FastPolyEval

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## **Chapter 1**

# **Fast Evaluation of Real and Complex Polynomials**

This documentation is availlable online at https://fvigneron.github.io/FastPolyEval. It also exists in PDF form: FastPolyEval\_doc.pdf. The source code can be found on GitHub.

#### 1.1 Abstract

FastPolyEval is a library, written in C, that aims at evaluating polynomials very efficiently, without compromising the accuracy of the result. It is based on the FPE algorithm (Fast Polynomial Evaluator) introduced in reference [1] (see Section References, Contacts and Copyright).

In FastPolyEval, the computations are done for real or complex numbers, in floating point arithmetic, with a fixed precision, which can be one of the machine types FP32, FP64, FP80 or an arbitrary precision based on MPFR.

Evaluations are performed on arbitrary (finite...) sets of points in the complex plane or along the real line, without geometrical constraints.

The average speed-up achieved by  ${\tt FastPolyEval}$  over H\"orner's scheme is illustrated on Figure 1.

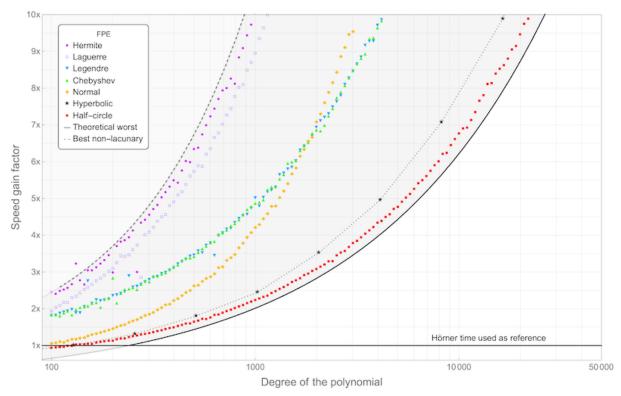


Figure 1.1 Speed gain of FastPolyEval versus Hörner for O(d) evaluations in precision p=53 MPFR.

## 1.2 Complexity & accuracy

 ${\tt FastPolyEval} \ \ \textbf{splits} \ \ \textbf{the evaluation process in two phases:}$ 

- A first phase, called **pre-processing**, analyses the coefficients of the polynomial (actually only the exponents) and determines an evaluator, based on a parcimonious representation of the polynomial.
- Subsequently, the **evaluator** is applied to each of the requested evaluation points. A second reduction is performed. Then the final result is computed.

The complexity of the pre-processing phase is bounded by  $O(d \log d)$  where d is the degree of the polynomial P(z). It is independent of the precision used to express the coefficients or requested for the rest of the computations. The FastPolyEval library is backed by theoretical results that guaranty that the average arithmetic complexity of the final evaluator is of order

 $O\left(\sqrt{d(p+\log d)}\right)$ 

where p is the precision of the computation, in bits. The averaging process corresponds to evaluation points z uniformly distributed either on the Riemann sphere or on the unit disk of the complex plane. The worst complexity of the evaluator does not exceed that of Hörner, i.e. O(d), and can drop as low as  $O(\log^2 d)$  in some favorable cases (see Figure 1 in Abstract).

The memory requirement of FastPolyEval is minimal. To handle a polynomial of degre d with p bits of precision, the memory requirement is O(dp). An additional memory O(kp) is required to perform k evaluations in one call.

Regarding accuracy, the theory guaranties that the relative error between the exact value of P(z) and the computed value does not exced  $2^{-p-c-1}$  where c is the number of cancelled leading bits, i.e.

$$c = \begin{cases} 0 & \text{if } |P(z)| \geq M(z), \\ \left\lfloor \log_2 |M(z)| \right\rfloor - \left\lfloor \log_2 |P(z)| \right\rfloor & \text{else,} \end{cases}$$

where  $M(z) = \max |a_j z^j|$  is the maximum modulus of the monomials of P(z) and  $\lfloor \cdot \rfloor$  is the floor function.

Note

The geometric preprocessing uses only the exponents of the coefficients, which is a significantly smaller amount of data to process than reading all the bits of the coefficients. For a high-precision high-degree evaluation at a **single** point, FastPolyEval can often outperform Hörner. The preprocessing of the exponents followed by the evaluation with a high precision of a parcimonious representation of the polynomial is more efficient than handling indiscriminately all the coefficients. This fact does not contradict that Hörner is a theoretical best for one single evaluation. Hörner has the best estimate on complexity that holds for **any** evaluation point. The advantage of FastPolyEval can be substantial, but it holds **on average**. Note that the worst case for the evaluator (no coefficient dropped) has the same complexity as Hörner. However, in that case, one can prove that the average complexity is much better, typicaly  $O(\log^2 d)$ .

For further details, precise statements and proofs, please see reference [1] in section References, Contacts and Copyright.

## 1.3 Description of the Fast Polynomial Evaluator (FPE) algorithm

In this section, we describe briefly the mathematical principles at the foundation of FastPolyEval.

## 1.3.1 General principles

FastPolyEval relies on two general principles.

- 1. **Lazy evaluation** in finite precision. When adding two floating points numbers with p bits, one can simply discard the smaller one if the orders of magnitude are so far apart that the leading bit of the smaller number cannot affect the bit in the last position of the larger number. When evaluating a polynomial of large degree, the orders of magnitude of the monomials tends to be extremely varied, which is a strong incentive to use lazy evaluations.
- 2. **Geometric selection principle**. For a given evaluation point, evaluating each monomial and sorting them in decreasing order of magnitude would be a very inefficient way of implementing lazy additions. Instead, FastPolyEval can identify the leading monomials using a simple geometric method that allows us to factor most of the work in a pre-processing phase, which is only needed once. At each evaluation point, a subsequent reduction produces a very parcimonious representation of the polynomial (see Figure 2).

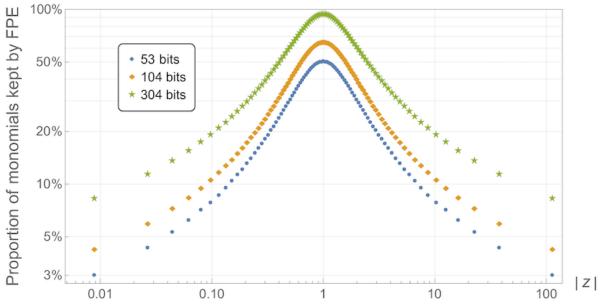


Figure 1.2 Parsimony of the representation used by FastPolyEval to evaluate a polynomial of degree 1000 (half-circle family).

## 1.3.2 Geometric selection principle

For a given polynomial P of degree d, one represents the modulus of the coefficients  $a_j$  in logarithmic coordinates, that is the scatter plot  $E_P$  of  $\log_2 |a_j|$  in function of  $j \in \{0,1,\ldots,d\}$ . One then computes the concave envelope  $\hat{E}_P$  of  $E_P$  (obviously piecewise linear) and one identifies the strip  $S_\delta(\hat{E}_P)$  situated below  $\hat{E}_P$  and of vertical thickness

$$\delta = p + |\log_2 d| + 4.$$

Note that the thickness of this strip is mostly driven by the precision p (in bits) that will be used to evaluate P. On Figure 3, the blue points represent  $E_P$ , the cyan line is  $\hat{E}_P$  and the strip  $S_\delta$  is colored in light pink.

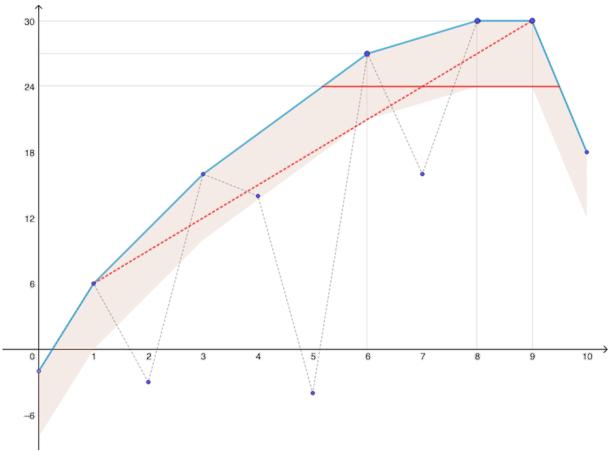


Figure 1.3 Concave cover of the oefficients of a polynomial (log-scale) and selection principle for a given precision.

The coefficients of P that lie in the strip  $S_{\delta}$  are pertinent for an evaluation with precision p. The others can safely be discarded because they will never be used at this precision.

## 1.3.3 Parcimonious representation at an arbitrary point

For a given  $z \in \mathbb{C}$ , a parcimonious representation of  $P(z) = \sum_{j=0}^d a_j z^j$  is obtained by selecting a proper subset of the indices  $J_p(z) \subset \{0,1,\ldots,d\}$  and discarding the other monomials:

$$Q_p(z) = \sum_{j \in J_p(z)} a_j z^j.$$

For computations with a precision of p bits, the values of  $Q_p(z)$  and P(z) are equivalent because the relative error does not exceed  $2^{-p-c-1}$  where c is the number of cancelled leading bits (defined in Section Complexity & accuracy).

The subset  $J_p(z)$  is obtained as a subset of the (indices of the) coefficients that respect the two following criteria in the logarithmic representation (see Figure 3):

- 1. the coefficient belongs to the strip  $S_{\delta}$ ,
- 2. the coefficient is above the longest segment of slope  $\tan \theta = -\log_2 |z|$  contained in  $S_\delta$ .

The selecting segment is always tangent to the lower edge of  $S_\delta$  or, in case of ambiguity (e.g. if  $S_\delta$  is a parallelogram), it is required to be. For |z|=1, the selecting segment is an horizontal line illustrated in solid red in Figure 3 above. The red dashed line corresponds to some value |z|<1. Figure 4 illustrates how the selection principle at an arbitrary point  $z\in\mathbb{C}$  can be transposed from the analysis performed on the raw coefficients, i.e. for |z|=1. In log-coordinates, one has indeed:  $\log_2\left(|a_jz^j|\right)=\log_2|a_j|-j\tan\theta$ . Selecting the coefficients such that  $\log_2\left(|a_jz^j|\right)$  differs from its maximum value by less than  $\delta$  (solid red in Figure 4) is equivalent to selecting those above the segment of slope  $\tan\theta$  in the original configuration (dashed line in Figure 3).

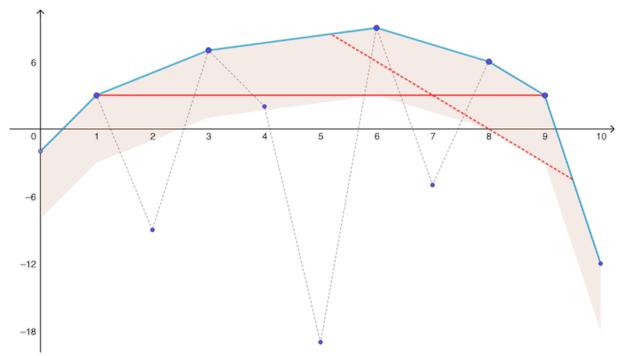


Figure 1.4 Transposition of the selection principle at an arbitrary evaluation point

## 1.3.4 Implementation of the algorithm

FastPolyEval computes Figure 3 and the strip  $S_\delta$  in the pre-processing phase and keeps only the subset of the coefficients that belong to that strip (the so-called "good" set  $G_p$  in <code>reference [1]</code>). In the evaluation phase, the subset of coefficients is thinned to  $J_p(z)$  for each evaluation point z using the 2nd criterion, thus providing the parcimonious representation  $Q_p(z)$  of P(z) at that point. The value of the polynomial is then computed using Hörner's method for  $Q_p$ . Theoretical results guaranty that, on average, the number of coefficients kept in  $J_p(z)$  is only of order  $\sqrt{d\delta}$ , which explains why the complexity of <code>FastPolyEval</code> is so advantageous.

For further details, see reference [1] in Section References, Contacts and Copyright.

## 1.4 Installation of FastPolyEval

FastPolyEval is distributed as source code, written in the C language. The source code can be downloaded from our public github repository.

#### 1.4.1 Prerequisites

First of all, don't panic, it's easy...

Obvioulsy, you will need a computer and a C compiler, for example GCC, though any other C compiler will be fine.

FastPolyEval relies on MPFR to handle floating point numbers with arbitrary precision. You need to install this library on your system if it is not already installed. Please follow the MPFR installation instructions to do so. Note that MPFR has one main depency, GMP, which will also need to be installed (see the GMP installation instructions). If you do not have admin privileges on your machine, you can still build those libraries in a local directory and instruct your compiler to look for the appropriate library path. For example, if you use GCC, see the documentation of option -L.

Note that on most OS, one can also install those libraries through a package manager (see Additional help for Linux, MacOS, Windows

Note

The libraries GMP and MPFR are **free** to download and use and are distributed under the Lesser General Public License, which enables developers of non-free programs to use GMP/MPFR in their programs. FastPolyEval is released under the BSD licence, with an attribution clause (see References, Contacts and Copyright), which means that you are **free to download**, **use**, **modify**, **distribute or sell**, **provided you give us proper credit**.

#### 1.4.2 Compile FastPolyEval

to get a basic help message. The default build command is:

This will create and populate a bin subdirectory of the downloaded folder with an app, called FastPolyEval. You may move the executable file to a convenient location. Alternatively, consider adding this folder to your PATH. The Makefile does not attempt this step for you. See Basic usage of FastPolyEval for additional help on how to use this app.

Note that the file.c and -I folder parameters must be repeated as necessary. The Makefile is simple enough and understanding it can provide additional guidance.

FastPolyEval switches automatically from hardware machine precision to emulated high-precision using MPFR (see Number formats). The format used for hardware numbers is chosen at the time of the compilation. You may edit the source file code/numbers/ntypes.h before the default build. Alternatively, you can execute make hardware

This should generate an automatically edited copy of this header file in a temporary folder and launch successive compilations. This build will populate the bin subdirectory with three apps, called FastPolyEval\_FP32, FastPolyEval\_FP64 and FastPolyEval\_FP80 corresponding to each possible choice.

#### 1.4.3 Additional help for Linux, MacOS, Windows

Github offers access to virtual machines that run on their servers. The corresponding tasks are called workflows. Each workflow serves as a guidline (read the subsection job:steps in the yml files) to perform similar actions on your computer. The directory .github/workflows on our GitHub repository contains a build workflow for each major OS: Linux, MacOS and Windows.

#### 1.4.4 Uninstall FastPolyEval

As the Makefile does not move the binaries and does not alter your PATH, cleanup is minimal. To remove the binary files generated in the build process, execute  $make\ clean$ 

To uninstall FastPolyEval from your system, simply delete the executable file and remove the downloaded sources.

## 1.5 Basic usage of FastPolyEval

FastPolyEval is used at the command line, either directly or through a shell script. A typical command line call has the following structure:

FastPolyEval -task prec parameter [optional\_parameter]

where prec is the requested precision for the computations.

## 1.5.1 Onboard help system

To call the onboard help with a list and brief description of all possible tasks, type  ${\tt FastPolyEval}$  -help

A detailed help exists for each task. For example, try FastPolyEval -eval -help.

The different tasks belong to 3 groups:

- · Tasks for generating and handling polynomials,
- · Tasks for generating and handling sets of complex numbers,
- · Tasks using the FPE algorithm for production use and benchmarking

and will be detailed below.

Note

In absence of argument, the default behavior is a call for help. The previous messaged can also be displayed respectively with FastPolyEval and FastPolyEval -eval.

#### 1.5.2 Number formats

The flags MACHINE\_LOW\_PREC and MACHINE\_EXTRA\_PREC in ntypes.h define what kind of machine numbers  $\begin{tabular}{l} FastPolyEval defaults to for low-precision computations, and the corresponding precision threshold that defines how low is "low". Note that the main limitation of machine numbers is the limited range of exponents. The numerical limits can easily be reached when evaluating a polynomial of high degree. On the contrary, MPFR number are virtually unlimited, with a default ceiling set to $$\simeq 2^{\pm 4 \times 10^{18}}$.}$ 

numbers/ntypes.h	Precision requested	Format	Numerical limit
MACHINE_LOW_PREC	up to 24	FP32, float	about $10^{-38}$ to $10^{+38}$
	25 and up	MPFR	practically unlimited
no flag	up to 53	FP64, double	about $10^{-308}$ to $10^{+308}$
i no nag	54 and up	MPFR	practically unlimited
MACHINE EXTRA PREC	up to 64	FP80, long double	about $10^{-4930}$ to $10^{+4930}$
WAOTHINE_EXTRA_FREG	65 and up	MPFR	practically unlimited

**Table 1.1 Number formats** 

#### Warning

If a number either read as input from a file or computed and destined to the output cannot be represented with the selected precision (inf or NaN exception), a warning is issued and the operation fails. Usually, the solution consists in using a higher precision (i.e. MPFR numbers). Anoter possible issue (if you are running Newton steps) is that you have entered the immediate neigborhood of a critical point, which induces a division by zero or almost zero. Try neutralizing the offending point.

Other numerical settings can be adjusted in ntypes.h, in particular :

- HUGE\_DEGREES sets the highest polynomial degree that can be handled (default  $2^{64} 2$ ),
- HUGE\_MP\_EXP sets the highest exponent that MPFR numbers can handle (default  $\pm 4 \times 10^{18}$ ).

#### 1.5.3 Input and outputs

 ${\tt FastPolyEval} \ \ \text{reads its input data from files and produces its output as file. The file format is {\tt CSV}. \ \ \textbf{To be valid}, \\ \textbf{the rest of the {\tt CSV} must contains a listing of complex numbers, written}$ 

where a is the real part and b is the imaginary part, in decimal form.

Depending on the context, the file will be interpreted as a set of evaluation points, a set of values, or the coefficients of a polynomial. For example, here is a valid file:

```
// An approximation of pi
3.14, 0
// A complex number close to the real axis
1.89755593218329076e+99, 2.35849881747969046e-427
```

Polynomials are written with the lowest degree first, so P(z)=1-2iz is represented by the file  $^{\rm 1}$  ,  $^{\rm 0}$   $^{\rm 0}$  ,  $^{\rm -2}$ 

Comments line are allowed: they start either with #, // or ;. Comment lines will be ignored. Be mindful of the fact that comments can induce an **offset** between the line count of the file and the internal line count of  $FastPoly \leftarrow Eval$ . Blank lines are not allowed. Lines are limited to 10 000 symbols (see array\_read), which puts a practical limit to the precision at around 15 000 bits. You can easily edit the code to push this limitation if you have the need for it.

#### Warning

As a general rule for the tasks of FastPolyEval, if an output file name matches the one of an input file, the operation is **safe**. However, the desired output will overwrite the previous version of the file.

#### Note

For users that want a turnkey solution to high-performance polynomial evaluations where the outputs of some computations are fed back as input to others, we recommend the use of FastPolyEval with data residing in a virtual RAM disk, on local solid-state drives or on similar low latency/high bandwidth storage solutions. If you have doubts on how to do this, please contact your system administrator.

#### 1.5.4 Tasks for generating and handling polynomials

FastPolyEval contains a comprehensive set of tools to generate new polynomials, either from scratch or by performing simple operations on other ones.

• Classical polynomials are generated with the tasks -Chebyshev, -Legendre, -Hermite, -Laquerre. The family -hyperbolic is defined recursively by

$$p_1(z) = z,$$
  $p_{n+1}(z) = p_n(z)^2 + z$ 

and plays a central role in the study of the Mandelbrot set (see e.g. reference [2] in References, Contacts and Copyright).

- One can build a polynomial from a predetermined set of roots (listed with multiplicity) by invoquing the task
   -roots.
- One can compute the sum (-sum), difference (-diff), product (-prod) or the derivative (-der) of polynomials.

## 1.5.5 Tasks for generating and handling sets of complex numbers

FastPolyEval contains a comprehensive set of tools to generate new sets of real and complex numbers, either from scratch or by performing simple operations on other ones.

- The real (-re) and imaginary (-im) parts of a list of complex numbers can be extracted. The results are real and therefore of the form x, 0. The complex conjugate (sign change of the imaginary part) is computed with -conj and the complex exponential with -exp.
- FastPolyEval can perform various interactions between valid CSV files.
  - 1. The concatenation (-cat) of two files writes a copy of the second one after a copy of the first one. For example, to rewrite a high-precision output file\_high\_prec.csv with a lower precision prec, use

```
FastPolyEval prec file_high_prec.csv /dev/null file_low_prec.csv
```

2. The -join task takes the real parts of two sequences and builds a complex number out of it. The imaginary parts are lost.

```
a, * (entry k from file_1)
b, * (entry k from file_2)
----
a, b (output k)
```

If the files have unequal lengh, the operation succeeds but stops once the shortest file runs out of entries. Be mindfull of offsets induced by commented lines (see Input and outputs).

3. The -tensor task computes a tensor product (i.e. complex multiplication line by line).

```
a, b (entry k from file_1)
c, d (entry k from file_2)
----
ac-bd, ad+bc (output k)
```

If the files have unequal lengh, the operation succeeds but stops once the shortest file runs out of entries. Be mindfull of offsets induced by commented lines (see Input and outputs).

- 4. The ¬grid task computes the grid product of the real part of the entries. The output file contains nb
   lines\_file\_1 × nb\_lines\_file\_2 lines and lists all the products possibles between the real part of entries in the first file with the real part of entries in the second file. The imaginary parts are ignored.
- Rotations (-rot) map the complex number a+ib to  $a\times e^{ib}$ . For example, to generate complex values from a real profile.csv and a set of phases phases.csv, you can use

```
FastPolyEval -join prec profile.csv phases.csv rot_tmp.csv
FastPolyEval -rot prec rot_tmp.csv complex_output.csv
rm -f rot_tmp.csv
```

- The -unif task writes real numbers in an arithmetic progression whose characteristics are specified by the parameters.
- The -sphere task writes polar coordinates approximating an uniform distribution on the Riemann sphere. The output value (a,b) represents Euler angles in the (vertical, horizontal) convention. It represents the point

$$(\cos a \cos b, \cos a \sin b, \sin a) \in \mathbb{S}^2 \subset \mathbb{R}^3.$$

The <code>-polar</code> task maps a pair of (vertical, horizontal) angles onto the complex plane by <code>stereographical projection</code>. To generate complex points that are uniformly distributed on the Riemann sphere, starting with <code>SEED</code> points at the equator, you can use the following code that combines those tasks. Note that there will be about  $SEED^2/\pi$  points on the sphere and that the points are computed in a deterministic way (they will be identical from one call to the next). A SEED of 178 produces about 10 000 complex points.

```
SEED=178
FastPolyEval -sphere prec $SEED tmp_file.csv
FastPolyEval -polar prec tmp_file.csv sphere.csv
rm -f tmp_file.csv
```

• FastPolyEval also contains two random generators (actually based on MPFR). The -rand task produces real random numbers that are uniformly distributed in an interval. The -normal task produces real random numbers with a Gaussian distribution whose characteristics are specified by the parameters. Use the -join task to merge the outputs of two -normal tasks into a complex valued normal distribution.

#### 1.5.6 Tasks using the FPE algorithm for production use and benchmarking

The main tasks of the FastPolyEval library are the following:

- -eval evaluates a polynomial on a set of points using the FPE algorithm.
- -evalD evaluates the derivative of a polynomial on a set of points using the FPE algorithm.

The precision of the computation and the name of the inputs (polynomial and points) & output (values) files are given as parameters. The first optional parameter specifies a second output file that contains a complementary report on the estimated quality of the evaluation at the precision chosen. For each evaluation point, this report contains an upper bound for the evaluation errors (in bits), a conservative estimate on the number of correct bits of the result, and the number of terms that where kept by the FPE algorithm.

For benchmark purposes (see reference [1] in Section References, Contacts and Copyright), we propose a set of optional parameters that specify how many times the preprocessing and the FPE algorithm should be run at each point (to improve the accuracy of the time measurement), whether the Hörner algorithm should also be run and, if so, how many times it should run.

The task -evalN evaluates one **Newton step** of a polynomial on a set of points, i.e.

$$NS(P, z) = \frac{P(z)}{P'(z)}.$$

Recall that Newton's method for finding roots of P consists in computing the sequence defined recursively by

$$z_{n+1} = z_n - NS(P, z_n).$$

The -iterN task iterates the Newton method a certain amount of times and with a given precision. It thus realizes a partial search of the roots of the polynomial. For best results, we recommend successive calls where the precision is gradually increased and the maximum number of iterations is reduced. For guidance in the choice of the starting points, please refer to reference [3] in Section References, Contacts and Copyright.

-analyse computes the concave cover and the intervals of |z| for which the evaluation strategy changes

The -analyse task computes the concave cover  $\hat{E}_P$ , the strip  $S_\delta$  (see Section Description of the Fast Polynomial Evaluator (FPE) a and the intervals of |z| for which the evaluation strategy of FPE (i.e. the reduced polynomial  $Q_p(z)$ ) changes. It is intended mostly for an illustrative purpose on low degrees, when the internals of the FPE algorithm can still be checked by hand. However, the intervals where a parsimonious representation is valid may also be of practical use (see reference [1] in Section References, Contacts and Copyright).

## 1.6 Notes about the implementation

For further details, please read the documentation associated to each source file.

Do not hesitate to contact us (see References, Contacts and Copyright) to signal bugs and to request new features. We are happy to help the development of the community of the users of FastPolyEval.

## 1.7 References, Contacts and Copyright

Please cite the reference [1] below if you use or distribute this software. The other citations are in order of appearance in the text:

- [1] R. Anton, N. Mihalache & F. Vigneron. Fast evaluation of real and complex polynomials. 2022. [ hal-03820369].
- [2] N. Mihalache & F. Vigneron. How to split a tera-polynomial. In preparation.
- [3] J.H. Hubbard, D. Schleicher, S. Sutherland. How to find all roots of complex polynomials by Newton's method. Invent. math., 146:1-33, 2001. [ Llink] on author's page.

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```

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#### 1.8 Thanks

It is our pleasure to thank our families who supported us in the long and, at times stressful, process that gave birth to the FastPolyEval library, in particular Ramona who co-authored reference [1], Sarah for a thorough proof-reading of [1] and Anna who suggested the lightning pattern for our logo.

We also thank Romeo, the HPC center of the University of Reims Champagne-Ardenne, on which we where able to benchmark our code graciously.

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# Chapter 2

# **Data Structure Index**

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# **Chapter 3**

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## **Chapter 4**

# **Data Structure Documentation**

## 4.1 array\_struct Struct Reference

A variable length array of machine floating point complex numbers.

#### **Data Fields**

• ulong len

the number of complex numbers in the array

· ulong size

the present capacity of the array (memory size in number of complex numbers)

• comp\_ptr zi

the elements of the array

## 4.1.1 Detailed Description

A variable length array of machine floating point complex numbers.

Definition at line 37 of file array.h.

## 4.2 arrayf\_struct Struct Reference

A variable length list of machine floating point complex numbers.

#### **Data Fields**

· ulong len

the number of complex numbers in the list

· ulong size

the present capacity of the list (memory size in number of complex numbers)

• compf\_ptr zi

the elements of the list

## 4.2.1 Detailed Description

A variable length list of machine floating point complex numbers.

Definition at line 38 of file arrayf.h.

## 4.3 comp\_struct Struct Reference

Multi-precision floating point complex numbers.

#### **Data Fields**

mpfr\_t x

the real part of the complex number

mpfr\_t y

the imaginary part of the complex number

## 4.3.1 Detailed Description

Multi-precision floating point complex numbers.

Definition at line 31 of file comp.h.

## 4.4 compf\_struct Struct Reference

Machine complex numbers.

#### **Data Fields**

· coeff tx

the real part of the complex number

· coeff\_t y

the imaginary part of the complex number

## 4.4.1 Detailed Description

Machine complex numbers.

Definition at line 29 of file compf.h.

## 4.5 concave\_struct Struct Reference

Description of a concave function computed from the coefficients of some polynomial.

#### **Data Fields**

prec\_t extraBits

extra bits for guarding, depending on the degree of the polynomial

· prec\_t prec

the precision that will be used to evaluate the polynomial, excluding extraBits

list\_t def

the definition of the concave map

list t all

all terms of the polynomial that may be used for evaluation

deg\_t start

the position in allPow of the largest power to evaluate (for given slope)

• deg\_t mid

the position in allPow of the power which gives the maximum modulus

• deg\_t end

the position in allPow of the least power to evaluate (for given slope)

## 4.5.1 Detailed Description

Description of a concave function computed from the coefficients of some polynomial.

Definition at line 35 of file concave.h.

## 4.6 eval\_struct Struct Reference

Evaluator of polynomials with multi-precision floating point coefficients.

## **Data Fields**

• poly P

the polynomial, with complex coefficients

• polyr Q

the polynomial, with real coefficients

· bool real

the type of polynomial to evaluate

· prec\_t prec

the precision of evaluations, in bits

· concave f

concave cover of the scales of coefficients

• pows zn

powers of a complex argument

powsr xn

powers of a real argument

real\_t valErr

the [approximative] upper bound for the absolute error of the last evaluation, in bits

· real t derErr

the [approximative] upper bound for the absolute error of the last derivative evaluation, in bits

· real\_t ntErr

the [approximative] upper bound for the absolute error of the last Newton term evaluation, in bits

• deg\_t terms

the number of polynomial terms computed by the last operation

· comp buf

a buffer for internal computations

mpfr\_t br

a real buffer for internal computations

## 4.6.1 Detailed Description

Evaluator of polynomials with multi-precision floating point coefficients.

Definition at line 41 of file eval.h.

## 4.7 evalf\_struct Struct Reference

Evaluator of polynomials with machine floating point coefficients.

#### **Data Fields**

polyf P

the polynomial, with complex coefficients

polyfr Q

the polynomial, with real coefficients

bool real

the type of polynomial to evaluate

concave f

concave cover of the magnitude of coefficients

· powsf zn

powers of a complex argument

• powsfr xn

powers of a real argument

real\_t valErr

the [approximative] upper bound for the absolute error of the last evaluation, in bits

real\_t derErr

the [approximative] upper bound for the absolute error of the last derivative evaluation, in bits

· real\_t ntErr

the [approximative] upper bound for the absolute error of the last Newton term evaluation, in bits

deg\_t terms

the number of polynomial terms computed by the last operation

## 4.7.1 Detailed Description

Evaluator of polynomials with machine floating point coefficients.

Definition at line 35 of file evalf.h.

## 4.8 help\_struct Struct Reference

Description of a basic help screen.

#### **Data Fields**

· char \* before

the first line to display

· int columnCount

the number of columns

• int \* columnWidths

the widths of all but the last column (array length should be 1 less than columnCount)

char \*\* headers

the column headers

· int linesCount

the number of lines / commands

char \*\*\* lines

the double array of messages

· char \* after

the last line to display

## 4.8.1 Detailed Description

Description of a basic help screen.

Each help screen contains a brief summary (before), some lines of messages (commands) and a final discussion (after). Lines are structures as an array of variable size, with descriptive headers.

Definition at line 73 of file help.h.

## 4.9 list\_struct Struct Reference

A list of real numbers that can be sorted, while keeping track of original order.

## **Data Fields**

· deg t size

the memory size allocated

deg\_t count

the number of elements

• deg\_t \* k

indexes, powers, the permutation of the numbers when sorted

real\_t \* s

the list of numbers

· bool sorted

the state of the list

## 4.9.1 Detailed Description

A list of real numbers that can be sorted, while keeping track of original order.

Definition at line 35 of file list.h.

## 4.10 poly\_struct Struct Reference

Polynomial with multi-precision floating point complex coefficients.

#### **Data Fields**

• deg\_t degree

the degree of the polynomial

• prec\_t prec

the precision of the coefficients, in bits

• comp\_ptr a

the coefficients

· bool modified

the status of the coefficients

· mpfr t buf1

a buffer

mpfr\_t buf2

another buffer

## 4.10.1 Detailed Description

Polynomial with multi-precision floating point complex coefficients.

Definition at line 31 of file poly.h.

## 4.11 polyf\_struct Struct Reference

Polynomial with machine floating point complex coefficients.

## **Data Fields**

· deg\_t degree

the degree of the polynomial

· compf\_ptr a

the coefficients

bool modified

the status of the coefficients

## 4.11.1 Detailed Description

Polynomial with machine floating point complex coefficients.

Definition at line 30 of file polyf.h.

## 4.12 polyfr\_struct Struct Reference

Polynomial with machine floating point real coefficients.

#### **Data Fields**

• deg\_t degree

the degree of the polynomial

•  $coeff_t * a$ 

the coefficients

· bool modified

the status of the coefficients

## 4.12.1 Detailed Description

Polynomial with machine floating point real coefficients.

Definition at line 31 of file polyfr.h.

## 4.13 polyr\_struct Struct Reference

Polynomial with multi-precision floating point complex coefficients.

## **Data Fields**

• deg\_t degree

the degree of the polynomial

• prec\_t prec

the precision of the coefficients, in bits

mpfr\_ptr a

the coefficients

· bool modified

the status of the coefficients

• mpfr\_t buf1

a buffer

mpfr\_t buf2

another buffer

## 4.13.1 Detailed Description

Polynomial with multi-precision floating point complex coefficients.

Definition at line 31 of file polyr.h.

## 4.14 pows\_struct Struct Reference

The powers of the complex number z using multi-precision floating point numbers.

#### **Data Fields**

```
    prec_t prec
```

the precision of the powers of z, in bits

• deg\_t size

the memory size allocated

· byte tps

the largest non-negative integer such that  $2^{\wedge}tps <= size$ 

bool \* computed

the status of powers

• comp\_ptr zn

the powers of z

mpfr\_t buf1

a buffer

mpfr\_t buf2

another buffer

· comp pth

a buffer

· comp res

another buffer

## 4.14.1 Detailed Description

The powers of the complex number z using multi-precision floating point numbers.

Definition at line 30 of file pows.h.

## 4.15 powsf\_struct Struct Reference

The powers of the complex number z using machine floating point numbers.

#### **Data Fields**

• deg\_t size

the memory size allocated

byte tps

the largest non-negative integer such that  $2^{\text{h}} tps < = size$ 

• bool \* computed

the status of powers

• compf\_ptr zn

the powers of z

· compf res

a buffer for results

## 4.15.1 Detailed Description

The powers of the complex number z using machine floating point numbers.

Definition at line 30 of file powsf.h.

## 4.16 powsfr\_struct Struct Reference

The powers of the real number x using machine floating point numbers.

#### **Data Fields**

· bool inited

the status of the value x

• coeff\_t x

the real number

## 4.16.1 Detailed Description

The powers of the real number  $\boldsymbol{x}$  using machine floating point numbers.

Definition at line 35 of file powsfr.h.

## 4.17 powsr\_struct Struct Reference

The powers of the real number  $\ensuremath{\mathbf{x}}$  using multi-precision floating point numbers.

## **Data Fields**

• prec\_t prec

the precision of the powers of x, in bits

· bool inited

the status of the value x

• mpfr\_t x

the real number

• mpfr\_t res

a buffer

## 4.17.1 Detailed Description

The powers of the real number  $\ensuremath{\mathbf{x}}$  using multi-precision floating point numbers.

Definition at line 37 of file powsr.h.

## **Chapter 5**

## **File Documentation**

## 5.1 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/apps.h File Reference

The implementation of the mini-apps with MPFR numbers.

#### **Functions**

array app\_join (long prec, array z1, array z2)

Joins the real parts of the sequences z1 and z2 as the real parts and imaginary parts of a new list.

• array app\_grid (long prec, array z1, array z2)

Computes the set product of the real parts of two sequences z1 and z2.

array app\_exp (long prec, array z)

Computes the complex exponential of a sequence z.

• array app\_rot (long prec, array z)

Computes a\*exp(ib) for each term a+ib of a sequence z of complex numbers.

• array app\_polar (long prec, array z)

Computes the complex numbers given by a sequence z of their polar coordinates on the sphere.

• array app\_unif (long prec, ulong n, mpfr\_t st, mpfr\_t en)

Returns the list of n real numbers that split the interval [st,en] in n-1 equal intervals.

• array app\_rand (long prec, ulong n, mpfr\_t st, mpfr\_t en)

Returns the list of n random real numbers in the interval [st,en], uniformly distributed.

array app\_normal (long prec, ulong n, mpfr\_t cent, mpfr\_t var)

Returns the list of n random real numbers, normally distributed with center cent and variance var.

array app\_sphere (long prec, ulong n)

Returns a list of n compelx numbers, uniformly distributed on the Riemann sphere.

bool app\_compare (long prec, array z1, array z2, char \*output)

Compares two list of complex values and reports the eventual errors.

• array app\_re (long prec, array z)

Returns the real parts of the numbers in the sequence z.

array app\_im (long prec, array z)

Returns the imaginary parts of the numbers in the sequence z.

array app\_conj (long prec, array z)

Returns the conjugates of the numbers in the sequence z.

array app\_tensor (long prec, array z1, array z2)

Computes tensor (or piontwise) product of the sequences z1 and z2.

bool app\_eval\_p (long prec, poly P, array z, char \*outFile, char \*outError, long count, char \*outHorner, long countHorner, const char \*\*inFiles)

Evaluates the polynomial P in all points in the list z, using the **FPE** algorithm.

bool app\_eval\_d (long prec, poly P, array z, char \*outFile, char \*outError, long count, char \*outHorner, long countHorner, const char \*\*inFiles)

Evaluates the derivative of the polynomial P in all points in the list z, using the **FPE** algorithm.

• bool app\_eval\_n (long prec, poly P, array z, char \*outFile, char \*outError, long count, char \*outHorner, long countHorner, const char \*\*inFiles)

Evaluates the Newton terms of the polynomial P in all points in the list z, using the **FPE** algorithm.

• bool app\_eval\_r (long prec, poly P, array z, ulong maxIter, char \*outFile, char \*outError, long count, char \*outHorner, long countHorner, const char \*\*inFiles)

Evaluates the Newton iterates of the polynomial P in all points in the list z, using the **FPE** algorithm.

• bool app\_analyse (long prec, poly P, char \*outFile, char \*outChange)

Analyses the polynomail P and outputs its concave cover, ignored coefficients and (optionally) the modules of complex numbers for which the reduced polynomial changes.

## 5.1.1 Detailed Description

The implementation of the mini-apps with MPFR numbers.

#### 5.1.2 Function Documentation

## 5.1.2.1 app\_analyse()

Analyses the polynomail P and outputs its concave cover, ignored coefficients and (optionally) the modules of complex numbers for which the reduced polynomial changes.

These analysis is performed for the evaluations of the P with prec bits of precision. The concave cover corresponds to the pre-processing phase of the **FPE** algorithm. The map  $k = \log_2 |a_k|$  is considered.

prec	the precision of evaluations
Р	the polynomial
outFile	the output file containing the concave cover and the ognored coefficients
outChange	the output file containing the intervals for $\log_2 2 z $ and the corresponding reduced polynomials of P

#### Returns

true if the analysis is complete, false if some error occurred.

## 5.1.2.2 app\_compare()

Compares two list of complex values and reports the eventual errors.

#### **Parameters**

prec	the precision of the result
z1	the fist list
z2	the second list
output	a file name for the output file, NULL if not used

#### Returns

true if the comparison is complete, false if some error occurred.

## 5.1.2.3 app\_conj()

```
array app_conj (
            long prec,
            array z )
```

Returns the conjugates of the numbers in the sequence  $\ensuremath{\mathrm{z}}.$ 

#### **Parameters**

prec	the precision of the result
Z	the list of points

## Returns

the conjugates of z, NULL if some error occurred.

#### 5.1.2.4 app\_eval\_d()

Evaluates the derivative of the polynomial  ${\mathbb P}$  in all points in the list z, using the **FPE** algorithm.

#### **Parameters**

prec	the precision of intermediary computations and of the result
Р	the polynomial
Z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

#### Returns

true if the evaluaion is complete, false if some error occurred.

## 5.1.2.5 app\_eval\_n()

Evaluates the Newton terms of the polynomial  ${\tt P}$  in all points in the list  ${\tt z}$ , using the **FPE** algorithm.

prec	the precision of intermediary computations and of the result
P	the polynomial

#### **Parameters**

Z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

## Returns

true if the evaluaion is complete, false if some error occurred.

## 5.1.2.6 app\_eval\_p()

Evaluates the polynomial  ${\mathbb P}$  in all points in the list z, using the **FPE** algorithm.

#### **Parameters**

prec	the precision of intermediary computations and of the result
P	the polynomial
Z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

#### Returns

true if the evaluaion is complete, false if some error occurred.

#### 5.1.2.7 app\_eval\_r()

Evaluates the Newton iterates of the polynomial  ${\mathbb P}$  in all points in the list z, using the **FPE** algorithm.

This is a method to approximate the roots of P, but there are no guarantees for the convergence. If the iterates escape far from the origin, the alogrith stops (for those starting points).

#### **Parameters**

prec	the precision of intermediary computations and of the result
P	the polynomial
Z	the list of evaluation points
maxIter	the maximum iterates for each starting point
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

## Returns

true if the evaluaion is complete, false if some error occurred.

## 5.1.2.8 app\_exp()

```
array app_exp ( \label{eq:condition} \mbox{long prec,} \\ \mbox{array } z \mbox{ )}
```

Computes the complex exponential of a sequence  $\ensuremath{\mathtt{z}}.$ 

prec	the precision of the result
Z	the list of points

#### Returns

the image by the complex exponential,  $\mathtt{NULL}$  if some error occurred.

## 5.1.2.9 app\_grid()

Computes the set product of the real parts of two sequences z1 and z2.

#### **Parameters**

prec	the precision of the result
z1	the first list
z2	the second list

#### Returns

the set product,  $\mathtt{NULL}$  if some error occurred.

#### 5.1.2.10 app\_im()

```
array app_im (
          long prec,
          array z )
```

Returns the imaginary parts of the numbers in the sequence  $\,z.\,$ 

#### **Parameters**

prec	the precision of the result
Z	the list of points

#### Returns

the imaginary parts in z,  $\mathtt{NULL}$  if some error occurred.

## 5.1.2.11 app\_join()

```
array z1, array z2)
```

Joins the real parts of the sequences z1 and z2 as the real parts and imaginary parts of a new list.

#### **Parameters**

prec	the precision of the result
z1	the first list
z2	the second list

#### Returns

the joint list,  $\mathtt{NULL}$  if some error occurred.

## 5.1.2.12 app\_normal()

```
array app_normal (
            long prec,
            ulong n,
            mpfr_t cent,
            mpfr_t var )
```

Returns the list of n random real numbers, normally distributed with center  $\mathtt{cent}$  and variance  $\mathtt{var}$ .

#### **Parameters**

prec	the precision of the result
n	the number of points, at least 2
cent	the center of the normal distribution
var	the variance of the normal distribution

## Returns

the list of random real numbers (in complex format),  $\mathtt{NULL}$  if some error occurred.

#### 5.1.2.13 app\_polar()

```
array app_polar ( \label{eq:polar} \mbox{long $prec$,} \\ \mbox{array $z$ )}
```

Computes the complex numbers given by a sequence z of their polar coordinates on the sphere.

#### **Parameters**

prec	the precision of the result
Z	the list of polar coordinates

#### Returns

the complex numbers given by their polar coordinates,  $\mathtt{NULL}$  if some error occurred.

## 5.1.2.14 app\_rand()

Returns the list of n random real numbers in the interval [st,en], uniformly distributed.

#### **Parameters**

prec	the precision of the result
n	the number of points, at least 2
st	the start point
en	the end point

#### Returns

the list of random real numbers (in complex format),  $\mathtt{NULL}$  if some error occurred.

## 5.1.2.15 app\_re()

```
array app_re (
            long prec,
            array z )
```

Returns the real parts of the numbers in the sequence  $\ensuremath{\mathtt{z}}.$ 

prec	the precision of the result
Z	the list of points

#### Returns

the real parts in z, NULL if some error occurred.

## 5.1.2.16 app\_rot()

```
\begin{array}{c} \texttt{array app\_rot (} \\ & \texttt{long } prec, \\ & \texttt{array } z \ ) \end{array}
```

Computes a\*exp(ib) for each term a+ib of a sequence z of complex numbers.

#### **Parameters**

prec	the precision of the result
Z	the list of points

#### Returns

the image by a+ib->a\*exp(ib), NULL if some error occurred.

## 5.1.2.17 app\_sphere()

```
array app_sphere (
            long prec,
            ulong n )
```

Returns a list of n compelx numbers, uniformly distributed on the Riemann sphere.

#### **Parameters**

prec	the precision of the result
n	the number of points, at least 2

#### Returns

the list of points uniformly distributed on the sphere,  $\mathtt{NULL}$  if some error occurred.

## 5.1.2.18 app\_tensor()

```
array z1, array z2)
```

Computes tensor (or piontwise) product of the sequences z1 and z2.

#### **Parameters**

prec	the precision of the result
<i>z</i> 1	the first list
z2	the second list

#### Returns

the tensor product, NULL if some error occurred.

## 5.1.2.19 app\_unif()

Returns the list of n real numbers that split the interval [st,en] in n-1 equal intervals.

#### **Parameters**

prec	the precision of the result
n	the number of points, at least 2
st	the start point
en	the end point

## Returns

the list of real numbers (in complex format),  $\mathtt{NULL}$  if some error occurred.

## 5.2 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/appsf.h File Reference

The implementation of the mini-apps with machine numbers.

## **Functions**

• arrayf appf\_join (arrayf z1, arrayf z2)

Joins the real parts of the sequences z1 and z2 as the real parts and imaginary parts of a new list.

• arrayf appf\_grid (arrayf z1, arrayf z2)

Computes the set product of the real parts of two sequences z1 and z2.

arrayf appf\_exp (arrayf z)

Computes the complex exponential of a sequence z.

arrayf appf\_rot (arrayf z)

Computes a\*exp(ib) for each term a+ib of a sequence z of complex numbers.

• arrayf appf\_polar (arrayf z)

Computes the complex numbers given by a sequence z of their polar coordinates on the sphere.

arrayf appf\_unif (ulong n, coeff\_t st, coeff\_t en)

Returns the list of n real numbers that split the interval [st,en] in n-1 equal intervals.

• bool appf\_compare (arrayf z1, arrayf z2, char \*output)

Compares two list of complex values and reports the eventual errors.

arrayf appf\_re (arrayf z)

Returns the real parts of the numbers in the sequence z.

arrayf appf\_im (arrayf z)

Returns the imaginary parts of the numbers in the sequence z.

arrayf appf\_conj (arrayf z)

Returns the conjugates of the numbers in the sequence z.

arrayf appf\_tensor (arrayf z1, arrayf z2)

Computes tensor (or piontwise) product of the sequences z1 and z2.

bool appf\_eval\_p (polyf P, arrayf z, char \*outFile, char \*outError, long count, char \*outHorner, long count
 Horner, const char \*\*inFiles)

Evaluates the polynomial P in all points in the list z, using the **FPE** algorithm.

• bool appf\_eval\_d (polyf P, arrayf z, char \*outFile, char \*outError, long count, char \*outHorner, long count

Horner, const char \*\*inFiles)

Evaluates the derivative of the polynomial P in all points in the list z, using the **FPE** algorithm.

Evaluates the Newton terms of the polynomial P in all points in the list z, using the **FPE** algorithm.

• bool appf\_eval\_r (polyf P, arrayf z, ulong maxIter, char \*outFile, char \*outError, long count, char \*outHorner, long countHorner, const char \*\*inFiles)

Evaluates the Newton iterates of the polynomial P in all points in the list z, using the FPE algorithm.

## 5.2.1 Detailed Description

The implementation of the mini-apps with machine numbers.

#### 5.2.2 Function Documentation

#### 5.2.2.1 appf\_compare()

Compares two list of complex values and reports the eventual errors.

z1	the fist list
z2	the second list
Generated b	የ ያልተለም name for the output file, NULL if not used

#### Returns

true if the comparison is complete, false if some error occurred.

## 5.2.2.2 appf\_conj()

```
\begin{array}{c} {\tt arrayf \ appf\_conj \ (} \\ {\tt arrayf \ } z \ ) \end{array}
```

Returns the conjugates of the numbers in the sequence z.

#### **Parameters**

```
z the list of points
```

## Returns

the conjugates of z, NULL if some error occurred.

## 5.2.2.3 appf\_eval\_d()

Evaluates the derivative of the polynomial  ${\mathbb P}$  in all points in the list z, using the **FPE** algorithm.

P	the polynomial
Z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

#### Returns

true if the evaluaion is complete, false if some error occurred.

## 5.2.2.4 appf\_eval\_n()

Evaluates the Newton terms of the polynomial P in all points in the list z, using the **FPE** algorithm.

#### **Parameters**

P	the polynomial
Z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

#### Returns

true if the evaluaion is complete, false if some error occurred.

## 5.2.2.5 appf\_eval\_p()

Evaluates the polynomial P in all points in the list z, using the **FPE** algorithm.

#### **Parameters**

P	the polynomial
Z	the list of evaluation points
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

#### Returns

true if the evaluaion is complete, false if some error occurred.

#### 5.2.2.6 appf\_eval\_r()

Evaluates the Newton iterates of the polynomial  ${\tt P}$  in all points in the list  ${\tt z}$ , using the **FPE** algorithm.

This is a method to approximate the roots of P, but there are no guarantees for the convergence. If the iterates escape far from the origin, the alogrith stops (for those starting points).

#### **Parameters**

P	the polynomial
Z	the list of evaluation points
maxIter	the maximum iterates for each starting point
outFile	the results output file name
outError	the errors list file name
count	the number of repetitions of the computing task
outHorner	the results output file name, computed by Horner's method
countHorner	the number of repetitions of the computing task by Horner's method
inFiles	a vector with the names of input files, for printing stats only

#### Returns

true if the evaluaion is complete, false if some error occurred.

## 5.2.2.7 appf\_exp()

```
\begin{array}{c} \texttt{arrayf appf\_exp (} \\ \texttt{arrayf } z \ ) \end{array}
```

Computes the complex exponential of a sequence  $\ensuremath{\mathtt{z}}.$ 

#### **Parameters**

```
z the list of points
```

#### Returns

the image by the complex exponential,  $\mathtt{NULL}$  if some error occurred.

## 5.2.2.8 appf\_grid()

Computes the set product of the real parts of two sequences z1 and z2.

#### **Parameters**

<i>z</i> 1	the first list
z2	the second list

### Returns

the set product,  $\mathtt{NULL}$  if some error occurred.

## 5.2.2.9 appf\_im()

```
\begin{array}{c} \mathtt{arrayf} \ \mathtt{appf\_im} \ ( \\ \\ \mathtt{arrayf} \ z \ ) \end{array}
```

Returns the imaginary parts of the numbers in the sequence  $\,z.\,$ 

```
z the list of points
```

#### Returns

the imaginary parts in z, NULL if some error occurred.

## 5.2.2.10 appf\_join()

Joins the real parts of the sequences z1 and z2 as the real parts and imaginary parts of a new list.

#### **Parameters**

z1	the first list
z2	the second list

#### Returns

the joint list,  $\mathtt{NULL}$  if some error occurred.

## 5.2.2.11 appf\_polar()

Computes the complex numbers given by a sequence z of their polar coordinates on the sphere.

## Parameters

```
z the list of polar coordinates
```

## Returns

the complex numbers given by their polar coordinates,  $\mathtt{NULL}$  if some error occurred.

## 5.2.2.12 appf\_re()

```
\begin{array}{c} \mathtt{arrayf} \ \mathtt{appf\_re} \ ( \\ \\ \mathtt{arrayf} \ z \ ) \end{array}
```

Returns the real parts of the numbers in the sequence  $\ensuremath{\mathtt{z}}.$ 

## **Parameters**

z the list of points

#### Returns

the real parts in z,  $\mathtt{NULL}$  if some error occurred.

#### 5.2.2.13 appf\_rot()

```
arrayf appf\_rot ( arrayf z )
```

Computes a\*exp(ib) for each term a+ib of a sequence z of complex numbers.

#### **Parameters**

z the list of points

#### Returns

the image by a+ib->a\*exp(ib), NULL if some error occurred.

## 5.2.2.14 appf\_tensor()

Computes tensor (or piontwise) product of the sequences z1 and z2.

#### **Parameters**

<i>z</i> 1	the first list
z2	the second list

## Returns

the tensor product,  $\mathtt{NULL}$  if some error occurred.

#### 5.2.2.15 appf\_unif()

```
arrayf appf_unif (
          ulong n,
          coeff_t st,
          coeff_t en )
```

Returns the list of n real numbers that split the interval [st,en] in n-1 equal intervals.

#### **Parameters**

n	the number of points, at least 2
st	the start point
en	the end point

#### Returns

the list of real numbers (in complex format),  $\mathtt{NULL}$  if some error occurred.

## 5.3 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/help.h File Reference

A basic help system for the mini-apps.

#### **Data Structures**

struct help\_struct

Description of a basic help screen.

#### **Macros**

- #define HELP\_MAIN 0
  - Indexes for help pages.
- #define **HELP\_HYP** 1
- #define HELP\_CHEBYshev 2
- #define **HELP\_LEGENDRE** 3
- #define HELP\_HERMITE 4
- #define **HELP\_LAGUERRE** 5
- #define **HELP\_SUM** 6
- #define **HELP\_DIFF** 7
- #define HELP PROD 8
- #define HELP\_CONCAT 9
- #define **HELP\_JOIN** 10
- #define HELP\_GRID 11
- #define **HELP\_EXP** 12
- #define **HELP\_ROT** 13
- #define HELP\_POLAR 14
- #define **HELP\_ROOTS** 15
- #define HELP\_DER 16

- #define **HELP\_UNIF** 17
- #define **HELP\_RAND** 18
- #define **HELP\_NORM** 19
- #define HELP\_SPHERE 20
- #define **HELP\_EVAL** 21
- #define **HELP EVALD** 22
- #define **HELP\_EVALN** 23
- #define **HELP\_NEWTON** 24
- #define HELP\_COMP 25
- #define HELP\_RE 26
- #define **HELP\_IM** 27
- #define HELP\_CONJ 28
- #define HELP TENSOR 29
- #define **HELP\_ANALYSE** 30
- #define HELP\_COUNT 31

The number of help pages.

• #define APP\_COUNT (HELP\_COUNT - 1)

The number of mini-apps.

## **Typedefs**

typedef help\_struct \* help

Practical wrapper for arrayf\_struct.

#### **Functions**

bool fpe\_help\_print (help h)

Prints the help screen described by h.

help fpe\_help\_get (int ind)

Return the help system in the list with index ind.

• void stats\_print (char \*mes, long prec, deg\_t deg, char \*numType, bool real, char \*polyFile, char \*ptsFile, char \*outFile, char \*outError, double timePP, long count, double timeEV, ulong tpts, char \*outHorner, double timeHo, ulong tptsho, ulong tit, ulong titho)

Prints computation stats in a standard format for automatic processing.

## 5.3.1 Detailed Description

A basic help system for the mini-apps.

## 5.3.2 Typedef Documentation

#### 5.3.2.1 help

```
typedef help_struct* help
```

Practical wrapper for arrayf\_struct.

To avoid the constant use \* and & the type  $help\_t$  is a pointer.

Definition at line 86 of file help.h.

## 5.3.3 Function Documentation

## 5.3.3.1 fpe\_help\_get()

```
help fpe_help_get (
          int ind )
```

Return the help system in the list with index ind.

#### **Parameters**

```
ind the index, use constants HELP_XXX
```

#### Returns

the help sytem with the given index. Returns the list,  $\mathtt{NULL}$  if  $\mathtt{ind}$  is an invalid request.

## 5.3.3.2 fpe\_help\_print()

```
bool fpe_help_print (
    help h )
```

Prints the help screen described by h.

#### **Parameters**

```
h the help screen to display
```

#### Returns

Boolean value expressing wether help could indeed be provided.

## 5.3.3.3 stats\_print()

```
char * outFile,
char * outError,
double timePP,
long count,
double timeEV,
ulong tpts,
char * outHorner,
double timeHo,
ulong tptsho,
ulong tpt,
ulong tit,
ulong titho)
```

Prints computation stats in a standard format for automatic processing.

## **Parameters**

mes	a short description of the computing task
prec	the precision used, in bits
deg	the degree of the polynomial
numType	the number type
real	true if it is a real polynomial, false otherwise
polyFile	the polynomial file name
ptsFile	the points list file name
outFile	the results output file name
outError	the errors list file name
timePP	pre-processing time in ns
count	the number of repetitions of the computing task
timeEV	evaluation time in ns
tpts	the total number of evaluation points (taking into acount the repetitions)
outHorner	the results output file name, computed by Horner's method
timeHo	the computing time in ns, by Horner's method
tptsho	the total number of evaluation by Horner's method
tit	total number of iterates, only for the iterative Newton method
titho	total number of iterates, only for the iterative Newton method, computed by Horner's method

# 5.4 /home/runner/work/FastPolyEval/FastPolyEval/code/apps/main.h File Reference

This is the entry point in the main app.

## **Macros**

- #define APP\_OK 0
- #define APP\_ERROR 1
- #define APP\_PARAMS 2

## **Typedefs**

typedef int(\* mainFuncf) (int argv, const char \*\*args)

The signature of a main function of an app in this project with machine numbers.

typedef int(\* mainFunc) (long prec, int argv, const char \*\*args)

The signature of a main function of an app in this project with arbitrary precision.

## 5.4.1 Detailed Description

This is the entry point in the main app.

Depending on the first command line parameter, it launches an internal app or presents a help screen to guide the user.

## 5.5 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/concave.h File Reference

Definition of a concave function computed from the coefficients of some polynomial.

#### **Data Structures**

· struct concave struct

Description of a concave function computed from the coefficients of some polynomial.

## **Macros**

• #define BITS GUARD 6

The extra bits that are needed as explained in [1].

## **Typedefs**

• typedef concave\_struct \* concave

Convenience pointer to concave\_struct.

## **Functions**

concave conc\_new (list I, prec\_t prec)

Computes the concave cover of the graph of a list 1 sorted in decreasing order.

• bool conc\_free (concave f)

Frees all the memory used by the concave map f, assuming the struct has been allocated with malloc(), for example with conc\_new().

• bool conc\_range (concave f, real\_t la)

Computes the range of indexes in  $f \rightarrow allPow$  to use for evaluating the original polynomial at z with  $la=log\_2|z|$ .

• bool conc\_range\_der (concave f, real\_t la)

Computes the range of indexes in  $f \rightarrow allPow$  to use for evaluating the derivative of the original polynomial at z with  $la=log\_2|z|$ .

## 5.5.1 Detailed Description

Definition of a concave function computed from the coefficients of some polynomial.

Admissible powers are for any of the original polynomial  ${\mathbb P}$  or its derivative  ${\mathbb P}$  ' .

## 5.5.2 Function Documentation

## 5.5.2.1 conc\_free()

Frees all the memory used by the concave map f, assuming the struct has been allocated with malloc(), for example with  $conc\_new()$ .

#### **Parameters**

```
f the map
```

### Returns

true if successfull, false otherwise.

#### 5.5.2.2 conc\_new()

```
concave conc_new (  \label{eq:list_l} \mbox{list } l, \\ \mbox{prec\_t } prec\ )
```

Computes the concave cover of the graph of a list 1 sorted in decreasing order.

Note

Retains the list of non-zero coefficients in all.

1	the sorted list
prec	the precision that will be used to evaluate the polynomial

#### Returns

the concave function above the graph of 1,  $\mathtt{NULL}$  if some error occurred.

#### 5.5.2.3 conc\_range()

Computes the range of indexes in f->allPow to use for evaluating the original polynomial at z with la=log $\leftarrow$  \_2|z|.

Stores the result in the f->start and respectively f->end.

Note

f->start>=f->end, otherwise the value of the polynomial is 0.

#### **Parameters**

f	the map
la	the slope, or log_2 z

#### Returns

true if successfull, false otherwise.

## 5.5.2.4 conc\_range\_der()

Computes the range of indexes in f->allPow to use for evaluating the derivative of the original polynomial at z with la=log\_2|z|.

Stores the result in the f->start and respectively f->end.

Note

f->start>=f->end, otherwise the value of the derivative is 0.

f	the map
la	the slope, or log_2 z

Returns

true if successfull, false otherwise.

# 5.6 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/eval.h File Reference

Definition of polynomial evaluator with arbitary precision coefficients.

#### **Data Structures**

· struct eval\_struct

Evaluator of polynomials with multi-precision floating point coefficients.

#### **Macros**

• #define MIN EVAL PREC 8

Minimum prcision for evaluators.

- #define MIN\_EVAL\_PREC\_STR "8"
- #define eval\_lastValError(ev) (ev->valErr)

The [approximative] upper bound for the error of the last evaluation, in bits. **Not** reported by the Newton term computation.

#define eval\_lastDerError(ev) (ev->derErr)

The [approximative] upper bound for the error of the last derivative evaluation, in bits. **Not** reported by the Newton term computation.

## **Typedefs**

typedef eval\_struct eval\_t[1]

Practical wrapper for eval\_struct.

typedef eval\_struct \* eval

Convenience pointer to eval\_struct.

#### **Functions**

• eval eval\_new (poly P, prec\_t prec)

Returns a new evaluator of the complex polynomial P.

eval eval\_new\_r (polyr Q, prec\_t prec)

Returns a new evaluator of the real polynomial Q.

bool eval\_free (eval ev)

Frees all the memory used by the evaluator ev, assuming the struct has been allocated with malloc(), for example with  $eval\_new()$  or with  $eval\_new\_r()$ .

bool eval\_val (comp v, eval ev, comp z)

Evaluates  $ev \rightarrow P(z)$  (or  $ev \rightarrow Q(z)$ ) using the method described in [1].

• bool eval der (comp d, eval ev, comp z)

Evaluates  $ev \rightarrow P'(z)$  (or  $ev \rightarrow Q'(z)$ ) using the method described in [1].

bool eval\_val\_der (comp v, comp d, eval ev, comp z)

```
Evaluates ev -> P(z) and ev -> P'(z) (or ev -> Q(z) and ev -> Q'(z)) using the method described in [1].

    bool eval_newton (comp nt, eval ev, comp z)

      Computes the Newthon method step of ev -> P (or ev -> Q) using the method described in [1].

    bool eval analyse (eval ev)

      Analyses the complex polynomial ev->P, after some of its coefficients have been changed.
bool eval_analyse_r (eval ev)
      Analyses the real polynomial ev \rightarrow Q, after some of its coefficients have been changed.

    bool eval val cc (comp v, eval ev, comp z)

      Evaluates ev \rightarrow P(x) using the method described in [1].

    bool eval_der_cc (comp d, eval ev, comp z)

      Evaluates ev \rightarrow P'(x) using the method described in [1].

    bool eval_val_der_cc (comp v, comp d, eval ev, comp z)

      Evaluates ev \rightarrow P(x) and ev \rightarrow P'(x) using the method described in [1].

    bool eval newton cc (comp nt, eval ev, comp z)

      Computes the Newthon method step of ev->P using the method described in [1].

    bool eval val cr (comp v, eval ev, mpfr t x)

      Evaluates ev \rightarrow P(x) using the method described in [1].

    bool eval der cr (comp d, eval ev, mpfr t x)

      Evaluates ev \rightarrow P'(x) using the method described in [1].

    bool eval_val_der_cr (comp v, comp d, eval ev, mpfr_t x)

      Evaluates ev \rightarrow P(x) and ev \rightarrow P'(x) using the method described in [1].

    bool eval_newton_cr (comp nt, eval ev, mpfr_t x)

      Computes the Newthon method step of ev->P using the method described in [1].

    bool eval_val_rc (comp v, eval ev, comp z)

      Evaluates ev \rightarrow 0 (x) using the method described in [1].

    bool eval der rc (comp d, eval ev, comp z)

      Evaluates ev \rightarrow Q'(x) using the method described in [1].

    bool eval_val_der_rc (comp v, comp d, eval ev, comp z)

      Evaluates ev \rightarrow Q(x) and ev \rightarrow Q'(x) using the method described in [1].

    bool eval_newton_rc (comp nt, eval ev, comp z)

      Computes the Newthon method step of ev->Q using the method described in [1].

    bool eval_val_rr (mpfr_t v, eval ev, mpfr_t x)

      Evaluates the real polynomial ev \rightarrow Q(x) using the method described in [1].

    bool eval_der_rr (mpfr_t d, eval ev, mpfr_t x)

      Evaluates the derivative of real polynomial ev \rightarrow Q'(x) using the method described in [1].

    bool eval_val_der_rr (mpfr_t v, mpfr_t d, eval ev, mpfr_t x)

      Evaluates ev \rightarrow Q(x) and ev \rightarrow Q'(x) using the method described in [1].

    bool eval_newton_rr (mpfr_t nt, eval ev, mpfr_t x)

      Computes the Newthon method step of the real polynomial ev->Q using the method described in [1].
```

## 5.6.1 Detailed Description

Definition of polynomial evaluator with arbitary precision coefficients.

#### 5.6.2 Typedef Documentation

#### 5.6.2.1 eval\_t

```
typedef eval_struct eval_t[1]
```

Practical wrapper for eval\_struct.

To avoid the constant use \* and & the type eval\_t is a pointer.

Definition at line 60 of file eval.h.

#### 5.6.3 Function Documentation

#### 5.6.3.1 eval\_analyse()

```
bool eval_analyse ( eval ev )
```

Analyses the complex polynomial ev->P, after some of its coefficients have been changed.

Note

The general functions  $eval\_val()$ ,  $eval\_der()$ ,  $eval\_val\_der()$  and  $eval\_newton()$  automatically analyse the appropriate polynomial. Use this function only with the optimized versions like  $eval \leftarrow \_val\_cx()$ .

## Parameters

```
ev the evaluator
```

#### Returns

true if ev is ready to use, false otherwise.

#### 5.6.3.2 eval\_analyse\_r()

```
bool eval_analyse_r ( eval ev )
```

Analyses the real polynomial ev->Q, after some of its coefficients have been changed.

Note

The general functions  $eval\_val()$ ,  $eval\_der()$ ,  $eval\_val\_der()$  and  $eval\_newton()$  automatically analyse the appropriate polynomial. Use this function only with the optimized versions like  $eval \leftarrow \_val\_rx()$ .

#### **Parameters**

```
ev the evaluator
```

#### Returns

true if ev is ready to use, false otherwise.

## 5.6.3.3 eval\_der()

```
bool eval_der (  \begin{array}{ccc} \operatorname{comp} \ d, \\ & \operatorname{eval} \ \operatorname{ev}, \\ & \operatorname{comp} \ z \ ) \end{array}
```

Evaluates ev -> P'(z) (or ev -> Q'(z)) using the method described in [1].

#### Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

#### **Parameters**

d	the result
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

#### 5.6.3.4 eval\_der\_cc()

Evaluates  $ev \rightarrow P'(x)$  using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

d	the result
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

## 5.6.3.5 eval\_der\_cr()

Evaluates  $ev \rightarrow P'(x)$  using the method described in [1].

#### Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

d	the result
ev	the evaluator
X	the real argument

## Returns

true if successfull, false otherwise.

## 5.6.3.6 eval\_der\_rc()

Evaluates  $ev \rightarrow Q'(x)$  using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

d	the result
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

## 5.6.3.7 eval\_der\_rr()

Evaluates the derivative of real polynomial ev -> Q'(x) using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

d	the derivative
ev	the evaluator
X	the real argument

## Returns

true if successfull, false otherwise.

#### 5.6.3.8 eval\_free()

```
bool eval_free (
     eval ev )
```

Frees all the memory used by the evaluator ev, assuming the struct has been allocated with malloc(), for example with  $eval\_new()$  or with  $eval\_new\_r()$ .

<i>ev</i> th	e evaluator
--------------	-------------

#### Returns

true if successfull, false otherwise.

## 5.6.3.9 eval\_new()

Returns a new evaluator of the complex polynomial P.

#### **Parameters**

Р	the complex polynomial
prec	the precision of evaluations, in bits

#### Returns

the new evaluator,  $\mathtt{NULL}$  if some error occurred.

## 5.6.3.10 eval\_new\_r()

Returns a new evaluator of the real polynomial Q.

#### **Parameters**

Q	the real polynomial
prec	the precision of evaluations, in bits

#### Returns

the new evaluator,  $\mathtt{NULL}$  if some error occurred.

## 5.6.3.11 eval\_newton()

```
bool eval_newton (
          comp nt,
```

```
eval ev, comp z)
```

Computes the Newthon method step of ev -> P (or ev -> Q) using the method described in [1].

#### Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

#### **Parameters**

nt	the Newton term
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

## 5.6.3.12 eval\_newton\_cc()

```
bool eval_newton_cc (  \begin{array}{ccc} \operatorname{comp} \ nt, \\ \operatorname{eval} \ \operatorname{ev}, \\ \operatorname{comp} \ z \ ) \end{array}
```

Computes the Newthon method step of ev->P using the method described in [1].

#### Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

### Parameters

nt	the Newton term
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

## 5.6.3.13 eval\_newton\_cr()

Computes the Newthon method step of ev->P using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

nt	the Newton term
ev	the evaluator
X	the real argument

#### Returns

true if successfull, false otherwise.

# 5.6.3.14 eval\_newton\_rc()

```
bool eval_newton_rc (  \begin{array}{c} \operatorname{comp}\ nt, \\ \operatorname{eval}\ \operatorname{ev}, \\ \operatorname{comp}\ z\ ) \end{array}
```

Computes the Newthon method step of ev->Q using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

nt	the Newton term
ev	the evaluator
Z	the complex argument

# Returns

## 5.6.3.15 eval\_newton\_rr()

Computes the Newthon method step of the real polynomial ev->Q using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

nt	the Newton term
ev	the evaluator
X	the real argument

#### Returns

true if successfull, false otherwise.

# 5.6.3.16 eval\_val()

```
bool eval_val (  \begin{array}{ccc} \operatorname{comp} \ v, \\ & \operatorname{eval} \ \operatorname{ev}, \\ & \operatorname{comp} \ z \ ) \end{array}
```

Evaluates ev -> P(z) (or ev -> Q(z)) using the method described in [1].

## Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

# **Parameters**

V	the result
ev	the evaluator
Z	the complex argument

# Returns

## 5.6.3.17 eval\_val\_cc()

Evaluates  $ev \rightarrow P(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

V	the result
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

# 5.6.3.18 eval\_val\_cr()

Evaluates  $ev \rightarrow P(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

V	the result
ev	the evaluator
X	the real argument

# Returns

# 5.6.3.19 eval\_val\_der()

Evaluates ev -> P(z) and ev -> P'(z) (or ev -> Q(z) and ev -> Q'(z)) using the method described in [1].

# Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

#### **Parameters**

V	the value
d	the derivative
ev	the evaluator
Z	the complex argument

## **Returns**

true if successfull, false otherwise.

# 5.6.3.20 eval\_val\_der\_cc()

Evaluates ev->P(x) and ev->P'(x) using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

V	the value
d	the derivative
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

# 5.6.3.21 eval\_val\_der\_cr()

Evaluates  $ev \rightarrow P(x)$  and  $ev \rightarrow P'(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

V	the value
d	the derivative
ev	the evaluator
Х	the real argument

# Returns

true if successfull, false otherwise.

# 5.6.3.22 eval\_val\_der\_rc()

Evaluates  $ev \rightarrow Q(x)$  and  $ev \rightarrow Q'(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

V	the value
d	the derivative
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.6.3.23 eval\_val\_der\_rr()

Evaluates  $ev \rightarrow Q(x)$  and  $ev \rightarrow Q'(x)$  using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

# **Parameters**

V	the value
d	the derivative
ev	the evaluator
X	the real argument

## Returns

true if successfull, false otherwise.

# 5.6.3.24 eval\_val\_rc()

Evaluates  $ev \rightarrow Q(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

V	the result
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

# 5.6.3.25 eval\_val\_rr()

Evaluates the real polynomial  $ev \rightarrow Q(x)$  using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

# **Parameters**

V	the value
ev	the evaluator
Х	the real argument

# Returns

true if successfull, false otherwise.

# 5.7 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/evalf.h File Reference

Definition of polynomials evaluator with machine floating point coefficients.

## **Data Structures**

struct evalf\_struct

Evaluator of polynomials with machine floating point coefficients.

## **Macros**

#define evalf\_lastValError(ev) (ev->valErr)

The [approximative] upper bound for the error of the last evaluation, in bits. **Not** reported by the Newton term computation.

#define evalf lastDerError(ev) (ev->derErr)

The [approximative] upper bound for the error of the last derivative evaluation, in bits. **Not** reported by the Newton term computation.

# **Typedefs**

• typedef evalf struct evalf t[1]

Practical wrapper for evalf\_struct.

typedef evalf struct \* evalf

Convenience pointer to evalf\_struct.

## **Functions**

evalf evalf\_new (polyf P)

Returns a new evaluator of the complex polynomial P.

evalf evalf\_new\_r (polyfr Q)

Returns a new evaluator of the real polynomial Q.

• bool evalf free (evalf ev)

Frees all the memory used by the evaluator ev, assuming the struct has been allocated with malloc(), for example with  $evalf_new()$  or with  $evalf_new_r()$ .

• bool evalf\_val (compf v, evalf ev, compf z)

Evaluates  $ev \rightarrow P(z)$  (or  $ev \rightarrow Q(z)$ ) using the method described in [1].

bool evalf\_der (compf d, evalf ev, compf z)

Evaluates  $ev \rightarrow P'(z)$  (or  $ev \rightarrow Q'(z)$ ) using the method described in [1].

• bool evalf\_val\_der (compf v, compf d, evalf ev, compf z)

Evaluates ev-P(z) and ev-P'(z) (or ev-P(z)) and ev-P(z) using the method described in [1].

bool evalf\_newton (compf nt, evalf ev, compf z)

Computes the Newthon method step of ev->P (or ev->Q) using the method described in [1].

bool evalf\_analyse (evalf ev)

Analyses the complex polynomial ev->P, after some of its coefficients have been changed.

bool evalf\_analyse\_r (evalf ev)

Analyses the real polynomial  $ev \rightarrow Q$ , after some of its coefficients have been changed.

bool evalf val cc (compf v, evalf ev, compf z)

Evaluates  $ev \rightarrow P(x)$  using the method described in [1].

bool evalf\_der\_cc (compf d, evalf ev, compf z)

Evaluates  $ev \rightarrow P'(x)$  using the method described in [1].

bool evalf\_val\_der\_cc (compf v, compf d, evalf ev, compf z)

Evaluates  $ev \rightarrow P(x)$  and  $ev \rightarrow P'(x)$  using the method described in [1].

bool evalf\_newton\_cc (compf nt, evalf ev, compf z)

```
Computes the Newthon method step of ev->P using the method described in [1].

    bool evalf_val_cr (compf v, evalf ev, coeff_t x)

      Evaluates ev \rightarrow P(x) using the method described in [1].

    bool evalf_der_cr (compf d, evalf ev, coeff_t x)

      Evaluates ev \rightarrow P'(x) using the method described in [1].

    bool evalf_val_der_cr (compf v, compf d, evalf ev, coeff_t x)

      Evaluates ev \rightarrow P(x) and ev \rightarrow P'(x) using the method described in [1].

    bool evalf_newton_cr (compf nt, evalf ev, coeff_t x)

      Computes the Newthon method step of ev->P using the method described in [1].

    bool evalf_val_rc (compf v, evalf ev, compf z)

      Evaluates ev \rightarrow Q(x) using the method described in [1].

    bool evalf_der_rc (compf d, evalf ev, compf z)

      Evaluates ev \rightarrow Q'(x) using the method described in [1].

    bool evalf_val_der_rc (compf v, compf d, evalf ev, compf z)

      Evaluates ev -> Q(x) and ev -> Q'(x) using the method described in [1].

    bool evalf_newton_rc (compf nt, evalf ev, compf z)

      Computes the Newthon method step of ev->Q using the method described in [1].

    coeff_t evalf_val_rr (evalf ev, coeff_t x)

      Evaluates the real polynomial ev \rightarrow Q(x) using the method described in [1].

    coeff_t evalf_der_rr (evalf ev, coeff_t x)

      Evaluates the derivative of real polynomial ev -> Q'(x) using the method described in [1].

    bool evalf val der rr (coeff t *v, coeff t *d, evalf ev, coeff t x)

      Evaluates ev \rightarrow Q(x) and ev \rightarrow Q'(x) using the method described in [1].

    coeff_t evalf_newton_rr (evalf ev, coeff_t x)

      Computes the Newthon method step of the real polynomial ev->Q using the method described in [1].
```

# 5.7.1 Detailed Description

Definition of polynomials evaluator with machine floating point coefficients.

# 5.7.2 Typedef Documentation

# \_

5.7.2.1 evalf\_t

```
typedef evalf_struct evalf_t[1]
```

Practical wrapper for evalf\_struct.

To avoid the constant use \* and & the type  $evalf\_t$  is a pointer.

Definition at line 51 of file evalf.h.

# 5.7.3 Function Documentation

# 5.7.3.1 evalf\_analyse()

Analyses the complex polynomial ev->P, after some of its coefficients have been changed.

Note

The general functions  $evalf_val()$ ,  $evalf_der()$ ,  $evalf_val_der()$  and  $evalf_newton()$  automatically analyse the appropriate polynomial. Use this function only with the optimized versions like  $evalf_val_cx()$ .

#### **Parameters**

ev the evaluator

## Returns

true if ev is ready to use, false otherwise.

# 5.7.3.2 evalf\_analyse\_r()

Analyses the real polynomial ev->Q, after some of its coefficients have been changed.

Note

The general functions  $evalf_val()$ ,  $evalf_der()$ ,  $evalf_val_der()$  and  $evalf_newton()$  automatically analyse the appropriate polynomial. Use this function only with the optimized versions like  $evalf_val_rx()$ .

# **Parameters**

ev the evaluator

# Returns

true if ev is ready to use, false otherwise.

# 5.7.3.3 evalf der()

```
bool evalf_der (
          compf d,
```

```
evalf ev, compf z)
```

Evaluates  $ev \rightarrow P'(z)$  (or  $ev \rightarrow Q'(z)$ ) using the method described in [1].

## Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

## **Parameters**

d	the result
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.7.3.4 evalf\_der\_cc()

```
bool evalf_der_cc (  \begin{tabular}{ll} $\operatorname{compf}\ d$, \\ & \operatorname{evalf}\ ev, \\ $\operatorname{compf}\ z$ ) \end{tabular}
```

Evaluates  $ev \rightarrow P'(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

# Parameters

d	the result
ev	the evaluator
Z	the complex argument

# Returns

# 5.7.3.5 evalf\_der\_cr()

Evaluates  $ev \rightarrow P'(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

d	the result
ev	the evaluator
X	the real argument

#### Returns

true if successfull, false otherwise.

# 5.7.3.6 evalf\_der\_rc()

Evaluates ev->Q'(x) using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

# **Parameters**

d		the result
ev	/	the evaluator
Z		the complex argument

# Returns

# 5.7.3.7 evalf\_der\_rr()

Evaluates the derivative of real polynomial ev -> Q'(x) using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

ev	the evaluator
X	the real argument

#### Returns

the result, NaN is some error occurred.

# 5.7.3.8 evalf\_free()

Frees all the memory used by the evaluator ev, assuming the struct has been allocated with malloc(), for example with  $evalf_new()$  or with  $evalf_new_r()$ .

## **Parameters**

```
ev the evaluator
```

#### Returns

true if successfull, false otherwise.

## 5.7.3.9 evalf\_new()

```
evalf evalf_new (
          polyf P )
```

Returns a new evaluator of the complex polynomial P.

#### **Parameters**

P the complex polynomial

# Returns

the new evaluator,  $\mathtt{NULL}$  if some error occurred.

# 5.7.3.10 evalf\_new\_r()

Returns a new evaluator of the real polynomial Q.

# **Parameters**

Q the real polynomial

## Returns

the new evaluator, NULL if some error occurred.

# 5.7.3.11 evalf\_newton()

Computes the Newthon method step of  $ev \rightarrow P$  (or  $ev \rightarrow Q$ ) using the method described in [1].

# Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

nt	the Newton term
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

# 5.7.3.12 evalf\_newton\_cc()

```
bool evalf_newton_cc (  \begin{array}{c} \operatorname{compf} \ nt, \\ \operatorname{evalf} \ \operatorname{ev}, \\ \operatorname{compf} \ z \ ) \end{array}
```

Computes the Newthon method step of ev->P using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

nt	the Newton term
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.7.3.13 evalf\_newton\_cr()

Computes the Newthon method step of ev->P using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

nt	the Newton term
ev	the evaluator
Χ	the real argument

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#### Returns

true if successfull, false otherwise.

# 5.7.3.14 evalf\_newton\_rc()

```
bool evalf_newton_rc (  \begin{array}{cccc} \operatorname{compf} \ nt, \\ \operatorname{evalf} \ ev, \\ \operatorname{compf} \ z \end{array} \right)
```

Computes the Newthon method step of ev->Q using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

nt	the Newton term
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.7.3.15 evalf\_newton\_rr()

Computes the Newthon method step of the real polynomial ev->Q using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

ev	the evaluator
X	the real argument

#### Returns

the result, NaN is some error occurred.

# 5.7.3.16 evalf\_val()

```
bool evalf_val (  \begin{tabular}{ll} $\operatorname{compf}\ v,$\\ $\operatorname{evalf}\ \operatorname{ev},$\\ $\operatorname{compf}\ z\ ) \end{tabular}
```

Evaluates  $ev \rightarrow P(z)$  (or  $ev \rightarrow Q(z)$ ) using the method described in [1].

#### Note

This function chooses the quickest variant to compute, depending if the polynomial of  $\operatorname{ev}$  and / or  $\operatorname{z}$  are real.

## **Parameters**

V	the result
ev	the evaluator
Z	the complex argument

### Returns

true if successfull, false otherwise.

# 5.7.3.17 evalf\_val\_cc()

Evaluates  $ev \rightarrow P(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

V	the result
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.7.3.18 evalf\_val\_cr()

Evaluates  $ev \rightarrow P(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

V	the result
ev	the evaluator
X	the real argument

## Returns

true if successfull, false otherwise.

# 5.7.3.19 evalf\_val\_der()

Evaluates  $ev \rightarrow P(z)$  and  $ev \rightarrow P'(z)$  (or  $ev \rightarrow Q(z)$  and  $ev \rightarrow Q'(z)$ ) using the method described in [1].

# Note

This function chooses the quickest variant to compute, depending if the polynomial of ev and / or z are real.

V	the value
d	the derivative
ev	the evaluator
Z	the complex argument

#### Returns

true if successfull, false otherwise.

# 5.7.3.20 evalf\_val\_der\_cc()

Evaluates ev -> P(x) and ev -> P'(x) using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

V	the value
d	the derivative
ev	the evaluator
Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.7.3.21 evalf\_val\_der\_cr()

Evaluates  $ev \rightarrow P(x)$  and  $ev \rightarrow P'(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

V	the value
d	the derivative
ev	the evaluator
X	the real argument

## Returns

true if successfull, false otherwise.

# 5.7.3.22 evalf\_val\_der\_rc()

Evaluates  $ev \rightarrow Q(x)$  and  $ev \rightarrow Q'(x)$  using the method described in [1].

## Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

# **Parameters**

	V	the value
ſ	d	the derivative
ſ	ev	the evaluator
	Z	the complex argument

## Returns

true if successfull, false otherwise.

# 5.7.3.23 evalf\_val\_der\_rr()

Evaluates ev -> Q(x) and ev -> Q'(x) using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

V	the value
d	the derivative
ev	the evaluator
Х	the real argument

#### Returns

true if successfull, false otherwise.

# 5.7.3.24 evalf\_val\_rc()

Evaluates  $ev \rightarrow Q(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

## **Parameters**

V	the result
ev	the evaluator
Z	the complex argument

# Returns

true if successfull, false otherwise.

# 5.7.3.25 evalf\_val\_rr()

Evaluates the real polynomial  $ev \rightarrow Q(x)$  using the method described in [1].

# Warning

For maximum speed, no checks are performed on the parameters, on the type of polynomial represented by ev nor if the polynomial has been pre-conditionned after the last coefficient update.

#### **Parameters**

ev	the evaluator
X	the real argument

## Returns

the result, NaN is some error occurred.

# 5.8 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/list.h File Reference

Definition of a list that can quickly sort real machine floating-point numbers and keep track of their permutation.

# **Data Structures**

• struct list\_struct

A list of real numbers that can be sorted, while keeping track of original order.

# **Macros**

• #define LIST FACTOR 1.2

The multiplicative factor by which to grow the lists.

• #define LIST\_TERM 100

The additive term by which to grow the lists.

# **Typedefs**

typedef list\_struct list\_t[1]

Practical wrapper for list\_struct.

typedef list\_struct \* list

Convenience pointer to <code>list\_struct</code>.

## **Functions**

• list list new (deg t size)

Returns a new list of machine real numbers, with storage space for size numbers.

bool list\_init (list I, deg\_t size)

Initializes an existing list 1 with storage space for size numbers.

• bool list\_free (list I)

Frees all the memory used by the list 1, assuming the struct has been allocated with malloc(), for example with  $list_new()$ .

bool list\_clear (list I)

Frees all the memory used by the list 1, but not the list 1 itself.

• list list\_clone (list I)

Returns a copy of the list 1.

bool list\_add (list I, deg\_t k, real\_t s)

Adds the couple (k,s) at a new position at the end of the list 1.

bool list\_trim (list I)

Trims the list 1 to minimal size to contain all its elements.

bool list\_sort (list I)

Sorts the list in descending order while preserving couples (k[i],s[i]) for all i.

# 5.8.1 Detailed Description

Definition of a list that can quickly sort real machine floating-point numbers and keep track of their permutation.

# 5.8.2 Typedef Documentation

## 5.8.2.1 list\_t

```
typedef list_struct list_t[1]
```

Practical wrapper for list\_struct.

To avoid the constant use \* and & the type list\_t is a pointer.

Definition at line 46 of file list.h.

# 5.8.3 Function Documentation

# 5.8.3.1 list\_add()

Adds the couple (k,s) at a new position at the end of the list 1.

# **Parameters**

1	the list
k	the index
s	the real number

# Returns

true if successfull, false otherwise.

# 5.8.3.2 list\_clear()

Frees all the memory used by the list  $\mathbb{1}$ , but not the list  $\mathbb{1}$  itself.

# **Parameters**



# Returns

true if successfull, false otherwise.

# 5.8.3.3 list\_clone()

Returns a copy of the list 1.

## **Parameters**



# Returns

the new list,  $\mathtt{NULL}$  if some error occurred.

# 5.8.3.4 list\_free()

Frees all the memory used by the list 1, assuming the struct has been allocated with malloc(), for example with  $list_new()$ .

# **Parameters**

```
/ the list
```

## Returns

true if successfull, false otherwise.

# 5.8.3.5 list\_init()

Initializes an existing list 1 with storage space for size numbers.

# Parameters

1	the list
size	the size of the list

## Returns

true if successfull, false otherwise.

# 5.8.3.6 list\_new()

```
list list_new (
          deg_t size )
```

Returns a new list of machine real numbers, with storage space for size numbers.

size	the size of the list

## Returns

the new list,  $\mathtt{NULL}$  if some error occurred.

# 5.8.3.7 list\_sort()

Sorts the list in descending order while preserving couples (k[i],s[i]) for all i.

# Warning

The memory usage will double during the operation, all cleared up before returning. In case of failure, the original list is destroyed.

## **Parameters**

```
I the list
```

# Returns

true if successfull, false otherwise.

## 5.8.3.8 list\_trim()

Trims the list 1 to minimal size to contain all its elements.

## **Parameters**

```
I the list
```

## Returns

true if successfull, false otherwise.

# 5.9 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/pows.h File Reference

Definition of a buffer for pre-computed powers of a complex number with arbitary precision.

# **Data Structures**

· struct pows struct

The powers of the complex number z using multi-precision floating point numbers.

# **Typedefs**

typedef pows struct pows t[1]

Practical wrapper for pows\_struct.

typedef pows\_struct \* pows

Convenience pointer to eval\_struct.

## **Functions**

• pows pows\_new (prec\_t prec, deg\_t size)

Returns a new buffer of powers of complex numbers of precision prec, with initial storage space for size powers.

bool pows\_free (pows zn)

Frees all the memory used by the buffer zn, assuming the struct has been allocated with malloc(), for example with  $pows\_new()$ .

bool pows set (pows zn, comp z)

Sets the complex number of which the powers will be computed by the buffer zn.

comp\_ptr pows\_pow (pows zn, deg\_t pow)

Computes  $z^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

• comp\_ptr pows\_pow\_once (pows zn, deg\_t pow)

Computes  $z^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

# 5.9.1 Detailed Description

Definition of a buffer for pre-computed powers of a complex number with arbitary precision.

# 5.9.2 Typedef Documentation

## 5.9.2.1 pows t

```
typedef pows_struct pows_t[1]
```

Practical wrapper for pows\_struct.

To avoid the constant use \* and & the type pows t is a pointer.

Definition at line 45 of file pows.h.

## 5.9.3 Function Documentation

# 5.9.3.1 pows\_free()

```
bool pows_free (
          pows zn )
```

Frees all the memory used by the buffer zn, assuming the struct has been allocated with malloc(), for example with  $pows\_new()$ .

#### **Parameters**

zn	the powers buffer
----	-------------------

# Returns

true if successfull, false otherwise.

## 5.9.3.2 pows\_new()

Returns a new buffer of powers of complex numbers of precision prec, with initial storage space for size powers.

## Warning

prec must be at least precf and size at most MAX\_DEG.

## **Parameters**

prec	the precision of the coefficients, in bits
size	the size of the buffer

#### Returns

the new buffer,  $\mathtt{NULL}$  if some error occurred.

# 5.9.3.3 pows\_pow()

Computes  $z^pow$  using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of z that have been computed to accelerate later calls of this function. Also, if pow is larger than the size of the buffer zn, it is automatically increased to store the result.

zn	the powers buffer
pow	the power to compute

#### Returns

the result  $\mathtt{z}^{\wedge}\mathtt{pow},\,\mathtt{NULL}$  if some error occurred.

# 5.9.3.4 pows\_pow\_once()

```
\begin{array}{c} {\tt comp\_ptr~pows\_pow\_once~(}\\ \\ {\tt pows~}zn,\\ \\ {\tt deg\_t~pow~)} \end{array}
```

Computes  $z^pow$  using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of z into zn.

#### **Parameters**

zn	the powers buffer
pow	the power to compute

## Returns

the result  $z^pow$ , NULL if some error occurred.

## 5.9.3.5 pows\_set()

```
bool pows_set ( \label{eq:pows_zn,} \begin{picture}(200,0) \put(0,0){\line(0,0){100}} \put(0,0){\l
```

Sets the complex number of which the powers will be computed by the buffer  ${\tt zn.}$ 

## **Parameters**

zn	the powers buffer
Z	the complex number

# Returns

true if successfull, false otherwise.

# 5.10 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/powsf.h File Reference

Definition of a buffer for pre-computed powers of a machine complex number.

## **Data Structures**

struct powsf struct

The powers of the complex number z using machine floating point numbers.

# **Typedefs**

```
typedef powsf_struct powsf_t[1]
```

Practical wrapper for powsf\_struct.

typedef powsf\_struct \* powsf

Convenience pointer to eval\_struct.

## **Functions**

· powsf powsf new (deg t size)

Returns a new buffer of powers of machine complex numbers, with initial storage space for size powers.

bool powsf\_free (powsf zn)

Frees all the memory used by the buffer zn, assuming the struct has been allocated with malloc(), for example with  $powsf_new()$ .

bool powsf set (powsf zn, compf z)

Sets the complex number of which the powers will be computed by the buffer zn.

compf\_ptr powsf\_pow (powsf zn, deg\_t pow)

Computes  $z^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

• compf\_ptr powsf\_pow\_once (powsf zn, deg\_t pow)

Computes  $z^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

# 5.10.1 Detailed Description

Definition of a buffer for pre-computed powers of a machine complex number.

# 5.10.2 Typedef Documentation

# 5.10.2.1 powsf\_t

```
typedef powsf_struct powsf_t[1]
```

Practical wrapper for powsf\_struct.

To avoid the constant use \* and & the type powsf t is a pointer.

Definition at line 41 of file powsf.h.

## 5.10.3 Function Documentation

# 5.10.3.1 powsf\_free()

```
bool powsf_free (
          powsf zn )
```

Frees all the memory used by the buffer zn, assuming the struct has been allocated with malloc(), for example with  $powsf_new()$ .

#### **Parameters**

```
zn the powers buffer
```

# Returns

true if successfull, false otherwise.

# 5.10.3.2 powsf\_new()

Returns a new buffer of powers of machine complex numbers, with initial storage space for size powers.

## Warning

size must be at most MAX\_DEG.

#### **Parameters**

```
size the size of the buffer
```

# Returns

the new buffer,  $\mathtt{NULL}$  if some error occurred.

# 5.10.3.3 powsf\_pow()

Computes  $z^pow$  using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of z that have been computed to accelerate later calls of this function. Also, if pow is larger than the size of the buffer zn, it is automatically increased to store the result.

## Warning

fails if pow==0

# **Parameters**

zn	the powers buffer
pow	the power to compute

## Returns

the result  $z^{\wedge}pow$ , NULL if some error occurred.

# 5.10.3.4 powsf\_pow\_once()

Computes  $z^pow$  using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of z into zn.

## **Parameters**

zn	the powers buffer
pow	the power to compute

# Returns

the result  $z^{\wedge}pow$ , NULL if some error occurred.

# 5.10.3.5 powsf\_set()

```
bool powsf_set ( \label{eq:powsf_zn,} \operatorname{powsf} \ zn, \operatorname{compf} \ z \ )
```

Sets the complex number of which the powers will be computed by the buffer  ${\tt zn.}$ 

## **Parameters**

zn	the powers buffer
Z	the complex number

# Returns

# 5.11 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/powsfr.h File Reference

Definition of a buffer for pre-computed powers of a machine real number.

## **Data Structures**

struct powsfr\_struct

The powers of the real number x using machine floating point numbers.

# **Typedefs**

typedef powsfr\_struct powsfr\_t[1]

Practical wrapper for powsfr\_struct.

typedef powsfr struct \* powsfr

Convenience pointer to eval\_struct.

# **Functions**

powsfr powsfr new (deg t size)

Returns a new buffer of powers of machine real numbers, with initial storage space for size powers.

bool powsfr\_free (powsfr xn)

Frees all the memory used by the buffer xn, assuming the struct has been allocated with malloc(), for example with  $powsfr_new()$ .

bool powsfr\_set (powsfr xn, coeff\_t x)

Sets the real number of which the powers will be computed by the buffer xn.

coeff\_t powsfr\_pow (powsfr xn, deg\_t pow)

Computes  $x^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

coeff\_t powsfr\_pow\_once (powsfr xn, deg\_t pow)

Computes  $x^pow$  using repeated squares method and the cache of previously computed powers.

# 5.11.1 Detailed Description

Definition of a buffer for pre-computed powers of a machine real number.

# 5.11.2 Typedef Documentation

# 5.11.2.1 powsfr\_t

```
typedef powsfr_struct powsfr_t[1]
```

Practical wrapper for powsfr\_struct.

To avoid the constant use \* and & the type powsfr\_t is a pointer.

Definition at line 56 of file powsfr.h.

# 5.11.3 Function Documentation

# 5.11.3.1 powsfr\_free()

```
bool powsfr_free (
          powsfr xn )
```

Frees all the memory used by the buffer xn, assuming the struct has been allocated with malloc(), for example with  $powsfr_new()$ .

## **Parameters**

xn the powers buffer

## Returns

true if successfull, false otherwise.

# 5.11.3.2 powsfr\_new()

Returns a new buffer of powers of machine real numbers, with initial storage space for size powers.

# Warning

size must be at most MAX\_DEG.

## **Parameters**

```
size the size of the buffer
```

# Returns

the new buffer,  $\mathtt{NULL}$  if some error occurred.

# 5.11.3.3 powsfr\_pow()

Computes  $x^pow$  using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of x that have been computed to accelerate later calls of this function. Also, if pow is larger than the size of the buffer xn, it is automatically increased to store the result.

## **Parameters**

xn	the powers buffer
pow	the power to compute

# Returns

the result  $x^pow$ , NaN if some error occurred.

## 5.11.3.4 powsfr\_pow\_once()

Computes  $x^pow$  using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of x.

# **Parameters**

xn	the powers buffer
pow	the power to compute

## Returns

the result  $x^pow$ , NULL if some error occurred.

# 5.11.3.5 powsfr\_set()

Sets the real number of which the powers will be computed by the buffer xn.

xn	the powers buffer
X	the real number

#### Returns

true if successfull, false otherwise.

# 5.12 /home/runner/work/FastPolyEval/FastPolyEval/code/eval/powsr.h File Reference

Definition of a buffer for pre-computed powers of a real number with arbitary precision.

## **Data Structures**

struct powsr struct

The powers of the real number x using multi-precision floating point numbers.

# **Typedefs**

typedef powsr\_struct powsr\_t[1]

Practical wrapper for powsr\_struct.

typedef powsr\_struct \* powsr

Convenience pointer to eval\_struct.

# **Functions**

• powsr powsr\_new (prec\_t prec, deg\_t size)

Returns a new buffer of powers of real numbers of precision prec, with initial storage space for size powers.

bool powsr\_free (powsr xn)

Frees all the memory used by the buffer xn, assuming the struct has been allocated with malloc(), for example with  $powsr_new()$ .

bool powsr\_set (powsr xn, mpfr\_t x)

Sets the real number of which the powers will be computed by the buffer xn.

mpfr\_ptr powsr\_pow (powsr xn, deg\_t pow)

Computes  $x^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

• mpfr\_ptr powsr\_pow\_once (powsr xn, deg\_t pow)

Computes  $x^{\wedge}pow$  using repeated squares method and the cache of previously computed powers.

# 5.12.1 Detailed Description

Definition of a buffer for pre-computed powers of a real number with arbitary precision.

# 5.12.2 Typedef Documentation

## 5.12.2.1 powsr\_t

```
typedef powsr_struct powsr_t[1]
```

Practical wrapper for powsr\_struct.

To avoid the constant use \* and & the type powsr\_t is a pointer.

Definition at line 63 of file powsr.h.

# 5.12.3 Function Documentation

# 5.12.3.1 powsr\_free()

```
bool powsr_free (
          powsr xn )
```

Frees all the memory used by the buffer xn, assuming the struct has been allocated with malloc(), for example with  $powsr\_new()$ .

#### **Parameters**

```
xn the powers buffer
```

## Returns

true if successfull, false otherwise.

# 5.12.3.2 powsr\_new()

Returns a new buffer of powers of real numbers of precision prec, with initial storage space for size powers.

# Warning

prec must be at least precf and size at most MAX\_DEG.

## **Parameters**

prec	the precision of the coefficients, in bits	
size	thessize of the buffer	

## Returns

the new buffer,  $\mathtt{NULL}$  if some error occurred.

# 5.12.3.3 powsr\_pow()

Computes  $x^pow$  using repeated squares method and the cache of previously computed powers.

It caches intermediary powers of x that have been computed to accelerate later calls of this function. Also, if pow is larger than the size of the buffer xn, it is automatically increased to store the result.

#### **Parameters**

xn	the powers buffer
pow	the power to compute

#### Returns

the result  $x^pow$ , NULL if some error occurred.

# 5.12.3.4 powsr\_pow\_once()

Computes  $x^pow$  using repeated squares method and the cache of previously computed powers.

It does **NOT** cache intermediary powers of x into xn.

## **Parameters**

xn	the powers buffer
pow	the power to compute

# Returns

the result  $x^pow$ , NULL if some error occurred.

## 5.12.3.5 powsr\_set()

```
bool powsr_set (
          powsr xn,
          mpfr_t x )
```

Sets the real number of which the powers will be computed by the buffer xn.

#### **Parameters**

xn	the powers buffer
X	the complex number

#### Returns

true if successfull, false otherwise.

# 5.13 /home/runner/work/FastPolyEval/FastPoly Eval/code/numbers/comp.h File Reference

Definition of MPFR complex numbers.

# **Data Structures**

struct comp\_struct

Multi-precision floating point complex numbers.

# **Macros**

```
• #define comp_init(d, prec)
```

Allocates memory for the digits of d.

• #define comp\_initz(d, prec)

Allocates memory for the digits of d and sets its value to 0.

• #define comp\_clear(d)

De-allocates the memory used by the digits of  ${\tt d}.$ 

- #define comp\_zero(d) (mpfr\_zero\_p((d)->x) && mpfr\_zero\_p((d)->y))

Tests if d==0.

• #define comp\_add(d, a, b)

Adds a to b and stores the result in d, all of type comp or comp\_ptr.

• #define comp\_set(d, a)

Sets d to a.

• #define comp\_setr(d, a)

Sets d to the real value a.

#define comp\_neg(d, a)

Sets d to -a.

• #define comp addr(d, a, r)

Adds the complex number a to the real number b and stores the result in d.

```
• #define comp_amu(d, a, r, buf)
      Adds the complex number a*r to d, where d, a are complex and r is unsigned integer.
• #define comp_sub(d, a, b)
      Subtracts b from a and stores the result in d, all of type comp or comp_ptr.
• #define comp_subr(d, a, r)
      Subtracts the real number b from the complex number a and stores the result in d.
• #define comp mul(d, a, b, buf1, buf2)
     Multiplies a to b and stores the result in d, all of type comp or comp_ptr.
• #define comp_div(d, a, b, b1, b2, b3)
      Divides a by b and stores the result in d, all of type comp or comp_ptr.

    #define comp_mod(m, a) mpfr_hypot((m), (a)->x, (a)->y, MPFR_RNDN);

      Computes the modulus of a and stores the result in m, a of type comp and m of type mpfr_t.
• #define comp_mulr(d, a, r)
      Multiplies the complex number a to the real number r and stores the result in d.
• #define comp_muli(d, a, i)
     Multiplies the complex number a to the integer i and stores the result in d.
• #define comp_mulu(d, a, i)
      Multiplies the complex number a to the unsigned integer i and stores the result in d.
#define comp_sqr(d, a, buf)
```

Squares a and stores the result in d, all of type comp or comp\_ptr.

# **Typedefs**

• typedef comp\_struct comp[1]

Practical wrapper for comp\_struct.

• typedef comp\_struct \* comp\_ptr

Convenience pointer to comp\_struct.

## **Functions**

```
    real_t comp_log2 (comp z)
        Computes the base 2 log of |z|.
    real_t real_log2 (mpfr_t x)
        Computes the base 2 log of |x|.
    real_t comp_s (comp z)
        Computes s (z).
    real_t mpfr_s (mpfr_t x)
        Computes s (x).
```

# 5.13.1 Detailed Description

Definition of MPFR complex numbers.

# 5.13.2 Macro Definition Documentation

# 5.13.2.1 comp\_add

Value:

```
\label{eq:mpfr_add((d)->x, (a)->x, (b)->x, MPFR_RNDN); $$ mpfr_add((d)->y, (a)->y, (b)->y, MPFR_RNDN); $$
```

Adds a to b and stores the result in d, all of type comp or comp\_ptr.

Definition at line 64 of file comp.h.

# 5.13.2.2 comp\_addr

```
#define comp_addr(
          d,
          a,
          r )
```

Value:

```
\label{eq:mpfr_add((d)->x, (a)->x, (r), MPFR_RNDN); } $$ mpfr_set((d)->y, (a)->y, MPFR_RNDN); $$
```

Adds the complex number a to the real number b and stores the result in d.

Definition at line 80 of file comp.h.

## 5.13.2.3 comp\_amu

Value:

```
mpfr_mul_ui((buf), (a) -> x, (r), MPFR_RNDN); \
mpfr_add((d) -> x, (d) -> x, (buf), MPFR_RNDN); \
mpfr_mul_ui((buf), (a) -> y, (r), MPFR_RNDN); \
mpfr_add((d) -> y, (d) -> y, (buf), MPFR_RNDN);
```

Adds the complex number a\*r to d, where d,a are complex and r is unsigned integer.

Definition at line 84 of file comp.h.

## 5.13.2.4 comp\_clear

```
\#define comp_clear( d )
```

Value:

```
mpfr_clear((d)->x); \
mpfr_clear((d)->y);
```

De-allocates the memory used by the digits of d.

Definition at line 57 of file comp.h.

# 5.13.2.5 comp\_div

Value:

```
mpfr_sqr((b3), (b)->x, MPFR_RNDN); \
mpfr_sqr((b2), (b)->y, MPFR_RNDN); \
mpfr_sqr((b2), (b)->y, MPFR_RNDN); \
mpfr_add((b3), (b3), (b2), MPFR_RNDN); \
mpfr_mul((b1), (a)->x, (b)->x, MPFR_RNDN); \
mpfr_mul((b2), (a)->y, (b)->y, MPFR_RNDN); \
mpfr_add((b1), (b1), (b2), MPFR_RNDN); \
mpfr_mul((b2), (a)->x, (b)->y, MPFR_RNDN); \
mpfr_mul((d)->y, (a)->y, (b)->x, MPFR_RNDN); \
mpfr_sub((d)->y, (d)->y, (b2), MPFR_RNDN); \
mpfr_div((d)->y, (d)->y, (b3), MPFR_RNDN); \
mpfr_div((d)->x, (b1), (b3), MPFR_RNDN);
```

Divides a by b and stores the result in d, all of type comp or comp\_ptr.

Definition at line 107 of file comp.h.

## 5.13.2.6 comp init

Value:

```
mpfr_init2((d)->x, prec); \
mpfr_init2((d)->y, prec);
```

Allocates memory for the digits of d.

Definition at line 47 of file comp.h.

## 5.13.2.7 comp\_initz

Value:

```
mpfr_init2((d)->x, prec); \
mpfr_init2((d)->y, prec); \
mpfr_set_zero((d)->x, 1); \
mpfr_set_zero((d)->y, 1);
```

Allocates memory for the digits of d and sets its value to 0.

Definition at line 51 of file comp.h.

#### 5.13.2.8 comp\_mul

Value:

```
mpfr_mul((buf1), (a) ->x, (b) ->x, MPFR_RNDN); \
mpfr_mul((buf2), (a) ->y, (b) ->y, MPFR_RNDN); \
mpfr_sub((buf1), (buf1), (buf2), MPFR_RNDN); \
mpfr_mul((buf2), (a) ->x, (b) ->y, MPFR_RNDN); \
mpfr_mul((d) ->y, (a) ->y, (b) ->x, MPFR_RNDN); \
mpfr_add((d) ->y, (d) ->y, (buf2), MPFR_RNDN); \
mpfr_set((d) ->x, (buf1), MPFR_RNDN); \
```

Multiplies a to b and stores the result in d, all of type comp or comp\_ptr.

Definition at line 98 of file comp.h.

## 5.13.2.9 comp muli

Value:

```
\label{eq:mpfr_mul_si((d)->x, (a)->x, (i), MPFR_RNDN); $$ mpfr_mul_si((d)->y, (a)->y, (i), MPFR_RNDN); $$
```

Multiplies the complex number a to the integer  $\dot{\text{\fontfamily}}$  and stores the result in d.

Definition at line 127 of file comp.h.

# 5.13.2.10 comp\_mulr

# Value:

```
\label{eq:mpfr_mul((d)->x, (a)->x, (r), MPFR_RNDN); } $$ mpfr_mul((d)->y, (a)->y, (r), MPFR_RNDN); $$
```

Multiplies the complex number a to the real number r and stores the result in d.

Definition at line 123 of file comp.h.

# 5.13.2.11 comp\_mulu

```
#define comp_mulu( d, a, i )
```

#### Value:

```
\label{eq:mpfr_mul_ui} $$ mpfr_mul_ui((d) -> x, (a) -> x, (i), MPFR_RNDN); $$ mpfr_mul_ui((d) -> y, (a) -> y, (i), MPFR_RNDN); $$
```

Multiplies the complex number a to the unsigned integer i and stores the result in d.

Definition at line 131 of file comp.h.

# 5.13.2.12 comp\_neg

## Value:

```
\label{eq:mpfr_neg(d)->x, (a)->x, MPFR_RNDN); $$ mpfr_neg(d)->y, (a)->y, MPFR_RNDN); $$
```

Sets d to -a.

Definition at line 76 of file comp.h.

# 5.13.2.13 comp\_set

```
#define comp_set( d, a)
```

Value:

```
\label{local_mpfr_set(d)-x, (a)-x, MPFR_RNDN);} $$ mpfr_set((d)-y, (a)-y, MPFR_RNDN); $$
```

Sets d to a.

Definition at line 68 of file comp.h.

# 5.13.2.14 comp\_setr

Value:

```
\label{eq:mpfr_set_norm} \begin{array}{lll} \text{mpfr\_set((d)->x, (a), MPFR\_RNDN);} & \\ \text{mpfr\_set\_zero((d)->y, 1);} \end{array}
```

Sets d to the real value a.

Definition at line 72 of file comp.h.

# 5.13.2.15 comp\_sqr

Value:

```
mpfr_sqr((buf), (a)->y, MPFR_RNDN); \
mpfr_mul((d)->y, (a)->x, (a)->y, MPFR_RNDN); \
mpfr_mul_2si((d)->y, (d)->y, 1, MPFR_RNDN); \
mpfr_sqr((d)->x, (a)->x, MPFR_RNDN); \
mpfr_sub((d)->x, (d)->x, (buf), MPFR_RNDN);
```

Squares a and stores the result in d, all of type comp or comp\_ptr.

Definition at line 135 of file comp.h.

## 5.13.2.16 comp\_sub

```
#define comp_sub(
          d,
          a,
          b)
```

Value:

```
\label{eq:mpfr_sub((d)->x, (a)->x, (b)->x, MPFR_RNDN); $$ mpfr_sub((d)->y, (a)->y, (b)->y, MPFR_RNDN); $$
```

Subtracts b from a and stores the result in d, all of type comp or comp\_ptr.

Definition at line 90 of file comp.h.

# 5.13.2.17 comp\_subr

```
#define comp_subr(
          d,
          a,
          r )
```

Value:

```
\label{linear_mpfr_sub((d)->x, (a)->x, (r), MPFR_RNDN); $$ mpfr_set((d)->y, (a)->y, MPFR_RNDN);$}
```

Subtracts the real number b from the complex number a and stores the result in d.

Definition at line 94 of file comp.h.

# 5.13.3 Typedef Documentation

## 5.13.3.1 comp

```
typedef comp_struct comp[1]
```

Practical wrapper for comp\_struct.

To avoid the constant use \* and & the type  $\mathtt{compf}$  is a pointer.

Definition at line 39 of file comp.h.

# 5.13.4 Function Documentation

# 5.13.4.1 comp\_log2()

```
\begin{tabular}{ll} real\_t & comp\_log2 & ( \\ & comp & z & ) \end{tabular}
```

Computes the base  $2 \log of |z|$ .

**Parameters** 

z the complex number

Returns

log\_2(|**z**|)

# 5.13.4.2 comp\_s()

```
real_t comp_s ( {\tt comp} \ z \ )
```

Computes s(z).

See also

[1]

**Parameters** 

z the complex number

Returns

[log\_2(|z|)]+1

# 5.13.4.3 mpfr\_s()

Computes s(x).

See also

[1]

**Parameters** 

x the real number

```
Returns
```

```
[log_2(|z|)]+1
```

# 5.13.4.4 real\_log2()

```
real_t real_log2 (
          mpfr_t x )
```

Computes the base  $2 \log of |x|$ .

#### **Parameters**

```
x the real number
```

#### Returns

$$log_2(|x|)$$

# 5.14 /home/runner/work/FastPolyEval/FastPoly Eval/code/numbers/compf.h File Reference

Definition of machine complex numbers.

# **Data Structures**

· struct compf\_struct

Machine complex numbers.

# **Macros**

```
• #define compf set(d, a)
```

Sets d to a.

• #define compf\_setr(d, a)

Sets d to the real value a.

• #define compf\_neg(d, a)

Sets d to -a.

• #define compf\_add(d, a, b)

Adds a to b and stores the result in d, all of type compf or compf\_ptr.

• #define compf\_addr(d, a, r)

Adds the complex number a to the real number b and stores the result in d.

#define compf\_sub(d, a, b)

Subtracts b from a and stores the result in d, all of type compf or compf\_ptr.

• #define compf\_subr(d, a, r)

Subtracts the real number b from the complex number a and stores the result in d.

- #define compf\_mul(d, a, b)
- #define compf\_mulr(d, a, r)

Multiplies the complex number a to the real number r and stores the result in d.

• #define compf amr(d, a, r)

Adds the complex number a\*r to d, where d,a are complex and r is real.

• #define compf sqr(d, a)

Squares a and stores the result in d, all of type compf or compf\_ptr.

• #define compf\_div(d, a, b)

Divides a by b and stores the result in d, all of type compf or compf\_ptr.

#define compf\_mod(a) fhypot((a)->x, (a)->y)

Computes the modulus of the complex number a.

• #define  $compf_dist(a, b)$  fhypot((a)->x - (b)->x, (a)->y - (b)->y)

Computes the distance between the complex numbera a and b.

- #define compf mod2(a) ((a)->x\*(a)->x+(a)->y\*(a)->y)
- #define compf\_log2(a) (plog2(compf\_mod(a)))

Computes the log\_2 of the modulus of the complex number a.

#define coeff\_log2(a) (plog2((a) < 0 ? -(a) : (a)))</li>

Computes the log 2 of the absolute value of the real number a.

#define compf\_s(a) (pfloor(plog2(compf\_mod(a))) + 1)

Computes the scale of the complex number a, see [1].

#define coeff\_s(a) (pfloor(coeff\_log2(a)) + 1)

Computes the scale of the real number a, see [1].

# **Typedefs**

typedef compf struct compf[1]

Practical wrapper for compf\_struct.

• typedef compf\_struct \* compf\_ptr

Convenience pointer to compf\_struct.

# 5.14.1 Detailed Description

Definition of machine complex numbers.

#### 5.14.2 Macro Definition Documentation

## 5.14.2.1 compf add

# Value:

(d) 
$$->x = (a) ->x + (b) ->x;$$
  
(d)  $->y = (a) ->y + (b) ->y;$ 

Adds a to b and stores the result in d, all of type compf or compf ptr.

Definition at line 63 of file compf.h.

# 5.14.2.2 compf\_addr

Value:

$$(d) -> x = (a) -> x + (r); \ (d) -> y = (a) -> y;$$

Adds the complex number  ${\tt a}$  to the real number  ${\tt b}$  and stores the result in  ${\tt d}$ .

Definition at line 67 of file compf.h.

# 5.14.2.3 compf\_amr

Value:

(d) 
$$->x += (a) ->x * (r); (d) ->y += (a) ->y * (r);$$

Adds the complex number a\*r to d, where d,a are complex and r is real.

Definition at line 87 of file compf.h.

# 5.14.2.4 compf\_div

Value:

Divides a by b and stores the result in d, all of type compf or compf\_ptr.

Definition at line 96 of file compf.h.

# 5.14.2.5 compf\_mod2

Computes the square of the modulus of the complex number a.

Warning

There is a danger of overflow, better use the slower compf\_mod () instead.

Definition at line 111 of file compf.h.

# 5.14.2.6 compf\_mul

Value:

```
coeff_t px = (a)->x * (b)->x - (a)->y * (b)->y; \ (d)->y = (a)->x * (b)->y + (a)->y * (b)->x; \ (d)->x = px;
```

Definition at line 78 of file compf.h.

# 5.14.2.7 compf\_mulr

Value:

$$(d) -> x = (a) -> x * (r); \ (d) -> y = (a) -> y * (r);$$

Multiplies the complex number a to the real number r and stores the result in d.

Definition at line 83 of file compf.h.

# 5.14.2.8 compf\_neg

Value:

(d) 
$$->x = -(a) ->x;$$
 \  
(d)  $->y = -(a) ->y;$ 

Sets d to -a.

Definition at line 59 of file compf.h.

# 5.14.2.9 compf\_set

Value:

(d) 
$$->x = (a) ->x;$$
 \  
(d)  $->y = (a) ->y;$ 

Sets d to a.

Definition at line 51 of file compf.h.

# 5.14.2.10 compf\_setr

```
#define compf_setr(
          d,
          a )
```

Value:

(d) 
$$->x = (a); \setminus (d) ->y = 0;$$

Sets d to the real value a.

Definition at line 55 of file compf.h.

# 5.14.2.11 compf\_sqr

Value:

Squares a and stores the result in d, all of type compf or compf\_ptr.

Definition at line 91 of file compf.h.

# 5.14.2.12 compf\_sub

Value:

(d) 
$$->x = (a) ->x - (b) ->x;$$
 \ (d)  $->y = (a) ->y - (b) ->y;$ 

Subtracts b from a and stores the result in d, all of type compf or compf\_ptr.

Definition at line 71 of file compf.h.

# 5.14.2.13 compf\_subr

Value:

(d) 
$$->x = (a) ->x - (r); \ (d) ->y = (a) ->y;$$

Subtracts the real number b from the complex number a and stores the result in d.

Definition at line 75 of file compf.h.

# 5.14.3 Typedef Documentation

## 5.14.3.1 compf

```
typedef compf_struct compf[1]
```

Practical wrapper for compf\_struct.

To avoid the constant use \* and & the type  $\mathtt{compf}$  is a pointer.

# Example of use:

```
compf c;
polyf cx = c->x;
```

Definition at line 43 of file compf.h.

# 5.15 /home/runner/work/FastPolyEval/FastPoly Eval/code/numbers/ntypes.h File Reference

Definition of basic types.

## **Macros**

· #define true 1

Boolean value true.

· #define false 0

Boolean value false.

• #define PI (3.14159265358979323846264338327950288L)

 $\pi$  with fp80 precision

- #define flog2 log2
- · #define fhypot hypot
- · #define ffloor floor
- #define **fpow** pow
- #define **fexp** exp
- #define fsin sin
- #define fcos cos
- #define ftan tan
- · #define mpfr getf mpfr get d
- #define precf 53
- #define PRECF\_STR "53"
- #define TYPEFP STR "FP64"
- #define TYPEF\_STR "double"
- #define INF\_M (-HUGE\_VAL)
- #define INF\_P HUGE VAL
- #define FMT\_COEFF "I"
- #define MAX\_EXP (sizeof(coeff\_t) == 8 ? 960 : 16320)
- #define HUGE DEGREES
- #define MAX\_DEG (UINT64\_MAX 1)
- #define FMT\_DEG PRIu64
- #define plog2 log2
- #define pexp2 exp2
- #define **phypot** hypot
- #define **pfloor** floor
- · #define pceil ceil
- #define mpfr\_getp mpfr\_get\_d
- #define **PEPS** 1E-200
- #define PDEL 1E-12
- · #define pexp exp
- · #define pcos cos
- #define psin sin
- #define ptan tan
- #define pldexp ldexp
- #define **pfrexp** frexp
- #define FMT\_REAL "I"
- #define HUGE\_PREC
- #define MAX\_PREC (16000000000000000000UL)
- #define HUGE\_MP\_EXP
- #define MAX\_MP\_EXP (400000000000000000L)

The integer number type to use for polynomial degrees and indexes.

- #define NEWTON CONV BITS 5
- #define NEWTON\_ESCAPE\_BITS 4

# **Typedefs**

typedef uint8\_t byte

byte **is** uint8

typedef uint16\_t word

word **is** uint16

· typedef uint32\_t uint

uint **is** uint 32

• typedef uint64\_t ulong

ulong **is** uint 64

· typedef byte bool

Logic type bool can take values true or false.

· typedef double coeff\_t

The machine number type to use for polynomial coefficients and evaluation.

· typedef ulong deg\_t

The integer number type to use for polynomial degrees and indexes.

typedef double real t

The machine number type to use for polynomial analysis and preconditionning.

typedef ulong prec\_t

The integer number type to use for polynomial degrees and indexes.

## **Functions**

bool ntypes\_check (void)

Use this function to check the compatibility of the machine with the settings above.

real\_t bits\_sum (real\_t b1, real\_t b2)

Computes  $log_2(2^b1+2^b2)$ , even if b1 or b2 are outside the exponent range of real\_t.

real\_t nt\_err (real\_t vb, real\_t evb, real\_t db, real\_t edb)

Computes log\_2 (ntErr), where ntErr is an upper bound for the error of the Newton term.

# 5.15.1 Detailed Description

Definition of basic types.

# 5.15.2 Function Documentation

# 5.15.2.1 bits\_sum()

Computes log\_2(2^b1+2^b2), even if b1 or b2 are outside the exponent range of real\_t.

#### **Parameters**

b1	first operand, in bits
b2	second operand, in bits

## Returns

the bits sum of the operands, that is the base 2 log of their base 2 exponentials

## 5.15.2.2 nt\_err()

Computes log\_2 (ntErr), where ntErr is an upper bound for the error of the Newton term.

#### **Parameters**

vb	log_2( value )
evb	log_2(valErr)
db	log_2( derivative )
edb	log_2(derErr)

## Returns

absolute error of the Newton term, as a power of 2

# 5.16 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/poly.h File Reference

Definition of complex polynomials with arbitary precision coefficients.

# **Data Structures**

struct poly\_struct

Polynomial with multi-precision floating point complex coefficients.

# **Typedefs**

typedef poly\_struct poly\_t[1]

Practical wrapper for poly\_struct.

typedef poly\_struct \* poly

Convenience pointer to  $poly\_struct$ .

## **Functions**

```
• poly poly new (deg t degree, prec t prec)
```

Returns a new complex polynomial of given degree, with coefficients of precision prec.

poly poly\_from\_roots (comp\_ptr roots, deg\_t degree, prec\_t prec)

Returns a new complex polynomial given the list of its roots, with coefficients of precision prec.

bool poly\_free (poly P)

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $poly_new()$ .

bool poly\_set (poly P, comp coeff, deg\_t ind)

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

• bool poly\_eval (comp res, poly P, comp z)

Evaluates P (z) using Horner's method.

bool poly\_eval\_r (comp res, poly P, mpfr\_t x)

Evaluates P(x) using Horner's method.

poly poly\_derivative (poly P)

Computes the derivative of P.

poly poly\_sum (poly P, poly Q)

Computes P+Q.

poly poly\_diff (poly P, poly Q)

Computes P-Q.

poly poly\_prod (poly P, poly Q)

Computes P\*Q.

poly poly\_sqr (poly P)

Computes the square of P.

# 5.16.1 Detailed Description

Definition of complex polynomials with arbitary precision coefficients.

# 5.16.2 Typedef Documentation

## 5.16.2.1 poly t

```
typedef poly_struct poly_t[1]
```

Practical wrapper for poly\_struct.

To avoid the constant use \* and & the type  $\texttt{poly\_t}$  is a pointer.

Definition at line 43 of file poly.h.

## 5.16.3 Function Documentation

## 5.16.3.1 poly\_derivative()

```
poly poly_derivative ( poly P)
```

Computes the derivative of P.

# **Parameters**

```
P the polynomial
```

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.16.3.2 poly\_diff()

```
poly poly_diff ( \label{eq:poly_P} \text{poly } P, \\ \text{poly } \mathcal{Q} \ )
```

Computes P-Q.

# **Parameters**

Р	a polynomial
Q	another polynomial

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.16.3.3 poly\_eval()

Evaluates P(z) using Horner's method.

# **Parameters**

res	the result
Р	the polynomial
Z	the argument

## Returns

true if successfull, false otherwise.

# 5.16.3.4 poly\_eval\_r()

Evaluates P (x) using Horner's method.

#### **Parameters**

res	the result
Р	the polynomial
X	the real argument

#### Returns

true if successfull, false otherwise.

# 5.16.3.5 poly\_free()

```
bool poly_free (
          poly P )
```

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $poly_new()$ .

#### **Parameters**

P the polynomia	al
-----------------	----

## Returns

true if successfull, false otherwise.

# 5.16.3.6 poly\_from\_roots()

Returns a new complex polynomial given the list of its roots, with coefficients of precision prec.

## Warning

prec must be at least precf

# **Parameters**

roots	the roots of the polynomial
degree	the degree of the polynomial
prec	the precision of the coefficients, in bits

# Returns

the new polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.16.3.7 poly\_new()

Returns a new complex polynomial of given degree, with coefficients of precision prec.

# Warning

prec must be at least precf

## **Parameters**

degree	the degree of the polynomial
prec	the precision of the coefficients, in bits

# Returns

the new polynomial,  $\mathtt{NULL}$  if the degree is larger than  $\mathtt{MAX\_DEG}.$ 

# 5.16.3.8 poly\_prod()

```
poly poly_prod ( \label{eq:poly_prod} \text{poly } P, \\ \text{poly } \mathcal{Q} \ )
```

# Computes P\*Q.

## **Parameters**

Р	a polynomial
Q	another polynomial

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.16.3.9 poly\_set()

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

# **Parameters**

Р	the polynomial
coeff	the coefficient
ind	the index

# Returns

true if successfull, false otherwise.

# 5.16.3.10 poly\_sqr()

```
poly poly_sqr (
          poly P )
```

Computes the square of P.

# **Parameters**

```
P the polynomial
```

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.16.3.11 poly\_sum()

```
poly poly_sum (  \begin{array}{c} \text{poly } P, \\ \text{poly } Q \end{array} )
```

Computes P+Q.

#### **Parameters**

Р	a polynomial
Q	another polynomial

#### Returns

the resulted polynomial, NULL if some error occurred.

# 5.17 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/polyf.h File Reference

Definition of complex polynomials with machine floating point coefficients.

# **Data Structures**

· struct polyf\_struct

Polynomial with machine floating point complex coefficients.

# **Typedefs**

typedef polyf\_struct polyf\_t[1]

Practical wrapper for polyf\_struct.

typedef polyf\_struct \* polyf

Convenience pointer to  $polyf\_struct$ .

## **Functions**

polyf polyf new (deg t degree)

Returns a new complex polynomial of given degree, with machine floating point coefficients.

• polyf polyf\_from\_roots (compf\_ptr roots, deg\_t degree)

Returns a new complex polynomial given the list of its roots, with machine floating point coefficients.

bool polyf\_free (polyf P)

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $polyr_new()$ .

bool polyf\_set (polyf P, compf coeff, deg\_t ind)

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

bool polyf\_eval (compf res, polyf P, compf z)

Evaluates P (z) using Horner's method.

bool polyf\_eval\_r (compf res, polyf P, coeff\_t x)

Evaluates P(x) using Horner's method.

polyf polyf\_derivative (polyf P)

Computes the derivative of P.

polyf polyf\_sum (polyf P, polyf Q)

Computes P+Q.

polyf polyf\_diff (polyf P, polyf Q)

Computes P-Q.

• polyf polyf\_prod (polyf P, polyf Q)

Computes P\*Q.

polyf polyf\_sqr (polyf P)

Computes the square of P.

# 5.17.1 Detailed Description

Definition of complex polynomials with machine floating point coefficients.

# 5.17.2 Typedef Documentation

# 5.17.2.1 polyf\_t

```
typedef polyf_struct polyf_t[1]
```

Practical wrapper for polyf\_struct.

To avoid the constant use \* and & the type polyf\_t is a pointer.

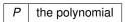
Definition at line 39 of file polyf.h.

# 5.17.3 Function Documentation

# 5.17.3.1 polyf\_derivative()

Computes the derivative of P.

# **Parameters**



# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.17.3.2 polyf\_diff()

```
polyf polyf_diff ( \label{eq:polyf_P} \text{polyf P,} \\ \text{polyf } \mathcal{Q} \ )
```

Computes P-Q.

# **Parameters**

Р	a polynomial
Q	another polynomial

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.17.3.3 polyf\_eval()

Evaluates P(z) using Horner's method.

## **Parameters**

res	the result
Р	the polynomial
Z	the argument

# Returns

true if successfull, false otherwise.

# 5.17.3.4 polyf\_eval\_r()

Evaluates P(x) using Horner's method.

# **Parameters**

res	the result
Р	the polynomial
Х	the real argument

#### Returns

true if successfull, false otherwise.

# 5.17.3.5 polyf\_free()

```
bool polyf_free (
          polyf P )
```

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $polyr\_new()$ .

#### **Parameters**

```
P the polynomial
```

## Returns

true if successfull, false otherwise.

# 5.17.3.6 polyf\_from\_roots()

Returns a new complex polynomial given the list of its roots, with machine floating point coefficients.

# **Parameters**

roots	the roots of the polynomial
degree	the degree of the polynomial

## Returns

the new polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.17.3.7 polyf\_new()

Returns a new complex polynomial of given degree, with machine floating point coefficients.

# **Parameters**

f the polynomial

# Returns

the new polynomial,  $\mathtt{NULL}$  if the degree is larger than  $\mathtt{MAX\_DEG}$ .

# 5.17.3.8 polyf\_prod()

```
polyf polyf_prod ( \label{eq:polyf_prod} \operatorname{polyf} P, \\ \operatorname{polyf} \ \mathcal{Q} \ )
```

Computes P\*Q.

# **Parameters**

Р	a polynomial
Q	another polynomial

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.17.3.9 polyf\_set()

Sets the coefficient of the polynomial  ${\tt P}$  corresponding to the power  ${\tt ind}$  to  ${\tt coeff}.$ 

# **Parameters**

Р	the polynomial
coeff	the coefficient
ind	the index

## Returns

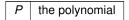
true if successfull, false otherwise.

# 5.17.3.10 polyf\_sqr()

```
polyf polyf_sqr (
          polyf P )
```

Computes the square of  $\ensuremath{\mathbb{P}}$ .

# **Parameters**



## Returns

the resulted polynomial, NULL if some error occurred.

# 5.17.3.11 polyf\_sum()

```
polyf polyf_sum (  \label{eq:polyf_polyf_polyf}  \mbox{polyf $P$,}   \mbox{polyf $Q$ )}
```

Computes P+Q.

# **Parameters**

P	a polynomial
Q	another polynomial

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/polyfr.h File Reference

Definition of real polynomials with machine floating point coefficients.

# **Data Structures**

struct polyfr\_struct

Polynomial with machine floating point real coefficients.

# **Typedefs**

typedef polyfr\_struct polyfr\_t[1]

Practical wrapper for polyfr\_struct.

typedef polyfr\_struct \* polyfr

Convenience pointer to polyfr\_struct.

## **Functions**

• polyfr\_new (deg\_t degree)

Returns a new real polynomial of given degree, with machine floating point coefficients.

bool polyfr\_free (polyfr P)

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $polyfr_new()$ .

bool polyfr\_set (polyfr P, coeff\_t coeff, deg\_t ind)

Sets the coefficient corresponding to the power ind to coeff.

coeff\_t polyfr\_get (polyfr P, deg\_t ind)

Returns the coefficient corresponding to the power ind.

bool polyfr\_eval\_c (compf res, polyfr P, compf z)

Evaluates P(z) using Horner's method.

coeff\_t polyfr\_eval (polyfr P, coeff\_t x)

Evaluates P (x) using Horner's method.

• polyf polyfr comp (polyfr P)

Return a complex version of the real polynomial P.

• polyfr polyfr\_derivative (polyfr P)

Computes the derivative of P.

• polyfr polyfr sum (polyfr P, polyfr Q)

Computes P+Q.

polyfr polyfr\_diff (polyfr P, polyfr Q)

Computes P-Q.

• polyfr polyfr\_prod (polyfr P, polyfr Q)

Computes P\*Q.

polyfr polyfr\_sqr (polyfr P)

Computes the square of P.

• polyfr polyf\_hyp (int n)

Computes the n-th hyperbolic polynomial, the n-th image of 0 under the iteration of  $z->z^{\wedge}2+c$ . It is a polynomial of degree  $2^{\wedge} \{n-1\}$  in c.

• polyfr polyf\_cheb (int n)

Computes the Chebyshev polynomial of degree n.

polyfr polyf\_leg (int n)

Computes the Legendre polynomial of degree n.

polyfr polyf\_her (int n)

Computes the Hermite polynomial of degree  $\it n$ .

polyfr polyf\_lag (int n)

Computes the Laguerre polynomial of degree n.

# 5.18.1 Detailed Description

Definition of real polynomials with machine floating point coefficients.

# 5.18.2 Typedef Documentation

# 5.18.2.1 polyfr\_t

```
typedef polyfr_struct polyfr_t[1]
```

Practical wrapper for polyfr\_struct.

To avoid the constant use \* and & the type polyfr\_t is a pointer.

Definition at line 40 of file polyfr.h.

# 5.18.3 Function Documentation

# 5.18.3.1 polyf\_cheb()

```
polyfr polyf_cheb ( int n)
```

Computes the Chebyshev polynomial of degree n.

## **Parameters**

```
n the degree of the polynomial
```

#### Returns

the Chebyshev polynomial,  $\mathtt{NULL}$  if some error occurred.

## 5.18.3.2 polyf\_her()

```
polyfr polyf_her (
          int n)
```

Computes the Hermite polynomial of degree n.

#### **Parameters**

n the degree of the polynomial

## Returns

the Hermite polynomial, NULL if some error occurred.

# 5.18.3.3 polyf\_hyp()

```
polyfr polyf_hyp ( int \ n \ )
```

Computes the n-th hyperbolic polynomial, the n-th image of 0 under the iteration of  $z->z^2+c$ . It is a polynomial of degree  $2^{n-1}$  in c.

## **Parameters**

```
n the order of the polynomial
```

## Returns

the hyperbolic polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18.3.4 polyf\_lag()

```
polyfr polyf_lag ( int \ n \ )
```

Computes the Laguerre polynomial of degree  $\ensuremath{n}$ .

# **Parameters**

```
n the degree of the polynomial
```

# Returns

the Laguerre polynomial, NULL if some error occurred.

# 5.18.3.5 polyf\_leg()

```
polyfr polyf_leg ( int n)
```

Computes the Legendre polynomial of degree n.

#### **Parameters**

n the degree of the polynomial

# Returns

the Legendre polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18.3.6 polyfr\_comp()

Return a complex version of the real polynomial  $\ensuremath{\mathbb{P}}$ .

# **Parameters**

```
P a polynomial
```

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18.3.7 polyfr\_derivative()

```
polyfr polyfr_derivative ( polyfr P )
```

Computes the derivative of P.

## **Parameters**

```
P the polynomial
```

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18.3.8 polyfr\_diff()

```
polyfr polyfr_diff ( \label{eq:polyfr_diff} \text{polyfr } P, \\ \text{polyfr } \mathcal{Q} \ )
```

# Computes P-Q.

## **Parameters**

Р	a polynomial
Q	another polynomial

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18.3.9 polyfr\_eval()

Evaluates P(x) using Horner's method.

# **Parameters**

Р	the polynomial
Χ	the argument

## Returns

the result, NaN if some error occurred.

# 5.18.3.10 polyfr\_eval\_c()

Evaluates P(z) using Horner's method.

# **Parameters**

res	the result
Р	the polynomial
Z	the argument

#### Returns

true if successfull, false otherwise.

# 5.18.3.11 polyfr\_free()

```
bool polyfr_free ( polyfr\ \textit{P}\ )
```

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $polyfr_new()$ .

#### **Parameters**

```
P the polynomial
```

#### Returns

true if successfull, false otherwise.

## 5.18.3.12 polyfr\_get()

Returns the coefficient corresponding to the power ind.

## **Parameters**

Р	the polynomial
ind	the index

# Returns

the coefficient corresponding to the power ind.

## 5.18.3.13 polyfr\_new()

Returns a new real polynomial of given degree, with machine floating point coefficients.

## **Parameters**

degree   the degree of the polynomial	degree	the degree of the polynomial
---------------------------------------	--------	------------------------------

# Returns

the new polynomial,  $\mathtt{NULL}$  if the degree is larger than  $\mathtt{MAX\_DEG}.$ 

# 5.18.3.14 polyfr\_prod()

```
polyfr polyfr_prod ( \label{eq:polyfr_prod} \text{polyfr } P, \\ \text{polyfr } \mathcal{Q} \ )
```

Computes P\*Q.

## **Parameters**

Р	a polynomial
Q	another polynomial

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.18.3.15 polyfr\_set()

Sets the coefficient corresponding to the power  $\verb"ind" to \verb"coeff".$ 

# **Parameters**

Р	the polynomial
coeff	the coefficient
ind	the index

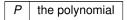
#### Returns

true if successfull, false otherwise.

# 5.18.3.16 polyfr\_sqr()

Computes the square of  $\mbox{\ensuremath{\mathbb{P}}}.$ 

## **Parameters**



#### Returns

the resulted polynomial, NULL if some error occurred.

# 5.18.3.17 polyfr\_sum()

```
polyfr polyfr_sum (  \label{eq:polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_polyfr_poly
```

Computes P+Q.

# **Parameters**

Р	a polynomial
Q	another polynomial

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19 /home/runner/work/FastPolyEval/FastPolyEval/code/poly/polyr.h File Reference

Definition of real polynomials with arbitary precision coefficients.

# **Data Structures**

• struct polyr\_struct

Polynomial with multi-precision floating point complex coefficients.

# **Typedefs**

```
    typedef polyr_struct polyr_t[1]
        Practical wrapper for polyr_struct.

    typedef polyr_struct * polyr
        Convenience pointer to polyr_struct.
```

#### **Functions**

• polyr polyr\_new (deg\_t degree, prec\_t prec)

Returns a new real polynomial of given degree, with coefficients of precision prec.

bool polyr free (polyr P)

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $polyr_new()$ .

bool polyr\_set (polyr P, mpfr\_t coeff, deg\_t ind)

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

bool polyr\_seti (polyr P, long coeff, deg\_t ind)

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

• bool polyr\_eval\_c (comp res, polyr P, comp z)

Evaluates P (z) using Horner's method.

bool polyr\_eval (mpfr\_t res, polyr P, mpfr\_t x)

Evaluates P(x) using Horner's method.

polyr polyr\_derivative (polyr P)

Computes the derivative of P.

polyr polyr\_sum (polyr P, polyr Q)

Computes P+Q.

polyr polyr\_diff (polyr P, polyr Q)

Computes P-Q.

• polyr polyr\_prod (polyr P, polyr Q)

Computes P\*Q.

polyr polyr\_sqr (polyr P)

Computes the square of P.

• polyr poly\_hyp (int n, prec\_t prec)

Computes the n-th hyperbolic polynomial, the n-th image of 0 under the iteration of  $z->z^{\wedge}2+c$ . It is a polynomial of degree  $2^{\wedge} \{n-1\}$  in c.

• polyr poly\_cheb (int n, prec\_t prec)

Computes the Chebyshev polynomial of degree n.

polyr poly\_leg (int n, prec\_t prec)

Computes the Legendre polynomial of degree n.

polyr poly\_her (int n, prec\_t prec)

Computes the Hermite polynomial of degree n.

• polyr poly\_lag (int n, prec\_t prec)

Computes the Laguerre polynomial of degree n.

# 5.19.1 Detailed Description

Definition of real polynomials with arbitary precision coefficients.

# 5.19.2 Typedef Documentation

# 5.19.2.1 polyr\_t

```
typedef polyr_struct polyr_t[1]
```

Practical wrapper for polyr\_struct.

To avoid the constant use \* and & the type polyr\_t is a pointer.

Definition at line 43 of file polyr.h.

## 5.19.3 Function Documentation

# 5.19.3.1 poly\_cheb()

```
polyr poly_cheb (
          int n,
          prec_t prec )
```

Computes the Chebyshev polynomial of degree n.

#### **Parameters**

n	the degree of the polynomial
prec	the precision of the coefficients

# Returns

the Chebyshev polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.2 poly\_her()

```
polyr poly_her (
          int n,
          prec_t prec )
```

Computes the Hermite polynomial of degree  ${\tt n}.$ 

## **Parameters**

n	the degree of the polynomial
prec	the precision of the coefficients

## Returns

the Hermite polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.3 poly\_hyp()

```
polyr poly_hyp (
          int n,
          prec_t prec )
```

Computes the n-th hyperbolic polynomial, the n-th image of 0 under the iteration of  $z->z^2+c$ . It is a polynomial of degree  $2^{n-1}$  in c.

#### **Parameters**

n	the order of the polynomial
prec	the precision of the coefficients

### Returns

the hyperbolic polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.4 poly\_lag()

Computes the Laguerre polynomial of degree  ${\tt n}.$ 

## **Parameters**

n	the degree of the polynomial
prec	the precision of the coefficients

# Returns

the Laguerre polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.5 poly\_leg()

```
polyr poly_leg (
          int n,
          prec_t prec )
```

Computes the Legendre polynomial of degree n.

# **Parameters**

n	the degree of the polynomial
prec	the precision of the coefficients

#### Returns

the Legendre polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.6 polyr\_derivative()

Computes the derivative of  ${\mathbb P}.$ 

#### **Parameters**

Р	the polynomial
---	----------------

# Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.7 polyr\_diff()

```
polyr polyr_diff ( \label{eq:polyr_P} \text{polyr } P, \\ \text{polyr } \mathcal{Q} \ )
```

Computes P-Q.

### **Parameters**

Р	a polynomial
Q	another polynomial

#### Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.8 polyr\_eval()

Evaluates P(x) using Horner's method.

## **Parameters**

res	the result
Р	the polynomial
Х	the real argument

#### Returns

true if successfull, false otherwise.

# 5.19.3.9 polyr\_eval\_c()

Evaluates  ${\tt P}$  (  ${\tt z}$  ) using Horner's method.

#### **Parameters**

res	the result
Р	the polynomial
Z	the argument

# Returns

true if successfull, false otherwise.

## 5.19.3.10 polyr\_free()

```
bool polyr_free (
          polyr P )
```

Frees all the memory used by the polynomial P, assuming the struct has been allocated with malloc(), for example with  $polyr\_new()$ .

## **Parameters**

P the polynomial	
------------------	--

#### Returns

true if successfull, false otherwise.

## 5.19.3.11 polyr\_new()

Returns a new real polynomial of given degree, with coefficients of precision prec.

# Warning

prec must be at least precf and the degree at most MAX\_DEG.

#### **Parameters**

degree	the degree of the polynomial
prec	the precision of the coefficients, in bits

#### Returns

the new buffer,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.12 polyr\_prod()

```
polyr polyr_prod ( \label{eq:polyr_prod} \text{polyr } P, \\ \text{polyr } \mathcal{Q} \ )
```

Computes P∗Q.

## **Parameters**

Р	a polynomial
Q	another polynomial

#### Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.19.3.13 polyr\_set()

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

#### **Parameters**

Р	the polynomial
coeff	the coefficient
ind	the index

#### Returns

true if successfull, false otherwise.

# 5.19.3.14 polyr\_seti()

Sets the coefficient of the polynomial P corresponding to the power ind to coeff.

# **Parameters**

P	the polynomial
coeff	the coefficient
ind	the index

#### Returns

true if successfull, false otherwise.

# 5.19.3.15 polyr\_sqr()

```
polyr polyr_sqr (
          polyr P )
```

Computes the square of P.

#### **Parameters**

#### Returns

the resulted polynomial, NULL if some error occurred.

## 5.19.3.16 polyr\_sum()

Computes P+Q.

## Parameters

Р	a polynomial
Q	another polynomial

## Returns

the resulted polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.20 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/array.h File Reference

Definition of a variable length array of arbitary precision complex numbers that are based on mpfr.

# **Data Structures**

· struct array\_struct

A variable length array of machine floating point complex numbers.

#### **Macros**

- #define ARRAY\_MIN\_SIZE 100
- #define ARRAY SIZE INCREASE 1.25

# **Typedefs**

• typedef array struct array t[1]

Practical wrapper for array\_struct.

typedef array struct \* array

Convenience pointer to array\_struct.

#### **Functions**

• array array\_new (ulong size)

Returns a new empty array with memory size at least size.

array array\_new\_polyr (polyr P, prec\_t prec)

Returns the array of coefficients of the real polynomial P.

array array\_new\_poly (poly P, prec\_t prec)

Returns the array of coefficients of the polynomial P.

• bool array\_free (array I)

Frees all the memory used by the array 1, assuming the struct has been allocated with malloc(), for example with  $array_new()$ .

bool array\_add (array I, comp z, prec\_t prec)

Adds the complex number z at the end of the array. The size of the array is automatically increased, if needed.

comp\_ptr array\_get (array I, ulong pos)

Returns the pointer of the element on position pos in the array 1.

bool array\_is\_real (array I)

Checks if all complex numbers in the array 1 are real.

long array\_first\_inf (array I)

Checks if there are infinite values in the list 1.

long array\_first\_nan (array l)

Checks if all complex numbers in the list 1 are well defined.

polyr array\_polyr (array I, prec\_t prec)

Returns the real polynomial with the coefficients the real parts of the complex numbers in the array 1.

poly array\_poly (array I, prec\_t prec)

Returns the polynomial with the coefficients in the array 1.

• bool array\_write (array I, char \*fileName, int digits, bool verbose)

Writes the array 1 to a CSV file with the given path fileName.

bool array\_append (array I, char \*fileName, int digits, bool verbose)

Writes the array 1 to the end of a CSV file with the given path fileName.

• array array\_read (char \*fileName, prec\_t prec, bool verbose)

Reads a array of complex numbers of precision prec from the CSV file with path fileName.

# 5.20.1 Detailed Description

Definition of a variable length array of arbitary precision complex numbers that are based on mpfr.

# 5.20.2 Typedef Documentation

# 5.20.2.1 array\_t

```
typedef array_struct array_t[1]
```

Practical wrapper for array\_struct.

To avoid the constant use \* and & the type <code>array\_t</code> is a pointer.

Definition at line 46 of file array.h.

## 5.20.3 Function Documentation

# 5.20.3.1 array\_add()

Adds the complex number z at the end of the array. The size of the array is automatically increased, if needed.

## **Parameters**

1	the array
Z	the new element to add to the array
prec	the precision of the number in the array

#### Returns

true if successfull, false otherwise.

# 5.20.3.2 array\_append()

Writes the array 1 to the end of a CSV file with the given path fileName.

#### **Parameters**

1	the array
fileName	the path of the CSV file
digits	the number of digits after the decimal point of the numbers in the file
verbose	true to print information about the error, if any

## Returns

true if successfull, false otherwise.

# 5.20.3.3 array\_first\_inf()

Checks if there are infinite values in the list 1.

#### **Parameters**

/ the list

## Returns

the position of the first infinite value in 1, -1 if there is none, LONG\_MAX if some error occurred.

# 5.20.3.4 array\_first\_nan()

Checks if all complex numbers in the list 1 are well defined.

## **Parameters**

I the list

## Returns

the position of the first undefined value in 1, -1 if there is none, LONG\_MAX if some error occurred.

## 5.20.3.5 array\_free()

Frees all the memory used by the array 1, assuming the struct has been allocated with malloc(), for example with  $array_new()$ .

## **Parameters**

```
I the array
```

#### Returns

true if successfull, false otherwise.

## 5.20.3.6 array\_get()

Returns the pointer of the element on position pos in the array 1.

#### **Parameters**

1	the array
pos	the position of the element

## Returns

the pointer to the element on position pos in 1, NULL if some error occurred.

# 5.20.3.7 array\_is\_real()

Checks if all complex numbers in the array 1 are real.

#### **Parameters**

I the array

#### Returns

true if all elements in the array are real, false otherwise.

# 5.20.3.8 array\_new()

```
array array_new (
          ulong size )
```

Returns a new empty array with memory size at least size.

#### **Parameters**

size	the number of elements to allocate memory for
------	---

# Returns

the array,  $\mathtt{NULL}$  if not enougn memory is available

# 5.20.3.9 array\_new\_poly()

Returns the array of coefficients of the polynomial  $\ensuremath{\mathbb{P}}.$ 

#### **Parameters**

Р	the polynomial
prec	the precision of the numbers in the array

#### Returns

the array,  $\mathtt{NULL}$  if some error occurred.

## 5.20.3.10 array\_new\_polyr()

Returns the array of coefficients of the real polynomial  $\ensuremath{\mathbb{P}}$ .

#### **Parameters**

Р	the real polynomial
prec	the precision of the numbers in the array

#### Returns

the array,  $\mathtt{NULL}$  if some error occurred.

# 5.20.3.11 array\_poly()

Returns the polynomial with the coefficients in the array 1.

#### **Parameters**

1	the array
prec	the precision of the coefficients of the polynomial

#### Returns

the polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.20.3.12 array\_polyr()

Returns the real polynomial with the coefficients the real parts of the complex numbers in the array 1.

# **Parameters**

1	the array
prec	the precision of the coefiicients of the polynomial

# Returns

the polynomial,  $\mathtt{NULL}$  if some coefficients are not real or some other error occurred.

## 5.20.3.13 array\_read()

Reads a array of complex numbers of precision prec from the CSV file with path fileName.

#### **Parameters**

fileName	the path of the CSV file
prec	the precision
verbose	true to print information about the file and the error, if any

## Returns

the array of complex numbers in the CSV file,  $\mathtt{NULL}$  if some error occurred.

## 5.20.3.14 array\_write()

Writes the array 1 to a CSV file with the given path fileName.

#### **Parameters**

1	the array
fileName	the path of the CSV file
digits	the number of digits after the decimal point of the numbers in the file
verbose	true to print information about the error, if any

#### Returns

true if successfull, false otherwise.

# 5.21 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/arrayf.h File Reference

Definition of a variable length array of machine floating point complex numbers.

#### **Data Structures**

· struct arrayf\_struct

A variable length list of machine floating point complex numbers.

## **Macros**

- #define LISTF\_MIN\_SIZE 100
- #define LISTF\_SIZE\_INCREASE 1.25

## **Typedefs**

• typedef arrayf\_struct arrayf\_t[1]

Practical wrapper for arrayf\_struct.

typedef arrayf\_struct \* arrayf

Convenience pointer to arrayf\_struct.

#### **Functions**

arrayf arrayf\_new (ulong size)

Returns a new empty list with memory size at least size.

arrayf arrayf\_new\_polyfr (polyfr P)

Returns the list of coefficients of the real polynomial P.

arrayf arrayf\_new\_polyf (polyf P)

Returns the list of coefficients of the polynomial P.

• bool arrayf free (arrayf I)

Frees all the memory used by the list 1, assuming the struct has been allocated with malloc(), for example with  $list_new()$ .

• bool arrayf\_add (arrayf I, compf z)

Adds the complex number z at the end of the list. The size of the list is automatically increased, if needed.

compf\_ptr arrayf\_get (arrayf I, ulong pos)

Returns the pointer of the element on position pos in the list 1.

bool arrayf\_is\_real (arrayf I)

Checks if all complex numbers in the list  $\ensuremath{\mathbb{I}}$  are real.

long arrayf\_first\_inf (arrayf l)

Checks if there are infinite values in the list 1.

long arrayf\_first\_nan (arrayf l)

Checks if all complex numbers in the list 1 are well defined.

• polyfr arrayf\_polyfr (arrayf I)

Returns the real polynomial with the coefficients the real parts of the complex numbers in the list 1.

polyf arrayf\_polyf (arrayf l)

Returns the polynomial with the coefficients in the list 1.

• bool arrayf\_write (arrayf I, char \*fileName, bool verbose)

Writes the list 1 to a CSV file with the given path fileName.

bool arrayf\_append (arrayf I, char \*fileName, bool verbose)

Writes the list 1 to the end of a CSV file with the given path fileName.

arrayf arrayf\_read (char \*fileName, bool verbose)

Reads a list of complex numbers from the CSV file with path fileName.

# 5.21.1 Detailed Description

Definition of a variable length array of machine floating point complex numbers.

# 5.21.2 Typedef Documentation

# 5.21.2.1 arrayf\_t

```
typedef arrayf_struct arrayf_t[1]
```

Practical wrapper for arrayf\_struct.

To avoid the constant use \* and & the type  ${\tt arrayf\_t}$  is a pointer.

Definition at line 47 of file arrayf.h.

## 5.21.3 Function Documentation

## 5.21.3.1 arrayf\_add()

Adds the complex number z at the end of the list. The size of the list is automatically increased, if needed.

#### **Parameters**

1	the list
Z	the new element to add to the list

# Returns

true if successfull, false otherwise.

## 5.21.3.2 arrayf\_append()

```
char * fileName,
bool verbose )
```

Writes the list 1 to the end of a CSV file with the given path  ${\tt fileName}.$ 

#### **Parameters**

1	the list
fileName	the path of the CSV file
verbose	true to print information about the error, if any

## Returns

true if successfull, false otherwise.

## 5.21.3.3 arrayf\_first\_inf()

Checks if there are infinite values in the list 1.

#### **Parameters**

```
/ the list
```

### Returns

the position of the first infinite value in 1, -1 if there is none, LONG\_MAX if some error occurred.

# 5.21.3.4 arrayf\_first\_nan()

```
long arrayf_first_nan ( arrayf 1)
```

Checks if all complex numbers in the list  $\ensuremath{\mathbb{1}}$  are well defined.

## **Parameters**



# Returns

the position of the first undefined value in 1, -1 if there is none, LONG\_MAX if some error occurred.

# 5.21.3.5 arrayf\_free()

Frees all the memory used by the list 1, assuming the struct has been allocated with malloc(), for example with  $list_new()$ .

## **Parameters**

```
I the list
```

#### Returns

true if successfull, false otherwise.

# 5.21.3.6 arrayf\_get()

Returns the pointer of the element on position pos in the list 1.

### **Parameters**

1	the list
pos	the position of the element

# Returns

the pointer to the element on position pos in 1, NULL if some error occurred.

## 5.21.3.7 arrayf\_is\_real()

Checks if all complex numbers in the list  $\ensuremath{\mathbb{1}}$  are real.

# **Parameters**

```
I the list
```

#### Returns

true if all elements in the list are real, false otherwise.

# 5.21.3.8 arrayf\_new()

```
arrayf arrayf_new (
            ulong size )
```

Returns a new empty list with memory size at least size.

#### **Parameters**

size the number of elements to allocate memory for

## Returns

the list,  $\mathtt{NULL}$  if not enougn memory is available

# 5.21.3.9 arrayf\_new\_polyf()

```
arrayf arrayf_new_polyf (
            polyf P )
```

Returns the list of coefficients of the polynomial  $\ensuremath{\mathbb{P}}$ .

#### **Parameters**

the polynomial

## Returns

the list,  $\mathtt{NULL}$  if some error occurred.

## 5.21.3.10 arrayf\_new\_polyfr()

```
arrayf arrayf_new_polyfr (
            polyfr P )
```

Returns the list of coefficients of the real polynomial  $\ensuremath{\mathbb{P}}$ .

#### **Parameters**

P the real polynomial

## Returns

the list,  $\mathtt{NULL}$  if some error occurred.

## 5.21.3.11 arrayf\_polyf()

Returns the polynomial with the coefficients in the list  $\ensuremath{\mathbb{1}}$ .

## **Parameters**

```
I the list
```

#### Returns

the polynomial,  $\mathtt{NULL}$  if some error occurred.

# 5.21.3.12 arrayf\_polyfr()

Returns the real polynomial with the coefficients the real parts of the complex numbers in the list 1.

#### **Parameters**

```
I the list
```

# Returns

the polynomial,  $\mathtt{NULL}$  if some coefficients are not real or some other error occurred.

# 5.21.3.13 arrayf\_read()

Reads a list of complex numbers from the CSV file with path fileName.

#### **Parameters**

fileName	the path of the CSV file
verbose	true to print information about the file and the error, if any

#### Returns

the list of complex numbers in the CSV file, NULL if some error occurred.

## 5.21.3.14 arrayf\_write()

Writes the list 1 to a CSV file with the given path fileName.

#### **Parameters**

1	the list
fileName	the path of the CSV file
verbose	true to print information about the error, if any

#### Returns

true if successfull, false otherwise.

# 5.22 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/chrono.h File Reference

Tools for precise time measuring.

## **Macros**

• #define BILLION 100000000L

One billion (nanoseconds in one second).

• #define MILLION 1000000L

One billion (miliseconds in one second).

• #define MINUTE 60000L

Miliseconds in one minute.

• #define HOUR (60 \* MINUTE)

Miliseconds in one hour.

#define DAY (24 \* HOUR)

Miliseconds in one day.

#define USED\_CLOCK CLOCK\_MONOTONIC

The ID of the system clock to use.

# **Typedefs**

· typedef struct timespec ptime

Short type name for precise time.

# **Functions**

• void millis (long ms, char \*str)

Formats the time duration in miliseconds ms into human readable string str.

• void nanos (long ns, char \*str)

Formats the time duration in nanoseconds ns into human readable string str.

ulong lap (ptime \*ts, char \*str)

Computes and prints the time lapse since ts.

void print\_time\_res (void)

Prints the timer resolution.

# 5.22.1 Detailed Description

Tools for precise time measuring.

# 5.22.2 Function Documentation

#### 5.22.2.1 lap()

```
ulong lap ( \label{eq:ptime} \mbox{ptime} \ * \ ts, \\ \mbox{char} \ * \ str \ )
```

Computes and prints the time lapse since  ${\tt ts.}$ 

Pretty prints the elapsed time into the string str and updates ts to the current time. Does not fail if str == NULL, can also be used as a starter for the chronometer.

Warning

The string str should be at least 90 bytes long.

## **Parameters**

ts	old time stamp
str	human readable string for the time increment

#### Returns

the total time in nanos

# 5.22.2.2 millis()

```
void millis ( \log \ ms, \operatorname{char} \ * \ str \ )
```

Formats the time duration in miliseconds ms into human readable string str.

# Warning

The string str should be at least 90 bytes long.

## **Parameters**

ms	the time lapse in miliseconds
str	the human readable print

# 5.22.2.3 nanos()

```
void nanos ( \log \ ns, \operatorname{char} \ * \ str \ )
```

Formats the time duration in nanoseconds ns into human readable string str.

# Warning

The string str should be at least 90 bytes long.

## **Parameters**

ns	the time lapse in miliseconds
str	the human readable print

# 5.23 /home/runner/work/FastPolyEval/FastPolyEval/code/tools/debug.h File Reference

A few basic tool for easy debug when usinf MPFR.

# **Functions**

```
• char * pm (mpfr_t x, int dig)
```

Return a string containing the value of x with dig digits.

• char \* pc (comp z, int dig)

Return a string containing the value of x with dig digits.

char \* pcf (compf z)

Return a string containing the value of z.

# 5.23.1 Detailed Description

A few basic tool for easy debug when usinf MPFR.

#### 5.23.2 Function Documentation

### 5.23.2.1 pc()

```
char* pc (  \begin{array}{c} \text{comp } z, \\ \text{int } dig \ ) \end{array}
```

Return a string containing the value of x with  $\operatorname{dig}$  digits.

The format is that of a CSV file line, the real and imaginary components are separated by a comma.

## Warning

The user is responsible to free the memory containg the results.

#### **Parameters**

Z	a complex number, with MPFR real and imaginary parts	
dig	the number of digits to print	]

## Returns

the string containing the value of z, NULL if some error occurred

## 5.23.2.2 pcf()

```
char* pcf ( \operatorname{compf}\ z )
```

Return a string containing the value of  $\ensuremath{\mathtt{z}}$ .

The format is that of a CSV file line, the real and imaginary components are separated by a comma.

## Warning

The user is responsible to free the memory containg the results.

## **Parameters**

```
z a complex number, with machine numbers real and imaginary parts
```

#### Returns

the string containing the value of z,  $\mathtt{NULL}$  if some error occurred

## 5.23.2.3 pm()

Return a string containing the value of x with dig digits.

#### Warning

The user is responsible to free the memory containg the results.

#### **Parameters**

X	a real number, MPFR
dig	the number of digits to print

## Returns

the string containing the value of z,  $\mathtt{NULL}$  if some error occurred