



ADVANCED PROCESS MODELLING FORUM

Online Model-based Applications (OMBAs)

Real-time monitoring of ethylene cracking furnaces

Mark Matzopoulos – Head of Chemicals, Petrochemicals & Refining



















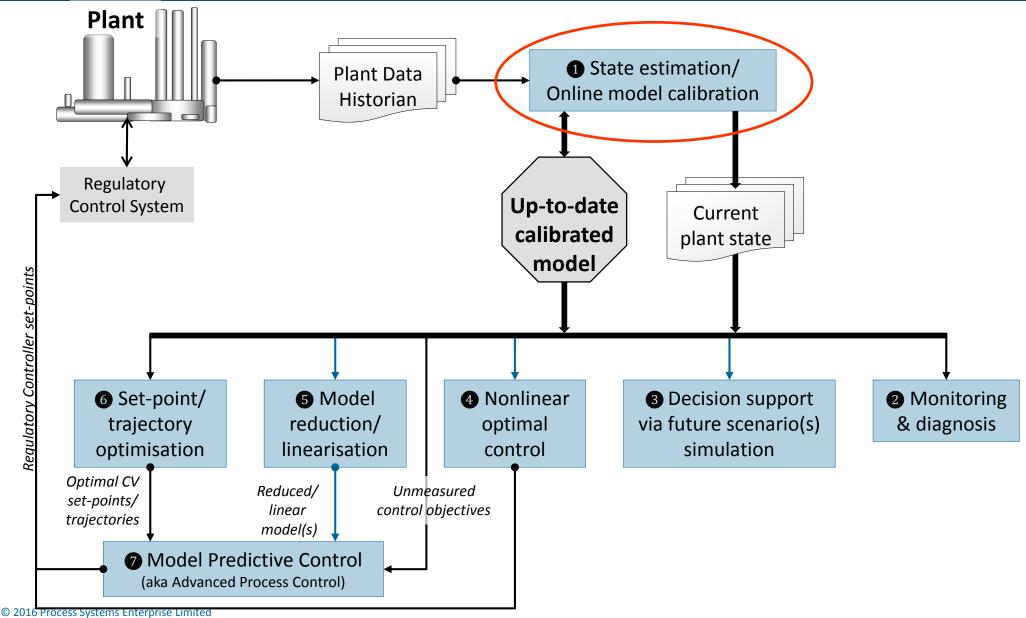




Online Model-Based Applications (OMBAs)

Integrated framework – the 'big picture'





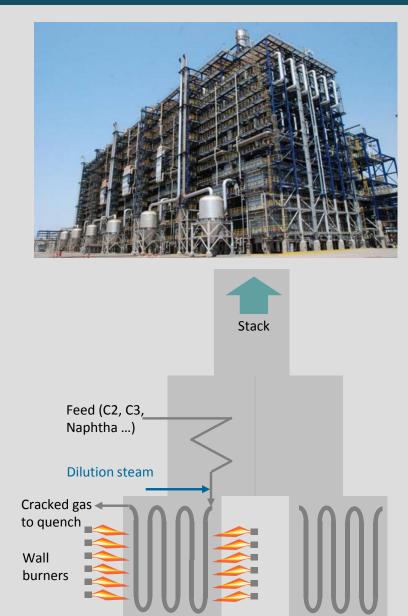
Background



Steam crackers



- Large, complex units at heart of petrochemical complexes
 - produce key building blocks: ethylene, propylene, butadiene, aromatics, acetylene
 - furnaces crack hydrocarbon feedstocks in the presence of steam
 - temperatures between 800–860°C
 - continuous coke deposition in coil,
 TLE and quench
- MAJOR CHALLENGE: predict rate of coking and effect on performance, particular yield prediction



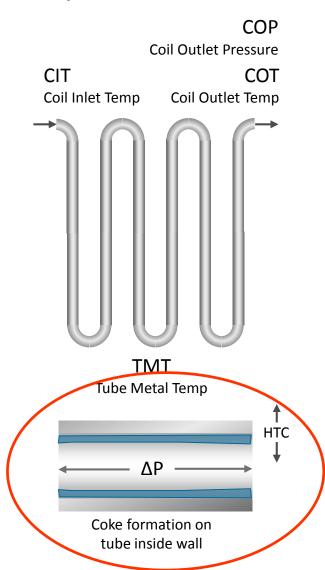
The challenge of coking



Coking

- occurs along length of coil
- can be exacerbated by changes in operation (feed flowrate, steam, etc. fluctuations)
- Effects increase over time
 - reduced heat transfer
 - increase in metal skin temperature
 - increasing pressure drop
- Operations interrupted for decoking
 - depends on feedstock, operating conditions
 - triggered by pressure drop (small diameter tubes) or metal temperature (larger tubes)
 - typically 60-90 days

Key variables



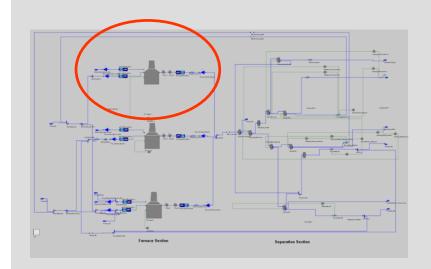
Approach

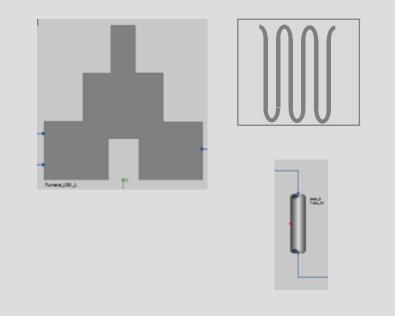


Model-based approach



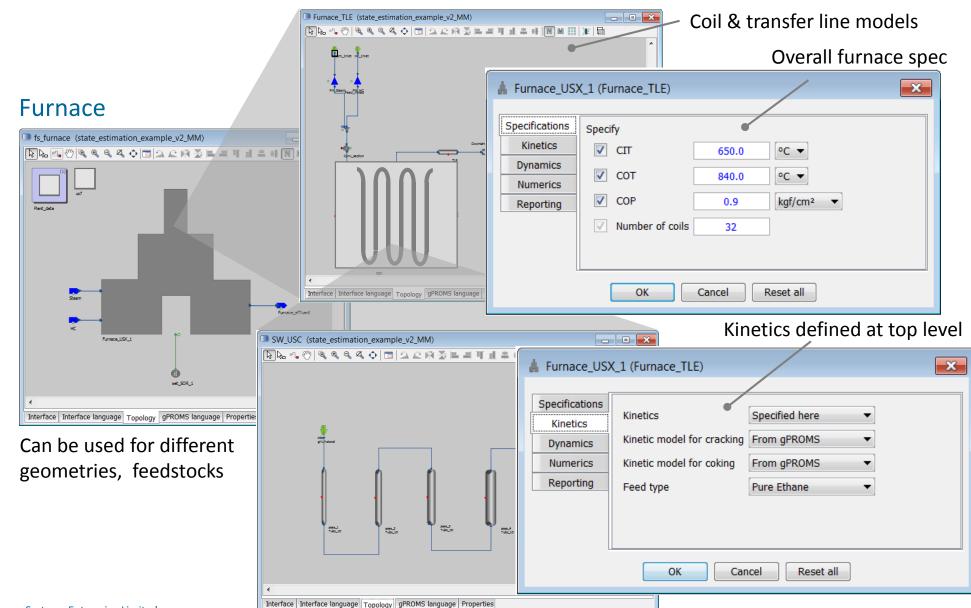
- First-principles model of furnace
 - modular, hierarchical models
 - multiscale, distributed
- Evolving gPROMS ProcessBuilder Olefins library





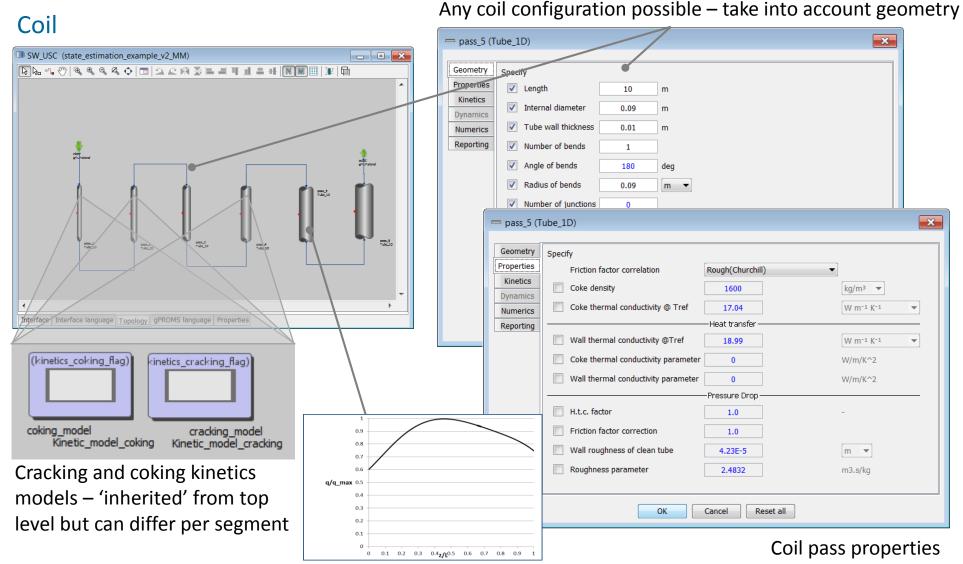
Furnace/coils – geometry





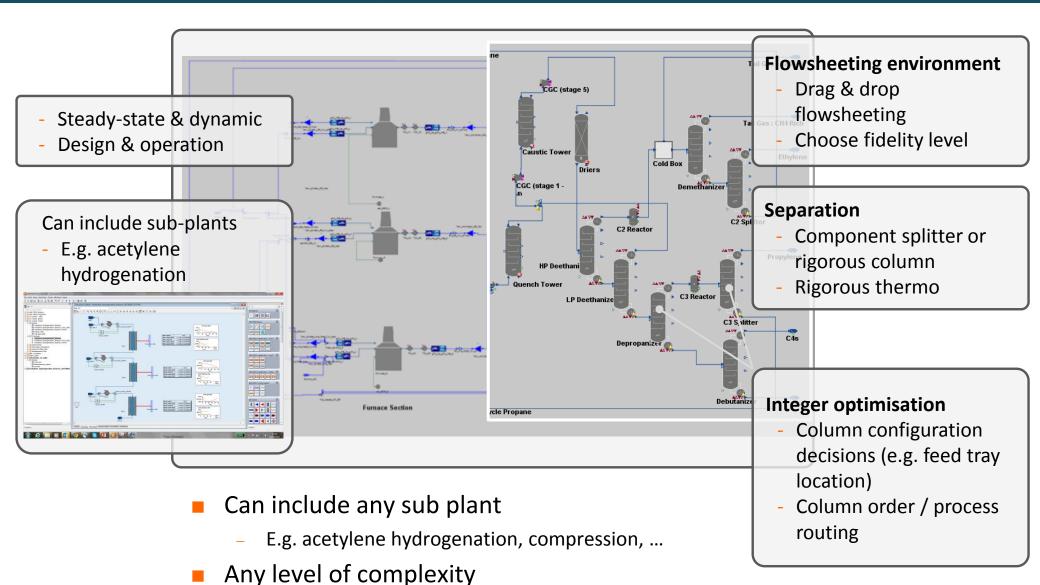
Furnace/coils – geometry and kinetics





Wider context — whole plant Typical application





Kinetics models



Reaction kinetics

Cracking model



Reaction #	Reaction rate
1	$R_1 = k_1 [C_3 H_8]$
2	$R_2 = \vec{k}_2 [C_3 H_8] - \frac{\vec{k}_2}{K_{eq,2}} [C_3 H_6][H_2]$
3	$R_3 = k_3 [C_3 H_8] [C_2 H_4]$
4	$R_4 = k_4[C_3H_6]$
5	$R_5 = k_5 [C_3 H_6]$
6	$R_6 = \vec{k}_6 [C_3 H_6] - \frac{\vec{k}_6}{K_{eq,6}} [C_2 H_2] [CH_4]$
7	$R_7 = k_7 [C_3 H_6] [C_2 H_6]$
8	$R_8 = \vec{k}_8 [C_2 H_6] - \frac{\vec{k}_8}{K_{eq,8}} [C_2 H_4] [H_2]$
9	$R_9 = \vec{k}_9 [C_2 H_4] [C_2 H_2] - \frac{\vec{k}_9}{K_{eq,9}} [C_4 H_6]$
10	$R_{10} = k_{10} [C_2 H_4] [C_2 H_6]$

Reference: Sundaram, K.M., & Froment, G.F. 1977. Modeling of thermal cracking kinetics – I: Thermal cracking of ethane, propane and their mixtures. Chemical Engineering Science, 32, 601{608.

$$k_i(T) = k_i(T_{ref}) \exp\left(-\frac{E_a}{R}\left(\frac{1}{T} - \frac{1}{T_{ref}}\right)\right)$$

Reaction kinetics

Coking model (dynamic)



Mass continuity equation for coke:

$$\frac{dm^{coke}(z)}{dt} = \frac{2R_i(z)}{R_W^2} r_{coking}(z)$$

Coking rate: Influential Very influential Not influential Not influential
$$r_{coking}(z) = k_{c1}c_{C_2H_4}(z) + k_{c2}\left(\frac{c_{C_2H_4}^2}{c_{C_3H_6}}\right) + k_{c3}c_{C_3H_6} + k_{c4}c_{1-3but}$$

with

$$k_i(T) = k_i(T_{ref}) \exp\left(-\frac{E_{a,i}}{R}\left(\frac{1}{T} - \frac{1}{T_{ref}}\right)\right), \quad i = c1, c2, \dots$$

Wauters, S., & Marin, G.B. 2002. Kinetic Modeling of Coke Formation during Steam Cracking. Ind. Eng. Chem. Res., 41, 2379{2391 Albright, L.F. 2002. Comments on 'Kinetic Modeling of Coke Formation during Steam Cracking'. Ind. Eng. Chem. Res., 41, 6210{6212 Plehiers et al (1990).

Reaction kinetics

Coking model implementation



Implemented as a custom kinetics model

```
Kinetic model coking (state estimation example v2 MM)
  93
      # Calculate the pyrolytic coking contribution
  96
      FOR z := 0 TO 1 DO
        reaction_rate_pyrolytic(z) {kg/m2/s} * 1E3 {g/kg} =
          #limit the reduction in diameter to prevent the model from failing due to pressure runaway
 99
          0.5 * (1 - TANH( 5 * (percentage reduction_diam(z) - percentage_reduction_diam_maximum)/2))
 100
 101
          # For first reaction conrrsidered in the model
 102
            10^log 10 kinetic constant ref temp('cl') {g coke/(m2.s)/(mol/m3)}
          * EXP(-activation_energy('cl') {J/mol} / up.gas_constant {J/mol/K} * (1 / temperature(z) {K} - 1 / temperature_refere
 103
 104
          * molar concentration('propylene',z) {mol/m3}
          # For second reaction considered in the model
 105
 106
          + 10^log_10_kinetic_constant_ref_temp('c2') {g coke/(m2.s)/(mol/m3)}
 107
          * EXP(-activation energy('c2') {J/mol} / up.gas constant {J/mol/K} * (1 / temperature(z) {K} - 1 / temperature refere
          * (molar concentration('ethylene',z) + 1E-9)'n C2H4 {mol/m3} {g/m2/s}
 108
 109
          # For second reaction considered in the model
 110
          + 10^log 10 kinetic constant ref temp('c3') {g coke/(m2.s)/(mol/m3)}
          * EXP(-activation energy('c3') {J/mol} / up.gas constant {J/mol/K} * (1 / temperature(z) {K} - 1 / temperature refere
 111
112
          * molar concentration('1,3-BUTADIENE',z) {mol/m3}
 113
          # This term is based on the model proposed by Plehiers et al (1990)
 114
          + 10^log 10 kinetic constant ref temp('c4')
 115
          * EXP(-activation energy('c4') {J/mol} / up.gas constant {J/mol/K} * (1 / temperature(z) {K} - 1 / temperature refere
 116
          * molar concentration('ethylene',z)^2
 117
          / (molar_concentration('propylene',z) + 1E-9)); {g/m2/s}
 118
 119
      END # FOR z := 0 TO 1 DO
 120
                                                       HI
           INS
    1:1
 Interface Interface language | Topology | qPROMS language | Properties
```

gCRACKER v. 1.0: Furnace Model

Pressure drop correlation



Pressure drop equation:

$$A(z)\frac{\partial p(z)}{\partial z} = F(z)\frac{\partial v(z)}{\partial z} - A(z)\rho(z)v(z)\left[\frac{2}{R_I(z)}f_{tube}(z) + \frac{NB}{L}f_{bend}(z)\right],$$

$$@z = L: \ p(z) = p^{outlet}$$

With

$$\frac{1}{\sqrt{4\left(\frac{f_{tube}}{f_{adjustment}}\right)}} = -2\log\left[\frac{\frac{K(z)}{d_i}}{3.71} + \left(\frac{7}{Re}\right)^{0.9}\right],$$

$$K(z) = K_{clean\ tube} + \alpha r_{coking}(z)$$

$$f_{bend}(z)\left(0.7 + \frac{\alpha}{90}0.35\right)(0.051 + 0.19\frac{2R_I(z)}{R_B})$$

gCRACKER v. 1.0: Furnace Model

Heat transfer model



$$\begin{split} q_{ext}(z)R_0 &= U(z)R_I(z)[T_I(z) - T_G(z)] = \\ &= \frac{\lambda_c[T_W(z) - T_I(z)]}{\ln\left(\frac{R_W}{R_I(z)}\right)} = \frac{\lambda_w[T_0(z) - T_W(z)]}{\ln\left(\frac{R_0}{R_W}\right)} \end{split}$$

 $R_0=$ external radius $R_w=$ internal radius of the tube $R_I(z)=$ radius at interface coke-gas Temperatures accordingly

$$U(z) = \frac{Nu(z)\lambda_G(z)}{2R_I(z)}$$

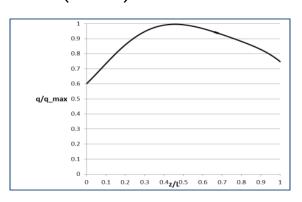
with

$$Nu(z) = 2.43E - 02Re(z)^{0.8} \Pr(z)^{0.4} + \frac{429.2}{l(z)^{0.0706}} - \frac{544.3}{\left(\frac{X(z)}{100}\right)^{0.0437}}$$

and

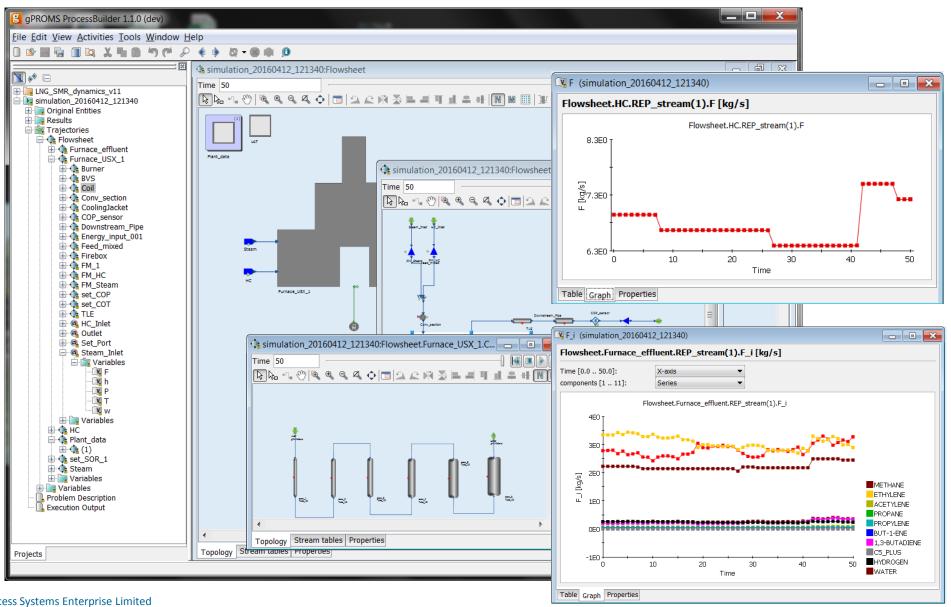
$$l(z) = \frac{2z}{Re(z) \Pr(z) R_I(z)}$$

 \Box An external *a priori* heat flux profile $q_{ext}(z)$ is assigned :



Execute simulation





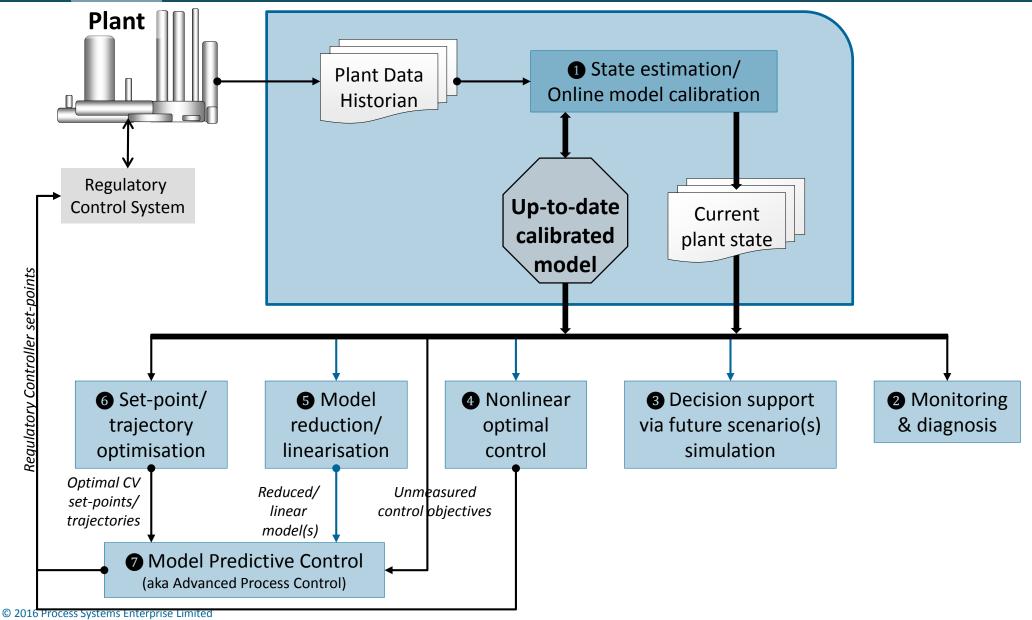
Online Model-based Application (OMBA)



Online Model-Based Applications (OMBAs)

Integrated framework – the 'big picture'

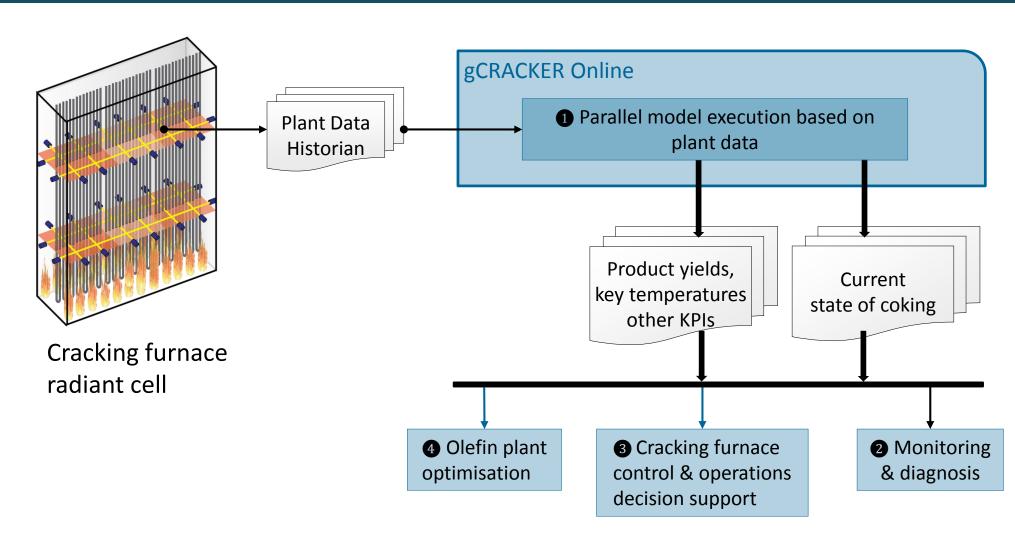




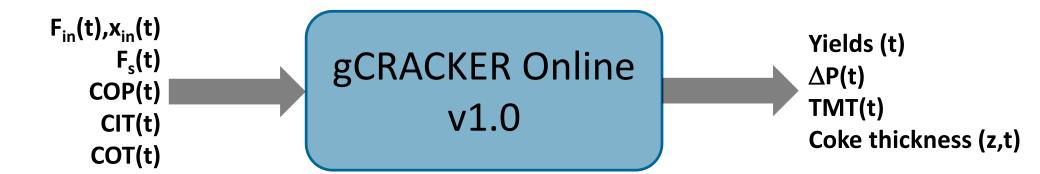
gCRACKER Online v1.0 approach

Parallel model execution



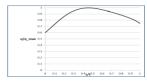






Uses gCRACKER model of furnace operation

- ethane/propane/mixed feeds
- given shape of axial heat flux profile



A dynamic simulation-based calculation based on quasi-steady-state model

- all inputs are specified degrees of freedom in the model
- all outputs are computed model variables
- execution much faster than real time

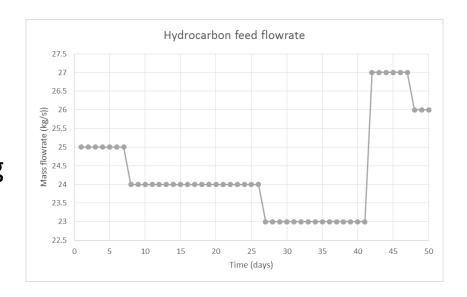
Successfully deployed online within DCS

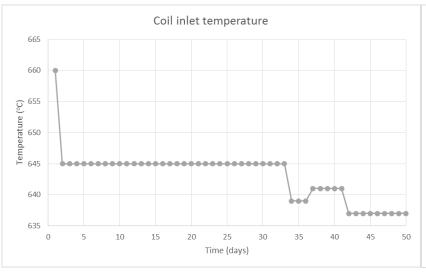
- 8 furnaces × 2 cells
- 16 gO:RUNs executing simultaneously in real time

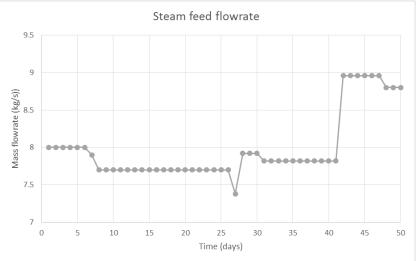
Trial



- Run of 50 days
- Changing feedstock rates, inlet temp, dilution steam
- Predict using proposed coking kinetics
- Compare outputs with plant data

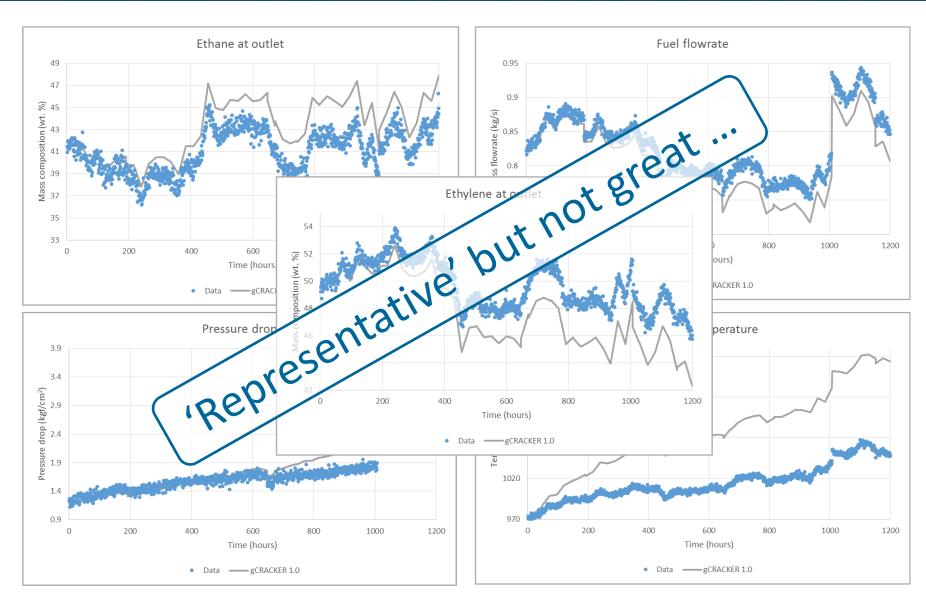




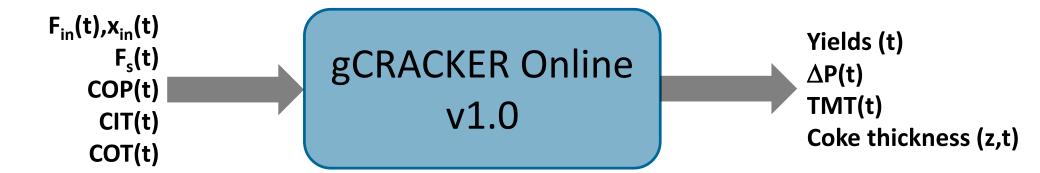


Results 1









Why?

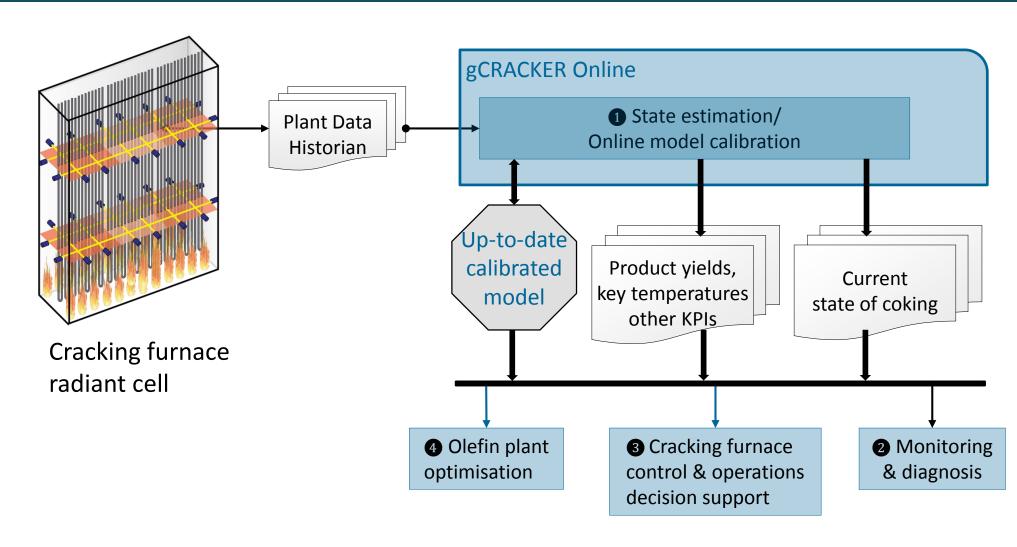
- Some of the inputs may not be accurate
 - e.g. COT not measured directly
- Model is subject to inaccuracies
 - characterisation of coking → prediction of coke thickness
 - heat losses → relation between conversion & fuel consumption?
- What if we have some additional ("redundant") measurements relating to model <u>outputs</u>?

CAN WE DO BETTER?

gCRACKER Online v2.0 approach

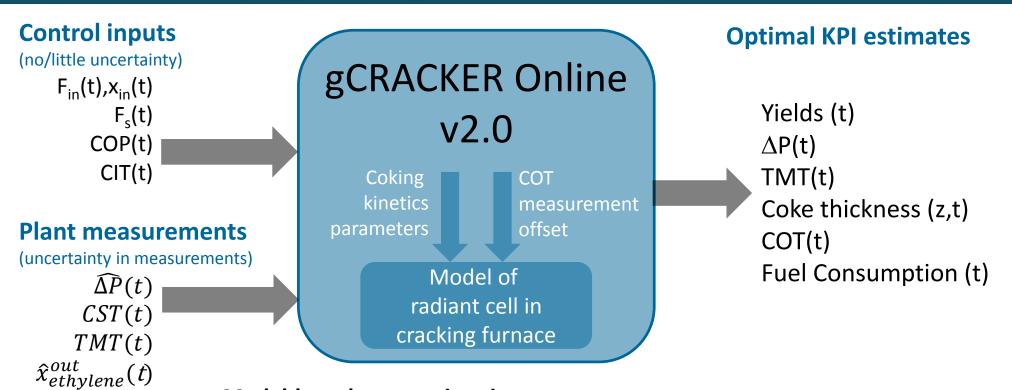
State estimation





CVs, MVs and KPI outputs





- Model-based state estimation
 - makes use of any available redundant measurements
 - takes account of uncertainty in both measurements and model
- Continuously self-calibrating model
 - coking kinetics
 - furnace heat losses

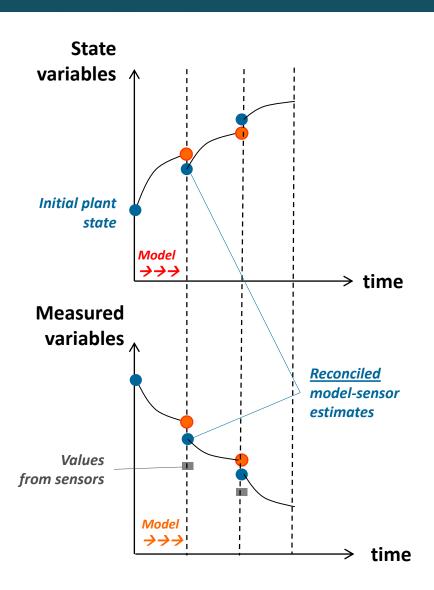
- Apply physical understanding to identify weak points of model
- Focus state estimation specifically on these points

 $\hat{x}_{ethane}^{out}(t)$

State Estimation

for Online Model-Based Applications





Reconcile

- model predictions
- sensor measurements
- to obtain a better estimate of the current state of the system
 - process variables
 - compositions, temperatures,
 pressures, flowrates,
 - plant characteristics that may gradually change during operation
 - catalyst activity
 - heat transfer coefficients
 - rotating equipment performance parameters
- ...and of the uncertainty in these estimates



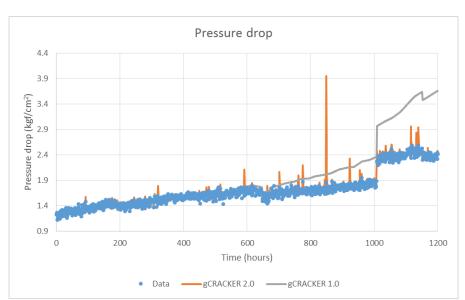
- Extended Kalman Filter (EKF) algorithm chosen
 - EKF is well-established and implementation is relatively simple
 - Investigating other options too
- Prototyped on large-scale client application
- → Now being formally implemented within gPROMS online toolkit using DAEBDF integrator

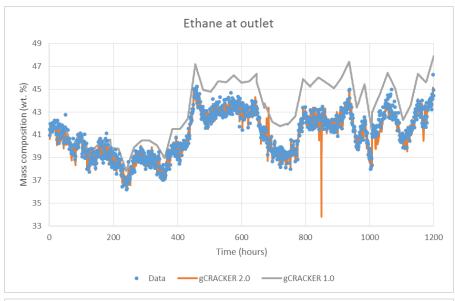
Results 1

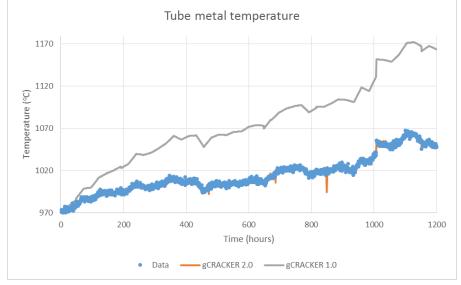


- Run against same plant data, but use state estimation to:
 - adjust state variables
 - adjust coking kinetics
 - adjust COT offset

- ...



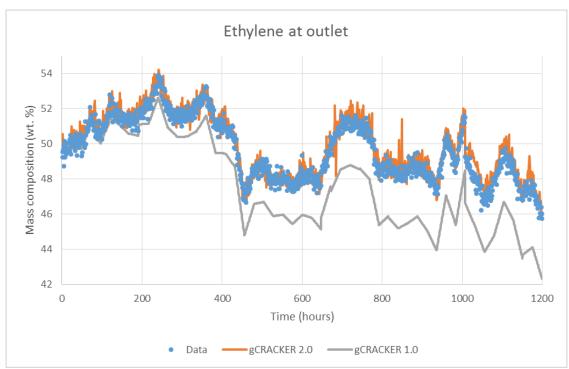


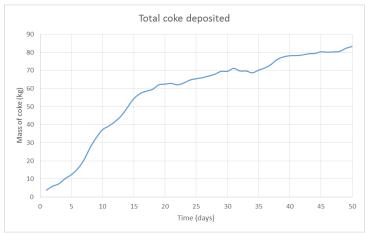


Results 2



- Key result: Ethylene
 <u>estimate</u>
- Plant measurementsNOT made availableto gCRACKER



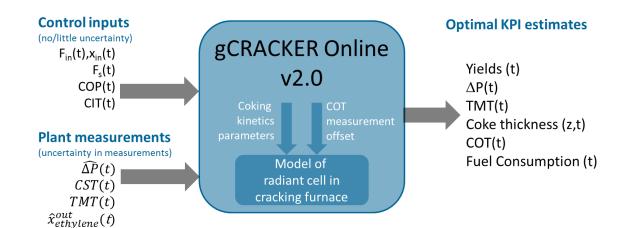


< Cumulative coke deposit also useful to know

Conclusions

 $\hat{x}_{ethane}^{out}(t)$



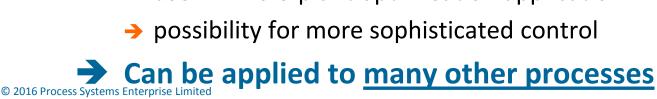


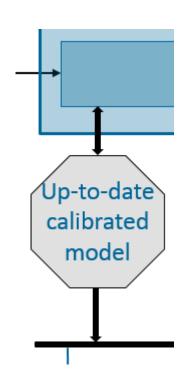
Mathematical structure

- ✓ PDAE system
- ✓ 200+ differential equations
- ✓ ~15000 algebraic equations
 - 1 2 hours for 50 days

Key information generated for each cell in each furnace

- 1. Reliable estimate of current state of coking
 - significant effect on optimal solution
- 2. Accurate KPI and other variable information
- 3. Up-to-date model
 - use in whole-plant optimisation application







Thank you



















