

## Inferential stats

- 1 Central limit theorem (CLT)
- 2 Hypothesis testing (Null hypothesis, Alternate hypothesis)
- 3 CI (Confidence interval) ✗
- 4 Significance value (critical value) ✗
- 5 two and one tail test - (acceptance and rejection area) ✗
- 6 Standard error
- 7 P-value ✗
- 8 Sampling technique
- 9 Point estimate
- 10 Type 1 and type 2 error ✗
- 11 t-test (t-test, Chi-square, F-test, ANOVA)

## Sampling techniques → with respect to population

1 Simple Random Sample

2 Stratified Sampling

3 Systematic Sampling

4 Cluster Sampling

What is Population.

→ City

→ Country

→ World

Complete data set wrt any entity

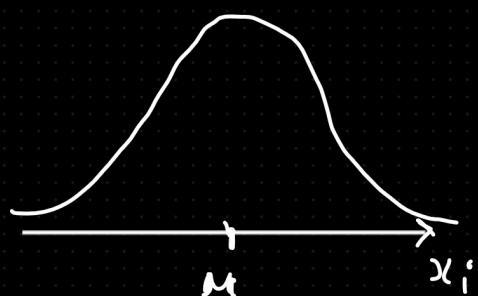
Sample ⇒ it is a subset or part of  
the population

① CLT ⇒ Population.

$$X \sim N(\mu, \sigma)$$

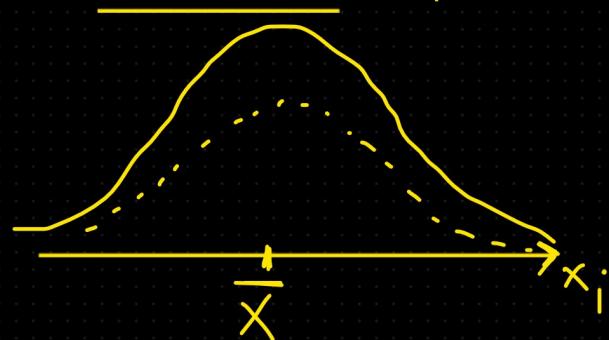
n = Sample Size ⇒ Any value

$$\Leftrightarrow n \geq 30$$



$$\left. \begin{aligned} S_1 &= \{x_1, x_2, x_3, \dots, x_n\} = \bar{x}_1 \\ S_2 &= \{x_1, x_2, x_3, \dots, x_n\} = \bar{x}_2 \\ S_3 &= \{x_1, x_2, x_3, \dots, x_n\} = \bar{x}_3 \\ &\vdots \\ S_n &= \{x_1, x_2, x_3, \dots, x_n\} = \bar{x}_n \end{aligned} \right\}$$

Normally Distributed



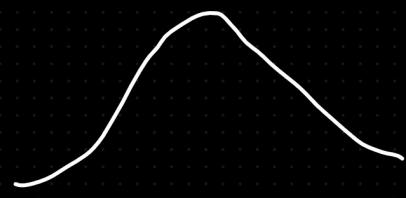
(Sampling Distribution)

↔ Sample mean Distribution

$$\leftarrow \bar{X} = N(\mu, \sigma)$$

Sampling Distribution of the mean

—



$$n = \text{Sample size}$$

$\equiv$

$$(n \geq 30)$$

$$\boxed{\bar{X} = N\left(\mu, \frac{\sigma}{\sqrt{n}}\right)}$$

Population Standard  
error

Point estimate  $\Rightarrow$  Population



Sample  $\Rightarrow$  mean

Sample size  $\Rightarrow$   $n \geq 30$

Point estimate

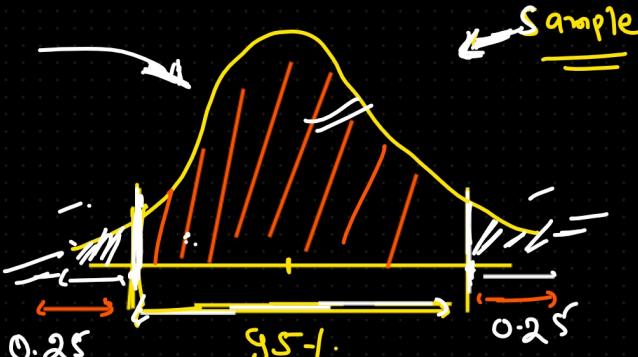
n  $\cdot$  of sample  $\Rightarrow$  K = 1, 2, 3, \dots, n

$1 \Rightarrow 35$   
 $2 \Rightarrow 30$   
 $3 \Rightarrow 37$

Sample  
30  
30  
30

## Hypothesis testing

- ① Null hypothesis ( $H_0$ )
- ② Alternative hypothesis ( $H_1$ )



ցՅ-1.

$$P \leq 0.1-1.$$

95-1.

$$P \leq 0.01$$

$C.I$  ցՅ-1.

$$P = 0.05$$

$P < 0.05$

## Hypothesis testing

(Any statement - or  
any assumption)



control

test

hypothesis (Null hypothesis)  $\Rightarrow H_0$  Person has not done any crime.

Evidence  $\rightarrow$  DNA test, fingerprints, CCTV footage

test → fail or  $P \leq \alpha$  →  
 accept null hypothesis  
 and we reject alternative hypothesis  
 → accept null hypothesis  
 and we reject alternative hypothesis  
 → reject the null hypothesis  
 and accept alternative hypo.

Statement  $\Rightarrow H_0$  (null hypothesis) (Population - hypothesis)  
 OR

Assumption

Population → Sample ← test (Z-test, t-test, chi-square, ANOVA, F-test)  
 (evidence)

(Point estimation, CI,  $\alpha \rightarrow P_{value}$ , Z-test, One-tail test)

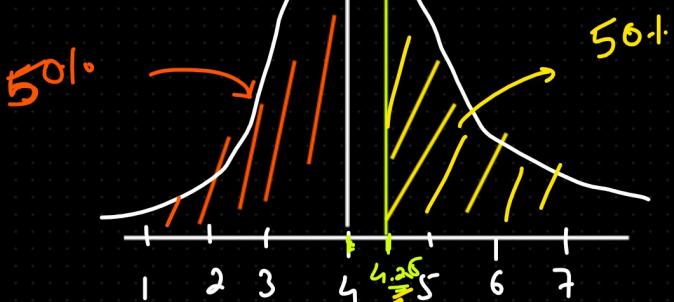
P-value  $\Rightarrow$  Probability value for the Null hypothesis to be true

$$\begin{array}{l} \text{95\% CI} \Rightarrow P \leq 0.05 \\ \text{99\% CI} \Rightarrow P \leq 0.01 \\ \text{99.9\% CI} \Rightarrow P \leq 0.001 \end{array}$$

Question  $X \sim N(4, 1)$

$$\downarrow \quad \downarrow$$

$$\mu \quad \sigma$$



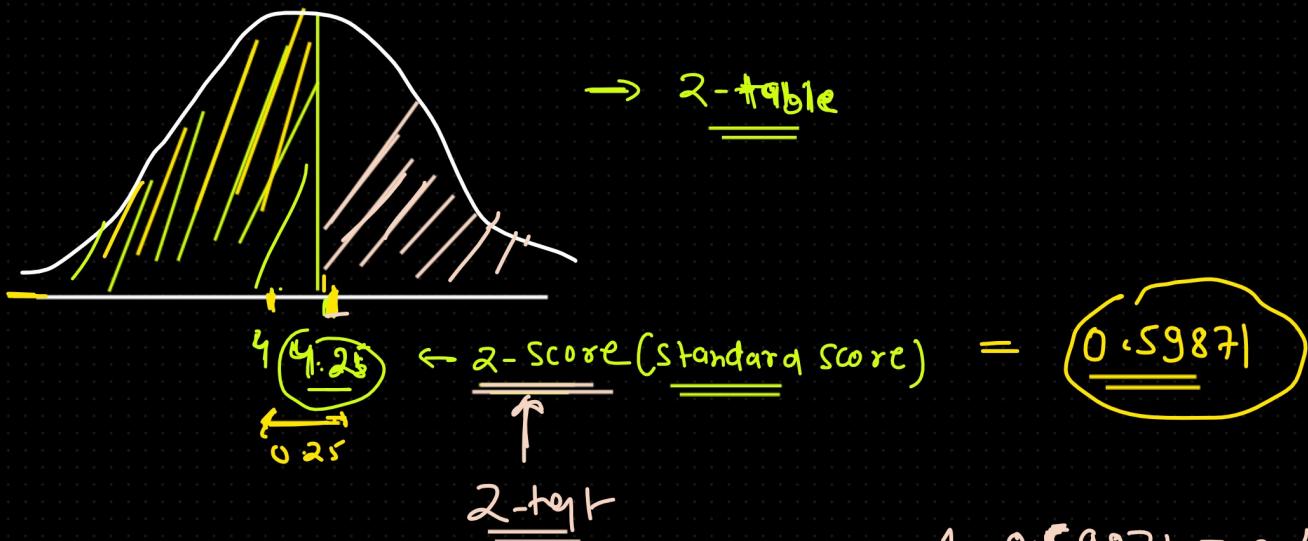
100\%

$$Z_i = 4.25$$

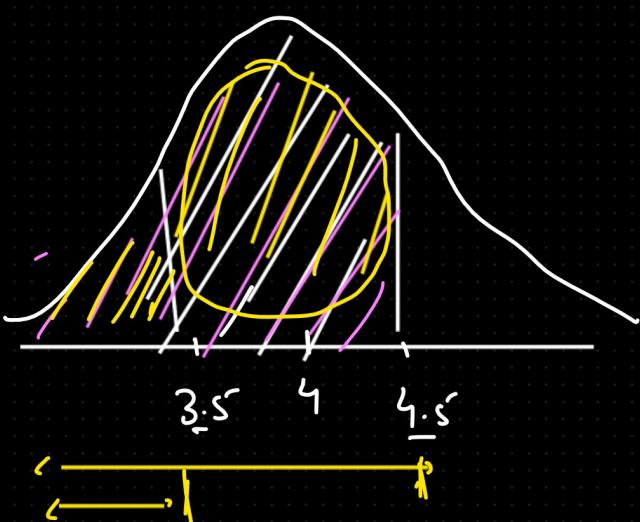
$$Z\text{-score} = \frac{\text{D.p.} - \text{mean}}{\text{- std}}$$

$$= \frac{4.25 - 4}{1} = 0.25$$

my D.P.  $\Rightarrow$  how many std dev from the mean



$$1 - 0.5987 = 0.4013 = \underline{\underline{0.131}}$$



$$\text{Data} = \begin{matrix} 3.5 \\ & \& \\ & 4.5 \end{matrix} \quad 0.30854$$

$$\text{Z-score} = \frac{3.5 - 4}{1} = -0.5$$

$$\text{Z-score} = \frac{4.5 - 4}{1} = +0.5$$

$$0.69146 - 0.30854 = 0.38292$$

$$= 38.29\%$$

$\downarrow$   
 $0.69146$

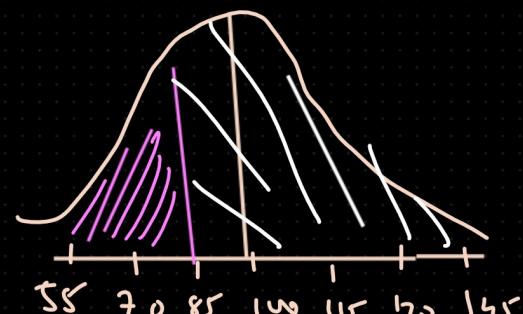
Q. In reading the avg IQ is 100, with the std dev of 15. What is the percentage of the population would you expect to have an IQ lower than 85.

$$\mu = 100, \sigma = 15$$

$$Z\text{-score} = \frac{85 - 100}{15} = \frac{-15}{15}$$
$$= -1$$

$$\underline{\text{AUC}} = 0.15866$$

$$\underline{\underline{15.86\%}} < \underline{85}$$



$$\text{IQ} \geq \underline{\underline{85}} \rightarrow 1 - 0.15866 = 0.8413$$
$$\Rightarrow \underline{84.13\%}$$

- (1) 2-tail
- (2) t-tail
- (3) ANOVA, f-test
- (4) Chi-square

(I) P value

two-one tail