FastPolyEval

1.0

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Chapter 1

Fast Evaluation of Real and Complex Polynomials

This documentation is availllable online at https://fvigneron.github.io/FastPolyEval. It also exists in PDF form: FastPolyEval_doc.pdf.

1.1 Abstract

FastPolyEval is a library, written in C, that aims at evaluating polynomials very efficiently, without compromising the accuracy of the result. It is based on the FPE algorithm (Fast Polynomial Evaluator) introduced in reference [1] (see Section References, Contacts and Copyright).

In FastPolyEval, the computations are done for real or complex numbers, in floating point arithmetic, with a fixed precision, which can be one of the machine types FP32, FP64, FP80 or an arbitrary precision based on MPFR.

Evaluations are performed on arbitrary (finite...) sets of points in the complex plane or along the real line, without geometrical constraints.

The average speed-up achieved by FastPolyEval over Hörner's scheme is illustrated on Figure 1.

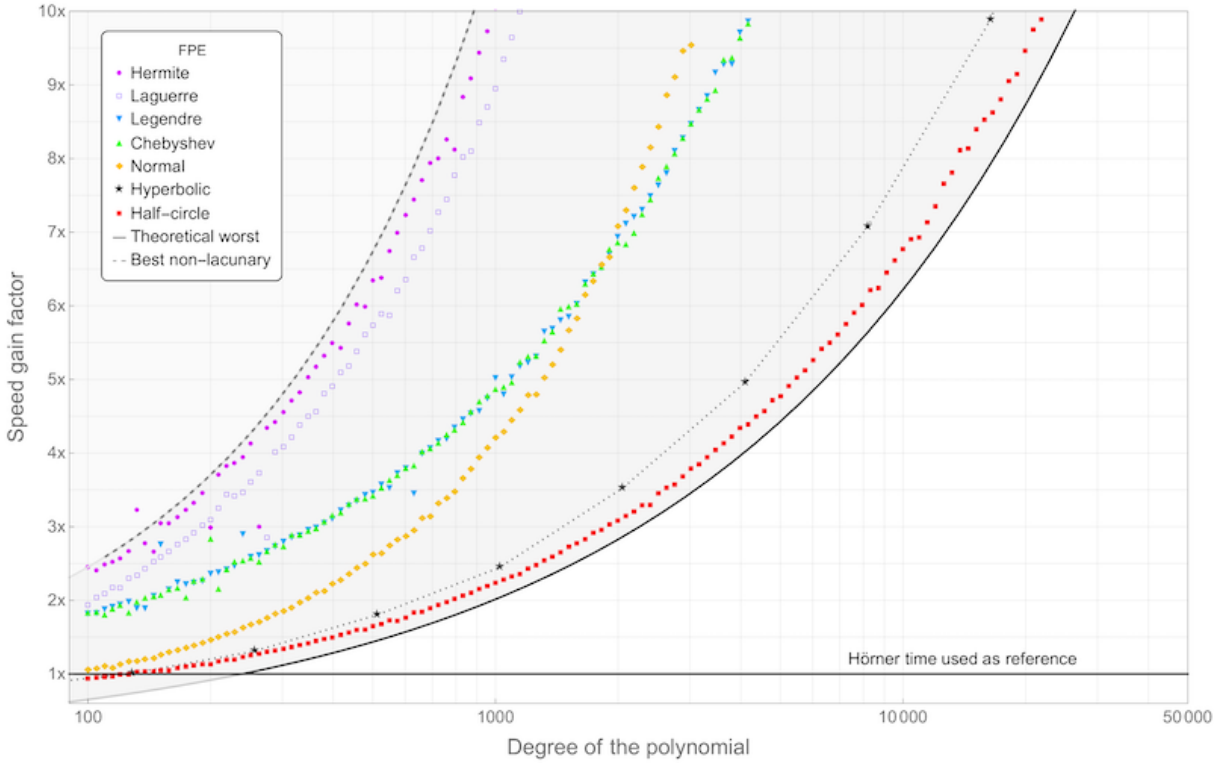

Figure 1.1 Speed gain of `FastPolyEval` versus Hörner for O(d) evaluations in precision p=53 MPFR.

1.2 Complexity & accuracy

`FastPolyEval` splits the evaluation process in two phases:

- A first phase, called **pre-processing**, analyses the coefficients of the polynomial (actually only the exponents) and determines an evaluator, based on a parcimonious representation of the polynomial.
- Subsequently, the **evaluator** is applied to each of the requested evaluation points. A second reduction is performed. Then the final result is computed.

The complexity of the pre-processing phase is bounded by $O(d \log d)$ where d is the degree of the polynomial $P(z)$. It is independent of the precision used to express the coefficients or requested for the rest of the computations. The `FastPolyEval` library is backed by theoretical results that guaranty that the average arithmetic complexity of the final evaluator is of order

$$O\left(\sqrt{d(p+\log d)}\right)$$

where p is the precision of the computation, in bits. The averaging process corresponds to evaluation points z uniformly distributed either on the Riemann sphere or on the unit disk of the complex plane. The worst complexity of the evaluator does not exceed that of Hörner, i.e. $O(d)$, and can drop as low as $O(\log^2 d)$ in some favorable cases (see Figure 1 in Abstract).

The memory requirement of `FastPolyEval` is minimal. To handle a polynomial of degre d with p bits of precision, the memory requirement is $O(dp)$. An additional memory $O(kp)$ is required to perform k evaluations in one call.

Regarding accuracy, the theory guaranties that the relative error between the exact value of $P(z)$ and the computed value does not exced 2^{-p-c-1} where c is the number of cancelled leading bits, i.e.

$$c = \begin{cases} 0 & \text{if } |P(z)| \geq M(z), \\ \lfloor \log_2 |M(z)| \rfloor - \lfloor \log_2 |P(z)| \rfloor & \text{else,} \end{cases}$$

where $M(z) = \max |a_j z^j|$ is the maximum modulus of the monomials of $P(z)$ and $\lfloor \cdot \rfloor$ is the floor function.

Note

The geometric preprocessing uses only the exponents of the coefficients, which is a significantly smaller amount of data to process than reading all the bits of the coefficients. For a high-precision high-degree evaluation at a **single** point, `FastPolyEval` can often outperform Hörner. The preprocessing of the exponents followed by the evaluation with a high precision of a parcimonious representation of the polynomial is more efficient than handling indiscriminately all the coefficients. This fact does not contradict that Hörner is a theoretical best for one single evaluation. Hörner has the best estimate on complexity that holds for **any** evaluation point. The advantage of `FastPolyEval` can be substantial, but it holds **on average**. Note that the worst case for the evaluator (no coefficient dropped) has the same complexity as Hörner. However, in that case, one can prove that the average complexity is much better, typicaly $O(\log^2 d)$.

For further details, precise statements and proofs, please see `reference [1]` in section References, Contacts and Copyright.

1.3 Description of the Fast Polynomial Evaluator (FPE) algorithm

In this section, we describe briefly the mathematical principles at the foundation of `FastPolyEval`.

1.3.1 General principles

`FastPolyEval` relies on two general principles.

1. **Lazy evaluation** in finite precision. When adding two floating points numbers with p bits, one can simply discard the smaller one if the orders of magnitude are so far apart that the leading bit of the smaller number cannot affect the bit in the last position of the larger number. When evaluating a polynomial of large degree, the orders of magnitude of the monomials tends to be extremely varied, which is a strong incentive to use lazy evaluations.
2. **Geometric selection principle**. For a given evaluation point, evaluating each monomial and sorting them in decreasing order of magnitude would be a very inefficient way of implementing lazy additions. Instead, `FastPolyEval` can identify the leading monomials using a simple geometric method that allows us to factor most of the work in a pre-processing phase, which is only needed once. At each evaluation point, a subsequent reduction produces a very parcimonious representation of the polynomial (see Figure 2).

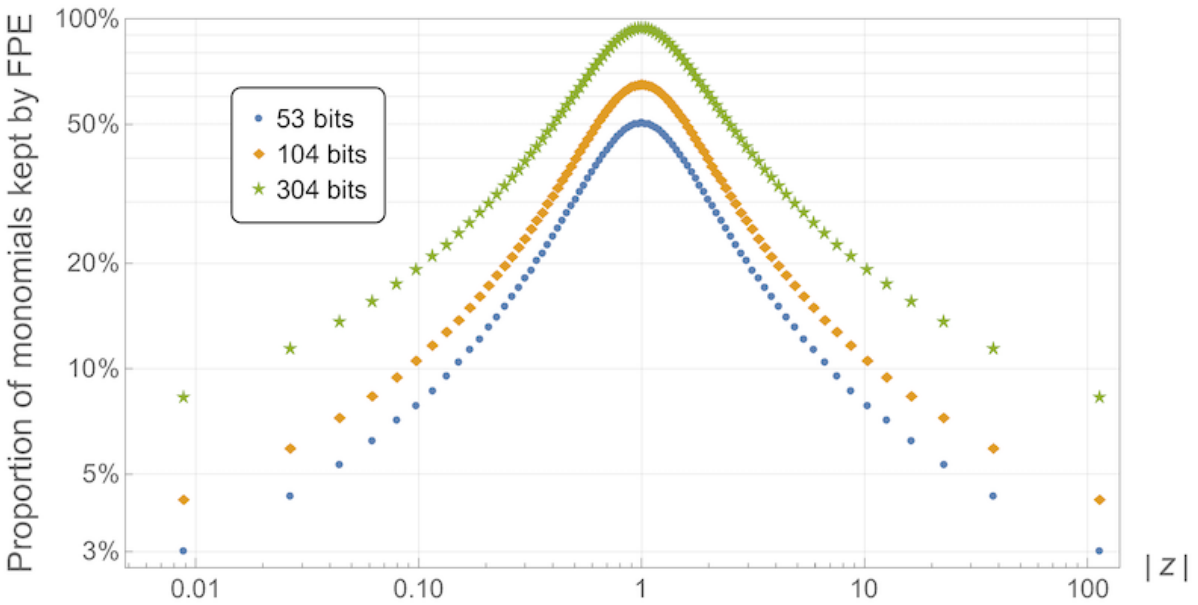

Figure 1.2 Parsimony of the representation used by `FastPolyEval` to evaluate a polynomial of degree 1000 (half-circle family).

1.3.2 Geometric selection principle

For a given polynomial P of degree d, one represents the modulus of the coefficients a_j in logarithmic coordinates, that is the scatter plot E_P of $\log_2 |a_j|$ in function of $j \in \{0, 1, \ldots, d\}$. One then computes the concave envelope $\hat{E}_P$ of E_P (obviously piecewise linear) and one identifies the strip $S_\delta(\hat{E}_P)$ situated below $\hat{E}_P$ and of vertical thickness

$$\delta = p + \lfloor \log_2 d \rfloor + 4.$$

Note that the thickness of this strip is mostly driven by the precision p (in bits) that will be used to evaluate P. On Figure 3, the blue points represent E_P, the cyan line is $\hat{E}_P$ and the strip S_δ is colored in light pink.

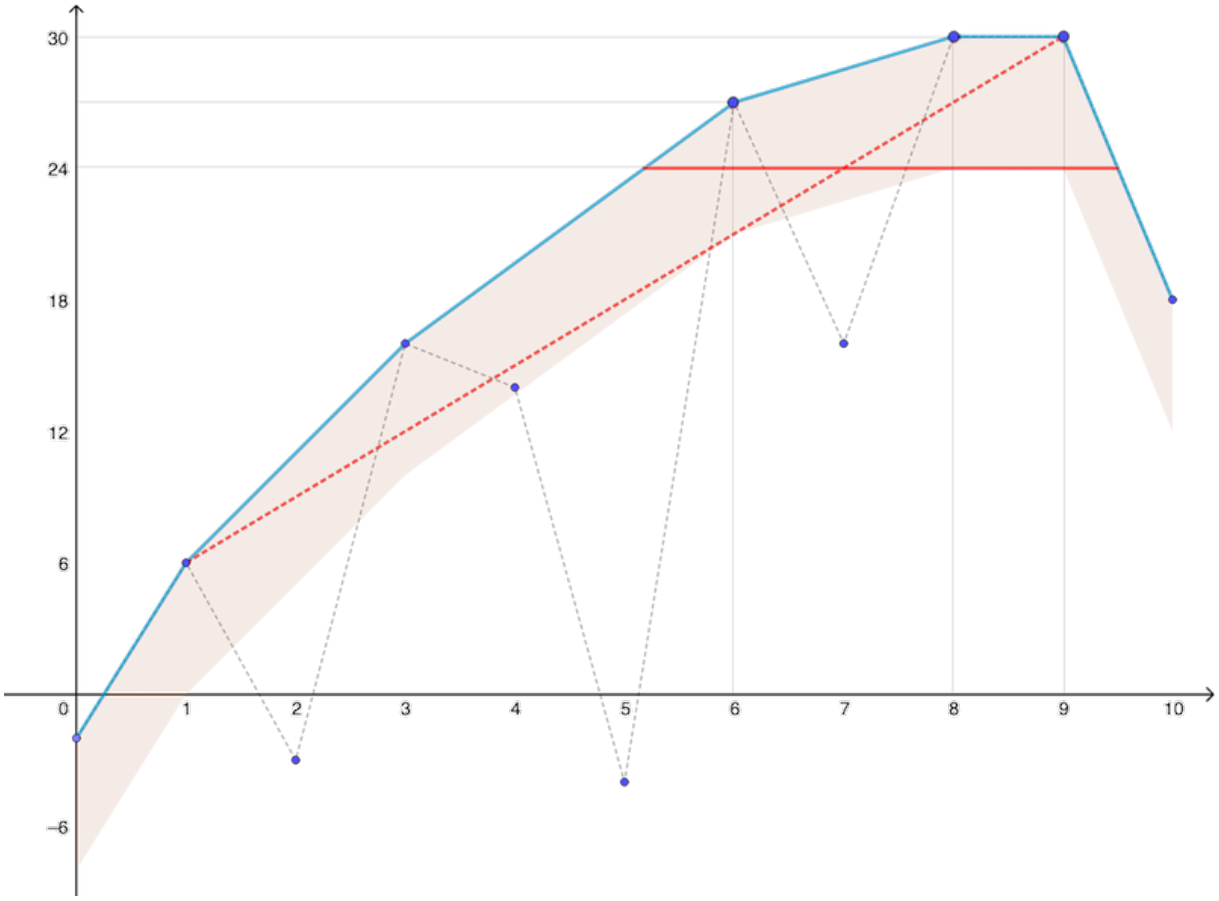

Figure 1.3 Concave cover of the oefficients of a polynomial (log-scale) and selection principle for a given precision.

The coefficients of P that lie in the strip S_δ are pertinent for an evaluation with precision p. The others can safely be discarded because they will never be used at this precision.

1.3.3 Parcimonious representation at an arbitrary point

For a given $z \in \mathbb{C}$, a parcimonious representation of $P(z) = \sum_{j=0}^{d} a_j z^j$ is obtained by selecting a proper subset of the indices $J_p(z) \subset \{0, 1, \ldots, d\}$ and discarding the other monomials:

$$Q_p(z) = \sum_{j \in J_p(z)} a_j z^j.$$

For computations with a precision of p bits, the values of $Q_p(z)$ and $P(z)$ are equivalent because the relative error does not exceed 2^{-p-c-1} where c is the number of cancelled leading bits (defined in Section Complexity & accuracy).

The subset $J_p(z)$ is obtained as a subset of the (indices of the) coefficients that respect the two following criteria in the logarithmic representation (see Figure 3):

1. the coefficient belongs to the strip S_δ,
2. the coefficient is above the longest segment of slope $\tan\theta = -\log_2|z|$ contained in S_δ.

The selecting segment is always tangent to the lower edge of S_δ or, in case of ambiguity (e.g. if S_δ is a parallelogram), it is required to be. For $|z| = 1$, the selecting segment is an horizontal line illustrated in solid red in Figure 3 above. The red dashed line corresponds to some value $|z| < 1$. Figure 4 illustrates how the selection principle at an arbitrary point $z \in \mathbb{C}$ can be transposed from the analysis performed on the raw coefficients, i.e. for $|z| = 1$. In log-coordinates, one has indeed: $\log_2\left(|a_j z^j|\right) = \log_2|a_j| - j\tan\theta$. Selecting the coefficients such that $\log_2\left(|a_j z^j|\right)$ differs from its maximum value by less than δ (solid red in Figure 4) is equivalent to selecting those above the segment of slope $\tan\theta$ in the original configuration (dashed line in Figure 3).

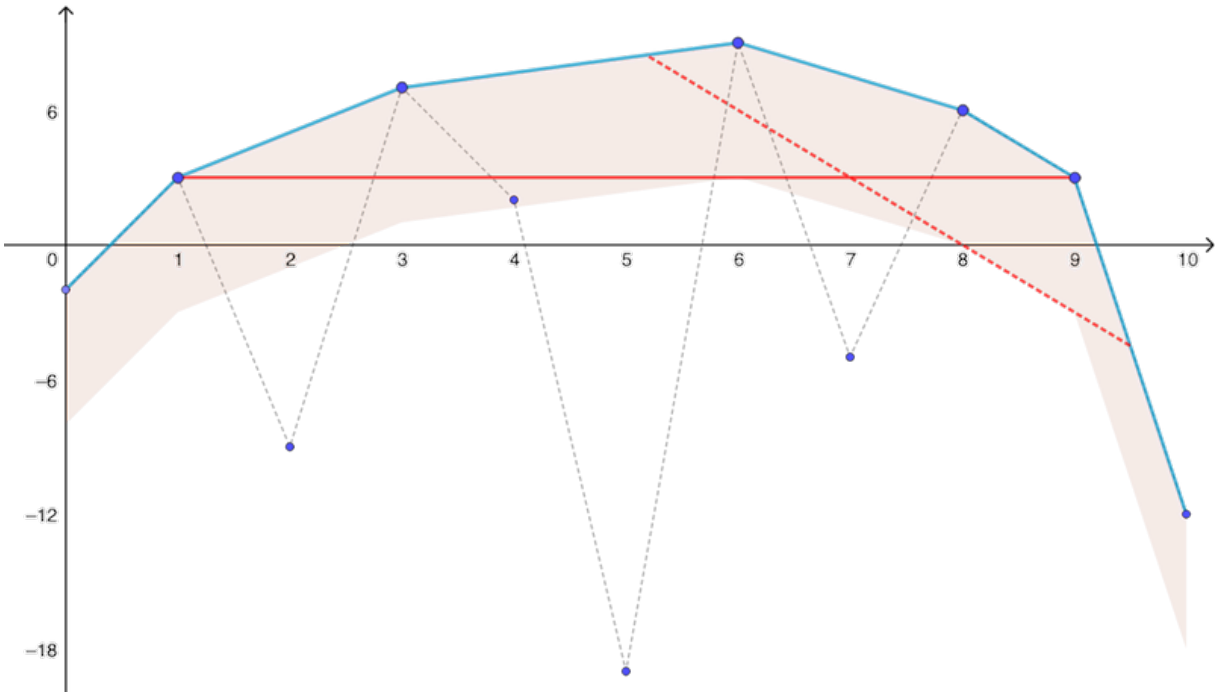

Figure 1.4 Transposition of the selection principle at an arbitrary evaluation point

1.3.4 Implementation of the algorithm

`FastPolyEval` computes Figure 3 and the strip S_δ in the pre-processing phase and keeps only the subset of the coefficients that belong to that strip (the so-called "good" set G_p in `reference [1]`). In the evaluation phase, the subset of coefficients is thinned to $J_p(z)$ for each evaluation point z using the 2nd criterion, thus providing the parcimonious representation $Q_p(z)$ of $P(z)$ at that point. The value of the polynomial is then computed using Hörner's method for Q_p. Theoretical results guaranty that, on average, the number of coefficients kept in $J_p(z)$ is only of order $\sqrt{d\delta}$, which explains why the complexity of `FastPolyEval` is so advantageous.

For further details, see `reference [1]` in Section References, Contacts and Copyright.

1.4 Installation of FastPolyEval

FastPolyEval is distributed as source code, written in the C language. The source code can be downloaded from our public github repository.

1.4.1 Prerequisites

First of all, don't panic, it's easy...

Obvioulsy, you will need a computer and a C compiler, for example GCC, though any other C compiler will be fine.

FastPolyEval relies on MPFR to handle floating point numbers with arbitrary precision. You need to install this library on your system if it is not already installed. Please follow the MPFR installation instructions to do so. Note that MPFR has one main depency, GMP, which will also need to be installed (see the GMP installation instructions). If you do not have admin privileges on your machine, you can still build those libraries in a local directory and instruct your compiler to look for the appropriate library path. For example, if you use GCC, see the documentation of option -L.

Note that on most OS, one can also install those libraries through a package manager (see Additional help for Linux, MacOS, Windows

Note

The libraries GMP and MPFR are **free** to download and use and are distributed under the Lesser General Public License, which enables developers of non-free programs to use GMP/MPFR in their programs. FastPolyEval is released under the BSD licence, with an attribution clause (see References, Contacts and Copyright), which means that you are **free to download, use, modify, distribute or sell, provided you give us proper credit**.

1.4.2 Compile FastPolyEval

Download the source code. In the command line, go to the code subfolder then type:

```
make
```

to get a basic help message. The default build command is:

```
make fpe
```

This will create and populate a bin subdirectory of the downloaded folder with an app, called FastPolyEval. You may move the executable file to a convenient location. Alternatively, consider adding this folder to your PATH. The Makefile does not attempt this step for you. See Basic usage of FastPolyEval for additional help on how to use this app.

If you prefer to compile by hand, the structure of your command line should be:

```
gcc all_source_files.c -o bin/FastPolyEval -I each_source_sub_folder_containing_header_files -Wall -lm -lgmp
      -lmpfr -O3
```

Note that the file.c and -I folder parameters must be repeated as necessary. The Makefile is simple enough and understanding it can provide additional guidance.

FastPolyEval switches automatically from hardware machine precision to emulated high-precision using MPFR (see Number formats). The format used for hardware numbers is chosen at the time of the compilation. You may edit the source file code/numbers/ntypes.h before the default build. Alternatively, you can execute

```
make hardware
```

This should generate an automatically edited copy of this header file in a temporary folder and launch successive compilations. This build will populate the bin subdirectory with three apps, called FastPolyEval_FP32, FastPolyEval_FP64 and FastPolyEval_FP80 corresponding to each possible choice.

1.4.3 Additional help for Linux, MacOS, Windows

Github offers access to virtual machines that run on their servers. The corresponding tasks are called `workflows`. Each workflow serves as a guidline (read the subsection `job:steps` in the `yml` files) to perform similar actions on your computer. The directory `.github/workflows` on our `GitHub repository` contains a `build` workflow for each major OS : Linux, MacOS and Windows.

1.4.4 Uninstall FastPolyEval

As the `Makefile` does not move the binaries and does not alter your `PATH`, cleanup is minimal. To remove the binary files generated in the build process, execute
```
make clean
```

To uninstall `FastPolyEval` from your system, simply delete the executable file and remove the downloaded sources.

1.5 Basic usage of FastPolyEval

`FastPolyEval` is used at the command line, either directly or through a shell script. A typical command line call has the following structure:
```
FastPolyEval -task prec parameter [optional_parameter]
```

where `prec` is the requested precision for the computations.

1.5.1 Onboard help system

To call the onboard help with a list and brief description of all possible tasks, type
```
FastPolyEval -help
```

A detailed help exists for each task. For example, try `FastPolyEval -eval -help`.

The different tasks belong to 3 groups:

- Tasks for generating and handling polynomials,
- Tasks for generating and handling sets of complex numbers,
- Tasks using the FPE algorithm for production use and benchmarking

and will be detailed below.

Note

In absence of argument, the default behavior is a call for help. The previous messaged can also be displayed respectively with `FastPolyEval` and `FastPolyEval -eval` .

1.5.2 Number formats

The flags `MACHINE_LOW_PREC` and `MACHINE_EXTRA_PREC` in ntypes.h define what kind of machine numbers `FastPolyEval` defaults to for low-precision computations, and the corresponding precision threshold that defines how low is "low". Note that the main limitation of machine numbers is the limited range of exponents. The numerical limits can easily be reached when evaluating a polynomial of high degree. On the contrary, MPFR number are virtually unlimited, with a default ceiling set to $\simeq 2^{\pm 4\times 10^{18}}$.

Table 1.1 Number formats

numbers/ntypes.h	Precision requested	Format	Numerical limit
MACHINE_LOW_PREC	up to 24	FP32, `float`	about 10^{-38} to 10^{+38}
	25 and up	MPFR	practically unlimited
no flag	up to 53	FP64, `double`	about 10^{-308} to 10^{+308}
	54 and up	MPFR	practically unlimited
MACHINE_EXTRA_PREC	up to 64	FP80, `long double`	about 10^{-4930} to 10^{+4930}
	65 and up	MPFR	practically unlimited

Warning

If a number either read as input from a file or computed and destined to the output cannot be represented with the selected precision (`inf` or `NaN` exception), a warning is issued and the operation fails. Usually, the solution consists in using a higher precision (i.e. MPFR numbers). Anoter possible issue (if you are running Newton steps) is that you have entered the immediate neigborhood of a critical point, which induces a division by zero or almost zero. Try neutralizing the offending point.

Other numerical settings can be adjusted in ntypes.h, in particular :

- `HUGE_DEGREES` sets the highest polynomial degree that can be handled (default $2^{64}-2$),
- `HUGE_MP_EXP` sets the highest exponent that MPFR numbers can handle (default $\pm 4 \times 10^{18}$).

1.5.3 Input and outputs

`FastPolyEval` reads its input data from files and produces its output as file. The file format is `CSV`. To be valid, the rest of the `CSV` must contains a listing of complex numbers, written

```
a, b
```

where `a` is the real part and `b` is the imaginary part, in decimal form.

Depending on the context, the file will be interpreted as a set of evaluation points, a set of values, or the coefficients of a polynomial. For example, here is a valid file:

```
// An approximation of pi
3.14, 0
// A complex number close to the real axis
1.89755593218329076e+99, 2.35849881747969046e-427
```

Polynomials are written with the lowest degree first, so $P(z) = 1 - 2iz$ is represented by the file

```
1, 0
0, -2
```

Comments line are allowed: they start either with `#`, `//` or ;. Comment lines will be ignored. Be mindful of the fact that comments can induce an **offset** between the line count of the file and the internal line count of `FastPoly↩Eval`. Blank lines are not allowed. Lines are limited to 10 000 symbols (see array_read), which puts a practical limit to the precision at around 15 000 bits. You can easily edit the code to push this limitation if you have the need for it.

Warning

As a general rule for the tasks of `FastPolyEval`, if an output file name matches the one of an input file, the operation is **safe**. However, the desired output will overwrite the previous version of the file.

Note

For users that want a turnkey solution to high-performance polynomial evaluations where the outputs of some computations are fed back as input to others, we recommend the use of `FastPolyEval` with data residing in a virtual RAM disk, on local solid-state drives or on similar low latency/high bandwidth storage solutions. If you have doubts on how to do this, please contact your system administrator.

1.5.4 Tasks for generating and handling polynomials

`FastPolyEval` contains a comprehensive set of tools to generate new polynomials, either from scratch or by performing simple operations on other ones.

- Classical polynomials are generated with the tasks `-Chebyshev`, `-Legendre`, `-Hermite`, `-Laguerre`. The family `-hyperbolic` is defined recursively by

$$p_1(z) = z, \qquad p_{n+1}(z) = p_n(z)^2 + z$$

  and plays a central role in the study of the Mandelbrot set (see e.g. reference [2] in References, Contacts and Copyright).
- One can build a polynomial from a predetermined set of roots (listed with multiplicity) by invoquing the task `-roots`.
- One can compute the sum (`-sum`), difference (`-diff`), product (`-prod`) or the derivative (`-der`) of polynomials.

1.5.5 Tasks for generating and handling sets of complex numbers

`FastPolyEval` contains a comprehensive set of tools to generate new sets of real and complex numbers, either from scratch or by performing simple operations on other ones.

- The real (`-re`) and imaginary (`-im`) parts of a list of complex numbers can be extracted. The results are real and therefore of the form `x`, `0` . The complex conjugate (sign change of the imaginary part) is computed with `-conj` and the complex exponential with `-exp`.
- `FastPolyEval` can perform various interactions between valid `CSV` files.
  1. The concatenation (`-cat`) of two files writes a copy of the second one after a copy of the first one. For example, to rewrite a high-precision output `file_high_prec.csv` with a lower precision `prec`, use
     ```
     FastPolyEval prec file_high_prec.csv /dev/null file_low_prec.csv
     ```
  2. The `-join` task takes the real parts of two sequences and builds a complex number out of it. The imaginary parts are lost.
     ```
     a, *    (entry k from file_1)
     b, *    (entry k from file_2)
     ----
     a, b    (output k)
     ```
     If the files have unequal lengh, the operation succeeds but stops once the shortest file runs out of entries. Be mindfull of offsets induced by commented lines (see Input and outputs).
  3. The `-tensor` task computes a tensor product (i.e. complex multiplication line by line).
     ```
     a, b    (entry k from file_1)
     c, d    (entry k from file_2)
     ----
     ac-bd, ad+bc  (output k)
     ```
     If the files have unequal lengh, the operation succeeds but stops once the shortest file runs out of entries. Be mindfull of offsets induced by commented lines (see Input and outputs).
  4. The `-grid` task computes the grid product of the real part of the entries. The output file contains nb_lines_file_1 $\times$ nb_lines_file_2 lines and lists all the products possibles between the real part of entries in the first file with the real part of entries in the second file. The imaginary parts are ignored.
- Rotations (`-rot`) map the complex number $a + ib$ to $a \times e^{ib}$. For example, to generate complex values from a real profile `profile.csv` and a set of phases `phases.csv`, you can use
  ```
  FastPolyEval -join prec profile.csv phases.csv rot_tmp.csv
  FastPolyEval -rot prec rot_tmp.csv complex_output.csv
  rm -f rot_tmp.csv
  ```

- The `-unif` task writes real numbers in an arithmetic progression whose characteristics are specified by the parameters.
- The `-sphere` task writes polar coordinates approximating an uniform distribution on the Riemann sphere. The output value (a, b) represents Euler angles in the (vertical, horizontal) convention. It represents the point

$$(\cos a \cos b, \cos a \sin b, \sin a) \in \mathbb{S}^2 \subset \mathbb{R}^3.$$

The `-polar` task maps a pair of (vertical, horizontal) angles onto the complex plane by stereographical projection. To generate complex points that are uniformly distributed on the Riemann sphere, starting with `SEED` points at the equator, you can use the following code that combines those tasks. Note that there will be about $SEED^2/\pi$ points on the sphere and that the points are computed in a deterministic way (they will be identical from one call to the next). A SEED of 178 produces about 10 000 complex points.

```
SEED=178
FastPolyEval -sphere prec $SEED tmp_file.csv
FastPolyEval -polar prec tmp_file.csv sphere.csv
rm -f tmp_file.csv
```

- `FastPolyEval` also contains two random generators (actually based on MPFR). The `-rand` task produces real random numbers that are uniformly distributed in an interval. The `-normal` task produces real random numbers with a Gaussian distribution whose characteristics are specified by the parameters. Use the `-join` task to merge the outputs of two `-normal` tasks into a complex valued normal distribution.

1.5.6 Tasks using the FPE algorithm for production use and benchmarking

The main tasks of the `FastPolyEval` library are the following:

- `-eval` evaluates a polynomial on a set of points using the FPE algorithm.
- `-evalD` evaluates the derivative of a polynomial on a set of points using the FPE algorithm.

The precision of the computation and the name of the inputs (polynomial and points) & output (values) files are given as parameters. The first optional parameter specifies a second output file that contains a complementary report on the estimated quality of the evaluation at the precision chosen. For each evaluation point, this report contains an upper bound for the evaluation errors (in bits), a conservative estimate on the number of correct bits of the result, and the number of terms that where kept by the FPE algorithm.

For benchmark purposes (see reference [1] in Section References, Contacts and Copyright), we propose a set of optional parameters that specify how many times the preprocessing and the FPE algorithm should be run at each point (to improve the accuracy of the time measurement), whether the Hörner algorithm should also be run and, if so, how many times it should run.

The task `-evalN` evaluates one **Newton step** of a polynomial on a set of points, i.e.

$$\mathrm{NS}(P, z) = \frac{P(z)}{P'(z)}.$$

Recall that Newton's method for finding roots of P consists in computing the sequence defined recursively by

$$z_{n+1} = z_n - \mathrm{NS}(P, z_n).$$

The `-iterN` task iterates the Newton method a certain amount of times and with a given precision. It thus realizes a partial search of the roots of the polynomial. For best results, we recommend successive calls where the precision is gradually increased and the maximum number of iterations is reduced. For guidance in the choice of the starting points, please refer to reference [3] in Section References, Contacts and Copyright.

-analyse computes the concave cover and the intervals of |z| for which the evaluation strategy changes

The `-analyse` task computes the concave cover $\hat{E}_P$, the strip S_δ (see Section Description of the Fast Polynomial Evaluator (FPE) a and the intervals of |z| for which the evaluation strategy of FPE (i.e. the reduced polynomial $Q_p(z)$) changes. It is intended mostly for an illustrative purpose on low degrees, when the internals of the FPE algorithm can still be checked by hand. However, the intervals where a parsimonious representation is valid may also be of practical use (see reference [1] in Section References, Contacts and Copyright).

1.6 Notes about the implementation

For further details, please read the documentation associated to each **source file**.

Do not hesitate to contact us (see References, Contacts and Copyright) to signal bugs and to request new features. We are happy to help the development of the community of the users of FastPolyEval.

1.7 References, Contacts and Copyright

Please cite the reference [1] below if you use or distribute this software. The other citations are in order of appearance in the text:

- **[1] R. Anton, N. Mihalache & F. Vigneron. Fast evaluation of real and complex polynomials. 2022. [hal-03820369].**
- [2] N. Mihalache & F. Vigneron. How to split a tera-polynomial. In preparation.
- [3] J.H. Hubbard, D. Schleicher, S. Sutherland. How to find all roots of complex polynomials by Newton's method. Invent. math., 146:1-33, 2001. [Llink] on author's page.

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1.8 Thanks

It is our pleasure to thank our families who supported us in the long and, at times stressful, process that gave birth to the FastPolyEval library, in particular Ramona who co-authored reference [1], Sarah for a thorough proof-reading of [1] and Anna who suggested the lightning pattern for our logo.

We also thank Romeo, the HPC center of the University of Reims Champagne-Ardenne, on which we where able to benchmark our code graciously.

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Chapter 2

Data Structure Index

2.1 Data Structures

Here are the data structures with brief descriptions:

Chapter 3

File Index

3.1 File List

Here is a list of all documented files with brief descriptions:

Chapter 4

Data Structure Documentation

4.1 array_struct Struct Reference

A variable length array of machine floating point complex numbers.

Data Fields

- ulong len
  the number of complex numbers in the array
- ulong size
  the present capacity of the array (memory size in number of complex numbers)
- comp_ptr zi
  the elements of the array

4.1.1 Detailed Description

A variable length array of machine floating point complex numbers.

Definition at line 37 of file array.h.

4.2 arrayf_struct Struct Reference

A variable length list of machine floating point complex numbers.

Data Fields

- ulong len
  the number of complex numbers in the list
- ulong size
  the present capacity of the list (memory size in number of complex numbers)
- compf_ptr zi
  the elements of the list

4.2.1 Detailed Description

A variable length list of machine floating point complex numbers.

Definition at line 38 of file arrayf.h.

4.3 comp_struct Struct Reference

Multi-precision floating point complex numbers.

Data Fields

- mpfr_t x
  the real part of the complex number
- mpfr_t y
  the imaginary part of the complex number

4.3.1 Detailed Description

Multi-precision floating point complex numbers.

Definition at line 31 of file comp.h.

4.4 compf_struct Struct Reference

Machine complex numbers.

Data Fields

- coeff_t x
  the real part of the complex number
- coeff_t y
  the imaginary part of the complex number

4.4.1 Detailed Description

Machine complex numbers.

Definition at line 29 of file compf.h.

4.5 concave_struct Struct Reference

Description of a concave function computed from the coefficients of some polynomial.

Data Fields

- prec_t extraBits
  extra bits for guarding, depending on the degree of the polynomial
- prec_t prec
  the precision that will be used to evaluate the polynomial, excluding `extraBits`
- list_t def
  the definition of the concave map
- list_t all
  all terms of the polynomial that may be used for evaluation
- deg_t start
  the position in `allPow` *of the largest power to evaluate (for given slope)*
- deg_t mid
  the position in `allPow` *of the power which gives the maximum modulus*
- deg_t end
  the position in `allPow` *of the least power to evaluate (for given slope)*

4.5.1 Detailed Description

Description of a concave function computed from the coefficients of some polynomial.

Definition at line 35 of file concave.h.

4.6 eval_struct Struct Reference

Evaluator of polynomials with multi-precision floating point coefficients.

Data Fields

- poly P
  the polynomial, with complex coefficients
- polyr Q
  the polynomial, with real coefficients
- bool real
  the type of polynomial to evaluate
- prec_t prec
  the precision of evaluations, in bits
- concave f
  concave cover of the scales of coefficients
- pows zn
  powers of a complex argument
- powsr xn
  powers of a real argument
- real_t valErr
  the [approximative] upper bound for the absolute error of the last evaluation, in bits
- real_t derErr
  the [approximative] upper bound for the absolute error of the last derivative evaluation, in bits
- real_t ntErr

the [approximative] upper bound for the absolute error of the last Newton term evaluation, in bits

- deg_t terms

  the number of polynomial terms computed by the last operation
- comp buf

  a buffer for internal computations
- mpfr_t br

  a real buffer for internal computations

4.6.1 Detailed Description

Evaluator of polynomials with multi-precision floating point coefficients.

Definition at line 41 of file eval.h.

4.7 evalf_struct Struct Reference

Evaluator of polynomials with machine floating point coefficients.

Data Fields

- polyf P

  the polynomial, with complex coefficients
- polyfr Q

  the polynomial, with real coefficients
- bool real

  the type of polynomial to evaluate
- concave f

  concave cover of the magnitude of coefficients
- powsf zn

  powers of a complex argument
- powsfr xn

  powers of a real argument
- real_t valErr

  the [approximative] upper bound for the absolute error of the last evaluation, in bits
- real_t derErr

  the [approximative] upper bound for the absolute error of the last derivative evaluation, in bits
- real_t ntErr

  the [approximative] upper bound for the absolute error of the last Newton term evaluation, in bits
- deg_t terms

  the number of polynomial terms computed by the last operation

4.7.1 Detailed Description

Evaluator of polynomials with machine floating point coefficients.

Definition at line 35 of file evalf.h.

4.8 help_struct Struct Reference

Description of a basic help screen.

Data Fields

- char * before
  the first line to display
- int columnCount
  the number of columns
- int * columnWidths
  the widths of all but the last column (array length should be 1 less than columnCount)
- char ** headers
  the column headers
- int linesCount
  the number of lines / commands
- char *** lines
  the double array of messages
- char * after
  the last line to display

4.8.1 Detailed Description

Description of a basic help screen.

Each help screen contains a brief summary (`before`), some `lines` of messages (commands) and a final discussion (`after`). Lines are structures as an array of variable size, with descriptive headers.

Definition at line 73 of file help.h.

4.9 list_struct Struct Reference

A list of real numbers that can be sorted, while keeping track of original order.

Data Fields

- deg_t size
  the memory size allocated
- deg_t count
  the number of elements
- deg_t * k
  indexes, powers, the permutation of the numbers when sorted
- real_t * s
  the list of numbers
- bool sorted
  the state of the list

4.9.1 Detailed Description

A list of real numbers that can be sorted, while keeping track of original order.

Definition at line 35 of file list.h.

4.10 poly_struct Struct Reference

Polynomial with multi-precision floating point complex coefficients.

Data Fields

- deg_t degree
  the degree of the polynomial
- prec_t prec
  the precision of the coefficients, in bits
- comp_ptr a
  the coefficients
- bool modified
  the status of the coefficients
- mpfr_t buf1
  a buffer
- mpfr_t buf2
  another buffer

4.10.1 Detailed Description

Polynomial with multi-precision floating point complex coefficients.

Definition at line 31 of file poly.h.

4.11 polyf_struct Struct Reference

Polynomial with machine floating point complex coefficients.

Data Fields

- deg_t degree
  the degree of the polynomial
- compf_ptr a
  the coefficients
- bool modified
  the status of the coefficients

4.11.1 Detailed Description

Polynomial with machine floating point complex coefficients.

Definition at line 30 of file polyf.h.

4.12 polyfr_struct Struct Reference

Polynomial with machine floating point real coefficients.

Data Fields

- deg_t degree
  the degree of the polynomial
- coeff_t * a
  the coefficients
- bool modified
  the status of the coefficients

4.12.1 Detailed Description

Polynomial with machine floating point real coefficients.

Definition at line 31 of file polyfr.h.

4.13 polyr_struct Struct Reference

Polynomial with multi-precision floating point complex coefficients.

Data Fields

- deg_t degree
  the degree of the polynomial
- prec_t prec
  the precision of the coefficients, in bits
- mpfr_ptr a
  the coefficients
- bool modified
  the status of the coefficients
- mpfr_t buf1
  a buffer
- mpfr_t buf2
  another buffer

4.13.1 Detailed Description

Polynomial with multi-precision floating point complex coefficients.

Definition at line 31 of file polyr.h.

4.14 pows_struct Struct Reference

The powers of the complex number `z` using multi-precision floating point numbers.

Data Fields

- prec_t prec
  the precision of the powers of `z`, in bits
- deg_t size
  the memory size allocated
- byte tps
  the largest non-negative integer such that `2^tps<=size`
- bool * computed
  the status of powers
- comp_ptr zn
  the powers of `z`
- mpfr_t buf1
  a buffer
- mpfr_t buf2
  another buffer
- comp pth
  a buffer
- comp res
  another buffer

4.14.1 Detailed Description

The powers of the complex number `z` using multi-precision floating point numbers.

Definition at line 30 of file pows.h.

4.15 powsf_struct Struct Reference

The powers of the complex number `z` using machine floating point numbers.

Data Fields

- deg_t size
  the memory size allocated
- byte tps
  the largest non-negative integer such that `2^tps<=size`
- bool * computed
  the status of powers
- compf_ptr zn
  the powers of `z`
- compf res
  a buffer for results

4.15.1 Detailed Description

The powers of the complex number `z` using machine floating point numbers.

Definition at line 30 of file powsf.h.

4.16 powsfr_struct Struct Reference

The powers of the real number `x` using machine floating point numbers.

Data Fields

- bool inited
  the status of the value `x`
- coeff_t x
  the real number

4.16.1 Detailed Description

The powers of the real number `x` using machine floating point numbers.

Definition at line 35 of file powsfr.h.

4.17 powsr_struct Struct Reference

The powers of the real number `x` using multi-precision floating point numbers.

Data Fields

- prec_t prec

  the precision of the powers of x, in bits
- bool inited

  the status of the value x
- mpfr_t x

  the real number
- mpfr_t res

  a buffer

4.17.1 Detailed Description

The powers of the real number x using multi-precision floating point numbers.

Definition at line 37 of file powsr.h.

Chapter 5

File Documentation

5.1 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/apps.h File Reference

The implementation of the mini-apps with MPFR numbers.

Functions

- array app_join (long prec, array z1, array z2)

  Joins the real parts of the sequences `z1` and `z2` as the real parts and imaginary parts of a new list.
- array app_grid (long prec, array z1, array z2)

  Computes the set product of the real parts of two sequences `z1` and `z2`.
- array app_exp (long prec, array z)

  Computes the complex exponential of a sequence `z`.
- array app_rot (long prec, array z)

  Computes `a*exp(ib)` for each term `a+ib` of a sequence `z` of complex numbers.
- array app_polar (long prec, array z)

  Computes the complex numbers given by a sequence `z` of their polar coordinates on the sphere.
- array app_unif (long prec, ulong n, mpfr_t st, mpfr_t en)

  Returns the list of `n` real numbers that split the interval [st,en] in `n-1` equal intervals.
- array app_rand (long prec, ulong n, mpfr_t st, mpfr_t en)

  Returns the list of `n` random real numbers in the interval [st,en], uniformly distributed.
- array app_normal (long prec, ulong n, mpfr_t cent, mpfr_t var)

  Returns the list of `n` random real numbers, normally distributed with center `cent` and variance `var`.
- array app_sphere (long prec, ulong n)

  Returns a list of `n` compelx numbers, uniformly distributed on the Riemann sphere.
- bool app_compare (long prec, array z1, array z2, char *output)

  Compares two list of complex values and reports the eventual errors.
- array app_re (long prec, array z)

  Returns the real parts of the numbers in the sequence `z`.
- array app_im (long prec, array z)

  Returns the imaginary parts of the numbers in the sequence `z`.
- array app_conj (long prec, array z)

  Returns the conjugates of the numbers in the sequence `z`.

- array app_tensor (long prec, array z1, array z2)

  Computes tensor (or piontwise) product of the sequences `z1` and `z2`.
- bool app_eval_p (long prec, poly P, array z, char ∗outFile, char ∗outError, long count, char ∗outHorner, long countHorner, const char ∗∗inFiles)

  *Evaluates the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool app_eval_d (long prec, poly P, array z, char ∗outFile, char ∗outError, long count, char ∗outHorner, long countHorner, const char ∗∗inFiles)

  *Evaluates the derivative of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool app_eval_n (long prec, poly P, array z, char ∗outFile, char ∗outError, long count, char ∗outHorner, long countHorner, const char ∗∗inFiles)

  *Evaluates the Newton terms of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool app_eval_r (long prec, poly P, array z, ulong maxIter, char ∗outFile, char ∗outError, long count, char ∗outHorner, long countHorner, const char ∗∗inFiles)

  *Evaluates the Newton iterates of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool app_analyse (long prec, poly P, char ∗outFile, char ∗outChange)

  Analyses the polynomail `P` and outputs its concave cover, ignored coefficients and (optionally) the modules of complex numbers for which the reduced polynomial changes.

5.1.1 Detailed Description

The implementation of the mini-apps with MPFR numbers.

5.1.2 Function Documentation

5.1.2.1 app_analyse()

```
bool app_analyse (
            long prec,
            poly P,
            char * outFile,
            char * outChange )
```

Analyses the polynomail `P` and outputs its concave cover, ignored coefficients and (optionally) the modules of complex numbers for which the reduced polynomial changes.

These analysis is performed for the evaluations of the `P` with `prec` bits of precision. The concave cover corresponds to the pre-processing phase of the **FPE** algortihm. The map `k->log_2|a_k|` is considered.

Parameters

prec	the precision of evaluations
P	the polynomial
outFile	the output file containing the concave cover and the ognored coefficients
outChange	the output file containing the intervals for `log_2|z|` and the corresponding reduced polynomials of `P`

Returns

true if the analysis is complete, false if some error occurred.

5.1.2.2 app_compare()

```
bool app_compare (
            long prec,
            array z1,
            array z2,
            char * output )
```

Compares two list of complex values and reports the eventual errors.

Parameters

prec	the precision of the result
z1	the fist list
z2	the second list
output	a file name for the output file, NULL if not used

Returns

true if the comparison is complete, false if some error occurred.

5.1.2.3 app_conj()

```
array app_conj (
            long prec,
            array z )
```

Returns the conjugates of the numbers in the sequence z.

Parameters

prec	the precision of the result
z	the list of points

Returns

the conjugates of z, NULL if some error occurred.

5.1.2.4 app_eval_d()

```
bool app_eval_d (
            long prec,
            poly P,
            array z,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the derivative of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

Parameters

prec	the precision of intermediary computations and of the result
P	the polynomial
z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.1.2.5 app_eval_n()

```
bool app_eval_n (
            long prec,
            poly P,
            array z,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the Newton terms of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

Parameters

prec	the precision of intermediary computations and of the result
P	the polynomial

Parameters

z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.1.2.6 app_eval_p()

```
bool app_eval_p (
            long prec,
            poly P,
            array z,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

Parameters

prec	the precision of intermediary computations and of the result
P	the polynomial
z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.1.2.7 app_eval_r()

```
bool app_eval_r (
            long prec,
            poly P,
            array z,
            ulong maxIter,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the Newton iterates of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

This is a method to approximate the roots of `P`, but there are no guarantees for the convergence. If the iterates escape far from the origin, the alogrith stops (for those starting points).

Parameters

prec	the precision of intermediary computations and of the result
P	the polynomial
z	the list of evaluation points
maxIter	the maximum iterates for each starting point
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.1.2.8 app_exp()

```
array app_exp (
            long prec,
            array z )
```

Computes the complex exponential of a sequence `z`.

Parameters

prec	the precision of the result
z	the list of points

Returns

the image by the complex exponential, `NULL` if some error occurred.

5.1.2.9 app_grid()

```
array app_grid (
            long prec,
            array z1,
            array z2 )
```

Computes the set product of the real parts of two sequences `z1` and `z2`.

Parameters

prec	the precision of the result
z1	the first list
z2	the second list

Returns

the set product, `NULL` if some error occurred.

5.1.2.10 app_im()

```
array app_im (
            long prec,
            array z )
```

Returns the imaginary parts of the numbers in the sequence `z`.

Parameters

prec	the precision of the result
z	the list of points

Returns

the imaginary parts in `z`, `NULL` if some error occurred.

5.1.2.11 app_join()

```
array app_join (
            long prec,
```

```
            array z1,
            array z2 )
```

Joins the real parts of the sequences `z1` and `z2` as the real parts and imaginary parts of a new list.

Parameters

prec	the precision of the result
z1	the first list
z2	the second list

Returns

the joint list, `NULL` if some error occurred.

5.1.2.12 app_normal()

```
array app_normal (
            long prec,
            ulong n,
            mpfr_t cent,
            mpfr_t var )
```

Returns the list of `n` random real numbers, normally distributed with center `cent` and variance `var`.

Parameters

prec	the precision of the result
n	the number of points, at least `2`
cent	the center of the normal distribution
var	the variance of the normal distribution

Returns

the list of random real numbers (in complex format), `NULL` if some error occurred.

5.1.2.13 app_polar()

```
array app_polar (
            long prec,
            array z )
```

Computes the complex numbers given by a sequence `z` of their polar coordinates on the sphere.

Parameters

prec	the precision of the result
z	the list of polar coordinates

Returns

the complex numbers given by their polar coordinates, `NULL` if some error occurred.

5.1.2.14 app_rand()

```
array app_rand (
            long prec,
            ulong n,
            mpfr_t st,
            mpfr_t en )
```

Returns the list of `n` random real numbers in the interval [st,en], uniformly distributed.

Parameters

prec	the precision of the result
n	the number of points, at least `2`
st	the start point
en	the end point

Returns

the list of random real numbers (in complex format), `NULL` if some error occurred.

5.1.2.15 app_re()

```
array app_re (
            long prec,
            array z )
```

Returns the real parts of the numbers in the sequence `z`.

Parameters

prec	the precision of the result
z	the list of points

Returns

the real parts in z, NULL if some error occurred.

5.1.2.16 app_rot()

```
array app_rot (
            long prec,
            array z )
```

Computes a*exp(ib) for each term a+ib of a sequence z of complex numbers.

Parameters

prec	the precision of the result
z	the list of points

Returns

the image by a+ib->a*exp(ib), NULL if some error occurred.

5.1.2.17 app_sphere()

```
array app_sphere (
            long prec,
            ulong n )
```

Returns a list of n compelx numbers, uniformly distributed on the Riemann sphere.

Parameters

prec	the precision of the result
n	the number of points, at least 2

Returns

the list of points uniformly distributed on the sphere, NULL if some error occurred.

5.1.2.18 app_tensor()

```
array app_tensor (
            long prec,
```

```
            array z1,
            array z2 )
```

Computes tensor (or piontwise) product of the sequences `z1` and `z2`.

Parameters

prec	the precision of the result
z1	the first list
z2	the second list

Returns

the tensor product, `NULL` if some error occurred.

5.1.2.19 app_unif()

```
array app_unif (
            long prec,
            ulong n,
            mpfr_t st,
            mpfr_t en )
```

Returns the list of `n` real numbers that split the interval [st,en] in `n-1` equal intervals.

Parameters

prec	the precision of the result
n	the number of points, at least `2`
st	the start point
en	the end point

Returns

the list of real numbers (in complex format), `NULL` if some error occurred.

5.2 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/appsf.h File Reference

The implementation of the mini-apps with machine numbers.

Functions

- arrayf appf_join (arrayf z1, arrayf z2)

  Joins the real parts of the sequences `z1` and `z2` as the real parts and imaginary parts of a new list.
- arrayf appf_grid (arrayf z1, arrayf z2)

  Computes the set product of the real parts of two sequences `z1` and `z2`.
- arrayf appf_exp (arrayf z)

  Computes the complex exponential of a sequence `z`.

- arrayf appf_rot (arrayf z)

  Computes `a*exp(ib)` for each term `a+ib` of a sequence `z` of complex numbers.
- arrayf appf_polar (arrayf z)

  Computes the complex numbers given by a sequence `z` of their polar coordinates on the sphere.
- arrayf appf_unif (ulong n, coeff_t st, coeff_t en)

  Returns the list of `n` real numbers that split the interval [st,en] in `n-1` equal intervals.
- bool appf_compare (arrayf z1, arrayf z2, char *output)

  Compares two list of complex values and reports the eventual errors.
- arrayf appf_re (arrayf z)

  Returns the real parts of the numbers in the sequence `z`.
- arrayf appf_im (arrayf z)

  Returns the imaginary parts of the numbers in the sequence `z`.
- arrayf appf_conj (arrayf z)

  Returns the conjugates of the numbers in the sequence `z`.
- arrayf appf_tensor (arrayf z1, arrayf z2)

  Computes tensor (or piontwise) product of the sequences `z1` and `z2`.
- bool appf_eval_p (polyf P, arrayf z, char *outFile, char *outError, long count, char *outHorner, long count↩ Horner, const char **inFiles)

  *Evaluates the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool appf_eval_d (polyf P, arrayf z, char *outFile, char *outError, long count, char *outHorner, long count↩ Horner, const char **inFiles)

  *Evaluates the derivative of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool appf_eval_n (polyf P, arrayf z, char *outFile, char *outError, long count, char *outHorner, long count↩ Horner, const char **inFiles)

  *Evaluates the Newton terms of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*
- bool appf_eval_r (polyf P, arrayf z, ulong maxIter, char *outFile, char *outError, long count, char *outHorner, long countHorner, const char **inFiles)

  *Evaluates the Newton iterates of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.*

5.2.1 Detailed Description

The implementation of the mini-apps with machine numbers.

5.2.2 Function Documentation

5.2.2.1 appf_compare()

```
bool appf_compare (
            arrayf z1,
            arrayf z2,
            char * output )
```

Compares two list of complex values and reports the eventual errors.

Parameters

z1	the fist list
z2	the second list
output	a file name for the output file, `NULL` if not used

Returns

true if the comparison is complete, false if some error occurred.

5.2.2.2 appf_conj()

```
arrayf appf_conj (
            arrayf z )
```

Returns the conjugates of the numbers in the sequence `z`.

Parameters

z	the list of points

Returns

the conjugates of `z`, `NULL` if some error occurred.

5.2.2.3 appf_eval_d()

```
bool appf_eval_d (
            polyf P,
            arrayf z,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the derivative of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

Parameters

P	the polynomial
z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.2.2.4 appf_eval_n()

```
bool appf_eval_n (
            polyf P,
            arrayf z,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the Newton terms of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

Parameters

P	the polynomial
z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.2.2.5 appf_eval_p()

```
bool appf_eval_p (
            polyf P,
            arrayf z,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

Parameters

P	the polynomial
z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.2.2.6 appf_eval_r()

```
bool appf_eval_r (
            polyf P,
            arrayf z,
            ulong maxIter,
            char * outFile,
            char * outError,
            long count,
            char * outHorner,
            long countHorner,
            const char ** inFiles )
```

Evaluates the Newton iterates of the polynomial `P` in all points in the list `z`, using the **FPE** algorithm.

This is a method to approximate the roots of `P`, but there are no guarantees for the convergence. If the iterates escape far from the origin, the alogrith stops (for those starting points).

Parameters

P	the polynomial
z	the list of evaluation points
maxIter	the maximum iterates for each starting point
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

Returns

true if the evaluaion is complete, false if some error occurred.

5.2.2.7 appf_exp()

```
arrayf appf_exp (
            arrayf z )
```

Computes the complex exponential of a sequence `z`.

Parameters

z	the list of points

Returns

the image by the complex exponential, `NULL` if some error occurred.

5.2.2.8 appf_grid()

```
arrayf appf_grid (
            arrayf z1,
            arrayf z2 )
```

Computes the set product of the real parts of two sequences `z1` and `z2`.

Parameters

z1	the first list
z2	the second list

Returns

the set product, `NULL` if some error occurred.

5.2.2.9 appf_im()

```
arrayf appf_im (
            arrayf z )
```

Returns the imaginary parts of the numbers in the sequence `z`.

Parameters

z	the list of points

Returns

the imaginary parts in `z`, `NULL` if some error occurred.

5.2.2.10 appf_join()

```
arrayf appf_join (
            arrayf z1,
            arrayf z2 )
```

Joins the real parts of the sequences `z1` and `z2` as the real parts and imaginary parts of a new list.

Parameters

z1	the first list
z2	the second list

Returns

the joint list, `NULL` if some error occurred.

5.2.2.11 appf_polar()

```
arrayf appf_polar (
            arrayf z )
```

Computes the complex numbers given by a sequence `z` of their polar coordinates on the sphere.

Parameters

z	the list of polar coordinates

Returns

the complex numbers given by their polar coordinates, `NULL` if some error occurred.

5.2.2.12 appf_re()

```
arrayf appf_re (
            arrayf z )
```

Returns the real parts of the numbers in the sequence `z`.

Parameters

z	the list of points

Returns

the real parts in `z`, `NULL` if some error occurred.

5.2.2.13 appf_rot()

```
arrayf appf_rot (
            arrayf z )
```

Computes `a*exp`(ib) for each term `a+ib` of a sequence `z` of complex numbers.

Parameters

z	the list of points

Returns

the image by `a+ib->a*exp`(ib), `NULL` if some error occurred.

5.2.2.14 appf_tensor()

```
arrayf appf_tensor (
            arrayf z1,
            arrayf z2 )
```

Computes tensor (or piontwise) product of the sequences `z1` and `z2`.

Parameters

z1	the first list
z2	the second list

Returns

the tensor product, `NULL` if some error occurred.

5.2.2.15 appf_unif()

```
arrayf appf_unif (
            ulong n,
            coeff_t st,
            coeff_t en )
```

Returns the list of `n` real numbers that split the interval [st,en] in `n-1` equal intervals.

Parameters

n	the number of points, at least `2`
st	the start point
en	the end point

Returns

the list of real numbers (in complex format), `NULL` if some error occurred.

5.3 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/help.h File Reference

A basic help system for the mini-apps.

Data Structures

- struct help_struct

  Description of a basic help screen.

Macros

- #define HELP_MAIN 0

  Indexes for help pages.
- #define **HELP_HYP** 1
- #define **HELP_CHEBYshev** 2
- #define **HELP_LEGENDRE** 3
- #define **HELP_HERMITE** 4
- #define **HELP_LAGUERRE** 5
- #define **HELP_SUM** 6
- #define **HELP_DIFF** 7
- #define **HELP_PROD** 8
- #define **HELP_CONCAT** 9
- #define **HELP_JOIN** 10
- #define **HELP_GRID** 11
- #define **HELP_EXP** 12
- #define **HELP_ROT** 13
- #define **HELP_POLAR** 14
- #define **HELP_ROOTS** 15
- #define **HELP_DER** 16

- #define **HELP_UNIF** 17
- #define **HELP_RAND** 18
- #define **HELP_NORM** 19
- #define **HELP_SPHERE** 20
- #define **HELP_EVAL** 21
- #define **HELP_EVALD** 22
- #define **HELP_EVALN** 23
- #define **HELP_NEWTON** 24
- #define **HELP_COMP** 25
- #define **HELP_RE** 26
- #define **HELP_IM** 27
- #define **HELP_CONJ** 28
- #define **HELP_TENSOR** 29
- #define **HELP_ANALYSE** 30
- #define HELP_COUNT 31

  The number of help pages.
- #define APP_COUNT (HELP_COUNT - 1)

  The number of mini-apps.

Typedefs

- typedef help_struct * help

  Practical wrapper for `arrayf_struct`.

Functions

- bool fpe_help_print (help h)

  Prints the help screen described by `h`.
- help fpe_help_get (int ind)

  Return the help system in the list with index `ind`.
- void stats_print (char *mes, long prec, deg_t deg, char *numType, bool real, char *polyFile, char *ptsFile, char *outFile, char *outError, double timePP, long count, double timeEV, ulong tpts, char *outHorner, double timeHo, ulong tptsho, ulong tit, ulong titho)

  Prints computation stats in a standard format for automatic processing.

5.3.1 Detailed Description

A basic help system for the mini-apps.

5.3.2 Typedef Documentation

5.3.2.1 help

```
typedef help_struct* help
```

Practical wrapper for `arrayf_struct`.

To avoid the constant use * and & the type `help_t` is a pointer.

Definition at line 86 of file help.h.

5.3.3 Function Documentation

5.3.3.1 fpe_help_get()

```
help fpe_help_get (
            int ind )
```

Return the help system in the list with index `ind`.

Parameters

ind	the index, use constants HELP_XXX

Returns

the help sytem with the given index. Returns the list, `NULL` if `ind` is an invalid request.

5.3.3.2 fpe_help_print()

```
bool fpe_help_print (
            help h )
```

Prints the help screen described by `h`.

Parameters

h	the help screen to display

Returns

Boolean value expressing wether help could indeed be provided.

5.3.3.3 stats_print()

```
void stats_print (
            char * mes,
            long prec,
            deg_t deg,
            char * numType,
            bool real,
            char * polyFile,
            char * ptsFile,
```

```
char * outFile,
char * outError,
double timePP,
long count,
double timeEV,
ulong tpts,
char * outHorner,
double timeHo,
ulong tptsho,
ulong tit,
ulong titho )
```

Prints computation stats in a standard format for automatic processing.

Parameters

mes	a short description of the computing task
prec	the precision used, in bits
deg	the degree of the polynomial
numType	the number type
real	true if it is a real polynomial, false otherwise
polyFile	the polynomial file name
ptsFile	the points list file name
outFile	the results output file name
outError	the errors list file name
timePP	pre-processing time in ns
count	the number of repetitions of the computing task
timeEV	evaluation time in ns
tpts	the total number of evaluation points (taking into acount the repetitions)
outHorner	the results output file name, computed by Horner's method
timeHo	the computing time in ns, by Horner's method
tptsho	the total number of evaluation by Horner's method
tit	total number of iterates, only for the iterative Newton method
titho	total number of iterates, only for the iterative Newton method, computed by Horner's method

5.4 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/main.h File Reference

This is the entry point in the main app.

Macros

- #define **APP_OK** 0
- #define **APP_ERROR** 1
- #define **APP_PARAMS** 2

Typedefs

- typedef int(∗ mainFuncf) (int argv, const char ∗∗args)

  The signature of a main function of an app in this project with machine numbers.
- typedef int(∗ mainFunc) (long prec, int argv, const char ∗∗args)

  The signature of a main function of an app in this project with arbitrary precision.

5.4.1 Detailed Description

This is the entry point in the main app.

Depending on the first command line parameter, it launches an internal app or presents a help screen to guide the user.

5.5 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/concave.h File Reference

Definition of a concave function computed from the coefficients of some polynomial.

Data Structures

- struct concave_struct

  Description of a concave function computed from the coefficients of some polynomial.

Macros

- #define BITS_GUARD 6

  The extra bits that are needed as explained in [1].

Typedefs

- typedef concave_struct ∗ concave

  Convenience pointer to `concave_struct`.

Functions

- concave conc_new (list l, prec_t prec)

  Computes the concave cover of the graph of a list `l` *sorted in decreasing order.*
- bool conc_free (concave f)

  Frees all the memory used by the concave map `f`*, assuming the struct has been allocated with* `malloc()`*, for example with* `conc_new()`.
- bool conc_range (concave f, real_t la)

  Computes the range of indexes in `f->allPow` *to use for evaluating the original polynomial at* `z` *with* `la=log_2|z|`.
- bool conc_range_der (concave f, real_t la)

  Computes the range of indexes in `f->allPow` *to use for evaluating the derivative of the original polynomial at* `z` *with* `la=log_2|z|`.

5.5.1 Detailed Description

Definition of a concave function computed from the coefficients of some polynomial.

Admissible powers are for any of the original polynomial `P` or its derivative `P'`.

5.5.2 Function Documentation

5.5.2.1 conc_free()

```
bool conc_free (
            concave f )
```

Frees all the memory used by the concave map `f`, assuming the struct has been allocated with `malloc()`, for example with `conc_new()`.

Parameters

f	the map

Returns

true if successfull, false otherwise.

5.5.2.2 conc_new()

```
concave conc_new (
            list l,
            prec_t prec )
```

Computes the concave cover of the graph of a list `l` sorted in decreasing order.

Note

Retains the list of non-zero coefficients in `all`.

Parameters

l	the sorted list
prec	the precision that will be used to evaluate the polynomial

Returns

the concave function above the graph of `l`, `NULL` if some error occurred.

5.5.2.3 conc_range()

```
bool conc_range (
            concave f,
            real_t la )
```

Computes the range of indexes in `f->allPow` to use for evaluating the original polynomial at `z` with `la=log_2|z|`.

Stores the result in the `f->start` and respectively `f->end`.

Note

`f->start>=f->end`, otherwise the value of the polynomial is `0`.

Parameters

f	the map
la	the slope, or `log_2|z|`

Returns

true if successfull, false otherwise.

5.5.2.4 conc_range_der()

```
bool conc_range_der (
            concave f,
            real_t la )
```

Computes the range of indexes in `f->allPow` to use for evaluating the derivative of the original polynomial at `z` with `la=log_2|z|`.

Stores the result in the `f->start` and respectively `f->end`.

Note

`f->start>=f->end`, otherwise the value of the derivative is `0`.

Parameters

f	the map
la	the slope, or `log_2|z|`

Returns

true if successfull, false otherwise.

5.6 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/eval.h File Reference

Definition of polynomial evaluator with arbitary precision coefficients.

Data Structures

- struct eval_struct

  Evaluator of polynomials with multi-precision floating point coefficients.

Macros

- #define MIN_EVAL_PREC 8

  Minimum prcision for evaluators.
- #define **MIN_EVAL_PREC_STR** "8"
- #define eval_lastValError(ev) (ev->valErr)

  The [approximative] upper bound for the error of the last evaluation, in bits. ***Not*** *reported by the Newton term computation.*
- #define eval_lastDerError(ev) (ev->derErr)

  The [approximative] upper bound for the error of the last derivative evaluation, in bits. ***Not*** *reported by the Newton term computation.*

Typedefs

- typedef eval_struct eval_t[1]

  Practical wrapper for `eval_struct`.
- typedef eval_struct * eval

  Convenience pointer to `eval_struct`.

Functions

- eval eval_new (poly P, prec_t prec)

  Returns a new evaluator of the complex polynomial `P`.
- eval eval_new_r (polyr Q, prec_t prec)

  Returns a new evaluator of the real polynomial `Q`.
- bool eval_free (eval ev)

  Frees all the memory used by the evaluator `ev`*, assuming the struct has been allocated with* `malloc()`*, for example with* `eval_new()` *or with* `eval_new_r()`.
- bool eval_val (comp v, eval ev, comp z)

  Evaluates `ev->P(z)` *(or* `ev->Q(z)`*) using the method described in [1].*
- bool eval_der (comp d, eval ev, comp z)

  Evaluates `ev->P'(z)` *(or* `ev->Q'(z)`*) using the method described in [1].*
- bool eval_val_der (comp v, comp d, eval ev, comp z)

Evaluates `ev->P(z)` and `ev->P'(z)` (or `ev->Q(z)` and `ev->Q'(z)`) using the method described in [1].

- bool eval_newton (comp nt, eval ev, comp z)

  Computes the Newthon method step of `ev->P` (or `ev->Q`) using the method described in [1].
- bool eval_analyse (eval ev)

  Analyses the complex polynomial `ev->P`, after some of its coefficients have been changed.
- bool eval_analyse_r (eval ev)

  Analyses the real polynomial `ev->Q`, after some of its coefficients have been changed.
- bool eval_val_cc (comp v, eval ev, comp z)

  Evaluates `ev->P(x)` using the method described in [1].
- bool eval_der_cc (comp d, eval ev, comp z)

  Evaluates `ev->P'(x)` using the method described in [1].
- bool eval_val_der_cc (comp v, comp d, eval ev, comp z)

  Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].
- bool eval_newton_cc (comp nt, eval ev, comp z)

  Computes the Newthon method step of `ev->P` using the method described in [1].
- bool eval_val_cr (comp v, eval ev, mpfr_t x)

  Evaluates `ev->P(x)` using the method described in [1].
- bool eval_der_cr (comp d, eval ev, mpfr_t x)

  Evaluates `ev->P'(x)` using the method described in [1].
- bool eval_val_der_cr (comp v, comp d, eval ev, mpfr_t x)

  Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].
- bool eval_newton_cr (comp nt, eval ev, mpfr_t x)

  Computes the Newthon method step of `ev->P` using the method described in [1].
- bool eval_val_rc (comp v, eval ev, comp z)

  Evaluates `ev->Q(x)` using the method described in [1].
- bool eval_der_rc (comp d, eval ev, comp z)

  Evaluates `ev->Q'(x)` using the method described in [1].
- bool eval_val_der_rc (comp v, comp d, eval ev, comp z)

  Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].
- bool eval_newton_rc (comp nt, eval ev, comp z)

  Computes the Newthon method step of `ev->Q` using the method described in [1].
- bool eval_val_rr (mpfr_t v, eval ev, mpfr_t x)

  Evaluates the real polynomial `ev->Q(x)` using the method described in [1].
- bool eval_der_rr (mpfr_t d, eval ev, mpfr_t x)

  Evaluates the derivative of real polynomial `ev->Q'(x)` using the method described in [1].
- bool eval_val_der_rr (mpfr_t v, mpfr_t d, eval ev, mpfr_t x)

  Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].
- bool eval_newton_rr (mpfr_t nt, eval ev, mpfr_t x)

  Computes the Newthon method step of the real polynomial `ev->Q` using the method described in [1].

5.6.1 Detailed Description

Definition of polynomial evaluator with arbitary precision coefficients.

5.6.2 Typedef Documentation

5.6.2.1 eval_t

```
typedef eval_struct eval_t[1]
```

Practical wrapper for `eval_struct`.

To avoid the constant use `*` and `&` the type `eval_t` is a pointer.

Definition at line 60 of file eval.h.

5.6.3 Function Documentation

5.6.3.1 eval_analyse()

```
bool eval_analyse (
            eval ev )
```

Analyses the complex polynomial `ev->P`, after some of its coefficients have been changed.

Note

The general functions `eval_val()`, `eval_der()`, `eval_val_der()` and `eval_newton()` automatically analyse the appropriate polynomial. Use this function only with the optimized versions like `eval_val_cx()`.

Parameters

ev	the evaluator

Returns

true if `ev` is ready to use, false otherwise.

5.6.3.2 eval_analyse_r()

```
bool eval_analyse_r (
            eval ev )
```

Analyses the real polynomial `ev->Q`, after some of its coefficients have been changed.

Note

The general functions `eval_val()`, `eval_der()`, `eval_val_der()` and `eval_newton()` automatically analyse the appropriate polynomial. Use this function only with the optimized versions like `eval_val_rx()`.

Parameters

ev	the evaluator

Returns

true if `ev` is ready to use, false otherwise.

5.6.3.3 eval_der()

```
bool eval_der (
            comp d,
            eval ev,
            comp z )
```

Evaluates `ev->P'(z)` (or `ev->Q'(z)`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

d	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.4 eval_der_cc()

```
bool eval_der_cc (
            comp d,
            eval ev,
            comp z )
```

Evaluates `ev->P'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.5 eval_der_cr()

```
bool eval_der_cr (
            comp d,
            eval ev,
            mpfr_t x )
```

Evaluates `ev->P'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the result
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.6 eval_der_rc()

```
bool eval_der_rc (
            comp d,
            eval ev,
            comp z )
```

Evaluates `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.7 eval_der_rr()

```
bool eval_der_rr (
            mpfr_t d,
            eval ev,
            mpfr_t x )
```

Evaluates the derivative of real polynomial `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the derivative
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.8 eval_free()

```
bool eval_free (
            eval ev )
```

Frees all the memory used by the evaluator `ev`, assuming the struct has been allocated with `malloc()`, for example with `eval_new()` or with `eval_new_r()`.

Parameters

ev	the evaluator

Returns

true if successfull, false otherwise.

5.6.3.9 eval_new()

```
eval eval_new (
            poly P,
            prec_t prec )
```

Returns a new evaluator of the complex polynomial `P`.

Parameters

P	the complex polynomial
prec	the precision of evaluations, in bits

Returns

the new evaluator, `NULL` if some error occurred.

5.6.3.10 eval_new_r()

```
eval eval_new_r (
            polyr Q,
            prec_t prec )
```

Returns a new evaluator of the real polynomial `Q`.

Parameters

Q	the real polynomial
prec	the precision of evaluations, in bits

Returns

the new evaluator, `NULL` if some error occurred.

5.6.3.11 eval_newton()

```
bool eval_newton (
            comp nt,
```

```
            eval ev,
            comp z )
```

Computes the Newthon method step of `ev->P` (or `ev->Q`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

nt	the Newton term
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.12 eval_newton_cc()

```
bool eval_newton_cc (
            comp nt,
            eval ev,
            comp z )
```

Computes the Newthon method step of `ev->P` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.13 eval_newton_cr()

```
bool eval_newton_cr (
            comp nt,
            eval ev,
            mpfr_t x )
```

Computes the Newthon method step of `ev->P` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.14 eval_newton_rc()

```
bool eval_newton_rc (
            comp nt,
            eval ev,
            comp z )
```

Computes the Newthon method step of `ev->Q` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.15 eval_newton_rr()

```
bool eval_newton_rr (
            mpfr_t nt,
            eval ev,
            mpfr_t x )
```

Computes the Newthon method step of the real polynomial `ev->Q` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.16 eval_val()

```
bool eval_val (
            comp v,
            eval ev,
            comp z )
```

Evaluates `ev->P(z)` (or `ev->Q(z)`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

v	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.17 eval_val_cc()

```
bool eval_val_cc (
            comp v,
            eval ev,
            comp z )
```

Evaluates `ev->P(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.18 eval_val_cr()

```
bool eval_val_cr (
            comp v,
            eval ev,
            mpfr_t x )
```

Evaluates `ev->P(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the result
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.19 eval_val_der()

```
bool eval_val_der (
             comp v,
             comp d,
             eval ev,
             comp z )
```

Evaluates `ev->P(z)` and `ev->P'(z)` (or `ev->Q(z)` and `ev->Q'(z)`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

v	the value
d	the derivative
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.20 eval_val_der_cc()

```
bool eval_val_der_cc (
             comp v,
             comp d,
             eval ev,
             comp z )
```

Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.21 eval_val_der_cr()

```
bool eval_val_der_cr (
            comp v,
            comp d,
            eval ev,
            mpfr_t x )
```

Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.22 eval_val_der_rc()

```
bool eval_val_der_rc (
            comp v,
            comp d,
            eval ev,
            comp z )
```

Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.23 eval_val_der_rr()

```
bool eval_val_der_rr (
            mpfr_t v,
            mpfr_t d,
            eval ev,
            mpfr_t x )
```

Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.6.3.24 eval_val_rc()

```
bool eval_val_rc (
            comp v,
            eval ev,
            comp z )
```

Evaluates `ev->Q(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.6.3.25 eval_val_rr()

```
bool eval_val_rr (
            mpfr_t v,
            eval ev,
            mpfr_t x )
```

Evaluates the real polynomial `ev->Q(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.7 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/evalf.h File Reference

Definition of polynomials evaluator with machine floating point coefficients.

Data Structures

- struct evalf_struct

  Evaluator of polynomials with machine floating point coefficients.

Macros

- #define evalf_lastValError(ev) (ev->valErr)

  The [approximative] upper bound for the error of the last evaluation, in bits. ***Not*** *reported by the Newton term computation.*
- #define evalf_lastDerError(ev) (ev->derErr)

  The [approximative] upper bound for the error of the last derivative evaluation, in bits. ***Not*** *reported by the Newton term computation.*

Typedefs

- typedef evalf_struct evalf_t[1]

  Practical wrapper for `evalf_struct`.
- typedef evalf_struct * evalf

  Convenience pointer to `evalf_struct`.

Functions

- evalf evalf_new (polyf P)

  Returns a new evaluator of the complex polynomial `P`.
- evalf evalf_new_r (polyfr Q)

  Returns a new evaluator of the real polynomial `Q`.
- bool evalf_free (evalf ev)

  Frees all the memory used by the evaluator `ev`*, assuming the struct has been allocated with* `malloc()`*, for example with* `evalf_new()` *or with* `evalf_new_r()`.
- bool evalf_val (compf v, evalf ev, compf z)

  Evaluates `ev->P(z)` *(or* `ev->Q(z)`*) using the method described in [1].*
- bool evalf_der (compf d, evalf ev, compf z)

  Evaluates `ev->P'(z)` *(or* `ev->Q'(z)`*) using the method described in [1].*
- bool evalf_val_der (compf v, compf d, evalf ev, compf z)

  Evaluates `ev->P(z)` *and* `ev->P'(z)` *(or* `ev->Q(z)` *and* `ev->Q'(z)`*) using the method described in [1].*
- bool evalf_newton (compf nt, evalf ev, compf z)

  Computes the Newthon method step of `ev->P` *(or* `ev->Q`*) using the method described in [1].*
- bool evalf_analyse (evalf ev)

  Analyses the complex polynomial `ev->P`*, after some of its coefficients have been changed.*
- bool evalf_analyse_r (evalf ev)

  Analyses the real polynomial `ev->Q`*, after some of its coefficients have been changed.*
- bool evalf_val_cc (compf v, evalf ev, compf z)

  Evaluates `ev->P(x)` *using the method described in [1].*
- bool evalf_der_cc (compf d, evalf ev, compf z)

  Evaluates `ev->P'(x)` *using the method described in [1].*
- bool evalf_val_der_cc (compf v, compf d, evalf ev, compf z)

  Evaluates `ev->P(x)` *and* `ev->P'(x)` *using the method described in [1].*
- bool evalf_newton_cc (compf nt, evalf ev, compf z)

Computes the Newthon method step of `ev->P` using the method described in [1].

- bool evalf_val_cr (compf v, evalf ev, coeff_t x)

  Evaluates `ev->P(x)` using the method described in [1].
- bool evalf_der_cr (compf d, evalf ev, coeff_t x)

  Evaluates `ev->P'(x)` using the method described in [1].
- bool evalf_val_der_cr (compf v, compf d, evalf ev, coeff_t x)

  Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].
- bool evalf_newton_cr (compf nt, evalf ev, coeff_t x)

  Computes the Newthon method step of `ev->P` using the method described in [1].
- bool evalf_val_rc (compf v, evalf ev, compf z)

  Evaluates `ev->Q(x)` using the method described in [1].
- bool evalf_der_rc (compf d, evalf ev, compf z)

  Evaluates `ev->Q'(x)` using the method described in [1].
- bool evalf_val_der_rc (compf v, compf d, evalf ev, compf z)

  Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].
- bool evalf_newton_rc (compf nt, evalf ev, compf z)

  Computes the Newthon method step of `ev->Q` using the method described in [1].
- coeff_t evalf_val_rr (evalf ev, coeff_t x)

  Evaluates the real polynomial `ev->Q(x)` using the method described in [1].
- coeff_t evalf_der_rr (evalf ev, coeff_t x)

  Evaluates the derivative of real polynomial `ev->Q'(x)` using the method described in [1].
- bool evalf_val_der_rr (coeff_t *v, coeff_t *d, evalf ev, coeff_t x)

  Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].
- coeff_t evalf_newton_rr (evalf ev, coeff_t x)

  Computes the Newthon method step of the real polynomial `ev->Q` using the method described in [1].

5.7.1 Detailed Description

Definition of polynomials evaluator with machine floating point coefficients.

5.7.2 Typedef Documentation

5.7.2.1 evalf_t

```
typedef evalf_struct evalf_t[1]
```

Practical wrapper for `evalf_struct`.

To avoid the constant use `*` and `&` the type `evalf_t` is a pointer.

Definition at line 51 of file evalf.h.

5.7.3 Function Documentation

5.7.3.1 evalf_analyse()

```
bool evalf_analyse (
            evalf ev )
```

Analyses the complex polynomial `ev->P`, after some of its coefficients have been changed.

Note

The general functions `evalf_val()`, `evalf_der()`, `evalf_val_der()` and `evalf_newton()` automatically analyse the appropriate polynomial. Use this function only with the optimized versions like `evalf_val_cx()`.

Parameters

ev	the evaluator

Returns

true if `ev` is ready to use, false otherwise.

5.7.3.2 evalf_analyse_r()

```
bool evalf_analyse_r (
            evalf ev )
```

Analyses the real polynomial `ev->Q`, after some of its coefficients have been changed.

Note

The general functions `evalf_val()`, `evalf_der()`, `evalf_val_der()` and `evalf_newton()` automatically analyse the appropriate polynomial. Use this function only with the optimized versions like `evalf_val_rx()`.

Parameters

ev	the evaluator

Returns

true if `ev` is ready to use, false otherwise.

5.7.3.3 evalf_der()

```
bool evalf_der (
            compf d,
```

```
            evalf ev,
            compf z )
```

Evaluates ev->P'(z) (or ev->Q'(z)) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

Parameters

d	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.4 evalf_der_cc()

```
bool evalf_der_cc (
            compf d,
            evalf ev,
            compf z )
```

Evaluates ev->P'(x) using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.5 evalf_der_cr()

```
bool evalf_der_cr (
            compf d,
            evalf ev,
            coeff_t x )
```

Evaluates ev->P'(x) using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the result
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.7.3.6 evalf_der_rc()

```
bool evalf_der_rc (
            compf d,
            evalf ev,
            compf z )
```

Evaluates ev->Q'(x) using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

d	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.7 evalf_der_rr()

```
coeff_t evalf_der_rr (
            evalf ev,
            coeff_t x )
```

Evaluates the derivative of real polynomial `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

ev	the evaluator
x	the real argument

Returns

the result, `NaN` is some error occurred.

5.7.3.8 evalf_free()

```
bool evalf_free (
            evalf ev )
```

Frees all the memory used by the evaluator `ev`, assuming the struct has been allocated with `malloc()`, for example with `evalf_new()` or with `evalf_new_r()`.

Parameters

ev	the evaluator

Returns

true if successfull, false otherwise.

5.7.3.9 evalf_new()

```
evalf evalf_new (
            polyf P )
```

Returns a new evaluator of the complex polynomial `P`.

Parameters

P	the complex polynomial

Returns

the new evaluator, `NULL` if some error occurred.

5.7.3.10 evalf_new_r()

```
evalf evalf_new_r (
            polyfr Q )
```

Returns a new evaluator of the real polynomial `Q`.

Parameters

Q	the real polynomial

Returns

the new evaluator, `NULL` if some error occurred.

5.7.3.11 evalf_newton()

```
bool evalf_newton (
            compf nt,
            evalf ev,
            compf z )
```

Computes the Newthon method step of `ev->P` (or `ev->Q`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

nt	the Newton term
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.12 evalf_newton_cc()

```
bool evalf_newton_cc (
            compf nt,
            evalf ev,
            compf z )
```

Computes the Newthon method step of `ev->P` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.13 evalf_newton_cr()

```
bool evalf_newton_cr (
            compf nt,
            evalf ev,
            coeff_t x )
```

Computes the Newthon method step of `ev->P` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.7.3.14 evalf_newton_rc()

```
bool evalf_newton_rc (
            compf nt,
            evalf ev,
            compf z )
```

Computes the Newthon method step of `ev->Q` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

nt	the Newton term
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.15 evalf_newton_rr()

```
coeff_t evalf_newton_rr (
            evalf ev,
            coeff_t x )
```

Computes the Newthon method step of the real polynomial `ev->Q` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

ev	the evaluator
x	the real argument

Returns

the result, `NaN` is some error occurred.

5.7.3.16 evalf_val()

```
bool evalf_val (
            compf v,
            evalf ev,
            compf z )
```

Evaluates `ev->P(z)` (or `ev->Q(z)`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

v	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.17 evalf_val_cc()

```
bool evalf_val_cc (
            compf v,
            evalf ev,
            compf z )
```

Evaluates `ev->P(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.18 evalf_val_cr()

```
bool evalf_val_cr (
            compf v,
            evalf ev,
            coeff_t x )
```

Evaluates `ev->P(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the result
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.7.3.19 evalf_val_der()

```
bool evalf_val_der (
            compf v,
            compf d,
            evalf ev,
            compf z )
```

Evaluates `ev->P(z)` and `ev->P'(z)` (or `ev->Q(z)` and `ev->Q'(z)`) using the method described in [1].

Note

This function chooses the quickest variant to compute, depending if the polynomial of `ev` and / or `z` are real.

Parameters

v	the value
d	the derivative
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.20 evalf_val_der_cc()

```
bool evalf_val_der_cc (
            compf v,
            compf d,
            evalf ev,
            compf z )
```

Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.21 evalf_val_der_cr()

```
bool evalf_val_der_cr (
            compf v,
            compf d,
            evalf ev,
            coeff_t x )
```

Evaluates `ev->P(x)` and `ev->P'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.7.3.22 evalf_val_der_rc()

```
bool evalf_val_der_rc (
            compf v,
            compf d,
            evalf ev,
            compf z )
```

Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.23 evalf_val_der_rr()

```
bool evalf_val_der_rr (
            coeff_t * v,
            coeff_t * d,
            evalf ev,
            coeff_t x )
```

Evaluates `ev->Q(x)` and `ev->Q'(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the value
d	the derivative
ev	the evaluator
x	the real argument

Returns

true if successfull, false otherwise.

5.7.3.24 evalf_val_rc()

```
bool evalf_val_rc (
            compf v,
            evalf ev,
            compf z )
```

Evaluates `ev->Q(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

v	the result
ev	the evaluator
z	the complex argument

Returns

true if successfull, false otherwise.

5.7.3.25 evalf_val_rr()

```
coeff_t evalf_val_rr (
            evalf ev,
            coeff_t x )
```

Evaluates the real polynomial `ev->Q(x)` using the method described in [1].

Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by `ev` nor if the polynomial has been pre-conditionned after the last coefficient update.

Parameters

ev	the evaluator
x	the real argument

Returns

the result, `NaN` is some error occurred.

5.8 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/list.h File Reference

Definition of a list that can quickly sort real machine floating-point numbers and keep track of their permutation.

Data Structures

- struct list_struct

  A list of real numbers that can be sorted, while keeping track of original order.

Macros

- #define LIST_FACTOR 1.2

  The multiplicative factor by which to grow the lists.
- #define LIST_TERM 100

  The additive term by which to grow the lists.

Typedefs

- typedef list_struct list_t[1]

  Practical wrapper for `list_struct`.
- typedef list_struct * list

  Convenience pointer to `list_struct`.

Functions

- list list_new (deg_t size)

  Returns a new list of machine real numbers, with storage space for `size` numbers.
- bool list_init (list l, deg_t size)

  Initializes an existing list `l` with storage space for `size` numbers.
- bool list_free (list l)

  Frees all the memory used by the list `l`, assuming the struct has been allocated with `malloc()`, for example with `list_new()`.
- bool list_clear (list l)

  Frees all the memory used by the list `l`, but not the list `l` itself.
- list list_clone (list l)

  Returns a copy of the list `l`.
- bool list_add (list l, deg_t k, real_t s)

  Adds the couple (k,s) at a new position at the end of the list `l`.
- bool list_trim (list l)

  Trims the list `l` to minimal size to contain all its elements.
- bool list_sort (list l)

  Sorts the list in descending order while preserving couples (k[i],s[i]) for all `i`.

5.8.1 Detailed Description

Definition of a list that can quickly sort real machine floating-point numbers and keep track of their permutation.

5.8.2 Typedef Documentation

5.8.2.1 list_t

```
typedef list_struct list_t[1]
```

Practical wrapper for `list_struct`.

To avoid the constant use `*` and `&` the type `list_t` is a pointer.

Definition at line 46 of file list.h.

5.8.3 Function Documentation

5.8.3.1 list_add()

```
bool list_add (
            list l,
            deg_t k,
            real_t s )
```

Adds the couple (k,s) at a new position at the end of the list `l`.

Parameters

l	the list
k	the index
s	the real number

Returns

true if successfull, false otherwise.

5.8.3.2 list_clear()

```
bool list_clear (
             list l )
```

Frees all the memory used by the list `l`, but not the list `l` itself.

Parameters

l	the list

Returns

true if successfull, false otherwise.

5.8.3.3 list_clone()

```
list list_clone (
             list l )
```

Returns a copy of the list `l`.

Parameters

l	the list

Returns

the new list, `NULL` if some error occurred.

5.8.3.4 list_free()

```
bool list_free (
            list l )
```

Frees all the memory used by the list `l`, assuming the struct has been allocated with `malloc()`, for example with `list_new()`.

Parameters

l	the list

Returns

true if successfull, false otherwise.

5.8.3.5 list_init()

```
bool list_init (
            list l,
            deg_t size )
```

Initializes an existing list `l` with storage space for `size` numbers.

Parameters

l	the list
size	the size of the list

Returns

true if successfull, false otherwise.

5.8.3.6 list_new()

```
list list_new (
            deg_t size )
```

Returns a new list of machine real numbers, with storage space for `size` numbers.

Parameters

size	the size of the list

Returns

the new list, `NULL` if some error occurred.

5.8.3.7 list_sort()

```
bool list_sort (
            list l )
```

Sorts the list in descending order while preserving couples (k[i],s[i]) for all `i`.

Warning

The memory usage will double during the operation, all cleared up before returning. In case of failure, the original list is destroyed.

Parameters

l	the list

Returns

true if successfull, false otherwise.

5.8.3.8 list_trim()

```
bool list_trim (
            list l )
```

Trims the list `l` to minimal size to contain all its elements.

Parameters

l	the list

Returns

true if successfull, false otherwise.

5.9 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/pows.h File Reference

Definition of a buffer for pre-computed powers of a complex number with arbitary precision.

Data Structures

- struct pows_struct

  The powers of the complex number `z` using multi-precision floating point numbers.

Typedefs

- typedef pows_struct pows_t[1]

  Practical wrapper for `pows_struct`.
- typedef pows_struct * pows

  Convenience pointer to `eval_struct`.

Functions

- pows pows_new (prec_t prec, deg_t size)

  Returns a new buffer of powers of complex numbers of precision `prec`, with initial storage space for `size` powers.
- bool pows_free (pows zn)

  Frees all the memory used by the buffer `zn`, assuming the struct has been allocated with `malloc()`, for example with `pows_new()`.
- bool pows_set (pows zn, comp z)

  Sets the complex number of which the powers will be computed by the buffer `zn`.
- comp_ptr pows_pow (pows zn, deg_t pow)

  Computes `z^pow` using repeated squares method and the cache of previously computed powers.
- comp_ptr pows_pow_once (pows zn, deg_t pow)

  Computes `z^pow` using repeated squares method and the cache of previously computed powers.

5.9.1 Detailed Description

Definition of a buffer for pre-computed powers of a complex number with arbitary precision.

5.9.2 Typedef Documentation

5.9.2.1 pows_t

```
typedef pows_struct pows_t[1]
```

Practical wrapper for `pows_struct`.

To avoid the constant use `*` and `&` the type `pows_t` is a pointer.

Definition at line 45 of file pows.h.

5.9.3 Function Documentation

5.9.3.1 pows_free()

```
bool pows_free (
            pows zn )
```

Frees all the memory used by the buffer `zn`, assuming the struct has been allocated with `malloc()`, for example with `pows_new()`.

Parameters

zn	the powers buffer

Returns

true if successfull, false otherwise.

5.9.3.2 pows_new()

```
pows pows_new (
            prec_t prec,
            deg_t size )
```

Returns a new buffer of powers of complex numbers of precision `prec`, with initial storage space for `size` powers.

Warning

`prec` must be at least `precf` and `size` at most `MAX_DEG`.

Parameters

prec	the precision of the coefficients, in bits
size	the size of the buffer

Returns

the new buffer, `NULL` if some error occurred.

5.9.3.3 pows_pow()

```
comp_ptr pows_pow (
            pows zn,
            deg_t pow )
```

Computes `z^pow` using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of `z` that have been computed to accelerate later calls of this function. Also, if `pow` is larger than the size of the buffer `zn`, it is automatically increased to store the result.

Parameters

zn	the powers buffer
pow	the power to compute

Returns

the result z^pow, NULL if some error occurred.

5.9.3.4 pows_pow_once()

```
comp_ptr pows_pow_once (
            pows zn,
            deg_t pow )
```

Computes z^pow using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of z into zn.

Parameters

zn	the powers buffer
pow	the power to compute

Returns

the result z^pow, NULL if some error occurred.

5.9.3.5 pows_set()

```
bool pows_set (
            pows zn,
            comp z )
```

Sets the complex number of which the powers will be computed by the buffer zn.

Parameters

zn	the powers buffer
z	the complex number

Returns

true if successfull, false otherwise.

5.10 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/powsf.h File Reference

Definition of a buffer for pre-computed powers of a machine complex number.

Data Structures

- struct powsf_struct

  The powers of the complex number `z` using machine floating point numbers.

Typedefs

- typedef powsf_struct powsf_t[1]

  Practical wrapper for `powsf_struct`.
- typedef powsf_struct * powsf

  Convenience pointer to `eval_struct`.

Functions

- powsf powsf_new (deg_t size)

  Returns a new buffer of powers of machine complex numbers, with initial storage space for `size` powers.
- bool powsf_free (powsf zn)

  Frees all the memory used by the buffer `zn`, assuming the struct has been allocated with `malloc()`, for example with `powsf_new()`.
- bool powsf_set (powsf zn, compf z)

  Sets the complex number of which the powers will be computed by the buffer `zn`.
- compf_ptr powsf_pow (powsf zn, deg_t pow)

  Computes `z^pow` using repeated squares method and the cache of previously computed powers.
- compf_ptr powsf_pow_once (powsf zn, deg_t pow)

  Computes `z^pow` using repeated squares method and the cache of previously computed powers.

5.10.1 Detailed Description

Definition of a buffer for pre-computed powers of a machine complex number.

5.10.2 Typedef Documentation

5.10.2.1 powsf_t

```
typedef powsf_struct powsf_t[1]
```

Practical wrapper for `powsf_struct`.

To avoid the constant use `*` and `&` the type `powsf_t` is a pointer.

Definition at line 41 of file powsf.h.

5.10.3 Function Documentation

5.10.3.1 powsf_free()

```
bool powsf_free (
            powsf zn )
```

Frees all the memory used by the buffer `zn`, assuming the struct has been allocated with `malloc()`, for example with `powsf_new()`.

Parameters

zn	the powers buffer

Returns

true if successfull, false otherwise.

5.10.3.2 powsf_new()

```
powsf powsf_new (
            deg_t size )
```

Returns a new buffer of powers of machine complex numbers, with initial storage space for `size` powers.

Warning

`size` must be at most `MAX_DEG`.

Parameters

size	the size of the buffer

Returns

the new buffer, `NULL` if some error occurred.

5.10.3.3 powsf_pow()

```
compf_ptr powsf_pow (
            powsf zn,
            deg_t pow )
```

Computes `z^pow` using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of `z` that have been computed to accelerate later calls of this function. Also, if `pow` is larger than the size of the buffer `zn`, it is automatically increased to store the result.

Warning

fails if pow==0

Parameters

zn	the powers buffer
pow	the power to compute

Returns

the result `z^pow`, `NULL` if some error occurred.

5.10.3.4 powsf_pow_once()

```
compf_ptr powsf_pow_once (
            powsf zn,
            deg_t pow )
```

Computes `z^pow` using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of `z` into `zn`.

Parameters

zn	the powers buffer
pow	the power to compute

Returns

the result `z^pow`, `NULL` if some error occurred.

5.10.3.5 powsf_set()

```
bool powsf_set (
            powsf zn,
            compf z )
```

Sets the complex number of which the powers will be computed by the buffer `zn`.

Parameters

zn	the powers buffer
z	the complex number

Returns

true if successfull, false otherwise.

5.11 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/powsfr.h File Reference

Definition of a buffer for pre-computed powers of a machine real number.

Data Structures

- struct powsfr_struct

  The powers of the real number `x` using machine floating point numbers.

Typedefs

- typedef powsfr_struct powsfr_t[1]

  Practical wrapper for `powsfr_struct`.
- typedef powsfr_struct * powsfr

  Convenience pointer to `eval_struct`.

Functions

- powsfr powsfr_new (deg_t size)

  Returns a new buffer of powers of machine real numbers, with initial storage space for `size` powers.
- bool powsfr_free (powsfr xn)

  Frees all the memory used by the buffer `xn`, assuming the struct has been allocated with `malloc()`, for example with `powsfr_new()`.
- bool powsfr_set (powsfr xn, coeff_t x)

  Sets the real number of which the powers will be computed by the buffer `xn`.
- coeff_t powsfr_pow (powsfr xn, deg_t pow)

  Computes `x^pow` using repeated squares method and the cache of previously computed powers.
- coeff_t powsfr_pow_once (powsfr xn, deg_t pow)

  Computes `x^pow` using repeated squares method and the cache of previously computed powers.

5.11.1 Detailed Description

Definition of a buffer for pre-computed powers of a machine real number.

5.11.2 Typedef Documentation

5.11.2.1 powsfr_t

```
typedef powsfr_struct powsfr_t[1]
```

Practical wrapper for `powsfr_struct`.

To avoid the constant use `*` and `&` the type `powsfr_t` is a pointer.

Definition at line 56 of file powsfr.h.

5.11.3 Function Documentation

5.11.3.1 powsfr_free()

```
bool powsfr_free (
            powsfr xn )
```

Frees all the memory used by the buffer `xn`, assuming the struct has been allocated with `malloc()`, for example with `powsfr_new()`.

Parameters

xn	the powers buffer

Returns

true if successfull, false otherwise.

5.11.3.2 powsfr_new()

```
powsfr powsfr_new (
            deg_t size )
```

Returns a new buffer of powers of machine real numbers, with initial storage space for `size` powers.

Warning

`size` must be at most `MAX_DEG`.

Parameters

size	the size of the buffer

Returns

the new buffer, `NULL` if some error occurred.

5.11.3.3 powsfr_pow()

```
coeff_t powsfr_pow (
            powsfr xn,
            deg_t pow )
```

Computes x^pow using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of x that have been computed to accelerate later calls of this function. Also, if pow is larger than the size of the buffer xn, it is automatically increased to store the result.

Parameters

xn	the powers buffer
pow	the power to compute

Returns

the result x^pow, NaN if some error occurred.

5.11.3.4 powsfr_pow_once()

```
coeff_t powsfr_pow_once (
            powsfr xn,
            deg_t pow )
```

Computes x^pow using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of x.

Parameters

xn	the powers buffer
pow	the power to compute

Returns

the result x^pow, NULL if some error occurred.

5.11.3.5 powsfr_set()

```
bool powsfr_set (
            powsfr xn,
            coeff_t x )
```

Sets the real number of which the powers will be computed by the buffer xn.

Parameters

xn	the powers buffer
x	the real number

Returns

true if successfull, false otherwise.

5.12 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/powsr.h File Reference

Definition of a buffer for pre-computed powers of a real number with arbitary precision.

Data Structures

- struct powsr_struct

  The powers of the real number `x` using multi-precision floating point numbers.

Typedefs

- typedef powsr_struct powsr_t[1]

  Practical wrapper for `powsr_struct`.
- typedef powsr_struct * powsr

  Convenience pointer to `eval_struct`.

Functions

- powsr powsr_new (prec_t prec, deg_t size)

  Returns a new buffer of powers of real numbers of precision `prec`, with initial storage space for `size` powers.
- bool powsr_free (powsr xn)

  Frees all the memory used by the buffer `xn`, assuming the struct has been allocated with `malloc()`, for example with `powsr_new()`.
- bool powsr_set (powsr xn, mpfr_t x)

  Sets the real number of which the powers will be computed by the buffer `xn`.
- mpfr_ptr powsr_pow (powsr xn, deg_t pow)

  Computes `x^pow` using repeated squares method and the cache of previously computed powers.
- mpfr_ptr powsr_pow_once (powsr xn, deg_t pow)

  Computes `x^pow` using repeated squares method and the cache of previously computed powers.

5.12.1 Detailed Description

Definition of a buffer for pre-computed powers of a real number with arbitary precision.

5.12.2 Typedef Documentation

5.12.2.1 powsr_t

```
typedef powsr_struct powsr_t[1]
```

Practical wrapper for `powsr_struct`.

To avoid the constant use `*` and `&` the type `powsr_t` is a pointer.

Definition at line 63 of file powsr.h.

5.12.3 Function Documentation

5.12.3.1 powsr_free()

```
bool powsr_free (
            powsr xn )
```

Frees all the memory used by the buffer `xn`, assuming the struct has been allocated with `malloc()`, for example with `powsr_new()`.

Parameters

xn	the powers buffer

Returns

true if successfull, false otherwise.

5.12.3.2 powsr_new()

```
powsr powsr_new (
            prec_t prec,
            deg_t size )
```

Returns a new buffer of powers of real numbers of precision `prec`, with initial storage space for `size` powers.

Warning

`prec` must be at least `precf` and `size` at most `MAX_DEG`.

Parameters

prec	the precision of the coefficients, in bits
size	thessize of the buffer

Returns

the new buffer, NULL if some error occurred.

5.12.3.3 powsr_pow()

```
mpfr_ptr powsr_pow (
            powsr xn,
            deg_t pow )
```

Computes x^pow using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of x that have been computed to accelerate later calls of this function. Also, if pow is larger than the size of the buffer xn, it is automatically increased to store the result.

Parameters

xn	the powers buffer
pow	the power to compute

Returns

the result x^pow, NULL if some error occurred.

5.12.3.4 powsr_pow_once()

```
mpfr_ptr powsr_pow_once (
            powsr xn,
            deg_t pow )
```

Computes x^pow using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of x into xn.

Parameters

xn	the powers buffer
pow	the power to compute

Returns

the result x^pow, NULL if some error occurred.

5.12.3.5 powsr_set()

```
bool powsr_set (
            powsr xn,
            mpfr_t x )
```

Sets the real number of which the powers will be computed by the buffer `xn`.

Parameters

xn	the powers buffer
x	the complex number

Returns

true if successfull, false otherwise.

5.13 /home/runner/work/FastPolyEval/FastPolyEval/code/numbers/comp.h File Reference

Definition of MPFR complex numbers.

Data Structures

- struct comp_struct

  Multi-precision floating point complex numbers.

Macros

- #define comp_init(d, prec)

  Allocates memory for the digits of `d`.
- #define comp_initz(d, prec)

  Allocates memory for the digits of `d` and sets its value to `0`.
- #define comp_clear(d)

  De-allocates the memory used by the digits of `d`.
- #define comp_zero(d) (mpfr_zero_p((d)->x) && mpfr_zero_p((d)->y))

  Tests if `d==0`.
- #define comp_add(d, a, b)

  Adds `a` to `b` and stores the result in `d`, all of type comp or comp_ptr.
- #define comp_set(d, a)

  Sets `d` to `a`.
- #define comp_setr(d, a)

  Sets `d` to the real value `a`.
- #define comp_neg(d, a)

  Sets `d` to `-a`.
- #define comp_addr(d, a, r)

Adds the complex number a to the real number b and stores the result in d.

- #define comp_amu(d, a, r, buf)

  *Adds the complex number a*r to d, where d,a are complex and r is unsigned integer.*

- #define comp_sub(d, a, b)

  Subtracts b from a and stores the result in d, all of type comp or comp_ptr.

- #define comp_subr(d, a, r)

  Subtracts the real number b from the complex number a and stores the result in d.

- #define comp_mul(d, a, b, buf1, buf2)

  Multiplies a to b and stores the result in d, all of type comp or comp_ptr.

- #define comp_div(d, a, b, b1, b2, b3)

  Divides a by b and stores the result in d, all of type comp or comp_ptr.

- #define comp_mod(m, a) mpfr_hypot((m), (a)->x, (a)->y, MPFR_RNDN);

  Computes the modulus of a and stores the result in m, a of type comp and m of type mpfr_t.

- #define comp_mulr(d, a, r)

  Multiplies the complex number a to the real number r and stores the result in d.

- #define comp_muli(d, a, i)

  Multiplies the complex number a to the integer i and stores the result in d.

- #define comp_mulu(d, a, i)

  Multiplies the complex number a to the unsigned integer i and stores the result in d.

- #define comp_sqr(d, a, buf)

  Squares a and stores the result in d, all of type comp or comp_ptr.

Typedefs

- typedef comp_struct comp[1]

  Practical wrapper for comp_struct.

- typedef comp_struct * comp_ptr

  Convenience pointer to comp_struct.

Functions

- real_t comp_log2 (comp z)

  Computes the base 2 log of |z|.

- real_t real_log2 (mpfr_t x)

  Computes the base 2 log of |x|.

- real_t comp_s (comp z)

  Computes s(z).

- real_t mpfr_s (mpfr_t x)

  Computes s(x).

5.13.1 Detailed Description

Definition of MPFR complex numbers.

5.13.2 Macro Definition Documentation

5.13.2.1 comp_add

```
#define comp_add(
              d,
              a,
              b )
```

Value:

```
mpfr_add((d)->x, (a)->x, (b)->x, MPFR_RNDN); \
mpfr_add((d)->y, (a)->y, (b)->y, MPFR_RNDN);
```

Adds `a` to `b` and stores the result in `d`, all of type comp or comp_ptr.

Definition at line 64 of file comp.h.

5.13.2.2 comp_addr

```
#define comp_addr(
              d,
              a,
              r )
```

Value:

```
mpfr_add((d)->x, (a)->x, (r), MPFR_RNDN); \
mpfr_set((d)->y, (a)->y, MPFR_RNDN);
```

Adds the complex number `a` to the real number `b` and stores the result in `d`.

Definition at line 80 of file comp.h.

5.13.2.3 comp_amu

```
#define comp_amu(
              d,
              a,
              r,
              buf )
```

Value:

```
mpfr_mul_ui((buf), (a)->x, (r), MPFR_RNDN); \
mpfr_add((d)->x, (d)->x, (buf), MPFR_RNDN); \
mpfr_mul_ui((buf), (a)->y, (r), MPFR_RNDN); \
mpfr_add((d)->y, (d)->y, (buf), MPFR_RNDN);
```

Adds the complex number `a*r` to `d`, where `d`,a are complex and `r` is unsigned integer.

Definition at line 84 of file comp.h.

5.13.2.4 comp_clear

```
#define comp_clear(
              d )
```

Value:

```
                              mpfr_clear((d)->x); \
                              mpfr_clear((d)->y);
```

De-allocates the memory used by the digits of d.

Definition at line 57 of file comp.h.

5.13.2.5 comp_div

```
#define comp_div(
              d,
              a,
              b,
              b1,
              b2,
              b3 )
```

Value:

```
                                    mpfr_sqr((b3), (b)->x, MPFR_RNDN); \
                                    mpfr_sqr((b2), (b)->y, MPFR_RNDN); \
                                    mpfr_add((b3), (b3), (b2), MPFR_RNDN); \
                                    mpfr_mul((b1), (a)->x, (b)->x, MPFR_RNDN); \
                                    mpfr_mul((b2), (a)->y, (b)->y, MPFR_RNDN); \
                                    mpfr_add((b1), (b1), (b2), MPFR_RNDN); \
                                    mpfr_mul((b2), (a)->x, (b)->y, MPFR_RNDN); \
                                    mpfr_mul((d)->y, (a)->y, (b)->x, MPFR_RNDN); \
                                    mpfr_sub((d)->y, (d)->y, (b2), MPFR_RNDN); \
                                    mpfr_div((d)->y, (d)->y, (b3), MPFR_RNDN); \
                                    mpfr_div((d)->x, (b1), (b3), MPFR_RNDN);
```

Divides a by b and stores the result in d, all of type comp or comp_ptr.

Definition at line 107 of file comp.h.

5.13.2.6 comp_init

```
#define comp_init(
              d,
              prec )
```

Value:

```
                              mpfr_init2((d)->x, prec); \
                              mpfr_init2((d)->y, prec);
```

Allocates memory for the digits of d.

Definition at line 47 of file comp.h.

5.13.2.7 comp_initz

```
#define comp_initz(
              d,
              prec )
```

Value:

```
                              mpfr_init2((d)->x, prec); \
                              mpfr_init2((d)->y, prec); \
                              mpfr_set_zero((d)->x, 1); \
                              mpfr_set_zero((d)->y, 1);
```

Allocates memory for the digits of `d` and sets its value to `0`.

Definition at line 51 of file comp.h.

5.13.2.8 comp_mul

```
#define comp_mul(
              d,
              a,
              b,
              buf1,
              buf2 )
```

Value:

```
                                    mpfr_mul((buf1), (a)->x, (b)->x, MPFR_RNDN); \
                                    mpfr_mul((buf2), (a)->y, (b)->y, MPFR_RNDN); \
                                    mpfr_sub((buf1), (buf1), (buf2), MPFR_RNDN); \
                                    mpfr_mul((buf2), (a)->x, (b)->y, MPFR_RNDN); \
                                    mpfr_mul((d)->y, (a)->y, (b)->x, MPFR_RNDN); \
                                    mpfr_add((d)->y, (d)->y, (buf2), MPFR_RNDN); \
                                    mpfr_set((d)->x, (buf1), MPFR_RNDN);
```

Multiplies `a` to `b` and stores the result in `d`, all of type comp or comp_ptr.

Definition at line 98 of file comp.h.

5.13.2.9 comp_muli

```
#define comp_muli(
              d,
              a,
              i )
```

Value:

```
                              mpfr_mul_si((d)->x, (a)->x, (i), MPFR_RNDN); \
                              mpfr_mul_si((d)->y, (a)->y, (i), MPFR_RNDN);
```

Multiplies the complex number `a` to the integer `i` and stores the result in `d`.

Definition at line 127 of file comp.h.

5.13.2.10 comp_mulr

```
#define comp_mulr(
              d,
              a,
              r )
```

Value:

```
mpfr_mul((d)->x, (a)->x, (r), MPFR_RNDN); \
mpfr_mul((d)->y, (a)->y, (r), MPFR_RNDN);
```

Multiplies the complex number `a` to the real number `r` and stores the result in `d`.

Definition at line 123 of file comp.h.

5.13.2.11 comp_mulu

```
#define comp_mulu(
              d,
              a,
              i )
```

Value:

```
mpfr_mul_ui((d)->x, (a)->x, (i), MPFR_RNDN); \
mpfr_mul_ui((d)->y, (a)->y, (i), MPFR_RNDN);
```

Multiplies the complex number `a` to the unsigned integer `i` and stores the result in `d`.

Definition at line 131 of file comp.h.

5.13.2.12 comp_neg

```
#define comp_neg(
              d,
              a )
```

Value:

```
mpfr_neg((d)->x, (a)->x, MPFR_RNDN); \
mpfr_neg((d)->y, (a)->y, MPFR_RNDN);
```

Sets `d` to `-a`.

Definition at line 76 of file comp.h.

5.13.2.13 comp_set

```
#define comp_set(
              d,
              a )
```

Value:

```
mpfr_set((d)->x, (a)->x, MPFR_RNDN); \
mpfr_set((d)->y, (a)->y, MPFR_RNDN);
```

Sets d to a.

Definition at line 68 of file comp.h.

5.13.2.14 comp_setr

```
#define comp_setr(
              d,
              a )
```

Value:

```
mpfr_set((d)->x, (a), MPFR_RNDN); \
mpfr_set_zero((d)->y, 1);
```

Sets d to the real value a.

Definition at line 72 of file comp.h.

5.13.2.15 comp_sqr

```
#define comp_sqr(
              d,
              a,
              buf )
```

Value:

```
mpfr_sqr((buf), (a)->y, MPFR_RNDN); \
mpfr_mul((d)->y, (a)->x, (a)->y, MPFR_RNDN); \
mpfr_mul_2si((d)->y, (d)->y, 1, MPFR_RNDN); \
mpfr_sqr((d)->x, (a)->x, MPFR_RNDN); \
mpfr_sub((d)->x, (d)->x, (buf), MPFR_RNDN);
```

Squares a and stores the result in d, all of type comp or comp_ptr.

Definition at line 135 of file comp.h.

5.13.2.16 comp_sub

```
#define comp_sub(
              d,
              a,
              b )
```

Value:

```
                              mpfr_sub((d)->x, (a)->x, (b)->x, MPFR_RNDN); \
                              mpfr_sub((d)->y, (a)->y, (b)->y, MPFR_RNDN);
```

Subtracts `b` from `a` and stores the result in `d`, all of type comp or comp_ptr.

Definition at line 90 of file comp.h.

5.13.2.17 comp_subr

```
#define comp_subr(
              d,
              a,
              r )
```

Value:

```
                              mpfr_sub((d)->x, (a)->x, (r), MPFR_RNDN); \
                              mpfr_set((d)->y, (a)->y, MPFR_RNDN);
```

Subtracts the real number `b` from the complex number `a` and stores the result in `d`.

Definition at line 94 of file comp.h.

5.13.3 Typedef Documentation

5.13.3.1 comp

```
typedef comp_struct comp[1]
```

Practical wrapper for `comp_struct`.

To avoid the constant use $*$ and `&` the type `compf` is a pointer.

Definition at line 39 of file comp.h.

5.13.4 Function Documentation

5.13.4.1 comp_log2()

```
real_t comp_log2 (
             comp z )
```

Computes the base `2 log` of $|z|$.

Parameters

z	the complex number

Returns

log_2(|z|)

5.13.4.2 comp_s()

```
real_t comp_s (
            comp z )
```

Computes s(z).

See also

[1]

Parameters

z	the complex number

Returns

[log_2(|z|)]+1

5.13.4.3 mpfr_s()

```
real_t mpfr_s (
            mpfr_t x )
```

Computes s(x).

See also

[1]

Parameters

x	the real number

Returns

[log_2(|z|)]+1

5.13.4.4 real_log2()

```
real_t real_log2 (
            mpfr_t x )
```

Computes the base 2 log of |x|.

Parameters

x	the real number

Returns

log_2(|x|)

5.14 /home/runner/work/FastPolyEval/FastPolyEval/code/numbers/compf.h File Reference

Definition of machine complex numbers.

Data Structures

- struct compf_struct

  Machine complex numbers.

Macros

- #define compf_set(d, a)

  Sets d to a.
- #define compf_setr(d, a)

  Sets d to the real value a.
- #define compf_neg(d, a)

  Sets d to -a.
- #define compf_add(d, a, b)

  Adds a to b and stores the result in d, all of type compf or compf_ptr.
- #define compf_addr(d, a, r)

  Adds the complex number a to the real number b and stores the result in d.
- #define compf_sub(d, a, b)

  Subtracts b from a and stores the result in d, all of type compf or compf_ptr.
- #define compf_subr(d, a, r)

Subtracts the real number b from the complex number a and stores the result in d.

- #define **compf_mul**(d, a, b)
- #define compf_mulr(d, a, r)

  Multiplies the complex number a to the real number r and stores the result in d.
- #define compf_amr(d, a, r)

  Adds the complex number a∗r to d, where d,a are complex and r is real.
- #define compf_sqr(d, a)

  Squares a and stores the result in d, all of type compf or compf_ptr.
- #define compf_div(d, a, b)

  Divides a by b and stores the result in d, all of type compf or compf_ptr.
- #define compf_mod(a) fhypot((a)->x, (a)->y)

  Computes the modulus of the complex number a.
- #define compf_dist(a, b) fhypot((a)->x - (b)->x, (a)->y - (b)->y)

  Computes the distance betwwen the complex numbera a and b.
- #define compf_mod2(a) ((a)->x ∗ (a)->x + (a)->y ∗ (a)->y)
- #define compf_log2(a) (plog2(compf_mod(a)))

  Computes the log_2 of the modulus of the complex number a.
- #define coeff_log2(a) (plog2((a) < 0 ? -(a) : (a)))

  Computes the log_2 of the absolute value of the real number a.
- #define compf_s(a) (pfloor(plog2(compf_mod(a))) + 1)

  Computes the scale of the complex number a, see [1].
- #define coeff_s(a) (pfloor(coeff_log2(a)) + 1)

  Computes the scale of the real number a, see [1].

Typedefs

- typedef compf_struct compf[1]

  Practical wrapper for compf_struct.
- typedef compf_struct ∗ compf_ptr

  Convenience pointer to compf_struct.

5.14.1 Detailed Description

Definition of machine complex numbers.

5.14.2 Macro Definition Documentation

5.14.2.1 compf_add

```
#define compf_add(
              d,
              a,
              b )
```

Value:

```
(d)->x = (a)->x + (b)->x; \
(d)->y = (a)->y + (b)->y;
```

Adds a to b and stores the result in d, all of type compf or compf_ptr.

Definition at line 63 of file compf.h.

5.14.2.2 compf_addr

```
#define compf_addr(
              d,
              a,
              r )
```

Value:

```
(d)->x = (a)->x + (r); \
(d)->y = (a)->y;
```

Adds the complex number `a` to the real number `b` and stores the result in `d`.

Definition at line 67 of file compf.h.

5.14.2.3 compf_amr

```
#define compf_amr(
              d,
              a,
              r )
```

Value:

```
(d)->x += (a)->x * (r); \
(d)->y += (a)->y * (r);
```

Adds the complex number `a*r` to `d`, where `d`,a are complex and `r` is real.

Definition at line 87 of file compf.h.

5.14.2.4 compf_div

```
#define compf_div(
              d,
              a,
              b )
```

Value:

```
{ \
coeff_t m2 = compf_mod2(b); \
coeff_t px = ((a)->x * (b)->x + (a)->y * (b)->y) / m2; \
(d)->y = ((a)->y * (b)->x - (a)->x * (b)->y) / m2; \
(d)->x = px;\
}
```

Divides `a` by `b` and stores the result in `d`, all of type compf or compf_ptr.

Definition at line 96 of file compf.h.

5.14.2.5 compf_mod2

```
#define compf_mod2(
              a ) ((a)->x * (a)->x + (a)->y * (a)->y)
```

Computes the square of the modulus of the complex number a.

Warning

There is a danger of overflow, better use the slower compf_mod() instead.

Definition at line 111 of file compf.h.

5.14.2.6 compf_mul

```
#define compf_mul(
              d,
              a,
              b )
```

Value:

```
coeff_t px = (a)->x * (b)->x - (a)->y * (b)->y; \
(d)->y = (a)->x * (b)->y + (a)->y * (b)->x; \
(d)->x = px;
```

Definition at line 78 of file compf.h.

5.14.2.7 compf_mulr

```
#define compf_mulr(
              d,
              a,
              r )
```

Value:

```
(d)->x = (a)->x * (r); \
(d)->y = (a)->y * (r);
```

Multiplies the complex number a to the real number r and stores the result in d.

Definition at line 83 of file compf.h.

5.14.2.8 compf_neg

```
#define compf_neg(
              d,
              a )
```

Value:

```
(d)->x = -(a)->x; \
(d)->y = -(a)->y;
```

Sets `d` to `-a`.

Definition at line 59 of file compf.h.

5.14.2.9 compf_set

```
#define compf_set(
              d,
              a )
```

Value:

```
(d)->x = (a)->x; \
(d)->y = (a)->y;
```

Sets `d` to `a`.

Definition at line 51 of file compf.h.

5.14.2.10 compf_setr

```
#define compf_setr(
              d,
              a )
```

Value:

```
(d)->x = (a); \
(d)->y = 0;
```

Sets `d` to the real value `a`.

Definition at line 55 of file compf.h.

5.14.2.11 compf_sqr

```
#define compf_sqr(
              d,
              a )
```

Value:

```
coeff_t px = (a)->x * (a)->x - (a)->y * (a)->y; \
(d)->y = 2 * (a)->x * (a)->y; \
(d)->x = px;
```

Squares `a` and stores the result in `d`, all of type compf or compf_ptr.

Definition at line 91 of file compf.h.

5.14.2.12 compf_sub

```
#define compf_sub(
                d,
                a,
                b )
```

Value:

```
(d)->x = (a)->x - (b)->x; \
(d)->y = (a)->y - (b)->y;
```

Subtracts `b` from `a` and stores the result in `d`, all of type compf or compf_ptr.

Definition at line 71 of file compf.h.

5.14.2.13 compf_subr

```
#define compf_subr(
                d,
                a,
                r )
```

Value:

```
(d)->x = (a)->x - (r); \
(d)->y = (a)->y;
```

Subtracts the real number `b` from the complex number `a` and stores the result in `d`.

Definition at line 75 of file compf.h.

5.14.3 Typedef Documentation

5.14.3.1 compf

```
typedef compf_struct compf[1]
```

Practical wrapper for `compf_struct`.

To avoid the constant use `*` and `&` the type `compf` is a pointer.

Example of use:

```
compf c;
polyf cx = c->x;
```

Definition at line 43 of file compf.h.

5.15 /home/runner/work/FastPolyEval/FastPolyEval/code/numbers/ntypes.h File Reference

Definition of basic types.

Macros

- #define true 1

  Boolean value true.
- #define false 0

  Boolean value false.
- #define PI (3.14159265358979323846264338327950288L)

  π with fp80 precision
- #define **flog2** log2
- #define **fhypot** hypot
- #define **ffloor** floor
- #define **fpow** pow
- #define **fexp** exp
- #define **fsin** sin
- #define **fcos** cos
- #define **ftan** tan
- #define **mpfr_getf** mpfr_get_d
- #define **precf** 53
- #define **PRECF_STR** "53"
- #define **TYPEFP_STR** "FP64"
- #define **TYPEF_STR** "double"
- #define **INF_M** (-HUGE_VAL)
- #define **INF_P** HUGE_VAL
- #define **FMT_COEFF** "l"
- #define **MAX_EXP** (sizeof(coeff_t) == 8 ? 960 : 16320)
- #define **HUGE_DEGREES**
- #define **MAX_DEG** (UINT64_MAX - 1)
- #define **FMT_DEG** PRIu64
- #define **plog2** log2
- #define **pexp2** exp2
- #define **phypot** hypot
- #define **pfloor** floor
- #define **pceil** ceil
- #define **mpfr_getp** mpfr_get_d
- #define **PEPS** 1E-200
- #define **PDEL** 1E-12
- #define **pexp** exp
- #define **pcos** cos
- #define **psin** sin
- #define **ptan** tan
- #define **pldexp** ldexp
- #define **pfrexp** frexp
- #define **FMT_REAL** "l"
- #define **HUGE_PREC**
- #define **MAX_PREC** (16000000000000000000UL)
- #define **HUGE_MP_EXP**
- #define MAX_MP_EXP (4000000000000000000L)

  The integer number type to use for polynomial degrees and indexes.
- #define **NEWTON_CONV_BITS** 5
- #define **NEWTON_ESCAPE_BITS** 4

Typedefs

- typedef uint8_t byte

  byte is uint8
- typedef uint16_t word

  word is uint16
- typedef uint32_t uint

  uint is uint32
- typedef uint64_t ulong

  ulong is uint64
- typedef byte bool

  Logic type bool can take values true or false.
- typedef double coeff_t

  The machine number type to use for polynomial coefficients and evaluation.
- typedef ulong deg_t

  The integer number type to use for polynomial degrees and indexes.
- typedef double real_t

  The machine number type to use for polynomial analysis and preconditionning.
- typedef ulong prec_t

  The integer number type to use for polynomial degrees and indexes.

Functions

- bool ntypes_check (void)

  Use this function to check the compatibility of the machine with the settings above.
- real_t bits_sum (real_t b1, real_t b2)

  Computes log_2(2^b1+2^b2), even if b1 or b2 are outside the exponent range of real_t.
- real_t nt_err (real_t vb, real_t evb, real_t db, real_t edb)

  Computes log_2(ntErr), where ntErr is an upper bound for the error of the Newton term.

5.15.1 Detailed Description

Definition of basic types.

5.15.2 Function Documentation

5.15.2.1 bits_sum()

```
real_t bits_sum (
            real_t b1,
            real_t b2 )
```

Computes log_2(2^b1+2^b2), even if b1 or b2 are outside the exponent range of real_t.

Parameters

b1	first operand, in bits
b2	second operand, in bits

Returns

the bits sum of the operands, that is the base `2 log` of their base `2` exponentials

5.15.2.2 nt_err()

```
real_t nt_err (
            real_t vb,
            real_t evb,
            real_t db,
            real_t edb )
```

Computes `log_2(ntErr)`, where `ntErr` is an upper bound for the error of the Newton term.

Parameters

vb	`log_2(`|value|`)`
evb	`log_2(valErr)`
db	`log_2(`|derivative|`)`
edb	`log_2(derErr)`

Returns

absolute error of the Newton term, as a power of `2`

5.16 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/poly.h File Reference

Definition of complex polynomials with arbitary precision coefficients.

Data Structures

- struct poly_struct

  Polynomial with multi-precision floating point complex coefficients.

Typedefs

- typedef poly_struct poly_t[1]

  Practical wrapper for `poly_struct`.
- typedef poly_struct * poly

  Convenience pointer to `poly_struct`.

Functions

- poly poly_new (deg_t degree, prec_t prec)

  Returns a new complex polynomial of given `degree`, with coefficients of precision `prec`.
- poly poly_from_roots (comp_ptr roots, deg_t degree, prec_t prec)

  Returns a new complex polynomial given the list of its `roots`, with coefficients of precision `prec`.
- bool poly_free (poly P)

  Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `poly_new()`.
- bool poly_set (poly P, comp coeff, deg_t ind)

  Sets the coefficient of the polynomial `P` corresponding to the power `ind` to `coeff`.
- bool poly_eval (comp res, poly P, comp z)

  Evaluates `P(z)` using Horner's method.
- bool poly_eval_r (comp res, poly P, mpfr_t x)

  Evaluates `P(x)` using Horner's method.
- poly poly_derivative (poly P)

  Computes the derivative of `P`.
- poly poly_sum (poly P, poly Q)

  Computes `P+Q`.
- poly poly_diff (poly P, poly Q)

  Computes `P-Q`.
- poly poly_prod (poly P, poly Q)

  Computes `P*Q`.
- poly poly_sqr (poly P)

  Computes the square of `P`.

5.16.1 Detailed Description

Definition of complex polynomials with arbitary precision coefficients.

5.16.2 Typedef Documentation

5.16.2.1 poly_t

```
typedef poly_struct poly_t[1]
```

Practical wrapper for `poly_struct`.

To avoid the constant use `*` and `&` the type `poly_t` is a pointer.

Definition at line 43 of file poly.h.

5.16.3 Function Documentation

5.16.3.1 poly_derivative()

```
poly poly_derivative (
            poly P )
```

Computes the derivative of `P`.

Parameters

P	the polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.16.3.2 poly_diff()

```
poly poly_diff (
            poly P,
            poly Q )
```

Computes `P-Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.16.3.3 poly_eval()

```
bool poly_eval (
            comp res,
            poly P,
            comp z )
```

Evaluates `P(z)` using Horner's method.

Parameters

res	the result
P	the polynomial
z	the argument

Returns

true if successfull, false otherwise.

5.16.3.4 poly_eval_r()

```
bool poly_eval_r (
            comp res,
            poly P,
            mpfr_t x )
```

Evaluates `P(x)` using Horner's method.

Parameters

res	the result
P	the polynomial
x	the real argument

Returns

true if successfull, false otherwise.

5.16.3.5 poly_free()

```
bool poly_free (
            poly P )
```

Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `poly_new()`.

Parameters

P	the polynomial

Returns

true if successfull, false otherwise.

5.16.3.6 poly_from_roots()

```
poly poly_from_roots (
            comp_ptr roots,
            deg_t degree,
            prec_t prec )
```

Returns a new complex polynomial given the list of its `roots`, with coefficients of precision `prec`.

Warning

`prec` must be at least `precf`

Parameters

roots	the roots of the polynomial
degree	the degree of the polynomial
prec	the precision of the coefficients, in bits

Returns

the new polynomial, `NULL` if some error occurred.

5.16.3.7 poly_new()

```
poly poly_new (
            deg_t degree,
            prec_t prec )
```

Returns a new complex polynomial of given `degree`, with coefficients of precision `prec`.

Warning

`prec` must be at least `precf`

Parameters

degree	the degree of the polynomial
prec	the precision of the coefficients, in bits

Returns

the new polynomial, `NULL` if the degree is larger than `MAX_DEG`.

5.16.3.8 poly_prod()

```
poly poly_prod (
            poly P,
            poly Q )
```

Computes `P*Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.16.3.9 poly_set()

```
bool poly_set (
            poly P,
            comp coeff,
            deg_t ind )
```

Sets the coefficient of the polynomial `P` corresponding to the power `ind` to `coeff`.

Parameters

P	the polynomial
coeff	the coefficient
ind	the index

Returns

true if successfull, false otherwise.

5.16.3.10 poly_sqr()

```
poly poly_sqr (
            poly P )
```

Computes the square of `P`.

Parameters

P	the polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.16.3.11 poly_sum()

```
poly poly_sum (
            poly P,
            poly Q )
```

Computes `P+Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.17 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/polyf.h File Reference

Definition of complex polynomials with machine floating point coefficients.

Data Structures

- struct polyf_struct

  Polynomial with machine floating point complex coefficients.

Typedefs

- typedef polyf_struct polyf_t[1]

  Practical wrapper for `polyf_struct`.
- typedef polyf_struct * polyf

  Convenience pointer to `polyf_struct`.

Functions

- polyf polyf_new (deg_t degree)

  Returns a new complex polynomial of given `degree`, with machine floating point coefficients.
- polyf polyf_from_roots (compf_ptr roots, deg_t degree)

  Returns a new complex polynomial given the list of its `roots`, with machine floating point coefficients.
- bool polyf_free (polyf P)

  Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `polyr_new()`.
- bool polyf_set (polyf P, compf coeff, deg_t ind)

  Sets the coefficient of the polynomial `P` corresponding to the power `ind` to `coeff`.
- bool polyf_eval (compf res, polyf P, compf z)

  Evaluates `P(z)` using Horner's method.
- bool polyf_eval_r (compf res, polyf P, coeff_t x)

  Evaluates `P(x)` using Horner's method.
- polyf polyf_derivative (polyf P)

  Computes the derivative of `P`.
- polyf polyf_sum (polyf P, polyf Q)

  Computes `P+Q`.
- polyf polyf_diff (polyf P, polyf Q)

  Computes `P-Q`.
- polyf polyf_prod (polyf P, polyf Q)

  Computes `P*Q`.
- polyf polyf_sqr (polyf P)

  Computes the square of `P`.

5.17.1 Detailed Description

Definition of complex polynomials with machine floating point coefficients.

5.17.2 Typedef Documentation

5.17.2.1 polyf_t

```
typedef polyf_struct polyf_t[1]
```

Practical wrapper for `polyf_struct`.

To avoid the constant use `*` and `&` the type `polyf_t` is a pointer.

Definition at line 39 of file polyf.h.

5.17.3 Function Documentation

5.17.3.1 polyf_derivative()

```
polyf polyf_derivative (
            polyf P )
```

Computes the derivative of `P`.

Parameters

P	the polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.17.3.2 polyf_diff()

```
polyf polyf_diff (
            polyf P,
            polyf Q )
```

Computes `P-Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.17.3.3 polyf_eval()

```
bool polyf_eval (
            compf res,
            polyf P,
            compf z )
```

Evaluates `P(z)` using Horner's method.

Parameters

res	the result
P	the polynomial
z	the argument

Returns

true if successfull, false otherwise.

5.17.3.4 polyf_eval_r()

```
bool polyf_eval_r (
            compf res,
            polyf P,
            coeff_t x )
```

Evaluates `P(x)` using Horner's method.

Parameters

res	the result
P	the polynomial
x	the real argument

Returns

true if successfull, false otherwise.

5.17.3.5 polyf_free()

```
bool polyf_free (
            polyf P )
```

Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `polyr_new()`.

Parameters

P	the polynomial

Returns

true if successfull, false otherwise.

5.17.3.6 polyf_from_roots()

```
polyf polyf_from_roots (
            compf_ptr roots,
            deg_t degree )
```

Returns a new complex polynomial given the list of its `roots`, with machine floating point coefficients.

Parameters

roots	the roots of the polynomial
degree	the degree of the polynomial

Returns

the new polynomial, `NULL` if some error occurred.

5.17.3.7 polyf_new()

```
polyf polyf_new (
            deg_t degree )
```

Returns a new complex polynomial of given `degree`, with machine floating point coefficients.

Parameters

degree	the degree of the polynomial

Returns

the new polynomial, `NULL` if the degree is larger than `MAX_DEG`.

5.17.3.8 polyf_prod()

```
polyf polyf_prod (
            polyf P,
            polyf Q )
```

Computes `P*Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.17.3.9 polyf_set()

```
bool polyf_set (
            polyf P,
            compf coeff,
            deg_t ind )
```

Sets the coefficient of the polynomial `P` corresponding to the power `ind` to `coeff`.

Parameters

P	the polynomial
coeff	the coefficient
ind	the index

Returns

true if successfull, false otherwise.

5.17.3.10 polyf_sqr()

```
polyf polyf_sqr (
            polyf P )
```

Computes the square of P.

Parameters

P	the polynomial

Returns

the resulted polynomial, NULL if some error occurred.

5.17.3.11 polyf_sum()

```
polyf polyf_sum (
            polyf P,
            polyf Q )
```

Computes P+Q.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, NULL if some error occurred.

5.18 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/polyfr.h File Reference

Definition of real polynomials with machine floating point coefficients.

Data Structures

- struct polyfr_struct

  Polynomial with machine floating point real coefficients.

Typedefs

- typedef polyfr_struct polyfr_t[1]

  Practical wrapper for `polyfr_struct`.
- typedef polyfr_struct * polyfr

  Convenience pointer to `polyfr_struct`.

Functions

- polyfr polyfr_new (deg_t degree)

  Returns a new real polynomial of given `degree`, with machine floating point coefficients.
- bool polyfr_free (polyfr P)

  Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `polyfr_new()`.
- bool polyfr_set (polyfr P, coeff_t coeff, deg_t ind)

  Sets the coefficient corresponding to the power `ind` to `coeff`.
- coeff_t polyfr_get (polyfr P, deg_t ind)

  Returns the coefficient corresponding to the power `ind`.
- bool polyfr_eval_c (compf res, polyfr P, compf z)

  Evaluates `P(z)` using Horner's method.
- coeff_t polyfr_eval (polyfr P, coeff_t x)

  Evaluates `P(x)` using Horner's method.
- polyf polyfr_comp (polyfr P)

  Return a complex version of the real polynomial `P`.
- polyfr polyfr_derivative (polyfr P)

  Computes the derivative of `P`.
- polyfr polyfr_sum (polyfr P, polyfr Q)

  Computes `P+Q`.
- polyfr polyfr_diff (polyfr P, polyfr Q)

  Computes `P-Q`.
- polyfr polyfr_prod (polyfr P, polyfr Q)

  Computes `P*Q`.
- polyfr polyfr_sqr (polyfr P)

  Computes the square of `P`.
- polyfr polyf_hyp (int n)

  Computes the `n-th` hyperbolic polynomial, the `n-th` image of `0` under the iteration of `z->z^2+c`. It is a polynomial of degree `2^{n-1}` in `c`.
- polyfr polyf_cheb (int n)

  Computes the Chebyshev polynomial of degree `n`.
- polyfr polyf_leg (int n)

  Computes the Legendre polynomial of degree `n`.
- polyfr polyf_her (int n)

  Computes the Hermite polynomial of degree `n`.
- polyfr polyf_lag (int n)

  Computes the Laguerre polynomial of degree `n`.

5.18.1 Detailed Description

Definition of real polynomials with machine floating point coefficients.

5.18.2 Typedef Documentation

5.18.2.1 polyfr_t

```
typedef polyfr_struct polyfr_t[1]
```

Practical wrapper for `polyfr_struct`.

To avoid the constant use `*` and `&` the type `polyfr_t` is a pointer.

Definition at line 40 of file polyfr.h.

5.18.3 Function Documentation

5.18.3.1 polyf_cheb()

```
polyfr polyf_cheb (
            int n )
```

Computes the Chebyshev polynomial of degree `n`.

Parameters

n	the degree of the polynomial

Returns

the Chebyshev polynomial, `NULL` if some error occurred.

5.18.3.2 polyf_her()

```
polyfr polyf_her (
            int n )
```

Computes the Hermite polynomial of degree `n`.

Parameters

n	the degree of the polynomial

Returns

the Hermite polynomial, NULL if some error occurred.

5.18.3.3 polyf_hyp()

```
polyfr polyf_hyp (
            int n )
```

Computes the n-th hyperbolic polynomial, the n-th image of 0 under the iteration of z->z^2+c. It is a polynomial of degree 2^{n-1} in c.

Parameters

n	the order of the polynomial

Returns

the hyperbolic polynomial, NULL if some error occurred.

5.18.3.4 polyf_lag()

```
polyfr polyf_lag (
            int n )
```

Computes the Laguerre polynomial of degree n.

Parameters

n	the degree of the polynomial

Returns

the Laguerre polynomial, NULL if some error occurred.

5.18.3.5 polyf_leg()

```
polyfr polyf_leg (
            int n )
```

Computes the Legendre polynomial of degree n.

Parameters

n	the degree of the polynomial

Returns

the Legendre polynomial, `NULL` if some error occurred.

5.18.3.6 polyfr_comp()

```
polyf polyfr_comp (
            polyfr P )
```

Return a complex version of the real polynomial `P`.

Parameters

P	a polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.18.3.7 polyfr_derivative()

```
polyfr polyfr_derivative (
            polyfr P )
```

Computes the derivative of `P`.

Parameters

P	the polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.18.3.8 polyfr_diff()

```
polyfr polyfr_diff (
            polyfr P,
            polyfr Q )
```

Computes `P-Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.18.3.9 polyfr_eval()

```
coeff_t polyfr_eval (
            polyfr P,
            coeff_t x )
```

Evaluates `P(x)` using Horner's method.

Parameters

P	the polynomial
x	the argument

Returns

the result, `NaN` if some error occurred.

5.18.3.10 polyfr_eval_c()

```
bool polyfr_eval_c (
            compf res,
            polyfr P,
            compf z )
```

Evaluates `P(z)` using Horner's method.

Parameters

res	the result
P	the polynomial
z	the argument

Returns

true if successfull, false otherwise.

5.18.3.11 polyfr_free()

```
bool polyfr_free (
            polyfr P )
```

Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `polyfr_new()`.

Parameters

P	the polynomial

Returns

true if successfull, false otherwise.

5.18.3.12 polyfr_get()

```
coeff_t polyfr_get (
            polyfr P,
            deg_t ind )
```

Returns the coefficient corresponding to the power `ind`.

Parameters

P	the polynomial
ind	the index

Returns

the coefficient corresponding to the power `ind`.

5.18.3.13 polyfr_new()

```
polyfr polyfr_new (
            deg_t degree )
```

Returns a new real polynomial of given `degree`, with machine floating point coefficients.

Parameters

degree	the degree of the polynomial

Returns

the new polynomial, `NULL` if the degree is larger than `MAX_DEG`.

5.18.3.14 polyfr_prod()

```
polyfr polyfr_prod (
            polyfr P,
            polyfr Q )
```

Computes `P*Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.18.3.15 polyfr_set()

```
bool polyfr_set (
            polyfr P,
            coeff_t coeff,
            deg_t ind )
```

Sets the coefficient corresponding to the power `ind` to `coeff`.

Parameters

P	the polynomial
coeff	the coefficient
ind	the index

Returns

true if successfull, false otherwise.

5.18.3.16 polyfr_sqr()

```
polyfr polyfr_sqr (
            polyfr P )
```

Computes the square of P.

Parameters

P	the polynomial

Returns

the resulted polynomial, NULL if some error occurred.

5.18.3.17 polyfr_sum()

```
polyfr polyfr_sum (
            polyfr P,
            polyfr Q )
```

Computes P+Q.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, NULL if some error occurred.

5.19 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/polyr.h File Reference

Definition of real polynomials with arbitary precision coefficients.

Data Structures

- struct polyr_struct

  Polynomial with multi-precision floating point complex coefficients.

Typedefs

- typedef polyr_struct polyr_t[1]

  Practical wrapper for `polyr_struct`.
- typedef polyr_struct * polyr

  Convenience pointer to `polyr_struct`.

Functions

- polyr polyr_new (deg_t degree, prec_t prec)

  Returns a new real polynomial of given `degree`*, with coefficients of precision* `prec`.
- bool polyr_free (polyr P)

  Frees all the memory used by the polynomial `P`*, assuming the struct has been allocated with* `malloc()`*, for example with* `polyr_new()`.
- bool polyr_set (polyr P, mpfr_t coeff, deg_t ind)

  Sets the coefficient of the polynomial `P` *corresponding to the power* `ind` *to* `coeff`.
- bool polyr_seti (polyr P, long coeff, deg_t ind)

  Sets the coefficient of the polynomial `P` *corresponding to the power* `ind` *to* `coeff`.
- bool polyr_eval_c (comp res, polyr P, comp z)

  Evaluates `P(z)` *using Horner's method.*
- bool polyr_eval (mpfr_t res, polyr P, mpfr_t x)

  Evaluates `P(x)` *using Horner's method.*
- polyr polyr_derivative (polyr P)

  Computes the derivative of `P`.
- polyr polyr_sum (polyr P, polyr Q)

  Computes `P+Q`.
- polyr polyr_diff (polyr P, polyr Q)

  Computes `P-Q`.
- polyr polyr_prod (polyr P, polyr Q)

  Computes `P*Q`.
- polyr polyr_sqr (polyr P)

  Computes the square of `P`.
- polyr poly_hyp (int n, prec_t prec)

  Computes the `n-th` *hyperbolic polynomial, the* `n-th` *image of* `0` *under the iteration of* `z->z^2+c`*. It is a polynomial of degree* `2^{n-1}` *in* `c`.
- polyr poly_cheb (int n, prec_t prec)

  Computes the Chebyshev polynomial of degree `n`.
- polyr poly_leg (int n, prec_t prec)

  Computes the Legendre polynomial of degree `n`.
- polyr poly_her (int n, prec_t prec)

  Computes the Hermite polynomial of degree `n`.
- polyr poly_lag (int n, prec_t prec)

  Computes the Laguerre polynomial of degree `n`.

5.19.1 Detailed Description

Definition of real polynomials with arbitary precision coefficients.

5.19.2 Typedef Documentation

5.19.2.1 polyr_t

```
typedef polyr_struct polyr_t[1]
```

Practical wrapper for `polyr_struct`.

To avoid the constant use `*` and `&` the type `polyr_t` is a pointer.

Definition at line 43 of file polyr.h.

5.19.3 Function Documentation

5.19.3.1 poly_cheb()

```
polyr poly_cheb (
            int n,
            prec_t prec )
```

Computes the Chebyshev polynomial of degree `n`.

Parameters

n	the degree of the polynomial
prec	the precision of the coefficients

Returns

the Chebyshev polynomial, `NULL` if some error occurred.

5.19.3.2 poly_her()

```
polyr poly_her (
            int n,
            prec_t prec )
```

Computes the Hermite polynomial of degree `n`.

Parameters

n	the degree of the polynomial
prec	the precision of the coefficients

Returns

the Hermite polynomial, `NULL` if some error occurred.

5.19.3.3 poly_hyp()

```
polyr poly_hyp (
            int n,
            prec_t prec )
```

Computes the `n-th` hyperbolic polynomial, the `n-th` image of `0` under the iteration of `z->z^2+c`. It is a polynomial of degree `2^{n-1}` in `c`.

Parameters

n	the order of the polynomial
prec	the precision of the coefficients

Returns

the hyperbolic polynomial, `NULL` if some error occurred.

5.19.3.4 poly_lag()

```
polyr poly_lag (
            int n,
            prec_t prec )
```

Computes the Laguerre polynomial of degree `n`.

Parameters

n	the degree of the polynomial
prec	the precision of the coefficients

Returns

the Laguerre polynomial, `NULL` if some error occurred.

5.19.3.5 poly_leg()

```
polyr poly_leg (
            int n,
            prec_t prec )
```

Computes the Legendre polynomial of degree `n`.

Parameters

n	the degree of the polynomial
prec	the precision of the coefficients

Returns

the Legendre polynomial, `NULL` if some error occurred.

5.19.3.6 polyr_derivative()

```
polyr polyr_derivative (
            polyr P )
```

Computes the derivative of `P`.

Parameters

P	the polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.19.3.7 polyr_diff()

```
polyr polyr_diff (
            polyr P,
            polyr Q )
```

Computes `P-Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.19.3.8 polyr_eval()

```
bool polyr_eval (
            mpfr_t res,
            polyr P,
            mpfr_t x )
```

Evaluates `P(x)` using Horner's method.

Parameters

res	the result
P	the polynomial
x	the real argument

Returns

true if successfull, false otherwise.

5.19.3.9 polyr_eval_c()

```
bool polyr_eval_c (
            comp res,
            polyr P,
            comp z )
```

Evaluates `P(z)` using Horner's method.

Parameters

res	the result
P	the polynomial
z	the argument

Returns

true if successfull, false otherwise.

5.19.3.10 polyr_free()

```
bool polyr_free (
            polyr P )
```

Frees all the memory used by the polynomial `P`, assuming the struct has been allocated with `malloc()`, for example with `polyr_new()`.

Parameters

P	the polynomial

Returns

true if successfull, false otherwise.

5.19.3.11 polyr_new()

```
polyr polyr_new (
            deg_t degree,
            prec_t prec )
```

Returns a new real polynomial of given `degree`, with coefficients of precision `prec`.

Warning

`prec` must be at least `precf` and the degree at most `MAX_DEG`.

Parameters

degree	the degree of the polynomial
prec	the precision of the coefficients, in bits

Returns

the new buffer, `NULL` if some error occurred.

5.19.3.12 polyr_prod()

```
polyr polyr_prod (
            polyr P,
            polyr Q )
```

Computes `P*Q`.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, `NULL` if some error occurred.

5.19.3.13 polyr_set()

```
bool polyr_set (
            polyr P,
            mpfr_t coeff,
            deg_t ind )
```

Sets the coefficient of the polynomial `P` corresponding to the power `ind` to `coeff`.

Parameters

P	the polynomial
coeff	the coefficient
ind	the index

Returns

true if successfull, false otherwise.

5.19.3.14 polyr_seti()

```
bool polyr_seti (
            polyr P,
            long coeff,
            deg_t ind )
```

Sets the coefficient of the polynomial `P` corresponding to the power `ind` to `coeff`.

Parameters

P	the polynomial
coeff	the coefficient
ind	the index

Returns

true if successfull, false otherwise.

5.19.3.15 polyr_sqr()

```
polyr polyr_sqr (
            polyr P )
```

Computes the square of P.

Parameters

P	the polynomial

Returns

the resulted polynomial, NULL if some error occurred.

5.19.3.16 polyr_sum()

```
polyr polyr_sum (
            polyr P,
            polyr Q )
```

Computes P+Q.

Parameters

P	a polynomial
Q	another polynomial

Returns

the resulted polynomial, NULL if some error occurred.

5.20 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/array.h File Reference

Definition of a variable length array of arbitary precision complex numbers that are based on mpfr.

Data Structures

- struct array_struct

  A variable length array of machine floating point complex numbers.

Macros

- #define **ARRAY_MIN_SIZE** 100
- #define **ARRAY_SIZE_INCREASE** 1.25

Typedefs

- typedef array_struct array_t[1]

  Practical wrapper for `array_struct`.
- typedef array_struct * array

  Convenience pointer to `array_struct`.

Functions

- array array_new (ulong size)

  Returns a new empty array with memory size at least `size`.
- array array_new_polyr (polyr P, prec_t prec)

  Returns the array of coefficients of the real polynomial `P`.
- array array_new_poly (poly P, prec_t prec)

  Returns the array of coefficients of the polynomial `P`.
- bool array_free (array l)

  Frees all the memory used by the array `l`, assuming the struct has been allocated with `malloc()`, for example with `array_new()`.
- bool array_add (array l, comp z, prec_t prec)

  Adds the complex number `z` at the end of the array. The size of the array is automatically increased, if needed.
- comp_ptr array_get (array l, ulong pos)

  Returns the pointer of the element on position `pos` in the array `l`.
- bool array_is_real (array l)

  Checks if all complex numbers in the array `l` are real.
- long array_first_inf (array l)

  Checks if there are infinite values in the list `l`.
- long array_first_nan (array l)

  Checks if all complex numbers in the list `l` are well defined.
- polyr array_polyr (array l, prec_t prec)

  Returns the real polynomial with the coefficients the real parts of the complex numbers in the array `l`.
- poly array_poly (array l, prec_t prec)

  Returns the polynomial with the coefficients in the array `l`.
- bool array_write (array l, char *fileName, int digits, bool verbose)

  Writes the array `l` to a CSV file with the given path `fileName`.
- bool array_append (array l, char *fileName, int digits, bool verbose)

  Writes the array `l` to the end of a CSV file with the given path `fileName`.
- array array_read (char *fileName, prec_t prec, bool verbose)

  Reads a array of complex numbers of precision `prec` from the CSV file with path `fileName`.

5.20.1 Detailed Description

Definition of a variable length array of arbitary precision complex numbers that are based on `mpfr`.

5.20.2 Typedef Documentation

5.20.2.1 array_t

```
typedef array_struct array_t[1]
```

Practical wrapper for `array_struct`.

To avoid the constant use `*` and `&` the type `array_t` is a pointer.

Definition at line 46 of file array.h.

5.20.3 Function Documentation

5.20.3.1 array_add()

```
bool array_add (
            array l,
            comp z,
            prec_t prec )
```

Adds the complex number `z` at the end of the array. The size of the array is automatically increased, if needed.

Parameters

l	the array
z	the new element to add to the array
prec	the precision of the number in the array

Returns

true if successfull, false otherwise.

5.20.3.2 array_append()

```
bool array_append (
            array l,
            char * fileName,
            int digits,
            bool verbose )
```

Writes the array `l` to the end of a CSV file with the given path `fileName`.

Parameters

l	the array
fileName	the path of the CSV file
digits	the number of digits after the decimal point of the numbers in the file
verbose	true to print information about the error, if any

Returns

true if successfull, false otherwise.

5.20.3.3 array_first_inf()

```
long array_first_inf (
            array l )
```

Checks if there are infinite values in the list `l`.

Parameters

l	the list

Returns

the position of the first infinite value in `l`, `-1` if there is none, LONG_MAX if some error occurred.

5.20.3.4 array_first_nan()

```
long array_first_nan (
            array l )
```

Checks if all complex numbers in the list `l` are well defined.

Parameters

l	the list

Returns

the position of the first undefined value in `l`, `-1` if there is none, LONG_MAX if some error occurred.

5.20.3.5 array_free()

```
bool array_free (
            array l )
```

Frees all the memory used by the array `l`, assuming the struct has been allocated with `malloc()`, for example with `array_new()`.

Parameters

l	the array

Returns

true if successfull, false otherwise.

5.20.3.6 array_get()

```
comp_ptr array_get (
            array l,
            ulong pos )
```

Returns the pointer of the element on position `pos` in the array `l`.

Parameters

l	the array
pos	the position of the element

Returns

the pointer to the element on position `pos` in `l`, `NULL` if some error occurred.

5.20.3.7 array_is_real()

```
bool array_is_real (
            array l )
```

Checks if all complex numbers in the array `l` are real.

Parameters

l	the array

Returns

true if all elements in the array are real, false otherwise.

5.20.3.8 array_new()

```
array array_new (
            ulong size )
```

Returns a new empty array with memory size at least `size`.

Parameters

size	the number of elements to allocate memory for

Returns

the array, `NULL` if not enougn memory is available

5.20.3.9 array_new_poly()

```
array array_new_poly (
            poly P,
            prec_t prec )
```

Returns the array of coefficients of the polynomial `P`.

Parameters

P	the polynomial
prec	the precision of the numbers in the array

Returns

the array, `NULL` if some error occurred.

5.20.3.10 array_new_polyr()

```
array array_new_polyr (
            polyr P,
            prec_t prec )
```

Returns the array of coefficients of the real polynomial `P`.

Parameters

P	the real polynomial
prec	the precision of the numbers in the array

Returns

the array, `NULL` if some error occurred.

5.20.3.11 array_poly()

```
poly array_poly (
            array l,
            prec_t prec )
```

Returns the polynomial with the coefficients in the array `l`.

Parameters

l	the array
prec	the precision of the coefiicients of the polynomial

Returns

the polynomial, `NULL` if some error occurred.

5.20.3.12 array_polyr()

```
polyr array_polyr (
            array l,
            prec_t prec )
```

Returns the real polynomial with the coefficients the real parts of the complex numbers in the array `l`.

Parameters

l	the array
prec	the precision of the coefiicients of the polynomial

Returns

the polynomial, `NULL` if some coefficients are not real or some other error occurred.

5.20.3.13 array_read()

```
array array_read (
            char * fileName,
            prec_t prec,
            bool verbose )
```

Reads a array of complex numbers of precision `prec` from the CSV file with path `fileName`.

Parameters

fileName	the path of the CSV file
prec	the precision
verbose	true to print information about the file and the error, if any

Returns

the array of complex numbers in the CSV file, `NULL` if some error occurred.

5.20.3.14 array_write()

```
bool array_write (
            array l,
            char * fileName,
            int digits,
            bool verbose )
```

Writes the array `l` to a CSV file with the given path `fileName`.

Parameters

l	the array
fileName	the path of the CSV file
digits	the number of digits after the decimal point of the numbers in the file
verbose	true to print information about the error, if any

Returns

true if successfull, false otherwise.

5.21 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/arrayf.h File Reference

Definition of a variable length array of machine floating point complex numbers.

Data Structures

- struct arrayf_struct

  A variable length list of machine floating point complex numbers.

Macros

- #define **LISTF_MIN_SIZE** 100
- #define **LISTF_SIZE_INCREASE** 1.25

Typedefs

- typedef arrayf_struct arrayf_t[1]

  Practical wrapper for `arrayf_struct`.
- typedef arrayf_struct * arrayf

  Convenience pointer to `arrayf_struct`.

Functions

- arrayf arrayf_new (ulong size)

  Returns a new empty list with memory size at least `size`.
- arrayf arrayf_new_polyfr (polyfr P)

  Returns the list of coefficients of the real polynomial `P`.
- arrayf arrayf_new_polyf (polyf P)

  Returns the list of coefficients of the polynomial `P`.
- bool arrayf_free (arrayf l)

  Frees all the memory used by the list `l`, assuming the struct has been allocated with `malloc()`, for example with `list_new()`.
- bool arrayf_add (arrayf l, compf z)

  Adds the complex number `z` at the end of the list. The size of the list is automatically increased, if needed.
- compf_ptr arrayf_get (arrayf l, ulong pos)

  Returns the pointer of the element on position `pos` in the list `l`.
- bool arrayf_is_real (arrayf l)

  Checks if all complex numbers in the list `l` are real.
- long arrayf_first_inf (arrayf l)

  Checks if there are infinite values in the list `l`.
- long arrayf_first_nan (arrayf l)

  Checks if all complex numbers in the list `l` are well defined.
- polyfr arrayf_polyfr (arrayf l)

  Returns the real polynomial with the coefficients the real parts of the complex numbers in the list `l`.
- polyf arrayf_polyf (arrayf l)

  Returns the polynomial with the coefficients in the list `l`.
- bool arrayf_write (arrayf l, char *fileName, bool verbose)

  Writes the list `l` to a CSV file with the given path `fileName`.
- bool arrayf_append (arrayf l, char *fileName, bool verbose)

  Writes the list `l` to the end of a CSV file with the given path `fileName`.
- arrayf arrayf_read (char *fileName, bool verbose)

  Reads a list of complex numbers from the CSV file with path `fileName`.

5.21.1 Detailed Description

Definition of a variable length array of machine floating point complex numbers.

5.21.2 Typedef Documentation

5.21.2.1 arrayf_t

```
typedef arrayf_struct arrayf_t[1]
```

Practical wrapper for `arrayf_struct`.

To avoid the constant use `*` and `&` the type `arrayf_t` is a pointer.

Definition at line 47 of file arrayf.h.

5.21.3 Function Documentation

5.21.3.1 arrayf_add()

```
bool arrayf_add (
            arrayf l,
            compf z )
```

Adds the complex number `z` at the end of the list. The size of the list is automatically increased, if needed.

Parameters

l	the list
z	the new element to add to the list

Returns

true if successfull, false otherwise.

5.21.3.2 arrayf_append()

```
bool arrayf_append (
            arrayf l,
```

```
            char * fileName,
            bool verbose )
```

Writes the list `l` to the end of a CSV file with the given path `fileName`.

Parameters

l	the list
fileName	the path of the CSV file
verbose	true to print information about the error, if any

Returns

true if successfull, false otherwise.

5.21.3.3 arrayf_first_inf()

```
long arrayf_first_inf (
            arrayf l )
```

Checks if there are infinite values in the list `l`.

Parameters

l	the list

Returns

the position of the first infinite value in `l`, `-1` if there is none, LONG_MAX if some error occurred.

5.21.3.4 arrayf_first_nan()

```
long arrayf_first_nan (
            arrayf l )
```

Checks if all complex numbers in the list `l` are well defined.

Parameters

l	the list

Returns

the position of the first undefined value in `l`, `-1` if there is none, LONG_MAX if some error occurred.

5.21.3.5 arrayf_free()

```
bool arrayf_free (
            arrayf l )
```

Frees all the memory used by the list `l`, assuming the struct has been allocated with `malloc()`, for example with `list_new()`.

Parameters

l	the list

Returns

true if successfull, false otherwise.

5.21.3.6 arrayf_get()

```
compf_ptr arrayf_get (
            arrayf l,
            ulong pos )
```

Returns the pointer of the element on position `pos` in the list `l`.

Parameters

l	the list
pos	the position of the element

Returns

the pointer to the element on position `pos` in `l`, `NULL` if some error occurred.

5.21.3.7 arrayf_is_real()

```
bool arrayf_is_real (
            arrayf l )
```

Checks if all complex numbers in the list `l` are real.

Parameters

l	the list

Returns

true if all elements in the list are real, false otherwise.

5.21.3.8 arrayf_new()

```
arrayf arrayf_new (
            ulong size )
```

Returns a new empty list with memory size at least `size`.

Parameters

size	the number of elements to allocate memory for

Returns

the list, `NULL` if not enougn memory is available

5.21.3.9 arrayf_new_polyf()

```
arrayf arrayf_new_polyf (
            polyf P )
```

Returns the list of coefficients of the polynomial `P`.

Parameters

P	the polynomial

Returns

the list, `NULL` if some error occurred.

5.21.3.10 arrayf_new_polyfr()

```
arrayf arrayf_new_polyfr (
            polyfr P )
```

Returns the list of coefficients of the real polynomial `P`.

Parameters

P	the real polynomial

Returns

the list, `NULL` if some error occurred.

5.21.3.11 arrayf_polyf()

```
polyf arrayf_polyf (
            arrayf l )
```

Returns the polynomial with the coefficients in the list `l`.

Parameters

l	the list

Returns

the polynomial, `NULL` if some error occurred.

5.21.3.12 arrayf_polyfr()

```
polyfr arrayf_polyfr (
            arrayf l )
```

Returns the real polynomial with the coefficients the real parts of the complex numbers in the list `l`.

Parameters

l	the list

Returns

the polynomial, `NULL` if some coefficients are not real or some other error occurred.

5.21.3.13 arrayf_read()

```
arrayf arrayf_read (
            char * fileName,
            bool verbose )
```

Reads a list of complex numbers from the CSV file with path `fileName`.

Parameters

fileName	the path of the CSV file
verbose	true to print information about the file and the error, if any

Returns

the list of complex numbers in the CSV file, `NULL` if some error occurred.

5.21.3.14 arrayf_write()

```
bool arrayf_write (
            arrayf l,
            char * fileName,
            bool verbose )
```

Writes the list `l` to a CSV file with the given path `fileName`.

Parameters

l	the list
fileName	the path of the CSV file
verbose	true to print information about the error, if any

Returns

true if successfull, false otherwise.

5.22 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/chrono.h File Reference

Tools for precise time measuring.

Macros

- #define BILLION 1000000000L

  One billion (nanoseconds in one second).
- #define MILLION 1000000L

  One billion (miliseconds in one second).
- #define MINUTE 60000L

  Miliseconds in one minute.
- #define HOUR (60 * MINUTE)

Miliseconds in one hour.

- #define DAY (24 ∗ HOUR)

  Miliseconds in one day.

- #define USED_CLOCK CLOCK_MONOTONIC

  The ID of the system clock to use.

Typedefs

- typedef struct timespec ptime

  Short type name for precise time.

Functions

- void millis (long ms, char ∗str)

  Formats the time duration in miliseconds `ms` *into human readable string* `str`*.*

- void nanos (long ns, char ∗str)

  Formats the time duration in nanoseconds `ns` *into human readable string* `str`*.*

- ulong lap (ptime ∗ts, char ∗str)

  Computes and prints the time lapse since `ts`*.*

- void print_time_res (void)

  Prints the timer resolution.

5.22.1 Detailed Description

Tools for precise time measuring.

5.22.2 Function Documentation

5.22.2.1 lap()

```
ulong lap (
            ptime * ts,
            char * str )
```

Computes and prints the time lapse since `ts`.

Pretty prints the elapsed time into the string `str` and updates `ts` to the current time. Does not fail if `str==NULL`, can also be used as a starter for the chronometer.

Warning

The string `str` should be at least `90` bytes long.

Parameters

ts	old time stamp
str	human readable string for the time increment

Returns

the total time in nanos

5.22.2.2 millis()

```
void millis (
            long ms,
            char * str )
```

Formats the time duration in miliseconds `ms` into human readable string `str`.

Warning

The string `str` should be at least `90` bytes long.

Parameters

ms	the time lapse in miliseconds
str	the human readable print

5.22.2.3 nanos()

```
void nanos (
            long ns,
            char * str )
```

Formats the time duration in nanoseconds `ns` into human readable string `str`.

Warning

The string `str` should be at least `90` bytes long.

Parameters

ns	the time lapse in miliseconds
str	the human readable print

5.23 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/debug.h File Reference

A few basic tool for easy debug when usinf MPFR.

Functions

- char * pm (mpfr_t x, int dig)

  Return a string containing the value of `x` with `dig` digits.
- char * pc (comp z, int dig)

  Return a string containing the value of `x` with `dig` digits.
- char * pcf (compf z)

  Return a string containing the value of `z`.

5.23.1 Detailed Description

A few basic tool for easy debug when usinf MPFR.

5.23.2 Function Documentation

5.23.2.1 pc()

```
char* pc (
            comp z,
            int dig )
```

Return a string containing the value of `x` with `dig` digits.

The format is that of a CSV file line, the real and imaginary components are separated by a comma.

Warning

The user is responsible to free the memory containg the results.

Parameters

z	a complex number, with MPFR real and imaginary parts
dig	the number of digits to print

Returns

the string containing the value of `z`, `NULL` if some error occurred

5.23.2.2 pcf()

```
char* pcf (
            compf z )
```

Return a string containing the value of `z`.

The format is that of a CSV file line, the real and imaginary components are separated by a comma.

Warning

The user is responsible to free the memory containg the results.

Parameters

z	a complex number, with machine numbers real and imaginary parts

Returns

the string containing the value of `z`, `NULL` if some error occurred

5.23.2.3 pm()

```
char* pm (
            mpfr_t x,
            int dig )
```

Return a string containing the value of `x` with `dig` digits.

Warning

The user is responsible to free the memory containg the results.

Parameters

x	a real number, MPFR
dig	the number of digits to print

Returns

the string containing the value of `z`, `NULL` if some error occurred