

① Data distribution.

② Probability.

③ Random variable

④ Probability distribution function

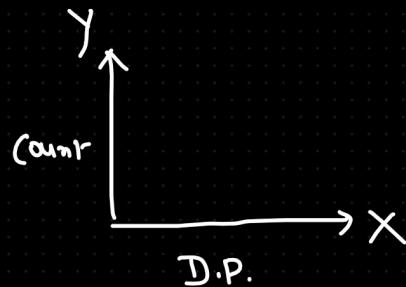
└ pmf (Probability mass fn)

└ PDF (Probability density fn)

CDF

pmf (discrete)

- ① Uniform dist-
- ② bernouli dist
- ③ binomial / multinomial
- ④ Poisson dist-



PDF (continuous)

- ① Normal dist-
- ② SND
- ③ Power law
- ④ Pareto dist-
- ⑤ log normal dist-
- ⑥ T, F, Chi-square dist.-

Probability.

Naive bayes algo

tent classification.

← ML

① Basic Prob. theory.

② Independent events

③ Dependent Event / Conditional Prob.

④ Naive bayes theorem

⑤ types of event in prob. like mutually exclusive events

$$\text{Coin} \Rightarrow P(H) \Rightarrow \frac{1}{2} = \underline{\underline{50\%}}$$

$$\text{toss } \underline{\underline{q}} \text{ coin.} \Rightarrow \frac{\text{fav. outcomes.}}{\text{total no. of outcome}}$$

$$P(\text{happening}) + P(\text{not happening}) = 1$$

$$\text{Dice.} \Rightarrow P(S) = \frac{1}{6}$$

$$P(A) + P'(A) = 1.$$

$$P(\text{not } S) = \frac{5}{6}$$

$$= 1 - \frac{1}{6} = \frac{6-1}{6} = \boxed{\underline{\underline{5/6}}}$$

Ques. bag \Rightarrow 5 marble balls

[4 balls are blue
1 is red]

Cards = 52.

What will be the Prob to get a long?

Prob to get a blue marble?

$$= \frac{4}{4+1} = \frac{4}{5}$$

$$\frac{4}{52} = \frac{1}{13}$$

Ques. two dice. \Rightarrow sum = 6

~~1~~ + ~~1~~ \Rightarrow 6
 $6 \times 6 = 36$

$$\frac{5}{36}$$

\square	+	\square	= 6
3		3	= 6
1		5	= 6
5	-	1	= 6
4		2	= 6
2		4	= 6
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Ques. $52 \Rightarrow$ King of hearts $\Rightarrow \frac{1}{52}$

Random Variable

$$X + 5 = 6$$

$$X = 6 - 5$$

traditional Variable \Rightarrow $X = 1$

→ Random Variable \Rightarrow Random experiment

(H, T)

(tossing a coin.)

$= (1, 2, 3, 4, 5, 6)$

(Dice Rolling)

(Pass or Fail)

(Exam Result)

Random Variable \Rightarrow
 ① Discrete =
 ② Continuous.

Coin, Dice, Cards. (Whole no.) =

H, T
 $\{1, 2, 3, 4, 5, 6\}$
 $\{C, S, D, H\}$

Continuous

Height-

$$a \leq \text{height} \leq b$$

Height \Rightarrow 5.6, 5.65, 5.655, 6.2,
6.21

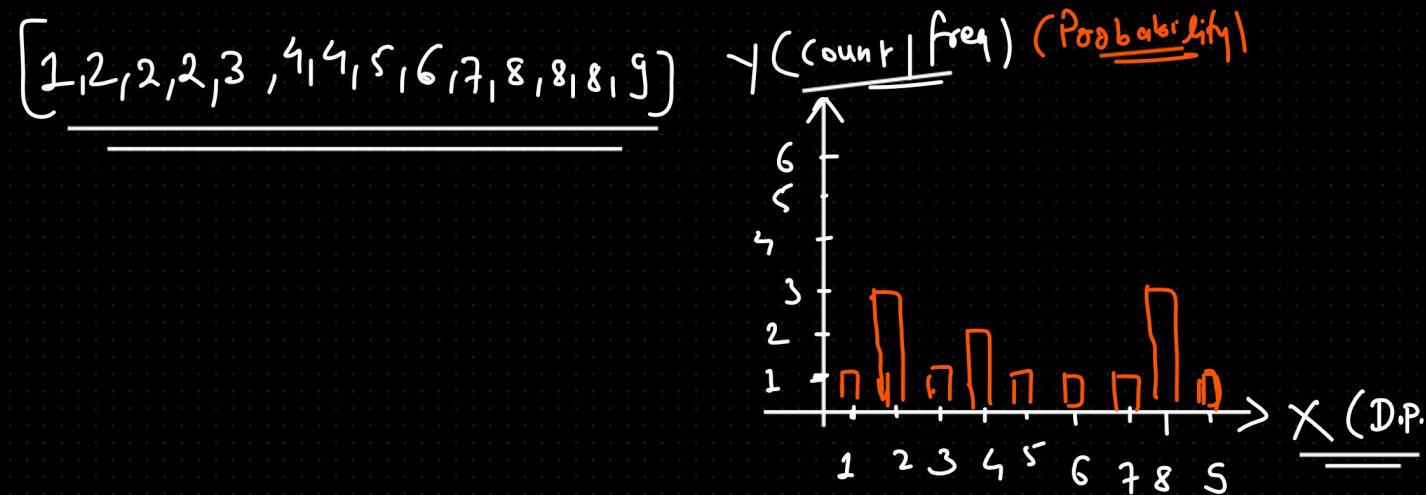
Probability mass function.

Weight

$$x \leq \text{weight} \leq y$$

Probability density function

Data distribution. $[2, 3, 4, 4, 2, 2, 1, 5, 6, 7, 8, 8, 8, 9]$



Data distribution.

Probability dist-

① Probability mass function (PMS) (Discrete variable)

② Probability function (PDF) (continuous variable)

density

Probability mass function.

(Discrete Var)

(Coin, Dice, marble, card)

$$\downarrow \\ P(X=x) = P_i$$

Coin

$$P(X=H) = \frac{1}{2} = 0.5$$

$$\begin{aligned} & \because 1 \leq P_i \geq 0 \Leftarrow \\ & \boxed{\sum P_i = 1} \Leftarrow \\ & \boxed{0 \leq P_i \leq 1} \end{aligned}$$

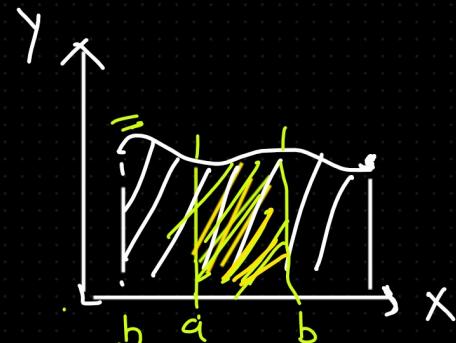
$$\begin{aligned} & \Rightarrow 1 - 0.5 = 0.5 \\ & \quad \uparrow \quad \swarrow \\ & \Leftarrow \boxed{0.5 + 0.5 = 1} \end{aligned}$$

Probability density function

(Continuous var)

(Height, weight, ID)

$$\boxed{+\infty \int_{-\infty}^{\infty} f(x) dx = 1}$$



$$\int_a^b f(x) dx = P$$

$$\begin{aligned} P(X=x) &= \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2} \\ &= \end{aligned}$$

$$\boxed{a \leq x \leq b}$$

Probability Mass function.

Probability Dist wrt. Discrete var.

① Uniform distribution.

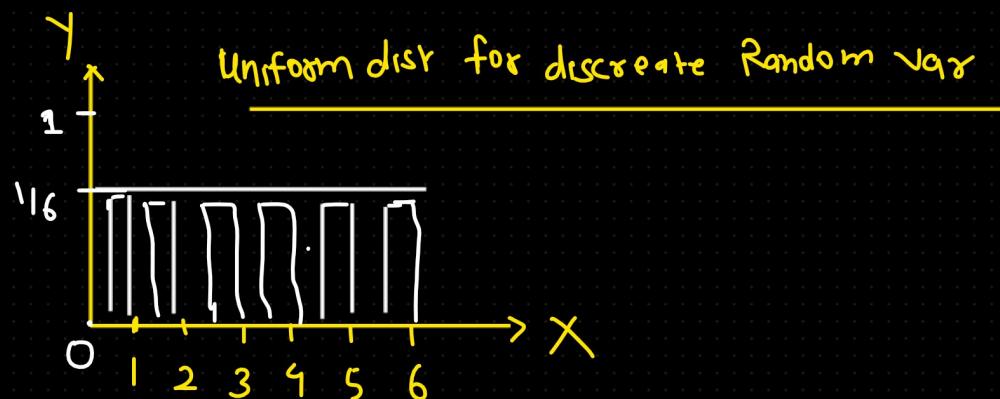
Dice. \Rightarrow

$$x=1 \quad x=2 \quad x=3 \quad x=4 \quad x=5 \quad x=6$$

↓↓

Random variable in dice.

$$\text{Prob for } \{1, 2, 3, 4, 5, 6\} \Rightarrow P(x=1) = \frac{1}{6}, \quad \frac{1}{6}, \quad \frac{1}{6}, \quad \frac{1}{6}, \quad \frac{1}{6}, \quad \frac{1}{6} = 1$$



Bernoulli dist (Binary outcome)

Y/N
0/1
P/F
H/T

Coin.
(H,T)

Random variable

Bernoulli dist \rightarrow (binary outcome)

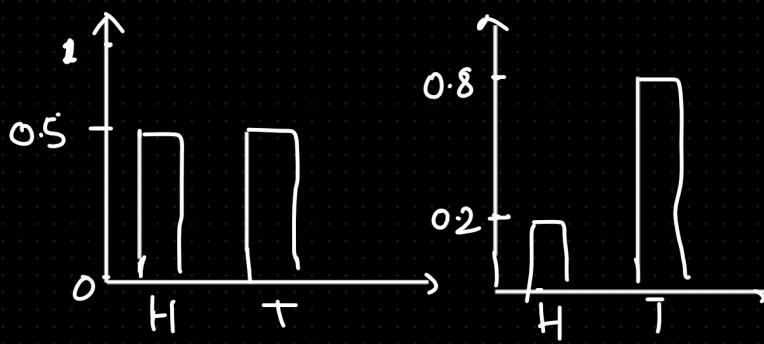
With only single try

toss \rightarrow coin \rightarrow only one time \Rightarrow H, T

Exam \rightarrow one time \rightarrow Pay full

Coin. $X = H$ $X = T$
 $P(X = \{H, T\}) = \frac{1}{2}$ $\frac{1}{2}$

- $\begin{cases} 0.3 & 0.7 \\ 0.4 & 0.6 \\ 0.2 & 0.8 \end{cases}$



H|T

P|F

R|L

$$P(X=x) = P^x \cdot (1-P)^{1-x}$$

$$\underline{\underline{S^0}} = 1$$

$$P(X=0) = P^0 \times (1-P)^{1-0}$$

$$P(X=0) = 1 \times (1-P)^1$$

$$P(X=1) = P$$

$$\underline{\text{Binomial dist}} \Rightarrow = \left[\binom{n}{r} p^r \cdot (1-p)^{n-r} \right] \Rightarrow$$

Bernoulli dist \rightarrow one try (binary outcome)

Binomial dist \Rightarrow n try (binary outcome)

Multinomial dist \Rightarrow n try (multiple outcome)

coin $\Rightarrow \{H, T\}$ \Rightarrow toss only one time

coin $\Rightarrow \{H, T\}$ \Rightarrow toss two times i want at least one head.
 (Consecutive)

1 2 \Rightarrow Head.

H H
H T-
T H-
T T

$$P(X=0) = \frac{1}{4}$$

$$P(X=1) = \frac{2}{4} = \frac{1}{2}$$

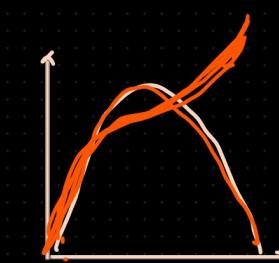
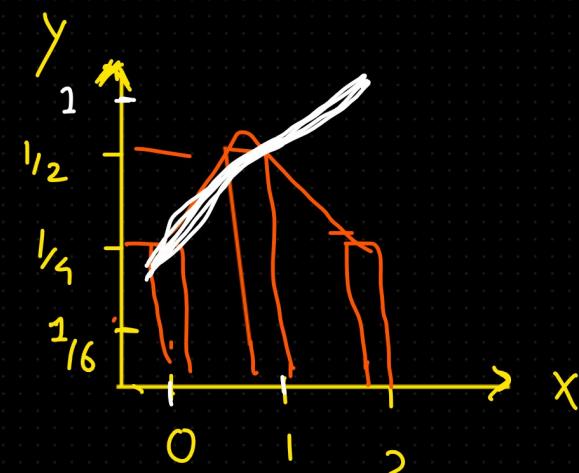
$$P(X=2) = \frac{1}{4}$$

Combinative.

$$\begin{aligned} & (1+2+3+4+5) \\ & \quad \boxed{3} \\ & 6+4 \\ & \quad \boxed{10+5} \\ & \quad \boxed{15} \end{aligned}$$

$$\underline{\underline{P(X \leq 1)}}$$

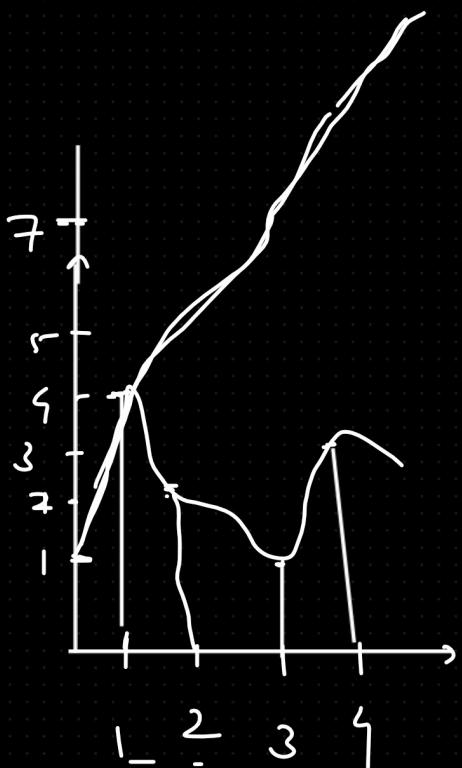
$$\begin{aligned} P(X=0) + P(X=1) \\ \frac{1}{4} + \frac{1}{2} = \frac{1+2}{4} = \frac{3}{4} \end{aligned}$$



$$P(X \leq 2)$$

$$P(X=0) + P(X=1) + P(X=2)$$

$$\frac{1}{4} + \frac{1}{2} + \frac{1}{4} = \frac{1+2+1}{4} = 1$$



$$P(1 \text{ and } 2) = \underline{\underline{1}} + \underline{\underline{3}} = \underline{\underline{4}} + \underline{\underline{2}} = \underline{\underline{6}}$$

= 6 People \Rightarrow

Blood group category

O⁺ B⁺ A⁺ AB⁺
= -3 -1 -1 -1

$$= \underline{5} \underline{C}_2 \underline{\left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^3} \text{ Binom}$$

$$\neq n_{C_3} P^x (1-P)^{n-x}$$

$$\Rightarrow \frac{6!}{3! \cdot 1! \cdot 1! \cdot 1!} \times \left(\frac{3}{6}\right)^3 \times \left(\frac{1}{6}\right)^1 \times \left(\frac{1}{6}\right)^1 \times \left(\frac{1}{6}\right)^1$$

Combination

$$7_{C_3} = ?$$

$$\frac{7 \times 6 \times 5}{3 \times 2 \times 1} =$$

$$\frac{7!}{3! \times (7-3)!} = \frac{7!}{3! \times 4!}$$

$$= \frac{7 \times 6 \times 5 \times 4!}{3! \times 4!}$$

$$= \frac{7 \times 6 \times 5}{3 \times 2 \times 1}$$

$$P(X = O^+) = \frac{3}{6}$$

$$P(X = A^+) = \frac{1}{6}$$

$$P(X = B^+) = \frac{1}{6}$$

$$P(X = AB^+) = \frac{1}{6}$$