Higher Dimensional Datasets, version 10

Load packages.

```
In [1]: require(data.table)
    require(deSolve)
    require(magrittr)
    require(randtoolbox)

Loading required package: data.table
    Loading required package: deSolve
    Loading required package: magrittr
    Loading required package: randtoolbox
    Loading required package: rngWELL
    This is randtoolbox. For an overview, type 'help("randtoolbox")'.
```

Function to generate simulations.

```
In [2]: | # Create a multivariate function with specified properties:
             tmax: maximum time
             multiplicities: number of correlations each parameter has
             degrees: polynomial degree of each parameter
             dimension: the dimension of the output
             returns a multivariate function of the vector of parameters and t
         ime
         makeGenerator <- function(multiplicities, degrees, dimension) {</pre>
             single <- function(degree) {</pre>
               x0 <- runif(1)
               z0 <- runif(1)
               function(x) {
                   if (x < x0)
                       0
                   else
                       z0 * (x - x0)^degree
               }
             }
             locations <- lapply(multiplicities, function(m) sample(1:dimensio)</pre>
         n, m, replace=TRUE))
             functions <- lapply(degrees, single)</pre>
             start <- runif(dimension, -0.25, 0.75)
             coefs <- matrix(runif(dimension^2, -0.25, 0.75), dimension, dimen</pre>
             shift <- matrix(runif(dimension^2, -0.25, 0.75), dimension, dimen
         sion)
             function(x, ts) {
                 z <- rep(0, dimension)</pre>
                 for (i in 1:length(locations))
                     for (j in locations[[i]])
                          z[j] \leftarrow z[j] + functions[[i]](x[i])
                 ode(start, ts, function(t, y, params) {list((coefs %*% y) * z
         * (1 - ((shift %*% y) * z)))})
         }
```

Reproducible random numbers.

```
In [3]: RNGkind("Mersenne-Twister", "Inversion", "Rejection")
In [4]: set.seed(46)
```

Create and save timeseries.

```
In [5]: n <- 10000
In [6]: ts <- seq(0, 3, 0.2)
         ts
         0 0.2 0.4 0.6 0.8 1 1.2 1.4 1.6 1.8 2 2.2 2.4 2.6 2.8 3
In [7]: for (m \text{ in } c(3, 20))
             for (k in c(3, 20))
                  if (m != 3 || k != 3) {
                      f.multiplicities <- sample(1:5, m, replace=TRUE)</pre>
                      f.degrees <- sample(0:3, m, replace=TRUE)</pre>
                      f <- makeGenerator(f.multiplicities, f.degrees, k)</pre>
                      xs <- sobol(n, m)</pre>
                      colnames(xs) <- paste("x", 1:m, sep="")</pre>
                      rownames(xs) <- 1:n</pre>
                      ys <- NULL
                      for (i in 1:n) {
                          x < -xs[i, ]
                           if (m == 3)
                               y < -f(x, 10 * ts)
                          else
                               y \leftarrow f(x, ts)
                          ys <- rbind(ys, data.table(case=i, y))</pre>
                      }
                      xs <- data.table(case = 1:n, xs)</pre>
                      colnames(ys) <- c("case", "time", paste("y", 1:k, sep=""</pre>
         ))
                      write.table(xs, file=paste("xs-", m, "x", k, "-v10.csv",
         sep=""), sep=",", quote=FALSE, row.names=FALSE)
                      write.table(ys, file=paste("ys-", m, "x", k, "-v10.csv",
         sep=""), sep=",", quote=FALSE, row.names=FALSE)
```

```
time
                                       y1
                                                           y2
     case
                        : 0.0
                                        :-0.2229
                                                            :0.02939
Min.
       :
             1
                 Min.
                                 Min.
                                                    Min.
1st Qu.: 2501
                 1st Qu.: 7.5
                                 1st Qu.:-0.2229
                                                    1st Qu.:0.02939
Median: 5000
                 Median :15.0
                                 Median :-0.2229
                                                    Median :0.02939
Mean
       : 5000
                 Mean
                        :15.0
                                 Mean
                                         :-0.2229
                                                    Mean
                                                            :0.02939
3rd Qu.: 7500
                 3rd Qu.:22.5
                                 3rd Qu.:-0.2229
                                                    3rd Qu.:0.02939
       :10000
                        :30.0
                                 Max.
                                         :-0.2229
                                                    Max.
                                                            :0.02939
Max.
                 Max.
      у3
                        y4
                                            у5
                                                              у6
Min.
       :0.1046
                  Min.
                         :-0.1258
                                     Min.
                                             :0.1668
                                                        Min.
                                                               :0.1705
1st Qu.:0.1046
                  1st Qu.:-0.1258
                                     1st Qu.:0.1668
                                                        1st Qu.:0.1705
Median :0.1046
                  Median :-0.1258
                                     Median :0.1668
                                                        Median :0.1705
Mean
       :0.1046
                  Mean
                          :-0.1258
                                     Mean
                                             :0.1668
                                                        Mean
                                                               :0.1709
3rd Qu.:0.1046
                  3rd Qu.:-0.1258
                                     3rd Qu.:0.1668
                                                        3rd Qu.:0.1705
                          :-0.1258
Max.
       :0.1046
                  Max.
                                     Max.
                                             :0.1668
                                                        Max.
                                                               :0.3275
      у7
                          у8
                                             у9
                                                              y10
Min.
       :-0.07119
                    Min.
                            :0.5788
                                      Min.
                                              :0.2749
                                                         Min.
                                                                :0.7372
1st Qu.:-0.07119
                    1st Qu.:0.5788
                                      1st Qu.:0.2749
                                                         1st Qu.:0.7372
Median :-0.07119
                                                         Median :0.7372
                    Median :0.5788
                                      Median :0.2749
       :-0.07096
                    Mean
                            :0.5788
                                      Mean
                                              :0.4511
                                                         Mean
                                                                :0.7372
Mean
3rd Qu.:-0.07119
                    3rd Qu.:0.5788
                                      3rd Qu.:0.3791
                                                         3rd Qu.:0.7372
Max.
       : 0.02512
                    Max.
                            :0.5788
                                      Max.
                                              :3.0931
                                                         Max.
                                                                :0.7372
                       y12
                                           y13
                                                              y14
     y11
                          :0.04645
                                             :0.09504
Min.
       :0.4623
                  Min.
                                     Min.
                                                         Min.
                                                                :0.2806
                  1st Qu.:0.04645
1st Qu.:0.4623
                                     1st Qu.:0.09504
                                                         1st Qu.:0.2806
Median :0.4623
                  Median :0.04645
                                     Median :0.09504
                                                         Median :0.2806
Mean
       :0.4623
                  Mean
                          :0.04676
                                     Mean
                                             :0.09504
                                                         Mean
                                                                :0.2811
3rd Qu.:0.4623
                  3rd Qu.:0.04645
                                     3rd Qu.:0.09504
                                                         3rd Qu.:0.2806
       :0.4623
                          :0.14906
Max.
                  Max.
                                     Max.
                                             :0.09504
                                                         Max.
                                                                :0.3003
     y15
                       y16
                                         y17
                                                            y18
                          :0.2917
                                                              :-0.02132
Min.
       :0.4125
                  Min.
                                            :0.0911
                                                      Min.
                                    Min.
1st Qu.:0.4125
                  1st Qu.:0.2917
                                    1st Qu.:0.0911
                                                       1st Qu.:-0.02132
Median :0.4125
                  Median :0.2917
                                    Median :0.0911
                                                      Median :-0.02132
Mean
       :0.4125
                  Mean
                          :0.2917
                                    Mean
                                            :0.0911
                                                      Mean
                                                              :-0.02132
3rd Qu.:0.4125
                  3rd Qu.:0.2917
                                    3rd Qu.:0.0911
                                                       3rd Qu.:-0.02132
       :0.4125
                          :0.2917
                                            :0.0911
                                                              :-0.02132
Max.
                  Max.
                                    Max.
                                                      Max.
     y19
                         v20
Min.
       :-0.03287
                    Min.
                            :0.5407
1st Qu.:-0.03287
                    1st Qu.:0.5407
Median :-0.03287
                    Median :0.5407
       :-0.03287
                            :0.6351
Mean
                    Mean
3rd Qu.:-0.03287
                    3rd Qu.:0.5818
       :-0.03287
                            :2.5931
Max.
                    Max.
```

In [9]: fread("ys-20x3-v10.csv") %>% summary

time у1 y2 case Min. :0.4195 Min. :0.00 Min. :0.4993 Min. : 1 1st Qu.: 2501 1st Qu.:0.75 1st Qu.:0.6134 1st Qu.:0.5818 Median : 5000 Median :1.50 Median :0.8127 Median :0.8661 Mean : 5000 Mean :1.50 Mean :0.9544 Mean :0.9165 3rd Qu.: 7500 3rd Qu.:2.25 3rd Qu.:1.1833 3rd Qu.:1.2168 Max. :10000 Max. :3.00 Max. :2.9487 Max. :1.9985

y3 Min. :-1.00688 1st Qu.: 0.02767 Median : 0.10449 Mean : 0.06336 3rd Qu.: 0.14834

Max. : 0.52410

In [10]: fread("ys-20x20-v10.csv") %>% summary

			_
	time	-	y2
Min. : 1			. :-3.99301
1st Qu.: 2501			Qu.:-0.91340
Median : 5000			ian :-0.41890
Mean : 5000			n :-0.48365
3rd Qu.: 7500			Qu.: 0.06929
Max. :10000			. : 2.49500
y3	y4	y5 Min. :-0.372126	yo
Min. :0.5752	Min. :-4.0103	Min. :-0.3/2120	MIN. :-0.10
373	1-+ 0 0 4121	1-+ 0 0 000222	1-+ 0 0 57
1st Qu.:0.6035	15t Qu.: 0.4131	1st Qu.:-0.098232	1st Qu.:-0.57
257 Median :0.6217	Median : 0.5349	Median : 0.003534	Median :-0.01
752	Median : 0.5549	Median : 0.005554	Median :-0.01
Mean :0.7131	Mean : 0.5122	Mean : 0.052012	Mean :-0.34
768	Mean : 0.3122	Mean : 0.052012	Medii :-0.34
3rd Qu.:0.7603	3rd Ou + 0 7352	3rd Qu.: 0.167168	3rd Qu.: 0.08
266	310 Qu., 0.7332	314 Qu 0.10/108	Jiu Qu., 0.00
Max. :1.6130	Max. :26.6816	Max. : 0.809911	Max. : 2.23
750	Max20.0010	Max 0.009911	Max 2.23
y7	y8	у9	y10
Min. :0.4848	Min. :-0.24560	Min. :-3.2654	Min. :0.5720
1st Qu.:0.4848	1st Qu.:-0.20817	1st Qu.: 0.3487	1st Qu.:0.5720
Median :0.4848	Median :-0.02356	Median : 0.4815	Median :0.5869
Mean :0.5243	Mean : 0.15453	Mean : 0.5258	Mean :0.6743
3rd Qu.:0.5094	3rd Qu.: 0.34993	3rd Qu.: 0.6762	3rd Qu.:0.6825
Max. :1.3364	Max. : 4.56972	Max. : 1.3579	Max. :2.0605
y11	y12	y13	y14
Min. :-2.4188	Min. :0.1320	Min. :-0.24258	Min. :-4.065
66			
1st Qu.: 0.5490	1st Qu.:0.1320	1st Qu.:-0.01273	1st Qu.: 0.048
67			
Median : 0.7178	Median :0.1320	Median :-0.01273	Median : 0.177
27			
Mean : 0.7117	Mean :0.1381	Mean : 0.06004	Mean : 0.301
54			
3rd Qu.: 0.8412	3rd Qu.:0.1354	3rd Qu.: 0.09370	3rd Qu.: 0.486
71			
Max. : 5.0888	Max. :0.2896	Max. : 0.77432	Max. : 1.837
72			
y15	y16	y17	y18
Min. :0.1428	Min. :-2.9651	Min. :-0.63421	Min. :0.2926
1st Qu.:0.1447	1st Qu.:-0.2468	1st Qu.: 0.05400	1st Qu.:0.3333
Median :0.1905	Median :-0.2113	Median : 0.08051	Median :0.4319
Mean :0.2784	Mean :-0.2694	Mean : 0.09200	Mean :0.4785
3rd Qu.:0.3495		3rd Qu.: 0.10599	3rd Qu.:0.5804
Max. :1.5073	Max. : 0.3458	Max. : 0.44155	Max. :1.6578
y19	y20		
Min. :-1.1064	Min. :-0.01253		
1st Qu.: 0.2657	1st Qu.: 0.13335		
Median : 0.4146	Median : 0.19258		
Mean : 0.3399	Mean : 0.27743		
3rd Qu.: 0.4431	3rd Qu.: 0.39444		
Max. : 3.2463	Max. : 1.84681		
4			———