

# Optical Breakdown

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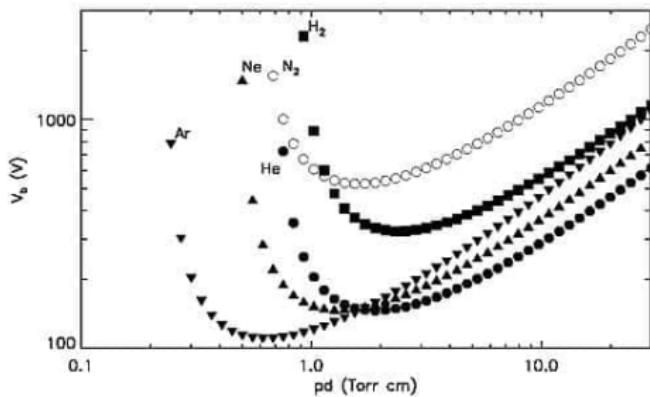
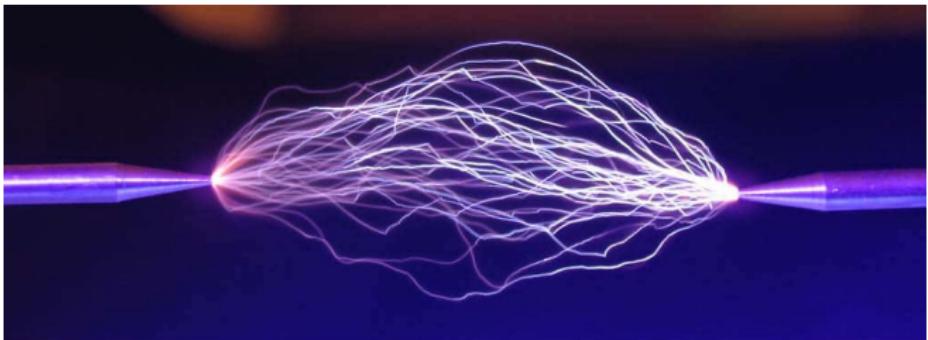
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## Abstract

Article studies optical breakdown effect in focused laser radiation. Theoretical description of breakdown formation in gases provided. Threshold fields are estimated. Spectra and oscillograms of breakdown spark measured in different substances.

# Introduction

# Static electrical breakdown

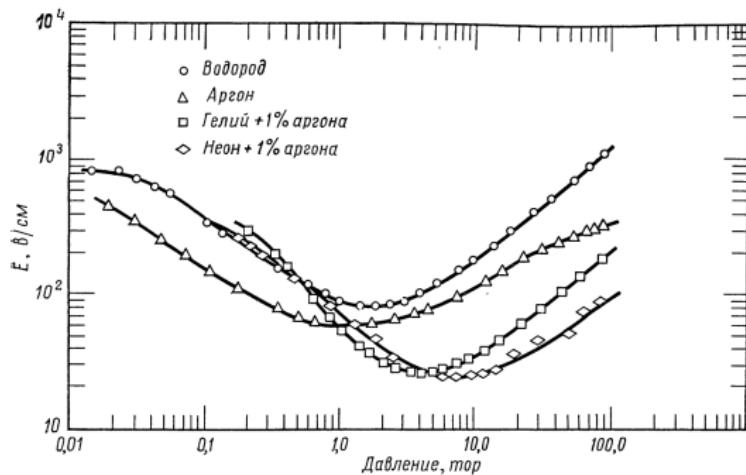


Paschen's law describes static electrical breakdown.

# Alternating-field electrical breakdown



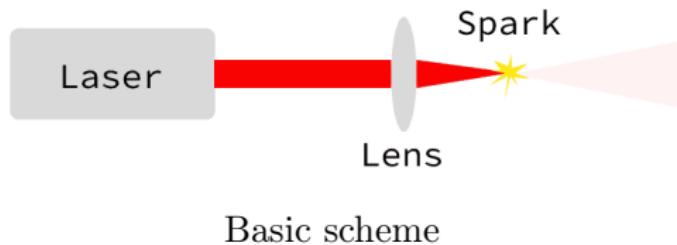
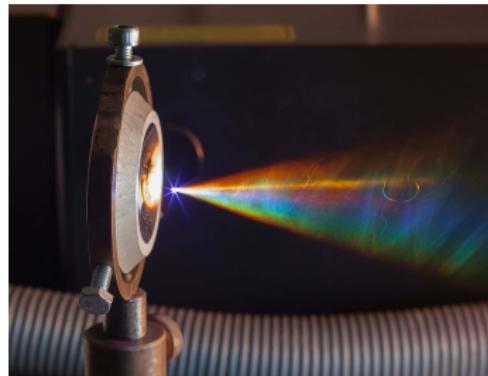
Mercury  
lamp



Threshold field on pressure  
( $f = 992$  MHz, diffusion length 0.631 cm)

Alternating field also induces breakdown.

# Optical breakdown



Femtosecond laser air  
breakdown

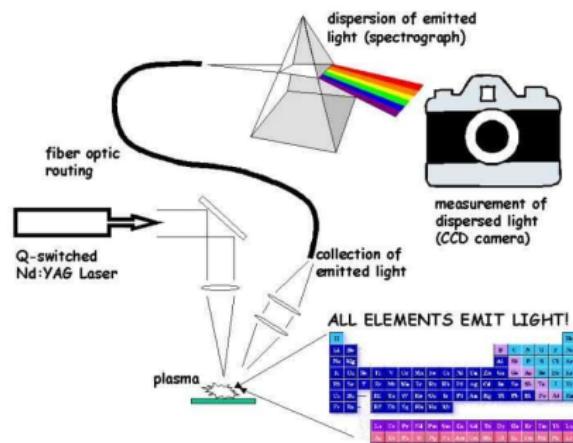
- Optical breakdown –  $E \approx 10^6 \div 10^7 \text{ V/cm}$ .
- Static and alternating field –  $E \approx 3 \cdot 10^4 \text{ V/cm}$ .

Characteristic parameters:

$$P \approx 30 \text{ MW}, \quad d = 0.2 \text{ mm}$$

$$S \approx 10^5 \text{ MW/cm}^2, \quad E \approx 6 \cdot 10^6 \text{ V/cm}$$

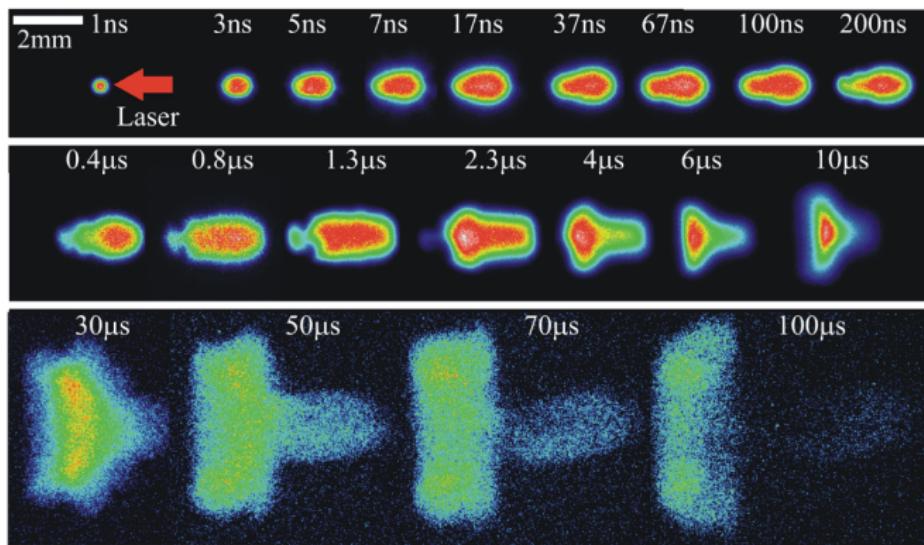
# Optical breakdown applications



Laser-Induced Breakdown Spectroscopy (LIBS)

- Laser-Induced Breakdown Spectroscopy.
- Connected with nuclear fusion.
- Development of quantum theory.

# Spark stages



Spark evolution in time

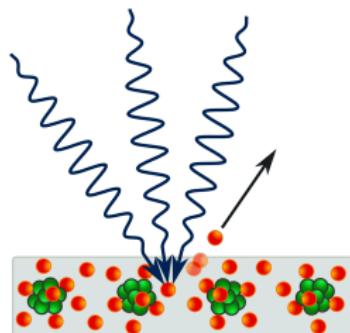
Three stages of laser spark:

- Breakdown: ionization and initial plasma formation.
- Plasma-photon interaction, plasma front movement.
- Shock wave spreading, glowing.

Theory

# Breakdown initiation – multiquantum photoeffect

Mechanism of atom ionization by radiation:



- $E$  – lightwave field.
- $\omega$  – lightwave frequency.
- $I$  – ionization energy.

Multiple photons are absorbed simultaneously:

$$n \cdot h\nu \sim n \cdot 2 \text{ eV} > I \sim 10 \div 20 \text{ eV}$$

Multiquantum photoelectric effect

## Multiquantum photoeffect probability

- $w$  – multiquantum photoeffect probability
- $n$  – number of absorbed photons
- $S$  – light intensity

$w \sim S \sim E^2$  – proportional to intensity.

$w \sim \frac{1}{I}$  – higher ionization energy implies lower probability.

$w \sim \frac{1}{\omega}$  – lower frequency implies more time to absorb photons.

$w \sim (\dots)^n$  –  $n$ -fold absorption.

$$w \sim \left( \frac{E^2}{\omega I} \right)^n$$

According to quantum mechanics L.V.Keldysh obtained:

$$w = B\omega n^{3/2} \left( \frac{\bar{e}e^2 E^2}{8m\omega^2 I} \right)^n \quad (1)$$

## Threshold field estimation

Within  $t_1 \approx 40$  ns in spot of  $r \approx 0.2$  mm  $N = 10^{13}$  electrons should appear:

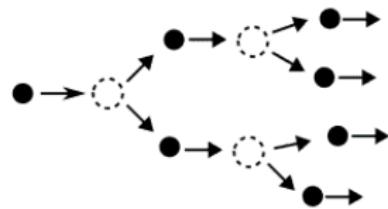
$$N = \frac{4}{3}\pi r^3 N_a t_1 w$$

$$E = \sqrt{\frac{8m\omega^2 I}{\bar{e}e^2}} \left[ \frac{w}{\omega n^{3/2}} \right]^{1/2n}$$

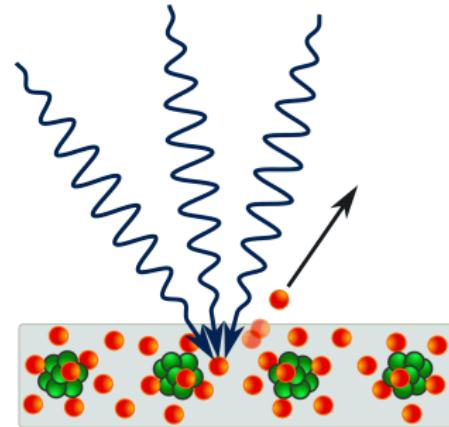
	Xenon	Argon	Air
Experiment <sup>1</sup> , V/cm	$(1.5 \div 2.3) \cdot 10^6$	$(2.7 \div 3.1) \cdot 10^6$	$(5 \div 13) \cdot 10^6$
Estimation, V/cm	$110 \cdot 10^6$	$150 \cdot 10^6$	$130 \cdot 10^6$

<sup>1</sup> According to: [1], [4], [5], [3], [6]

# Breakdown development – Avalanche vs Photoeffect



Electron avalanche

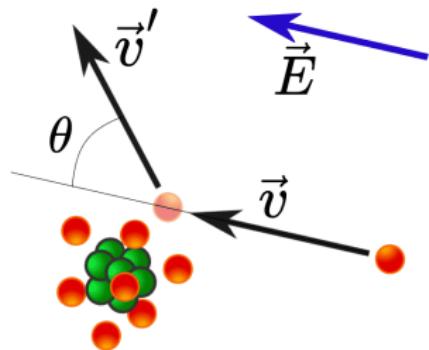


Multiquantum photoeffect

Breakdown development:

- $p \geq 1 \text{ atm}$  – electron avalanche.
- $p \ll 1 \text{ atm}$  – multiquantum photoeffect.

# Energy growth – classic theory



Electron-atom collision

Motion equation with 'friction':

$$m\dot{v} = -mv\nu_m - eE \quad E = E_0 \exp(-i\omega t)$$

$\nu_m = \nu_c(\overline{1 - \cos \theta})$  – effective collision frequency.

Work done by field on electron:

$$d\varepsilon/dt = \frac{e^2 E^2 \nu_m}{m(\omega^2 + \nu_m^2)}$$

Isolated electron cannot take away field energy. Collision is essential condition.

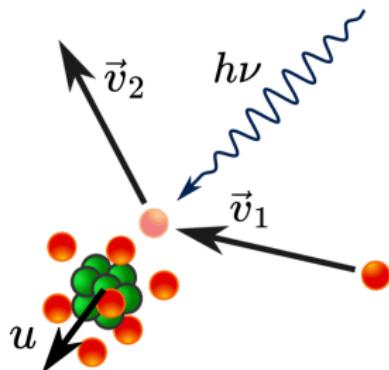
$$\varepsilon_{\text{osc}} = e^2 E_0^2 / 4m\omega^2 \sim 0.01 \text{ eV}$$

$\varepsilon \sim 5 \text{ eV}$  – electron energy

$$\boxed{\varepsilon \gg \varepsilon_{\text{osc}} \gg h\nu}$$

(2)

# Energy growth – quantum theory



Photon absorption

Photon energy is much higher than oscillation energy:

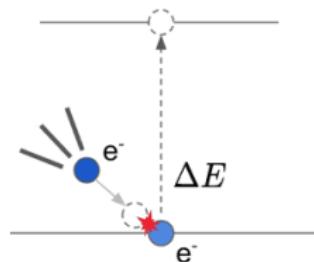
$$h\nu = 1.8 \text{ eV} \gg \varepsilon_{\text{osc}} \approx 2.3 \cdot 10^{-2} \text{ eV}$$

(ruby laser,  
 $\omega = 2.7 \cdot 10^{15} \text{ Hz}$ ,  $E \approx 10^7 \text{ V/cm}$ )

Quantum mechanics shows that classic formula conditions can be enhanced:

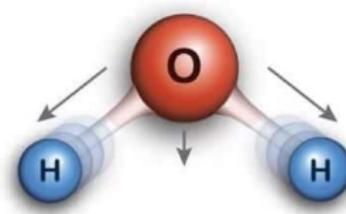
$$\varepsilon \geq h\nu \gg \varepsilon_{\text{osc}}$$

# Electron energy loss



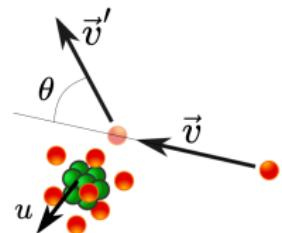
Excitation by collision

Non-elastic  
 $\varepsilon \sim 2/3I \div 3/4I$   
(inert gases)



Molecular vibrations

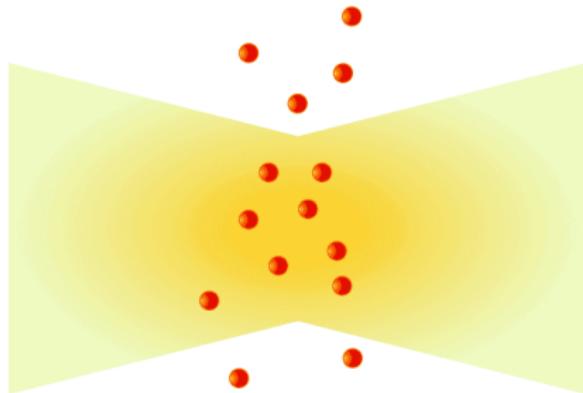
Non-elastic  
Whole range of  $\varepsilon$   
(molecular gases)



Collision recoil

Elastic  
All collisions

## Electron losses



Electron diffusion

Main loss mechanism – diffusion from focus spot.

## Breakdown criterion

- Pressure  $p \ll 100$  atm  $\Rightarrow$  energy losses  $\ll$  diffusion.
- Laser impulse time  $t_1$  is very short  $\Rightarrow$  diffusion is negligible.

Electron amount:

$$N_e = N_0 e^{\nu_i t} \quad \nu_i = \frac{1}{I} \frac{d\varepsilon}{dt}$$

$\nu_i$  – electron-atom ionization frequency,

Within impulse time  $t_1 \approx 40$  ns  $N_1 \approx 10^{13}$  electrons should appear:

$$\boxed{\nu_i > \frac{\ln(N_1/N_0)}{t_1}}$$

# Threshold field estimation

Combining ionization frequency  $\nu_i$  with energy growth  $d\varepsilon/dt$ :

$$E = \left[ \frac{m\omega^2 I}{e^2 \nu_m t_1} \ln \frac{N_1}{N_0} \right]^{1/2}$$

	Xenon	Argon	Air
Experiment <sup>2</sup> , V/cm	$(1.5 \div 2.3) \cdot 10^6$	$(2.7 \div 3.1) \cdot 10^6$	$(5 \div 13) \cdot 10^6$
Estimation 1, V/cm	$110 \cdot 10^6$	$150 \cdot 10^6$	$130 \cdot 10^6$
Estimation 2, V/cm	$1.5 \cdot 10^6$	$2.7 \cdot 10^6$	$2.4 \cdot 10^6$

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<sup>2</sup>According to: [1], [4], [5], [3], [6]

# Measurements and Results

# Experimental setup

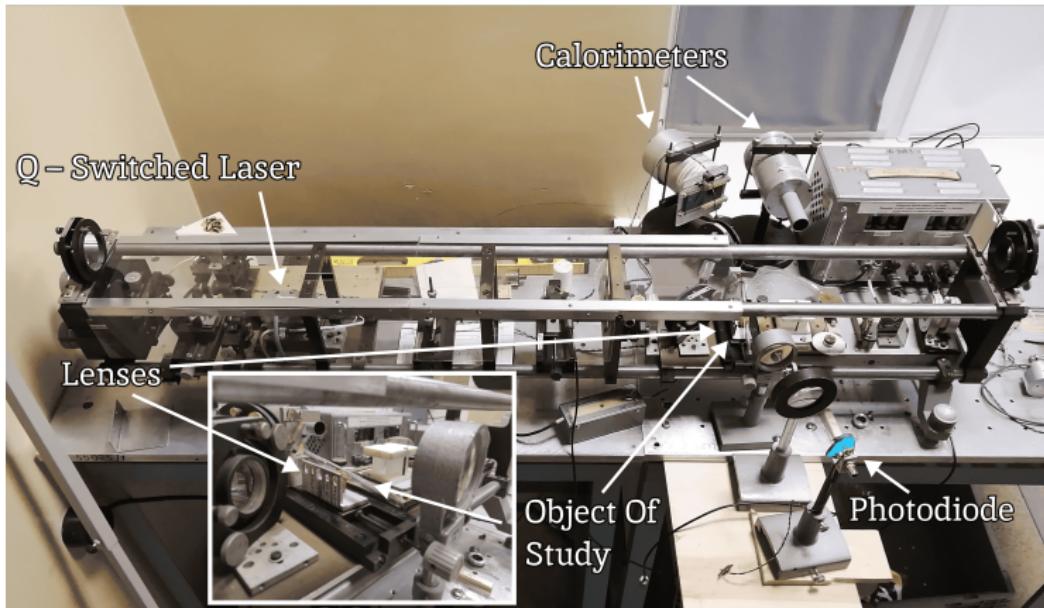
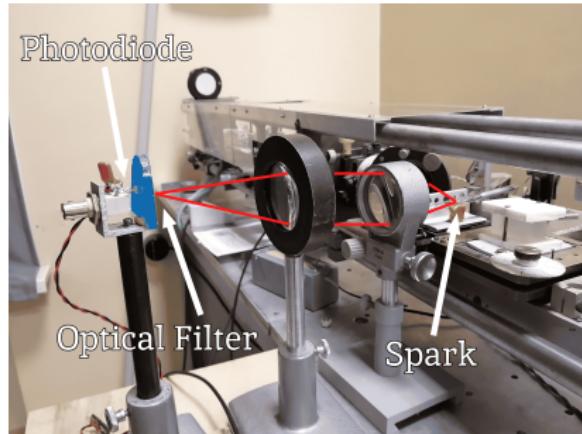
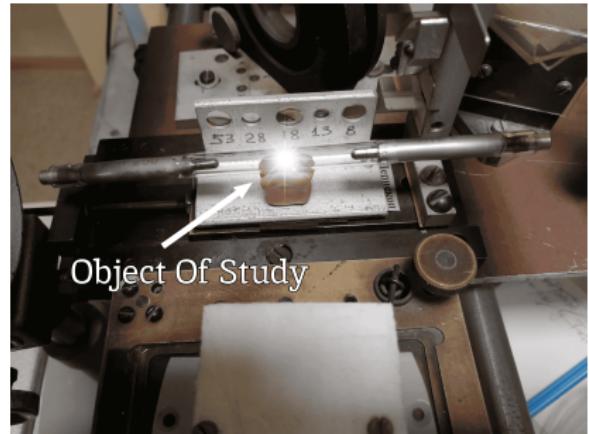


Photo of the experimental setup

# Experimental setup

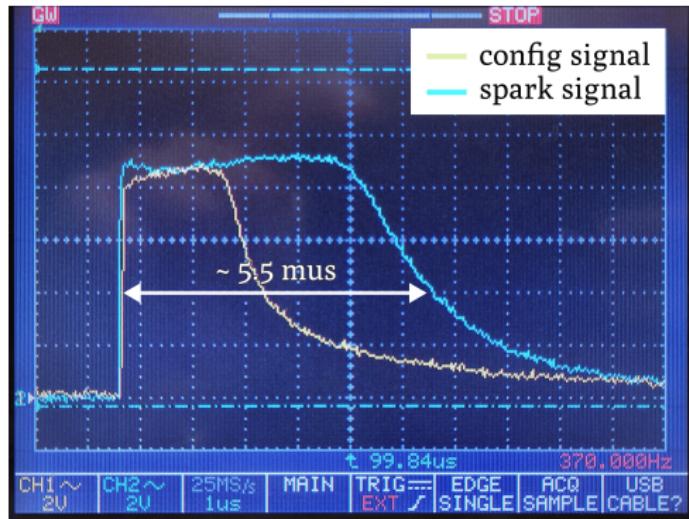


The lens system captures the spark's light



Platform with a set of lenses for beam focusing

# Air breakdown



Intensity over time

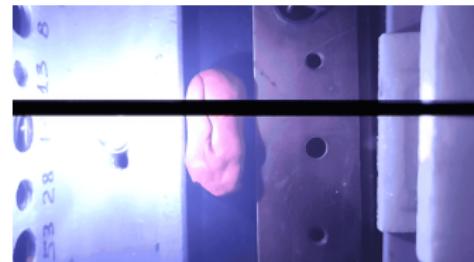
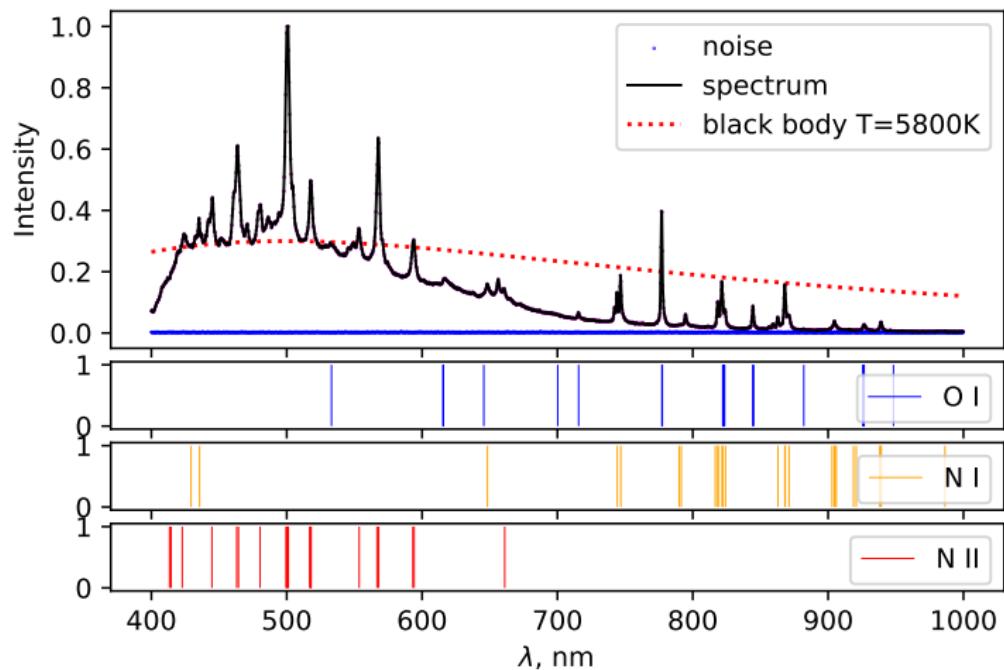


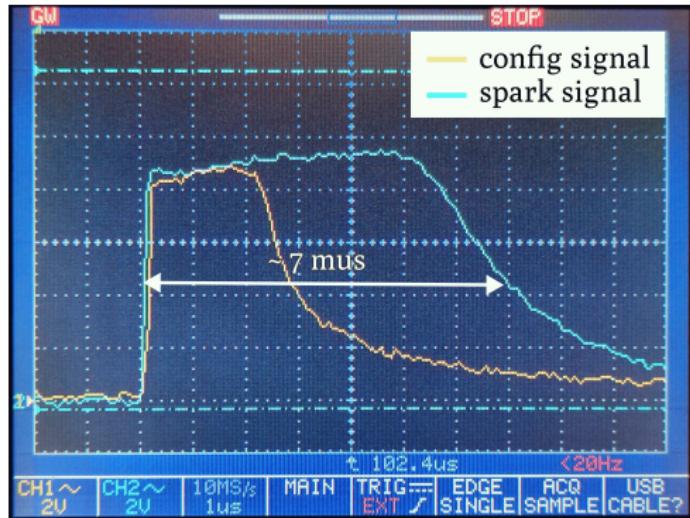
Photo of the spark

# Air breakdown



Breakdown spectrum

# Xenon breakdown

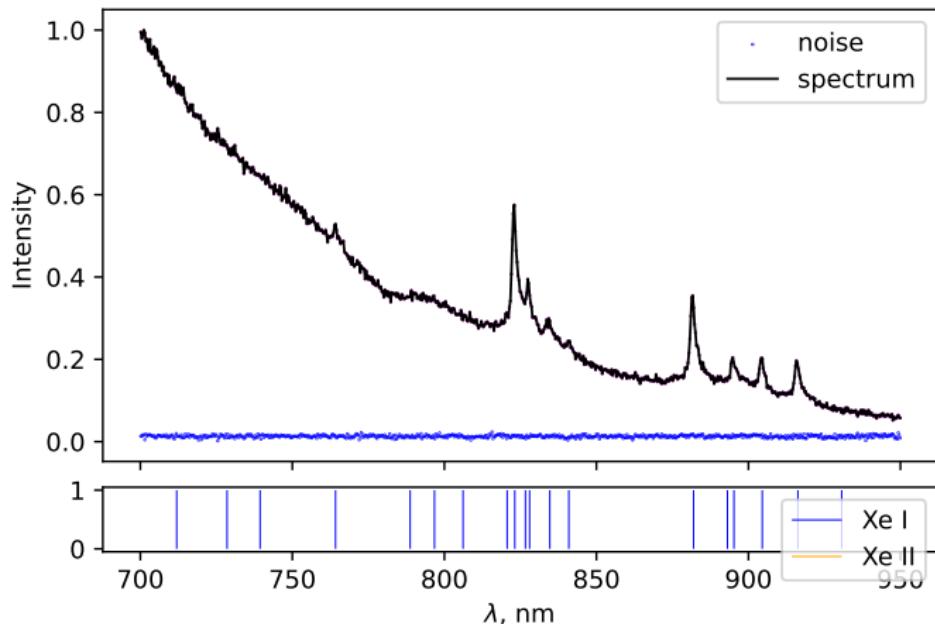


Intensity over time



Photo of the spark

# Xenon breakdown

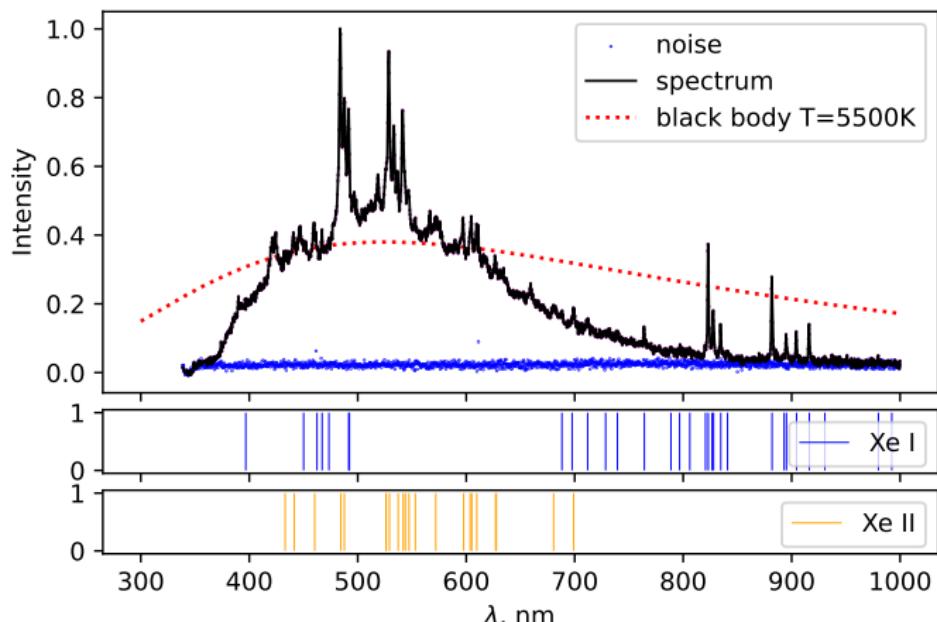


Breakdown spectrum



Lamp  
ДКСИІ

# Xenon breakdown

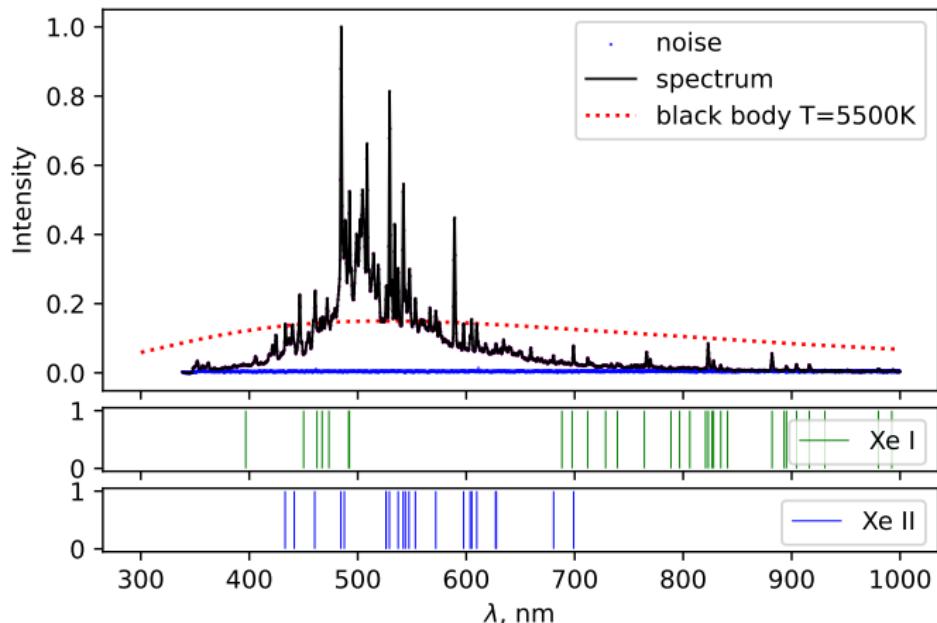


Breakdown spectrum



Lamp  
ИФП-800

# Xenon breakdown

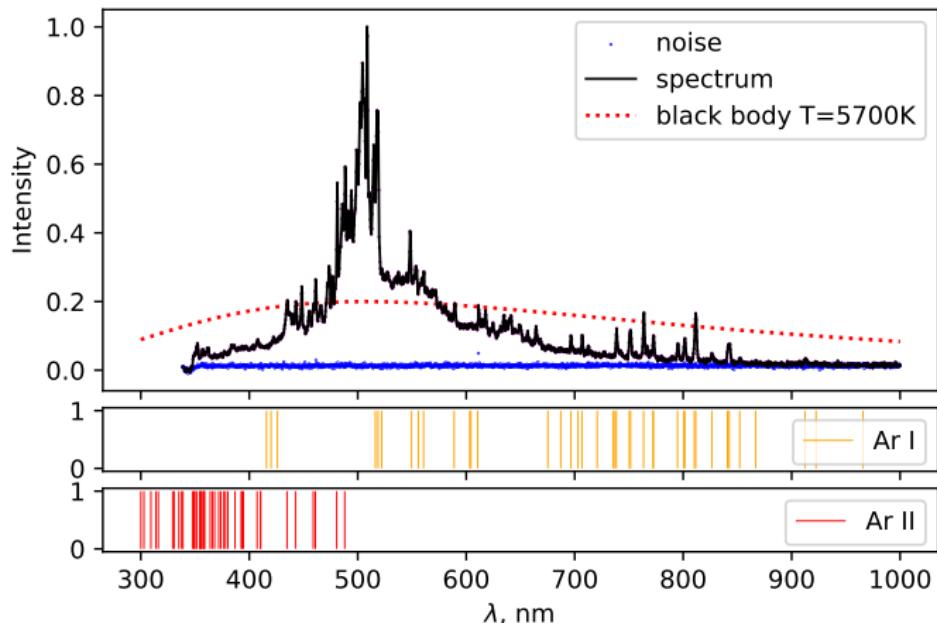


Breakdown spectrum



Thyratron  
TT3-  
0.1/1.3

# Argon breakdown

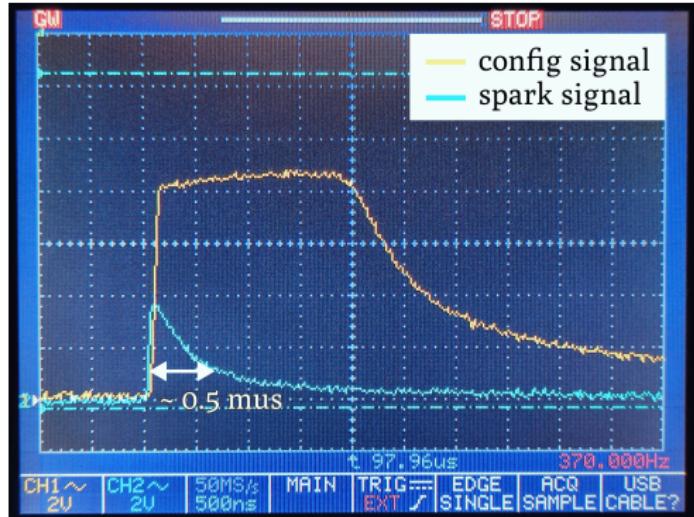


Breakdown spectrum



Thyratron  
ТГИ1-3/1

# Water breakdown



Intensity over time

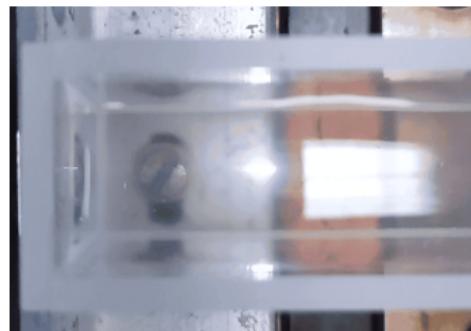
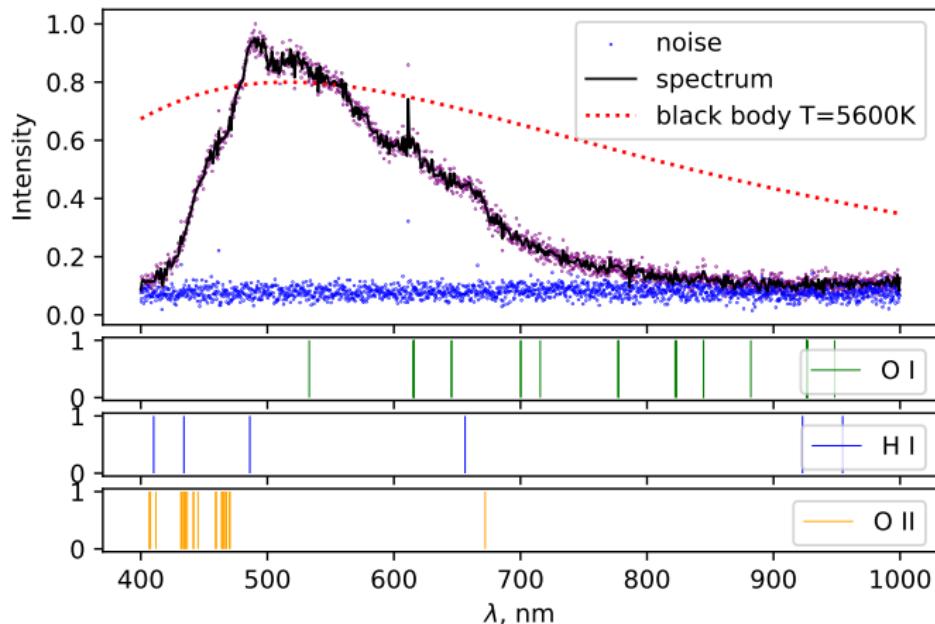
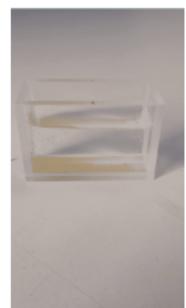


Photo of the spark

# Water breakdown

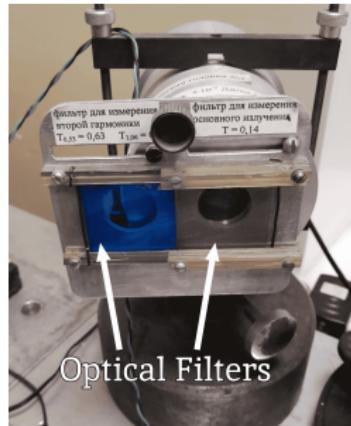


Breakdown spectrum



Water cuvette

# Peak intensity estimation



Calorimeter  
measures impulse  
energy

Energy measured by calorimeter:

$$W = (0.08 \pm 0.01) \text{ J.}$$

The diameter of spot in the focal plane:

$$d = \theta f = (54 \pm 16) \mu\text{m},$$

$\theta \approx 3.0 \cdot 10^{-3}$  rad – beam divergence,  
 $f = 18 \text{ mm}$  – focal length.

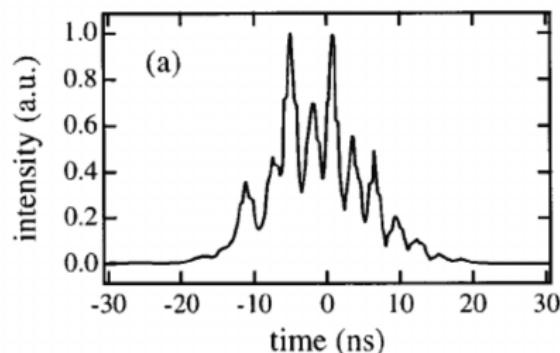
# Peak intensity estimation

Impulse peak intensity:

$$S_{\min} = \Theta \cdot \frac{W}{\tau \left( \frac{\pi d^2}{4} \right)} = (1.8 \pm 0.6) \cdot 10^{11} \frac{\text{W}}{\text{cm}^2},$$

$\tau = 40$  ns – pulse time,

$\Theta \sim 2$  – pulseform factor.



Temporal profile of the passively Q switched Nd pump laser

# Conclusion

# Conclusion

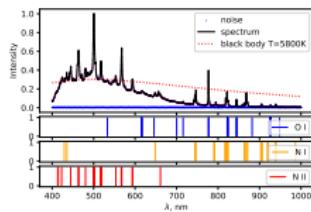
- Laser breakdown was achieved. Threshold field for air was measured.

$$E_{air} = 8.2 \cdot 10^6 \text{ V/cm}$$

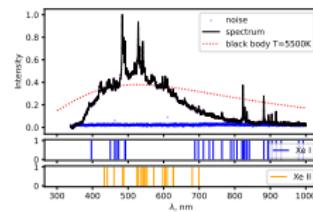
- Theoretical threshold fields agree with experiment for atomic gases.

	Xenon	Argon	Air
Experiment <sup>3</sup> , V/cm	$(1.5 \div 2.3) \cdot 10^6$	$(2.7 \div 3.1) \cdot 10^6$	$(5 \div 13) \cdot 10^6$
Estimation, V/cm	$1.5 \cdot 10^6$	$2.7 \cdot 10^6$	$2.4 \cdot 10^6$

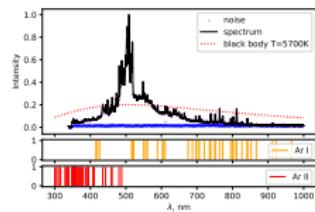
- Spectra and time characteristics of sparks were collected.



Air spectrum



Xenon spectrum



Argon spectrum

<sup>3</sup>According to: [1], [4], [5], [3], [6]

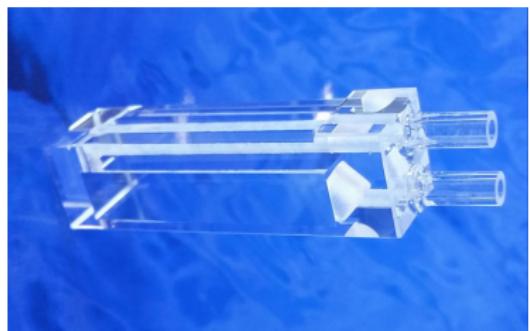
# Possible improvements

Our work can be enhanced:

- Use high-precision photodiodes to measure laser impulse.
- Obtain spark pictures with CCD/ICCD camera.
- Measure threshold fields in optical gas cuvette.
- Apply more advanced theory for estimation (kinetic equations for electrons).



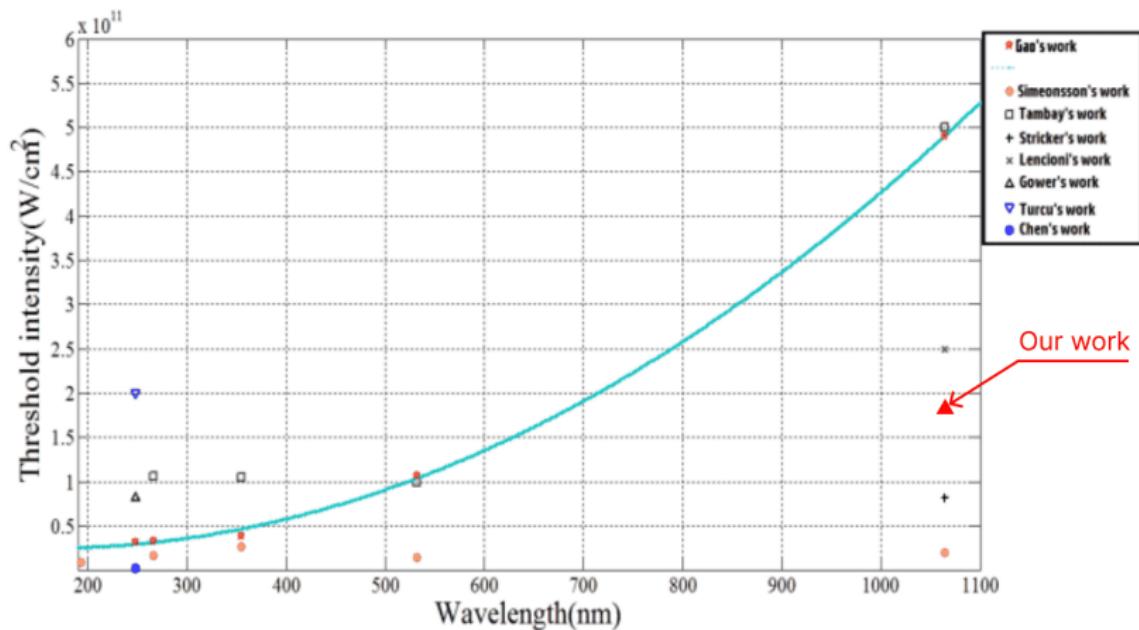
ICCD camera



Optical gas cuvette

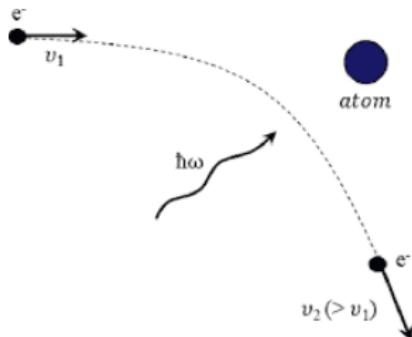
Thank you for your attention!

## Appendix: Air breakdown threshold



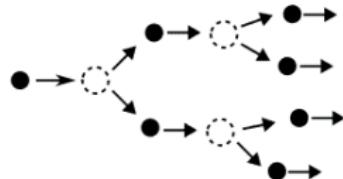
Variety of threshold fields

## Appendix: Electron avalanche



Inverse bremsstrahlung

- Classic: in alternating field oscillation energy converts to heat in collisions.
- Quantum: electron absorbs photons on collisions.

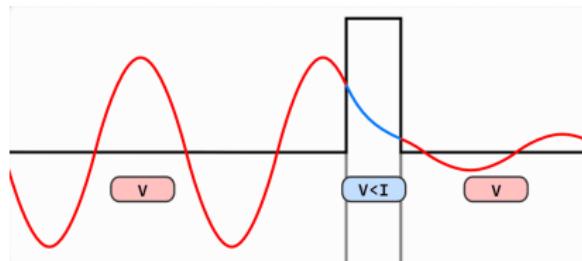


Electron avalanche

Electron avalanche develops.

## Appendix: Tunneling vs Photoeffect

Two mechanisms of electron ejection by radiation:



Quantum tunneling

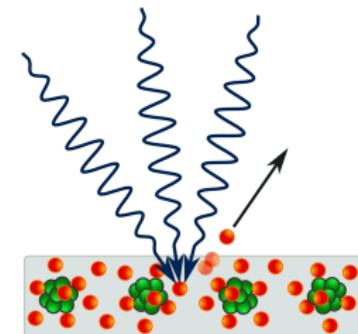
- $E$  – lightwave field.
- $\omega$  – lightwave frequency.
- $I$  – ionization energy.

$\Delta \sim \frac{I}{eE}$  – potential barrier width.

$v \sim \sqrt{I/m}$  – electron velocity.

$\tau \sim \Delta/v \sim \frac{\sqrt{Im}}{eE}$  – electron time-of-flight of barrier.

$\omega\tau \ll 1$  – 'static' field condition.



Multiquantum photoelectric effect

$\omega\tau \gg 1$  – condition of many quanta absorption on oscillation.

Estimation on optical frequencies gives  $\omega\tau \gg 1$ .

-  Y. P. Raizer, 'Laser Spark and Propagation of Discharges'.
-  S. S. Harilal, B. E. Brumfield, M. C. Phillips, 'Lifecycle of laser-produced air sparks'.
-  Kai-Ting Yen, Chih-Hung Wu, Pin-Hsun Wang, Pi-Hui Tuan, Kuan-Wei Su, 'Investigating the Threshold Conditions of Air Breakdown with Mode-Locked Q-Switched Laser Pulses, and the Temporal Dynamics of Induced Plasma with Self-Scattering Phenomenon'
-  F. Morgan, 'Laser beam induced breakdown in helium and argon'.
-  Yosr E. E-D. Gamal, M. A. Mahmoud, Nagia Dawood, 'Numerical investigation of the threshold intensity dependence on gas pressure in the breakdown of xenon by different laser wavelengths'.
-  Zhixing Gao, Lixuan Hana, Jing Lia, 'Investigation of laser induced air breakdown thresholds at 1064, 532, 355, 266 and 248nm'.
-  H. Nishimura, T. Matsuda, A. Danjo, 'Elastic Scattering of Electrons from Xenon'.
-  K. P. Subramanian, V. Kumar, 'Total electron scattering cross sections for argon, krypton and xenon at low electron energies'.
-  A. Roldan, J.M. Perez, 'Energy deposition model for low-energy electrons (10–10 000 eV) in air'.