## AIND-Planning Project

## **Optimal Plans**

| Problem 1.   |                                 |
|--|---------------------------------|
| Init(At(C1, SFO) ∧ At(C2, JFK)   | Load(C1, P1, SFO)               |
| $\wedge$ At(P1, SFO) $\wedge$ At(P2, JFK)  | Fly(P1, SFO, JFK)               |
| $\land$ Cargo(C1) $\land$ Cargo(C2)  | Load(C2, P2, JFK)               |
| $\wedge$ Plane(P1) $\wedge$ Plane(P2)  | Fly(P2, JFK, SFO)               |
|  | Unload(C2, P2, SFO)             |
| Goal(At(C1, JFK) ∧ At(C2, SFO))  | Unload(C1, P1, JFK)             |
| Problem 2.   |                                 |
| $Init(At(C1, SFO) \land At(C2, JFK) \land At(C3, ATL)$                               | Load(C1, P1, SFO)               |
| $\wedge$ At(P1, SFO) $\wedge$ At(P2, JFK) $\wedge$ At(P3, ATL)                       | Fly(P1, SFO, JFK)               |
| $\land$ Cargo(C1) $\land$ Cargo(C2) $\land$ Cargo(C3)                                | Load(C2, P2, JFK)               |
| $\land$ Plane(P1) $\land$ Plane(P2) $\land$ Plane(P3)                                | Fly(P2, JFK, SFO)               |
|  | Load(C3, P3, ATL)               |
| Goal(At(C1, JFK) $\land$ At(C2, SFO) $\land$ At(C3, SFO))                            | Fly(P3, ATL, SFO)               |
|  | Unload(C3, P3, SFO)             |
|  | Unload(C2, P2, SFO)             |
|  | Unload(C1, P1, JFK)             |
| Problem 3.   |                                 |
| $Init(At(C1,SFO) \land At(C2,JFK) \land At(C3,ATL) \land At(C4,ORD)$                 | Load(C2, P2, JFK)               |
| $\land$ At(P1, SFO) $\land$ At(P2, JFK)  | Fly(P2, JFK, ORD)               |
| $\land$ Cargo(C1) $\land$ Cargo(C2) $\land$ Cargo(C3) $\land$ Cargo(C4)              | Load(C4, P2, ORD)               |
| $\land$ Plane(P1) $\land$ Plane(P2)  | Fly(P2, ORD, SFO)               |
| $\land$ Airport(JFK) $\land$ Airport(SFO) $\land$ Airport(ATL) $\land$ Airport(ORD)) | Lo <mark>ad(C1, P1, SFO)</mark> |
| Goal(At(C1, JFK) $\wedge$ At(C3, JFK) $\wedge$ At(C2, SFO) $\wedge$ At(C4, SFO))     | Fly(P1, SFO, ATL)               |
|  | Load(C3, P1, ATL)               |
|  | Fly(P1, ATL, JFK)               |
|  | Unload(C4, P2, SFO)             |
|  | Unload(C3, P1, JFK)             |
|  | Unload(C2, P2, SFO)             |
|  | Unload(C1, P1, JFK)             |

Priya: Awesome: Good work! You have identified the optimal no. of steps for each of the 3 problems.

• Compare and contrast non-heuristic search result metrics (optimality, time elapsed, number of node expansions) for Problems 1,2, and 3. Include breadth-first, depth-first, and at least one other uninformed non-heuristic search in your comparison; Your third choice of non-heuristic search may be skipped for Problem 3 if it takes longer than 10 minutes to run, but a note in this case should be included.

| Search                    | expansions | goal tests | new nodes | plan length | time    |
|---------------------------|------------|------------|-----------|-------------|---------|
| breadth_first_search      | 43         | 56         | 180       | 6           | 0.2525  |
| breadth_first_tree_search | 1458       | 1459       | 5960      | 6           | 10.6024 |
| depth_first_graph_search  | 21         | 22         | 84        | 20          | 0.1643  |
| depth_limited_search      | 101        | 271        | 414       | 50          | 0.5415  |
| uniform_cost_search       | 55         | 57         | 224       | 6           | 0.2941  |

In problem 1, depth\_first variants failed to deliver optimal plans, even though they perform well in term expansions, goal tests and new nodes. Overall, breadth\_first\_search is the winning search (optimal, fast).

| Search                   | expansions | goal tests | new nodes | plan length | time     |
|--------------------------|------------|------------|-----------|-------------|----------|
| breadth_first_search     | 3343       | 4609       | 30509     | 9           | 79.2501  |
| depth_first_graph_search | 624        | 625        | 5602      | 619         | 17.2183  |
| uniform_cost_search      | 4852       | 4854       | 44030     | 9           | 119.1123 |

| Search                   | expansions | goal tests | new nodes | plan length | time     |
|--------------------------|------------|------------|-----------|-------------|----------|
| breadth_first_search     | 14663      | 19098      | 129631    | 12          | 538.4931 |
| depth_first_graph_search | 408        | 409        | 3364      | 392         | 12.5751  |
| uniform_cost_search      | 18223      | 18225      | 159618    | 12          | 661.3171 |

We see similar results for problems 2 and 3. Depth\_first explored the fewest numbers of nodes, which in turn had the shortest execution time, however, failed to deliver optimal plans. In problem 2, the returned plan's length was 619, comprised of many repeated steps.

Breadth\_first\_search overall outperforms and delivers optimal plans. However, we could see that there's a need for 'smarter' (heuristic-based) searches since execution time is getting too long.

Priya: Very neat comparison of all the different search results on problems 1, 2 and 3.

Priya: Suggestion: The link below has an interesting comparison of the BFS and DFS methods on when to chose

one vs the other: http://stackoverflow.com/que stions/3332947/when-is-it-practical-to-use-dfs-vs-bfs

• Compare and contrast heuristic search result metrics using A\* with the "ignore preconditions" and "level-sum" heuristics for Problems 1, 2, and 3.

| Problem 1                           | expansions | goal tests | new nodes | plan length | time     |
|-------------------------------------|------------|------------|-----------|-------------|----------|
| recursive_best_first_search h_1     | 4229       | 4230       | 17023     | 6           | 21.8154  |
| greedy_best_first_graph_search h_1  | 7          | 9          | 28        | 6           | 0.0371   |
| astar_search h_1                    | 55         | 57         | 224       | 6           | 0.2855   |
| astar_search h_ignore_preconditions | 41         | 43         | 170       | 6           | 0.4099   |
| astar_search h_pg_levelsum          | 11         | 13         | 50        | 6           | 0.6041   |
| Problem 2                           | expansions | goal tests | new nodes | plan length | time     |
| greedy_best_first_graph_search h_1  | 990        | 992        | 8910      | 21          | 30.644   |
| astar_search h_1                    | 4852       | 4854       | 44030     | 9           | 153.2734 |
| astar_search h_ignore_preconditions | 1450       | 1452       | 13303     | 9           | 43.2556  |
| astar_search h_pg_levelsum          | 86         | 88         | 841       | 9           | 10.21    |
| Problem 3                           | expansions | goal tests | new nodes | plan length | time     |
| greedy_best_first_graph_search h_1  | 5578       | 5580       | 49150     | 22          | 193.103  |
| astar_search h_1                    | 18223      | 18225      | 159618    | 12          | 665.9928 |
| astar_search h_ignore_preconditions | 5040       | 5042       | 44944     | 12          | 175.4908 |
| astar_search h_pg_levelsum          | 325        | 327        | 3002      | 12          | 44.5952  |

Most of the search strategies deliver optimal plans (except for greedy\_best\_first\_graph in Problems 2 and 3). The recursive\_best\_first strategy reached optimal plan, but had prohibitive running time and node expansions (relatively).

Among the A\*, we can see a clear pattern of improvement from h\_1 to h\_ignore\_preconditions to h\_pg\_levelsum. This reflects the degrees of admissibility among the heuristics. However, there is a reverse trend in execution time in problem 1. This is possibly due to the increase in heuristic complexity outweighing the numbers of nodes explored as these are small.

• What was the best heuristic used in these problems? Was it better than non-heuristic search planning methods for all problems? Why or why not?

A\* with pg\_levelsum heuristics outperform everything else, shortest execution time in general, fewest nodes explored, and deliver optimal plans.

Note: Some searches were not performed due to prohibitive execution time (hours+)

Priya: Well done! All algorithms have been implemented properly

Priya: Required: You have summarized well the performance of the algorithms. However please explain the reason for the observed results using at least one appropriate justification from the video lessons or from outside resources (e.g., Norvig and Russells textbook). Example why does ignore preconditions run faster than pg\_levelsum? why can DFS not find the optimal plan length? Please don't forget to site your references like you did in your research report

Priya: This is an important point. Better heuristics like level sum

may be more efficient in reducing the no. of expansions but costly in terms of taking more time.

Priya: I agree with your conclusiobn