

## Homework #3

Instructor: Dr. Zafeirakis Zafeirakopoulos  
Assistant: Gizem Süngü

Name:

Student Id:

**Course Policy:** Read all the instructions below carefully before you start working on the assignment, and before you make a submission.

- It is not a group homework. Do not share your answers to anyone in any circumstance. Any cheating means at least -100 for both sides.
- Do not take any information from Internet.
- No late homework will be accepted.
- For any questions about the homework, send an email to gizemsungu@gtu.edu.tr.
- Submit your homework (both your latex and pdf files in a zip file) into the course page of Moodle.
- Save your latex, pdf and zip files as "Name\_Surname\_StudentId".{tex, pdf, zip}.
- The answer which has only calculations without any formula and any explanation will get zero.
- The deadline of the homework is 02/06/20 23:55.

**Problem 1:**

(15+20=35 points)

Kuru Kahveci Mehmet Efendi (the producer), which is a coffee brand, supplies coffee beans to a coffee shop (the consumer) in Kadikoy. The coffee is supplied as 50 packages at each order and each package has 1 kg coffee beans. The consumer regards an order as acceptable provided that there are not more than 5 packages which have stale coffee beans. Rather than test all packages in the order, 10 packages are selected at random and tested.

(a) Find the probability that out of a sample of 10,  $d = 0, 1, 2, 3, 4, 5$  are stale when there are actually 5 stale packages in the order.

**(Solution)**

(b) Suppose that the consumer will accept the order provided that not more than  $m$  stale packages are found in the sample of 10.

- Find the probability that the order is accepted when there are 5 stale packages in the order.

**(Solution)**

- Find the probability that the order is rejected when there are 3 stale packages in the order.

**(Solution)**

**Problem 2:**

(20+5=25 points)

Hairdresser and barber shops reopened in Turkey under strict hygiene rules after almost two months at the 11th of May. Regarding to "new normal" rules, the number of customers arriving per hour at a hairdresser should be under control by the owner of the hairdresser shop. The hairdresser can accept at most 4 customers per hour with its conditions. Before arranging appointments with the customers, the owner wants to estimate whether there can be more demands than the owner can accept. The number of customers arriving per hour is assumed to follow a Poisson distribution with mean  $\lambda = 6$ .

(a) Compute the probability that more than 12 customers will arrive in a 3-hour period.

*(Solution)*

(b) What is the mean number of arrivals during a 3-hour period?

*(Solution)*

**Problem 3:**

(8+8+8+8+8=40 points)

Given a normal distribution with  $\mu = 35$  and  $\sigma = 7$ , find

(a) the normal curve area to the right of  $x = 21$ .

*(Solution)*

(b) the normal curve area to the left of  $x = 25$ .

*(Solution)*

(c) the normal curve area between  $x = 32$  and  $x = 41$ .

*(Solution)*

(d) the value of  $x$  that has 60% of the normal curve area to the left.

*(Solution)*

(e) the two values of  $x$  that contain the middle 75% of the normal curve area.

*(Solution)*