



**Felipe Vieira Cortes**

**Type Reference**

**Tese de Doutorado**

Thesis presented to the Programa de Pós-graduação em Informática, do Departamento de Informática da PUC-Rio in partial fulfillment of the requirements for the degree of Doutor em Informática.

Advisor: Prof. Roberto Ierusalimsky

Rio de Janeiro  
March 2018



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To my parents, for their support  
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## **Abstract**

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The acquisition of triangular meshes typically introduces undesired noise...

## **Keywords**

Geometry Processing; Mesh Denoising; Adaptive Patches.

## Resumo

Cortes, Felipe V.; Ierusalimschy, Roberto. **Referência de tipos**. Rio de Janeiro, 2018. 23p. Tese de Doutorado – Departamento de Informática, Pontifícia Universidade Católica do Rio de Janeiro.

A aquisição de malhas triangulares normalmente introduz ruídos indesejados...

## Palavras-chave

Procesamento Geométrico; Remoção de ruído de malha; Vizinhança adaptativa.

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## List of Abbreviations

ADI – Análise Digital de Imagens

BIF – *Banded Iron Formation*

*My beautifull epigraph*

**Wassily Kandinsky**, *Regards sur le passé.*

# 1

## Introduction

Nowadays 3D surface models are used in several fields and industries such as medicine, engineering, entertainment, geo-exploration, architecture, cultural heritage and so on. These models can be acquired from a variety of sources like 3D scanning, 3D imaging, multi-view stereo reconstruction, CAD modeling, etc. The data generated by these techniques should be processed to be available for production or any task where it can be used (visualization, simulation, animation, interaction, etc.). This processing step is called digital geometry processing which is a field of computer science that uses mathematical models and algorithms (BOTSCH et al., 2010). Figure 1.1 shows some examples of noisy meshes.

This document is structured as follows. In Chapter 2 we present some previous work relevant to our problem. In Chapter 3 we explain our proposal. In Chapter 4 we show our results. Finally, in Chapter 5 we present our conclusion and future work.

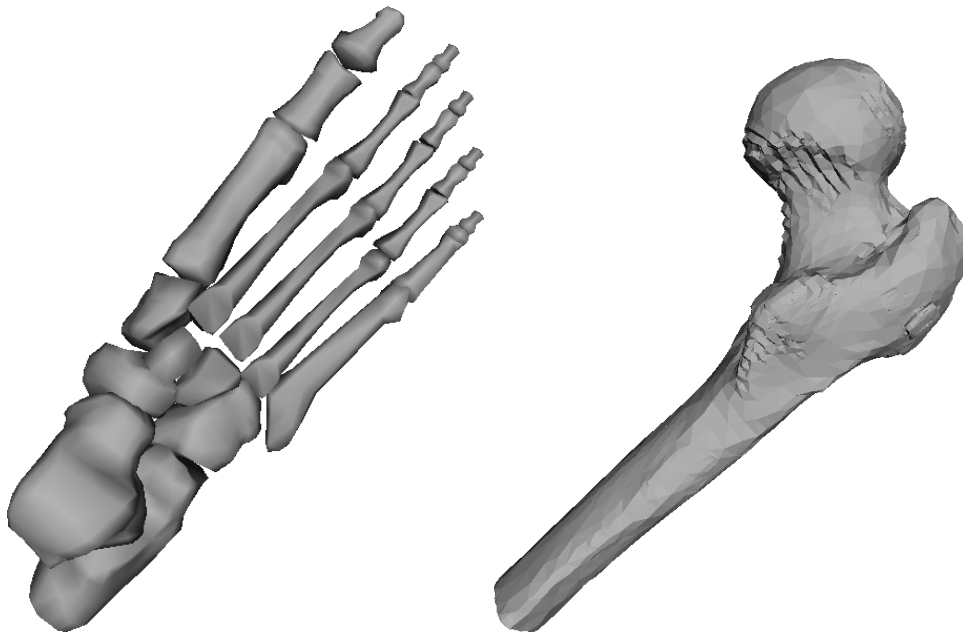
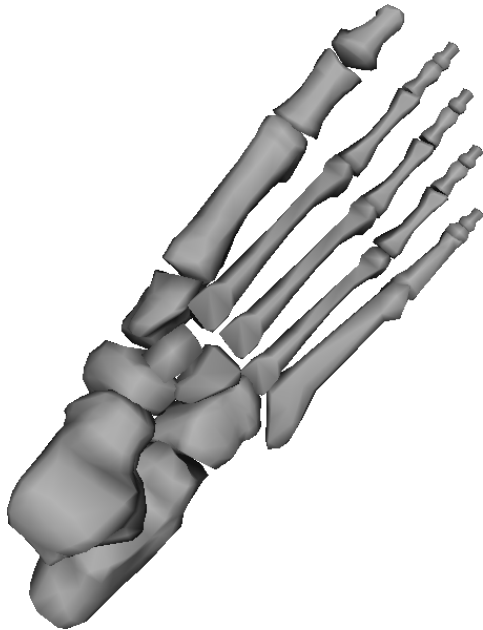


Figure 1.1: Meshes generated from medical data. Data obtained from the AIM@SHAPE Shape Repository (AIM@SHAPE..., )

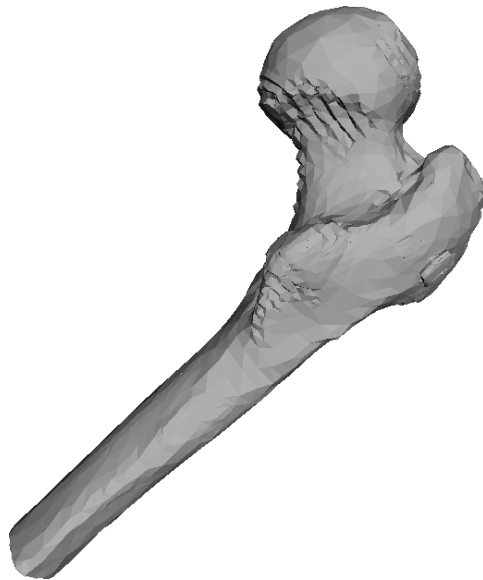
## 2

### Previous Work

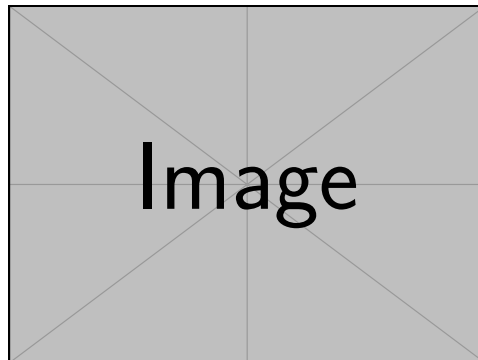
Early smoothing methods tried to minimize... In the figure 2.2d we see...



(a) Bamboo-pile Vertically Inserted Position



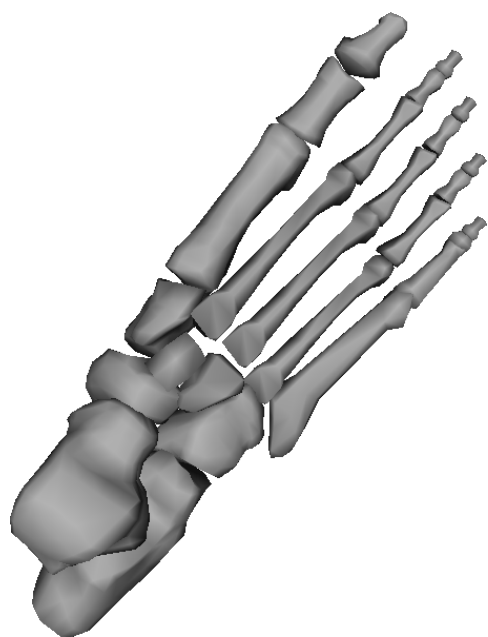
(b) Bamboo-pile Normal Inserted Position



(c) bamboo-pile Inserted 45° angle

Figure 2.1: A set of three subfigures: (a) describes the first subfigure; (b) describes the second subfigure; (c) describes the third subfigure.

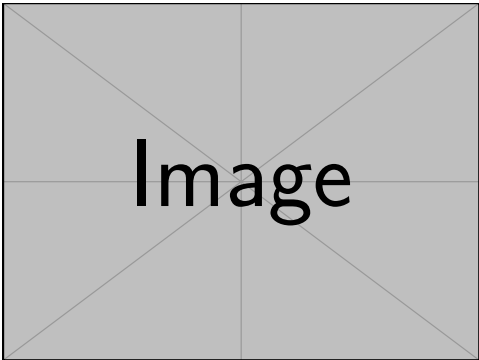




(a) Bamboo-pile Vertically Inserted Position

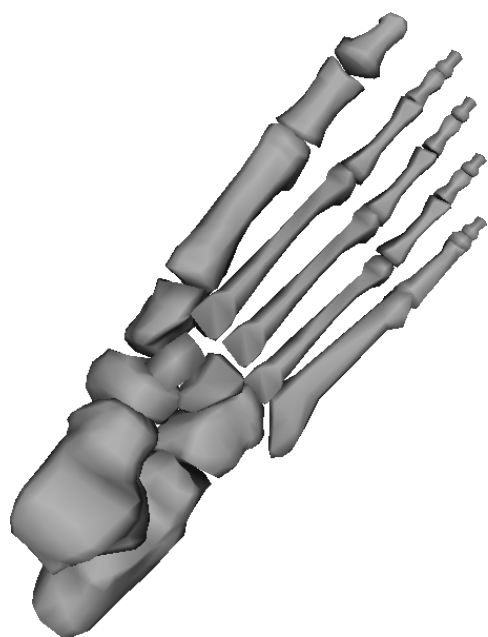


(b) Bamboo-pile Normal Inserted Position

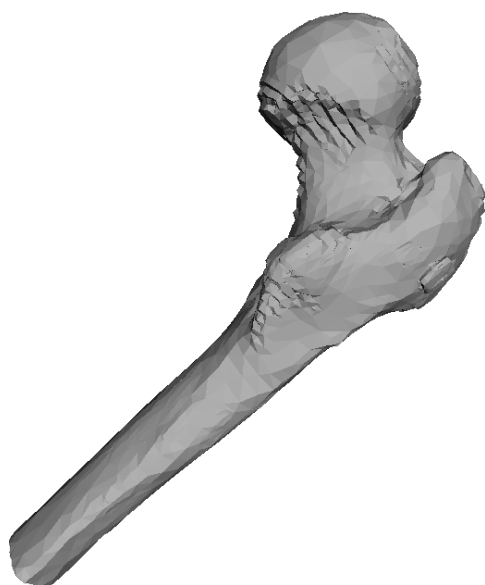


(c) bamboo-pile Inserted 45° angle

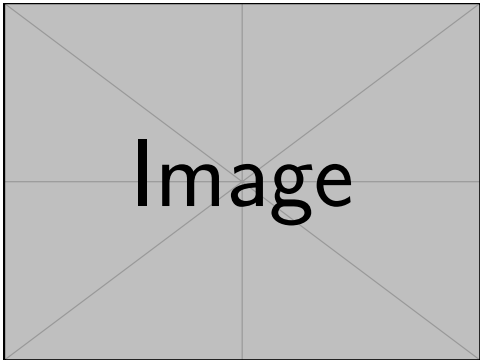
Figure 2.2: A set of six subfigures in two pages.



(d) Bamboo-pile Vertically Inserted Position



(e) Bamboo-pile Normal Inserted Position



(f) bamboo-pile Inserted 45° angle

Figure 2.2: A set of six subfigures in two pages.(Continuation)

### 3 Proposal

Equation example 1:

$$\begin{aligned} \min_u \int_{x_i \in X} \int_{x_j \in X} q_{ij} u_i u_j da + \int_{x_i \in X} \|x' - x_i\| u_i da \\ s.t. \quad u \in [0, 1] \quad \wedge \quad \int_{x_i \in X} u da = a_0, \end{aligned} \quad (3-1)$$

Equation exmaple 2:

$$\begin{aligned} \min_{\mathbf{u}} \alpha \mathbf{u}^T \mathbf{A}^T \mathbf{Q} \mathbf{A} \mathbf{u} + \beta \mathbf{d}^T \mathbf{a}' \mathbf{A} \mathbf{u} + \gamma \mathbf{u}^T \mathbf{G}^T \mathbf{G} \mathbf{u} + \delta \mathbf{f}^T \mathbf{a}' \mathbf{A} \mathbf{u} \\ s.t. \quad \mathbf{0} \leq \mathbf{u} \leq \mathbf{1} \wedge \mathbf{a}^T \mathbf{u} = a_0. \end{aligned} \quad (3-2)$$

Equation example 3:

$$\mathbf{G} = (g_{ij}) = \begin{cases} \sum_{f_k \in N_f(f_i)} l_{ik} & i = j \\ -l_{ij} & e_{ij} \in E \\ 0 & \text{otherwise} \end{cases} \quad (3-3)$$

---

#### Code 1: Mean Filter

---

```

1 #
   -----#

2 # Create filter function
3 # l is the width of window
4 #
   -----#

5 meanfilter <- function( l, imagem ) {
6   if( l%%2 == 0 )
7     print("Please, type an odd number!")
8   imagem.result <- imagem
9   lp1d2 <- (l-1)/2
10  L <- dim(imagem)[1]
11  C <- dim(imagem)[2]
12  for( j in as.integer(lp1d2+1) : as.integer(C-lp1d2)) {
13    for( i in as.integer(lp1d2+1) : as.integer(L-lp1d2)) {
14      imagem.result[i,j] <- mean(imagem[as.integer(i-lp1d2):as.
        integer(i+lp1d2), as.integer(j-lp1d2):as.integer(j+lp1d2)
        ])
15    }
16  }

```

```

17  print("Image filtered with success!")
18  return(imagem.result)
19  }
20  #
    -----#
21  # End of Script.
22  #
    -----#

```

---

**Algorithm 1:** Escolha das amostras iniciais

---

**Input:** Malha e quantidade de pontos a ser amostrado

**Output:** Pontos amostrados na malha

- 1 *Crie um vetor de números randômicos entre  $[0, 1]$  com a quantidade de pontos a ser amostrada e ordene-o*
  - 2 *Calcule a área total dos triângulos da malha*
  - 3 **for**  $i = 0$  **to**  $\text{numeroDePontos}$  **do**
  - 4     *Navegue entre as faces acumulando a sua  $\frac{\text{area}}{\text{areaTotal}}$  até achar a face com valor acumulado  $\geq \text{numerosRandomicos}[i]$*
  - 5     *Pegue um ponto randômico dentro da face utilizando o método de Turk e adicione no vetor do resultado*
-

# 4

## Results

Table example. Table 4.1 shows results.

Table 4.1: Results for devil mesh

	Mean Vertex Dis- tance	L2 Vertex Based	Mean Quadric	MSAE	L2 Nor- mal Based	Tangential	Mean Discrete Curva- ture	Area Error	Volume Error
(FLEISHMAN; DRORI; COHEN- OR, 2003) (JONES; DU- RAND; DES- BRUN, 2003) (SUN et al., 2007) (ZHENG et al., 2011) (HE; SCHAE- FER, 2013) (ZHANG et al., 2015) (YADAV; REITE- BUCH; POLTH- IER, 2016) Ours	0.061277	0.110973	0.236219	19.697900	0.055170	0.047678	0.090284	0.051443	0.045645
	0.001293	0.002800	0.002289	21.237300	0.021589	0.013026	0.087991	0.000364	0.002621
	0.001439	0.002880	0.003540	14.043200	0.012654	0.008911	0.055849	0.007806	0.000582
	0.000713	0.001537	0.001824	12.171400	0.009654	0.005781	0.054567	0.005617	0.000425
	0.002531	0.004560	0.007108	13.830100	0.017459	0.010314	0.114528	0.001686	0.001786
	0.001623	0.003079	0.005048	10.454200	0.015233	0.008054	0.094668	0.002629	0.001326
	0.000737	0.001548	0.001493	16.880800	0.014129	0.006974	0.079952	0.000209	0.002375
	0.000987	0.001902	0.002686	11.574200	0.010632	0.006796	0.075106	0.003970	0.000722

## 4.1

### Comparison

## 5

### Conclusion and future work

We proposed an algorithm for triangular mesh denoising with detail preservation...

---

#### Code 2: Mean Filter

---

```
1 #
   -----#

2 # Create filter function
3 # l is the width of window
4 #
   -----#

5 meanfilter <- function( l, imagem ) {
6   if( l%%2 == 0 )
7     print("Please, type an odd number!")
8   imagem.result <- imagem
9   lp1d2 <- (l-1)/2
10  L <- dim(imagem)[1]
11  C <- dim(imagem)[2]
12  for( j in as.integer(lp1d2+1) : as.integer(C-lp1d2)) {
13    for( i in as.integer(lp1d2+1) : as.integer(L-lp1d2)) {
14      imagem.result[i,j] <- mean(imagem[as.integer(i-lp1d2):as.
15                                integer(i+lp1d2), as.integer(j-lp1d2):as.integer(j+lp1d2)
16                                ])
17    }
18  }
19  print("Image filtered with success!")
20  return(imagem.result)
21 #
   -----#

21 # End of Script.
22 #
   -----#
```

---

## 6

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