Chapter 10

Hashing (one session)

Data Structures and Algorithms in Java

Objectives (continued)

Discuss the following topics:

- Hash Functions for Extendible(extensible) Files
- Hashing in java.util
- · Case Study: Hashing with Buckets

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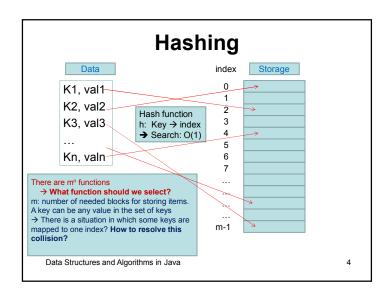
Objectives

- Linear Searching: O(n)
- Binary Searching: O(logn)
- Is there a more efficient way for searching?

Discuss the following topics:

- Hashing
- Hash Functions
- · Collision Resolution
- Deletion
- · Perfect Hash Functions

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Hashing

- To find a function (h) that can transform a
 particular key (K) (a string, number or record)
 into an index in the table used for storing items
 of the same type as K, the function h is called a
 hash function
- If h transforms different keys into different numbers, it is called a perfect hash function
- To create a perfect hash function, the table has to contain at least the same number of positions as the number of elements being hashed

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10.1- Common Hash Functions

 The division method is the preferred choice for the hash function if very little is known about the keys

TSize = sizeof(table), as in $h(K) = K \mod TSize$

 In the folding method, the key is divided into several parts which are combined or folded together and are often transformed in a certain way to create the target address: h(K) = sum of parts mod TSize

Example1: K= 123-45-6789 \rightarrow sum 3 parts:123 + 45 + 6789= 1368 \rightarrow h(K)=1367 mod TSize Example2: K= 123-45-6789 \rightarrow Sum 5 parts:12 + 34+56+78+9 = 189 \rightarrow h(K) = 189 mod TSize

Example3: K= "abcd" \rightarrow h(K)= "abcd" xor "efgh"

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Hash Functions (continued)

 In the mid-square method, the key is squared and the middle or mid part of the result is used as the address

 In the extraction method, only a part of the key is used to compute the address

Example: Concatenate two beginning digits and two ending digits: $K = 123-45-6789, h(K) = 1289 \mod TSize$

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Hash Functions (continued)

 Using the radix transformation, the key K is transformed into another number base; K is expressed in a numerical system using a different radix

```
Example: Use the base of 9 K = 345_{10} = 423_9 \rightarrow , f(K) = 423 \mod Tsize ( =23 if Tsize=100 )
```

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10.2- Collision Resolution

Open Addressing Method

- when a key collides with another key, the collision is resolved by finding an available table entry other than the position (address) to which the colliding key is originally hashed. Common methods:
 - Linear probing(dò tuyến tính), the simplest method.
 Probing p(i) with i=1, 2, 3,... → norm(h(K) + p(i))
 norm is a function as a normalizer. A common normalizer is h(h(K) + p(i))
 - Example: p(i)=i, h(K) = (h(K) + i) mod TSize
 - Quadratic probing (dò bậc 2) , p(i) = ai² norm(h(K) + ai²) Example: p(i)= \pm i², h(K) = (h(K) \pm i²) mod TSize

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Collision Resolution (continued)

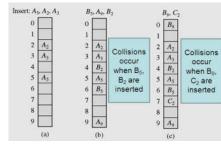


Figure 10-1 Resolving collisions with the linear probing method.

Subscripts indicate the home positions of the keys being hashed.

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Collision Resolution (continued)

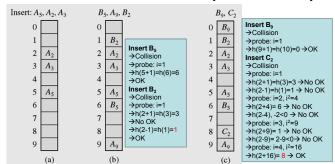


Figure 10-2 Using quadratic probing for collision resolution $h(K) = (h(K) \pm i^2) \mod 10$

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Collision Resolution (continued)

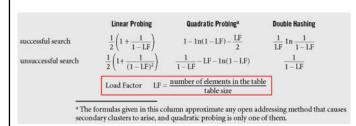


Figure 10-3 Formulas approximating, for different hashing methods, the average numbers of trials for successful and unsuccessful searches (Knuth, 1998)

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Ý nghĩa Load Factor

- Tham số α $\alpha = \frac{N}{SIZE}$
- · Băm đ/c mở: mức độ đầy (load factor)
 - α tăng thì khả năng va chạm tăng
 - Khi thiết kế, cần đánh giá max của N để lựa chọn SIZE
 - α không nên vượt quá 2/3
 - · Băm dây chuyền: độ dài trung bình của một dây chuyền

| | | Băm đ/c mở, Thăm dò tuyến tính | Băm đ/c mở, Thăm dò bình phương | Băm dây chuyền |
|----------------------------|------------------------|--|---------------------------------------|----------------------|
| Thời gian trung bình | Tìm kiếm thành công | $\frac{1}{2}\left(1+\frac{1}{1-\alpha}\right)$ | $\frac{-\ln(1-\alpha)}{\alpha}$ | $1+\frac{1}{\alpha}$ |
| | Tìm kiếm thất bại | $\frac{1}{2}\left(1+\frac{1}{(1-\alpha)^2}\right)$ | $\frac{1}{1-\alpha}$ | α |

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Collision Resolution (continued)

Chaining Method

- Keys do not have to stored in table itself, each
 position of the table is associated with a linked
 list or chain of structures whose info fields
 store keys or references to keys
- This method is called separate chaining, and a table of references (pointers) is called a scatter table

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Collision Resolution (continued)

h(K) → index of a linked list of elements having the same value of hask function.

 $K \rightarrow h(K) \rightarrow index$ $\rightarrow traverse$ the appropriate list to find the element having this key.

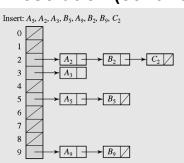


Figure 10-5 In chaining, colliding keys are put on the same linked list

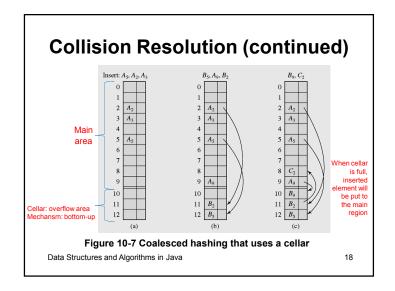
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Collision Resolution (continued)

- A version of chaining called coalesced hashingbăm theo nhóm sử dụng array- (or coalesced chaining) combines linear probing with chaining
- An overflow area known as a cellar can be allocated to store keys for which there is no room in the table

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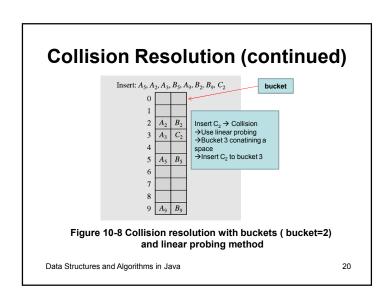


Collision Resolution (continued)

Bucket Addressing

- To store colliding elements in the same position in the table can be achieved by associating a bucket with each address
- A bucket is a block of space large enough to store multiple items

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Collision Resolution (continued) $\begin{array}{c|ccccc} 0 & & & & & \\ \hline 2 & A_2 & B_2 & & & \\ \hline 3 & A_3 & & & & \\ \hline 4 & & & & & \\ \hline 5 & A_5 & B_5 & & & \\ \hline 6 & & & & & \\ \hline 7 & & & & & \\ \hline 8 & & & & & \\ \hline 9 & A_9 & B_9 & & & \\ \hline Data Structures and Algorithms in Java$ 21

10.3- Deletion

- Structure and collision resolution of the hash table will decide the way by which its elements are deleted. Thay can be
 - Linear search for deletion
 - Linear search to locate the linked list of the subgroup then delete an element in this linked list.
 - Linear search to locate the subgroup then delele an element in this subgroup, update references to next elements in the same subgroup.

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Ý nghĩa Load Factor

- Tham số α $\alpha = \frac{N}{SIZE}$
- · Băm đ/c mở: mức độ đầy (load factor)
 - α tăng thì khả năng va chạm tăng
 - Khi thiết kế, cần đánh giá max của N để lựa chọn SIZE
 - α không nên vượt quá 2/3
 - Băm dây chuyển: độ dài trung bình của một dây chuyển

| | | Băm đ/c mở, Thăm dò tuyến tính | Băm đ/c mở, Thăm dò bình phương | Băm dây chuyền |
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| Thời gian trung bình | Tìm kiếm thành công | $\frac{1}{2}\left(1+\frac{1}{1-\alpha}\right)$ | $\frac{-\ln(1-\alpha)}{\alpha}$ | $1+\frac{1}{\alpha}$ |
| | Tìm kiếm thất bại | $\frac{1}{2}\left(1+\frac{1}{(1-\alpha)^2}\right)$ | $\frac{1}{1-\alpha}$ | α |

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Deletion

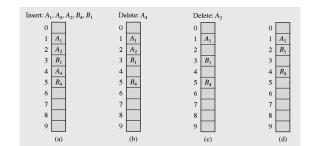
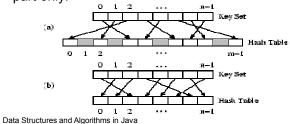


Figure 10-10 Linear search in the situation where both insertion and deletion of keys are permitted

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10.4- Perfect Hash Functions (*)

- If a function requires only as many cells in the table as the number of data so that no empty cell remains after hashing is completed, it is called a minimal perfect hash function
- (*) You need to know essential features on this part only.



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Perfect Hash Functions

Cichelli's method

- Cichelli's method is an algorithm to construct a minimal perfect hash function
- · It is used to hash a relatively small number of reserved words
- Where g is the function to be constructed

 $h(word) = (length(word) + g(firstletter(word)) + g(lastletter(word))) \mod TSize$

- The algorithm has three parts:
 - Computation of the letter occurrences
 - Ordering the words
 - Searching

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Perfect Hash Functions

Cichelli's method

- Choose a value of max;
- Compute the number of occurrences of each first letter and last letter in the set of all words.
- Order all words in accordance to the frequency of occurrence of yhe first and the last letters;

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Cichelli's Method

Perfect Hash Fns 2

This is used primarily when it is necessary to hash a relatively small collection of keys, such as the set of reserved words for a programming language.

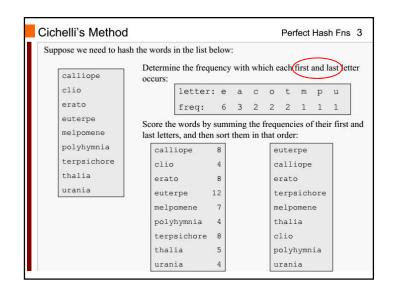
The basic formula is:

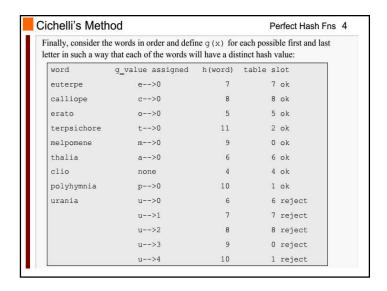
h(S) = S.length() + g(S[0]) + g(S[S.length()-1])

where g () is constructed using Cichelli's algorithm so that h() will return a different hash value for each word in the set.

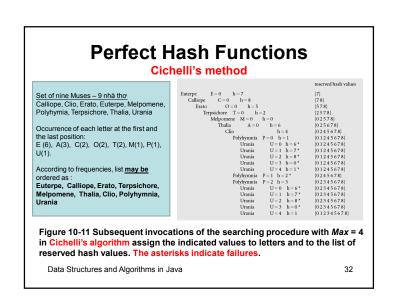
The algorithm has three phases:

- computation of the letter frequencies in the words
- ordering the words
- searching





Cichelli's Method Perfect Hash Fns 5 Cichelli's method imposes a limit on the search at this point (we're assuming it's 5 steps), and so we back up to the previous word and redefine the mapping there: g_value assigned h(word) table slot word polyhymnia 10 p-->0 1 reject 11 p-->1 2 reject p-->2 12 u-->0 6 reject urania u-->1 7 reject 11-->2 8 reject 0 reject 11-->4 10 1 ok So, if we define g () as determined above, then h () will be a minimal perfect hash function on the given set of words. The primary difficulty is the cost, because the search phase can degenerate to exponential performance, and so it is only practical for small sets of words.



Perfect Hash Functions

The FHCD Algorithm

 The FHCD algorithm, an extension of Cechelli's approach, devised by Thomas Sager, searches for a minimal perfect hash function of the form (modulo *TSize*), where g is the function to be determined by the algorithm

 $h(word) = h_0(word) + g(h_1(word)) + g(h_2(word))$

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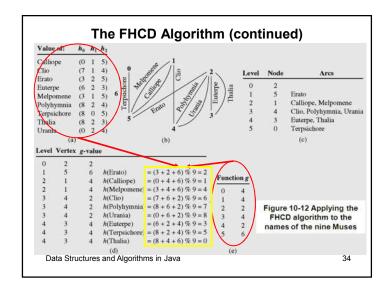
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Review

- Static Hashing
- Dynamic Hashing
- -Extendible hashing
- -Linear Hashing

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10.5- Hash Functions for Extendible Files (*)

- File=table.
- Expandable hashing, dynamic hashing, and extendible hashing methods distribute keys among buckets in a similar fashion
- Data → h(Data) → index → buckets[index]
- The main difference is the structure of the index (directory)
- In expandable hashing and dynamic hashing, a binary tree is used as an index of buckets
- · In extendible hashing, a directory of records is kept in a table

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Extendible Hashing

- Extendible hashing accesses the data stored in buckets indirectly through an index that is dynamically adjusted to reflect changes in the file
- Extendible hashing allows the file to expand without reorganizing it, but requires storage space for an index
- Values returned by such a hash function are called **pseudokeys**

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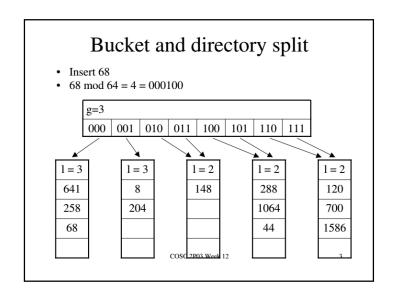
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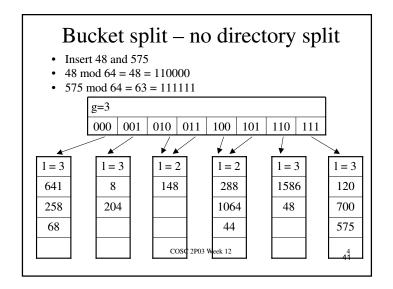
Extendible Hashing Example

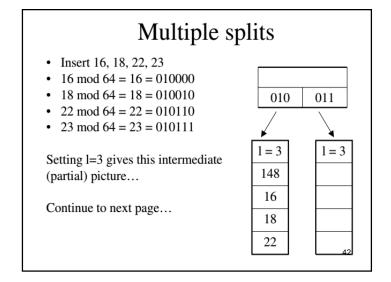
- Suppose that g=2 and bucket size = 4.
- Suppose that we have records with these keys and hash function h(key) = key mod 64:

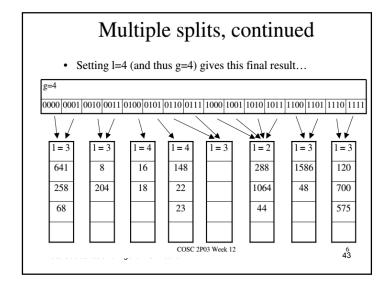
| key | $h(key) = key \mod 64$ | bit pattern |
|------|------------------------|-------------|
| 288 | 32 | 100000 |
| 8 | 8 | 001000 |
| 1064 | 40 | 101000 |
| 120 | 56 | 111000 |
| 148 | 20 | 010100 |
| 204 | 12 | 001100 |
| 641 | 1 | 000001 |
| 700 | 60 | 111100 |
| 258 | 2 | 000010 |
| 1586 | 50 | 110010 |
| 44 | 44 | 101010 |

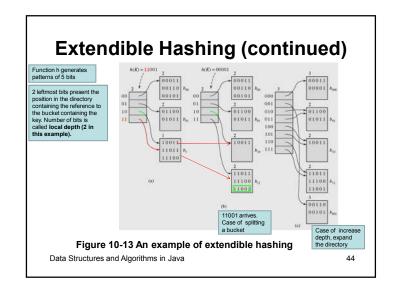
Extendible Hashing Example directory and bucket structure g=2 00 01 10 11 1 = 21 = 21 = 21 = 28 148 288 120 204 1064 700 641 44 1586 258 Data Structures and Algorithms in Java 39









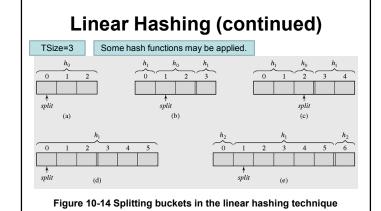


Linear Hashing

- With this method, no index is necessary because new buckets generated by splitting existing buckets are always added in the same linear way, so there is no need to retain indexes
- A bucket is full when its loading factor exceeds a certain level. This bucket will be splitted.
- A reference split indicates which bucket is to be split next
- After the bucket is divided, the keys in this bucket are distributed between this bucket and the newly created bucket, which is added to the end of the table

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Linear Hashing (continued)

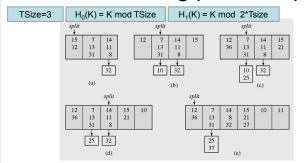


Figure 10-15 Inserting keys to buckets and overflow areas with the linear hashing technique

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10.6- Hashing in java.util The HashMap class

- HashMap is an implementation of the interface
- A map is a collection that holds pairs (key, value) or entries
- A hash map is a collection of singly linked lists (buckets); that is, chaining is used as a collision resolution technique
- In a hash map, both null values and null keys are permitted

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HashMap (continued)

| Method | Operation |
|--------------------------------------|---|
| void clear() | Remove all the objects from the hash map. |
| Object clone() | Return a copy of the hash map without cloning its elements. |
| boolean containsKey(Object key) | Return true if the hash map contains the object key. |
| boolean containsValue(Object val) | Return true if the hash map contains the object val. |
| Set entrySet() | Return a set containing all the pairs (key, value) in the hash map. |
| boolean equals(Object ob) | Return true if the current hash map and object ob are equal (inherited). |
| int hashCode() | Return the hash code for the hash map (inherited). |
| Object get(Object key) | Return the object associated with key. |
| HashMap() | Create an empty hash map with initial capacity equal to 16 and the load factor equal to .75. |
| HashMap(int ic) | Create an empty hash map with initial capacity ic and the load factor equal to .75; throw IllegalArgumentException if ic < 0. |
| HashMap(int ic, float lf) | Create an empty hash map with initial capacity ic and the load factor if; throw IllegalArgumentException if ic < 0 or |

Figure 10-16 Methods in class HashMap including three inherited methods

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HashMap (continued)

```
This example (in textbook) demonstates how to use the HashMap class to manage a list of person < name, age,hashCode> in which the hasCode is the sum of charcter codes in the field name.
```

Click to go the HashSet class

```
import java.io.*;
import java.util.HashMap;

class Person (
    private String name;
    int age;
    private int hashcode = 0;
    public Person(String n, int a) {
        name = n; age = a;
        for (int i = 0; i c name.length(); i**)
            hashcode += name.charAt(i);
    }
    public Person() {
        thia(**,0);
    }
    public boolean equals(object p) {
        return name.equals(((Person)p).name);
    }
    public int hashcode() {
        return hashcode;
    }
    public String toString() {
        return "(" + name + "," + age + ")";
    }
}
```

Figure 10-17 Demonstrating the operation of the methods in class HashMap

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HashMap (continued)

| HashMap(Map m) | Create a hash map with copies of elements from map m; throw NullPointerException if m is null. |
|---------------------------------------|---|
| boolean isEmpty() | Return true if the hash map contains no elements, false otherwise. |
| Set keySet() | Return a set containing all the keys of the hash map. |
| Object put(Object key, Object val) | Put the pair (key, val) in the hash map; return a value associated with key if there is any in the hash map, null otherwise. |
| void putAll(Map m) | Add objects from map to the current hash map; throw NullPointerException if m is null. |
| void rehash() | A protected method to increase the capacity of the hashtable; the method is called automatically when the number of keys in the hashtable is greater than the product of the load factor and the current capacity. |
| Object remove(Object key) | Remove the pair (key, corresponding value) from the hash map and return the value associated currently with key in the hash map. |
| int size() | Return the number of objects in the hash map. |
| String toString() | Return a string representation of the hash map that contains the string representation of all the elements (inherited). |
| Collection values() | Return a collection with all the values contained in the hash map. |

Figure 10-16 Methods in class HashMap including three inherited methods (continued)

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HashMap (continued)

```
class TestHashMap {
   public static void main(String[] a) {
        HashMap cities = new HashMap();
        cities.put(new Person("Gregg",25),"Pittsburgh");
        cities.put(new Person("Bill",30),"Boston");
        cities.put(new Person("Bill",20),"Belmont");
        System.out.println(cities);
        // ((Ann,30)=Boston, (Gregg,25)=Pittsburgh, (Bill,20)=Belmont);
        cities.put(new Person("Gregg",30),"Austin");
        System.out.println(cities);
        // ((Ann,30)=Boston, (Gregg,25)=Austin, (Bill,20)=Belmont);
        System.out.println(cities.containsKey(new Person("Ann",30)));
        // true
        System.out.println(cities.containsValue("Boston"));
        // true
        System.out.println(cities.size());
        // 3
```

Figure 10-17 Demonstrating the operation of the methods in class HashMap (continued)

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HashMap (continued)

```
Bystem.out.println(cities.get(new Person("Ann",30))) // Boston
System.out.println(cities.get(new Person("Ann",30))) // Boston
System.out.println(cities.values(1))
// ((Ann,30)=Boston, (Gregg,35)-Austin, (Bill,20)=Belmont)
System.out.println(cities.values(1))
// (Boston, Austin, Belmont)
System.out.println(cities.log/Bet(1))
// ((Ann,30), (Gregg,35), (Bill,20))
// (Boston, Boston, (Gregg,35)-Austin, (Fay,44)=molt,
// ((Ann,30), (Gregg,35)-Austin, (Fay,44)=molt,
// ((Ann,30)=Boston, (Gregg,35)-Austin, (Fay,44)=molt,
// moll-Beshville)
System.out.println(cities.get(new Person("Kay",44)));
// mill
System.out.println(cities.get(new Person("Kay",44)));
// system.out.println(cities.get(new Person("Kay",44)));
// true
System.out.println(cities.containsKey(new Person("Stan",55)));
// true
System.out.println(cities.containsKey(new Person("Stan",55)));
// false
```

Figure 10-17 Demonstrating the operation of the methods in class HashMap (continued)

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The HashSet class

- HashSet is another implementation of a set (an object that stores unique elements)
- Class hierarchy in java.util for HashSet is:

```
Object → AbstractCollection → AbstractSet → HashSet
```

• HashSet is implemented in terms of HashMap

```
public HashSet() {
    map = new HashMap();
}
```

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HashSet (continued)

boolean add(Object ob) Add ob to the hash set if it is not already there; return true if boolean addAll(Collection c) Add all the elements from the collection c to the hash set; return true if the hash set was modified (); throw NullPointerException if c is null (inherited). Remove all the objects from the bash set. void clear() Object clone() Return a copy of the hash set without cloning its elements. boolean contains (Object ob) Return true if the hash set contains the object ob. Return true if the hash set contains all elements in the collection containsAll(Collection c) ${\tt c; throw \, Null Pointer Exception \, if \, c \, is \, null \, (inherited)}.$ boolean equals (Object ob) Return true if the current hash set and object ob are equal int hashCode() Return the hash code for the hash set (inherited). Create an empty hash set with initial capacity equal to 16 and the HashSet() HashSet(int ic) Create an empty hash set with initial capacity ic and the load factor equal to .75; throw IllegalArgumentException if

Figure 10-18 Methods in class HashSet including some inherited methods

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HashSet (continued)

```
HashSet(int ic, float lf)
                                       Create an empty hash set with initial capacity ic and the load
factor 1f; throw IllegalArgumentException if ic < 0
                                        Create a hash set with copies of elements from c: throw
HashSet(Collection c)
boolean isEmpty()
                                        Return true if the hash set contains no elements, false otherwise
boolean iterator()
                                        Return an iterator over the elements in the hash set: the iteration
                                        order can change over time.
boolean remove(Object ob)
                                        Remove ob from the hash set and return true if ob was in the
                                        Remove from the hash set all elements contained in collection c;
boolean
removeAll(Collection c)
                                        return true if any element was removed; throw
                                        NullPointerException if c is null (inherited).
                                        Remove from the hash set all elements that are not in the collection
retainAll(Collection c)
                                        c: return true if any element was removed; throw
                                        NullPointerException if c is null (inherited)
Object[] toArray()
                                        Copy all elements from the hash set to a newly created array and
```

Figure 10-18 Methods in class HashSet including some inherited methods (continued)

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HashSet (continued)

Object[] toArray(Object
a[])

Copy all elements from the hash set to the array a if a is large enough or to a newly created array and return the array; throw ArrayStoreException if the class type of any element in the hash set is not the same as or does not extend the class type of a; throw NullPointerException if a is null (inherited).

String toString()

Return the number of objects in the hash set.

Return a string representation of the hash set that contains the string representation of all the elements (inherited).

Figure 10-18 Methods in class HashSet including some inherited methods (continued)

Data Structures and Algorithms in Java

HashSet (continued)

```
public Person() {
    this("",0);
}
public boolean equals(Object p) {
    return name.equals(((Person)p).name);
}
public int compareTo(Object p) {
    return name.compareTo(((Person)p).name);
}
public int hashCode() {
    return hashcode;
}
public String toString() {
    return "(" + name + "," + age + ")";
}
```

Figure 10-19 Demonstrating the operation of the methods in class HashSet (continued)

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HashSet (continued)

This example demonstates how to use the HashSet class to manage a list of person < name, age,hashCode> in which the hasCode is the sum of charcter codes in the field name.

Click to go to the HashTable class

Figure 10-19 Demonstrating the operation of the methods in class HashSet

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HashSet (continued)

```
class TestHashSet {
   public static void main(String[] ar) {
          HashSet hashset1 = new HashSet();
hashset1.add(new Integer(40));
           hashsetl.add(new Integer(60));
           System.out.println(hashset1);
hashset1.add(new Integer(50));
                                                               // [40, 60]
                                                             // [40, 50, 60]
           System.out.println(hashset1):
           hashsetl.add(new Integer(50));
System.out.println(hashsetl);
           System.out.println(hashsetl.contains(new Integer(50))): // true
           System.out.println(hashset1.contains(new Integer(70))); // false
HashSet hashset2 = new HashSet();
           hashset2.add(new Integer(30)):
           hashset2.add(new Integer(40));
hashset2.add(new Integer(50));
                                                            // [30, 40, 50]
           System.out.println(hashset2);
           // union: [40, 50, 60] and [30, 40, 50] ==> [30, 40, 50, 60]
           System.out.println(hashsetl); // 30, 40, 50, 60, hashsetl.remove(new Integer(30));
System.out.println(hashsetl); // [40, 50, 60] hashsetl.retainAll(hashset2); // [40, 50]
           // intersection: [40, 50, 60] and [30, 40, 50] ==> [40, 50]
System.out.println(hashset1); // [40, 50]
```

Figure 10-19 Demonstrating the operation of the methods in class HashSet (continued)

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HashSet (continued)

```
// [40, 50, 60]
hashset1.add(new Integer(60));
hashset1.removeAll(hashset2);
// difference: [40, 50, 60] and [30, 40, 50] ==> [60]
System.out.println(hashset1); // [60]
hashset1.add(null);
System.out.println(hashset1);
                                 // [60, null]
HashSet pSet = new HashSet();
Person[] p = {new Person("Gregg", 25), new Person("Ann", 30),
             new Person("Bill",20), new Person("Gregg",35),
            new Person("Kay", 30)};
for (int i = 0; i < p.length; i++)
   pSet.add(p[i]);
System.out.println(pSet);
// [(Ann,30), (Gregg,25), (Kay,30), (Bill,20)]
java.util.Iterator it = pSet.iterator();
((Person)it.next()).age = 50;
System.out.println(pSet);
// [(Ann,50), (Gregg,25), (Kay,30), (Bill,20)]
pSet.add(new Person("Craig",40));
```

Figure 10-19 Demonstrating the operation of the methods in class HashSet (continued)

Data Structures and Algorithms in Java

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The Hashtable class

- A Hashtable is roughly equivalent (gàn tương đương) to a HashMap except that it is synchronized and does not permit null values with methods to operate on hash tables
- The class Hashtable is considered a legacy class, just like the class Vector
- Class hierarchy in java.util is:

```
Object → Dictionary → Hashtable
```

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HashSet (continued)

```
System.out.println(pSet);
// [(Ann,50), (Gregg,25), (Kay,30), (Craig,40), (Bill,20)]
// (Gregg,25) true
// (Ann,50) true
// (Gregg, 35) true
// (Kay, 30) true
// Using an array to sort elements in the hashset:
Person[] pArray = (Person[]) pSet.toArray(new Person[0]);
for (int i = 0; i < p.length; i++)
    System.out.print(pArray[i] + " ");
System.out.println();
// (Ann,50) (Gregg,25) (Kay,30) (Craig,40) (Bill,20)
Arrays.sort(pArray):
for (int i = 0; i < p.length; i++)
    System.out.print(pArray[i] + " ");
System.out.println();
// (Ann,50) (Bill,20) (Craig,40) (Gregg,25) (Kay,30)
System.out.println(pSet);
```

Figure 10-19 Demonstrating the operation of the methods in class HashSet (continued)

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Hashtable (continued)

| Method Operation | |
|--|-----------|
| | |
| void clear() Remove all the objects from the hashtable. | |
| Object clone() Return a copy of the hashtable without cloning its o | elements. |
| boolean contains (Object Return true if the hashtable contains the object val) Return true if the hashtable contains the object val) | al; throw |
| boolean Return true if the hashtable contains the object k contains Key(Object key) NullPointerException if key is null. | ey; throw |
| boolean Return true if the hashtable contains the object v contains Value(Object val) throw NullPointerException if val is null. | |
| Enumeration elements() Return an enumeration of the values in the hashtab | ole. |
| Set entrySet() Return a set containing all the pairs (key, value) in the hashtable. | he |

Figure 10-20 Methods of the class Hashtable including three inherited methods

Data Structures and Algorithms in Java

Hashtable (continued)

boolean equals(Object ob)

Return true if the current hashtable and object ob are equal.

Return the object associated with key; throw NullPointerException if key is null.

int hashCode()

Return the hash code for the hashtable.

Create an empty hashtable with initial capacity equal to 11 and the load factor equal to .75.

Hashtable(int ic)

Create an empty hashtable with initial capacity ic and the load factor equal to .75; throw IllegalArgumentException if

Figure 10-20 Methods of the class Hashtable including three inherited methods (continued)

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Hashtable (continued)

void rehash() A protected method to increase the capacity of the hashtable; the method is called automatically when the number of keys in the hashtable is greater than the product of the load factor and the current capacity. Remove the pair (${\tt key}, {\tt corresponding}\ {\tt value})$ from the hashtable Object remove(Object key) and return the value associated currently with key in the hashtable; throw NullPointerException if key int size() Return the number of objects in the hashtable. String toString() Return a string representation of the hashtable that contains the string representation of all the objects. Collection values() Return a Collection object with all the values contained in the

Figure 10-20 Methods of the class Hashtable including three inherited methods (continued)

Data Structures and Algorithms in Java

Hashtable (continued)

Hashtable(int ic, float lf) Create an empty hashtable with initial capacity ic and the load factor lf; throw IllegalArgumentException if ic < 0 or 1f < 0. Hashtable(Map m) Create a hashtable with copies of elements from map m; throw NullPointerExceptionifmis null. Return true if the hashtable contains no elements, false otherwise. boolean isEmptv() Enumeration keys() Return an enumeration containing all the keys of the hashtable. Set keySet() Return a set containing all the keys of the hashtable. Object put(Object key, Put the pair (key, val) in the hashtable; return a value associated with key if there is any in the hashtable, null otherwise; throw Object val) NullPointerException if key or val is null. void putAll(Map m) Add objects from map m to the current hashtable; throw NullPointerException if m is null.

Figure 10-20 Methods of the class Hashtable including three inherited methods (continued)

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Hashtable (continued)

```
import java.io.*;
                                       This example demonstates how
import java.util.*;
                                       to use the HashTable class to
                                       manage a list of person
class Person {
   private String name;
                                       < name, age> with two cases:
   public int age;
                                       Case 1: Key of a persion is an
   public Person(String s, int i) {
      name = s; age = i;
                                       Case 2: Key of a persion is an
                                       object that belongs to the SSN
   Person() {
                                      class, a pre-defined class.
      this("",0):
   public String toString() {
      return "(" + name + "," + age + ")";
                                                 Click to go to the
   public boolean equals(Object p) {
                                                    case study
      return name.equals(((Person)p).name);
```

Figure 10-21 A program demonstrating operations of the Hashtable methods

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Hashtable (continued)

Figure 10-21 A program demonstrating operations of the Hashtable methods (continued)

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Hashtable (continued)

Figure 10-21 A program demonstrating operations of the Hashtable methods (continued)

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Hashtable (continued)

Figure 10-21 A program demonstrating operations of the Hashtable methods (continued)

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Hashtable (continued)

```
print(hashTable1.keys());
// 11111111, 222222222, 123456789
print(hashTable1.values().iterator());
// (Kathy,30), (Kathy,20), (Larry,25)
Iterator it = hashTable1.values().iterator();
((Person)it.next()).age = 28;
System.out.println(hashTable1);
// (111111111=(Kathy,28), 22222222=(Kathy,20), 123456789=(Larry,25)}
hashTable1.put(new Integer(11111111),new Person("Jerry",20));
System.out.println(hashTable1);
// (111111111=(Jerry,20), 22222222=(Kathy,20), 123456789=(Larry,25)}
hashTable1.put(new Integer(1111113),new Person("Frank",30));
```

Figure 10-21 A program demonstrating operations of the Hashtable methods (continued)

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Hashtable (continued)

```
System.out.println(hashTable1);

// (111111113=(Frank,30), 123456789=(Larry,25), 222222222=(Kathy,20),

// 111111111_Agrry,20),
System.out.println(hashTable1.get(new Integer(11111111))); // (Jerry,20)
System.out.println(hashTable1.contains(new Person("Jerry",20))); // true
System.out.println(hashTable1.containsValue(new Person("Jerry",20))); // true
System.out.println(hashTable1.remove(new Integer(111111111))); // (Jerry,20)
System.out.println(hashTable1);

// (22222222=(Kathy,20), 123456789=(Larry,25))
```

Figure 10-21 A program demonstrating operations of the Hashtable methods (continued)

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Bài tập

- Xây dựng chương trình tự điển, dữ liệu được tải lên từ file như sau
 - hello,xin chao
 - study,hoc

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Hashtable (continued)

```
Hashtable hashTable2 = new Hashtable();
hashTable2.put(new SSN(121456789),new Person("Larry",28));
hashTable2.put(new SSN(1111111),new Person("Kathy",30));
System.out.println(hashTable2);
// {11111111-(Kathy,30), 123456789-(Larry,28)}
hashTable2.put(new SSN(22222222),new Person("Kathy",20));
System.out.println(hashTable2);
// {22222222-(Kathy,20), 111111111-(Kathy,30), 123456789-(Larry,28)}
hashTable2.put(new SSN(11111111),new Person("Jerry",25));
System.out.println(hashTable2);
// {22222222-(Kathy,20), 111111111-(Jerry,25), 123456789-(Larry,28)}
hashTable2.put(new SSN(11111113),new Person("Frank",30));
System.out.println(hashTable2);
// {22222222-(Kathy,20), 111111113-(Frank,30), 11111111-(Jerry,25),
// {22222222-(Kathy,20), 111111113-(Frank,30), 11111111-(Jerry,25),
// {23456789-(Larry,28)}
}
```

Figure 10-21 A program demonstrating operations of the Hashtable methods (continued)

Data Structures and Algorithms in Java

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Case Study: Hashing with Buckets

This example(in the textbook) depicts how to implement hashing data in a file.

Do yourself

Click to go to the Summary

```
import java.io.*;
import java.io.*;
import java.io.riio;

public class FileHashing {
    private final int bucketSize = 2, tableSize = 3, strlen = 20;
    private final int recorden = strlen;
    private final ptve empt - "", delMarker - "*;
    private long[] positions;
    private long[] positions;
    private BundetreamBeader iar = new InputStreamBeader(System.in);
    private BundendomcossFile outfile;
    private RandomAccossFile outfile;
    private RandomAccossFile outfile;
    private RandomAccossFile overflow;
    public FileHashing() {
    }
    }
    private void print(byte[] s) { // print a byte array;
        for(int x = 0; x < s.length; k++)
        System.out.print((char)s[k]);
    }
    private long hash(byte[] s) {
        long xor = 0, pack;
    }
}</pre>
```

for (slength = s.length; s[slength-1] == ' '; slength--);

Figure 10-22 Implementation of hashing using buckets

Data Structures and Algorithms in Java

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

```
outfile.write(line);
  done = inserted = true;
}
else if (comparesTo(name,line) == 0) {
  print(line);
   System.out.println(" is already in the file");
   return;
}
else counter++;
if (counter == bucketSize)
  done = true;
else outfile.seek(address+counter*recordLen);
```

Figure 10-22 Implementation of hashing using buckets (continued)

Data Structures and Algorithms in Java

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Case Study: Hashing with Buckets (continued)

```
private int comparesTo(byte[] s1, byte[] s2) { // same length
   for (int i = 0; i < s1.length; i++) // of s1 and s2
       if (s1[i] != s2[i])
                                   ] // is assumed;
           return s1[i] - s2[i];
   return 0:
private void insert() throws IOException (
   insertion(getName());
private void insertion(byte[] line) throws IOException (
   bvte[] name = new bvte[recordLen];
   boolean done = false, inserted = false;
   int counter = 0:
   long address = hash(line);
   outfile.seek(address):
   while (!done && outfile.read(name) != -1) {
      if (name[0] == empty || name[0] == delMarker) {
           outfile.seek(address+counter*recordLen);
```

Figure 10-22 Implementation of hashing using buckets (continued)

Data Structures and Algorithms in Java

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Case Study: Hashing with Buckets (continued)

```
if (inserted) {
    done = false;
    counter = 0;
    overflow.seek(0);
    while (idone & overflow.read(name) != -1) {
        if (name(0] == delMarker)
            done = true;
        else if (comparesTo(name,line) == 0) {
            print(line);
            System.out.println(* is already in the file*);
            return;
        }
        else counter++;
    }
    if (done)
        overflow.seek(counter*recordLen);
    else overflow.seek(counter*low.length());
        overflow.write(line);
}
```

Figure 10-22 Implementation of hashing using buckets (continued)

Data Structures and Algorithms in Java

```
private void delete() throws IOException {
   byte[] line = getName();
   long address = hash(line);
   outfile.seek(address);
   int counter = 0;
   boolean done = false, deleted = false;
   byte[] name = new byte[recordLen];
```

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

```
if (!deleted) {
    done = false;
    counter = 0;
    overflow.seek(0);
    while (!done && overflow.read(name) != -1) {
        if (compares*To(line,name) == 0) {
            overflow.seek(counter*recordLen);
            overflow.write(delMarker);
            done = deleted = true;
        }
        else counter*+;
        overflow.seek(counter*recordLen);
     }
}
if (!deleted) {
    print(line);
     System.out.println(" is not in database");
}
```

Figure 10-22 Implementation of hashing using buckets (continued)

Data Structures and Algorithms in Java

Case Study: Hashing with Buckets (continued)

```
while (!done && outfile.read(name) != -1) {
   if (comparesTo(line,name) == 0) {
      outfile.seek(address+counter*recordLen);
      outfile.write(delMarker);
      done = deleted = true;
   }
   else counter++;
   if (counter == bucketSize)
      done = true;
   else outfile.seek(address+counter*recordLen);
```

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

```
private void swap(long[] arr, int i, int j) {
    long tmp = arr[i]; arr[i] = arr[j]; arr[j] = tmp;
}

private int partition(int low, int high) throws IOException {
    byte[] rec = new byte[recordLen];
    int i, lastSmall;
    swap(positions,low,(low+high)/2);
    outfile.seek(positions[low]*recordLen);
    outfile.read(pivot);
```

Figure 10-22 Implementation of hashing using buckets (continued)

Data Structures and Algorithms in Java

```
for (lastSmall = low, i = low+1; i <= high; i++) {
    outfile.seek(positions[i]*recordLen);
    outfile.read(rec);
    if (comparesTo(rec,pivot) < 0) {
        lastSmall++;
        swap(positions,lastSmall,i);
    }
} swap(positions,low,lastSmall);
return lastSmall;
}</pre>
```

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

```
private void sort(int low, int high) throws IOException {
    if (low < high) {
        int pivotLoc = partition(low, high);
        sort(low, pivotLoc-1);
        sort(pivotLoc+1, high);
    }
}

private void sortFile() throws IOException {
    byte[] rec = new byte[recordLen];
    sort(1,(int)positions[0]); // positions[0] contains the # of elements;
    for (int i = 1; i <= positions[0]; i++) { // put data from
        outfile.seek(positions[i]*recordLen); // outfile in sorted order
        outfile.read(rec);
        sorted.write(rec); // in file sorted;
    }
}</pre>
```

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

Figure 10-22 Implementation of hashing using buckets (continued)

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Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

```
}
combineFiles();
sortFile();
outfile.close();
sorted.close();
overflow.close();
fIn.close();
   (new File(".\\","names")).delete();
   (new File(".\\","sorted")).renameTo(new File(".\\","names"));
} catch (IOException ioe) {
}
}
```

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

Figure 10-22 Implementation of hashing using buckets (continued)

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Case Study: Hashing with Buckets (continued)

Figure 10-22 Implementation of hashing using buckets (continued)

Data Structures and Algorithms in Java

Summary

- Common hash functions include the division, folding, mid-square, extraction and radix transformation methods.
- Collision resolution includes the open addressing, chaining, and bucket addressing methods.
- Cichelli's method is an algorithm to construct a minimal perfect hash function

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Summary (continued)

- A hash map is a collection of singly linked lists (buckets); that is, chaining is used as a collision resolution technique
- HashSet is another implementation of a set (an object that stores unique elements)
- A Hashtable is roughly equivalent to a HashMap except that it is synchronized and does not permit null values with methods to operate on hash tables

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Summary (continued)

- The FHCD algorithm searches for a minimal perfect hash function of the form (modulo TSize), where g is the function to be determined by the algorithm
- In expandable hashing and dynamic hashing, a binary tree is used as an index of buckets
- In extendible hashing, a directory of records is kept in a table

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Notices about using hash tables

- · When should hashtables be used:
 - Elements in a group are different and insertion and search are main operations.
- What are things to be concerned before a hashtable is implemented?
 - Choose a key for each element: number/string?
 - Choose a hash function
 - Choose a collision resolution

because these things will affect on algorithms that will be selected in our hashtable.

Data Structures and Algorithms in Java

This lecture has no tutorial. Re-code samples in the textbook.

Thank you.

Data Structures and Algorithms in Java