NOTES ON PROLOG EXECUTION

ERIC MARTIN

1. Program

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concat(a, Y, Y).
concat(f(X), Y, f(Z)) := concat(X, Y, Z).
concat(g(X), Y, g(Z)) := concat(X, Y, Z).
compress(a, a).
compress(f(a), f(a)).
compress(g(a), g(a)).
compress(f(f(X)), Y) := compress(f(X), Y).
compress(g(g(X)), Y) := compress(g(X), Y).
compress(f(g(X)), f(Y)) := compress(g(X), Y).
compress(g(f(X)), g(Y)) := compress(f(X), Y).
accumulator_reverse(a, X, X).
accumulator_reverse(f(X), Y, Z) :- accumulator_reverse(X, f(Y), Z).
accumulator_reverse(g(X), Y, Z) := accumulator_reverse(X, g(Y), Z).
reverse(X, Y) :- accumulator_reverse(X, a, Y).
relation(X, Y, Z) :- concat(X, Y, U), compress(U, V), reverse(V, Z).
relation(X, Y, Z) :- concat(Y, X, U), compress(U, V), reverse(V, Z).
                          2. QUERY: RELATION(f(f(g(f(A))))), f(f(g(g(A)))), X)
goals\_solution\_list: [([relation(f(f(g(f(a)))), f(g(g(a))), X)], {X: X})]
   goals: [relation(f(f(g(f(a)))), f(g(g(a))), X)]
                                                solution: {X: X}
   goal: relation(f(f(g(f(a)))), f(g(g(a))), X)
   clause: relation(X, Y, Z) :- concat(X, Y, U), compress(U, V), reverse(V, Z).
                                                                          variable renaming: {X: X_0}
   head: relation(X_0, Y, Z)
   mgu: \{X: Z, Y: f(g(g(a))), X_0: f(f(g(f(a))))\}
   clause: relation(X, Y, Z) :- concat(Y, X, U), compress(U, V), reverse(V, Z).
                                                                          variable renaming: {X: X_0}
   head: relation(X_0, Y, Z)
   mgu: \{X: Z, Y: f(g(g(a))), X_0: f(f(g(f(a))))\}
goals_solution_list: [([concat(f(f(g(f(a)))), f(g(g(a))), U), compress(U, V), reverse(V, Z)], {X: Z}),
                    ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
   goals: [concat(f(f(g(f(a)))), f(g(g(a))), U), compress(U, V), reverse(V, Z))]
                                                                        solution: {X: Z}
   goal: concat(f(f(g(f(a)))), f(g(g(a))), U)
   clause: concat(f(X), Y, f(Z)) :- concat(X, Y, Z). variable renaming: {X: X_0, Z: Z_0}
   head: concat(f(X_0), Y, f(Z_0))
   mgu: \{U: f(Z_0), Y: f(g(g(a))), X_0: f(g(f(a)))\}
([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
   goals: [concat(f(g(f(a))), f(g(g(a))), Z_0), compress(f(Z_0), V), reverse(V, Z)]
   goal: concat(f(g(f(a))), f(g(g(a))), Z_0)
   clause: concat(f(X), Y, f(Z)) := concat(X, Y, Z).
                                                  variable renaming: {X: X_0, Z: Z_1}
   head: concat(f(X_0), Y, f(Z_1))
   mgu: \{Z_0: f(Z_1), Y: f(g(g(a))), X_0: g(f(a))\}
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2 ERIC MARTIN

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([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goal: concat(g(f(a)), f(g(g(a))), Z_1)
    clause: concat(g(X), Y, g(Z)) := concat(X, Y, Z).
                                                       variable renaming: {X: X_0, Z: Z_0}
   head: concat(g(X_0), Y, g(Z_0))
    mgu: \{Z_1: g(Z_0), Y: f(g(g(a))), X_0: f(a)\}
([\mathsf{concat}(f(\mathsf{g}(\mathsf{g}(\mathsf{a}))),\ f(f(\mathsf{g}(f(\mathsf{a})))),\ \mathsf{U}),\ \mathsf{compress}(\mathsf{U},\ \mathsf{V}),\ \mathsf{reverse}(\mathsf{V},\ \mathsf{Z})],\ \{\mathtt{X}\colon\,\mathsf{Z}\})]
    goal: concat(f(a), f(g(g(a))), Z_0)
    clause: concat(f(X), Y, f(Z)) := concat(X, Y, Z).
                                                     variable renaming: {X: X_0, Z: Z_1}
   head: concat(f(X_0), Y, f(Z_1))
   mgu: \{Z_0: f(Z_1), Y: f(g(g(a))), X_0: a\}
\frac{\text{goals\_solution\_list:}}{\text{goals\_solution\_list:}} [([\text{concat(a, f(g(g(a))), Z_1), compress(f(f(g(f(Z_1)))), V), reverse(V, Z)], {X: Z}),}
                     ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [concat(a, f(g(g(a))), Z_1), compress(f(f(g(f(Z_1)))), V), reverse(V, Z)]  solution: \{X: Z\}
    goal: concat(a, f(g(g(a))), Z_1)
    clause: concat(a, Y, Y).
                               variable renaming: {}
    head: concat(a, Y, Y)
    mgu: \{Z_1: Y, Y: f(g(g(a)))\}
goals_solution_list: [([compress(f(f(g(f(f(g(g(a))))))), V), reverse(V, Z)], {X: Z}),
                     ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [compress(f(f(g(f(f(g(g(a))))))), V), reverse(V, Z)]
                                                                 solution: {X: Z}
    goal: compress(f(f(g(f(f(g(g(a))))))), V)
    clause: compress(f(X)), Y) := compress(f(X), Y). variable renaming: \{X: X_0\}
   head: compress(f(f(X_0)), Y)
    mgu: \{V: Y, X_0: g(f(f(g(g(a)))))\}
\begin{tabular}{ll} {\tt goals\_solution\_list:} & $[([compress(f(g(f(f(g(g(a)))))), Y), reverse(Y, Z)], \{X: Z\}), $] \end{tabular}
                     ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [compress(f(g(f(f(g(g(a)))))), Y), reverse(Y, Z)] solution: \{X: Z\}
    goal: compress(f(g(f(f(g(g(a)))))), Y)
    clause: compress(f(g(X)), f(Y)) := compress(g(X), Y). variable renaming: \{X: X_0, Y: Y_0\}
    head: compress(f(g(X_0)), f(Y_0))
    mgu: \{Y: f(Y_0), X_0: f(f(g(g(a))))\}
goals\_solution\_list: [([compress(g(f(f(g(g(a))))), Y_0), reverse(f(Y_0), Z)], \{X: Z\}),
                     ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [compress(g(f(f(g(g(a))))), Y_0), reverse(f(Y_0), Z)]
                                                                 solution: {X: Z}
    goal: compress(g(f(f(g(g(a))))), Y_0)
    clause: compress(g(f(X)), g(Y)) := compress(f(X), Y). variable renaming: \{X: X_{-}0\}
   head: compress(g(f(X_0)), g(Y))
   mgu: \{Y_0: g(Y), X_0: f(g(g(a)))\}
goals_solution_list: [([compress(f(f(g(g(a)))), Y), reverse(f(g(Y)), Z)], {X: Z}),
                     ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [compress(f(f(g(g(a)))), Y), reverse(f(g(Y)), Z)]
                                                             solution: {X: Z}
    goal: compress(f(f(g(g(a)))), Y)
    clause: compress(f(X)), Y) := compress(f(X), Y). variable renaming: \{X: X_0, Y: Y_0\}
    head: compress(f(f(X_0)), Y_0)
    mgu: \{Y: Y_0, X_0: g(g(a))\}
goals_solution_list: [([compress(f(g(g(a))), Y_0), reverse(f(g(Y_0)), Z)], {X: Z}),
                     ([\mathsf{concat}(f(g(g(a))),\ f(f(g(f(a)))),\ U),\ \mathsf{compress}(U,\ V),\ \mathsf{reverse}(V,\ Z)],\ \big\{\mathtt{X}\colon\, \mathtt{Z}\big\})]
    goals: [compress(f(g(g(a))), Y_0), reverse(f(g(Y_0)), Z)]
                                                              solution: {X: Z}
    goal: compress(f(g(g(a))), Y_0)
    clause: compress(f(g(X)), f(Y)) := compress(g(X), Y). variable renaming: \{X: X_{-}0\}
   head: compress(f(g(X_0)), f(Y))
   mgu: \{Y_0: f(Y), X_0: g(a)\}
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([\mathsf{concat}(f(g(g(a))),\ f(f(g(f(a)))),\ U),\ \mathsf{compress}(U,\ V),\ \mathsf{reverse}(V,\ Z)],\ \big\{\mathtt{X}\colon\, \mathtt{Z}\big\})]
    goals: [compress(g(g(a)), Y), reverse(f(g(f(Y))), Z)] solution: \{X: Z\}
    goal: compress(g(g(a)), Y)
    clause: compress(g(g(X)), Y) := compress(g(X), Y). variable renaming: \{X: X_0, Y: Y_0\}
    head: compress(g(g(X_0)), Y_0)
    mgu: {Y: Y_0, X_0: a}
goals\_solution\_list: [([compress(g(a), Y_0), reverse(f(g(f(Y_0))), Z)], {X: Z}),
                        ([\mathsf{concat}(f(\mathsf{g}(\mathsf{g}(\mathsf{a}))),\ f(f(\mathsf{g}(f(\mathsf{a})))),\ \mathsf{U}),\ \mathsf{compress}(\mathsf{U},\ \mathsf{V}),\ \mathsf{reverse}(\mathsf{V},\ \mathsf{Z})],\ \big\{\mathtt{X}\colon \mathsf{Z}\big\})]
                                                                  solution: {X: Z}
    goals: [compress(g(a), Y_0), reverse(f(g(f(Y_0))), Z)]
    goal: compress(g(a), Y_0)
    clause: compress(g(a), g(a)).
                                         variable renaming: {}
    head: compress(g(a), g(a))
    mgu: {Y_0: g(a)}
goals_solution_list: [([reverse(f(g(f(g(a)))), Z)], {X: Z}),
                        ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [reverse(f(g(f(g(a)))), Z)]
                                             solution: {X: Z}
    goal: reverse(f(g(f(g(a)))), Z)
    clause: reverse(X, Y) :- accumulator_reverse(X, a, Y). variable renaming: {X: X_0}
    head: reverse(X_0, Y)
    mgu: \{Z: Y, X_0: f(g(f(g(a))))\}
goals_solution_list: [([accumulator_reverse(f(g(f(g(a)))), a, Y)], {X: Y}),
                        ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [accumulator_reverse(f(g(f(g(a)))), a, Y)]
                                                               solution: {X: Y}
    goal: accumulator_reverse(f(g(f(g(a)))), a, Y)
    clause: accumulator_reverse(f(X), Y, Z) :- accumulator_reverse(X, f(Y), Z). variable renaming: {X: X_0, Y: Y_0}
    head: accumulator_reverse(f(X_0), Y_0, Z)
    mgu: \{Y: Z, Y_0: a, X_0: g(f(g(a)))\}
\label{eq:goals_solution_list} \begin{split} & goals\_solution\_list \colon \mbox{\tt [([accumulator\_reverse(g(f(g(a))), f(a), Z)], $\{X$: Z$),} \end{split}
                        ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [accumulator_reverse(g(f(g(a))), f(a), Z)]
                                                              solution: {X: Z}
    goal: accumulator_reverse(g(f(g(a))), f(a), Z)
    clause: accumulator_reverse(g(X), Y, Z) :- accumulator_reverse(X, g(Y), Z).
                                                                                            variable renaming: {X: X_0, Z: Z_0}
    head: accumulator_reverse(g(X_0), Y, Z_0)
    mgu: \{Z: Z_0, Y: f(a), X_0: f(g(a))\}
goals_solution_list:[([accumulator_reverse(f(g(a)), g(f(a)), Z_0)], \{X: Z_0\}),
                        ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
                                                                 solution: {X: Z_0}
    goals: [accumulator_reverse(f(g(a)), g(f(a)), Z_0)]
    goal: accumulator_reverse(f(g(a)), g(f(a)), Z_0)
    clause: accumulator_reverse(f(X), Y, Z) :- accumulator_reverse(X, f(Y), Z). variable renaming: {X: X_0}
    head: accumulator_reverse(f(X_0), Y, Z)
    mgu: \{Z_0: Z, Y: g(f(a)), X_0: g(a)\}
goals_solution_list: [([accumulator_reverse(g(a), f(g(f(a))), Z)], {X: Z}),
                        ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: [accumulator_reverse(g(a), f(g(f(a))), Z)]
                                                              solution: {X: Z}
    goal: accumulator_reverse(g(a), f(g(f(a))), Z)
    clause: accumulator_reverse(g(X), Y, Z) :- accumulator_reverse(X, g(Y), Z). variable renaming: {X: X_0, Z: Z_0}
    head: accumulator_reverse(g(X_0), Y, Z_0)
    mgu: \{Z: Z_0, Y: f(g(f(a))), X_0: a\}
goals_solution_list: [([accumulator_reverse(a, g(f(g(f(a)))), Z_0)], {X: Z_0}),
                        ([\mathsf{concat}(f(\mathsf{g}(\mathsf{g}(\mathsf{a}))),\ f(f(\mathsf{g}(f(\mathsf{a})))),\ \mathsf{U}),\ \mathsf{compress}(\mathsf{U},\ \mathsf{V}),\ \mathsf{reverse}(\mathsf{V},\ \mathsf{Z})],\ \big\{\mathtt{X}\colon \mathsf{Z}\big\})]
    goals: [accumulator_reverse(a, g(f(g(f(a)))), Z_0)]
                                                                 solution: {X: Z_0}
    goal: accumulator_reverse(a, g(f(g(f(a)))), Z_0)
    clause: accumulator_reverse(a, X, X).
                                                 variable renaming: {X: X_0}
    head: accumulator_reverse(a, X_0, X_0)
    mgu: \{Z_0: X_0, X_0: g(f(g(f(a))))\}
goals_solution_list: [([], X: g(f(g(f(a))))),
                        ([concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)], \{X: Z\})]
    goals: []
                  solution: \{X: g(f(g(f(a))))\}
    YIELDED SOLUTION: {X: g(f(g(f(a))))}
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goals: [concat(f(g(g(a))), f(f(g(f(a)))), U), compress(U, V), reverse(V, Z)]
                                                                                                                       solution: {X: Z}
     goal: concat(f(g(g(a))), f(f(g(f(a)))), U)
     clause: concat(f(X), Y, f(Z)) := concat(X, Y, Z).
                                                                                 variable renaming: {X: X_0, Z: Z_0}
     head: concat(f(X_0), Y, f(Z_0))
     mgu: \{U: f(Z_0), Y: f(f(g(f(a)))), X_0: g(g(a))\}
\frac{\text{goals\_solution\_list:}}{\text{[([concat(g(g(a)), f(f(g(f(a)))), Z\_0), compress(f(Z\_0), V), reverse(V, Z)], } \{X: Z\})]}
     goals: [concat(g(g(a)), f(f(g(f(a)))), Z_0), compress(f(Z_0), V), reverse(V, Z)]  solution: \{X: Z\}
     goal: concat(g(g(a)), f(f(g(f(a)))), Z_0)
                                                                               variable renaming: {X: X_0, Z: Z_1}
     clause: concat(g(X), Y, g(Z)) := concat(X, Y, Z).
     head: concat(g(X_0), Y, g(Z_1))
     mgu: \{Z_0: g(Z_1), Y: f(f(g(f(a)))), X_0: g(a)\}
goals: [concat(g(a), f(f(g(f(a)))), Z_1), compress(f(g(Z_1)), V), reverse(V, Z)]
                                                                                                                             solution: {X: Z}
     goal: concat(g(a), f(f(g(f(a)))), Z_1)
     clause: concat(g(X), Y, g(Z)) :- concat(X, Y, Z).
                                                                                 variable renaming: {X: X_0, Z: Z_0}
     head: concat(g(X_0), Y, g(Z_0))
     mgu: \{Z_1: g(Z_0), Y: f(f(g(f(a)))), X_0: a\}
goals: [concat(a, f(f(g(f(a)))), Z_0), compress(f(g(g(Z_0))), V), reverse(V, Z)] solution: \{X: Z\}
     goal: concat(a, f(f(g(f(a)))), Z_0)
     clause: concat(a, Y, Y).
                                             variable renaming: {}
     head: concat(a, Y, Y)
     mgu: \{Z_0: Y, Y: f(f(g(f(a))))\}
goals_solution_list: [([compress(f(g(g(f(g(f(a))))))), V), reverse(V, Z)], \{X: Z\})]
     goals: [compress(f(g(g(f(f(g(f(a))))))), V), reverse(V, Z)]
     goal: compress(f(g(g(f(f(g(f(a))))))), V)
     clause: compress(f(g(X)), f(Y)) := compress(g(X), Y). variable renaming: \{X: X_{-}0\}
     head: compress(f(g(X_0)), f(Y))
     mgu: \{V: f(Y), X_0: g(f(f(g(f(a)))))\}
\begin{tabular}{ll} \beg
     goals: [compress(g(g(f(f(g(f(a)))))), Y), reverse(f(Y), Z)]
                                                                                               solution: {X: Z}
     goal: compress(g(g(f(f(g(f(a)))))), Y)
     head: compress(g(g(X_0)), Y_0)
     mgu: \{Y: Y_0, X_0: f(f(g(f(a))))\}
goals_solution_list: [([compress(g(f(g(f(a)))), Y_0), reverse(f(Y_0), Z)], {X: Z})]
     goals: [compress(g(f(f(g(f(a))))), Y_0), reverse(f(Y_0), Z)]
                                                                                                 solution: {X: Z}
     goal: compress(g(f(f(g(f(a))))), Y_0)
     clause: compress(g(f(X)), g(Y)) := compress(f(X), Y). variable renaming: \{X: X_{-}0\}
     head: compress(g(f(X_0)), g(Y))
     mgu: \{Y_0: g(Y), X_0: f(g(f(a)))\}
\frac{\text{goals\_solution\_list:}}{\text{[([compress(f(f(g(f(a)))), Y), reverse(f(g(Y)), Z)], {X: Z}))]}}
     goals: [compress(f(f(g(f(a)))), Y), reverse(f(g(Y)), Z)]
                                                                                          solution: {X: Z}
     goal: compress(f(f(g(f(a)))), Y)
     clause: compress(f(X)), Y) := compress(f(X), Y). variable renaming: \{X: X_0, Y: Y_0\}
     head: compress(f(f(X_0)), Y_0)
     mgu: {Y: Y_0, X_0: g(f(a))}
goals_solution_list: [([compress(f(g(f(a))), Y_0), reverse(f(g(Y_0)), Z)], {X: Z})]
     goal: compress(f(g(f(a))), Y_0)
     clause: compress(f(g(X)), f(Y)) := compress(g(X), Y). variable renaming: \{X: X_{=}0\}
     head: compress(f(g(X_0)), f(Y))
     mgu: \{Y_0: f(Y), X_0: f(a)\}
\begin{tabular}{ll} {\tt goals\_solution\_list:} & [([compress(g(f(a)), Y), reverse(f(g(f(Y))), Z)], {\tt X: Z}))] \\ \end{tabular}
     goals: [compress(g(f(a)), Y), reverse(f(g(f(Y))), Z)]
                                                                                    solution: {X: Z}
     goal: compress(g(f(a)), Y)
     clause: compress(g(f(X)), g(Y)) := compress(f(X), Y). variable renaming: \{X: X_0, Y: Y_0\}
     head: compress(g(f(X_0)), g(Y_0))
     mgu: {Y: g(Y_0), X_0: a}
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\label{eq:goals_solution_list} \begin{split} & goals\_solution\_list: \ [([compress(f(a), Y_0), \, reverse(f(g(f(g(Y_0)))), \, Z)], \, \{X: \, Z\})] \end{split}
   goals: [compress(f(a), Y_0), reverse(f(g(f(g(Y_0)))), Z)]
                                                              solution: {X: Z}
    goal: compress(f(a), Y_0)
    clause: compress(f(a), f(a)).
                                    variable renaming: {}
    head: compress(f(a), f(a))
   mgu: {Y_0: f(a)}
goals_solution_list: [([reverse(f(g(f(g(f(a))))), Z)], {X: Z})]
    goals: [reverse(f(g(f(g(f(a))))), Z)]
                                          solution: {X: Z}
    goal: reverse(f(g(f(g(f(a))))), Z)
    clause: reverse(X, Y) :- accumulator_reverse(X, a, Y). variable renaming: {X: X_0}
   head: reverse(X_0, Y)
    mgu: \{Z: Y, X_0: f(g(f(g(f(a)))))\}
goals\_solution\_list: [([accumulator\_reverse(f(g(f(g(f(a))))), a, Y)], {X: Y})]
    goals: [accumulator_reverse(f(g(f(g(f(a))))), a, Y)]
                                                          solution: {X: Y}
   goal: accumulator_reverse(f(g(f(g(f(a))))), a, Y)
    clause: accumulator_reverse(f(X), Y, Z) :- accumulator_reverse(X, f(Y), Z).
                                                                                 variable renaming: {X: X_0, Y: Y_0}
   head: accumulator_reverse(f(X_0), Y_0, Z)
   mgu: \{Y: Z, Y_0: a, X_0: g(f(g(f(a))))\}
goals: [accumulator_reverse(g(f(g(f(a)))), f(a), Z)]
                                                          solution: {X: Z}
    goal: accumulator_reverse(g(f(g(f(a)))), f(a), Z)
    clause: accumulator_reverse(g(X), Y, Z) :- accumulator_reverse(X, g(Y), Z).
                                                                                 variable renaming: {X: X_0, Z: Z_0}
    head: accumulator_reverse(g(X_0), Y, Z_0)
    mgu: \{Z: Z_0, Y: f(a), X_0: f(g(f(a)))\}
goals: [accumulator_reverse(f(g(f(a))), g(f(a)), Z_0)]
                                                            solution: {X: Z_0}
    goal: accumulator_reverse(f(g(f(a))), g(f(a)), Z_0)
    clause: accumulator_reverse(f(X), Y, Z) :- accumulator_reverse(X, f(Y), Z).
                                                                                 variable renaming: {X: X_0}
   head: accumulator_reverse(f(X_0), Y, Z)
   mgu: \{Z_0: Z, Y: g(f(a)), X_0: g(f(a))\}
goals_solution_list: [([accumulator_reverse(g(f(a)), f(g(f(a))), Z)], {X: Z})]
    goals: [accumulator_reverse(g(f(a)), f(g(f(a))), Z)]
                                                          solution: {X: Z}
    goal: accumulator_reverse(g(f(a)), f(g(f(a))), Z)
    clause: accumulator_reverse(g(X), Y, Z) :- accumulator_reverse(X, g(Y), Z).
                                                                                 variable renaming: {X: X_0, Z: Z_0}
    head: accumulator_reverse(g(X_0), Y, Z_0)
    mgu: \{Z: Z_0, Y: f(g(f(a))), X_0: f(a)\}
goals_solution_list: [([accumulator_reverse(f(a), g(f(g(f(a)))), Z_0)], \{X: Z_0\})]
    goals: [accumulator_reverse(f(a), g(f(g(f(a)))), Z_0)]
                                                            solution: {X: Z_0}
    goal: accumulator_reverse(f(a), g(f(g(f(a)))), Z_0)
    clause: accumulator_reverse(f(X), Y, Z) :- accumulator_reverse(X, f(Y), Z).
                                                                                 variable renaming: {X: X_0}
   head: accumulator_reverse(f(X_0), Y, Z)
    mgu: \{Z_0: Z, Y: g(f(g(f(a)))), X_0: a\}
goals_solution_list: [([accumulator_reverse(a, f(g(f(g(f(a))))), Z)], {X: Z})]
    goals: [accumulator_reverse(a, f(g(f(g(f(a))))), Z)]
                                                          solution: {X: Z}
    goal: accumulator_reverse(a, f(g(f(g(f(a))))), Z)
    clause: accumulator_reverse(a, X, X).
                                            variable renaming: {X: X_0}
    head: accumulator_reverse(a, X_0, X_0)
   mgu: \{Z: X_0, X_0: f(g(f(g(f(a)))))\}
goals_solution_list: [([], {X: f(g(f(g(f(a)))))})]
               solution: {X: f(g(f(g(f(a)))))}
    YIELDED SOLUTION: {X: f(g(f(g(f(a)))))}
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