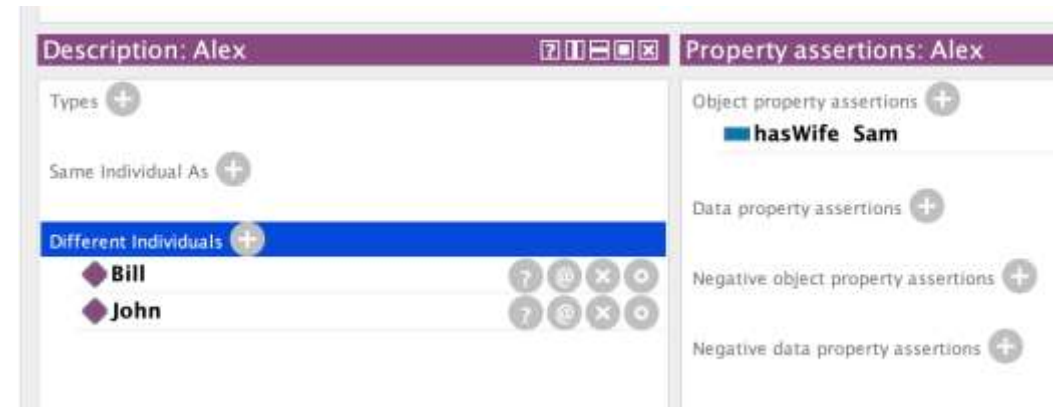
OWL: Enumerated class (owl:oneOf)

- Define a class by listing its exact members (a “closed list”).
- Example:
 - Bill, John and Mary are members of the class PartyGuests

[illegible]

OWL: Distinct individuals (owl:differentFrom)

- OWL **does NOT** assume different names = different entities (no “Unique Name Assumption”).
- Example, Alex and John might be considered the same
- To avoid this, we assert that they are different
 - Alex different from John and from Bill



```
[ rdf:type owl:AllDifferent ;  
  owl:distinctMembers ( :Alex  
                           :Bill  
                           )  
] .
```

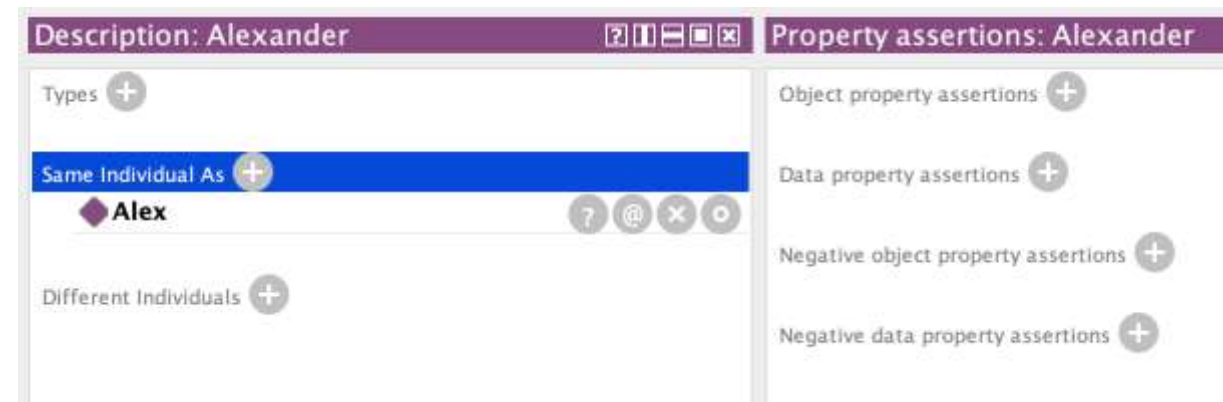
```
[ rdf:type owl:AllDifferent ;  
  owl:distinctMembers ( :Alex  
                           :John  
                           )  
] .
```

OWL: Same individuals ([owl:sameAs](#))

- With OWL we can assert that two individuals are the same
- Example: if Alex and Alexander are the same

```
:Alex rdf:type owl:NamedIndividual ;  
      owl:sameAs :Alexander ;  
      :hasWife :Sam ;
```

- [Owl:sameAs](#) combines all properties of two instances
 - The two become indistinguishable
- This might not be the behaviour sought for your application
 - In such a case use [skos:exactMatch](#) or [skos:closeMatch](#)



Property restrictions- existential quantification (some / \exists)

$$C(x) \Rightarrow \exists y, p(x, y)$$

- P some C = “there exists at least 1 value of property P that is in class C”

```
:Parent rdf:type owl:Class ;  
  owl:equivalentClass [  
    rdf:type owl:Class ;  
    owl:intersectionOf (  
      [ rdf:type owl:Class ;  
        owl:unionOf ( :Father :Mother )  
      ]  
      [ rdf:type owl:Restriction ;  
        owl:onProperty :hasChild ;  
        owl:someValuesFrom :Person  
      ]  
    )  
  ] .
```

- This is expressed as: *every parent **has at least one** child who is a person*

Description: Parent

Equivalent To +

●

 hasChild **some** Parent

●

 Father **or** Mother

SubClass Of +

?

Property restrictions- Universal quantification

‘only’ does NOT guarantee existence of children.

A HappyPerson with no stated children still satisfies: hasChild only HappyPerson.

$\forall y, p(x, y)$



- A person is happy only if their children are happy
- $\text{HappyPerson} \sqsubseteq \text{hasChild only HappyPerson}$
- $\text{HappyPerson}(x) \rightarrow \forall y (\text{hasChild}(x,y) \rightarrow \text{HappyPerson}(y))$
- This is expressed as: children of *happy person* *must all be happy*.

```
:HappyPerson rdf:type owl:Class ;  
  owl:equivalentClass [  
    owl:intersectionOf (  
      [ rdf:type owl:Restriction ;  
        owl:onProperty :hasChild ;  
        owl:allValuesFrom :HappyPerson  
      ]  
    )  
  ] .
```

Property restrictions – Closure (some + only)

- $P \text{ some } X$ = at least one P-value is in X
- $P \text{ only } X$ = all P-values (if any) are in X
- Together = **at least** one exists AND all are of class X
- Example:
 - $\text{HappyPerson} \sqsubseteq (\text{hasChild some HappyPerson}) \sqcap (\text{hasChild only HappyPerson})$
 - = A happy person has at least one child, and all their children are happy.



```
:HappyPerson rdf:type owl:Class ;
              owl:equivalentClass [ owl:intersectionOf ( [ rdf:type owl:Restriction ;
                                                                owl:onProperty :hasChild ;
                                                                owl:someValuesFrom :HappyPerson
                                                            ]
                                                            [ rdf:type owl:Restriction ;
                                                                owl:onProperty :hasChild ;
                                                                owl:allValuesFrom :HappyPerson
                                                            ]
                                                        ) ;
              rdf:type owl:Class
            ] ;
```

Property restrictions – Closure (some + only) cont.

- With using **only**:
 - **MeatLoversPizza** \sqsubseteq (hasTopping only Meat)
 - BUT a Plain Crust (no toppings) is technically a Meat Lovers pizza because it has "only meat".
- Correct version?
 - **MeatLoversPizza** \sqsubseteq (hasTopping some Meat) \sqcap (hasTopping only Meat)
 - Some: *You must have at least one meat topping.*
 - Only: *You are forbidden from having anything other than meat.*

Property restrictions- Restriction on individual (value/hasValue)

- P value a = To be in this group, you must be connected to 'a'.
- Example:
 - JohnChildren = people whose parent is John
 - *hasParent value John*
 - "Ali"
 - class: Italian
 - *madeIn*
 - "Gu"

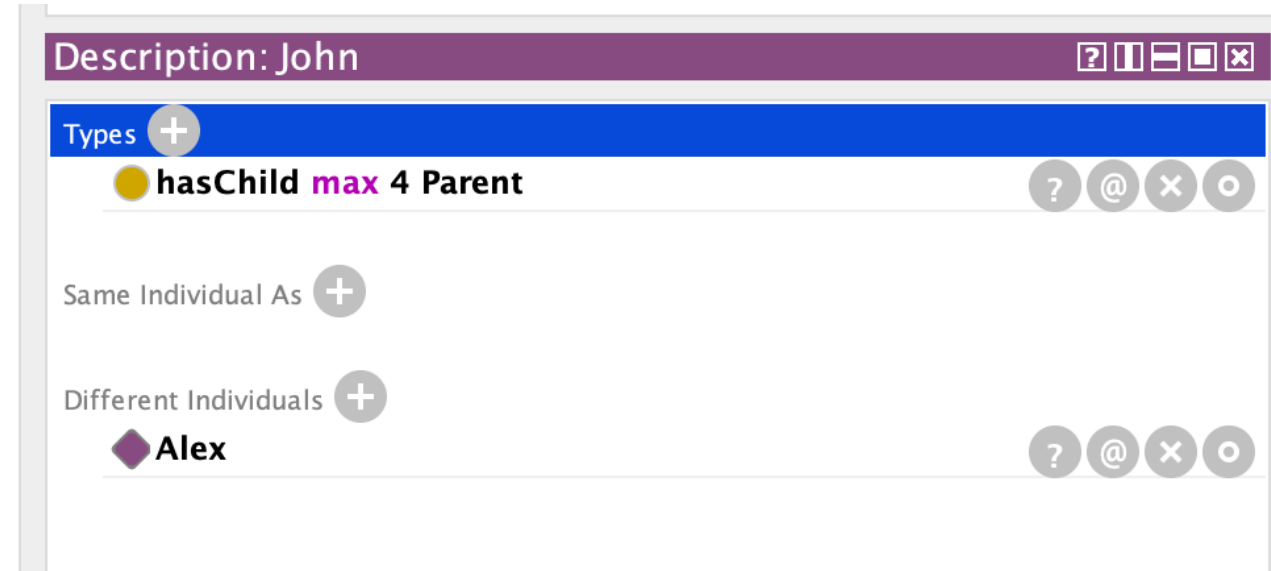


What the reasoner can infer (if using EquivalentTo)?

- ✓ If Mary hasParent John → Mary is a JohnChildren
- ✓ If Mary is a JohnChildren → Mary hasParent John

OWL: Cardinality restriction (max)

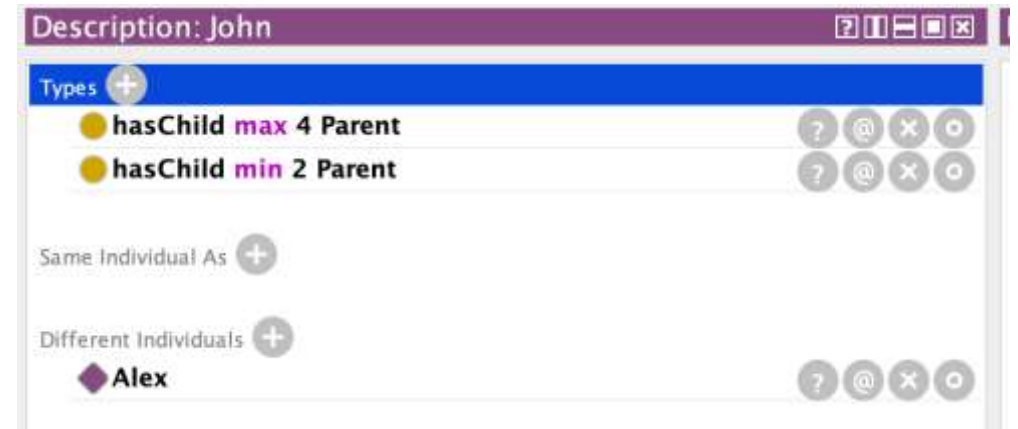
- For upper bound/limit.
- $P \text{ max } n \text{ C} = \text{at most } n$ **DIFFERENT/DISTINCT** values of property P are in class C
- Example:
 - John has at most 4 children who are parents
- Qualified vs unqualified:
 - *hasChild max 4*
 - at most 4 children (any type)
 - *hasChild max 4 Parent*
 - at most 4 children that are Parents



```
:John rdf:type owl:NamedIndividual ,  
[ rdf:type owl:Restriction ;  
  owl:onProperty :hasChild ;  
  owl:maxQualifiedCardinality "4"^^xsd:nonNegativeInteger ;  
  owl:onClass :Parent  
] ,
```

OWL: Cardinality restriction (min)

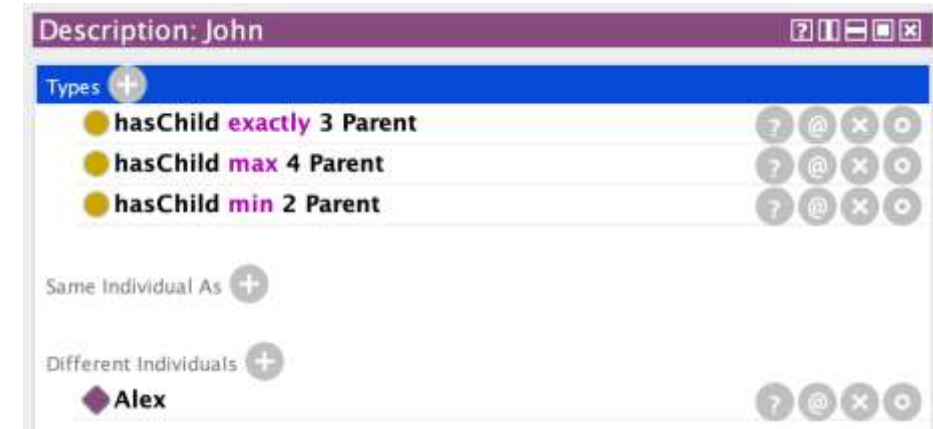
- $P \text{ min } n \text{ C}$ = **at least** n values of property P are in class C (= at least n **DIFFERENT** individuals in C)
- Example
 - John has **at least** 2 children who are parents
 - $\rightarrow \text{hasChild min 2 Parent}$
- Qualified vs unqualified?



```
:John rdf:type owl:NamedIndividual ,  
      [ rdf:type owl:Restriction ;  
        owl:onProperty :hasChild ;  
        owl:minQualifiedCardinality "2"^^xsd:nonNegativeInteger ;  
        owl:onClass :Parent  
      ] ,
```

OWL: Cardinality restriction (exactly)

- We can use *owl:qualifiedCardinality* to specify the **exact number** of individuals related by a certain property that also ***belong to a specific class***.
- $P \text{ exactly } n \ C = (P \text{ min } n \ C) \text{ AND } (P \text{ max } n \ C)$
 - exactly n **DIFFERENT** values of property P that are in class C
- Example
 - John has **exactly** 3 children who are of type Parent.
- Qualified vs unqualified.



Using exactly, min and max in an ontology increases its complexity

```
:John rdf:type owl:NamedIndividual ,  
      [ rdf:type owl:Restriction ;  
        owl:onProperty :hasChild ;  
        owl:qualifiedCardinality "3"^^xsd:nonNegativeInteger ;  
        owl:onClass :Parent  
      ] ,
```

OWL reasoning notes...

- Data: John has 3 children...
 - Child A
 - Child B
 - Child 3
- Question: Does John have 4 children?
- OWL/Semantic is under OWA.

OWL: Cardinality restriction (unqualified)

- Unqualified cardinality = counting WITHOUT a type constraint
- $P \text{ exactly } n$ = exactly n distinct values for property P (any type)
 - (similar idea for $P \text{ min } n$, $P \text{ max } n$)
- Example
 - Define for a “fully married man” that the number of wives is 4



OWL: Cardinality restriction (qualified vs unqualified)

Cardinality can count:

1. fillers of a **specific TYPE** (qualified), or
2. fillers of **ANY type** (unqualified)

Qualified cardinality (type matters):

- $\text{Person} \sqsubseteq \text{hasPet min 1 Cat}$

Unqualified cardinality (type does NOT matter):

- $\text{Person} \sqsubseteq \text{hasPet min 1}$

OWL: property characteristics - Inverse (owl:inverseOf)

- Edge reversal in a graph:
 - If p is the inverse of q , then:
 - $p(x, y) \leftrightarrow q(y, x)$
- Example
 - *hasHusband* is the inverse property of *hasWife*
 - *hasParent* inverseOf *hasChild*
 - $hasParent(Alice, Bob) \rightarrow hasChild(Bob, Alice)$
 - $hasChild(Bob, Alice) \rightarrow hasParent(Alice, Bob)$

Description: hasHusband

Equivalent To +

SubProperty Of +

hasSpouse

Inverse Of +

hasWife

```
:hasHusband rdf:type owl:ObjectProperty ;  
             rdfs:subPropertyOf :hasSpouse ;  
             owl:inverseOf :hasWife ;
```


OWL: property characteristics (symmetry/asymmetric)

Symmetric property (two-way):

- If $P(x, y)$

- the re
 - direct

- Example

- hasSp
 - ha

hasSpouse(Mary, John)

If `:John :hasWife :Mary`,
hasHusband inverseOf hasWife,
what can we infer???

```
:hasSpouse rdf:type owl:ObjectProperty ,  
            owl:SymmetricProperty ;
```

- hasChild is asymmetric

```
:hasChild rdf:type owl:ObjectProperty ;  
          owl:inverseOf :hasParent ;  
          rdf:type owl:AsymmetricProperty ;  
          rdfs:domain :Person ;  
          rdfs:range :Person ;
```

Characteristics: hasChild

functional
inverse functional
transitive
symmetric
asymmetric
reflexive
irreflexive

OWL: property characteristics (disjoint)

- Two properties P and Q are disjoint if they can NEVER hold for the same pair (x, y).
 - Formal: $\text{NOT} (P(x, y) \text{ AND } Q(x, y))$
- Example
 - *hasChild disjointWith hasSpouse*
 - hasChild and hasSpouse are disjoint
- So you cannot have:
 - hasChild(John, Mary) AND hasSpouse(John, Mary)
- What if?
 - hasChild(John, Mary) AND hasSpouse(John, Anna)

Description: hasChild

Equivalent To +

SubProperty Of +

Inverse Of +
hasParent

Domains (Intersection) +
Person

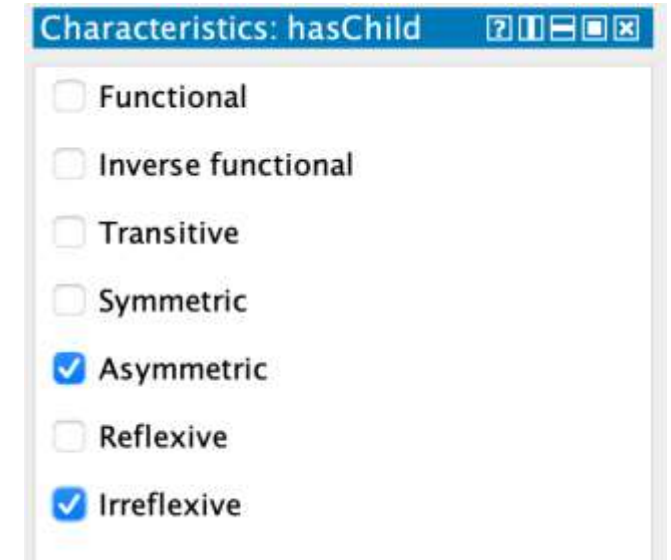
Ranges (Intersection) +
Person

Disjoint With +
hasSpouse

```
:hasChild rdf:type owl:ObjectProperty ;  
          owl:inverseOf :hasParent ;  
          rdf:type owl:AsymmetricProperty ;  
          rdfs:domain :Person ;  
          rdfs:range :Person ;  
          owl:propertyDisjointWith :hasSpouse ;
```

OWL: property characteristics (reflexive/irreflexive)

- A property is reflexive if the domain and range can be the same.
 - The property can be applied to yourself
 - For every individual x : $P(x, x)$
- Irreflexive is when the range and domain **cannot** be the same.
- Example: assuming there is only one John (same IRI)
 - *knows(John, John)* ✓
 - *isSameNationalityAs(John, John)* ✓
 - *hasChild(John, John)* is irreflexive !
 - *isTallerThan(John, John)*?



Characteristics: hasChild

- ☐ Functional
- ☐ Inverse functional
- ☐ Transitive
- ☐ Symmetric
- ☒ Asymmetric
- ☐ Reflexive
- ☒ Irreflexive

```
:hasChild rdf:type owl:ObjectProperty ;  
          owl:inverseOf :hasParent ;  
          rdf:type owl:AsymmetricProperty ,  
                owl:IrreflexiveProperty ;
```

OWL: property characteristics (functional vs. inverse functional)

- Functional means one individual from the domain can only be related to one individual from the range.
- Inverse functional is the opposite
- Example

- hasHusband is functional

```
:hasHusband rdf:type owl:ObjectProperty ;  
            rdfs:subPropertyOf :hasSpouse ;  
            owl:inverseOf :hasWife ;  
            rdf:type owl:FunctionalProperty ;
```

- hasWife is inverseFunctional is irreflexive

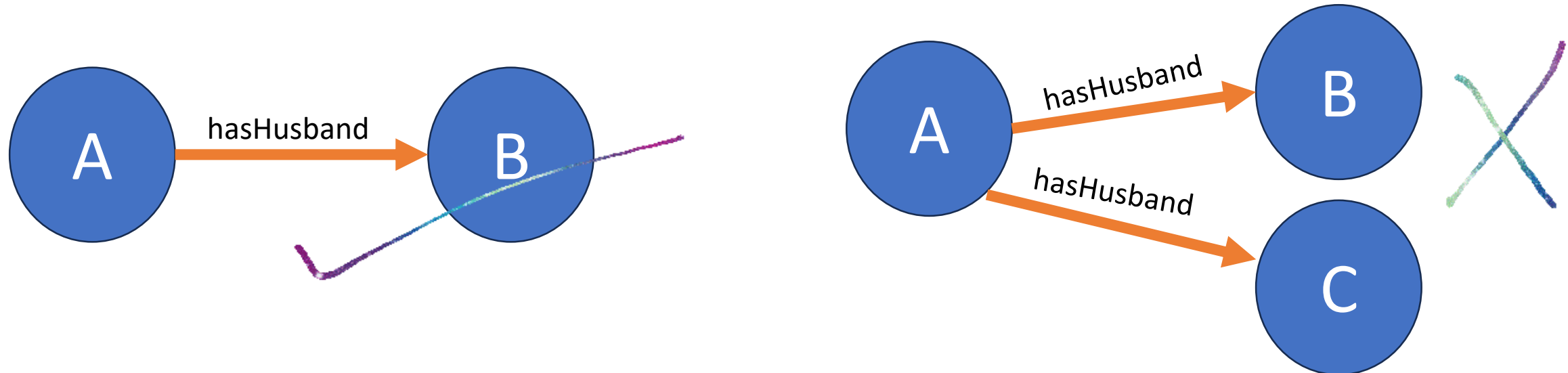
```
:hasWife rdf:type owl:ObjectProperty ;  
         rdfs:subPropertyOf :hasSpouse ;  
         rdf:type owl:InverseFunctionalProperty ,  
                 owl:AsymmetricProperty ;
```

The image shows two side-by-side windows from an OWL editor, likely Protégé, showing the configuration for property characteristics. The left window is titled 'Characteristics: hasHusband' and the right is 'Characteristics: hasWife'. Both windows have a list of checkboxes for different property characteristics.

Property	Functional	Inverse functional	Transitive	Symmetric	Asymmetric	Reflexive	Irreflexive
hasHusband	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
hasWife	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

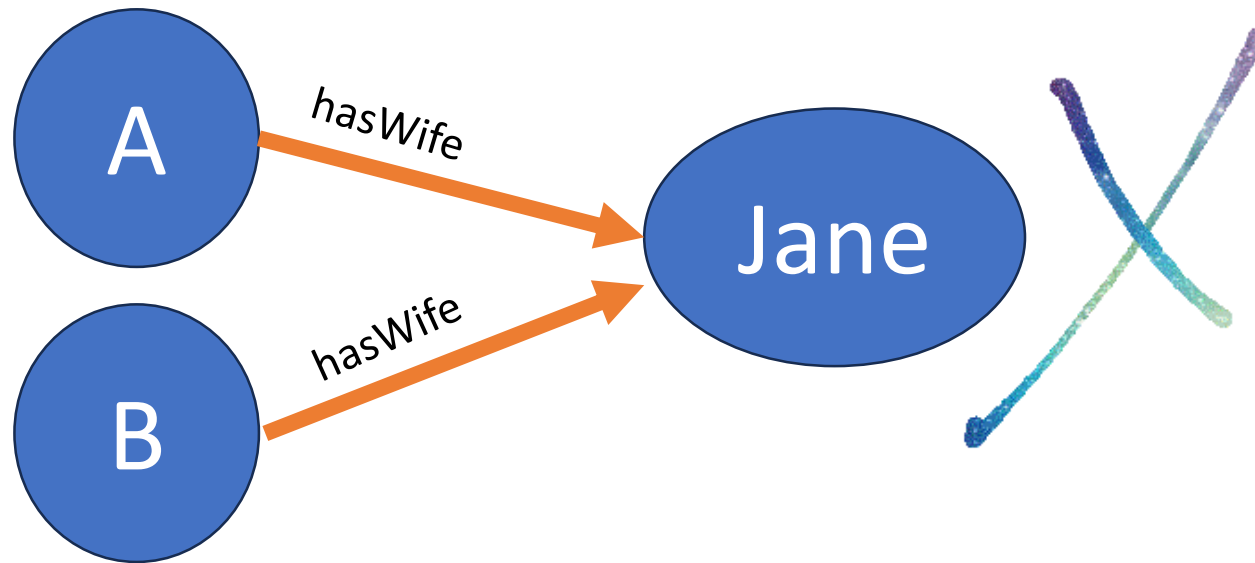
OWL: property characteristics (functional vs. inverse functional) cont.

- Functional = One person \rightarrow One value.
 - "Source" (the tail of the arrow) can only have **one** arrow coming out of it
- Inverse functional = One value \leftarrow One person
 - "Target" (the head of the arrow) can only have **one** arrow pointing into it
- *hasHusband* is **functional**



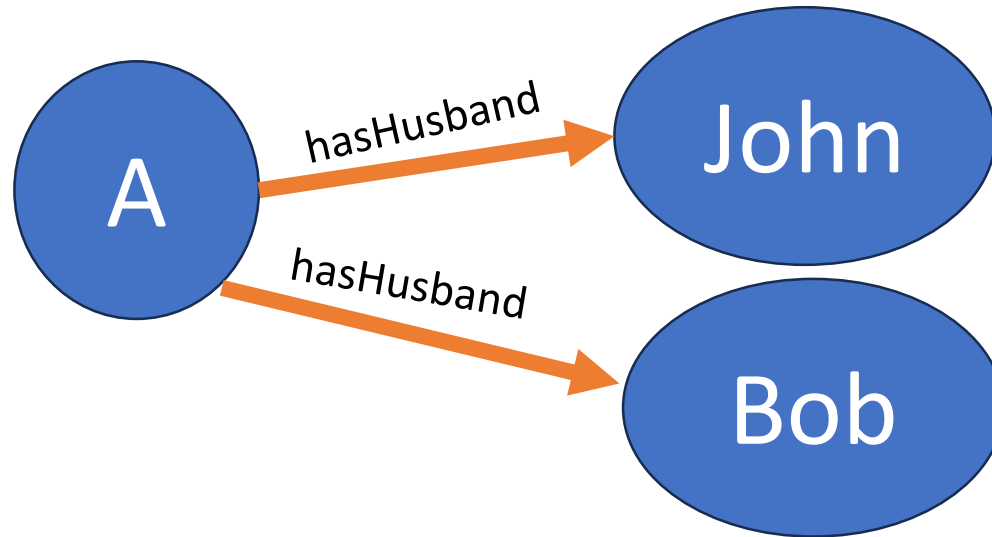
OWL: property characteristics (functional vs. inverse functional) cont.

- "Target" (the head of the arrow) can only have one arrow pointing into it
- If *hasWife* is ***inverse functional***...



OWL: property characteristics (functional vs. inverse functional) cont.

- *hasHusband* is functional



OWL: property characteristics (functional vs. inverse functional) cont.

If P is functional, then P is inverse functional too?

- Property: *hasBirthCity*
 - *Functional*? Yes! A person has only one birth city (Source \rightarrow 1 Target).
 - “John hasBirthCity KL”
 - *Inverse functional*? No! Millions of people can be born in the same city.

If P is inverse functional, then P is functional too?

- Property: *ownsCarWithPlate*
 - *Inverse Functional*? Yes! A specific license plate (the target) belongs to only one owner (the source). (1 Source \leftarrow Target).
 - “Zihau ownsCarWithPlate \rightarrow ABC123”
 - *Functional*? No! One person can own more than one cars with different plates.

OWL: property characteristics (functional vs. inverse functional) cont.

Then can we set both functional and inverse functional together?

- Yes! The 1:1 relationship.
- Property: *hasHusband* (in a strictly monogamous model).
- **Functional**: A wife has only one husband.
- **Inverse Functional**: A husband has only one wife.
- The Result? A perfect "marriage" of the two rules where 1 source matches exactly 1 target.

OWL: property characteristics (transitive)

- if **x** is related to **y**, and **y** is related to **z**, then **x** is related to **z**.
- Example:
 - isOlder:
 - *John isOlder Charlie*
 - *Charlie isOlder Bob*
 - Then... *John isOlder Bob*

```
:hasBrother rdf:type owl:ObjectProperty ;  
            rdfs:subPropertyOf owl:topObjectProperty ;  
            rdf:type owl:TransitiveProperty ;  
            rdfs:domain :Person ;  
            rdfs:range :Man ;
```

The screenshot shows a software interface for defining an OWL property. It is divided into two main panels: 'Characteristics' on the left and 'Description: hasBrother' on the right.

Characteristics Panel: This panel contains a list of checkboxes for property characteristics. The 'Transitive' checkbox is checked, while all others are unchecked.

- ☐ Functional
- ☐ Inverse functional
- ☒ Transitive
- ☐ Symmetric
- ☐ Asymmetric
- ☐ Reflexive
- ☐ Irreflexive

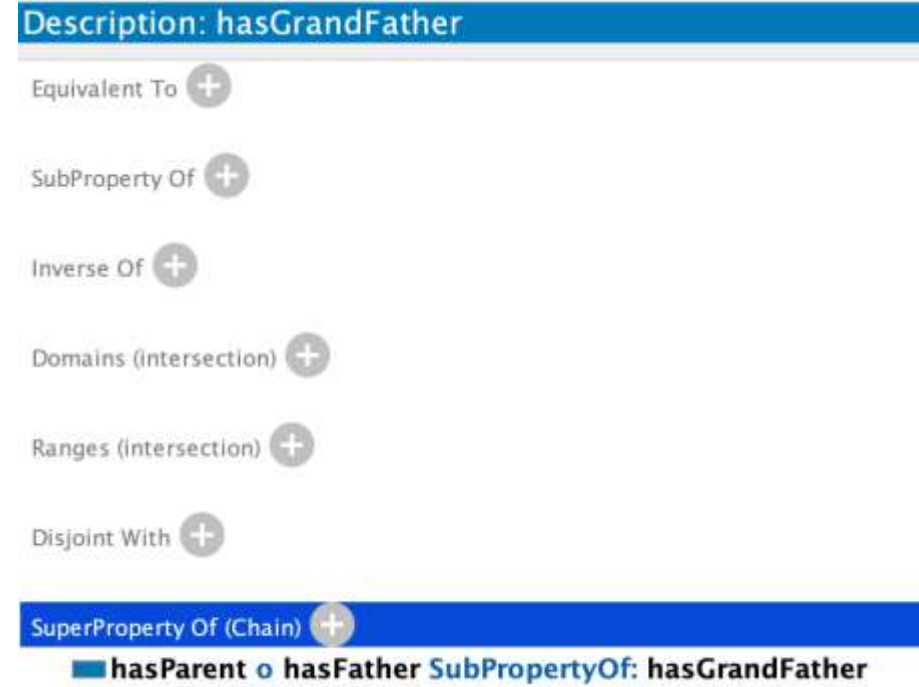
Description: hasBrother Panel: This panel shows the logical relationships and constraints for the 'hasBrother' property.

- Equivalent To:** A plus sign icon (+) is shown, indicating no equivalent properties are currently defined.
- SubProperty Of:** A plus sign icon (+) is shown, with 'owl:topObjectProperty' listed below it, indicating that 'hasBrother' is a subproperty of the top object property.
- Inverse Of:** A plus sign icon (+) is shown, indicating no inverse property is currently defined.
- Domains (intersection):** A plus sign icon (+) is shown, with 'Person' listed below it, indicating that the domain of 'hasBrother' is 'Person'.
- Ranges (intersection):** A plus sign icon (+) is shown, with 'Man' listed below it, indicating that the range of 'hasBrother' is 'Man'.

OWL: property characteristics (property chain)

- We can define a property as a chain (sequence) of other properties
 - If $p(x, y)$ AND $q(y, z)$ then $r(x, z)$
- Example, hasGrandFather can be defined as the chain of hasParent and hasFather
 - $\text{hasParent}(x, y)$ AND $\text{hasFather}(y, z) \Rightarrow \text{hasGrandFather}(x, z)$
- Note: Property chain is not “transitive”! It creates a NEW property!

```
:hasGrandFather rdf:type owl:ObjectProperty ;  
                owl:propertyChainAxiom ( :hasParent  
                                           :hasFather  
                                           ) ;
```



Data properties and restrictions

Data values may be untyped or typed (eg int, boolean, float etc). The types available will depend on tool support, but will include those specified in the [XSD](#) recommendation.

Constants can be expressed without type by just enclosing them in double quotes, or with type
`hasAge value "21"^^long`

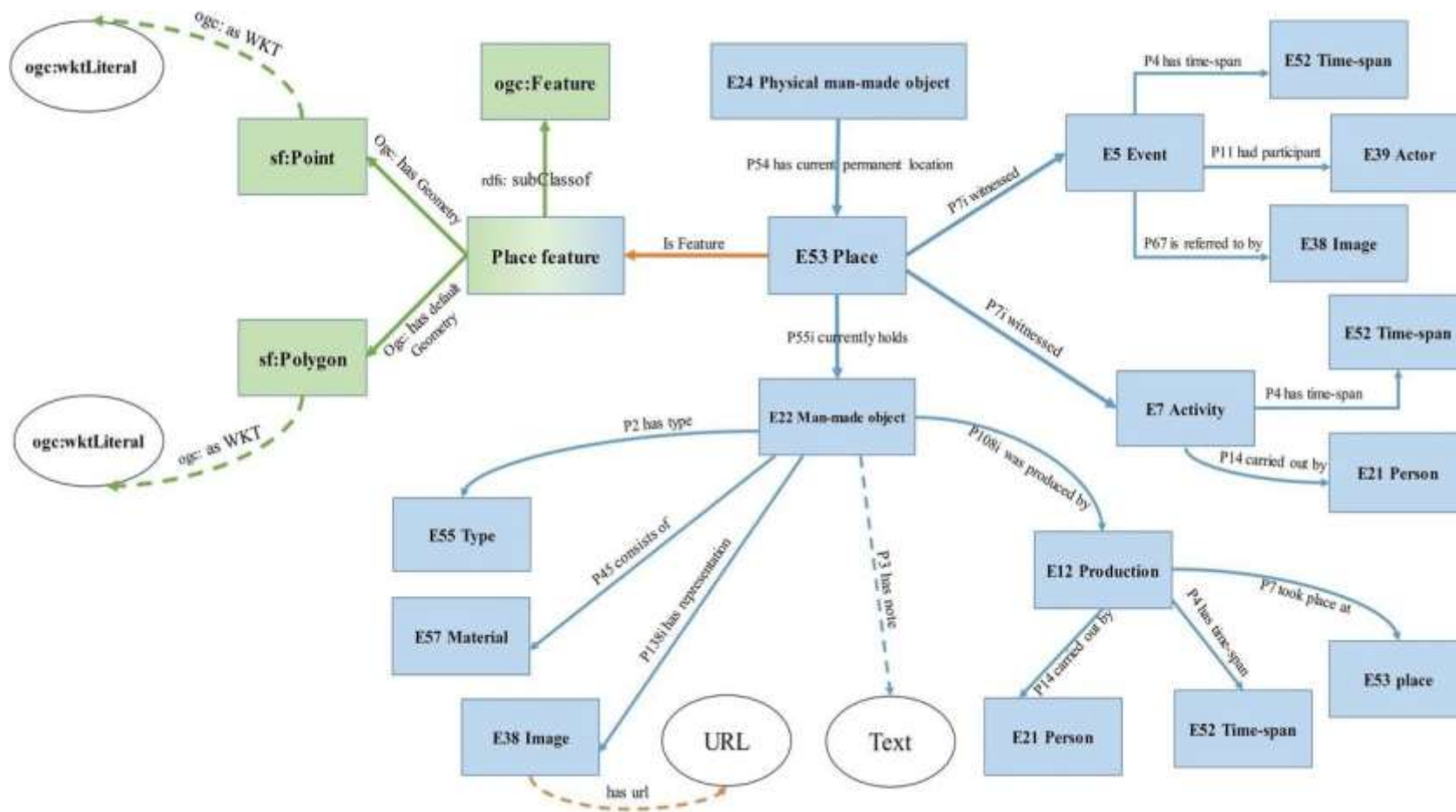
Usage of these datatypes in more general expressions is possible through their shortened name
`hasAge some int`

Several additional [XSD facets](#) can also be used to create new datatypes
`Person and hasAge some int[>= 65]`

Multiple facets can also be used. For example, when wishing to express numeric ranges
`Person and hasAge some int[>= 18, <= 30]`

XSD facet	Meaning
< x, <= x	less than, less than or equal to x (more info)
> x, >= x	greater than, greater than or equal to x (more info)
length x	For strings, the number of characters must be equal to x (more info)
maxLength x	For strings, the number of characters must be less than or equal to x (more info)
minLength x	For strings, the number of characters must be greater than or equal to x (more info)
pattern regexp	The lexical representation of the value must match the regular expression, regexp (more info)
totalDigits x	Number can be expressed in x characters (more info)
fractionDigits x	Part of the number to the right of the decimal place can be expressed in x characters (more info)

Please note: some xsd datatypes and facets may not be supported by particular reasoners at this current time. A [report on the current status of reasoner implementations](#) is available



- How can Knowledge Graphs (KGs) enhanced Large Language Models (LLMs)?
- How can LLMs support and enhance Knowledge Graphs?

LLMs Empowered by KGs

Knowledge injection:

- Limitations of LLMs:
 - generate inaccurate or nonsensical information (hallucinations),
 - Lack of domain specific knowledge

Knowledge-Augmented Language Model PromptING (KAPING)

- Retrieved relevant facts from a KG.
- Add these facts to the user's input question.
- Construct a richer prompt for the LLM.

(a) Language Model Prompting w/o Knowledge Augmentation

[Prompt]

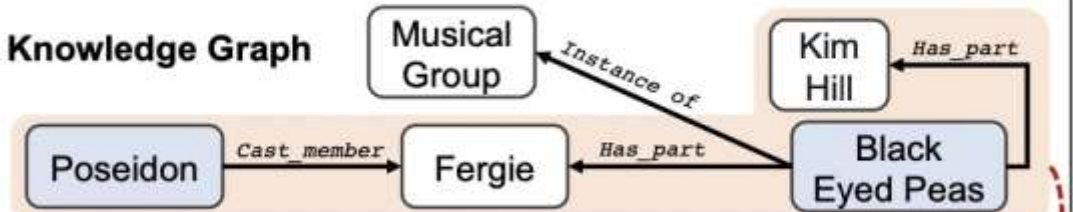
Question: Which member of Black Eyed Peas appeared in Poseidon?
Answer:

[Generated Answer]

Tariq Ali

(b) Knowledge-Augmented Language Model Prompting

Knowledge Graph



[Prompt]

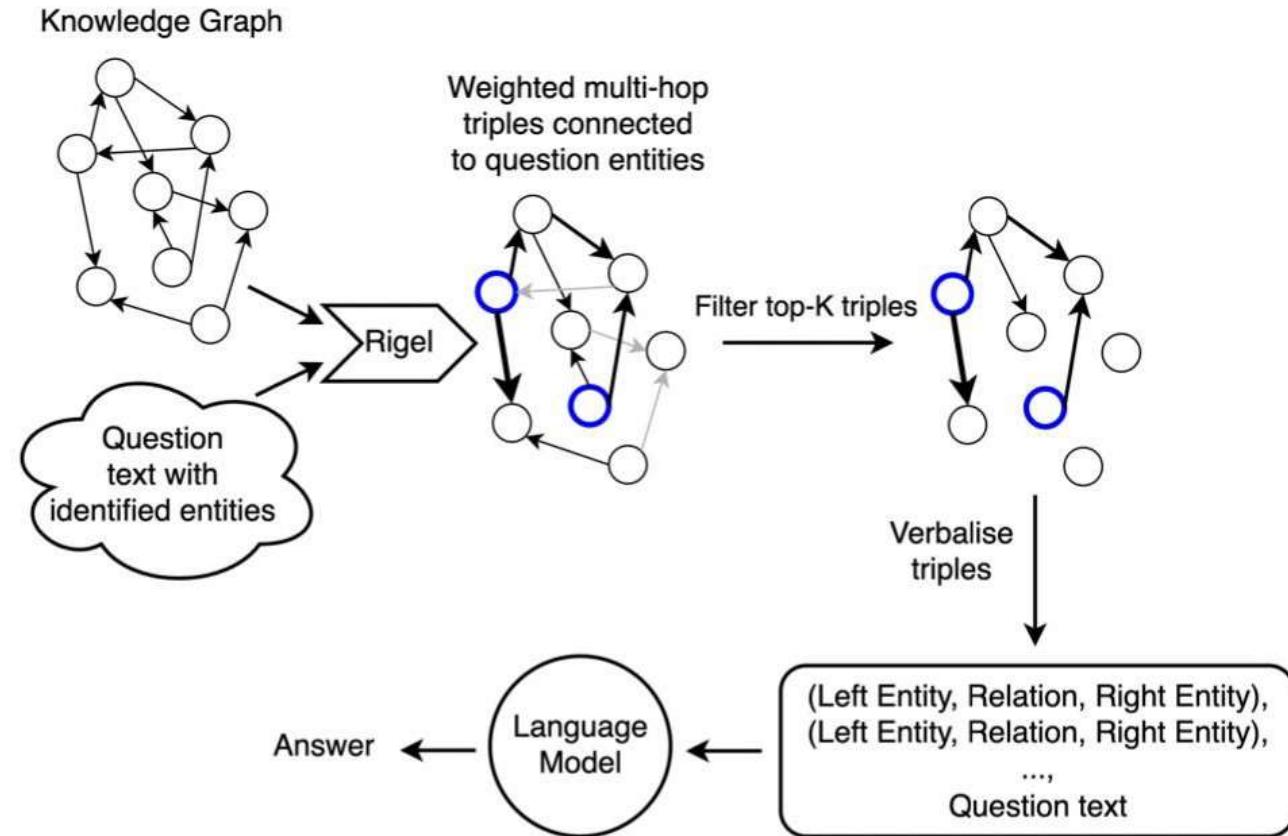
Below are the facts that might be relevant to answer the question: (Black Eyed Peas, has part, Fergie), (Black Eyed Peas, has part, Kim Hill), (Poseidon, cast member, Fergie)
Question: Which member of Black Eyed Peas appeared in Poseidon?
Answer:

[Generated Answer]

Fergie

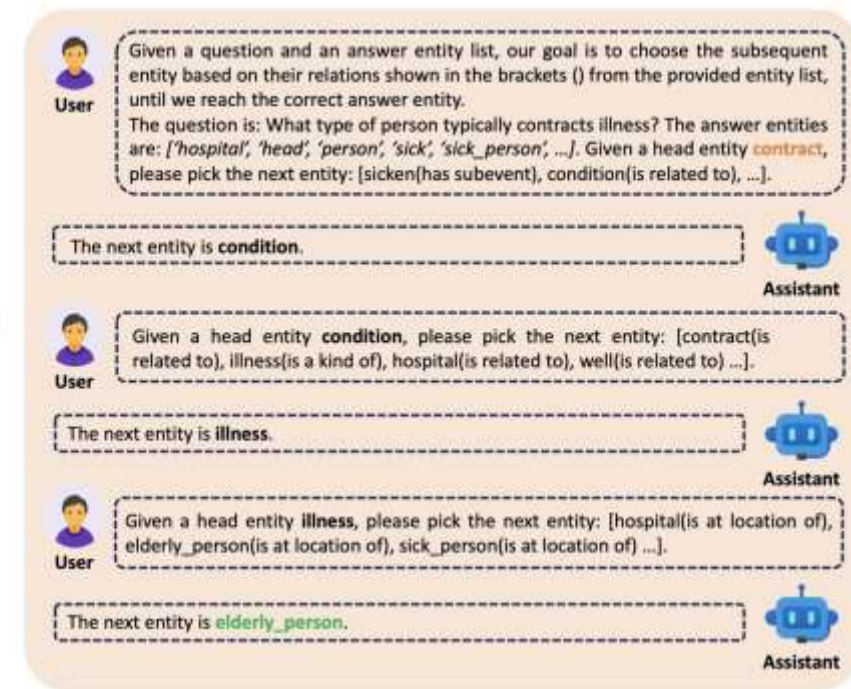
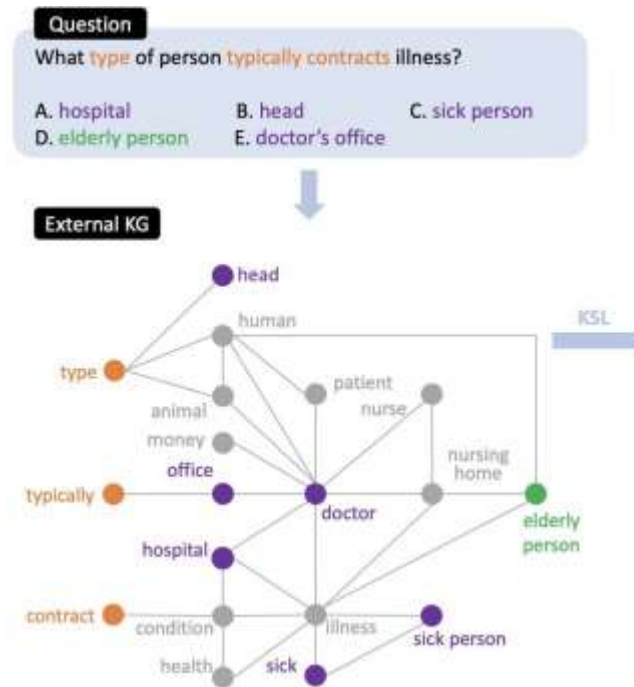
LLMs Empowered by KGs

- LLMs often struggle with complex, multi-step reasoning because they rely on probabilistic text generation.
- **Knowledge Graph-augmented Language Models for Complex Question Answering (KGQA)**
 - The facts from the KG were weighted/ ranked by a KGQA before being fed into the LLM



LLMs Empowered by KGs

- **Knowledge Solver:** teaches LLMs to traverse KGs in a multi-hop way to reason the answer to a question.
- For given question answer choices pair [q, A], encode G_{sub} into text prompt TK to inject knowledge into LLMs.
- G_{sub} contains all nodes on the k-hop paths between nodes in V_q and V_a .



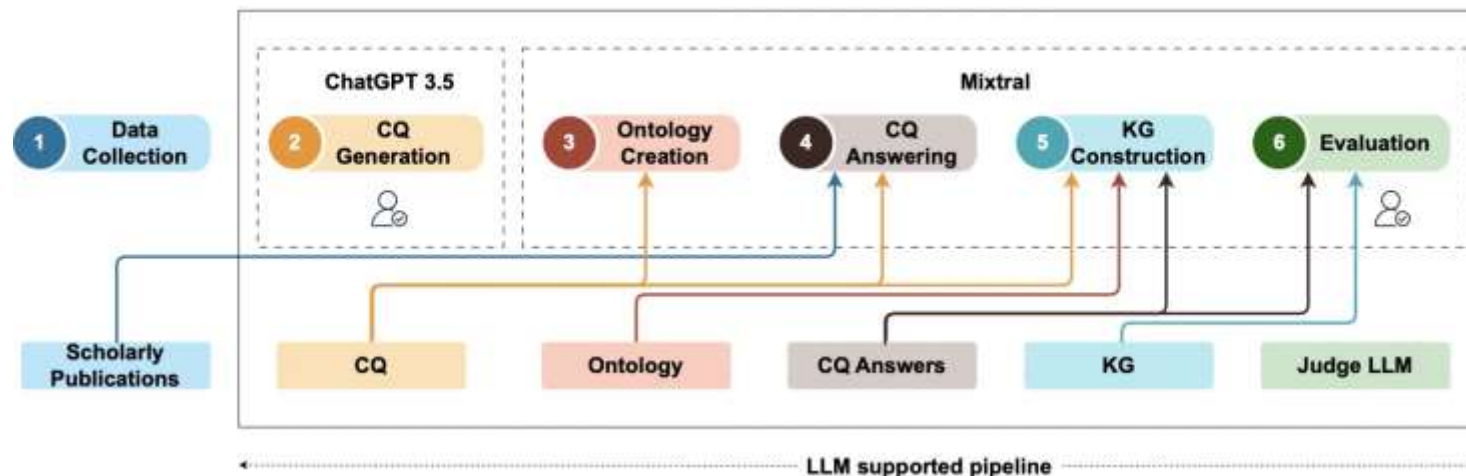
KGs Empowered by LLMs

Knowledge graph construction.

- time-consuming and costly construction process of KGs

An LLM supported approach to *ontology* and *knowledge graph* construction

- **CQ (competency questions), generation:** prompt ChatGPT-3.5 to get abstract-level questions
- **Extract all concepts and their relationships** from the CQs.
- **Constructed an ontology** for describing information using an in-context example containing a basic ontology structure
- **CQ Answering:** retrieved answers for all the CQs
- **KG generation:** prompt the LLM to extract key entities, relationships, and concepts from the answers and map them onto the ontology to generate the KG.



KGs Empowered by LLMs

Class Hierarchy

- owl:Thing
 - prov:Activity
 - TrainingProcedure
 - Deployment
 - FineTuning
 - ModelSelectionProcess
 - PostProcessing
 - PreprocessingStep
 - prov:Entity
 - Model
 - Architecture
 - Bias
 - BiasAddressing
 - Consideration
 - ConvergenceCriteria
 - DataFormat
 - DatasetVersion
 - DecisionMakingProcess
 - EthicalImplication
 - Explanation
 - HardwareInfrastructure
 - Hyperparameter
 - Initialization
 - InputData
 - LearningRateSchedule
 - Method
 - Metric
 - NumberOfModels
 - OptimizationAlgorithm
 - PredictionClassification
 - PrivacySecurityMeasure
 - RepositoryLink
 - Reproducibility
 - SensitiveData
 - SoftwareFrameworkLibrary
 - Source
 - StateOfTheArt
 - Tool
 - TransformationAugmentation
 - Transparency
 - UncertaintyConfidence
 - UpdateFrequency
 - VersioningStrategy
 - WeightConfiguration
 - prov:Process
 - DeepLearningPipeline

Object Property Hierarchy

- owl:topObjectProperty
 - addresses
 - builtWith
 - capturesUncertainty
 - deployedOn
 - discusses
 - documentsUpdates
 - explains
 - generates
 - handlesSensitively
 - hasAnnotationLabel
 - hasArchitecture
 - hasConsideration
 - hasConvergenceCriteria
 - hasDataFormat
 - hasHyperparameter
 - hasLearningRateSchedule
 - hasNumberOfModels
 - hasPostProcessing
 - hasRepositoryLink
 - hasSource
 - hasTransformationAugmentation
 - hasTransparency
 - hasVersioningStrategy
 - hasWeightConfiguration
 - implements
 - involves
 - isFineTunedWith
 - isInitializedWith
 - isStateOfTheArt
 - managesDatasetVersion
 - provides
 - runsOn
 - selectedBy
 - sufficientToReproduce
 - takesIntoAccount
 - updatedByRetraining
 - usedDifferently
 - usedFor
 - usedInModel
 - usesMethodTool
 - usesOptimizationAlgorithm

Object Property Description

Annotations

- rdfs:label
- hasConvergenceCriteria
- rdfs:comment
- A relation between a training procedure and its convergence criteria.

Equivalent To

- TrainingProcedure

SubProperty Of

- ConvergenceCriteria

Inverse Of

-

Domains (Intersection)

- TrainingProcedure

Ranges (Intersection)

- ConvergenceCriteria

Disjoint With

-

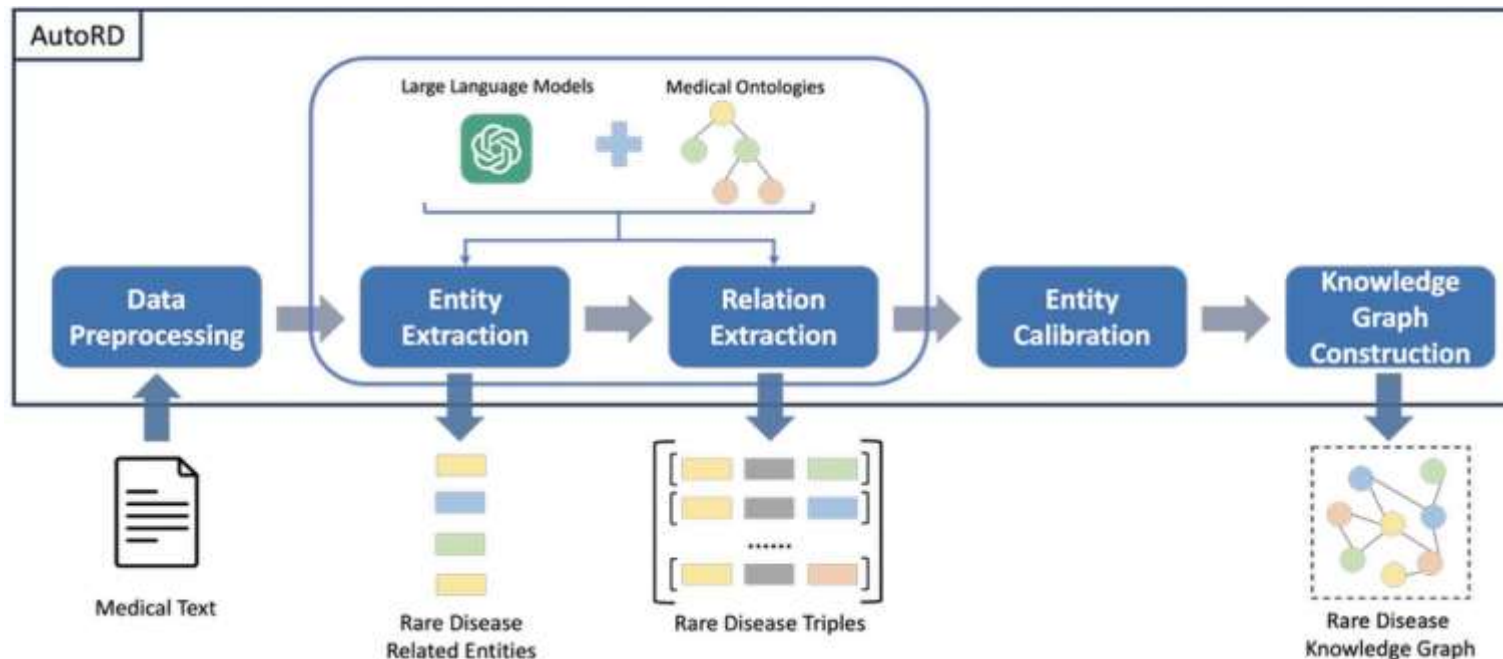
SuperProperty Of (Chain)

-

Provenance is information about entities, activities, and people involved in producing a piece of data or thing, which can be used to form assessments about its quality, reliability or trustworthiness.

KGs Empowered by LLMs

AutoRD: An Automatic and End-to-End System for Rare Disease Knowledge Graph Construction Based on Ontology-enhanced Large Language Models



KGs Empowered by LLMs

Extract More Terms	Extract Entities	Extract Relations	Calibrate Entities
<pre>### Task: (Extract entities: "anaphor", "medical_term"...)</pre> <p>## Definition:</p> <p>## Entity:</p> <p>(Define entities, including "rare_disease", "disease", "symptom_and_sign", "anaphor", "medical_term".)</p> <p>### Notice:</p> <p>(Remind the model of some considerations...)</p> <p>(Provide extracted "medical_terms".)</p> <p>{medical_terms}</p> <p>### Input Text:</p> <p>(Provide text.)</p> <p>{text}</p> <p>### Output format</p> <p>## Entity Representation:</p> <p>(Define entity representation.)</p> <p>## Your output should be a single JSON object in the following format:</p> <p>(Define the format of response.)</p> <p>### Output:</p>	<pre>### Task: (Extract entities: "rare_disease", "disease", "symptom_and_sign", "anaphor"...)</pre> <p>## Definition:</p> <p>## Entity:</p> <p>(Define entities, including "rare_disease", "disease", "symptom_and_sign", "anaphor".)</p> <p>### Notice:</p> <p>(Remind the model of some considerations...)</p> <p>### Examples</p> <p>Here are some examples of input text and target entities:</p> <p>{examples}</p> <p>### Input (Give Passage): {text}</p> <p>### Extracted Medical Terms: {medical_terms}</p> <p>### Extracted Anaphor: {anaphor}</p> <p>### Rare Disease Knowledge: {rare_disease_knowledge}</p> <p>### Output format</p> <p>## Entity Representation:</p> <p>(Define entity representation.)</p> <p>## Your output should be a single JSON object in the following format:</p> <p>(Define the format of response.)</p> <p>### Output:</p>	<pre>### Task: (Extract relations: "produces", "increases_risk_of", "is_a", "is_acron", "is_synon", "anaphora"...)</pre> <p>## Definition:</p> <p>## Entity:</p> <p>(Define entities, including "rare_disease", "disease", "symptom_and_sign", "anaphor".)</p> <p>## Relation:</p> <p>(Define relations, including "produces", "increases_risk_of", "is_a", "is_acron", "is_synon", "anaphora".)</p> <p>### Notice:</p> <p>(Remind the model of some considerations...)</p> <p>### Examples</p> <p>Here are some examples of input text and target entities:</p> <p>{examples}</p> <p>### Input (Give Passage): {text}</p> <p>### Extracted Entities: {entities}</p> <p>### Rare Disease Knowledge: {rare_disease_knowledge}</p> <p>### Output format</p> <p>## Entity Representation:</p> <p>(Define entity representation.)</p> <p>## Relation Representation:</p> <p>(Define relation representation.)</p> <p>## Your output should be a single JSON object in the following format:</p> <p>(Define the format of response.)</p> <p>### Output:</p>	<pre>### Task: (Verify all extracted entities and relations...)</pre> <p>## Definition:</p> <p>## Entity:</p> <p>(Define entities, including "rare_disease", "disease", "symptom_and_sign", "anaphor".)</p> <p>## Relation:</p> <p>(Define relations, including "produces", "increases_risk_of", "is_a", "is_acron", "is_synon", "anaphora".)</p> <p>### Notice:</p> <p>(Remind the model of some considerations...)</p> <p>### Input (Give Passage): {text}</p> <p>### Extracted Entities: {entities}</p> <p>### Extracted Relations: {relations}</p> <p>### Output format</p> <p>## Entity Representation:</p> <p>(Define entity representation.)</p> <p>## Relation Representation:</p> <p>(Define relation representation.)</p> <p>## Your output should be a single JSON object in the following format:</p> <p>(Define the format of response.)</p> <p>### Output:</p>

This figure presents the simplified content of all prompts. The black text represents the original text of the instructions. Grey text indicates a summary of each part of the instructions. Blue text highlights the prompt slots, where external information and inputs can be inserted.

KGs Empowered by LLMs

Automated Construction of Theme-specific Knowledge Graphs

Problem description: Given a specific theme and a set of documents D with each document $d \in D$ describing relevant content about the theme, our task aims to extract the theme-related knowledge triples from D

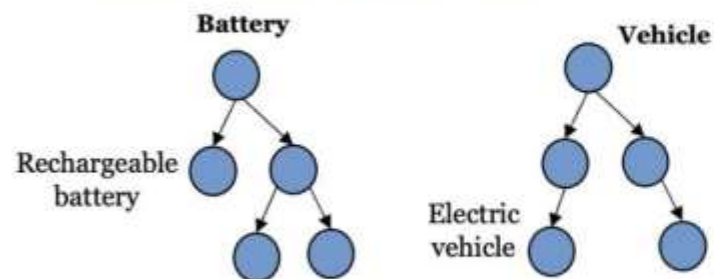
Example (“EV battery” Theme KG construction). Given the theme “EV-battery” and the following text:

“Deep cycle batteries are used to provide continuous electricity to run electric vehicles like forklifts”, the output of theme-specific knowledge graph construction may include the following possible knowledge triples: *(deep cycle batteries, provide, continuous electricity), (deep cycle batteries, be power source of, electric vehicles), (deep cycle batteries, be power source of, forklifts), (electric vehicles, include, forklifts).*

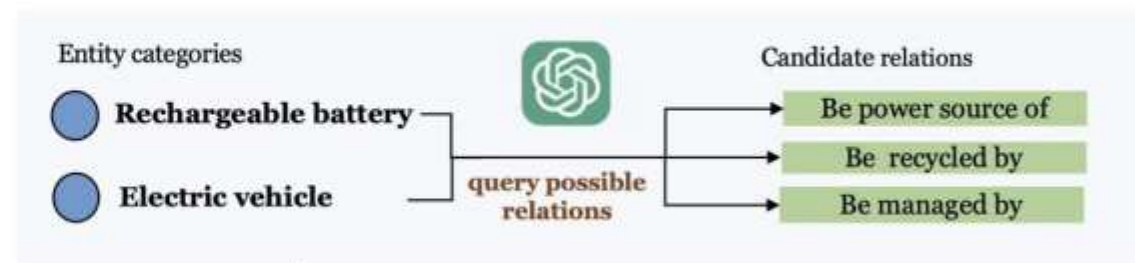
KGs Empowered by LLMs

Ontology Construction (Theme: Electric Vehicle Battery)

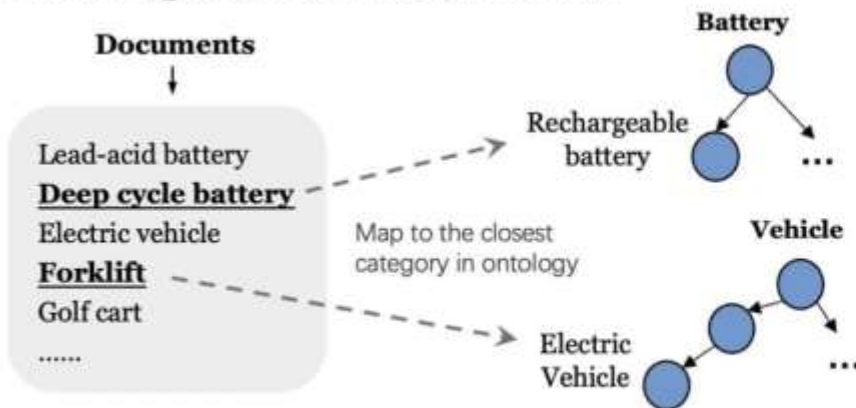
Entity Ontology: from Wiki



Relation Ontology: by LLMs

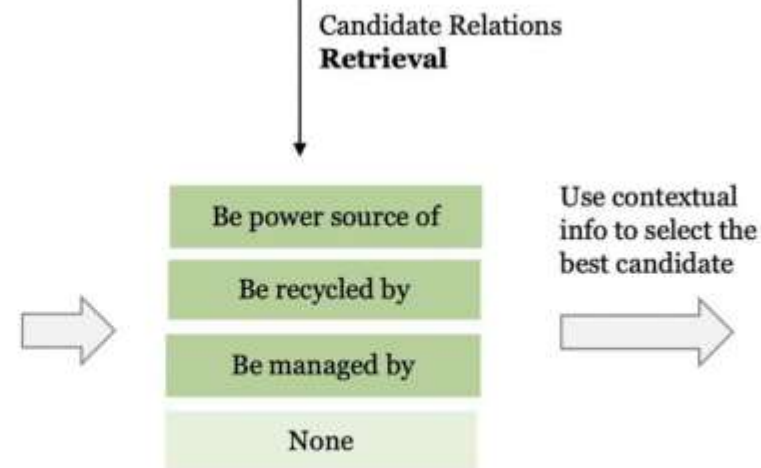


Theme-specific KG Construction

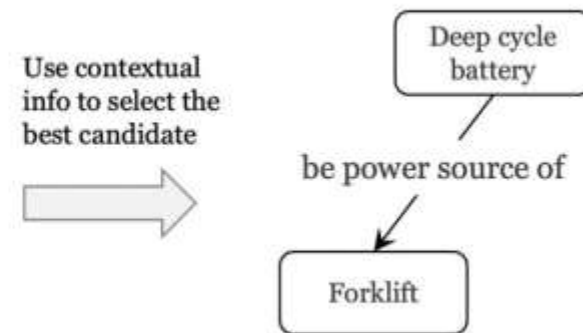


1. Entity Recognition

2. Entity Typing



3. Candidate Relations Retrieval



4. Relation Extraction