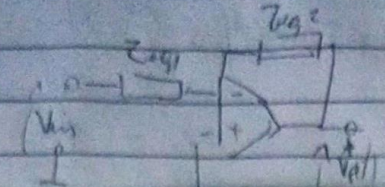


Prova (1)

a) $G = \frac{R_2}{R_1} = \frac{V_{out}}{V_{in}}$



$$C_1 = 0,1 \cdot 10^{-3} \rightarrow \frac{1}{5 \cdot 0,1 \cdot 10^{-3}} = \frac{10^4}{5} = \frac{10 \cdot 10^3}{5}$$

$$Z_{eq1} = \frac{(R_1 + C_1 \parallel R_2)}{R_1 + (1 \parallel R_2)} \quad \left(2,4 \cdot 10^3 + \frac{10 \cdot 10^3}{5} \right) \cdot 1,6 \cdot 10^3$$

$$Z_{eq1} = 1,6 \cdot 10^3 \cdot \left(2,4 + \frac{10}{5} \right) \quad \left(2,4 + \frac{10}{5} + 1,6 \right) \cdot 10^3$$

$$Z_{eq1} = \left(3,84 + \frac{16}{s} \right) \cdot 10^3 \cdot \frac{s}{4s+10} = \frac{3840s}{4s+10} + \frac{16 \cdot 10^3 \cdot s}{s(4s+10)}$$

$$Z_{eq1} = \frac{3840s}{4s+10} + 16 \cdot 10^3 \cdot \frac{s}{4s+10} = \frac{3840s + 16 \cdot 10^3}{4s+10}$$

$$Z_{eq2} = \frac{(R_3 + C_2) \cdot R_4}{R_3 + R_4 + C_2} \Rightarrow C_2 = 0,2 \cdot 10^{-3} \rightarrow 2 \cdot 10^{-4} \rightarrow \frac{10^4}{25} = \frac{5 \cdot 10^3}{5}$$

$$\left(10^3 + \frac{5 \cdot 10^3}{s} \right) \cdot 6,8 \cdot 10^3 \cdot \frac{s}{7,8s+5} = \frac{6,8 \cdot 10^3 \cdot s(1 + \frac{5}{s})}{7,8s+5} = \frac{6,8 \cdot 10^3 (s+5)}{7,8s+5}$$

$$\frac{10^3 (1 + 6,8 + \frac{5}{s})}{7,8s+5} = \frac{(7,8 \cdot 5)}{7,8s+5} = \frac{7,8s+5}{7,8s+5}$$

$$\frac{6,8 \cdot 10^3 (s+5)}{7,8s+5} = \frac{6,8 \cdot 10^3 s + 34 \cdot 10^3}{7,8s+5}$$

$$- \frac{Z_{eq2}}{Z_{eq1}} = \frac{6,8 \cdot 10^3 s + 34 \cdot 10^3}{7,8s+5} \cdot \frac{4s+10}{3,84s + 16 \cdot 10^3} = \frac{27,2s^2 + 68s + 136s + 340}{29,95s^2 + 124,4s + 19,2s + 40}$$

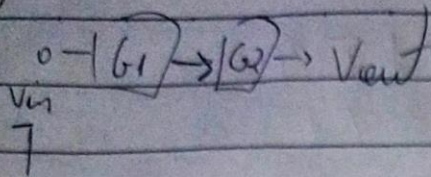
$$- \frac{Z_{eq2}}{Z_{eq1}} = \frac{27,2s^2 + 204s + 340}{29,95s^2 + 144s + 40} \quad \text{dividindo por } 29,95 \Rightarrow \frac{0,9s^2 + 6,81s + 11,35}{s^2 + 4,80s + 2,67}$$

$$\left(3.84 + \frac{10}{5} \right) \left(7.4 + \frac{5}{5} \right)$$

$$28.41$$

$$\textcircled{b} \quad - \frac{R_6}{R_5} = G = \frac{550}{1000} = -0.55$$

① ②

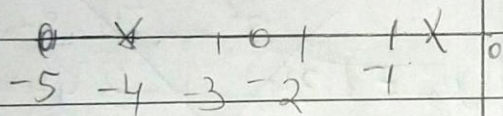


$$V_{out} = V_{in} \cdot G_1 \cdot G_2 \quad \frac{V_{out}}{V_{in}} = G_1 \cdot G_2$$

$$G_{total} = 0,55 \cdot \frac{0,9s^2 + 6,41s + 11,35}{s^2 + 4,8s + 2,67}$$

$$G_T = \frac{0,495s^2 + 3,745s + 6,242}{s^2 + 4,8s + 2,67}$$

③



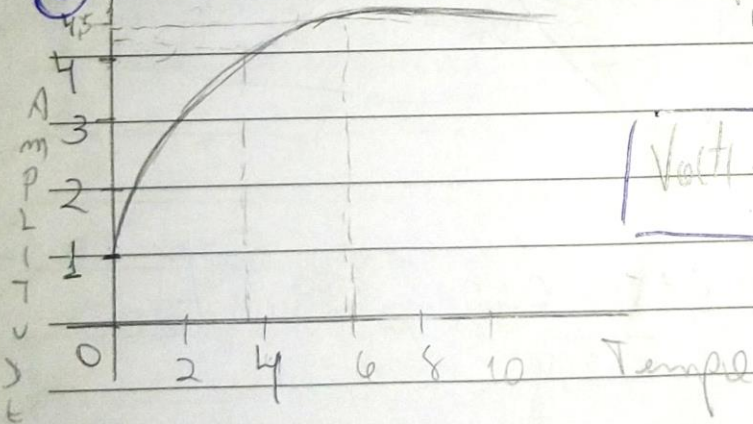
④ $V_{in}(t) = 2 [V]$

$\frac{2}{s} \cdot G_T = V_{out}(s)$

$F(s) = \frac{2(0,495s^2 + 3,745s + 6,242)}{s(s^2 + 4,8s + 2,67)}$

⑤

$V_{in} = 2$



Aplicando MATLAB

$\frac{4,167}{s} - \frac{3,745s + 6,242}{s^2 + 4,8s + 2,67}$

$V_{out}(t) = 4,167 - 3,64e^{-2,14t} (\cos(1,75t) + 0,94 \sin(1,75t))$

⑥

Como tem s^2 ele é um de segunda ordem pelo configuração dos polos, e obtendo o gráfico em classificação como superamortecido.

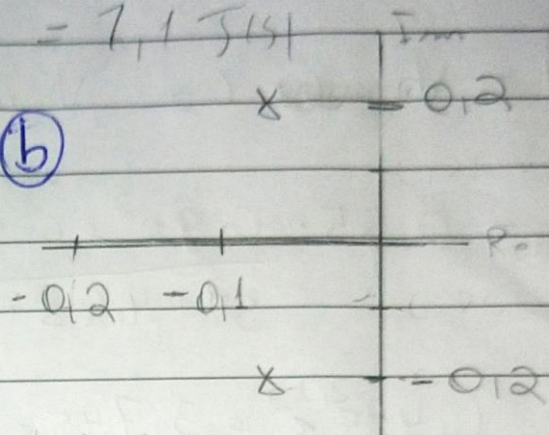
$$\textcircled{a} \quad 40,2 \ddot{\theta}(t) + 6,1 \dot{\theta}(t) + 1,4 \theta(t) = 7,1 T(t)$$

$$\textcircled{a} \quad s^2 40,2 \Theta(s) + s \cdot 6,1 \Theta(s) + 1,4 \Theta(s) = 7,1 T(s)$$

$$\Theta(s) (s^2 40,2 + s \cdot 6,1 + 1,4) = 7,1 T(s)$$

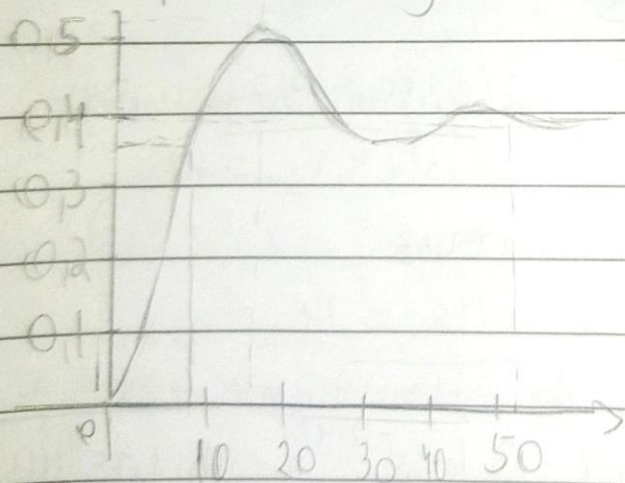
$$G = \frac{\Theta}{T} = \frac{7,1}{s^2 40,2 + s \cdot 6,1 + 1,4}$$

$$\textcircled{b}$$



$$\textcircled{c} \quad \text{Valor final} = \underline{0,394} \quad , \quad \text{instanto de pico} = \underline{15,78 = T_p}$$

$$\text{Tempo de acomodação} = \underline{T_s = 51,5 s}$$



$$\textcircled{d} \quad G(s) = \frac{k}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

$$\omega_n = 1,34 \quad k = 3,944$$

$$2\zeta\omega_n = 6,1$$

$$\zeta = \frac{6,1}{2 \cdot 1,34} = 2,27$$

$$\textcircled{2} d) \quad k = \frac{4100}{0,1} \cdot \frac{0,394}{0,1} = \boxed{3,94}$$

$$v_p = \frac{0,512 - 0,394}{0,394}$$

$$v_p = 30\%$$

$$\ln 0,3 = \frac{-\tilde{z}\pi}{\sqrt{1-\tilde{z}^2}} \quad \ln(0,3) = \frac{-\tilde{z}\pi}{\sqrt{1-\tilde{z}^2}} \Rightarrow 1,2 = \frac{-\tilde{z}\pi}{\sqrt{1-\tilde{z}^2}}$$

$$1,45 (1-\tilde{z}^2) = \tilde{z}^2 \pi^2$$

$$1,45 = 11,3 \tilde{z}^2$$

$$\tilde{z}^2 = 0,128$$

$$\boxed{\tilde{z} = 0,357}$$

$$T_p = \pi$$

$$\omega_n \sqrt{1-\tilde{z}^2}$$

$$\omega_n = \frac{\pi}{15,78 \sqrt{1-\tilde{z}^2}} = 0,213 \text{ [w/s]}$$

2 e) m00 olendum

$$\ln 0,05 = \frac{-\tilde{z}\pi}{\sqrt{1-\tilde{z}^2}}$$

$$-3 = \frac{-\tilde{z}\pi}{\sqrt{1-\tilde{z}^2}} \Rightarrow 9 = \frac{\tilde{z}^2 \pi^2}{1-\tilde{z}^2} \Rightarrow 9(1-\tilde{z}^2) = \tilde{z}^2 \pi^2 \therefore 9 - 9\tilde{z}^2 = \tilde{z}^2 \pi^2$$

$$\frac{9}{18,46} = \tilde{z}^2$$

$$T_p = 10 = \pi$$

$$\omega_n \sqrt{1-\tilde{z}^2}$$

$$\omega_n = \frac{\pi}{10 \sqrt{1-\tilde{z}^2}} = \boxed{0,43}$$

$$\boxed{\tilde{z} = 0,69}$$

$$x = 0,3$$

$$-0,3$$

$$x = -0,3$$

Q.1

~~Se~~ Eu consideraria um subnormal máximo Admissível de 0,1%, pois visto que a precisão é muito importante por qualquer milímetro ser fatal, é bem ser cada vez mais próximo de zero