



# Introduction to Prolog

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*CSCI3180 Principles of Programming Languages*

## Tutorial 9

# Imperative vs Declarative

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- 👤 Develop a program to solve a problem
  - ✦ What the problem is
  - ✦ How to solve the problem
- 👤 Imperative
  - ✦ **How to solve** the problem
  - ✦ Take longer time to develop a program
- 👤 Declarative
  - ✦ Do not worry about how to solve the problem
  - ✦ **What the problem is**
  - ✦ Less time for program development

# Prolog

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- 🏠 Prolog programming is divided into two stages.
  - ✦ Asserting what is true (building a program).
    - 🏠 Facts
    - 🏠 Rules
  - ✦ Asking what you want to know (running a program).
    - 🏠 Query

# SICStus Prolog

- 🌐 You are supposed to test your work on the machine "solar1.cse.cuhk.edu.hk" under SICStus 3.12.7, by directly typing "sics".

```
sparc1.cs.cuhk.hk:/uac/gds/cyhong> sics
SICStus 3.12.7 (sparc-solaris-5.7): Fri Oct 6 00:12:30 MET DST 2006
Licensed to cse.cuhk.edu.hk
| ?- █
```

- 🌐 Prolog Prompt: | ?-
- 🌐 To load a file containing Prolog code

\$ sics

```
| ?- ['asg2.pl'].
| ?- consult('asg2.pl').
| ?- reconsult('asg2.pl').
```

Alternatively...

```
| ?- [asg2].
| ?- consult(asg2).
| ?- reconsult(asg2).
```

# Example: Basic Idea

## Knowledge Base

likes(peter,mary).

likes(may,sam).

likes(sam,may).

likes(mary,sam).

**Facts**

canMarry(X,Y) :- likes(X,Y), likes(Y,X).

**Rule**

## Queries

| ?- canMarry(May,sam).

yes

| ?- canMarry(peter,mary).

no

| ?- canMarry(X, may).

X = sam.

| ?- canMarry(X, Y).

# Anonymous Variables

🕒 A variable begin with *underscore* `_`

🕒 Knowledge Base:

`likes(peter,mary).`

`likes(peter,alice).`

`| ?- likes(peter,Who).`

`Who = mary ? ;`

`Who = alice ? ;`

`no`

`| ?- likes(peter,_who).`

`yes`

`| ?- likes(peter,_).`

`yes`

`| ?- likes(john,_who).`

`no`

`| ?-`

Who does Peter like?

Does Peter like anybody?

# Syntax

---

- Finite set of clauses

- Clause (Rules)** : Head and Body

Syntax:  $A :- B_1, B_2, B_3 .$

- Fact**: Clause without Body and **variables**

Syntax:  $A .$

- $\text{likes}(\text{peter}, X)$  is a rule

- Comments**:

**% comment line**

**/\* comment block \*/**

# Syntax

## Rules

Syntax:  $A :- A_1, A_2.$

IF

AND

## Rule Ordering

- Match sequentially, from top to down

$A :- A_1, A_2.$

$A :- B_1, B_2.$



The first one is matched first, and then the second rule

## Goal Ordering

- Ordering of terms within the body of a rule
- Answered sequentially, from left to right

$A :- A_1, A_2.$

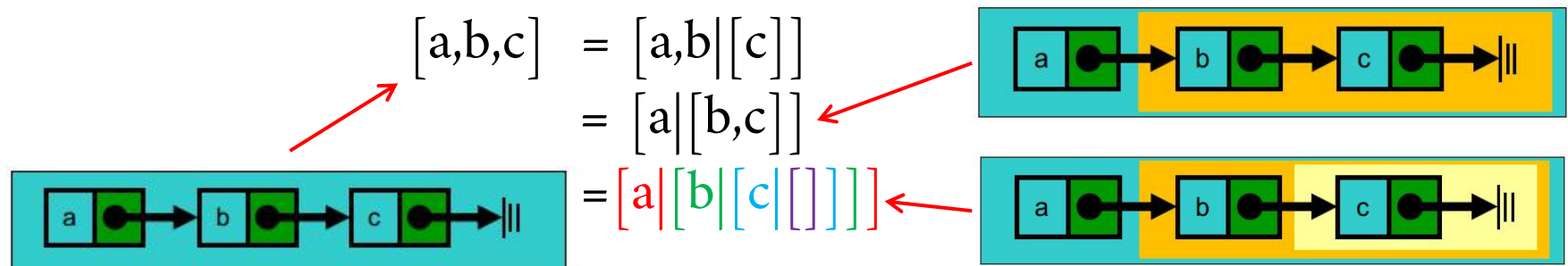


$A_1$  answered first and then  $A_2$



# Lists

- Prolog's built-in list representation
- `[]` denote empty list
- Syntactic sugar:  $[X|Y]$ 
  - $X$  is the **head** and  $Y$  is the **tail** of list
- Example: a list (a, b, c)



# append/3

```
append([], L, L).
```

```
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

If :  $\overset{\text{L1}}{\boxed{[3, 4]}} + \overset{\text{L2}}{\boxed{[5, 6, 7]}} = \overset{\text{L3}}{\boxed{[3, 4, 5, 6, 7]}}$

Then:  $[2, \boxed{3, 4}] + \boxed{[5, 6, 7]} = [2, \boxed{3, 4, 5, 6, 7}]$

# append/3

---

```
append([], L, L).
```

```
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

List 1

$[x_1, x_2, \dots, x_n]$

List 2

$[y_1, y_2, \dots, y_n]$

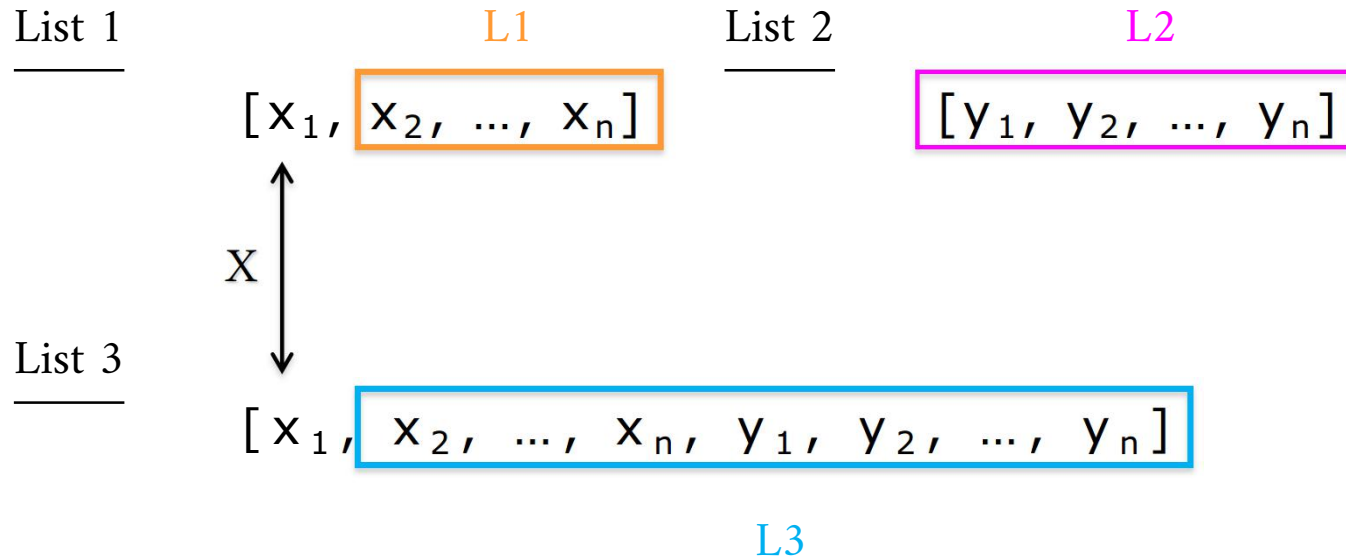
List 3

$[x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n]$

# append/3

`append([], L, L).`

`append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).`



# append/3

```
append([], L, L).
```

```
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

List 1

$[x_1, \boxed{x_2, \dots, x_n}]$

L1

List 2

$[\boxed{y_1, y_2, \dots, y_n}]$

L2

List 3

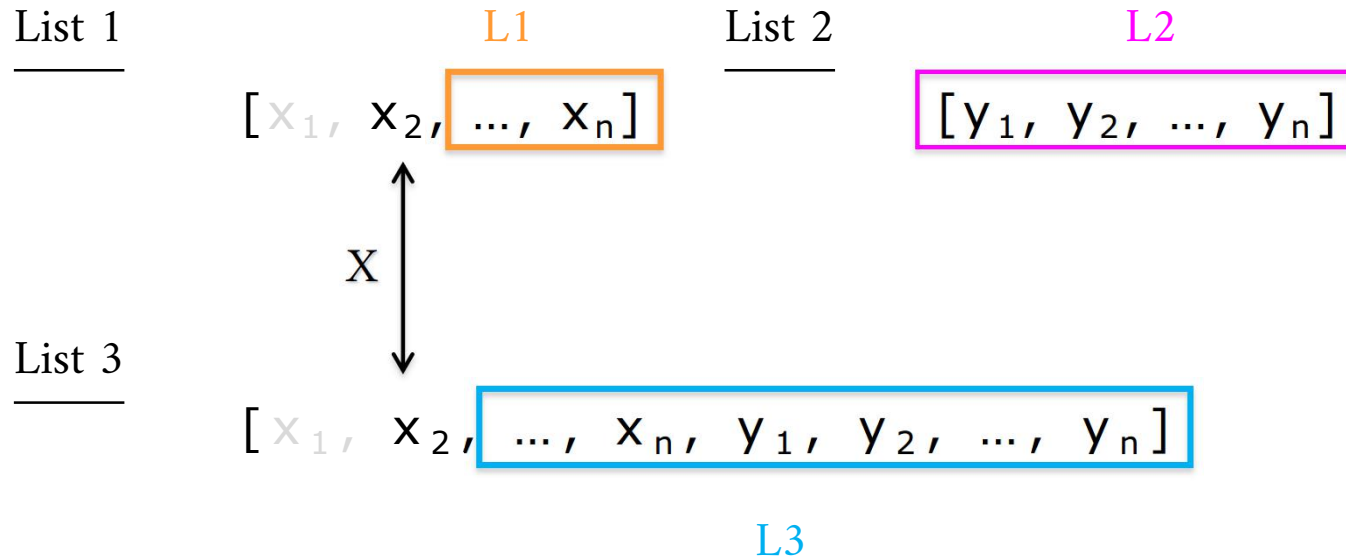
$[x_1, \boxed{x_2, \dots, x_n, y_1, y_2, \dots, y_n}]$

L3

# append/3

`append([], L, L).`

`append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).`



# append/3

```
append([], L, L).  
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

List 1

$[x_1, x_2, \dots, x_n]$

List 2

L

$[y_1, y_2, \dots, y_n]$

List 3

$[x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n]$

L

It is true !

# append/3

```
append([], L, L).
```

```
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

List 1

L1  
[x<sub>1</sub>, x<sub>2</sub>, ..., x<sub>n</sub>]

List 2

L2  
[y<sub>1</sub>, y<sub>2</sub>, ..., y<sub>n</sub>]

List 3

[x<sub>1</sub>, x<sub>2</sub>, ..., x<sub>n</sub>, y<sub>1</sub>, y<sub>2</sub>, ..., y<sub>n</sub>]

L3

It is true !



# append/3

---

```
append([], L, L).  
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

List 1

$[x_1, x_2, \dots, x_n]$

List 2

$[y_1, y_2, \dots, y_n]$

List 3

$[x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n]$

It is true !

# uses of append/3

---

```
append([], L, L).
```

```
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

## Check concatenation

```
| ?- append([1,2],[3,4],[1,2,3,4]).
```

← true

```
| ?- append([1,2],[4,5],[1,2,3,4]).
```

← false

## Concatenate 2 lists

```
| ?- append([1,2],[3,4],L).
```

```
L = [1,2,3,4] ? ;
```

```
no
```

# uses of append/3

---

```
append([], L, L).
```

```
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

## Check head element

```
| ?- append([1],_,[1,2,3,4]).
```

```
| ?- append([2],_,[1,2,3,4]).
```

## Check last element

```
| ?- append(_,[4],[1,2,3,4]).
```

```
| ?- append(_,[1],[1,2,3,4]).
```

# uses of append/3

---

```
append([], L, L).  
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

## 🕒 Find head element

```
| ?- append([H],_,[1,2,3,4]).
```

## 🕒 Find last element

```
| ?- append(_,[E],[1,2,3,4]).
```

# uses of append/3

```
append([], L, L).  
append([X|L1], L2, [X|L3]) :- append(L1, L2, L3).
```

## 🏠 Subtract last part of a list

```
| ?- append(L, [3,4], [1,2,3,4]).
```

## 🏠 Subtract first part of a list

```
| ?- append([1,2], L, [1,2,3,4]).
```

## 🏠 Decompose a list

```
| ?- append(L1, L2, [1,2,3,4]).
```

```
L1 = [],  
L2 = [1,2,3,4] ? ;  
L1 = [1],  
L2 = [2,3,4] ? ;  
L1 = [1,2],  
L2 = [3,4] ? ;  
L1 = [1,2,3],  
L2 = [4] ? ;  
L1 = [1,2,3,4],  
L2 = [] ? ;  
no
```

🏠 more ...

# Assignment 4 Q1 - list operation

---

🏠 `element_last(X, L)`

- ✦ which is true if the last element in list L is X
- ✦ `?- element_last(e, [a,b,c,d,e]).`
- ✦ True

# Q1 - list operation

---

🏠 `element_n(X, L, N)`

✦ which is true if the Nth element in list L is X.

✦ `| ?- elementn(c, [a,b,c,d,e], s(s(s(0)))).`

✦ True

# Q1 - list operation

---

🏠 `remove_n(X, L1, N, L2)`

- ✦ get the resulting list L2 that is obtained from L1 by removing the N th element, as well as get the removed element X.
- ✦ `| ?- remove_n(X, [a,b,c,d,e], s(s(s(0))), L2).`
- ✦ `X = c,`  
`L2 = [a, b, d, e].`



# Q1 - list operation

---

🏠 `remove_n(X, L1, N, L2)`

- ✦ get the resulting list L2 that is obtained from L1 by removing the N th element, as well as get the removed element X.
- ✦ `| ?- remove_n(X, [a,b,c,d,e], s(s(s(0))), L2).`
- ✦ `X = c,`  
`L2 = [a, b, d, e].`

# Q1 - list operation

---

🕒 `insert_n(X, L1, N, L2)`

✦ get the resulting list L2 that is obtained by inserting X to the position before Nth element of list L1.

✦ `| ?- insertn(h, [a,b,c], s(s(0)), L2).`

✦ `L2 = [a,h,b,c]`

do it with `remove_n` !

# Q1 - list operation

---

🏠 repeat\_three(L1, L2)

- ✦ get the resulting list L2 that repeats each element in list L1 for three times.
- ✦ | ?- repeat\_three([a,b,c,d,e],X).
- ✦ X = [a,a,a,b,b,b,c,c,c,d,d,d,e,e,e]

## Q2 - Multiway tree

---

- 🌲 A multi-way tree is composed of a root and a sequence of sub-trees (children), which are multi-way tree themselves. The list of sub-trees of a certain node is also called a forest.
- 🌲 In Prolog, we represent a multi-way tree by the term `mt(X, F)`, where `X` denotes the root and `F` denotes the forest of sub-trees.

## Q2 - Multiway tree

---

- 🕒 Represent the multiway tree shown in Figure 1 as a Prolog term.
  - ✦ (Hint: represent forest as a list of multiway trees).

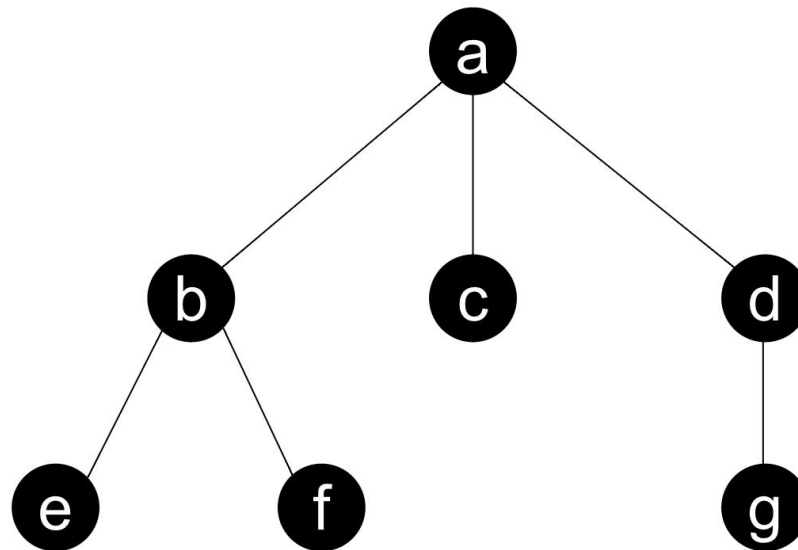


Figure 1: An example of multi-way tree

## Q2 - Multiway tree

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- 🕒 Define the predicate *is\_tree(Term)*
- 🕒 Define the predicate *num\_node(Tree, N)*
- 🕒 Define *sum\_length(Tree, L)*
  - ✦ which is true if "L" is the sum of lengths of all internal paths in "Tree".

## Q2 - Multiway tree

🕒 *sum\_length(Tree, L)*

✦ The length of an internal path from the root node  $r$  to an internal node  $n$  is the distance from  $r$  to  $n$ .

✦ 
$$L = 1(b) + 1(c) + 1(d) + 2(e) + 2(f) + 2(g) = 9$$

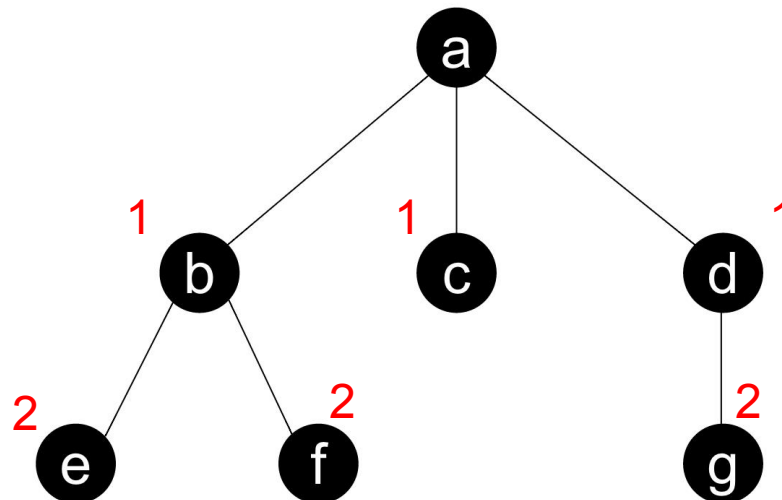


Figure 1: An example of multi-way tree