

Fuzzy Modelling

Exercise 9

Design a fuzzy controller. The controller has two inputs and one output. The range of changes for the input signals are ZX1, ZX2 and for the output signal is ZY.

The changes of the input signals are described using three symmetric triangular membership functions. The changes of the output signal are described using five symmetric Gaussian membership functions.

The modal values of the triangular membership functions are equal: $x1_{m1}$, $x1_{m2}$, $x1_{m3}$ and $x2_{m1}$, $x2_{m2}$, $x2_{m3}$. The bases of the triangular membership functions have the same length. The modal values of the Gaussian membership functions are equal: u_{m1} , u_{m2} , u_{m3} , u_{m4} , u_{m5} . The width coefficients of the Gaussian membership functions are equal. The rule base contains nine rules.

Table 1. The rule base of the fuzzy controller

u	x1			
x2		N	Z	P
	N	NN	N	Z
	Z	N	Z	P
	P	Z	P	PP

R1: IF x1 is N AND x2 is N THEN u is NN

R2: IF x1 is N AND x2 is Z THEN u is N

R3: IF x1 is N AND x2 is P THEN u is Z

.....

R9: IF x1 is P AND x2 is P THEN u is PP

Determine the change in the characteristics of the controller for the following height of the intersection of the output membership function h_{1U} , h_{2U} . The height of the intersection of input membership function is equal h_X .

Show in the graphic form:

- the model of the controller,
- the input triangular membership functions,
- the output Gaussian membership functions,
- the rule base
- the characteristics of the controller.

a)

$$ZX1 = [-4, 4] \quad x1_{m1} = -2 \quad x1_{m2} = 0 \quad x1_{m3} = 2$$

$$ZX2 = [-6, 6] \quad x2_{m1} = -4 \quad x2_{m2} = 0 \quad x2_{m3} = 4$$

$$ZU = [-8, 8] \quad u_{m1} = -6 \quad u_{m2} = -3 \quad u_{m3} = 0 \quad u_{m4} = 3 \quad u_{m5} = 6$$

case a1

$$h_{1U} = 0.25 \quad h_X = 0.50$$

case a2

$$h_{2U} = 0.75 \quad h_X = 0.50$$

b)

$$\begin{array}{llllll}
 ZX1 = [-5, 5] & x1_{m1} = -3 & x1_{m2} = 0 & x1_{m3} = 3 & & \\
 ZX2 = [-7, 7] & x2_{m1} = -5 & x2_{m2} = 0 & x2_{m3} = 5 & & \\
 ZU = [-10, 10] & u_{m1} = -8 & u_{m2} = -4 & u_{m3} = 0 & u_{m4} = 4 & u_{m5} = 8 \\
 \text{case b1} & & & & & \\
 h_{1U} = 0.25 & h_X = 0.50 & & & & \\
 \text{case b2} & & & & & \\
 h_{2U} = 0.75 & h_X = 0.50 & & & &
 \end{array}$$

The modal values of the triangular membership functions and the Gaussian membership functions:

$$\begin{array}{l}
 \text{mod}(A) = x_m : \\
 \mu_A(x_m) = 1 \quad \wedge \quad \text{card}(\text{nuc}(A)) = 1
 \end{array} \tag{1}$$