Project Report 1

Dingyi Zhuang, Tianyu Shi, Fuyuan Lyu February 11, 2020

In this project, we implement two basic machine learning models: logistic regression and naive bayes. These models are tested upon four classification datasets: Ionosphere Dataset, Iris Dataset, Car Evaluation Dataset and Adult Dataset. These datasets contain various types of features: both continuous and discrete. In the preprocessing phase, we first discretize all the continuous features and targets, handling the missing values and auto-correlated features. In the experiment phase, apart from reporting evaluation metrics upon various models with different datasets, we further investigate the influence of different learning rates, different stopping criteria, hyper-parameter tuning, feature selection and dataset selection.

1 Introduction

Classification tasks is one of the most common and important task in machine learning community. Given certain features, classification task is to categorize which class is most likely to be. In this project, we implement two basic machine learning models: logistic regression and naive bayes, and test their performance upon four datasets: Ionosphere Dataset¹, Adult Dataset², Iris Dataset³ and Car Evaluation Dataset⁴. All the features are discretized during the pre-processing phase. We further investigate the influence of different training techniques, such as hyper-parameter tuning and feature selections, upon the performance of the models.

2 Datasets

The targets of all these four datasets are categorical classification (including binary classification). We exam four datasets to find that no missing values exist. We use *replace* function in *pandas* module to process all the target values into categorical count value. We will briefly describe the specific features and then introduce how to extract/process the features.

Ionosphere Dataset

Ionosphere dataset contains 34 radar data (real values between -1 and 1) with 351 rows[1]. We find their distribution with respect to the "good" or "bad" target, which is reflected in Figure 1. We then remove radar 1 feature which is always 0. We can see that good class and bad class have quite distinct patterns in the antennas power value, which is essential in the following classification. We also fill between the intervals of good-class feature distribution to find that such surface is quite similar to the auto-correlated signals. Therefore, we use Principal Component Analysis (PCA) to reduce the dimensions from 34 into 10 to learn the low-rank representation for more efficient and powerful training.

¹https://archive.ics.uci.edu/ml/datasets/ionosphere

 $^{^2 {\}tt https://archive.ics.uci.edu/ml/datasets/Adult}$

³https://archive.ics.uci.edu/ml/datasets/Iris

⁴https://archive.ics.uci.edu/ml/datasets/Car+Evaluation



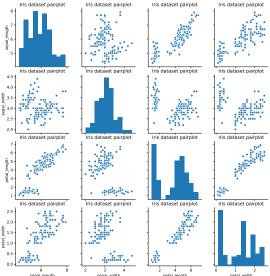
Figure 1: Distribution of average numerical features given "good" or "bad" class in ionosphere dataset

Adult Dataset

Adult dataset aims to predict whether income exceeds \$50K/yr based on census data[2]. There are 32561 records and 14 features included with datatypes of continuous count values, continuous real values and categorical/binary values. We min-max normalize continuous values (both count and real), discretize normalized real values into 10 categories and leave everything else untouched.

Iris Dataset

There are 4 continuous real value attributes, whose basic statistic information are listed in Figure 2 and Table 1, where sl,sw,pw,pw stand for $sepal\ length$, $sepal\ width$, $petal\ width$, $petal\ length$ [3]. Linear correlation between features can be found, e.g. petal length & petal width and petal length & sepal length. We also min-max, normalize and then discretize the normed real values.



| sepal_length | 8 | | 3 sepal_width | | 2 peta | 4 al_length | | O | petal_w | idth | |
|--------------|----|----|------------------|------|-----------|----------------|------------|-------|---------|------|--|
| Figure | 2: | Pa | airpl | ot o | f iris | da | $_{ m ta}$ | feati | ure | s | |

| sl | sw | $_{ m pl}$ | pw |
|------|---|---|---|
| 150 | 150 | 150 | 150 |
| 5.84 | 3.05 | 3.75 | 1.19 |
| 0.82 | 0.43 | 1.76 | 0.76 |
| 4.3 | 2.0 | 1.0 | 0.1 |
| 5.1 | 2.8 | 1.6 | 0.3 |
| 5.8 | 3.0 | 4.3 | 1.3 |
| 6.4 | 3.3 | 5.1 | 1.8 |
| 7.9 | 4.4 | 6.9 | 2.5 |
| | 150 5.84 0.82 4.3 5.1 5.8 6.4 | 150 150 5.84 3.05 0.82 0.43 4.3 2.0 5.1 2.8 5.8 3.0 6.4 3.3 | 150 150 150 5.84 3.05 3.75 0.82 0.43 1.76 4.3 2.0 1.0 5.1 2.8 1.6 5.8 3.0 4.3 6.4 3.3 5.1 |

Table 1: Iris data description

Car Evaluation Dataset

In Car Evaluation Dataset, we use 1728 records from 6 categorical features of cars, e.g. price, door number and capacity, to predict the safety level of the cars [4]. This dataset is quite straightforward, we only transform the raw data into categorical features to predict the categorical safety level.

3 Results

Accuracy comparison on four datasets

From Table 2, for accuracy of each model, we find that our implemented logistic regression model can work well on small datasets (iris and ionosphere datasets) but worse in larger dataset (car and adult datasets) compared with sklearn model. In the contrary, naive bayes work well on large dataset but worse in small dataset.

| | iris | car | adult | ionosphere |
|------------------------------|------|----------------------|-------|------------|
| logistic regression(ours) | 0.75 | 0.65 | 0.66 | 0.80 |
| logistic regression(sklearn) | 0.93 | 0.87 | 0.82 | 0.82 |
| naive bayes(ours) | 0.34 | 0.69 | 0.76 | 0.67 |
| naive bayes(sklearn) | 0.74 | 0.69 | 0.75 | 0.81 |

Table 2: Accuracy of our implemented model in four datasets comparing to sklearn module

Furthermore, we compare the different evaluation metrics for binary classification, where ionosphere dataset and adult dataset are selected. Details can be found in Table 3, where **o** stands for our model and **s** for results after running *sklearn* module. We found that our model have lower precision and recall on class 1 for large dataset (adult data), which can explain why the model fail to show the performance like *sklearn* model. We plan to investigate more in the characteristic of the features in large dataset.

| | | | ionosphere/adult | dataset | | | |
|--------------|--------------|--------------|------------------|-----------|-----------|-----------|--------------------------|
| | precision(o) | precision(s) | recall(o) | recall(s) | f1(o) | f1(s) | $\operatorname{support}$ |
| class 0 | 1.00/0.93 | 0.90/0.83 | 0.48/0.49 | 0.48/0.95 | 0.65/0.64 | 0.86/0.89 | 33/4937 |
| class 1 | 0.69/0.35 | 0.85/0.71 | 1.00/0.88 | 1.00/0.39 | 0.81/0.51 | 0.88/0.51 | 37/1575 |
| macro avg | 0.84/0.64 | 0.88/0.77 | 0.74/0.68 | 0.74/0.67 | 0.73/0.57 | 0.87/0.70 | 70/6512 |
| weighted avg | 0.83/0.79 | 0.87/0.80 | 0.76/0.58 | 0.76/0.81 | 0.74/0.61 | 0.87/0.79 | 70/6512 |

Table 3: Different evaluation metrics of our implemented model in binary-target datasets comparing to sklearn module

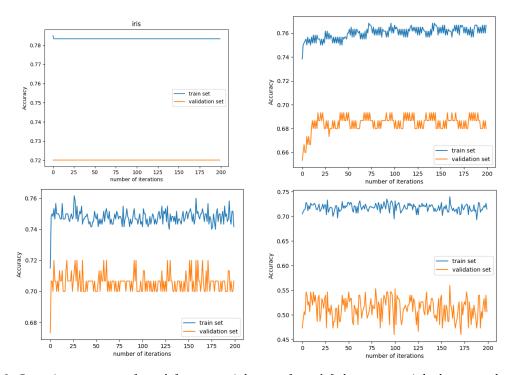


Figure 3: Learning rate test, from left top to right top, from left bottom to right bottom, the learning rates are: 0.001, 0.01, 0.1 and 1

Learning rate test

We mainly test learning rates with stopping threshold 0.05 in four datasets, a specific case on iris dataset is shown in Figure 4. For small learning rate, like 0.0001, the accuracy makes no change during the gradient decent, which means that it converges very slow. When the learning rate is very big such as 1, the accuracy will fluctuate sharply, which means that it will become unstable during gradient descent.

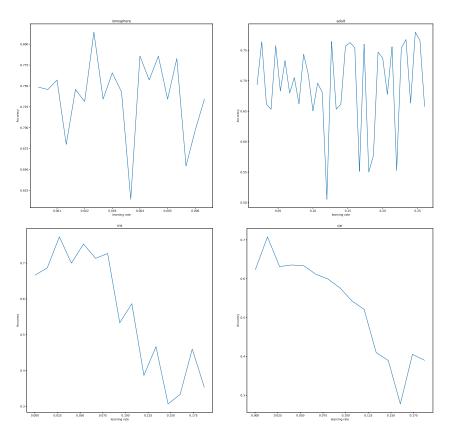


Figure 4: Hyperparameter search for learning rates in different datasets, from left bottom to right bottom, the learning rates are: ionosphere, adult, iris and car datasets

We also find similar effect on four data set, with different learning rate range. For example, in iris dataset, the best learning rate in our experiment should be around 0.01. But in adult data set it should be 0.1. Then, we perform hyperparameter search in a smaller range of learning rate, which is shown in Figure 5. According to our experiment, we find the best learning rate for iris dataset should be 0.025, ionosphere dataset should be 0.0025, car dataset should be 0.015 and adult dataset should be 0.24.

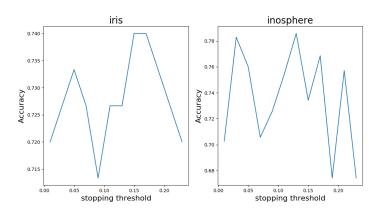


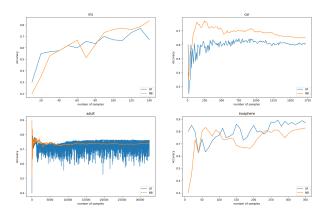
Figure 5: Best stopping criterion for Ionosphere Dataset and Iris Dataset given optimal learning rate

Stopping criteria for logistic regression

We also investigate the stopping criteria on four datasets. The stopping criteria is considered as a threshold for change in the value of cost function. From Figure 5, we find there are not much influence on accuracy for car and adult datasets because these two datasets are very big, our model may need to run max iteration to meet the optimal solution. We find that for iris and ionosphere datasets, there will be optimal criteria, which are 0.15 and 0.14 respectively.

Accuracy as a function of the size of dataset

From Figure 6 we can find that accuracy increases when sample size is roughly less than 200. However, the accuracy becomes stable even the sample size continues growing.



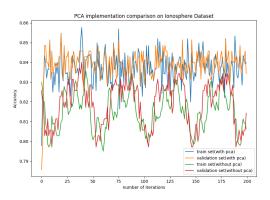


Figure 6: Learning rate test, from left top to right top, from left bottom to right bottom, the learning rates are: 0.001, 0.01, 0.1 and 1

Figure 7: Training and validation accuracy comparison before and after using PCA

Dimension reduction comparison

Because ionosphere has strong auto-correlation, we use PCA to reduce the dimensions for better training results, which can be reflected in Figure 7. It can be found that accuracy on both training and validation sets perform better if PCA is applied. By using PCA for dimension reduction, we can learn better representation of features.

4 Discussion and Conclusion

In this report, we implement logistic regression and naive bayes models. They are tested on four categorical classification datasets. In data cleaning part, we check missing values, discretize the real values and reduce dimensions for auto-correlated features. We test the accuracy and impact of learning rate, stopping criteria and dimension reduction, where we all choose a improved strategy. As future work, we still need to look into why our model would perform less accuracy and efficient than *sklearn* module.

5 Statement of Contributions

- Dingyi Zhunag: Data preprocessing, data analysis and report formating.
- Fuyuan Lyu: Model implementation and report writing.
- Tianyu Shi: Running experiment, data visualization and data analysis.

References

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